PS-B7 Microscopic theory of the thermal response of topological superconductors

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Gravitational Chern-Simons theory

 $S_{\rm eff}^{\rm G} = \frac{C}{96\pi} \int dt d^2 x \,\epsilon^{\mu\nu\rho} {\rm tr} \left(\omega_{\mu} \partial_{\nu} \omega_{\rho} + \frac{2}{3} \omega_{\mu} \omega_{\nu} \omega_{\rho} \right)$

$$F_{\rm eff} = \int d^2 x \frac{2\kappa_H T}{v^2} \phi \Omega$$

Thermal current flows only along the boundary. [M. Stone, PRB 85, 184503 (2012)] K. Nomura et al., PRL 108, 026802 (2012).

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Dirac fermion + gravitational field

$$H = \int d^2 x \sqrt{g} \psi^{\dagger} \left[-iv e^{j}{}_{\alpha} \gamma^{0} \gamma^{\alpha} \overleftrightarrow{\partial_{j}} + m \gamma^{0} \right] \psi$$

$$F_{\rm eff} = \frac{\kappa_H T}{2\nu} \int_D d^2 x \, \epsilon^{jk} \partial_j h h_{k0} \qquad \kappa_H$$

$$H = \operatorname{sgn}(m) \frac{\pi T}{12}$$

1) Gravitational potential + rotation

$$g_{\mu\nu} = \begin{pmatrix} 1 + 2\phi & \Omega y/\nu & -\Omega x/\nu \\ \Omega y/\nu & -1 + 2\phi & 0 \\ -\Omega x/\nu & 0 & -1 + 2\phi \end{pmatrix}$$

Phenomenological effective free energy

$$F_{\rm eff} = \int d^2 x \frac{2\kappa_H T}{v^2} \phi \Omega$$

2) Gravitational potential (+ Luttinger's relation)

$$g_{\mu\nu} = \begin{pmatrix} 1+2\phi & 0 & 0\\ 0 & -1+2\phi & 0\\ 0 & 0 & -1+2\phi \end{pmatrix}$$

Quantized thermal Hall current

 $j_T^k = \kappa_H \epsilon^{kl} \partial_l T$