

# Formation spectra of deeply bound pionic atoms in the $(d, {}^3\text{He})$ reactions

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# Introduction

Deeply bound pionic atom ... Useful system to study pion properties at finite density

- Pion-Nucleus optical potential : Strong correlation of parameters

$$2\mu V_{\text{opt}}^s = -4\pi[\varepsilon_1\{b_0\rho(r) + b_1\delta\rho(r)\} + \varepsilon_2 B_0\rho^2(r)]$$

- GOR relation + Tomozawa-Weinberg relation

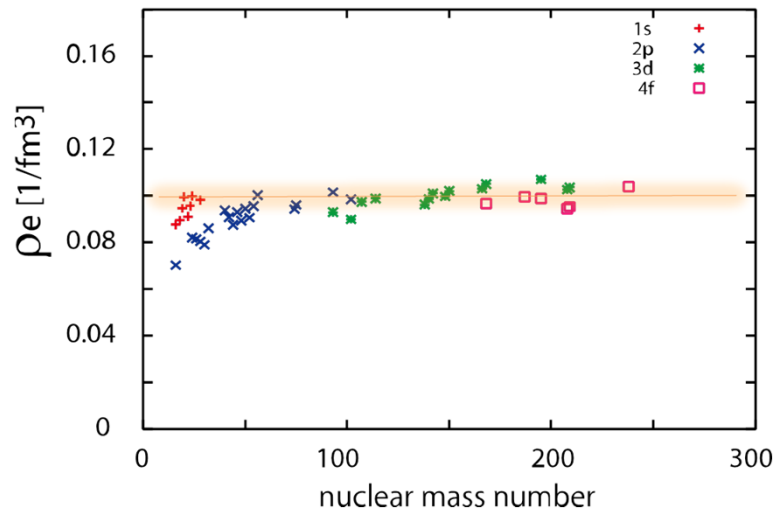
$$\frac{\langle \bar{q}q \rangle_\rho}{\langle \bar{q}q \rangle_0} \simeq \frac{f_\pi^{*2}}{f_\pi^2} \simeq \frac{b_1^{\text{free}}}{b_1^*(\rho)} = 0.78 \pm 0.05 @ \rho \simeq 0.6\rho_0 : \text{Partial Restoration of Chiral Symmetry}$$

$\sim 0.67 @ \rho = \rho_0$

K. Suzuki *et al.*, PRL92(04)072302

D. Jido, T. Hatsuda and T. Kunihiro, PLB 670(08)109

- Nuclear density probed by pionic atom : Only limited at  $\rho \simeq 0.6\rho_0$



## Our Motivation

We want to extract information on pion properties at **various densities**

➔ More Systematic/Accurate information on pionic states from (d, <sup>3</sup>He) spectra

# Our studies

Experimental Data; Systematic/Accurate information

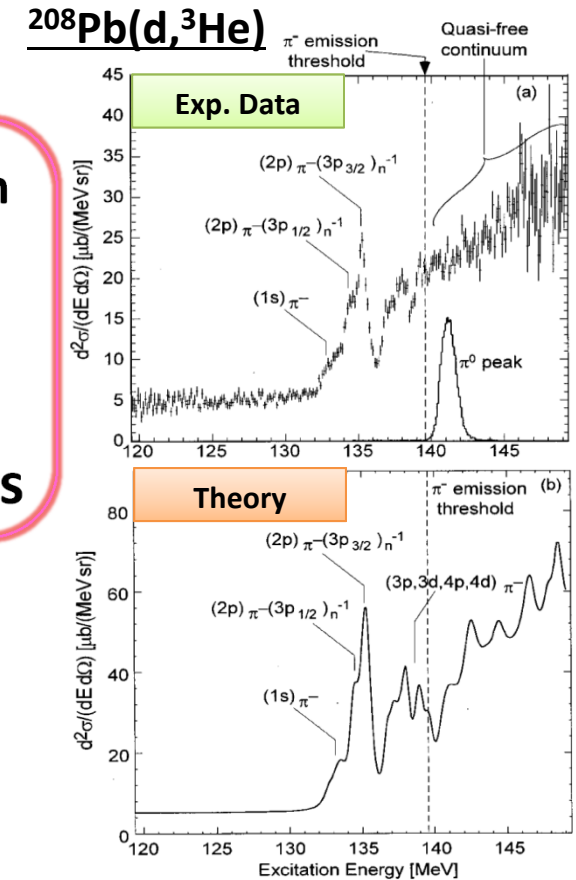
Direct comparison

Theoretical Formation Spectrum of pionic atoms

➔ We know pion properties at various densities

## In this talk

- $^{122}\text{Sn}(d,^3\text{He})$  spectra at finite angles
  - Experimental data @RIBF/RIKEN, T. Nishi-san's talk
- $^{117}\text{Sn}(d,^3\text{He})$  spectra
  - Odd-neutron nuclear target  $J^p=1/2^+$
  - Next Experiment @RIBF/RIKEN, K. Itahashi *et al.* RIBF-027
- Updated theoretical calculation
  - Green's Function Method

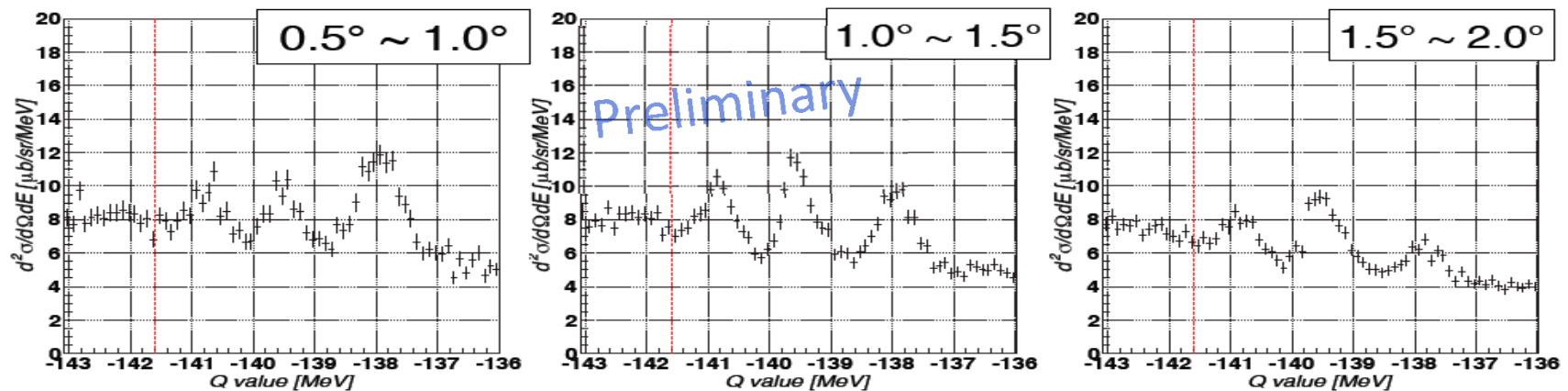


K. Itahashi *et al.*, PRC62(00)025202

# $^{122}\text{Sn}(d, ^3\text{He})$ spectra at finite angles

N. Ikeno, H. Nagahiro and S. Hirenzaki, EPJA47 (2011) 161

Experimental Data : JPS 2013 Autumn Meeting, T. Nishi-san's slide



# Formulation: Effective Number Approach

➤ Formation cross section (Bound state + Unbound state)

$$\left( \frac{d^2\sigma}{dE_{\text{He}} d\Omega_{\text{He}}} \right)_A^{\text{lab}} = \left( \frac{d\sigma}{d\Omega_{\text{He}}} \right)_{\text{ele}}^{\text{lab}} \sum_{ph} K \left( \frac{\Gamma}{2\pi} \frac{1}{\Delta E^2 + \Gamma^2/4} N_{\text{eff}} + \frac{2p_{\pi} E_{\pi}}{\pi} N_{\text{eff}} \right)$$

$$\Delta E = Q + m_{\pi} - B_{\pi} + S_n - 6.787 \text{MeV}$$

- **Elementary cross section**  $\left( \frac{d\sigma}{d\Omega_{\text{He}}} \right)_{\text{ele}}^{\text{lab}}$  : Experimental data (d+n→<sup>3</sup>He + π<sup>-</sup>)  
M. Betigeri *et al.*, NPA690(01)473

- **Kinematical correction factor:**

$$K = \left[ \frac{|\vec{p}_{\text{He}}^A| E_n E_{\pi}}{|\vec{p}_{\text{He}}| E_n^A E_{\pi}^A} \left( 1 + \frac{E_{\text{He}}}{E_{\pi}} \frac{|\vec{p}_{\text{He}}| - |\vec{p}_d| \cos\theta_{d\text{He}}}{|\vec{p}_{\text{He}}|} \right) \right]^{\text{lab}}$$

Difference of kinematics between d+n→<sup>3</sup>He + π<sup>-</sup> and A(d,<sup>3</sup>He)(A-1)⊗π<sup>-</sup>

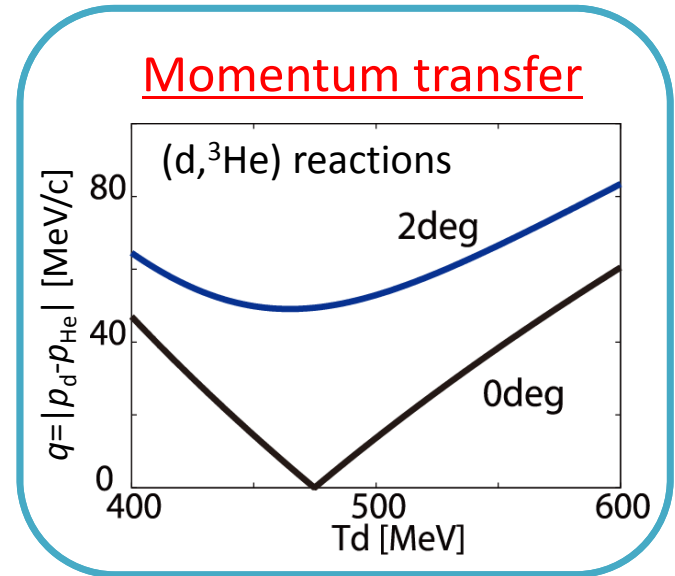
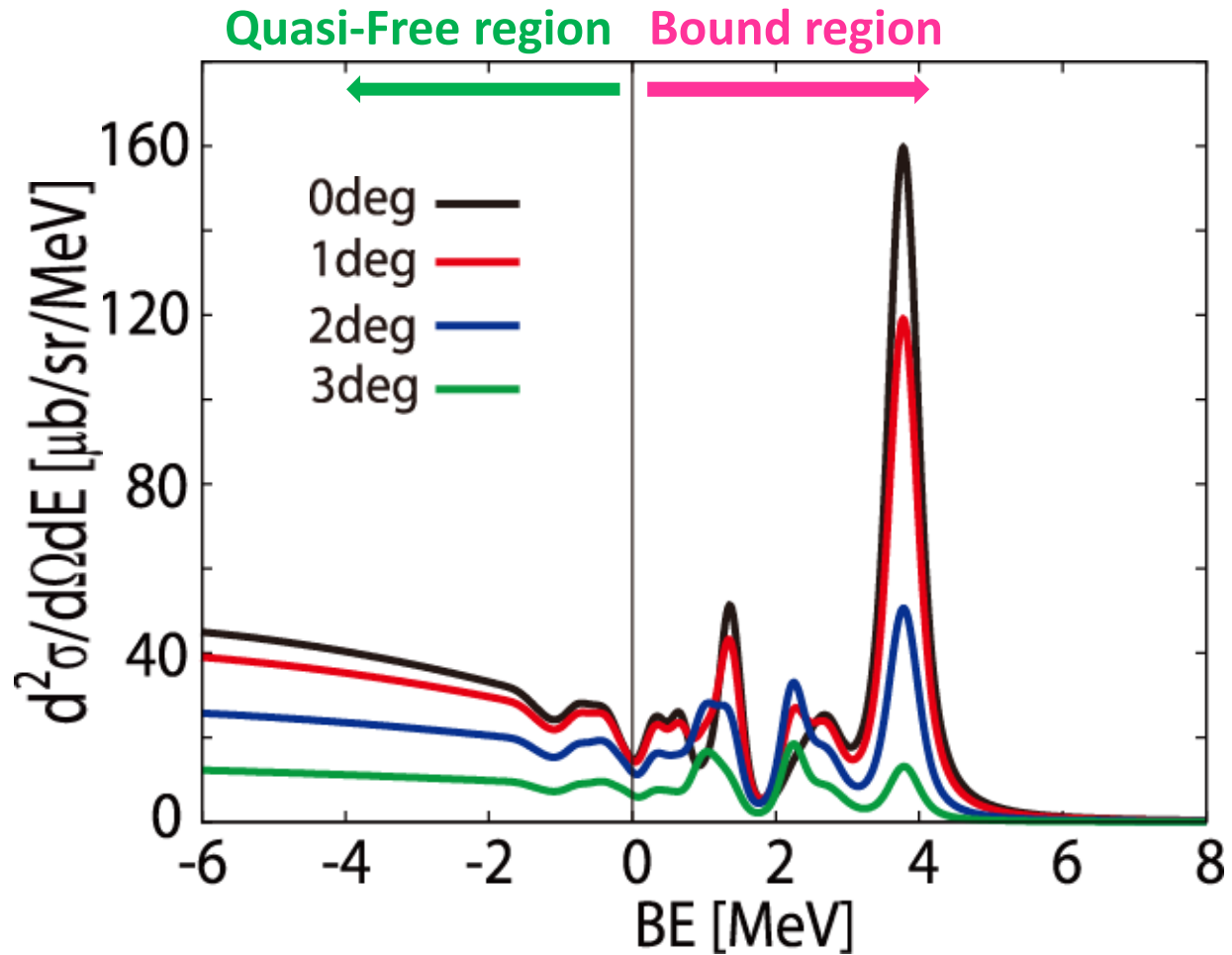
N. Ikeno, H. Nagahiro and S. Hirenzaki, EPJA47 (2011) 161

- **Effective Number:**

$$N_{\text{eff}} = \sum_{JMm} \left| \int d\vec{r} e^{i\vec{q}\cdot\vec{r}} D(\vec{r}) \xi_{\frac{1}{2}m}^{\dagger} [\phi_{\ell_{\pi}}^*(\vec{r}) \otimes \psi_{j_n}(\vec{r})]_{JM} \right|^2$$

# Numerical results

➤  $^{122}\text{Sn}(d, ^3\text{He})$  spectra at Finite angles



Energy resolution  
 $\Delta E = 300 \text{ keV}$

Neutron wave function:  
H. Koura *et al.*, NPA671(2000)96

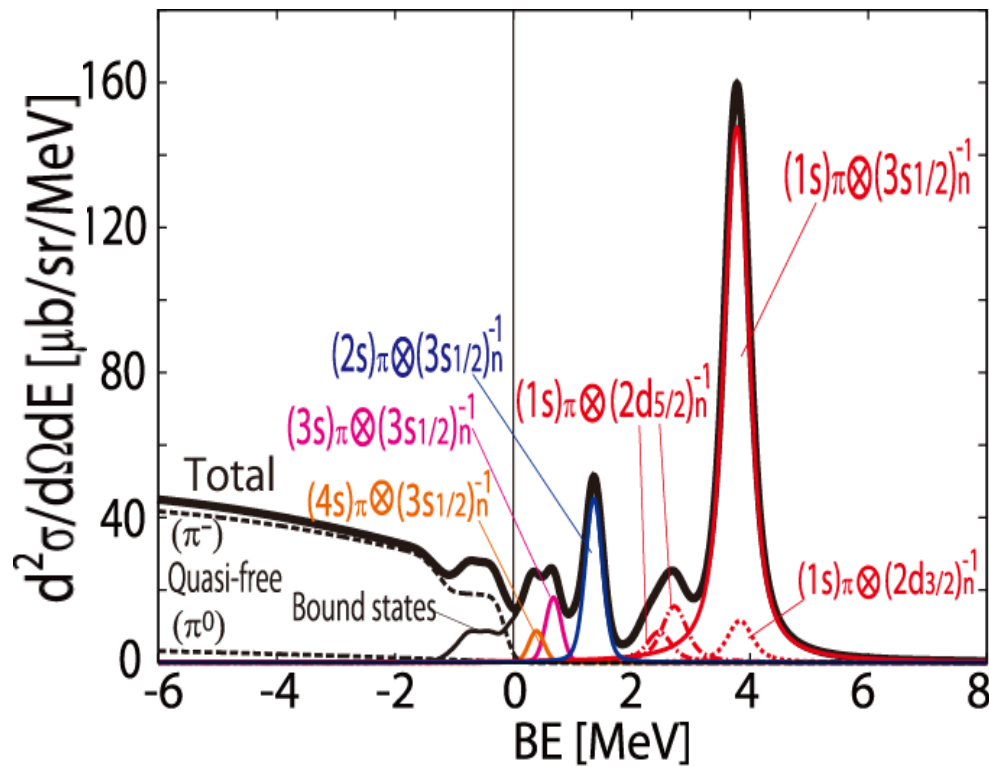
Spectra have a strong angular dependence.

# Numerical results

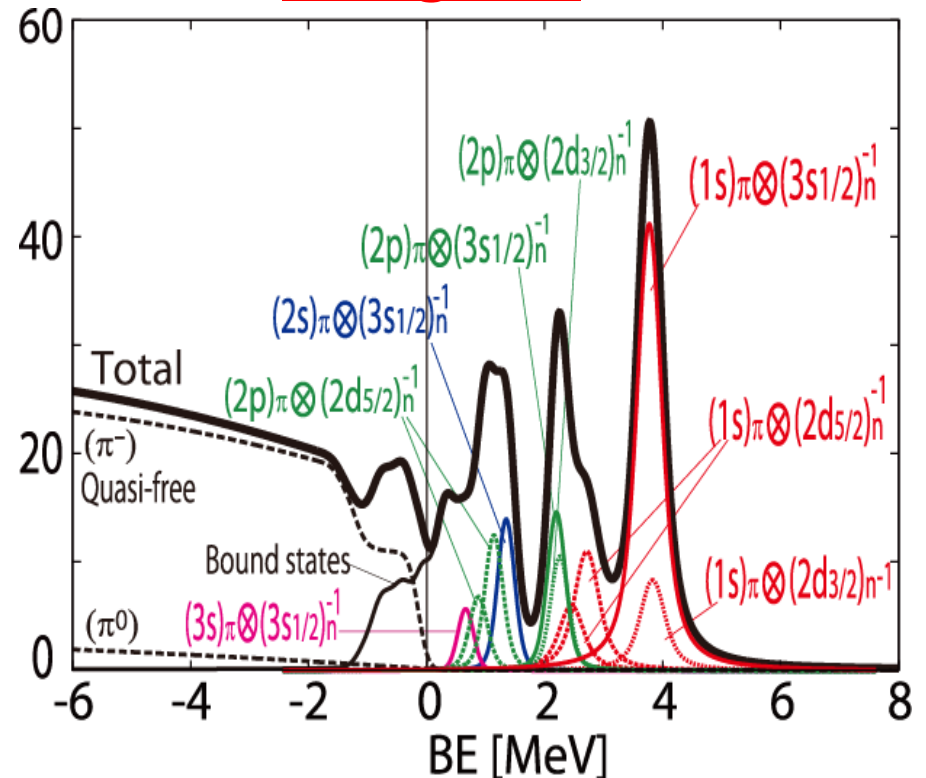
➤ Dominant Subcomponent  $[(nl)_\pi \otimes (nl_j)_n^{-1}]$

Energy resolution  
 $\Delta E = 300 \text{ keV}$

0 degrees



2 degrees

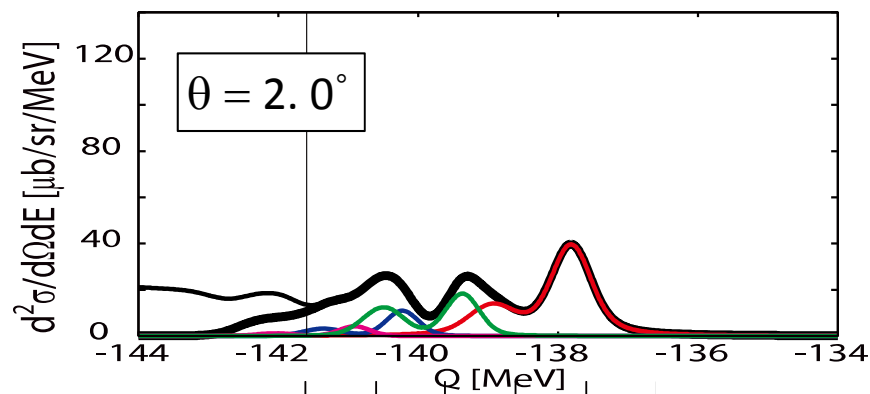
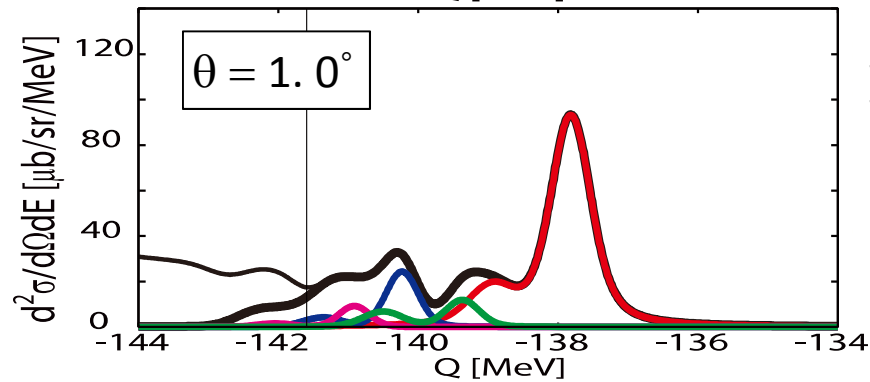
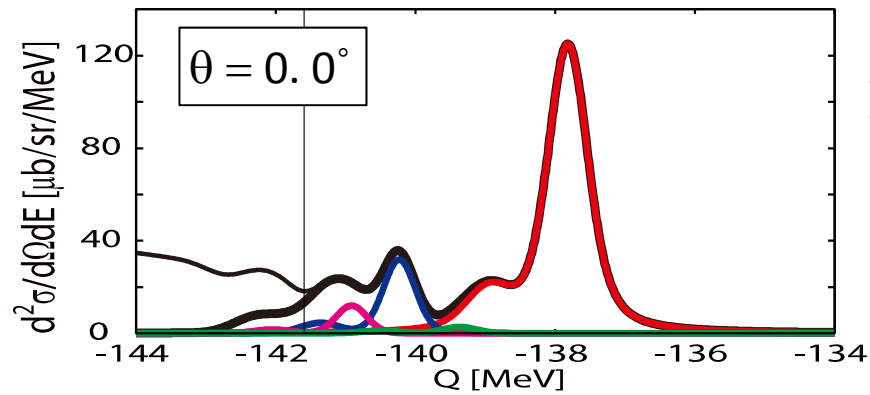


We can obtain information on deeply bound pionic **2p** state in addition to **1s** and **2s** states.

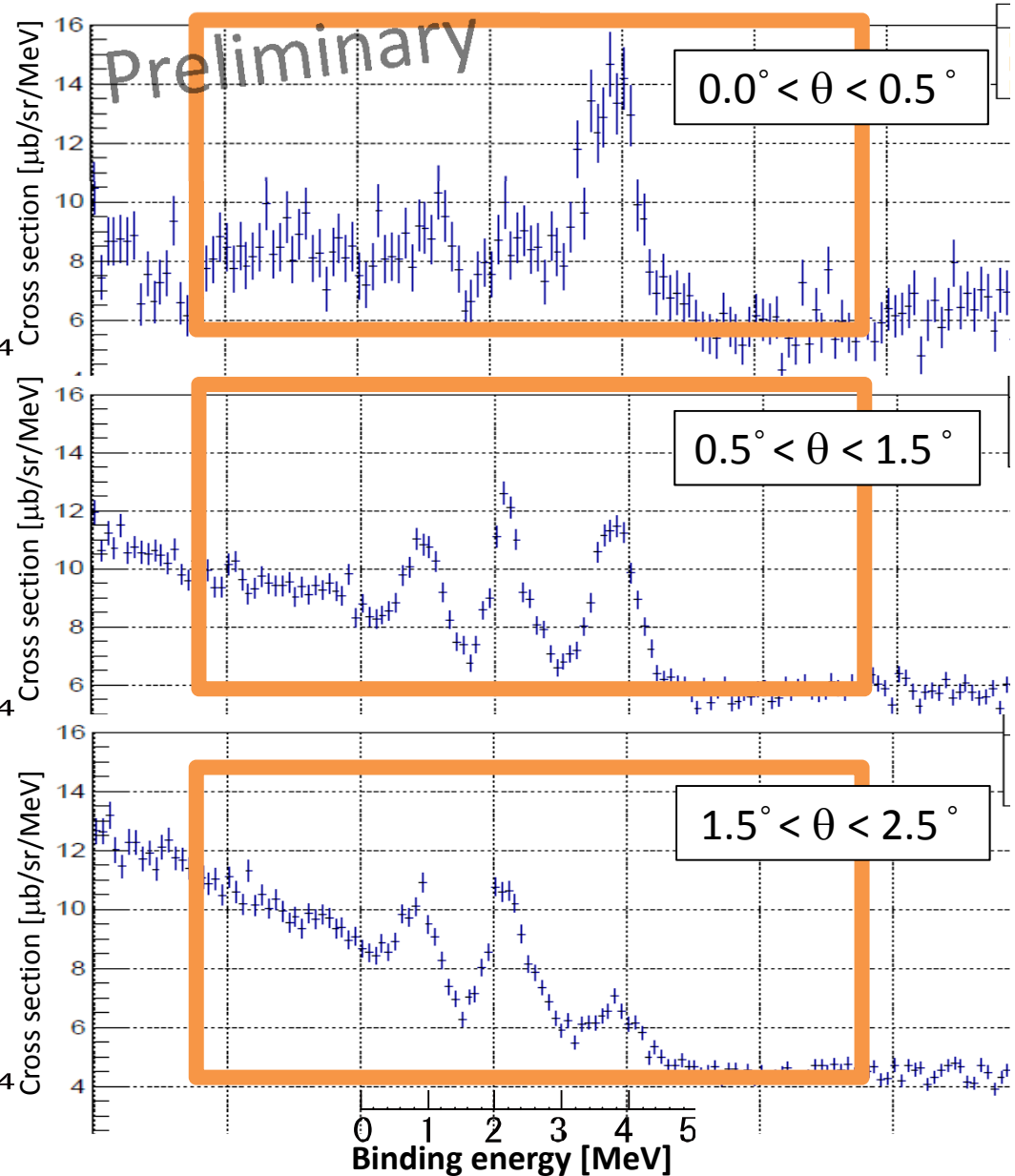
**This will be important to reduce uncertainties in neutron distribution.**

# Theory vs. Experiment

T. Nishi, private communication



Energy resolution  $\Delta E = 500 \text{ keV}$   
Binding energy [MeV]





# **$^{117}\text{Sn}(d,^3\text{He})$ spectra:**

## Odd-neutron nuclear target

N. Ikeno , J. Yamagata-Sekihara, H. Nagahiro and S. Hirenzaki, PTEP(2013) 063D01

# Interests of Odd target

## Odd-neutron nuclear target: $J^P=1/2^+$

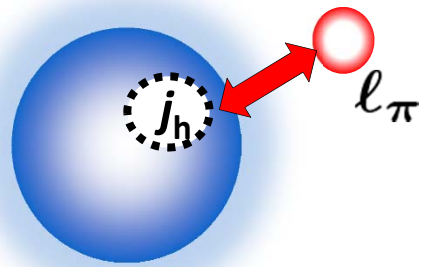
Sn: 

$^{115}\text{Sn}$ $1/2^+$	$^{116}\text{Sn}$ $0^+$	$^{117}\text{Sn}$ $1/2^+$	$^{118}\text{Sn}$ $0^+$	$^{119}\text{Sn}$ $1/2^+$	$^{120}\text{Sn}$ $0^+$	$^{121}\text{Sn}$ $3/2^+$	$^{122}\text{Sn}$ $0^+$	$^{123}\text{Sn}$ $11/2^-$	$^{124}\text{Sn}$ $0^+$
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- Pionic atom spectroscopy on the wider region in nuclear chart
- Pionic state free from residual interaction effect  $[\pi^- \otimes 0^+]$

## Even-Even Nucleus: $J^P=0^+$

Final state: pion particle - neutron hole  $[\pi \otimes n^{-1}]$



### “Residual interaction effect”

- Level splitting between different J state
- Energy shift

$$|(\ell_\pi \otimes j_h^{-1})_J\rangle$$

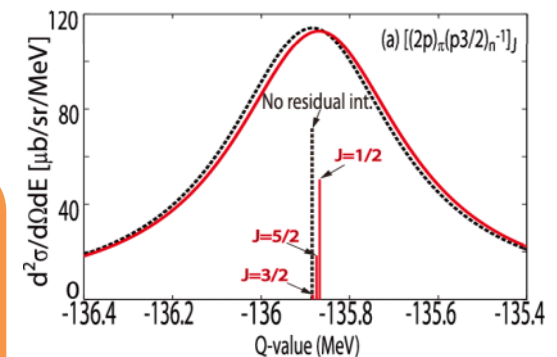
Additional difficulty to determine B.E. and parameters in  $V_{opt}$

### [Exp. Error] vs. [Shift due to Residual Int.]



Observation of pionic states free from these effects is very important to obtain more accurate information from data.

$^{116}\text{Sn}$ complex energy shift		
$j_h^{-1}$	1s [keV]	2p [keV]
$3s_{1/2}^{-1}$	-15.4-4.2i	<b>J=1/2</b> -4.0-1.1i
		<b>J=3/2</b> -4.0-1.1i
$2d_{3/2}^{-1}$	-15.9-4.8i	<b>J=1/2</b> -9.1-3.1i
		<b>J=3/2</b> 0.3+0.3i
		<b>J=5/2</b> -5.2-1.8i
<b>Exp. Error <math>\pm 24</math> [keV] @GSI</b>		



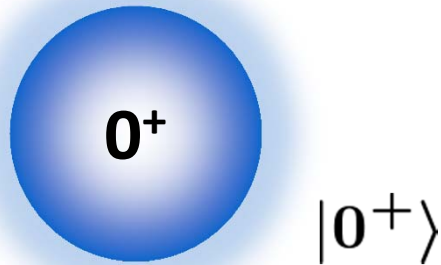
S. Hirenzaki *et al.* PRC60(99)058202;  
N. Nose-Togawa *et al.* PRC71(05)061601(R)

# Formulation: Even vs. Odd target

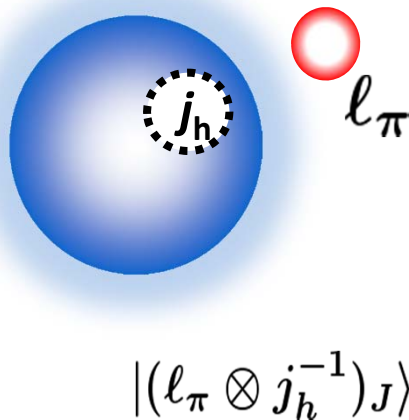
## ➤ Effective Number

Even target:  $^{122}\text{Sn} (0^+)$

Initial:

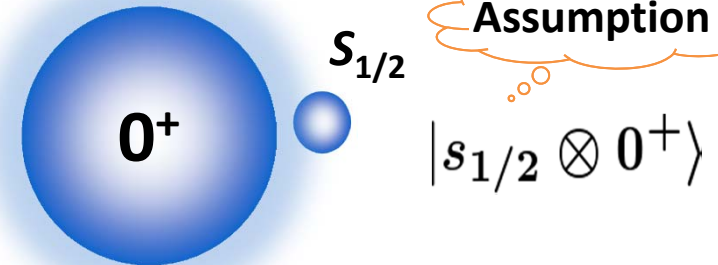


Final:



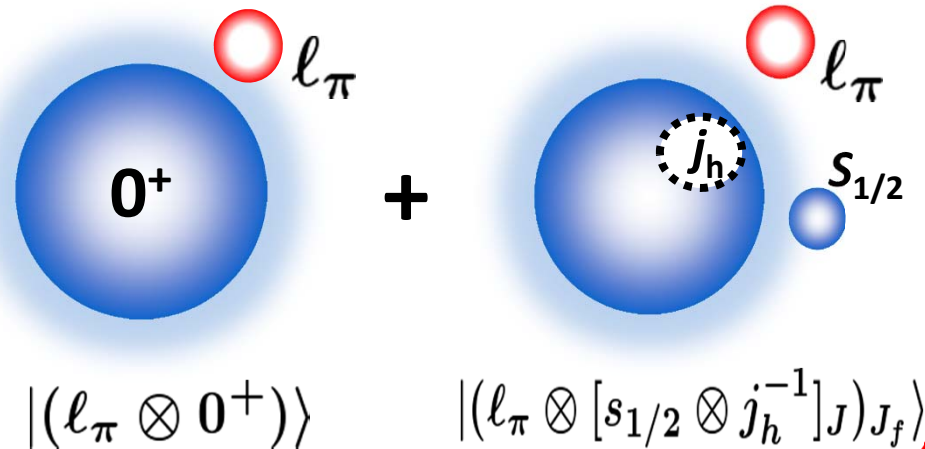
Odd target:  $^{117, 119}\text{Sn} (1/2^+)$

Initial:



Final:

- (1) neutron pick-up from  $s_{1/2}$  orbit
- (2) neutron pick-up  $j_h$  orbit from other than  $s_{1/2}$

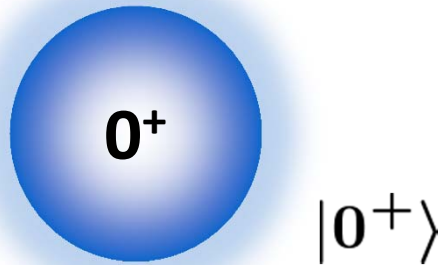


# Formulation: Even vs. Odd target

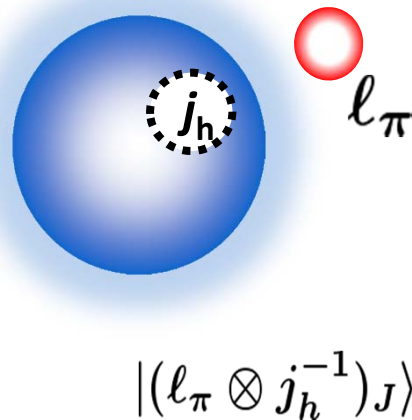
## ➤ Effective Number

Even target:  $^{122}\text{Sn} (0^+)$

Initial:

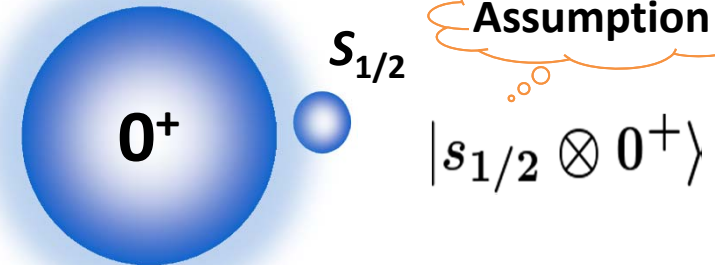


Final:



Odd target:  $^{117, 119}\text{Sn} (1/2^+)$

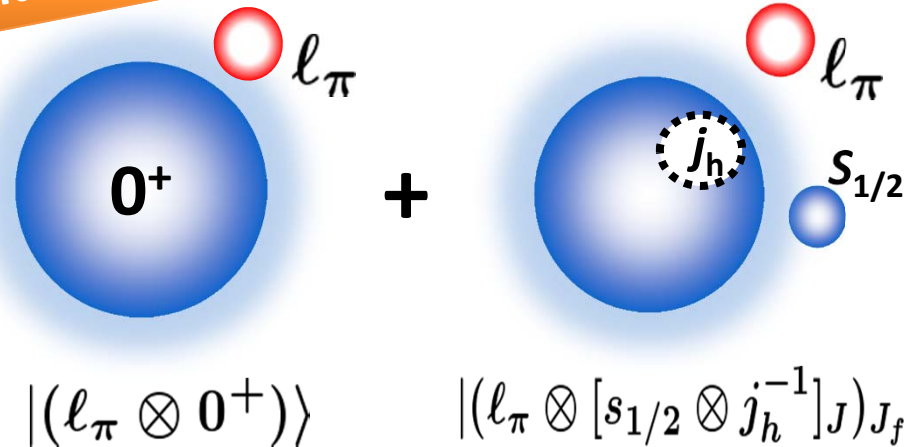
Initial:



Final:

- (1) neutron pick-up from  $s_{1/2}$  orbit  
 (2) neutron pick-up  $j_h$  orbit from other than  $s_{1/2}$

No Residual Interaction



➤ Realistic neutron configurations for the target and the daughter nucleus: Exp. Data

**Even target:  $^{122}\text{Sn} (0^+)$**

**Excited level of  $^{121}\text{Sn}$**

Exp. Data:  $^{122}\text{Sn}(d,t)^{121}\text{Sn}$   
 E. J. Schneid et al., Phys. Rev. 156 (1967) 1316

Neutron hole orbit $j_h$	Ex [MeV]
3s1/2	0.06
2d3/2	0.00
2d5/2	1.11
	1.37
1g7/2	0.90
1h11/2	0.05

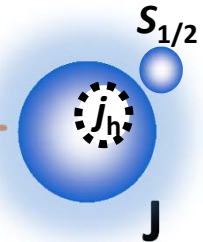
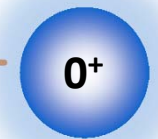


**Odd target:  $^{117}\text{Sn} (1/2^+)$**

**Excited level of  $^{116}\text{Sn}$**

Exp. Data:  $^{117}\text{Sn}(d,t)^{116}\text{Sn}$ ,  
 J. M. Schippers et al., NPA510(1990)70

$J^P$	Neutron hole orbit $j_h$	Ex [MeV]
0+	3s1/2	0.00
		1.76
		2.03
		2.55
1+	2d3/2	2.59
		2.96
2+	2d3/2 and 2d5/2	1.29
		2.23
		3.23
		3.37
		3.47
		3.59
		3.77
		3.95
3+	2d5/2 and 1g7/2	3.00
		3.42
		3.71
		3.18
4+	1g7/2	2.39
		2.53
		2.80
		3.05
		3.10
5-	1h11/2	2.37
6-	1h11/2	2.77



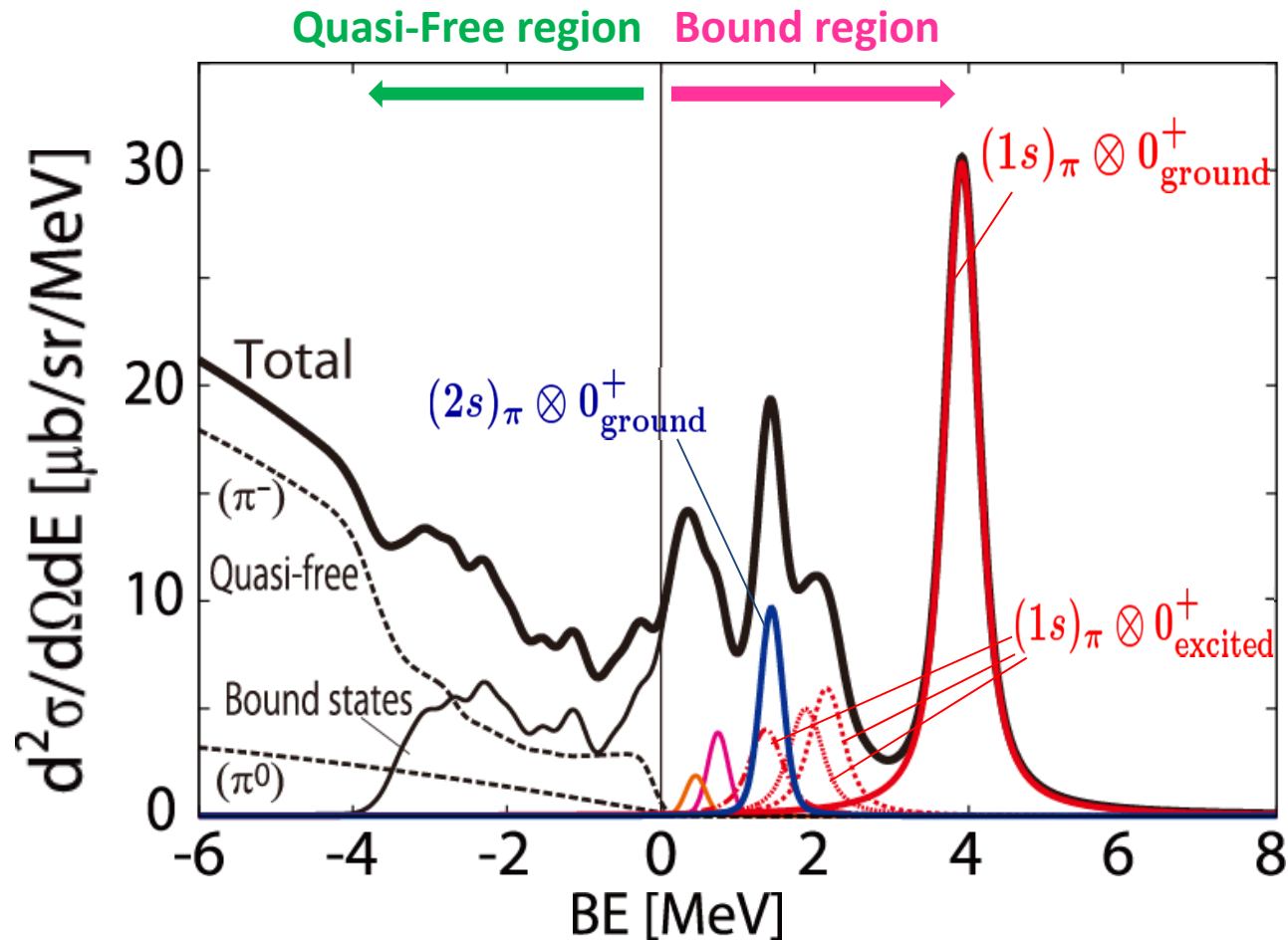
- ✓ Many excited levels
- ✓ Large excitation energies (Ex)

**➔ Pionic atom formation spectra:  
 Expected to be  
 Complicated and broad spectra**

# Numerical Results: Odd target

➤  $^{117}\text{Sn}(d, ^3\text{He})$  spectra at 0 degrees

Neutron wave function:  
H. Koura *et al.*, NPA671(2000)96



Energy resolution  
 $\Delta E = 300 \text{ keV}$

Dominant  
Subcomponent:  
 $[(nl)_\pi \otimes J^P]$

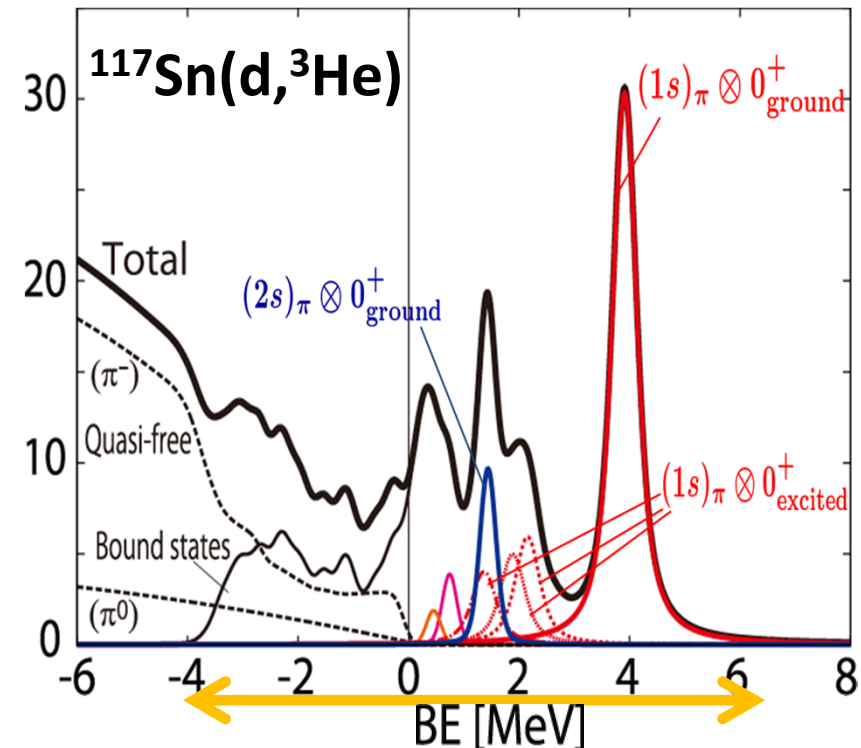
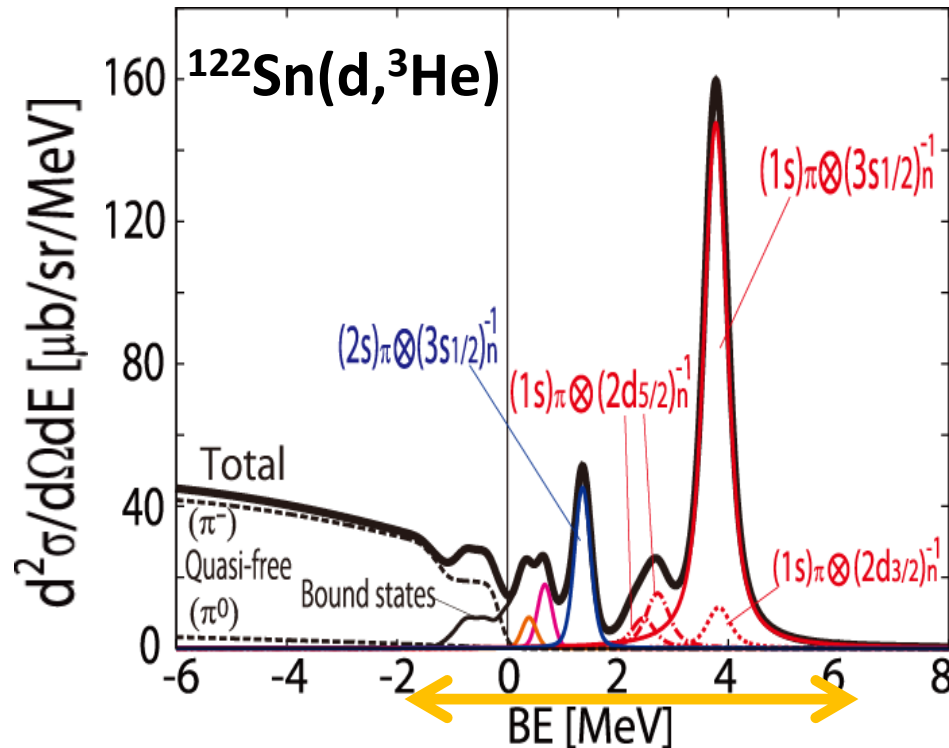
- We can see clear peak structure of  $[(1s)_\pi \otimes ^{116}\text{Sn}(0^+)]$ .
  - No residual interaction effect

# Numerical Results: Even vs. Odd target

## 0 degrees

Even target:  $^{122}\text{Sn} (0^+)$

Odd target:  $^{117}\text{Sn} (1/2^+)$



- Pionic 1s state formation with neutron s-hole state is large in both spectra.
- Bound pionic state formation spectra in  $^{117}\text{Sn}(d,^3\text{He})$  are spread over wider energy range.
- Absolute value of cross section in  $^{117}\text{Sn}(d,^3\text{He})$  is smaller.

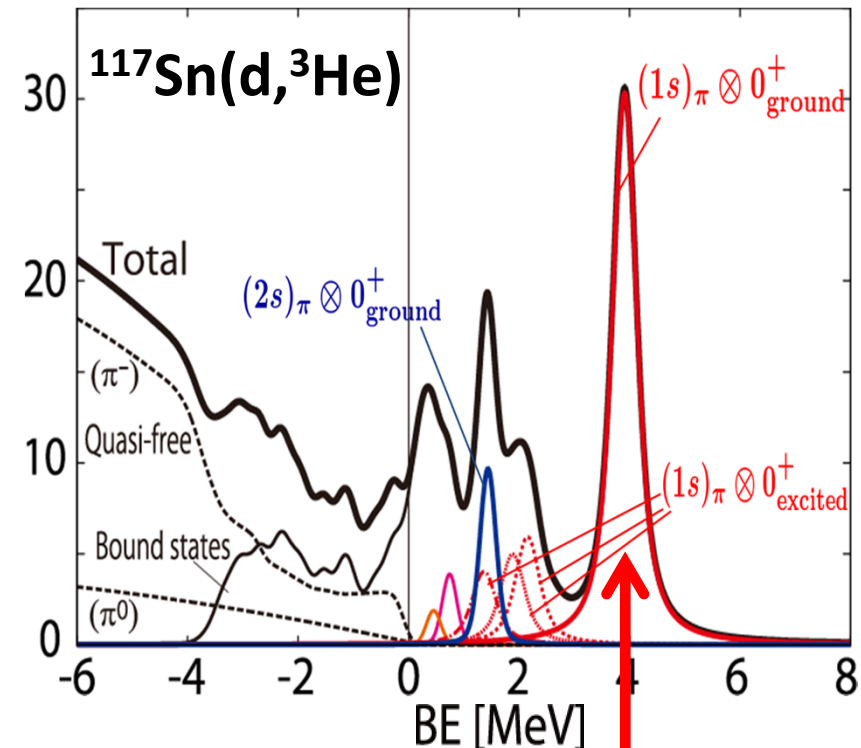
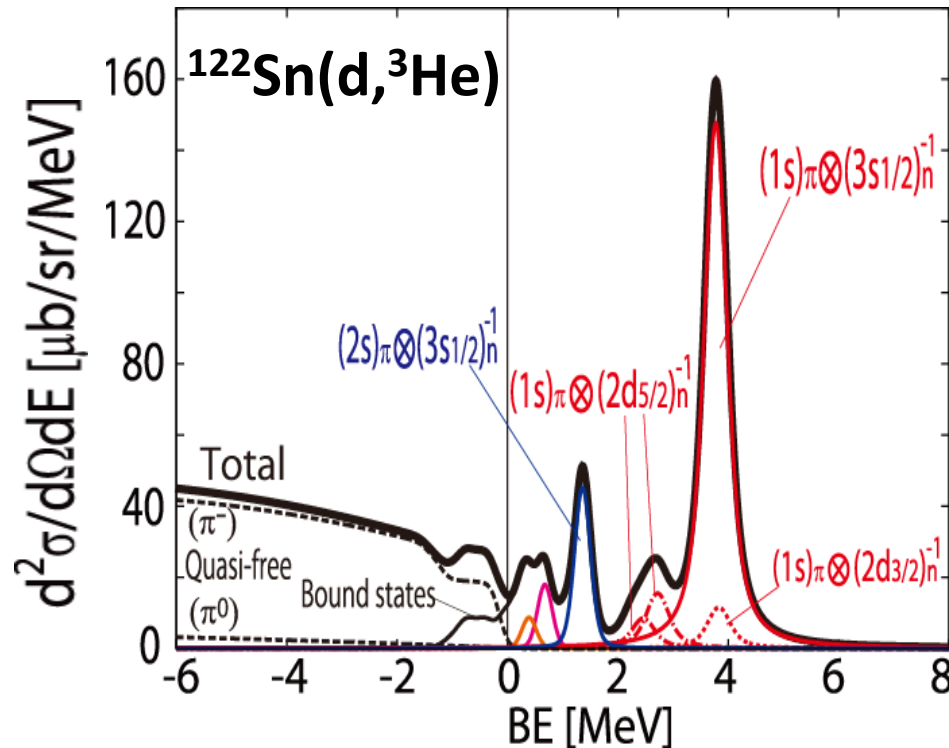


# Numerical Results: Even vs. Odd target

## 0 degrees

Even target:  $^{122}\text{Sn} (0^+)$

Odd target:  $^{117}\text{Sn} (1/2^+)$



**Odd target: Isolated peak and single subcomponent (No residual interaction effect)**

→ This pionic 1s state is preferable for extracting accurate information on BE and parameters in  $V_{\text{opt}}$



# Updated theoretical calculation:

Spectra calculated by Green's Function Method

N. Ikeno , J. Yamagata-Sekihara, H. Nagahiro, S. Hirenzaki, in preparation

## Future Experiments @RIBF/RIKEN

- ✓ Better Energy Resolution
- ✓ More Precise Shapes of Spectrum
  - Various nuclear targets, - Finite angles reactions, ...



**We need to update the theoretical spectra.**

# Formulation: Green's Function Method

➤ Formation cross section O. Morimatsu, K. Yazaki, NPA435(85)727, NPA483(88)493

$$\left( \frac{d^2\sigma}{dE_{\text{He}}d\Omega_{\text{He}}} \right)_A^{\text{lab}} = \left( \frac{d\sigma}{d\Omega_{\text{He}}} \right)_{\text{ele}}^{\text{lab}} \times -\frac{1}{\pi} \text{Im} \sum_f \left[ \tau_f^\dagger G(E) \tau_f \times K \right]$$

- Elementary cross section  $\left( \frac{d\sigma}{d\Omega_{\text{He}}} \right)_{\text{ele}}^{\text{lab}}$

- Kinematical correction factor  $K$

- Green's function for  $\pi^-$  interacting with the nucleus

$$G(E, \vec{r}, \vec{r}') = \langle n^{-1} | \phi_\pi(\vec{r}) \frac{1}{E - H_\pi + i\varepsilon} \phi_\pi^\dagger(\vec{r}') | n^{-1} \rangle$$

- transition amplitude

$$\tau_f(\vec{r}) = \chi_f^*(\vec{r}) \xi_{1/2, m_s}^* \left[ Y_{\ell_\pi}^*(\hat{\vec{r}}) \otimes \psi_{j_n}(\vec{r}) \right]_{JM} \chi_i(\vec{r})$$

$$\chi_f^*(\vec{r}) \chi_i(\vec{r}) = \exp \left( i\vec{q} \cdot \vec{r} \frac{m_C}{m_C + m_\pi} \right) F(\vec{r})$$

## Advantages:

- ✓ We can include Bound and Quasi-free contributions simultaneously.
- ✓ We can include an infinite number of Bound State contributions.
- ✓ We do not assume Lorentz distribution as the shape of peak structure.

# Numerical results: Green vs. Neff

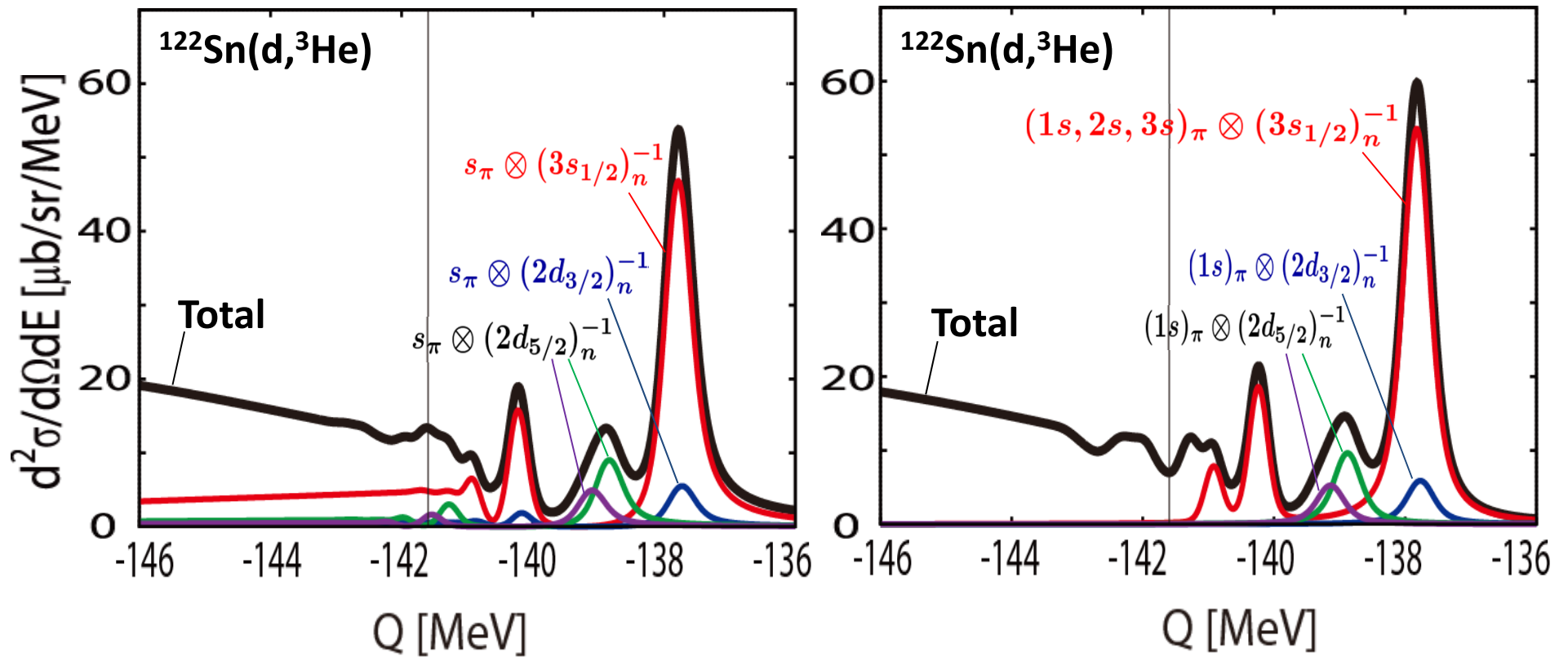
Energy resolution  
 $\Delta E=300\text{keV}$

➤  $^{122}\text{Sn}(d,^3\text{He})$  spectra at 0 degrees

Neutron wave function:  
Harmonic Oscillator

Green

Neff



Both Methods seem to provide the very similar spectra.

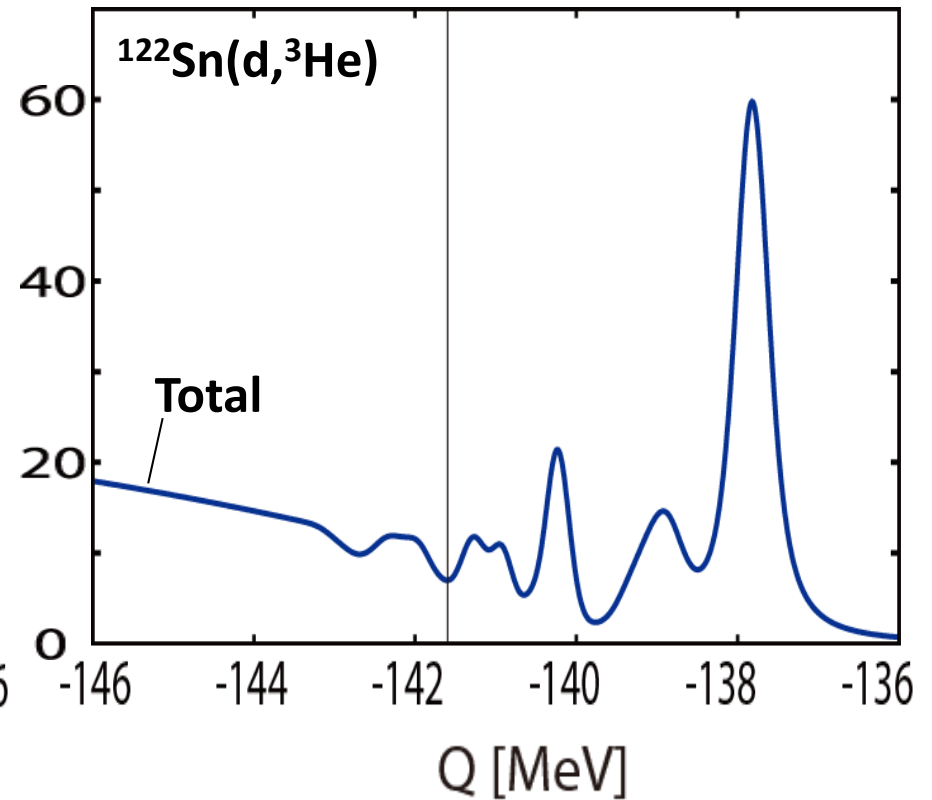
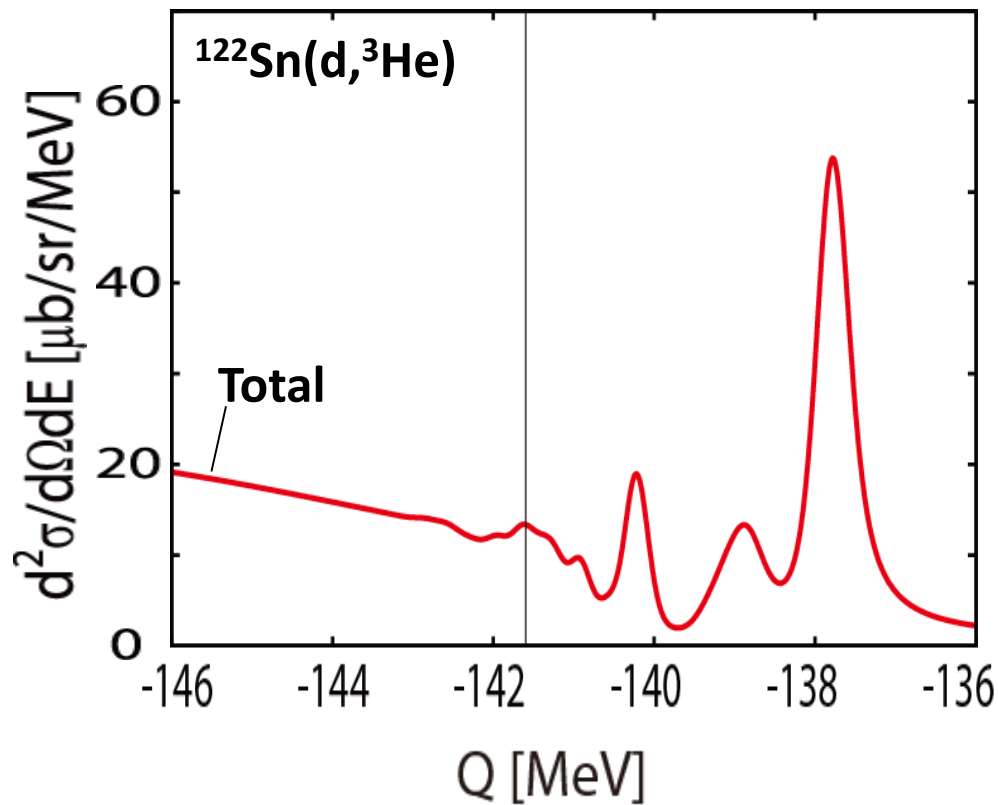
# Numerical results: Green vs. Neff

➤  $^{122}\text{Sn}(d,^3\text{He})$  spectra at 0 degrees

Energy resolution  
 $\Delta E=300\text{keV}$

Green

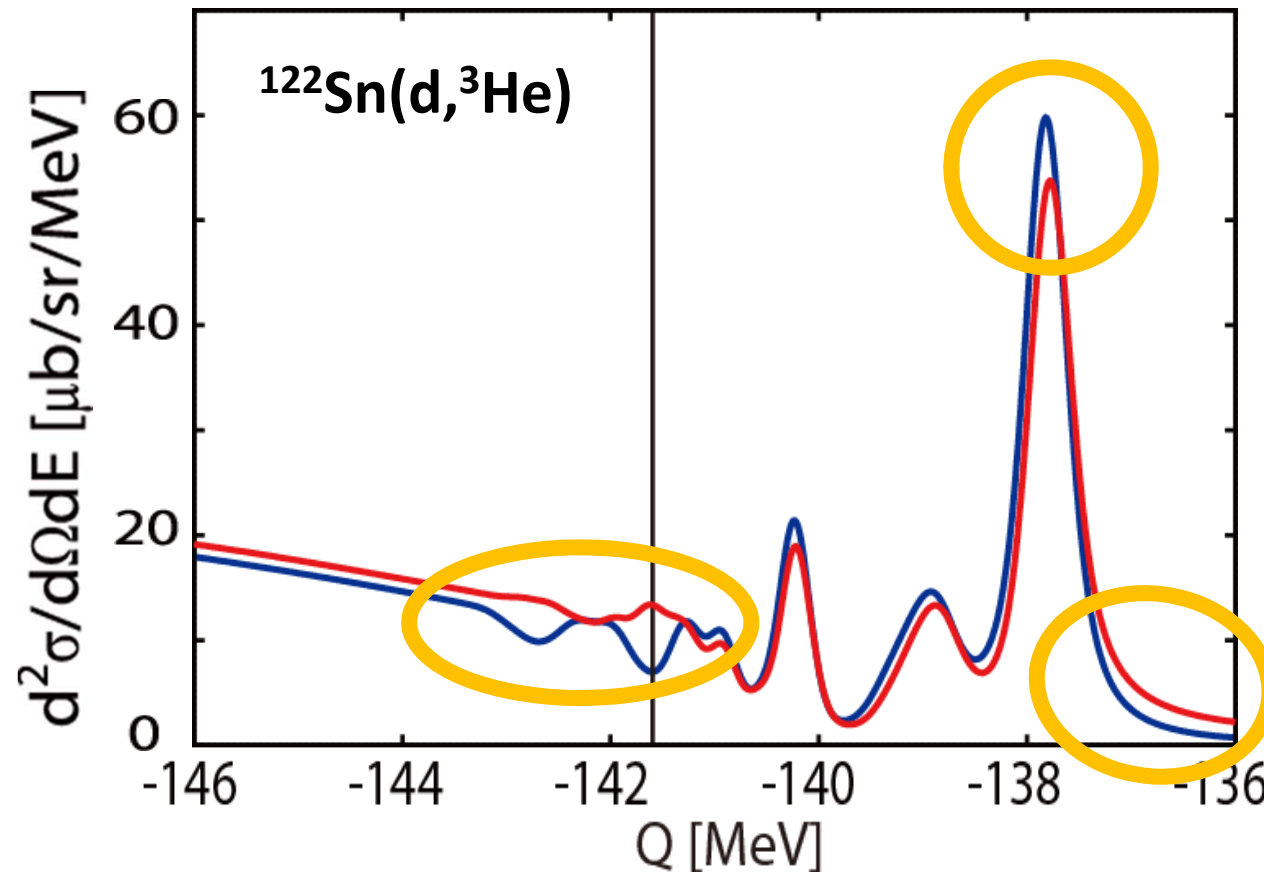
Neff



# Numerical results: Green vs. Neff

➤  $^{122}\text{Sn}(d,^3\text{He})$  spectra at 0 degrees

Energy resolution  
 $\Delta E=300\text{keV}$



## Differences between both spectra

(1) Near threshold, (2) Height and position of peak, (3) Tail of peak structure

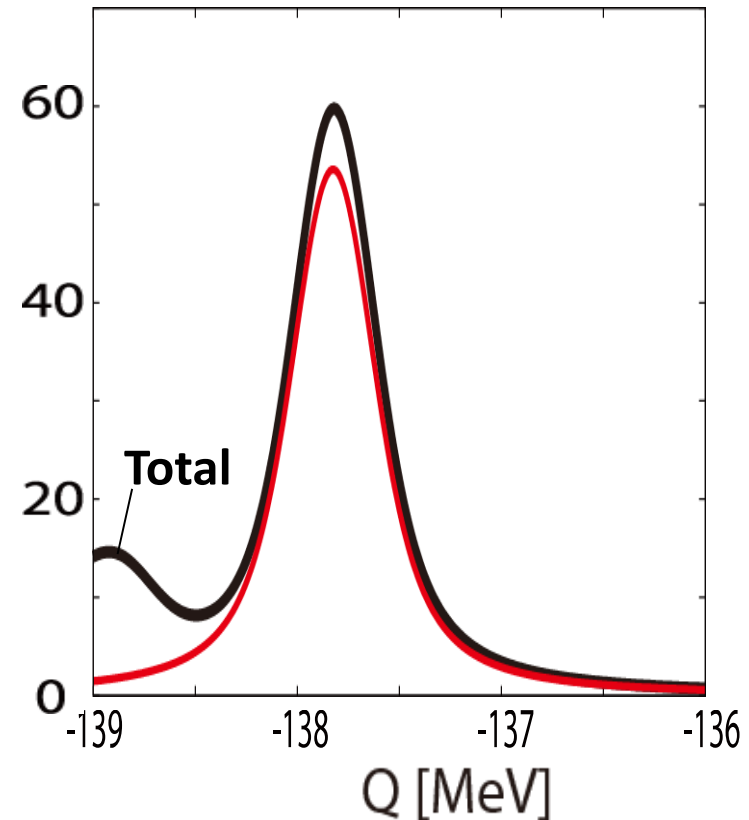
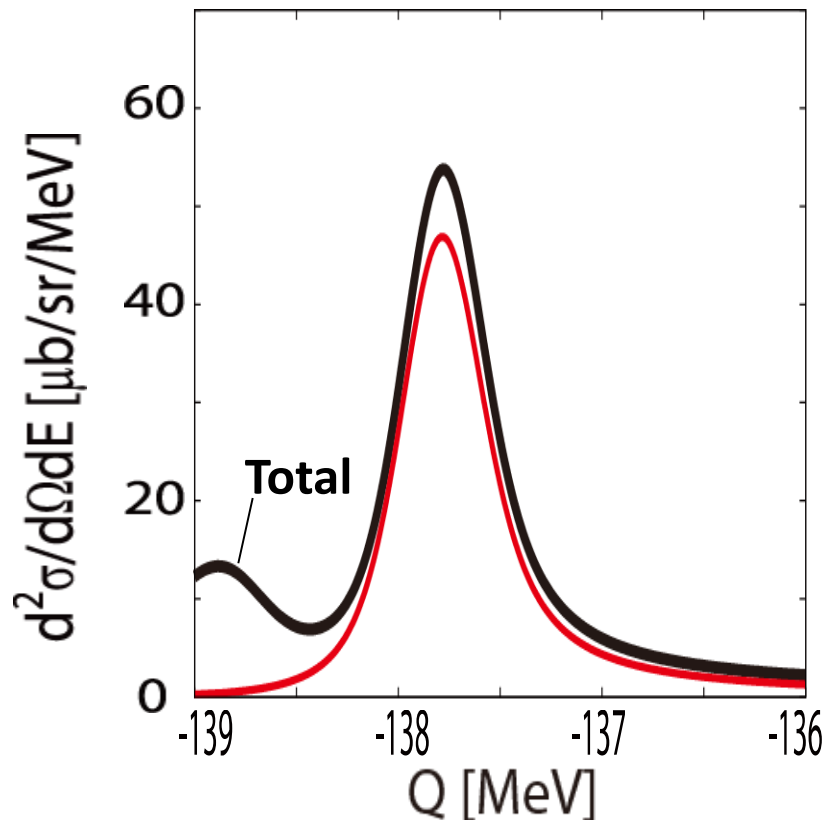
# Numerical results: Green vs. Neff

Energy resolution  
 $\Delta E=300\text{keV}$

We focus on subcomponent of  $(1s)_\pi \otimes (3s_{1/2})_n^{-1}$

**Green**

**Neff**



Different behavior of peak structure (**Green**: Asymmetric, **Neff**: Symmetric)

→ Precise theoretical spectrum is important to deduce pion properties in nuclei from future high resolution experiment

# Summary    **Theoretical Formation Spectra of pionic atoms**

## ➤ $^{122}\text{Sn}(d,^3\text{He})$ spectra at finite angles

- ✓ Spectra have strong angular dependence.
- ✓ Different subcomponents dominate at different angles.  
 $(1s)_\pi$ ,  $(2s)_\pi$ : 0 degrees,  $(2p)_\pi$ : 2degrees
- ➔ Simultaneous observation of various states in one nuclide (Good!)
- ✓ Comparison with theory and experiment at finite angles
  - **Qualitative** behavior --- reasonable agreements
  - **Quantitative** behavior --- some problems

## ➤ $^{117}\text{Sn}(d,^3\text{He})$ spectra: Odd-neutron nuclear target

- ✓ We can see clear peak structure of  $[(1s)_\pi \otimes ^{116}\text{Sn}(0^+)]$ .
  - **No residual interaction effect**
- ➔ More precise information than that of even target case can be expected.
- ✓ Absolute value of cross section are significantly smaller.

## ➤ **Updated Theoretical Calculation**

- $^{122}\text{Sn}(d,^3\text{He})$  spectra calculated by Green's Function Method
- ✓ We get **more precise formation spectrum theoretically** which is suited to be compared with high resolution future experimental data.