Di-neutron correlation in Borromean nuclei



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¹¹Li, ⁶He

What is the spatial structure of valence neutrons? Compact? Or Extended?

- 1. Introduction: Di-neutron correlation
- 2. Three-body model for ¹¹Li and ⁶He
 - Spatial structure (geometry) of valence neutrons
 - El strength
- 3. 1-Dimensional 3-body model
- 4. Summary

Borromean nuclei and Di-neutron correlation

Borromean nuclei: unique three-body systems



FIG. 1. Spatial correlation density plot for the 0^+ ground state of ⁶He. Two components—di-neutron and cigarlike—are shown schematically.

Yu.Ts. Oganessian, V.I. Zagrebaev, and J.S. Vaagen, *PRL82('99)4996* M.V. Zhukov et al., *Phys. Rep. 231('93)151*



G.F. Bertsch, H. Esbensen, Ann. of Phys., 209('91)327

Borromean nuclei and Di-neutron correlation



G.F. Bertsch, R.A. Broglia, and C. Riedel, NPA91('67)123

F. Catara, A. Insolia, E. Maglione, and A. Vitturi, PRC29('84)1091

How to probe the strong dineutron correlation?

•Coulomb excitations?



T. Aumann et al., PRC59('99)1252

6.0

* (indirect) evidence for dineutron correlation

dineutron correlation in the ground state?

Experimental evidence: T. Nakamura et al., PRL96('06)252502

Recent Coulomb dissociation data of ¹¹Li



renewed interests in dineutron correlations in weakly bound nuclei

c.f. M. Matsuo et al., PRC71('05)064326 PRC73('06)044309



H. Esbensen, K. Hagino, P. Mueller, and H. Sagawa, PRC76('07)024302

•spatial structure of dineutron (cf. a large pair coherence length?)

•dineutron correlation in heavy nuclei?

•E1 excitations?

•Pair transfer?

What is the spatial structure of the valence neutrons?



n

To what extent is this picture correct?



Three-body model with density-dependent delta force



$$H = \frac{p_1^2}{2m} + \frac{p_2^2}{2m} + V_{nC}(r_1) + V_{nC}(r_2) + V_{nn} + \frac{(p_1 + p_2)^2}{2A_c m}$$

$$H = \frac{p_1^2}{2m} + \frac{p_2^2}{2m} + V_{nC}(r_1) + V_{nC}(r_2) + V_{nn} + \frac{(p_1 + p_2)^2}{2A_c m}$$



$$V_{nn}(r_1, r_2) = \delta(r_1 - r_2) \left(v_0 + \frac{v_{\rho}}{1 + \exp[(r_1 - R_{\rho})/a_{\rho}]} \right)$$

- \checkmark contact interaction
- \checkmark v₀: free n-n
- ✓ density dependent term: medium many-body effects

$$H = \frac{p_1^2}{2m} + \frac{p_2^2}{2m} + V_{nC}(r_1) + V_{nC}(r_2) + V_{nn} + \frac{(p_1 + p_2)^2}{2A_c m}$$

$$\Psi_{gs}(\mathbf{r},\mathbf{r}') = \mathcal{A} \sum_{nn'lj} \alpha_{nn'lj} \Psi_{nn'lj}^{(2)}(\mathbf{r},\mathbf{r}')$$



Two-particle density for the ground state of ¹¹Li and ⁶He



 \diamond Role of pairing correlation

configuration mixing of different parity states



2n-rms distance



P. Schuck, J. of Phys. G37('10)064040

2n-rms distance





Study of Deuteron-Cluster Deformation Using the Reaction ${}^{6}\text{Li}(d, tp){}^{4}\text{He}$

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PRL32('74)173

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cf. "di-proton" correlation

¹⁷Ne = ¹⁵O + p + p (
$$S_{2p}$$
 = 0.944 MeV)
v_{pp} = density-dep. contact interaction + Coulomb



$$\langle v_{pp}^{(nucl)} \rangle = -3.26 \text{ MeV}$$

 $\langle v_{pp}^{(Coul)} \rangle = 0.448 \text{ MeV} \longleftarrow \text{about 14\%}$
contribution

T. Oishi, K. Hagino, and H. Sagawa, PRC82('10)024315

cf. "di-proton" correlation

	¹⁷ Ne	¹⁷ Ne (No Coulomb)	¹⁶ C
$\langle V_{\rm pp}^{(N)} \rangle$ (MeV)	-3.26	-2.76	-3.88
$\langle V_{\rm pp}^{(C)} \rangle$ (MeV)	0.448	0	0
$P([s_{1/2}]^2)$ (%)	15.16	15.91	20.69
$P([d_{5/2}]^2)(\%)$	75.19	75.68	64.97
$P([d_{3/2}]^2)(\%)$	3.83	3.26	6.63
$\langle r_{\rm NN}^2 \rangle^{1/2} ~({\rm fm})$	4.688	4.749	4.579
$\langle r_{\rm C-2N}^2 \rangle^{1/2}$ (fm)	3.037	3.037	3.099
$\delta \langle r^2 \rangle^{1/2}~({\rm fm})$	1.267	1.273	1.306
$\langle \theta_{12} \rangle$ (deg)	76.64	76.03	74.35
	exact treatment	switch off the Coulomb, but renormalize the nuclear force	
	for Coulomb		

T. Oishi, K. Hagino, and H. Sagawa, PRC82('10)024315



T. Oishi, K. Hagino, and H. Sagawa, arXiv:1109.2994 [nucl-th] Phys. Rev. C, in press.







Dipole excitations

Response to the dipole field:

$$\begin{array}{c}
B_k(E1) = 3 \left| \left\langle \Psi_1^k | \hat{D}_0 | \Psi_{gs} \right\rangle \right|^2 \\
\text{excited states ground state} \\
\text{fnote) analytic expression for a single-particle potential model} \\
\psi_b(r) \sim h_l(ik_br), \quad \psi_c(r) \sim j_l(k_cr) \\
\begin{pmatrix} 0.25 \\ 0.2 \\ 0.2 \\ 0.2 \\ 0.15 \\ 0.05 \\$$

Dipole excitations



recoil term



K.Hagino and H. Sagawa, PRC76('07)047302



The relative motion $r = r_1 - r_2$ is not affected by the dipole operator.

Probing dineutron correlation with E1 excitation?

especially with energy (and angular) distribution(s)?

New 2n correlation experiment (Nakamura et al.)



T. Nakamura et al., unpublished



e, (MeV)

H. Esbensen and G.F. Bertsch, NPA542('92)310



K.H., H. Sagawa, T. Nakamura, S. Shimoura, PRC80('09)031301(R)





K.H., H. Sagawa, T. Nakamura, S. Shimoura, PRC80('09)031301(R)



K.H., H. Sagawa, T. Nakamura, S. Shimoura, PRC80('09)031301(R)



K.H., H. Sagawa, T. Nakamura, S. Shimoura, PRC80('09)031301(R)

Analysis with three-body model



How to probe the strong dineutron correlation?

•Coulomb excitations? \longrightarrow A problem: an external field is too weak



K.H., H. Sagawa, T. Nakamura, S. Shimoura, PRC80('09)031301(R)

How to probe the strong dineutron correlation?

•Coulomb excitations? •Nuclear breakup?



M. Assie et al., Eur. Phys. J. A42 ('09) 441

cf. 4-body CDCC for exclusive cross sections?

How to probe the strong dineutron correlation?

- Coulomb excitations?Nuclear breakup?
- •Pair transfer?



How to probe the strong dineutron correlation?

Coulomb excitations?Nuclear breakup?

•Pair transfer?

✓ Reaction mechanism?

- sequential vs simultaneous
- Q-value, angular momentum matchings
- ✓ Role of dineutron correlation (on the surface)?
- ✓Influence to other reaction processes (e.g., subbarrier fusion)?

have not yet been fully clarified

 \rightarrow to be discussed on the next Monday





Recent experiments for transfer reaction of neutron-rich nuclei



A. Chatterjee et al., PRL101('08)032701

I. Tanihata et al., PRL100('08)192502

It is timely to construct:

a new theory of pair transfer with dineutron correlation.

 \rightarrow need a deep understanding of reaction dynamics

a simple and intuitive schematic model

One-dimensional three-body model

Two interacting neutrons in a one-dimensional potential well:

$$H = -\frac{\hbar^2}{2m}\frac{d^2}{dx_1^2} + V(x_1) - \frac{\hbar^2}{2m}\frac{d^2}{dx_2^2} + V(x_2) + v_{nn}(x_1, x_2)$$

density-dependent contact interaction:

$$v_{nn}(x,x') = -g\left(1 - \frac{1}{1 + e^{(|x| - R)/a}}\right)\delta(x - x')$$



$$\Psi_{gs}(x_1, x_2) = \sum_{n \le n'} \alpha_{nn'} \Psi_{nn'}(x_1, x_2)$$

$$\Psi_{nn'}(x_1, x_2) \propto S[\phi_n(x_1)\phi_{n'}(x_2)] \times |S=0\rangle$$

•S = 0 state: symmetric for the spatial part of wf

Х

•*n*, *n*': the same parity

Similar one-dimensional model for two-electron systems

He atom $(^{4}\text{He} + e^{-} + e^{-})$

H⁻ atom $(p + e^{-} + e^{-})$



double ionization by intense laser fields



SAE: single active electron approximation NS: non-sequential

J.B. Watson et al., PRL78('97)1884

cf. TDH(F) for a one-dimensional system

B. Yoon and J.W. Negele, PRA16('77) 1451

PHYSICAL REVIEW A

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Time-dependent Hartree approximation for a one-dimensional system of bosons with attractive δ -function interactions*

B. Yoon and J. W. Negele[†]

Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139 (Received 29 November 1976)

The time-dependent Hartree approximation is compared with an exact solution for the scattering between two N-particle bound states in the case of a 1-dimensional system of bosons with attractive δ -function interactions. It is shown that to leading order in N, the approximation is exact, and arguments are presented relating this asymptotic agreement to the nonsaturation of the bound states.

$$H = -\frac{1}{2} \sum_{i=1}^{N} \frac{\partial^2}{\partial x_i^2} - g \sum_{i< j=1}^{N} \delta(x_i - x_j)$$



Ground state properties

two-particle density: $|\Psi_{gs}(x_1, x_2)|^2$





$$\Psi_{gs}(x_1, x_2) = \Psi_{ee}(x_1, x_2) + \Psi_{oo}(x_1, x_2)$$

$$\longrightarrow \rho_2(x_1, x_2) = |\Psi_{ee}(x_1, x_2)|^2 + |\Psi_{oo}(x_1, x_2)|^2$$

$$+ 2\Psi_{ee}(x_1, x_2)\Psi_{oo}(x_1, x_2)$$



x₁ (fm)

Nuclear Breakup Process



Time-dependent two-particle Schroedinger equation:

$$i\hbar \frac{\partial}{\partial t} \Psi(x_1, x_2, t) = [H + V_{\text{ext}}(x_1, x_2, t)] \Psi(x_1, x_2, t)$$
$$V_{\text{ext}}(x_1, x_2, t) = \sum_{i=1,2} V_c e^{-t^2/2\sigma_t^2} e^{-(x_i - x_0)^2/2\sigma_x^2}$$
$$V_c = 3 \text{ MeV}, \sigma_t = 2.1 \text{ hbar/MeV}, x_0 = 0$$

two-particle density at $t = t_{ini}$





"dineutron emission"

large (bc) component





≻Pairing: enhances the breakup

≻Correlated: (cc) process

≻Uncorrelated: (bc) process

 P_{cc} : 2 neutron breakup P_{bc} : 1 neutron breakup

Application to 2p radioactivity



T. Maruyama, T. Oishi, K.H., preliminary



'fort.11' u 1:2:3

t > 0





sequential 2p emission ($x_2 \sim 0$)

'fort.11' u 1:2:3

Three-body model with density-dependent contact interaction

180

160

140

120

100

80

60

40

20

2

 θ_{12} (deg)

Ground state of ¹¹Li and ⁶He

≻similar di-neutron correlation

Energy distribution of neutrons from the E1 excitations in ¹¹Li and ⁶He

continuum responses
 the shape of distributions: primarily determined
 by n-core dynamics rather than n-n
 energy distribution: very different between ¹¹Li and ⁶He
 s-wave virtual state in ¹¹Li

cf. similar dineutron correlations in the g.s. One dimensional model for 2n halo nuclei

≻simple, and schematic model. detailed studies of dynamics

