

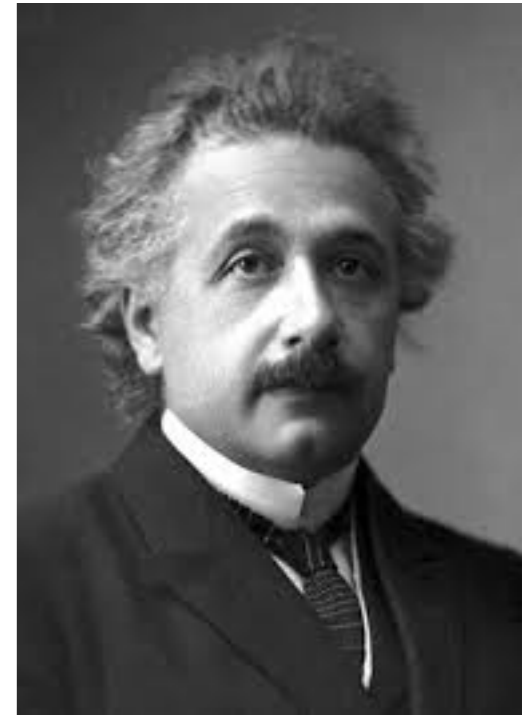
# SUSY dark matter, axion, LHC and ILC



Howard Baer  
University of Oklahoma

DSU2015, Kyoto

twin pillars of guidance:  
naturalness & simplicity



“The appearance of fine-tuning in a scientific theory is like a cry of distress from nature, complaining that something needs to be better explained”

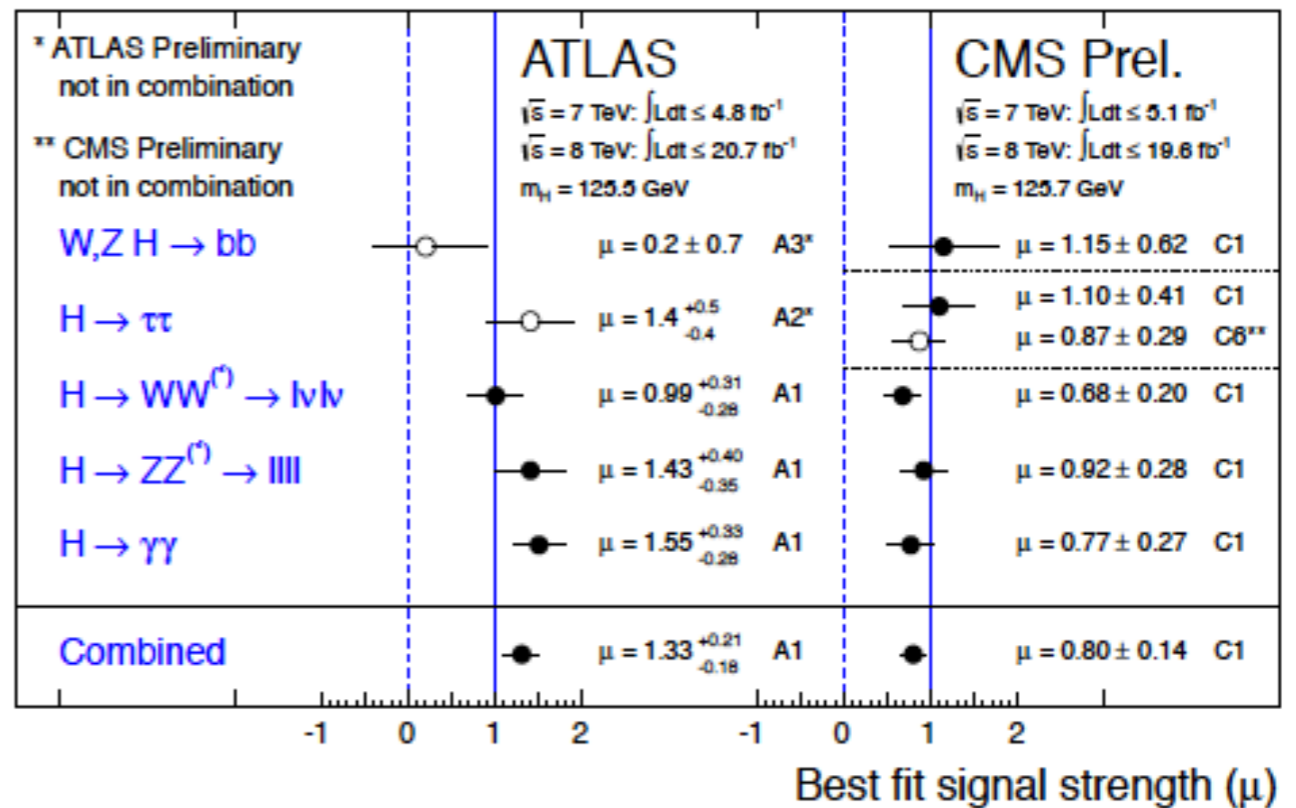
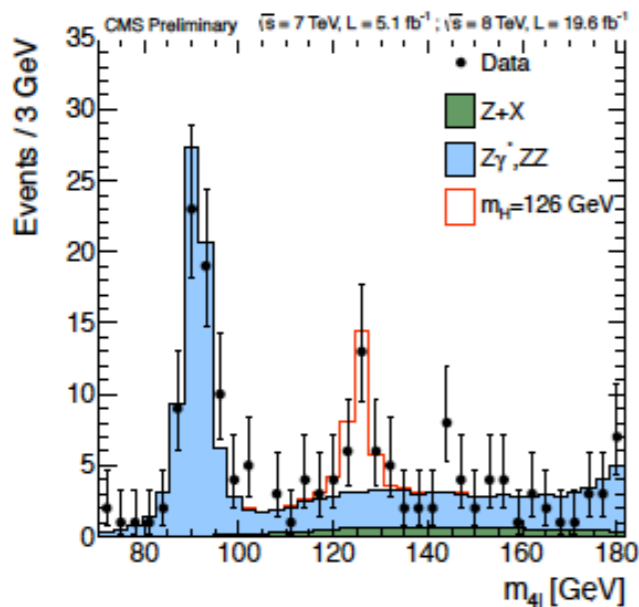
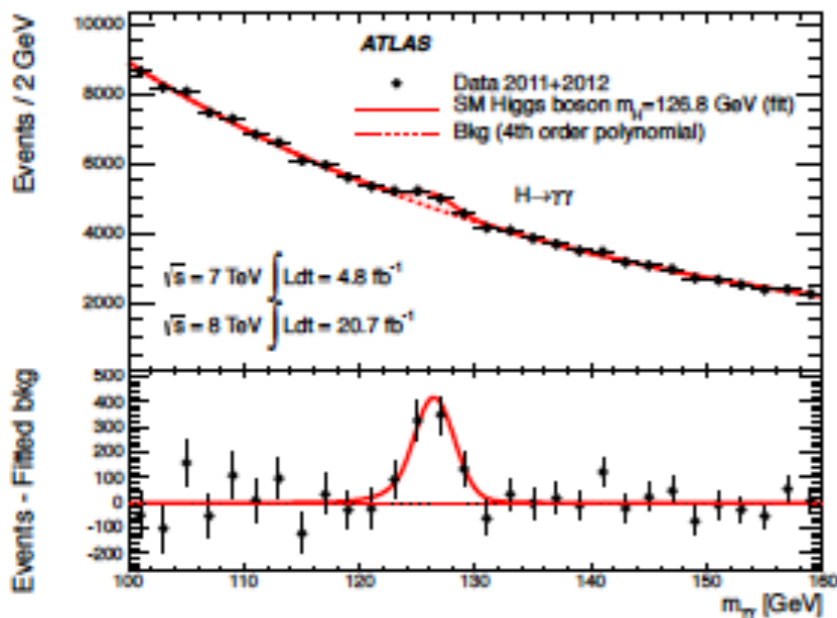
S. Weinberg

“Everything should be made as simple as possible, but not simpler”

A. Einstein

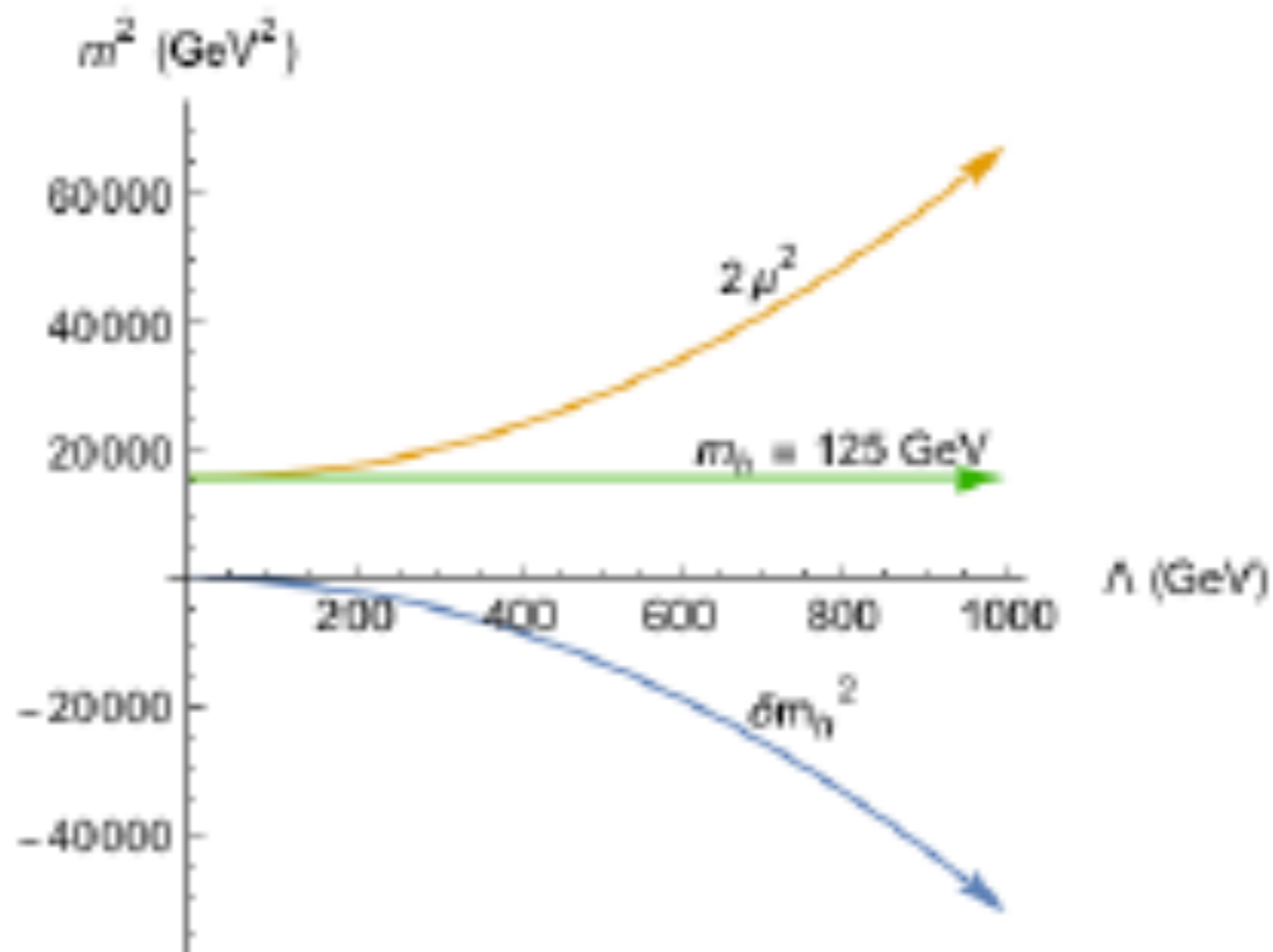
# Brief summary of SM:

We have found a very SM-like Higgs boson with  $m(h)=125$  GeV at LHC but nothing yet beyond the SM



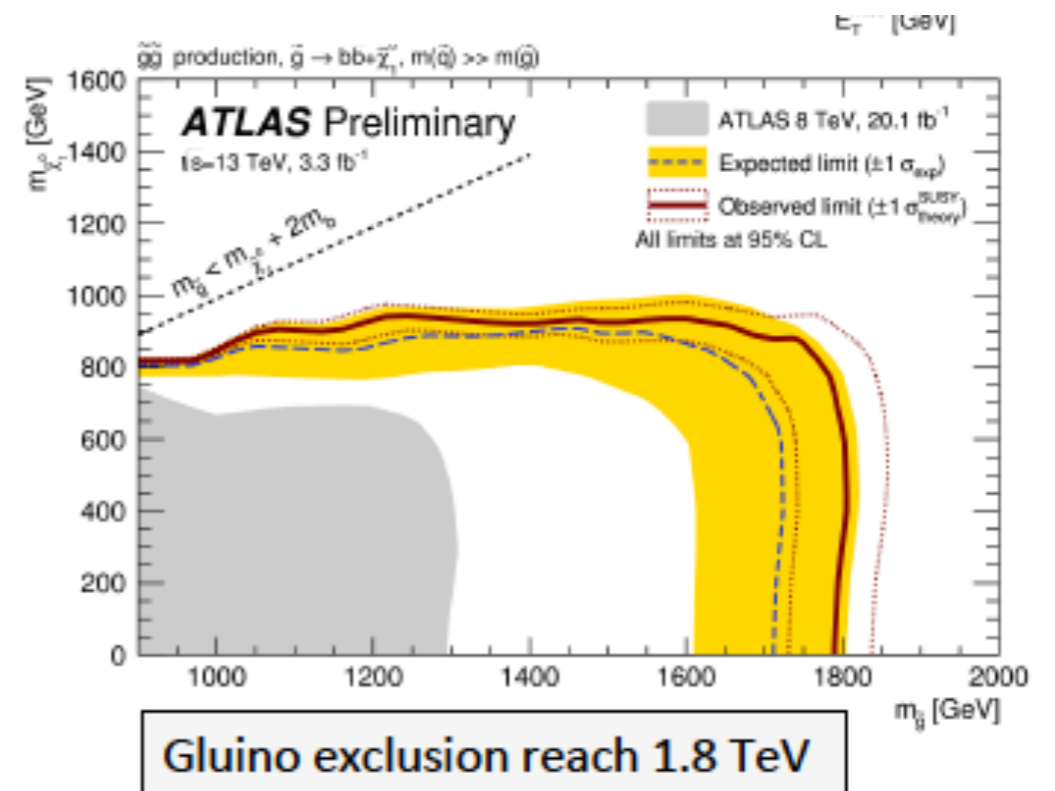
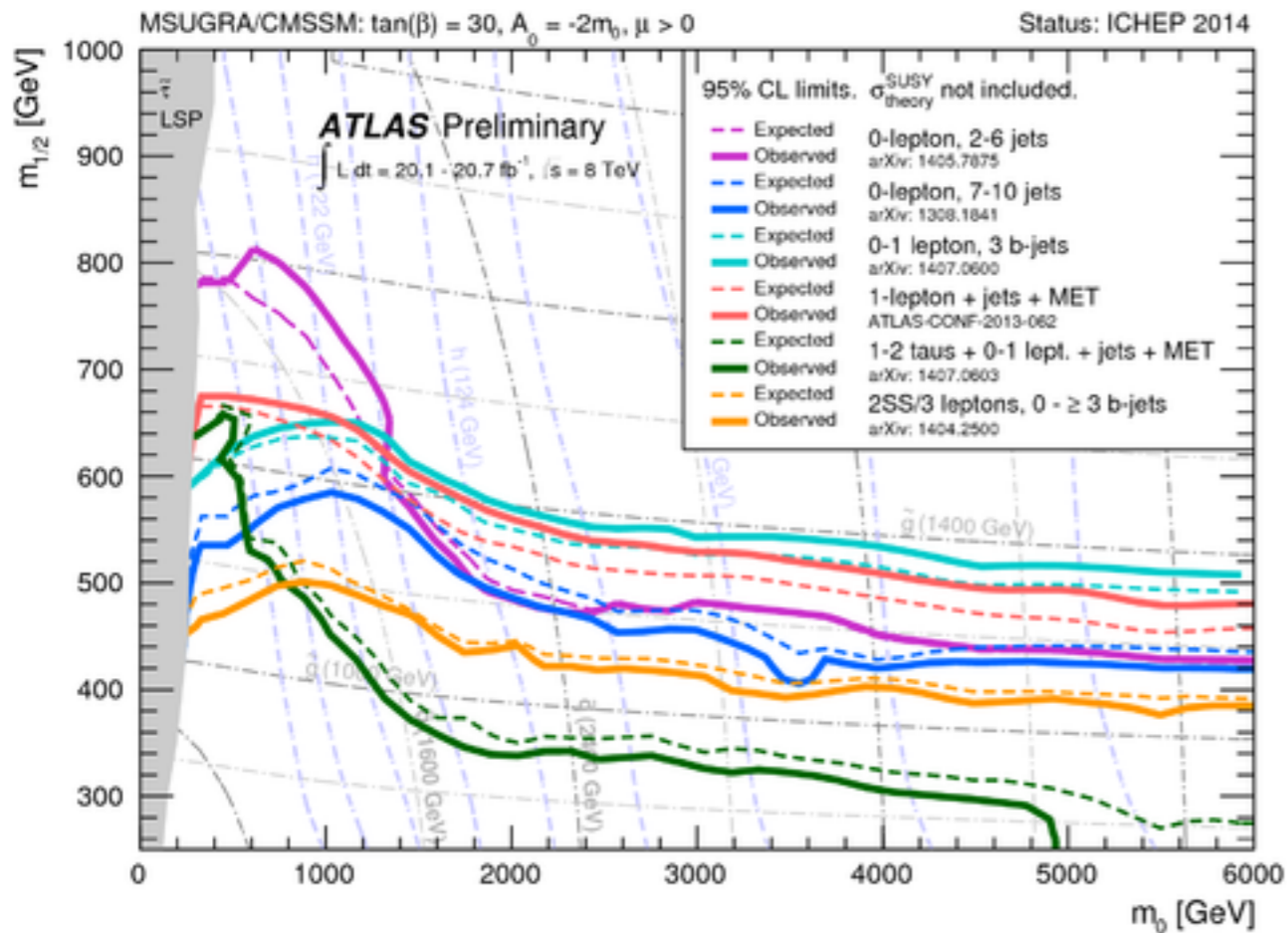
# But the Higgs mass problem remains

Wilson 1972  
Weinberg  
Gildener



Independent radiative corrections to  $m(h)$  should be smaller than  $m(h)$ : SM only valid below  $\sim 1 \text{ TeV}$

# SUSY tames scalar mass problem in elegant fashion: but where are sparticles?



$$m_{\tilde{g}} > 1.3 \text{ TeV for } m_{\tilde{q}} \gg m_{\tilde{g}}$$

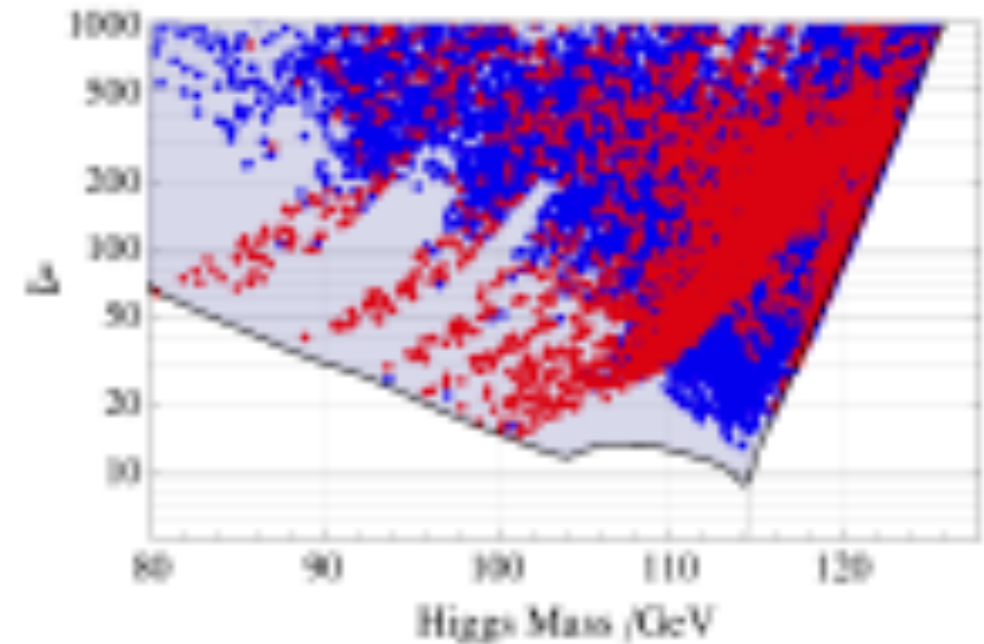
$$m_{\tilde{g}} > 1.8 \text{ TeV}$$

$$m_{\tilde{g}} > 1.8 \text{ TeV for } m_{\tilde{q}} \sim m_{\tilde{g}}$$

$$m_{\tilde{t}_1} \sim \text{multi-TeV for } m_h \simeq 125 \text{ GeV}$$

These bounds appear in sharp conflict with EW “naturalness”

	mass
gluino	400 GeV
uR	400 GeV
eR	350 GeV
chargino	100 GeV
neutralino	50 GeV

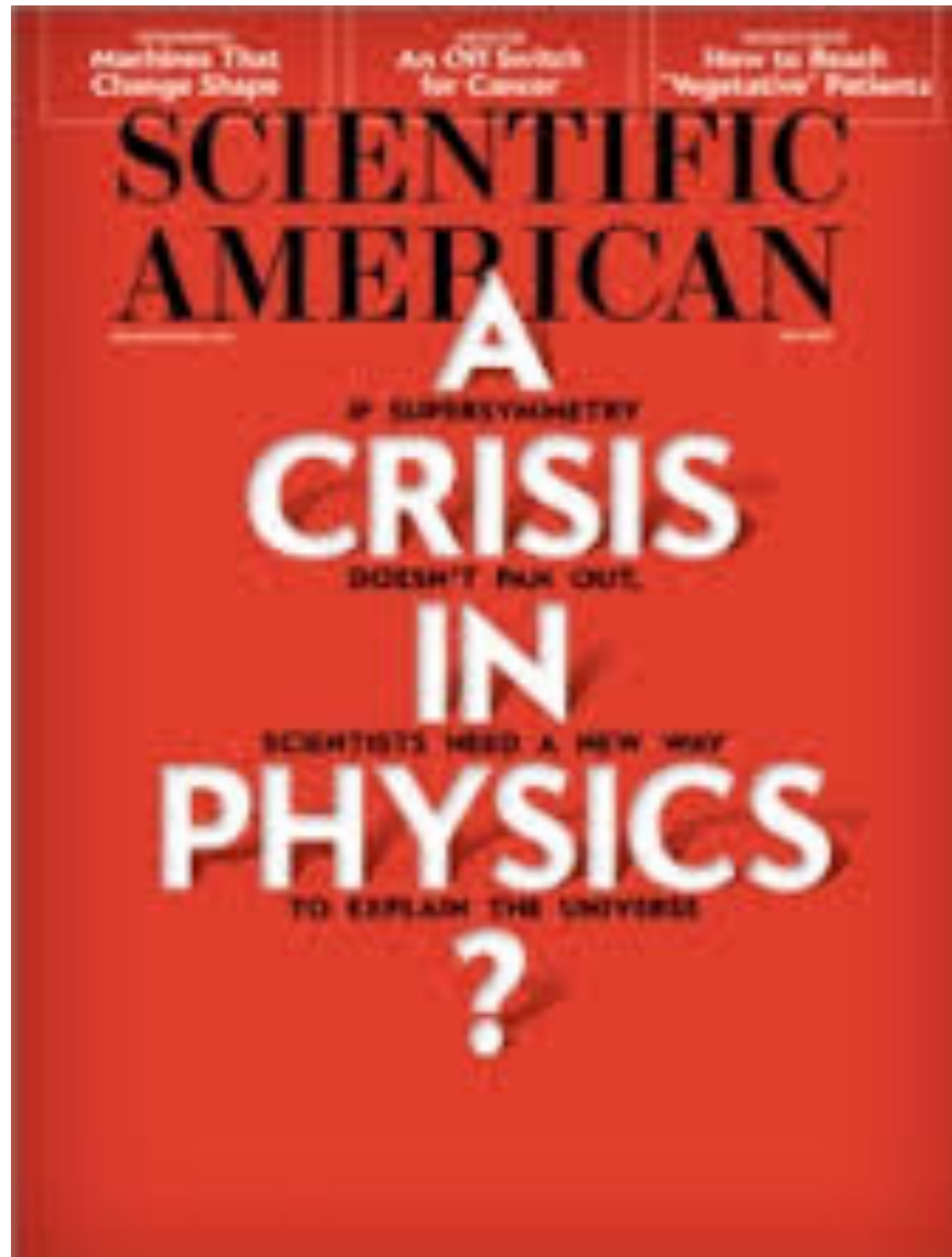


Cassel, Ghilencea, Ross, 2009

$\Delta \rightarrow 1000$   
as  $m_h \rightarrow 125$  GeV  
0.1% tuning!?

Barbieri-Giudice 10% bounds, 1987

# Is there a crisis in physics?



short answer:  
**No!** but there may be a crisis  
in how theorists  
calculate naturalness

*This unshakable fidelity to supersymmetry is widely shared. Particle theorists do admit, however, that the idea of natural supersymmetry is already in trouble and is headed for the dustbin of history unless superpartners are discovered soon...*

“...settling the ultimate fate of naturalness is perhaps the most profound theoretical question of our time”

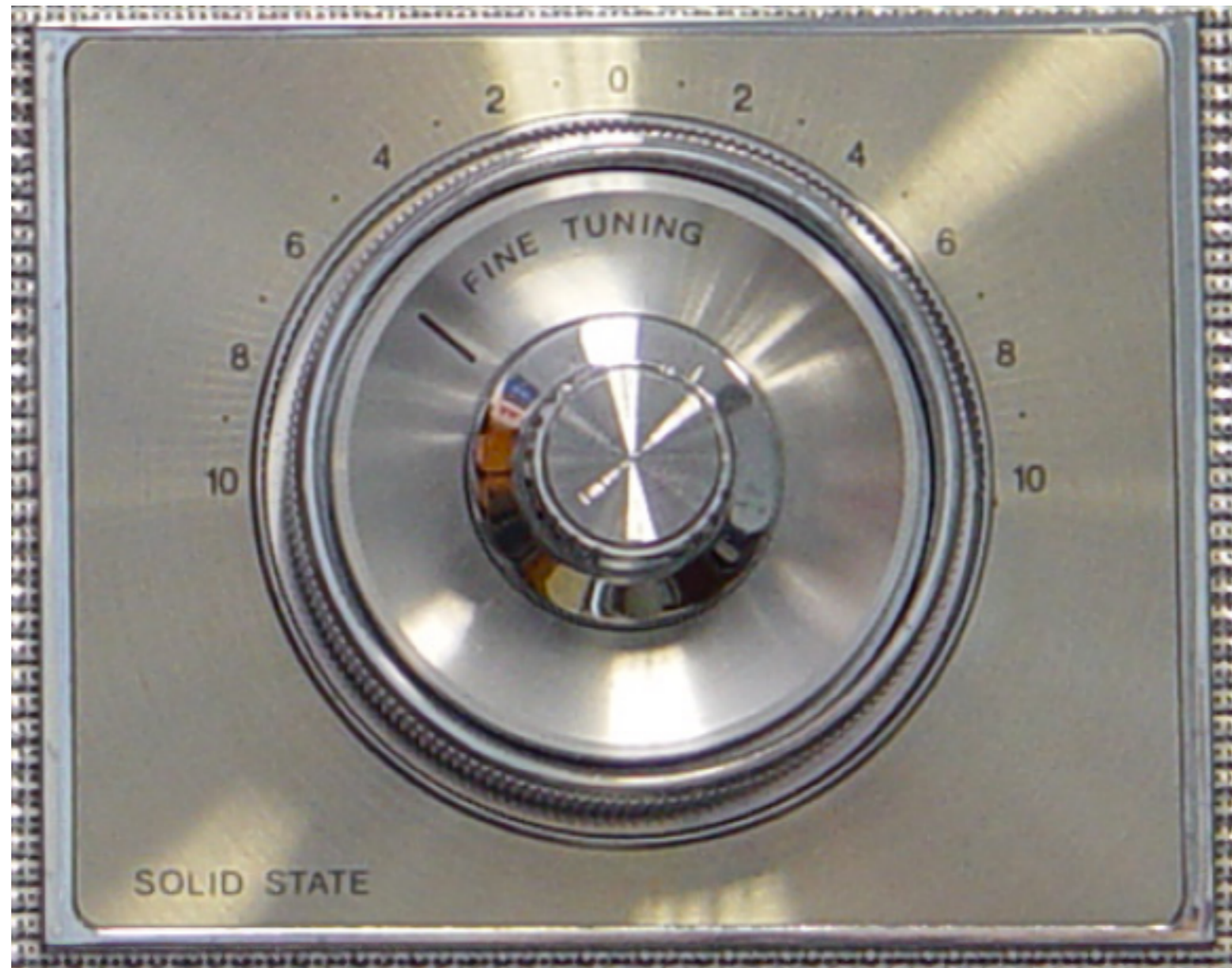


Arkani-Hamed et al.,  
arXiv:1511.06495

“Given the magnitude of the stakes involved,  
it is vital to get a clear verdict  
on naturalness from experiment”

This should be matched by theoretical scrutiny  
of what we mean by naturalness

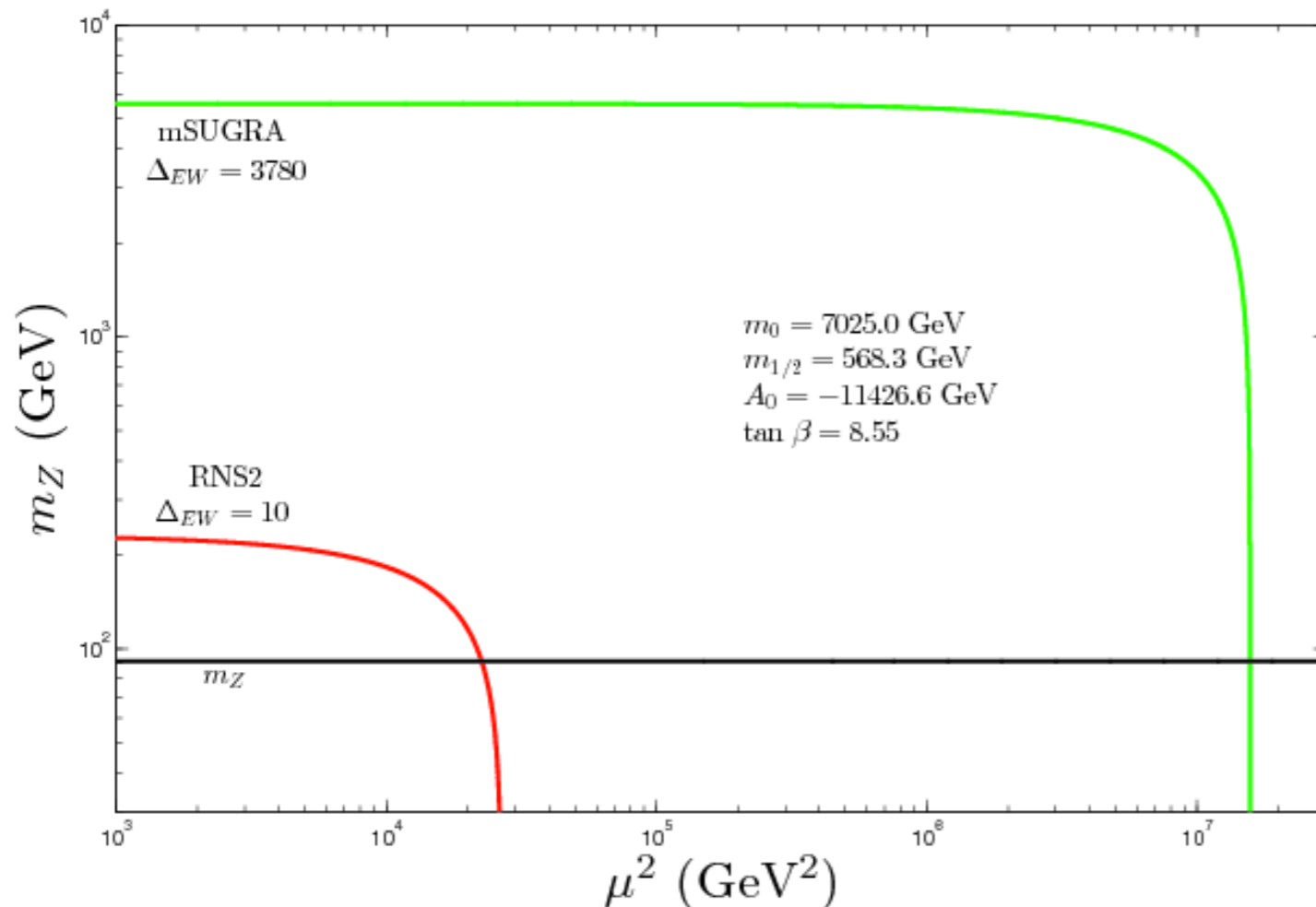
# Three measures of fine-tuning:



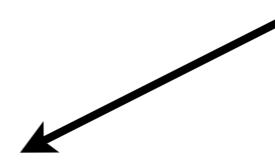


First: simple electroweak fine-tuning in SUSY:  
 dial value of  $\mu$  so that Z mass comes out right:  
 everybody does it but it is hidden inside spectra  
 codes (Isajet, SuSpect, SoftSUSY, Spheno, SSARD)

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \Sigma_u^u - \mu^2$$



e.g. in CMSSM/  
 mSUGRA:  
 one then concludes  
 nature  
 gives this:



**#1:** Most conservative, simple measure:  $\Delta_{EW}$

Working only at the weak scale, minimize scalar potential: calculate  $m(Z)$  or  $m(h)$

No large uncorrelated cancellations in  $m(Z)$  or  $m(h)$

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \sim -m_{H_u}^2 - \Sigma_u^u - \mu^2$$

$$\Delta_{EW} \equiv \max_i |C_i| / (m_Z^2/2) \quad \text{with} \quad C_{H_u} = -m_{H_u}^2 \tan^2 \beta / (\tan^2 \beta - 1) \quad \text{etc.}$$

simple, direct, unambiguous interpretation:

- $|\mu| \sim m_Z \sim 100 - 200 \text{ GeV}$
- $m_{H_u}^2$  should be driven to small negative values such that  $-m_{H_u}^2 \sim 100 - 200 \text{ GeV}$  at the weak scale and
- that the radiative corrections are not too large:  $\Sigma_u^u \lesssim 100 - 200 \text{ GeV}$

CETUP\*-12/002, FTPI-MINN-12/22, UMN-TH-3109/12, UH-511-1195-12

Radiative natural SUSY with a 125 GeV Higgs boson

Howard Baer,<sup>1</sup> Vernon Barger, Peisi Huang,<sup>2</sup> Azar Mustafayev,<sup>3</sup> and Xerxes Tata<sup>4</sup>

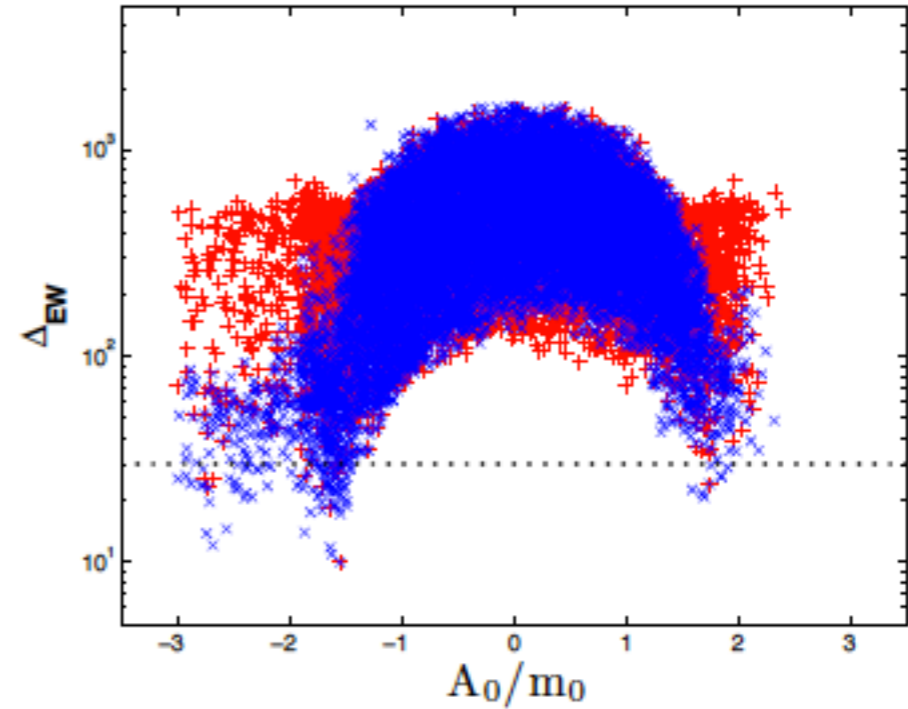
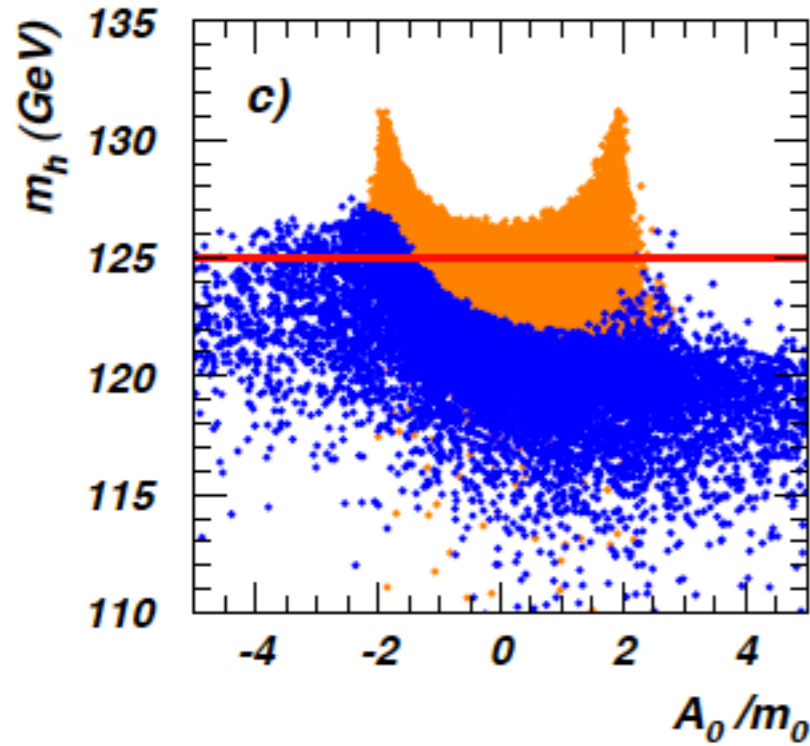
<sup>1</sup>Dept. of Physics and Astronomy, University of Oklahoma, Norman, OK, 73019, USA

<sup>2</sup>Dept. of Physics, University of Wisconsin, Madison, WI 53706, USA

<sup>3</sup>W. I. Fine Institute for Theoretical Physics, University of Minnesota, Minneapolis, MN 55455, USA

PRL109 (2012) 161802

Large value of  $A_t$  reduces  $\Sigma_u^u(\tilde{t}_{1,2})$  contributions to  $\Delta_{EW}$  while uplifting  $m_h$  to  $\sim 125$  GeV



$$\Sigma_u^u(\tilde{t}_{1,2}) = \frac{3}{16\pi^2} F(m_{\tilde{t}_{1,2}}^2) \left[ f_t^2 - g_Z^2 \mp \frac{f_t^2 A_t^2 - 8g_Z^2 (\frac{1}{4} - \frac{2}{3}x_W) \Delta_t}{m_{\tilde{t}_2}^2 - m_{\tilde{t}_1}^2} \right]$$

$$\Delta_t = (m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)/2 + M_Z^2 \cos 2\beta (\frac{1}{4} - \frac{2}{3}x_W)$$

$$F(m^2) = m^2 \left( \log \frac{m^2}{Q^2} - 1 \right) \quad Q^2 = m_{\tilde{t}_1} m_{\tilde{t}_2}$$

## #2: Higgs mass or large-log fine-tuning $\Delta_{HS}$

It is tempting to pick out one-by-one quantum fluctuations **but** must combine log divergences before taking any limit

$$m_h^2 \simeq \mu^2 + m_{H_u}^2 + \delta m_{H_u}^2|_{rad}$$

$$\frac{dm_{H_u}^2}{dt} = \frac{1}{8\pi^2} \left( -\frac{3}{5}g_1^2 M_1^2 - 3g_2^2 M_2^2 + \frac{3}{10}g_1^2 S + 3f_t^2 X_t \right) \quad X_t = m_{Q_3}^2 + m_{U_3}^2 + m_{H_u}^2 + A_t^2$$

neglect gauge pieces, S,  $m_{H_u}$  and running;  
then we can integrate from  $m(SUSY)$  to  $\Lambda$

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

$$\Delta_{HS} \sim \delta m_h^2 / (m_h^2/2) < 10$$

$$m_{\tilde{t}_{1,2}, \tilde{b}_1} < 500 \text{ GeV}$$

$$m_{\tilde{g}} < 1.5 \text{ TeV}$$

**old natural SUSY**

then

$A_t$  can't be too big

Most claims against SUSY stem from **overestimates** of EW fine-tuning.

These arise from violations of the

**Prime directive on fine-tuning:**

“Thou shalt not claim fine-tuning of **dependent** quantities one against another!”

HB, Barger, Mickelson, Padeffke-Kirkland, arXiv:1404.2277

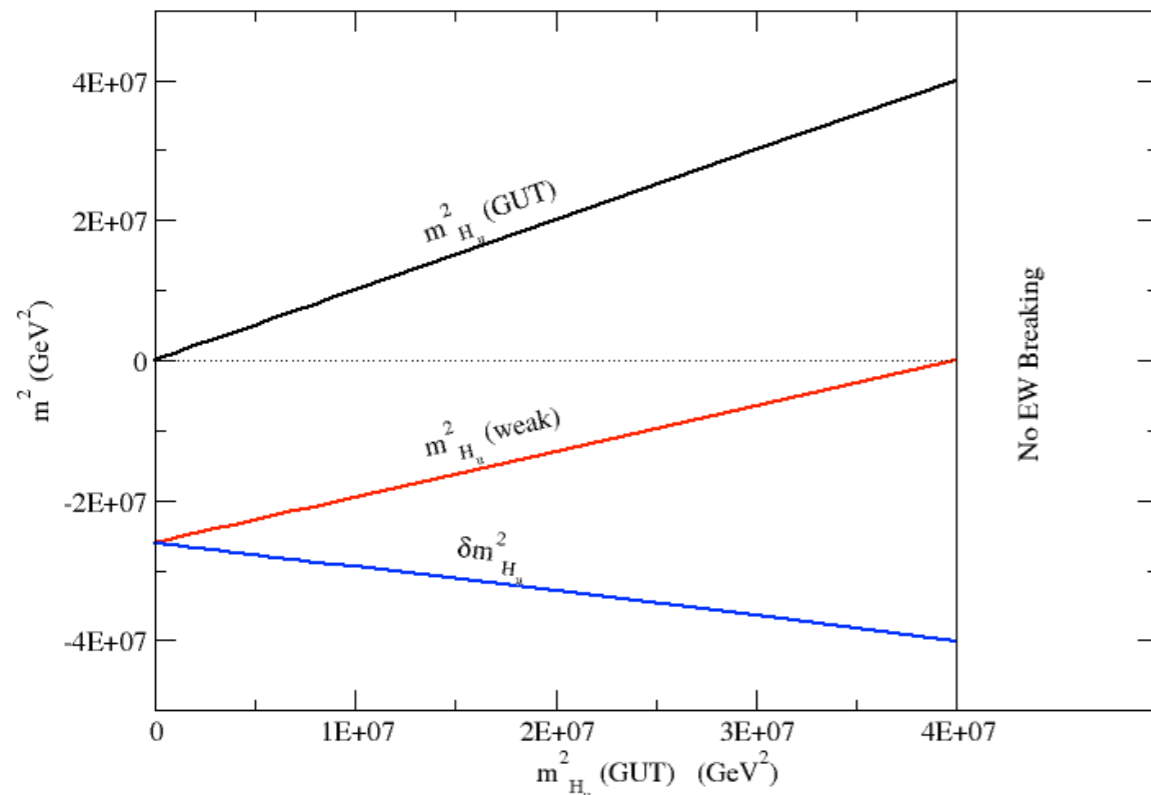


Is  $\mathcal{O} = \mathcal{O} + b - b$  fine-tuned for  $b > \mathcal{O}$ ?

What's wrong with this argument?  
 In zeal for simplicity, have made several simplifications: most **egregious** is that one sets  $m(H_u)^2=0$  at beginning to simplify

$m_{H_u}^2(\Lambda)$  and  $\delta m_{H_u}^2$  are *not* independent!

**violates prime directive!**



The larger  $m_{H_u}^2(\Lambda)$  becomes, then the larger becomes the cancelling correction!

HB, Barger, Savoy

To fix: combine dependent terms:

$$m_h^2 \simeq \mu^2 + (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2) \text{ where now both } \mu^2 \text{ and } (m_{H_u}^2(\Lambda) + \delta m_{H_u}^2) \text{ are } \sim m_Z^2$$

After re-grouping:

$$\Delta_{HS} \simeq \Delta_{EW}$$

Instead of: the radiative correction  $\delta m_{H_u}^2 \sim m_Z^2$   
we now have: the radiatively-corrected  $m_{H_u}^2 \sim m_Z^2$

Recommendation: put this horse out to pasture

$$\delta m_{H_u}^2 \sim -\frac{3f_t^2}{8\pi^2} (m_{Q_3}^2 + m_{U_3}^2 + A_t^2) \ln(\Lambda/m_{SUSY})$$

R.I.P.

sub-TeV 3rd generation squarks **not** required for naturalness



### #3: EENZ/BG traditional measure $\Delta_{BG}$

Such a re-grouping is properly used in the EENZ/BG measure:

$$\Delta_{BG} \equiv \max_i [c_i], \quad \text{where } c_i = \left| \frac{\partial \ln m_Z^2}{\partial \ln p_i} \right| = \left| \frac{p_i}{m_Z^2} \frac{\partial m_Z^2}{\partial p_i} \right|$$

the  $p_i$  constitute the fundamental parameters of the model.

for pMSSM, obviously  $\Delta_{BG} \simeq \Delta_{EW}$

What about models defined at high scale?

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 - m_{H_u}^2 \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2 \simeq -m_{H_u}^2 - \mu^2$$

express **weak scale value** in terms of high scale parameters

Express  $m(Z)$  in terms of GUT scale parameters:

$$m_Z^2 \simeq -2m_{H_u}^2 - 2\mu^2 \quad (\text{weak scale relation})$$

$$-2\mu^2(m_{SUSY}) = -2.18\mu^2$$

$$\begin{aligned} -2m_{H_u}^2(m_{SUSY}) = & 3.84M_3^2 + 0.32M_3M_2 + 0.047M_1M_3 - 0.42M_2^2 \\ & + 0.011M_2M_1 - 0.012M_1^2 - 0.65M_3A_t - 0.15M_2A_t \\ & - 0.025M_1A_t + 0.22A_t^2 + 0.004m_3A_b \\ & - 1.27m_{H_u}^2 - 0.053m_{H_d}^2 \\ & + 0.73m_{Q_3}^2 + 0.57m_{U_3}^2 + 0.049m_{D_3}^2 - 0.052m_{L_3}^2 + 0.053m_{E_3}^2 \\ & + 0.051m_{Q_2}^2 - 0.11m_{U_2}^2 + 0.051m_{D_2}^2 - 0.052m_{L_2}^2 + 0.053m_{E_2}^2 \\ & + 0.051m_{Q_1}^2 - 0.11m_{U_1}^2 + 0.051m_{D_1}^2 - 0.052m_{L_1}^2 + 0.053m_{E_1}^2, \end{aligned}$$

all GUT scale parameters

Ibanez, Lopez, Munoz;  
Lleyda, Munoz

Kane, King

Abe, Kobayashi, Omura;  
S. P. Martin

For generic parameter choices,  $\Delta_{BG}$  is large

But if:  $m_{Q_{1,2}} = m_{U_{1,2}} = m_{D_{1,2}} = m_{L_{1,2}} = m_{E_{1,2}} \equiv m_{16}(1,2)$  then  $\sim 0.007m_{16}^2(1,2)$

Even better:  $m_{H_u}^2 = m_{H_d}^2 = m_{16}^2(3) \equiv m_0^2 \Rightarrow -0.017m_0^2$

For correlated parameters, EWFT collapses in 3rd gen. sector!

Feng, Matchev, Moroi

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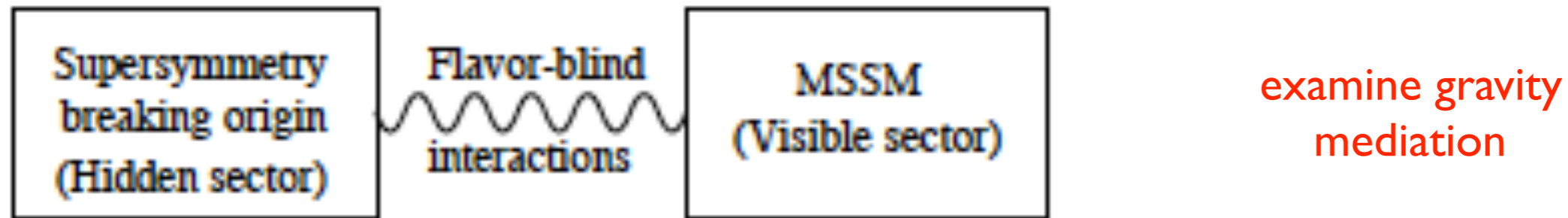
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Feng, Matchev, Moroi

- Usually  $\Delta_{BG}$  is applied to *multi-parameter effective theories* where multiple soft terms are adopted as parameter set.
- For these theories, the multiple soft terms parametrize our ignorance of details of the hidden sector SUSY breaking.
- But in supergravity, for any given hidden sector, soft terms are all *dependent* and can be computed as multiples of  $m_{3/2}$ .

Thus, the usual evaluation of  $\Delta_{BG}$  also **violates the prime directive!**

To properly apply BG measure, need to identify **independent** soft breaking terms



For any particular SUSY breaking hidden sector, each soft term is some multiple of gravitino mass  $m_{3/2}$

$$\begin{aligned} m_{H_u}^2 &= a_{H_u} \cdot m_{3/2}^2, \\ m_{Q_3}^2 &= a_{Q_3} \cdot m_{3/2}^2, \\ A_t &= a_{A_t} \cdot m_{3/2}, \\ M_i &= a_i \cdot m_{3/2}, \\ &\dots \end{aligned}$$

Soni, Weldon (1983);  
Kaplunovsky, Louis (1992);  
Brignole, Ibanez, Munoz (1993)

Since we don't know hidden sector, we impose parameters which parameterize our ignorance:

**but this doesn't mean each parameter is independent**

e.g. dilaton-dominated SUSY breaking:  $m_0^2 = m_{3/2}^2$  with  $m_{1/2} = -A_0 = \sqrt{3}m_{3/2}$

Writing each soft term as a multiple of  $m(3/2)$  then we allow for correlations/cancellations:

$$m_Z^2 = -2.18\mu^2 + a \cdot m_{3/2}^2$$

GUT scale param's

numerical co-efficient which depends on hidden sector

for naturalness, then

$$\mu^2 \sim m_Z^2 \quad \text{and} \quad a \cdot m_{3/2}^2 \sim m_Z^2$$

either  $m_{3/2} \sim m_Z$  or  $a$  is small

$$m_Z^2 \simeq -2\mu^2(\text{weak}) - 2m_{H_u}^2(\text{weak}) \simeq -2.18\mu^2(\text{GUT}) + a \cdot m_{3/2}^2$$

then

$$-m_{H_u}^2(\text{weak}) \sim a \cdot m_{3/2}^2 \sim m_Z^2$$

$$\lim_{n_{SSB} \rightarrow 1} \Delta_{BG} \rightarrow \Delta_{EW}$$

Thus, correctly applying these measures by first collecting dependent quantities, we find that— at tree level— all agree:

$$\Delta_{HS} \simeq \Delta_{BG} \simeq \Delta_{EW}$$

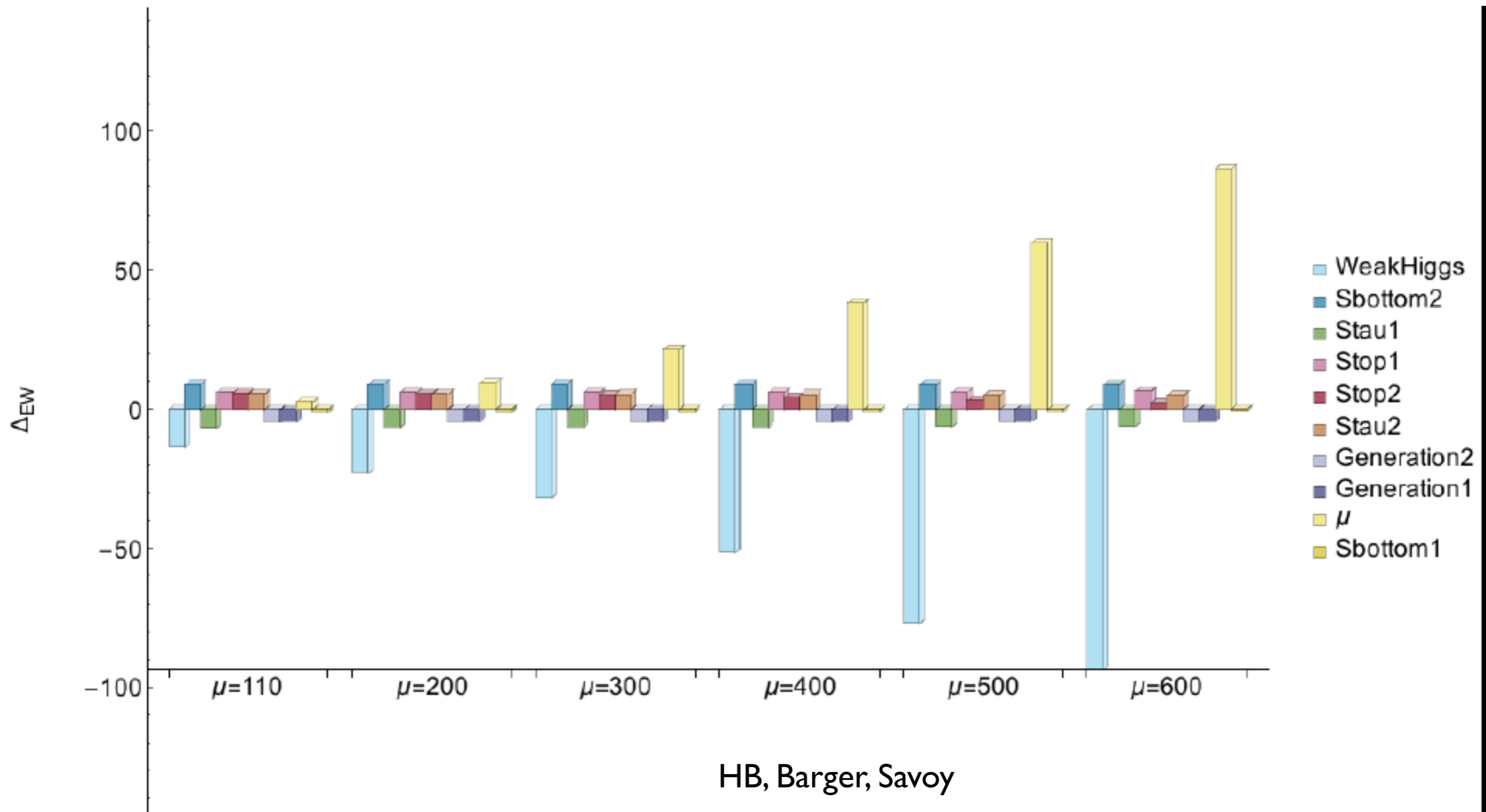
Due to ease of use and including radiative corrections, and due to its explicit model independence, we will use

$\Delta_{EW}$   
for remainder of talk

hard wired in  
Isasugra



# How much is too much fine-tuning?

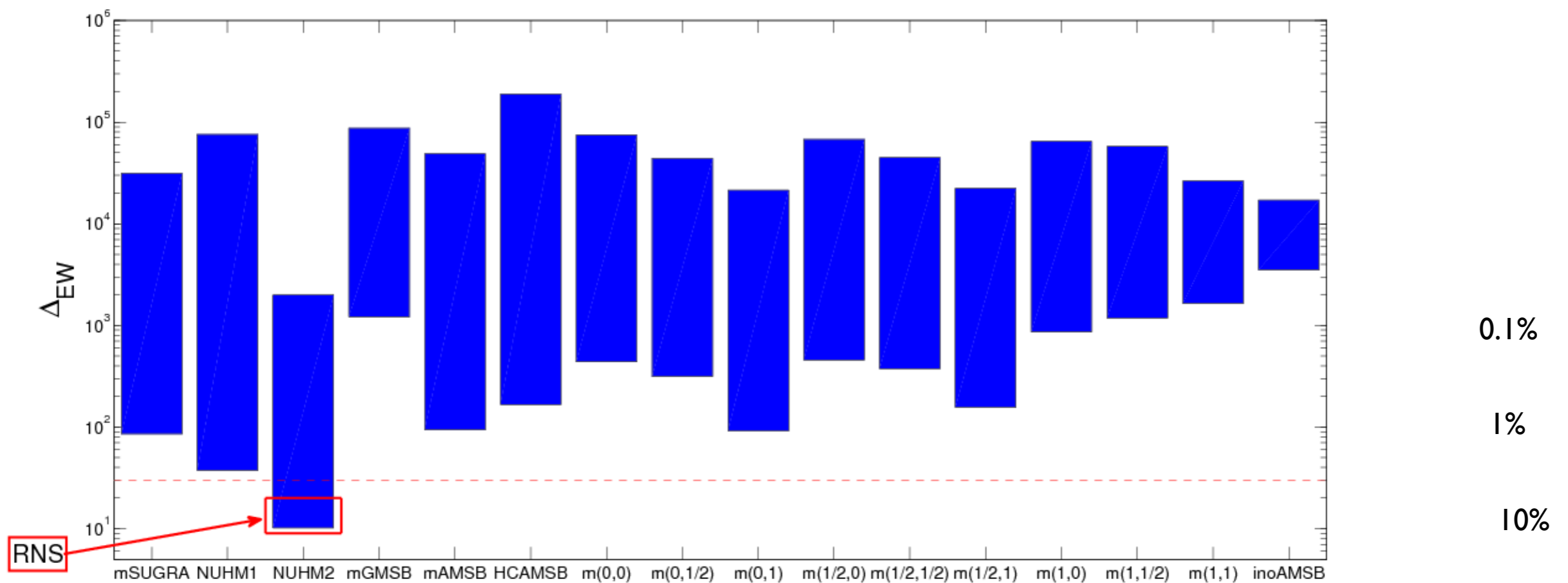


Visually, large fine-tuning has already developed by  $\mu \sim 350$  or  $\Delta_{EW} \sim 30$

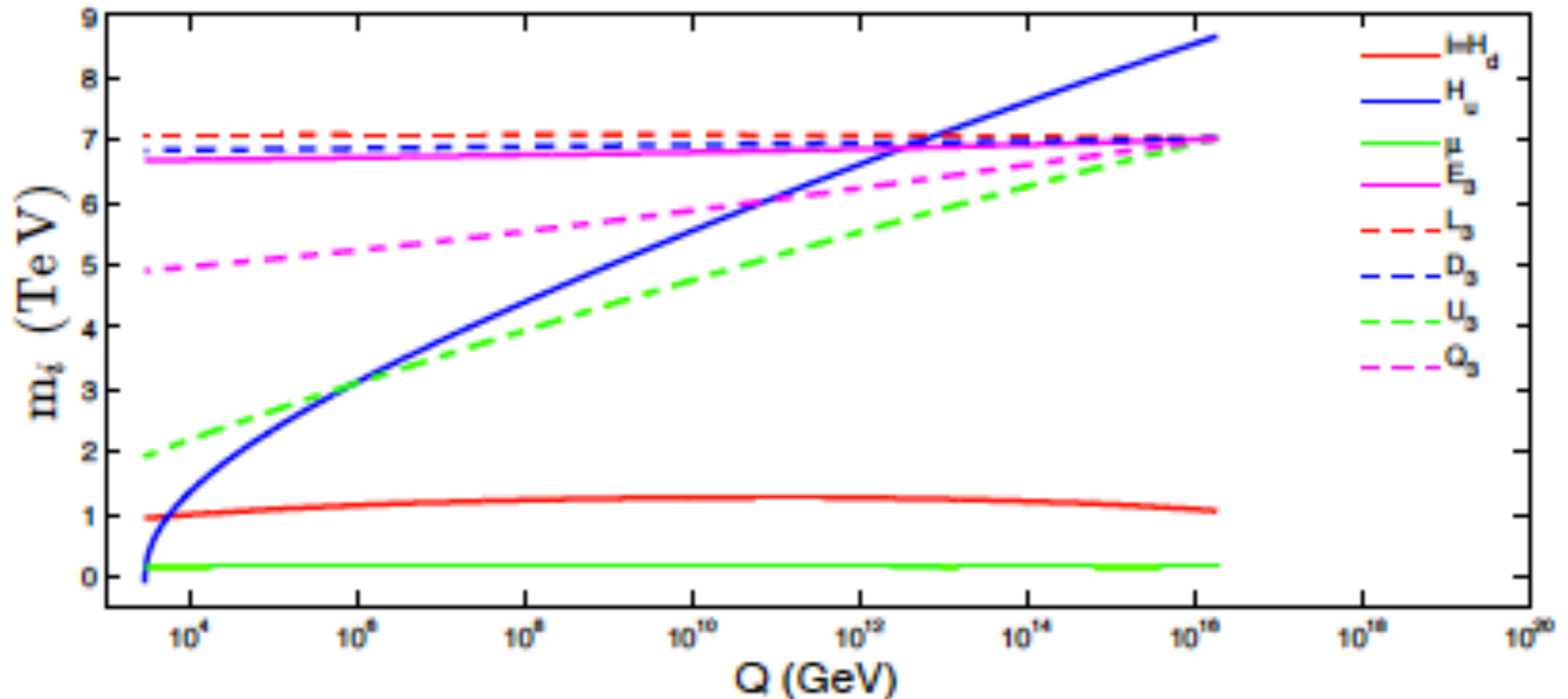
$\Delta_{EW}$  is highly selective:  
 most constrained models are ruled out  
 except NUHM2 and its generalizations:

J. Ellis, K. Olive and Y. Santoso, *Phys. Lett. B* 539 (2002) 107; J. Ellis, T. Falk, K. Olive and Y. Santoso, *Nucl. Phys. B* 652 (2003) 259; H. Baer, A. Mustafayev, S. Profumo, A. Belyaev and X. Tata, *J. High Energy Phys.* 0507 (2005) 065.

scan over p-space with  $m(h)=125.5\pm 2.5$  GeV:



Applied properly, all three measures agree:  
**naturalness is unambiguous and highly predictive!**



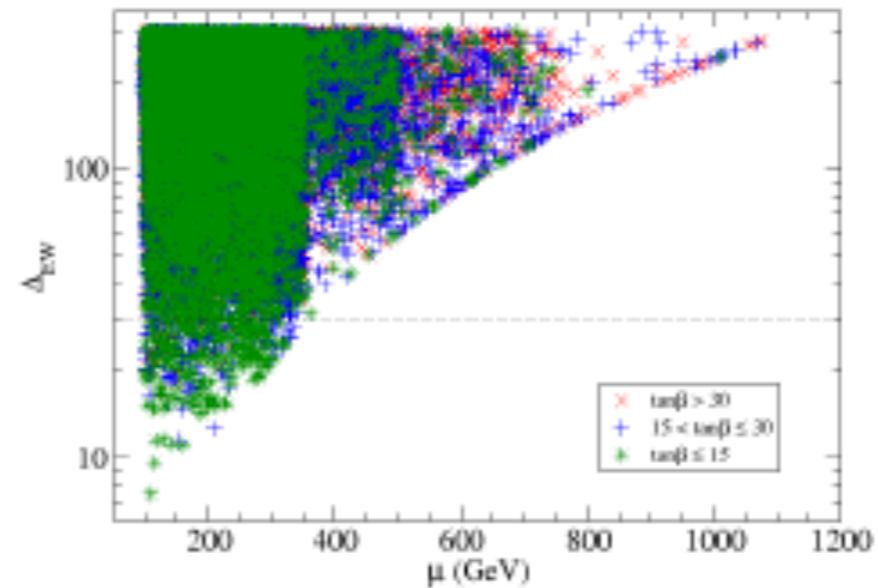
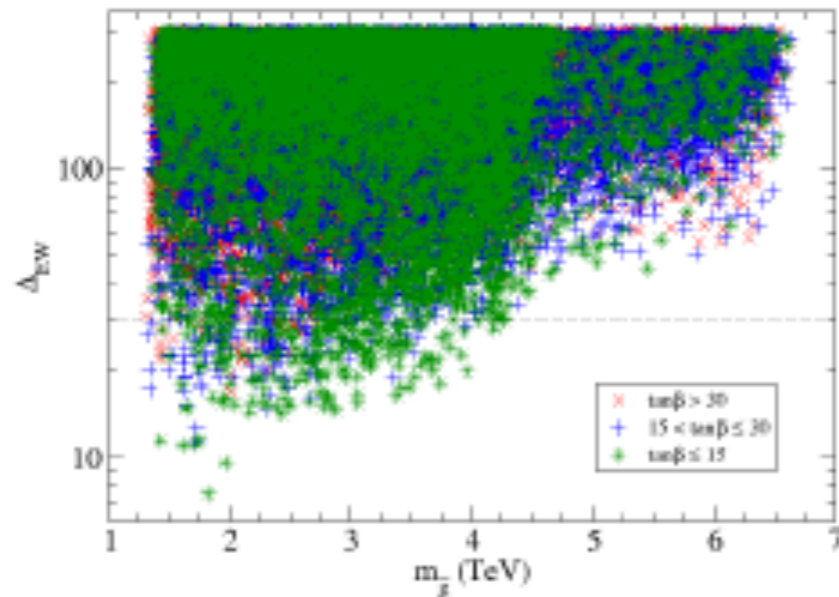
Radiatively-driven natural SUSY, or RNS:

(typically need  $m_{H_u} \sim 25\text{-}50\%$  higher than  $m_0$ )

H. Baer, V. Barger, P. Huang, A. Mustafayev and X. Tata, *Phys. Rev. Lett.* **109** (2012) 161802.

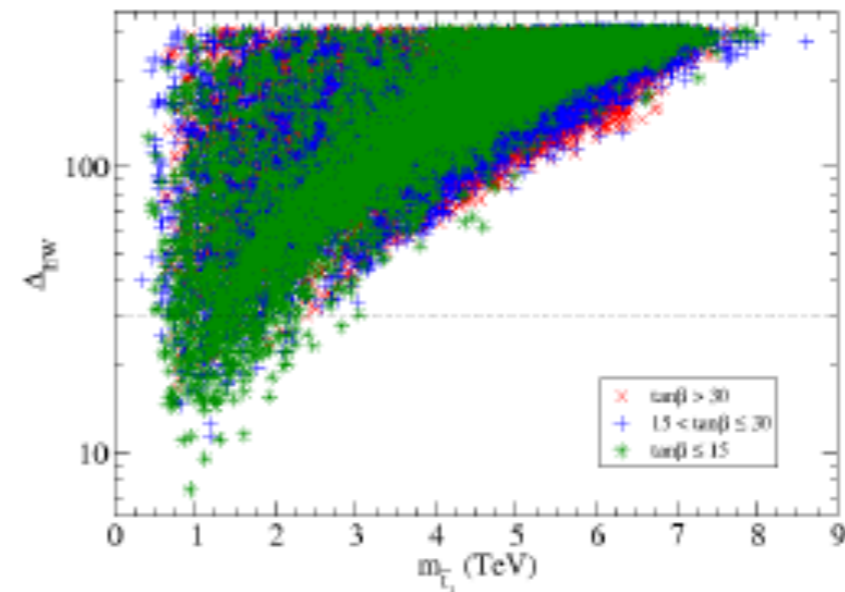
H. Baer, V. Barger, P. Huang, D. Mickelson, A. Mustafayev and X. Tata, *Phys. Rev. D* **87** (2013) 115028 [arXiv:1212.2655 [hep-ph]].

# Upper bounds on sparticle masses:



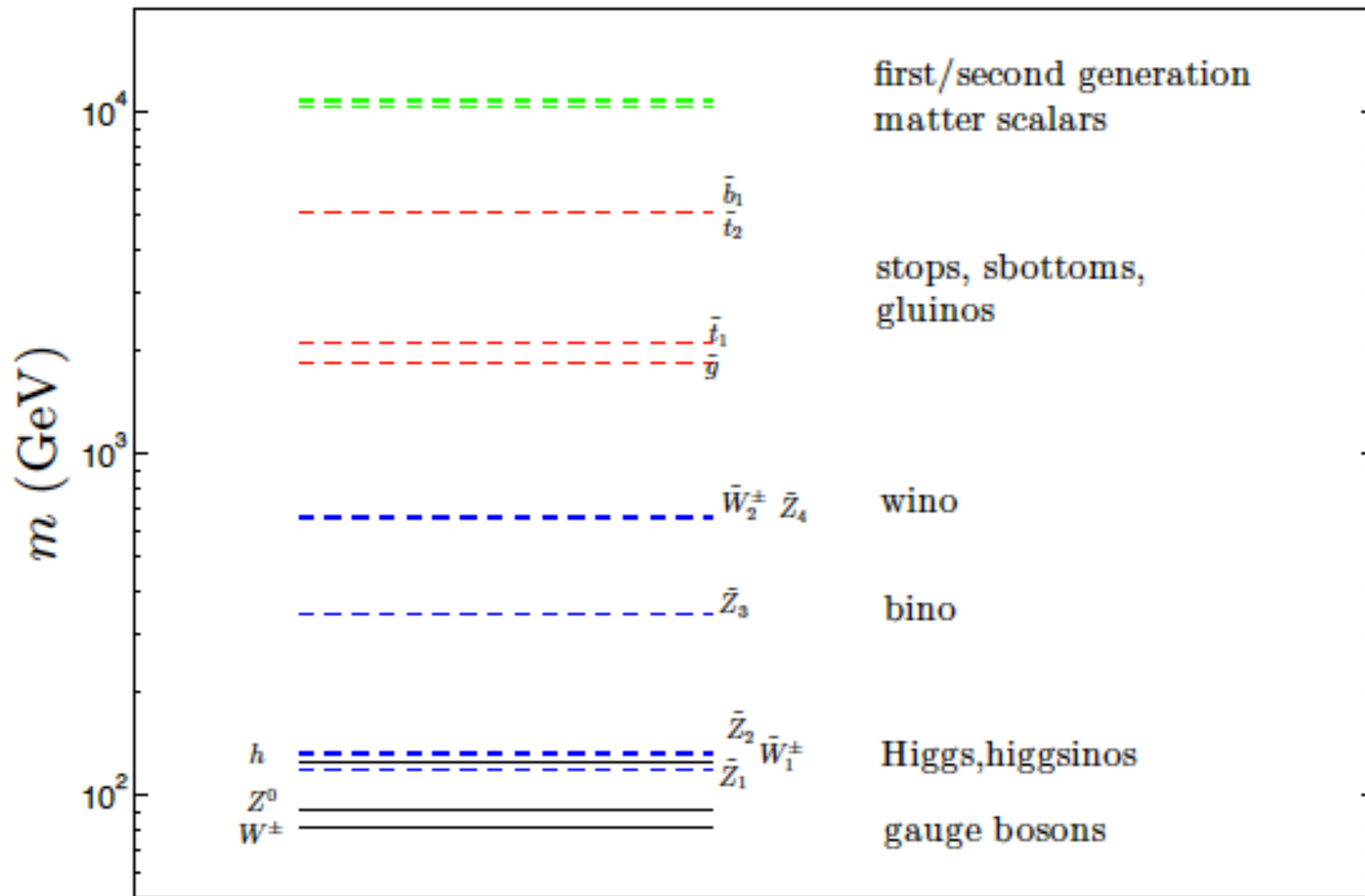
$\Delta_{EW} < 30$  upper bounds:

$m(\text{gluino}) < 4 \text{ TeV}$   
 $\mu < 350 \text{ GeV}$   
 $m(t_1) < 3 \text{ TeV}$



higher than old NS models and  
allows for  $m(h) \sim 125 \text{ GeV}$  within MSSM

# Typical spectrum for low $\Delta_{EW}$ models



There is a Little Hierarchy, but it is **no problem**

$$\mu \ll m_{3/2}$$

SUSY  $\mu$  problem:  $\mu$  term is SUSY, not SUSY breaking:  
expect  $\mu \sim M_{\text{Pl}}$  but phenomenology requires  $\mu \sim m(Z)$

- NMSSM:  $\mu \sim m(3/2)$ ; beware singlets!
- Giudice–Masiero:  $\mu$  forbidden by some symmetry:  
generate via Higgs coupling to hidden sector
- Kim–Nilles: invoke SUSY version of DFSZ axion  
solution to strong CP:

KN: PQ symmetry forbids  $\mu$  term,  
but then it is generated via PQ breaking

Little Hierarchy due to mismatch between  
PQ breaking and SUSY breaking scales?

$$\mu \sim \lambda f_a^2 / M_P$$

$$m_{3/2} \sim m_{\text{hid}}^2 / M_P$$

$$f_a \ll m_{\text{hid}}$$

Higgs mass tells us where  
to look for axion!

$$m_a \sim 6.2 \mu\text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right)$$

# Little Hierarchy from radiative PQ breaking? exhibited within context of MSY model

Murayama, Suzuki, Yanagida (1992);  
Gherghetta, Kane (1995)

Choi, Chun, Kim (1996)

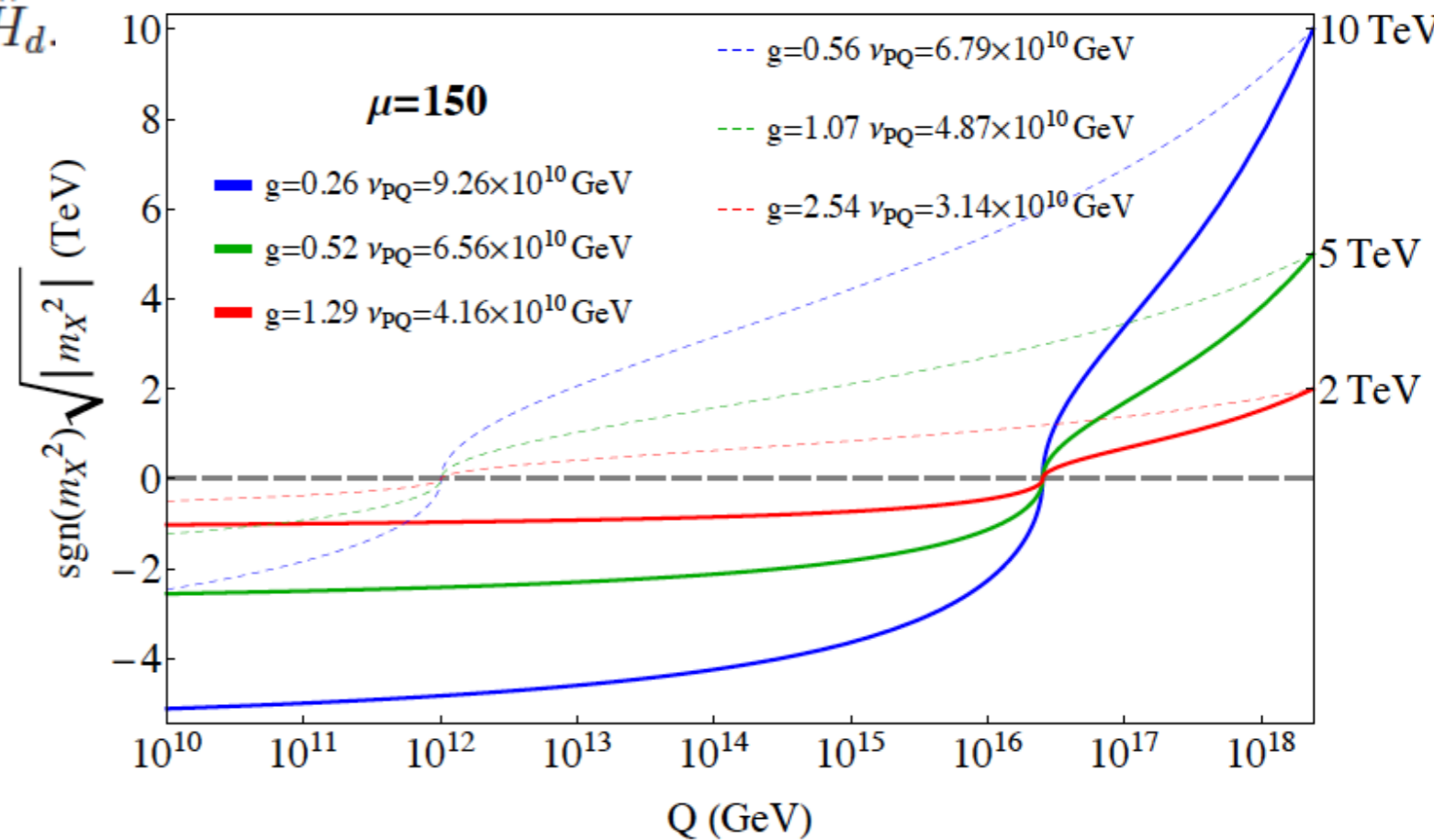
Bae, HB, Serce, PRD91 (2015) 015003

## augment MSSM with PQ charges/fields:

$$\hat{f}' = \frac{1}{2} h_{ij} \hat{X} \hat{N}_i^c \hat{N}_j^c + \frac{f}{M_P} \hat{X}^3 \hat{Y} + \frac{g}{M_P} \hat{X} \hat{Y} \hat{H}_u \hat{H}_d.$$

$$M_{N_i^c} = v_X h_i |_{Q=v_X}$$

$$\mu = g \frac{v_X v_Y}{M_P}.$$

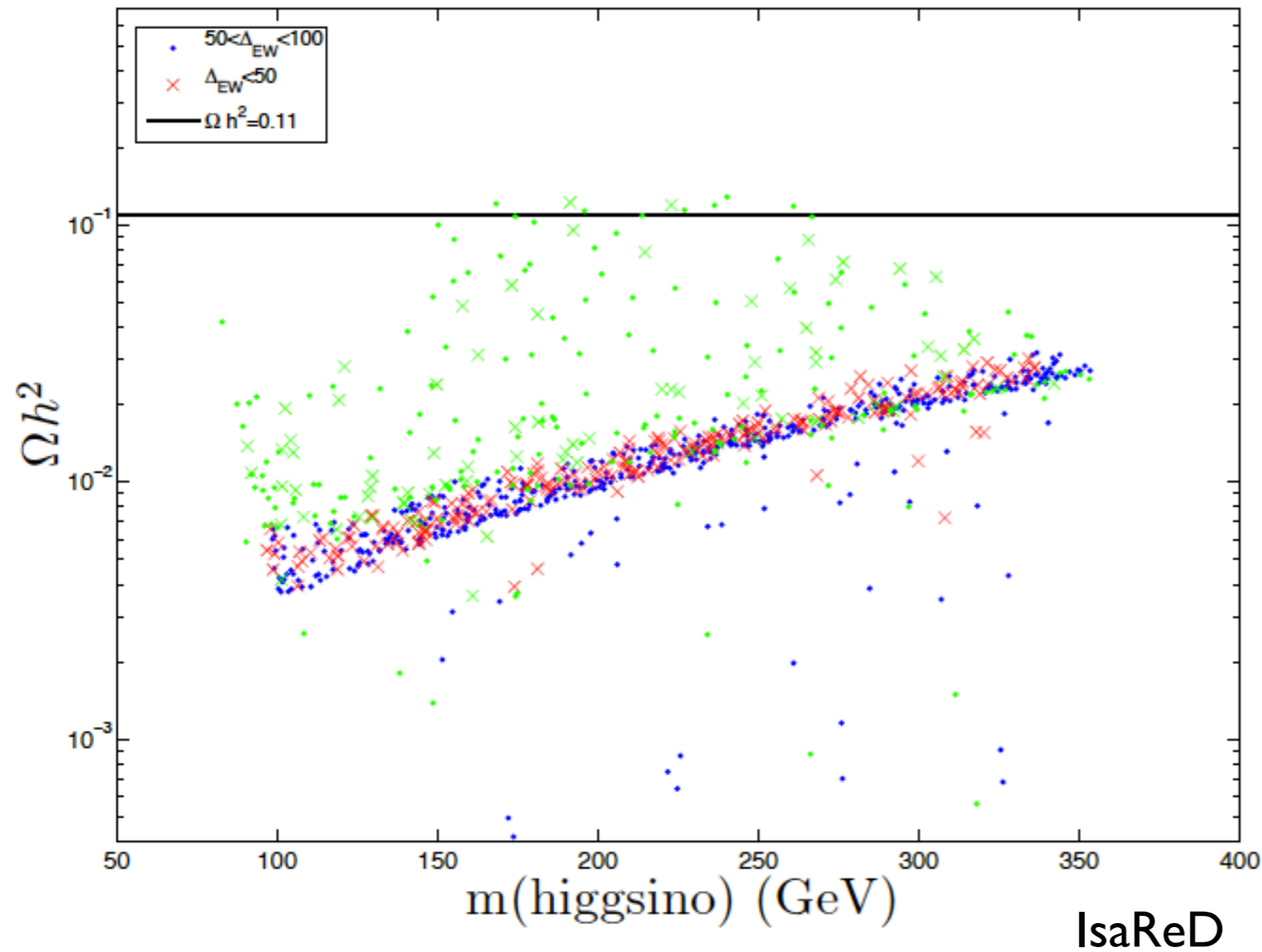


Large  $m_{3/2}$  generates small  $\mu \sim 100 - 200$  GeV!

Dark matter in  
Radiatively-driven Natural SUSY



# Mainly higgsino-like WIMPs thermally underproduce DM



green: excluded;  
red/blue: allowed

HB, Barger, Mickelson

Factor of 10–15 too low

But so far we have addressed only **Part 1**  
of fine-tuning problem:

In QCD sector, the term  $\frac{\bar{\theta}}{32\pi^2} F_{A\mu\nu} \tilde{F}_A^{\mu\nu}$  must occur

But neutron EDM says it is not there: strong CP problem

(frequently ignored by SUSY types)

Best solution after 35 years:

PQWW/KSVZ/DFSZ **invisible axion**

In SUSY, axion accompanied by axino and saxion

Changes DM calculus:

expect mixed WIMP/axion DM (**2 particles**)

## Axion cosmology

★ Axion field eq'n of motion:  $\theta = a(x)/f_a$

$$- \ddot{\theta} + 3H(T)\dot{\theta} + \frac{1}{f_a^2} \frac{\partial V(\theta)}{\partial \theta} = 0$$

$$- V(\theta) = m_a^2(T) f_a^2 (1 - \cos \theta)$$

– Solution for  $T$  large,  $m_a(T) \sim 0$ :

$$\theta = \text{const.}$$

–  $m_a(T)$  turn-on  $\sim 1$  GeV

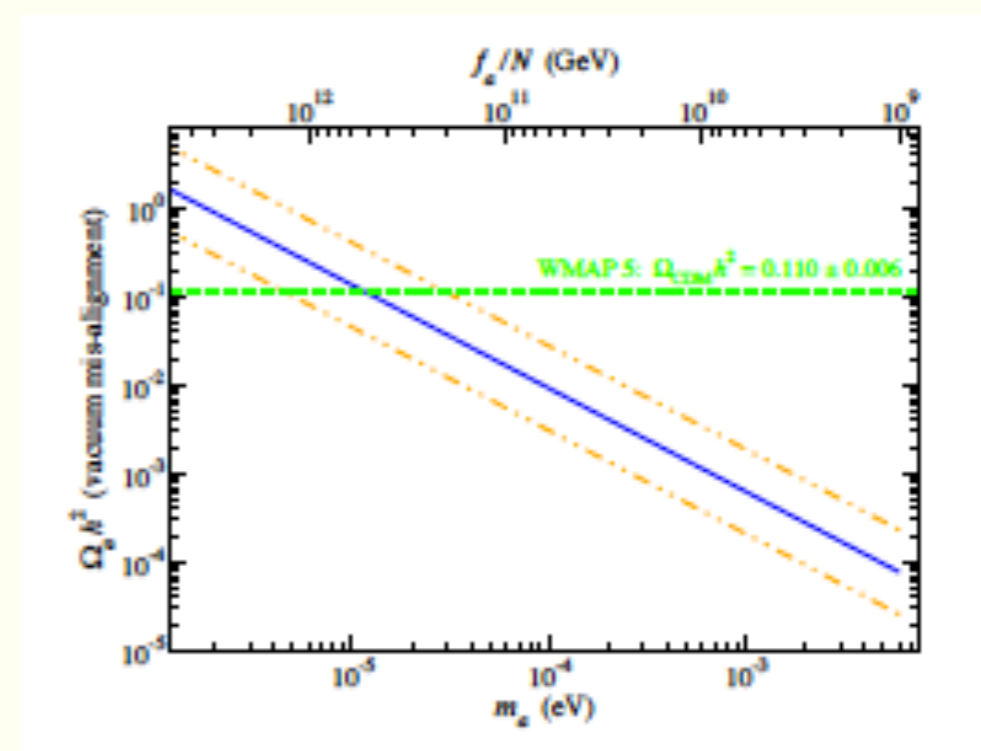
★  $a(x)$  oscillates,

creates axions with  $\vec{p} \sim 0$ :

production via vacuum mis-alignment

$$\star \Omega_a h^2 \sim \frac{1}{2} \left[ \frac{6 \times 10^{-6} \text{ eV}}{m_a} \right]^{7/6} \theta_i^2 h^2$$

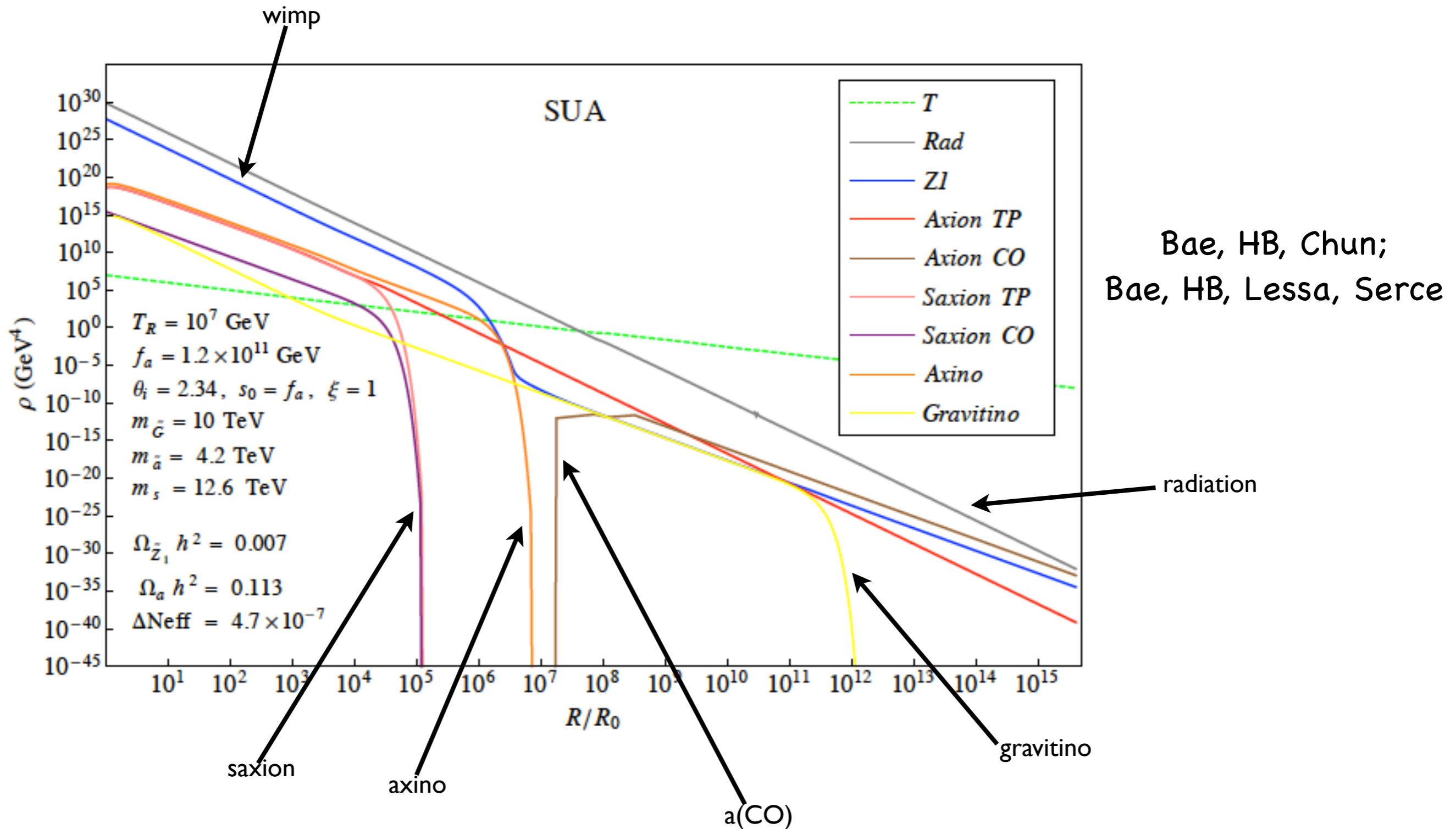
★ astro bound: stellar cooling  $\Rightarrow f_a \gtrsim 10^9 \text{ GeV}$

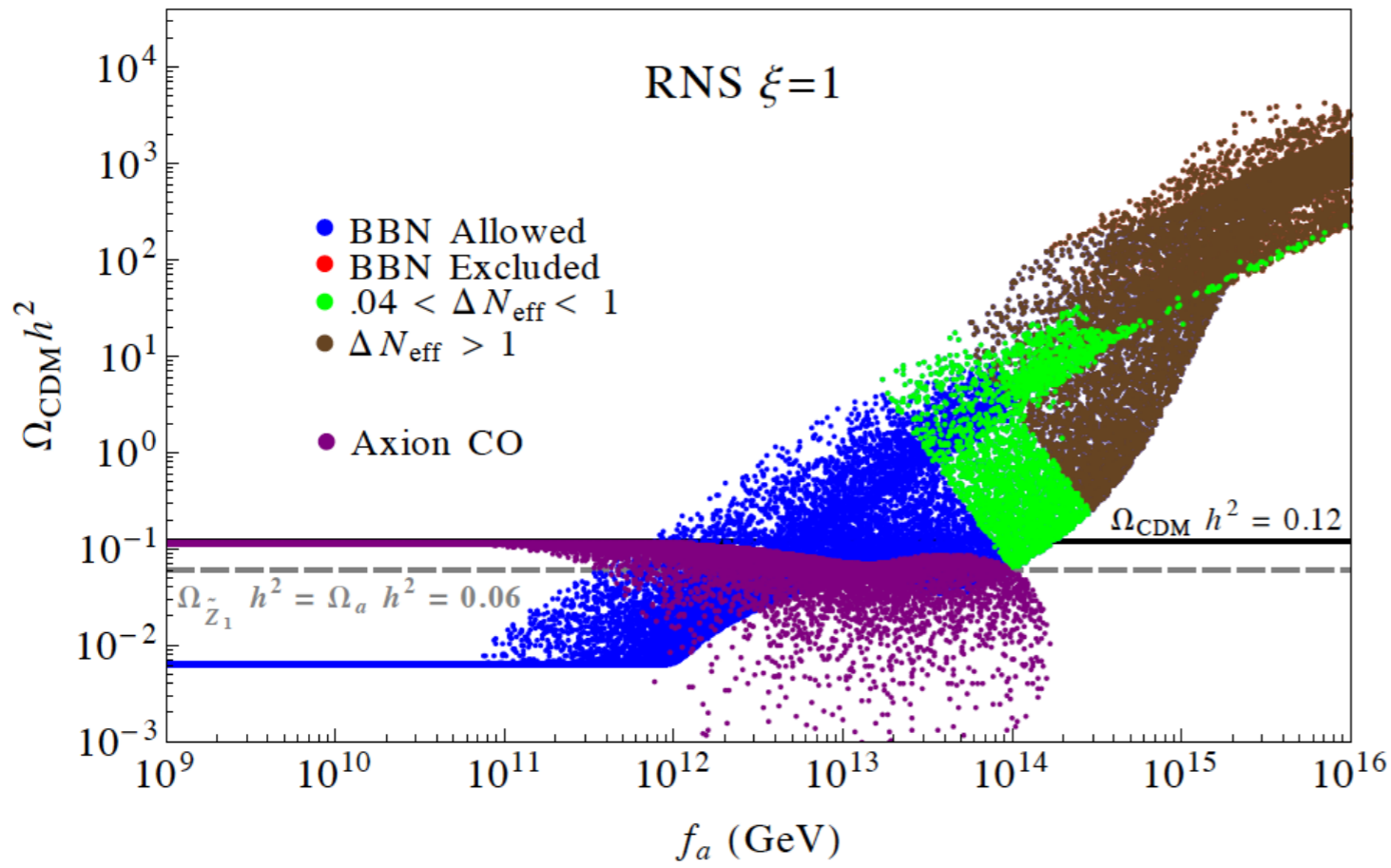


# mixed axion-neutralino production in early universe

- neutralinos: thermally produced (TP) or NTP via  $\tilde{a}$ ,  $s$  or  $\tilde{G}$  decays
  - re-annihilation at  $T_D^{s,\tilde{a}}$
- axions: TP, NTP via  $s \rightarrow aa$ , bose coherent motion (BCM)
- saxions: TP or via BCM
  - $s \rightarrow gg$ : entropy dilution
  - $s \rightarrow SUSY$ : augment neutralinos
  - $s \rightarrow aa$ : dark radiation ( $\Delta N_{eff} < 1.6$ )
- axinos: TP
  - $\tilde{a} \rightarrow SUSY$  augments neutralinos
- gravitinos: TP, decay to SUSY

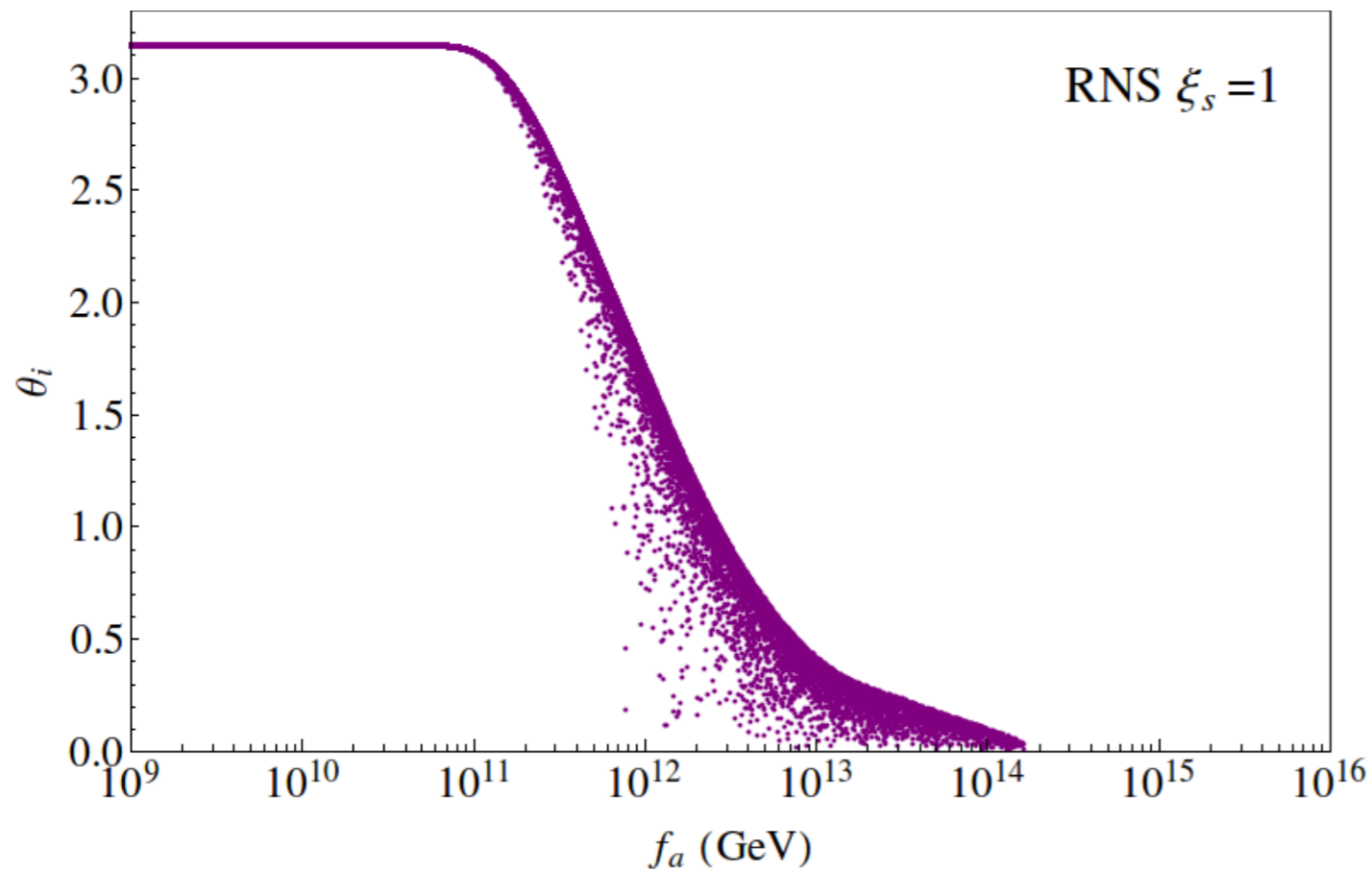
# DM production in SUSY DFSZ: solve eight coupled Boltzmann equations



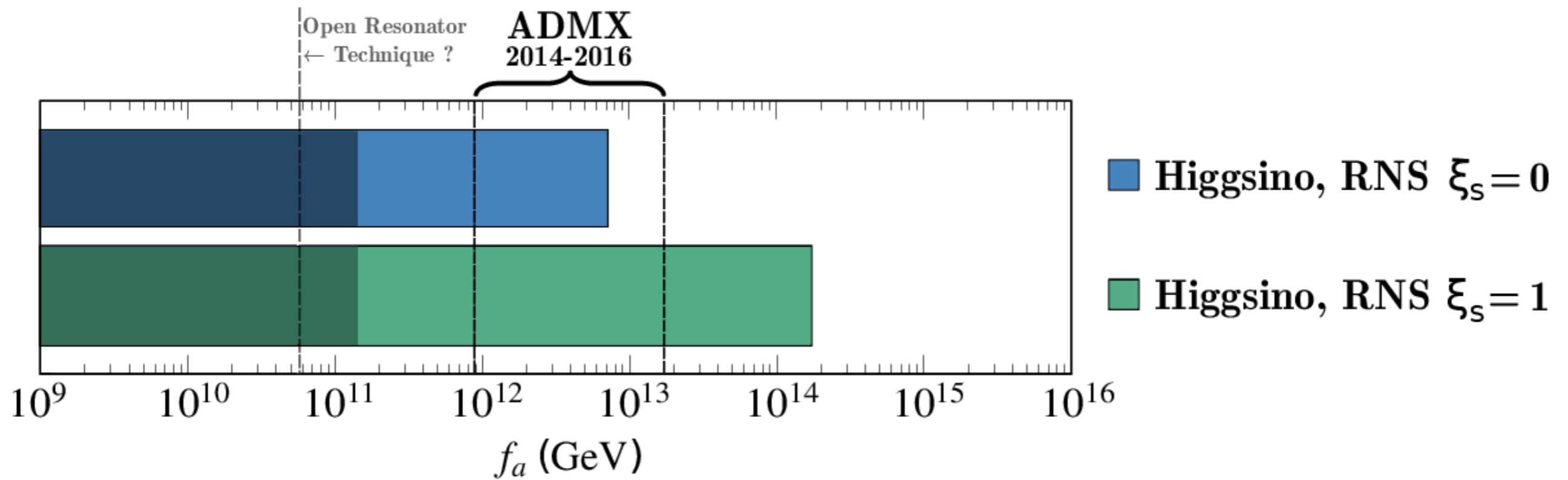


higgsino abundance

axion abundance



**mainly axion CDM**  
 for  $f_a < \sim 10^{12}$  GeV;  
 for higher  $f_a$ , then  
 get increasing wimp  
 abundance



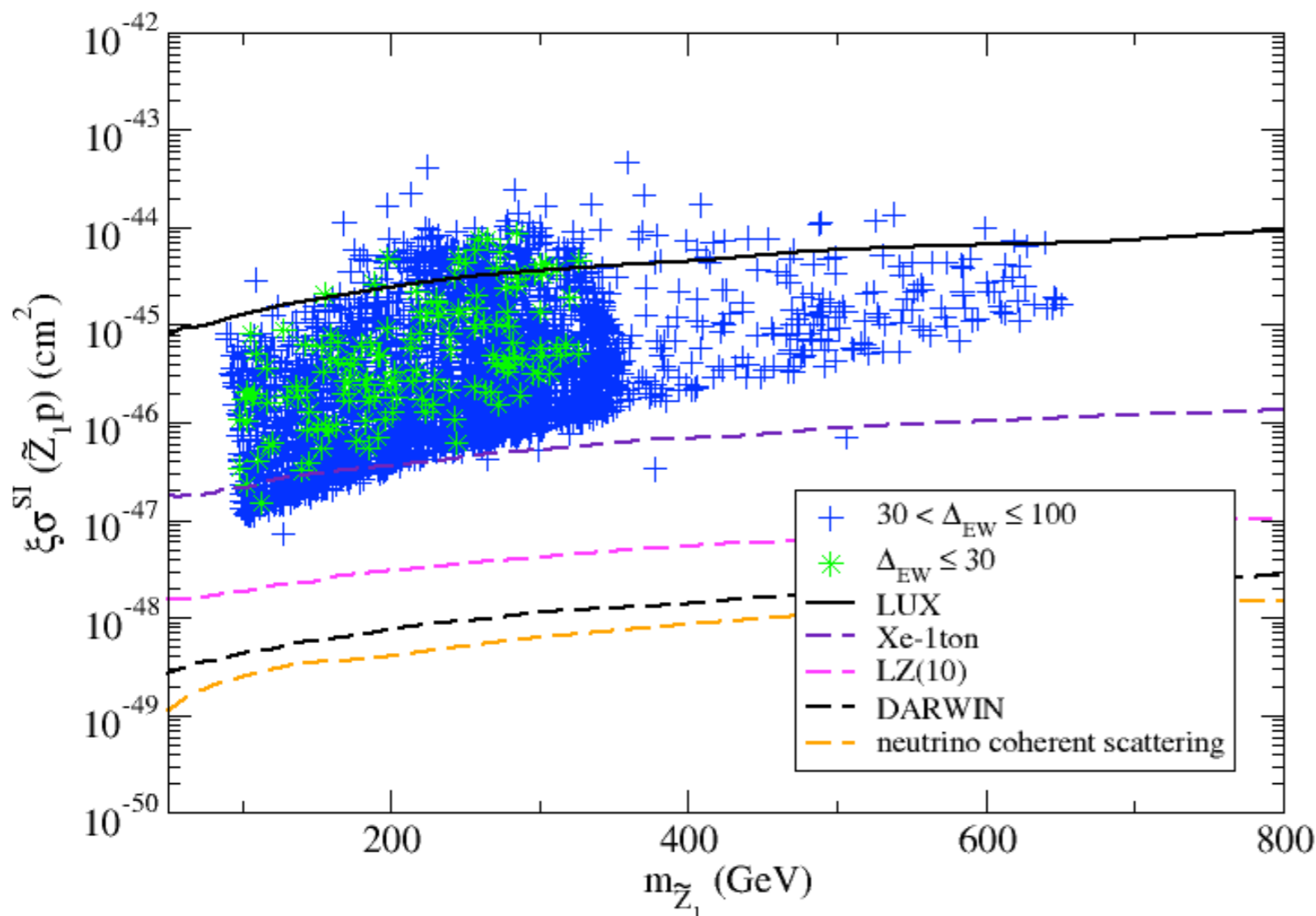
range of  $f_a$  expected from SUSY  
with radiatively-driven naturalness  
compared to ADMX axion reach

# Direct higgsino detection rescaled for minimal local abundance

Bae, HB, Barger, Savoy, Serce

$$\mathcal{L} \ni -X_{11}^h \bar{\tilde{Z}}_1 \tilde{Z}_1 h$$

$$X_{11}^h = -\frac{1}{2} (v_2^{(1)} \sin \alpha - v_1^{(1)} \cos \alpha) (g v_3^{(1)} - g' v_4^{(1)})$$

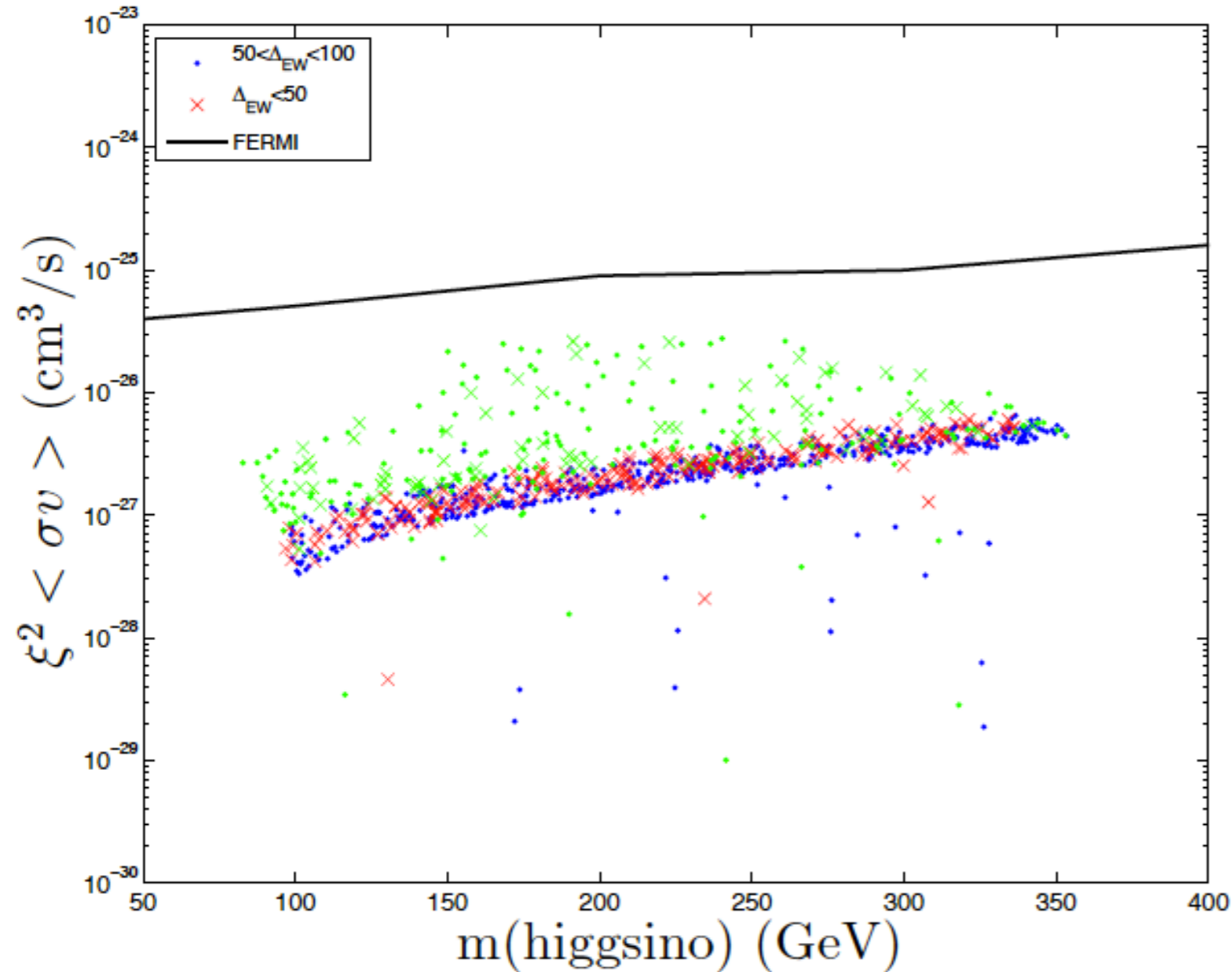


Deployment of Xe-1ton,  
LZ, SuperCDMS  
coming soon!

Can test completely with ton scale detector  
or equivalent (subject to minor caveats)



# Higgsino detection via halo annihilations:



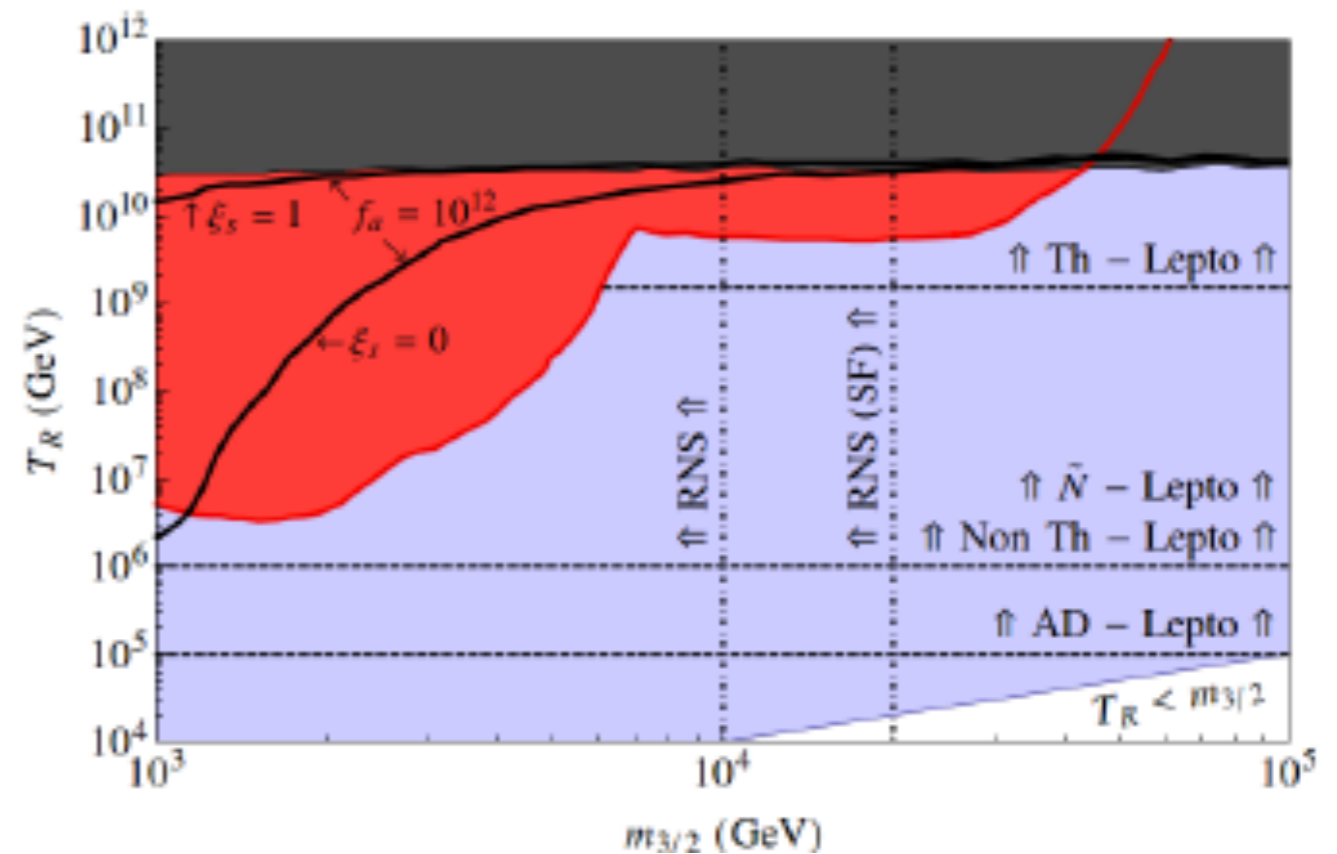
green: excluded by Xe-100

annihilation rate is high but rescaling is **squared**

Gamma-ray sky signal is factor 10-20 below current limits

# Baryogenesis scenarios for radiative natural SUSY

- thermal leptogenesis
- non-thermal (inflaton decay)
- oscillating sneutrino
- Affleck-Dine (AD)

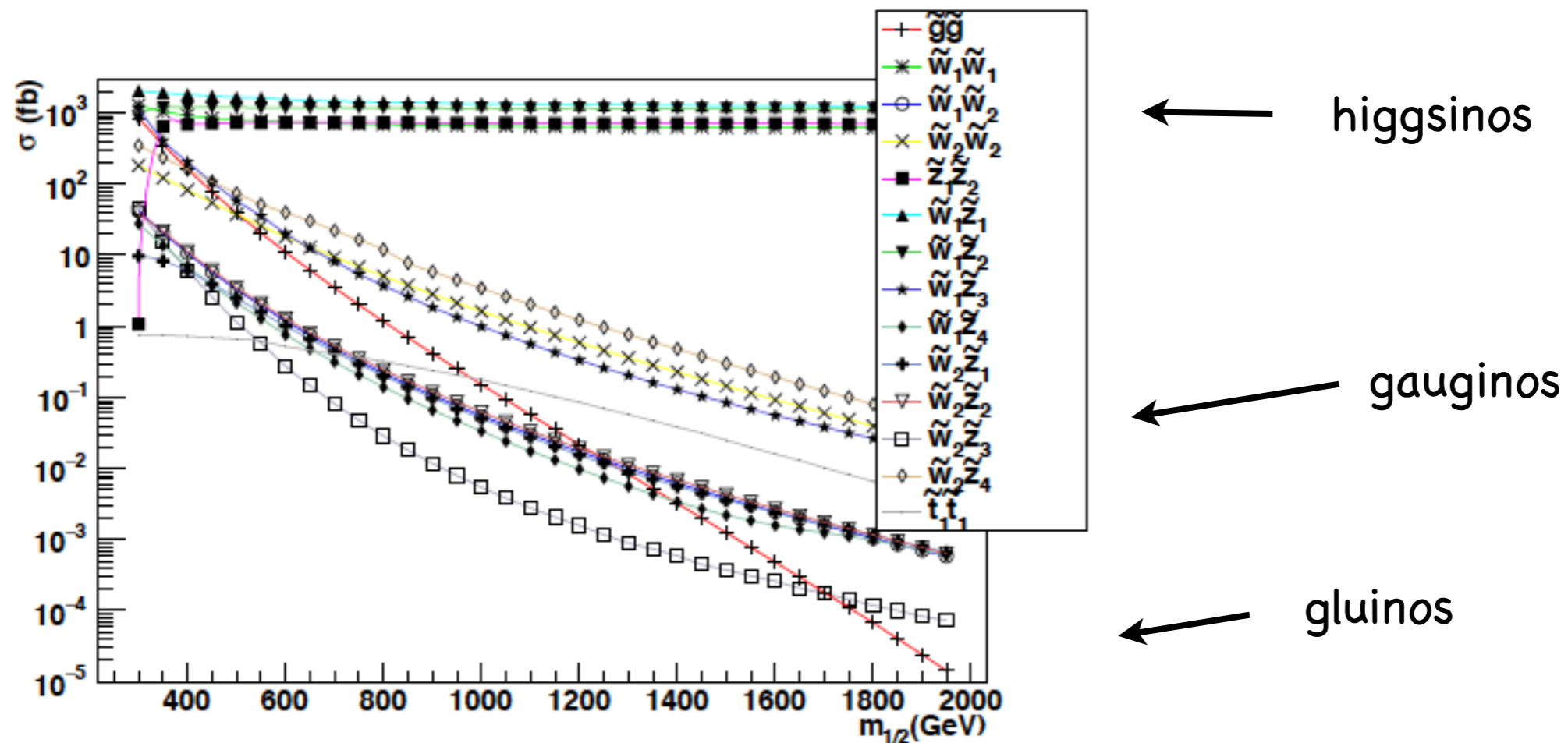


gravitino problem plus  
axino/saxion problem:  
still plenty room

$$f_a = 10^{11}, 10^{12} \text{ GeV}$$

# Prospects for discovering RNS at LHC and ILC

# Sparticle prod'n along RNS model-line at LHC14:



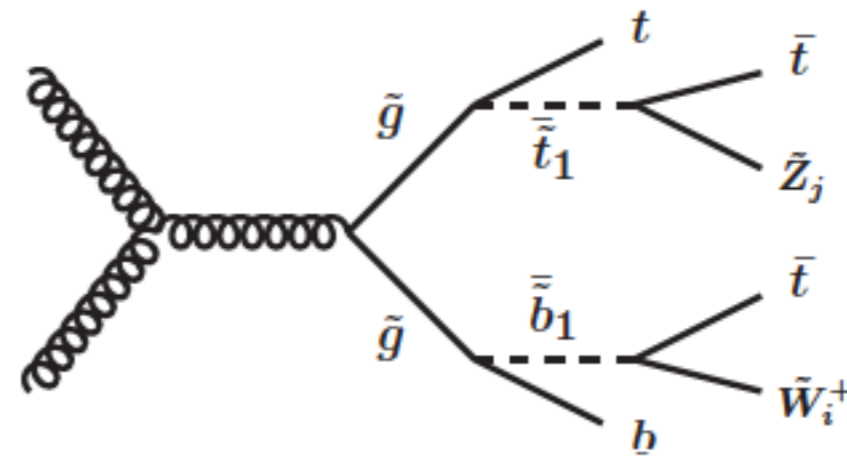
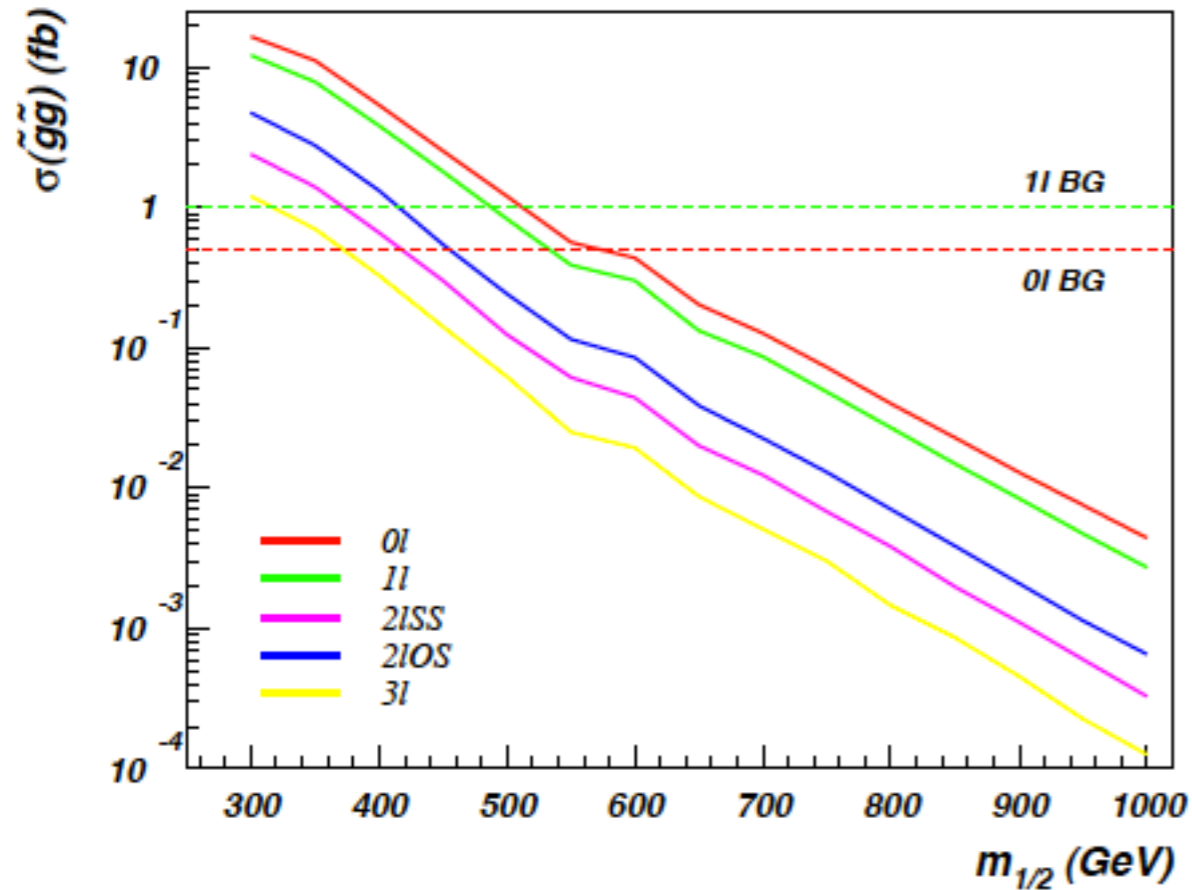
higgsino pair production dominant—but only soft visible energy release from higgsino decays

largest visible cross section: **wino pairs**

gluino pairs sharply dropping

# gluino pair cascade decay signatures

NUHM2:  $m_0=5\text{ TeV}$ ,  $A_0=-1.6m_0$ ,  $\tan\beta=15$ ,  $\mu=150\text{ GeV}$ ,  $m_A=1\text{ TeV}$



Particle	dom. mode	BF
$\tilde{g}$	$\tilde{t}_1 t$	$\sim 100\%$
$\tilde{t}_1$	$b\tilde{W}_1$	$\sim 50\%$
$\tilde{Z}_2$	$\tilde{Z}_1 f\bar{f}$	$\sim 100\%$
$\tilde{Z}_3$	$\tilde{W}_1^\pm W^\mp$	$\sim 50\%$
$\tilde{Z}_4$	$\tilde{W}_1^\pm W^\mp$	$\sim 50\%$
$\tilde{W}_1$	$\tilde{Z}_1 f\bar{f}'$	$\sim 100\%$
$\tilde{W}_2$	$\tilde{Z}_i W$	$\sim 50\%$

Table 1: Dominant branching fractions of various sparticles along the RNS model line for  $m_{1/2} = 1\text{ TeV}$ .

Int. lum. ( $\text{fb}^{-1}$ )	$\tilde{g}\tilde{g}$
10	1.4
100	1.6
300	1.7
1000	1.9

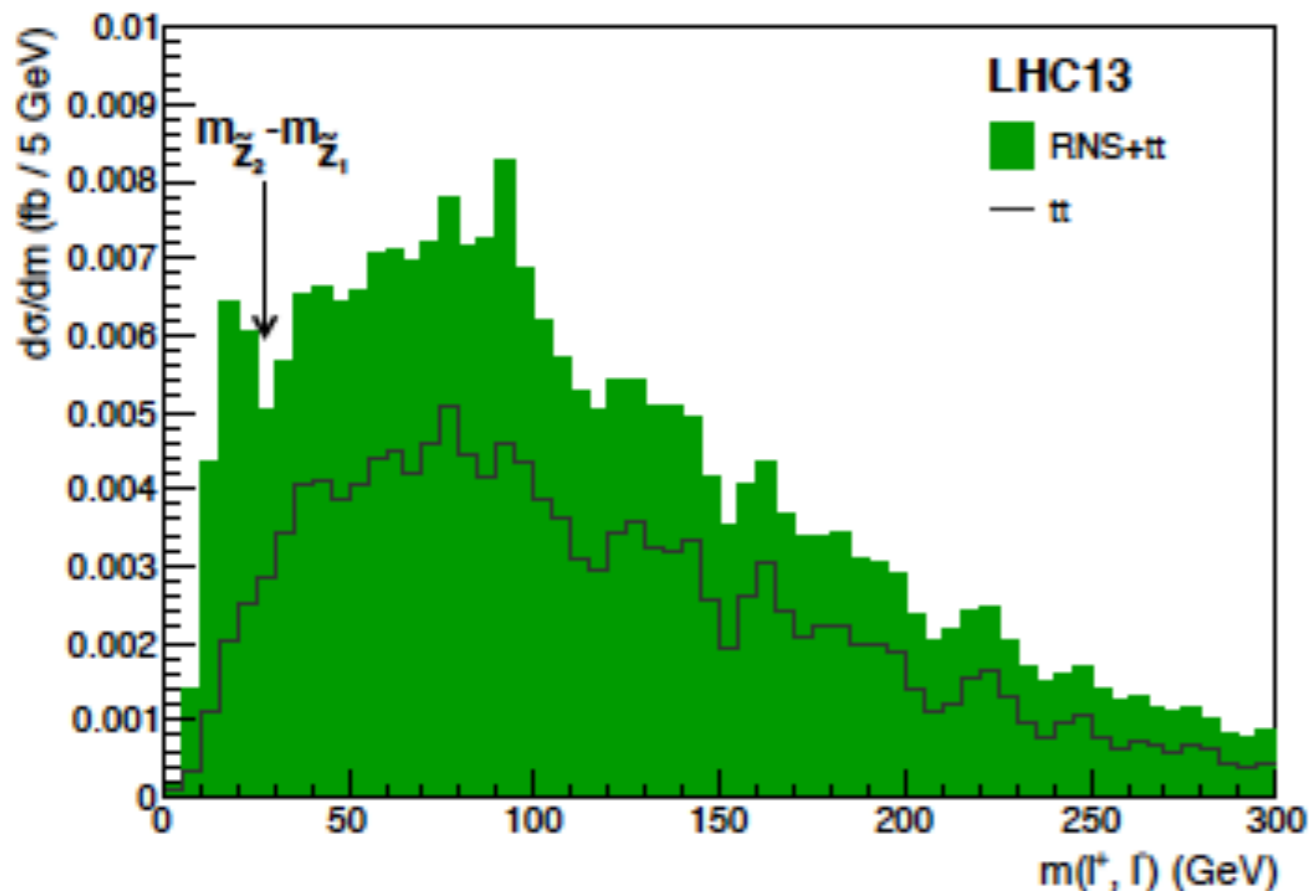
LHC14 reach  
in  $m(\text{gluino})$  (TeV)

since  $m(\text{gluino})$  extends to  $\sim 4\text{ TeV}$ ,  
LHC14 can see about half the low EWFT  
parameter space in these modes

LHC14 has some reach for RNS;  
 if a signal is seen, should be  
 characteristic

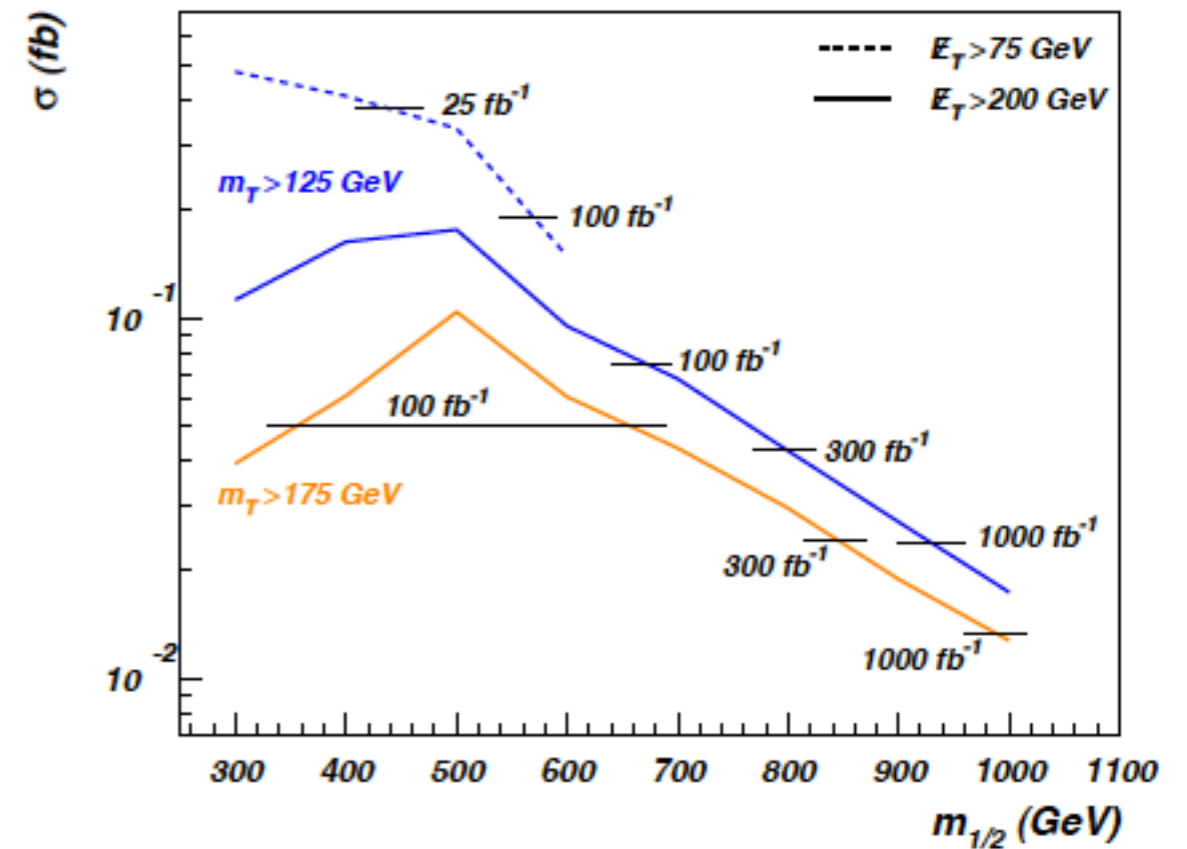
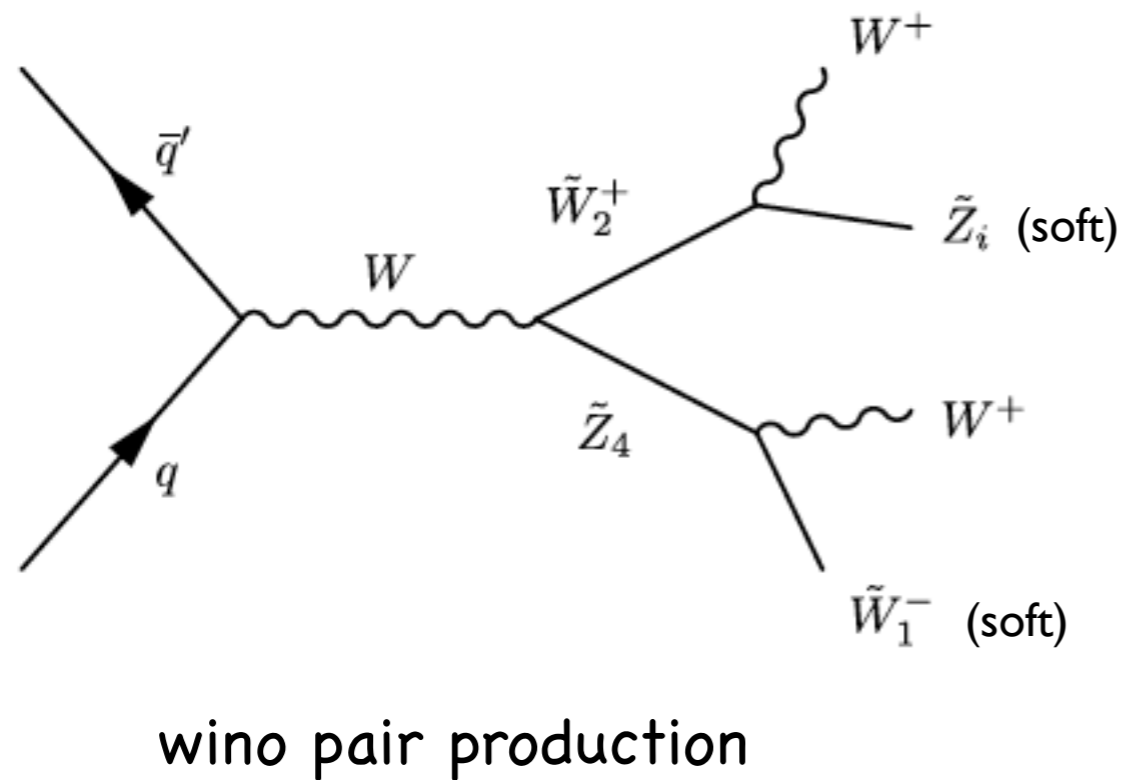
Int. lum. ( $\text{fb}^{-1}$ )	$\tilde{g}\tilde{g}$	SSdB	$WZ \rightarrow 3\ell$	$4\ell$
10	1.4	–	–	–
100	1.6	1.6	–	$\sim 1.2$
300	1.7	2.1	1.4	$\gtrsim 1.4$
1000	1.9	2.4	1.6	$\gtrsim 1.6$

$5\sigma$  reach of LHC14 in terms of  $m_{\tilde{g}}$  for various Int. Lum.



OS/SF dilepton mass  
 edge apparent from  
 cascade decays  
 with  $z_2 \rightarrow z_1 + l + l\bar{l}$

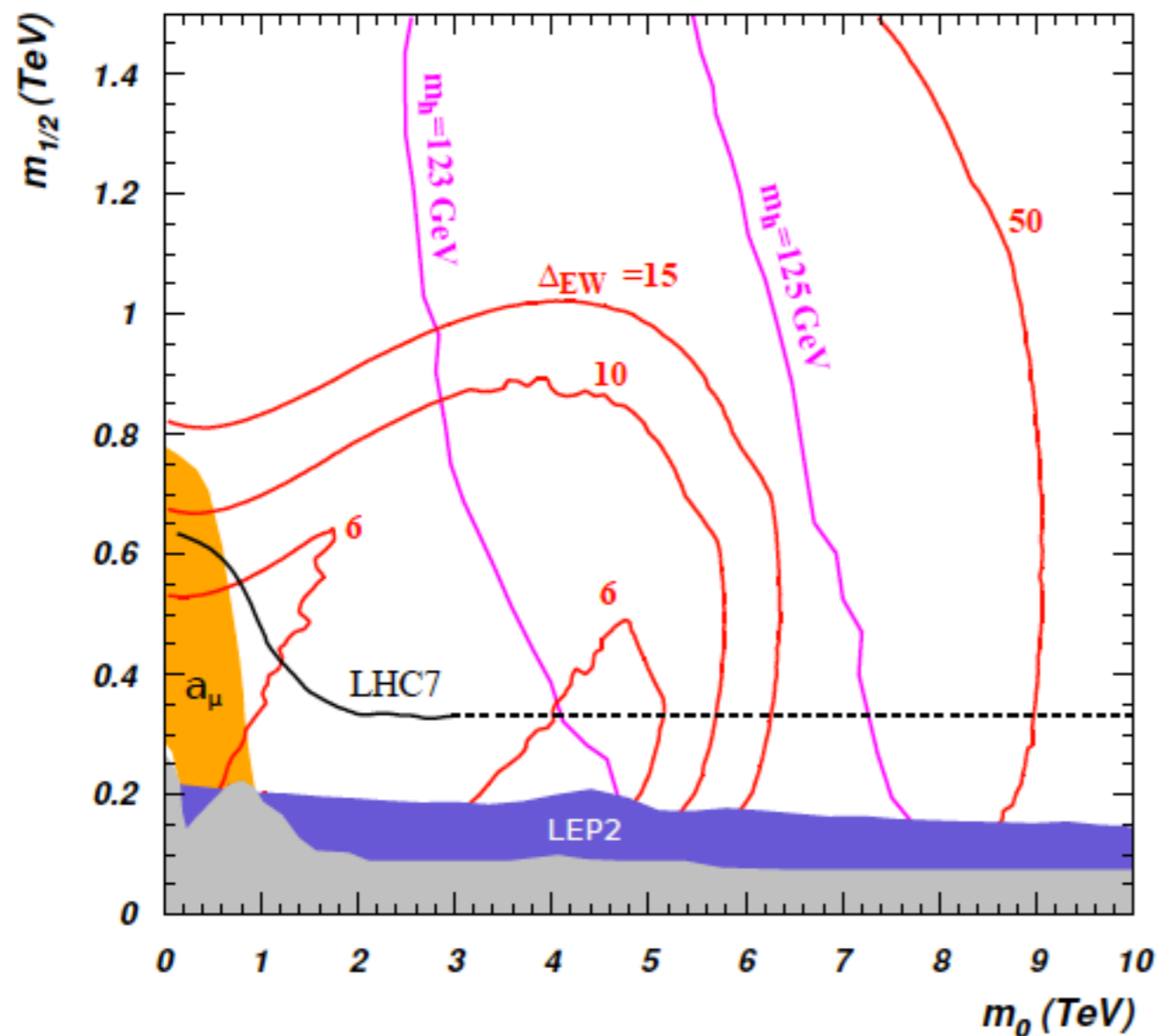
# Characteristic same-sign diboson (SSdB) signature from SUSY models with light higgsinos!



This channel offers best reach of LHC14 for RNS;  
it is also indicative of wino-pair prod'n  
followed by decay to higgsinos

Good old  $m_0$  vs.  $m_{1/2}$  plane still viable, but require low  $\mu$  (NUHM2)

NUHM2:  $\tan\beta=10$ ,  $A_0=-1.6m_0$ ,  $\mu=150$  GeV,  $m_t=173.2$  GeV

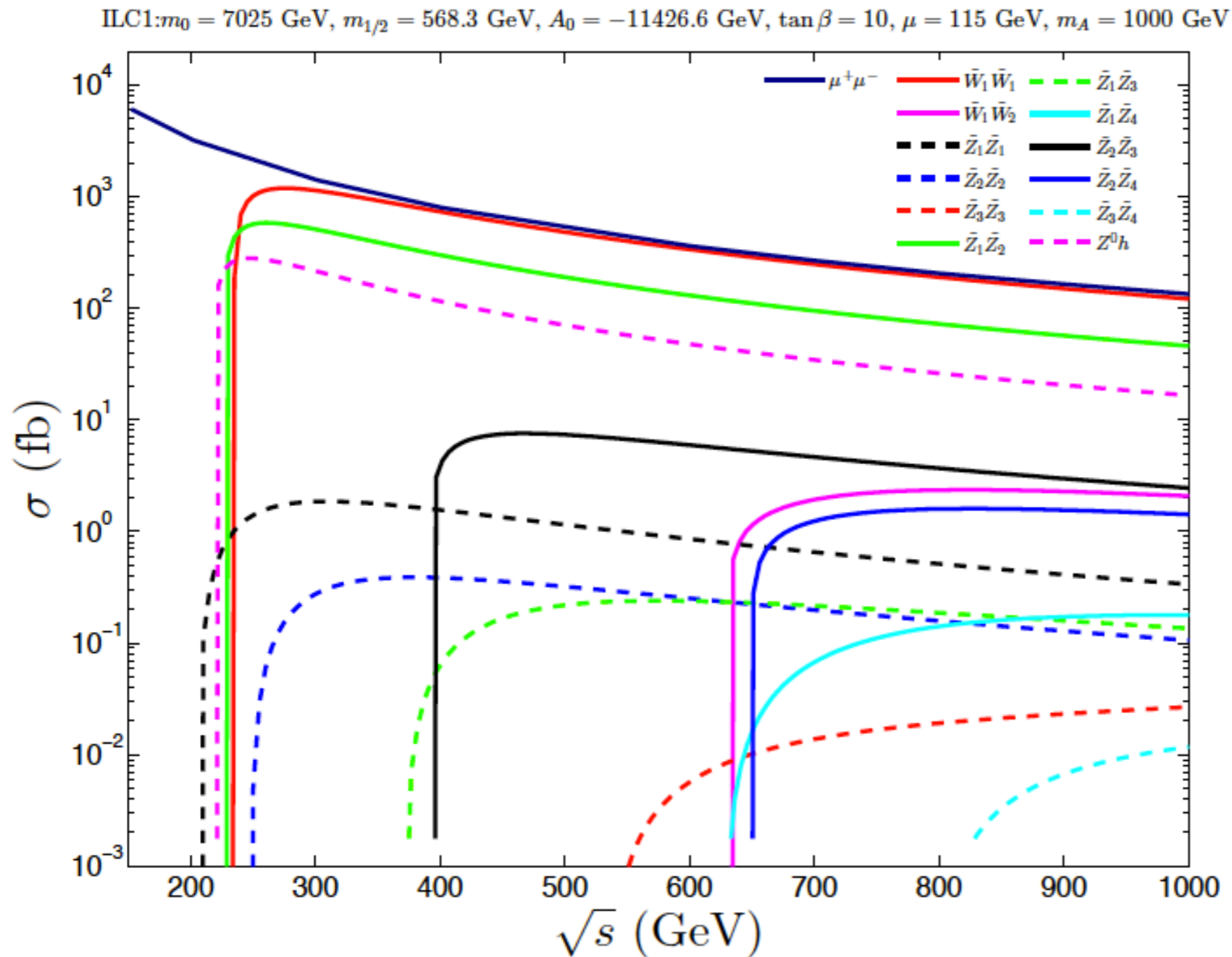


$\mu = 150$  GeV throughout which is allowed for NUHM2



# Smoking gun signature: light higgsinos at ILC:

ILC is Higgs/higgsino factory!



$$\sigma(\text{higgsino}) \gg \sigma(Zh)$$

10–15 GeV higgsino mass  
gaps no problem  
in clean ILC environment

HB, Barger, Mickelson, Mustafayev, Tata  
arXiv:1404.7510

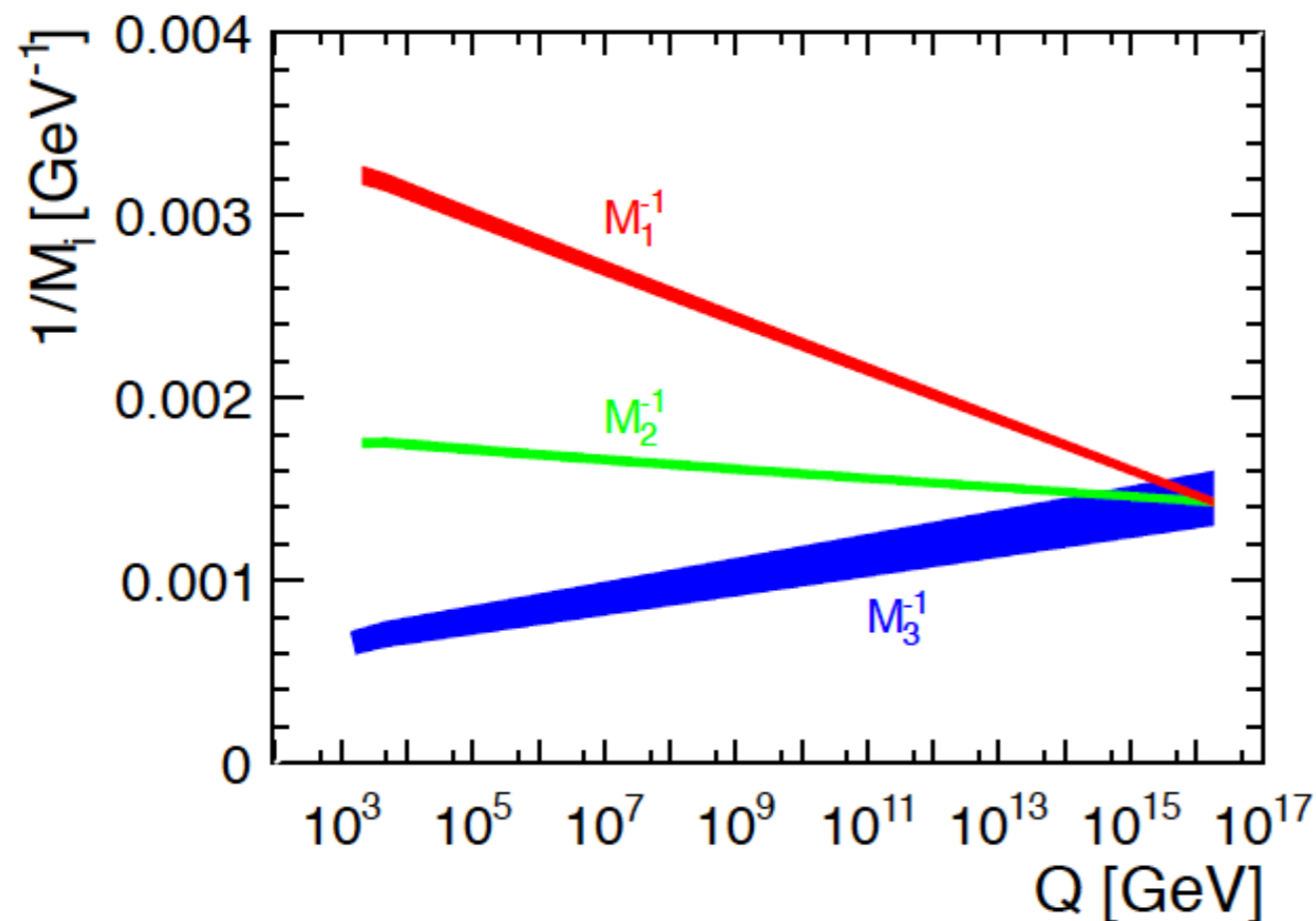
ILC either sees light higgsinos or natural SUSY dead

# In SUSY with radiatively-driven naturalness, can still test unification

Higgsino mass  $\Rightarrow \mu$

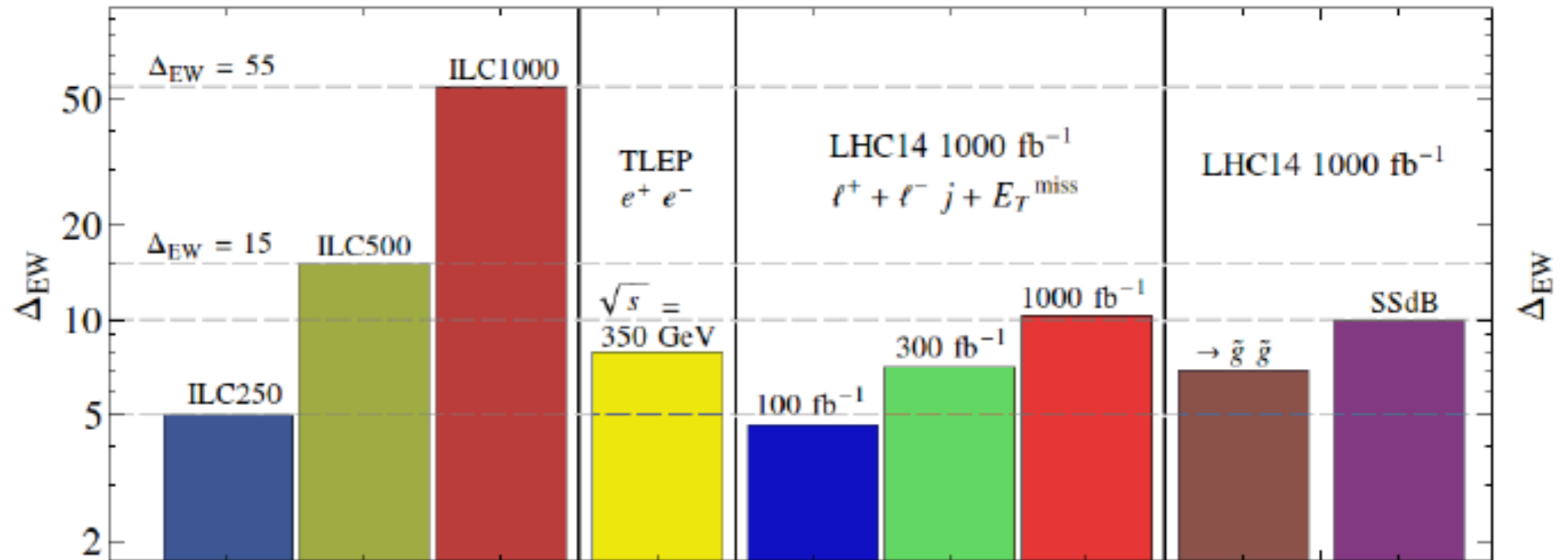
Higgsino mass gaps  $\Rightarrow M_1$  and  $M_2$

Measure  $M_3$  at LHC else use unification to predict  $m_{\tilde{g}}$



testing gaugino mass unification at ILC

# Future collider reach for naturalness



Bae, HB, Nagata, Serce

When to give up on naturalness in MSSM?  
 If ILC(600–700 GeV) sees no light higgsinos

# message to MEXT committee

The simplest, most natural version of supersymmetry predicts light higgsinos with mass 100-300 GeV  
(the closer to  $m(W,Z,h)$  the better)

These states are difficult, maybe impossible, to detect at LHC while ILC would be a **higgsino factory**:  
can test naturalness, unification, dark matter...

ILC is highly worthy of the investment!

# Conclusions: status of SUSY post LHC8

- SUSY EWFT **non-crisis**: EWFT allowed at 10% level in radiatively-driven natural SUSY: SUGRA GUT paradigm is just fine in NUHM2 but CMSSM/others fine-tuned
- naturalness maintained for  $\mu \sim 100\text{--}200$  GeV;  $t_1 \sim 1\text{--}2$  TeV,  $t_2 \sim 2\text{--}4$  TeV, highly mixed;  $m(\tilde{g}, \tilde{l}, \tilde{n}) \sim 1\text{--}4$  TeV
- LHC14 w/  $300 \text{ fb}^{-1}$  can see about half of RNS parameter space
- **$e^+e^-$  collider with  $\sqrt{s} \sim 500\text{--}600$  GeV needed to find predicted light higgsino states**
- Discovery of and precision measurements of light higgsinos at ILC!
- RNS spectra characterized by mainly higgsino-like WIMP: standard relic underabundance
- SUSY DFSZ/MSY invisible axion model: solves strong CP and  $\mu$  problems while allowing for  $\mu \sim m(Z)$
- Expect mainly axion CDM with 5–10% higgsino-like WIMPs over much of p-space
- Ultimately detect **both axion and higgsino-like WIMP**