

**Hydrodynamical models for
a successful/failed jet from a massive star
and implications to low-luminosity GRBs**

Akihiro Suzuki

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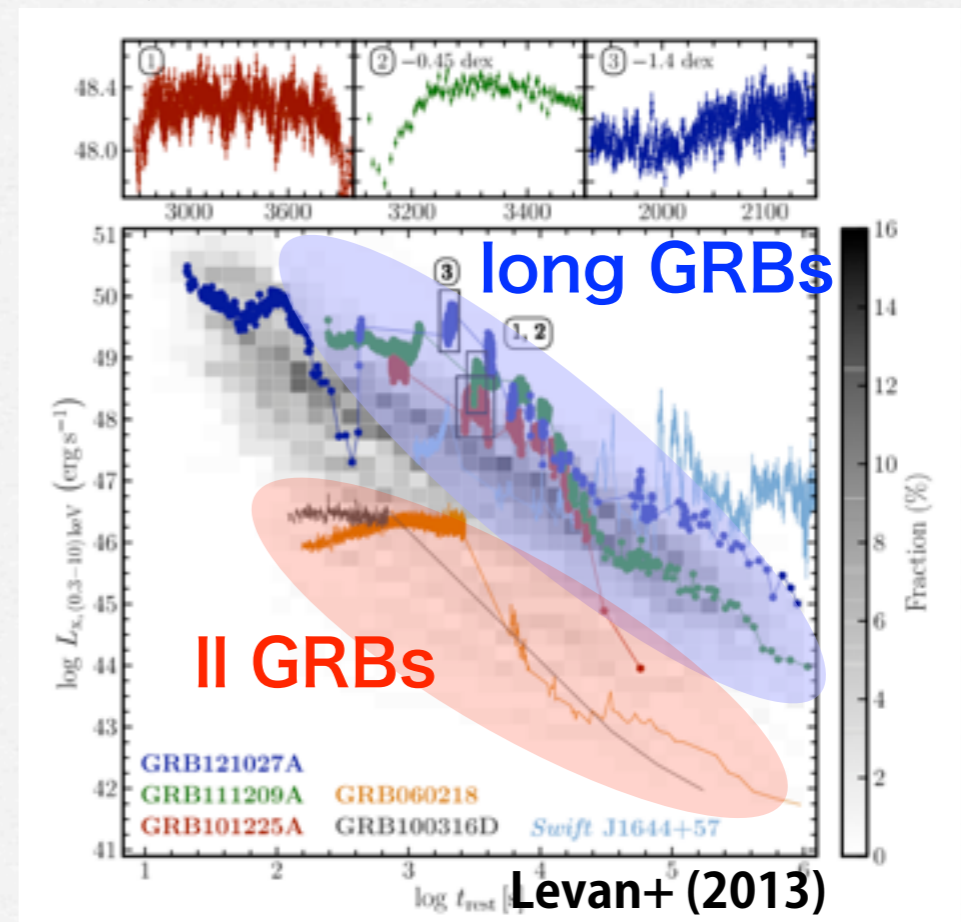
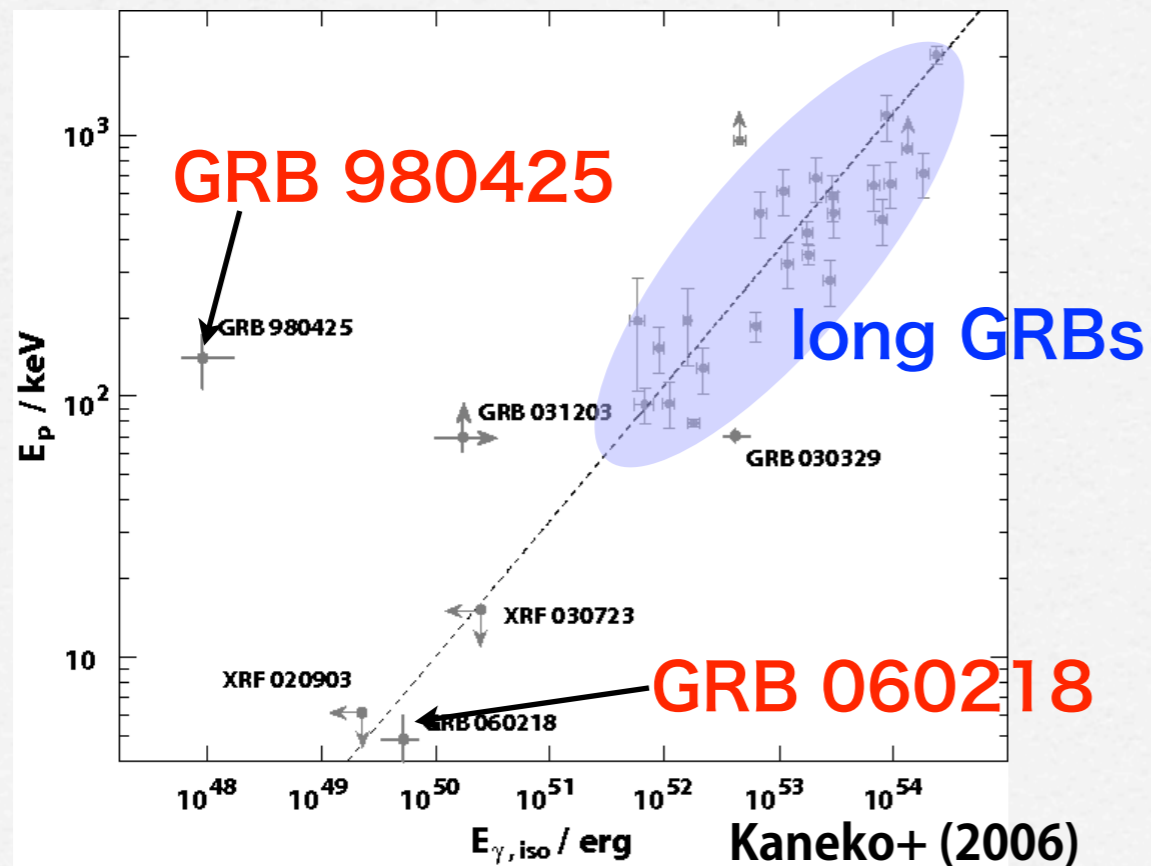
GRB-SNe, YITP Nov. 2013

Outline

- Brief introduction of low-luminosity GRBs
- Jet models
- Implications to emission from low-luminosity GRBs
- Summary

Low-luminosity GRBs

- ☑ less energetic and less luminous subgroup of long GRBs
- ☑ They are found in the nearby universe. The event rate is high
e.g., 230^{+490}_{-190} Gpc⁻³ yr⁻¹ (Soderberg+ 2006), 100-1800 Gpc⁻³ yr⁻¹ (Guetta&Della Valle 2007)
- ☑ They are accompanied by broad-lined Ic supernovae
- ☑ Ex.) GRB 980425/SN 1998bw, GRB 060218/SN 2006aj, GRB100316D/ SN2010bh



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	Luminosity $L_{\gamma, \text{iso}}$	Isotropic energy E_{iso}	Duration T_{90}	peak energy E_p
GRB 980425 SN 1998bw	$6 \times 10^{46} \text{ erg/s}$	$9 \times 10^{47} \text{ erg}$	35 s	122 keV
GRB 060218 SN 2006aj	$2 \times 10^{46} \text{ erg/s}$	$4 \times 10^{49} \text{ erg}$	2100 s	4.7 keV
GRB 100316D SN 2010bh	$5 \times 10^{46} \text{ erg/s}$	$6 \times 10^{49} \text{ erg}$	1300 s	18 keV

from Hjorth (2011)

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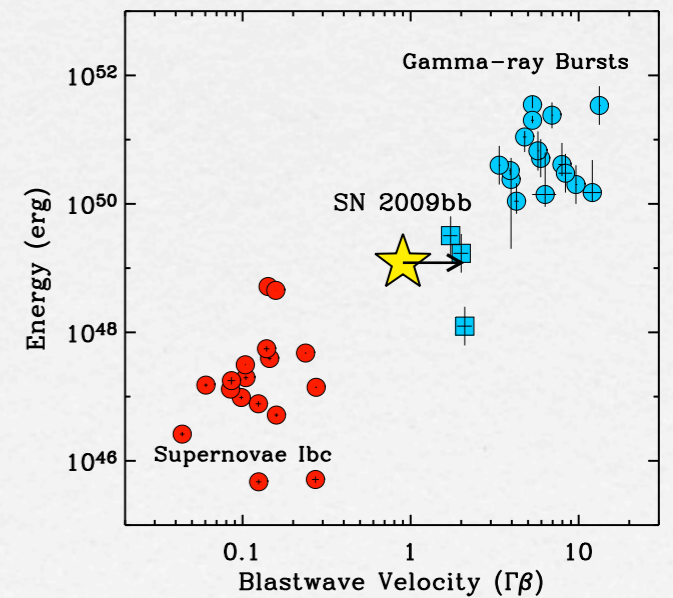
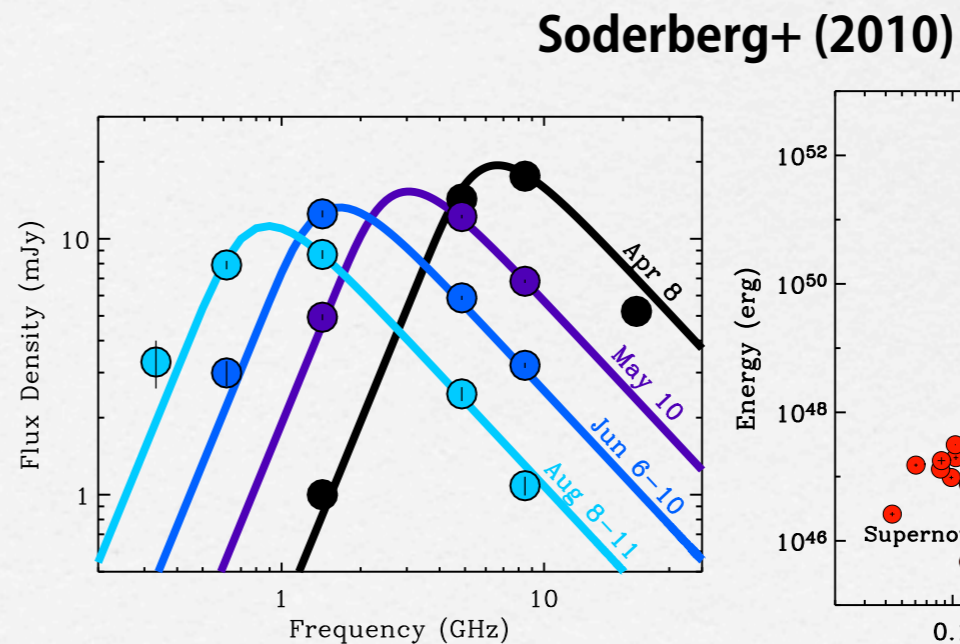
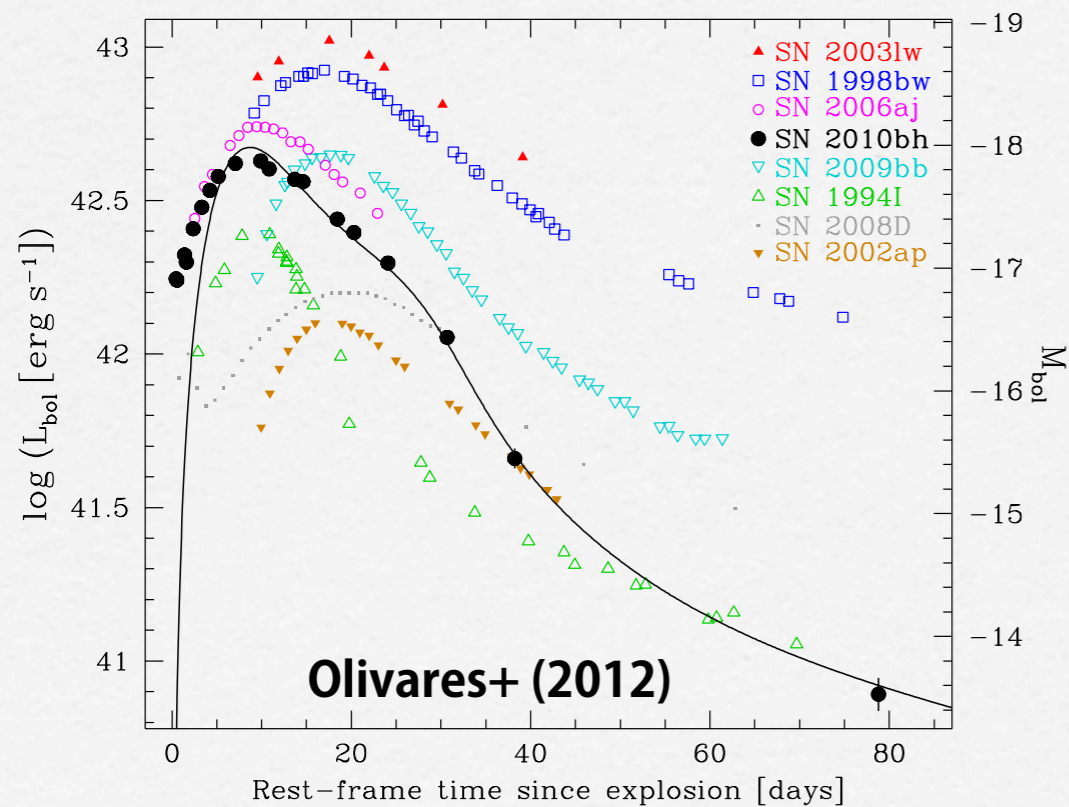
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Question to answer: What is their origin?
What mechanism is responsible for X- and γ - ray emission

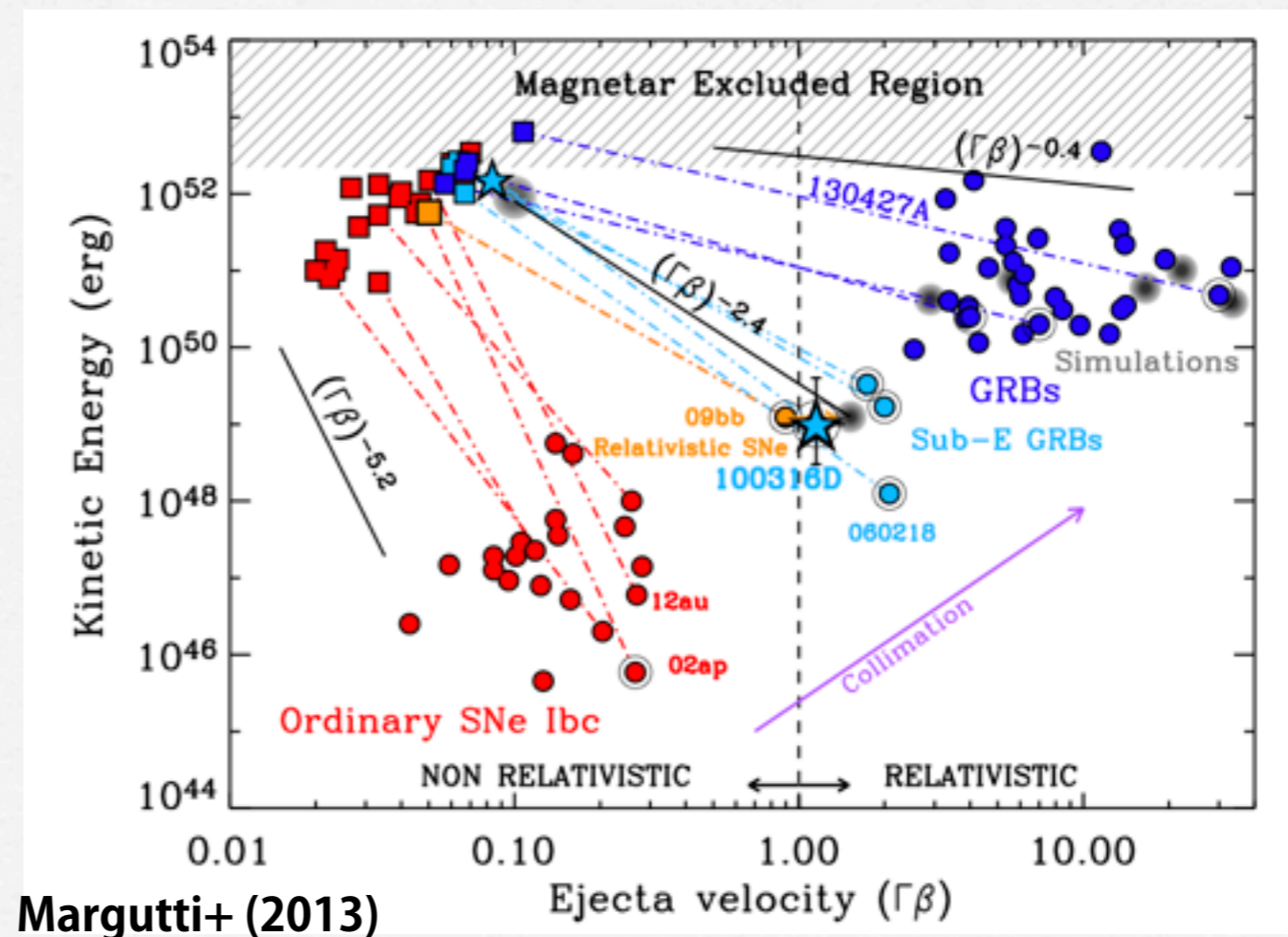
Connection to HNe, engine-driven SNe

- ☑ Optical observations: kinetic energy of non-relativistic ejecta is found by light curve modeling and spectroscopy : $v_{\text{ph}} \sim 0.1c$, $E_{\text{kin}} \sim 10^{52}\text{-}10^{53}$ erg
- ☑ Radio observations: kinetic energy of the blast wave is found by using synchrotron emission model : $\Gamma v = (1\text{-}2)c$, $E_{\text{kin}} \sim 10^{49}$ erg



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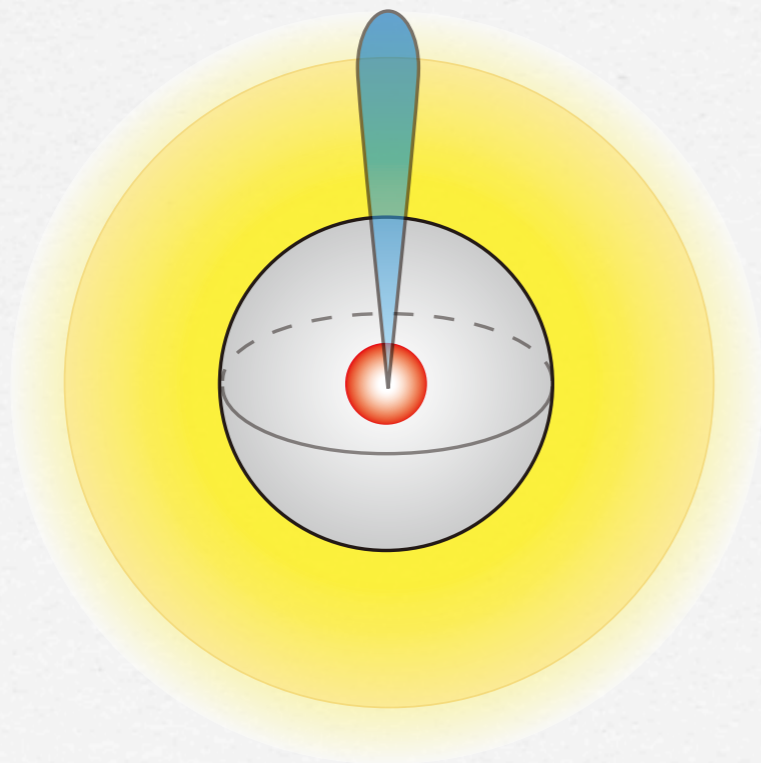


Failed jet hypothesis

- ☑ E_{kin} for relativistic ejecta $\ll E_{\text{kin}}$ for non-relativistic ejecta \rightarrow It is suggested that failed jet model produce such events.

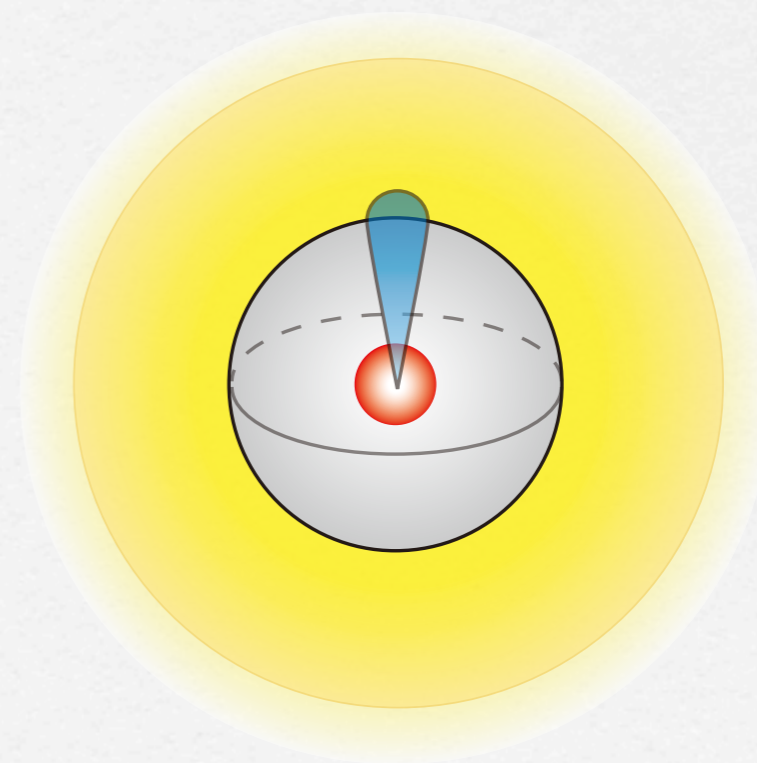
Ultra-relativistic jet:

E_{kin} for rel. ejecta $\sim E_{\text{kin}}$ for non-rel. ejecta



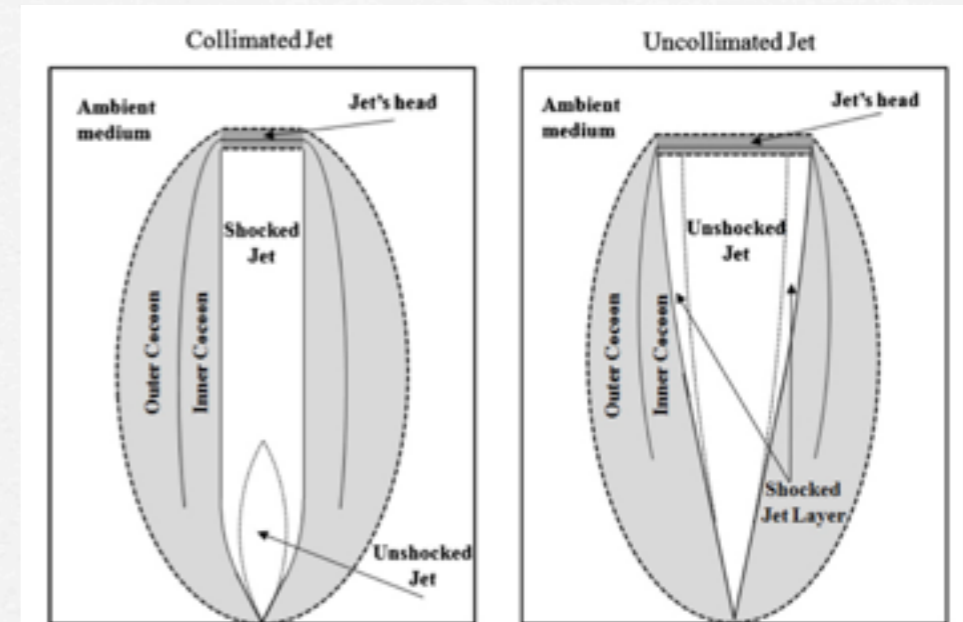
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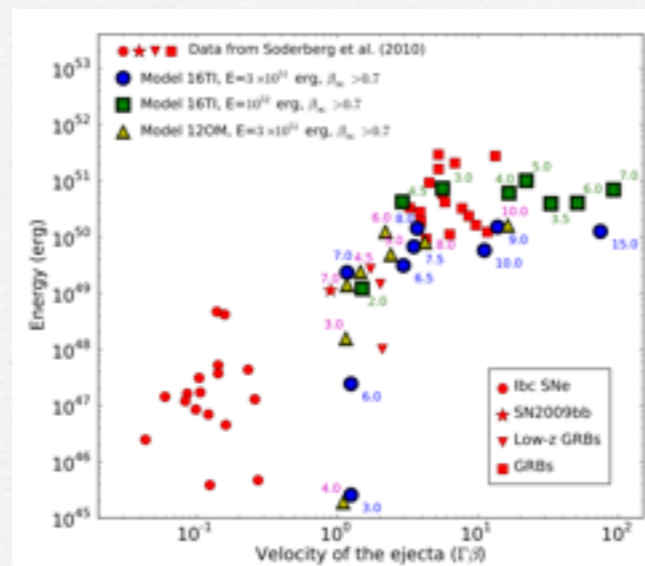
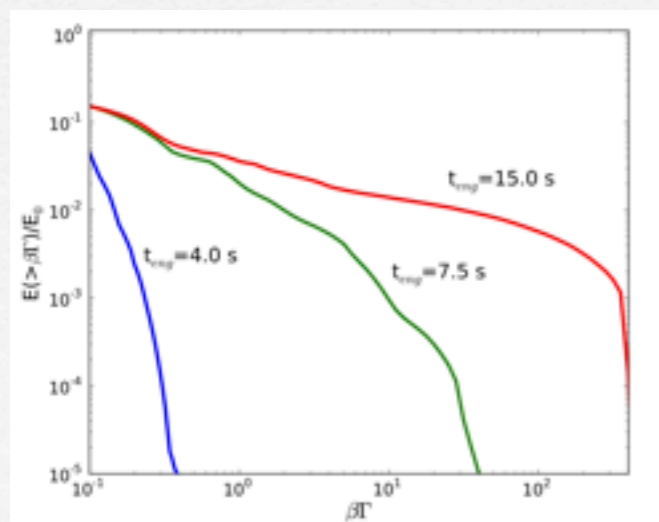


Failed jet hypothesis

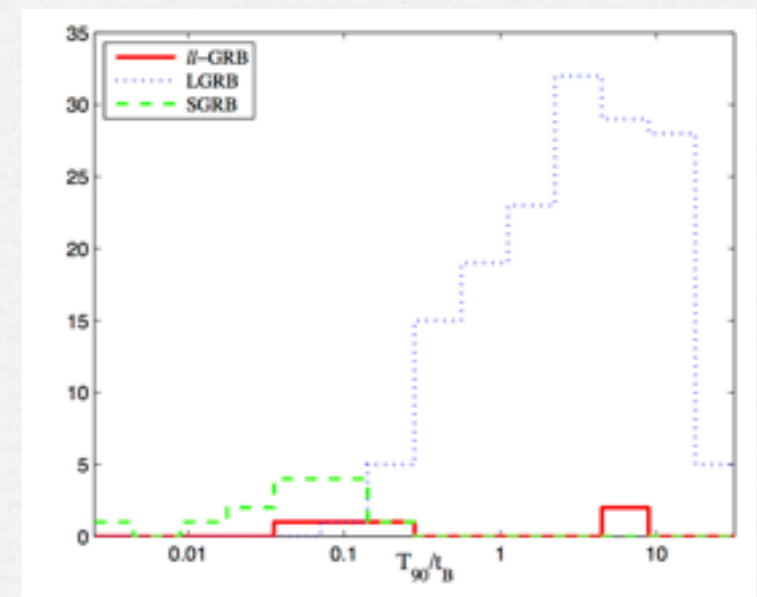
- ☑ E_{kin} for relativistic ejecta $\ll E_{\text{kin}}$ for non-relativistic ejecta \rightarrow It is suggested that failed jet model produce such events.
- ☑ Many works to reveal whether or not an ultra-relativistic jet succeed in penetrating a massive star (e.g., Bromberg+2011a,b, Lazzati+2011)



Bromberg+ (2011a,b)

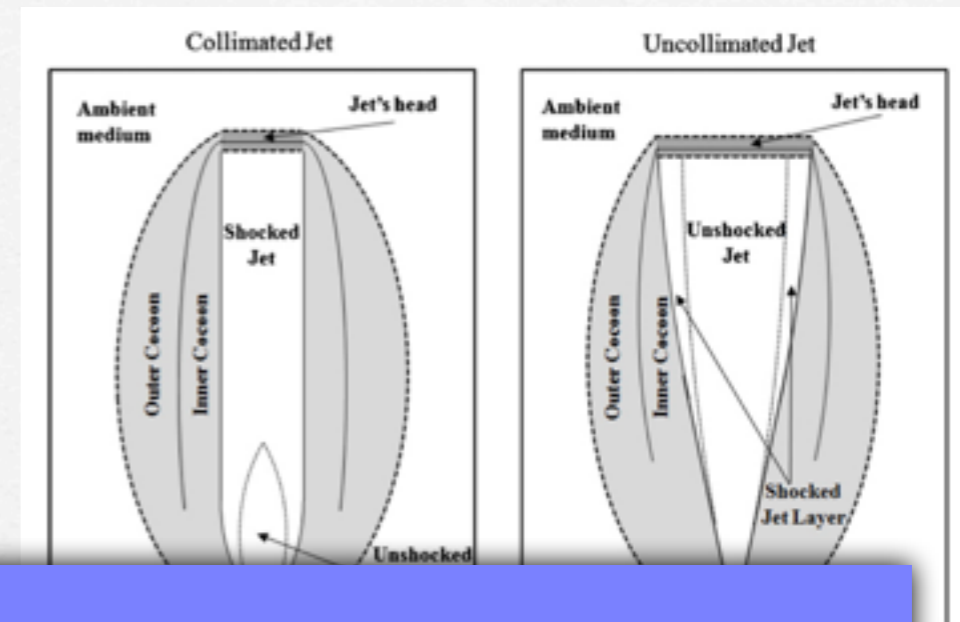


Lazzati+ (2011)



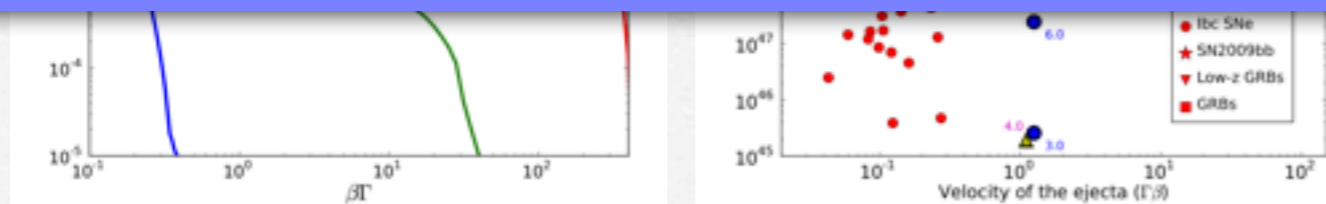
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This study

1. carry out a series simulations of jet propagation in a massive star and identify a model corresponding to low-luminosity GRBs.
2. carry out further calculations to reveal the properties of the model, including nucleosynthesis calculations and CSM interaction.



Lazzati+ (2011)

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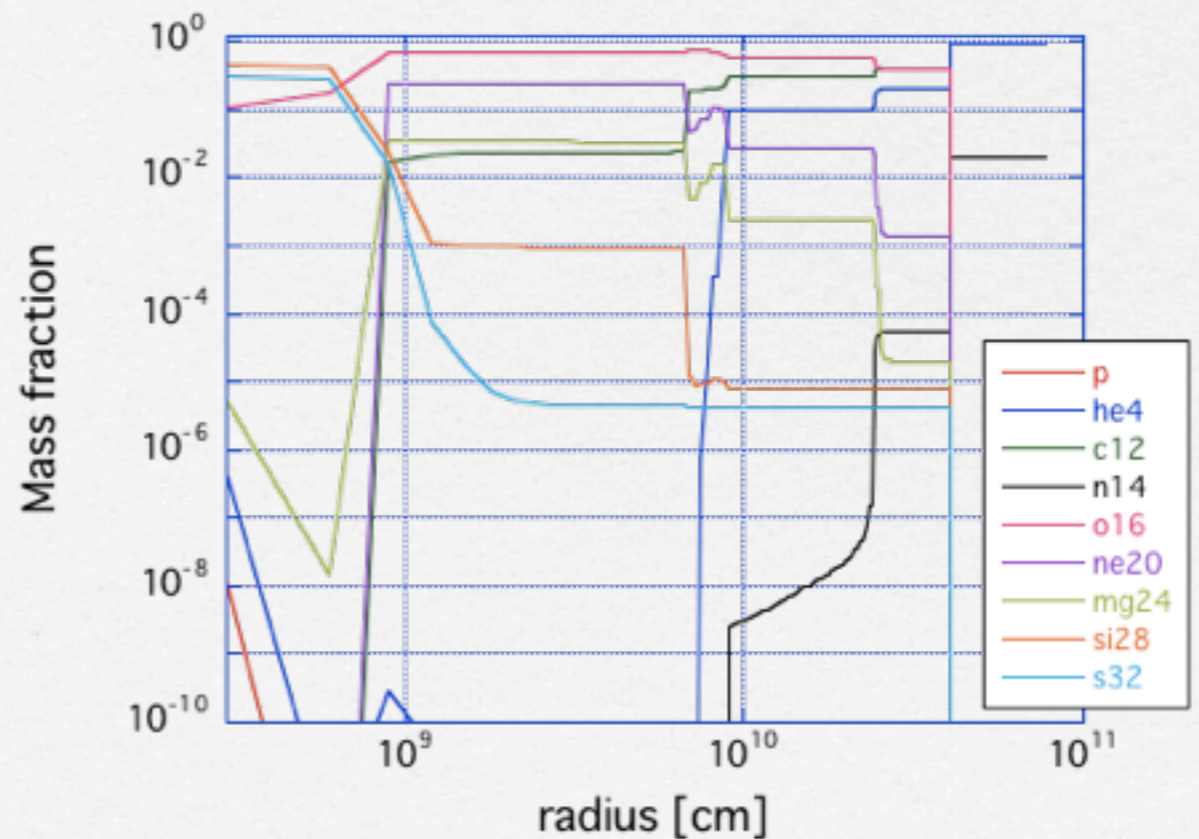
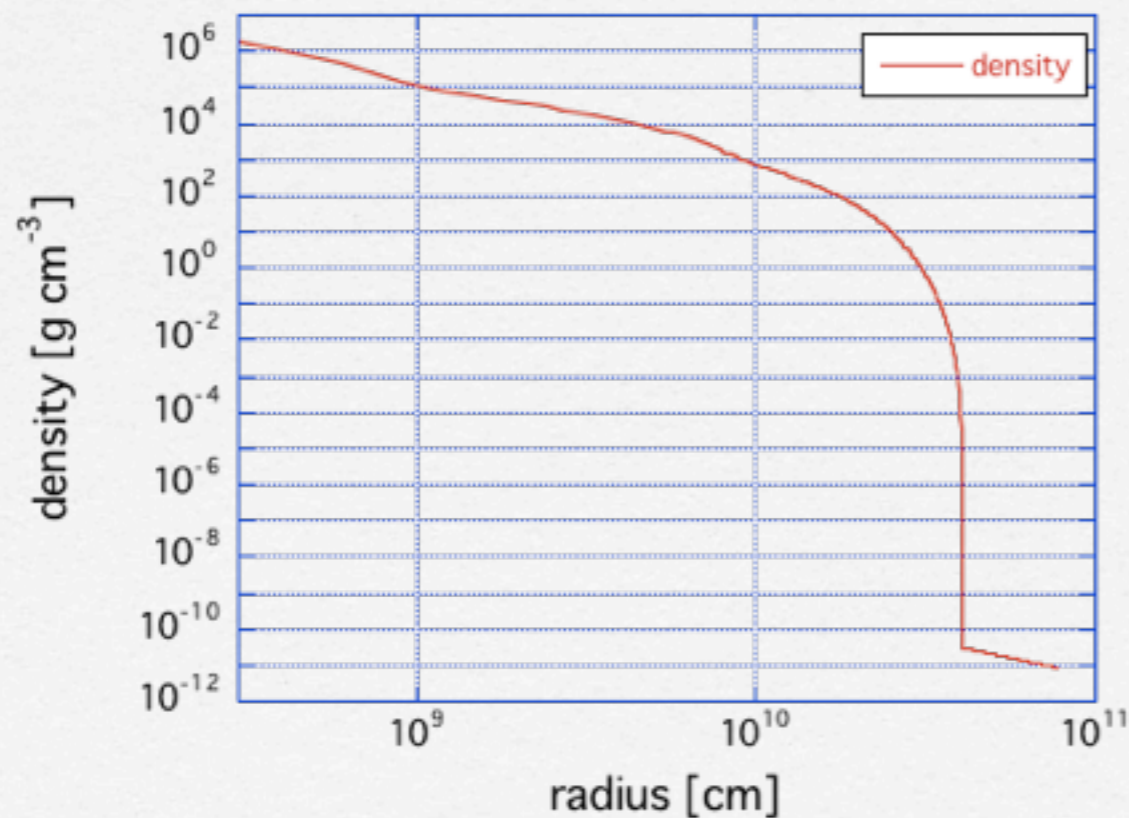
GRB jet simulation

- ☑ 4096 × 512 mesh
- ☑ Woosley&Heger(2006) 16Ti model
- ☑ WR star
- ☑ final mass ~ 14M_☉
- ☑ Radius ~ 3 × 10¹⁰cm

$$\rho_{\text{ext}} = \rho_{\text{w}}(r) + \rho_{\text{ISM}}$$

$$\rho_{\text{w}} = \frac{\dot{M}}{4\pi r^2 v_{\text{w}}}$$

$$\rho_{\text{ISM}} = 100 m_{\text{u}} \text{ g cm}^{-3}$$



Jet injection

- ☑ injection radius: $R_{in} = 3 \times 10^8 \text{cm}$
- ☑ total energy: $E = 5 \times 10^{52} \text{erg}$
- ☑ energy deposition rate: $dE/dt = 200, 100, 50, 20, 10, 5, 2, 0.5 \times 10^{51} \text{erg/s}$
- ☑ half opening angle: $\theta_j = 10^\circ$
- ☑ initial jet Lorentz factor: $\Gamma_j = 5$
- ☑ specific internal energy: $\epsilon_0/c^2 = 20$
- ☑ CSM: $\dot{M} = 10^{-7} M_\odot/\text{yr}, v_w = 1000 \text{km/s}$

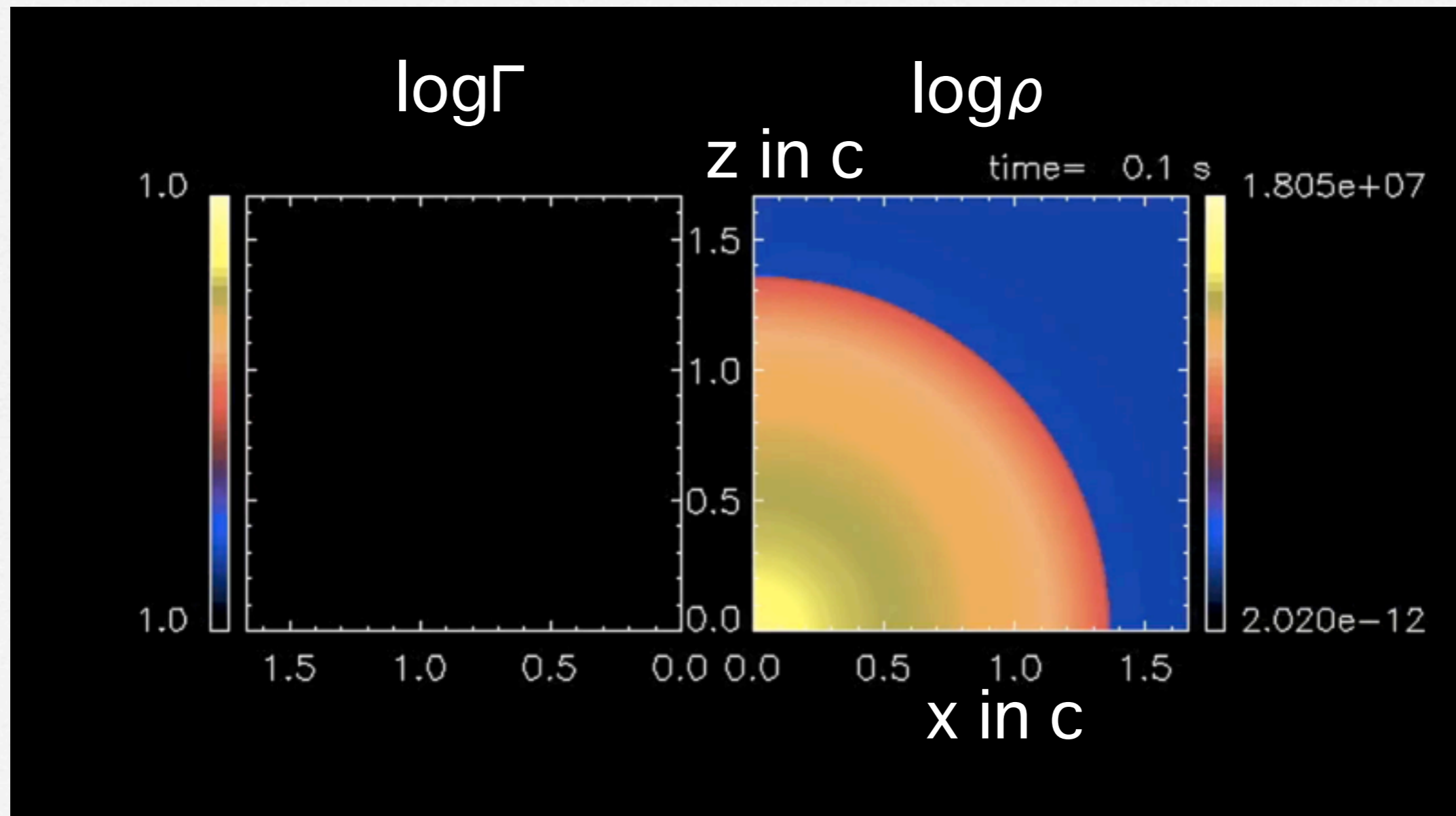
$$v_j = \sqrt{1 - \frac{1}{\Gamma_j^2}},$$

$$\rho_0 = \frac{\dot{E}}{2\pi R_{in}^2 (1 - \cos \theta_j) v_j [(1 + \gamma \epsilon_0) \Gamma_j^2 - \Gamma_j]},$$

$$p_0 = (\gamma - 1) \rho_0 \epsilon_0.$$

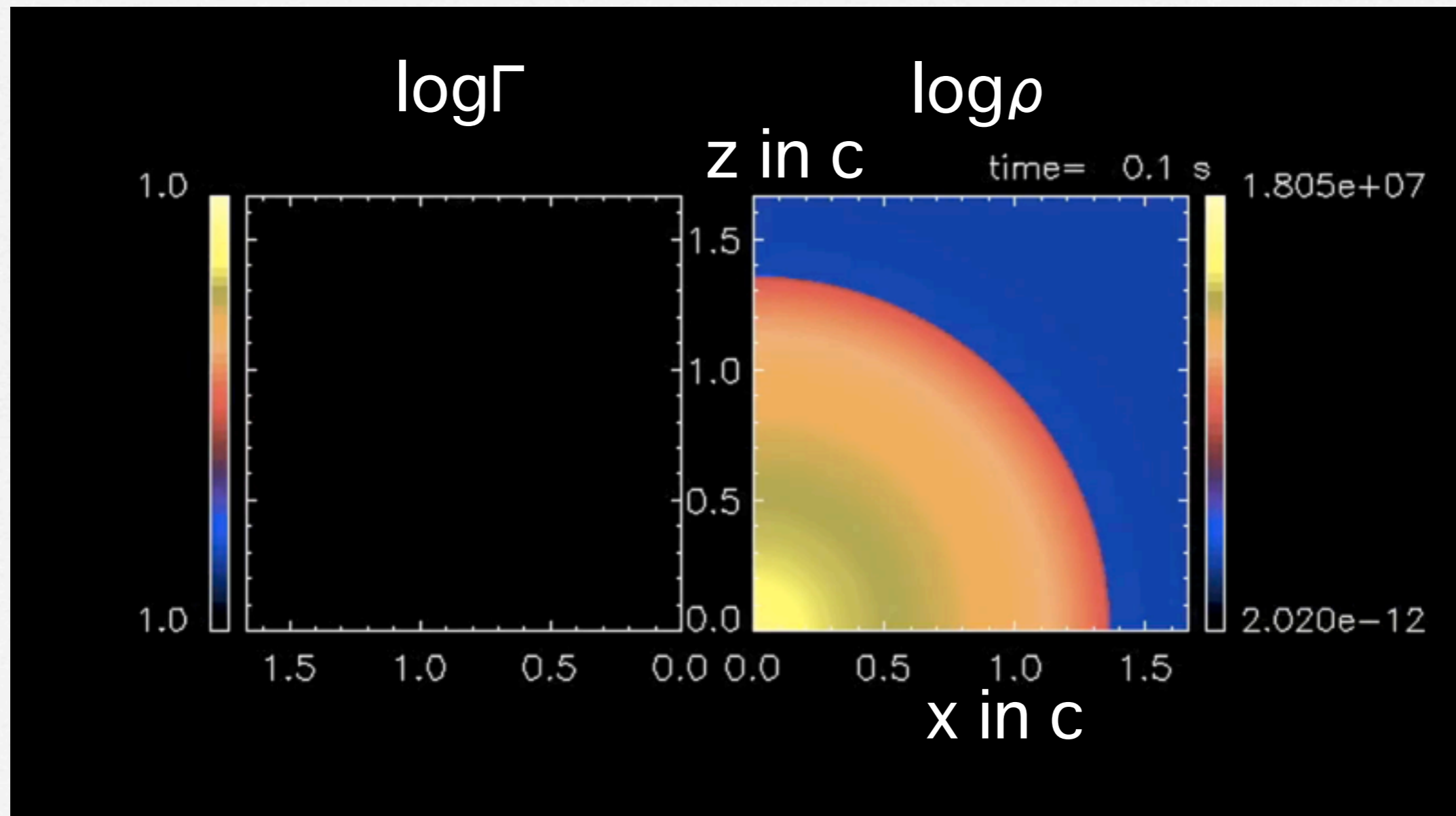
Jet models

- ☑ ultra-relativistic jet is formed successfully (jet break time < jet injection time)
low dE/dt ($=0.5 \times 10^{51}$ erg/s)
- ☑ left: Lorentz factor right: density
long t_{inj} ($=50$ s)



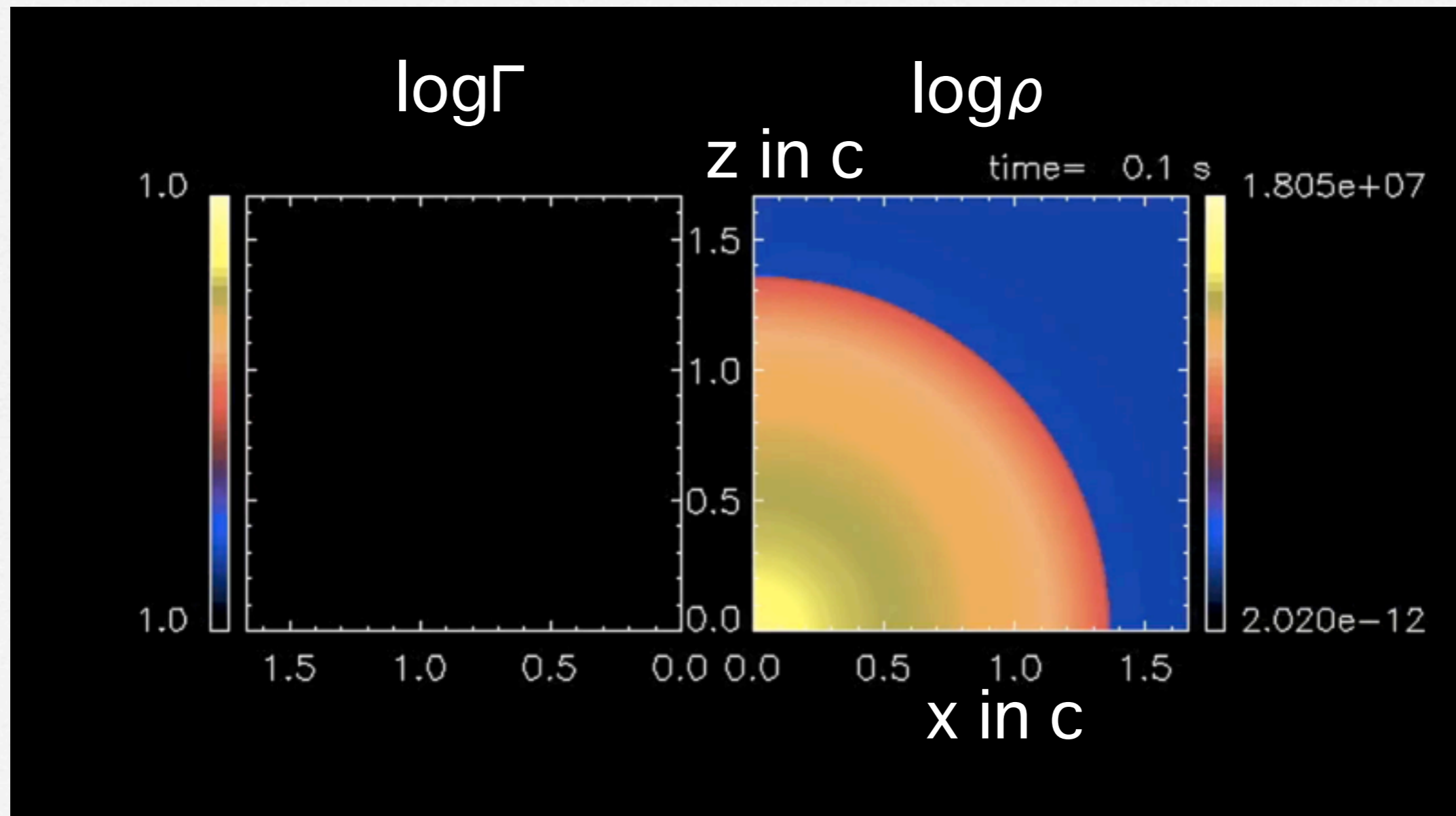
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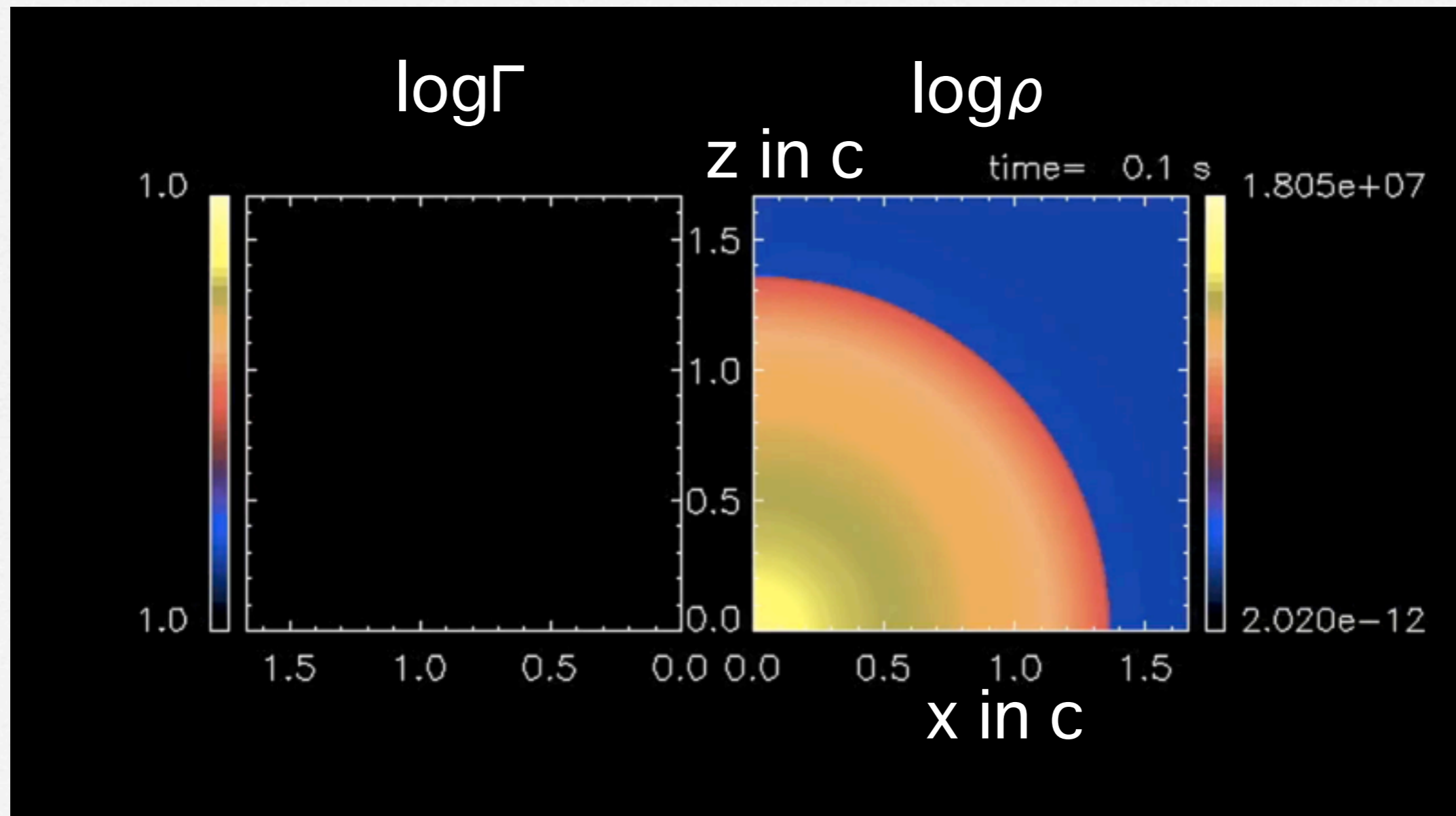
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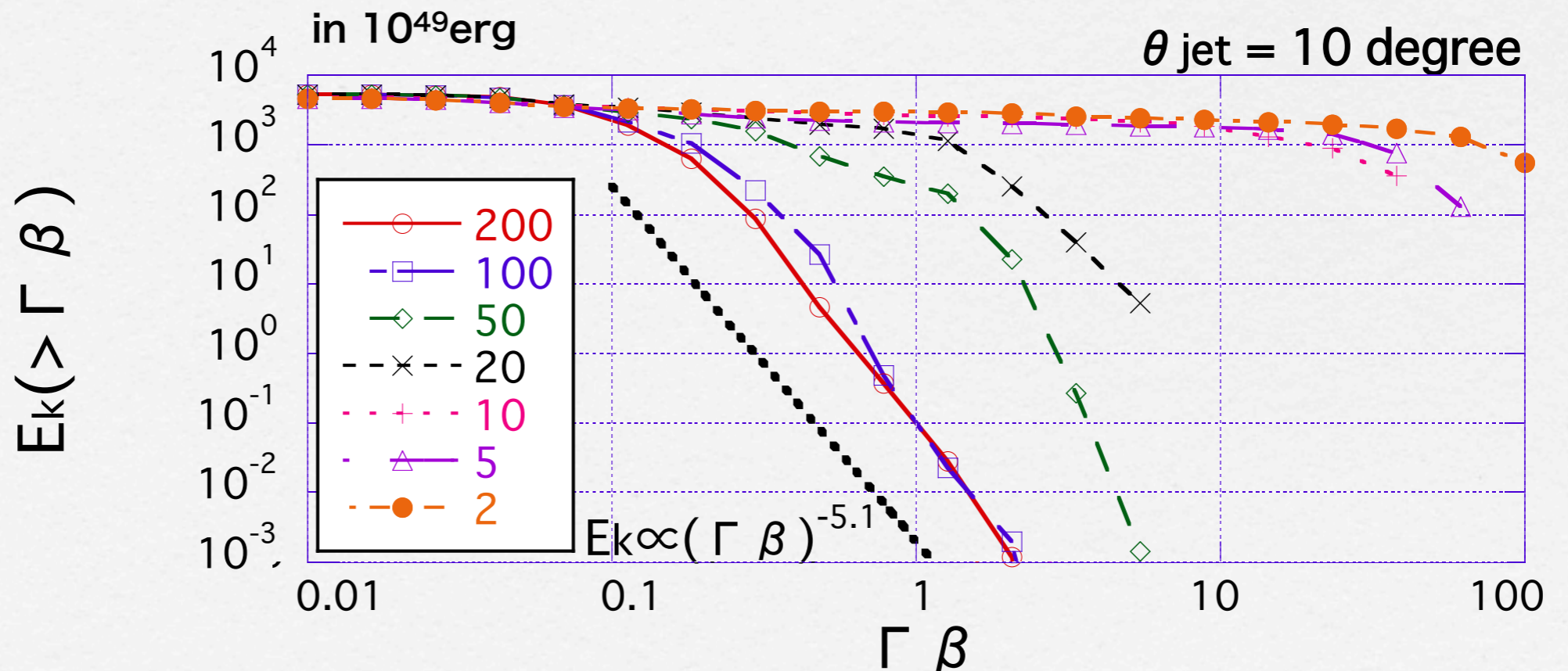


Kinetic energy distribution

- kinetic energy distribution of the ejecta at ~ 200 sec after the jet injection

$$E_k(> \Gamma \beta) = \int \Gamma(\Gamma - 1) \rho dV,$$

- Models with ultra-relativistic jet show flat distributions
- For models with nearly spherical blast waves, the distribution falls at $\Gamma \beta < a$ few



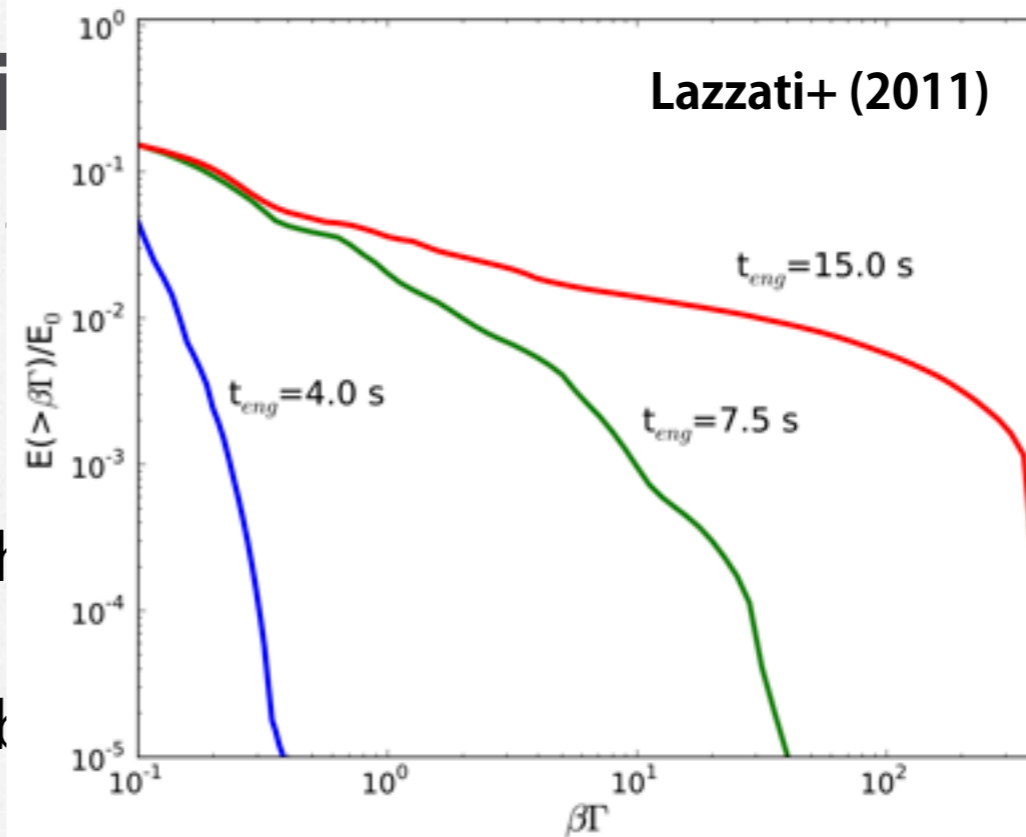
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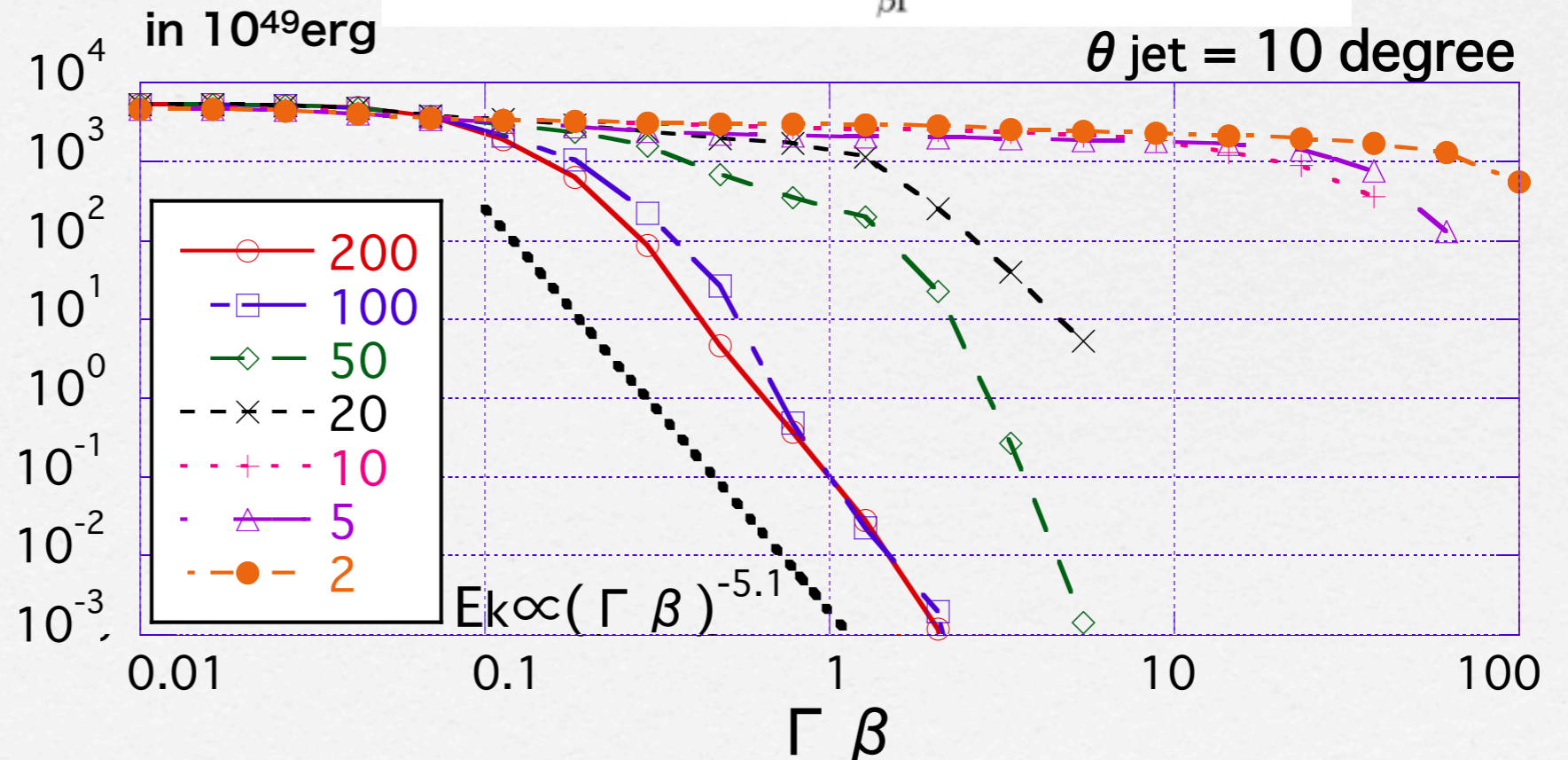
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$E_k(>\Gamma\beta)$

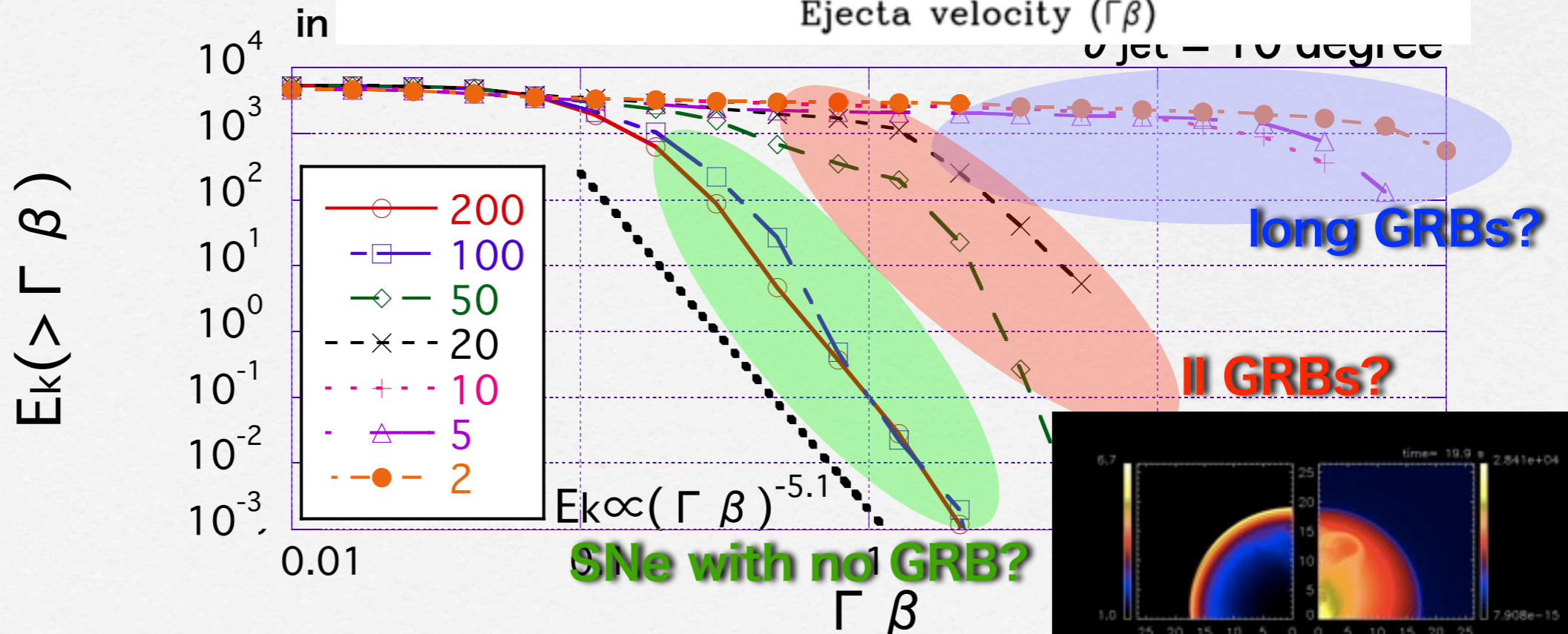
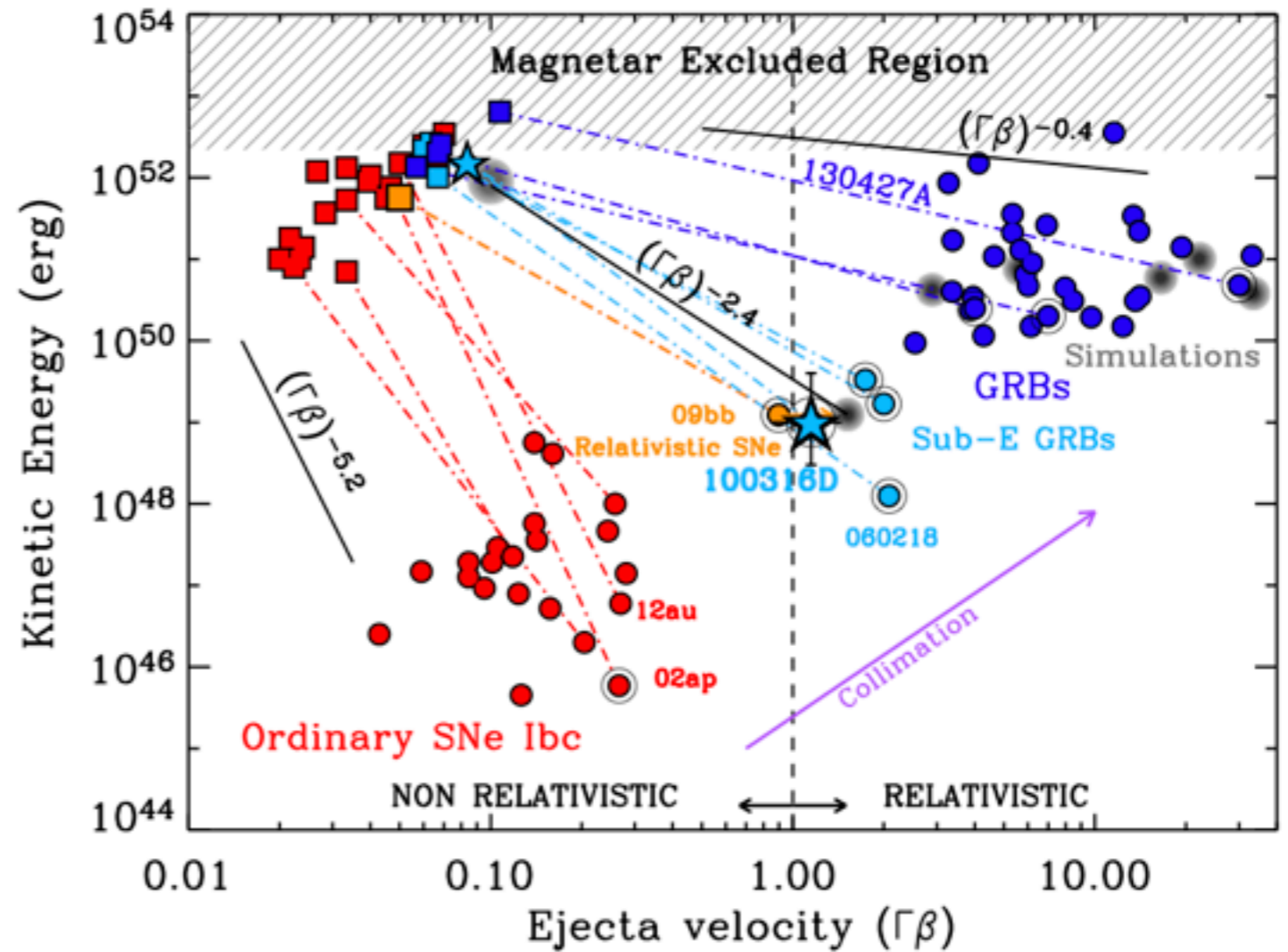


n

$3 < a$

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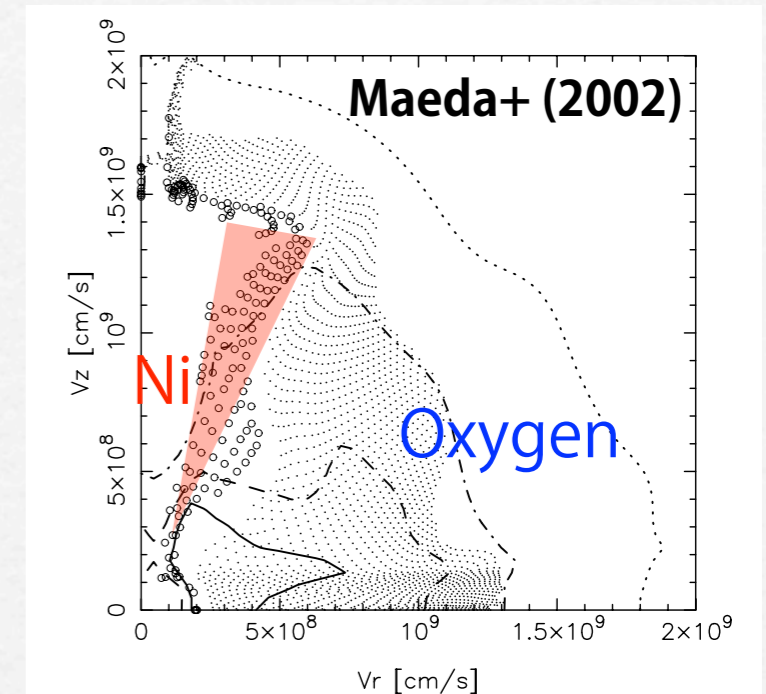


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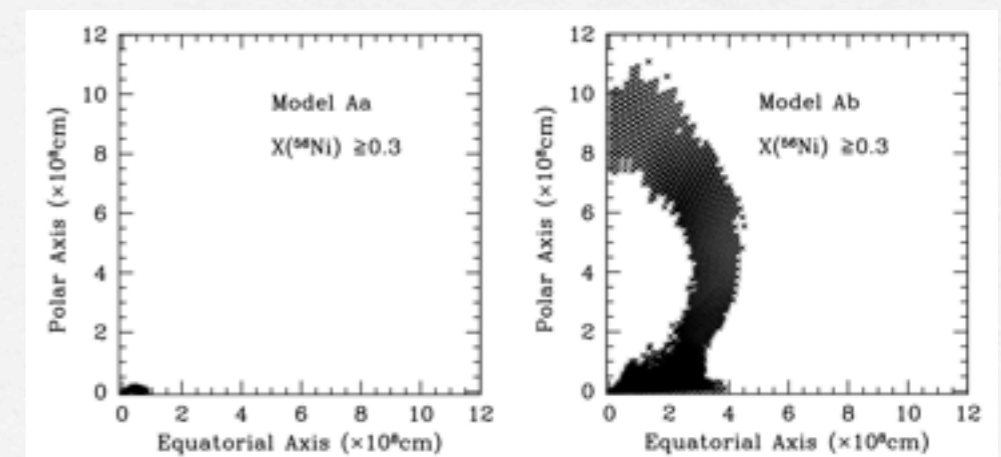
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Nucleosynthesis

- ☑ Post-process nucleosynthesis calculations
- ☑ Many earlier works in the context of bipolar explosion in SNe (e.g., Nagataki+1997,2003,2005, Maeda+2002,Tominaga+2007)
- ☑ ^{56}Ni mass: (e.g., Nagataki+2003,Tominaga+2007)
 - slow energy deposition $\Rightarrow M(^{56}\text{Ni}) \ll 0.1 M_{\odot}$
 - instantaneous energy injection $\Rightarrow M(^{56}\text{Ni}) \sim 0.1 M_{\odot}$
- ☑ ^{56}Ni distribution:
 - region with high $X(^{56}\text{Ni})$ is formed around the jet and a region with unburned ^{16}O is surrounding the region
 - \Rightarrow consistent with optical spectra of some HNe

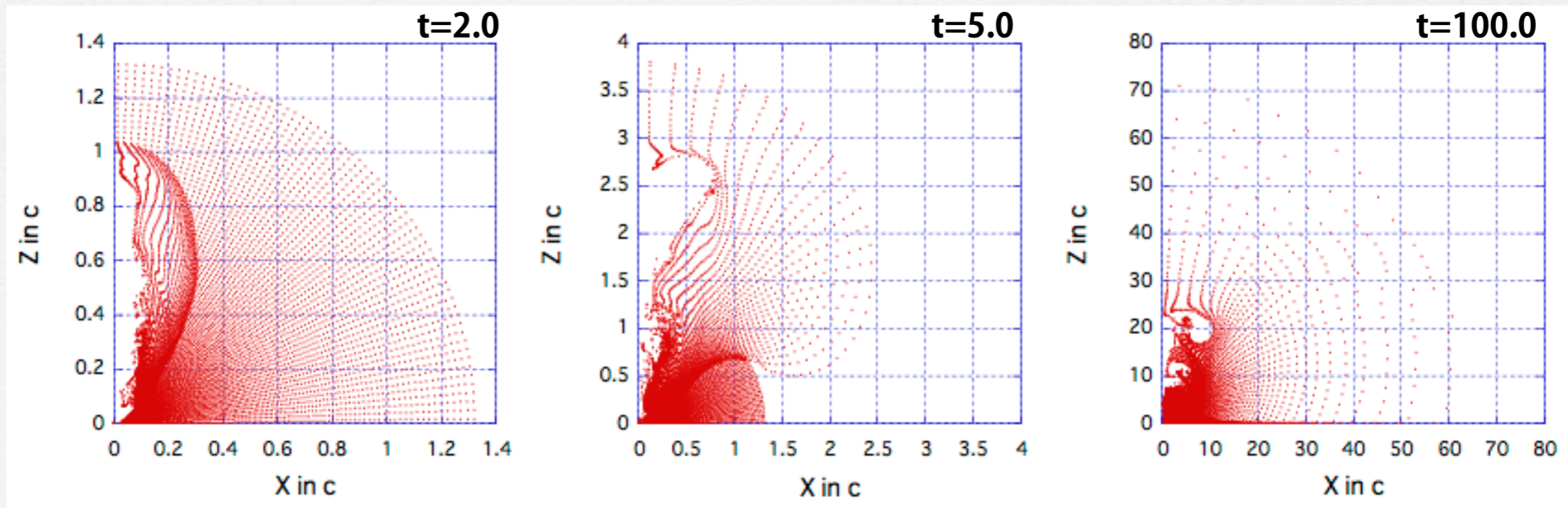


Nagataki+ (2003)



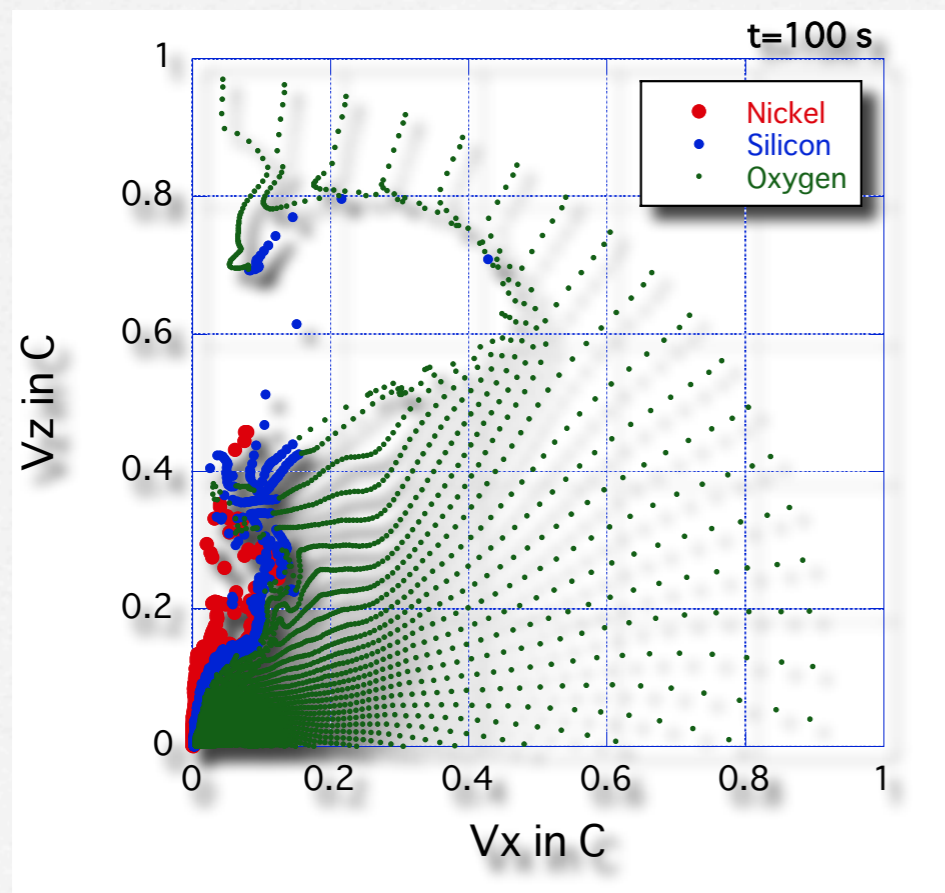
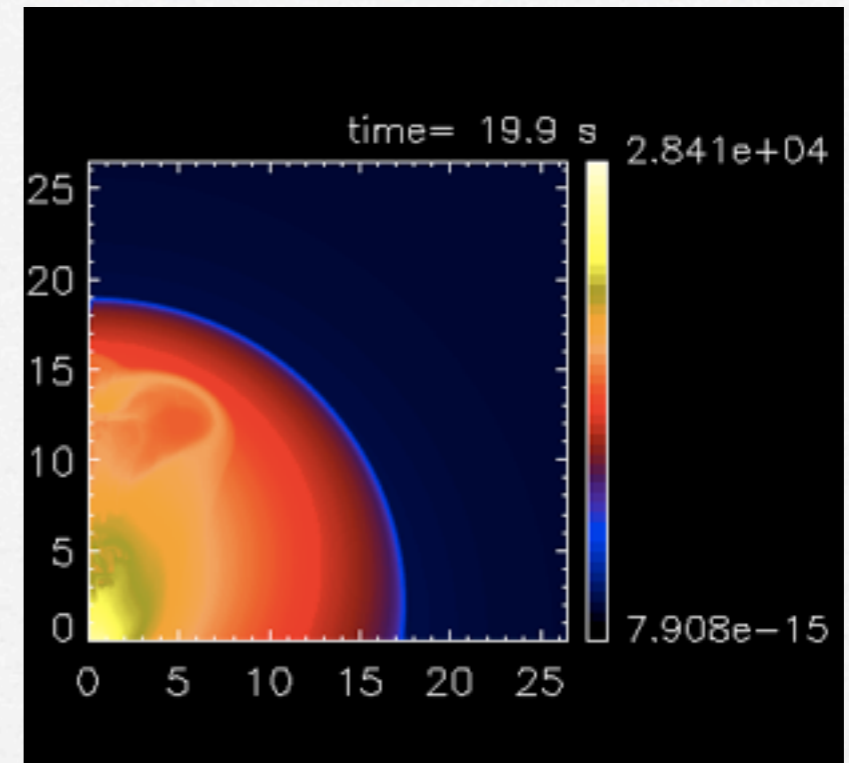
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- ☑ Tracer particle method is employed

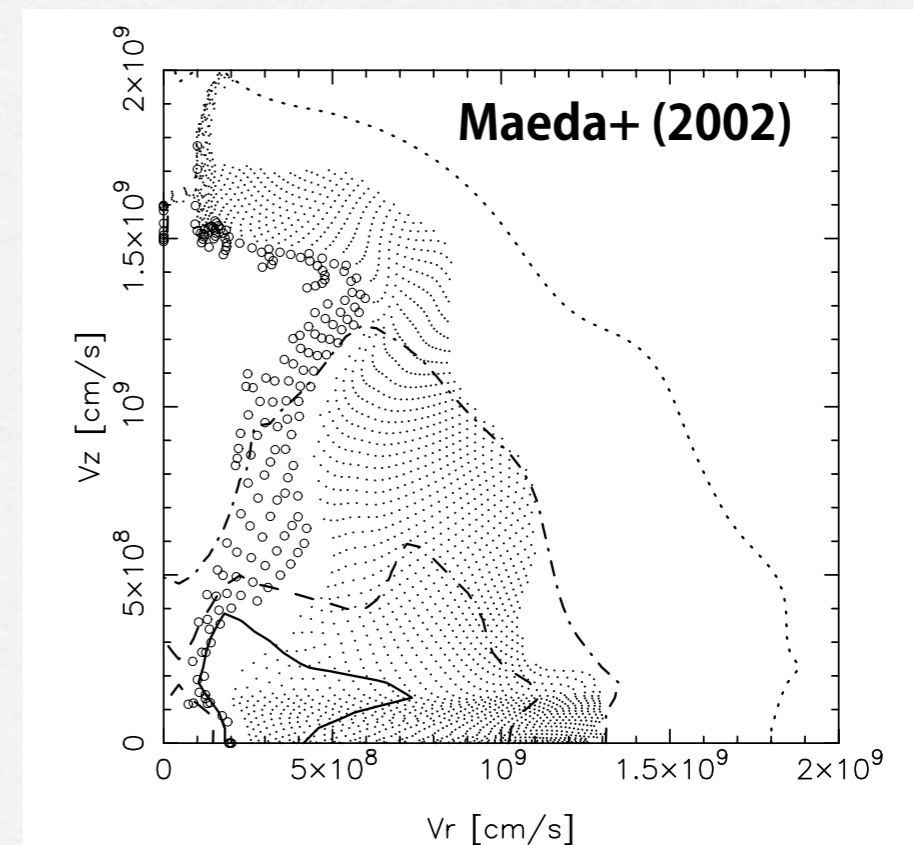


Nucleosynthesis

- ☑ Distributions of elements are similar to earlier works in the context of HNe.
- ☑ Particles that contains ^{56}Ni have velocities $< 0.3c$
- ☑ Ni mass $\sim 0.13 M_{\odot}$, smaller by a factor of 2-3 than observed values

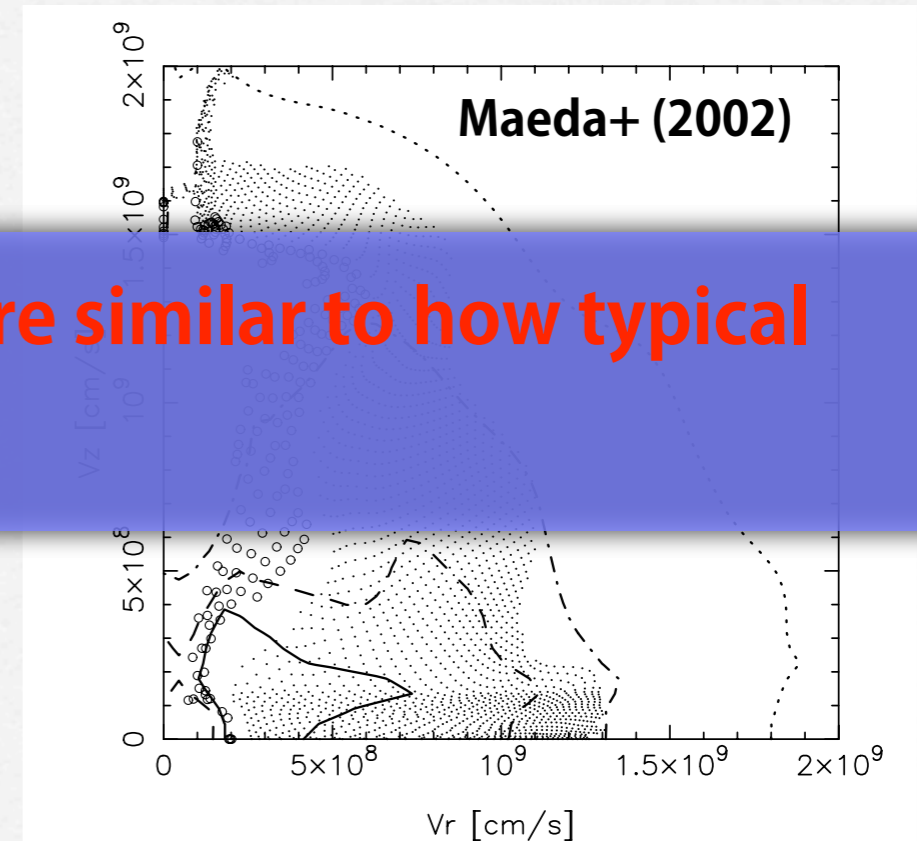
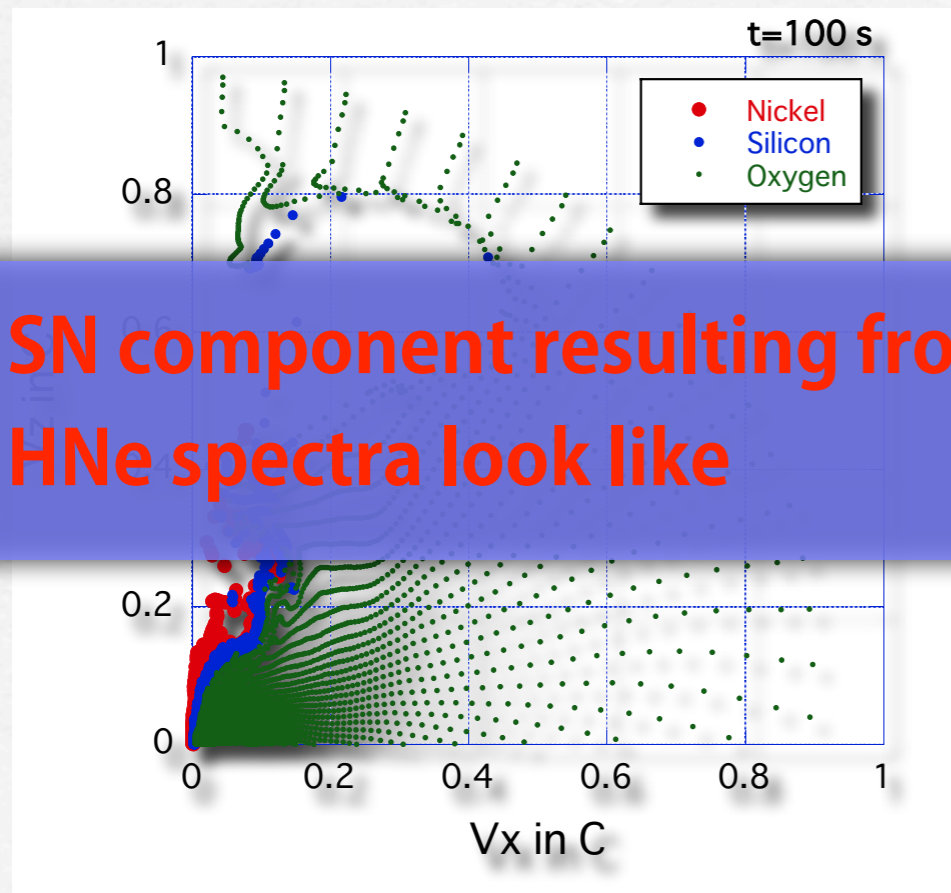
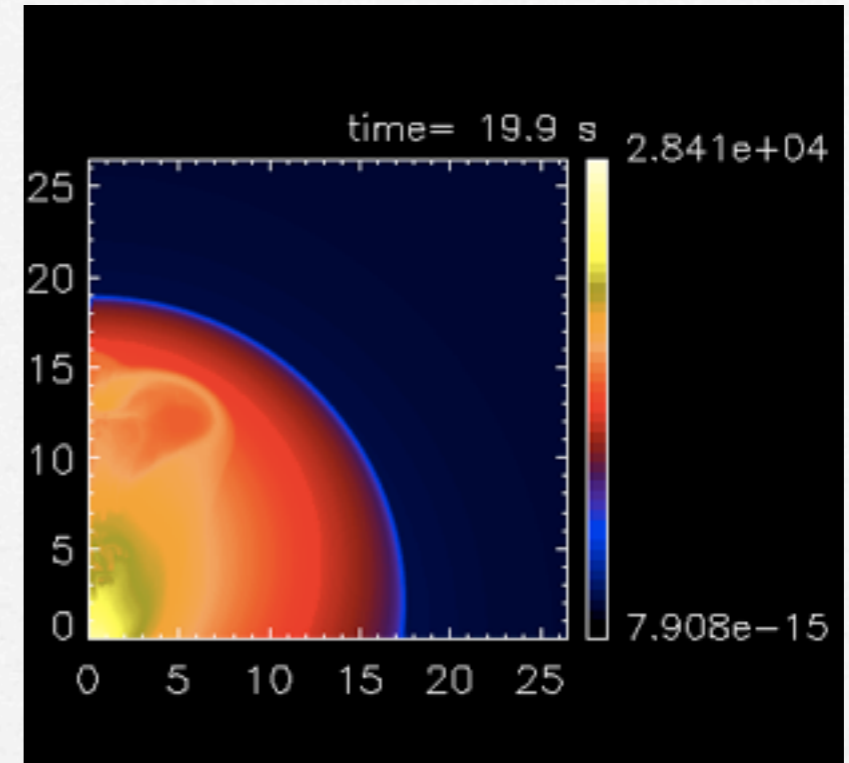


- : $X(^{56}\text{Ni}) > 0.1$
- : $X(^{28}\text{Si}) > 0.1$
- : $X(^{16}\text{O}) > 0.1$



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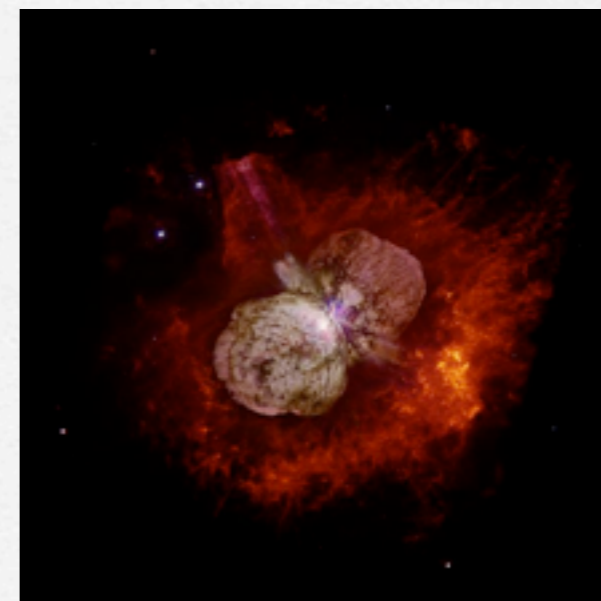


SN component resulting from failed jet are similar to how typical HNe spectra look like

- : $X(^{56}\text{Ni}) > 0.1$
- : $X(^{28}\text{Si}) > 0.1$
- : $X(^{16}\text{O}) > 0.1$

CSM interaction

- ☑ Dense circumstellar medium is expected around the progenitor star.
- ☑ ejecta-CSM interaction efficiently convert the kinetic energy of the ejecta into the internal energy and thus might give rise to bright emission in X-ray and gamma-ray.
- ☑ Some earlier works for the collision of mildly relativistic ejecta with CSM (e.g., Tan +2001).



η Carinae ©NASA

Jet injection

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- ☑ total energy: $E = 5 \times 10^{52} \text{erg}$
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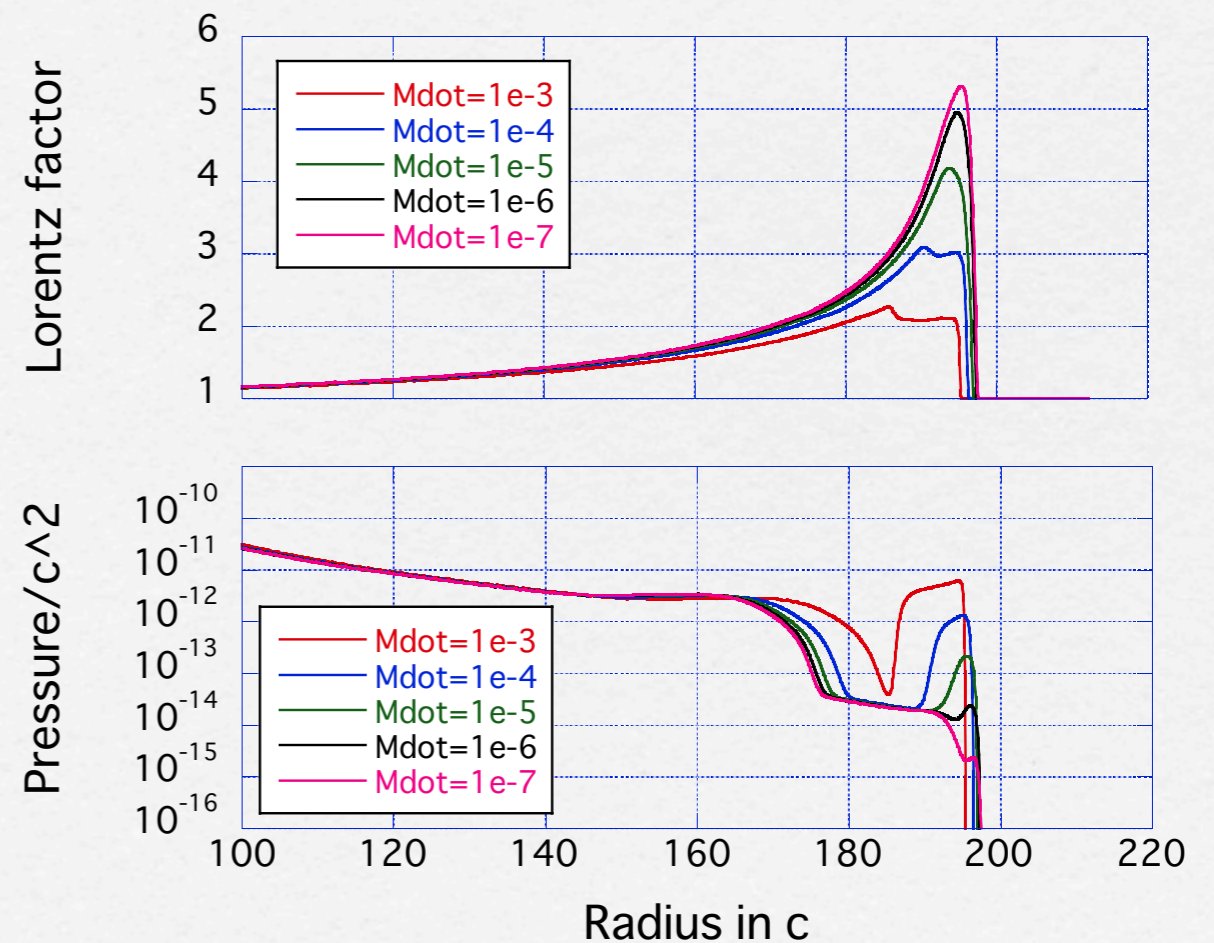
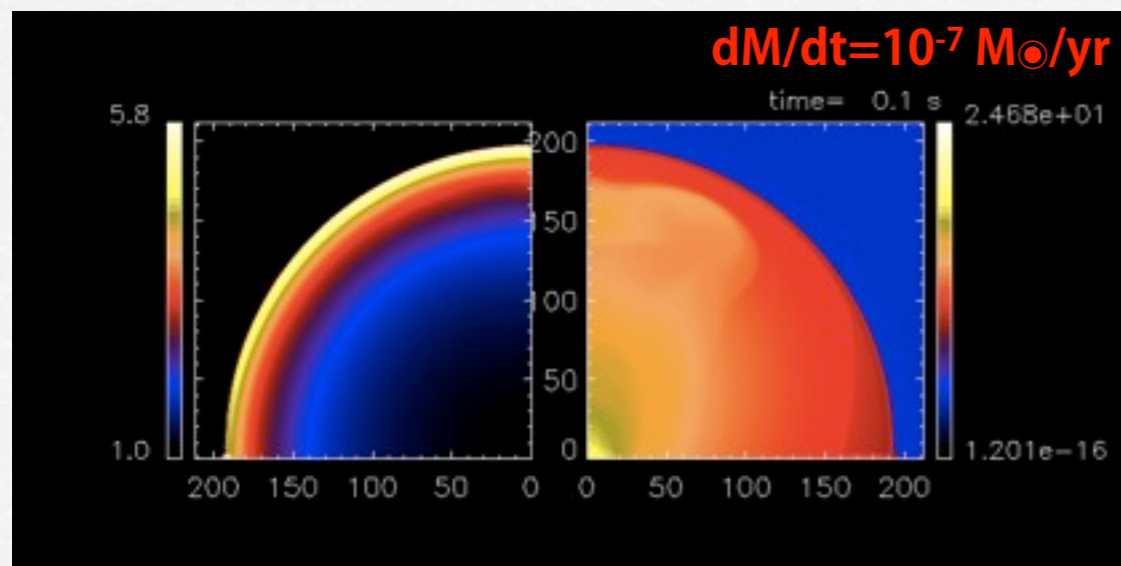
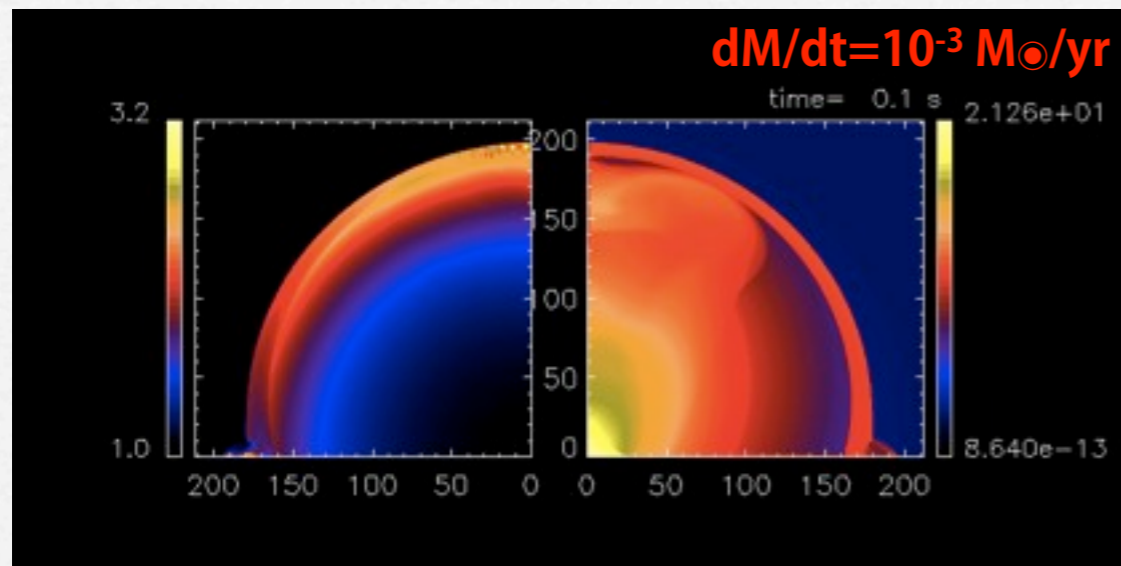
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$$p_0 = (\gamma - 1) \rho_0 \epsilon_0.$$

CSM interaction

- ☑ Models with dense CSM lead to “forward shock - reverse shock” system
- ☑ Models with dilute CSM lead to “forward shock - rarefaction wave” system



CSM interaction

- ☑ The internal energy flux F in the shocked region is of the order of 10^{20} - 10^{21} erg/s/cm² for models with $\dot{M}=10^{-3}, 10^{-4}, 10^{-5} M_{\odot}/\text{yr}$ flux : $F = P/(\gamma - 1) \times \Gamma^2 v_r$
- ☑ assume the internal energy is dominated by photons and some fraction of photons can decouple from the shocked region,

ε : fraction of the energy emitted as photons

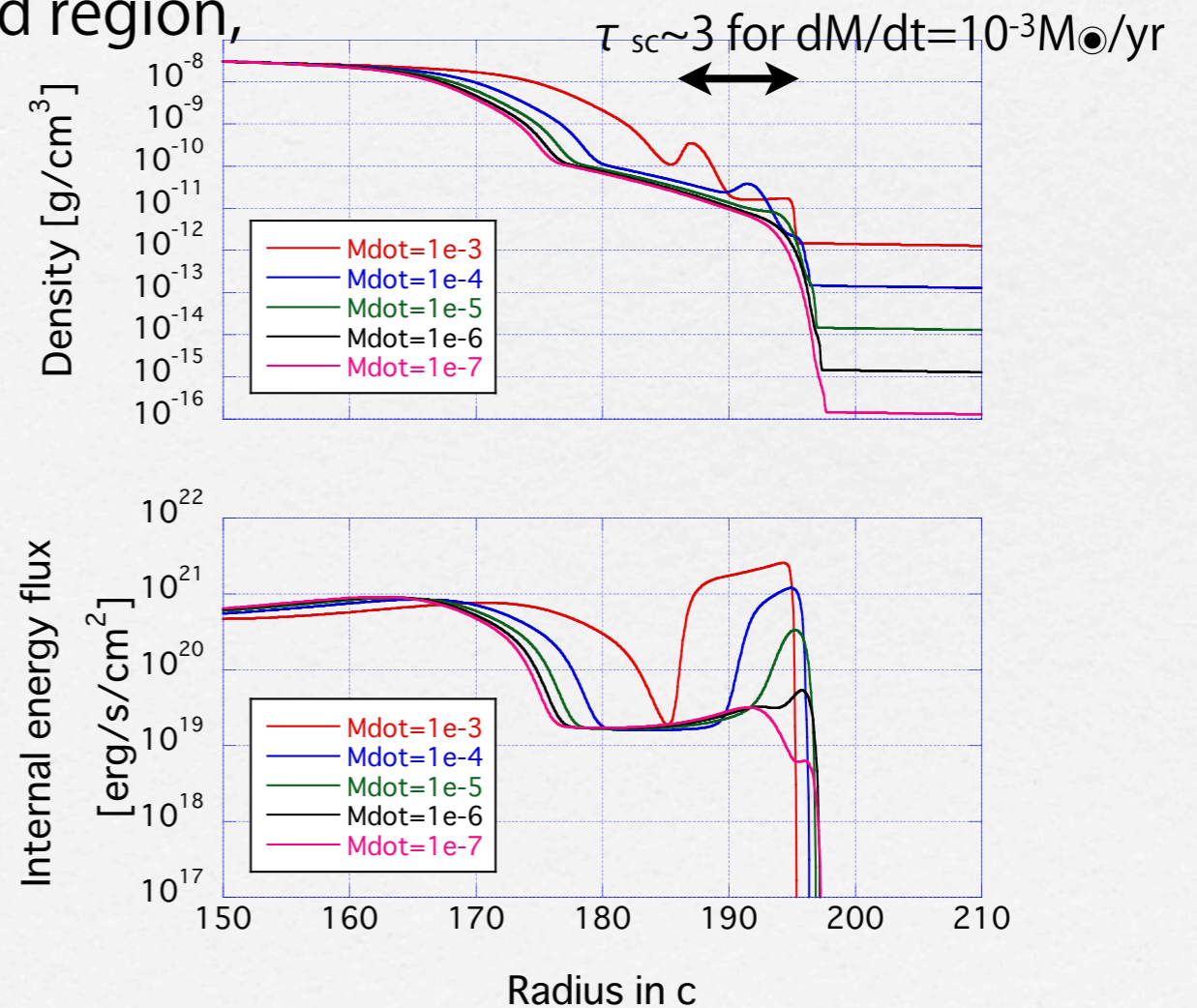
$$L \sim 4 \pi R^2 F \varepsilon$$

$$\sim 4 \times 10^{46} \varepsilon \text{ erg/s}$$

$$\times (R/6 \times 10^{12} \text{cm})^2 (F/10^{20} \text{ erg s}^{-1} \text{cm}^{-2})$$

However, thermal equilibrium between radiation and gas is not achieved!

CSM interaction has a potential to produce emission with $L \sim 10^{46-47}$ erg/s



Summary

- ☑ Failed jet is promising to explain low-luminosity GRBs.
- ☑ Ultra-relativistic jet is failed to be created
 - ➔ kinetic energy of the relativistic ejecta is much smaller than the kinetic energy of the non-relativistic one
- ☑ Explosive nucleosynthesis in the failed jet model
 - ➔ similar result to HNe cases
- ☑ The interaction of the ejecta with dense CSM is investigated
 - ➔ CSM interaction has a possibility in producing highly energetic emission with $L_{\gamma,iso} \sim 10^{46} - 10^{47}$ erg/s

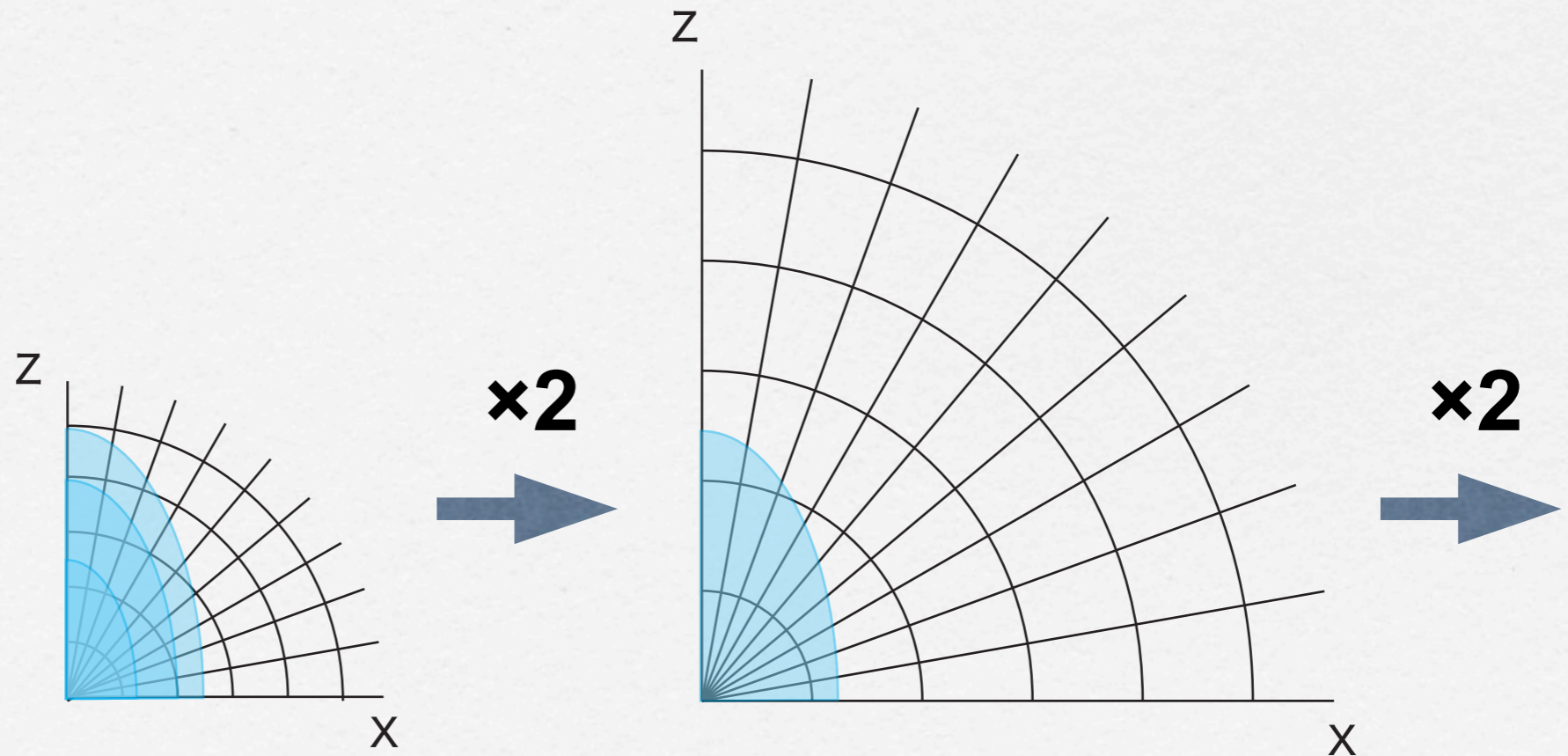
Mapping procedure

☑ dynamical range is huge

➔ jet $\sim 10^{13-14}$ cm \Leftrightarrow Fe core $\sim 10^{8-9}$ cm

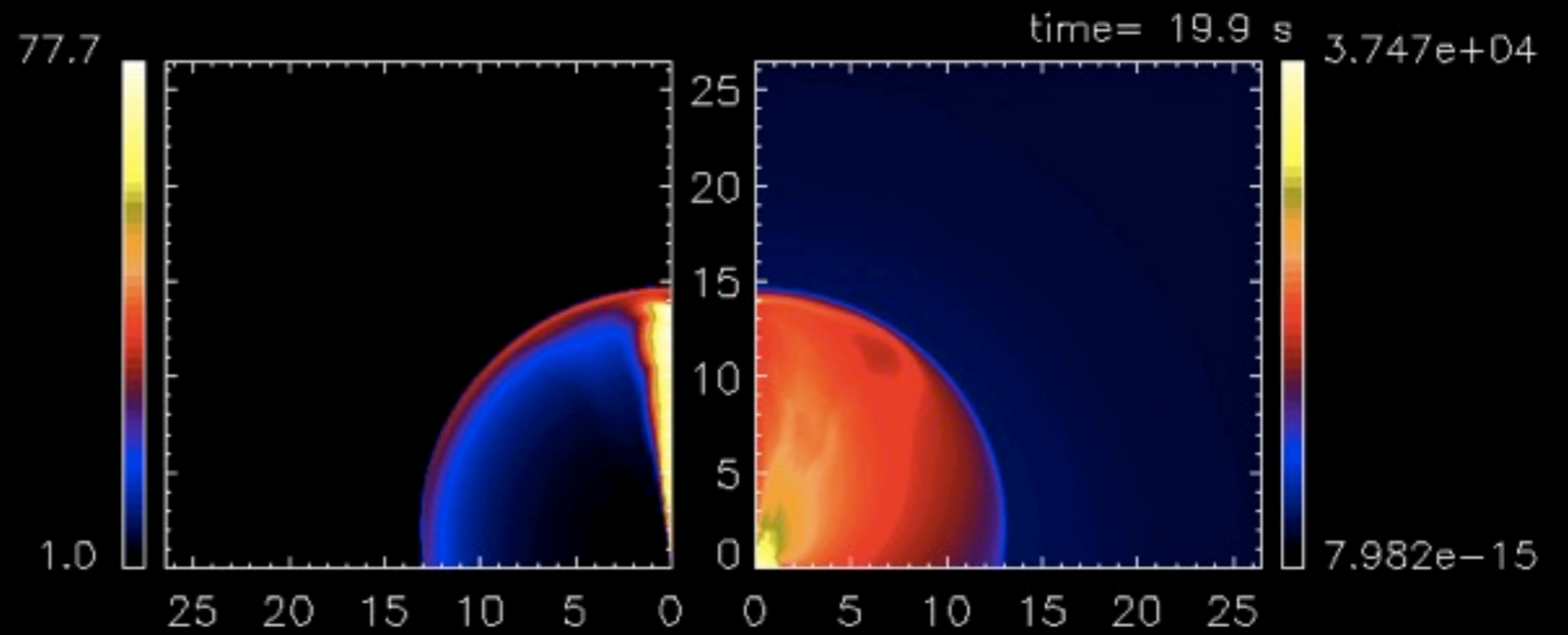
☑ Courant condition limits the time step $\Delta t < c \Delta x$

☑ The numerical domain doubles as the ejecta expand. The resolution is halved.



Results

Ultra-relativistic jet



Mildly relativistic
blast wave

