

Deformation of an Expanding Void in Redshift Space

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Introduction

- Peculiar velocity of a spherical void is determined by Ω and δ . [1]
- Cross-correlation between CMB & LSS indicates existence of nonlinear voids $> 100\text{Mpc}$ [2,3]



Can we test universe model by observation of voids?
How does expanding void look in z-space?

References

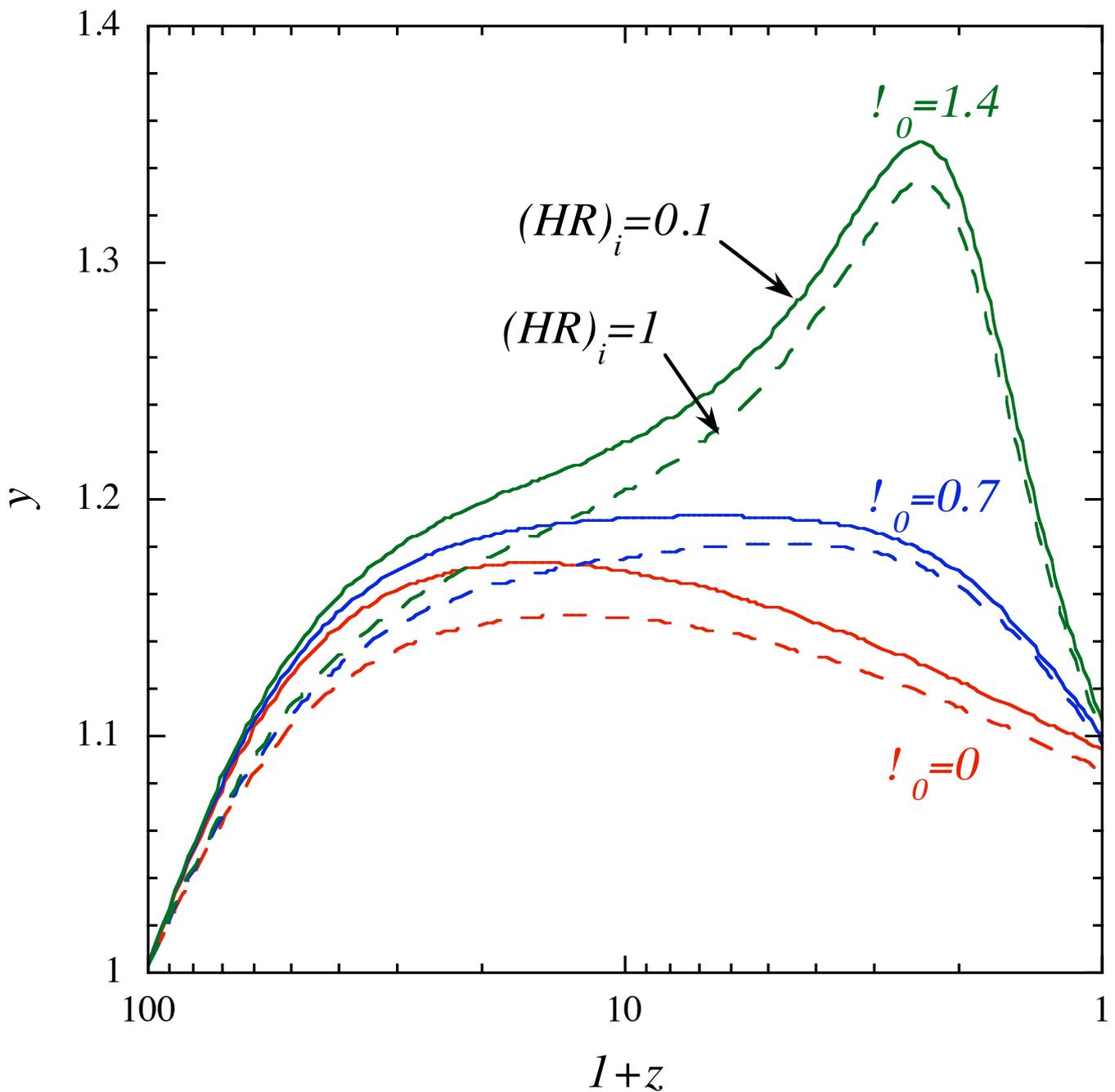
- [1] NS, K. Maeda, H. Sato, 1993, PTP
- [2] B. Granett, M. Neyrinck & I. Szapudi, 2008, ApJL
- [3] K. Inoue, NS & K.Tomita 2010, ApJ

Dynamics of void

- **Time evolution of shell velocity of empty void**

$$y \equiv 1 + v/HR$$

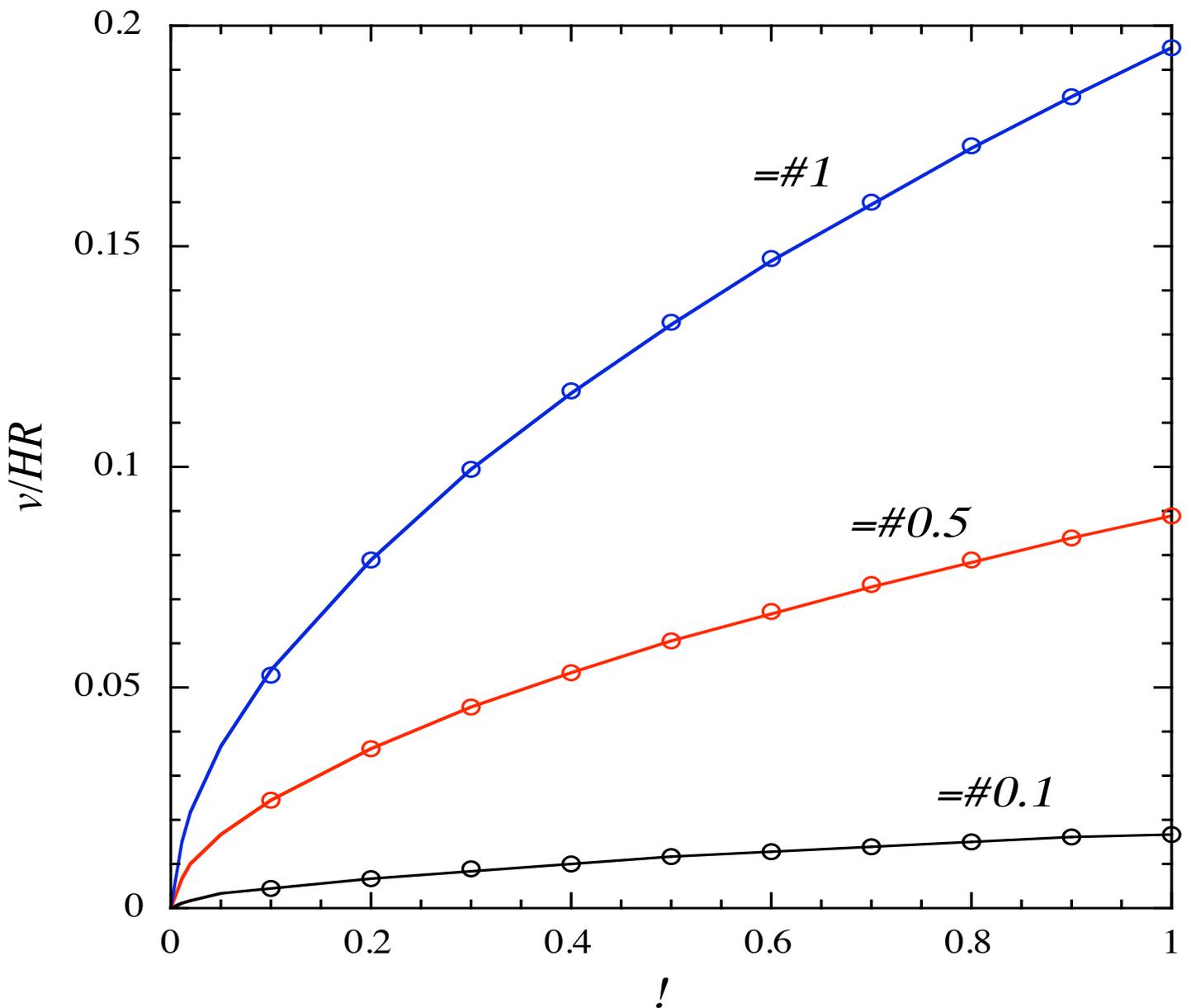
Fix $\Omega_0=0.3$ and change λ_0 .



- **Velocity vs Ω and δ for non-empty voids**

Fitting formula:

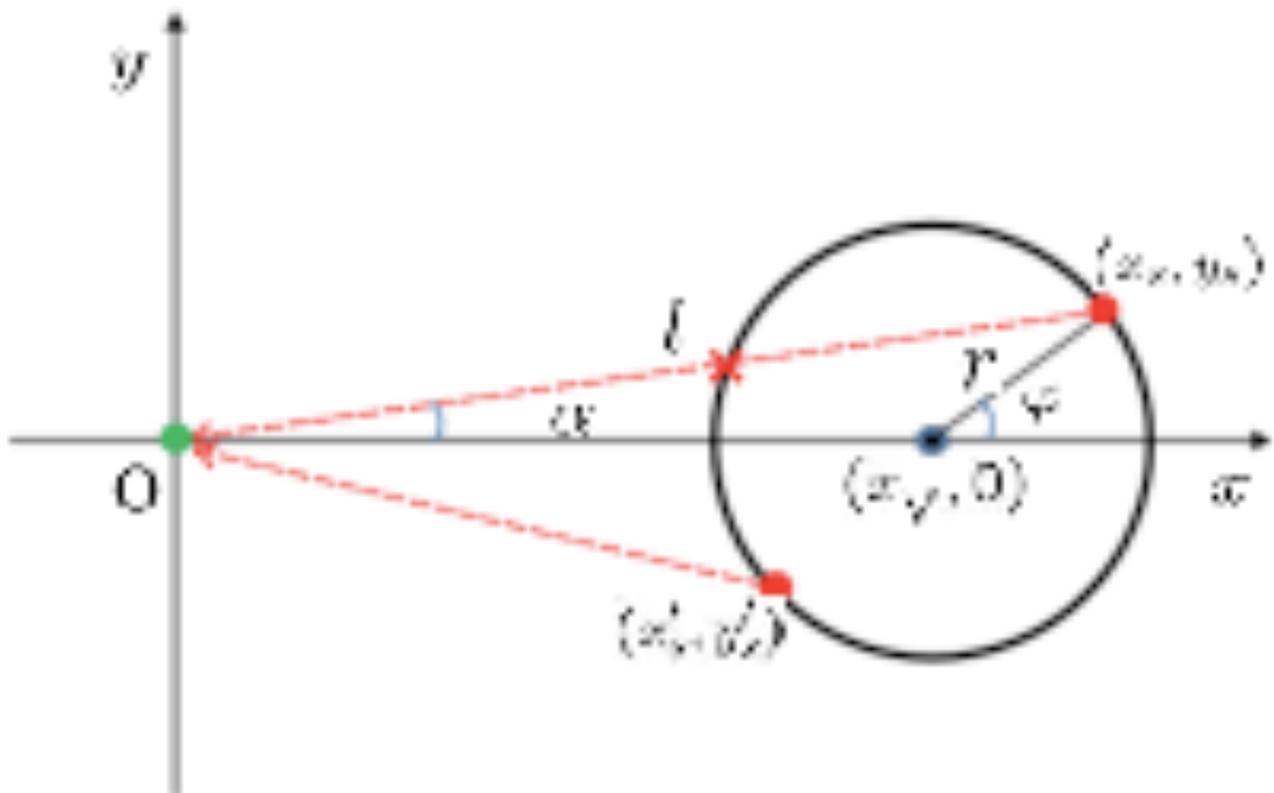
$$y - 1 = \frac{v}{HR} = \frac{\Omega^{0.56}}{6} (|\delta| + 0.1|\delta|^2 + 0.07|\delta|^3), \quad \text{for } \Omega + \lambda = 1$$



Deformation of void in redshift space

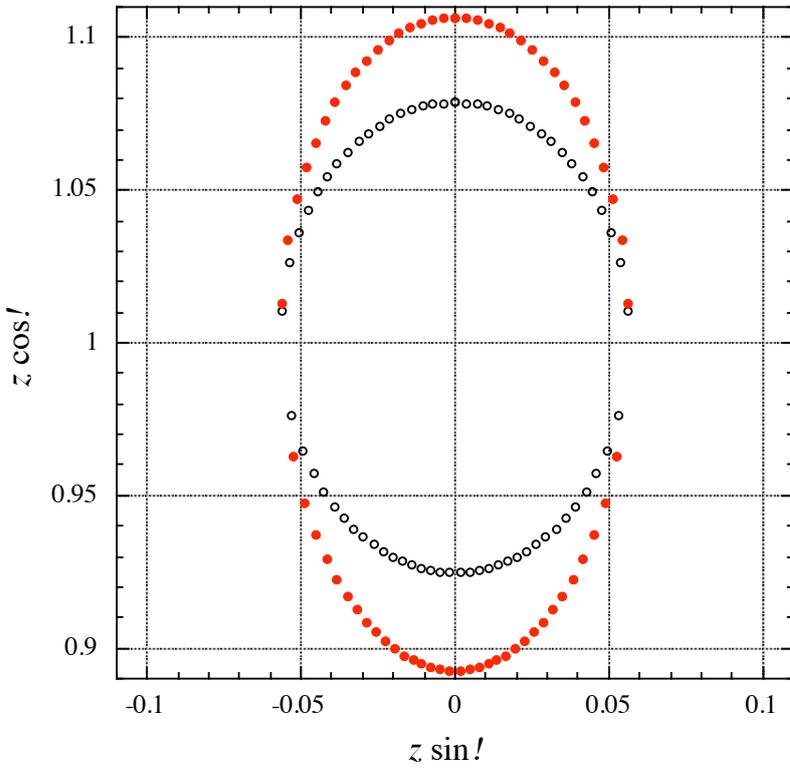
- **Analysis method**

- Solve equation of motion of shell.
- Solve null geodesic equations from shell to observer.

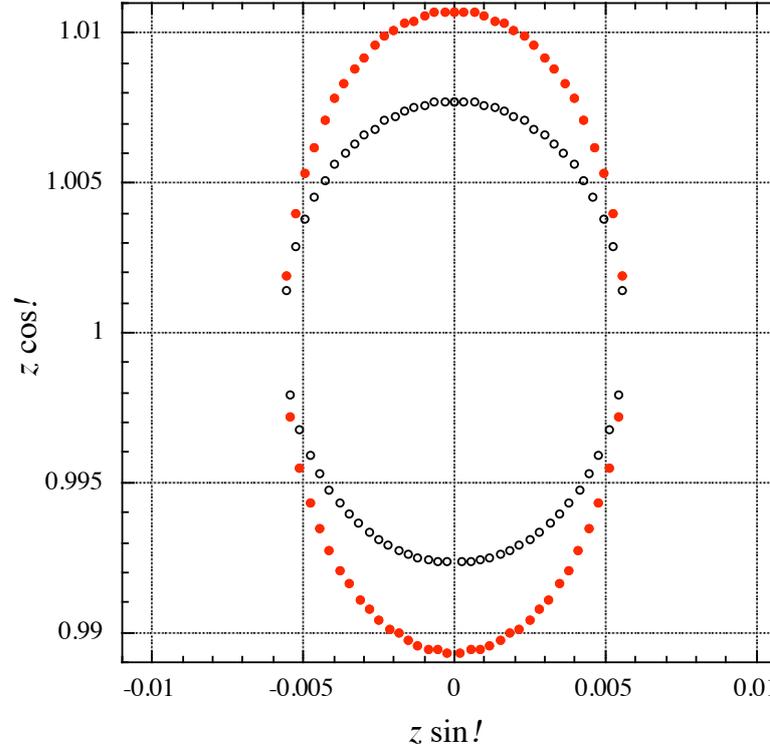


- **Dependence on void size**

Deformation ratio is almost independent of size.



(a) $0.1H_0^{-1}$,



(b) $0.01H_0^{-1}$

Figure 3: The image in the redshift space of an empty void at $z_V = 1$. The observer is located at the origin $(0, 0)$. We show two voids with different scales, i.e., the present sizes of voids are (a) $R_0 = 0.1H_0^{-1}$ and (b) $0.01H_0^{-1}$, respectively. Note that the observed sizes of voids are $R_V(z_V = 1) = 0.0437H_0^{-1}$ for (a) and $0.00437H_0^{-1}$ for (b), respectively. The red dots denote the image in the redshift space for the universe with $\Omega_0 = 0.3$ and $\lambda_0 = 0.7$. For a reference, we also show a $r = \text{constant}$ surface ($r = r(z = 1)$) in the $\Omega_0 = 0.3$ universe by the small black circles. Although the void is spherical, the shape of the $r = \text{constant}$ surface is not spherical because the physical radius with $r = \text{constant}$ changes in time.

- **Dependence on z (location)**

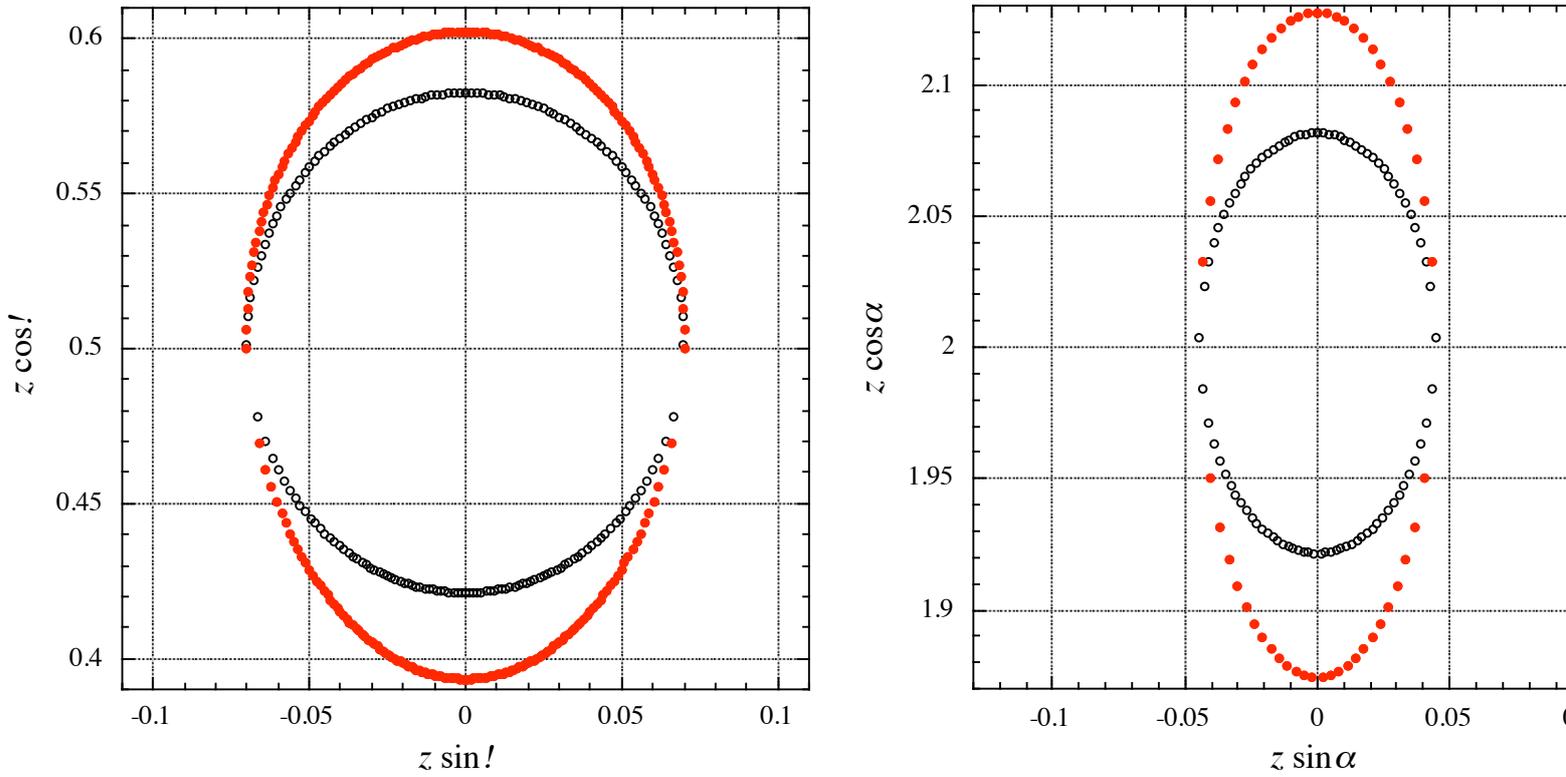
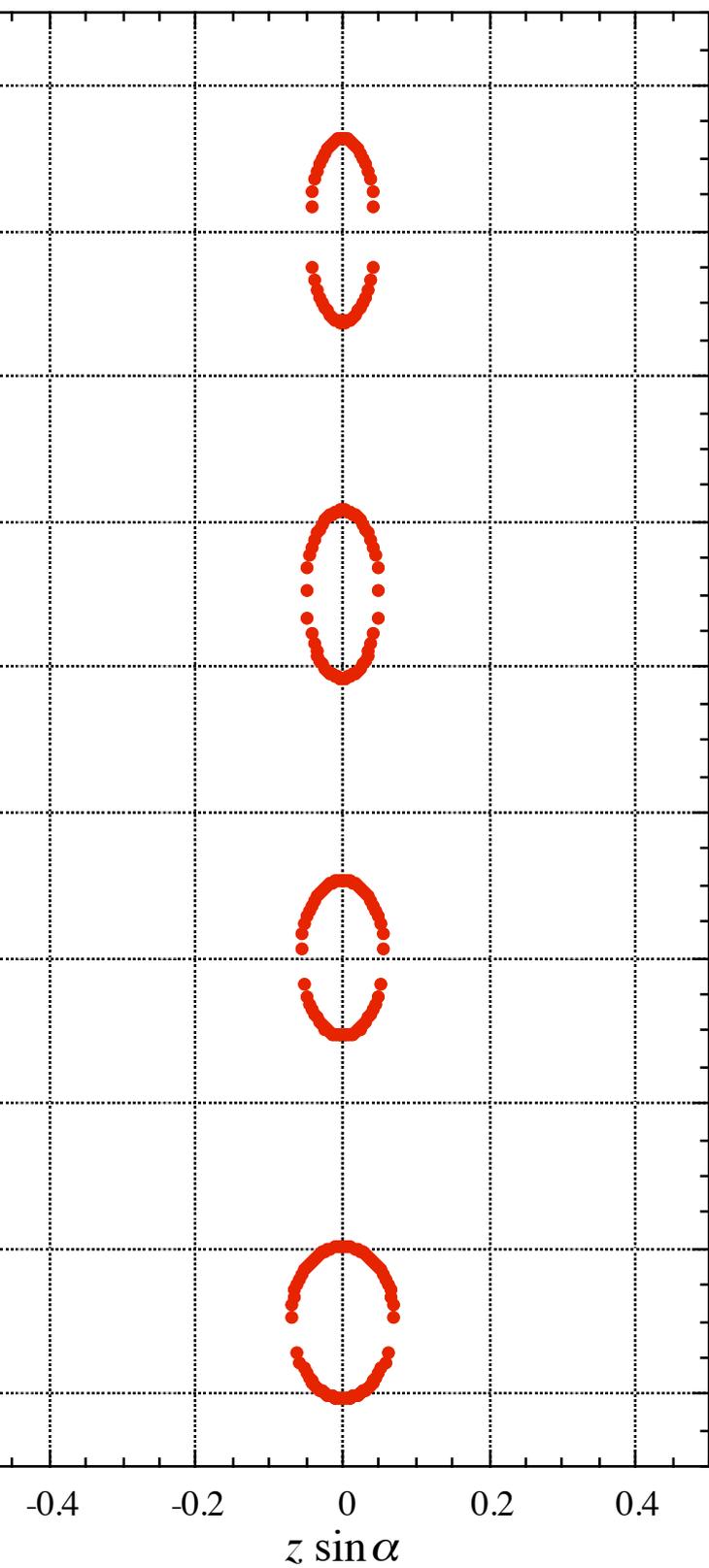
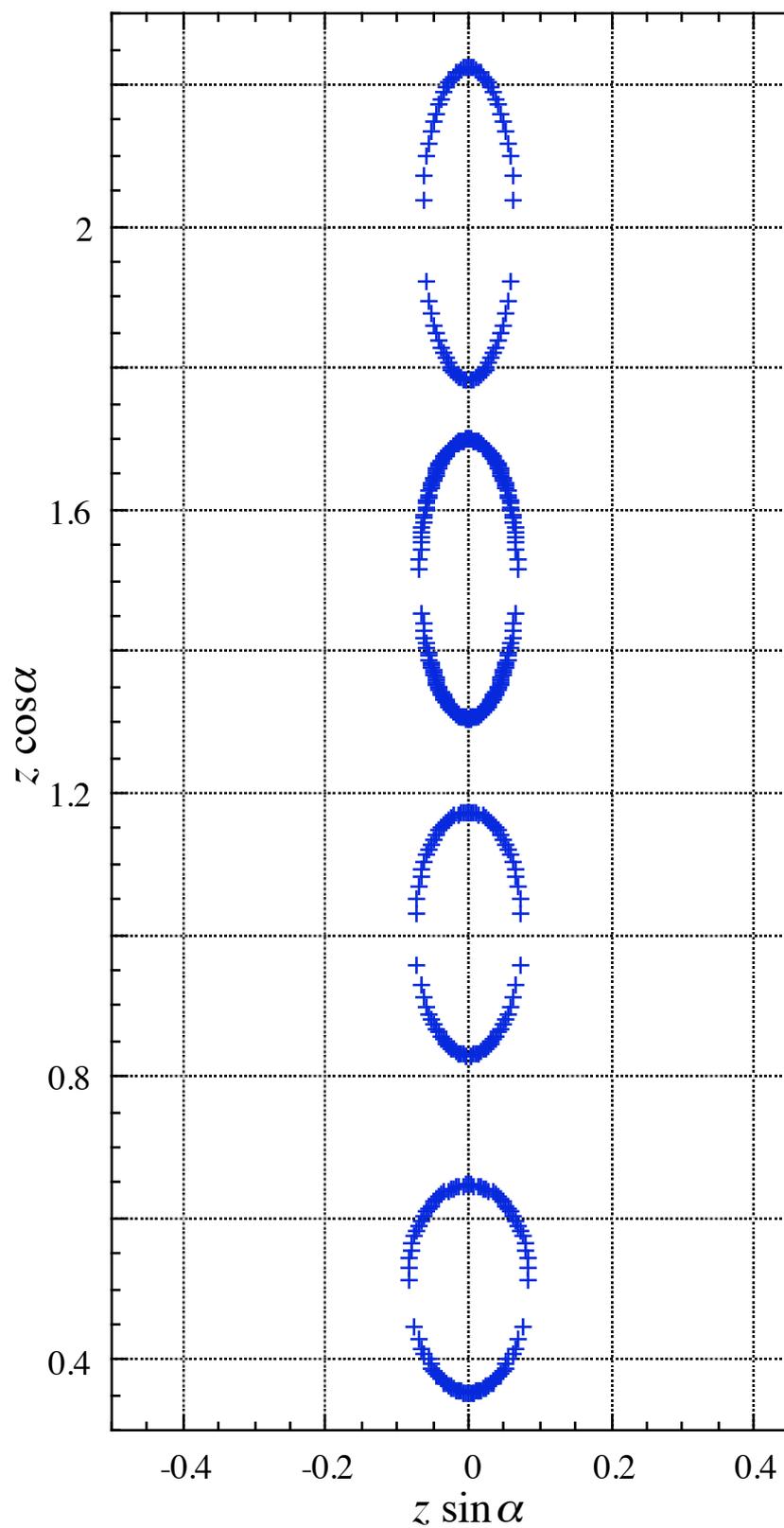


Figure 4: The image in the redshift space of an empty void located at $z_V = 0.5$ (a) and at $z_V = 2$ (b). We choose the scale of the void is $R_0 = 0.1H_0^{-1}$. The red dots and the small black circles are the same as those in Fig. 4. Note that the observed sizes of voids are $a_0r(z = 0.5) = 0.0616H_0^{-1}$ (a), and $a_0r(z = 2) = 0.0269H_0^{-1}$ (b), respectively.

Dependence on universe model



$\Omega_0=0.3, \lambda_0=0.7$



$\Omega_0=1, \lambda_0=0$

Summary: how much is shape of void deformed?

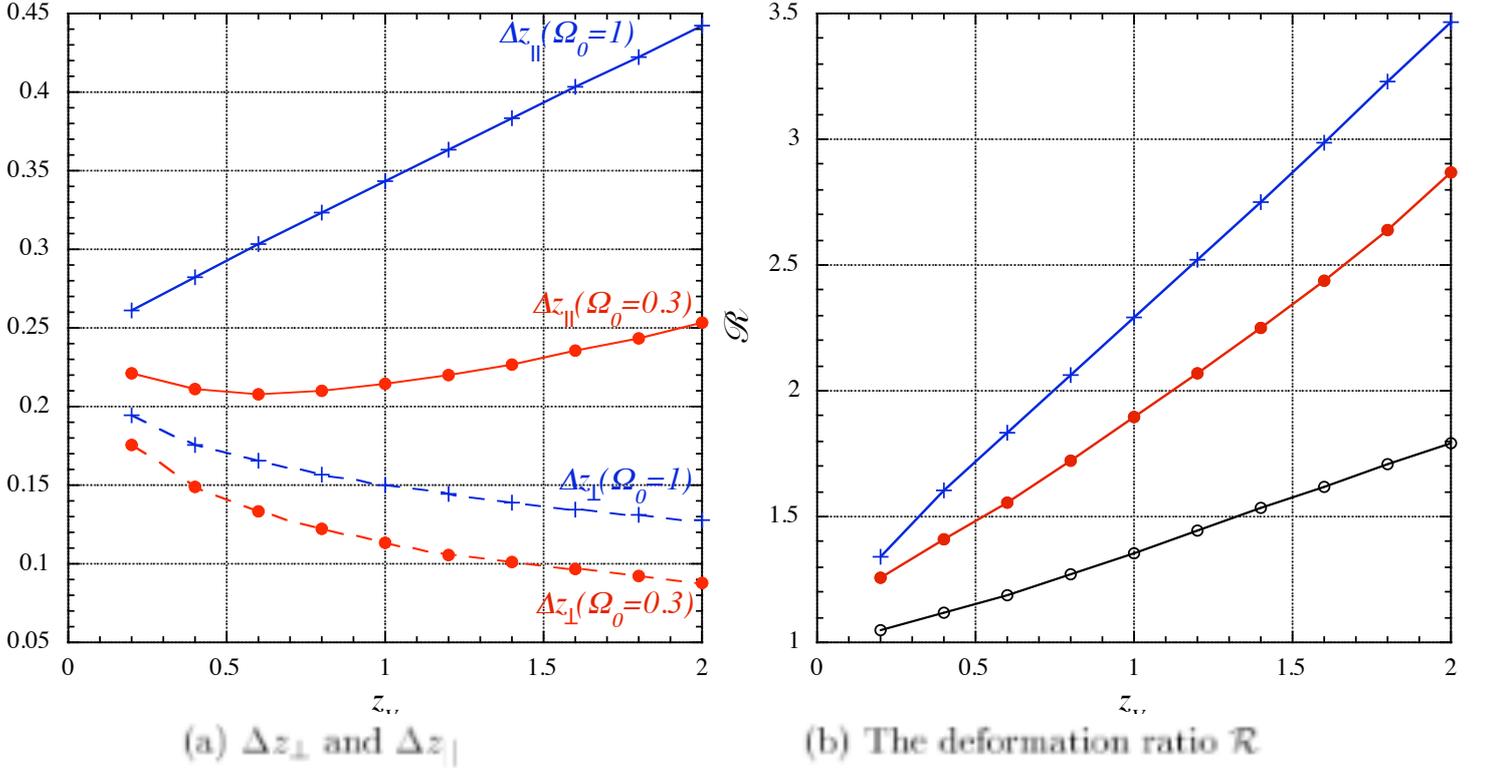


Figure 6: (a) The semi-major axis Δz_{\parallel} and the semi-minor axis Δz_{\perp} in terms of the distance z_v . We find that Δz_{\perp} always decreases as z_v increases because the observed void size gets small. On the other hand, Δz_{\parallel} increases as z_v increases due to the Doppler effect except for nearby voids for $\Omega_0 = 0.3$. (b) The deformation ratio \mathcal{R} of the shape of a void in the red shift space, which is defined by $\mathcal{R} = \Delta z_{\parallel} / \Delta z_{\perp}$, where Δz_{\parallel} and Δz_{\perp} are the semi-major axis and semi-minor axis radii of the void shape in the redshift space, respectively. The ratio \mathcal{R} increases as the distance z_v increases. We also find the ratio \mathcal{R} highly depends on the background cosmological model, which may give us some information on a cosmological constant.

Conclusions

- We show dynamics of spherical void and its deformation in redshift space.
 - Expanding void is prolonged in light of sight.
 - Deformation ratio depends on **universe model** and **void location**, but **independent of size**.
- If voids $>100\text{Mpc}$ at $z\sim 1$ exist, we will find such a deformation in future deep sky survey, and confirm existence of Λ .