

2020/12/16

CGP internal workshop

Cosmic tension:

Headache in Planck Λ CDM cosmology

Atsushi Taruya

Plan of talk

Review of H_0 tension

Local measurement of
the Hubble parameter

discrepancy

Λ CDM model
determined by Planck

$$H_0 = 74.0 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

(Riess et al. '19)

$$H_0 = 67.4 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

(Planck 2018 results IV)

Possibilities

- Both of them are correct, Λ CDM model is wrong (new physics)
but, some (most?) of the proposed scenarios has some troubles
- Either of them is wrong
due to unknown systematics
- Or both are wrong

Hubble parameter

Fundamental quantity characterizing the expansion of the Universe

$$H(t) \equiv \frac{\dot{a}(t)}{a(t)} \quad a(t) : \text{Scale factor of the Universe}$$

Friedmann
equation

$$3H^2(t) = 8\pi G \left\{ \underbrace{\rho_m(t)}_{\text{matter}} + \underbrace{\rho_{\text{DE}}(t)}_{\text{dark energy}} \right\} - \underbrace{\frac{K}{a^2}}_{\text{curvature}}$$

In particular, Hubble parameter at the present time is called

$$H_0$$

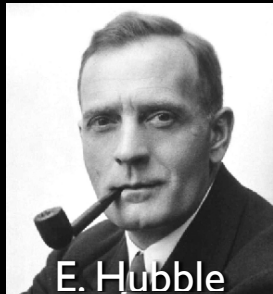
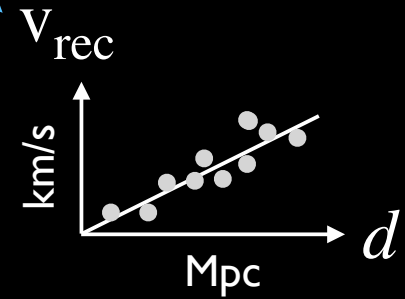
A precision determination of H_0 is important in cosmology, and is a basis to clarify the nature of dark energy or cosmic acceleration

(Local) measurement of H_0

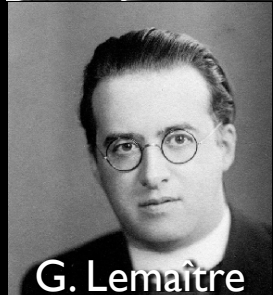
Hubble-Lemaître law

Recession velocity of galaxies is linearly proportional to distance:

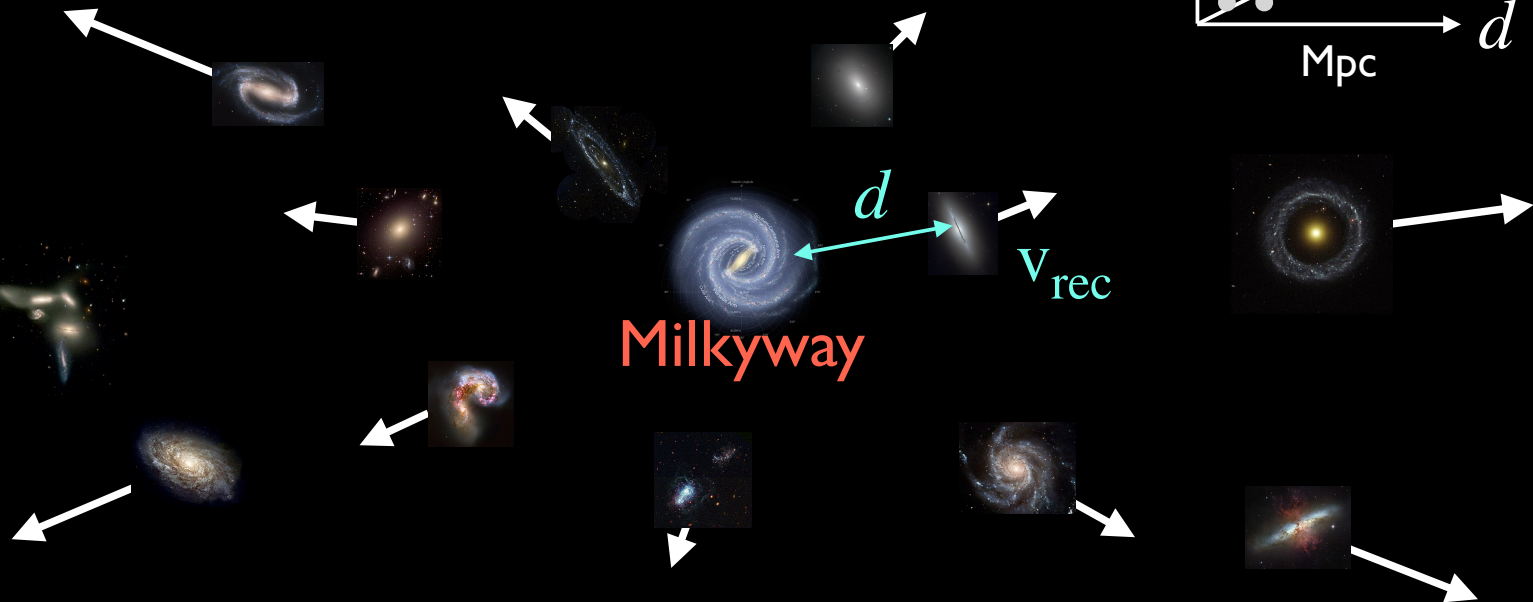
$$v_{\text{rec}} = H_0 d$$



E. Hubble



G. Lemaître

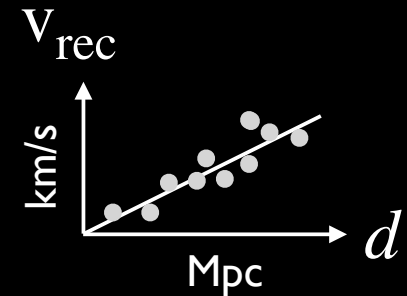


(Local) measurement of H_0

Hubble-Lemaître law

Recession velocity of galaxies is linearly proportional to distance:

$$v_{\text{rec}} = H_0 d$$



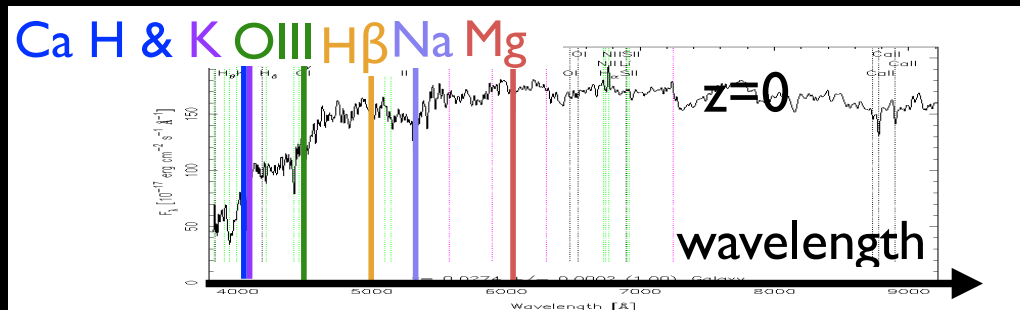
Cosmological redshift

$$z \equiv \frac{\Delta\lambda}{\lambda} = \frac{v_{\text{rec}}}{c}$$

Spectroscopic measurement



Nearby galaxy

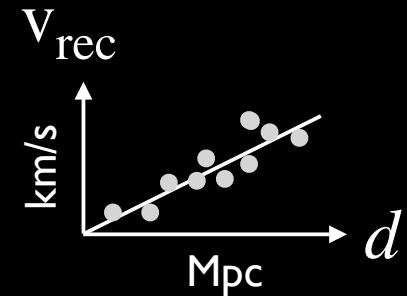


(Local) measurement of H_0

Hubble-Lemaître law

Recession velocity of galaxies is linearly proportional to distance:

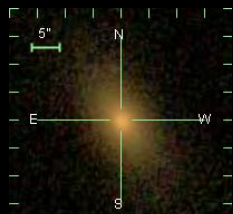
$$v_{\text{rec}} = H_0 d$$



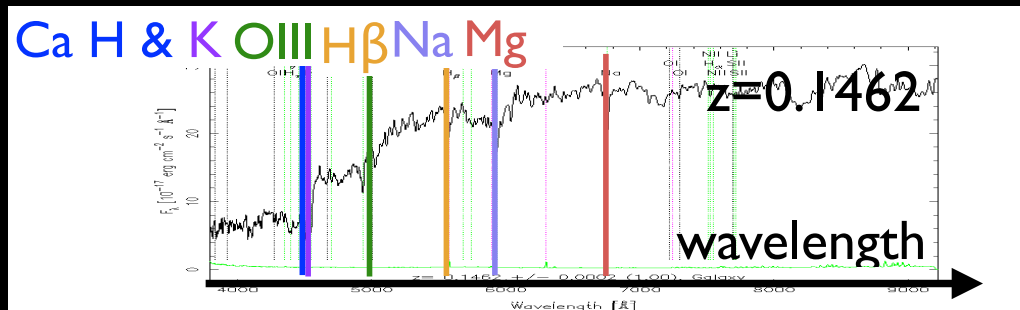
Cosmological
redshift

$$z \equiv \frac{\Delta\lambda}{\lambda} = \frac{v_{\text{rec}}}{c}$$

Spectroscopic
measurement



Distant galaxy

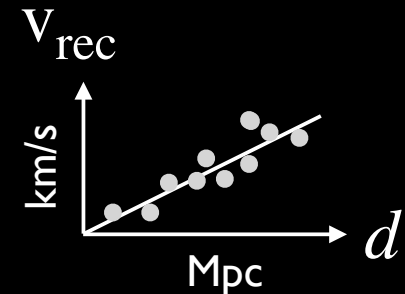


(Local) measurement of H_0

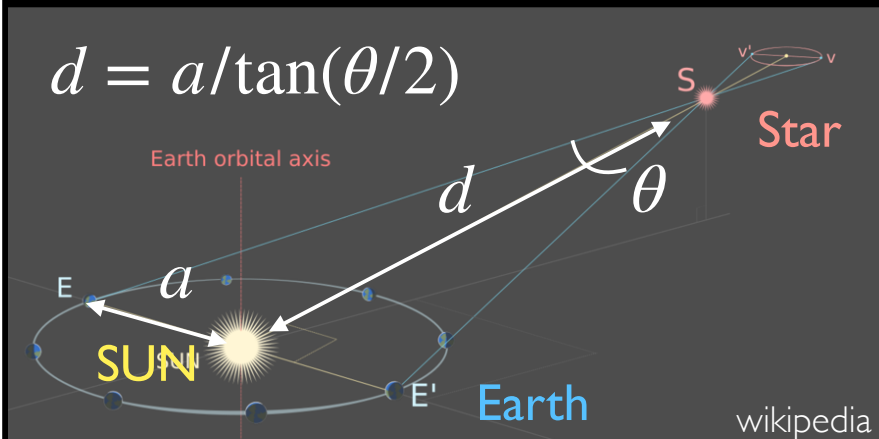
Hubble-Lemaître law

Recession velocity of galaxies is linearly proportional to distance:

$$v_{\text{rec}} = H_0 d$$



Distance measurement is the most difficult part :

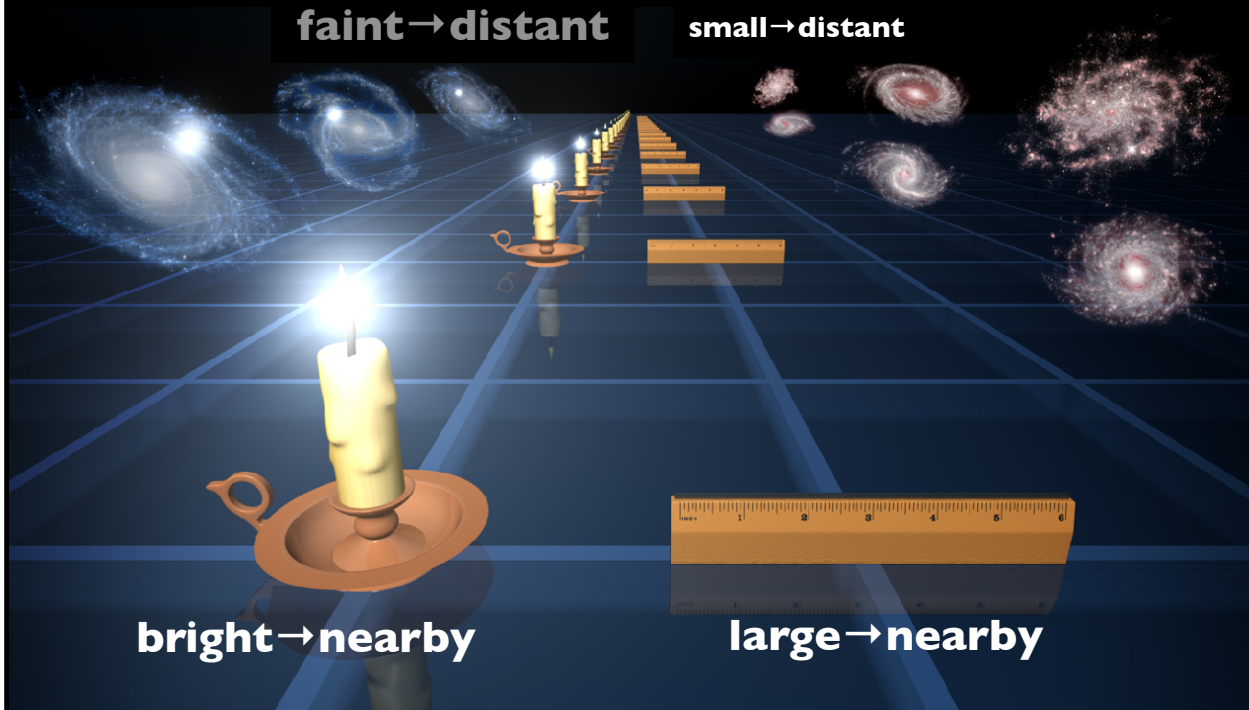


For closer objects ($< 10^4$ light years),
an accurate measurement can be
made by using parallax method
(e.g., Gaia, HST)

Distance measurements

For much farther objects ($d > 10^4$ light years),

the distance measurement can be still made if we *a priori* know the size or luminosity of the objects



Such an object is called

Standard candle

Or

Standard ruler

Note—.

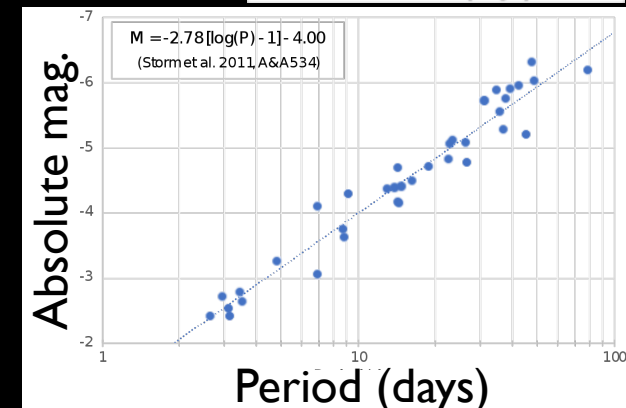
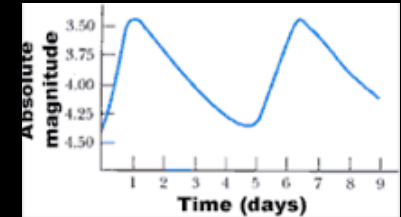
There recently appears
standard siren

Standard(izable) candles

Cepheid variable

Pulsating stars that periodically gets bright & faint

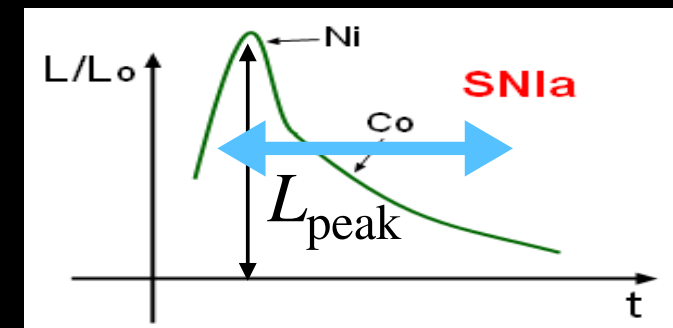
(Empirical) period-luminosity relation



Type-Ia Supernova

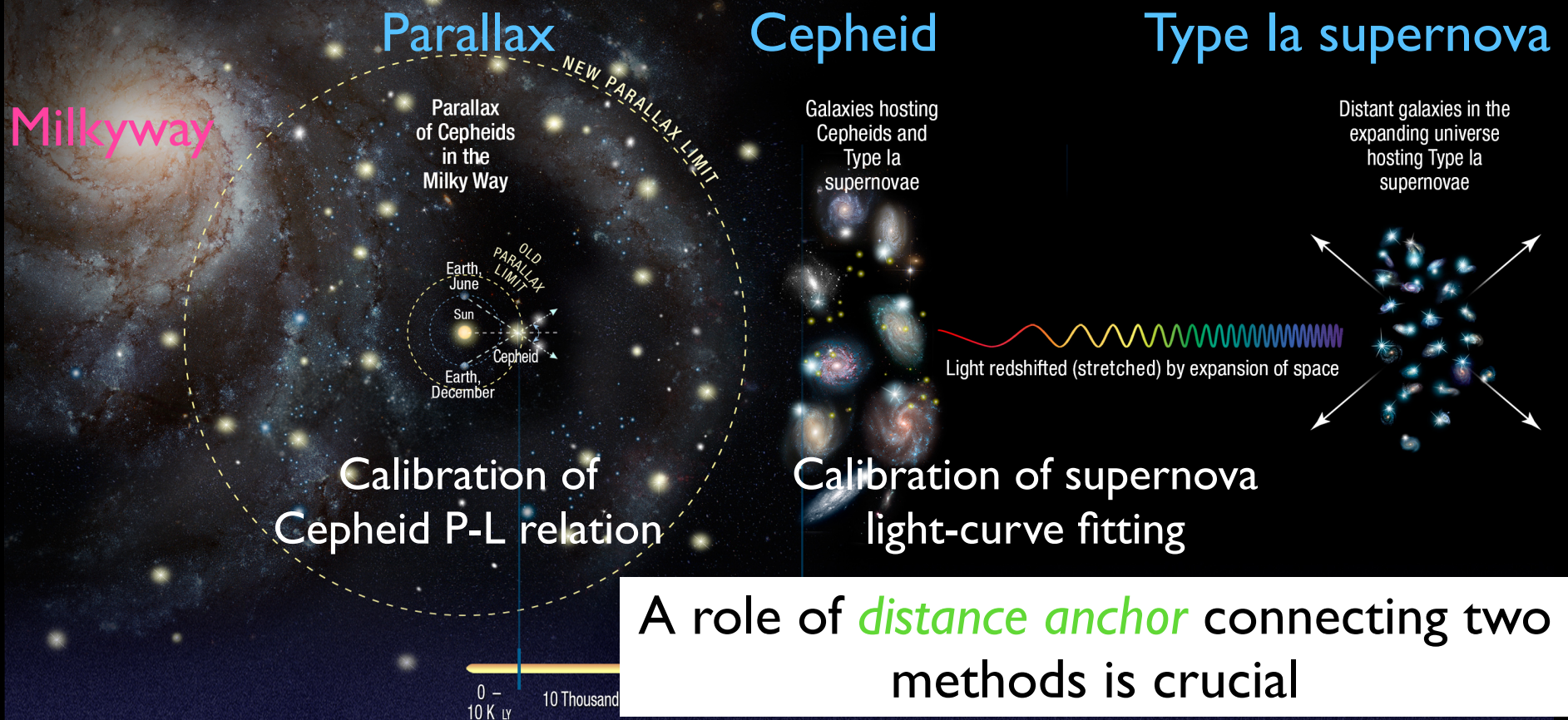
A type of supernova that occurs in binary systems

Tight relation between peak luminosity & decay time scale



Distance ladder

Three steps to the Hubble Constant





Adam Riess

(2011 Nobel
Laureate)

SH₀ES



(SNe, H₀, for the Equation of State of dark energy)

A precision local measurement of H₀ using Hubble space telescope (photometric obs. of Cepheid & SNe Ia)

Distance anchors to calibrate Cepheid P-L relation:

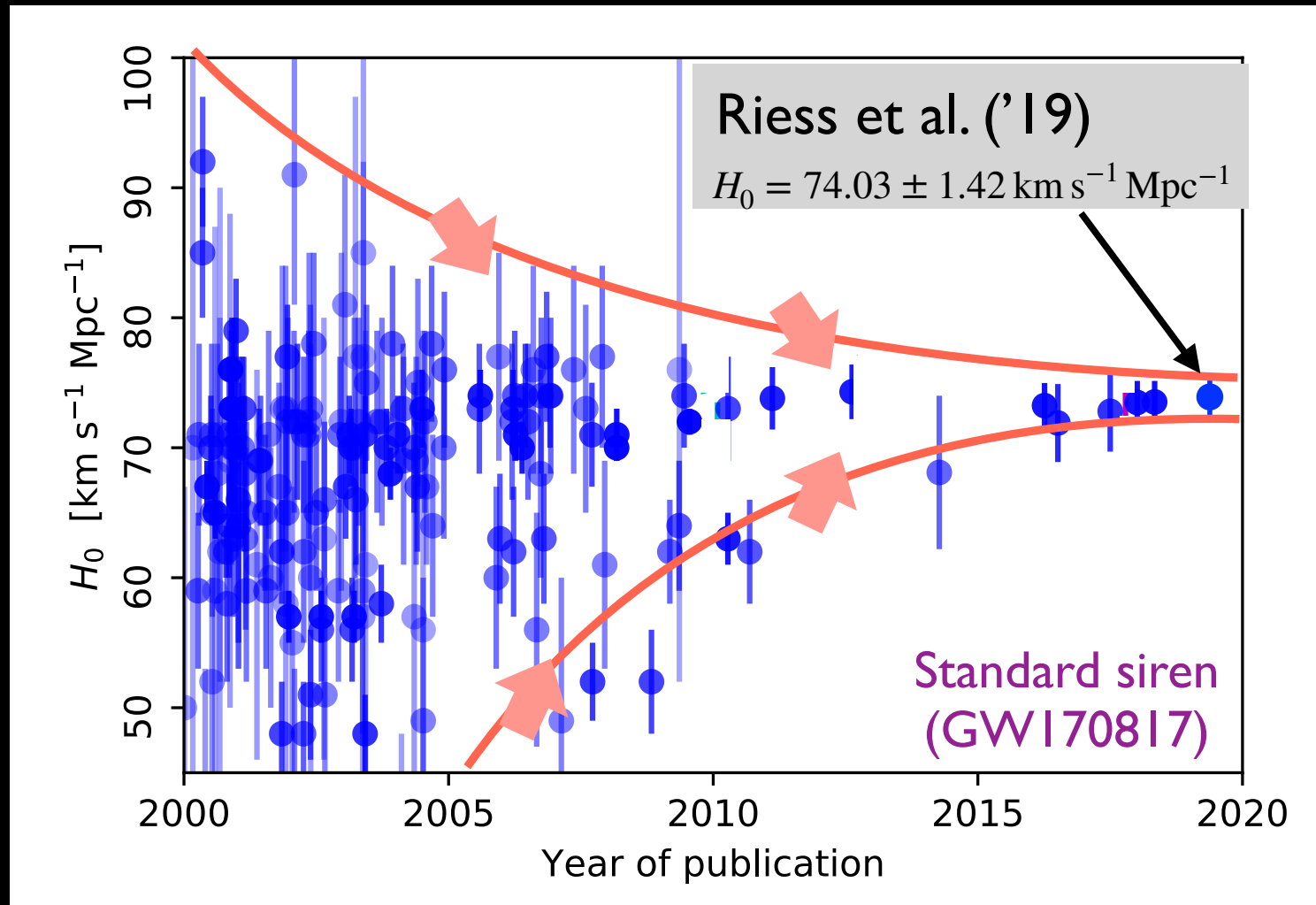
- Parallaxes → Milkyway Cepheids
- 20 Detached eclipsing binaries → LMC Cepheid
(Large Magellanic Cepheid)
- VLBI obs. of water masers → NGC4258 Cepheid

1.9%
precision

$$H_0 = 74.03 \pm 1.42 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

Riess et al. ('19)

Time evolution of H_0 measurement

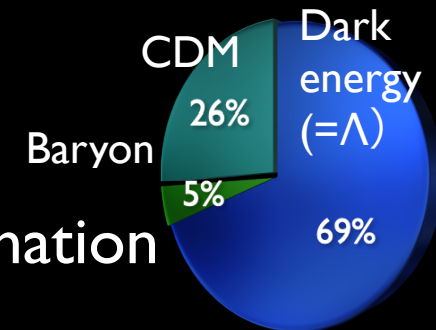


Alternative method

We can rely on the standard cosmological model

Lambda Cold Dark Matter (Λ CDM) model

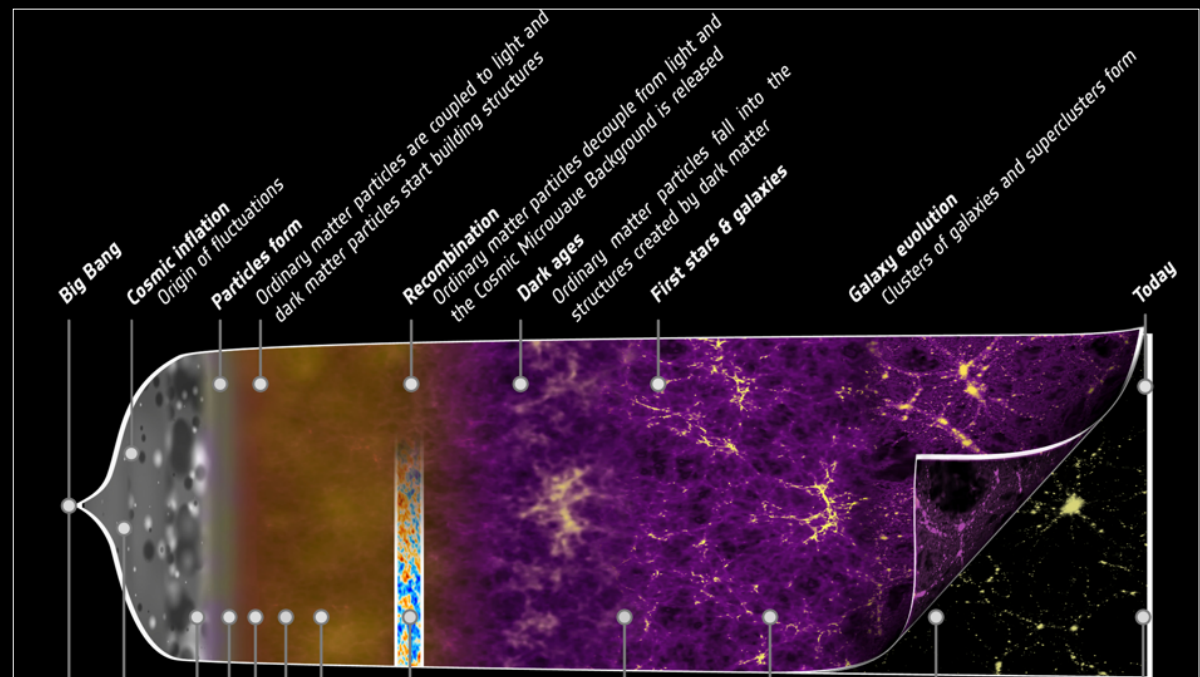
describes both cosmic expansion & structure formation
(with parameters including H_0)



Based on the theory of
structure formation,

H_0 can be inferred from
the observations of
high-redshift universe

(Inverse distance ladder)

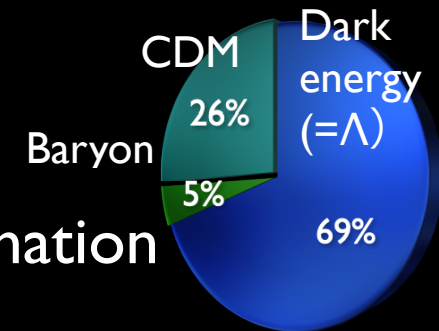


Alternative method

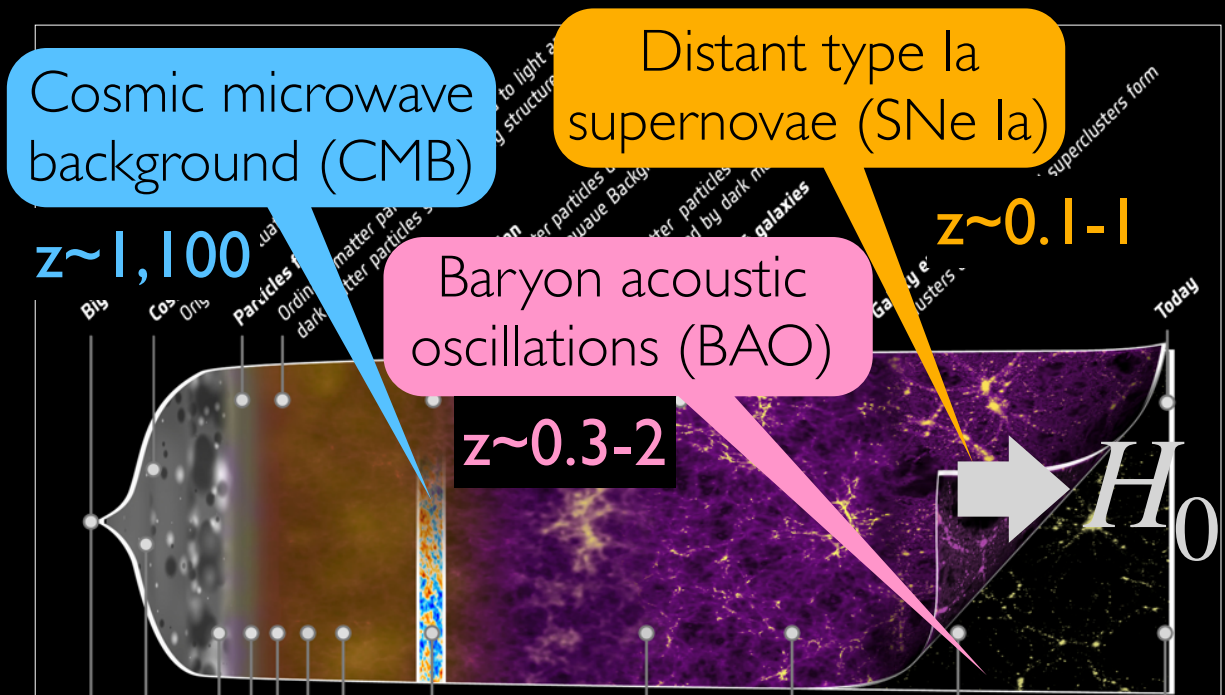
We can rely on the standard cosmological model

Lambda Cold Dark Matter (Λ CDM) model

describes both cosmic expansion & structure formation
(with parameters including H_0)



Based on the theory of structure formation,
 H_0 can be inferred from the observations of **high-redshift** universe
(*Inverse distance ladder*)



Cosmic microwave background (CMB)

'Relic' radiation emitted at 380,000 years after Big-Bang

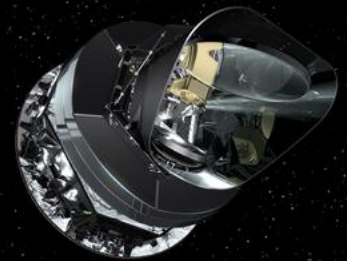
Tiny anisotropies offers a powerful cosmological probe

➔ Standard cosmological model

Planck satellite (ESA) provides high-precision data of

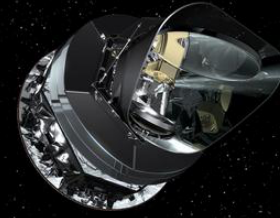
- temperature
- polarization
- gravitational lensing

Help tightening cosmological constraints

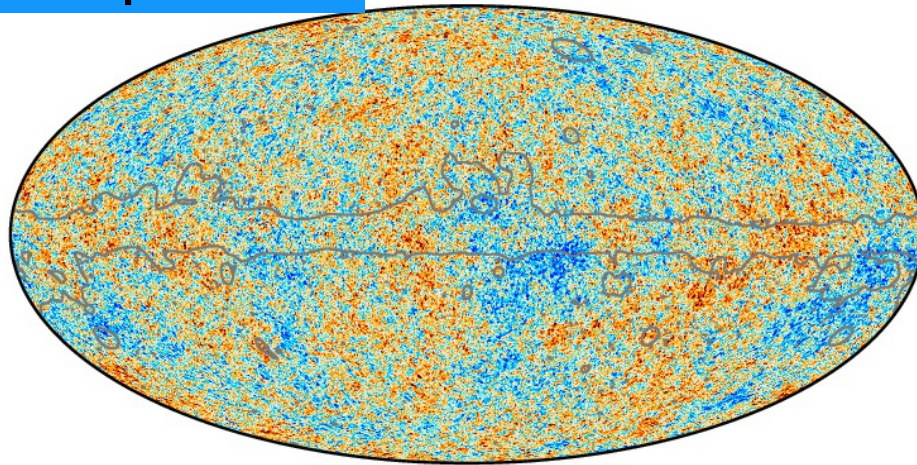


Planck (2009-2013)

Planck 2018

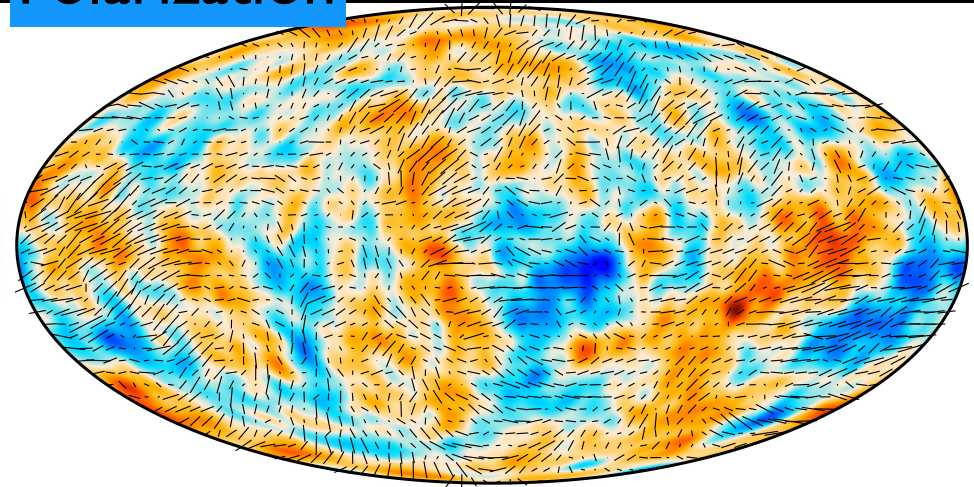


Temperature



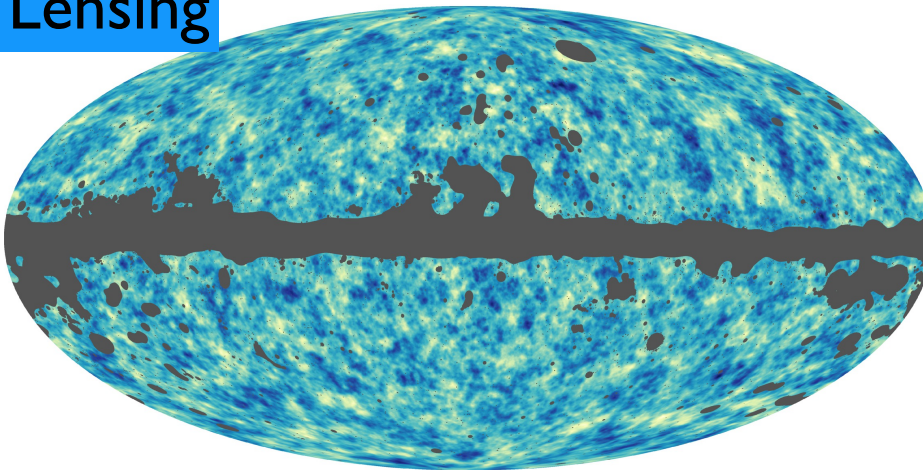
-300 300 μK

Polarization



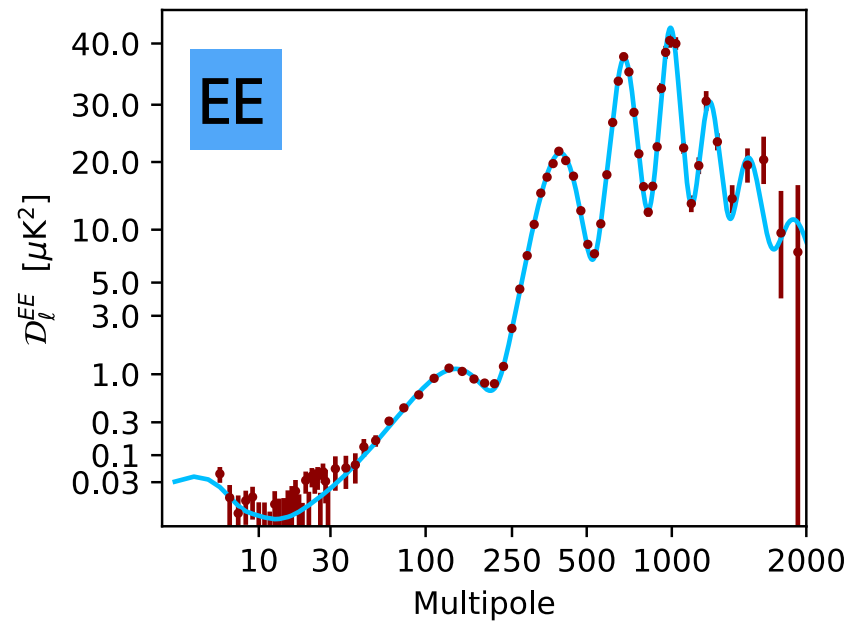
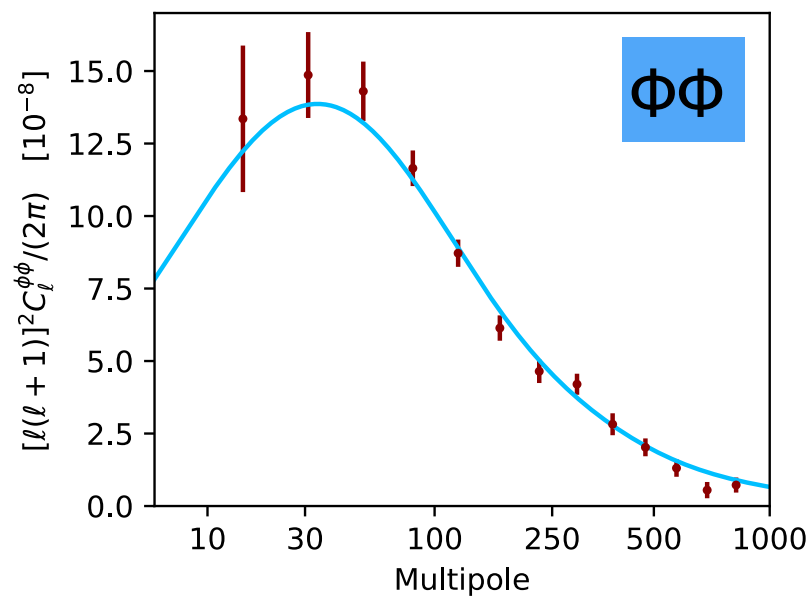
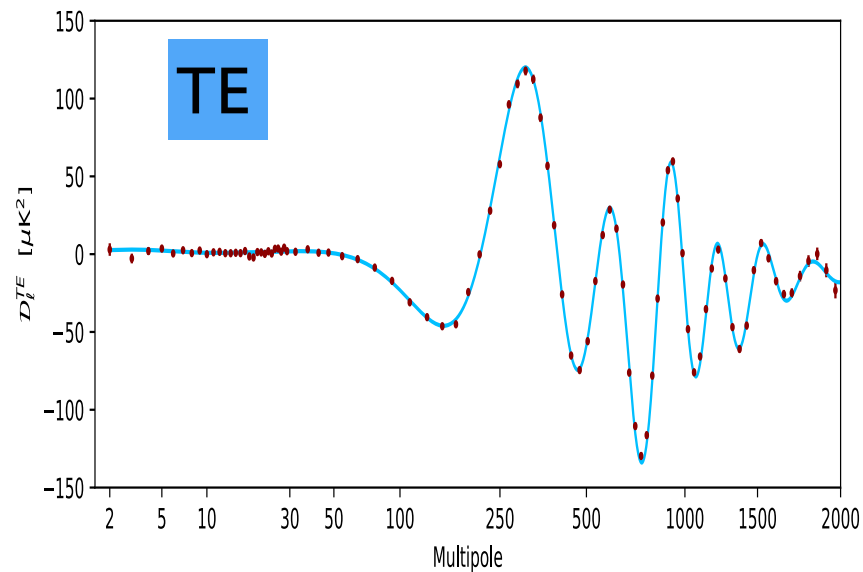
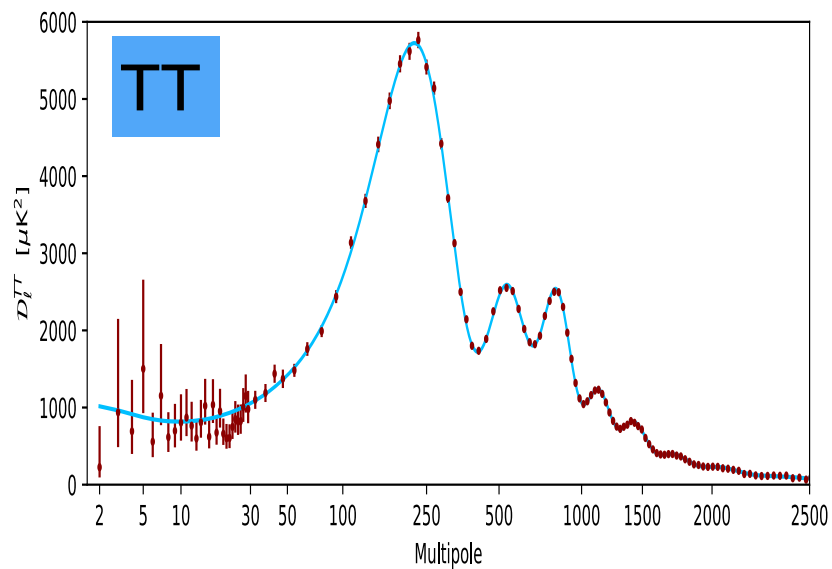
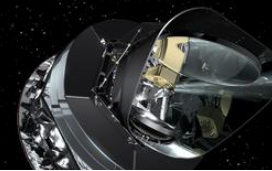
0.41 μK -160 160 μK

Lensing

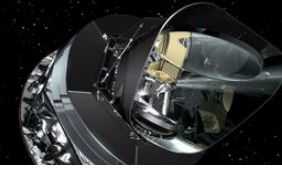


-0.0016 0.0016

Planck 2018



Planck 2018



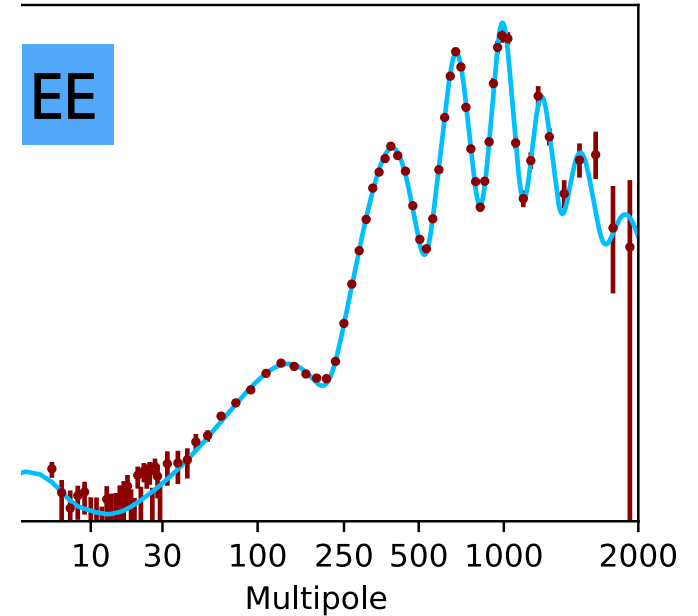
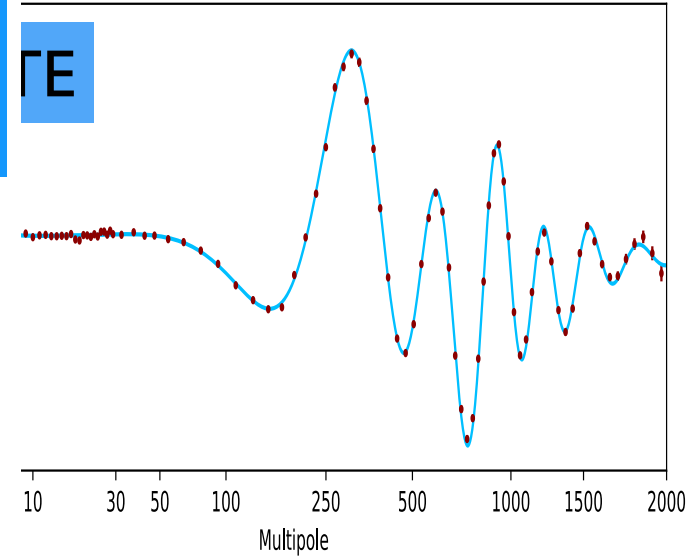
Parameter	Planck alone
$\Omega_b h^2$	0.02237 ± 0.00015
$\Omega_c h^2$	0.1200 ± 0.0012
$100\theta_{MC}$	1.04092 ± 0.00031
τ	0.0544 ± 0.0073
$\ln(10^{10} A_s)$	3.044 ± 0.014
n_s	0.9649 ± 0.0042
<hr/>	
H_0	67.36 ± 0.54
Ω_Λ	0.6847 ± 0.0073
Ω_m	0.3153 ± 0.0073
$\Omega_m h^2$	0.1430 ± 0.0011
$\Omega_m h^3$	0.09633 ± 0.00030
σ_8	0.8111 ± 0.0060
$\sigma_8(\Omega_m/0.3)^{0.5}$	0.832 ± 0.013
z_{re}	7.67 ± 0.73
Age[Gyr]	13.797 ± 0.023
r_* [Mpc]	144.43 ± 0.26
$100\theta_*$	1.04110 ± 0.00031
r_{drag} [Mpc]	147.09 ± 0.26
z_{eq}	3402 ± 26
k_{eq} [Mpc ⁻¹]	0.010384 ± 0.000081

Base Λ CDM parameters

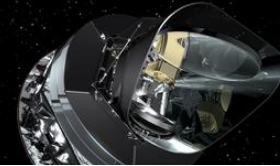
- temperature
- polarization
- lensing



derived parameters



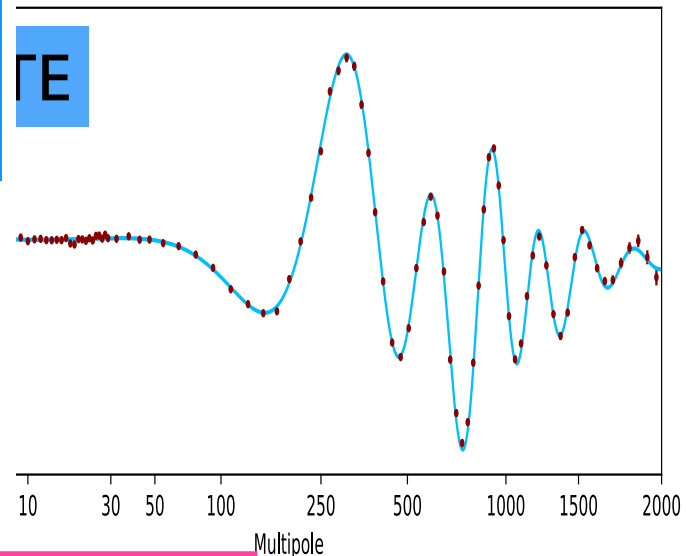
Planck 2018



Parameter	Planck alone
$\Omega_b h^2$	0.02237 ± 0.00015
$\Omega_c h^2$	0.1200 ± 0.0012
$100\theta_{MC}$	1.04092 ± 0.00031
τ	0.0544 ± 0.0073
$\ln(10^{10} A_s)$	3.044 ± 0.014
n_s	0.9649 ± 0.0042
H_0	67.36 ± 0.54
Ω_Λ	0.6847 ± 0.0073
Ω_m	0.3153 ± 0.0073
$\Omega_m h^2$	0.1430 ± 0.0011
$\Omega_m h^3$	0.09633 ± 0.00030
σ_8	0.8111 ± 0.0060
$\sigma_8(\Omega_m/0.3)^{0.5}$..	0.832 ± 0.013
z_{re}	7.67 ± 0.73
Age[Gyr]	13.797 ± 0.023
r_* [Mpc]	144.43 ± 0.26
$100\theta_*$	1.04110 ± 0.00031
r_{drag} [Mpc]	147.09 ± 0.26
z_{eq}	3402 ± 26
k_{eq} [Mpc ⁻¹]	0.010384 ± 0.000081

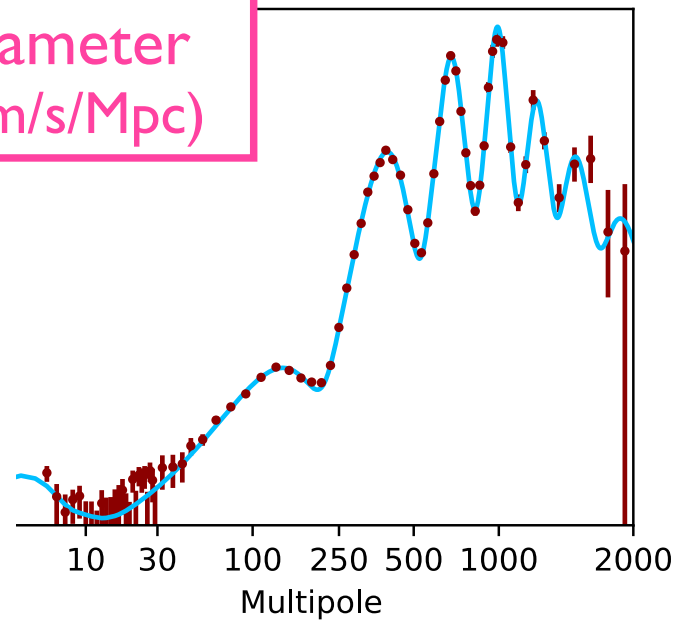
Base Λ CDM parameters

- temperature
- polarization
- lensing



Hubble parameter
(in units of km/s/Mpc)

derived parameters



H₀ tension

Model-independent

Local measurement by SH₀ES
(distance ladder)

VS

Planck CMB measurement
assuming Λ CDM model

$$H_0 = 74.0 \pm 1.4 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

(Riess et al. '19)

$$H_0 = 67.4 \pm 0.5 \text{ km s}^{-1} \text{ Mpc}^{-1}$$

(Planck 2018 results IV)

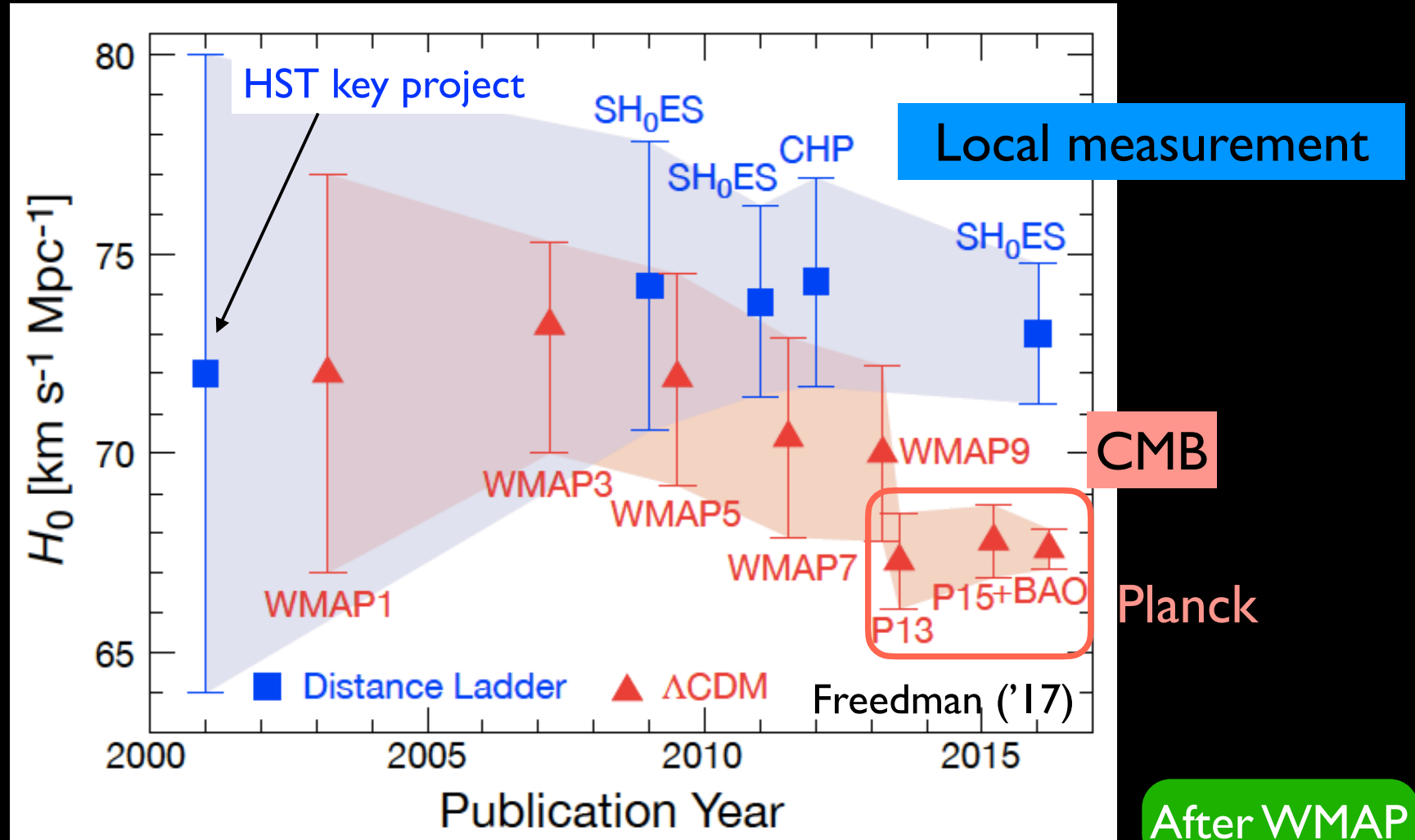
Deviation of Planck H₀ from local measurement is at **4.4 σ** level
(99.999% for Gaussian errors)

Discrepancy remains statistically significant even if other parameters are allowed to vary.

(spatial curvature, dark energy EOS, neutrino mass, ...)

This is actually not the first to highlight the discrepancy

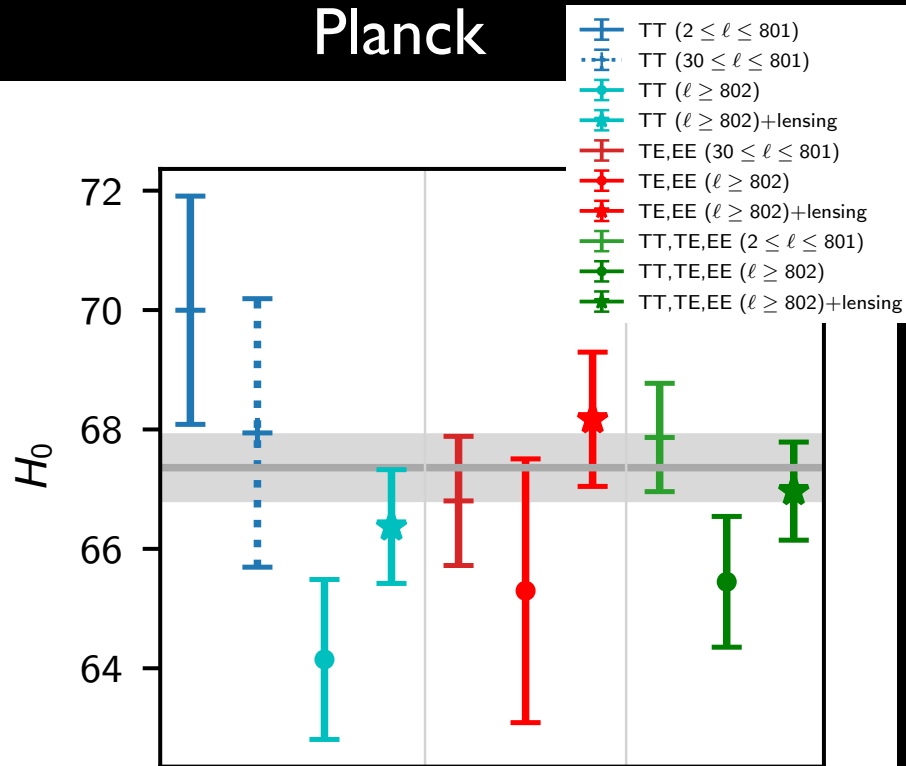
Time evolution of competing H_0



Local measurements prefer a **large** H_0 , while CMB prefer a **small** H_0

Systematics ?

Planck



SH₀ES

Table 5
Best Estimates of H_0 Including Systematics

Anchor(s)	Value ($\text{km s}^{-1} \text{Mpc}^{-1}$)
LMC	74.22 ± 1.82
Two anchors	
LMC + NGC 4258	73.40 ± 1.55
LMC + MW	74.47 ± 1.45
NGC 4258 + MW	73.94 ± 1.58
Three anchors (preferred)	
NGC 4258 + MW + LMC	74.03 ± 1.42

Planck 2018 result IV

Riess et al. ('19)

Depending on how they combine the data set, the tension may be alleviated, but it seems difficult to completely resolve the tension

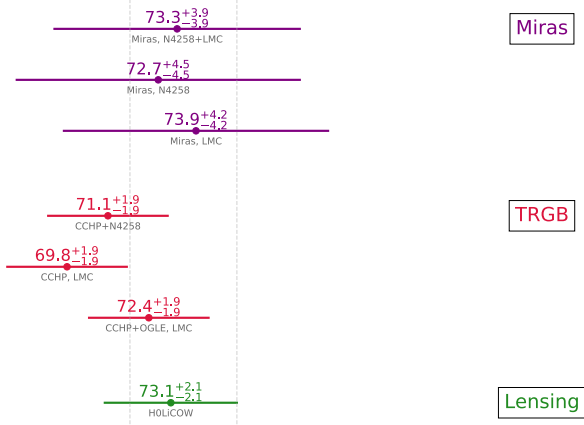
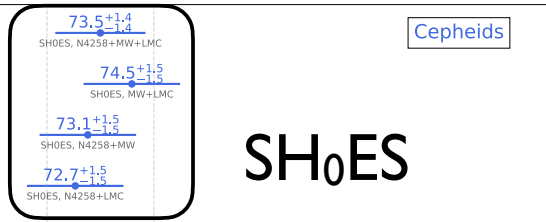
Other H_0 measurements

Riess (arXiv:2001.03624)

SN Ia Distance Ladders

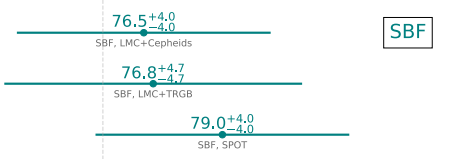
1

Late Universe



SBF Distance Ladders

2



Single Rung

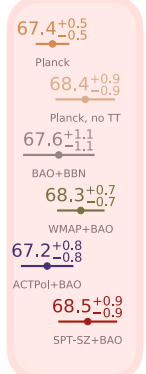
3, 4



H_0 [km s⁻¹ Mpc⁻¹]

Early & Lat

Early

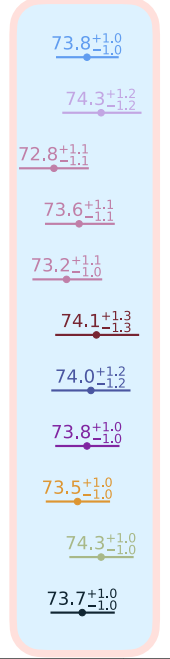


CMB & BAO

- No BAO
- Planck, no TT
- No CMB
- No Planck, CMB + BAO
- No Planck, CMB + BAO
- No Planck, CMB + BAO

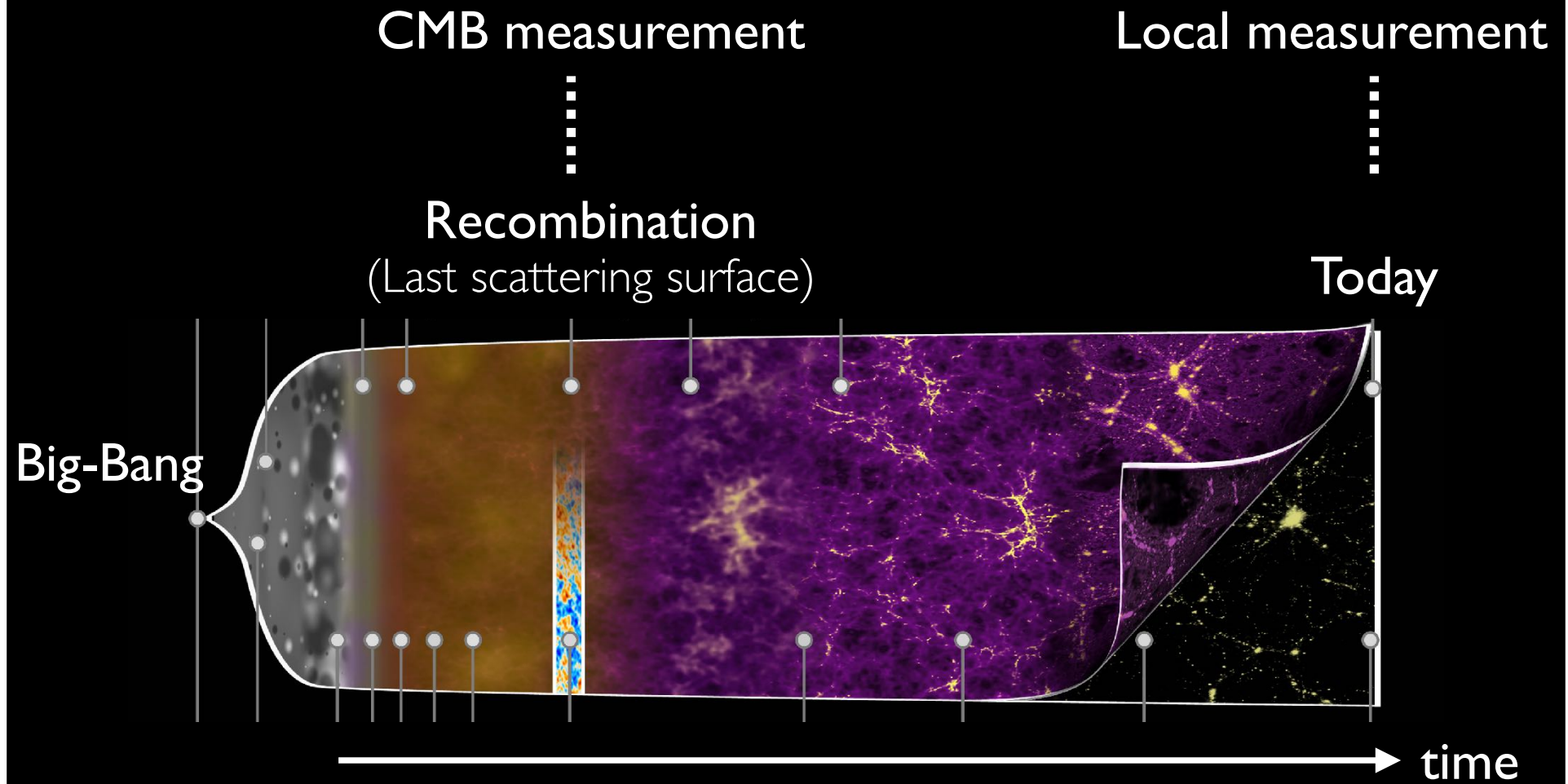
Late

= 1+2+3+4



H_0 [km s⁻¹ Mpc⁻¹]

Relieving H_0 tension by 'new' physics

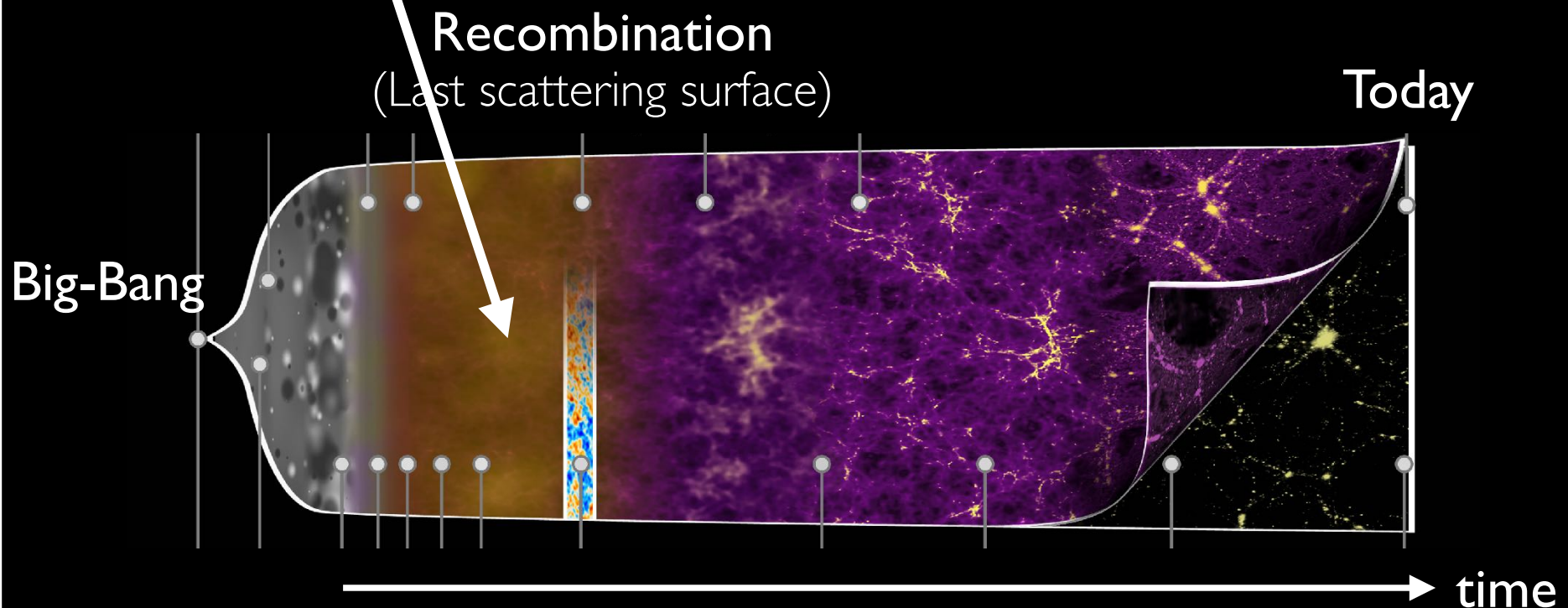


Relieving H_0 tension by 'new' physics

Early-time solution

change cosmic expansion before recombination or recombination history

measurement



Relieving H_0 tension by 'new' physics

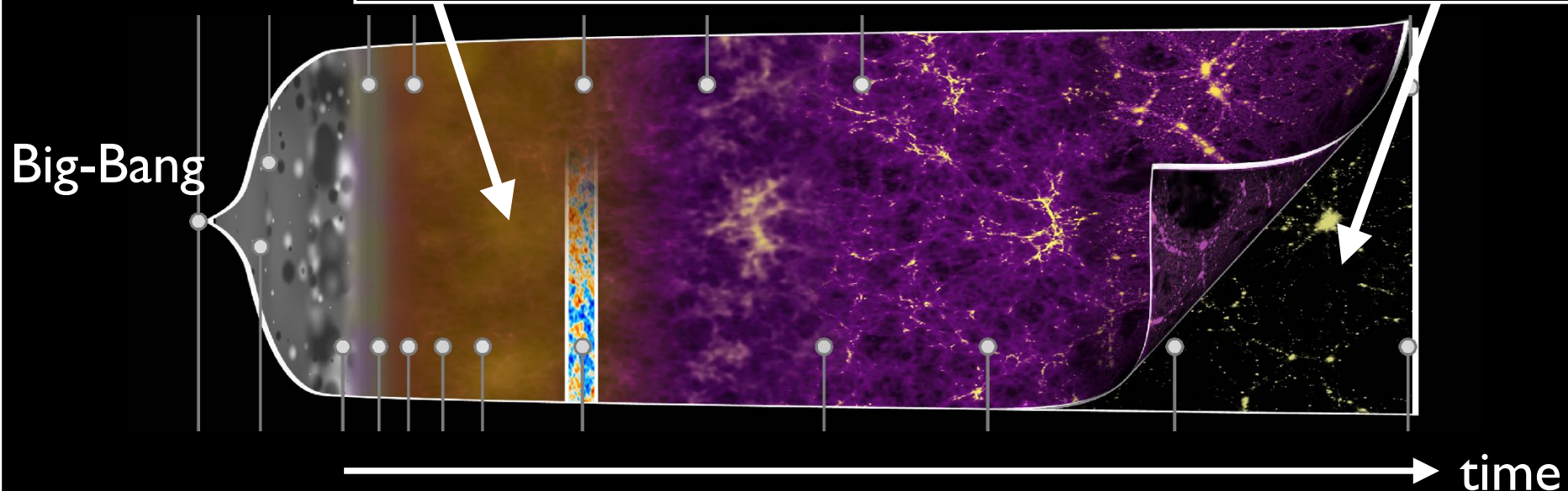
Early-time solution

change cosmic expansion before recombination or recombination history

measurement

Late-time solution

change cosmic expansion in the nearby universe



Incomplete

Proposed scenarios

Early-time or Late-time solution

- Early dark energy @ rad-matter equality
Poulin, Smith, Karwal & Kamionkowski ('19)
- Strongly self-interacting neutrinos with $N_{\text{eff}} \sim 4$
Kreisch, Cyr-Rachine & Doré ('19)
- Early-time modification of gravity
Braglia et al. ('20)
- Nonlinear small-scale fluctuations by primordial magnetic field
Jedamzik & Pogosian ('20)
- Change of background CMB temperature
Ivanov, Ali-Haimoud & Lesgourgues ('20); Bose & Lombrizer ('20)
- Time varying electron mass
Sekiguchi & Takahashi ('20)
- Late-time modification of gravity
(Generalized Proca, MTMG)
De Felice, Mukohyama & Pookkillath ('20)
De Felice, Geng, Pookkillath & Yin ('20)

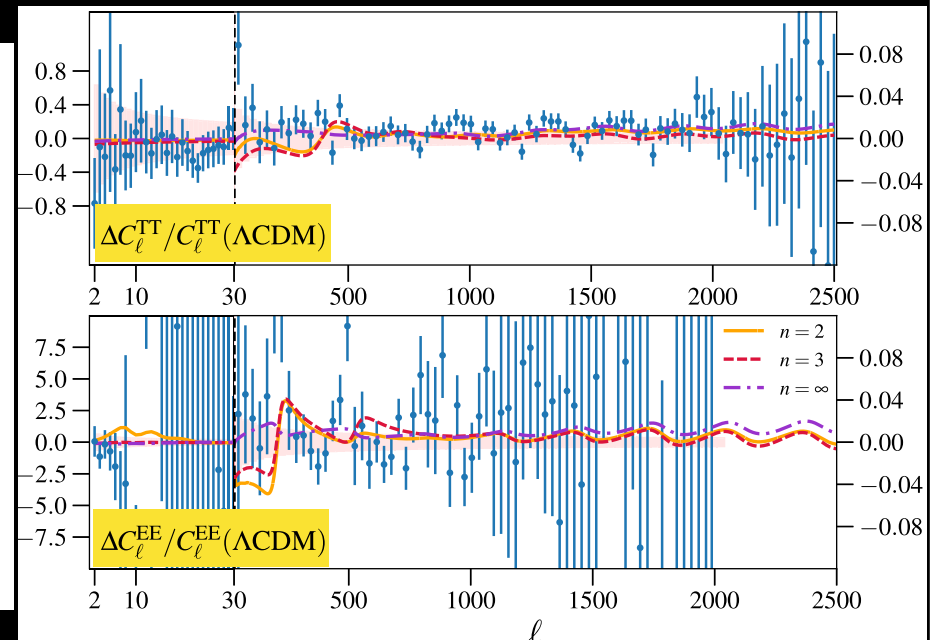
Early dark energy

Adding a tiny amount of dark energy at the time of pre-recombination epoch Poulin et al. ('19)

2 parameters: a_c , $f_{\text{EDE}}(a_c)$

a_c : scale factor at which DE contribution become maximum

Parameter	ΛCDM	Early DE (n=3)
$100\theta_s$	$1.04198(1.04213) \pm 0.0003$	$1.04138(1.0414) \pm 0.0004$
$100\omega_b$	$2.238(2.239) \pm 0.014$	$2.255(0.258) \pm 0.022$
ω_{cdm}	$0.1179(0.1177) \pm 0.0012$	$0.1272(0.1299) \pm 0.0045$
$10^9 A_s$	$2.176(2.14) \pm 0.051$	$2.176(2.177) \pm 0.054$
n_s	$0.9686(0.9687) \pm 0.0044$	$0.9812(0.9880) \pm 0.0080$
τ_{reio}	$0.075(0.068) \pm 0.013$	$0.068(0.068) \pm 0.013$
$\log_{10}(a_c)$...	$-3.737(-3.696)^{+0.110}_{-0.094}$
$f_{\text{EDE}}(a_c)$...	$0.050(0.058)^{+0.024}_{-0.019}$
$r_s(z_{\text{rec}})$	$145.05(145.1) \pm 0.26$	$140.3(138.9)^{+1.9}_{-2.3}$
S_8	$0.824(0.814) \pm 0.012$	$0.838(0.842) \pm 0.015$
H_0	$68.18(68.33) \pm 0.54$	$70.6(71.6) \pm 1.3$



$$\rightarrow z_c \simeq 5,000 \ \& \ f_{\text{EDE}}(a_c) \equiv \left. \frac{\rho_{\text{EDE}}}{\rho_{\text{tot}}} \right|_{a_c} \simeq 0.05$$

- Incompatible with LSS data (Shape of P(k))
- **S8 tension** remains significant

S_8 tension

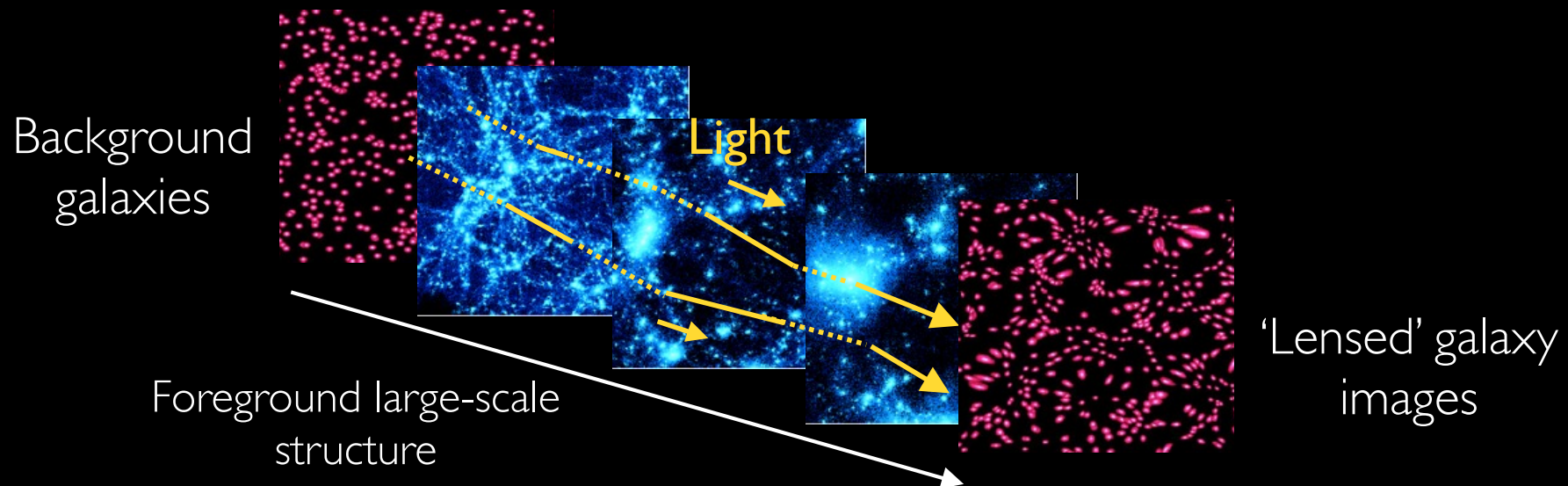
Yet another tension with Planck CMB

$$S_8 \equiv \sigma_8 (\Omega_m / 0.3)^{0.5}$$

RMS fluctuation
amplitude at 8 Mpc/h

Density parameter of
(non-relativistic) matter

Weak-lensing observations prefer a larger S_8 than that of Planck



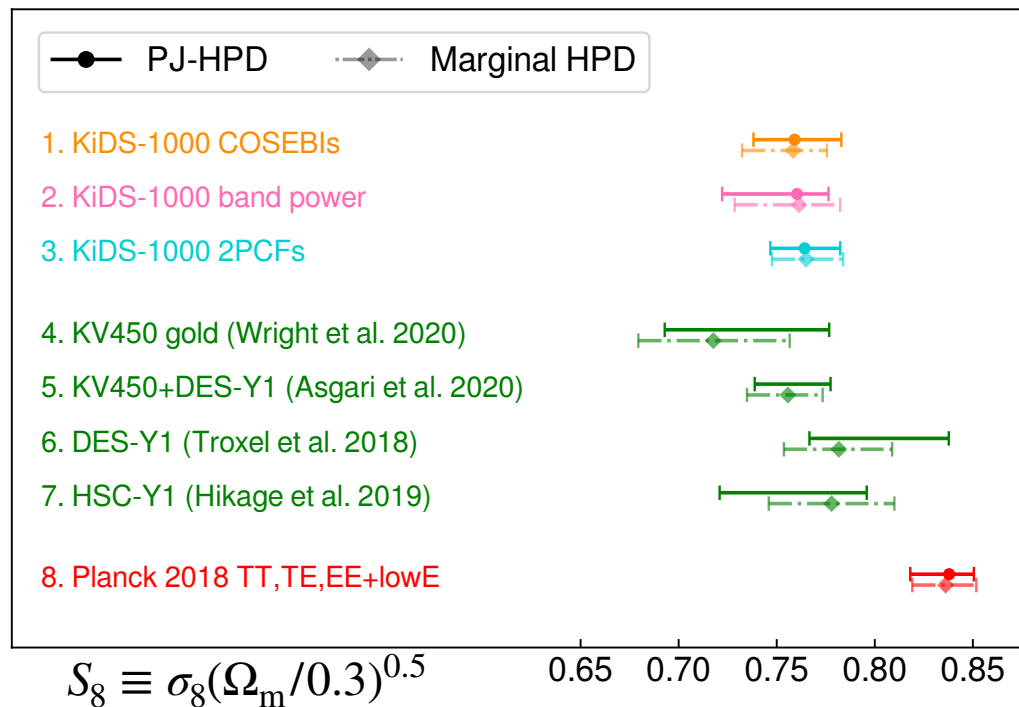
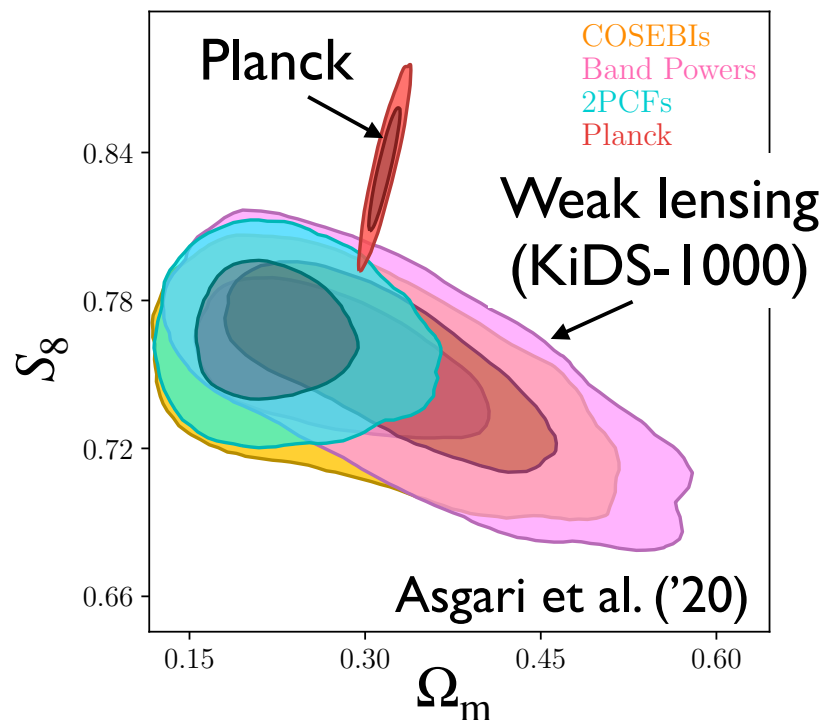
S_8 tension

Yet another tension with Planck CMB

$$S_8 \equiv \sigma_8 (\Omega_m / 0.3)^{0.5}$$

RMS fluctuation
amplitude at 8 Mpc/h

Density parameter of
(non-relativistic) matter



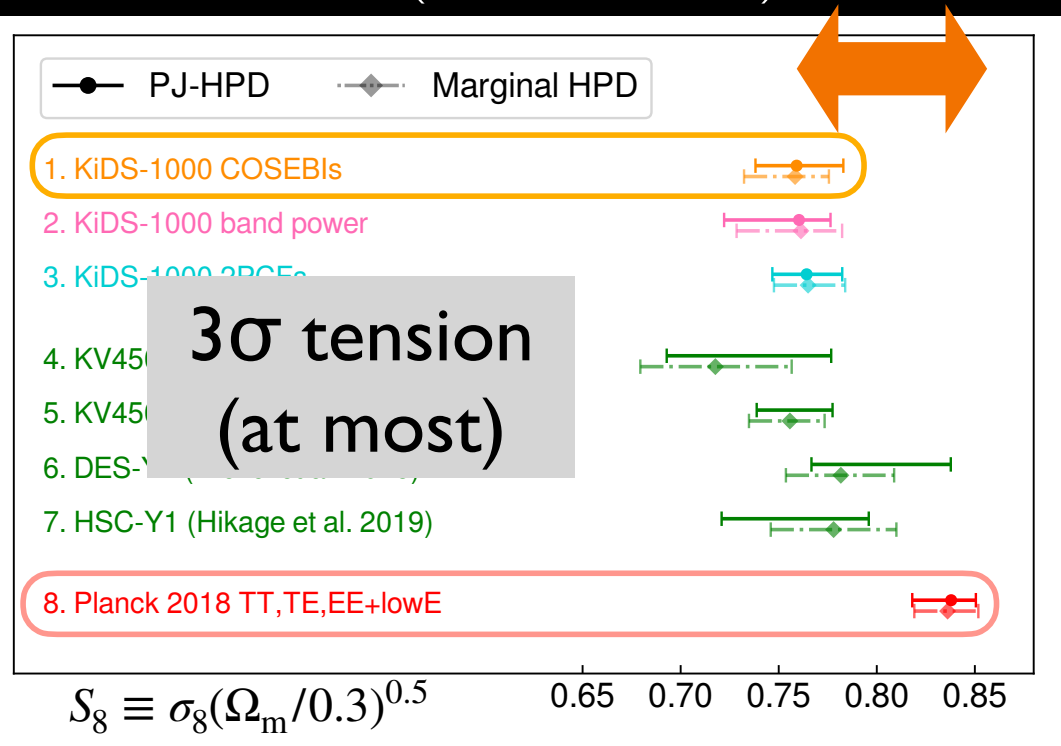
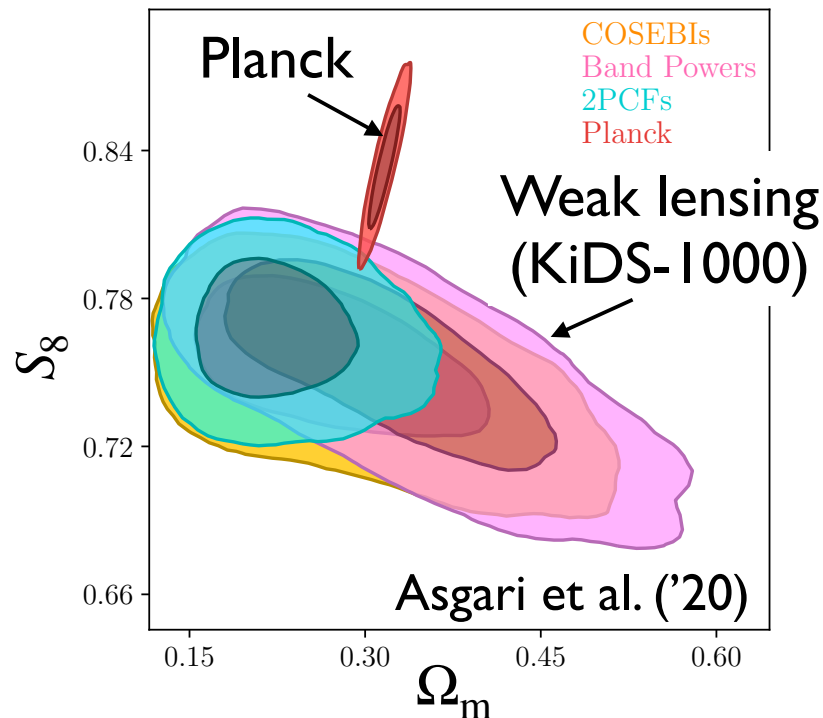
S_8 tension

Yet another tension with Planck CMB

$$S_8 \equiv \sigma_8 (\Omega_m / 0.3)^{0.5}$$

RMS fluctuation amplitude at 8 Mpc/h

Density parameter of (non-relativistic) matter



Summary

H_0 tension appears manifest and gets serious since the CMB measurements by Planck

- Low- z measurements prefer higher H_0 (*model-indept. distance ladder*)
- Hi- z measurements prefer lower H_0 (*based on Λ CDM model*)

New physics ? but most of the (early-time) solutions has troubles

Another tension (**S_8 tension**) is now highlighted

and has to be solved simultaneously (if possible)

Unknown systematics ?

Planck has some internal anomalies

- A_L (lensing) anomaly
- Curvature anomaly

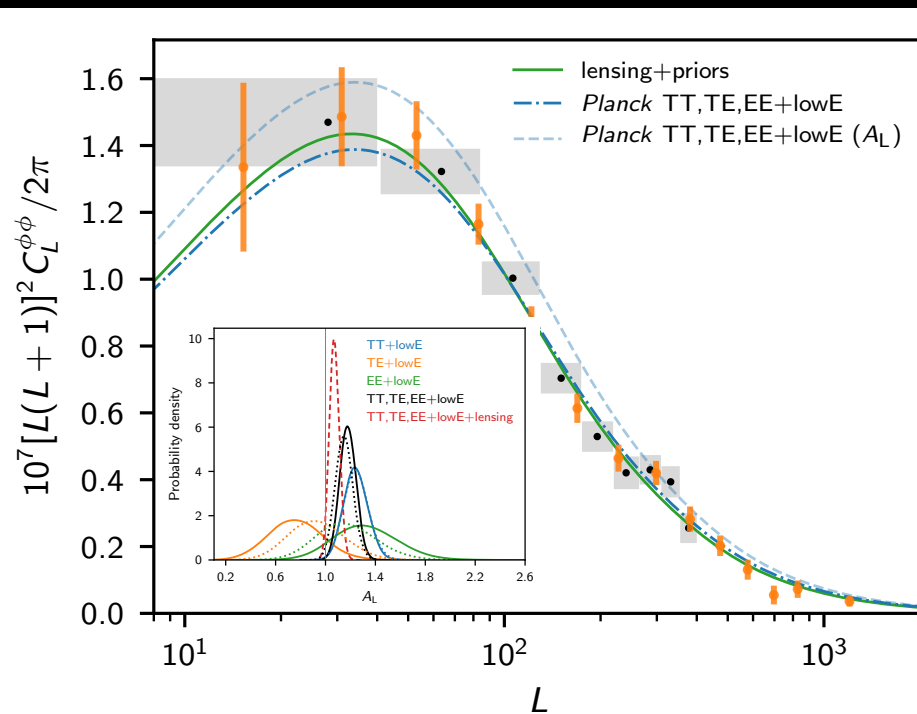
SH0ES internal inconsistencies G. Efstathiou ('20)

Planck internal anomalies

Planck 2018 results VI.

A_L anomaly

Allowing the lensing amplitude to vary gives a larger best-fit value

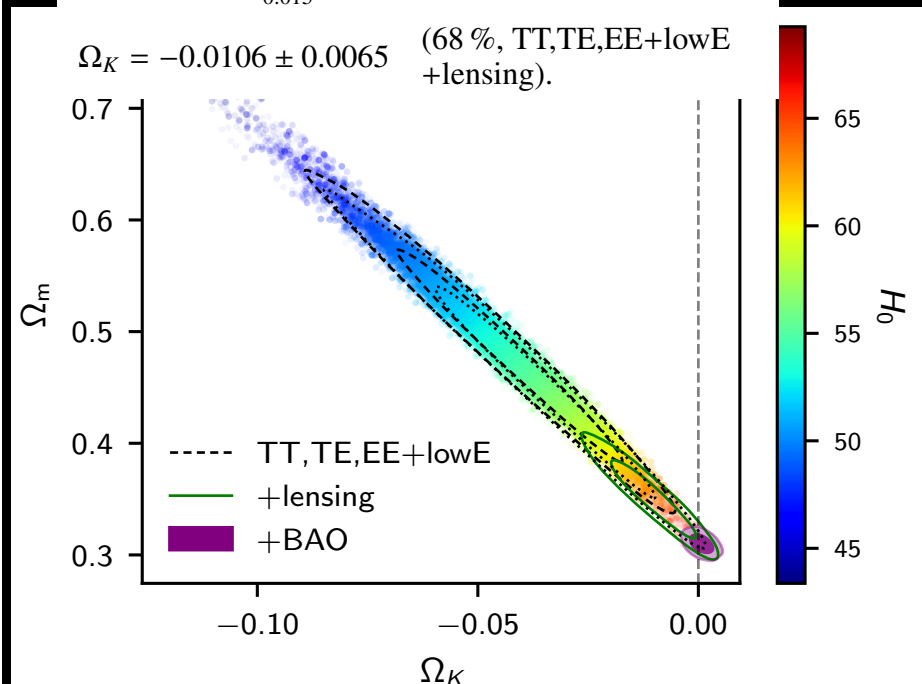


Curvature anomaly

One parameter extension to Λ CDM prefer positive curvature

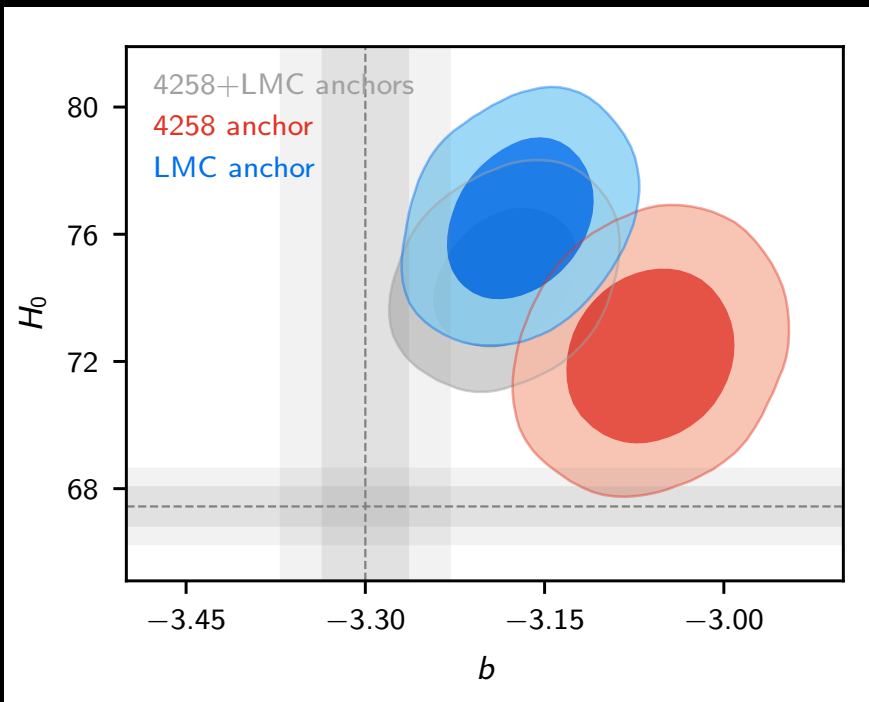
$$\Omega_K = -0.044^{+0.018}_{-0.015} \quad (68\%, \text{Planck TT,TE,EE+lowE}),$$

$$\Omega_K = -0.0106 \pm 0.0065 \quad (68\%, \text{TT,TE,EE+lowE} \\ \text{+lensing}).$$

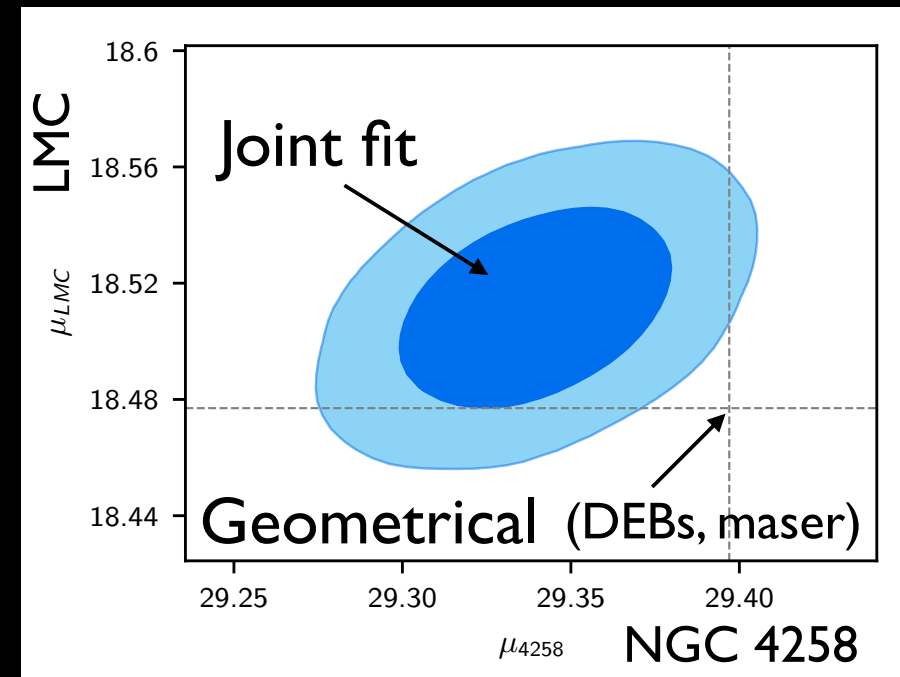


SH₀ES internal consistency

No prior on P-L relation



slope of P-L relation



Distance moduli

Efstathiou ('20)