

Exotic dibaryons with a heavy antiquark

Yasuhiro Yamaguchi¹

in collaboration with

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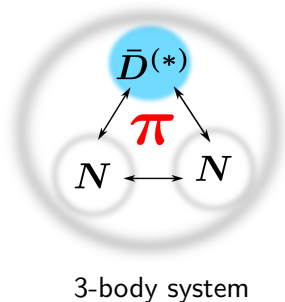
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YITP international workshop on Hadron in Nucleus

10/31-11/2 2013, Maskawa Hall in Kyoto University, Japan

- 1 Introduction
 - Heavy Quark Spin Symmetry
 - π exchange potential between heavy meson and nucleon.
- 2 Results of $\bar{D}^{(*)}NN$ and $B^{(*)}NN$
- 3 Results of $P^{(*)}NN$ in $m_Q \rightarrow \infty$
- 4 Summary

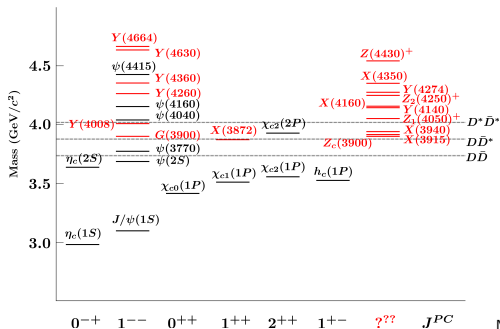


Exotic hadrons in the heavy quark region

Introduction

- New particles (XYZ) with heavy quarks: Belle, BaBar...
- These states cannot be explained by **a simple quark model** (Baryons qqq , Meson $q\bar{q}$). \rightarrow Exotic hadrons

In charm sector,



Charmonium $c\bar{c}$
and
Exotic hadrons

Fig.: Charmonium spectroscopy.

N. Brambilla, et al. Eur.Phys.J.C **71**(2011)1534
S. Godfrey and N. Isgur, PRD**32**(1985)189

Exotic hadrons in the heavy quark region

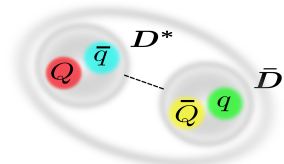
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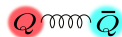
Structures of exotic hadrons. (Meson)



Tetraquark
(Compact)



Hadronic molecule



$Q\bar{Q}g$ hybrid

...

Q : Heavy quark (c, b), q : Light quark (u, d)

Exotic hadrons in the heavy quark region

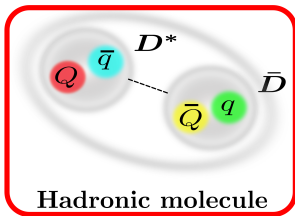
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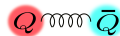
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- Hadron molecules: Loosely bound state or resonance of two hadrons. Candidates? $X(3872)$, Z_b ...

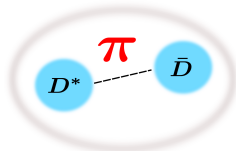
S.K.Choi *et al.*, PRL**91** (2003) 262001, A.Bondar, *et al.*, PRL**108**(2012)122001

Hadronic molecule and π exchange potential

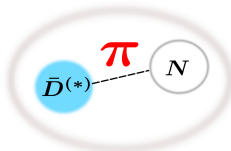
Introduction

Hadronic molecules

Meson-Meson



Meson-Baryon



- Driving force to form molecules: π exchange potential ?
- In the heavy quark region,

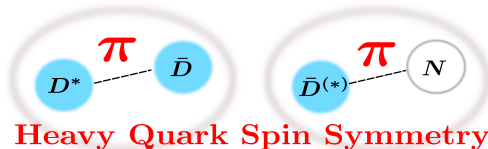
Hadronic molecule and π exchange potential

Introduction

Hadronic molecules

Meson-Meson

Meson-Baryon



- Driving force to form molecules: π exchange potential ?
 - In the heavy quark region, π exchange potential is enhanced by **the Heavy Quark Spin Symmetry**.
 - Meson-Meson molecules: The importance of **the tensor force** in “Deuson” N. A. Törnqvist, Z. Phys. C **61** (1994) 525
 - $\bar{D}N$ and BN ($\bar{Q}qqqq$) \rightarrow **Genuinely Exotics!**
T. D. Cohen, *et al.*, PRD**72**(2005)074010, S. Yasui and K. Sudoh, PRD**80**(2009)034008
Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD**84**(2011)014032 and PRD**85**(2012)054003
- \Leftrightarrow KN ($\bar{s}qqqq$) doesn't exist due to a repulsive force.

Heavy Quark Spin Symmetry and Heavy meson

Introduction

Heavy Quark Spin Symmetry

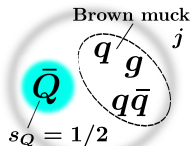
N.Isgur, M.B.Wise, PRL66,1130

- In the heavy quark limit ($m_Q \rightarrow \infty$),

$$\vec{J} = \vec{s}_Q + \vec{j}$$

s_Q : Heavy quark spin, j : the total angular momentum of the [brown muck](#)

([Brown muck](#): Everything other than the heavy quark in the hadron)



\triangleright $s_Q = 1/2$ and j are decoupled

$$\Rightarrow \text{Degenerate states} \begin{cases} (j + 1/2)^P \\ (j - 1/2)^P \end{cases} \quad (j \neq 0)$$

Heavy Quark Spin Symmetry and Heavy meson

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Heavy Quark Spin Symmetry

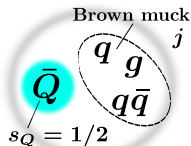
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\Downarrow Heavy meson

P^* P $\left\{ \begin{array}{l} \text{Heavy pseudoscalar meson } P(0^-) \text{ and} \\ \text{Heavy vector meson } P^*(1^-) \text{ are degenerate.} \end{array} \right.$

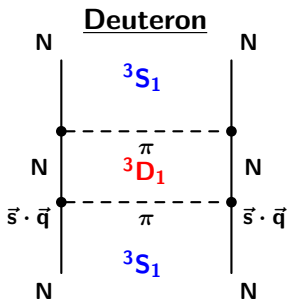
Indeed, mass splitting between P and P^* is **small**.

$$\begin{cases} m_{B^*} - m_B \sim 45 \text{ MeV} \\ m_{D^*} - m_D \sim 140 \text{ MeV} \end{cases} \Leftrightarrow \begin{array}{l} \text{For strange sector} \\ m_{K^*} - m_K \sim 400 \text{ MeV} \end{array}$$

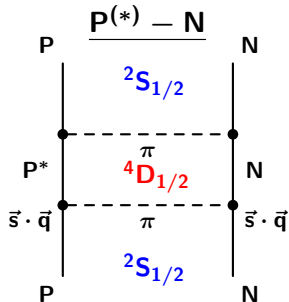
The one pion exchange potential in $P^{(*)}N$ system.

Introduction

- The π exchange potential (OPEP) appears through **$PP^*\pi$ and $P^*P^*\pi$ vertices**. ($PP\pi$ is forbidden.)
 → The OPEP is enhanced when P and P^* are degenerate.
- The OPEP is important in the heavy meson system.
- The OPEP(**Tensor force**) generates a **strong attraction** in Analogy with Deuteron.

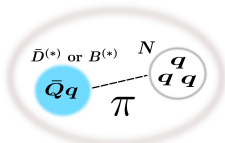


Tensor force \Rightarrow ${}^3S_1 - {}^3D_1$



$PN({}^2S_{1/2}) - P^*N({}^4D_{1/2})$

$P(*)N$ molecule (2-body system) (previous works)



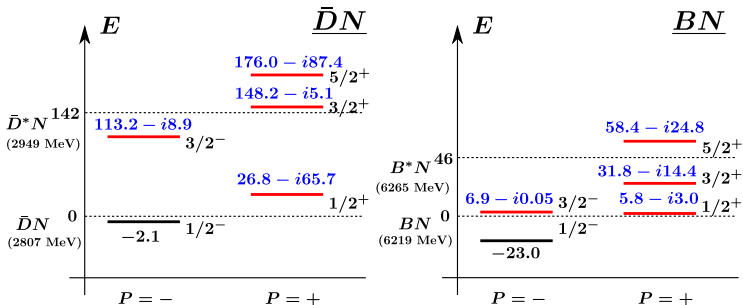
Exotic baryons!

▷ Bound and resonant states were obtained.

S. Yasui and K. Sudoh, PRD80(2009)034008

Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD84(2011)014032, PRD85(2012)054003

▷ **The tensor force of OPEP** plays an important role.

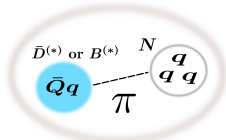


— : Bound state

— : Resonance ($E_{re} - i\Gamma/2$) Unit: MeV

Y.Y., S.Ohkoda, S.Yasui and A.Hosaka, PRD84 014032 (2011) and PRD85 054003 (2012)

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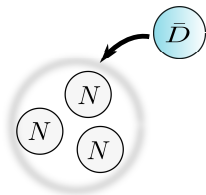
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▷ **The tensor force of OPEP** plays an important role.

$P^{(*)}$ nuclei (Few body or many body)?



• $P^{(*)}$ nuclei ($P^{(*)} = \bar{D}^{(*)}, B^{(*)}$) → Exotics!

- Impurity effects e.g. glue-like effect.
- Heavy meson-nucleon interaction.

• several works for $\bar{D}(B)$ meson in nuclear matter and in ^{12}C , ^{208}Pb ...

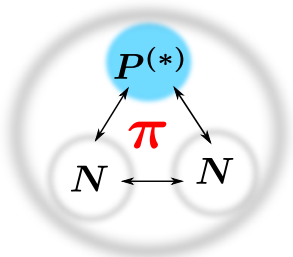
e.g. C. Garcia-Recio, *et al.*, PRC**85** (2012)025203.

S. Yasui and K. Sudoh, PRC**87**(2013)015202.

• However, there is **no study for few-body $\bar{D}(B)$ nuclei** in the literature so far.

Main Subject

- Exotic dibaryons with a heavy antiquark, $\bar{D}^{(*)}NN$ and $B^{(*)}NN$ (3-body system).



$$P^{(*)}NN$$
$$(P^{(*)} = \bar{D}^{(*)}, B^{(*)})$$

- $P = \bar{D}(\bar{c}q), B(\bar{b}q) \rightarrow$ **Genuinely exotic states!**
 \Leftrightarrow **KNN doesn't exist.** (KN interaction is repulsive force.)
- We study **bound and resonant states** by solving the coupled-channel Schrödinger equations for **PNN and P*NN channels.**
- We employ only OPEP. ($\rho, \omega \dots \rightarrow$ Future Work)

Lagrangian($P^{(*)} - N$) and Form factor

▷ Lagrangian

- **Heavy-light chiral Lagrangian** R.Casalbuoni *et al.* PhysRept.281(1997)145

$$\mathcal{L}_{\pi HH} = ig_{\pi} \text{Tr} [H_b \gamma_{\mu} \gamma^5 \mathcal{A}_{ba}^{\mu} \bar{H}_a], \quad g_{\pi} = 0.59 \text{ for } \bar{D} \text{ and } B$$

From $D^* \rightarrow D\pi$ decay

$$H_a = \frac{1 + \not{v}}{2} [\mathbf{P}_{a\mu}^* \gamma^{\mu} - \mathbf{P}_a \gamma^5], \quad \bar{H}_a = \gamma^0 H_a \gamma^0$$

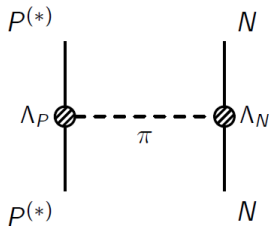
vector pseudoscalar

- **Bonn model** R.Machleidt *et al.* Phys Rept.149(1987)1

$$\mathcal{L}_{\pi NN} = ig_{\pi NN} \bar{N}_b \gamma^5 N_a \hat{\pi}_{ba}, \quad g_{\pi NN}^2 / 4\pi = 13.6$$

From NN data

▷ Form factor ($P^{(*)}N$)



Lagrangian($P^{(*)} - N$) and Form factor

▷ Lagrangian

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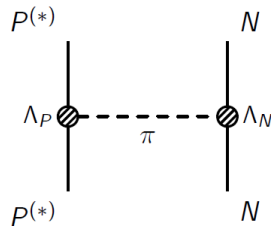
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$$F(\vec{q}) = \frac{\Lambda_N^2 - m_{\pi}^2}{\Lambda_N^2 + |\vec{q}|^2} \frac{\Lambda_P^2 - m_{\pi}^2}{\Lambda_P^2 + |\vec{q}|^2}$$



- 1 Λ_N is fixed to reproduce the Deuteron. (NN system)
- 2 Λ_P ; We assume $\Lambda_P/\Lambda_N = r_N/r_P$.

$$\begin{cases} \Lambda_D = 1.35\Lambda_N \\ \Lambda_B = 1.29\Lambda_N \end{cases} \Rightarrow \begin{matrix} \Lambda_N = 830 \text{ MeV} \\ \Lambda_D = 1121 \text{ MeV} \\ \Lambda_B = 1070 \text{ MeV} \end{matrix}$$

S.Yasui and K.Sudoh PRD**80**(2009)034008

$P^{(*)}N$ ($P^{(*)} = \bar{D}^{(*)}, B^{(*)}$) and NN interactions

- π exchange potential between $P^{(*)}(= \bar{D}^{(*)}, B^{(*)})$ and N

$$V_{PN-P^*N} = -\frac{g_\pi g_{\pi NN}}{\sqrt{2}m_N f_\pi} \frac{1}{3} \left[\vec{\epsilon}^\dagger \cdot \vec{\sigma} C(r) + S_\epsilon T(r) \right] \vec{\tau}_P \cdot \vec{\tau}_N$$

$$V_{P^*N-P^*N} = \frac{g_\pi g_{\pi NN}}{\sqrt{2}m_N f_\pi} \frac{1}{3} \left[\vec{T} \cdot \vec{\sigma} C(r) + S_T T(r) \right] \vec{\tau}_P \cdot \vec{\tau}_N$$

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$C(r)$: Central force, $T(r)$: Tensor force

$$g_\pi = 0.59 \text{ for } \bar{D} \text{ and } B, \quad g_{\pi NN}^2/4\pi = 13.6$$

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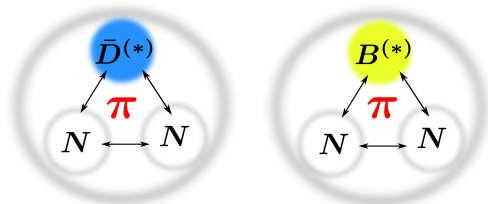
- NN int.: AV8' potential B. S. Pudliner, *et.al.*, PRC**56**(1997)1720

$$v'_8(r) = \sum_{p=1,8} v'_p(r) \mathcal{O}^p$$

$$\mathcal{O}^{p=1-8} = \begin{cases} \text{Central} & [1, \vec{\sigma}_1 \cdot \vec{\sigma}_2] \otimes [1, \vec{\tau}_1 \cdot \vec{\tau}_2] & (4 \text{ operators}) \\ \text{Tensor} & S_{12} \otimes [1, \vec{\tau}_1 \cdot \vec{\tau}_2] & (2) \\ \text{LS} & \vec{L} \cdot \vec{S} \otimes [1, \vec{\tau}_1 \cdot \vec{\tau}_2] & (2) \end{cases}$$

Results of $P^{(*)}NN$ states (3-body)

Exotic dibaryon states: $\bar{D}^{(*)}NN$, $B^{(*)}NN$



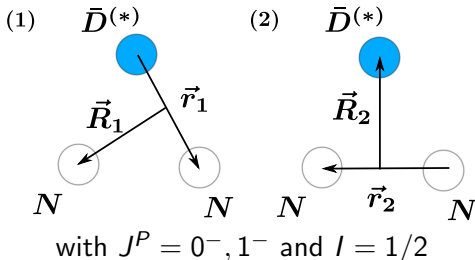
with $J^P = 0^-, 1^-$ and $I = 1/2$

Bound state and Resonance

- Wave functions are expressed by the Gaussian expansion method. E. Hiyama, *et al.*, Prog.Part.Nucl.Phys.51(2003)223
- Resonances \rightarrow Complex scaling method S.Aoyama,*et al.*,PTP116,1(2006)

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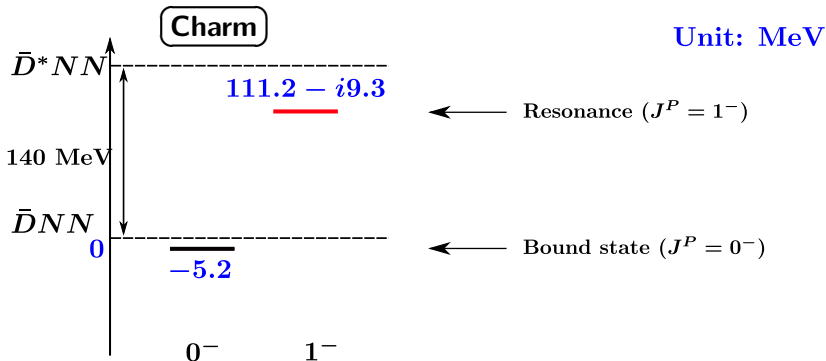
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Results of $\bar{D}^{(*)}NN$ and $B^{(*)}NN$ with $I = 1/2$ (Exotic)

$\bar{D}NN$ and BNN

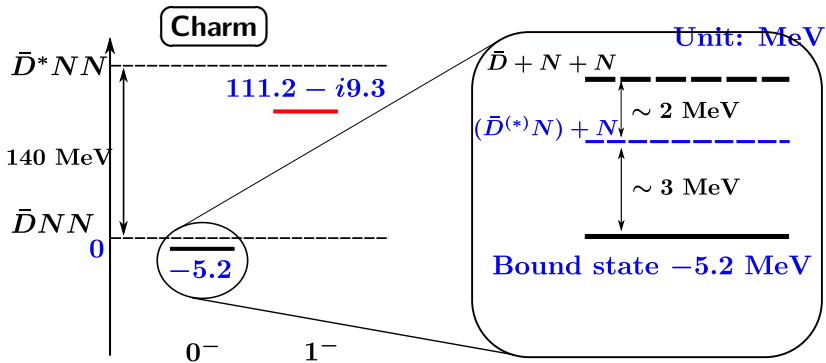
- **Bound states** for $J^P = 0^-$ and **Resonances** for $J^P = 1^-$ are found!
YY, S. Yasui, and A. Hosaka, arXiv:1309.4324 [nucl-th]



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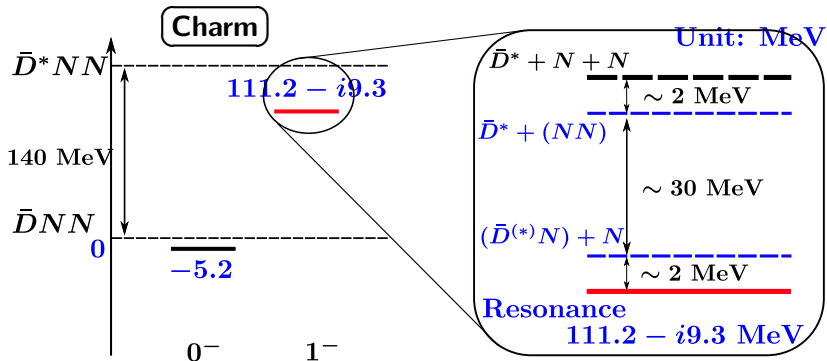


- $\bar{D}NN(0^-)$ locates below $\bar{D}N(1/2^-) + N$ threshold.

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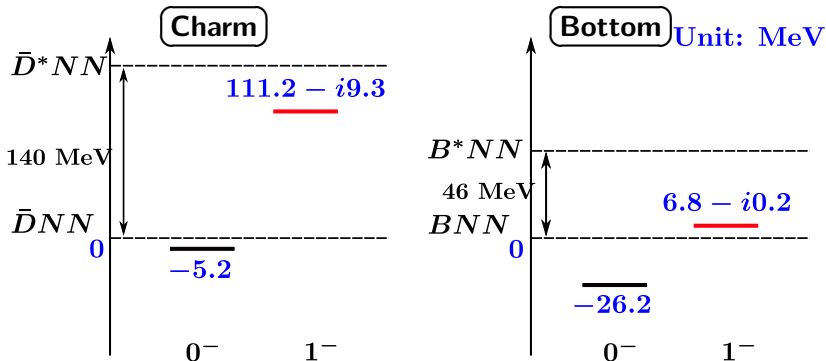


- $\bar{D}NN(0^-)$ locates below $\bar{D}N(1/2^-) + N$ threshold.
- $\bar{D}NN(1^-)$ locates below $\bar{D}^* + NN(1^+)$ and $\bar{D}N(3/2^-) + N$ thresholds.

Results of $\bar{D}^{(*)}NN$ and $B^{(*)}NN$ with $I = 1/2$ (Exotic)

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- $BNN > \bar{D}NN$ due to large reduced mass and small Δm_{BB^*} .

Results of $\bar{D}^{(*)}NN$ and $B^{(*)}NN$ with $I = 1/2$ (Exotic)

$\bar{D}NN$ and BNN

- Energy expectation values

The bound state of $\bar{D}NN(0^-)$

$\bar{D}^{(*)}NN$	$\langle V_{\bar{D}N-\bar{D}^*N} \rangle$	$\langle V_{\bar{D}^*N-\bar{D}^*N} \rangle$	$\langle V_{NN} \rangle$
Central	-2.3	-0.1	-9.5
Tensor	-47.1	0.7	-0.2
LS	—	—	-0.03

YY, S. Yasui, and A. Hosaka, arXiv:1309.4324 [nucl-th]

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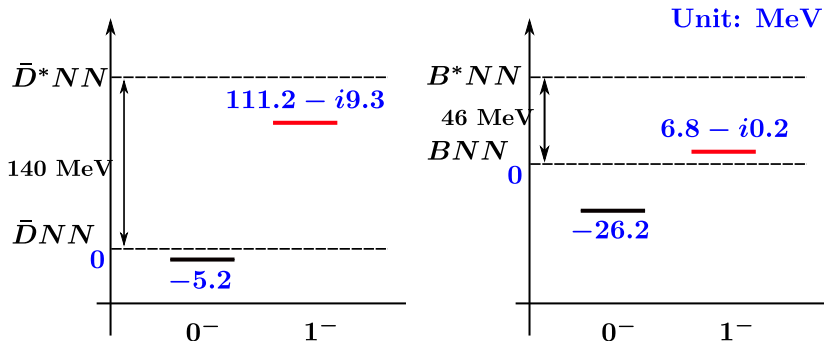
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- Tensor force of $\bar{D}N - \bar{D}^*N$ **mixing** component generates **the strong attraction**.
- For V_{NN} , **central force** is stronger than **tensor force**.
 $\Rightarrow NN(0^+)$ subsystem dominates in the bound state,
 while $NN(1^+)$ (=Deuteron) is minor.

Results of $\bar{D}^{(*)}NN$ and $B^{(*)}NN$ with $I = 1/2$ (Exotic)

$\bar{D}NN$ and BNN

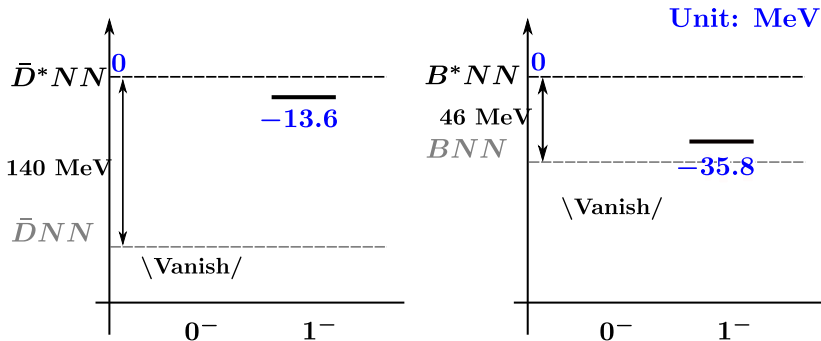
- If PNN channels are switched off...



Results of $\bar{D}^{(*)}NN$ and $B^{(*)}NN$ with $I = 1/2$ (Exotic)

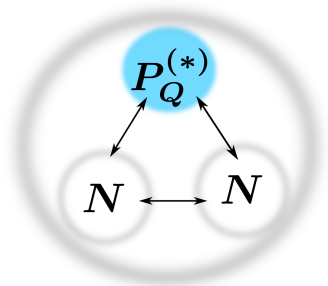
$\bar{D}NN$ and BNN

- If PNN channels are switched off...



- The bound states for $J^P = 0^-$ vanish.
 $\Rightarrow PN - P^{*}N$ mixing components are very important!
- For $J^P = 1^-$ channel, the bound states survive.
 \Rightarrow **Feshbach resonance!**

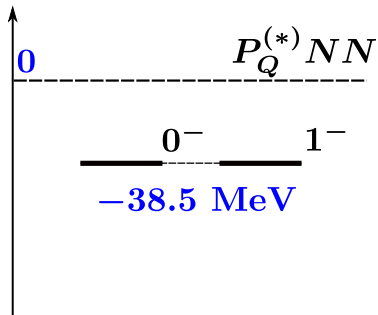
Results of $P_Q^{(*)}$ NN states ($m_Q \rightarrow \infty$)



$$P_Q^{(*)} NN \quad (m_{P_Q^{(*)}} - m_{P_Q} = 0)$$

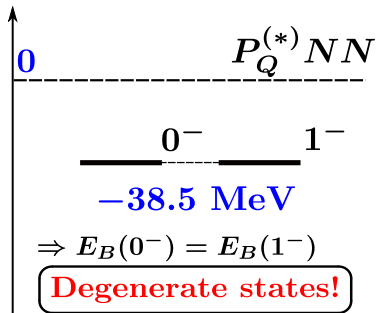
Results of $P_Q^{(*)} NN$ in $m_Q \rightarrow \infty$ (Exotic)

- We find bound states both for $J^P = 0^-$ and 1^- !



Results of $P_Q^{(*)} NN$ in $m_Q \rightarrow \infty$ (Exotic)

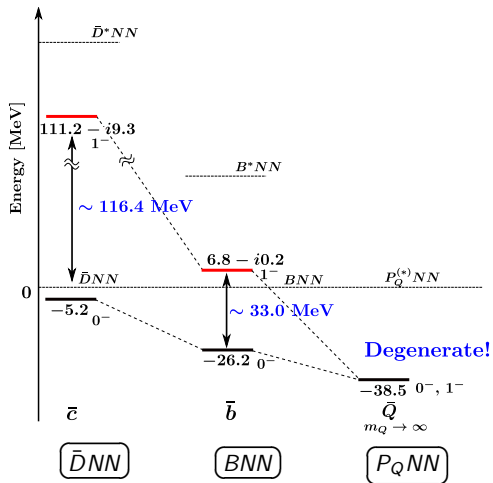
- We find bound states both for $J^P = 0^-$ and 1^- !



- $P^{(*)} NN$: Degenerate states $(j - 1/2, j + 1/2)^P = (0, 1)^-$
 \rightarrow Brown muck $[qNN]^P$ has $j^P = 1/2^+$.

Results of $P_Q^{(*)}NN$ in $m_Q \rightarrow \infty$ (Exotic)

- Energy-levels for $\bar{D}NN$, BNN and $P_Q NN(m_Q \rightarrow \infty)$



- Splitting between $E(1^-)$ and $E(0^-)$ decreases as m_Q increases.

Summary

- We have investigated genuinely exotic dibaryons formed by $P^{(*)}NN$.
- The π exchange potential was employed between a heavy meson $P^{(*)}$ and a nucleon N .
- For the $\bar{D}NN$ and BNN states, we have found the bound states with $J^P = 0^-$ and resonances with $J^P = 1^-$ for $I = 1/2$.
- **Tensor force of π exchange** plays a crucial role to produce a strong attraction.
- The **PN – P*N mixing** component is important to yield these states.
- In $m_Q \rightarrow \infty$, we have obtained the degenerate states of $J^P = 0^-$ and 1^- .

Back up

Central force and Tensor force

- Central force $C(r)$ and Tensor force $T(r)$

$$C(r) = \int \frac{d^3q}{(2\pi)^3} \frac{m_\pi^2}{\vec{q}^2 + m_\pi^2} e^{i\vec{q}\cdot\vec{r}} F(\Lambda_P, \vec{q}) F(\Lambda_N, \vec{q})$$

$$S_T(\hat{r}) T(r) = \int \frac{d^3q}{(2\pi)^3} \frac{-\vec{q}^2}{\vec{q}^2 + m_\pi^2} S_T(\hat{q}) e^{i\vec{q}\cdot\vec{r}} F(\Lambda_P, \vec{q}) F(\Lambda_N, \vec{q})$$

$$F(\Lambda, \vec{q}) = \frac{\Lambda^2 - m_\pi^2}{\Lambda^2 + \vec{q}^2}$$