Probing Features in the Primordial Power Spectrum

Arman Shafieloo

Korea Astronomy and Space Science Institute (KASI) & University of Science and Technology (UST)

> General Relativity - The Next Generation February 19 - 23, 2018 YITP, Kyoto University

Standard Model of Cosmology

Using measurements and statistical techniques to place sharp constraints on parameters of the standard cosmological model.

Baryon density

 Ω_{h}

Dark Matter is Cold and weakly Interacting: Ω_{dm}

FLRW

Neutrino mass and radiation density: *fixed* by assumptions and CMB temperature

Dark Energy is Cosmological Constant:

 $\Omega_{\Lambda} = 1 - \Omega_b - \Omega_{dm}$

Universe is Flat

Initial Conditions: Form of the Primordial Spectrum is *Power-law*

 n_s, A_s

Epoch of reionization

au

Hubble Parameter and the Rate of Expan H_0

Standard Model of Cosmology

Using measurements and statistical techniques to place sharp constraints on parameters of the standard cosmological model.

Baryon density

FLRW

Combination of Assumptions

Dark Energy is *Cosmological Constant*:

 $\Omega_{\Lambda} = 1 - \Omega_b - \Omega_{dm}$

Universe is Flat

Epoch of reionization

Hubble Parameter and the Rate of Expan H₀

 $\boldsymbol{\tau}$

 n_s, n_s

Standard Model of Cosmology

combination of *reasonable* assumptions!



But there can be always a but.....

Beyond the Standard Model of Cosmology



- The universe might be more complicated than its current standard model (Vanilla Model).
- There might be some extensions to the standard model in defining the cosmological quantities.
- This needs proper investigation, using advanced statistical methods, high performance computational facilities and high quality observational data.

How to go Beyond the Standard Model of Cosmology?

•



• Finding features in the data beyond the flexibility of the standard model (using non-parametric reconstructions or using hyper-functions).

 Introducing theoretical/phenomenological models that can explain the data better (statistically significant) with respect to the standard model.

Finding tension among different independent data assuming the standard model (making sure there is no systematic).

Implementing well cooked statistical approaches to get the most out of the data is essential!

Testing deviations from an assumed model (without comparing different models)

Gaussian Processes:

Modeling of the data around a mean function searching for features by looking at the likelihood space of the hyperparameters.

Bayesian Interpretation of Crossing Statistic:

Comparing a model with its own possible variations considering a hyperfunction.

Gaussian Process

Efficient in statistical modeling of stochastic variables
 Derivatives of Gaussian Processes are Gaussian
 Processes

Provides us with all covariance matrices

Mean Function

Data

Shafieloo, Kim & Linder, PRD 2012 Shafieloo, Kim & Linder, PRD 2013



Detection of the features in the residuals







GP Reconstruction of Planck TT, TE, EE spectra

Aghamousa, Hamann & Shafieloo, JCAP 2017





Excellent agreement between Planck & the best-fit LCDM



GP Reconstruction of Planck TT, TE, EE spectra Aghamousa, Hamann & Shafieloo, JCAP 2017





l

Bayesian Interpretation of Crossing Statistics

- To deal with unknown uncertainties/ systematics in the data.
- To go beyond averaging nature of Chi square statistic (as a core metric in most statistical analysis) extracting more information from the data.

Theoretical Model

Crossing Function

 $\mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\mathrm{modified}}^{N} = \mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\Omega_{\mathrm{b}}, \Omega_{\mathrm{CDM}}, \mathrm{H}_{0}, \tau, \mathrm{A}_{\mathrm{s}}, \mathrm{n}_{\mathrm{s}}} \times T_{N}(C_{0}, C_{1}, C_{2}, ..., C_{N}, \ell).$

•

$$\begin{split} T_0(C_0,x) &= C_0 \\ T_{\rm I}(C_0,C_1,x) &= T_0(C_0,x) + C_1 \ x \\ T_{\rm II}(C_0,C_1,C_2,x) &= T_{\rm I}(C_0,C_1,x) + C_2(2x^2-1) \\ T_{\rm III}(C_0,C_1,C_2,C_3,x) &= T_{\rm II}(C_0,C_1,C_2,x) + C_3(4x^3-3x) \\ T_{\rm IV}(C_0,C_1,C_2,C_3,C_4,x) &= T_{\rm III}(C_0,C_1,C_2,C_3,x) + C_4(8x^4-8x^2+1) \\ T_{\rm V}(C_0,C_1,C_2,C_3,C_4,C_5,x) &= T_{\rm IV}(C_0,C_1,C_2,C_3,C_4,x) + C_5(16x^5-20x^3+5x). \end{split}$$

Shafieloo et al JCAP 2011 Shafieloo, JCAP 2012a Shafieloo, JCAP 2012b

$$x = \ell / \ell_{\max} - \ell$$

$$\ell_{\rm max} = 2500$$

Chebychev polynomials have the properties of orthogonality and convergence within the limited range of -1 < x < 1.



Crossing parameters marginalized over cosmological parameters fitting TT data Test of consistency between LCDM model and Planck 2015 data 5 0.0

-0.8

-1.6

1.6

0.8

0.8

-1.6

1.6

0.8

5 0.0

-0.8

-1.6

5 0.0









Why to go beyond Power-Law PPS if data consistent to the standard model (and single field inflation) ?

- 1. PL is consistent to the data, but there might be other interesting forms of PPS also consistent to the current data. This can have important theoretical implications to consider more complicated inflationary scenarios or alternative models.
- 2. Non-PL forms of the PPS possibly result to different background parameters fitting the same data. Crucial for cosmological parameter estimation and studying late universe.
- 3. Might help (or may not) resolving tensions between different cosmological observations within the framework of the LCDM model.
- 4. Power-law PPS (and standard model in general) is boring.







Model Independent Estimation of Primordial Spectrum



Figure 4. Reconstruction of the shape of the primordial power spectrum in 16 bands after marginalising over the Hubble constant, baryon and dark matter densities, and the redshift of reionization.

What is usually done: Binning Primordial Spectrum







Direct Reconstruction of the Primordial Spectrum

Modified Richardson-Lucy Deconvolution

→ Iterative algorithm.
 → Not sensitive to the initial guess.
 → Enforce positivity of P(k).
 [G(l,k) is positive definite and C₁ is positive]

$$C_{\ell} = \sum_{i} G_{\ell k_i} P_{k_i}$$

$$P_{k}^{(i+1)} - P_{k}^{(i)} = P_{k}^{(i)} \times \left[\sum_{\ell=2}^{\ell=900} \widetilde{G}_{\ell k}^{\mathrm{un-binned}} \left\{ \left(\frac{C_{\ell}^{\mathrm{D}} - C_{\ell}^{\mathrm{T}(i)}}{C_{\ell}^{\mathrm{T}(i)}} \right) \operatorname{tanh}^{2} \left[Q_{\ell} (C_{\ell}^{\mathrm{D}} - C_{\ell}^{\mathrm{T}(i)}) \right] \right\}_{\mathrm{un-binned}} + \sum_{\ell_{\mathrm{binned}} > 900} \widetilde{G}_{\ell k}^{\mathrm{binned}} \left\{ \left(\frac{C_{\ell}^{\mathrm{D}} - C_{\ell}^{\mathrm{T}(i)}}{C_{\ell}^{\mathrm{T}(i)}} \right) \operatorname{tanh}^{2} \left[\frac{C_{\ell}^{\mathrm{D}} - C_{\ell}^{\mathrm{T}(i)}}{\sigma_{\ell}^{\mathrm{D}}} \right]^{2} \right\}_{\mathrm{binned}} \right], \quad (1)$$

Shafieloo & Souradeep PRD 2004 ; Shafieloo et al, PRD 2007; Shafieloo & Souradeep, PRD 2008; Nicholson & Contaldi JCAP 2009 Hamann, Shafieloo & Souradeep JCAP 2010 Hazra, Shafieloo & Souradeep PRD 2013 Hazra, Shafieloo & Souradeep JCAP 2013 Hazra, Shafieloo & Souradeep JCAP 2014 Hazra, Shafieloo & Souradeep JCAP 2014

$$Q_{\ell} = \sum_{\ell'} (C_{\ell'}^{\mathrm{D}} - C_{\ell'}^{\mathrm{T}(i)}) COV^{-1}(\ell, \ell'),$$

Hazra, Shafieloo, Souradeep, in prep 2018



Primordial Power Spectrum from WMAP





Our symbol	Spectra	$Multipoles(\ell)$	Scales
α	low-l	2-49	Largest scales
a	$100~{\rm GHz}\times100~{\rm GHz}$	50-1200	Intermediate scales
ь	$143~{\rm GHz}\times143~{\rm GHz}$	50-2000	Intermediate scales
1	$217~{\rm GHz}\times217~{\rm GHz}$	500-2500	Small scales
2	$143~{\rm GHz}\times217~{\rm GHz}$	500-2500	Small scales

Primordial Power Spectrum from Planck

Hazra, Shafieloo & Souradeep, JCAP 2014





Starobinsky (1992) *Kink in the potential* Vilenkin and Ford (1982) *Pre-inflationary radiation dominated era* Contaldi et al, (2003) *Pre-inflationary kinetic dominated era* Cline et al, (2003) *Exponential cut off*

Shafieloo & Souradeep (2004) Direct Reconstruction

TABLE II: Best fit values of parameters specifying the initial power spectrum (k_*, α, R_*, n_s) and other relevant cosmological parameters for a class of model power spectra with a infrared cutoff (dataset used: WMAP TT data).

Parameter	Expo-cutoff EC(II)	Starobinsky SB(III)	Kin. Dom. KD(IV)	VF VF(V)	Expo-staro(a) ^{\dagger} ES-a(VI)	Expo-staro(b) [‡] ES-b(VI)	Power Law PL(I)
$k_*(\times 10^{-4}) \mathrm{Mpc}^{-1}$	$3.0^{+4.8}_{-2.9}$	$3.1^{+5.8}_{-2.8}$	$3.5^{+3.0}_{-3.3}$	$0.4^{+0.7}_{-0.3}$	$3.0^{+0.5}_{-2.0}$	$3.1^{+5.8}_{-2.1}$	_
α	$9.6\substack{+0.3\\-8.6}$	_	-	_	$0.58\substack{+4.6\\-0.43}$	$0.72^{+9.1}_{-0.55}$	
R_*	-	$0.73\substack{+0.25 \\ -0.14}$	-	-	$0.17\substack{+0.80\\-0.15}$	$0.35\substack{+0.63 \\ -0.20}$	_
n_s	$0.95\substack{+0.16 \\ -0.03}$	$0.98\substack{+0.14 \\ -0.07}$	$1.4\substack{+0.09 \\ -0.90}$	$1.0\substack{+0.04 \\ -0.15}$	$0.96\substack{+0.15 \\ -0.08}$	$0.99\substack{+0.08\\-0.12}$	$0.96\substack{+0.30\\-0.05}$
τ	$0.014\substack{+0.37\\-0.004}$	$0.15\substack{+0.25 \\ -0.14}$	$0.17\substack{+0.09 \\ -0.15}$	$0.01 {}^{+0.35}_{-0.001}$	$0.26_{-0.08}^{+0.15}$	$0.28\substack{+0.12 \\ -0.27}$	$0.014\substack{+0.500\\-0.004}$
z_{re}^{a}	$3.2^{+21.7}_{-0.7}$	$16.3^{+11.5}_{-13.9}$	$17.8^{+4.9}_{-15.2}$	$2.7^{+23.5}_{-0.22}$	$23.8_{-5.0}^{+5.9}$	$23.5^{+3.9}_{-21.0}$	$3.2^{+26.6}_{-0.83}$
Ω_{Λ}	$0.70\substack{+0.16 \\ -0.18}$	$0.71_{\pm 0.24}^{\pm 0.17}$	$0.70\substack{+0.13 \\ -0.21}$	$0.71\substack{+0.12 \\ -0.20}$	$0.74\substack{+0.13 \\ -0.10}$	$0.75_{-0.23}^{+0.12}$	$0.65\substack{+0.24 \\ -0.23}$
$\Omega_b h^2$	$0.022\substack{+0.006\\-0.001}$	$0.023\substack{+0.005\\-0.004}$	$0.024\substack{+0.001\\-0.002}$	$0.023\substack{+0.005\\-0.002}$	$0.023\substack{+0.004\\-0.003}$	$0.025\substack{+0.002\\-0.005}$	$0.023\substack{+0.009\\-0.002}$
$-\ln \mathcal{L}$	484.89	484.89	485.18	486.46	483.44	484.45	486.28
$\chi^2_{\rm eff} \equiv -2\ln {\cal L}$	969.78	969.78	970.36	972.92	966.88	968.90	972.56
d.o.f.	891	891	892	892	890	890	893

Theoretical Implication: Importance of the Features in the primordial spectrum

Beyond Power-Law: there are some other models consistent to the data.



Beyond Power-Law: there are some other models consistent to the data.



	Individual likelihoods comparison							
Individual	Baseline	WWI-a	WWI-b	WWI-c WWI-d		WWI'		
likelihood		$\Delta_{\rm DOF} = 4$	$\Delta_{ m DOF} = 2$					
TT	761.1	762	761.9	762.8	762.8	762.4		
lowT	15.4	8.2	13.4	12.1	13	10.2		
Total	778.1	772.1 (-6)	777 (-1.1)	777 (-1.1)	778.4 (0.3)	775 (-3.1)		
EE	751.2	748.8	747.2	748.6	750.2	746.8		
lowTEB	10493.6	10490	10495.6	10492.4	10495.7	10492.2		
Total	11248.8	11241.8 (-7)	11246.2 (-2.6)	11244.5 (-4.3)	11249.3(0.5)	11242.3 (-6.5)		
TTTEEE	2431.7	2432.7	2422.6	2427.8	2421.7	2426.5		
lowTEB	10497	10490.8	10495.1	10493.4	10495.3	10492.7		
Total	Total 12935.6 1292		12924.2 (-11.4)	12927.6 (-8)	12923.4 (-12.2)	12925.2 (-10.4)		
TT	764.5	763.6	762.2	764.4	762.9	762.8		
\mathbf{EE}	753.9	754.8	750.5	750.8	750.8	751		
\mathbf{TE}	932	933.4	928.7	929.2	927	928.8		
lowTEB	10498.4	10490.4	10495.8	10493.7	10495.6	10492.4		
BKP	41.6	42	42	42.6	41.8	42.9		
Total	12997	12991 (-6)	12985.9 (-11.1)	12987.2 (-9.8)	12985 (-12)	12985.1 (-11.9)		
TTTEEE	2431.7	2432.8	2421.4	2426.7	2421	2425.7		
lowTEB	10498.5	10490.5	10495.5	10493.6	10495.8	10492.6		
BKP	41.6	42	42.7	42	41.9	42.5		
Total	12978.3	12971.3 (-7)	12967.3 (-11)	12968.6 (-9.7)	12965 (-13.3)	12968.6 (-9.7)		
TT (bin1)	8402.1	8404.1	8403.9	8405.2	8402.1	8401.9		
lowT	lowT 15.4 8.3		13.3	11.9	13.2	10.3		
Total	8419.6	8414.7 (-4.9)	8419.5 (-0.1)	8419.8 (0.2)	8418.1 (-1.5)	8414.4 (-5.2)		
TTTEEE (bin1)	24158.2	24158.6	24149	24155	24148.4	24151.5		
lowTEB	10497.6	10490.3	10493.4	10493.6	10495.3	10492.7		
Total	34661.9	34655.3 (-6.6)	34650.5 (-11.4)	34654.4 (-7.5)	34649.5 (-12.4)	34650.6 (-11.3)		

Beyond Power-Law: there are some other models consistent to the data.

Wiggly Whipped Inflation

Hazra, Shafieloo, Smoot, JCAP 2013 Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2014A Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2014B Hazra, Shafieloo, Smoot, Starobinsky, PRL 2014 Hazra, Shafieloo, Smoot, Starobinsky, JCAP 2016







Forms of PPS and Effects on the Background Cosmology

- Flat Lambda Cold Dark Matter Universe (LCDM) with power–law form of the primordial spectrum
- It has 6 main parameters.

 $C_l = \sum G(l,k)P$

3

obs

 $P(k) = A_{\rm s} \left[\frac{k}{k}\right]^{n_{\rm s}-1}$

G(I,

 Ω_{b}

 Ω_m

 H_{0}

au

A

 n_{s}

Forms of PPS and Effects on the Background Cosmology

 Cosmological parameter estimation with free form primordial power spectrum

2

 $C_l =$

4

G(l,k)

C obs

3

G(I,k

2

P(k)





WMAP9 Data

Red Contours: Power Law PPS

Blue Contours: Free Form PPS

Hazra, Shafieloo & Souradeep, PRD 2013

Planck 2015

Considering Crossing hyperfunctions and effect on background parameters.



Shafieloo & Hazra, JCAP 2017

Planck 2015

Considering Crossing hyperfunctions and effect on background parameters.

Planck polarization data and local H0 measurements seems having irresolvable tension. Maybe either or both have systematics? If not, new physics might be the answer.

Notice:

Planck was designed to be a full sky temperature anisotropy probe

Shafieloo & Hazra, JCAP 2017



Complete reconstruction analysis with Planck polarization data

Works to do soon! (near future)

Full picture

$$C_{\ell}^{TT} = \int \frac{dk}{k} P(k) \quad G_{\ell}^{TT}(k)$$
$$C_{\ell}^{EE} = \int \frac{dk}{k} P(k) \quad G_{\ell}^{EE}(k)$$
$$C_{\ell}^{BB} = \int \frac{dk}{k} P(k) \quad G_{\ell}^{BB}(k)$$
$$C_{\ell}^{BB} = \int \frac{dk}{k} P(k) \quad G_{\ell}^{BB}(k)$$

Searching for correlations!

$$P_{S}(k), P_{T}(k), P_{iso}(k)$$

Primordial power spectra from Early universe Post recombination Radiative transport kernels in a **given** cosmology

 $G_{\ell}^{TT}(k), G_{\ell}^{EE}(k), G_{\ell}^{BB}(k), G_{\ell}^{TE}(k)$

Works to do soon! (maybe near future)

Joint constraint on inflationary features using the two and three-point correlations of temperature and polarization anisotropies





Bispectrum in terms of the reconstructed power spectrum and its first two derivatives

Appleby, Gong, Hazra, Shafieloo, Sypsas, PLB 2015

Features with Future of CMB

With Cosmic Origins Explorer (CORE)-like survey specification



- Large scale suppressions can not be detected with high significance
- Some of the intermediate and small scale oscillations can be detected, if present





From 2D to 3D

Using LSS data to test early universe scenarios

Key issues:

1. We need to estimate matter power spectrum but we observe galaxies. Hence we have to model the bias and estimate its parameters accurately and precisely to connect the observables to theory. Bias modeling would be different for different surveys and susceptible to systematics.

2. Does power spectrum (or bi-spectrum, etc) necessarily contains all the information in 3D data of LSS? Can't reducing dimensionality of the data wash out some information?

0.8156 0.9619

P15+HFI

0.319

66.93

From 2D to 3D



N-Body Simulation (DESI like)

L'Huillier, Shafieloo, Hazra, Smoot, Starobinsky arXiv:1710.10987





or LSS matter power spectrum.

3.0

2.5

2.0

1.5

1.0

Model

P15

WWIA

WWID

P15+HFI

 $P_s(k) (\mathrm{Mpc}^3)$

From 2D to 3D



N-Body Simulation (DESI like)

L'Huillier, Shafieloo, Hazra, Smoot, Starobinsky arXiv:1710.10987

10²

100

z = 0.7

z = 0

101

 $\log_{10} \mathcal{M}_{P15}$

10²

From 2D to 3D



N-Body Simulation (DESI like)

L'Huillier, Shafieloo, Hazra, Smoot, Starobinsky arXiv:1710.10987



From 2D to 3D



N-Body Simulation (DESI like)

L'Huillier, Shafieloo, Hazra, Smoot, Starobinsky arXiv:1710.10987



From 2D to 3D



N-Body Simulation (DESI like)

L'Huillier, Shafieloo, Hazra, Smoot, Starobinsky arXiv:1710.10987



Using mass-weighted halo density

Summary

- Standard power-law form of the primordial spectrum explains the current data well.
- Many models with features can be still consistent to the data. It is not only about getting closer to the actual inflation model but also the effect on late universe.
- Finding approaches to use efficiently large scale structure data to break the degeneracies between early universe scenarios is an important challenge.
- Using all power of the data is important. Probably we have to go beyond power-spectrum, bispectrum or conventional analysis.