

#### **Probing the nuclear wave function**

Removing nucleon(s) from occupied orbital → *Cross sections (probability)* depend on the single-particle occupancy & *overlap* of many-body wave functions

Full Knowledge of Correlations → Complete Understanding of Nuclear Properties



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微視的核反応理論による物理 Kyoto, Aug 1-3, 2011

### **Nucleon Correlations using Direct Reactions**

### **Spectroscopic Overlaps**



**Cross Section Measurements Coupled with Reaction and Structure theories** 

Reaction Model : Interface between Observables ↔ Nuclear Structure Knowledge



# Outline



**Systematic Framework** – Quantitative Knowledge of Correlations (structure & dynamics of many-body system)

**Tools: Transfer & Knockout Reactions** 



Spectroscopic Factor



Two-nucleon Overlap



Measurements

- What we have learned from Direct Reactions
- Next Steps for Complete Knowledge & towards Goals
- Needs of Theory Support

Diff. Sensitivity → Collective (longer) / Tensor / Short-range Correlations



### **Spectroscopic Factor (SF)**



**Cross Sections + Reaction Model** 

→ Spectroscopic Factors (expt) Quantify Occupancy → Correlation Effects How good the effective interaction in Shell Model can describe the correlations ?

 $\frac{SF_{exp}}{SF_{SM}} = 1$ 

SM description is accurate

How much ? What is the Isospin Dependence of nucleon correlations?



Some correlations missing in the interactions ?



(e,e'p) – Stable nuclei (near closed shell)

- <u>Constant</u>~30-40% of SF reduction compared to theory
- Correlations missing in shell-model interactions

L. Lapikas, Nucl. Phys. A553, 297c (1993)

How about Transfer Reactions ?

Transfer Reactions -- long history ( >50 years) → abundant data, but Problems in SF(expt) !

### **Experimental SF from Transfer Reactions**



### ADWA (consistent set)

✓ Johnson-Soper (JS) Adiabatic Approximation takes care of d-break-up effects

✓ Use global p and n optical potential with standardized parameters (CH89)

✓ Include finite range & nonlocality corrections

✓ *n*-potential : Woods-Saxon shape  $r_o$ =1.25 &  $a_o$ =0.65 fm; depth adjusted to reproduce experimental binding energy

TWOFNR, M. Igarashi et al.,

X.D. Liu et al., Phys Rev. C 69 (2004) 064313 J. Lee et al., Phys. Rev. C75 (2007) 064320



### **Survey of Spectroscopic Factor (Transfer Reactions)**



Extend to 88 nuclei (ground-state) : Found 225 relevant papers Re-analyzed (unified model) > 430 data sets → Extracted 88 SF(expt) Benchmark → 20 % agreement to theory

**Extend Survey to excited states :** 

Re-analyzed >2,000 data (>300 papers)

 $\rightarrow$  Extracted 565 SF(expt)

$$SF_{exp} / SF_{theory} \approx 1$$

Do we understand all the correlations ?

M.B. Tsang, J. Lee et al., Phys. Rev. Lett 95, 222501 (2005)
M.B. Tsang, J. Lee et al., Phys. Rev. Lett 102, 062501 (2009)
J. Lee, M. B. Tsang et al., Phys. Rev. C75, 064320 (2007)
J. Lee, M. B. Tsang et al., Phys. Rev. C79, 054611 (2009)



### **Suppression of SFs in Transfer Reactions**





Constant ~30% reduction in SFs

J. Lee et al., Phys. Rev. C 73, 044608 (2006)

CH89 + ro=1.25 fm with minimum assumption → consistent SF(expt) with Shell Model

Microscopic Input in Reaction Model

→ JLM potential & Hartree-Fock (SK20)

 $r_o=1.25 \text{ fm} \rightarrow HF \text{ rms radius}$ 

Global CH89  $\rightarrow$  JLM + HF densities



• Transfer reactions do not yield <u>absolute</u> SF; Systematic approach  $\rightarrow$  <u>relative</u> SF can be obtained <u>reliably</u> over a wide range of nuclei

• Nuclear structure purpose  $\rightarrow$  Relative normalized SFs

### **Isospin Dependence of Nucleon Correlations**





### Nucleon Knockout with Fast Beams on <sup>9</sup>Be / <sup>12</sup>C Target



High incident energy  $\rightarrow$  Reaction only affects a nucleon at surface

#### **Reaction Theory: Eikonal & Sudden Approximations**

J. Tostevin et al., J. Phys. G, Part. Phys. 25, 735 (1999)

✓ Large reaction cross sections (*few mb*)
✓ Thick reaction target
→ Powerful technique with high luminosity

**One-nucleon knockout -- away from stability** 

- Rs strongly depends on separation energy
- More correlation effect strongly bound valence nucleon

A. Gade et al., Phys. Rev. C 77, 044306 (2008) and reference therein



### **Isospin Dependence of Nucleon Correlations**



**Q: Isospin Dependence ?** 

#### Knockout reactions: Yes & Strong

A. Gade et al., Phys. Rev. C 77, 044306 (2008) & reference therein

**Transfer reactions: Weak** 

p(<sup>34,36,46</sup>Ar,d) at 33 MeV/A

S NSCL

J. Lee et al., Phys. Rev. Lett 104, 112701 (2010)

Systematic difference between two probes !

*Incompatibility → Incomplete understanding in underlying reaction mechanism* 

<u>Transfer Reaction</u> ✓ Future NSCL 09084: <sup>34,46</sup>Ar(p,d) at 70 MeV/A - same energy as knockout reactions for direct comparison

**Knockout Reaction ?** 

### **Is Strong Dependence Theoretically Explaned ?**



#### **Knockout reactions: Strong Dependence**

<u>Applicability of Modal</u> using Eikonal & Sudden approximations (core-inert) to existing knockout reaction data ?

#### **Dispersive Optical Model (DOM)** (elastic-scattering & bound-level data for <sup>40-49</sup>Ca)

R.J. Charity et al., Phys. Rev. C 76, 044314 (2007)

#### **Self-consistent Green's Functions + FRPA**

C. Barbieri & W. H. Dickhoff, arXiv:0901.1920v1



### **Knockout Reaction Models**



✓ Measuring core-excitation channels → justify over-prediction due to inert-core assumption

#### <u>3. (p,pN) knockout mechanism ?</u>

Reduction Factor (Rs)

- "Proton" target structure-less probe
- simpler reaction mechanism
- sensitive to larger part of wave function
- $\checkmark$  Comparing physics from diff. reaction mechanisms



1	. Invar	iant with	h beam	energy l	<u>?</u>			
S	Sudden Approx - 70MeV/A high enough ?							
✓ ]	Data at e	energies	of 200-	300 Me	V/A ne	eded		
2	2. Inert-	<u>core ? (1</u>	<u>reaction</u>	n mecha	nism)			
	one	-nucleon ren	noval	non eiko	nal			
	P (a)	(b)	(C)	(d)	2 (e)			
Direct KO Multiple scattering/ Core excitation Evaporation								
	Intr	anuclea	r Casca	ade Mo	del ( <i>IN</i>	<b>(C)</b>		

(with nuclear-structure input)

Proj.		ℓj	$C^2S$	σ <sub>exp</sub> (mb)	$\sigma_{ m casc}$	$\sigma_{\rm evap}$ (mb)	σ	σ <sub>eik</sub> (mb)	δ
$^{14}O$	-n	$p_{3/2}$	3.7	$13.4 \pm 1.4$	11.6	4.2	15.8	50	0.3
	-p	$p_{1/2}$	1.8	$67 \pm 6$	22.5	31.4	53.9	41.2	1.3
<sup>24</sup> Si	-n	$d_{5/2}$	1.7	$9.8 \pm 1.0$	9.7	2.6	12.3	23.3	0.5
	-p	$d_{5/2}$	3.4	$67.3\pm3.5$	24.8	19.7	44.5	65.5	0.7
$^{24}O$	-n	s <sub>1/2</sub>	1.8	$63 \pm 7$	34.3	4.2	38.5	51.2	0.8
<sup>28</sup> S	-n	$d_{5/2}$	3.1	$11.9\pm1.2$	12.6	3.2	15.8	33.2	0.5
<sup>32</sup> Ar	-n	<i>d</i> <sub>5/2</sub>	4.1	$10.4 \pm 1.3$	11.2	7.1	18.3	34.6	0.5

C. Louchart et al., Phys. Rev. C 83, 011601 (R) (2011)



# **Needs of Reaction Theory Support**

### Single-particle Overlap (SF)



#### **Transfer Reactions:**

- ✓ DWBA + adiabatic approach
- Assess uncertainties in reaction models
- Check reliability for high-energy transfer
- Extend optical model potential to exotic nuclei



#### <sup>9</sup>Be or <sup>12</sup>C-induced Knockout Reactions:

- ✓ Surrey-Reaction Model (J.A. Tostevin (Surrey))
- ✓ Intra-Nuclear Cascade Model (F. Flavigny (CEA Saclay))
- Another Reaction model (K. Minomo, M. Yahiro (Kyushu Univ.))
- Check energy dependence
- Include core-breaking effects for deeply-bound nucleon removal

#### **Proton-induced** (*p*,*pN*) Knockout Reactions:

- ✓ CDCC calculations (T. Matsumoto (Hokkaido Univ.))
- ✓ DWIA calculations (S. Kawase (CNS) code: THREEDEE)

#### Model $\rightarrow$ carbon-induced & proton-induced reaction on the same footing

• Future work (K. Minomo (Kyushu Univ.))

### **Two-nucleon Overlap**

### **Two-like nucleon Transfer Reaction**



#### Similarity between pairing field and 2-body transfer operator

Two-nucleon transfer reactions like (t,p) or  $(p,t) \rightarrow$  specific tool to probe T=1 pair correlations

Spectra from (p,t) reactions

S.J. Freeman et al. PRC 75 051301(R) (2007)

Ground-state composed of BCS pairs, twonucleon transfer cross sections enhanced

R.A. Broglia et al., Adv. Nucl. Phys. 6, 287 (1973)

<sup>76</sup>Ge & <sup>76,78</sup>Se(p,t) strength: predominately to the ground states → simple BCS paired states

How to get more quantitative + systematic knowledge of *nn-pairing* ?



### nn-pairing in Sn Isotopes

Pair Transition density – Skyrme HFB + QRPA approach





### Advanced 2n Transfer Calculations

Calculation of *absolute (p,t)* cross sections:

- Proper pairing interaction
- Multistep (successive, simultaneous)



G. Potel, R.A.	Broglia et al.	, accepted by	Phys. Rev. Lett
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	$\sigma(\mu b)$					
	5.11 MeV	6.1 MeV	10.07 MeV	15.04 MeV		
total	$1.29 \times 10^{-17}$	$3.77 \times 10^{-8}$	39.02	750.2		
successive	$9.48 \times 10^{-20}$	$1.14 \times 10^{-8}$	44.44	863.8		
simultaneous	$1.18 \times 10^{-18}$	$8.07 \times 10^{-9}$	10.9	156.7		
non-orthogonal	$2.17 \times 10^{-17}$	$7.17 \times 10^{-8}$	22.68	233.5		
non-orth.+sim.	$1.31 \times 10^{-17}$	$3.34 \times 10^{-8}$	3.18	17.4		
pairing	$1.01 \times 10^{-19}$	$6.86  imes 10^{-10}$	0.97	14.04		





Q1: Best reaction energy for 2N-transfer expt. ? Energy region  $\rightarrow$  large cross sections & good control of reaction mechanism (calculation). Q2: Targets (*p*,<sup>6</sup>*Li*,<sup>18</sup>*O*) - mechanism described ?

Ans: from Reliable Reaction Calc.



### **Neutron-Proton Pair Correlations**



### **Neutron-Proton Transfer Reactions**

PRL 94, 162502 (2005) PHYSICAL REVIEW LETTERS

week ending 29 APRIL 2005

#### **Deuteron Transfer in** N = Z **Nuclei**

P. Van Isacker,<sup>1</sup> D. D. Warner,<sup>2</sup> and A. Frank<sup>3</sup>

 <sup>1</sup>Grand Accélérateur National d'Ions Lourds, B.P. 55027, F-14076 Caen Cedex 5, France
 <sup>2</sup>CCLRC Daresbury Laboratory, Daresbury, Warrington WA4 4AD, United Kingdom
 <sup>3</sup>Instituto de Ciencias Nucleares, UNAM, Apdo. Postal 70-543, 04510 México, D.F. Mexico (Received 14 September 2004; published 29 April 2005)

#### Interacting Boson Model (IBM-4)

TABLE I. Predicted deuteron-transfer intensities  $C_T^2$  between even-even (EE) and odd-odd (OO) N = Z nuclei in the SU(4) (b/a = 0) and  $U_T(3) \otimes U_S(3)$   $(|b/a| \gg 1)$  limits.

	Limit	Reaction	$C_{T=0}^{2}$	$C_{T=1}^{2}$
	b/a = 0	$EE \rightarrow OO_{T=0}$	$\frac{1}{2}(N_{\rm b}+6)$	0
		$EE \rightarrow OO_{T=1}$	0	$\frac{1}{2}(N_{\rm b}+6)$
		$OO_{T=0} \rightarrow EE$	$\frac{1}{2}(N_{\rm b}+1)$	0
		$OO_{T=1} \rightarrow EE$	0	$\frac{1}{2}(N_{\rm b}+1)$
	$b/a \ll -1$	$EE \rightarrow OO_{T=0}$	$N_{\rm b} + 3$	0
T=0	stronger	$EE \rightarrow OO_{T=1}$	0	3
- •		$OO_{T=0} \rightarrow EE$	$N_{\rm b} + 1$	0
	$b/a \gg +1$	$EE \rightarrow OO_{T=0}$	3	0
<b>T</b> 1		$EE \rightarrow OO_{T=1}$	0	$N_{\rm b} + 3$
<i>I=1</i>	stronger	$OO_{T=1} \rightarrow EE$	0	$N_{\rm b} + 1$

T=0 (T=1) pairing: enhanced transfer probabilities  $\theta^+ \rightarrow 1^+ (\theta^+ \rightarrow \theta^+)$  levels



Measure the np transfer cross section to T=1 and T=0 states Absolute  $\sigma(T=1)$  and  $\sigma(T=0)$  – character and strength of the correlations  $\sigma(T=1) / \sigma(T=0)$  – interplay of T=1 and T=0 pairing modes

### Framework of *np*-transfer for pairing



NISHINA C E N T E R

Systematic measurements spanning *sd*-shell nuclei → Consistency

<sup>24</sup>Mg(<sup>3</sup>He,p), <sup>32</sup>S(<sup>3</sup>He,p)

<sup>24</sup>Mg(p,<sup>3</sup>He), <sup>28</sup>Si(p,<sup>3</sup>He) & <sup>40</sup>Ca(p,<sup>3</sup>He)



Framework & Baseline -- studies of np pairing in heavier N=Z nuclei (RI Beams)

### *np*-Transfer Reactions – Collaborative Efforts





#### New Structure of *np*-pairing:

- M. Horoi (CMU): transfer amplitudes from SM / pair operators
- Y. Sun (SJTU): matrix elements from spherical/ projected SM
- M. Matsuo (Niigata): formulating *np*-pairing using QRPA
- J. Meng (PKU): including T=0 *np*-pairing based on MF
- S.G. Zhou (CAS): extending SLAP to include *np*-pairing

#### **Reaction Calculations + different structure models for** *np***-pairing**



### **Neutron-Proton Knockout Reactions**



Reaction  ${}^{12}C + {}^{12}C \rightarrow X + anything$ (inclusive cross sections)

Sensitivity → Longer-Range of Correlations

For <sup>12</sup>C, 4*p* & 4*n* on  $p_{3/2}$  shell →No correlation: factor of 2.67 (pair counting)

**Reaction Model** → **Underlying Physics** 

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V	cross sections.	- IM Kidd at al
Λ	250 MeV/nucleon	PRC 37, 2613 (1988)
<sup>6</sup> Li	26.35±2.1	, ( ,
<sup>7</sup> Li	> 17.19±1.3	
<sup>8</sup> Li	$> 1.33 \pm 0.34$	
<sup>7</sup> Be	22.64±1.49	2
<sup>9</sup> Be	10.44±0.85	<i>-2p</i>
<sup>10</sup> Be	5.88±9.70	
<sup>11</sup> Be	$0.36 \pm 0.26$	-
<sup>8</sup> <b>B</b>	< 3.21±0.59	- <i>-nn</i>
<sup>10</sup> <b>B</b>	47.50±2.42	
<sup>11</sup> <b>B</b>	65.61±2.55	- <i>factor of 8 !</i>
${}^{12}\mathbf{B}$	<0.49±0.67	
<sup>10</sup> C	5.33±0.81	<b>)</b>
''C	55.97±4.06	-2n

### **Two-Nucleon Knockout Model**



#### **Theoretical Cross sections:**

Reaction: Eikonal & Sudden approximation Structure: 2N Overlap from Shell Model

J. Tostevin, B.A. Brown, PRC 74, 064604 (2006)

E.C. Simpson and J. Tostevin et al., PRL 102, 132502 (2009)

#### 2*n* or 2*p* knockout (T=1)



D. Bazin et al., Phys. Rev. Lett. 91, 012501 (2003)
K. Yoneda et al., Phys. Rev. C 74, 021303(R) (2006)
A. Gade et al., Phys. Rev. C 74, 021302(R) (2006)
P. Fallon et al., PRC 81, 041302(R) (2010)

**Factor of 2** over-prediction  $\rightarrow$  insufficient 2N correlations in Shell Models in <u>sd-pf shell</u>

Framework to quantitatively assess descriptions of 2n & 2p T=1 correlations

### <sup>12</sup>C – Interesting Physics found & hidden

#### Advanced Model *np* removal with T=0

#### First Calculations : np removal from <sup>12</sup>C

E.C. Simpson and J.A. Tostevin, PRC 83, 014605 (2011).

Residue	$J_f^{\pi}$	Т	$\sigma_{ m str}$	$\sigma_{\rm ds}$	$\sigma_{ m dif}$	$\sigma_{-2N}$
<sup>10</sup> C	0+	1	1.59	0.64	0.06	2.30
	2+	1	1.96	0.71	0.06	2.74
-2n					Sum	5.04
					Expt.	$4.11\pm0.22$
<sup>10</sup> Be	$0^{+}$	1	1.65	0.68	0.07	2.40
	2+	1	2.02	0.74	0.07	2.83
-2p	2+	1	0.88	0.32	0.03	1.23
ľ	0+	1	0.04	0.01	0.00	0.06
p-shell					Sum	6.52
I					Expt.	$5.81\pm0.29$
$^{10}B$	3+	0	5.11	2.00	0.20	7.30
	1+	0	2.47	1.01	0.10	3.58
	0+	1	1.62	0.66	0.07	2.35
-np	1+	0	1.81	0.69	0.07	2.57
	2+	0	0.63	0.24	0.02	0.89
	3 <sup>+a</sup>	0	1.14	0.43	0.04	1.62
	2+b	1	1.99	0.72	0.07	2.33
	1+a	0	0.30	0.10	0.01	0.41
	2 <sup>+a</sup>	0	0.75	0.28	0.03	1.05
					Sum	19.02
					Expt.	$35.10 \pm 3.40$

T=0 *np*-<u>spatial</u> correlations in the wave functions are insufficient



T=0 cross-sections – sensitive to effective interactions !

Data needed (exclusive measurement): - guide Theoretical Developments - gain Detailed knowledge

Wave Functions from different models: -Variation Monte Carlo w/ 3-body force (ab initio) I. Brida (ANL) - Tensor optimized shell model T. Myo (Osaka IT)

### *np* knockout $\rightarrow$ T=0 *np* pairing ?







# **Needs of Reaction Theory Support**

### **Two-Nucleon Overlap**



#### **Transfer Reactions:**

- No reliable models developed
- Study reliability for high-energy transfer
- Study reaction mechanism with light targets
- How to incorporate structure information

#### <sup>9</sup>Be or <sup>12</sup>C-induced *np*-Knockout Reactions:

- ✓ Surrey-Reaction Model (need data to verify)
- Develop new Reaction model (T=0 & T=1 pair formulism)
- Check energy dependence & Core-inert approximation

### Proton-induced (p,pd) Knockout Reactions:

- ✓ Reaction Model (QMD, Y. Watanabe (Kyushu Univ.))
- Different way to probe correlations
- How to extract structure information

#### Future: Alpha Correlations using Direct Reactions → Need reaction model !



### **Outlook – Direct Reactions**





E365: np-transfer Systematic Measurement spanning sd-shell nuclei



NSCL 09084: <sup>34,46</sup>Ar(p,d) at 70 A MeV

Future-proposed: Carbon-induced & proton-induced Knockout reactions of <sup>14</sup>O & <sup>36</sup>Ca at 250 A MeV

Future-proposed: First exclusive *np*-knockout of <sup>12</sup>C, <sup>28</sup>Si & <sup>40</sup>Ca

Future-proposed: <sup>14</sup>O beams on <sup>12</sup>C & CH<sub>2</sub> targets at 60 A MeV Proton- & carbon-induced knockout (**diffractive & stripping** part separated) Existing data (p,d) at 51 MeV @ GANIL  $\rightarrow$  also learn relative influence

Idea: <sup>14</sup>O at 60 A MeV on CH<sub>4</sub> (Active Target) + *n*-detection  $\rightarrow$  Corebreaking effects: <sup>12</sup>C  $\rightarrow$  <sup>4</sup>He + <sup>4</sup>He + <sup>3</sup>He + n (*support from reaction theorist !*)

#### **Intense Beams + Powerful Detectors + Computing → Dynamics of Nuclear Systems**

**Reliable reaction calculations:** 

➢ Need for experimental planning (setup, reaction energy) → most useful data
 ➢ Interpret data → mechanism behind nucleon correlations (underlying forces)

# Acknowledgement



Plans of Correlation Studies using 1N & 2N Knockout and Transfer Reactions



<u>Structure:</u> M. Matsuo (Niigata), Y. Utsuno (JAEA), I. Brida (ANL), T. Myo (Osaka IT), M. Horoi (CMU), J. Meng (Peking), Y. Sun (SJYU), S.G. Zhou (CAS)
(*In progress: 2N-overlap ab initio & TOSM, MF sensitive to T=0*)



**Experiment:** RIKEN group, RCNP group, A.O. Macchiavelli (BNL), A. Obertelli (CEA Saclay), R. Shane (MSU)

