



Non-Gaussianity in a nucleated bubble

YITP, Kyoto University

Kazuyuki Sugimura

(Collaborator : D. Yamauchi, T. Tanaka and M. Sasaki)



Contents

- Introductions
 - non-Gaussianity
 - bubble nucleation
- Formulation and sample calculation
 - toy model
 - QFT on instanton background
 - inhomogeneous non-Gaussianity
- Conclusions and Future works



Introductions

Inflation and observation

□ Inflation explains beginning of Big Bang

- Horizon problem
- Flatness problem
- Monopole problem

□ CMB 2-point correlation agrees astonishingly with the prediction from inflation

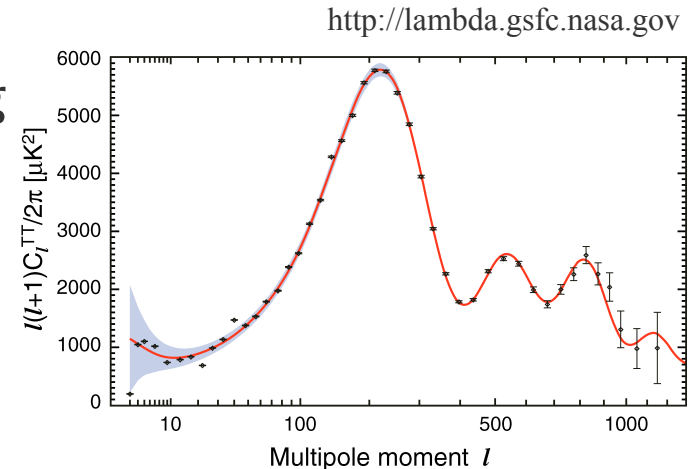
□ CMB 3-point correlation is now getting within reach

- Current status of local type Non-Gaussianity (WMAP7yr)

$$f_{\text{NL}} = 32 \pm \underline{42} \text{ (95\% C.L.)}$$

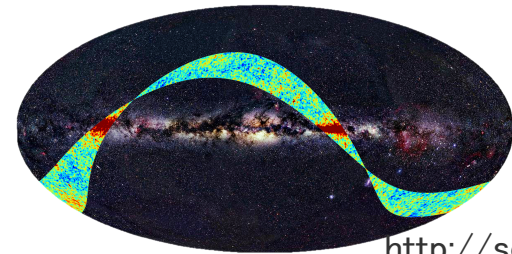


$$\sim \underline{5} \text{ Planck data (2013?)}$$



Non-Gaussianity tells us detail of inflation

Planck first light(2009)



<http://sci.esa.int>

□ simple slow-roll inflation model

- predict small non-Gaussianity and might be disfavored by Planck
- thinking beyond slow-roll approximation may become necessary



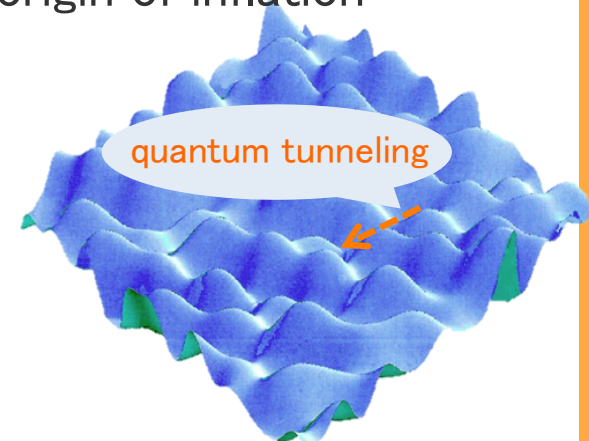
detail of inflation



the secret origin of inflation

□ inflation in string landscape (Susskind, 2003)

- possesses more details than simple slow-roll model
 - local potential minima
 - multi-field
- realization of inflation in string theory
- attractive candidate explanation for the origin of inflation



<http://journalofcosmology.com>

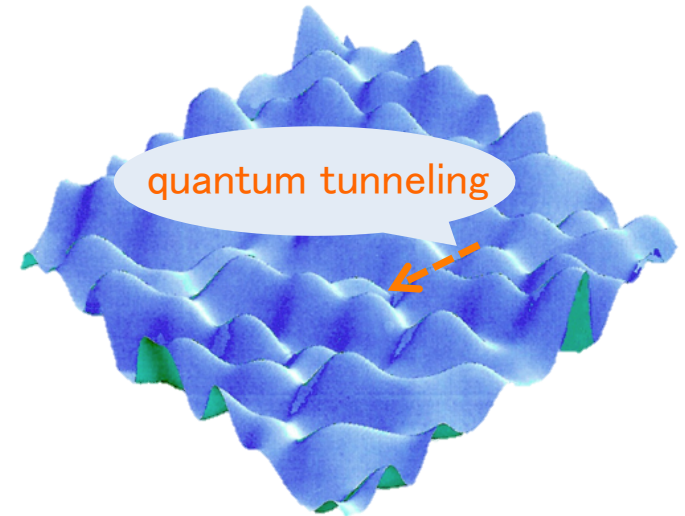


Bubble nucleation in string landscape

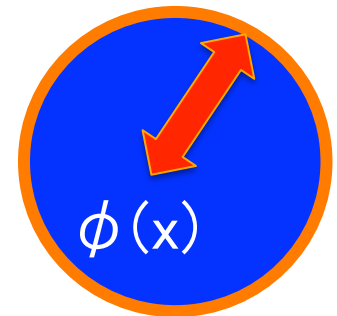
- tunneling of scalar field
 - many local minima in string landscape
 - transition between local minima occurs by quantum tunneling in inflationary era
 - transition occurs locally to keep causality

➔ Bubble nucleation

- non-Gaussianity generation by the nucleated bubble
 - non-linear interaction between scalar field and bubble
 - how to calculate?
 - what kind of feature?



<http://journalofcosmology.com>



Bubble

We will answer these questions using toy model!



Formulation and sample calculation of non-Gaussianity from bubble

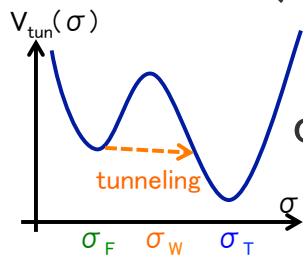
Toy model (1)

consider two-field model

- tunneling field : $\sigma(x)$
- test field : $\phi(x)$
- we will calculate 3-point function of $\phi(x)$ under the influence of tunneling field $\sigma(x)$ as background
- first step towards realistic model \rightarrow neglect gravitational effect

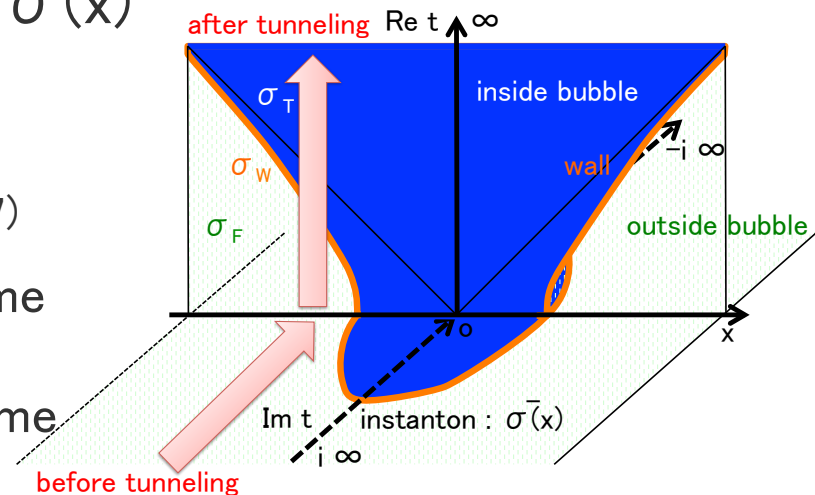
Background : bubble nucleation of $\sigma(x)$

- tunneling potential : $V_{\text{tun}}(\sigma)$
- $O(4)$ symmetric instanton : $\bar{\sigma}(x)$ (Coleman 1977)



classical solution in imaginary time

analytical continuation to real time



(we consider $V_{\text{tun}}(\sigma)$ which possesses thin wall instanton)

Toy model(2)

□ another test field $\phi(x)$

- we consider interaction with tunneling field

$$V_{\text{int}}(\phi, \sigma) = \lambda(\sigma) \phi^3$$

$$\lambda(x) = \lambda(\bar{\sigma}(x))$$

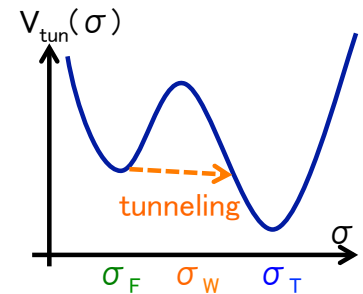
$$V_{\text{int}}(\phi, x) = \lambda(x) \phi^3$$

- we consider a model with significant 3-pt self coupling only near bubble wall

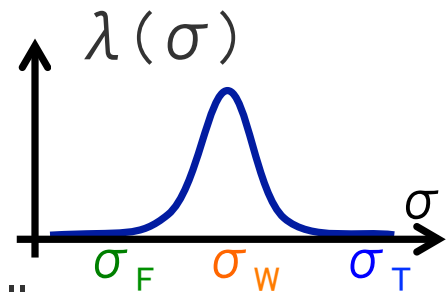
□ Indicator for non-Gaussianity

- 3-point function of the test field at the same space-time point

$$\langle \phi^3(t_0, \mathbf{x}) \rangle \quad (\langle \phi^3(t_0, \mathbf{x}) \rangle = 0 \text{ in free field theory})$$



background bubble



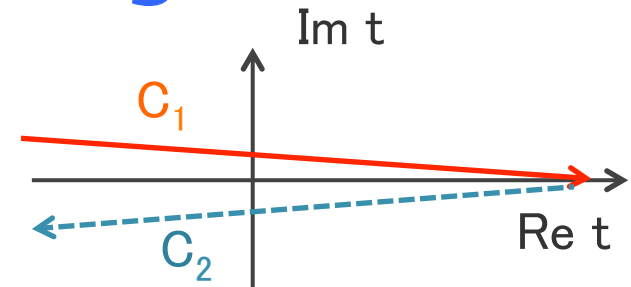
How can we describe QFT on instanton background, or tunneling?

QFT on instanton background

usual in-in formalism (Mardacena 2002)

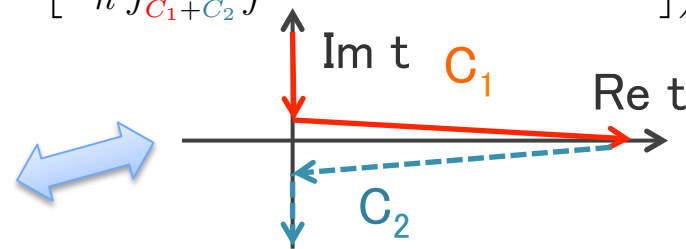
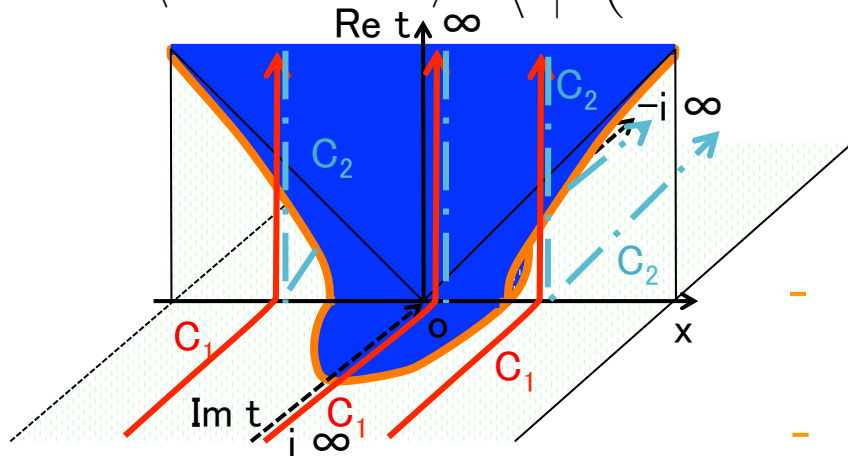
$$\langle \phi(x_1)\phi(x_2)\phi(x_3) \rangle = \langle 0 | P \left(\phi(x_1)\phi(x_2)\phi(x_3) \exp \left[-\frac{i}{\hbar} \int_{C_1+C_2} dt H_I[\phi(x)] \right] \right) | 0 \rangle$$

- integration of H_I along in-in time path



In-in formalism on instanton background (preliminary)

$$\langle \phi(x_1)\phi(x_2)\phi(x_3) \rangle = \langle 0 | P \left(\phi(x_1)\phi(x_2)\phi(x_3) \exp \left[-\frac{i}{\hbar} \int_{C_1+C_2} dt \int d^3\mathbf{x} \sqrt{-g} V_{\text{int}}(\bar{\sigma}(x), \phi(x)) \right] \right) | 0 \rangle$$



- in-in time path including imaginary time
- interactions during tunneling
- V_{int} depends on background bubble

We have derived this formulation in Quantum Mech.

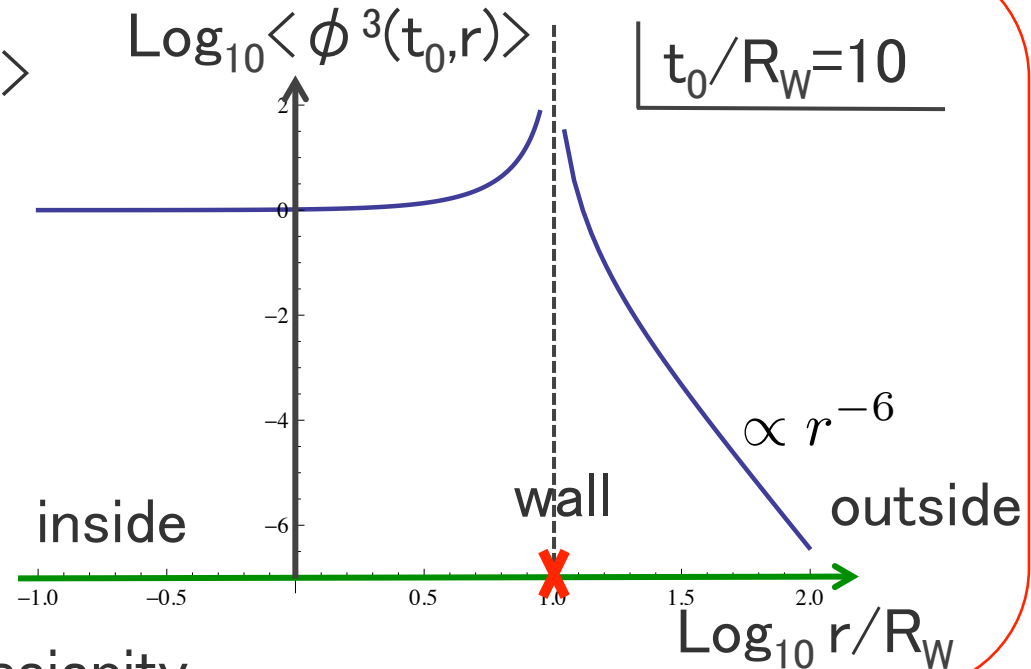
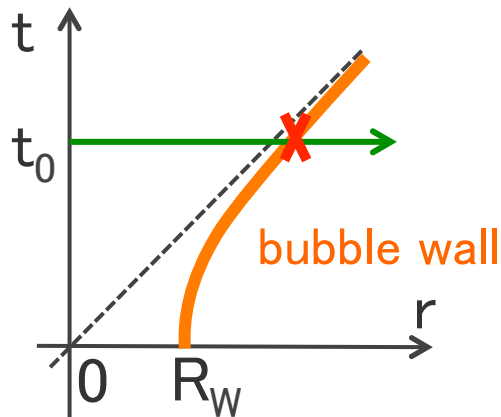
- solving tunneling wave function (in free theory cf. Yamamoto 1993)
- derivation in QFT is now in progress!!

Result (preliminary)

$\langle \phi^3(t_0, \mathbf{x}) \rangle = 0$ in free field theory

3-point function $\langle \phi^3(t_0, r) \rangle$

- along $t=t_0$ surface



inhomogeneity in non-Gaussianity

- asymptotic dependence

- far outside the bubble
- near the bubble wall
- around the center of the bubble

$$\langle \phi^3 \rangle \propto r^{-6}$$

$$\langle \phi^3 \rangle \rightarrow \infty \quad (\text{due to thin-wall approximation})$$

$$\langle \phi^3 \rangle \rightarrow \text{const.}$$

This is the first calculation of non-Gaussian correlation on $O(4)$ -symmetric instanton background!!

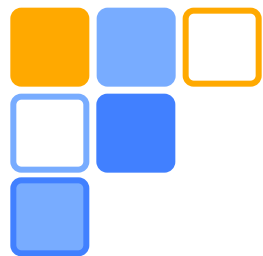


Conclusions and future works



Conclusions

- We have studied non-Gaussianity when a bubble is nucleated by quantum tunneling of scalar field
- Non-linear interactions with a bubble during and after its nucleation generate non-Gaussianity
- 3-point function of test scalar field on instanton background was calculated in a toy model using in-in formalism through imaginary time
- Calculated non-Gaussianity has radial dependence



Future works

- Calculation of observable in realistic model
 - including gravitational effect
 - inflationary background
 - open inflation
- Derivation of in-in formalism through imaginary time in Quantum Field Theory
 - Only Quantum Mech. case has been derived
- Special analysis in observation
 - analysis targeting inhomogeneous Non-Gaussianity has been left untouched
 - we may find a trace of bubble nucleation in inflationary era, and it might be an outcome of string landscape