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# Low-lying continuum states of drip-line Oxygen isotopes

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## Motivation

### Emission from doorway-state

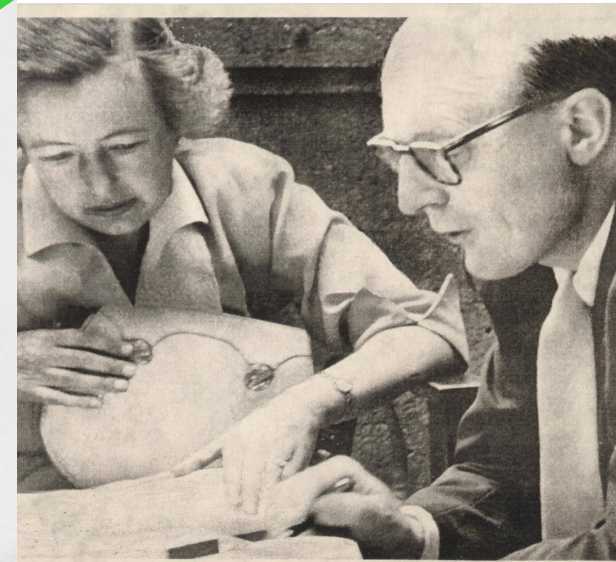
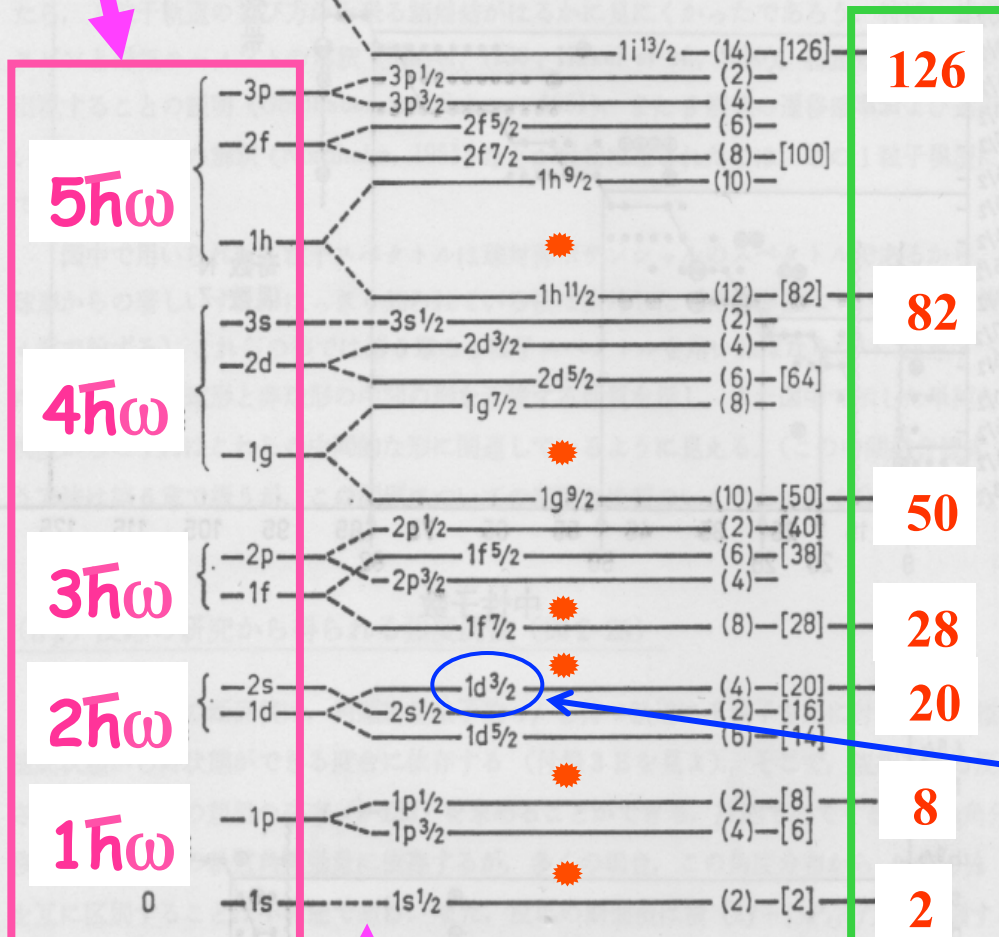
A bound state is shifted to continuum suddenly through a nuclear reaction

V.S.

### Emission from single-particle resonance

Eigenvalues of HO potential

Magic numbers  
Mayer and Jensen (1949)



Mayer & Jensen

$d_{3/2}$

図 2-23 1 粒子軌道の順序。図は G. Mayer and J. H. D. Jensen, *Elementary Theory of Nuclear Shell Structure*, 1955 年に出版された。

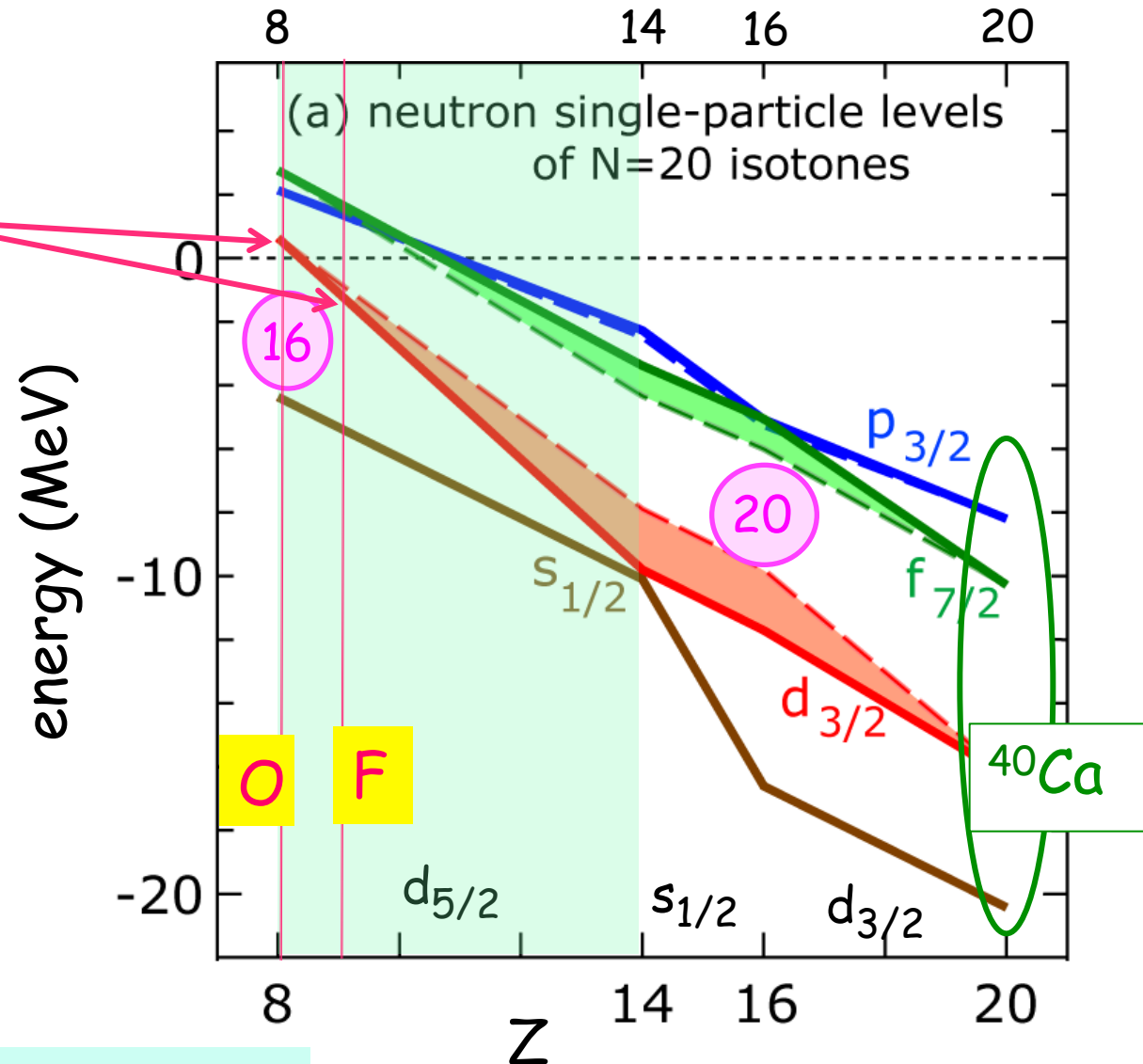
Spin-orbit splitting

# Neutron single-particle energies at $N=20$ for $Z=8\sim 20$

solid line : full (central + tensor)

dashed line : central only

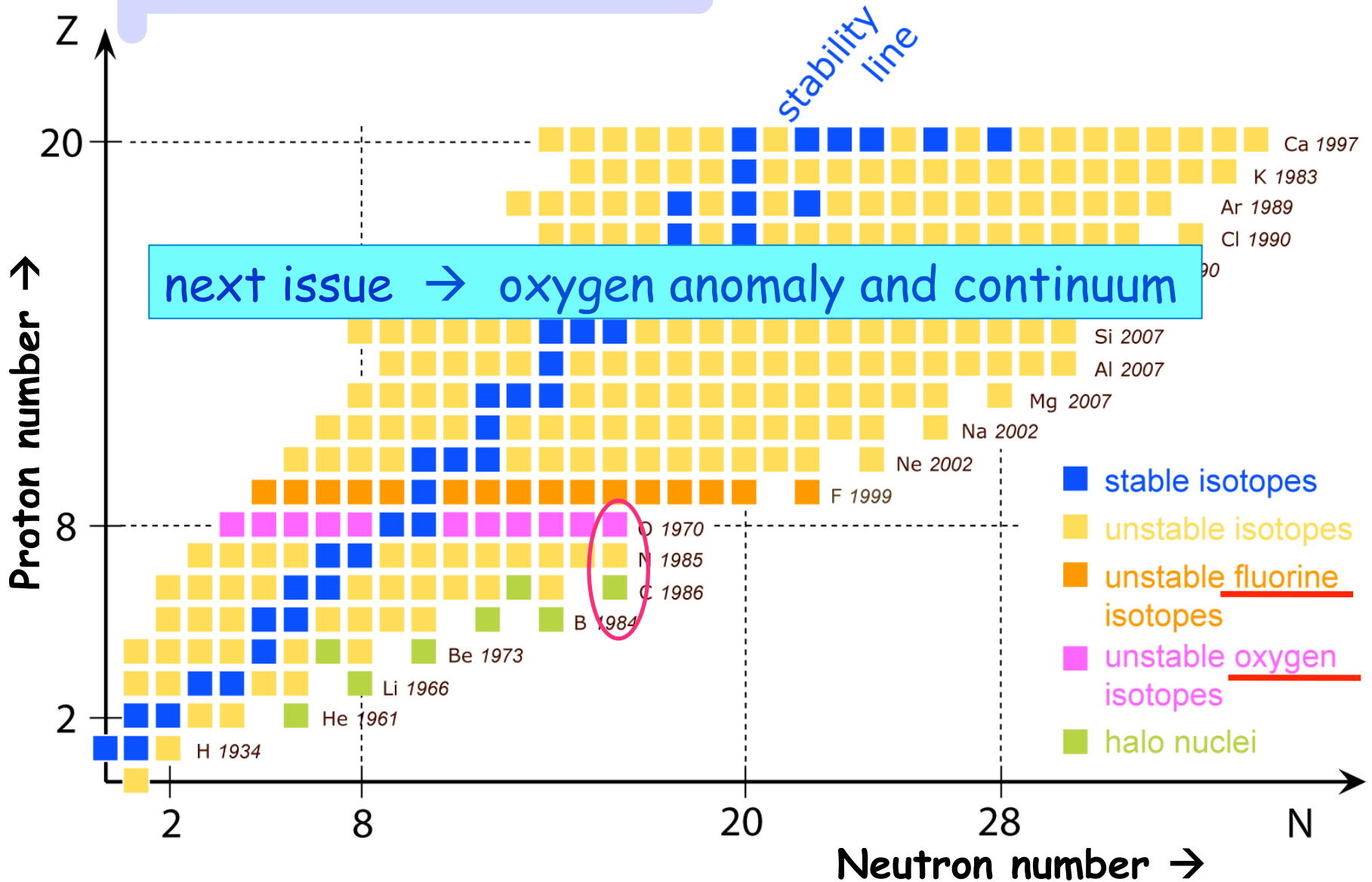
$d_{3/2}$   
bound in F  
unbound in O  
due to  
interplay  
between  
tensor and  
three-body  
forces



One of the Backgrounds

# Nuclear Chart - Left Lower Part -

Why is the drip line of Oxygen so near ?



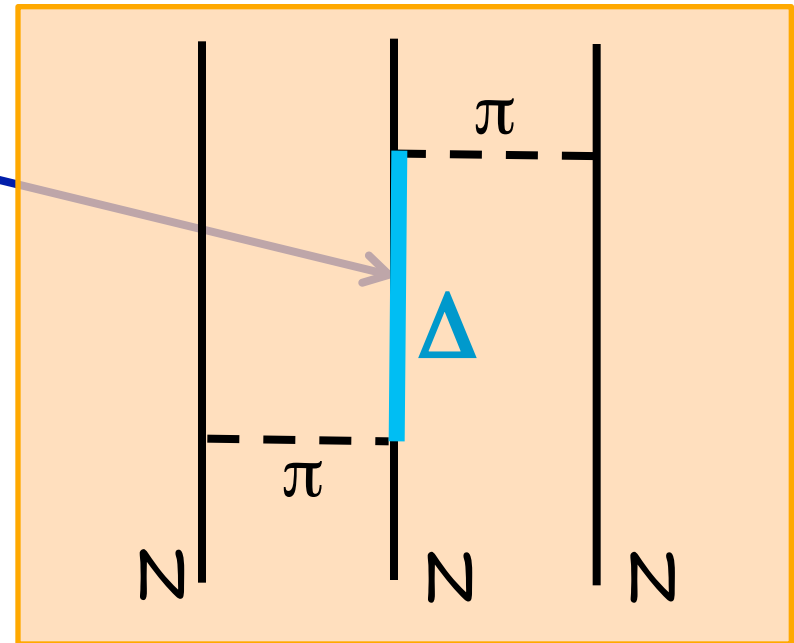
# The clue : Fujita-Miyazawa 3N mechanism ( $\Delta$ -hole excitation)

Progress of Theoretical Physics, Vol. 17, No. 3, March 1957

## Pion Theory of Three-Body Forces

Jun-ichi FUJITA and Hironari MIYAZAWA

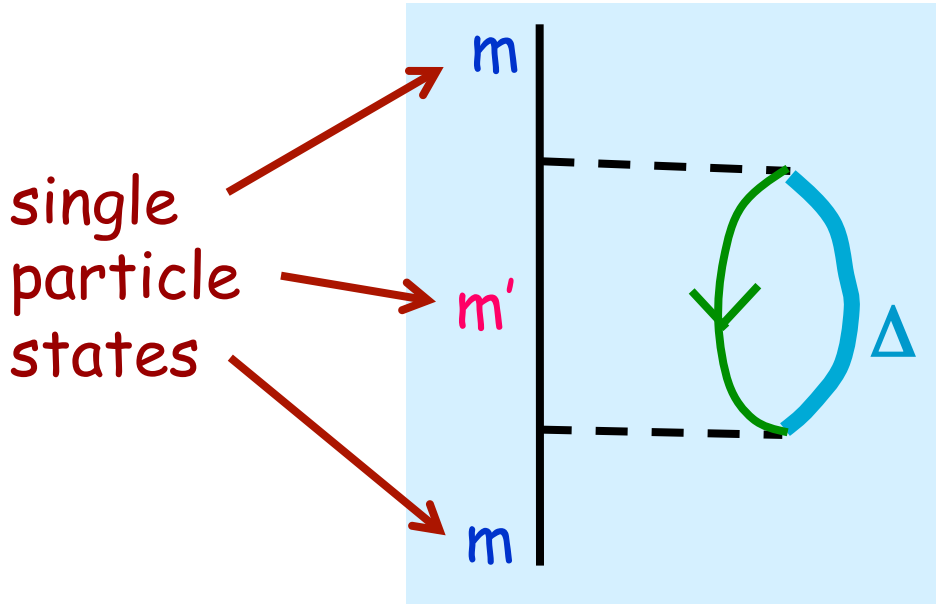
$\Delta$  particle  
 $m=1232$  MeV  
 $S=3/2, I=3/2$



Miyazawa, 2007



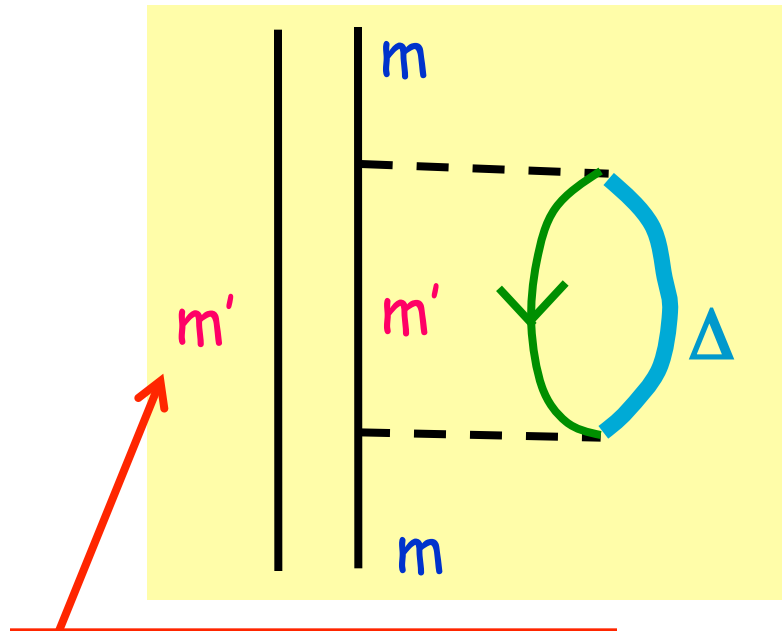
# Pauli blocking effect on the renormalization of single-particle energy



Renormalization of single particle energy due to

$\Delta$ -hole excitation

→ more binding (attractive)

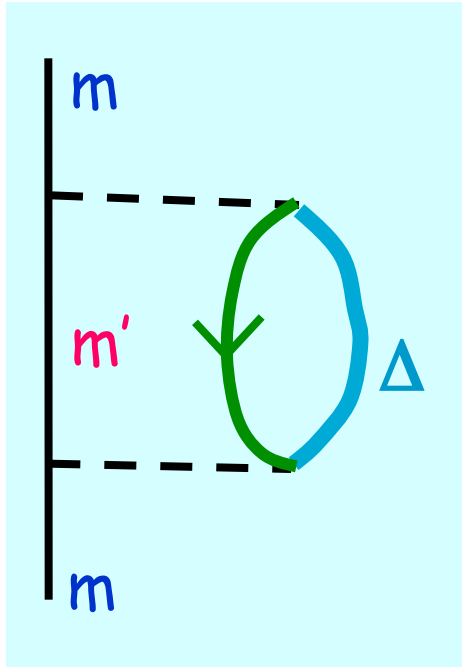


Another valence particle in state  $m'$

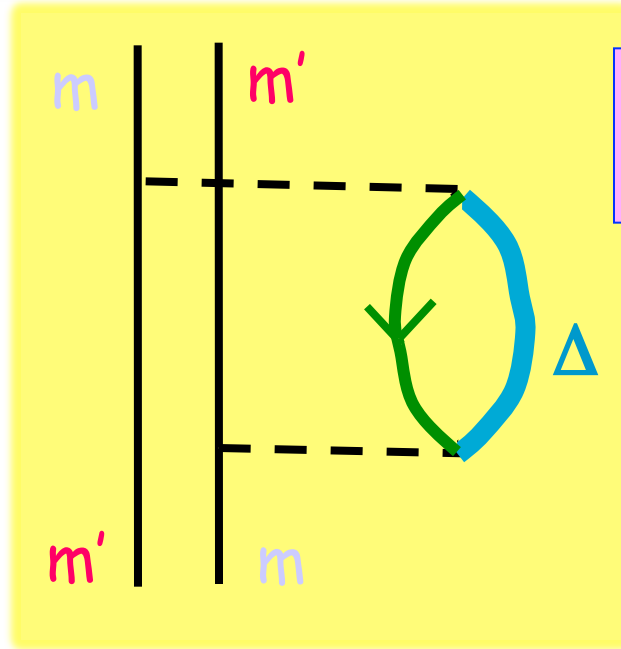
Pauli Forbidden  
→ *The effect is suppressed*



# Most important message with Fujita-Miyazawa 3NF



+



Pauli blocking

Effective monopole repulsive interaction

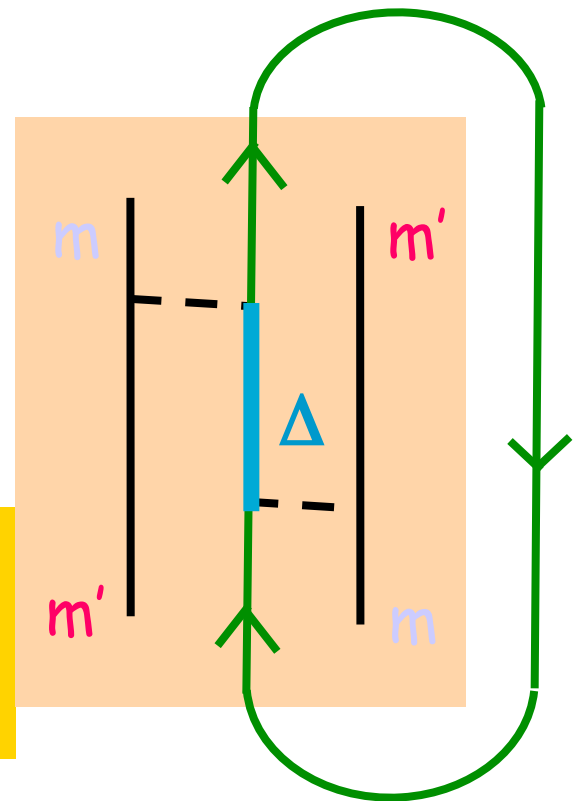


Renormalization of single particle energy

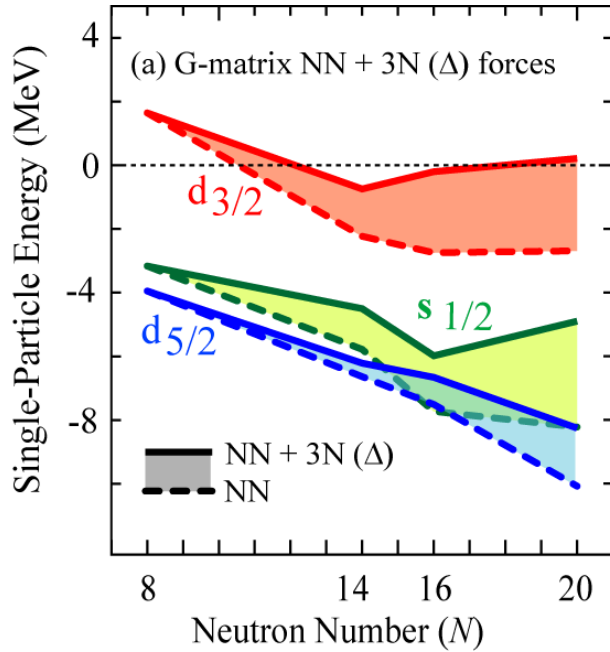
same



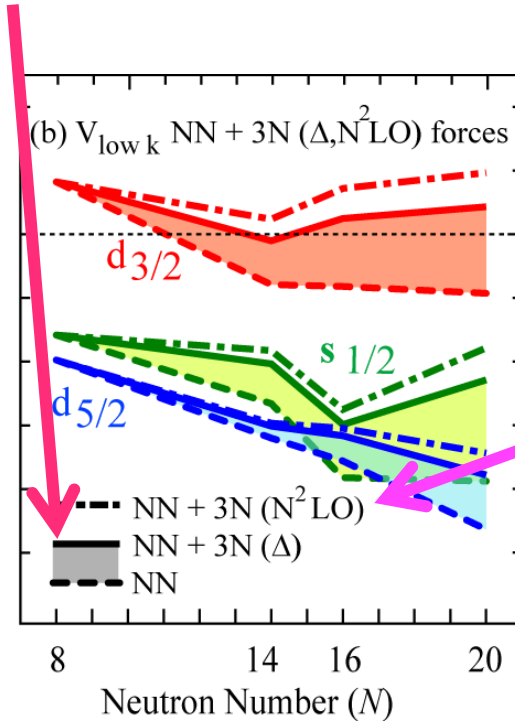
Monopole part of Fujita-Miyazawa 3-body force



(i)  $\Delta$ -hole excitation in a conventional way



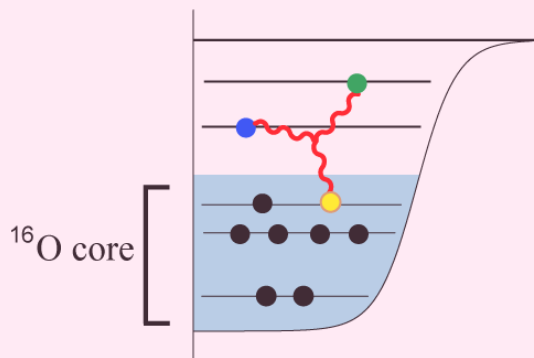
(ii) EFT with  $\Delta$



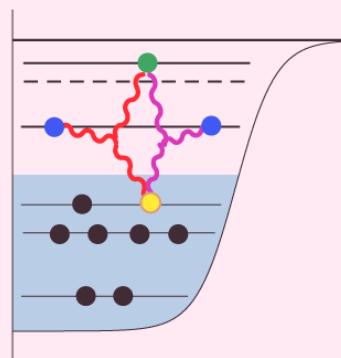
(iii) EFT incl. contact terms ( $N^2\text{LO}$ )

$\Delta$ -hole dominant role in determining oxygen drip line

(c) 3-body interaction

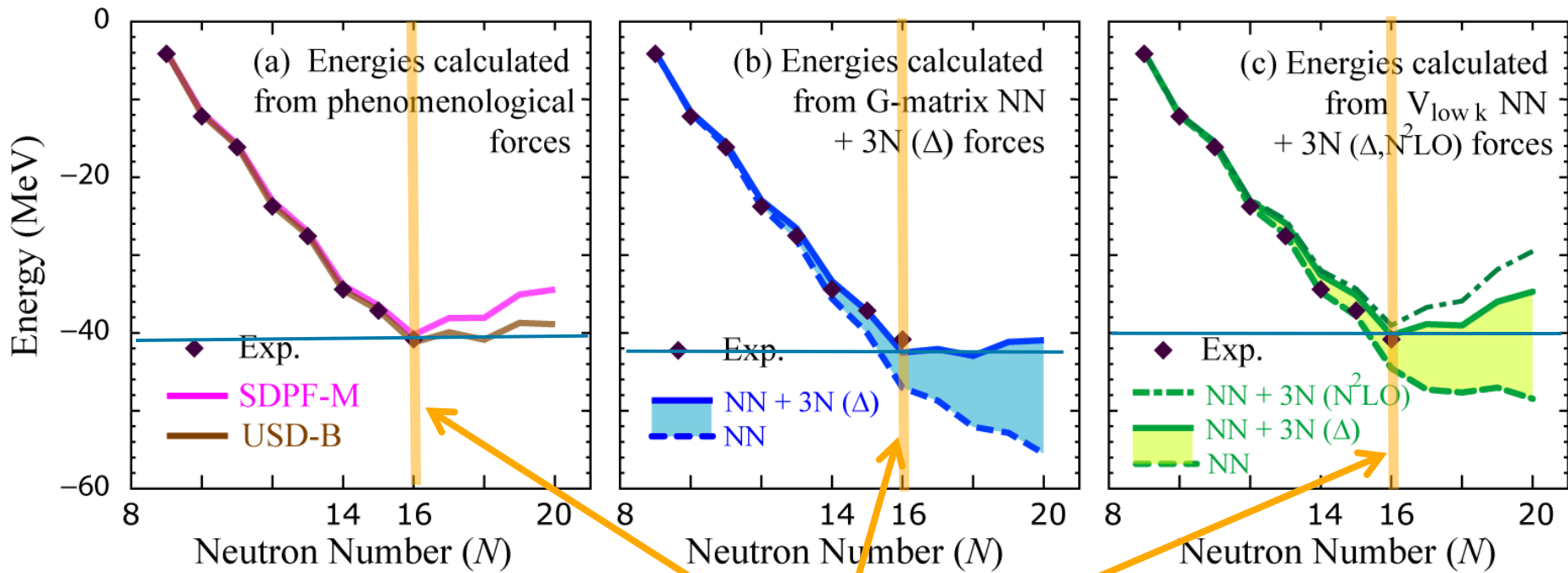
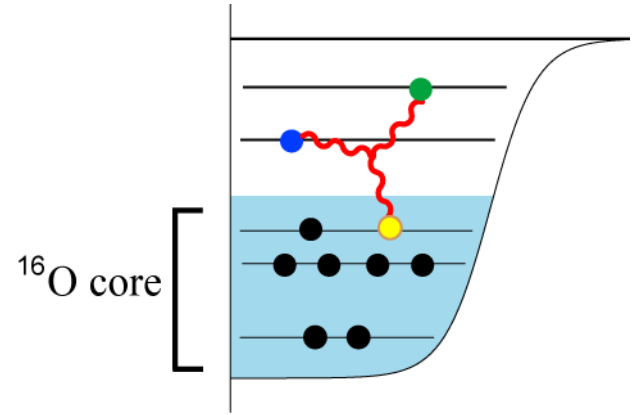


(d) 3-body interaction with one more neutron added to (c)



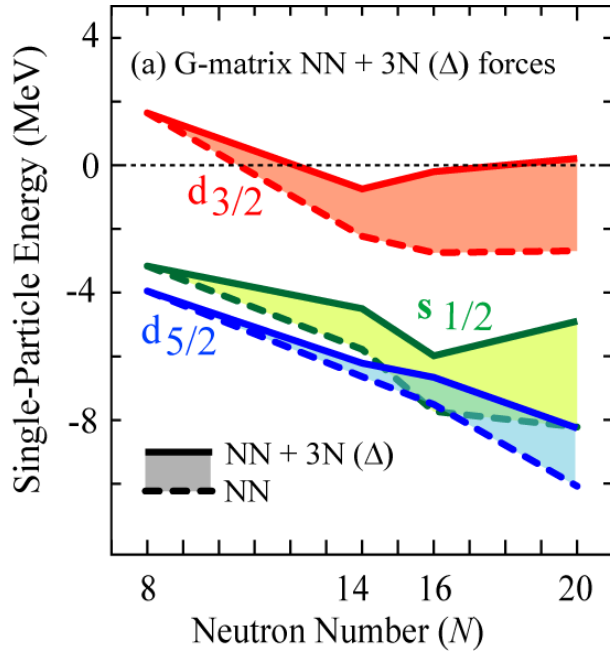
# Ground-state energies of oxygen isotopes

$NN$  force +  $3N$ -induced  $NN$  force  
 (Fujita-Miyazawa force)

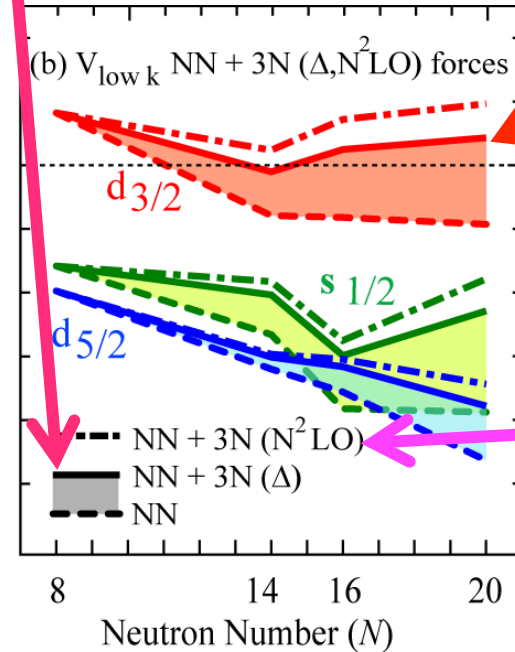


Drip line

(i)  $\Delta$ -hole excitation in a conventional way



(ii) EFT with  $\Delta$

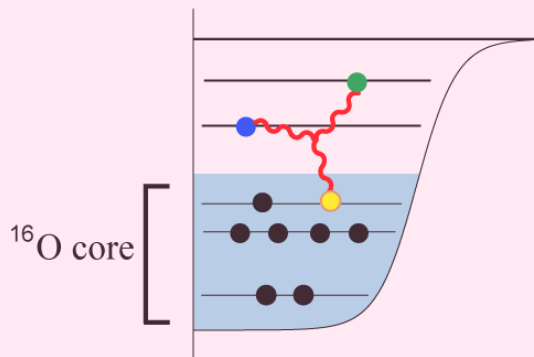


in continuum,  
but calculated  
as a bound state  
 $\Rightarrow$  to be discussed  
now

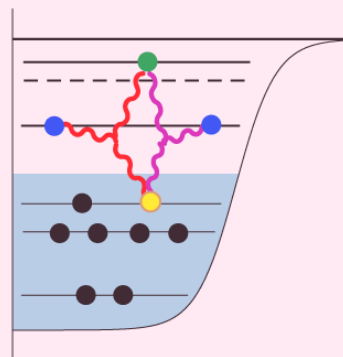
(iii) EFT incl. contact  
terms ( $N^2\text{LO}$ )

$\Delta$ -hole dominant  
role in  
determining  
oxygen drip line

(c) 3-body interaction



(d) 3-body interaction with one more neutron added to (c)



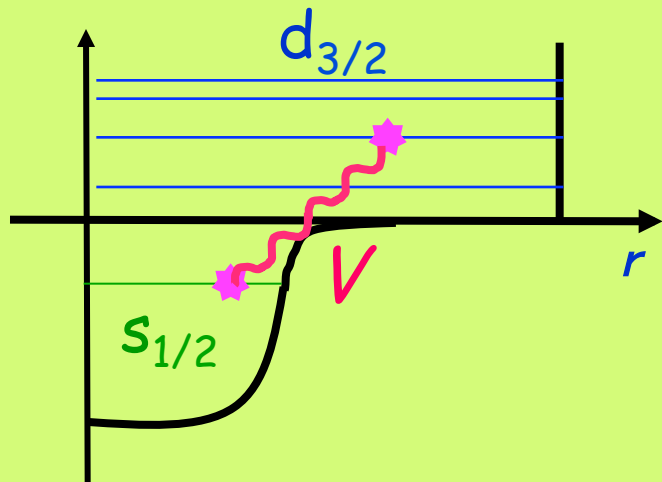
# Continuum-coupled shell model (CCSM)

$$\text{Hamiltonian: } H = H_0 + \hat{V} = \sum_j \tilde{\epsilon}_j n_j + \hat{V}$$

$$H_0 = T + U_{WS} + V_{\text{wall}} = \sum_j \tilde{\epsilon}_j n_j$$

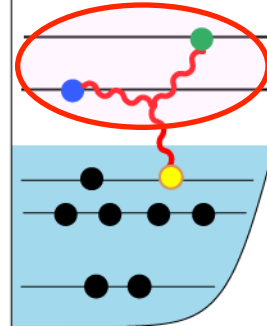
approximated  
by Gaussian

basis state-vector (denoted by  $j$ ):  
bound states + discretized continuum states  
wall very far (3000 fm, ~3000 basis states)



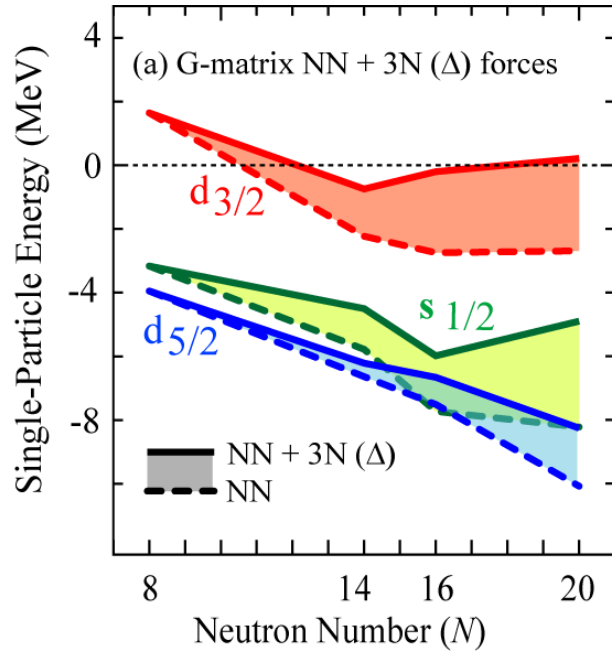
$V_{NN} +$

$^{16}\text{O}$  core

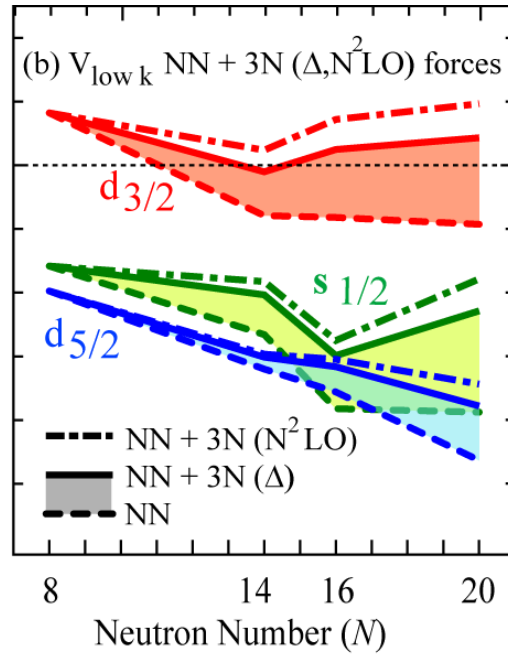


included

(i)  $\Delta$ -hole excitation in a conventional way

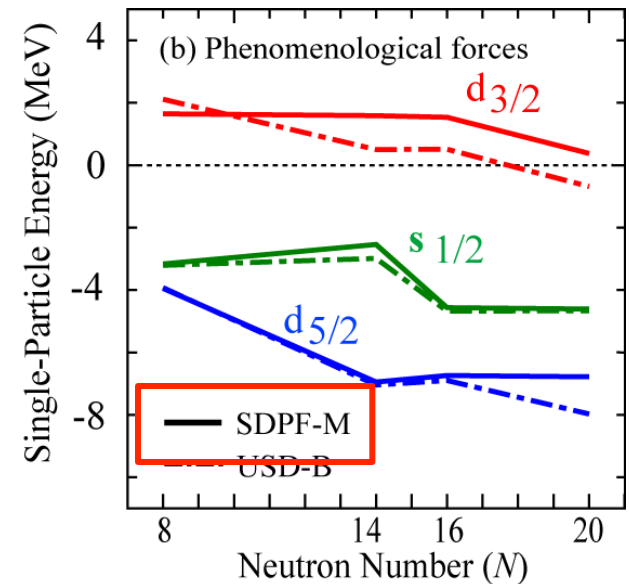
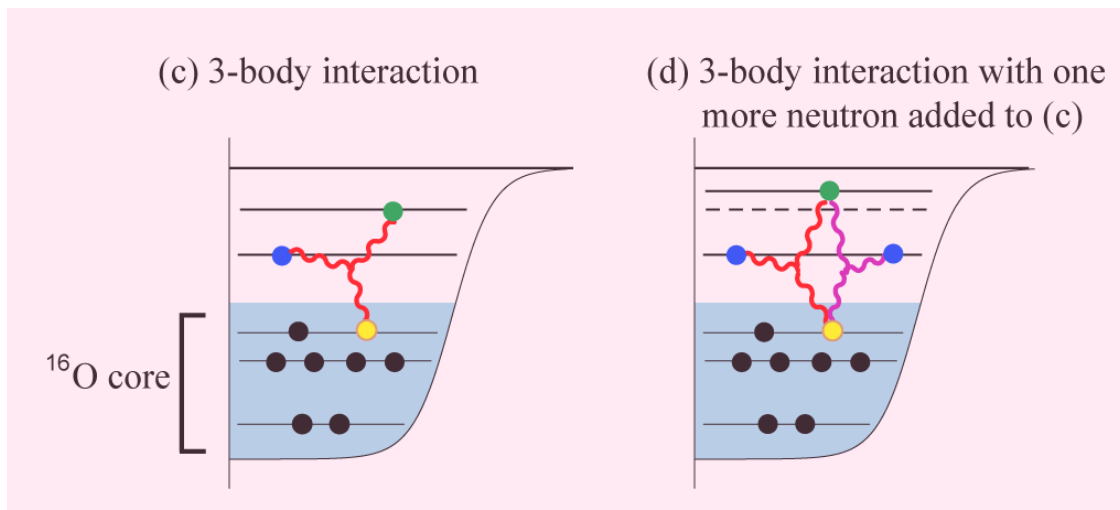


(ii) EFT with  $\Delta$



$\Delta$ -hole dominant role in determining oxygen drip line

phenomenological shell model



$$\hat{V}(r) = \sum_{i=1,2} g_i (1 + a_i \sigma \cdot \sigma) e^{-r^2/d_i^2}$$

$$d_{1,2} = 1.4, 0.7 \text{ fm}$$

SDPF-M TBME = TBME of this  $V(r)$   
for HO wave functions

$$\langle 1s_{1/2} 0d_{3/2} | V | 1s_{1/2} 0d_{3/2} \rangle_{J=1,2}$$

$$\langle 0d_{3/2} 0d_{3/2} | V | 0d_{3/2} 0d_{3/2} \rangle_{J=0,2}$$

under the assumption that 3-body force effect  
is included in SDPF-M interaction effectively

$V(r)$  is fixed only by interaction

$^{24}O = ^{22}O + 2n$  in the space

ground state :  $2n$  in  $1s_{1/2}$

excited states of  $1^+$  and  $2^+$  :

$$|iJ^+\rangle = |1s_{1/2} \otimes id_{3/2}; J^+\rangle$$



discretized continuum  $id_{3/2}$  ( $i = 1, 2, \dots$ )

$1s_{1/2}$  : solution of Woods-Saxon potential with observed  $S_n$

diagonalize  $H$

Eigenfunctions :

$$|J_k^+\rangle = \sum_i c_i^{(J,k)} |iJ^+\rangle$$



Reaction mechanism

-> Doorway state

# Removal of one proton and one neutron from $^{26}\text{F}$

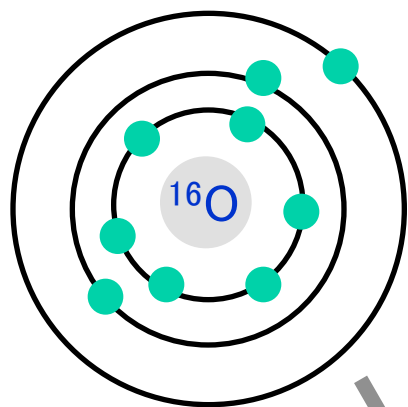
$^9\text{Be}(^{26}\text{F}, ^{24}\text{O})\text{X}$

C. Hoffman,  
M. Thoennessen et al.

knockout reaction @MSU (2009)

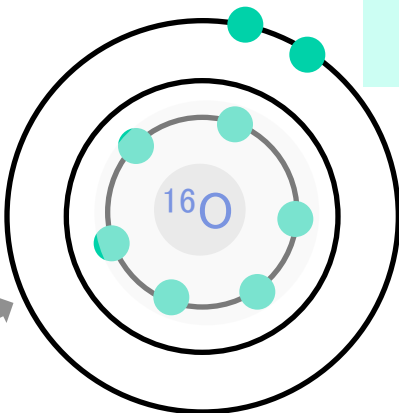
less probable

$\Leftarrow$  large  $s_{1/2}$ - $d_{3/2}$  neutron gap



bound nucleus  
 $^{26}\text{F}$

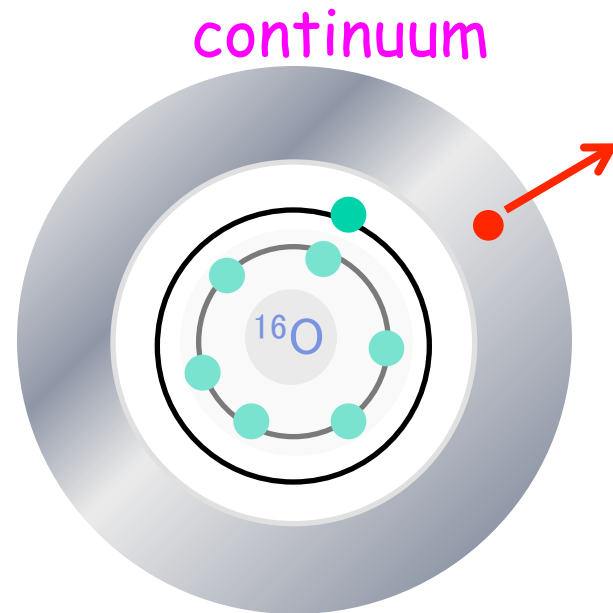
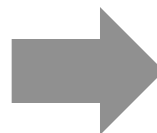
-p  
-n



doorway state

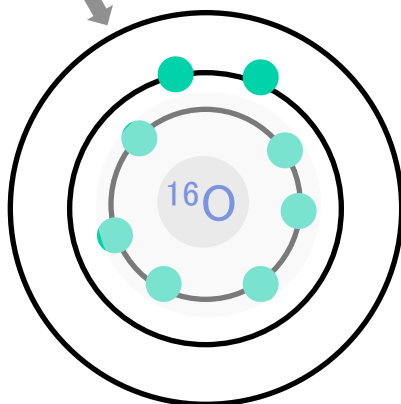
$$|1s_{1/2}0d_{3/2}; J_k^+\rangle$$

H.O.



excited states in  $^{24}\text{O}$

$$H^{\text{CCSM}}|J_k^+\rangle = E_k|J_k^+\rangle$$



ground state  
 $1s_{1/2}$  is bound.

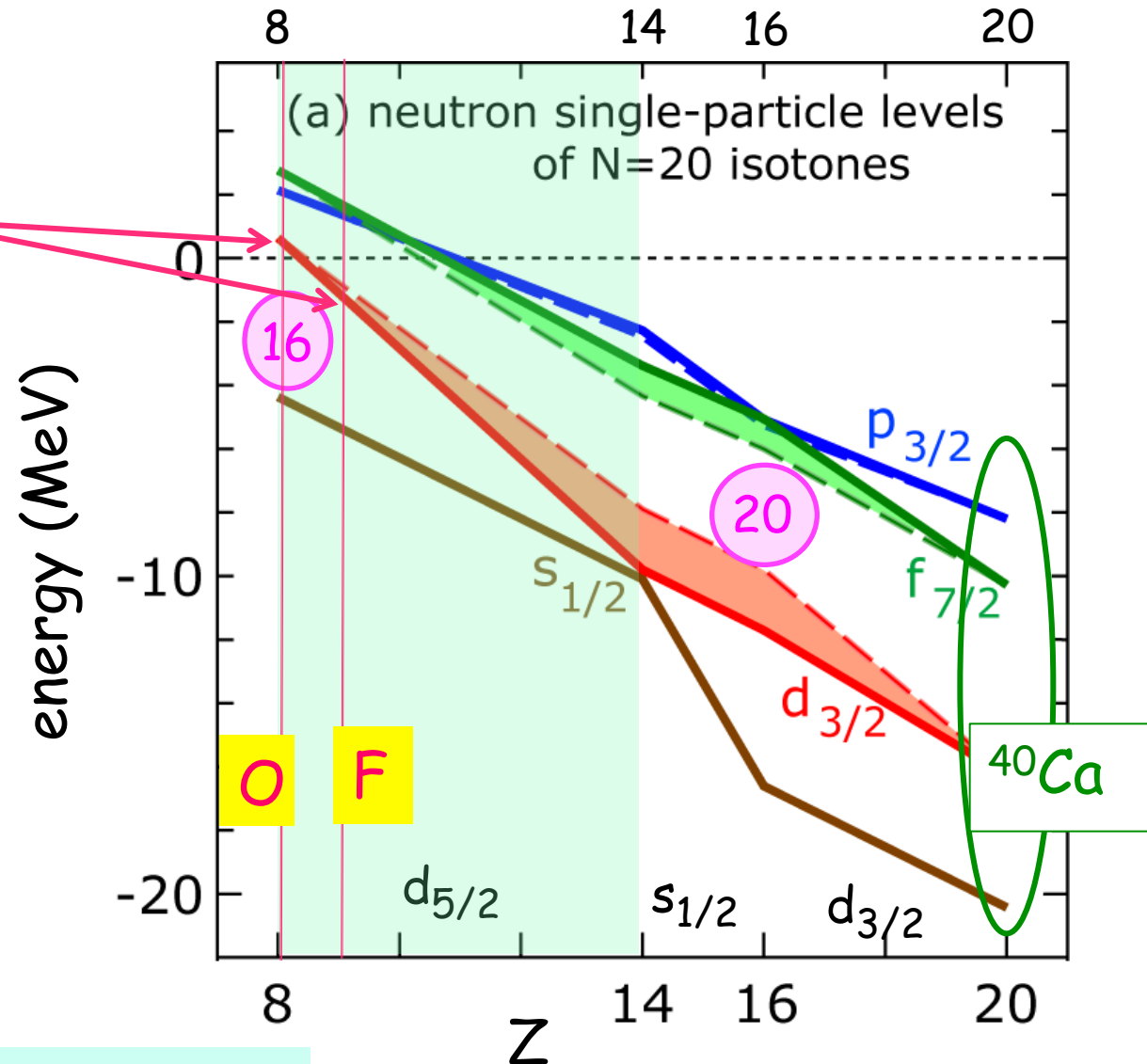
Kanungo et al. (2009)

# Neutron single-particle energies at $N=20$ for $Z=8\sim 20$

solid line : full (central + tensor)

dashed line : central only

$d_{3/2}$   
 bound in F  
 unbound in O  
 due to  
 interplay  
 between  
 tensor and  
 three-body  
 forces



## Removal of one proton and one neutron from $^{26}\text{F}$

Before the removal, neutron  $d_{3/2}$  is well-bound in  $^{26}\text{F}$  and can be described by a HO wave function.

Sudden removal  $\rightarrow$  doorway state with HO  $d_{3/2}$

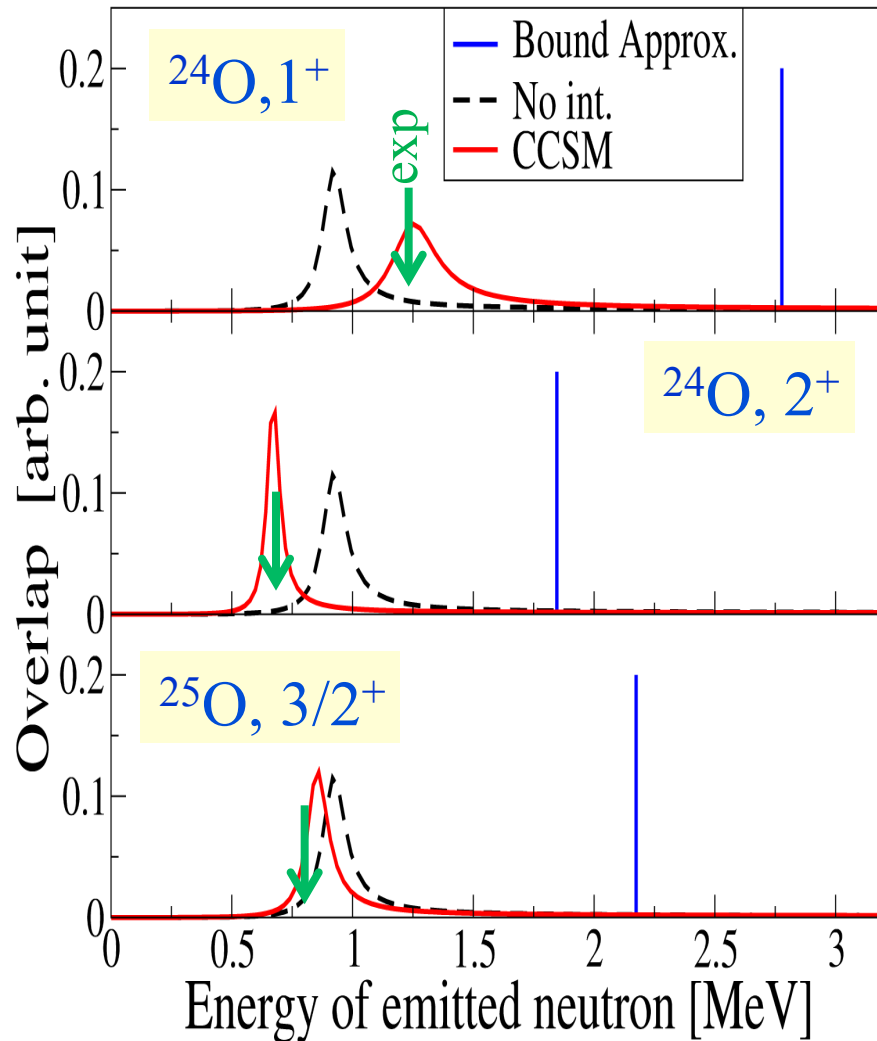
Decay of neutron from this  $d_{3/2}$

through overlap with continuum states :

$$\zeta_k^{(J)} \equiv \langle J_k^+ | 1s_{1/2} 0d_{3/2}; J^+ \rangle = \sum_i c_i^{(J,k)} \langle i d_{3/2} | 0 d_{3/2} \rangle$$

$$p_k^{(J)} \equiv |\zeta_k^{(J)}|^2 \quad \rightarrow \text{Spectrum of emitted neutron}$$

# Low-lying Continuum Spectra in $^{24}\text{O}$



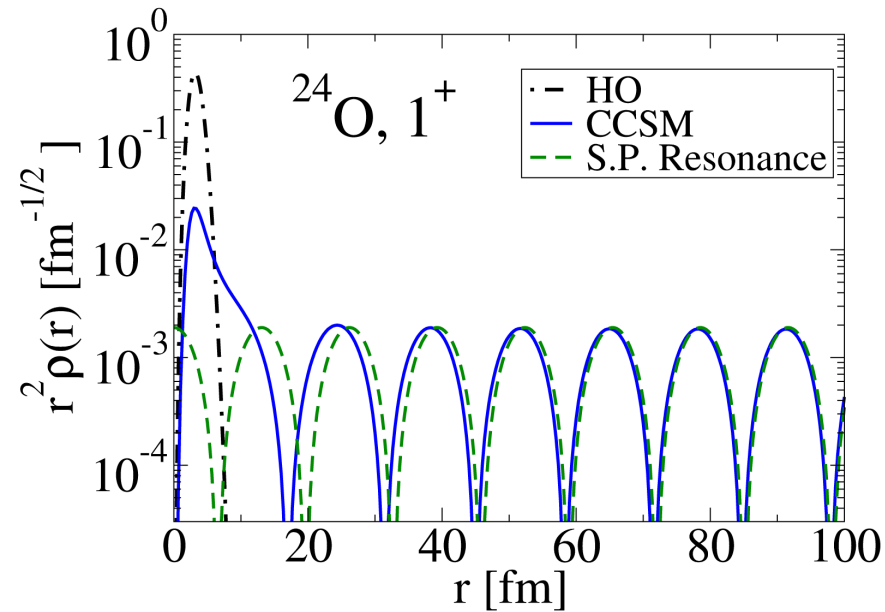
Doorway state ==> continuum states in  $^{24}\text{O}$

$$p_k^J = |\langle J_k^+ | \Phi_{\text{doorway}} \rangle|^2 = \left| \sum_i C_i^{(k)} \langle id_{3/2} | 0d_{3/2} \rangle \right|^2$$

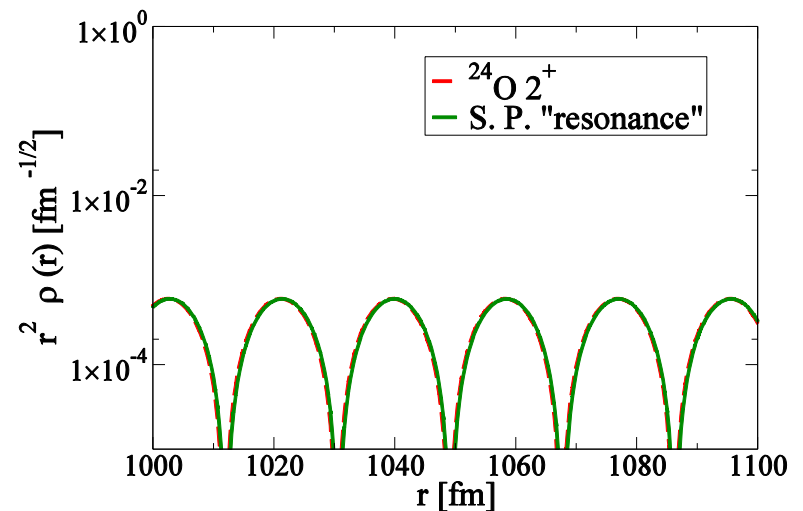
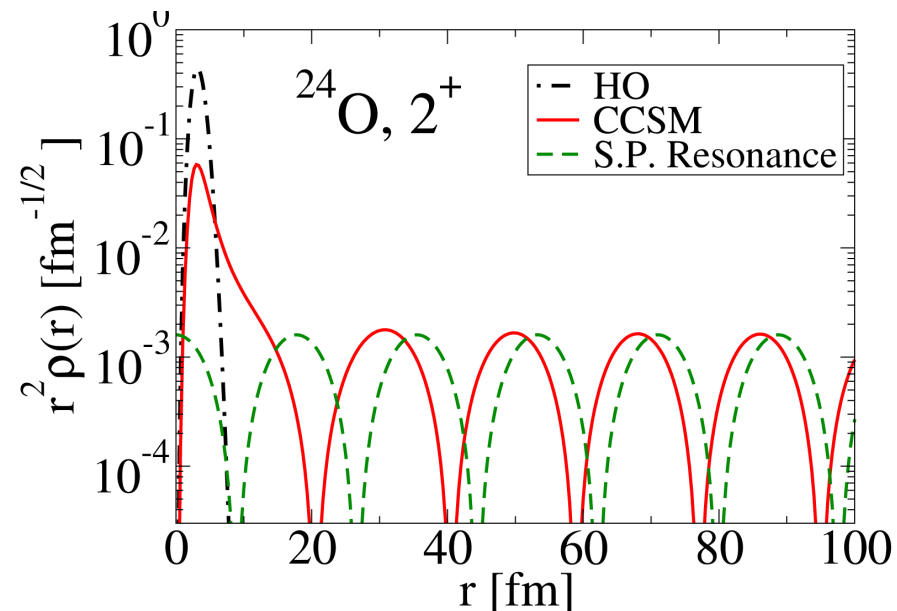
- **bound approximation:**  
Normal shell model with the same Hamiltonian : NO continuum effect
- **CCSM :** With continuum effect  
*incl. residual interaction*
- **no int. :** With continuum effect but  
*no residual interaction.*

- Continuum effect is about 1 MeV
- No bound excited state.
- 1<sup>+</sup>-2<sup>+</sup> splitting by 2-body interaction
- 1<sup>+</sup>-2<sup>+</sup> splitting is in good agreement with experiments.

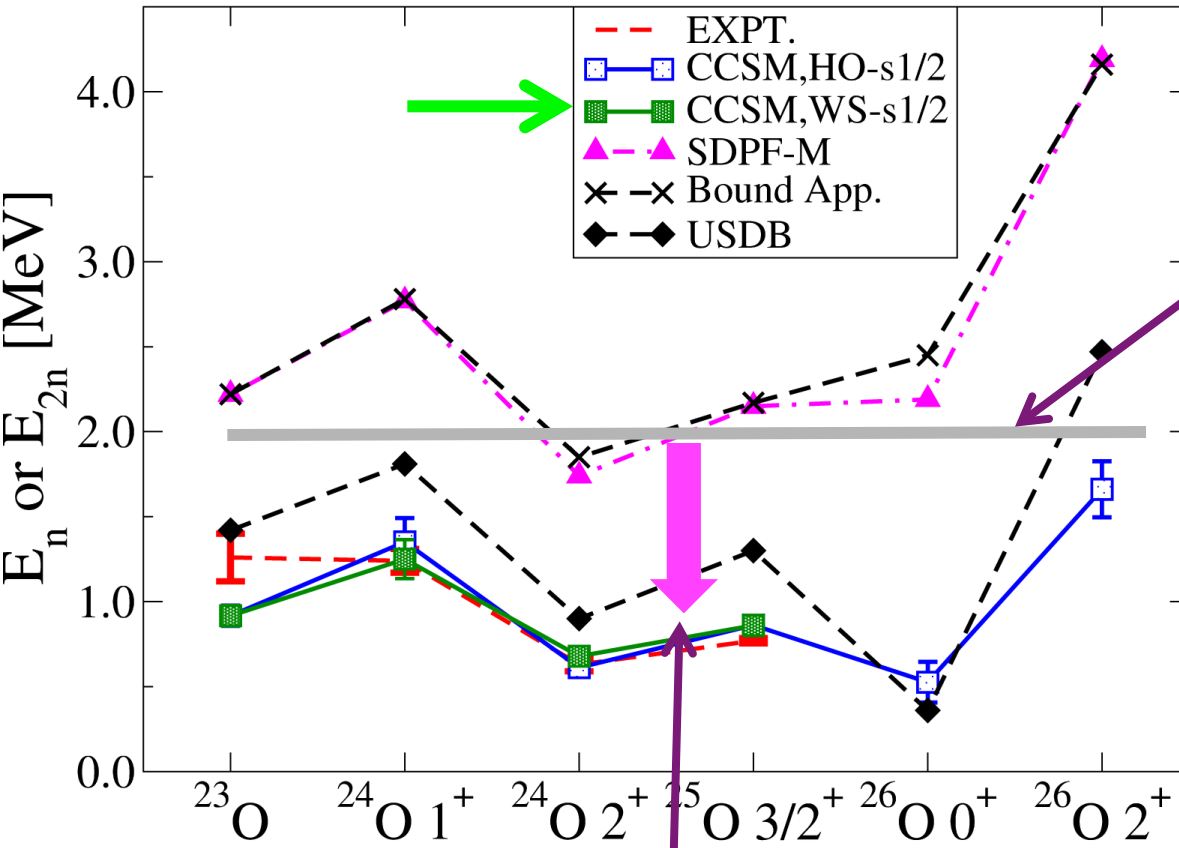
# Radial density (w.f.) of continuum states in $^{24}\text{O}$



- Notable difference between  $1^+$  and  $2^+$  states.
- The peak states in CCSM reproduce the behavior of “resonance wave” at far distance (phase shift of  $\pi/2$ ).

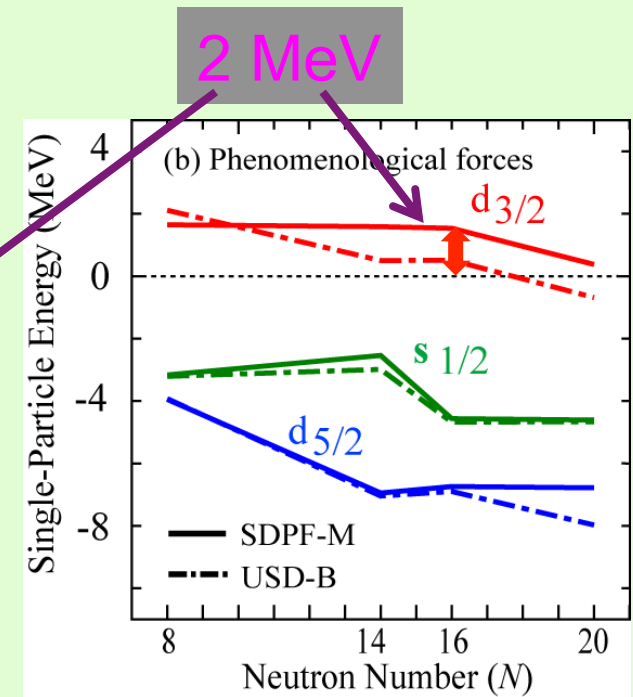


# Peak Energies of neutron emission



Lowering due to continuum effect

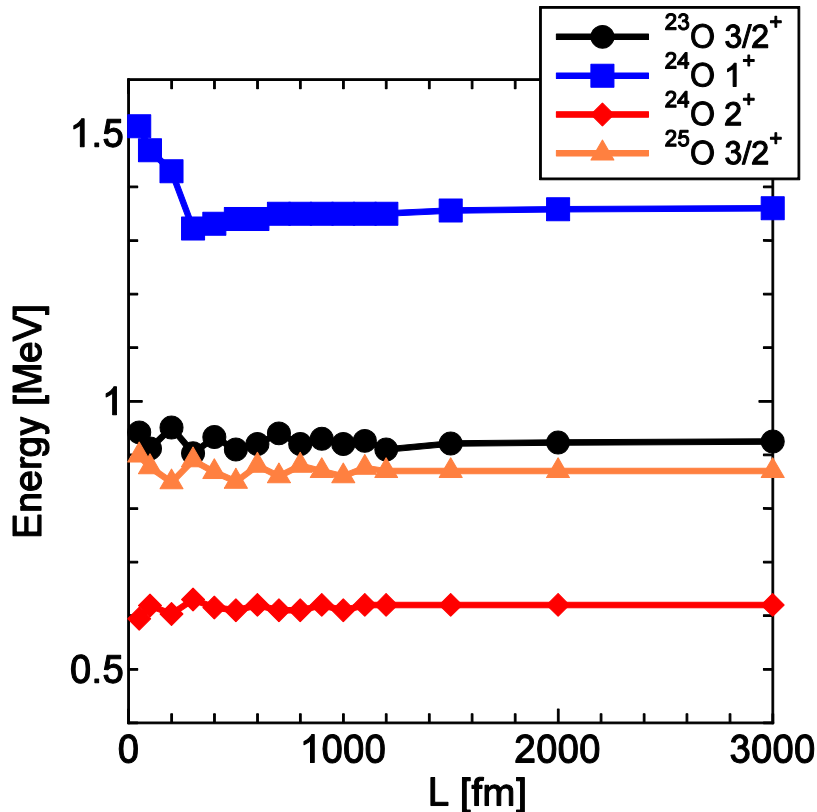
# SPE as bound state



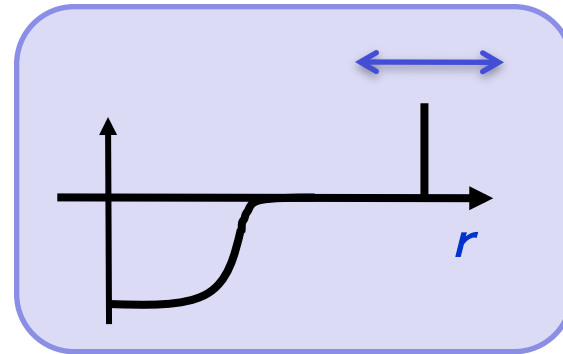
Exp. : MSU (Hoffman et al),  
RIKEN (Elekes et al)

Continuum spectra are consistent with the shell evolution

# Convergence with respect to boundary condition



The peak energies as a function of L.



- The results do not change so much if L is taken to be sufficiently large.
- Even usual values of  $L \sim 50$  fm are not stable.



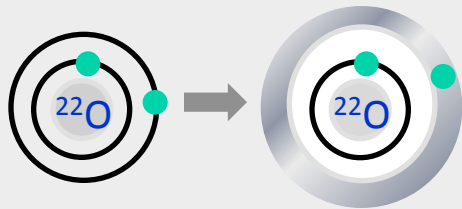
Comparison to

single-particle resonance

# Effective phase shift and one-body reduction

Can many-body resonance be described by effective one-body problem?

CCSM



CCSM: continuum spectra are obtained by taking the overlap between the doorway state and CCSM eigenstates in continuum.

Effective phase shift



We define effective phase shift by introducing 1-body reduction of CCSM wave function.

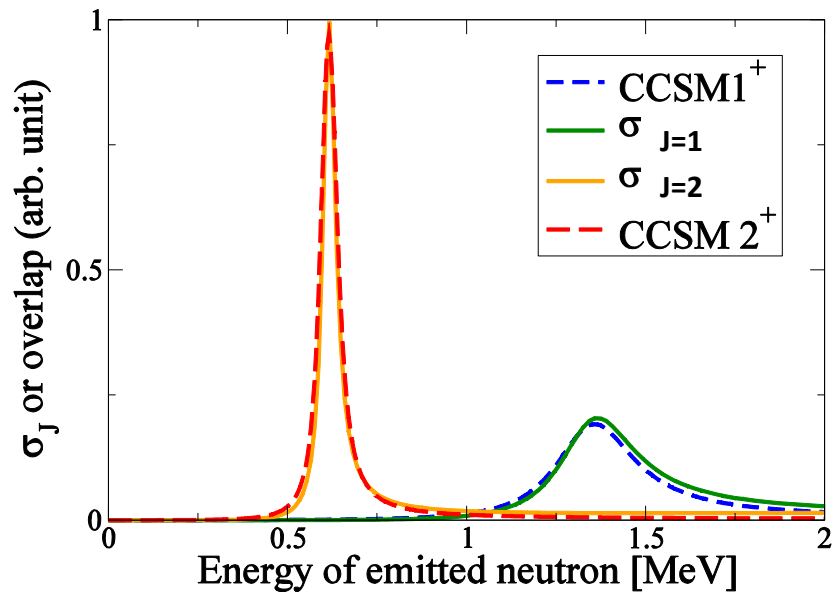
$$\begin{aligned} |J_k^+\rangle &= \sum_i c_i^{(J,k)} |1s_{1/2} \otimes id_{3/2}; J\rangle \\ &=: |1s_{1/2} \otimes \tilde{d}_{3/2;J,k}; J\rangle \end{aligned}$$

$$|\tilde{d}_{3/2;J,k}; J\rangle = \sum_i c_i^{(J,k)} |id_{3/2}\rangle$$

One can then obtain **phase shift**, and can use it for calculating the cross section.

$$\sigma_J = \frac{4\pi}{k^2} (2l + 1) \sin^2 \delta_J$$

# Effective phase shift and one-body reduction

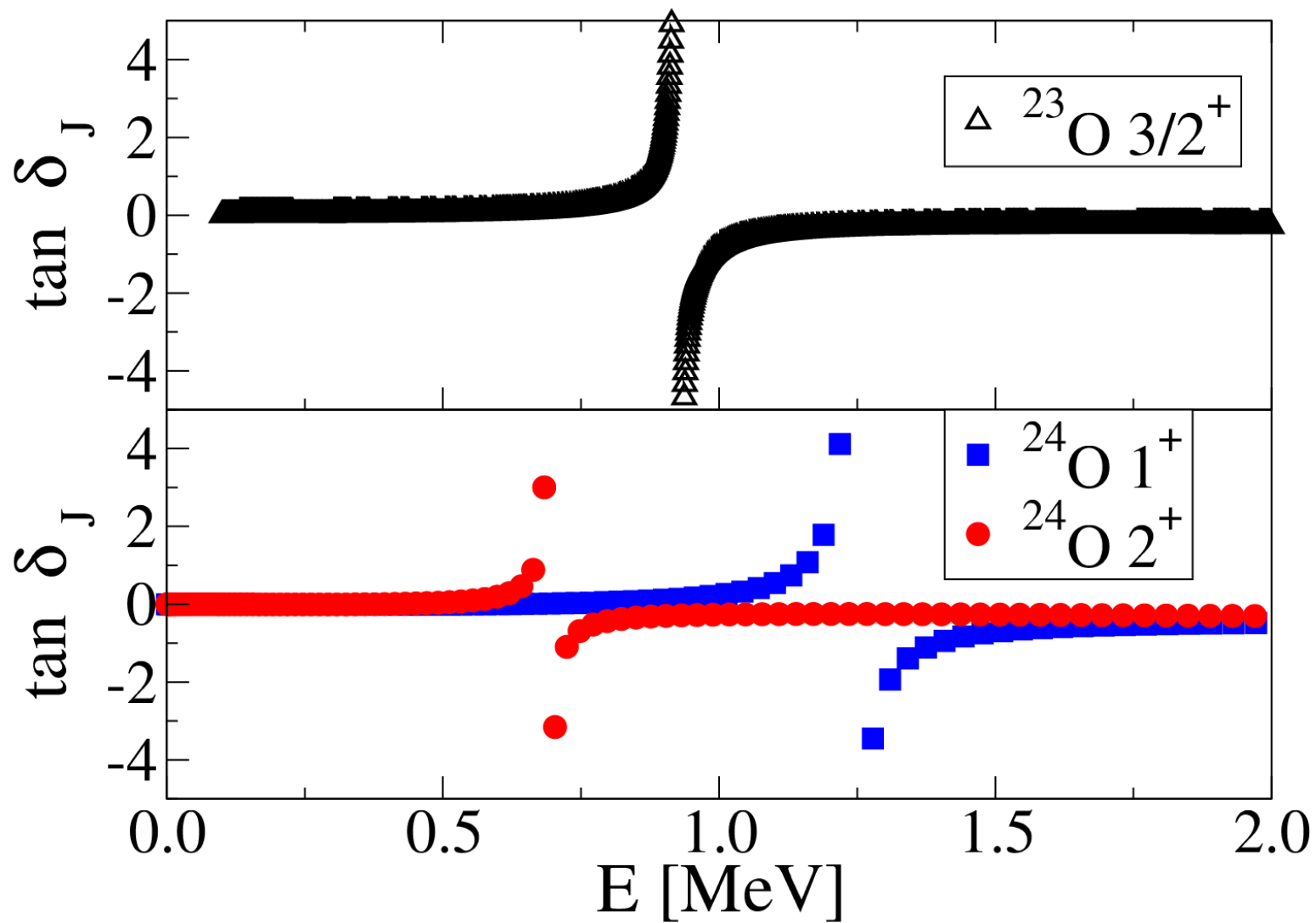


- CCSM (doorway state approach) and effective phase shift approach give very similar results for peak positions.
- Notable difference appears for the width of 2+ in  $^{24}\text{O}$ .
  - Doorway state decays faster. -

Unit : MeV	$^{23}\text{O}$	$^{24}\text{O}$	
states	3/2+	1+	2+
CCSM E	0.92	1.35	0.61
CCSM $\Gamma$	0.11	0.28	<b>0.06</b>
Phase shift E	0.92	1.36	0.61
Phase shift $\Gamma$	0.11	0.28	<b>0.04</b>

50 % longer life time

# Phase shift



Although resonance state and doorway state are different, continuum spectra are similar.

What is the meaning of single-particle resonance states in complex dynamical processes such as multi-nucleon transfer heavy-ion reactions ???

Time scale of the heavy-ion reaction may be shorter than the resonance life time.

Coupling to continuum lowers the (peak) energies by more than 1 MeV for oxygen isotopes.

spectroscopy in continuum