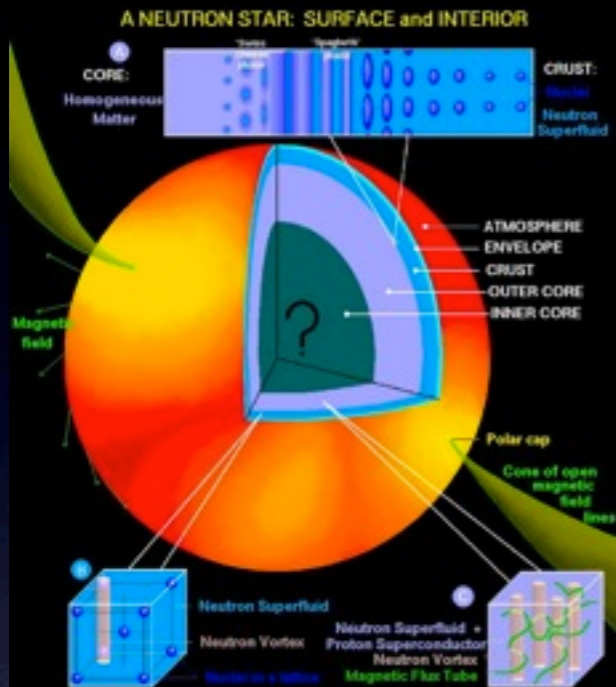


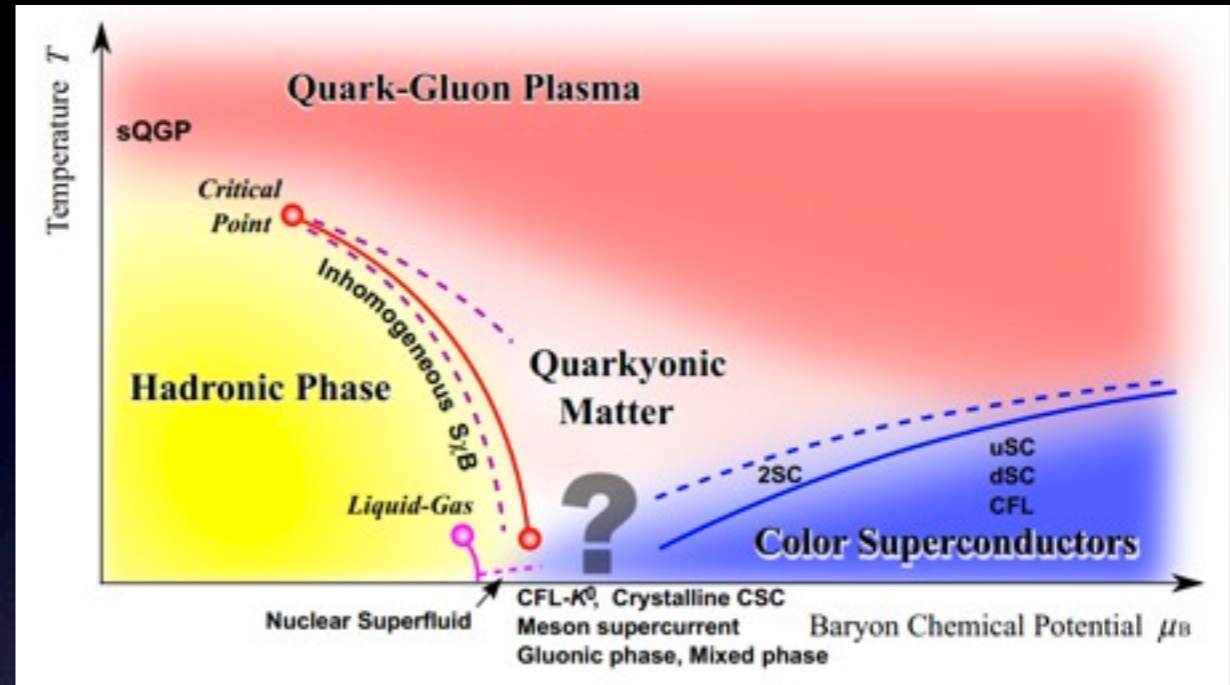
# Hadron-Quark Crossover and Neutron Star Observations

Kota Masuda (Univ. of Tokyo / RIKEN)  
with Tetsuo Hatsuda (RIKEN) and Tatsuyuki Takatsuka (RIKEN)

## NS observations



## QCD phase diagram



Fukushima, Hatsuda (2010)

## Mass

$$(1.97 \pm 0.04)M_{\odot}$$

Demorest *et al.* (2010)

$$(2.01 \pm 0.04)M_{\odot}$$

Antoniadis *et al.* (2013)

## Cooling

Cooling of CAS-A  
Heinke *et al.* (2010)

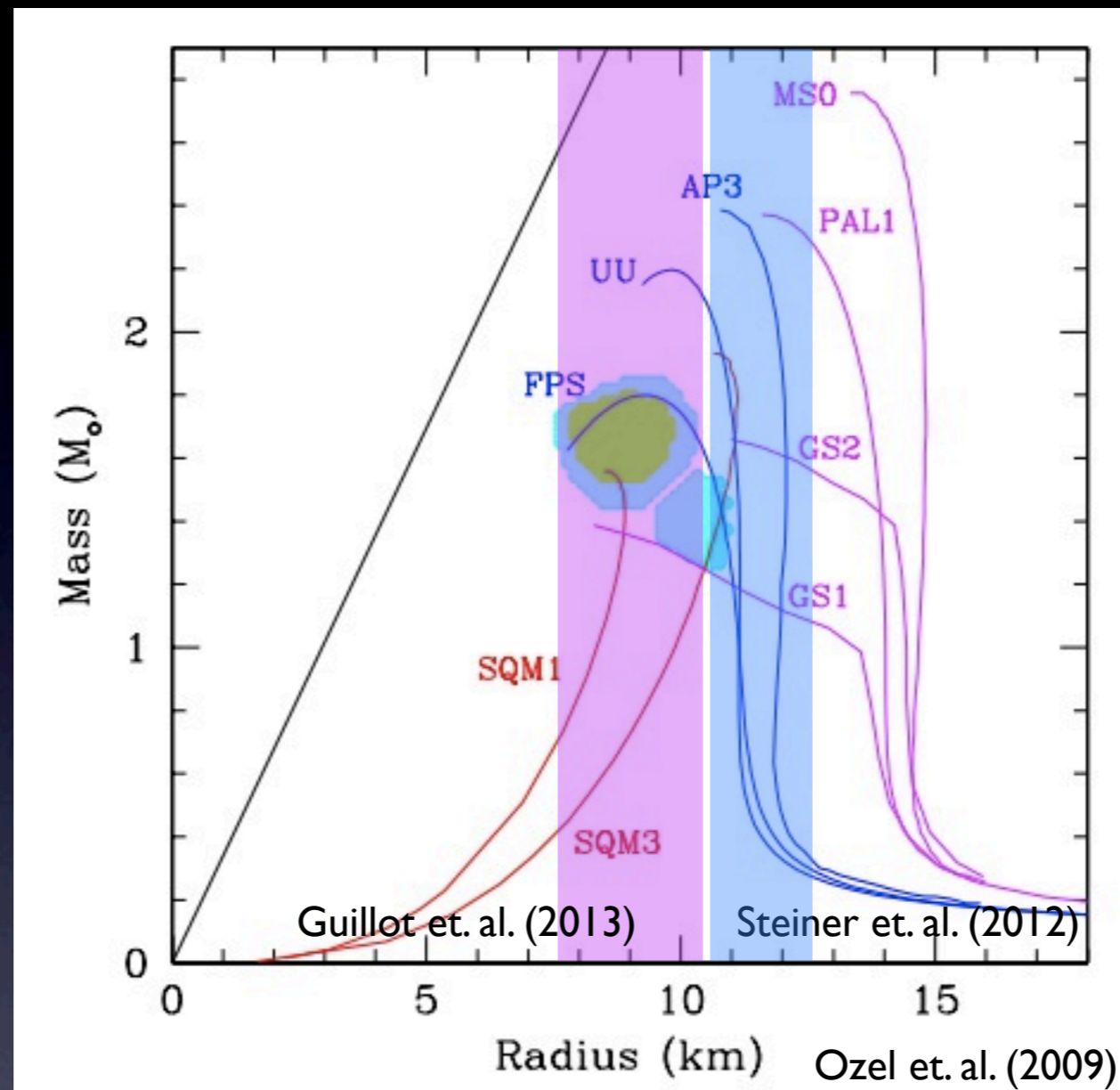
## EOS

Relation to stiffness of EOS and the existence of the exotic components ?

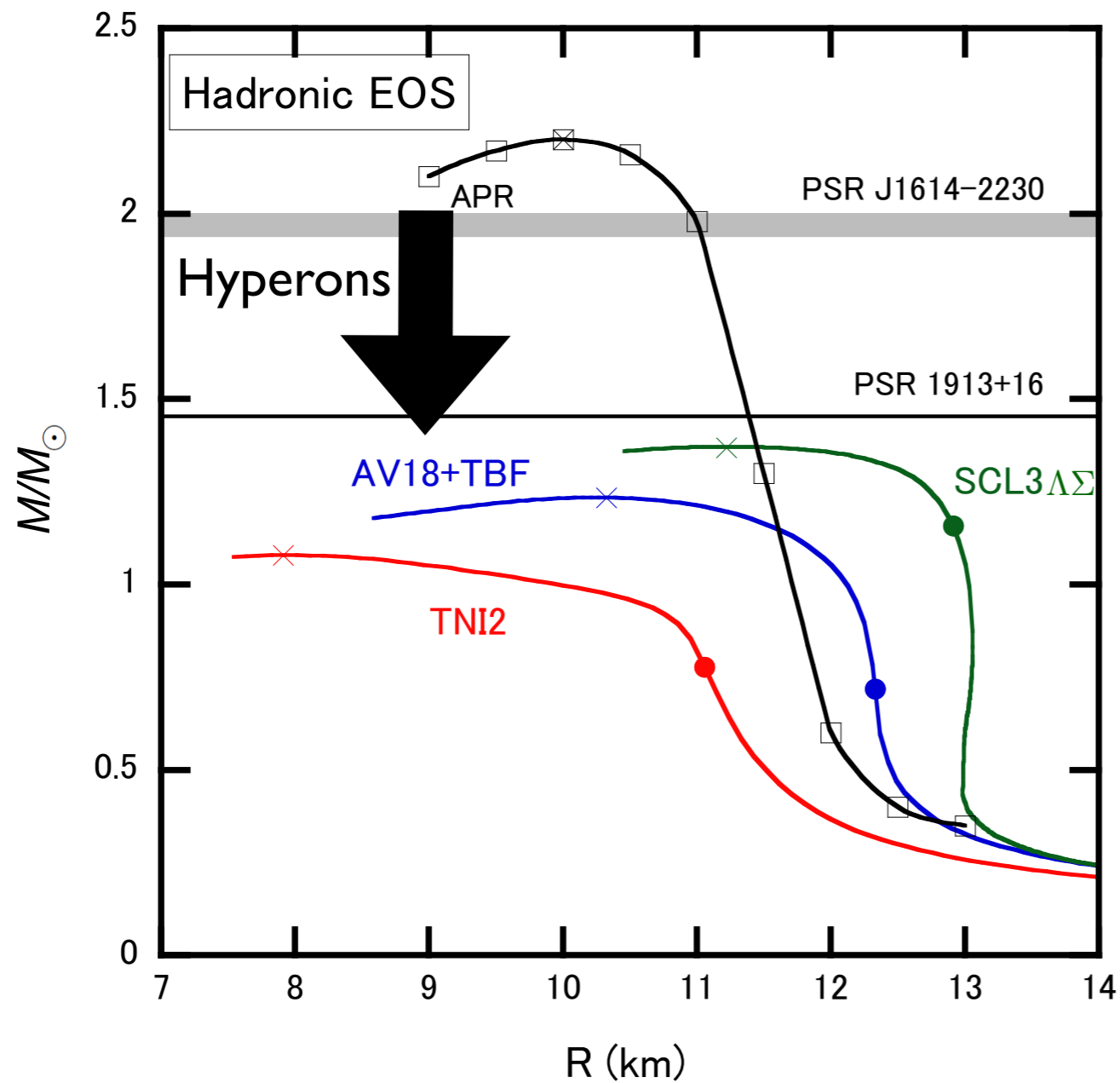
## Superfluid / Superconducting phase

Relation to nucleon and quark superfluidity inside NSs ?

# Neutron Star Radius



- Radius can make constraints on EOS at low density region
- However, there are some different estimations.



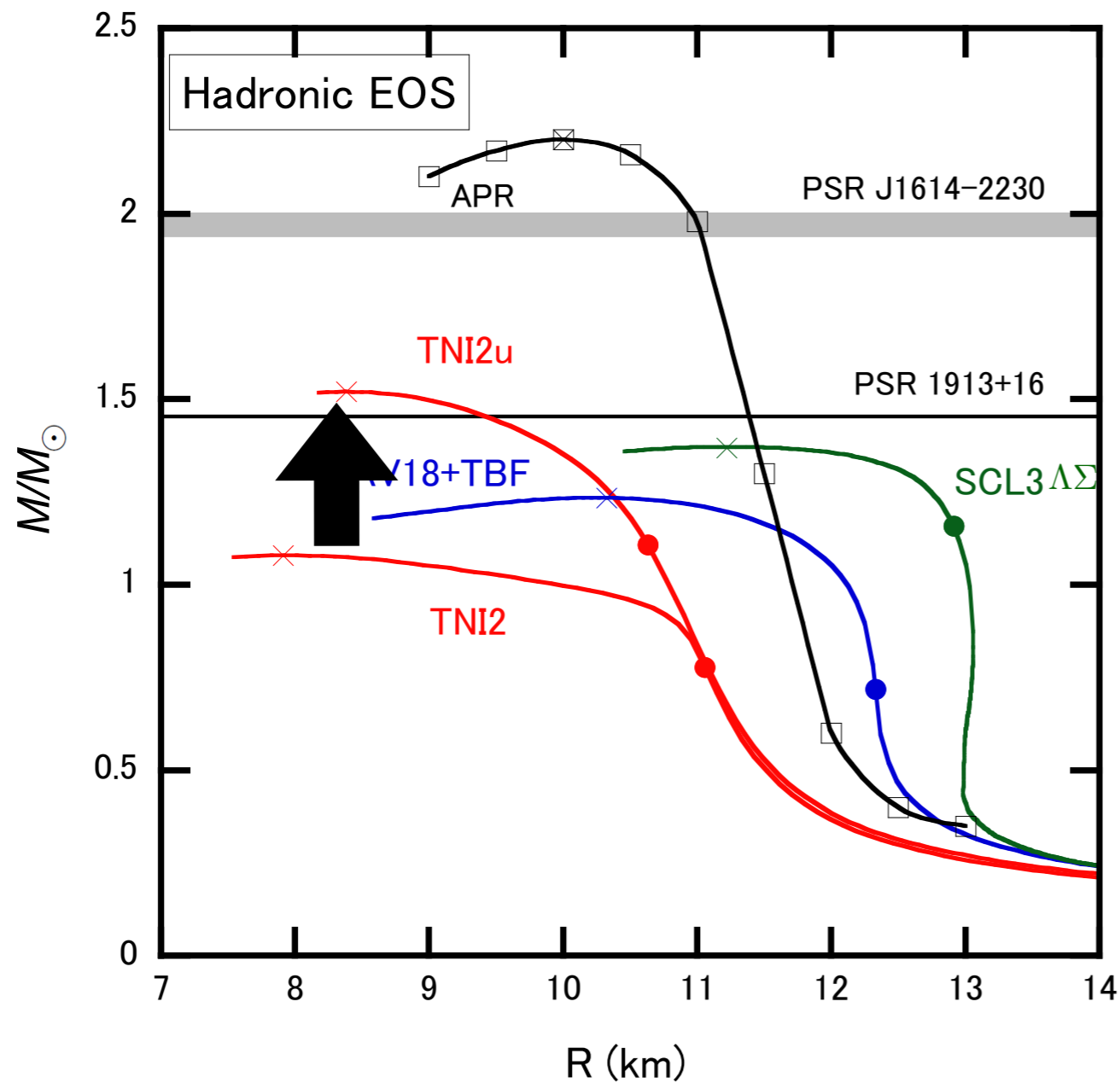
	(1)	(2)	(3)
	AV18+TBF	TNI2	SCL3ΛΣ
Method	BHF	BHF	RMF
2NF	AV18	Reid	
3NF	Yes	Yes	No
Hyperons	Yes	Yes	Yes

(1) Baldo *et al.* (2000), Schulze *et al.* (2010)

(2) Nishizaki *et al.* (2001,2002)

(3) Tsubakihara *et al.* (2010)

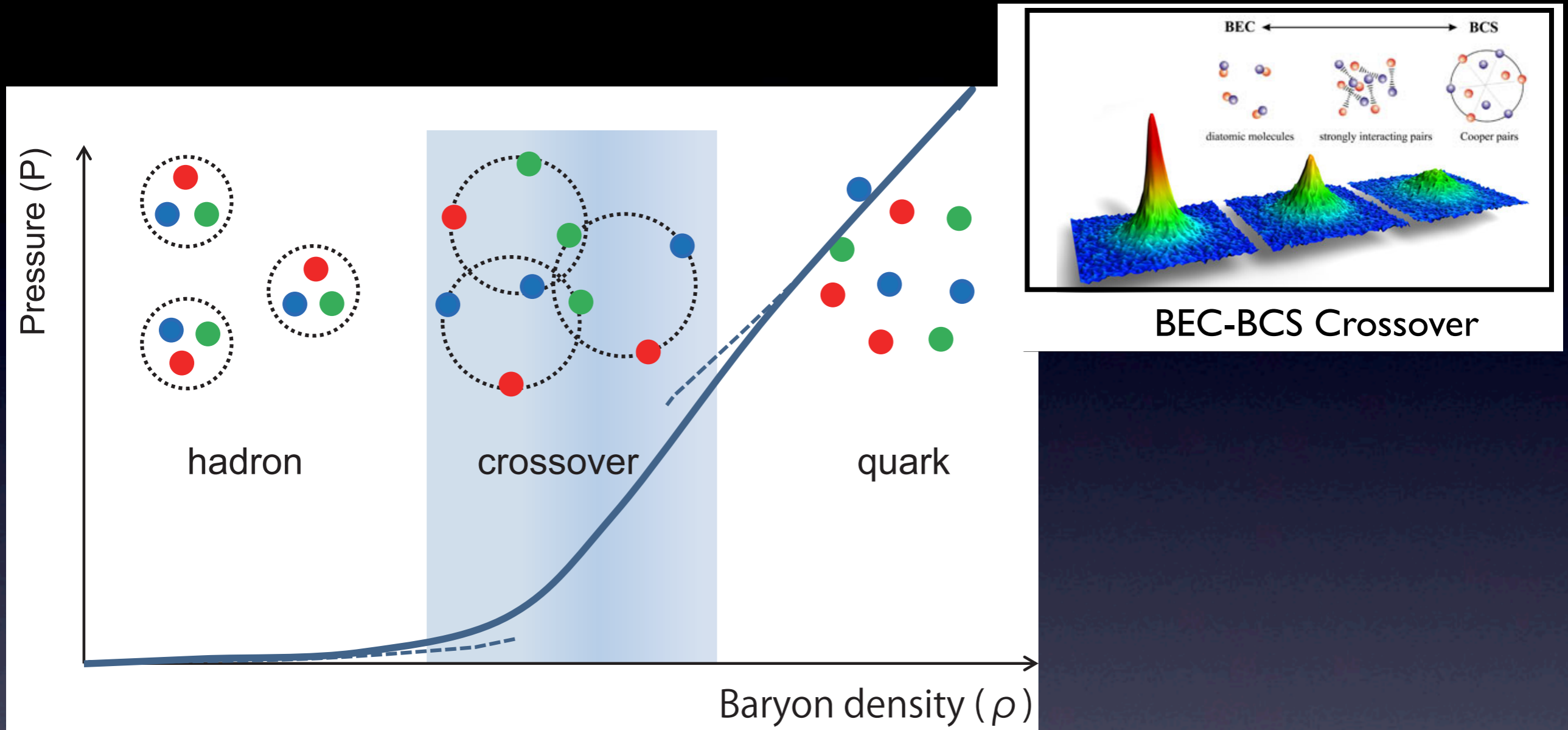
- Hyperons soften EOS → Maximum mass is less than  $1.44M_{\odot}$



	TNI2	TNI2u
“NNN”	Yes	Yes
“NNY” “NYY” “YYY”	No	Yes

- Universal 3-body force stiffens EOS → Maximum mass is larger than  $1.44M_{\odot}$
- However maximum mass cannot exceed  $2M_{\odot}$

# Hadron-Quark Crossover



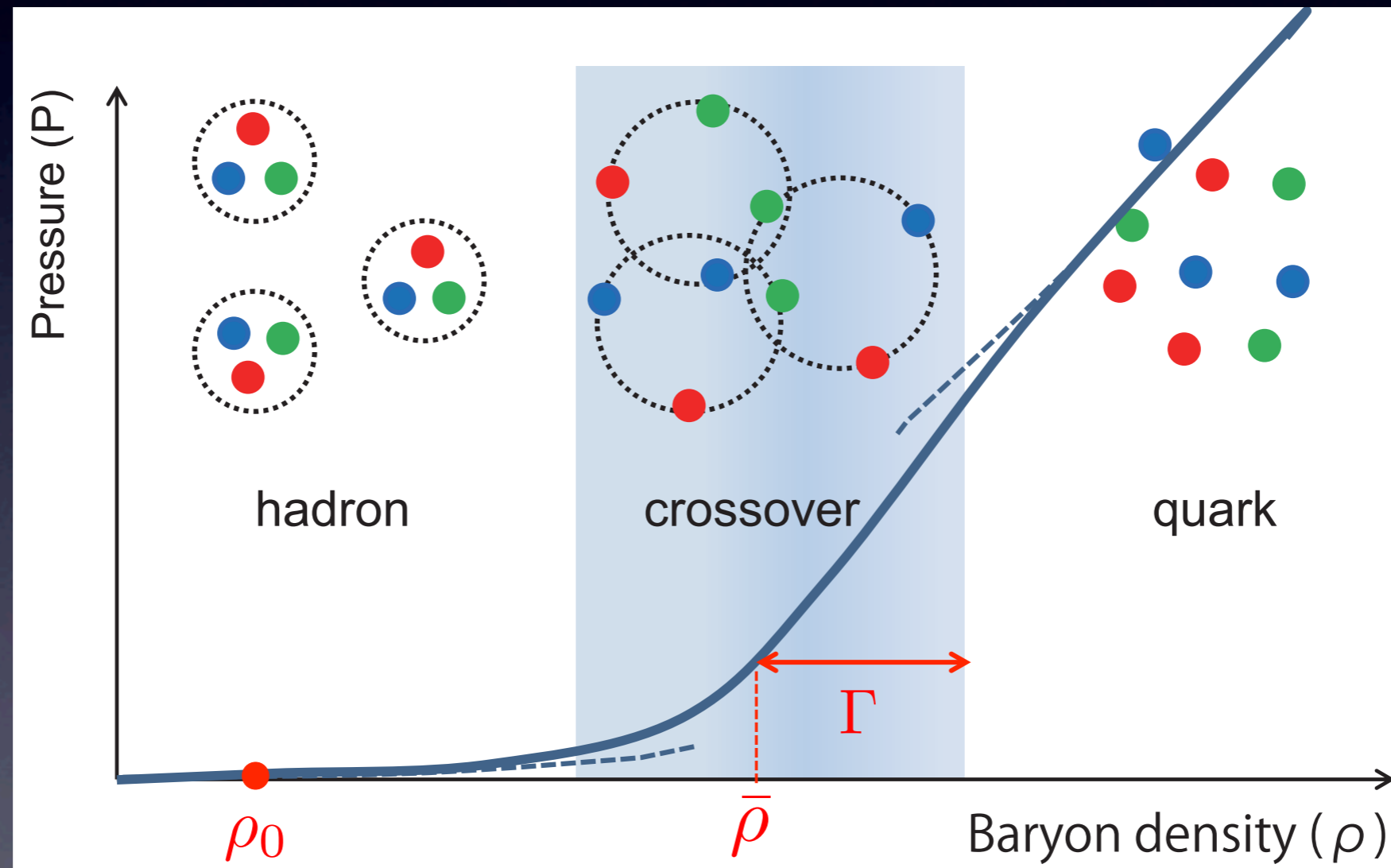
We seek the possibility of crossover

Ref.)  
Baym (1979)  
Celik, Karsch and Satz (1980)  
Fukushima (2004)  
Hatsuda, Tachibana, Yamamoto and Baym (2006)

# Method of Interpolation

Phenomenological interpolation:  $P(\rho)$

$$\begin{cases} P = p_H \times f_- + p_Q \times f_+ & f_{\pm} = \frac{1 \pm \tanh(\frac{\rho - \bar{\rho}}{\Gamma})}{2} \\ P = \rho^2 \frac{\partial(\varepsilon/\rho)}{\partial \rho} \end{cases}$$



Condition for  $\bar{\rho}$  :  $f_+ < 0.1$  at  $\rho_0 \rightarrow \bar{\rho} > \rho_0 + 2\Gamma$

(2+1)-flavor NJL Lagrangian (u,d,s,  $e^-$ ,  $\mu^-$ )

$$L_{NJL} = \bar{q}(i\not{\partial} - m)q + \frac{G_s}{2} \sum_{a=0}^8 [(\bar{q}\lambda^a q)^2 + (\bar{q}i\gamma_5\lambda^a q)^2] - \frac{g_v}{2} (\bar{q}\gamma^\mu q)^2 + G_D [\det \bar{q}(1 + \gamma_5)q + \text{h.c.}]$$

$$\downarrow$$

$$\Omega = -\frac{T}{V} \ln Z \quad \left\{ \begin{array}{l} M_i = m_i - 2G_s \langle \bar{q}_i q_i \rangle - 2G_D \langle \bar{q}_j q_j \rangle \langle \bar{q}_k q_k \rangle \\ \mu_i \rightarrow \mu_i^{\text{eff}} \equiv \mu_i - g_v \sum_i \langle q_i^\dagger q_i \rangle \end{array} \right.$$

$$= \Omega_q(M, \mu^{\text{eff}}) + \Omega_l + G_s \sum \langle \bar{q}_i q_i \rangle^2 + 4G_D \langle \bar{q}_i q_i \rangle \langle \bar{q}_j q_j \rangle \langle \bar{q}_k q_k \rangle - \frac{1}{2} g_v \left( \sum_i \langle q_i^\dagger q_i \rangle \right)^2$$

$$\Omega_q(\mu^{\text{eff}}) = -T \sum_i \sum_l \int \frac{d^3 p}{(2\pi)^3} \text{Tr} \ln \left( \frac{1}{T} S_i^{-1}(i\omega_l, \vec{p}) \right),$$

$$S_i^{-1} = \not{p} - \mu^{\text{eff}} \gamma^0 - M_i, \quad p^0 = i\omega_l = (2l + 1)\pi T$$

Gap equations:  $\frac{\partial \Omega}{\partial \langle \bar{q}_i q_i \rangle} = 0$

Parameter sets

cutoff (MeV)	$G_s \Lambda^2$	$G_D \Lambda^5$	$m_{u,d}(\text{MeV})$	$m_s(\text{MeV})$
631.4	3.67	9.29	5.5	135.7

Hatsuda and Kunihiro (1994)

$$0 \leq g_v \leq 1.5 G_s$$

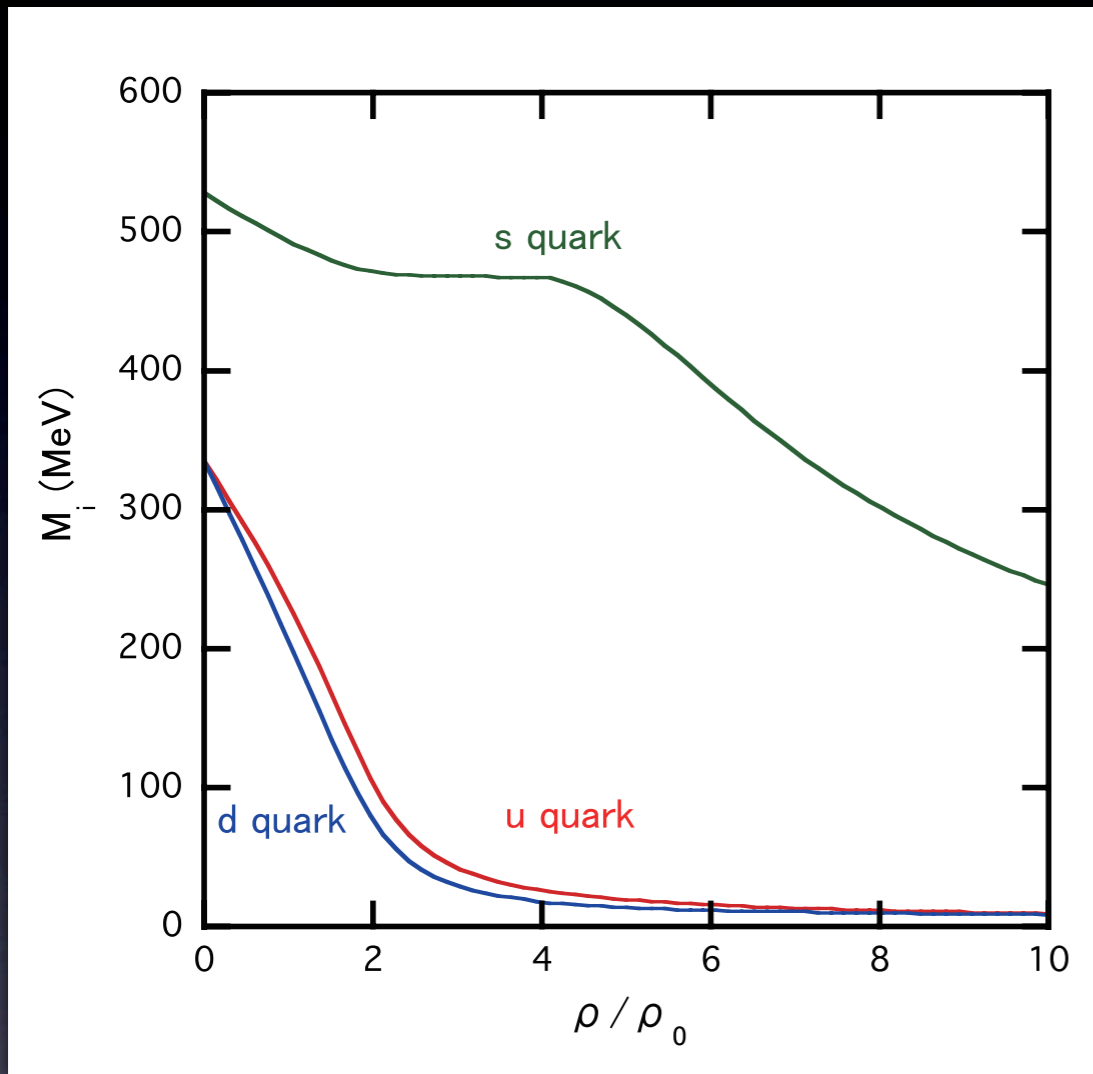
(Fierz:  $G_V = 0.5 G_s$ )

Bratovic et al. (2012)

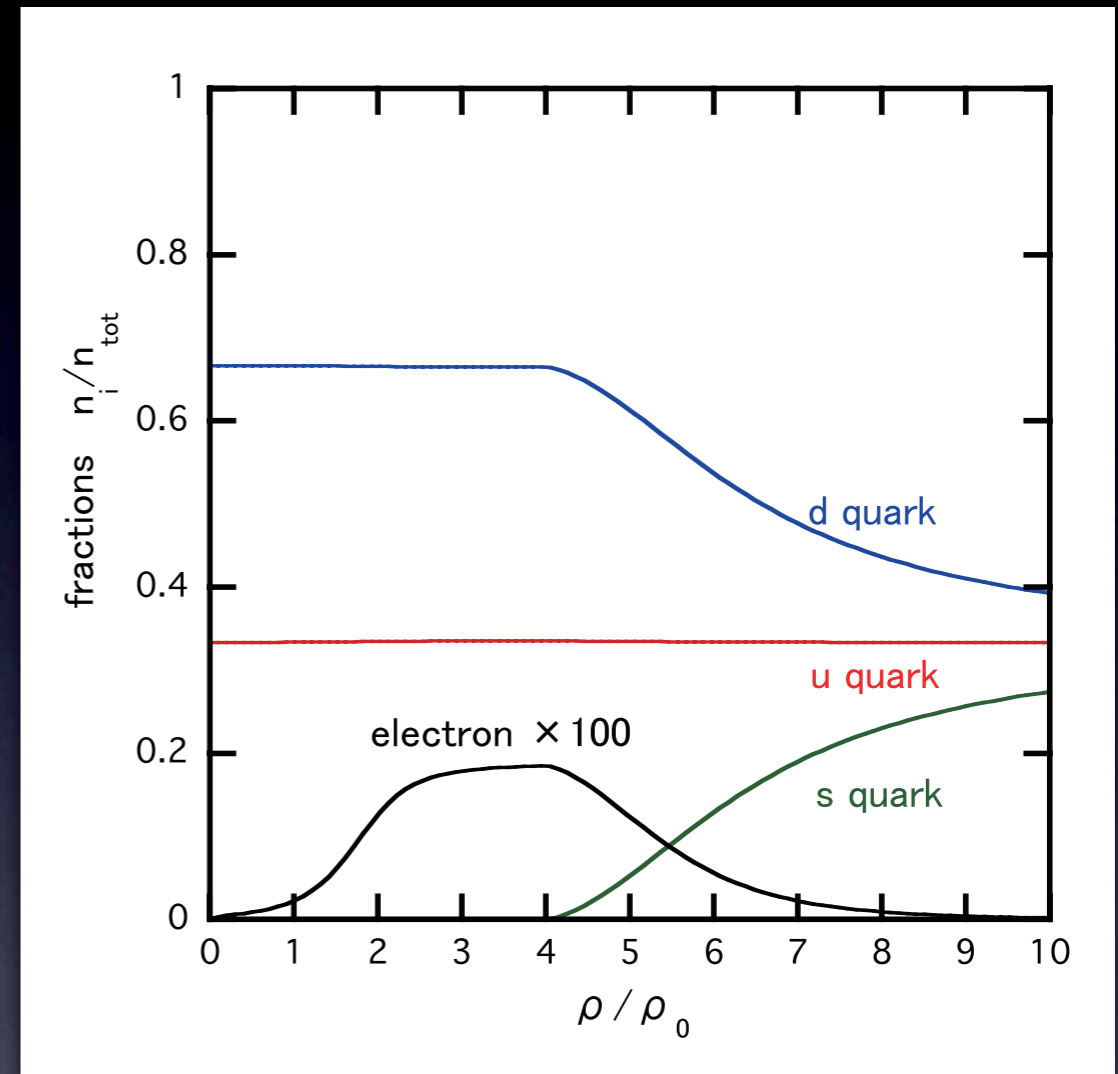
**Conditions:**  
 1. beta-equilibrium  
 2. charge neutrality



## Constituent mass



## Number fraction

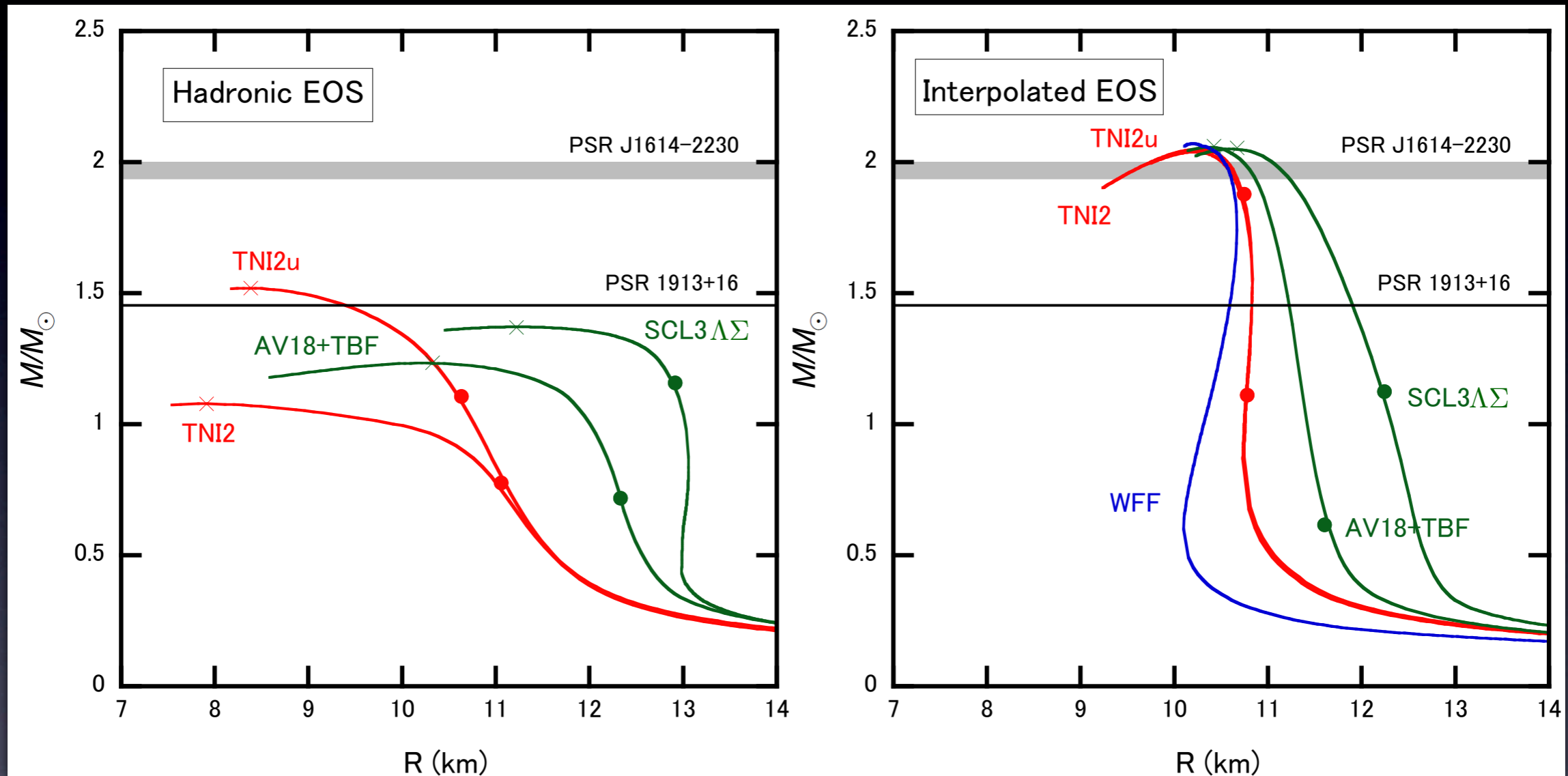


### Chiral restoration

- u,d quark : low densities
- s quark :  $4 \rho_0$
- s quark starts to appear above  $4 \rho_0$
- SU(3) flavor symmetric matter at high densities
- muon does not appear due to  $\left\{ \begin{array}{l} \text{s quark} \\ \text{charge neutrality} \end{array} \right.$
- figures do not depend on the magnitude of vector interaction

# Results (I): Effects of Q-EOS

M-R relation  $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$   $g_v = G_S$

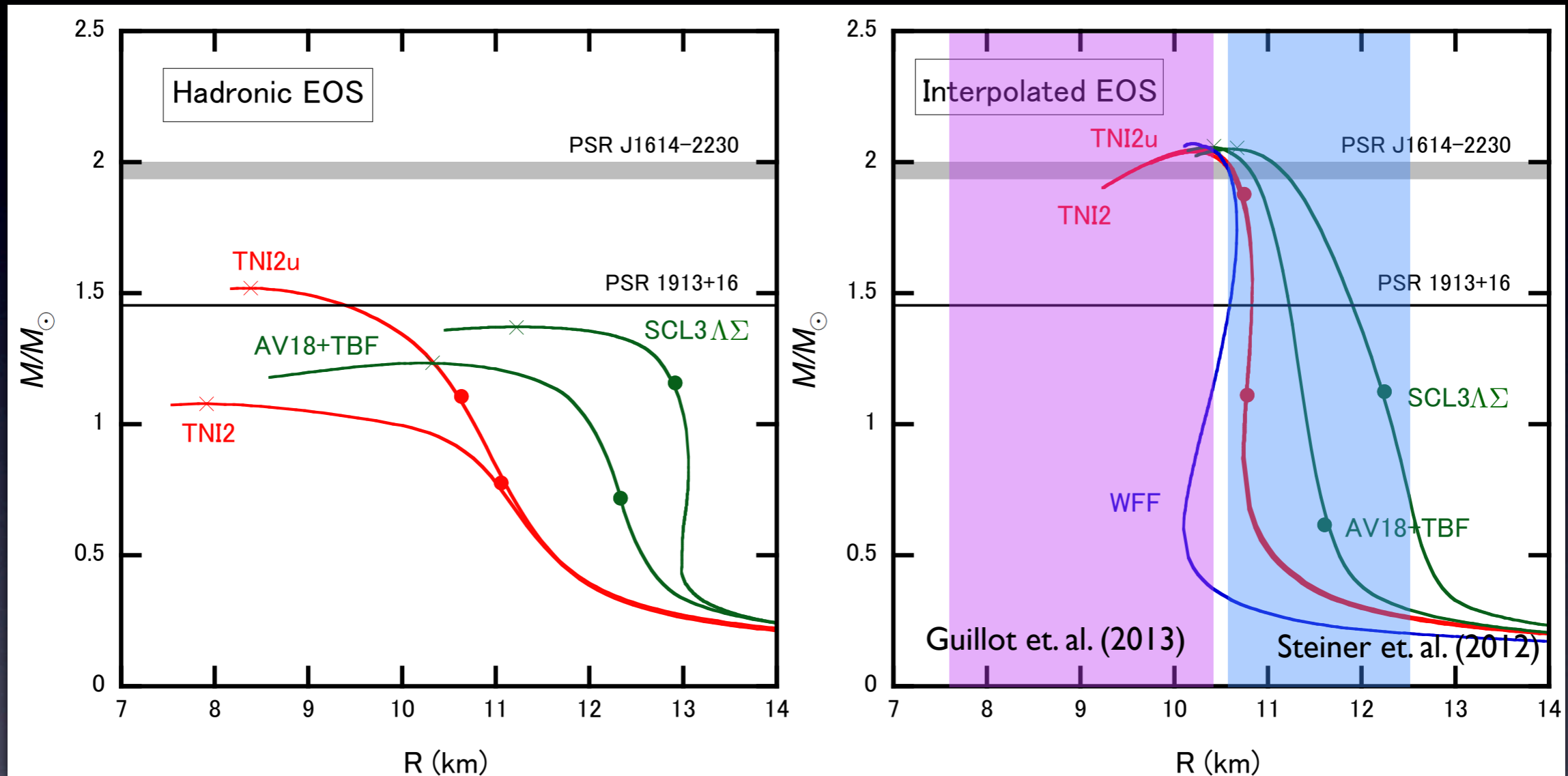


- Maximum mass exceeds 2 solar mass, no matter what kind of H-EOS is taken

# Results (I): Effects of Q-EOS

9/16

M-R relation  $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0) \quad g_v = G_S$

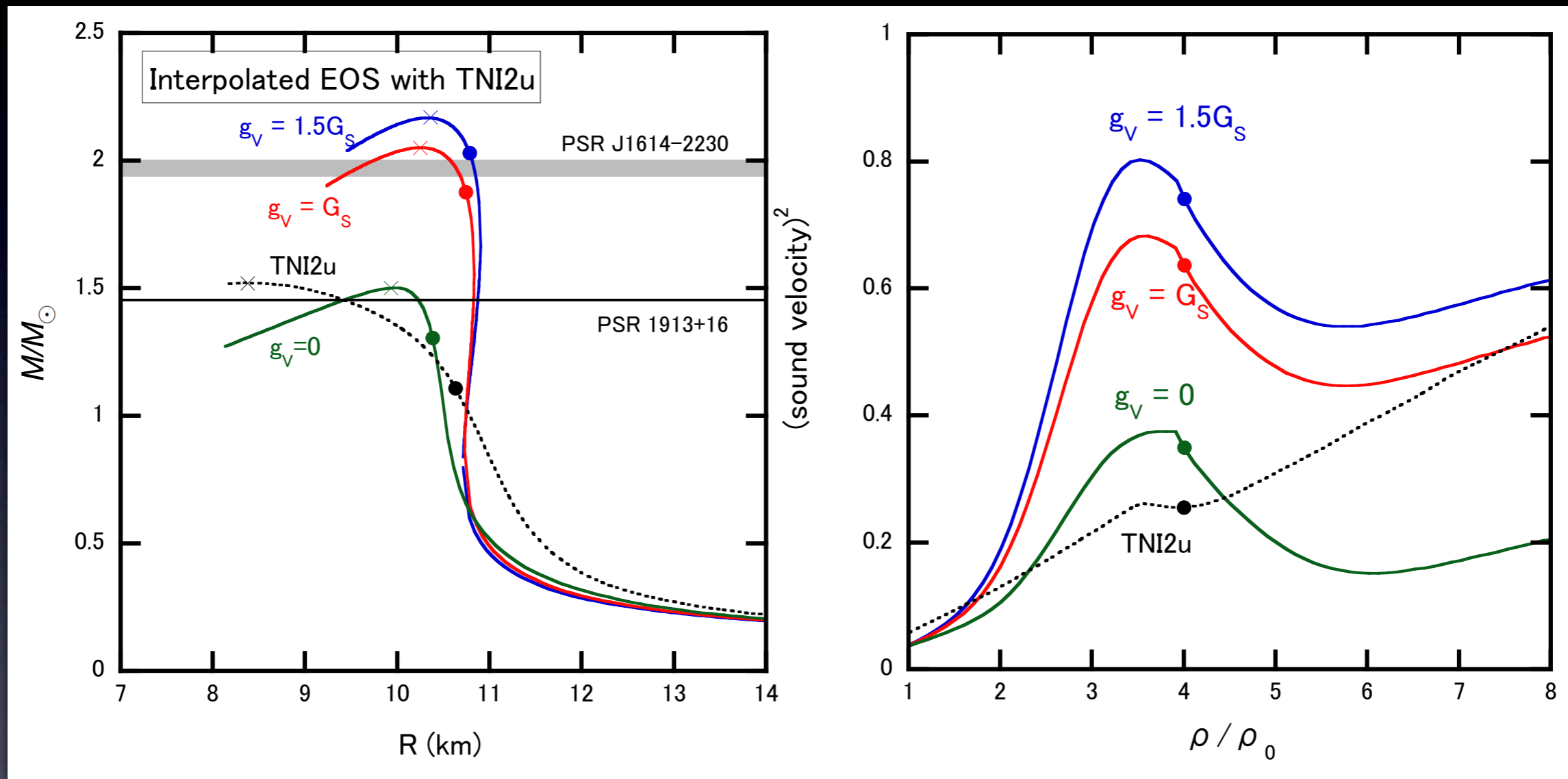


- Maximum mass exceeds 2 solar mass, no matter what kind of H-EOS is taken
- Radius is essentially controlled by hadronic EOS.

# Results (2): Sound Velocity

10/16

M-R relation  $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0) \quad g_v = G_S$

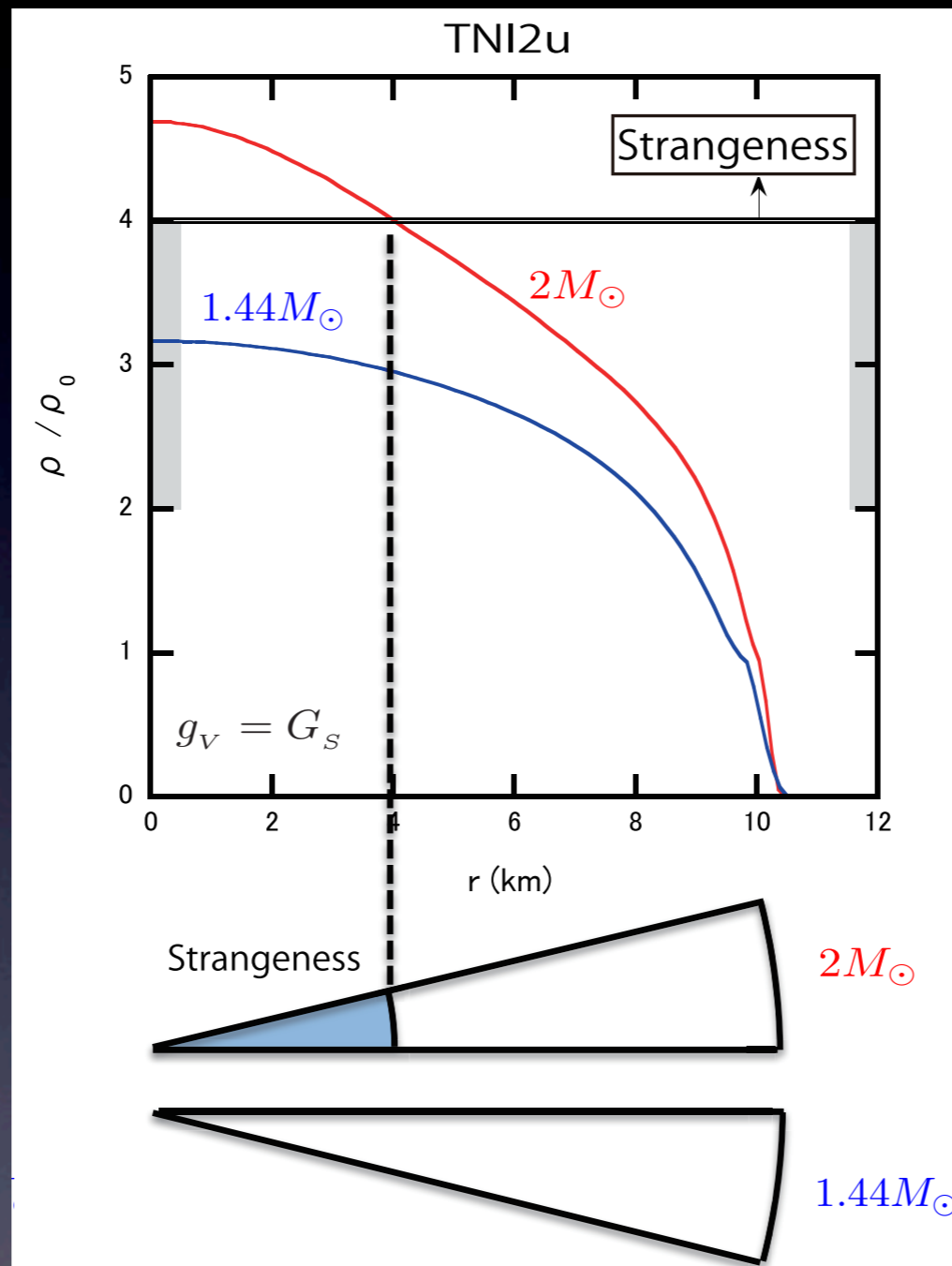


- The emergence of strangeness softens EOS
- Due to the interpolation, the sound velocity increases rapidly in the crossover region

# Results (3): Strangeness Core

11/16

$\rho - r$  relation  $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$   $g_v = G_S$

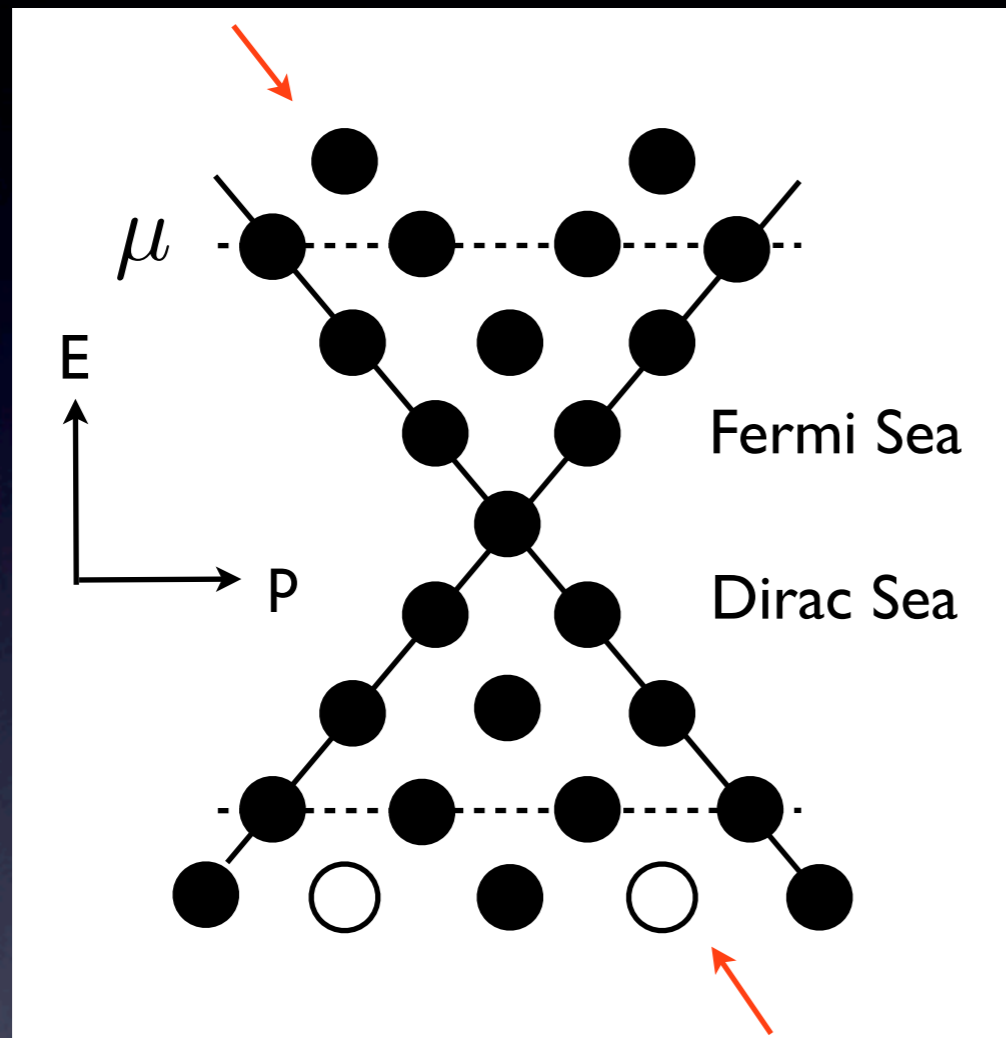


Typical NSs with universal 3-body force do not include strangeness inside themselves

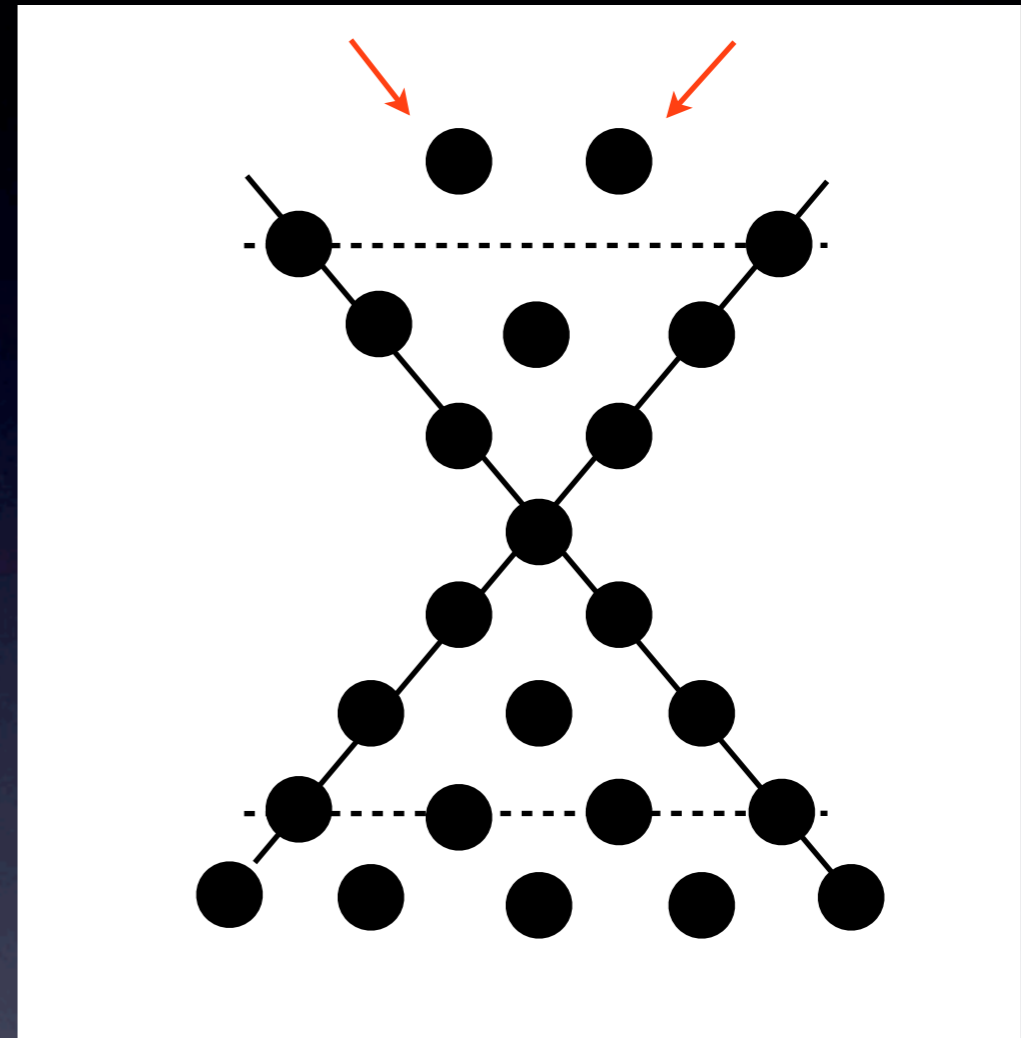
→ possibility of solving cooling problem

# Color Superconductivity (CSC)

- Chiral Condensate



- Diquark Condensate



Alford

- NJL model

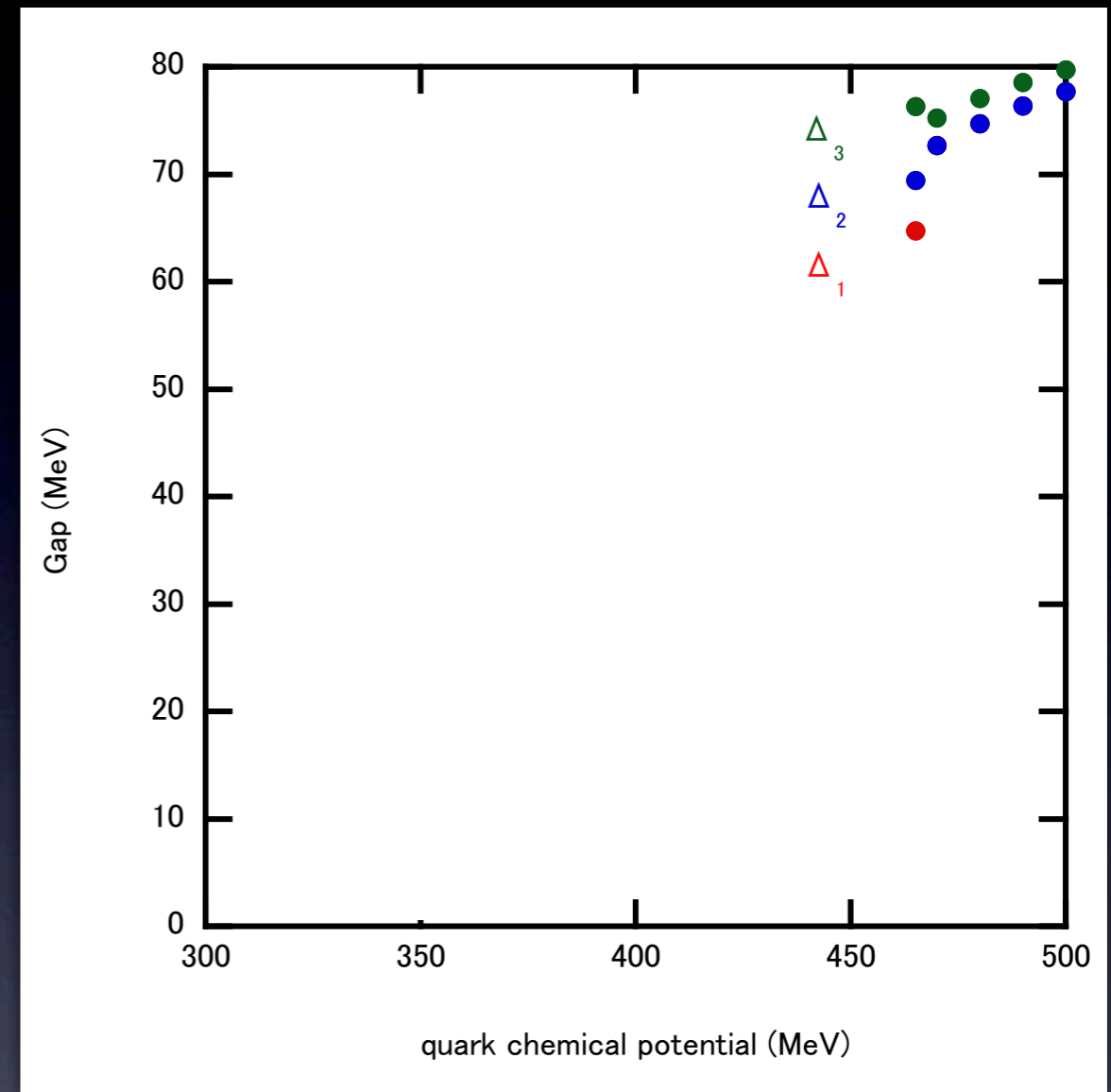
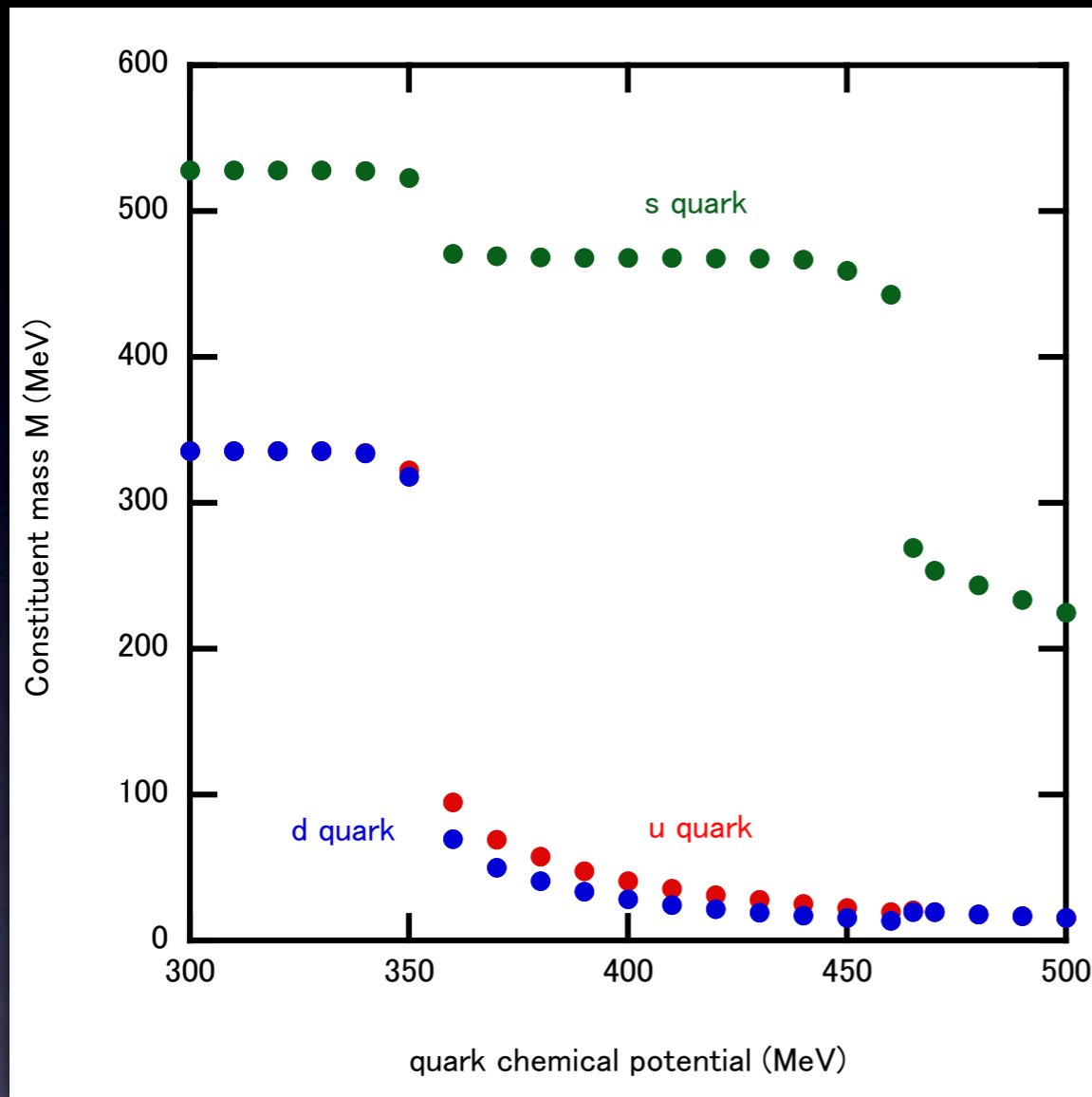
$$L_{\text{CSC}} = L_{\text{NJL}} + \frac{H}{2} \sum_{A=2,5,7} \sum_{A'=2,5,7} (\bar{q} i \gamma_5 \tau_A \lambda_{A'} C \bar{q}^T) (q^T C i \gamma_5 \tau_A \lambda_{A'} q)$$

$$H = \frac{3}{4} G_s$$

(Fierz)

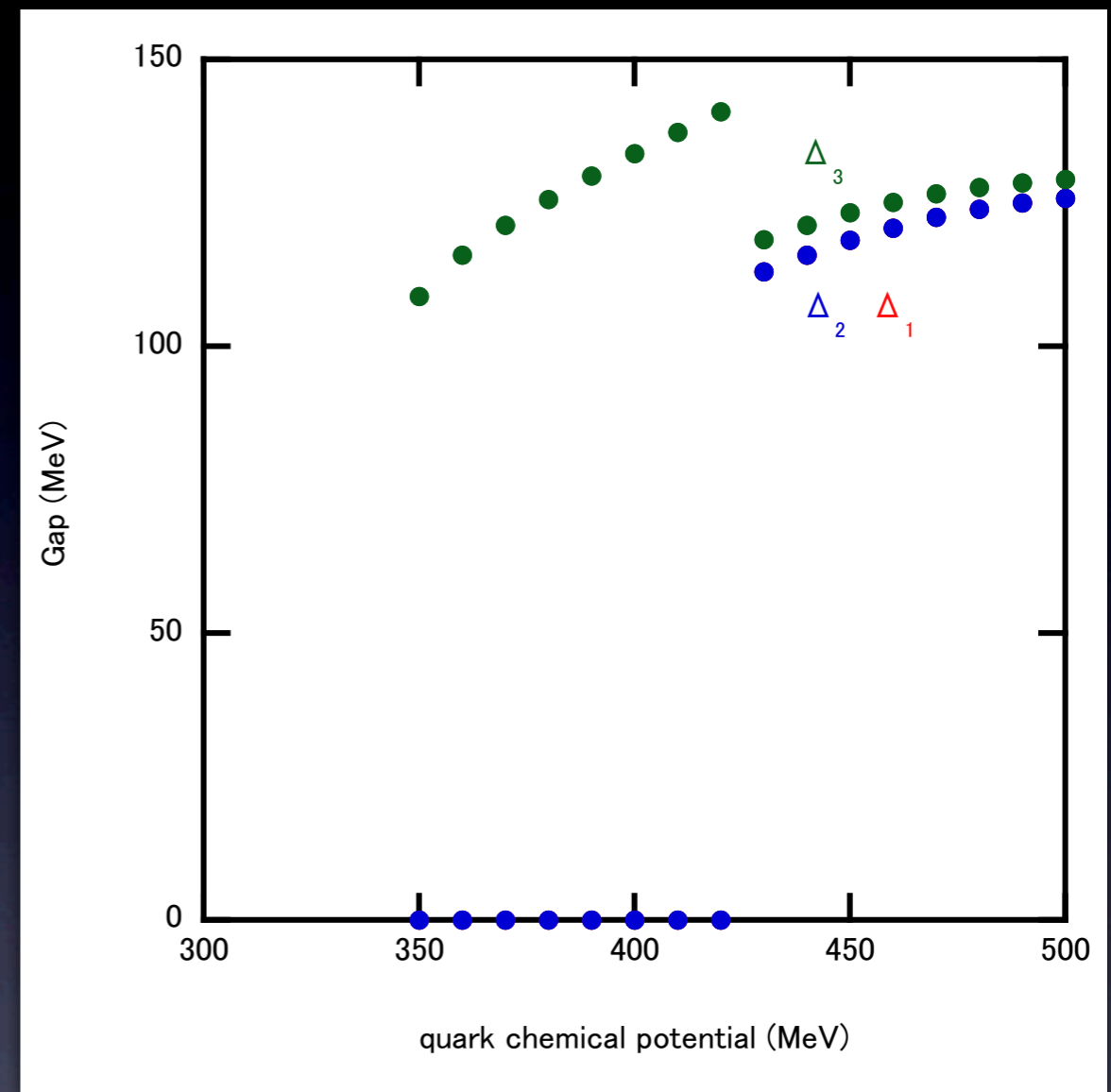
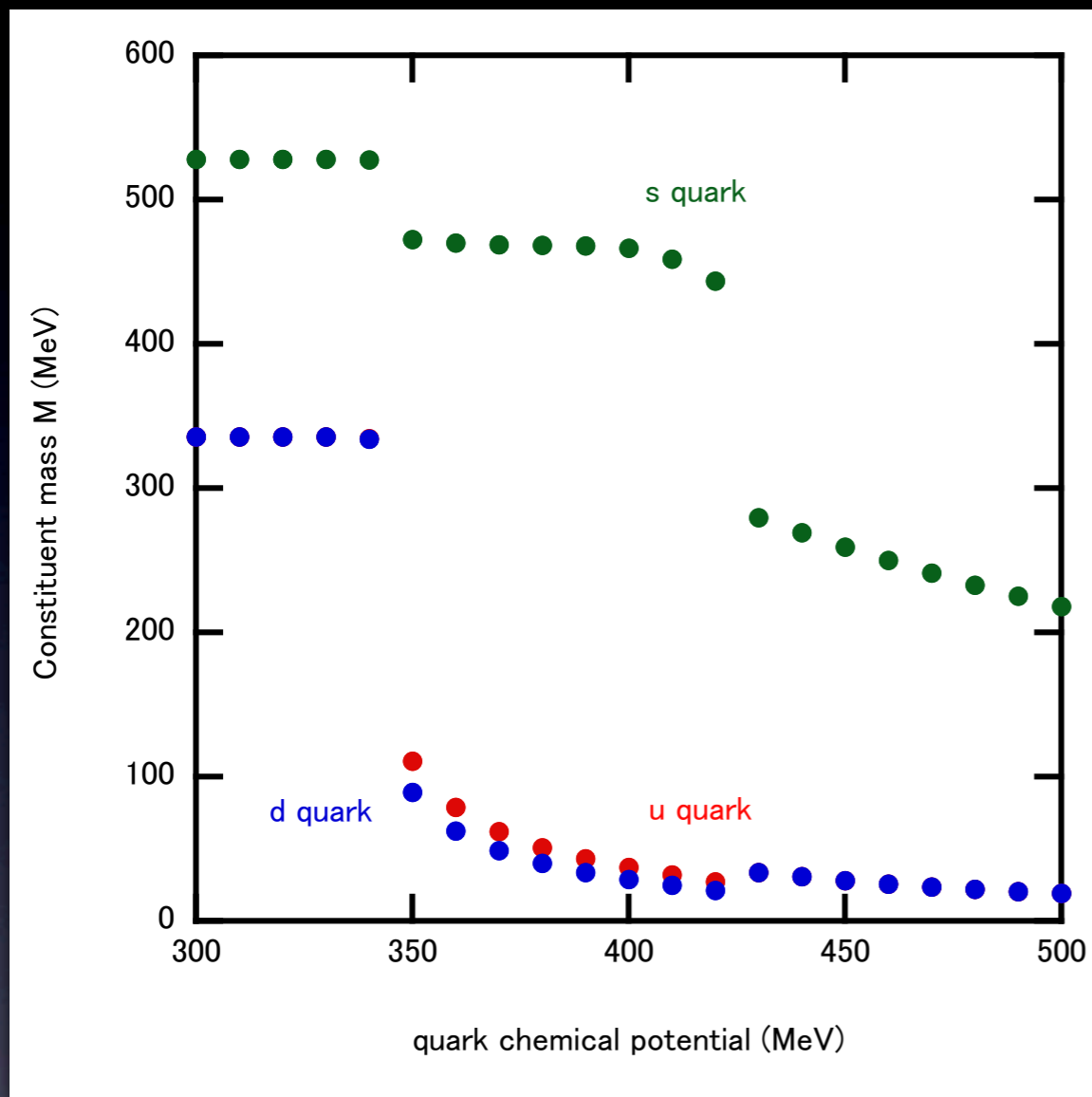
# Results (4): Case I $H = \frac{3}{4}G_s$

$$g_v = 0$$

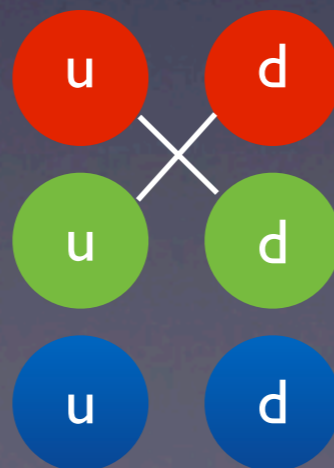


# Results (5): Case 2 $H = G_s$

$$g_v = 0$$



2SC phase



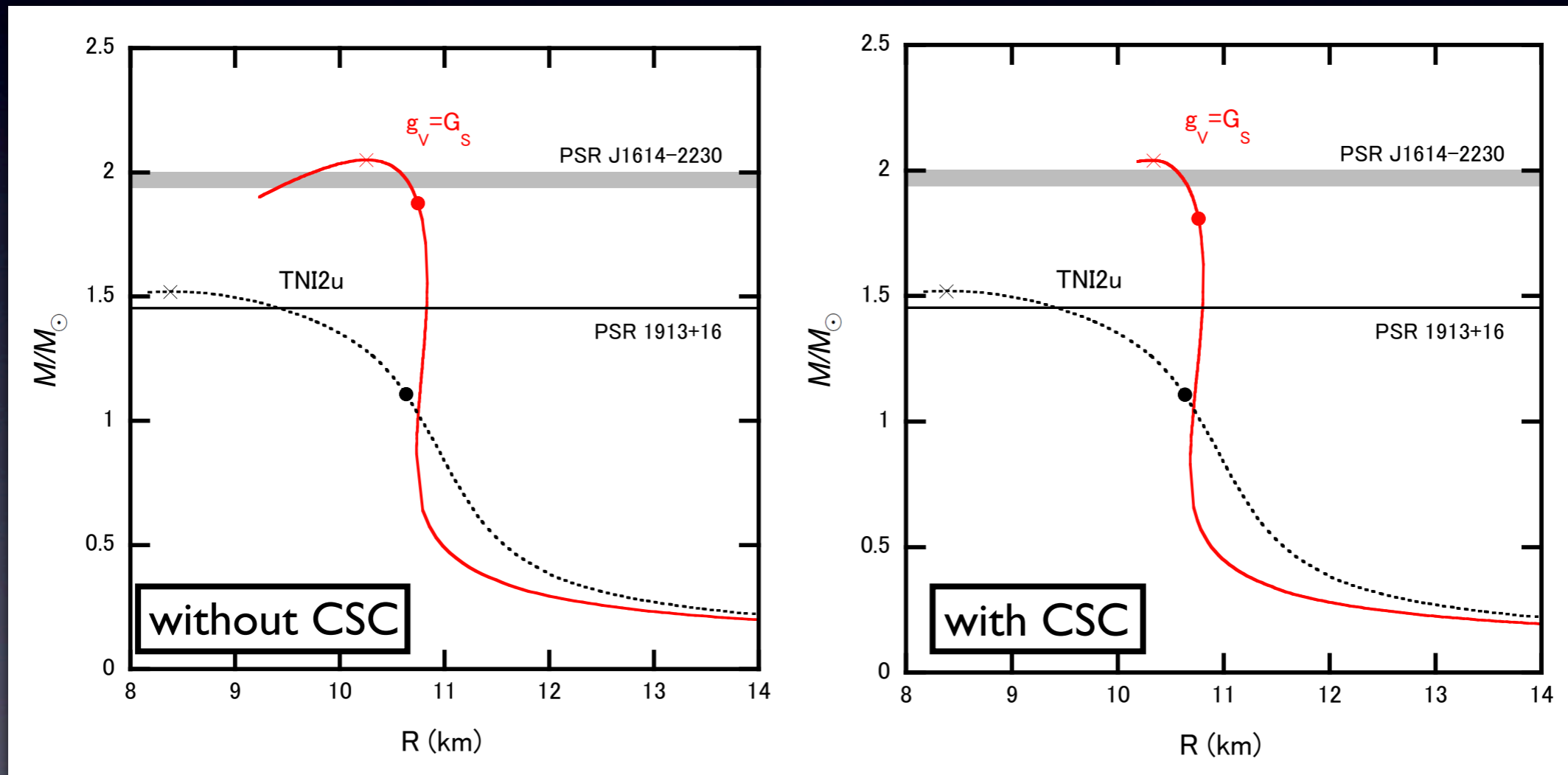


# Results (6): Effects of CSC

Diquark condensation with  $J^P = 0^+$

$$L_{\text{CSC}} = L_{\text{NJL}} + \frac{H}{2} \sum_{A=2,5,7} \sum_{A'=2,5,7} (\bar{q} i \gamma_5 \tau_A \lambda_{A'} C \bar{q}^T) (q^T C i \gamma_5 \tau_A \lambda_{A'} q)$$

M-R relation  $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$   $g_v = G_S$   $H = \frac{3}{4}G_S$



- CSC softens EOS, but the effects of CSC is very small

## Summary

- (1) Crossover occurs at relatively low densities
- (2) Quarks are strongly interacting at and above the crossover region

### EOS at $T=0$

(A) Interpolated EOS can become stiffer due to the presence of quark matter



Observation of very massive neutron star cannot exclude the existence of the quark matter core

(B) CSC phase does not have effects on the maximum mass

However, CSC may have large effect on phenomena related to transport.

### \* Other Characteristics:

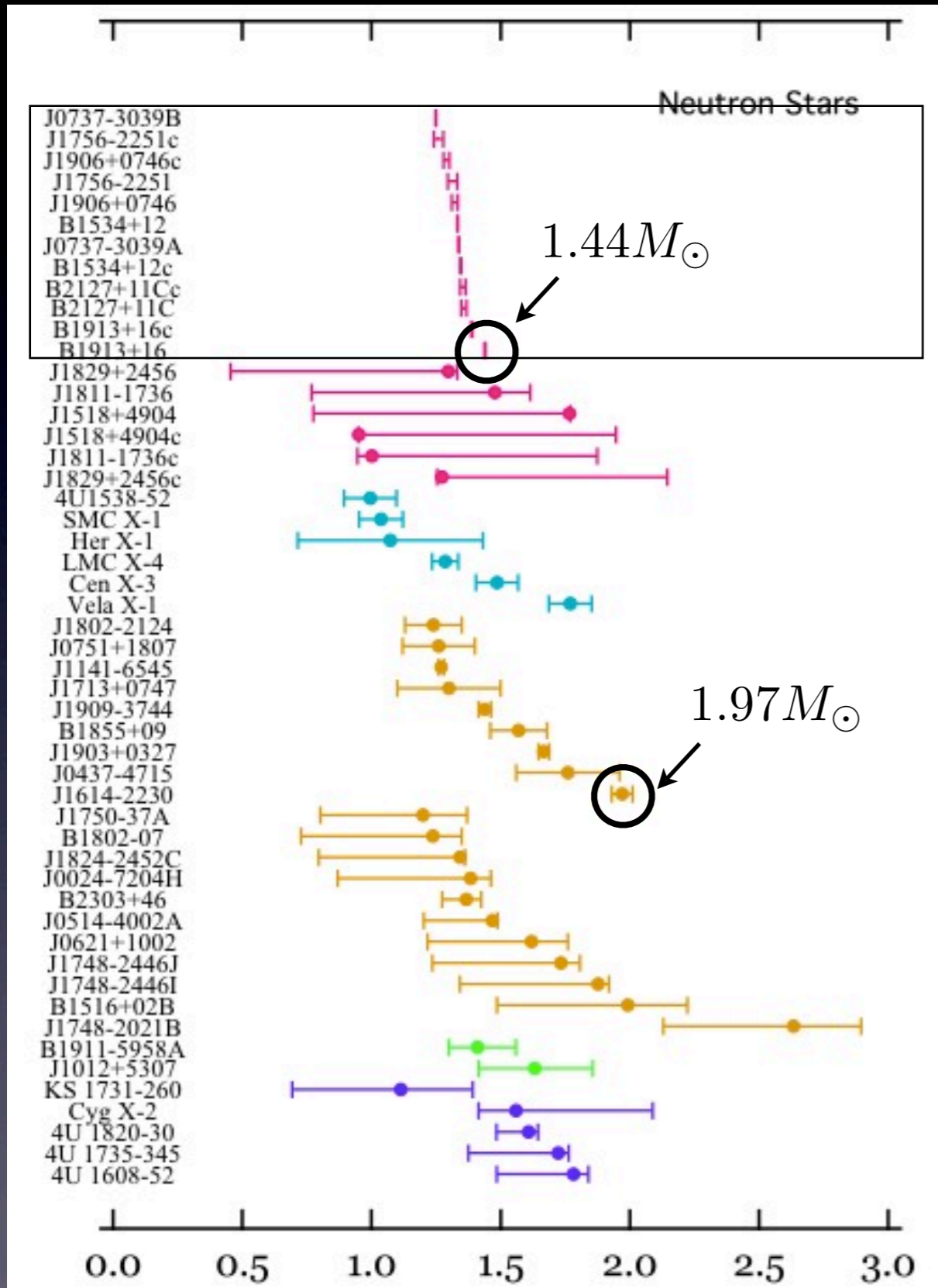
1. Radius is essentially controlled by hadronic EOS
2. Interpolated EOS with the repulsive 3-body force among nucleons and hyperons have a impact on the cooling problem of neutron star with hyperon core

### \* Perspective

1. Cooling with 2SC+X phase by using our hadron-quark crossover model.
2. Constraints on the EOS from other observables such as neutron star radius.

Back Up Slide

# Introduction: Massive Neutron Star



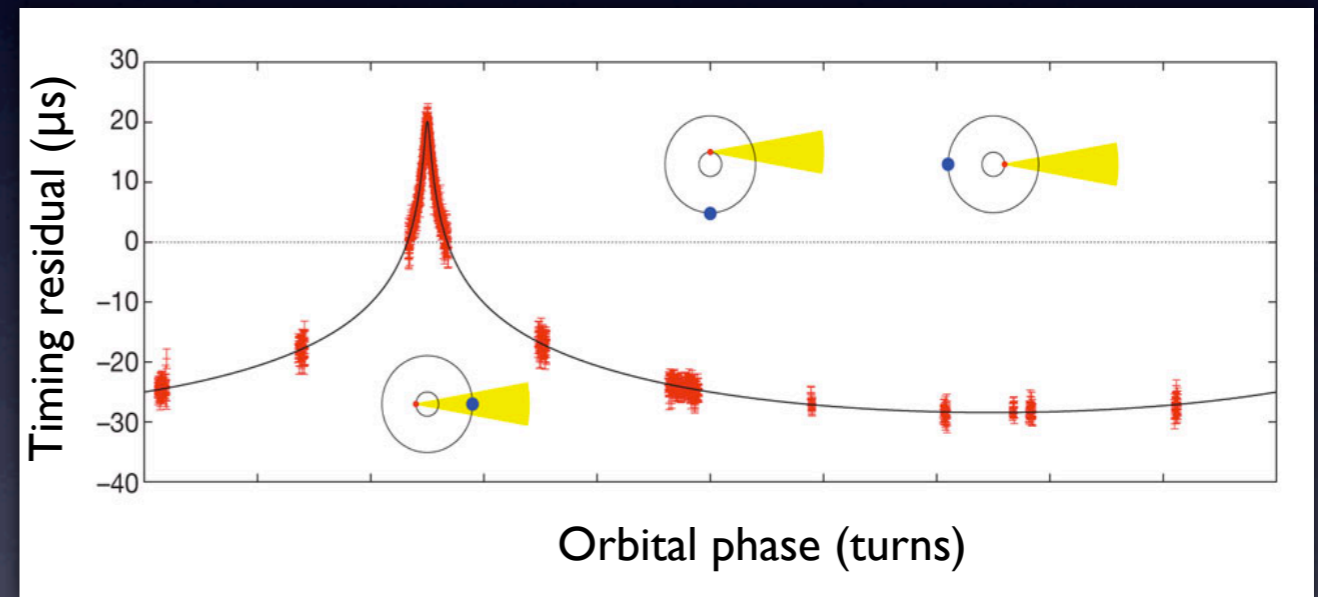
Ozel et al. (2012)

Typical value of the observed mass for double NS binaries  $\sim 1.4M_{\odot}$



In 2010, NS (PSR J1614-2230, NS-WD binary) with  $M = (1.97 \pm 0.04)M_{\odot}$  was found

Shapiro delay



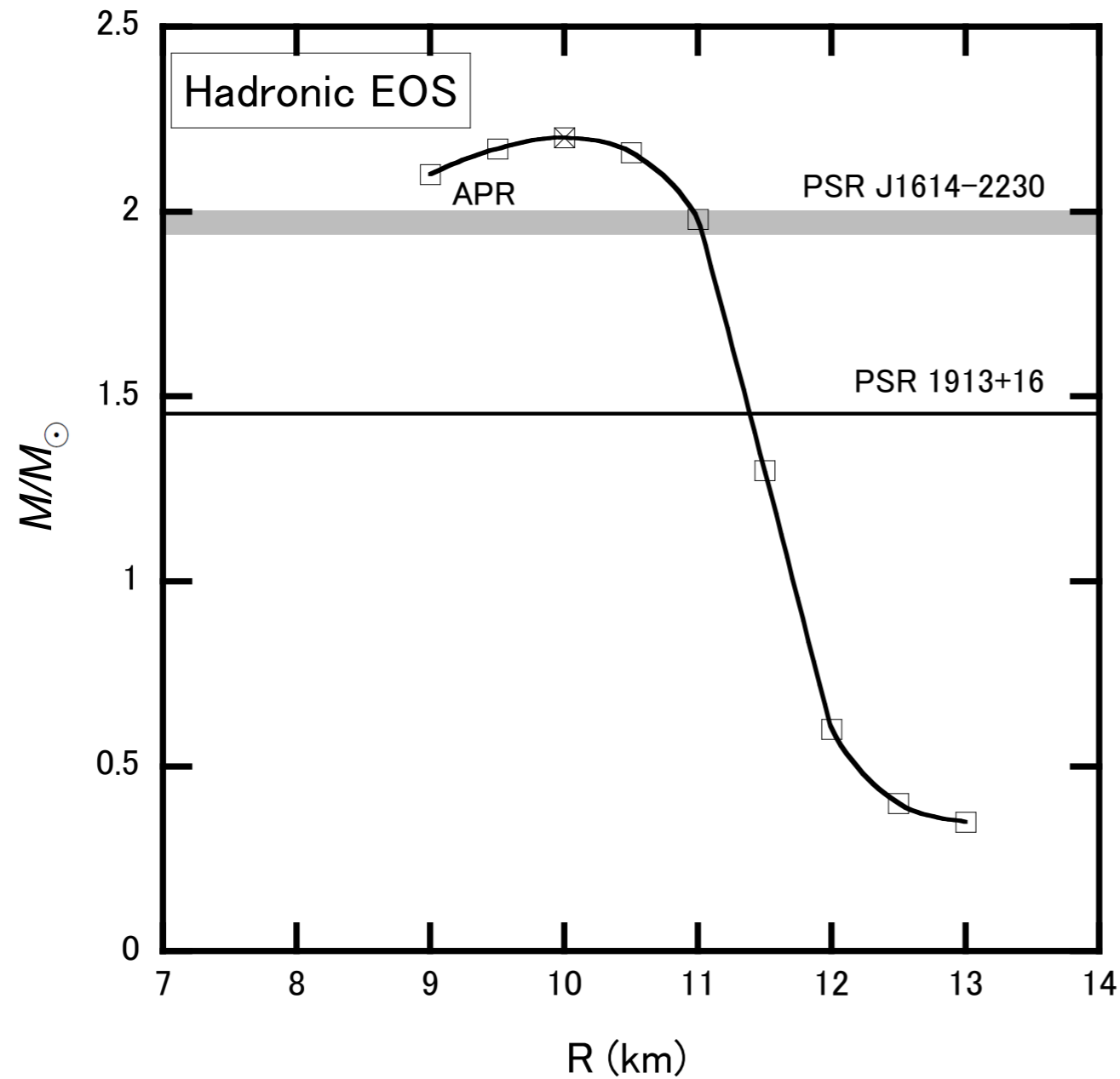
Demorest et al. (2010)

Key Questions:

Any EOS which can explain  $2M_{\odot}$  NS?

The fate of the quark matter inside a heavy NS?

# Introduction: Hadronic EOSs



	APR
Method	Variational
2NF	AV18
3NF	Yes
Hyperons	No

Akmal *et al.* (1998)

# EOS at $\rho \gg \bar{\rho}$

(2+1)-flavor NJL Lagrangian (u,d,s,  $e^-$ ,  $\mu^-$ )

$$L_{NJL} = \bar{q}(i\not{\partial} - m)q + \frac{G_s}{2} \sum_{a=0}^8 [(\bar{q}\lambda^a q)^2 + (\bar{q}i\gamma_5\lambda^a q)^2] - \frac{g_v}{2} (\bar{q}\gamma^\mu q)^2 + G_D [\det \bar{q}(1 + \gamma_5)q + \text{h.c.}]$$

Parameter set

cutoff (MeV)	$G_s\Lambda^2$	$G_D\Lambda^5$	$m_{u,d}(MeV)$	$m_s(MeV)$
631.4	3.67	9.29	5.5	135.7

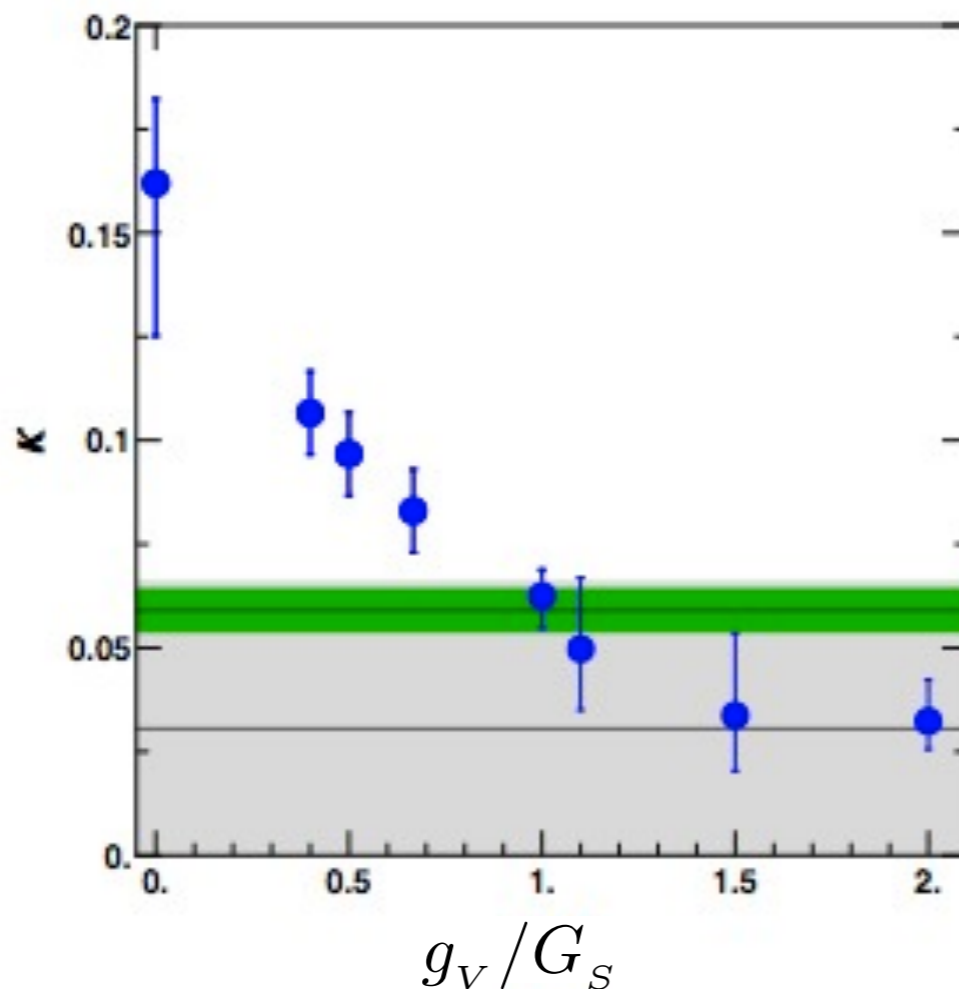
Hatsuda and Kunihiro (1994)

$$0 \leq g_v \leq 1.5G_s$$

Conditions:

1. beta-equilibrium
2. charge neutrality

Recent estimate of  $g_v$



$$\kappa = -T_c \left. \frac{d^2 T_c(\mu)}{d\mu^2} \right|_{\mu^2 = 0}$$

$$\longrightarrow g_v \sim G_s$$

$$g_v \geq 0 : \text{repulsive}$$

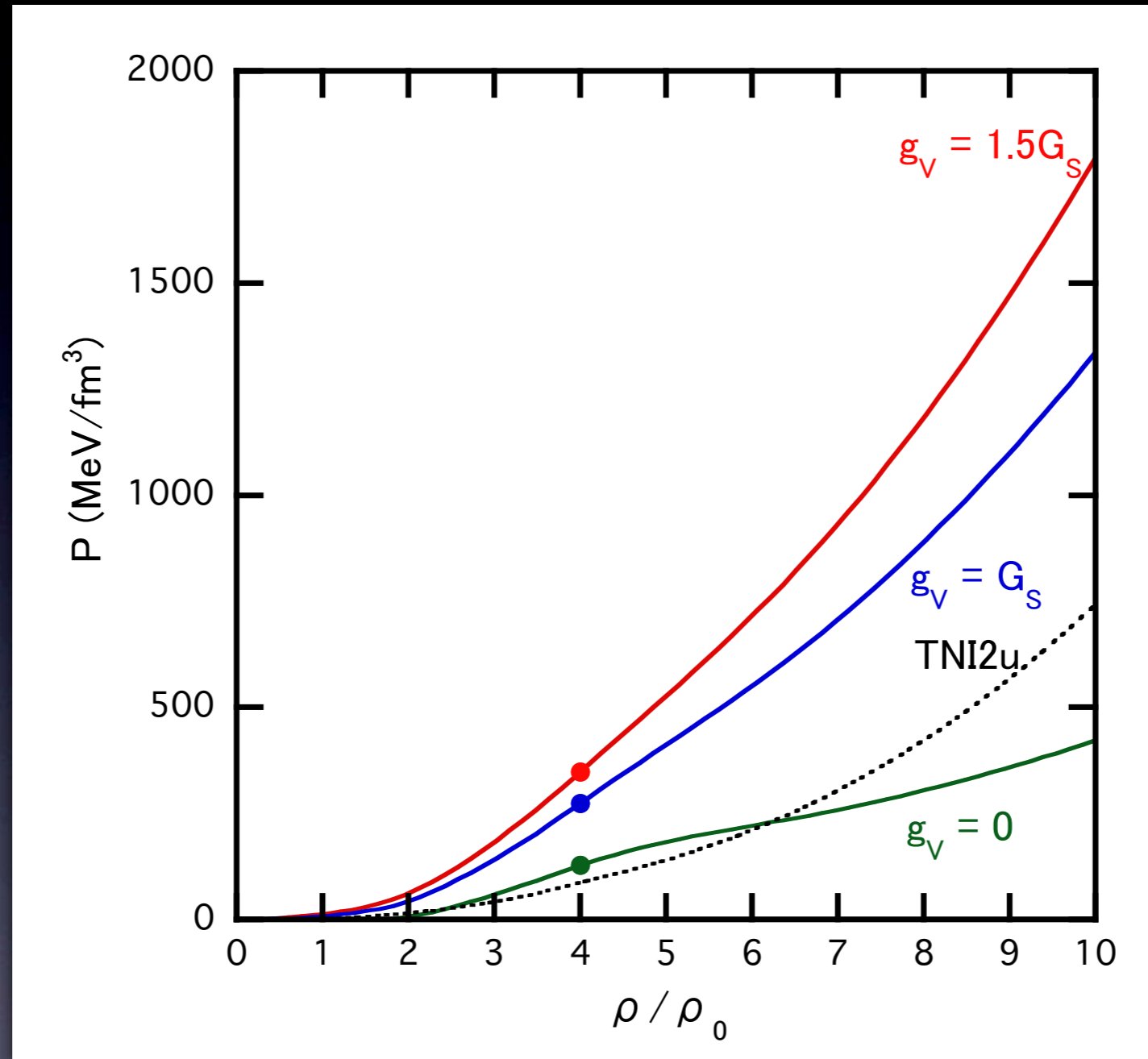
$$g_v/G_s = 0 : \text{no-repulsion}$$

$$g_v/G_s = 1.0 : \text{medium repulsion}$$

$$g_v/G_s = 1.5 : \text{strong repulsion}$$

Bratovic et al., Phys. Lett. B719 (2013)

Pressure P



- EOS becomes stiffer as  $g_V$  increases due to the universal repulsion

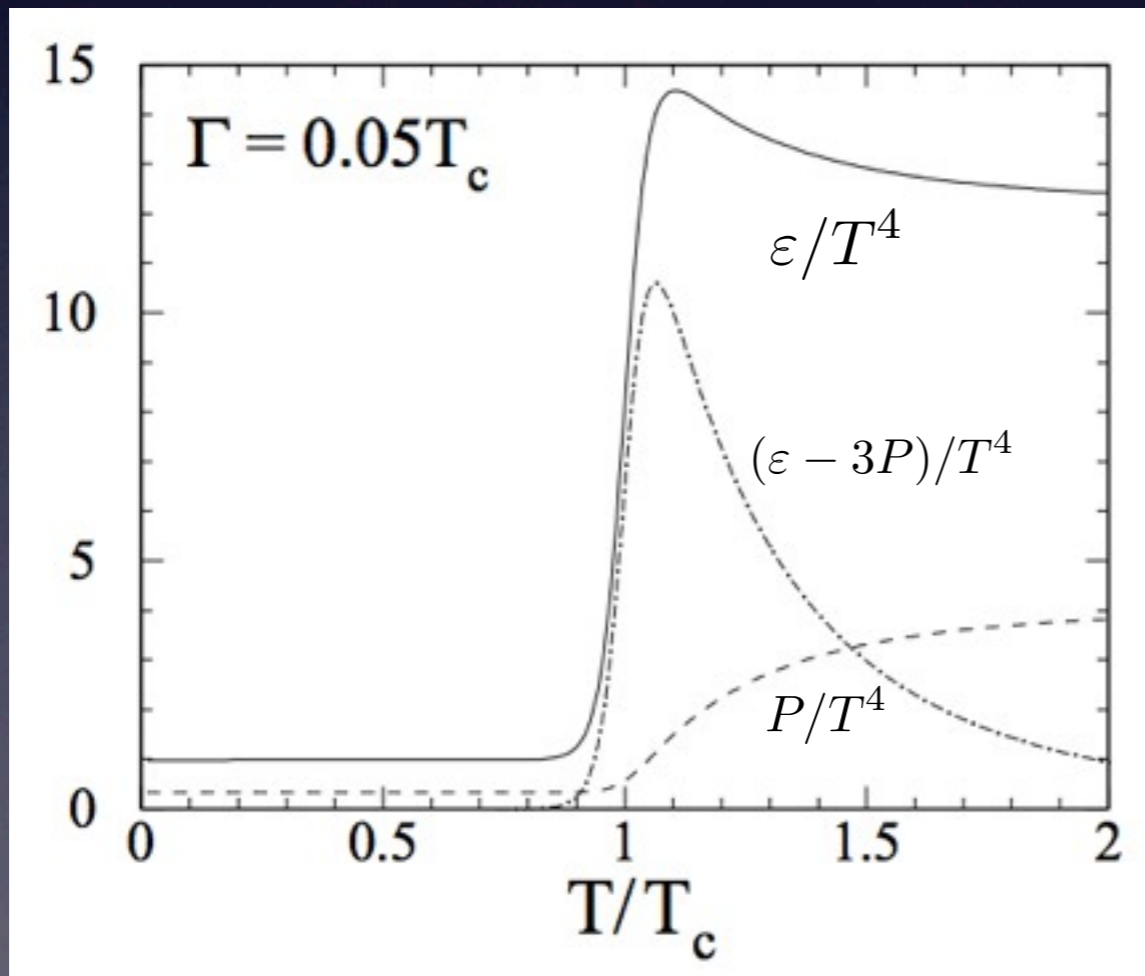
# Crossover at finite temperature

- Phenomenological Interpolation:  $s(T)$

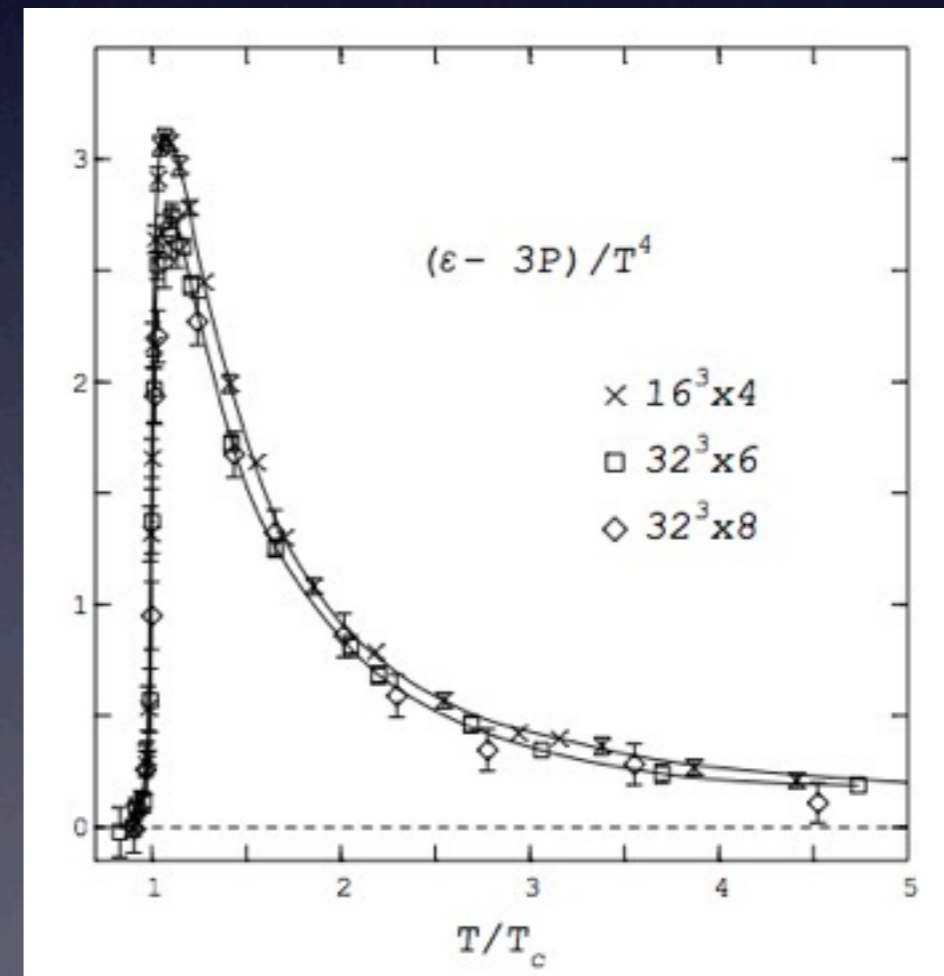
$s$ : entropy density,  $T$ : temperature

Asakawa, Hatsuda (1995)

$$\left\{ \begin{array}{l} s(T) = s_h(T)w_h(T) + s_q(T)w_q(T) \\ w_q(T) = \frac{n(1 + \tanh(\frac{T-T_c}{\Gamma}))}{m(1 - \tanh(\frac{T-T_c}{\Gamma})) + n(1 + \tanh(\frac{T-T_c}{\Gamma}))} \end{array} \right.$$



Phenomenological Interpolation



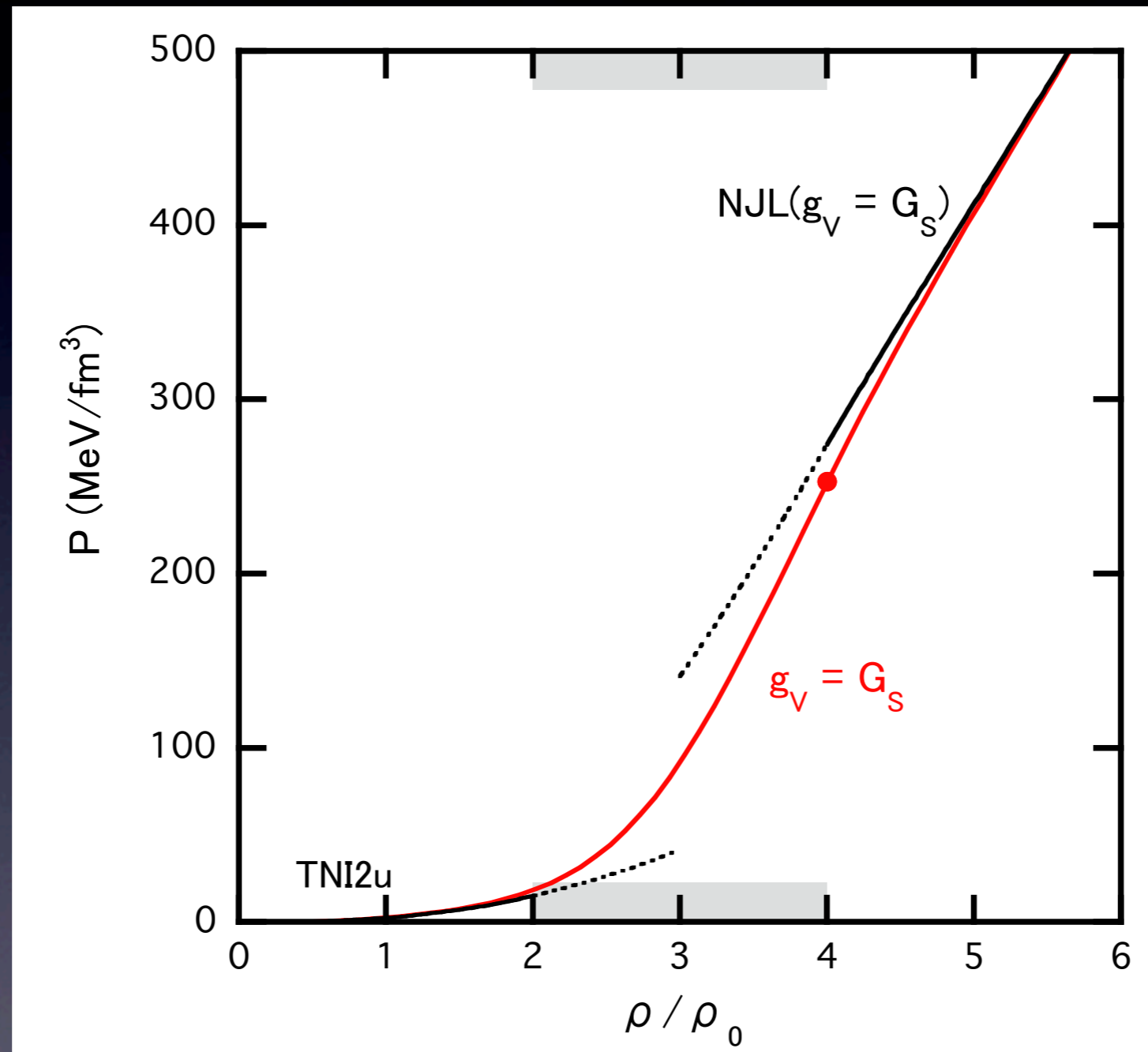
lattice QCD Karsch (1995)



# Interpolated EOS

H-EOS: TNI2u, Q-EOS: NJL

$$g_v = G_S \quad (\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$$



- In the crossover region, interpolated EOS is larger than H-EOS.
- Rapid stiffening of the EOS in the crossover region

# Results (2): Effects of parameters

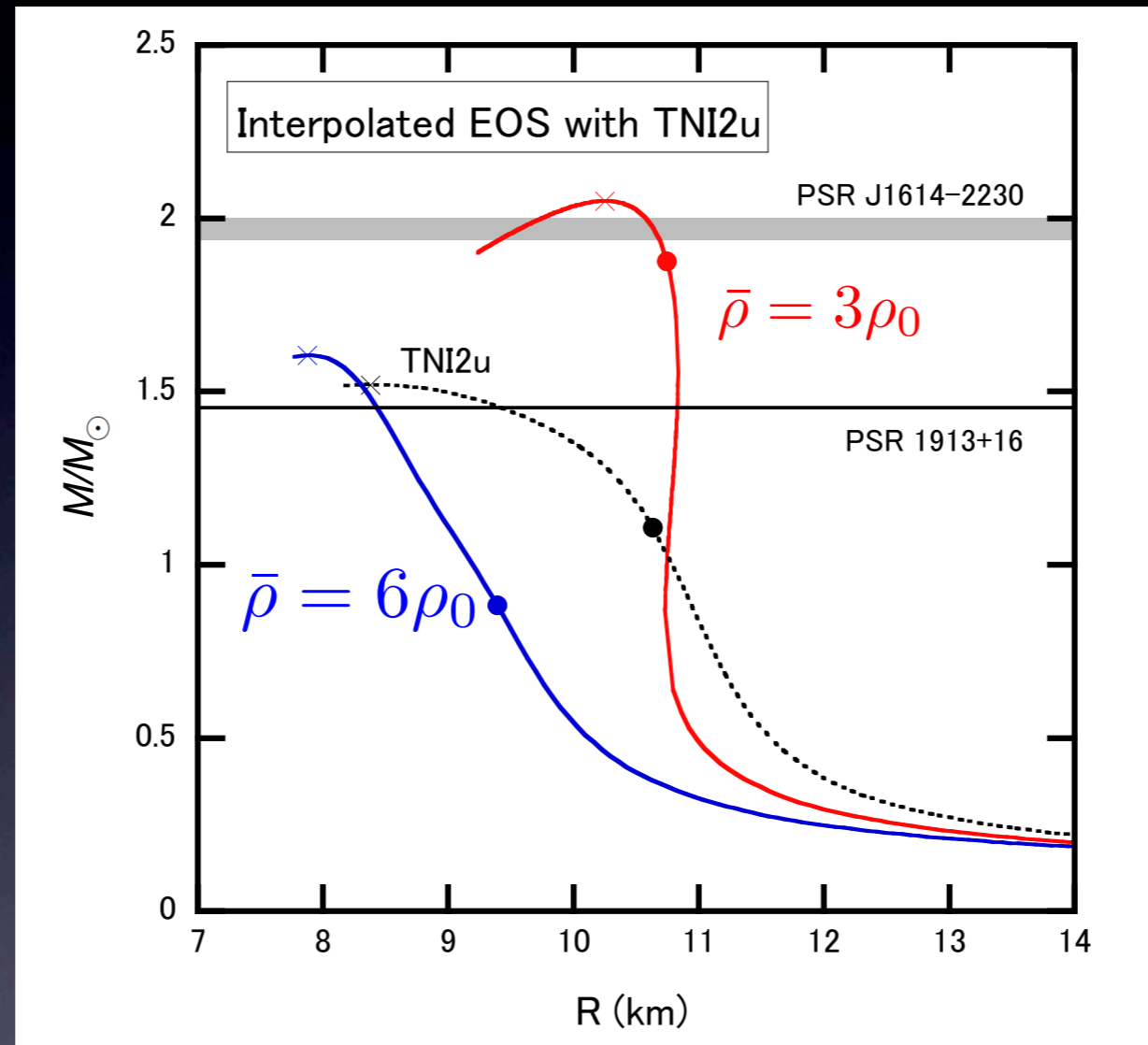
How maximum mass depends on  $\bar{\rho}$ ,  $\Gamma$

$\bar{\rho}$	$\Gamma/\rho_0 = 1$		$\Gamma/\rho_0 = 2$	
	$g_v = G_s$	$g_v = 1.5G_s$	$g_v = G_s$	$g_v = 1.5G_s$
$3\rho_0$	2.05	2.17	-	-
$4\rho_0$	1.89	1.97	-	-
$5\rho_0$	1.73	1.79	1.74	1.80
$6\rho_0$	1.60	1.64	1.62	1.66

Crossover occurs at relatively low densities and quarks are strongly interacting  $\longrightarrow 2M_\odot$

# Results (2): Effects of Crossover Density ( $\bar{\rho}$ )

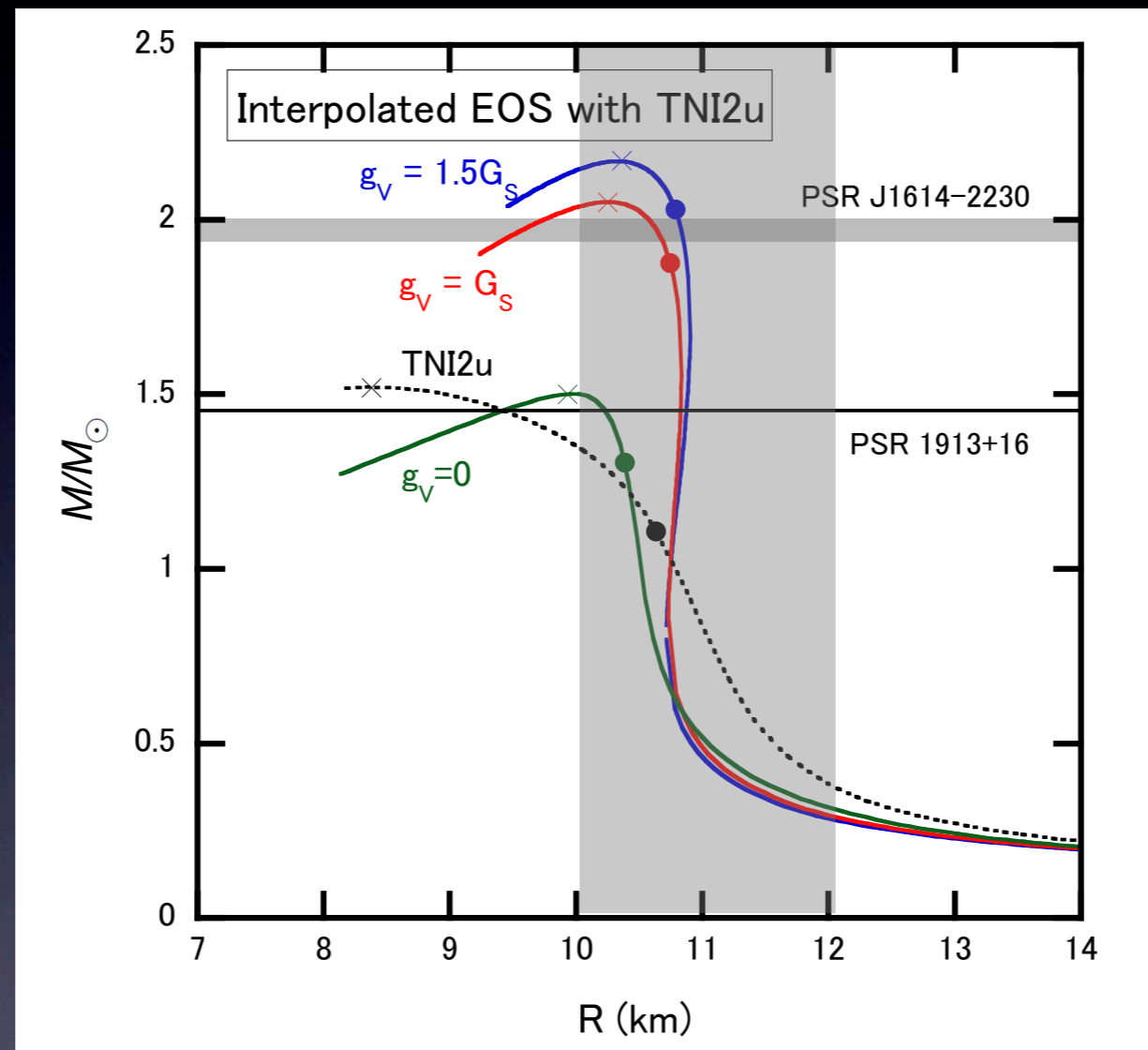
M-R relation  $\Gamma = \rho_0$   $g_v = G_S$



- Crossover occurs at relatively low densities  $\longrightarrow 2M_\odot$

# Results (3): Effects of Vector Int. ( $g_v$ )

M-R relation  $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$



- The maximum mass exceeds  $2M_{\odot}$  only if the vector type repulsion is as strong as the scalar interaction
- Radius: about 11 km

# CSC Lagrangian

$$L_{\text{CSC}} = L_{\text{NJL}} + \frac{H}{2} \sum_{A=2,5,7} \sum_{A'=2,5,7} (\bar{q} i \gamma_5 \tau_A \lambda_{A'} C \bar{q}^T) (q^T C i \gamma_5 \tau_A \lambda_{A'} q) \quad H = \frac{3}{4} G_s$$

by Fierz

$$q^C = C \bar{q}^T \quad \Psi = \frac{1}{\sqrt{2}} \begin{pmatrix} q \\ q^C \end{pmatrix}$$

$$\Delta_1 = -H s_{55}, \quad \Delta_2 = -H s_{77}, \quad \Delta_3 = -H s_{22}$$

$$\Omega(T, \mu_{u,d,s}) = -\frac{T}{2} \sum_{\ell} \int \frac{d^3 p}{(2\pi)^3} \text{Tr} \ln \left( \frac{S^{-1}(i\omega_{\ell}, \mathbf{p})}{T} \right) + G_s \sum_i \sigma_i^2$$

$$+ 4G_D \sigma_u \sigma_d \sigma_s - \frac{1}{2} g_V \left( \sum_i n_i \right)^2 + \frac{1}{2H} \sum_{\text{color}} |\Delta_c|^2$$

$$S^{-1} = \begin{pmatrix} S_{0+}^{-1} & \Phi^{-} \\ \Phi^{+} & S_{0-}^{-1} \end{pmatrix} \quad (\Phi^{-})_{ab}^{\alpha\beta} = - \sum_{\text{color}} \varepsilon^{\alpha\beta c} \varepsilon_{abc} \Delta_c \gamma_5, \quad \Phi^{+} = \gamma^0 (\Phi^{-})^{\dagger} \gamma^0$$

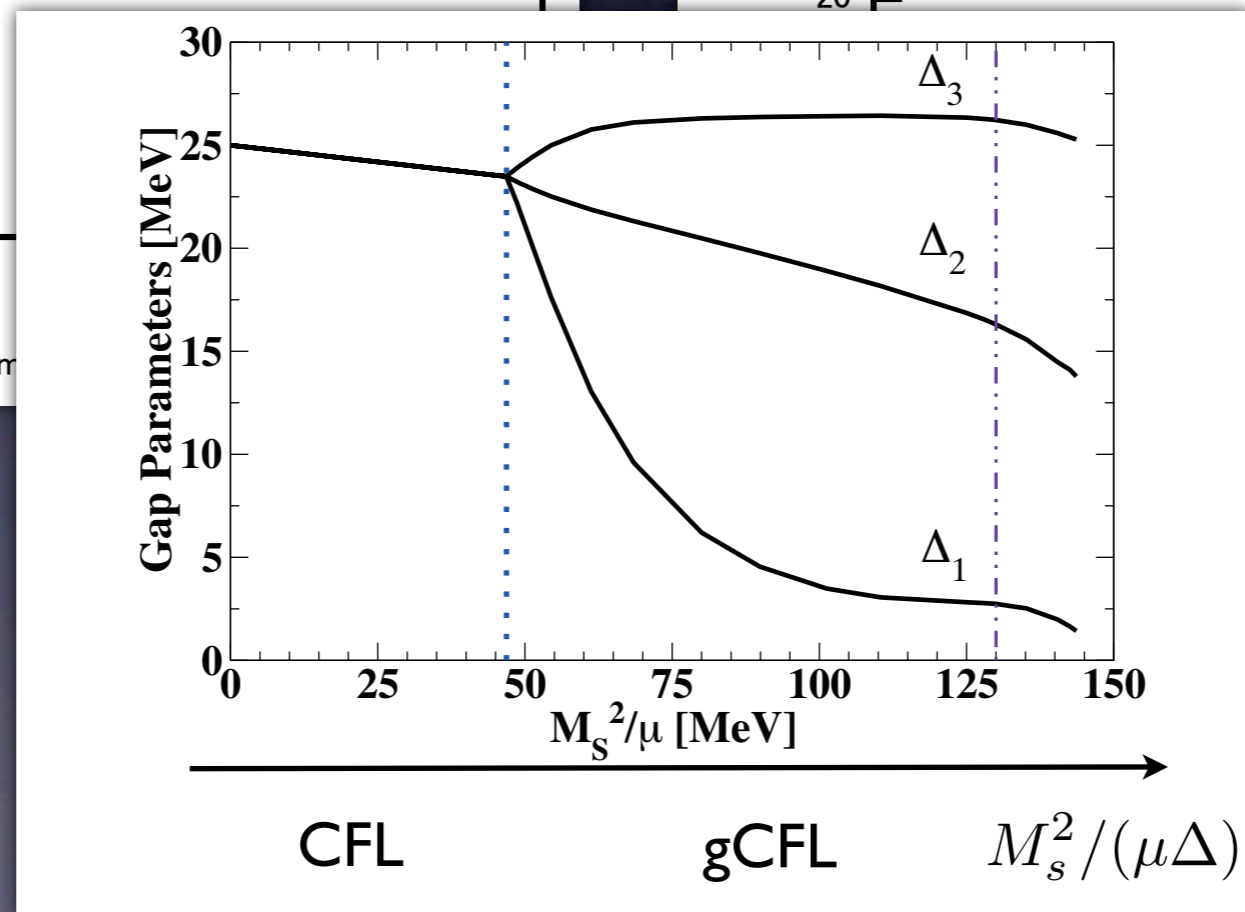
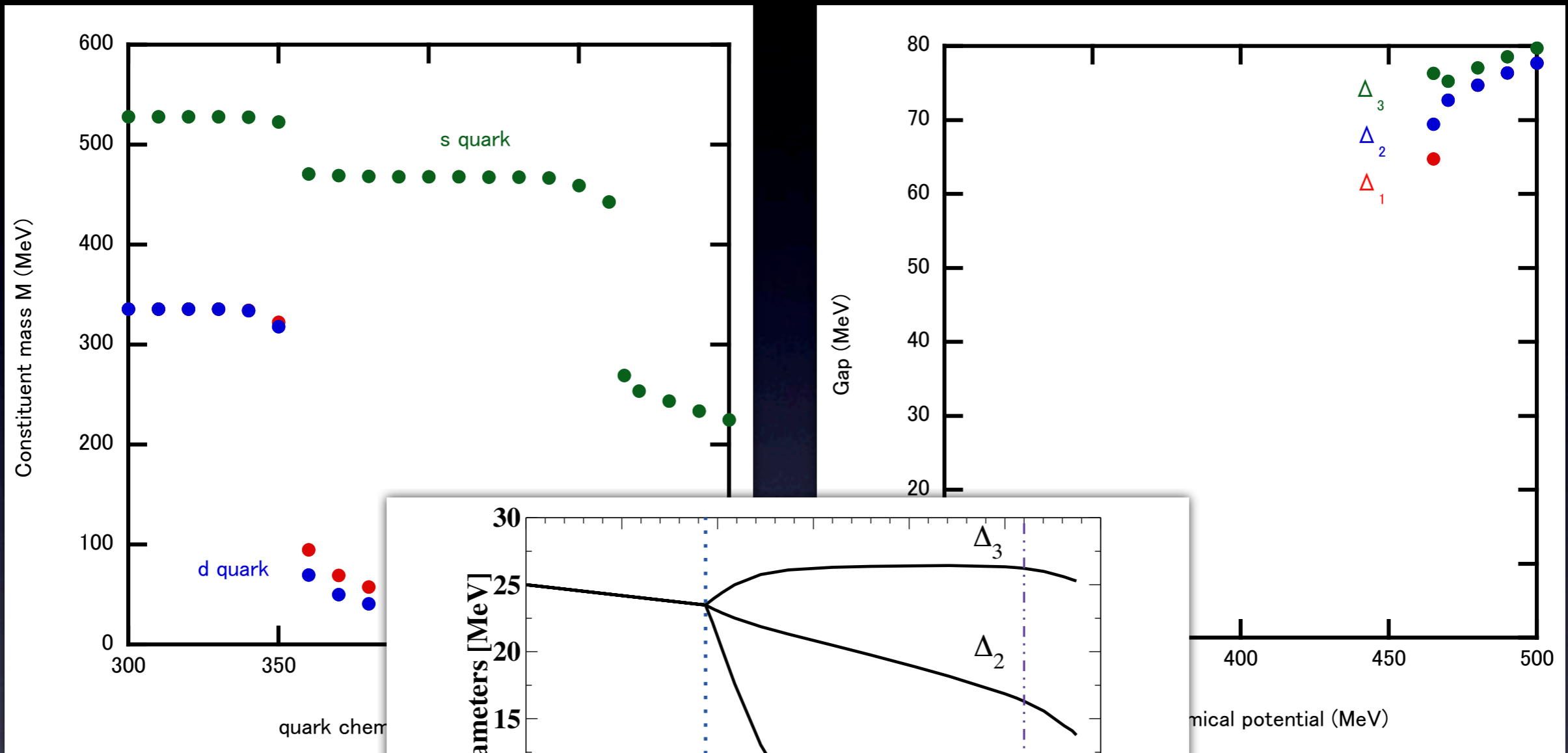
$$S_{0\pm}^{-1} = p - M \pm \tilde{\mu} \gamma^0$$

$$\tilde{\mu} = \mu - \frac{1}{2} \mu_3 - \frac{1}{2\sqrt{3}} \mu_8$$



# Results (5): Case I $H = \frac{3}{4}G_s$

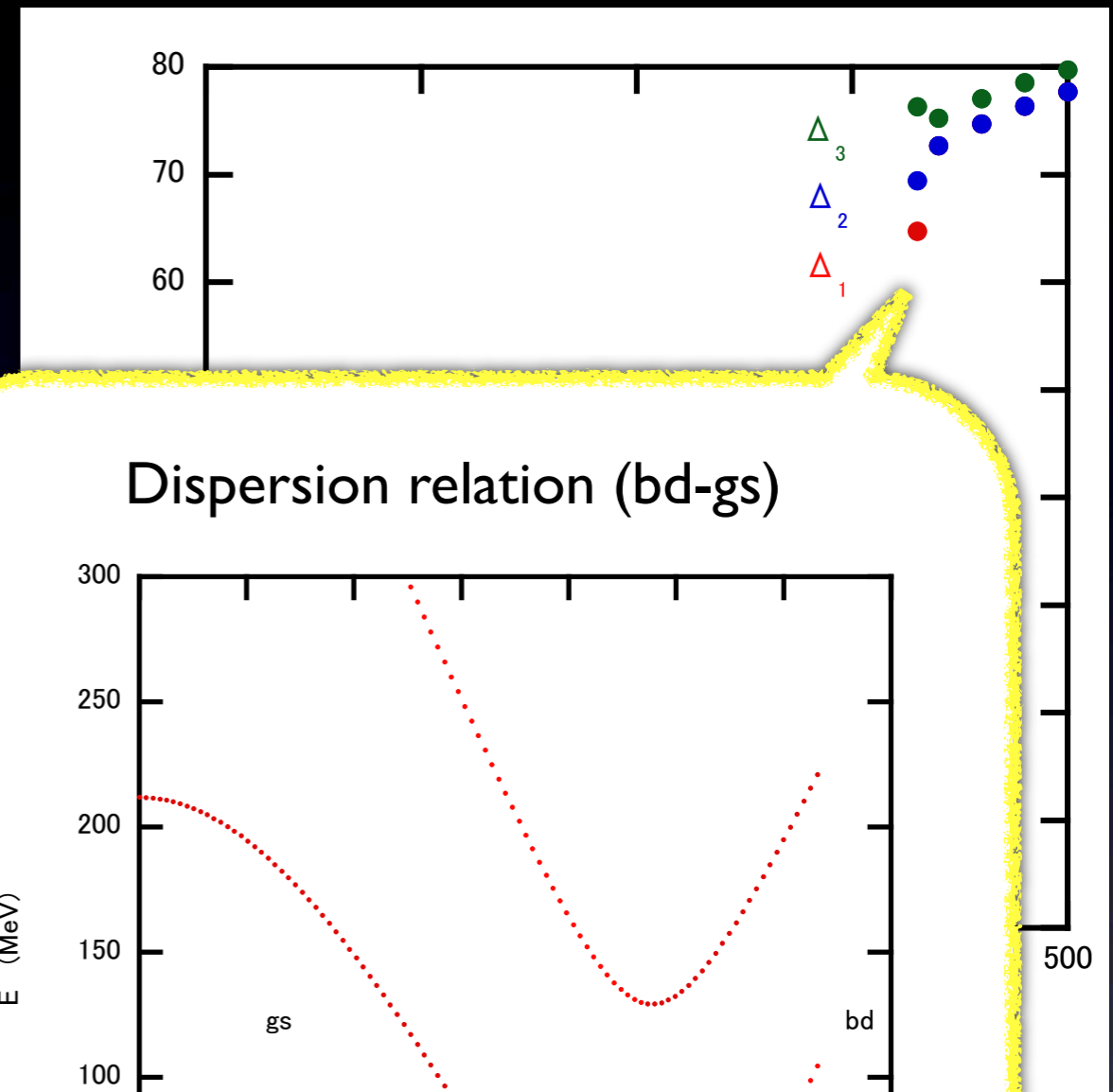
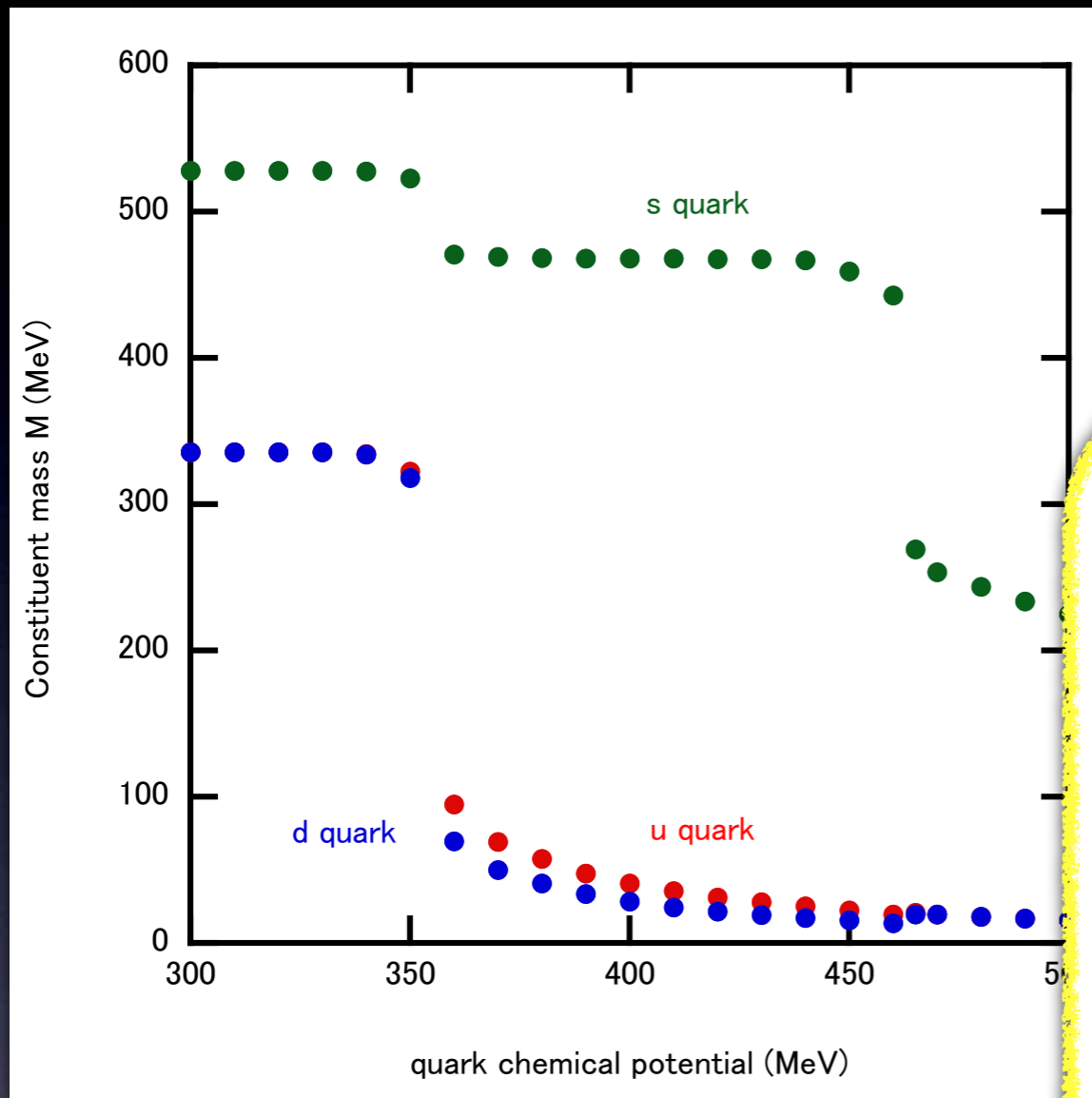
$g_v = 0$



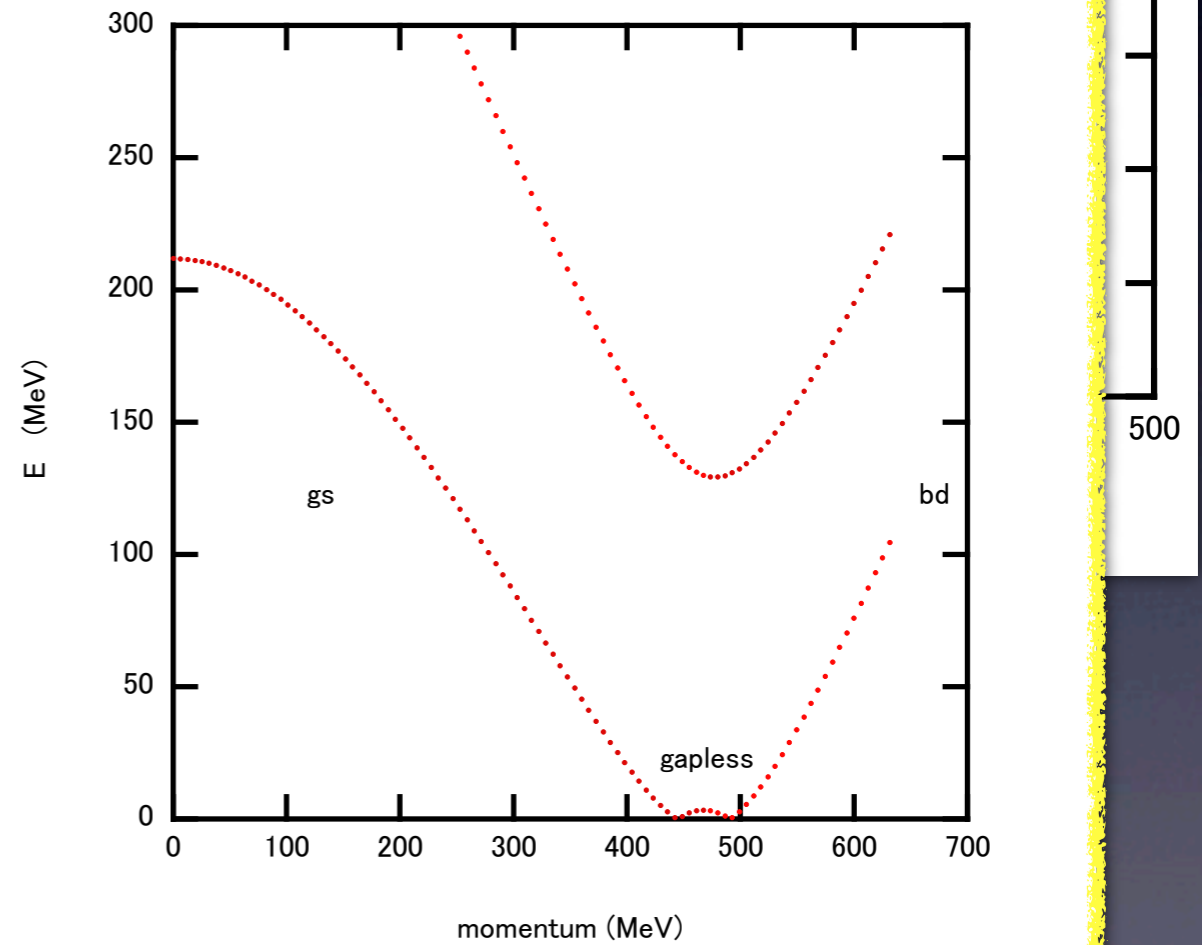
Alford (2004)

# Results (5): Gap parameter

$$g_v = 0$$



Dispersion relation (bd-gs)



gapless phase



# Another Interpolation

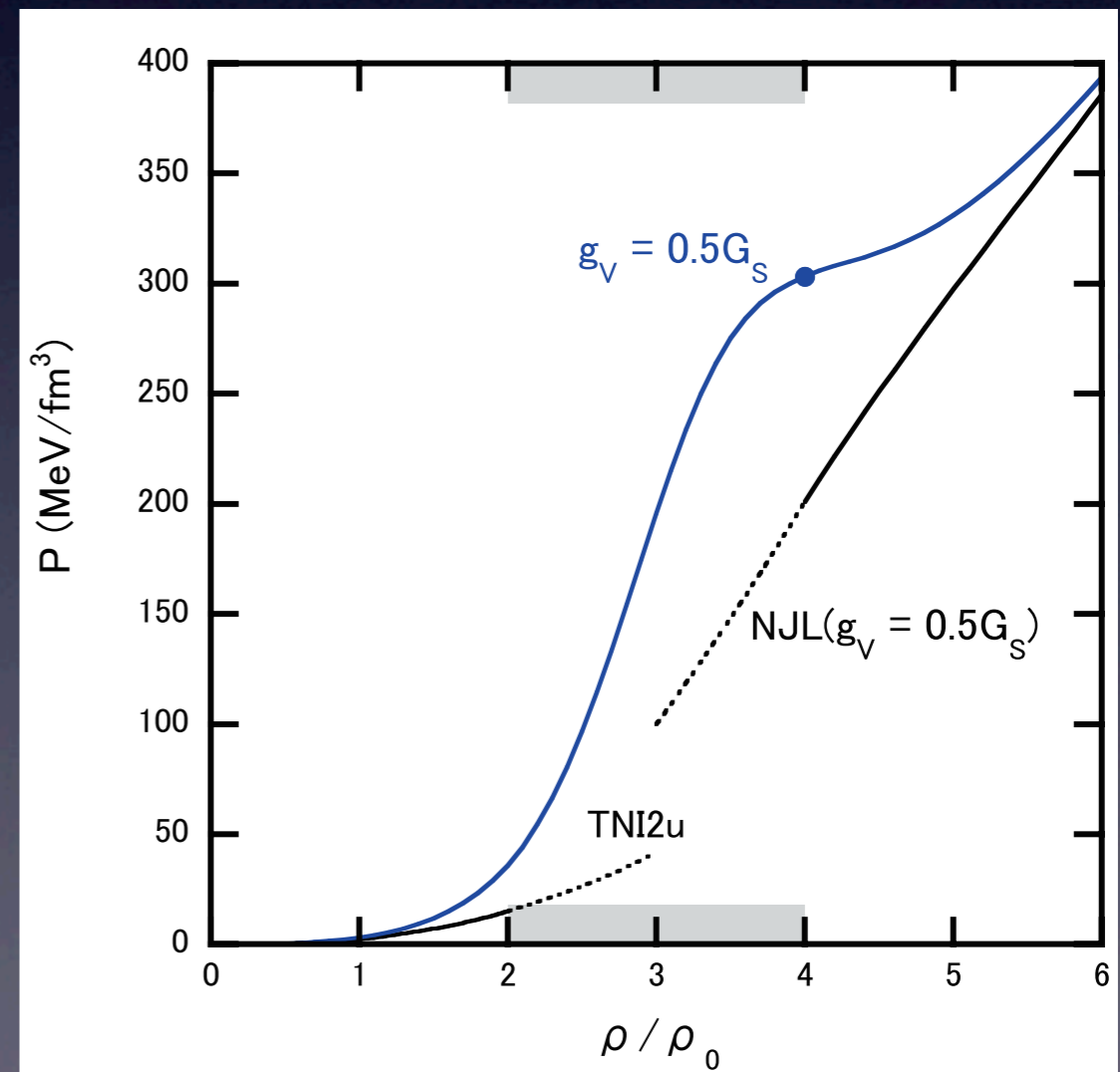
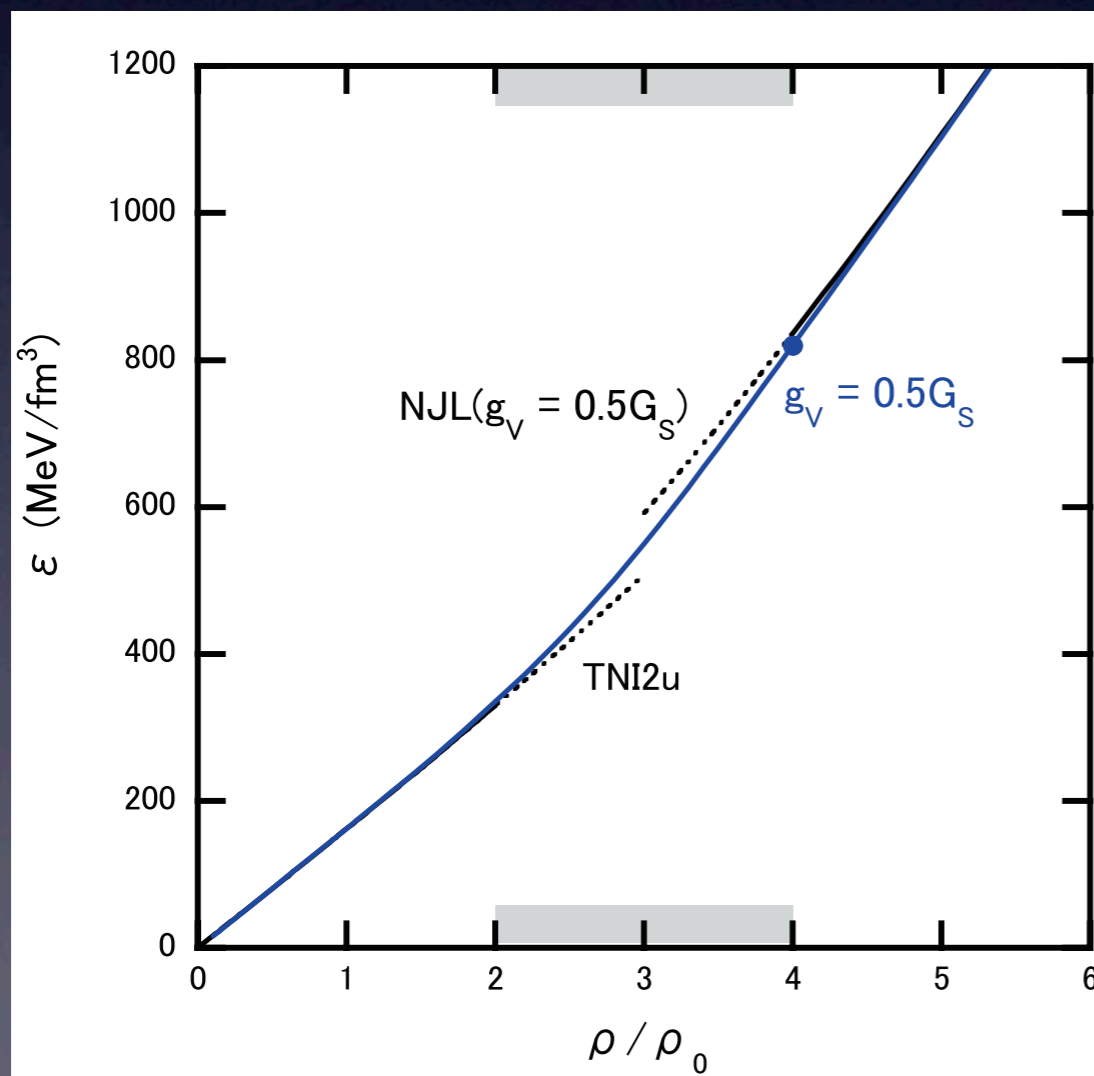
21/29

Phenomenological interpolation:  $\varepsilon(\rho)$

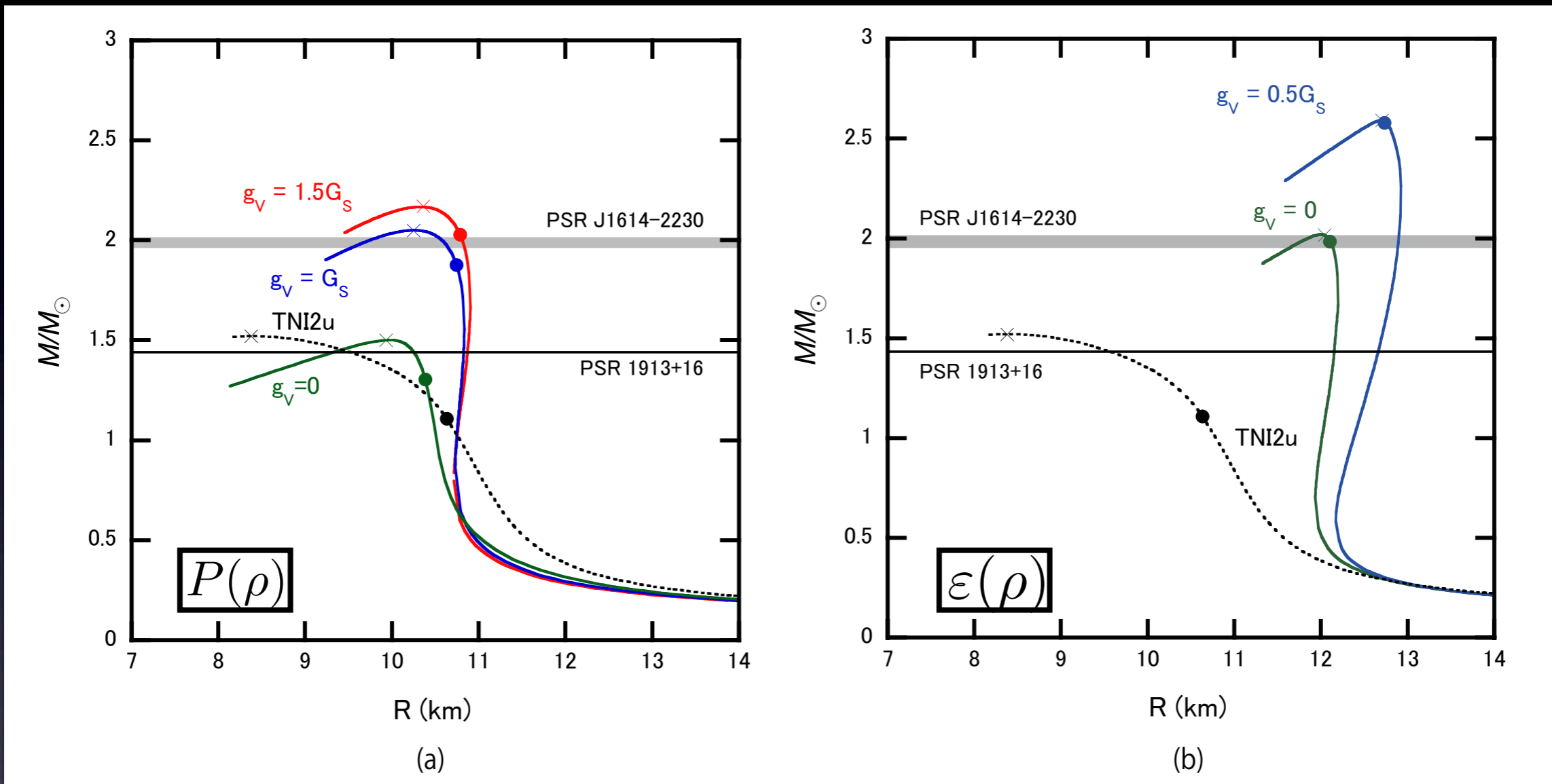
$$\left\{ \begin{array}{l} \varepsilon = \varepsilon_H \times f_- + \varepsilon_Q \times f_+ \\ P = \rho^2 \frac{\partial(\varepsilon/\rho)}{\partial \rho} \end{array} \right. \quad f_{\pm} = \frac{1 \pm \tanh\left(\frac{\rho - \bar{\rho}}{\Gamma}\right)}{2}$$

H-EOS: TNI2u, Q-EOS: NJL

$$g_v = 0.5G_s \quad (\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$$



M-R relation  $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$

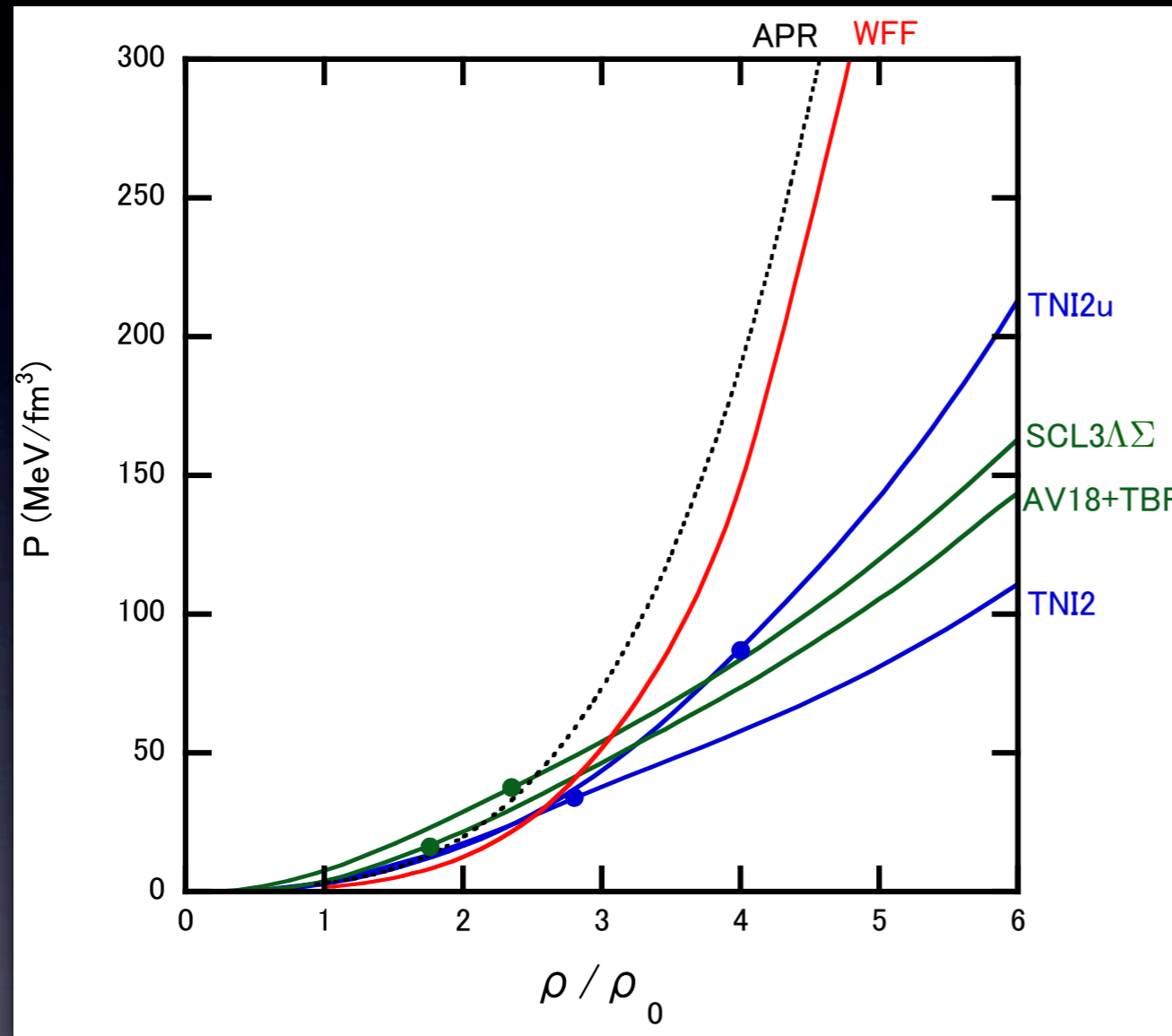


- The  $\epsilon$ -interpolation makes EOS stiff more drastically than the P-interpolation.
- Even for  $(g_v, \bar{\rho}) = (0, 3\rho_0)$ , the maximum mass can exceed  $1.97M_\odot$

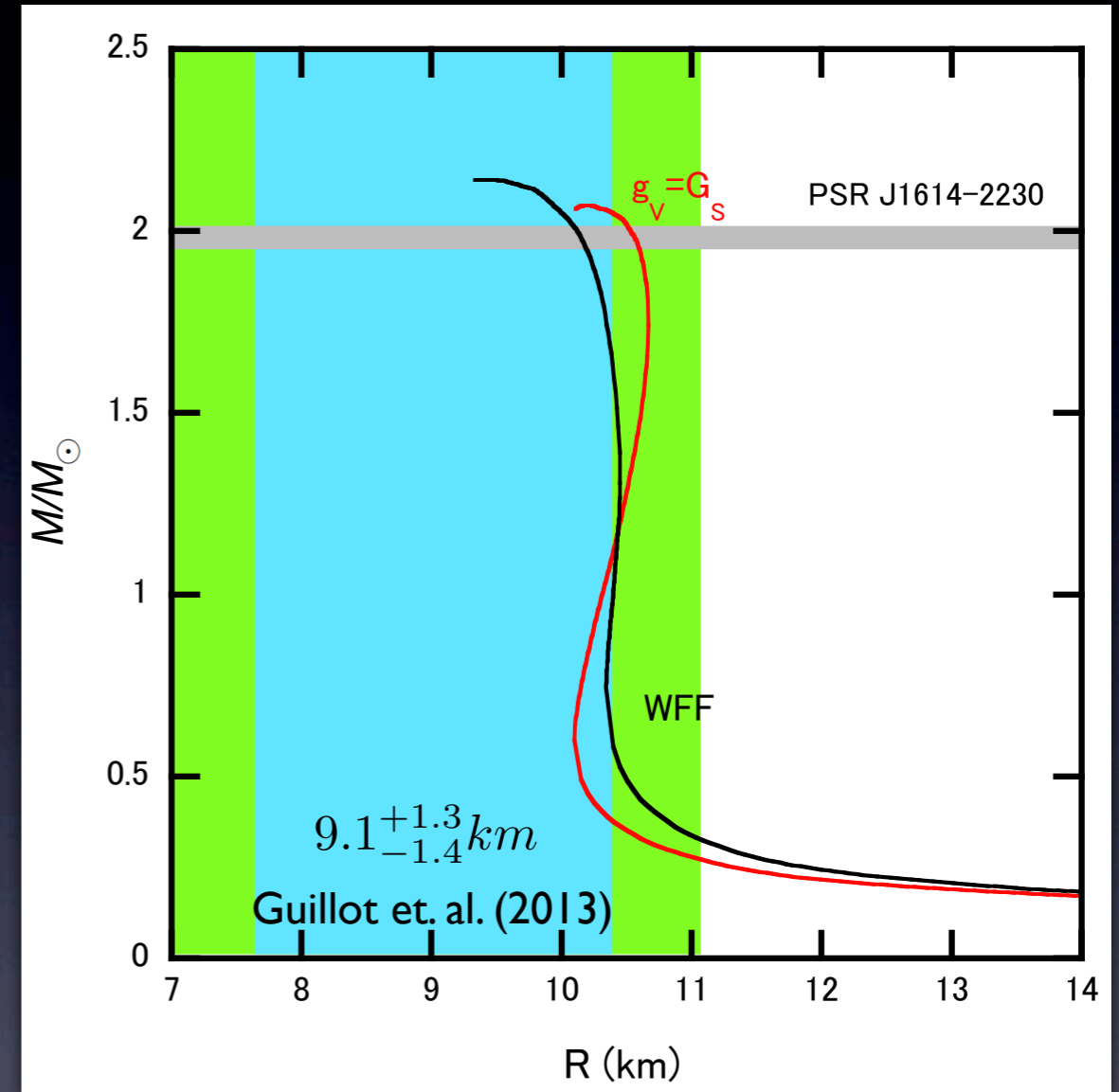
# Results (2): Radius

9/16

## Hadronic EOSs



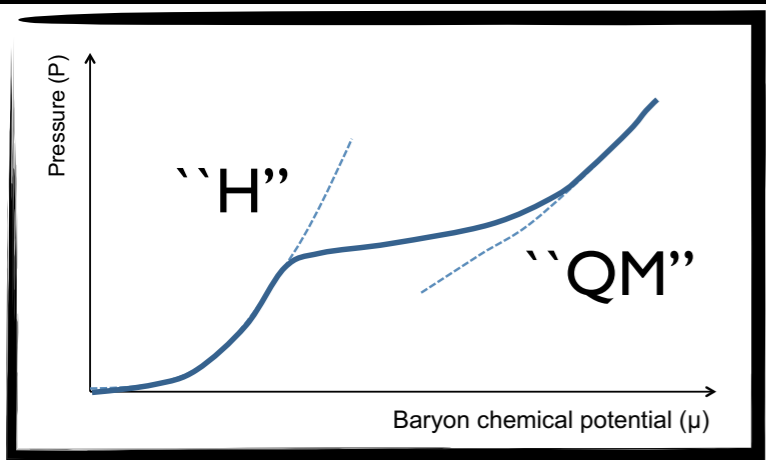
## M-R relation $(\bar{\rho}, \Gamma) = (3\rho_0, \rho_0)$ $g_v = G_S$



- We use WFF EOS as hadronic EOS (Wiringa et. al., 1988)
- Radius is essentially controlled by hadronic EOS.

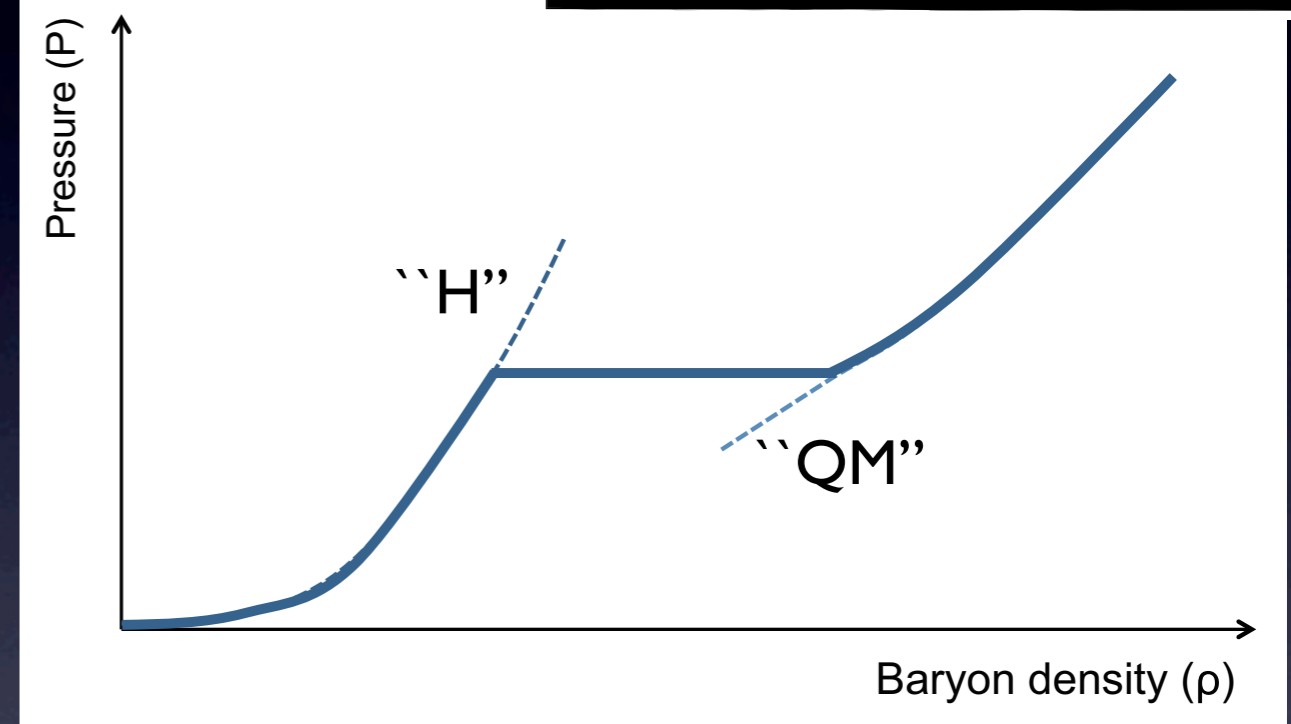
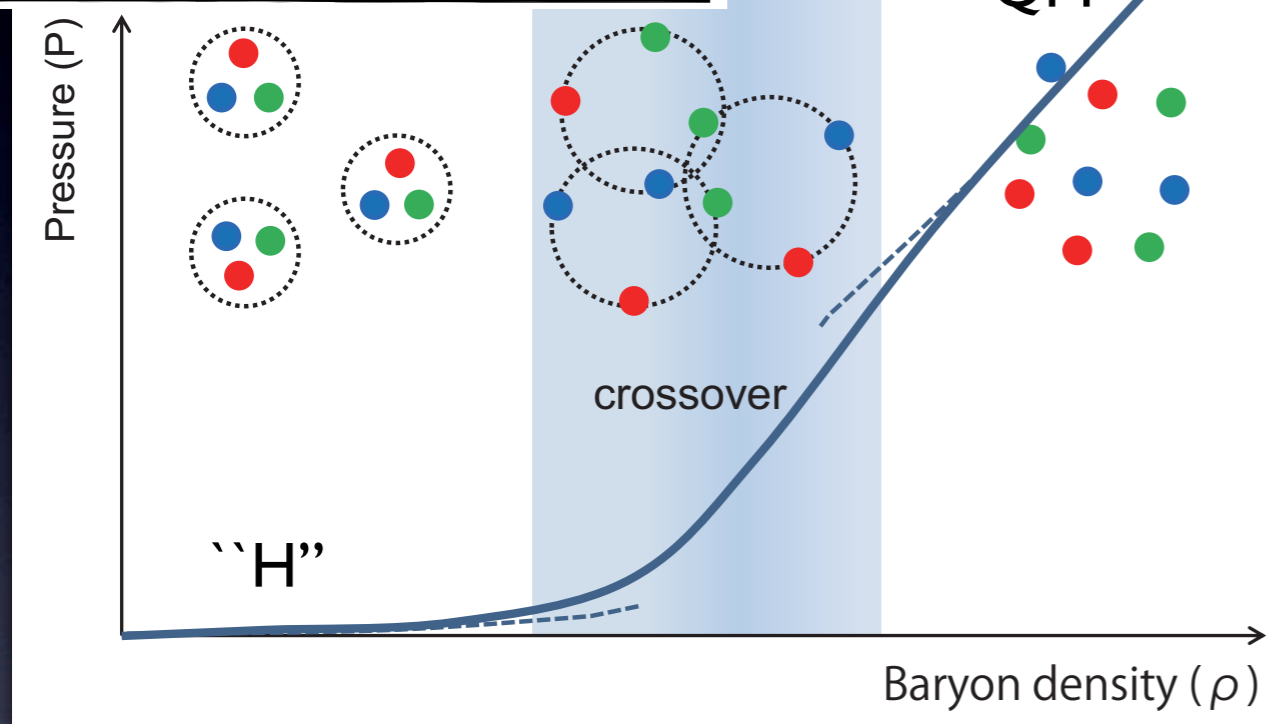
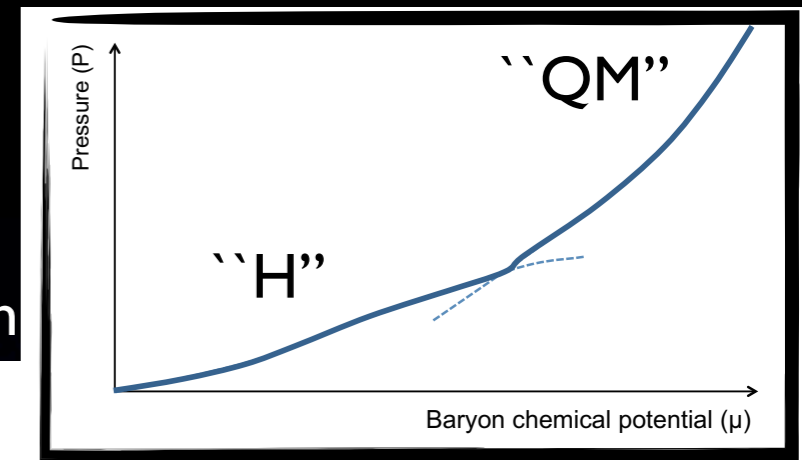
# Crossover vs. 1st order Transition

15/16



Crossover

1st order Transition



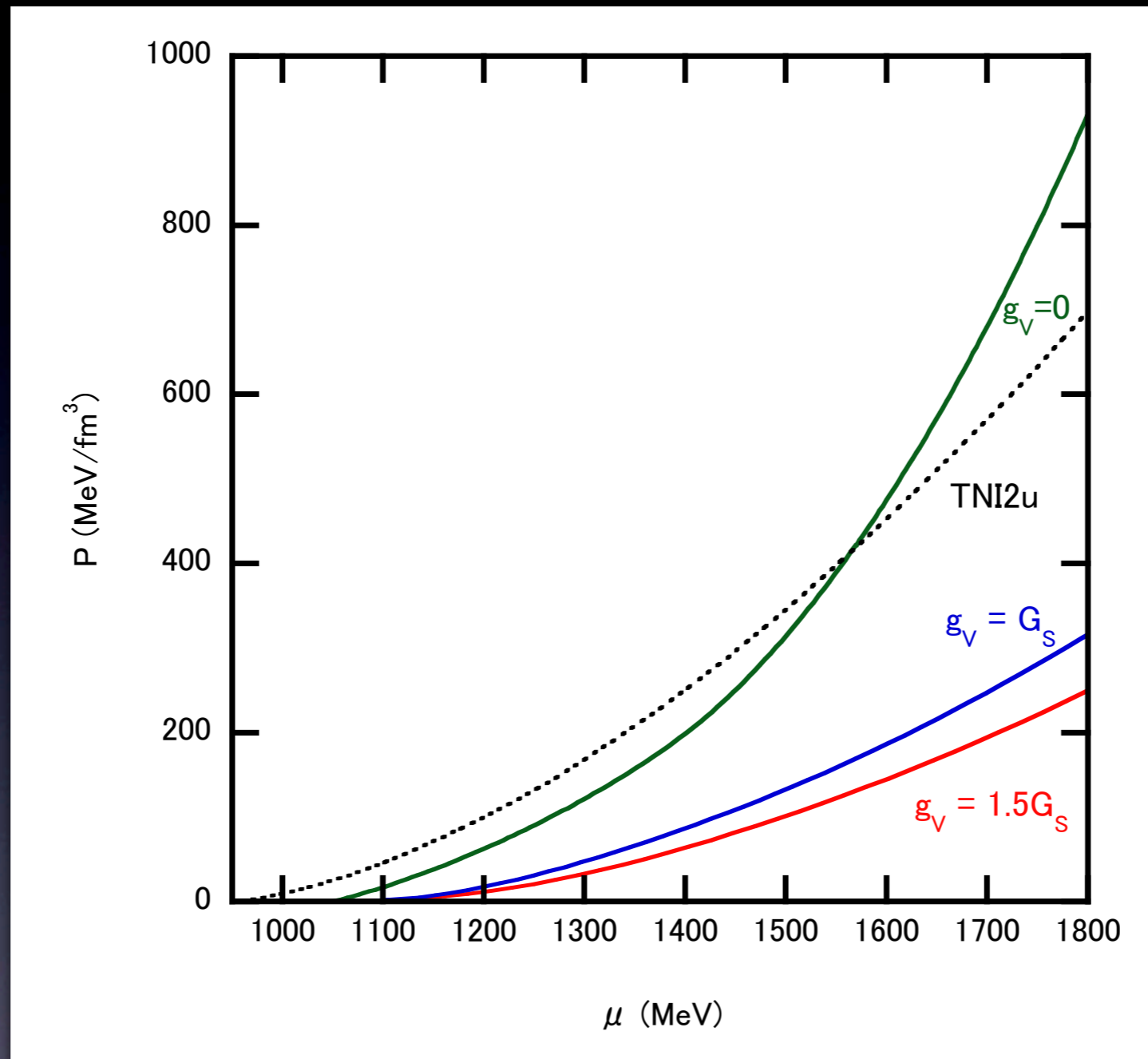
“QM” **stiffens** EOS

“QM” **softens** EOS

$$M > 2M_{\odot}$$

$$M < 2M_{\odot}$$

# Crossover vs. 1st order Transition (Example)



In the case of  $g_V = 1.0, 1.5G_S$ , H-EOS and Q-EOS do not cross at all densities

# Neutron Star Observation

Observables:

binary period  $P_b$

projection of the pulsar's semimajor axis on the line of sight  $x \equiv asini/c$

eccentricity  $e$

time of periastron  $T_0$

longitude of periastron  $\omega_0$

mass function

$$f = \frac{(m_2 \sin i)^3}{M^2}$$

+

General relativity effects:

the advance of periastron of the orbit  $\dot{\omega}$

Doppler + gravitational redshift  $\gamma$

the orbital decay  $\dot{P}_b$

range parameter  $r$

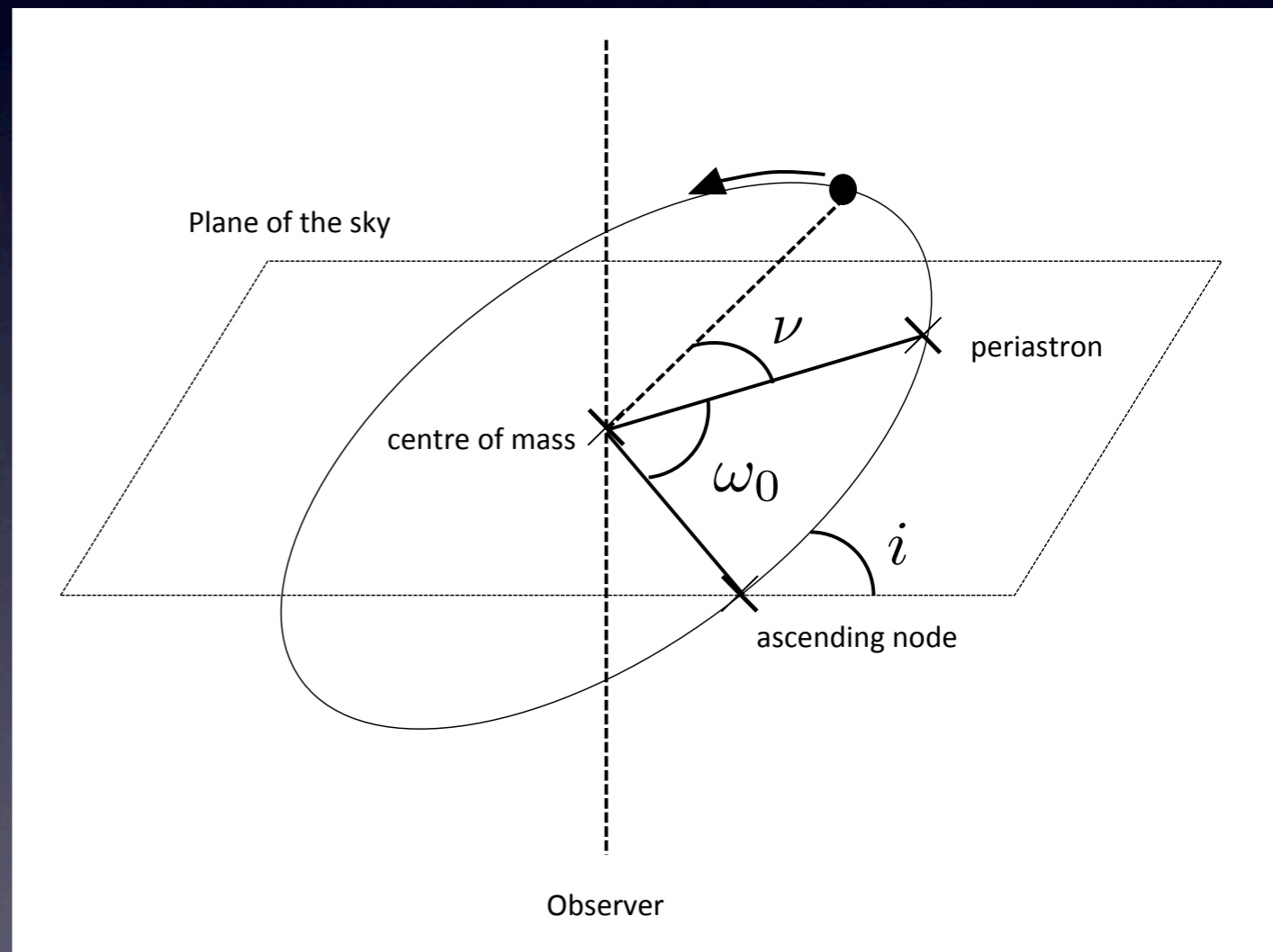
shape parameter  $s$

↑

Shapiro delay:  $\Delta = 2r \log \frac{1 + e \cos \nu}{1 - s \sin(\omega + \nu)}$

Mass fraction  $f$  + 2 general relativity effects

→ Mass estimation



# Universal 3-body force

TNI model

$$\begin{aligned}v_{TNI} &= v_{TNA} + v_{TNR} \\ &= v_2 e^{-(r/\lambda_a)^2} \rho e^{-\eta_2 \rho} (\boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2)^2 + v_1 e^{-(r/\lambda_r)^2} (1 - e^{-\eta_1 \rho})\end{aligned}$$

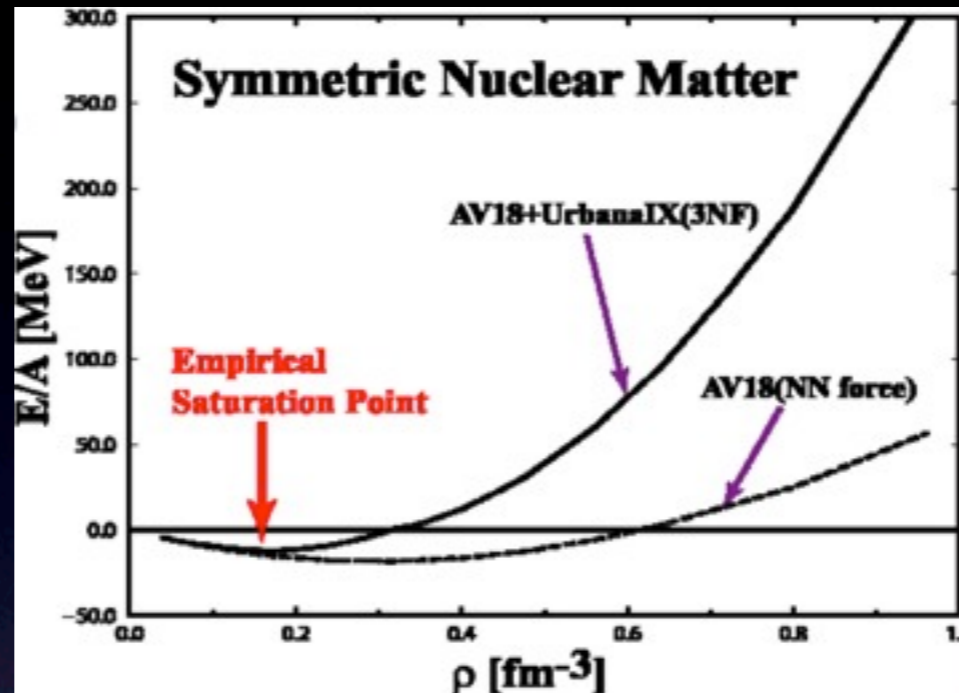
Urbana UIX model

$$\begin{aligned}v_{ijk} &= v_{ijk}^{2\pi} + v_{ijk}^R \\ &= A \sum_{\text{cyc}} \left( \{X_{ij}, X_{jk}\} \{\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j, \boldsymbol{\tau}_j \cdot \boldsymbol{\tau}_k\} + \frac{1}{4} [X_{ij}, X_{jk}] [\boldsymbol{\tau}_i \cdot \boldsymbol{\tau}_j, \boldsymbol{\tau}_j \cdot \boldsymbol{\tau}_k] \right) + U \sum_{\text{cyc}} T^2(r_{ij}) T^2(r_{jk})\end{aligned}$$

$$X_{ij} = Y(r_{ij}) \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j + T(r_{ij}) S_{ij}$$

# H-EOS: Universal 3-body force

3-body force is needed for saturation property



Akmal et al. (1998)

- From the point of view of NS observation, 3-body force is needed for the stiffness of EOS
- 3-body force between YN and YY can delay the appearance of the exotic components

## Universal 3-body force

• TNI model:

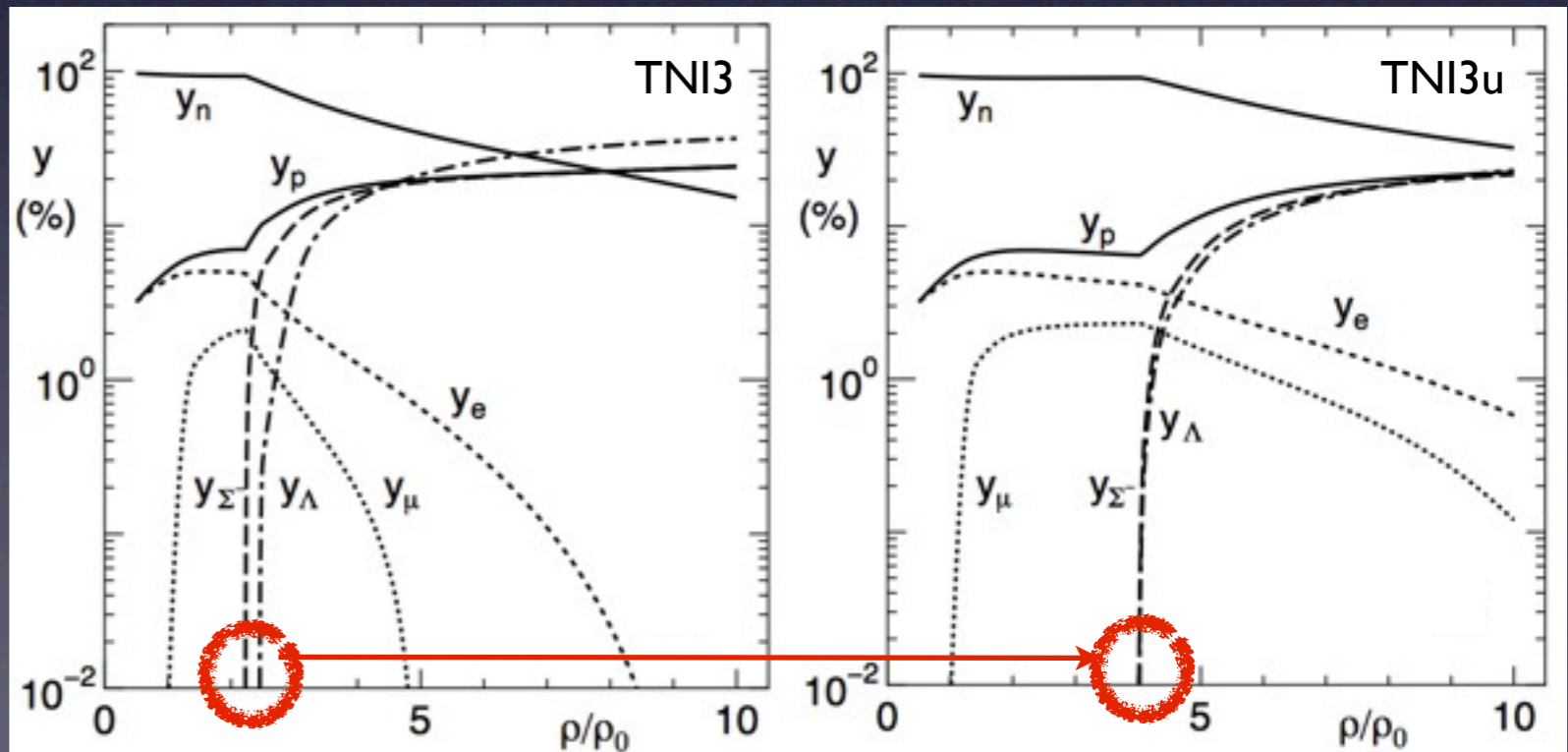
G-matrix

NN : Reid soft-core potential

YN,YY: Nijmegen type-D  
hard-core potential

TNI2(3):

$\kappa=250(300)\text{MeV}$



Nishizaki et al. (2002)



# Cooling Problem

Rapid cooling is occurred by hyperons ( $\Upsilon$ -Durca)

$$\left\{ \begin{array}{l} \Lambda \rightarrow p + l + \bar{\nu}_l, \quad p + l \rightarrow \Lambda + \nu_l \\ \Sigma^- \rightarrow \Lambda + l + \bar{\nu}_l, \quad \Lambda + l \rightarrow \Sigma^- + \nu_l \end{array} \right.$$

