

Gravitational-Wave Astronomy

Current Status and Future Prospects

Patrick Brady

Gravitational Waves in GR

Spacetime interval can be written as

$$ds^2 = (\eta_{\alpha\beta} + h_{\alpha\beta}) dx^\alpha dx^\beta$$

where $\eta_{\alpha\beta}$ is the Minkowski metric and $h_{\alpha\beta}$ is a metric perturbation

For weak gravitational fields, the leading order solution is

$$h_{ij} = \frac{2G}{c^4} \frac{1}{r} \frac{d^2 Q_{ij}}{dt^2} \sim \frac{G}{c^4} \frac{mv^2}{r}$$

Mass Quadrupole

$$Q_{ij} \approx \int \rho \left(x_i x_j - \frac{1}{3} \delta_{ij} x^2 \right) d^3 x$$

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quadrupole variation

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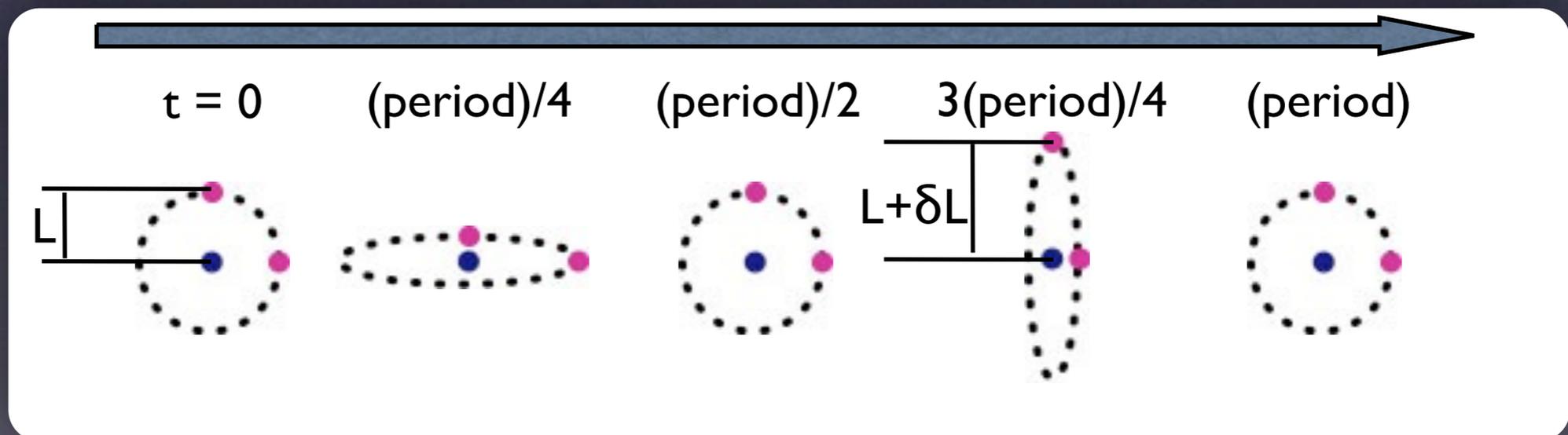
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Physical Effects of the Waves

- As gravitational waves pass, they change the distance between neighboring bodies
- GR predicts two polarizations

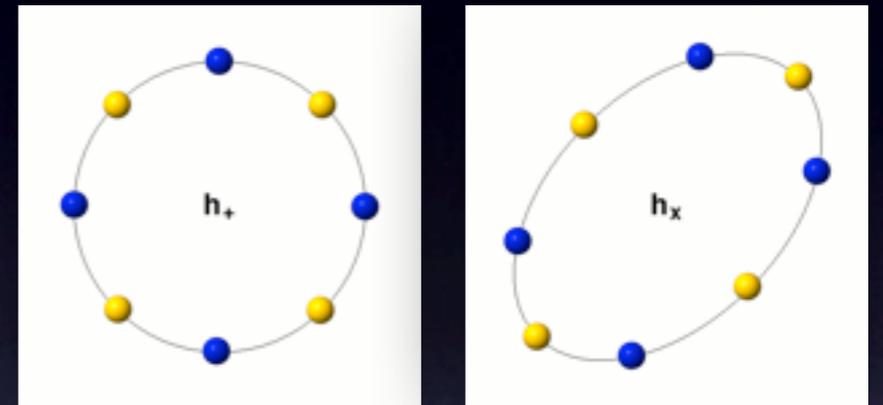
Animations: Warren Anderson

- Fractional change in distance is the strain given by $h = \delta L / L$



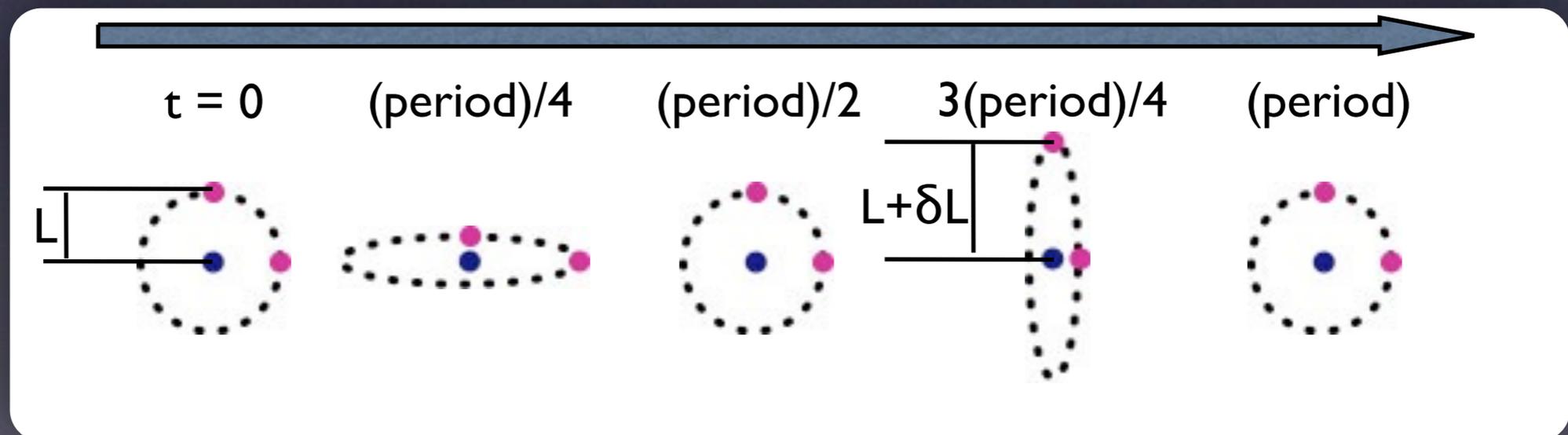
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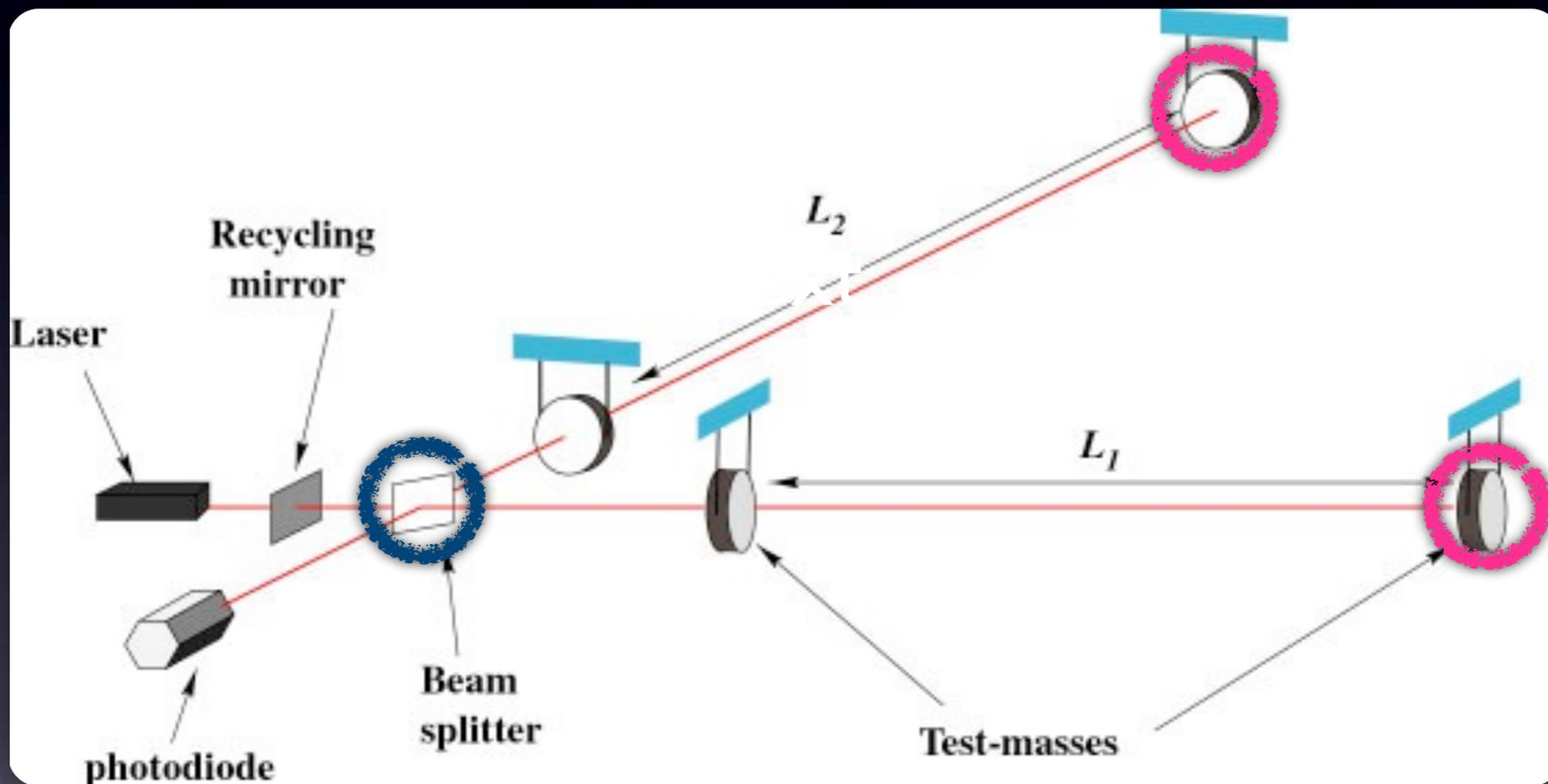
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Schematic Detector

As gravitational waves pass, they change the distance between neighboring bodies...



...causing the interference pattern to change at the photodiode

Global Network of Gravitational-wave Detectors

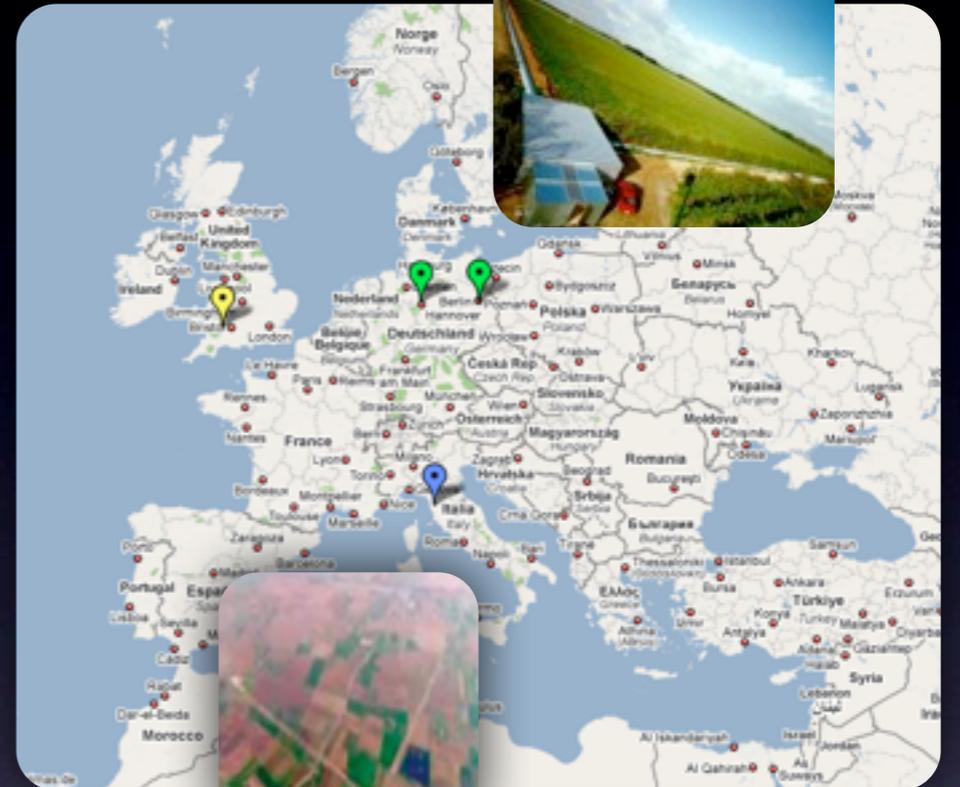
LIGO Hanford



LIGO Livingston



GE600



Virgo



Global Network of Gravitational-wave Detectors

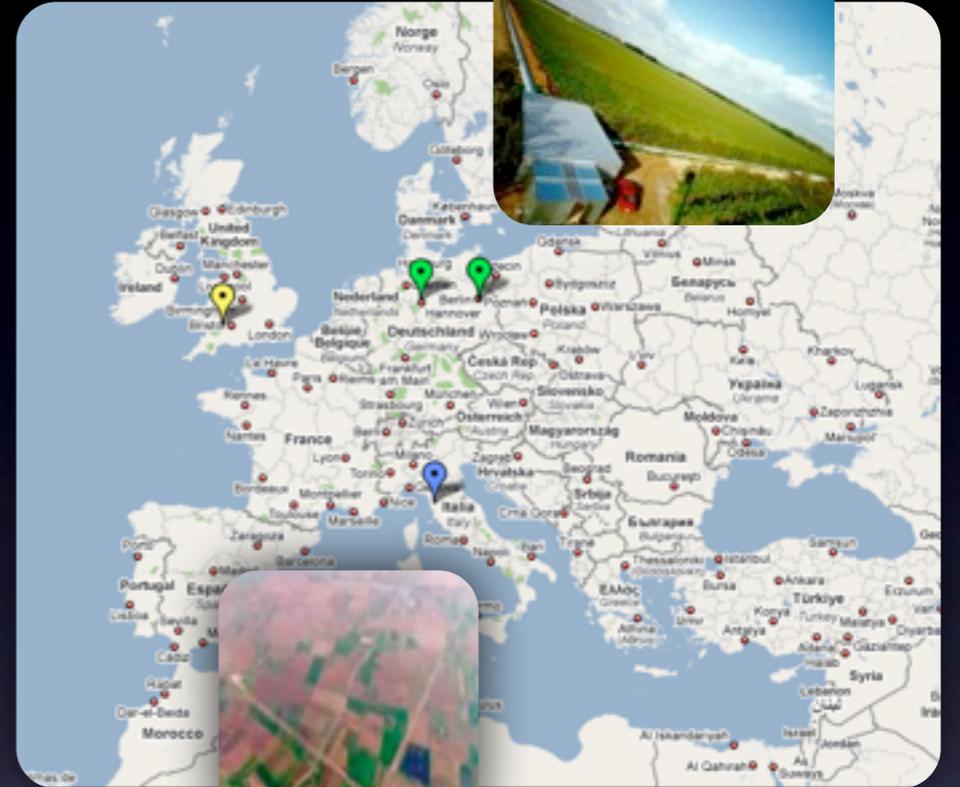
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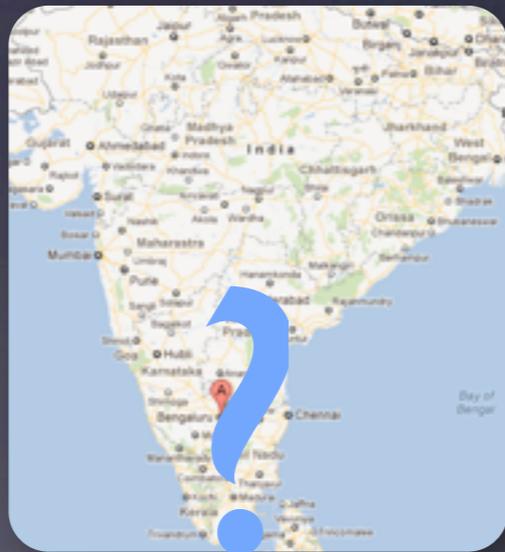


Virgo

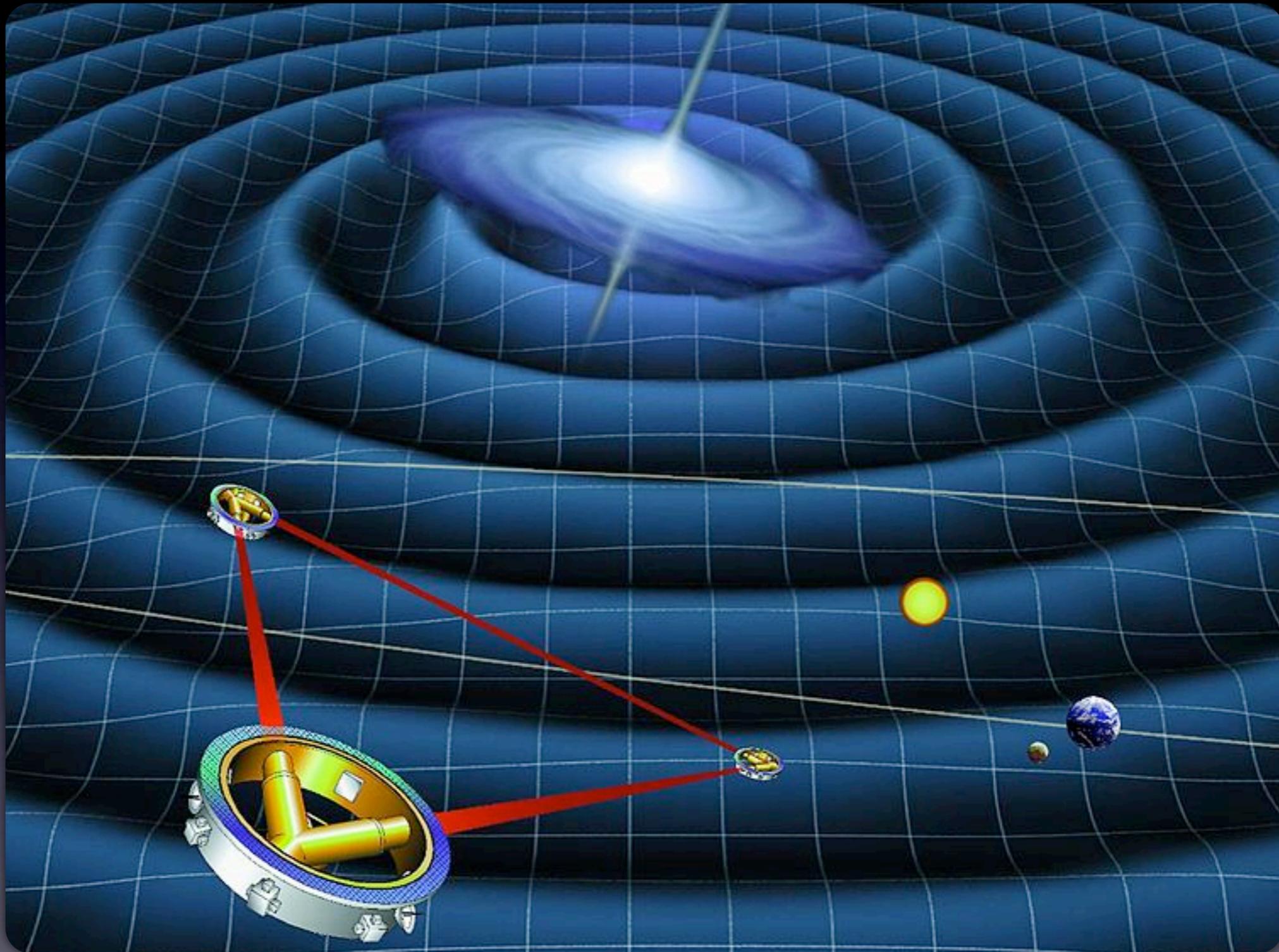
Kagra



LIGO India

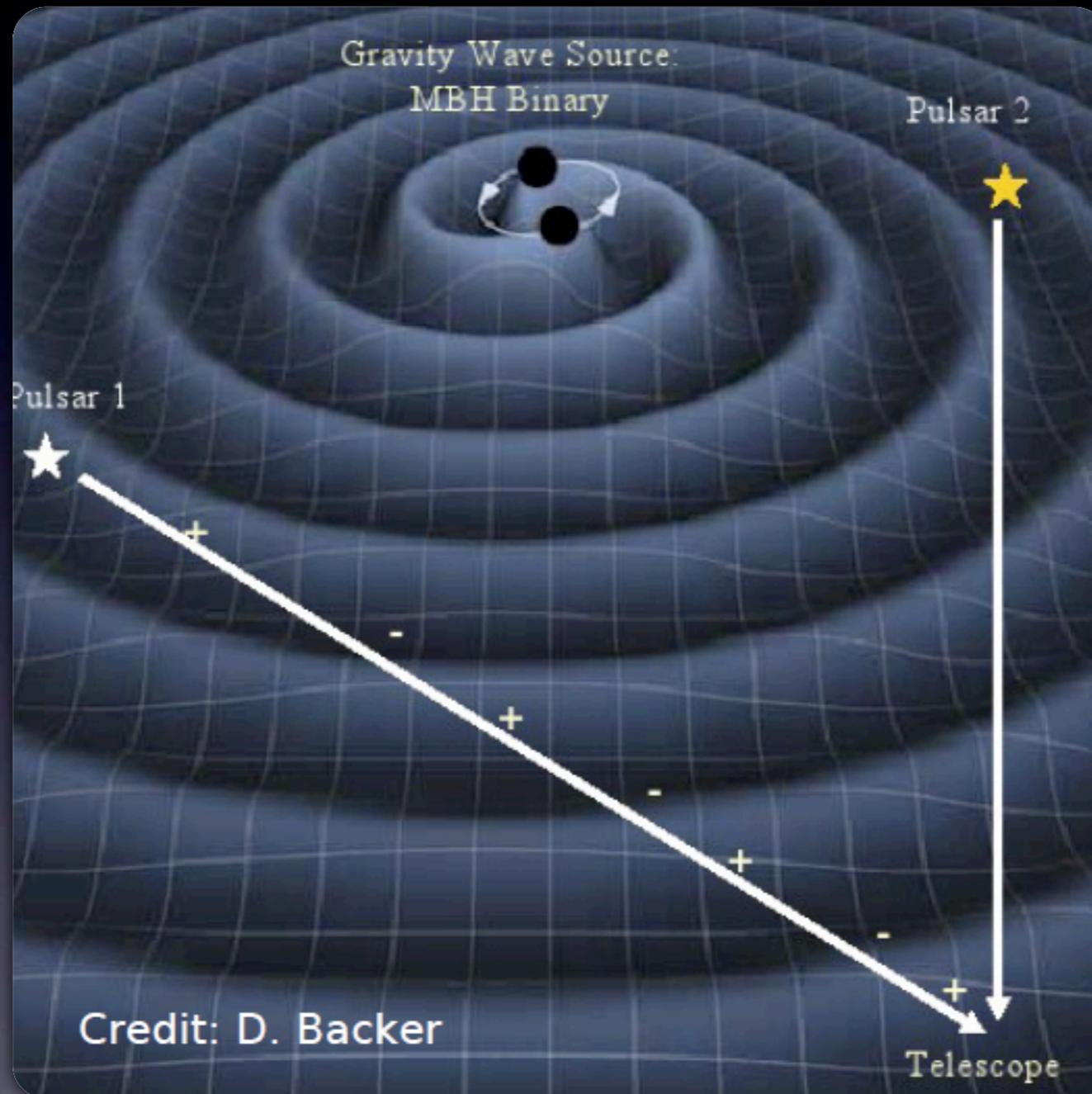


Space-Based Detectors



DECIGO & LISA

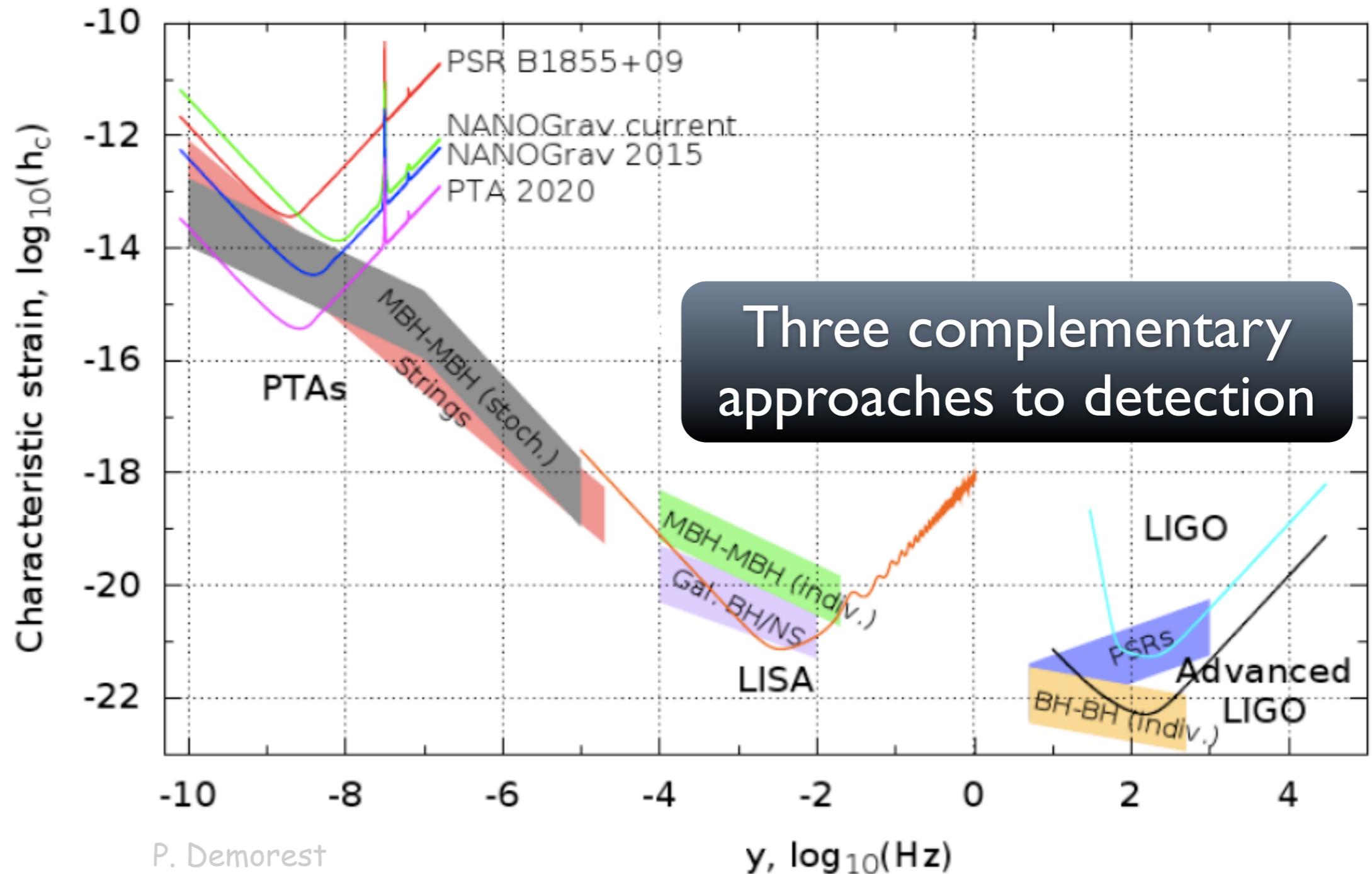
Pulsar Timing



International Pulsar Timing Array (IPTA)
includes NANOGrav, EPTA,

Gravitational-Wave Spectrum

Courtesy: NanoGrav, M. McLaughlin, P. Demorest



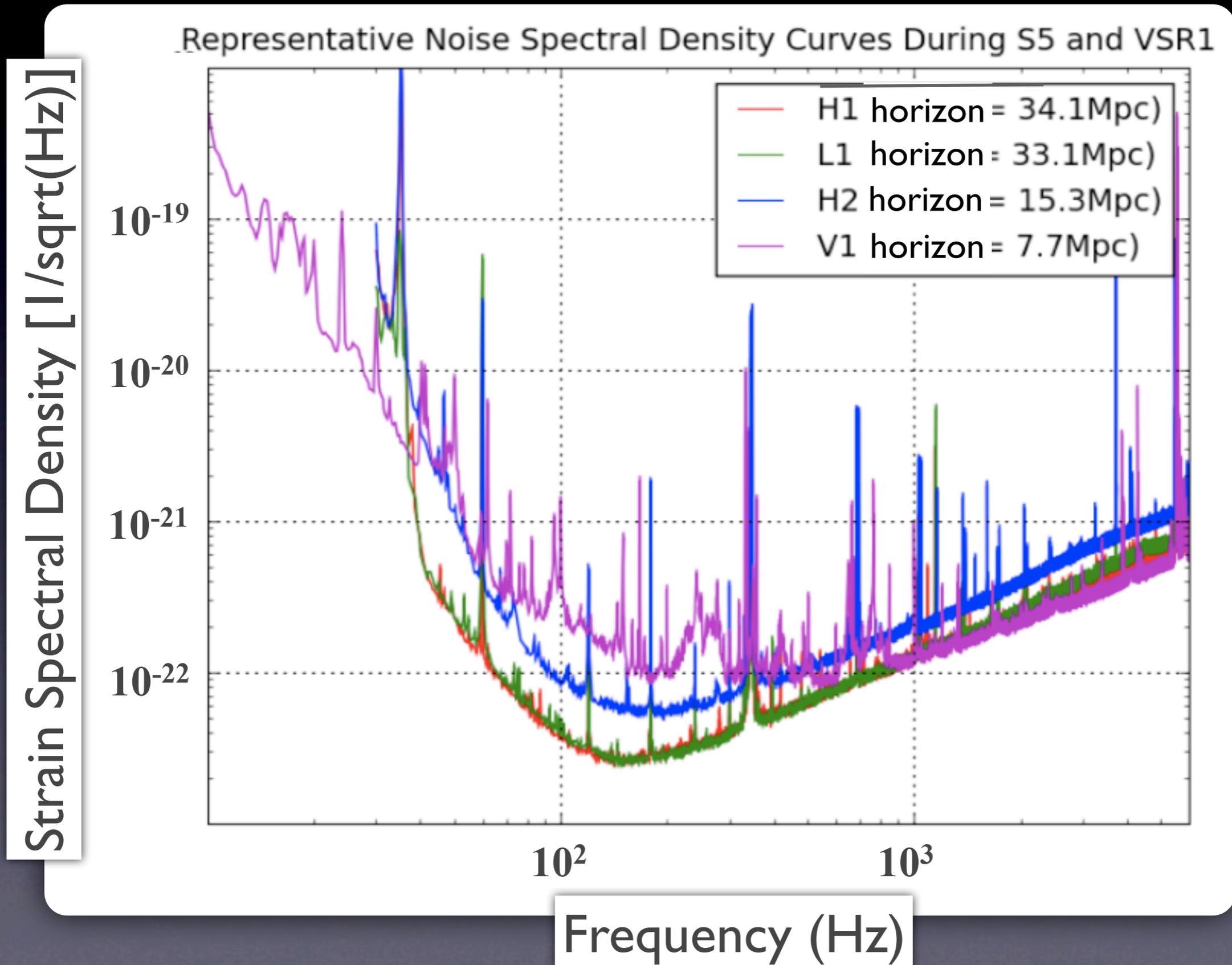
Motivation

- To test relativistic gravity and to develop gravitational wave detection as an astronomical probe
- Anticipated gravitational-wave signals
 - Transient signals: compact binary coalescence, supernovae, cosmic string kinks, black-hole ringdown.
 - Continuous signals: spinning neutron stars in isolation & in binaries.
 - Stochastic signals from cosmological sources.
 - Serendipitous signals: unanticipated sources in all these categories
- Gravitational waves carry information about the structure and dynamics of the sources

LIGO & Virgo Observing Runs



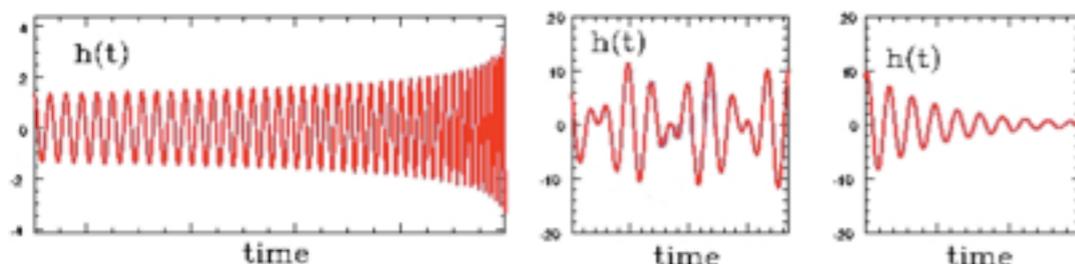
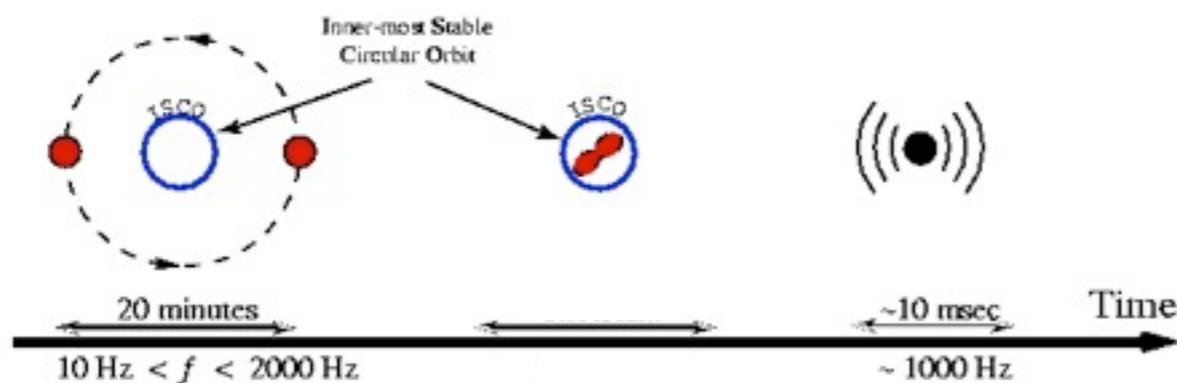
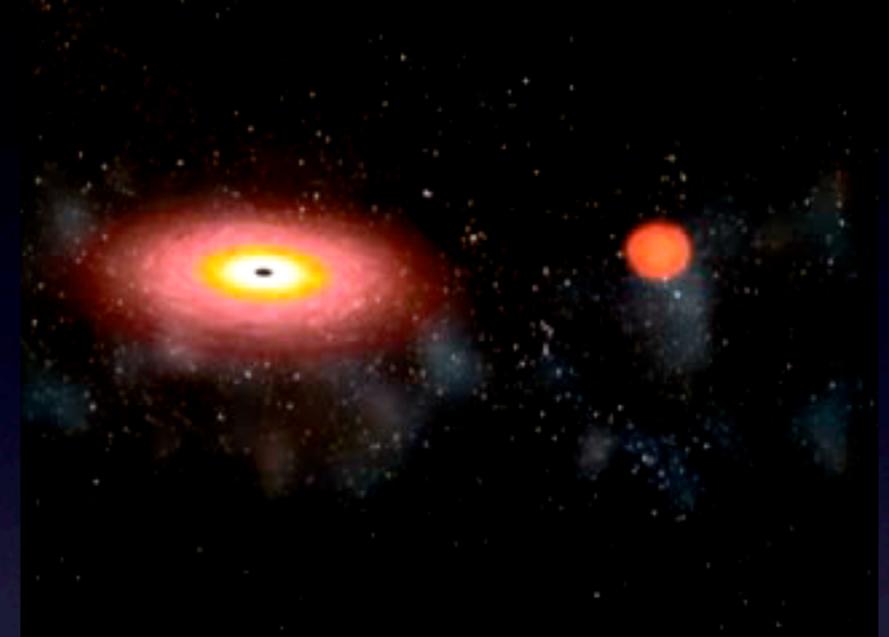
S5/VSR1 Sensitivity



Compact Binaries

- Pairs of black holes, neutron stars, or a black hole and neutron star
- As they orbit one another, they emit gravitational waves causing the objects to get closer together, eventually merging

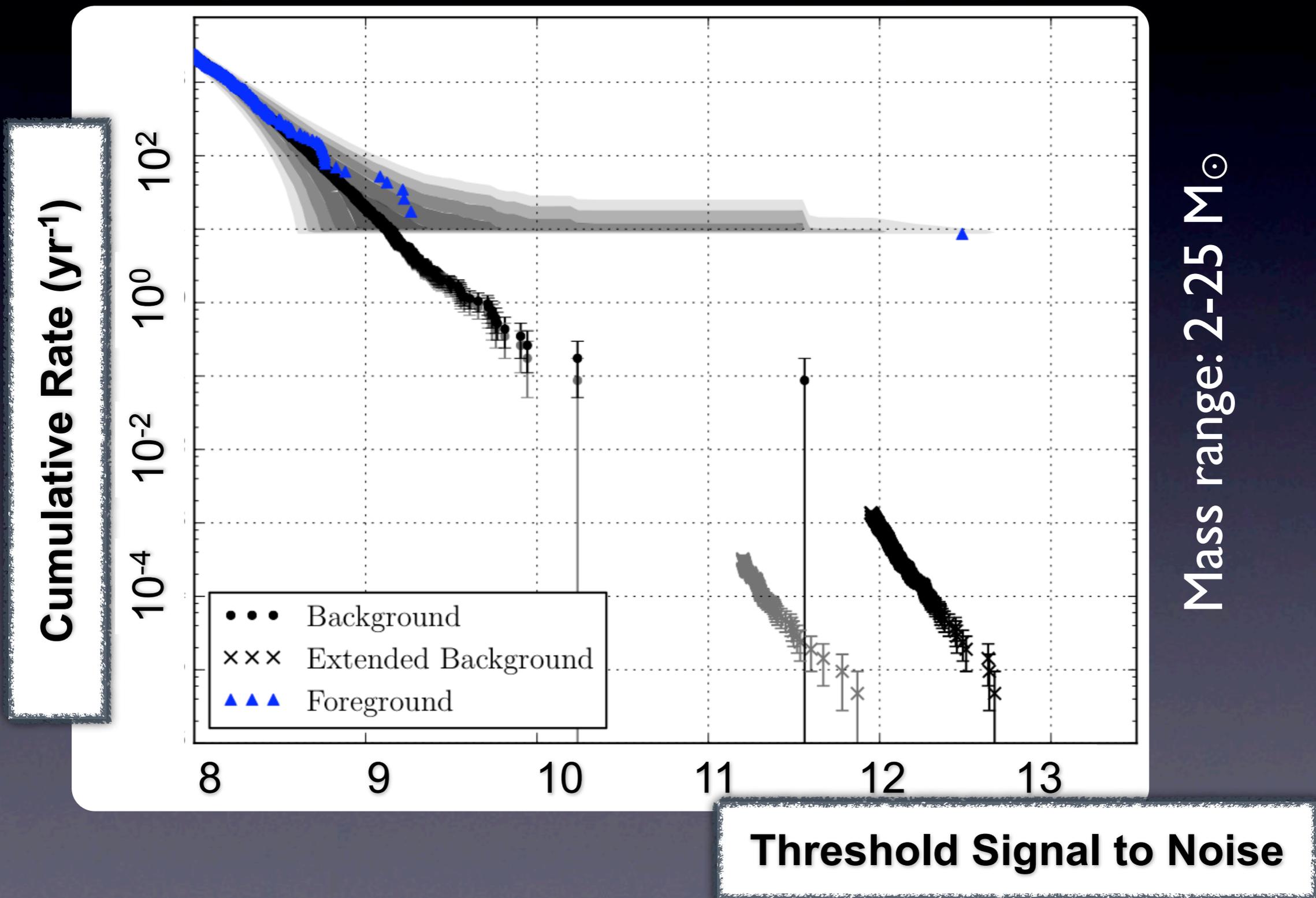
Credit: Dana Berry, NASA



$$h_{ij} \sim \frac{4GM}{c^4} \frac{v^2}{r}$$

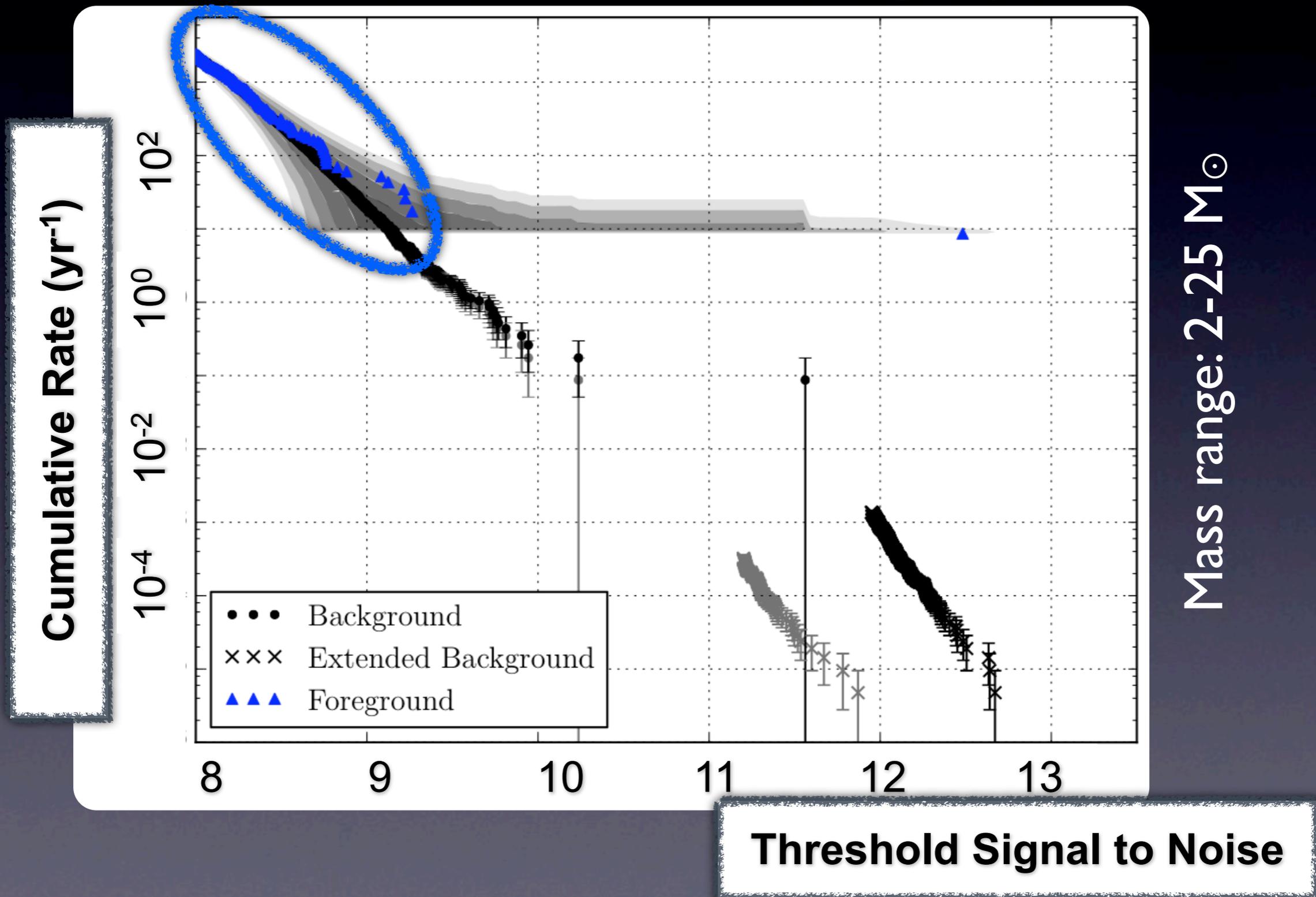
S6/VSR2 Compact Binary Foreground

(Includes blind injection signal)



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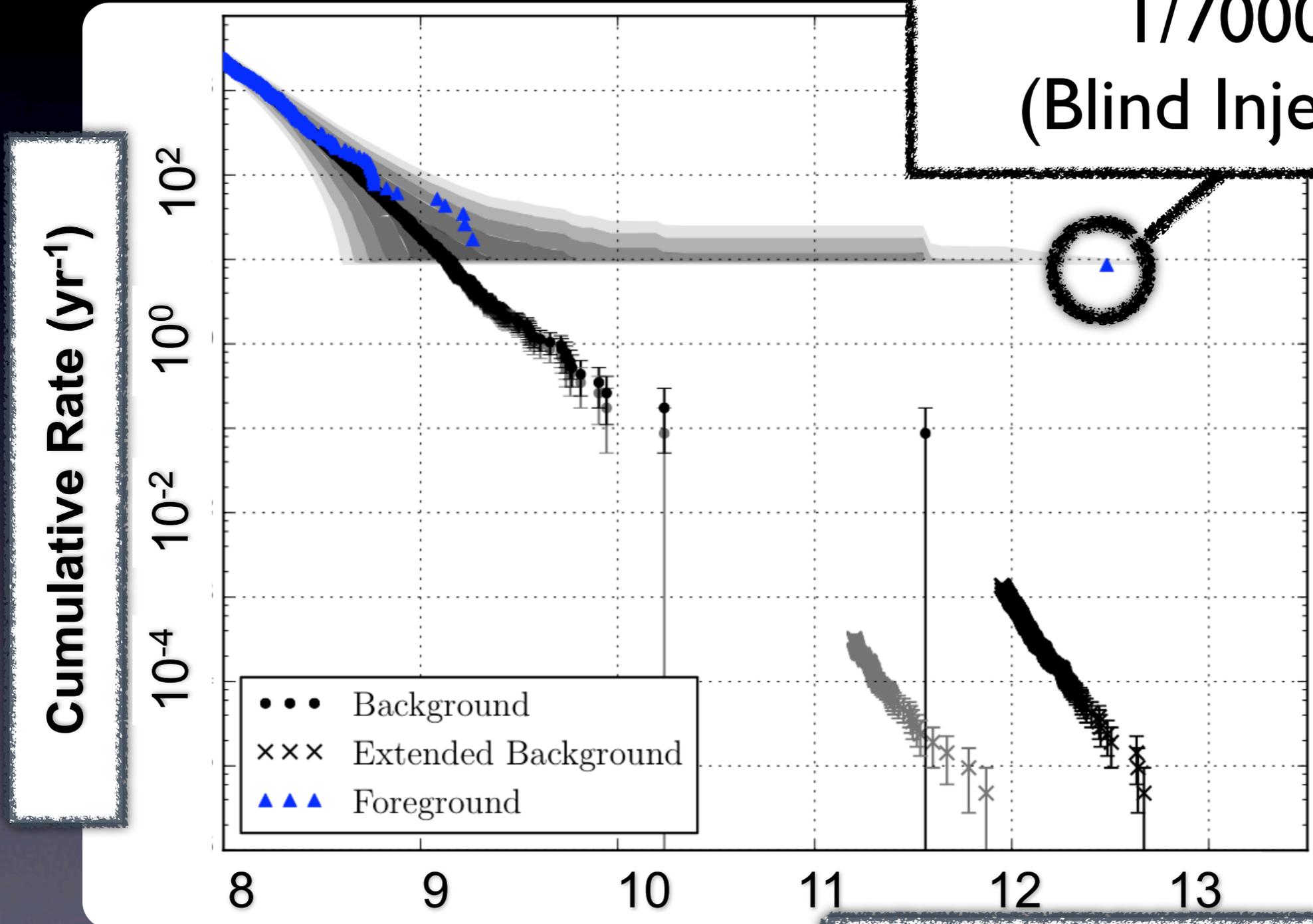


S6/VSR2 Compact Binary Foreground

(Includes blind injections)

Big Dog Event:
1/7000yr
(Blind Injection)

<http://ligo.org/science/GW100916/>



Cumulative Rate (yr⁻¹)

Mass range: 2-25 M_⊙

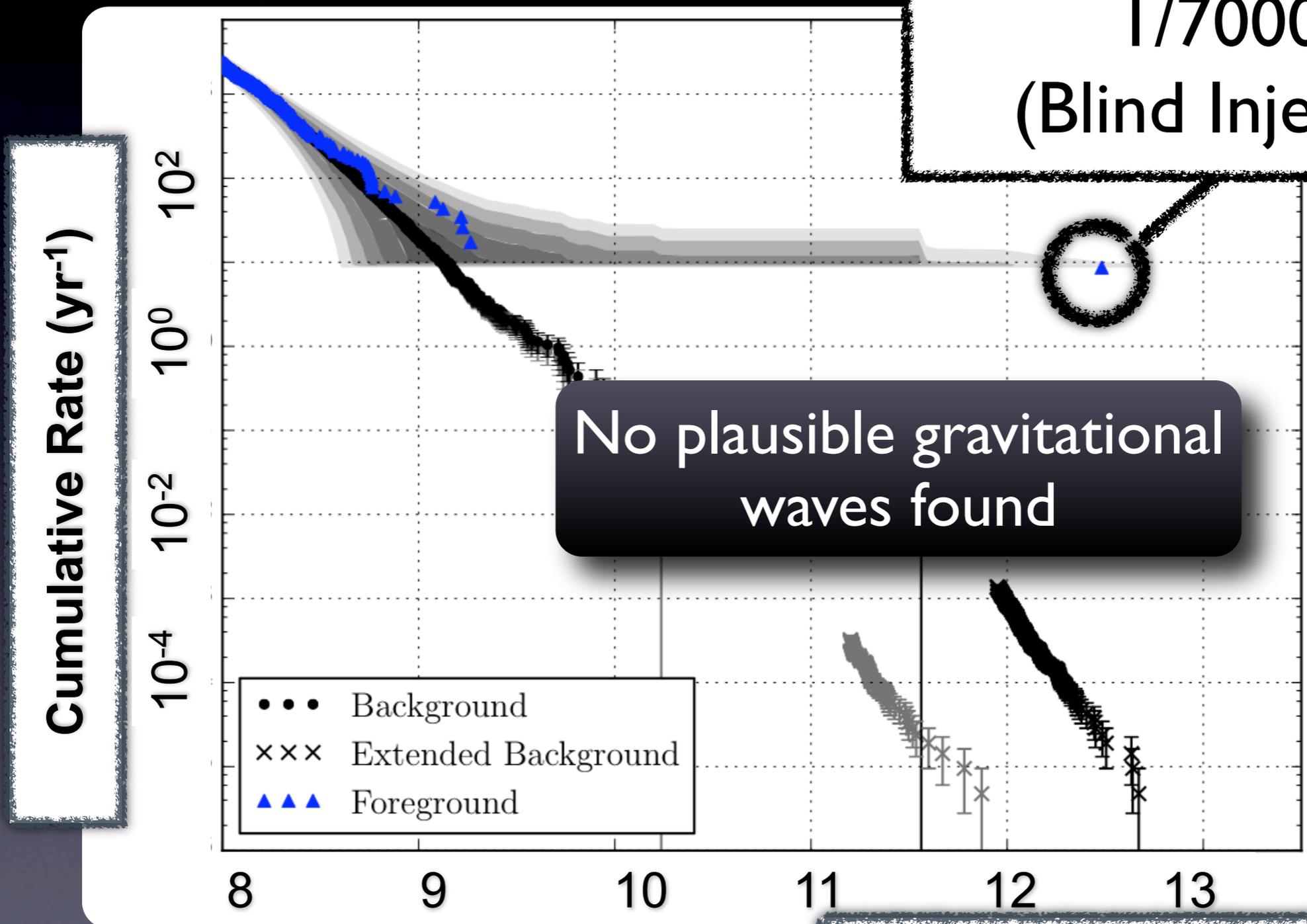
Threshold Signal to Noise

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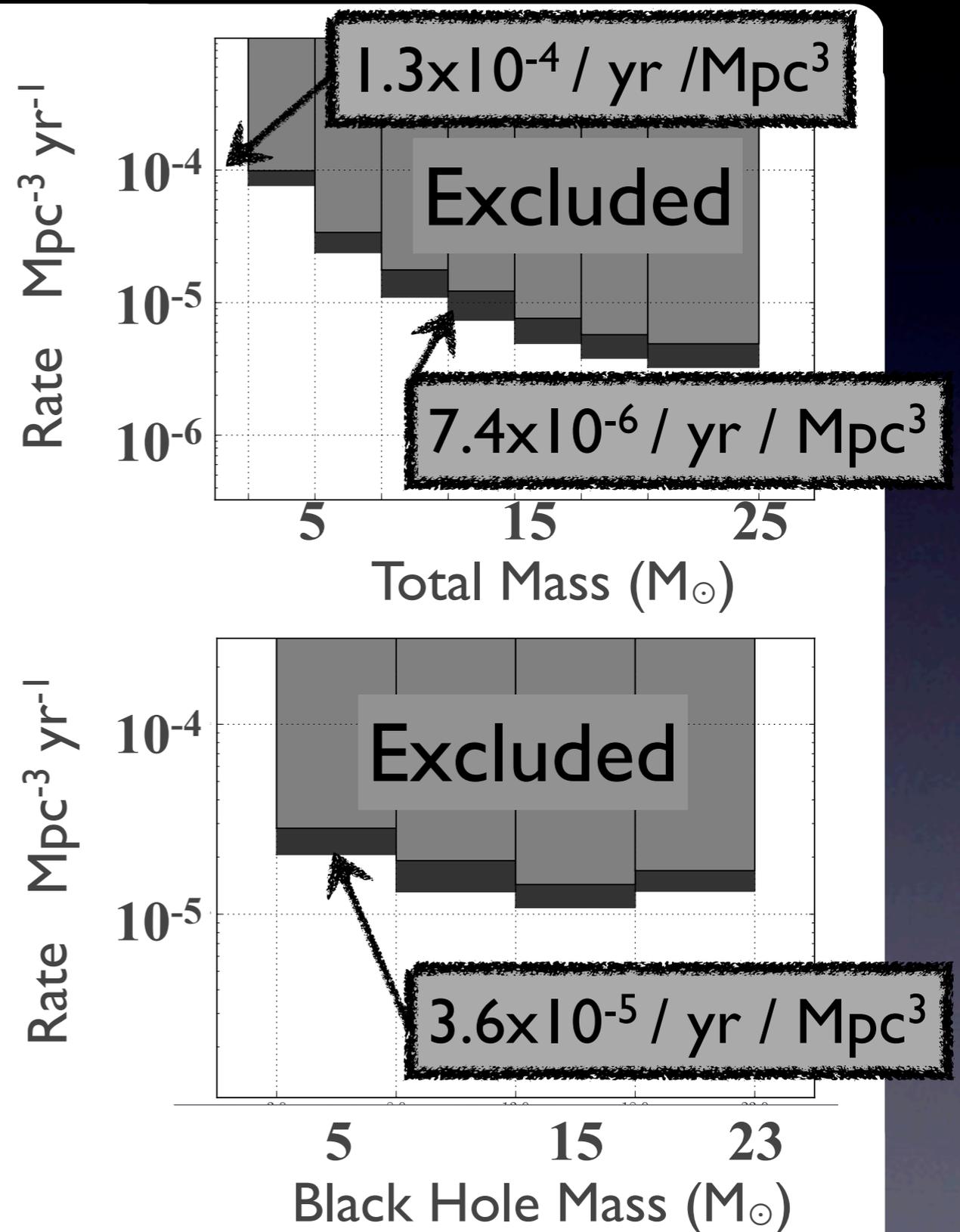


Threshold Signal to Noise

Searches for compact binaries

No plausible gravitational waves found

- Reasonable rate estimate for binary neutron stars is $\sim 1 \times 10^{-6} / \text{yr} / \text{Mpc}^3$
- Neutron star black hole rates are $\sim 3 \times 10^{-8} / \text{yr} / \text{Mpc}^3$
- Black hole binaries are $\sim 5 \times 10^{-9} / \text{yr} / \text{Mpc}^3$



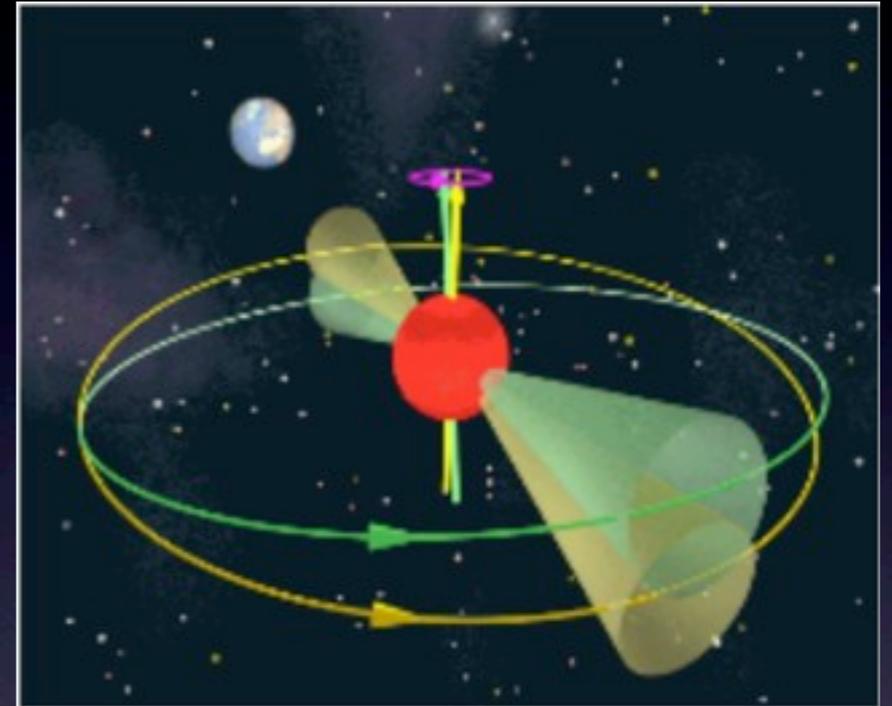
LIGO-Virgo, Phys Rev D85 (2012) 082002
[arXiv:1111.7314]

Continuous Signals

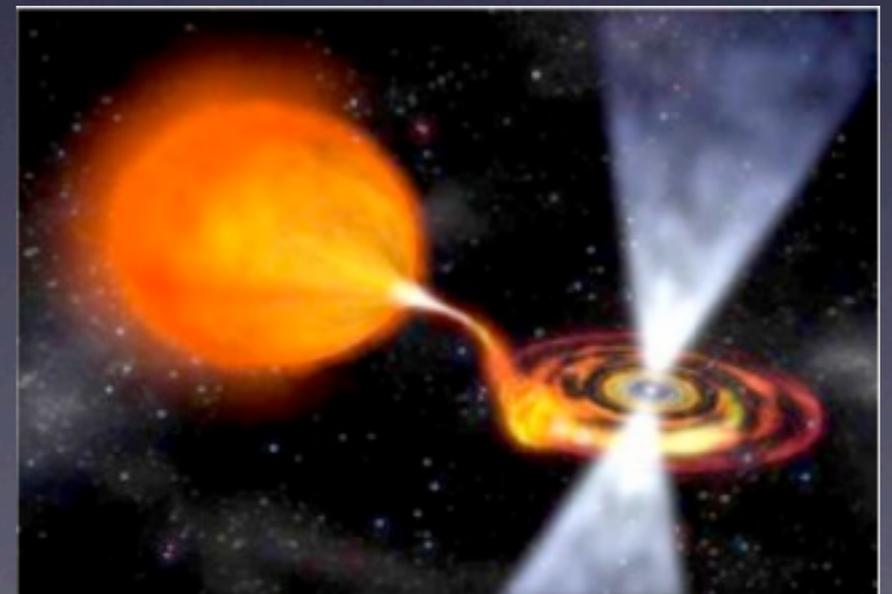
- Signals last as long as, or longer than, the observation time
- Known radio pulsars could also emit gravitational waves
- Unknown radio pulsars that are not beamed toward earth
- Signal strength is given by

$$h_0 = \frac{16\pi^2 G}{c^4} \frac{\epsilon I f^2}{r}$$

Credit: M. Kramer



Credit: Dana Berry/NASA



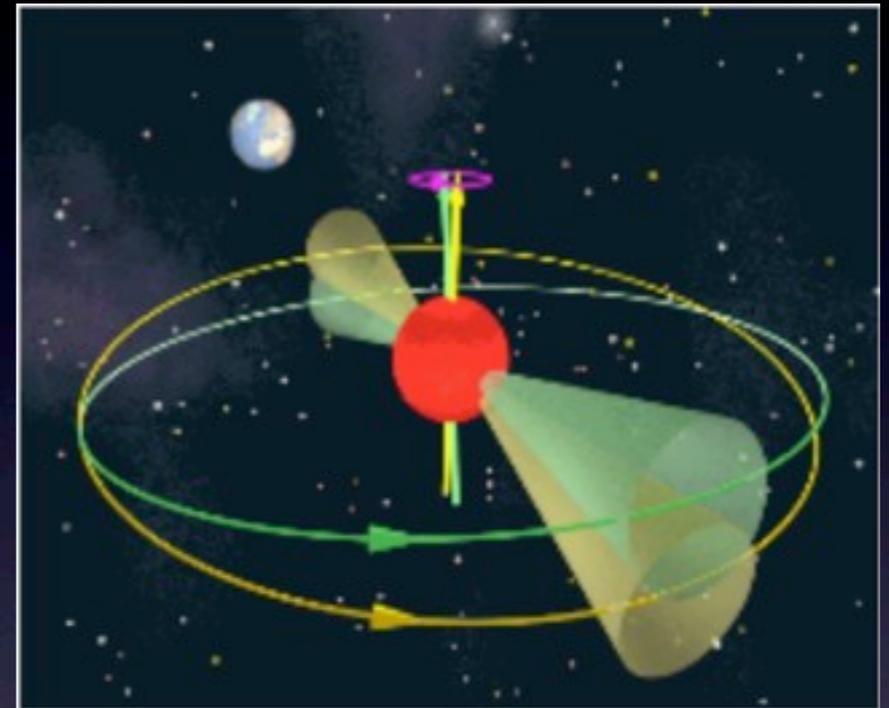
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gravitational ellipticity

Credit: M. Kramer



Credit: Dana Berry



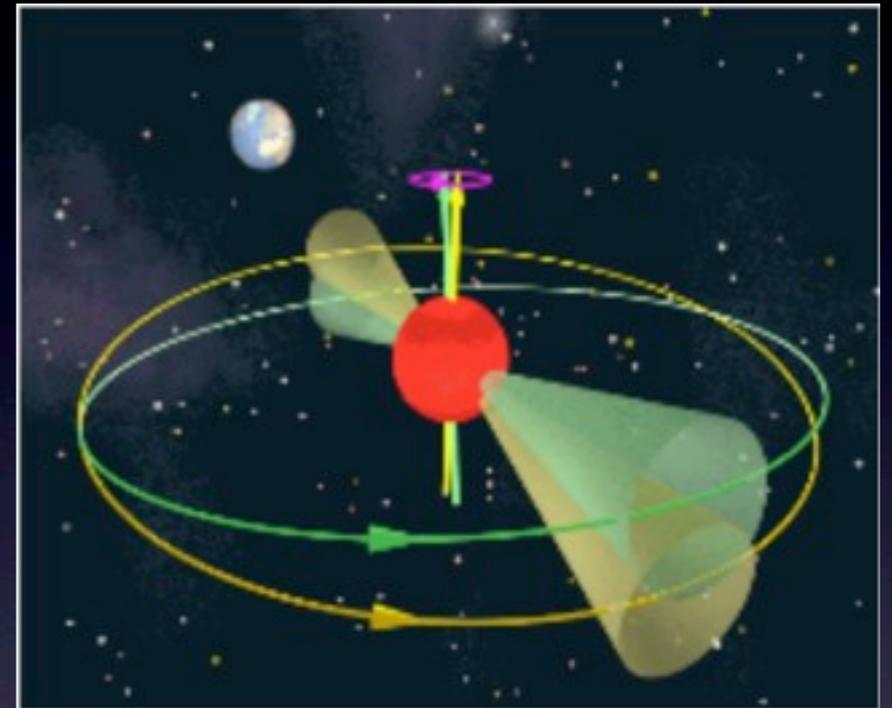
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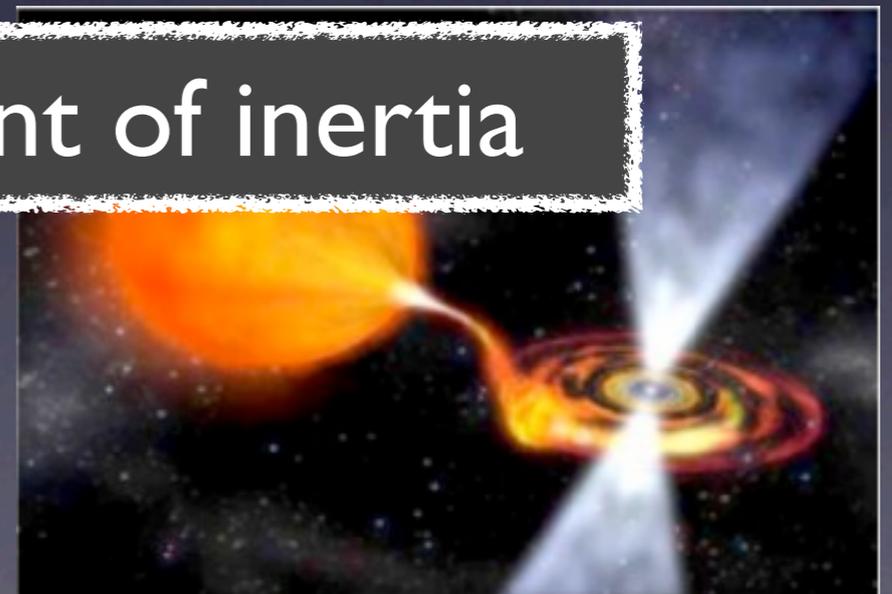
$$h_0 = \frac{16\pi^2 G}{c^4} \frac{I \omega^2}{r}$$

moment of inertia

Credit: M. Kramer



Credit: Dana Berry



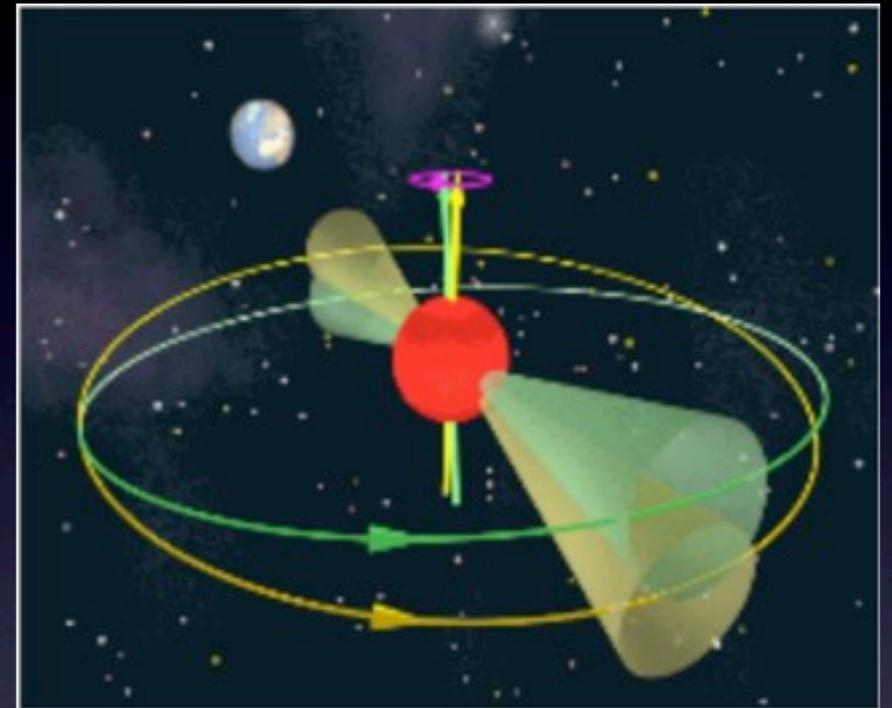
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rotational frequency

Credit: M. Kramer



Credit: Dana Berry

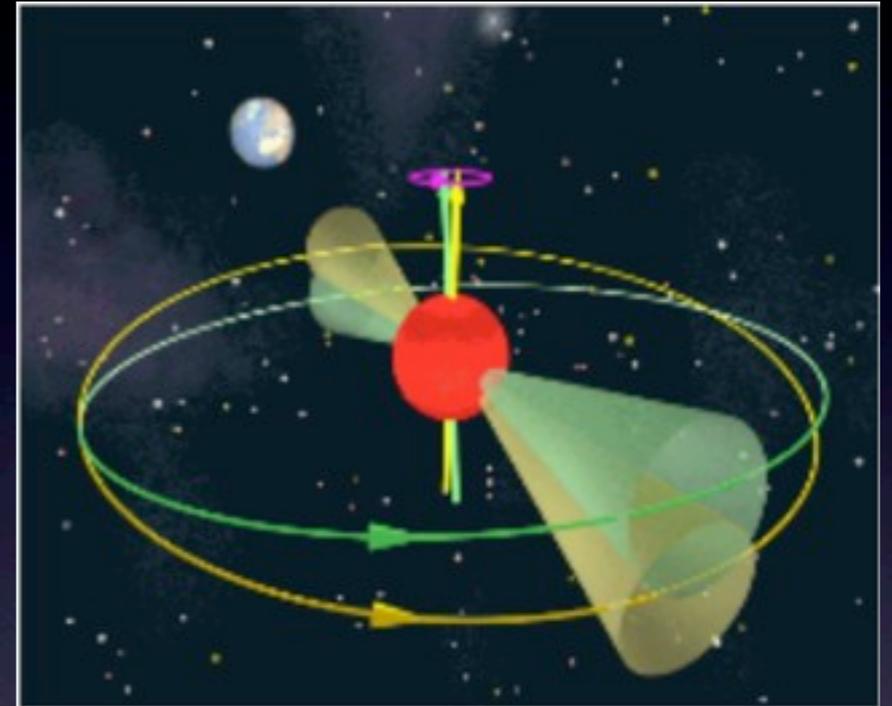


Continuous Signals

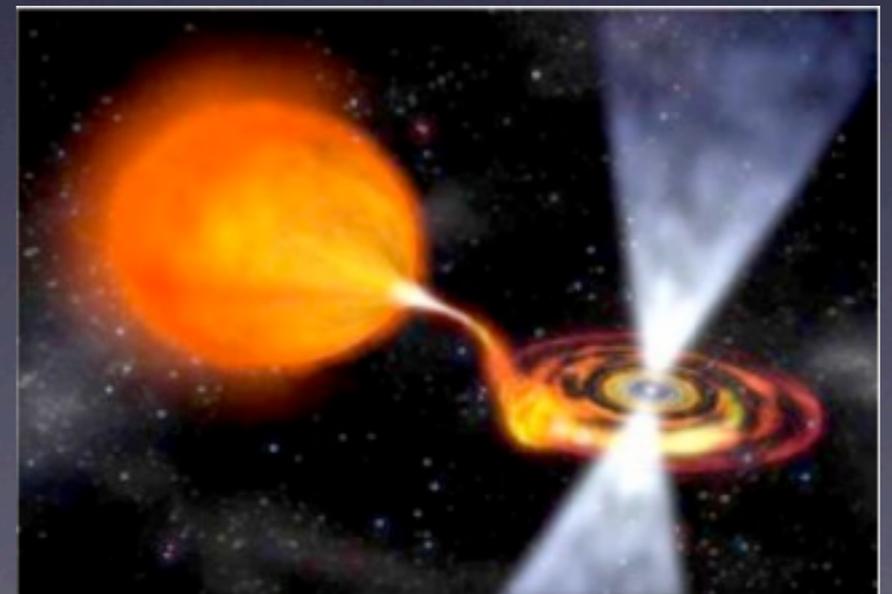
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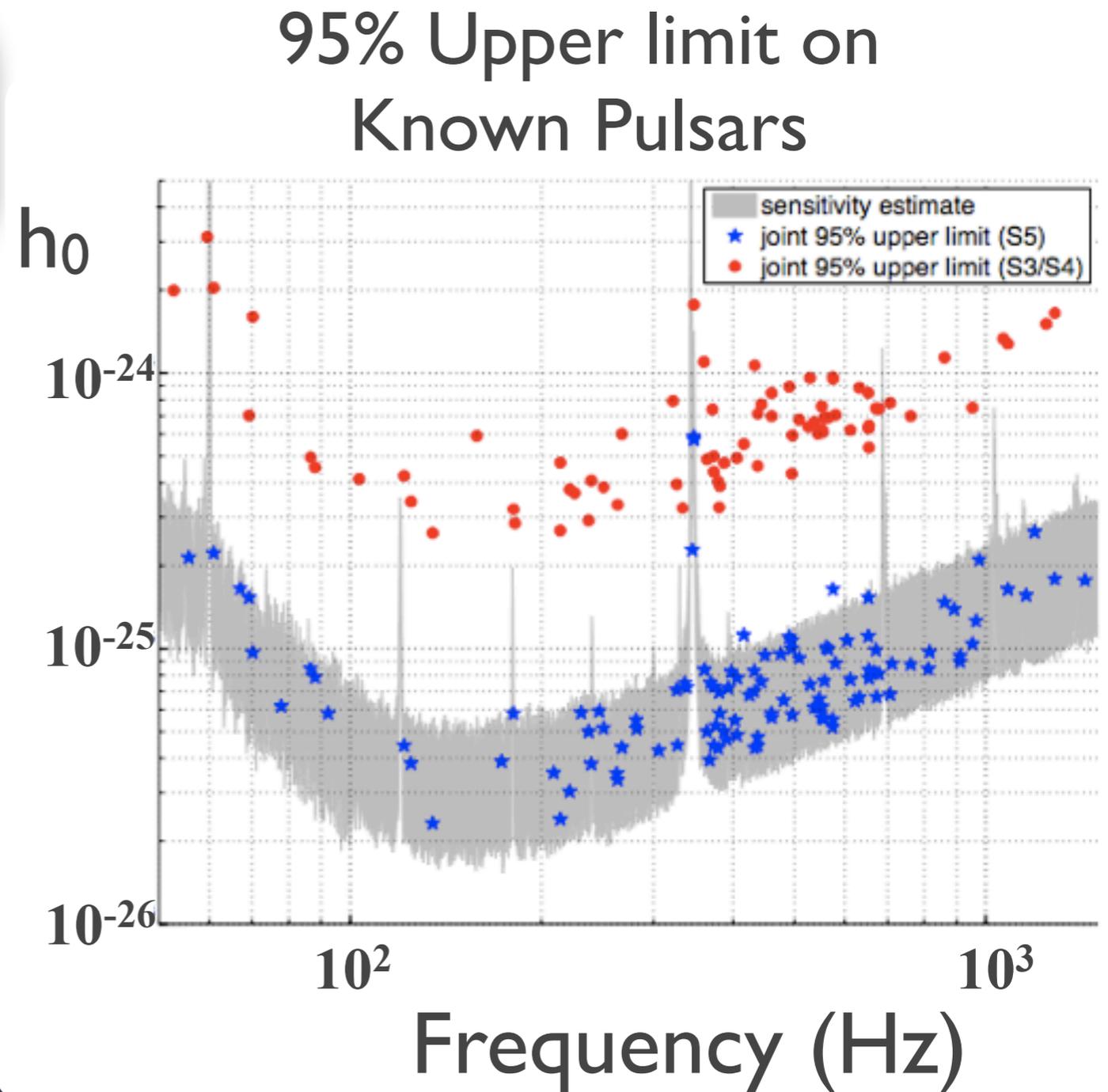
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Searches for continuous waves

No plausible gravitational waves found

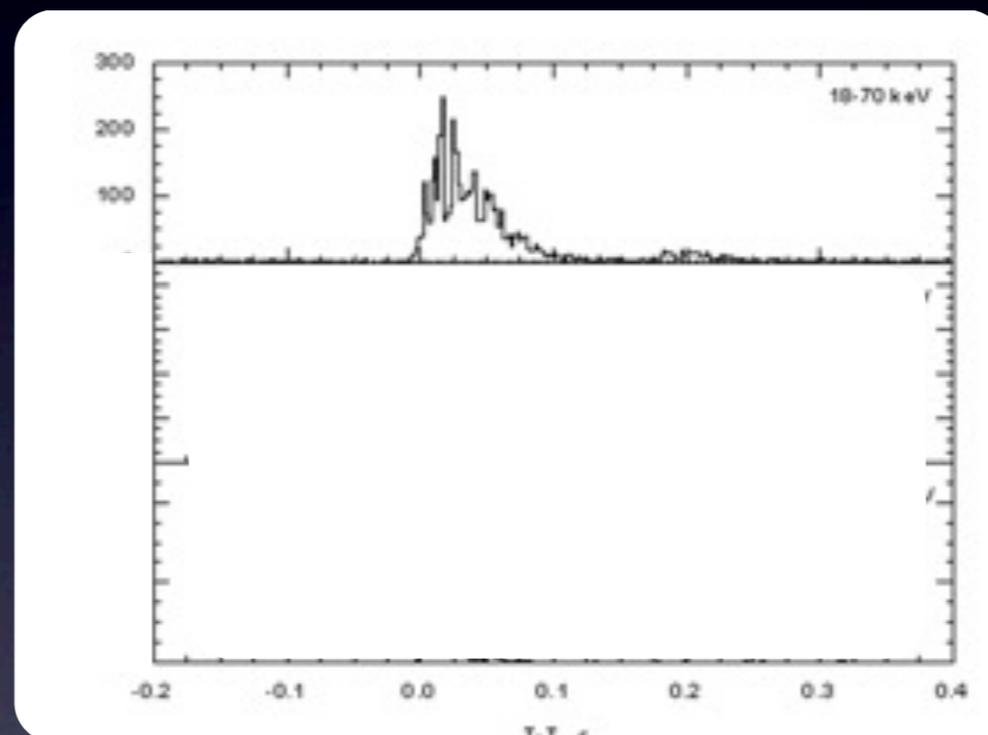
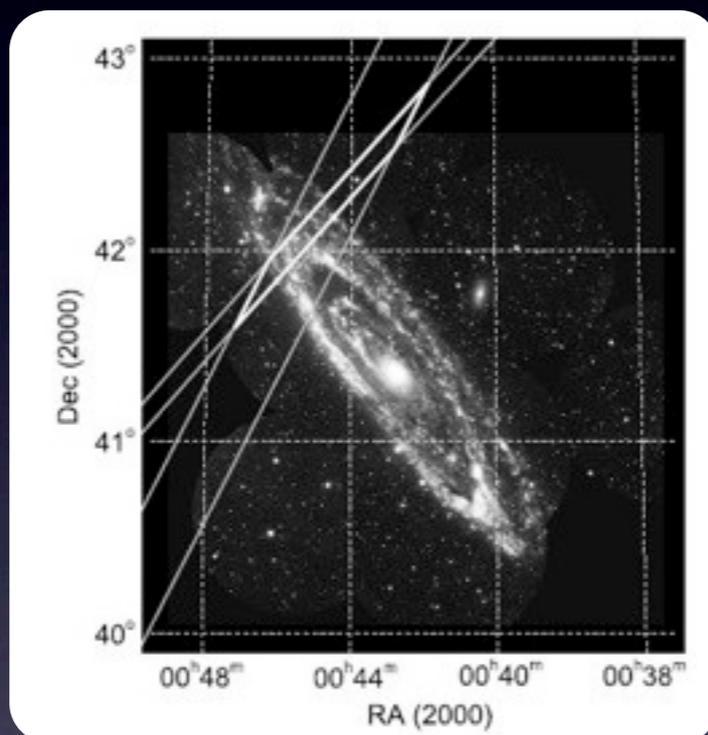
- Strength of gravitational waves depends on gravitational ellipticity
- Radio observations of Crab pulsar spindown constrain maximum gravitational ellipticity around 10^{-3}
- LIGO-Virgo non-detection of gravitational waves constrains gravitational ellipticity of Crab at $\sim 10^{-4}$



LIGO-Virgo, "Searches for gravitational waves from known pulsars with S5 LIGO data," *Astrophys. J.* 713 (2010) 671 [arXiv:0909.3583]

GW Astronomy

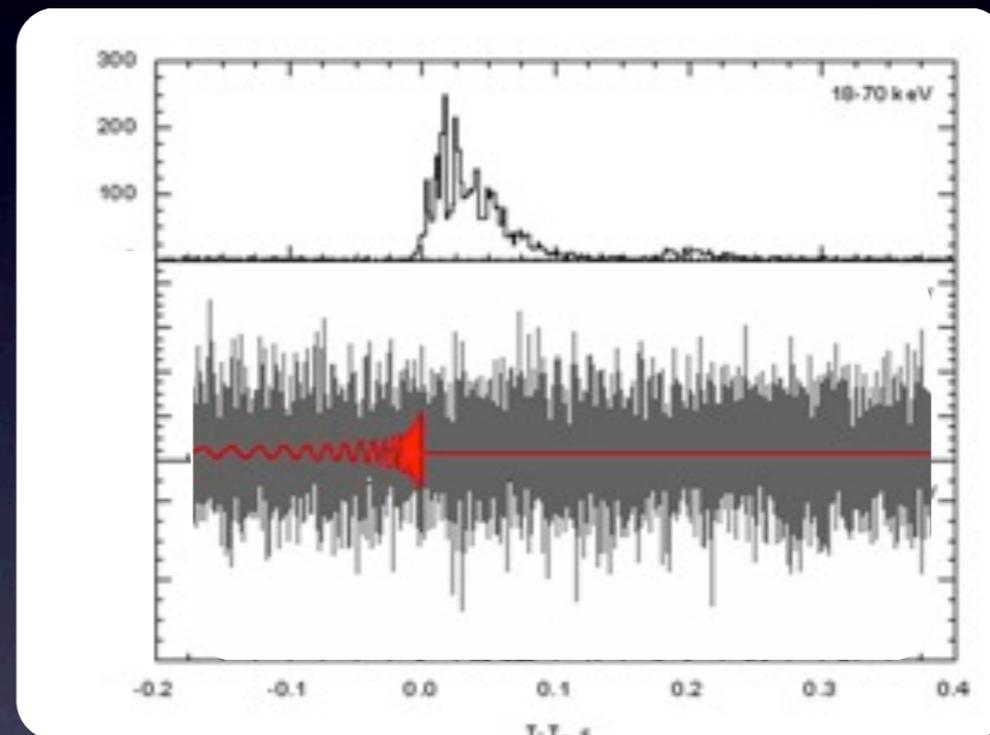
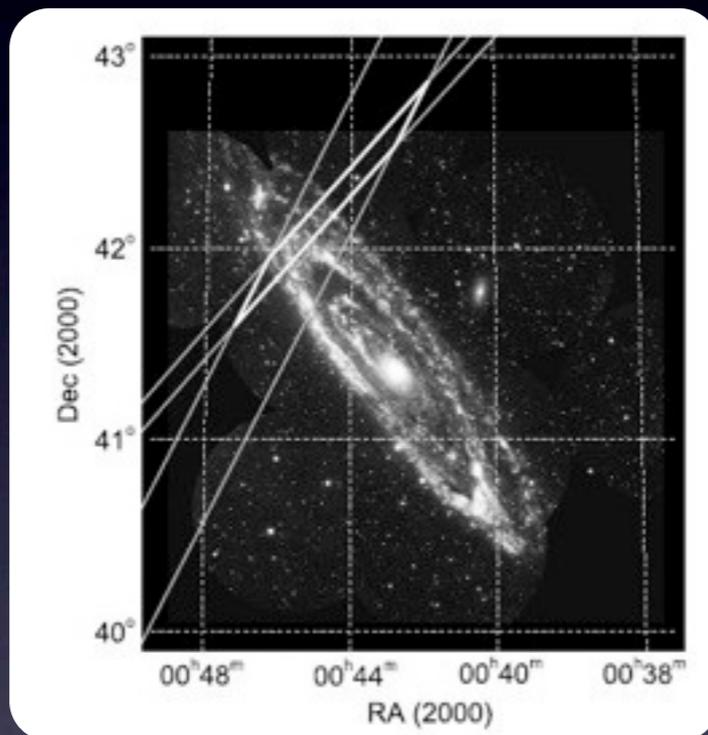
Trying to add a soundtrack to astronomical events



- Soft-gamma Repeaters. LSC, Phys. Rev. D 76 (2007) 062003 [astro-ph/0703419]; Astrophys. J. 701 (2009) L68-L74. [arXiv:0905.0005]
- Gamma-ray Bursts. LSC, Phys. Rev. D 77 (2008) 062004 [arXiv:0709.0766]; Astrophys. J. 681 (2008) 1419 [arXiv:0711.1163].
- Gamma-ray Bursts. LIGO-Virgo, Astrophys. J. 715 (2010) 1438 [arXiv:0908.3824]; Astrophys. J. 715 (2010) 1453 [arXiv:1001.0165]; Astrophys. J. 760 (2012) 12 [arXiv:1205.2216]

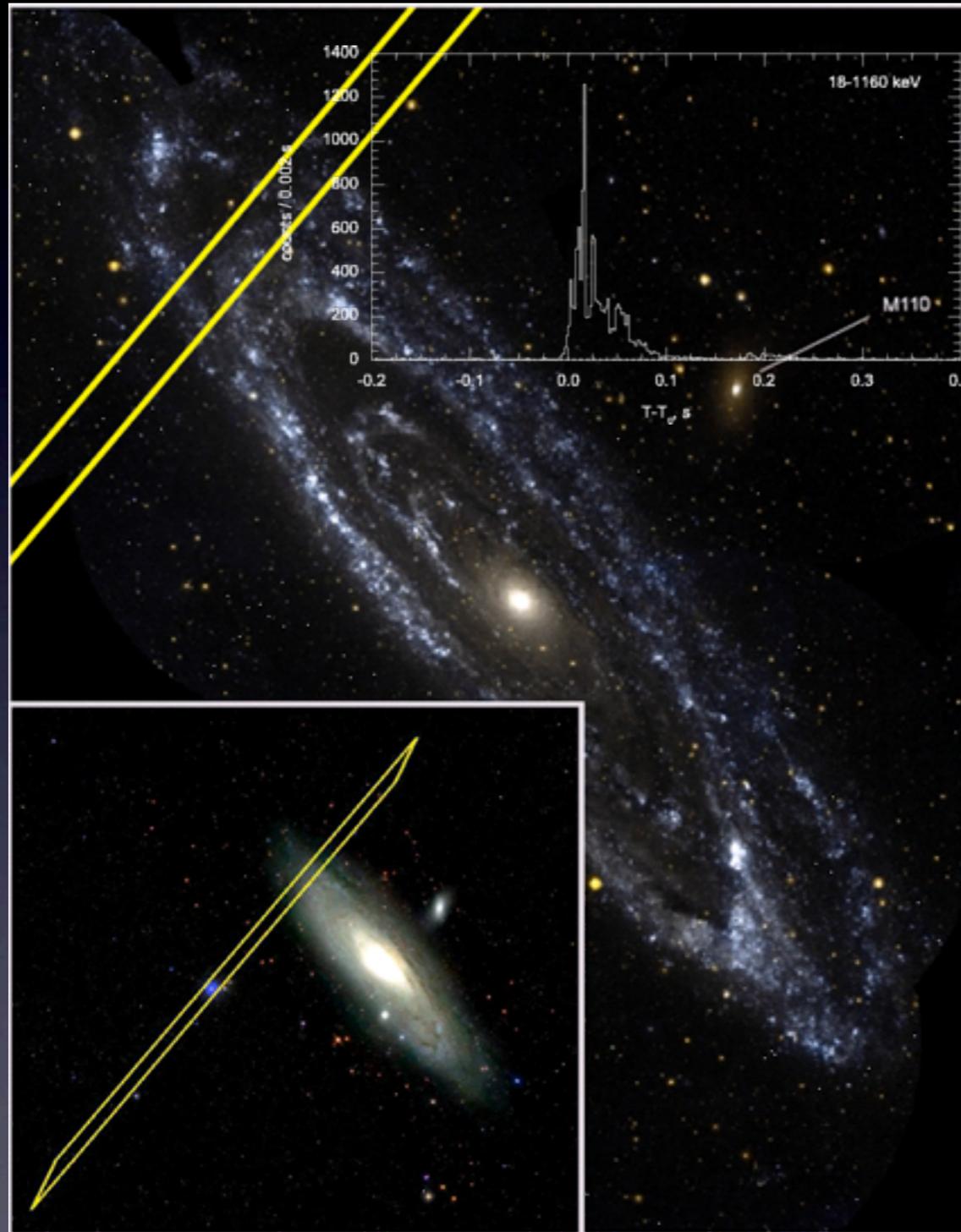
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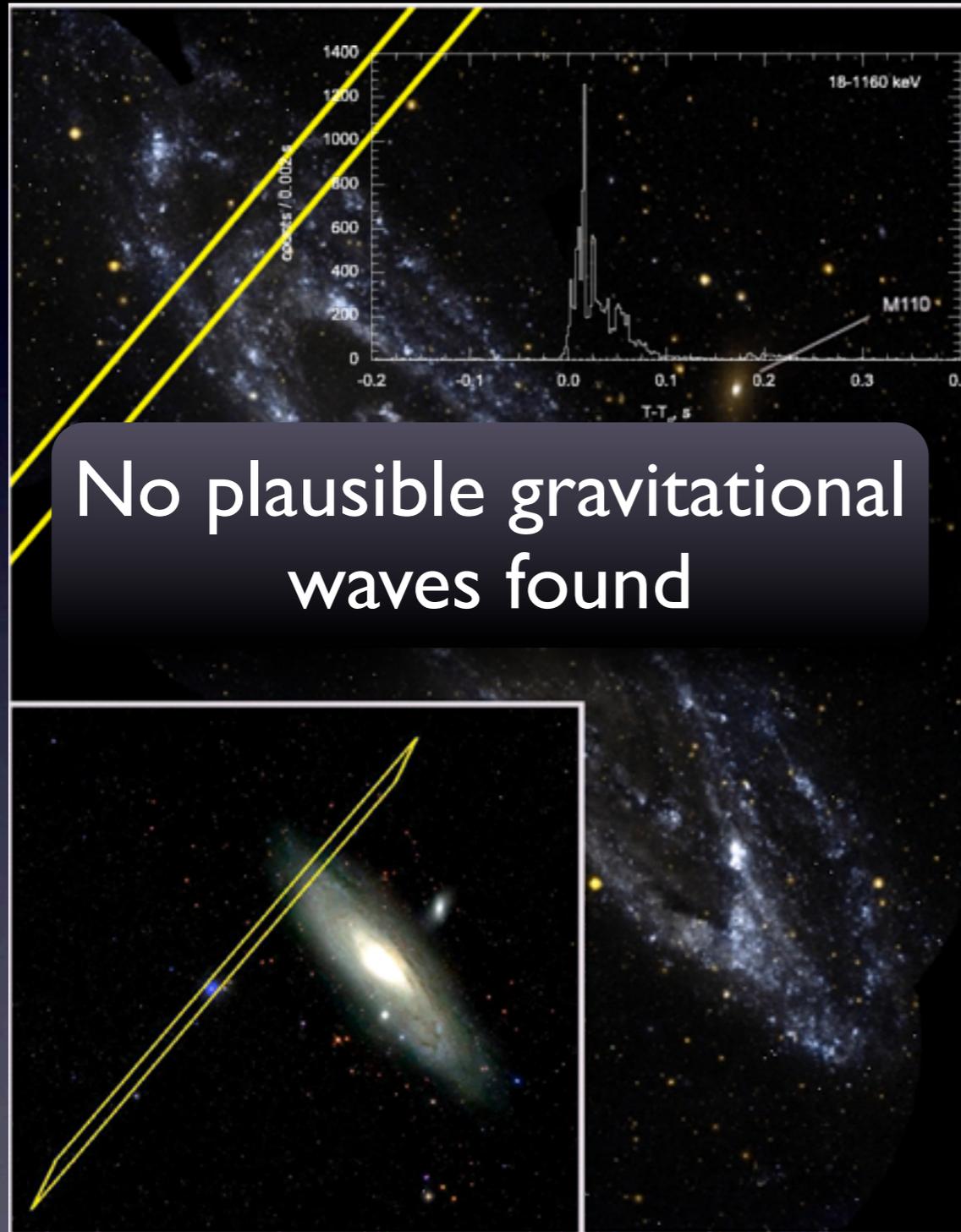
Example: GRB 070201



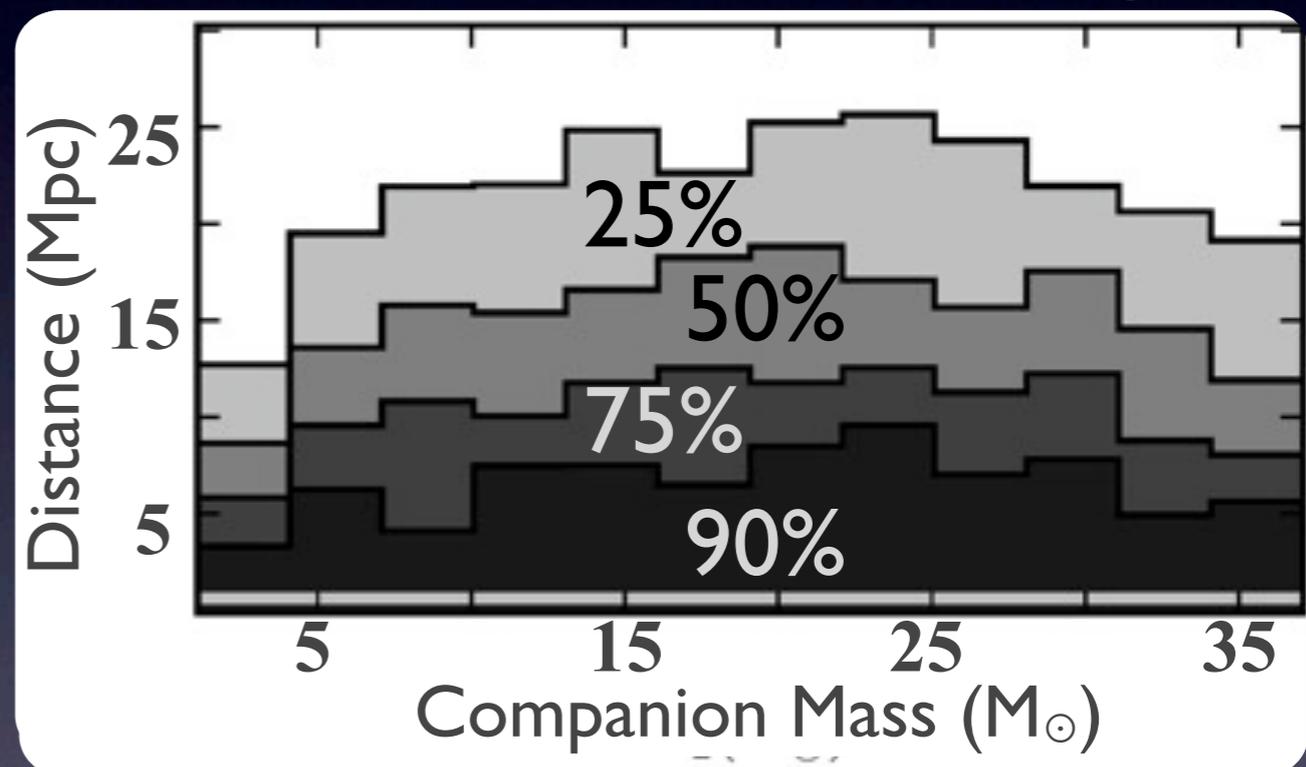
- Short gamma-ray burst
- Interplanetary Network error box included M₃₁ at ~700 kpc!

- Ruled out compact binary progenitor in M31, but could not rule out SGR.

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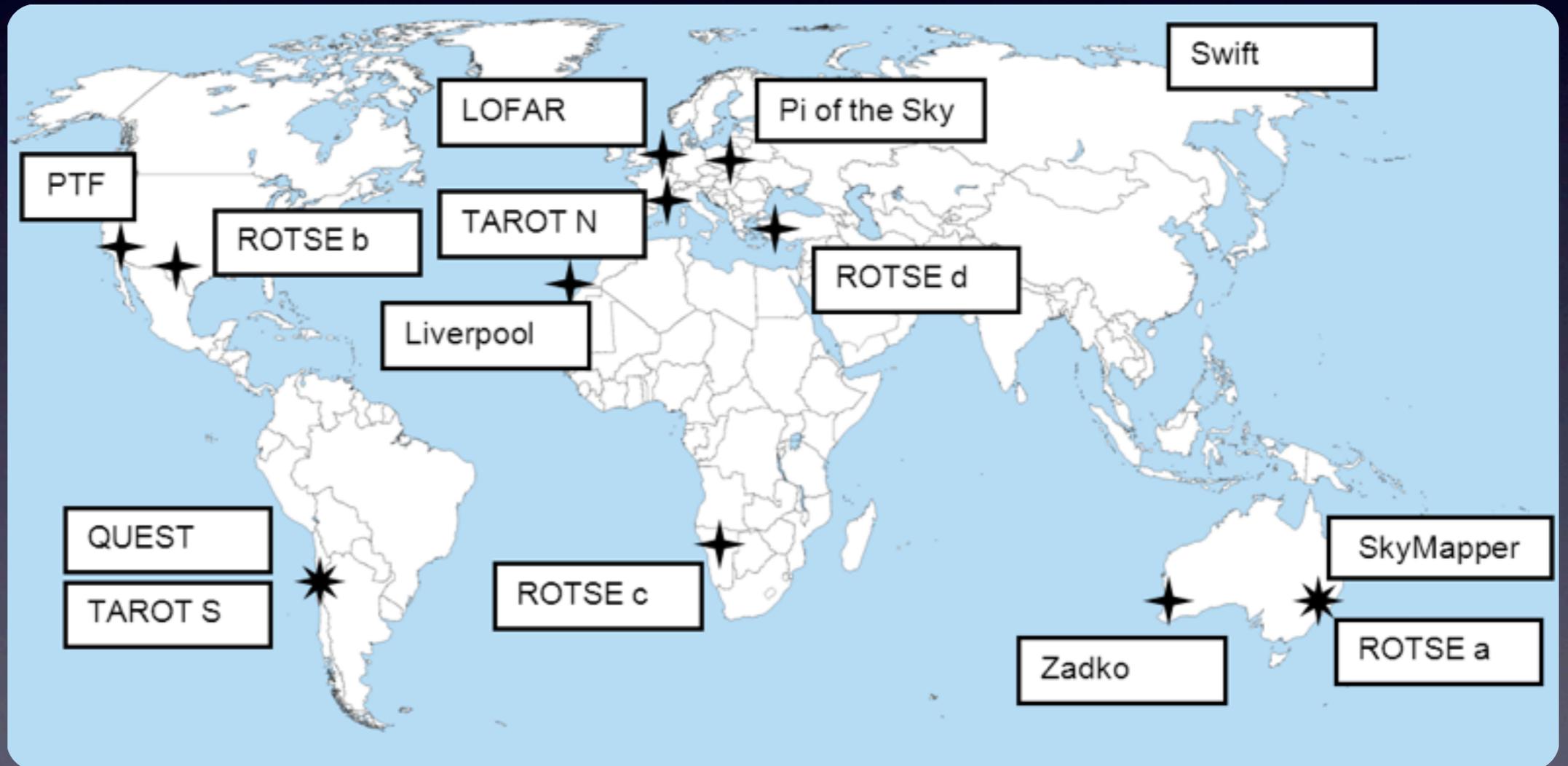
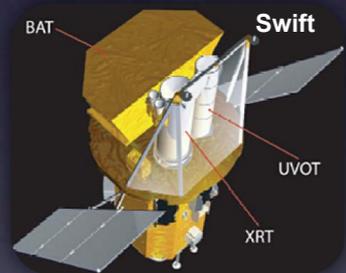
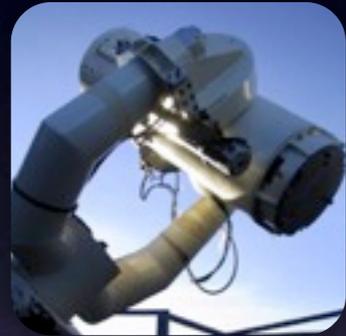


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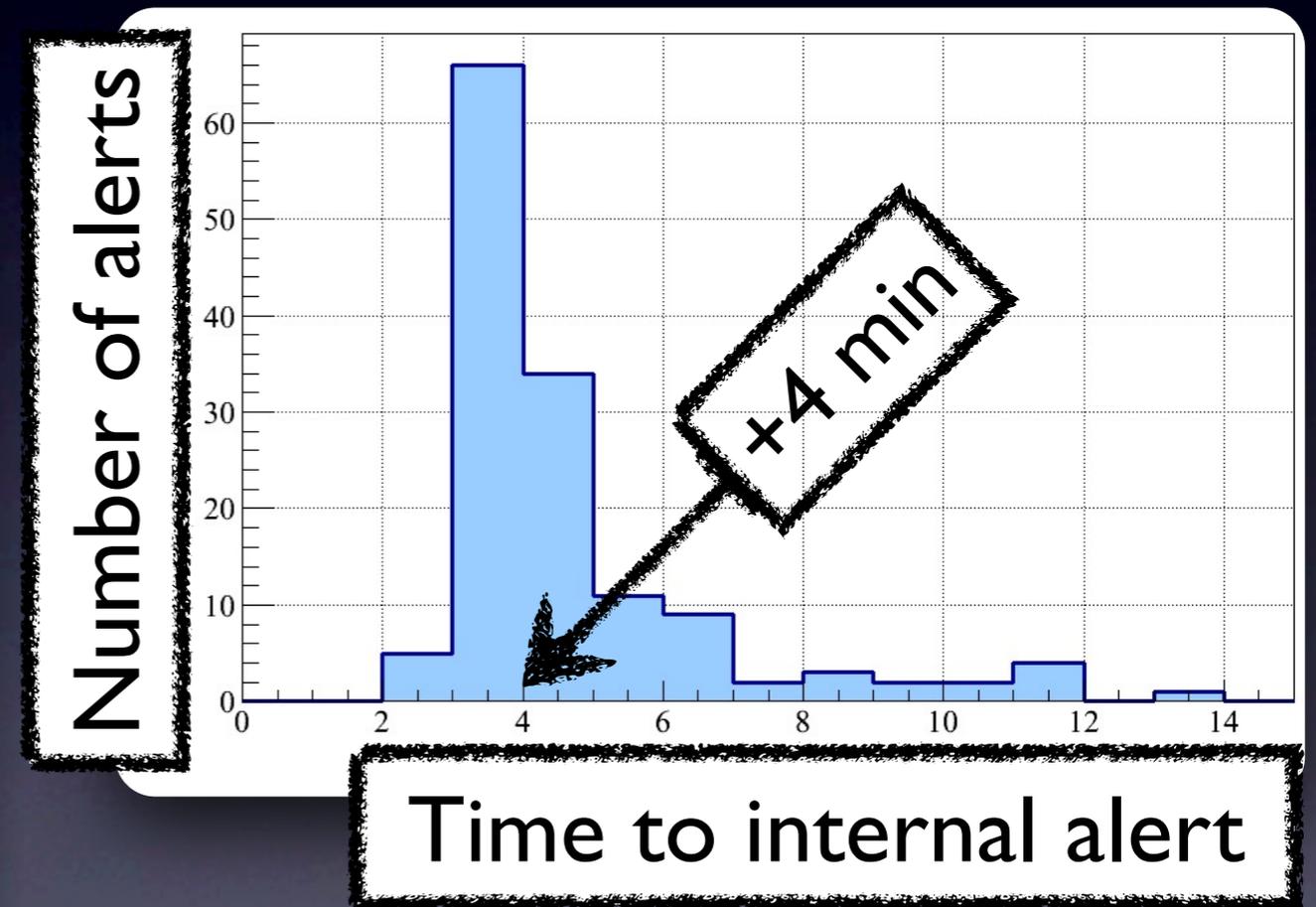
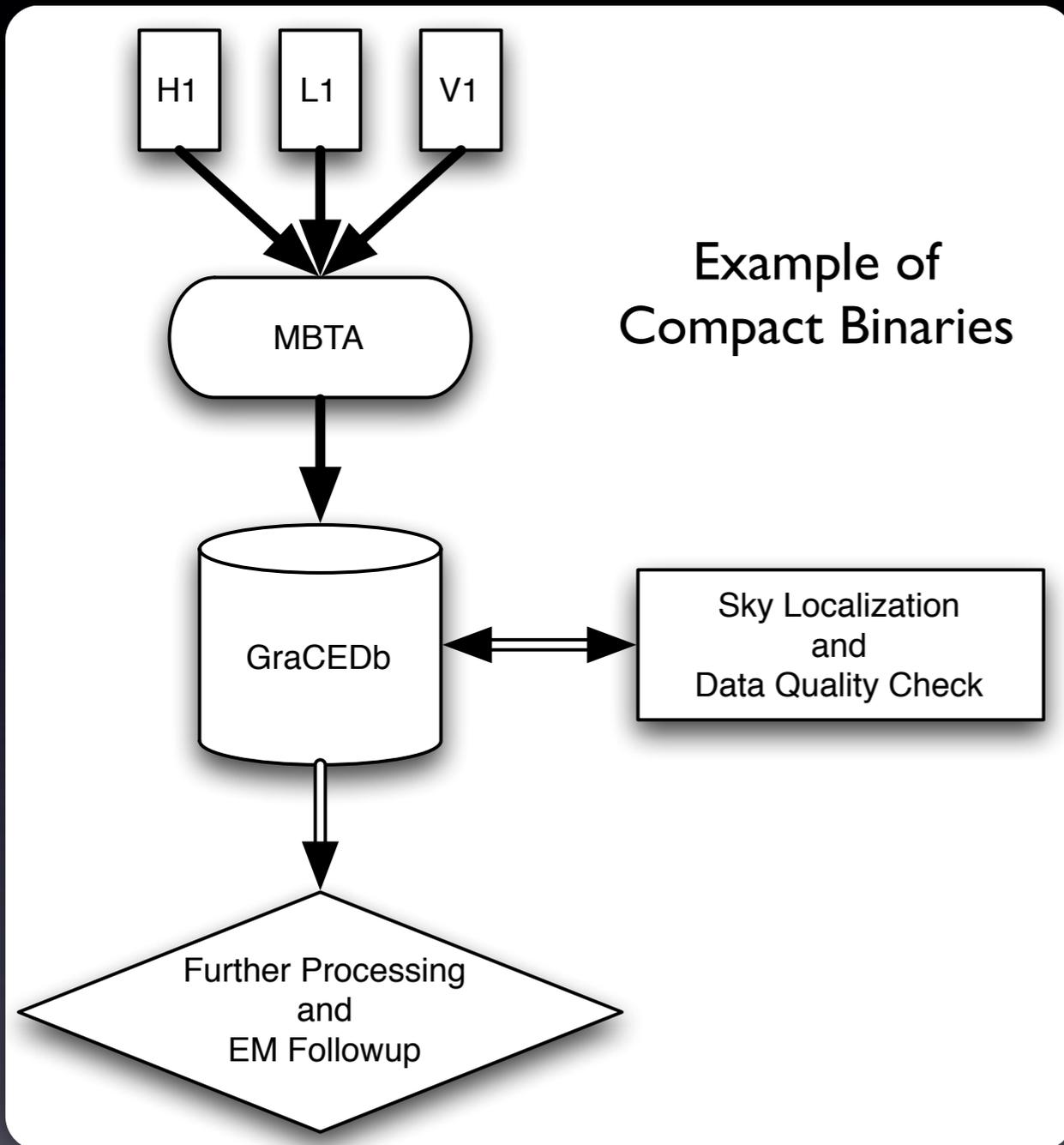
LSC. "Implications for the Origin of GRB 070201 from LIGO Observations", *Ap.J.*, 681:1419–1430 (2008). [arXiv:0711.1163](https://arxiv.org/abs/0711.1163)

Connecting GW and EM observations

- LIGO-Virgo partners for the S6/VSR2/VSR3 science runs

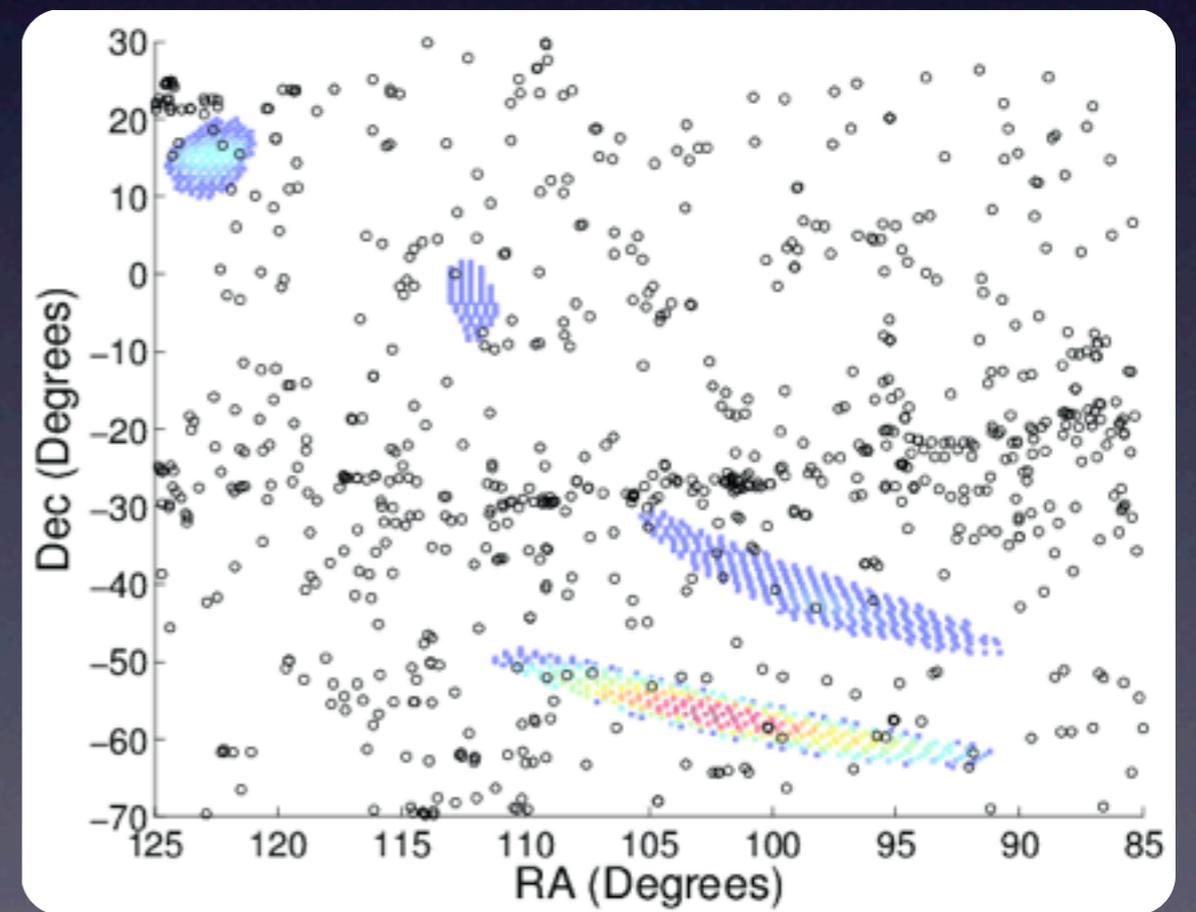
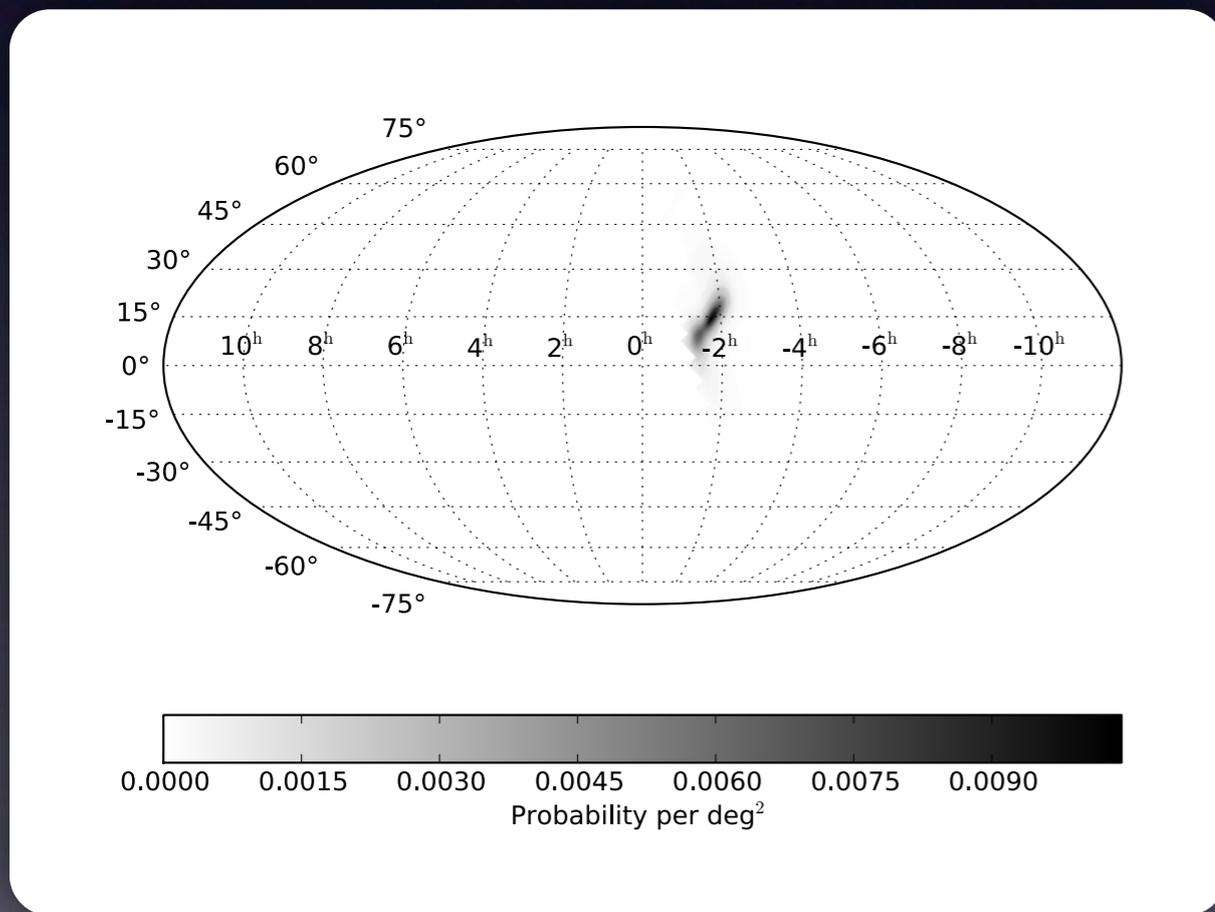


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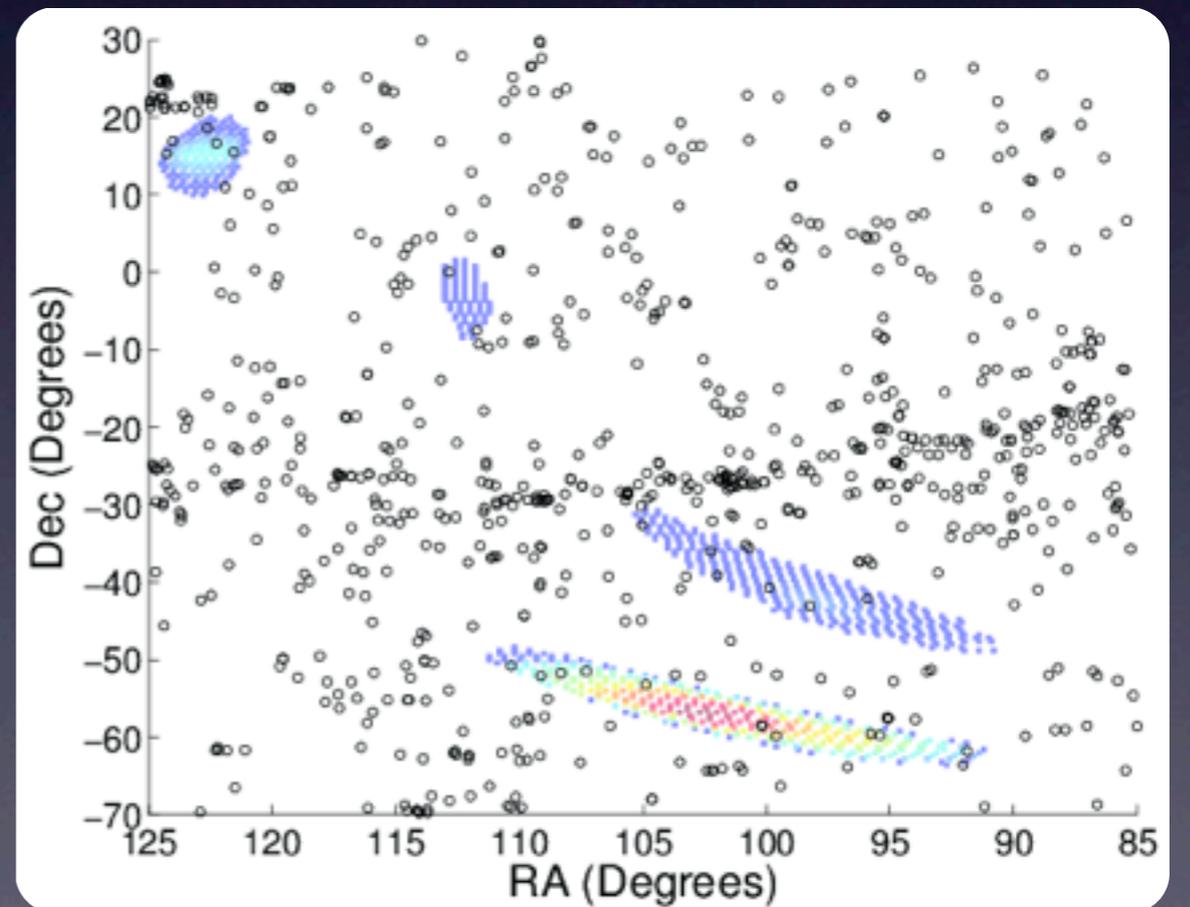
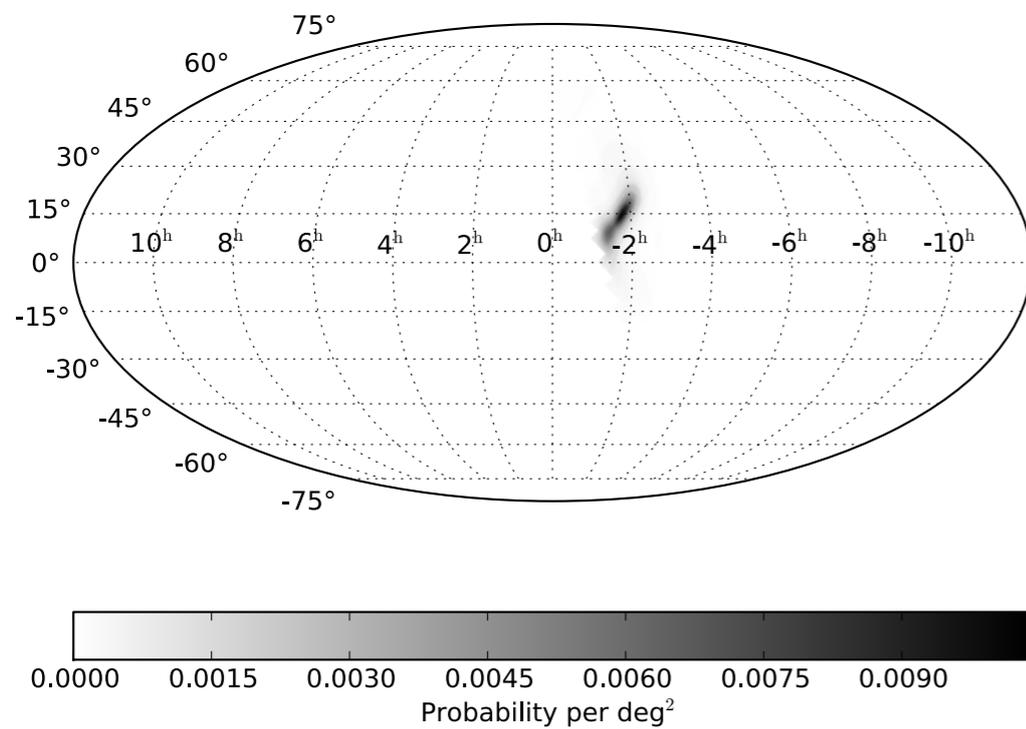
+45min

Sky Maps



Sky Maps

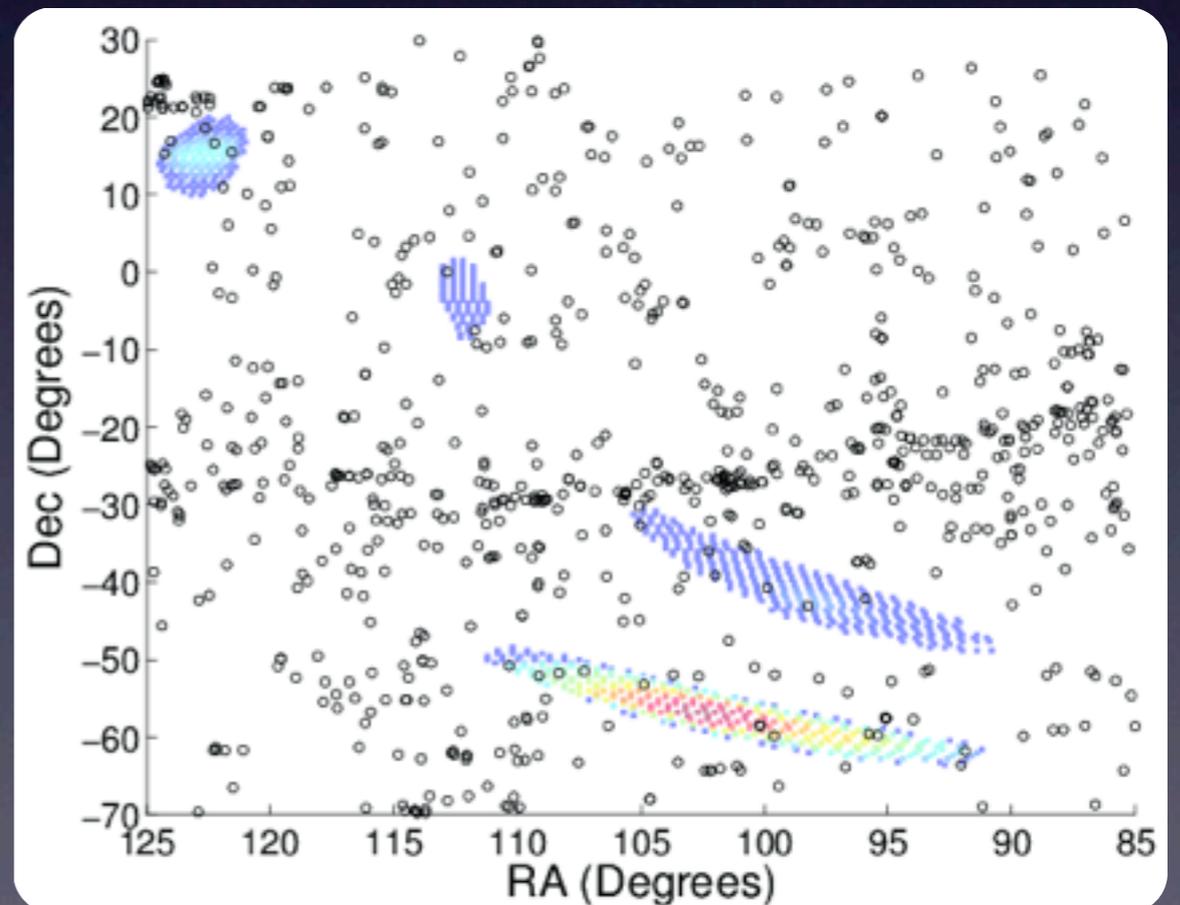
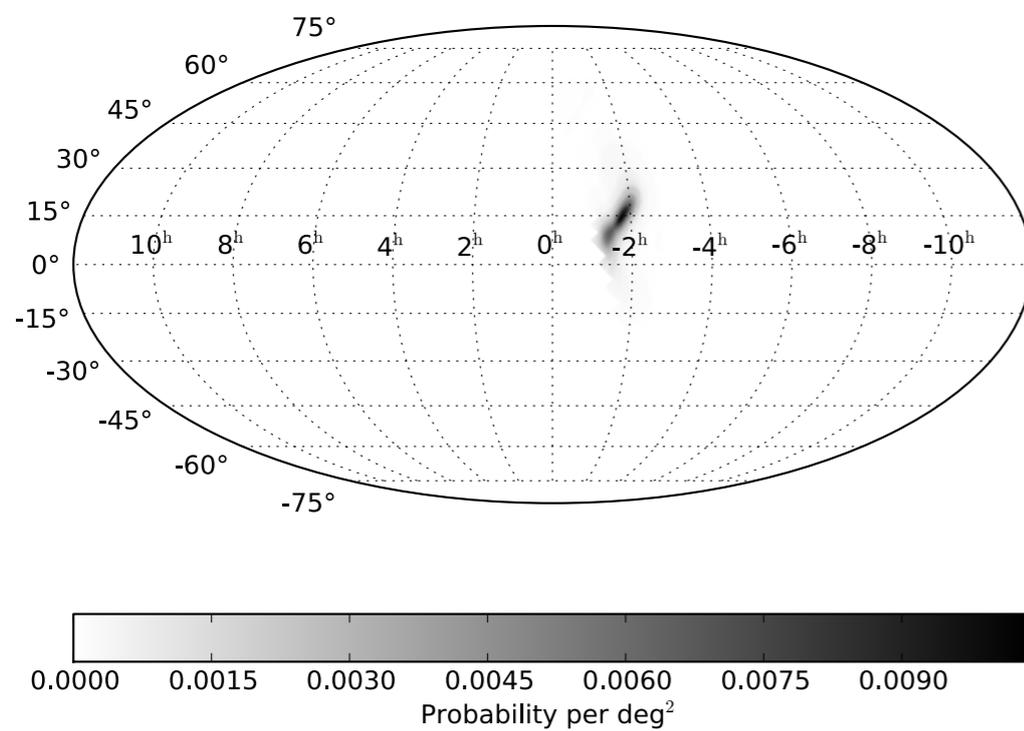
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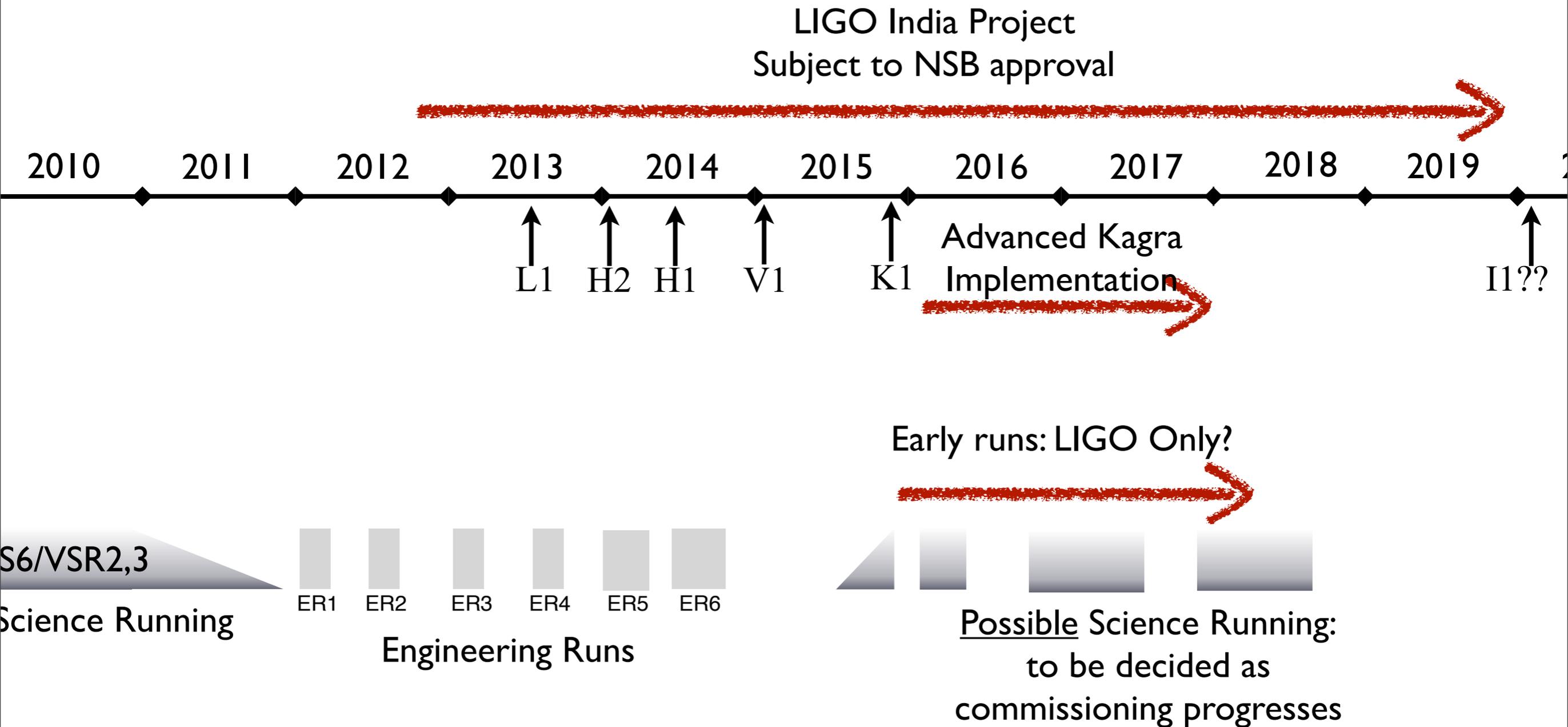
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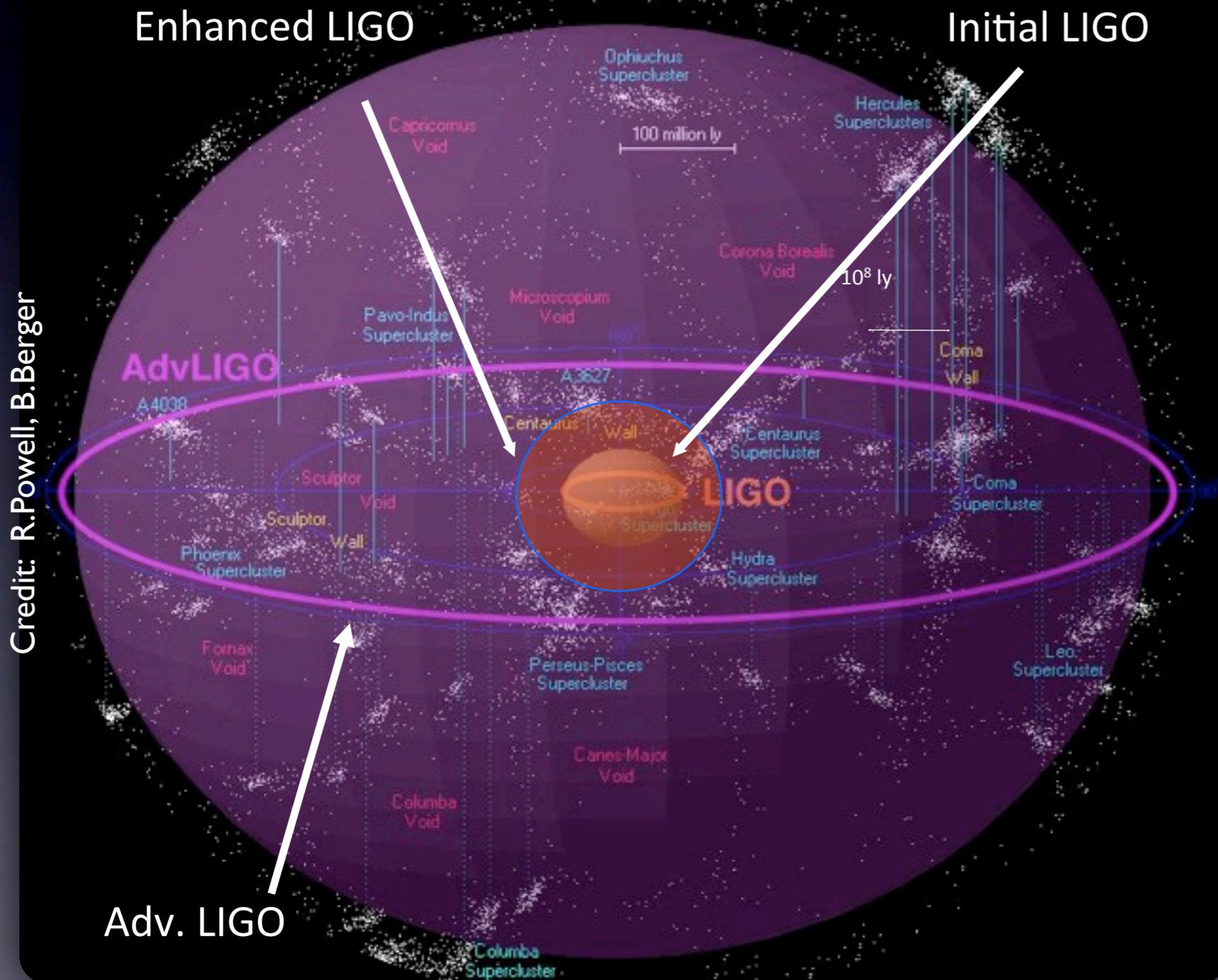
Analysis of EM data forthcoming



Tentative Timing



Looking forward to 2016



Credit: R.Powell, B.Berger

- Advanced LIGO
- project in full swing
- acceptance 2014/15
- 10 x Initial LIGO
- 1000 x more sources
- 40 BNS per year