

Pairing in dilute matter and in exotic nuclei

Q0. Do we have **good ab initio description of Δ** in typical systems?

Dilute uniform matter, stable nuclei

BCS-BEC crossover, small Cooper pair

Di-neutron correlation in n-rich nuclei

Q1. **In which situations** does the di-neutron correlation become prominent ?

Halo, skin, light /heavy, separation energy

Q2. What are **theoretical measures** of the di-neutron correlation ?

Coherence length? Short distance prob.?

Q3. **Relation** to the BCS-BEC in dilute matter?

Q4. What are **experimental observables** of the di-neutron correlation?

Exotic pairing

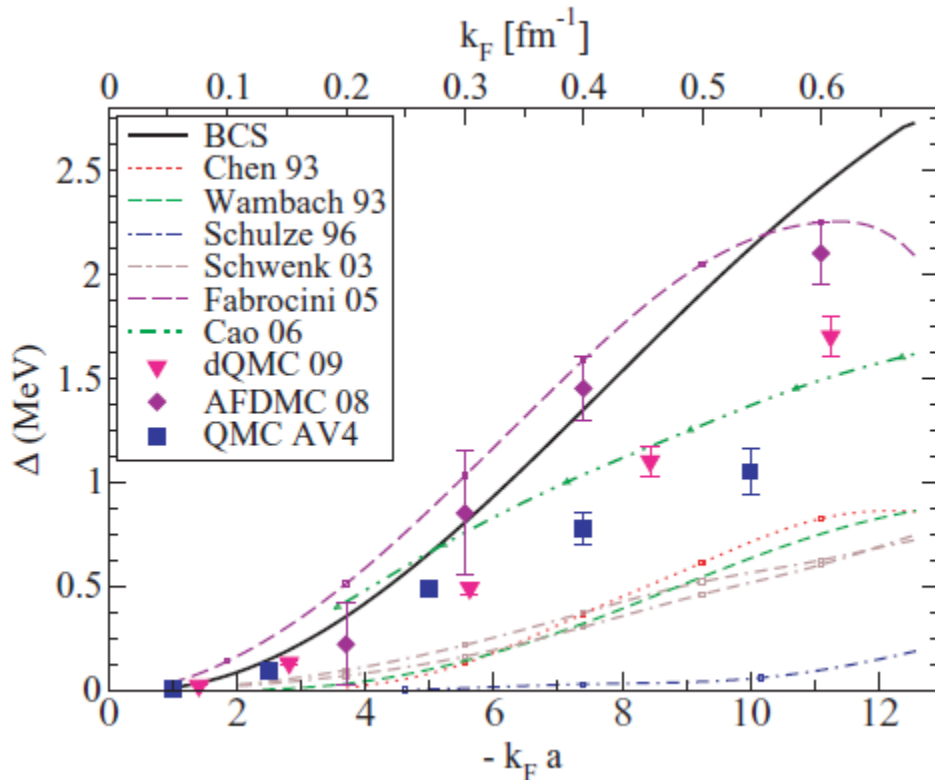
Q5. T=0 np-pairing ?

Q6. Its relation to quarteting & clusterization ?

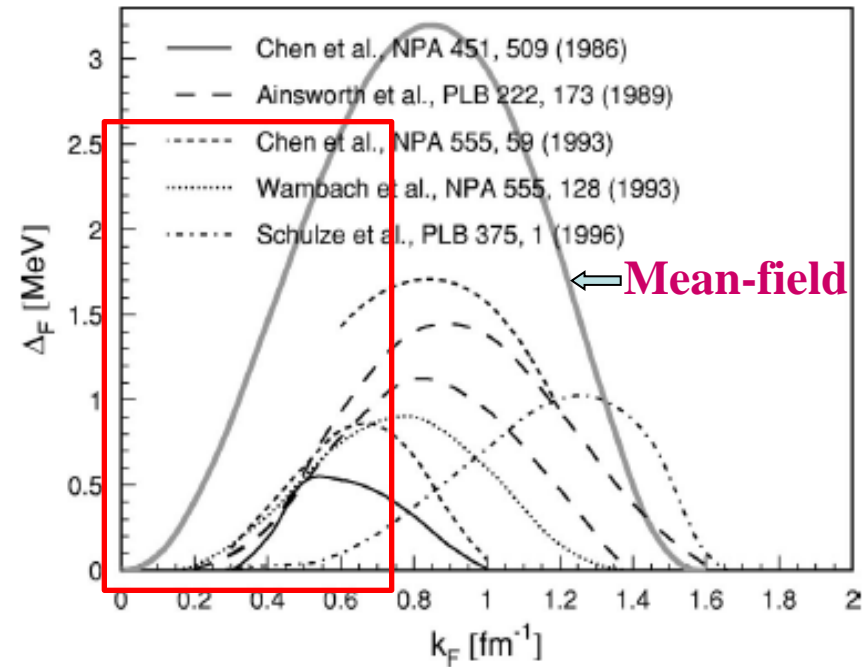
Q0. Do we have good ab initio description of Δ in simple systems?

pairing gap in dilute neutron matter

$\Delta = (1 \sim 0.5) \Delta_{\text{mean-field}}$ in recent calculations



Gezerlis & Carlson, PRC81 (2010)



Lombardo & Schulze 2001

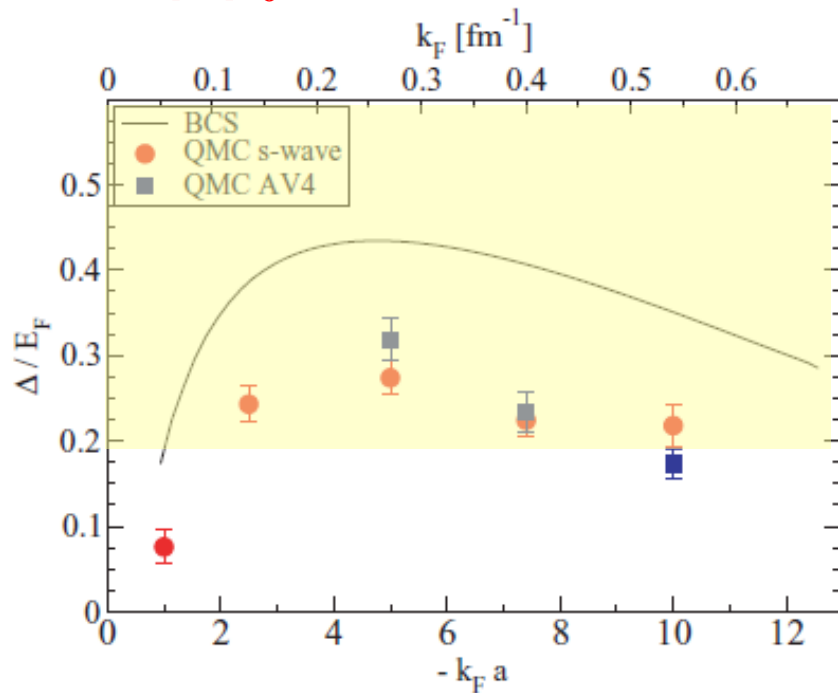
Strong coupling pairing in dilute matter & BCS-BEC crossover

Large scattering length $a = -18\text{fm}$ for nn-attraction

“Large” pair gap vs. Fermi energy $\Delta/e_F > 0.2$ at low-densities

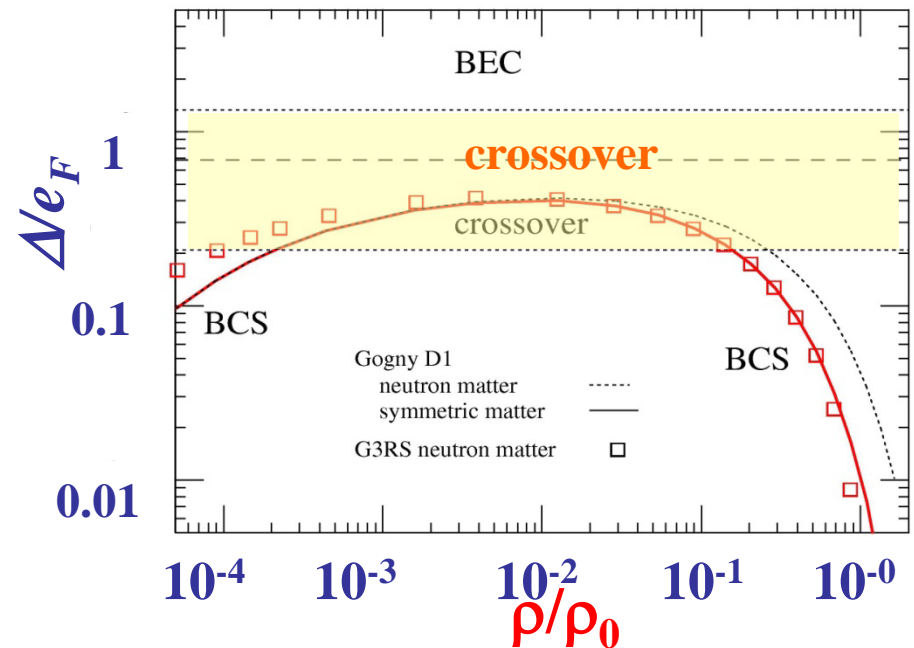
Monte-Carlo calculation

$$\rho/\rho_0 = 10^{-3} \sim 0.5 \times 10^{-1}$$



Mean-field calculation (BCS approx.)

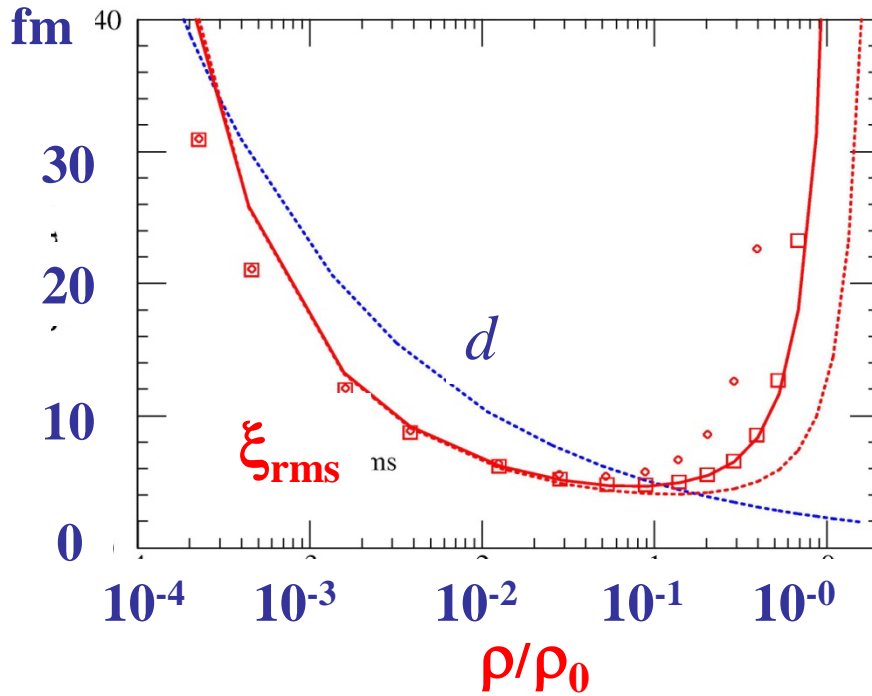
$$\rho/\rho_0 = 10^{-4} \sim 2 \times 10^{-1}$$



Q3. How can we relate the di-neutron correlation to the BCS-BEC in dilute matter?
 How do we learn the pairing in dilute matter

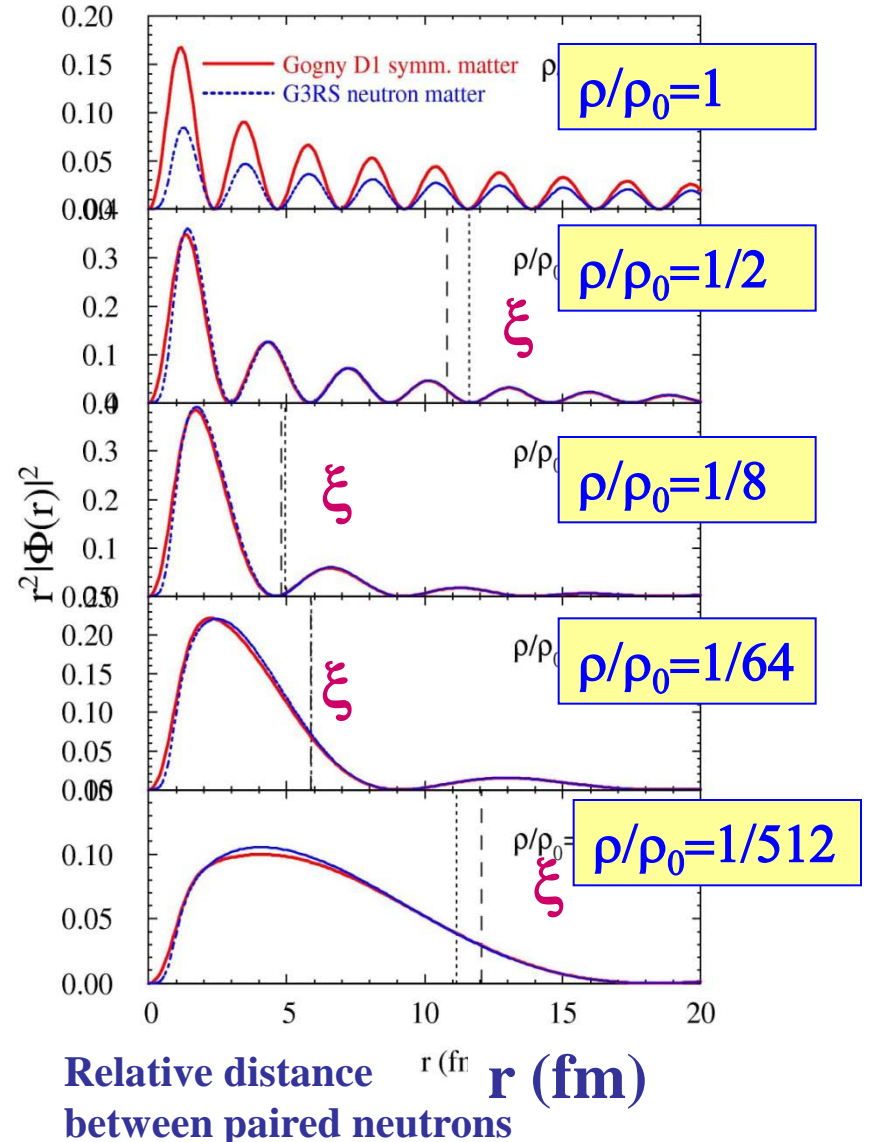
BCS calculation using A bare force (G3RS)
 Gogny force (D1)

Neutron pairing gap



Pair wave function has large amplitude at short relative distances $r \sim 2-3$ fm

Cooper pair wave function



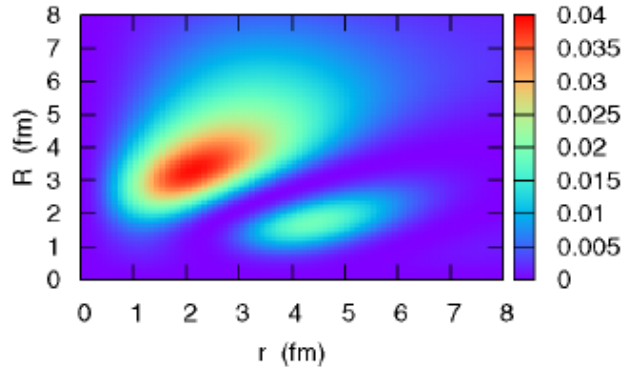
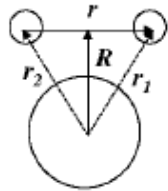
MM, PRC73,044309(2006)

Margueron et al, PRC77,054309(2008)

Q1. In which situations does the di-neutron correlation become prominent ?

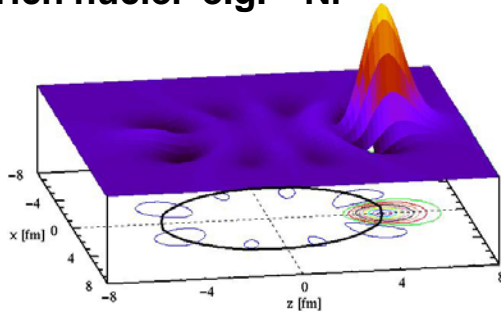
Halo, skin, light /heavy, separation energy

1. 2n-halo nuclei e.g. ^{11}Li G.F.Bertsch, H.Esbensen, Ann. Phys. 209(1991) 327



Hagino, Sagawa, Carbonell,
Schuck, PRL99, 022506(2007)

2. Heavy n-rich nuclei e.g. ^{84}Ni

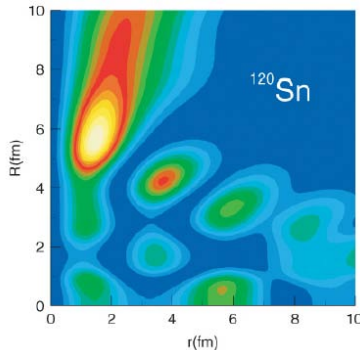


Matsuo, Mizuyama,
Serizawa
PRC71,064326(2005)

4. Slab, Semi-infinite matter

Kanada-Enyo, et al,
PRC79,054305(2009)
Pankratov, et al. PRC79,
024309 (2009)

3. Heavy stable nuclei



e.g. ^{18}O , ^{210}Pb , (alpha in ^{212}Pb)

Ibarra et al. NPA288, 397 (1977)
Janouch & Liotta PRC27,896 (1983)

e.g. ^{120}Sn

etc

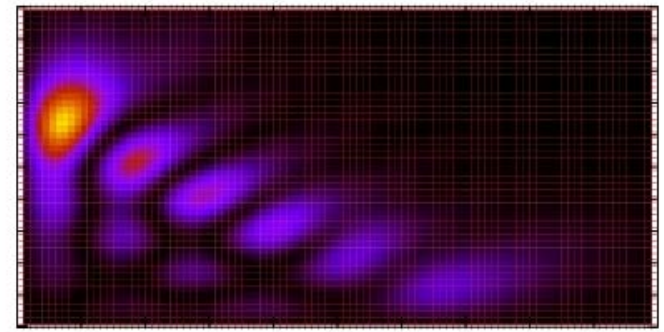
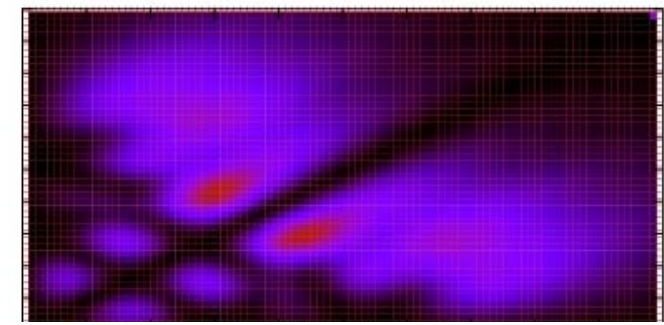
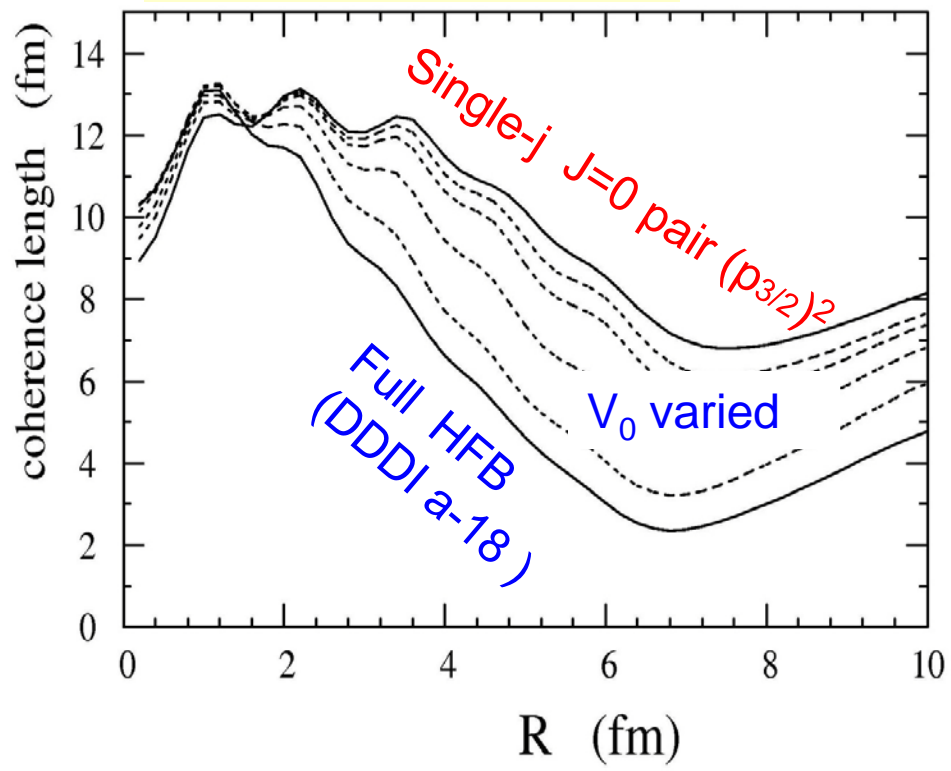
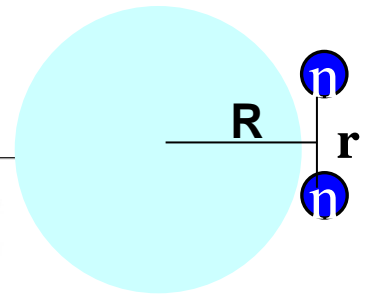
Pillet, Sandulescu, Schuck, PRC76,
024310 (2007)

Q2. What are (theoretical) measures of the di-neutron correlation ?

Rms radius of 'Cooper pair' as a function of R

¹⁴²Sn

$$\xi = \langle r^2 \rangle = \frac{\int r^2 P_c(R, r) dr}{\int P_c(R, r) dr}$$



It is influenced by geometrical effect of finite volume

[1] Pillet, Sandulescu, Schuck, Berger, PRC81 (2010)

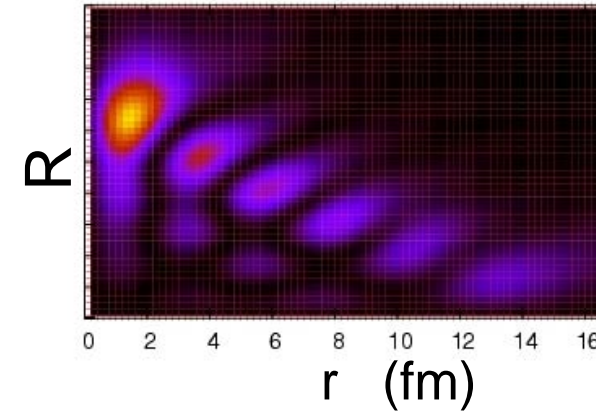
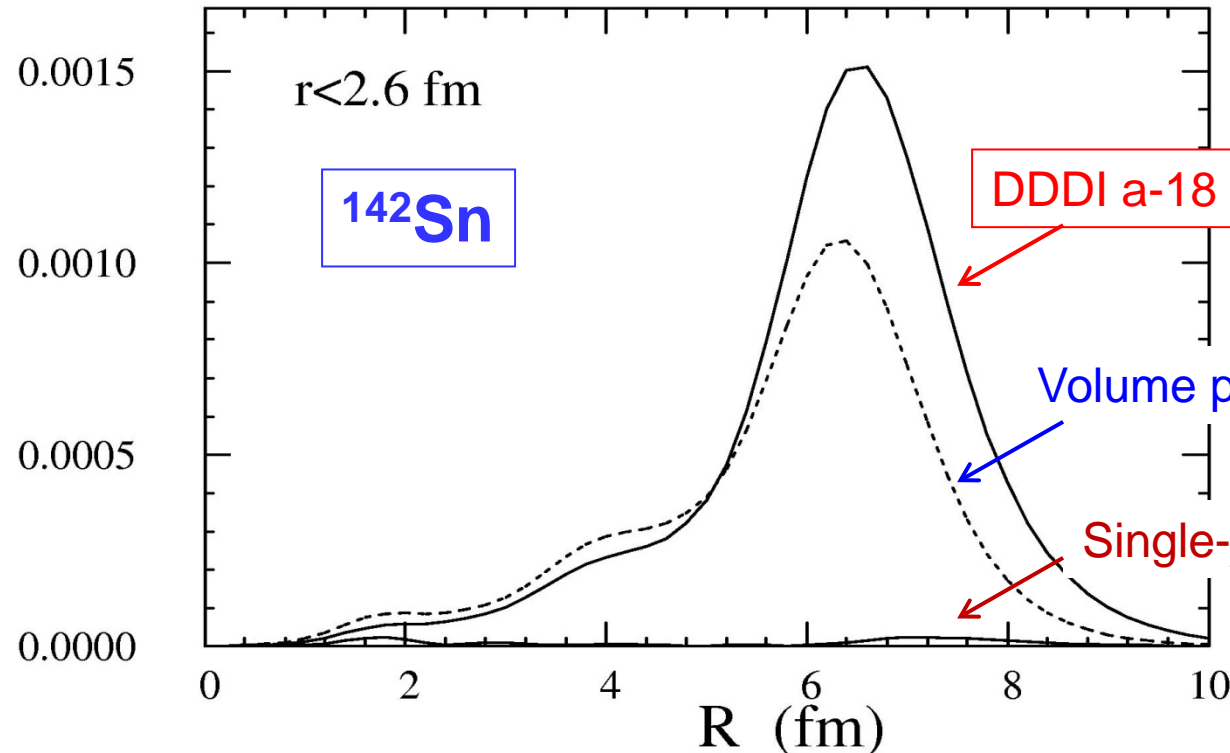
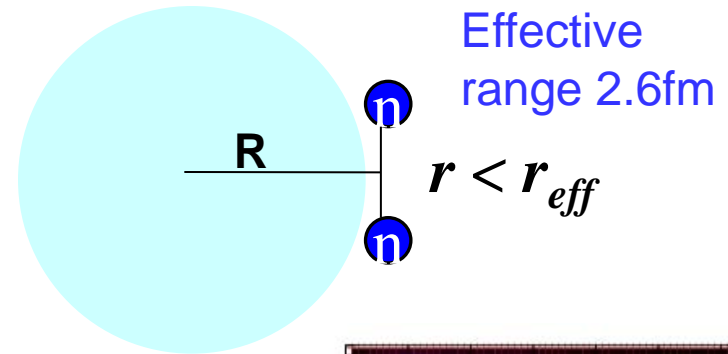
And also by the surface spatial correlation (especially in halo).

[2] Hagino et al J Phys.G37 (2010)

Pair contact probability $r < 2.6$ fm

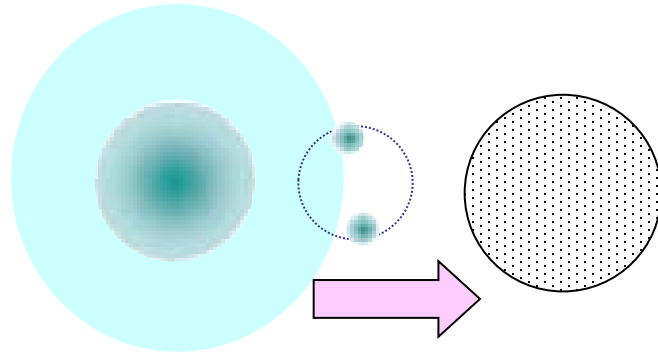
Probability of pair at short relative distances within the interaction range

$$p(R) = \int_0^{r_{eff}} P_c(R, r) dr$$



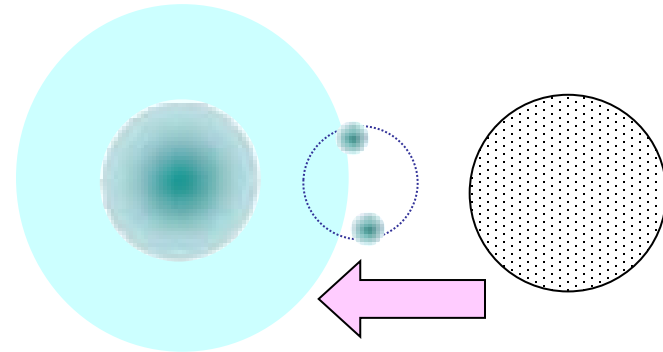
Q4. What are (experimental) observables of the di-neutron correlation?

Pair transfers in neutron-rich nuclei



Pair removal

$^{132}\text{Sn}\sim^{140}\text{Sn}$ precursory 0^+_2
 $^{142}\text{Sn}\sim$ enhanced 0^+_2 transfer



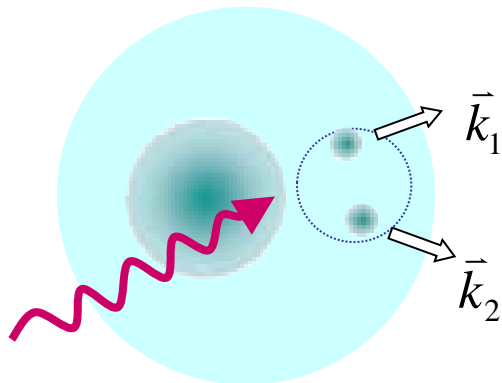
Pair addition

Shimoyama's presentation on Oct.24

$2n$ break-up through soft dipole excitation in nuclei near n -drip line

^{11}Li , ^6He , etc.

$2n$ correlation ??



Hagino et al., PRC80, 031301 (2009)
 Kikuchi et al., PRC81, 044308 (2010)

