

# The CMB bispectrum from vector-mode perturbations induced by primordial magnetic fields

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- ▶ MS + in prep. of full paper

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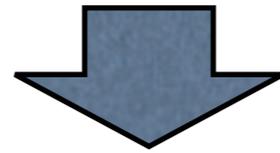
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❖ collaborators:

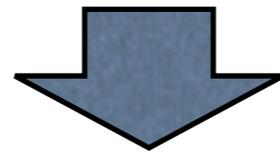
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# Abstract

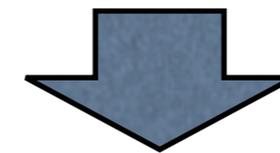
one of the studies to probe the nature of the early universe :  
constraint on Primordial Magnetic field (PMF) by the analysis of  
CMB bispectrum



PMF can become a source of CMB bispectra generated from  
scalar, vector and tensor-mode perturbations

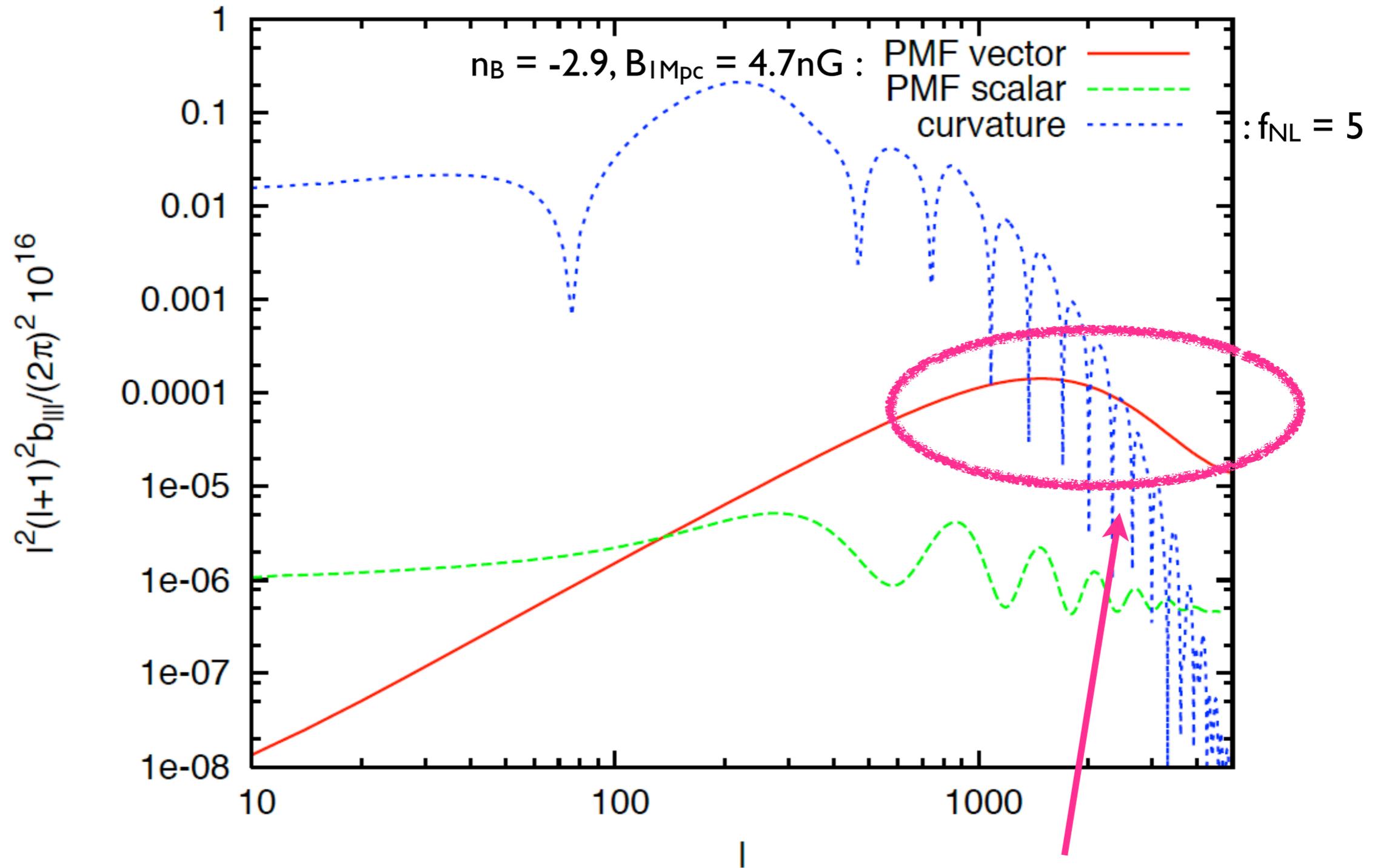


So far, for simplicity, only the dependence on scalar magnetic  
mode has been considered, despite greater effect of vector one



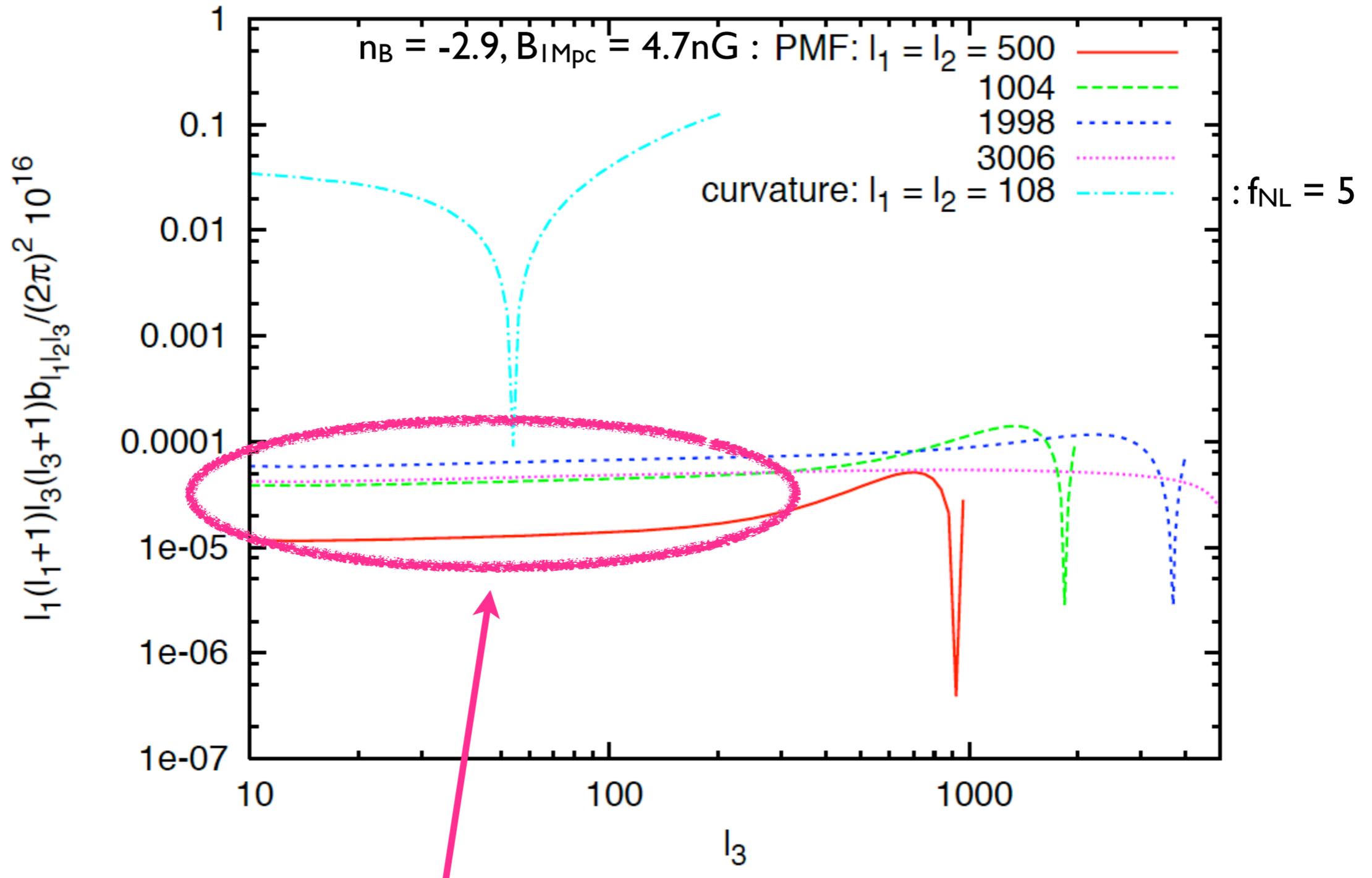
We compute the contribution of vector mode  
and update bound on the magnitude of PMF

# CMB reduced bispectrum of intensity mode for $l_1 = l_2 = l_3$

$$b_{\ell_1 \ell_2 \ell_3} \equiv \sqrt{\frac{(4\pi)}{(2\ell_1+1)(2\ell_1+2)(2\ell_1+3)}} \begin{pmatrix} \ell_1 & \ell_2 & \ell_3 \\ 0 & 0 & 0 \end{pmatrix}^{-1} B_{\ell_1 \ell_2 \ell_3}$$


vector component of  $b_{\text{III}}$  dominates at small scale

# CMB reduced bispectrum of intensity mode for $l_1 = l_2 \neq l_3$



the shape of vector bispectrum for  $n_B = -2.9$  is close to the local-type configuration due to  $b_{lll} \propto l_3^{-2}$

# Constraints

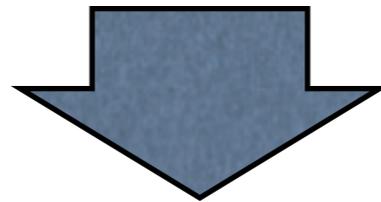
● our bispectrum of magnetic vector mode ( $n_B = -2.9$ )

$$\ell_1(\ell_1 + 1)\ell_3(\ell_3 + 1)b_{\ell_1\ell_2\ell_3} \sim -2 \times 10^{-19} \left( \frac{B_{1\text{Mpc}}}{4.7\text{nG}} \right)^6$$

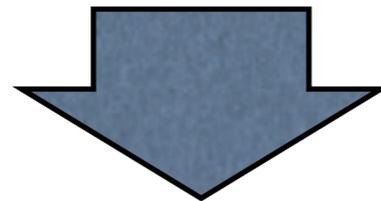
VS

● bispectrum from PNG in the curvature perturbations

$$\ell_1(\ell_1 + 1)\ell_3(\ell_3 + 1)b_{\ell_1\ell_2\ell_3} \sim 4 \times 10^{-18} f_{\text{NL}}^{\text{local}}$$



$$\left( \frac{B_{1\text{Mpc}}}{1\text{nG}} \right) \sim 7.74 |f_{\text{NL}}^{\text{local}}|^{1/6} \quad (\text{for } n_B = -2.9)$$



tighter by factor of two  
than Seshadri + (2009)!!

▶ WMAP :  $|f_{\text{NL}}| < 100$    $B_{1\text{Mpc}} < 17\text{nG}$  

▶ PLANCK :  $|f_{\text{NL}}| < 5$    $B_{1\text{Mpc}} < 10\text{nG}$