Universal Ideas from Microstate Geometries

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Based on Collaborations with:

I. Bena, J. de Boer, G. Gibbons, B. Niehoff, M. Shigemori, O. Vasilakis arXiv:1305.0957 and arXiv:1311.4538

<u>Outline</u>

- Motivation for Microstate Geometries
- Solitons, horizonless solutions and topology
 <u>Microstate geometries as solitons</u>
- Lessons from holographic field theory
 - Two new scales for black-hole physics
- Microstate geometries and microstate structure
- BPS Microstate structure visible within supergravity - The superstratum
- Current status + Speculative ideas...

Information Loss via Hawking Radiation

Particle creation near horizon of black hole





After black-hole light-crossing time

$$|\psi\rangle = \frac{1}{\sqrt{2}} (|0\rangle_{BH} \otimes |0\rangle_{\infty} + |1\rangle_{BH} \otimes |1\rangle_{\infty})$$

State of quantum of Hawking Radiation

$$\rho = \operatorname{Tr}_{BH}(|\psi\rangle\langle\psi|) = \frac{1}{2}(_{\infty}|0\rangle\langle0|_{\infty} + _{\infty}|1\rangle\langle1|_{\infty})$$

Entanglement entropy of N Hawking quanta: = $N \log(2)$

After black hole fully evaporates:



Cannot be described by unitary evolution in Quantum Mechanics

An old conceit:

Fix the information problem with small corrections to GR?

e.g. via stringy or quantum gravity ((*Riemann*)ⁿ) corrections to radiation? Entangled State of Hawking Radiation

$$\begin{split} |\Psi\rangle &= \frac{1}{\sqrt{2}} \left(|0\rangle_{_{\rm BH}} \otimes |0\rangle_{_{\rm CO}} + |1\rangle_{_{\rm BH}} \otimes |1\rangle_{_{\rm OO}} \right) \\ &+ \varepsilon \left(|0\rangle_{_{\rm BH}} \otimes |0\rangle_{_{\rm OO}} - |1\rangle_{_{\rm BH}} \otimes |1\rangle_{_{\rm OO}} \right) + \varepsilon_{_{1}} |0\rangle_{_{\rm BH}} \otimes |1\rangle_{_{\rm OO}} + \varepsilon_{_{2}} |1\rangle_{_{\rm BH}} \otimes |0\rangle_{_{\rm OO}} \end{split}$$

Hawking evaporation is extremely slow ...

$$\frac{t_{evap}}{\hbar c^4} = \frac{5120 \,\pi \, G^2 \, M^3}{\hbar \, c^4} \approx 6.6 \times 10^{74} \, \left(\frac{M}{M_\odot}\right)^3 \, s \, \approx \, 2.1 \times 10^{67} \, \left(\frac{M}{M_\odot}\right)^3 \, years$$

Restore the pure state over vast time period for evaporation?

Mathur (2009): No! Corrections cannot be small for information recovery

 \Rightarrow There must be O(1) changes to the Hawking states at the horizon.

Resolving Black Holes

There must be new O(1) physics at the horizon scale

Fuzzballs



A mechanism for resolving the problem in string theory <u>Firewalls</u>

FIRST LAW OF FIREWALL PHYSICS ...



Unsupported superstructure

Unitary Evolution and Black Holes

Earliest motivation from AdS/CFT:



What this should involve ...



- Smooth geometry
- Finite red shift
- Fluxes + geometric moduli ٠

Order parameter(s); Energy Gap

Microstate geometries \Rightarrow

Microstate Geometry Program

Find mechanisms and structures that resolve singularities and prevent the formation of horizons in the low-energy (*massless*) limit of string theory: Supergravity

- Stringy resolutions on horizon scale ⇒ Very long-range effects ⇒
 Massless fields (only other scale in String theory is the Planck scale)
- Massless sector means before any compactification scale is introduced

Definition

- Solution to the bosonic sector of supergravity as a low-energy limit of string theory
- Smooth, horizonless solutions with the same asymptotic structure as a given black hole or black ring

Singularity resolved; Horizon removed



Are there horizonless, smooth solitons in supergravity?

The Komar Mass/Smarr Formula

If there is time-translation invariance then energy is conserved: There is a vector field (Killing vector) K generating time translations.

$$\frac{K^{\mu}}{\partial x^{\mu}} = \frac{\partial}{\partial t}$$

D-dimensional space-time, sectioned by hypersurfaces, Σ , with Gaussian (D-2)-spheres, S^{D-2} , at infinity



There is then an associated conserved ADM mass:

$$\frac{K^{\mu}K^{\nu}g_{\mu\nu}}{M^{\nu}} = g_{00} \approx -1 + \frac{16\pi G_D}{(D-2)A_{D-2}}\frac{M}{\rho^{D-3}} + \dots$$
 at infinity

Moreover

$$d * d\mathbf{K} = -2 * (\mathbf{K}^{\mu} \mathbf{R}_{\mu\nu} dx^{\nu}) \qquad \mathbf{R}_{\mu\nu} = 8\pi G_D \left(\mathbf{T}_{\mu\nu} - \frac{1}{(D-2)} \mathbf{T} g_{\mu\nu} \right)$$

If Σ is smooth with no interior boundaries:

$$M = -\frac{1}{16\pi G_D} \frac{(D-2)}{(D-3)} \int_{S^{D-2}} *dK = \int_{\Sigma} T_{00} d\Sigma$$

No Solitons without Horizons via the Smarr Formula

$$M = \frac{1}{8\pi G_D} \frac{(D-2)}{(D-3)} \int_{\Sigma} *_D \left(\frac{K^{\mu} R_{\mu\nu} dx^{\nu}}{D} \right)$$

Strategy:

Assume time-independent matter as well as time-independent metric

Equations of motion for massless field theory

$$\Rightarrow \quad *(K^{\mu}R_{\mu\nu}dx^{\nu}) = d(\gamma_{D-2}) \quad \text{for some global (D-2)-form, } \gamma.$$

$$\Rightarrow \quad \mathsf{M} \equiv \mathbf{0}$$

 \Rightarrow Space-time can only be globally flat, $\mathbb{R}^{D-1,1}$

<u>Intuition</u>: Massless fields travel at the speed of light ... only a black hole can hold such things into a star.

How do you show that: $*(K^{\mu}R_{\mu\nu}dx^{\nu}) = d(\gamma_{D-2})$?

Bosonic sector of a generic massless (ungauged) supergravity

• Graviton, $g_{\mu\nu}$ • Scalars, Φ^A • Tensor gauge fields, $F_{(p)}^{K}$ Scalar matrices in kinetic terms: $Q_{JK}(\Phi)$, $M_{AB}(\Phi)$ Bianchi: $d(F_{(p)}^{K}) = 0$ Equations of motion: $d*(Q_{JK}(\Phi) F_{(p)}^{K}) = 0$ Ignoring Chern Simons terms <u>Define</u>: $G_{J,(D-p)} \equiv *(Q_{JK}(\Phi) F_{(p)}^{K})$ and Q^{JK} by $Q^{IK} Q_{KJ} = \delta^{I}_{J}$ then: $d(F_{(p)}^{K}) = 0$ and $d(G_{J,(D-p)}) = 0$ Ignoring Chern Simons terms

Einstein equations:

$$R_{\mu\nu} = Q_{IJ} \left[F^{I}_{\mu\rho_{1}...\rho_{p-1}} F^{J}_{\nu}{}^{\rho_{1}...\rho_{p-1}} - c g_{\mu\nu} F^{I}_{\rho_{1}...\rho_{p}} F^{J\rho_{1}...\rho_{p}} \right] + M_{AB} \left[\partial_{\mu} \Phi^{A} \partial_{\nu} \Phi^{B} \right] = a Q_{IJ} F^{I}_{\mu\rho_{1}...\rho_{p-1}} F^{J}_{\nu}{}^{\rho_{1}...\rho_{p-1}} + M_{AB} \left[\partial_{\mu} \Phi^{A} \partial_{\nu} \Phi^{B} \right] + b Q^{IJ} G_{I \mu\rho_{1}...\rho_{D-p-1}} G_{J\nu}{}^{\rho_{1}...\rho_{D-p-1}}$$
for some constants a.b and c

<u>Time Independent Solutions</u>

Killing vector, K, is time-like at infinity

Assume time-independent matter:

Assume time-independent matter:

$$\mathcal{L}_{K}F^{I} = 0, \quad \mathcal{L}_{K}\Phi^{A} = 0$$

$$\Rightarrow \quad \mathcal{L}_{K}G_{I} = 0$$

$$K^{\mu}R_{\mu\nu} = a Q_{IJ}K^{\mu}F^{I}_{\mu\rho_{1}\dots\rho_{p-1}}F^{J}_{\nu}{}^{\rho_{1}\dots\rho_{p-1}} + M_{AB}\left[K^{\mu}\partial_{\mu}\Phi^{A}\partial_{\nu}\Phi^{B}\right]$$

$$+ \ b \, Q^{IJ} \, K^{\mu} \, G_{I \, \mu \rho_1 \dots \rho_{D-p-1}} \, G_{J \, \nu} \, {}^{\rho_1 \dots \rho_{D-p-1}}$$

•
$$\mathcal{L}_{K}\Phi^{A} = 0 \iff K^{\mu}\partial_{\mu}\Phi^{A} = 0 \Rightarrow$$
 Scalars drop out of $R_{\mu\nu}K^{\mu}$

- Cartan formula for forms: $\mathcal{L}_{K}\omega \stackrel{\mathbf{0}}{=} d(i_{K}(\omega)) + i_{K}(d\omega)$ $d(F_{(p)}) = 0, \ d(G_{|,(D-p)}) = 0 \implies d(i_{K}(F_{(p)})) = 0, \ d(i_{K}(G_{|,(D-p)})) = 0$
- Ignore topology: $i_{\mathbf{K}}(\mathbf{F}_{(p)}) = d\boldsymbol{\alpha}_{(p-2)}$, $i_{\mathbf{K}}(\mathbf{G}_{|,(D-p)}) = d\boldsymbol{\beta}_{|,(D-p-2)}$
- Define (D-2)-form, $\gamma_{D-2} = a \alpha_{(p-2)} \wedge G_{J,(D-p)} + b \beta_{J,(D-p-2)} \wedge F_{(p)}^{J}$ Then: $*(K^{\mu}R_{\mu\nu}dx^{\nu}) = d(\gamma_{D-2})$

 \Rightarrow M = 0 \Rightarrow "No Solitons Without Horizons"

Omissions:

- Chern-Simons terms
- Topology

Equations of motion in generic massless supergravity:

$$d*(Q_{JK}(\Phi) F_{(p)}^{K}) = Chern-Simons terms$$

$$\Rightarrow d(G_{J,(D-p)}) = Chern-Simons terms$$

$$\Rightarrow *(K^{\mu}R_{\mu\nu}dx^{\nu}) = d(\gamma_{D-2}) + Chern-Simons terms$$

 $i_{\mathbf{K}}(\mathbf{F}_{(p)}) \neq d\boldsymbol{\alpha}_{(p-2)}, \quad i_{\mathbf{K}}(\mathbf{G}_{J,(D-p)}) \neq d\boldsymbol{\beta}_{J,(D-p-2)}$

⇒ M ~ Topological contributions + Chern-Simons terms

Five Dimensional Supergravity

N=2 Supergravity coupled to two vector multiplets

Three Maxwell Fields, F^{I} , two scalars, X^{I} , $X^{1}X^{2}X^{3} = 1$

$$S = \int \sqrt{-g} d^{5}x \Big(R - \frac{1}{2} Q_{IJ} F^{I}_{\mu\nu} F^{J\mu\nu} - Q_{IJ} \partial_{\mu} X^{I} \partial^{\mu} X^{J} - \frac{1}{24} C_{IJK} F^{I}_{\mu\nu} F^{J}_{\rho\sigma} A^{K}_{\lambda} \bar{\epsilon}^{\mu\nu\rho\sigma\lambda} \Big)$$
$$Q_{IJ} = \frac{1}{2} \operatorname{diag} \left((X^{1})^{-2}, (X^{2})^{-2}, (X^{3})^{-2} \right)$$

Three forms: $G_{J} \equiv *_{5} (Q_{JK}(X) F^{K})$

Four-dimensional spatial base slices, Σ :

- Assume simply connected \Rightarrow $i_{K}F^{J} = d\lambda^{J}$
- Topology of interest: $H_2(\Sigma, Z) \neq 0$

$$i_{\boldsymbol{K}}(G_I) - \frac{1}{2} C_{IJK} \lambda^J F^K = d\beta_I + H_I^{Harmonic}$$

Chern-Simons terms cancel in the Smarr Formula ...

Only topology contributes via the H_{I} ...

No Solitons without Topology

If Σ is a smooth hypersurface with no interior boundaries

$$M = \frac{3}{16\pi G_5} \int_{\Sigma} K^{\mu} R_{\mu\nu} d\Sigma^{\nu} = \frac{1}{16\pi G_5} \int_{\Sigma} H_J \wedge F^J$$

The mass can be topologically supported by the cohomology $H^2(\Sigma, R)$

Stationary end-state of star held up by topological flux ...

- Black-Hole Microstate?
- A new object: A Topological Star

Only assumed time independence: Not simply for BPS objects

Topological Stars



Smooth 2-cycles threaded by fluxes

 $\sigma_a^J = \int_{\Lambda} F^J$

 $\widehat{\sigma}^a_J = \int_{\Delta_a} H_J$

Mass, M ~ Magnetic fluxes
$$\hat{\sigma}_J \wedge \sigma^J$$

Chern-Simons Interaction: $\nabla_{\rho} F^{J \rho}{}_{\mu} \sim C_{IJK} \epsilon_{\mu\alpha\beta\gamma\delta} F^{J \alpha\beta} F^{K \gamma\delta}$ Electric Charge, $Q_I \sim$ Magnetic fluxes $\mathcal{O}^J \wedge \mathcal{O}^K$

On Σ : F fluxes have self-dual and anti-self-dual parts $\sigma = \sigma^+ + \sigma^-$ <u>Mass</u>, M ~ $|\sigma^+|^2 + |\sigma^-|^2$ <u>Charge</u>, Q ~ $|\sigma^+|^2 - |\sigma^-|^2$

<u>BPS topological stars</u> $\sigma = \sigma^{\pm}$

The Status of **BPS** Microstate Geometries in Five Dimensions

- There are vast families of smooth, horizonless `microstate geometries'
- ★ New physics at the horizon scale
 - ⇒ The cap-off and the non-trivial topology, "bubbles," arise at the original horizon scale



- ★ There are scaling microstate geometries with AdS throats that can be made arbitrarily long but cap off smoothly
- ★ Families of solutions: Large moduli spaces of cycles; fluctuations around cycles
- Holography in the long AdS throat: All these solutions represent black-hole microstates
 - ⇒ Semi-classical sampling of black-hole microstate structure
 - "Topological stars" = coherent microstates of black holes

Scale 1: The Energy Gap

 λ_{gap} = maximally redshifted wavelength, at infinity of lowest collective mode of bubbles at the bottom of the throat.

 $E_{gap} \sim (\lambda_{gap})^{-1}$

The spectrum is black hole is now gapped
 The gap is determined by "depth," Z_{max}
 Traditional black holes: E_{gap} = 0

BPS black holes



Classical microstate geometries: AdS throats that can be made arbitrarily long

 $\Rightarrow \mathbf{Z}_{max}$ arbitrarily big $\Rightarrow \mathbf{E}_{gap}$ arbitrarily small

Semi-classical quantization of the moduli of the geometry:

 \star The throat depth, or z_{max} , is not a free parameter

 $\star E_{gap}$ is determined by the charge structure of the geometry

Exactly matches E_{gap} for the stringy excitations underlying the original state counting of Strominger and Vafa

Bena, Wang and Warner, arXiv:0706.3786 de Boer, El-Showk, Messamah, Van den Bleeken, arXiv:0807.4556 arXiv:0906.0011



This is an example of a phase/geometric transition in string theory ...

- * Magnitude of fluxes , $\sigma = Order$ parameter of new phases
- * Size of the bubbles, $\lambda_T = Transition Scale$ is a new scale in the topological phase

 $\begin{array}{rcl} \text{Supergravity equations} &\Rightarrow \lambda_{\mathsf{T}} & \sim & \text{Magnitude of fluxes} \,, \sigma \\ & \text{Balance:} & \textit{Gravity} \longleftrightarrow & \textit{Flux expansion force} \end{array}$

Classically: Freely choosable parameter. Can have $\lambda_T \gg \ell_p$ Quantum mechanics: Could λ_T be dynamically generated?

Two new scales in black-hole physics





Microstate geometry: M, ℓ_p + two new scales

- ***** Scale of a typical cycle, λ_{T}
- * "Depth" of the "throat"

Physical "depth" defined by $Z_{max} = maximum redshift$ between infinity and the bubbles at the bottom of the throat

Traditional black holes: $\lambda_T = 0$, $Z_{max} = \infty$

Lessons from Holographic Field Theory



Infra-red limits of Holographic Flows



- Klebanov-Strassler
- Polchinski-Strassler
- Dijkgraaf-Vafa
- Lin, Lunin, Maldacena

+ IR geometry: Branes undergo phase transition to "bubbled geometry"

- ★ IR phase of field theory ⇔ Fluxed IR geometry: Fluxes dual to order parameter of IR phase
- * Transition scale, $\lambda_T \sim \lambda_{SQCD}$
- ★ Singular IR Geometry: wrong IR phase of theory ...
- ★ Black-hole IR Geometry: all vevs vanish ...

Microstate geometries: Same principles applied to black-hole field theory... From holographic perspective the new scales in black-hole physics closely parallel the emergence of confining IR phase and scale in QCD...

Microstate Structure

Microstate geometries *provide a mechanism* to replace singularities and horizons within string theory and support structure where the horizon would be located in a conventional black hole ...

In the supegravity approximation microstate geometries represent the only possible time-independent mechanism: topology and cohomological fluxes

Separate issue from mechanism of support:

- What structures do you want to support in place of a classical horizon?
- How can this represent these microstates of a black hole?

★ The complete description of all microstates will be intrinsically stringy ..

★ Schwarzschild Microstates are intrinsically hot ...

finite temperature firewall?

Follow-up question within geometries ...

To what extent is the microstate structure visible from semi-classical analysis within the supegravity approximation?

BPS Fluctuating Bubbled Geometries

Bubbled geometries can have BPS shape fluctuations that depend upon "transverse/internal dimensions." These shape fluctuations can go down to E_{gap} and/or the Planck scale, ℓ_p .

Most of the semi-classical entropy probably lies in the shape fluctuations...

Extensive work in five-dimensions: BPS shape fluctuations on 2-cycles depend upon functions of one variable: Expect entropy like that of a supertube $S \sim \sqrt{Q_1 Q_2} \sim Q$

shape mode

If fluctuations localized at the bottom of a scaling solution then one can get entropy enhancement: Magnetic dipole-dipole interactions can make supertube much floppier than in flat space $\Rightarrow S \sim Q^{5/4}$

Semi-classical quantization of five-dimensional BPS solutions: $S \sim Q^{5/4}$ de Boer, El-Showk, Messamah, Van den Bleeken, arXiv:0807.4556, arXiv:0906.0011 Black hole entropy: $S \sim \sqrt{Q_1 Q_2 Q_3} \sim Q^{\frac{3}{2}}$

The Superstratum:

An intrinsically new BPS bound state/microstate geometry in six dimensions.



⇒ BPS configurations that depend upon *functions of two variables* Preserves the 4 supersymmetries if the D1-D5-P system
 Smooth in the D1-D5-P duality frame: A microstate geometry.

The Superstratum: Another Perspective



The D1-D5-P system was the basis of the original counting by Strominger and Vafa ...

The underlying CFT is the orbifold $S_N(T^4)$...

 $N = N_1 N_5$ $c = 6N = 6N_1 N_5$

Carry momentum $P \Rightarrow S = 2\pi \sqrt{N_1 N_5 P}$

Transverse motions *appear* only involve the internal T^4

However the chiral primaries of the D1-D5 theory are the twist fields of S_N

Fundamental twists: Pairwise interchanges σ_{ij} i, j = 1,...,N Carry the fundamental representation = vector of SO(4) of the *R-symmetry* group = Rotation group in space-time

- ⇒ Chiral primaries of the D1-D5 theory carry space-time polarizations
- ⇒ Back-reaction visible as angular momentum shape modes in space time

Generators of S_N are $\sigma_{j j+1}$ j = 1,...,N-1

N-1 independent momentum carriers: angular momentum shape modes

How the quantization of the superstratum might work



BPS configurations that depend upon *functions of two variables*

- Shape modes in R⁴ directions arise from quantization of D1-D5 system
- There are $N = N_1 N_5$ independent angular shape modes, each of which can carry z-momentum
- Each angular shape mode carries a polarization vector in R⁴ and has four fermonic counterparts \Rightarrow c = 6 N₁ N₅ visible as space-time fluctuations

When semi-classically quantized we hope that each of these modes acts as an independent momentum carrier ...

If so then: **S** = $2\pi\sqrt{N_1N_5P}$

would follow from semi-classical quantization of supergravity!

The Overall Picture

- String theory has new phases dominated by topological fluxes that can prevent the formation of black holes → Topological Stars/Black hole microstates
- Transition to new phase \leftrightarrow Formation of bubbles supported by flux

 \rightarrow Order parameter and new scale in Nature: $\lambda_T = Transition$ Scale

- Extra-dimensions of space-time are crucial: $\lambda_T \sim Scale of extra dimensions near topological star$
- The new phase smoothly caps-off the space-time before a horizon forms: \rightarrow Limits the red-shift; makes the spectrum of fluctuations gapped, E_{gap}
- The new phases represent new "infra-red" vacua of string theory
- Fluctuations about these new phases represent the microstate structure
- Vast families of BPS examples explicitly constructed Semi-classical description of black-hole microstate structure/thermodynamics?

This viewpoint is a natural and direct outgrowth of holographic field theories

<u>Current Issues in Microstate Geometries:</u>

BPS solutions

- Vast families of classical solutions, with huge moduli spaces ...
 - → Semi-classical description of black-hole entropy?

Superstratum: quite possibly yes!

• Quantum fluctuations about these backgrounds

→ Complete description of black-hole microstate structure?Promising but still subject to debate

Non-BPS extremal solutions

Similar to BPS story: but technically much harder

Non-BPS, non-extremal solutions

Very little known but near-BPS picture seems very promising: BPS microstate structures are perturbatively stable

More Speculative Ideas...

Other "more stringy" mechanisms have been proposed for changing the physics at the horizon scale.

- Brane polarization effects: e.g. angular momentum; Myers effect
- Non-Abelian degrees of freedom: e.g. pure Higgs branch fields

These are generically in corners of the moduli space of the background in which the gravitational back-reaction is minimized/ignored because the string coupling is weak or the number of quanta is small ...

Increasing the string coupling or the number of quanta creates a strong back-reaction and Higgs branch fields condense. Then one can use supergravity ...

.. and in supegravity the only possible mechanism is that of microstate geometries and based on topological fluxes.

Conversely, one can view such brane-polarization or non-Abelian effects as limiting behavior of *microstate geometries* and thus these other mechanisms can be understood as more general classes of *microstate solutions* that can be linked to *microstate geometries* by tuning parameters.

More Speculative Ideas: Collapse to a Black Hole

Mathur: 0805.3716; 0905.4483; Mathur and Turton: 1306.5488

A shell of spherically symmetric matter collapses to a *microstate geometry*...

How can this happen?



Consider a particle falling into a black hole ...



Probability of tunneling during infall time $\sim O(1)!$

Black hole formation is intrinsically a quantum tunneling transition!

Final thought...

Maybe in spite of its macroscopic size, the near-horizon properties of black holes are dominated by quantum effects ... and this is what makes the O(1) changes to horizon-scale physics

So then what good is all this classical supergravity analysis?

It identifies the long-range, large scale degrees of freedom that control physics at the horizon scale ... and maybe we only have to perform the semi-classical quantization of all these relatively simple degrees of freedom to get a good picture of what is really happening at the horizon of a black hole ..

Conclusions

 <u>Microstate Geometries</u>: Classify and study smooth, horizonless solutions to supergravity

Miraculous existence through spatial topology and Chern-Simons terms

- Emerge from geometric phase transitions:
 Singular brane sources → Smooth cohomological fluxes
- Mechanism for supporting matter before a horizon forms
 - ★ New "flux-dominated" phases of string theory
 - * Support the microstate structure of black holes in whatever stringy form
 - ***** Topological stars in Nature?
- Semi-classical technique for understanding the detailed microstate structure of black holes
- New scales in black-hole physics: Transition scale, λ_T , and maximum red-shift, Z_{max} ; related to E_{gap} of fluctuation spectrum
- For BPS microstate geometries, supergravity modes of the superstratum may be sufficient to provide a semi-classical description of the black-hole entropy