



First-Order Magnetic Raman Scattering from Magnetic-Field Induced Higgs Mode through Second-Order Magnetic Raman Process

Haruhiko KUROE and Tomoyuki SEKINE

Sophia University

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K. Kusakabe (Sophia Univ.)

Dr. F. Yamada (TITech)

Prof. M. Matsumoto

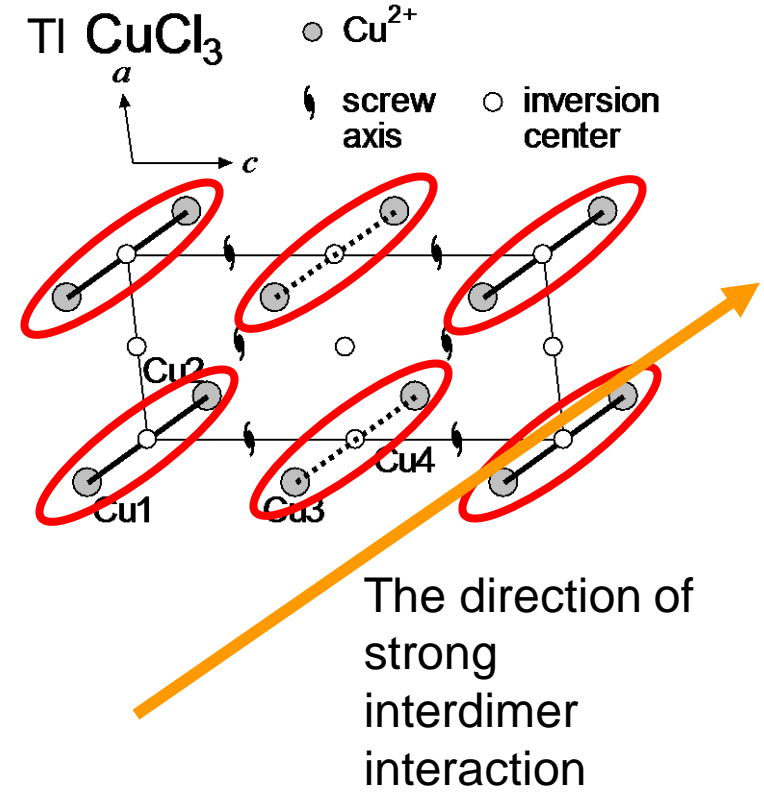
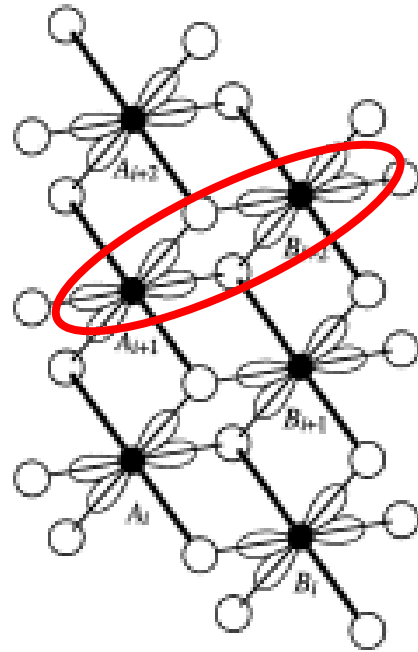
Dr. A. Oosawa (TITech/Sophia)

(Shizuoka Univ.) Prof. H. Tanaka (TITech)

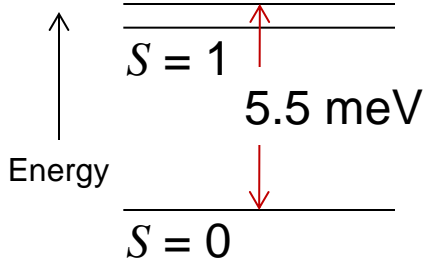
Contents

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2. Inelastic Light Scattering [Raman Scattering, (RS)]
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TiCuCl₃



Spin Dimer

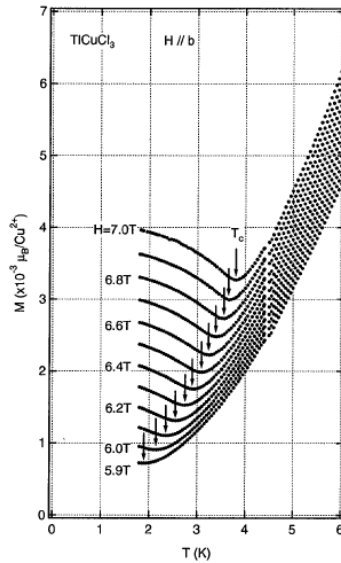


(a) ● Cu²⁺ ○ Cl⁻

[K. Takatsu *et al.*, J. Phys. Soc. Jpn. 66 (1997) 1611.]

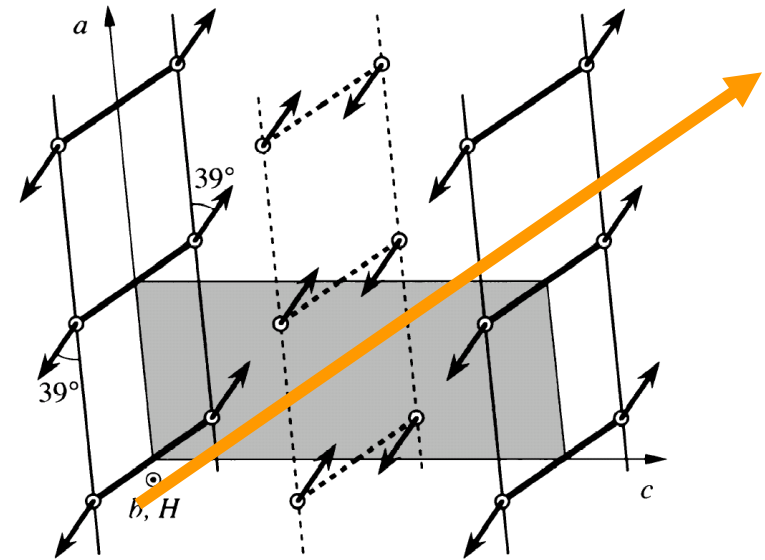
Crystal and magnetic structures in TiCuCl₃

Magnetic-Field Induced Ordered Phase: Bose-Einstein Condensation of Magnons



Magnetic-Field induced
 Néel order

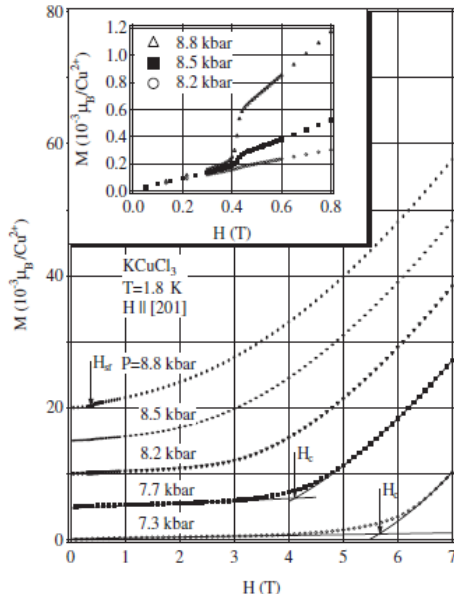
[A. Oosawa *et al.*, JPCM 11 (1999) 265.]



Magnetic structure
 under magnetic field

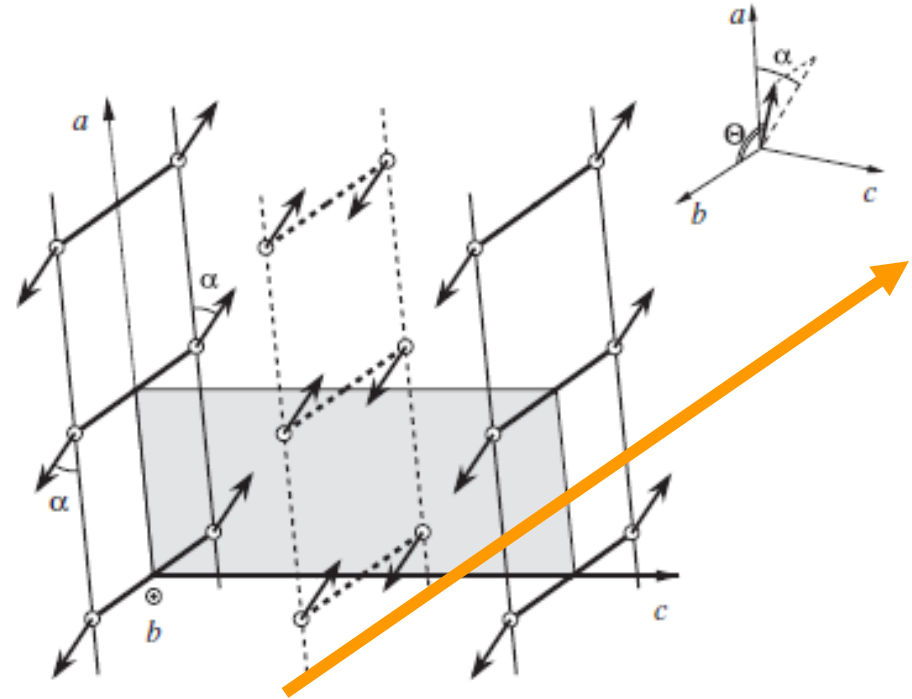
[H. Tanaka *et al.*, JPSJ 70 (2001) 939.]

Pressure Induced Ordered Phase: Pure Higgs Mode



Magnetization

[Goto *et al.*, JPSJ 75 (2006) 064703.]



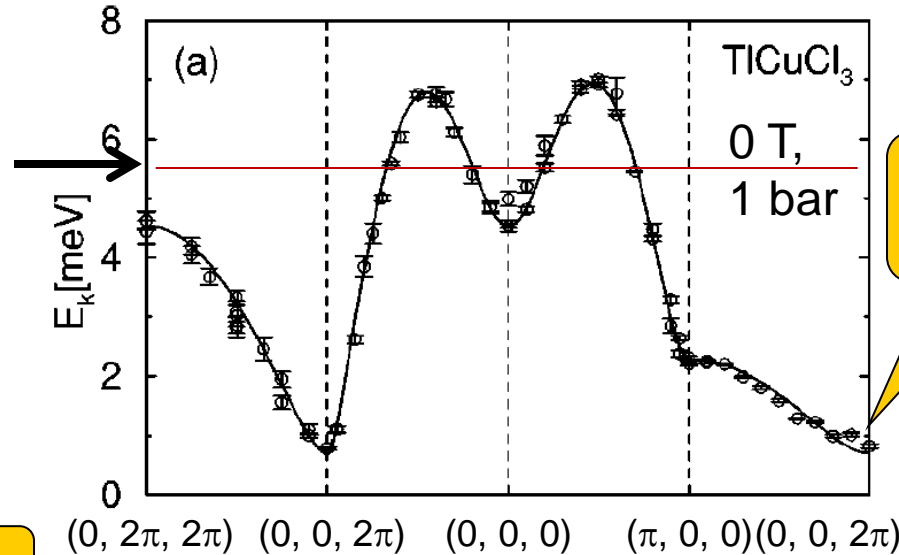
Magnetic structure

[Goto *et al.*, JPSJ 75 (2006) 064703.]

Results under high pressures will be available on poster P12.

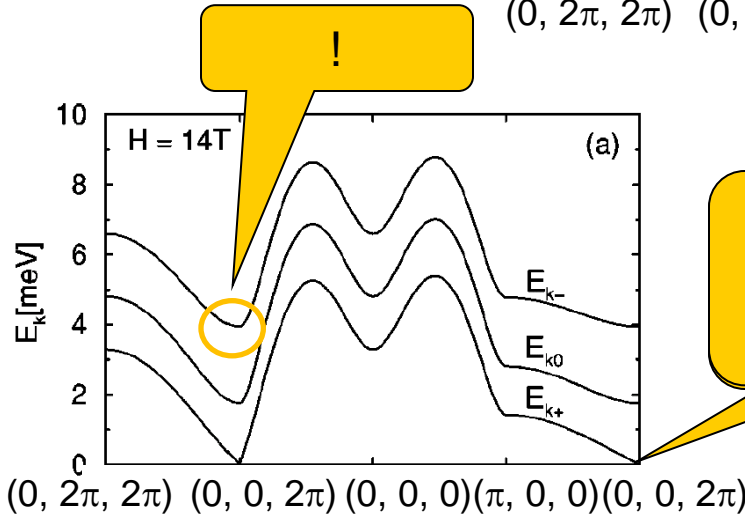
Dispersion Relation: Experiments and Theory

Energy of Spin dimer:
 5.5 meV

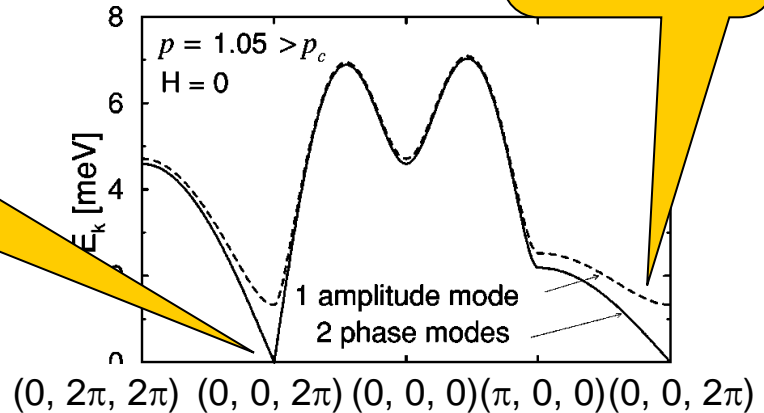


Spin Gap
 (massive)

Higgs
 Mode
 (massive)



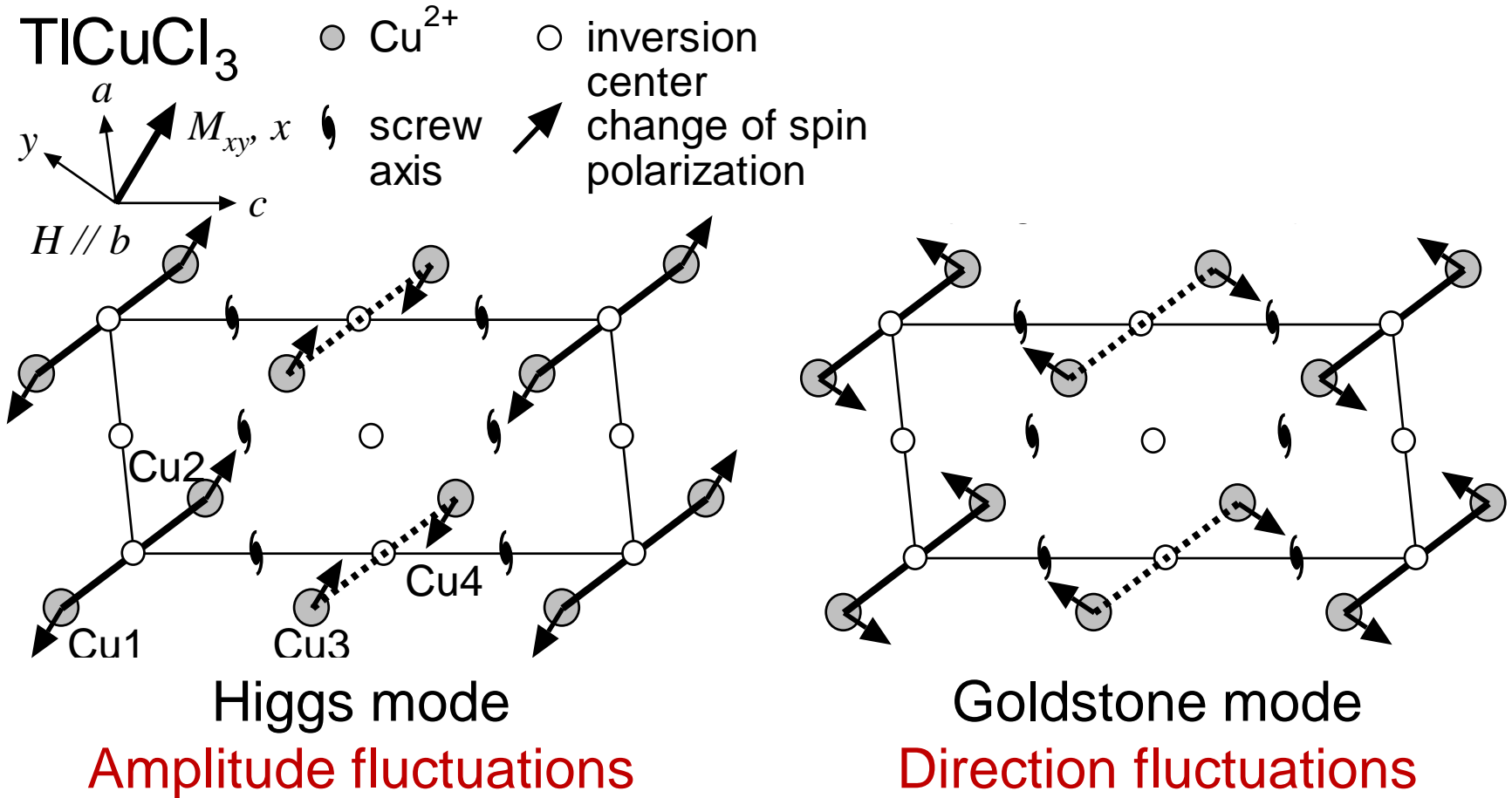
Goldstone
 Mode
 (massless)



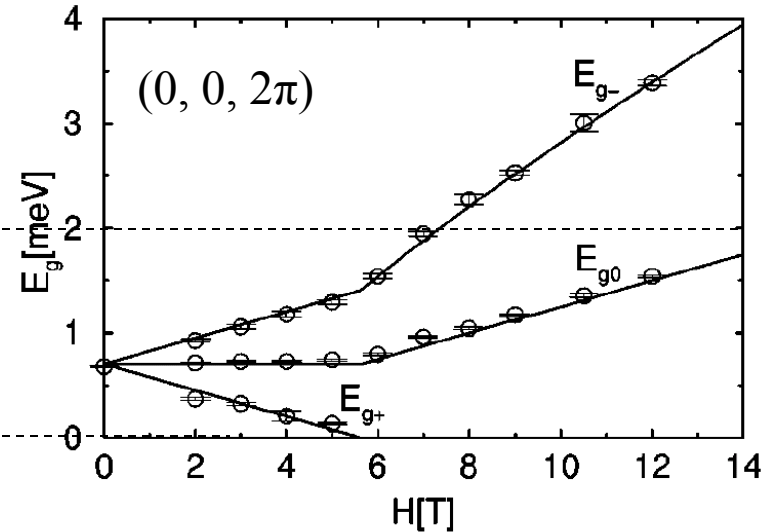
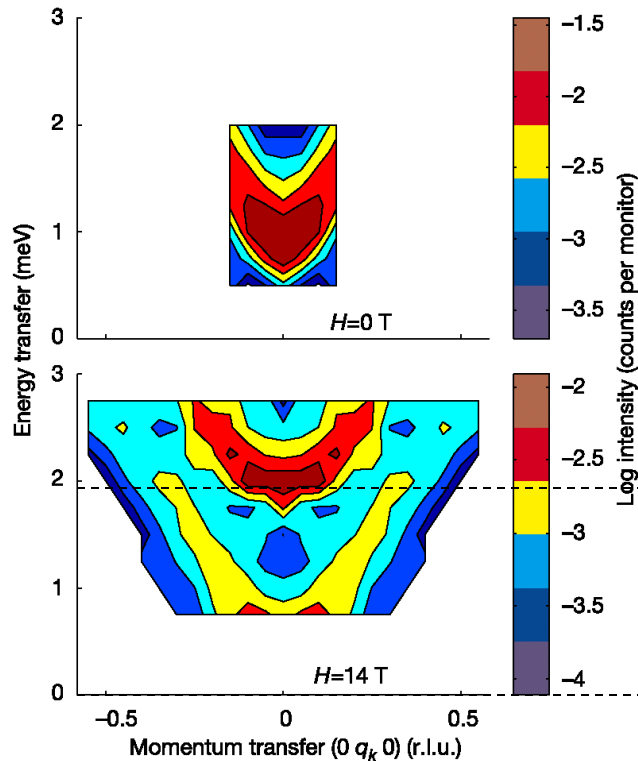
[Experiments: N. Cavadini et al., Phys. Rev. B 63 (2004) 172414.]

[Calculation: M. Matsumoto *et al.*, PRB 69 (2004) 054423.]

Fluctuation of Magnetic Moments



Magnon Excitations under Magnetic Field



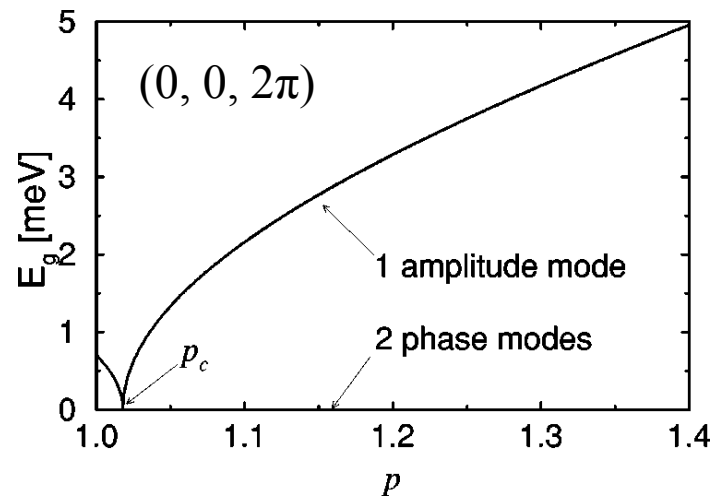
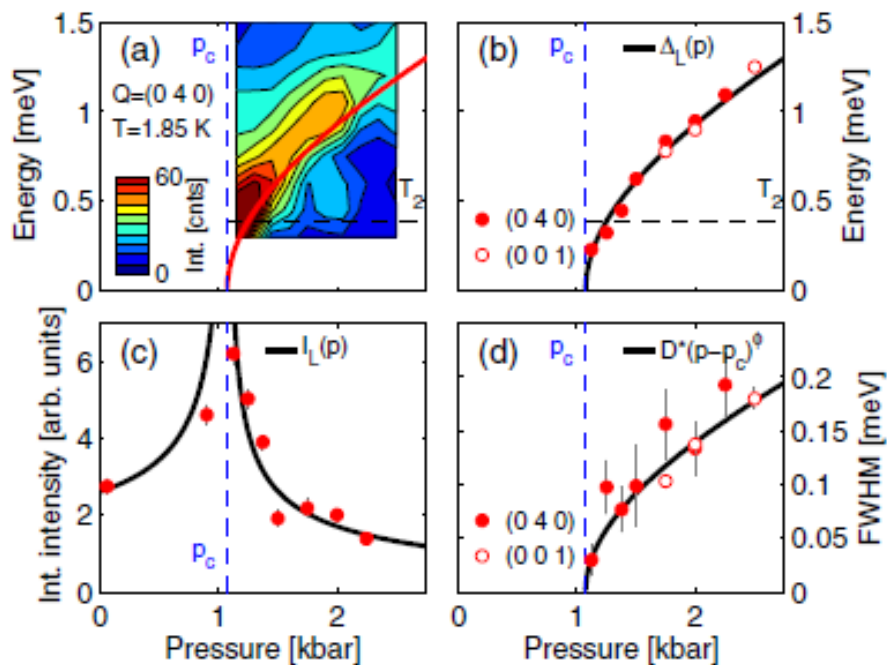
Inelastic neutron
 scattering in TiCuCl_3

[Ch. Rüegg *et al.*, *Nature* **423** (2003) 62.]

Calculation using
 bond-operator theory

[M. Matsumoto *et al.*, *PRB* **69** (2004) 054423.]

Magnon Excitations under High Pressure




Calculation using
 bond-operator theory

[M. Matsumoto *et al.*, PRB 69 (2004) 054423.]

Inelastic neutron
 scattering in TiCuCl_3
 [Ch. Rüegg *et al.*, PRL 100 (2008)
 205701.]

Results under high pressures will be available on poster P12.

Latest Topic: Finite-Temperature Effects



ARTICLES

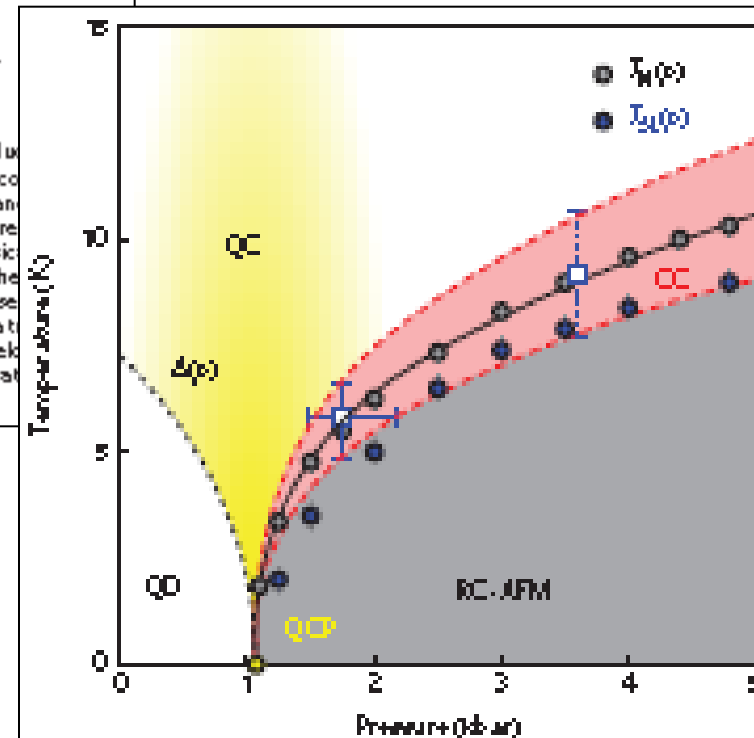
PUBLISHED ONLINE 6 APRIL 2014 | DOI: 10.1038/NPHYS2902

Quantum and classical criticality in a dimerized quantum antiferromagnet

P. Merchant¹, B. Normand², K. W. Krämer², M. Boehm⁴, D. F. McMorrow¹ and Ch. Rüegg^{1,5,6*}

A quantum critical point (QCP) is a singularity in the phase diagram arising because of quantum mechanical fluctuations. The exotic properties of some of the most enigmatic physical systems, including unconventional metals and superconductors, have been related to the importance of critical quantum fluctuations near such a point. However, direct and continuous control of these fluctuations has been difficult to realize. Here we achieve this control in a high-pressure, high-resolution neutron scattering experiment on the dimer material TiCuCl₂. By measuring the magnetic excitation spectrum across the entire quantum critical phase we illustrate the similarities between quantum and thermal melting of magnetic order. We prove the critical nature of the unconventional longitudinal (Higgs) mode of the ordered phase by damping it thermally. We demonstrate the development of two types of criticality, quantum and classical, and use their static and dynamic scaling properties to conclude that quantum and thermal fluctuations can behave largely independently near a QCP.

Results under high pressures will be available on poster P12.



Merchant *et al.*, Nature Physics
 10 (2014) 373–379.

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Raman Scattering (RS):

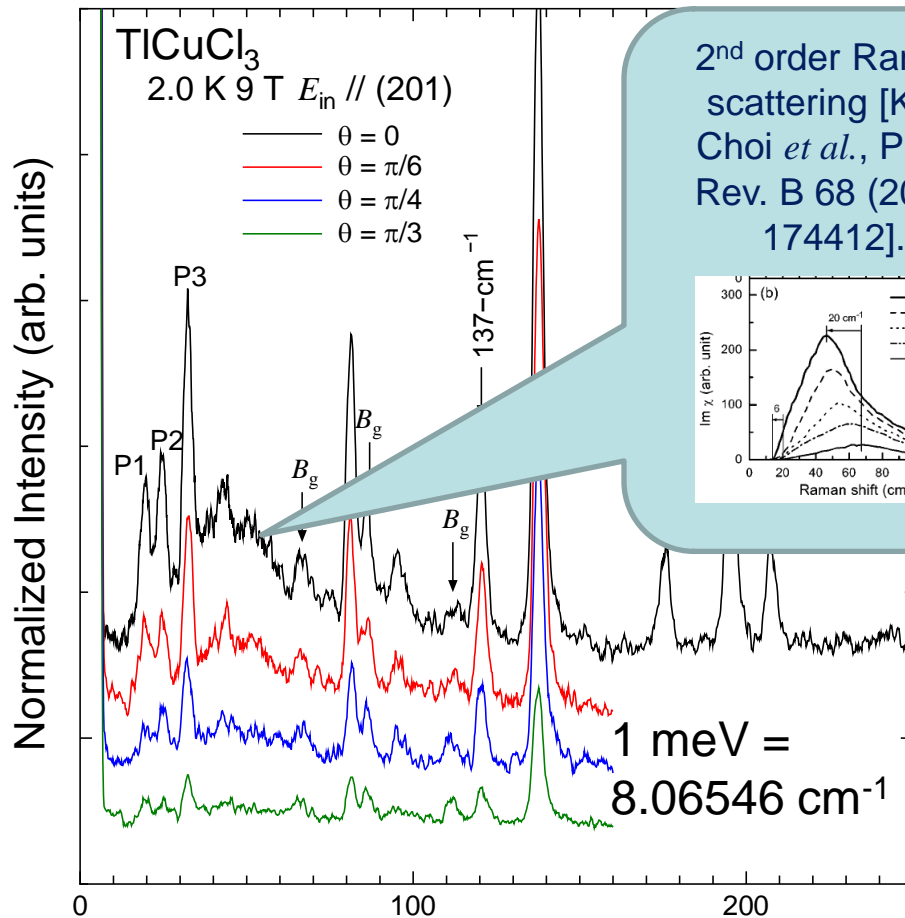
- Inelastic light scattering;
- Detection of phonon modes at the chemical Γ point;
- High resolution;
- Symmetry sensitive;
- Small amount of sample;
- Multi-extreme condition; ... and
- **Detection of the Higgs mode
at the magnetic Γ Point !**



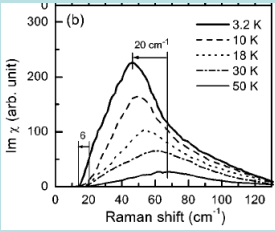
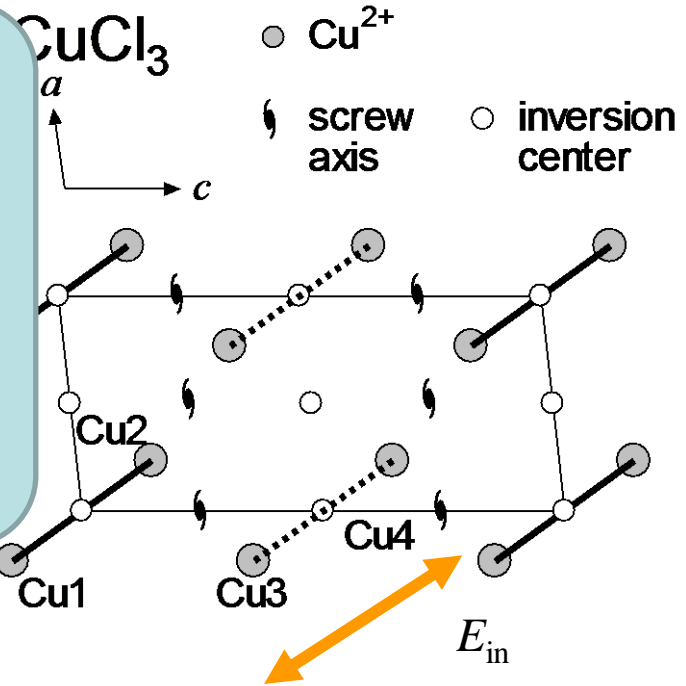
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Polarization Characteristics



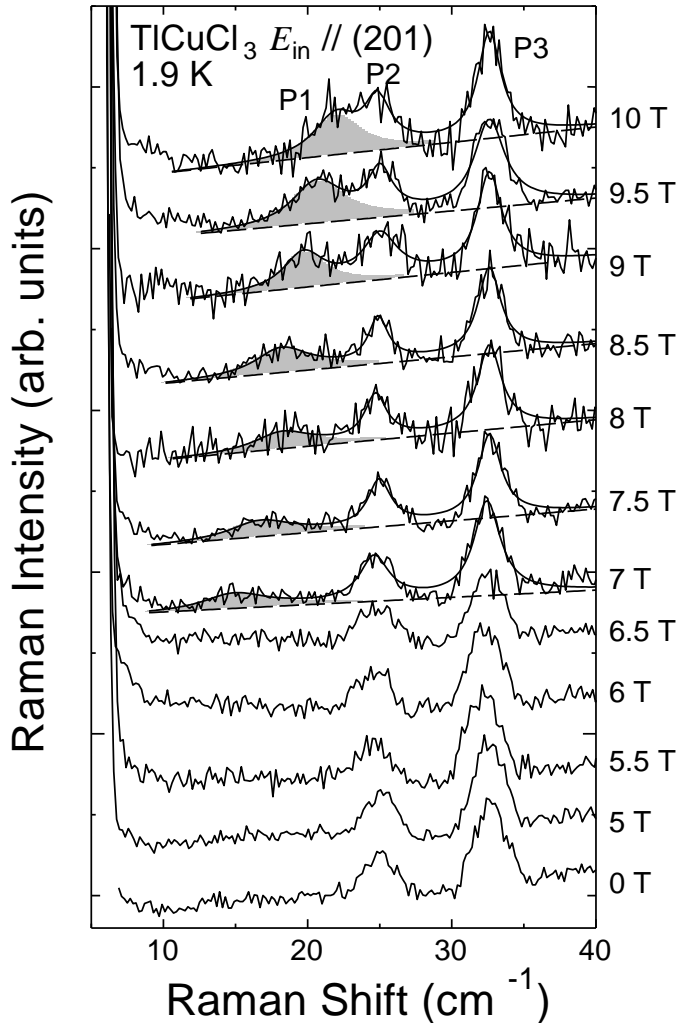
2nd order Raman scattering [K.-Y Choi *et al.*, Phys. Rev. B 68 (2003) 174412].

P1 mode was strongly observed for the incident light is polarized along the direction of strong interdimer interaction

Polarized Raman spectra.
 P1 mode has the A_g symmetry.

Result in TlCuCl_3 under Magnetic Field



P1 peak is due to the Higgs mode.

Fitting function

$$I = \sum_{i=1-3} \frac{k_i^2 \omega_i \Gamma_i}{(\omega^2 - \omega_i^2)^2 + (\omega \Gamma_i)^2} + (\text{background})$$

$$(\text{background}) = a\omega + b$$

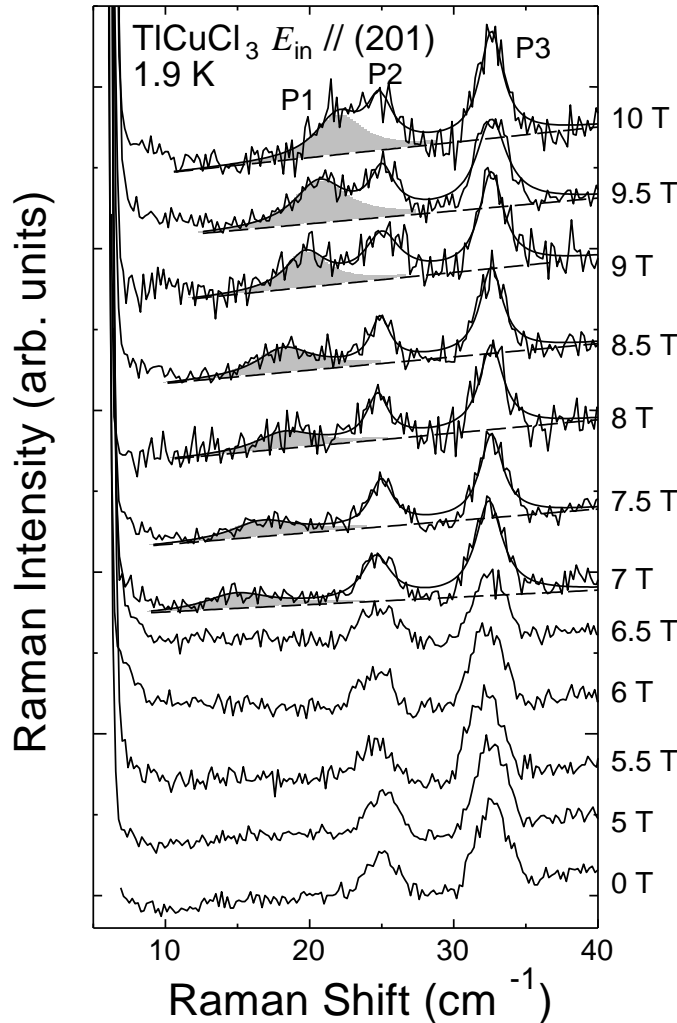
$\hbar\omega_i$ Excitation energy of P_i ($i = 1-3$)

Γ_i Halfwidth ($1/2\Gamma_i$ is lifetime)

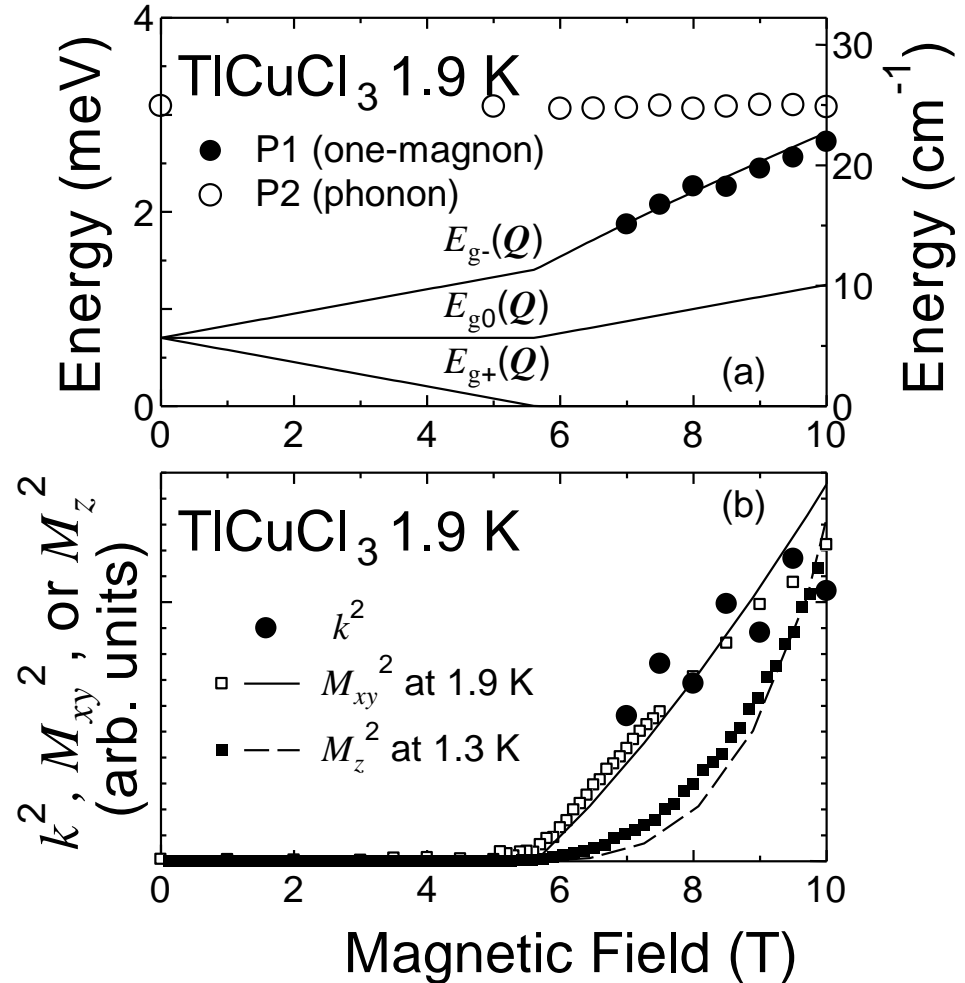
k_i Coupling coefficient

$$1 \text{ meV} = 8.06546 \text{ cm}^{-1}$$

Result in TICuCl_3 under Magnetic Field



P1 peak is due to the Higgs mode.



Magnetic field dependences of P1 energy (upper panel) and integrated intensity (lower panel).

Summary of Experimental Results:

- ❑ We observe strong magnetic RS when the incident light is polarized along the direction of strong interdimer interaction;
- ❑ 1st Order magnetic RS never appears below H_c or below p_c ;
- ❑ Raman intensity is proportional to M_{xy}^2 ;
- ❑ Energy of the P1 peak is well described by the energy of the Higgs mode;
- ❑ Halfwidth of the P1 peak under high pressures is proportional to the P1-peak energy.

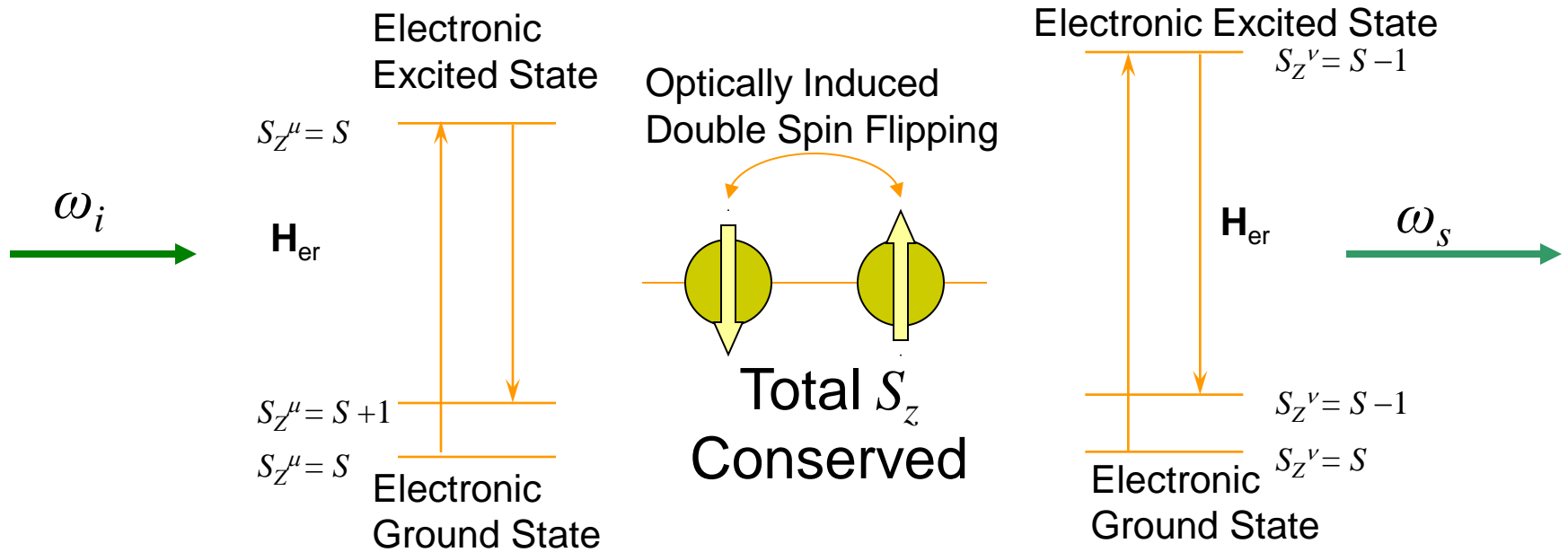
We should understand these facts theoretically to clarify the fact that

Magnetic RS detects the Higgs mode.

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Second-order magnetic RS: Optically Induced Spin Exchange



P. A. Fleury and R. Loudon, Phys. Rev. 166 (1968) 514.

Effective Raman operator
$$R = \sum_{i,j} F_{i,j} (\hat{E}_{in} \cdot \hat{r}_{i,j}) (\hat{E}_{sc} \cdot \hat{r}_{i,j}) \vec{S}_i \cdot \vec{S}_j$$

\vec{S}_i $S = 1/2$ Spin at site i

$\hat{r}_{i,j}$ Unit vector connecting sites i, j

$\hat{E}_{in(sc)}$ Polarization of incident (scattered) light

$F_{i,j}$ Amplitude factor

Summary of Experimental Results:

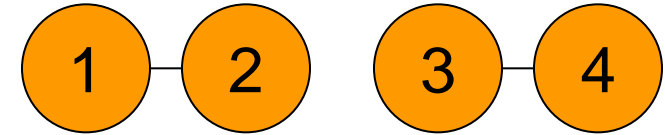
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- Raman intensity is proportional to M_{xy}^2 ;
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- Halfwidth of the P1 peak under high pressures is proportional to the P1-peak energy.

We should understand these facts theoretically to clarify the fact that

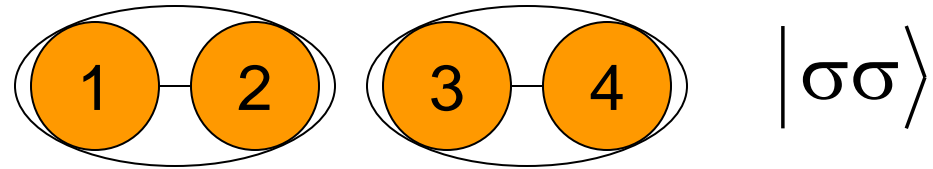
Magnetic RS detects the Higgs mode.

The Toy

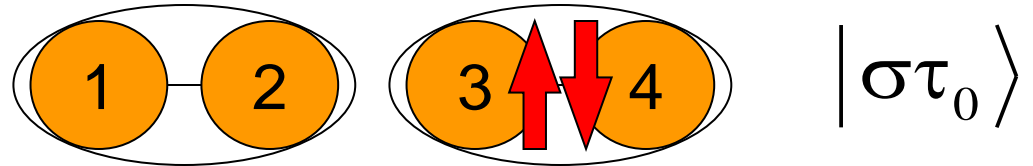
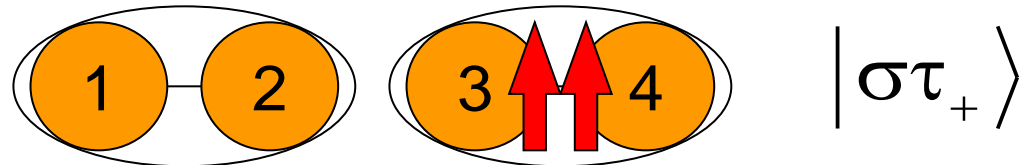
Two $S = \frac{1}{2}$ Spin dimers with
 degrees of freedom (DoF) $2^4 = 16$



Singlet state (DoF 1)

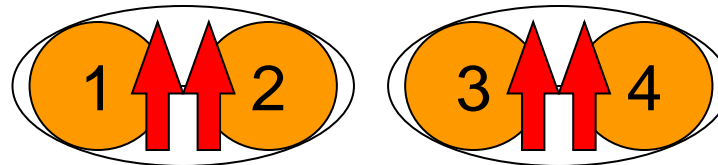


One magnon state
 (DoF 6)

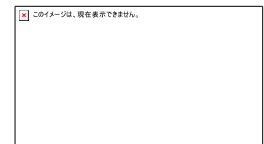


...

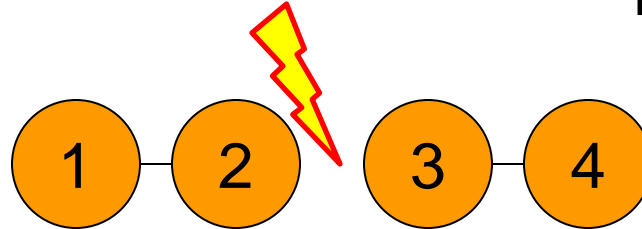
Two magnon state
 (DoF 9)



...



Operate Effective Raman Operator



$$\begin{aligned}
 \tilde{R}|\sigma\sigma\rangle &= \vec{S}_2 \cdot \vec{S}_3 |\sigma\sigma\rangle \\
 &= \left\{ \frac{S_2^+ S_3^- + S_2^- S_3^+}{2} + S_2^z S_3^z \right\} \left\{ \frac{|\uparrow\downarrow\uparrow\downarrow\rangle - |\downarrow\uparrow\uparrow\downarrow\rangle - |\uparrow\downarrow\downarrow\uparrow\rangle + |\downarrow\uparrow\downarrow\uparrow\rangle}{2} \right\} \\
 &= \left\{ \frac{|\uparrow\uparrow\downarrow\downarrow\rangle + |\downarrow\downarrow\uparrow\uparrow\rangle}{4} \right\} + \frac{1}{4} \left\{ \frac{-|\uparrow\downarrow\uparrow\downarrow\rangle - |\downarrow\uparrow\uparrow\downarrow\rangle - |\uparrow\downarrow\downarrow\uparrow\rangle - |\downarrow\uparrow\downarrow\uparrow\rangle}{2} \right\} \\
 &= \frac{1}{4} (|\tau_+ \tau_- \rangle + |\tau_- \tau_+ \rangle - |\tau_0 \tau_0 \rangle)
 \end{aligned}$$

Excitation between singlet state to two magnon state;

Conservation of angular momentum

$$\begin{aligned}
 \tilde{R}|\sigma\tau_+\rangle &= \vec{S}_2 \cdot \vec{S}_3 |\sigma\tau_+\rangle \\
 &= \left\{ \frac{S_2^+ S_3^- + S_2^- S_3^+}{2} + S_2^z S_3^z \right\} \left\{ \frac{|\uparrow\downarrow\uparrow\uparrow\rangle - |\downarrow\uparrow\uparrow\uparrow\rangle}{\sqrt{2}} \right\} \\
 &= \frac{S_2^+ S_3^- + S_2^- S_3^+}{2} \left\{ \frac{|\uparrow\downarrow\uparrow\uparrow\rangle - |\downarrow\uparrow\uparrow\uparrow\rangle}{\sqrt{2}} \right\} + S_2^z S_3^z \left\{ \frac{|\uparrow\downarrow\uparrow\uparrow\rangle - |\downarrow\uparrow\uparrow\uparrow\rangle}{\sqrt{2}} \right\} \\
 &= \frac{|\uparrow\uparrow\downarrow\uparrow\rangle}{2\sqrt{2}} + \frac{1}{4} \left\{ \frac{-|\uparrow\downarrow\uparrow\uparrow\rangle - |\downarrow\uparrow\uparrow\uparrow\rangle}{\sqrt{2}} \right\} \\
 &= \frac{1}{4} \frac{|\uparrow\uparrow\downarrow\uparrow\rangle - |\uparrow\uparrow\uparrow\downarrow\rangle}{\sqrt{2}} + \frac{1}{4} \frac{|\uparrow\uparrow\downarrow\uparrow\rangle + |\uparrow\uparrow\uparrow\downarrow\rangle}{\sqrt{2}} - \frac{1}{4} \frac{|\uparrow\downarrow\uparrow\uparrow\rangle + |\downarrow\uparrow\uparrow\uparrow\rangle}{\sqrt{2}} \\
 &= \frac{1}{4} |\tau_+\sigma\rangle + \frac{1}{4} |\tau_+\tau_0\rangle - \frac{1}{4} |\tau_0\tau_+\rangle
 \end{aligned}$$

Excitation between one magnon state to two magnon state;

Conservation of angular momentum

Summary of Experimental Results:

- ☑ We observe strong magnetic RS when the incident light is polarized along the direction of strong interdimer interaction;
- ☑ 1st order magnetic RS never appears below H_c or below p_c ;
- ☐ Raman intensity is proportional to M_{xy}^2 ;
- ☐ Energy of the P1 peak is the same as that of the Higgs mode;
- ☐ Halfwidth of the P1 peak under high pressures is proportional to the P1-peak energy.

We should understand these facts theoretically to clarify the fact that

Magnetic RS detects the Higgs mode.

Singlet-triplet mixing under magnetic field

M. Matsumoto *et al.*, PRB 69 (2004) 054423.

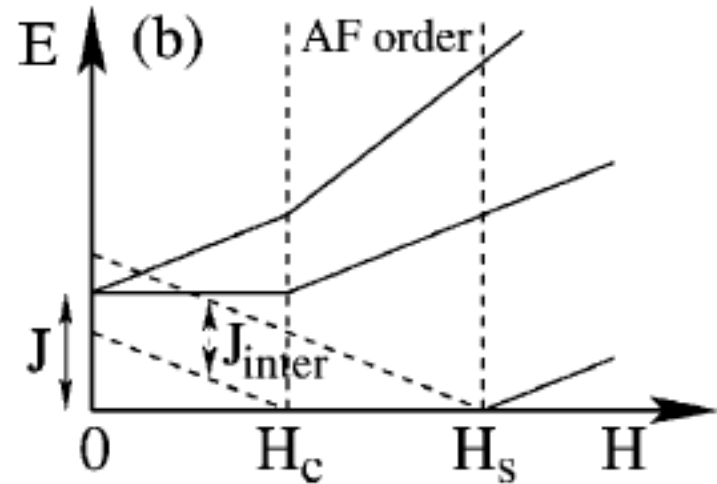
In ordered phase ($H_c < H < H_s$)

$$a_i = us_i + v(fe^{i\mathbf{Q}\cdot\mathbf{r}_i}t_{i+} + ge^{i\mathbf{Q}\cdot\mathbf{r}_i}t_{i-}),$$

$$b_{i+} = u(ft_{i+} + gt_{i-}) - ve^{i\mathbf{Q}\cdot\mathbf{r}_i}s_i,$$

$$b_{i0} = t_{i0},$$

$$b_{i-} = ft_{i-} - gt_{i+},$$



Magnetic RS detects
 singlet-triplet mixing

Writing effective Raman operator using s_i and $t_{i\alpha}$



Intradimer part

$$R_{\text{intra}} = F_{\text{intra}} (\hat{E}_{\text{in}} \cdot \hat{d}) (\hat{E}_{\text{sc}} \cdot \hat{d})$$

$$\times \sum_i \left(-\frac{3}{4} s_i^\dagger s_i + \sum_{\alpha=0,\pm} \frac{1}{4} t_{i\alpha}^\dagger t_{i\alpha} \right)$$

Interdimer part

$$R_{\text{inter}} = F_{\text{inter}} (\hat{E}_{\text{in}} \cdot \hat{R}_{ij}) (\hat{E}_{\text{sc}} \cdot \hat{R}_{ij})$$

$$\times \sum_{ij} \left\{ [t_{i\alpha}^\dagger t_{j\alpha} s_j^\dagger s_i + t_{i\alpha}^\dagger t_{j\bar{\alpha}}^\dagger s_i s_j + \text{H.c.}] + [t_{i0}^\dagger t_{j0} (t_{i+}^\dagger t_{j+} + t_{i-}^\dagger t_{j-}) + \text{H.c.}] \right.$$

$$\left. - [t_{i0}^\dagger t_{j0} (t_{i+}^\dagger t_{j-}^\dagger + t_{i-}^\dagger t_{j+}^\dagger) + \text{H.c.}] + (t_{i+}^\dagger t_{i+} - t_{i-}^\dagger t_{i-}) (t_{j+}^\dagger t_{j+} - t_{j-}^\dagger t_{j-}) \right\}$$

Writing the singlet-triplet mixing in the k space

$$s_k, t_{k+}, t_{k0}, t_{k-}$$

$$a_k, b_{k+}, b_{k0}, b_{k-}$$

$$a_k = us_k + vft_{k+Q+} + vgt_{k+Q-}$$

$$b_{k+} = -vs_{k+Q} + uft_{k+} + ugt_{k-}$$

$$b_{k-} = ft_{k-} - gt_{k+}$$

$$b_{k0} = t_{k0}$$

Matsumoto *et al.*,
 PRL 89, 077203 (2002),
 PRB 69, 054423 (2004).

The magnetic Γ point

Writing effective Raman operator with the basis of b_{k0} , $b_{k\pm}$:

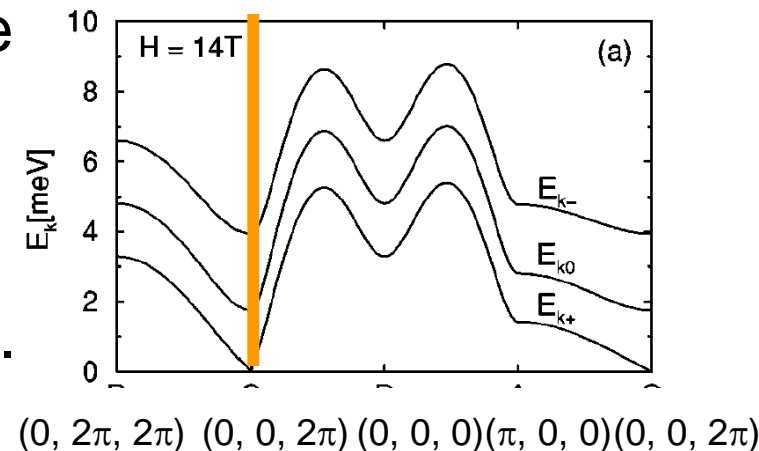
$$\begin{aligned}
 R_{\text{intra}} &= F_{\text{intra}} (\hat{E}_{\text{in}} \cdot \hat{d}) (\hat{E}_{\text{sc}} \cdot \hat{d}) \sum_k \left(-\frac{3}{4} s_k^\dagger s_k + \sum_{\alpha=0,\pm} \frac{1}{4} t_{k\alpha}^\dagger t_{k\alpha} \right) \\
 &= F_{\text{intra}} (\hat{E}_{\text{in}} \cdot \hat{d}) (\hat{E}_{\text{sc}} \cdot \hat{d}) \left[\left(\frac{1}{4} - u^2 \right) \bar{a}^2 + \underbrace{uv\bar{a}} (b_{Q+}^\dagger + b_{Q+}) + \sum_k \left\{ \left(\frac{1}{4} - v^2 \right) b_{k+}^\dagger b_{k+} + \frac{1}{4} b_{k-}^\dagger b_{k-} + \frac{1}{4} b_{k0}^\dagger b_{k0} \right\} \right]
 \end{aligned}$$

$$uv \propto M_{xy}$$

$$I = \frac{2\pi}{\hbar} |\langle f | R_{\text{intra}} | i \rangle|^2$$

1st order magnetic RS Is observed in the second-order Raman process:

1. above H_c ;
2. at the Γ point;
3. with the intensity proportional to M_{xy}^2 .



Summary of Experimental Results:

- ☑ We observe strong magnetic RS when the incident light is polarized along the direction of strong interdimer interaction;
- ☑ 1st order magnetic RS never appears below H_c or below p_c ;
- ☑ Raman intensity is proportional to M_{xy}^2 ;
- ☐ Energy of the P1 peak is the same as that of the Higgs mode;
- ☐ Halfwidth of the P1 peak under high pressures is proportional to the P1-peak energy.

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Diagonalization to calculate scattering intensity

Matsumoto *et al.*,
 PRL 89, 077203 (2002),
 PRB 69, 054423 (2004).

$$\begin{aligned} a_k &= us_k + vft_{k+Q^+} + vgt_{k+Q^-} \\ b_{k^+} &= -vs_{k+Q} + uft_{k^+} + ugt_{k^-} \\ b_{k^-} &= ft_{k^-} - gt_{k^+} \\ b_{k0} &= t_{k0} \end{aligned}$$

$$s_k, t_{k^+}, t_{k0}, t_{k^-}$$

$$a_k, b_{k^+}, b_{k0}, b_{k^-}$$

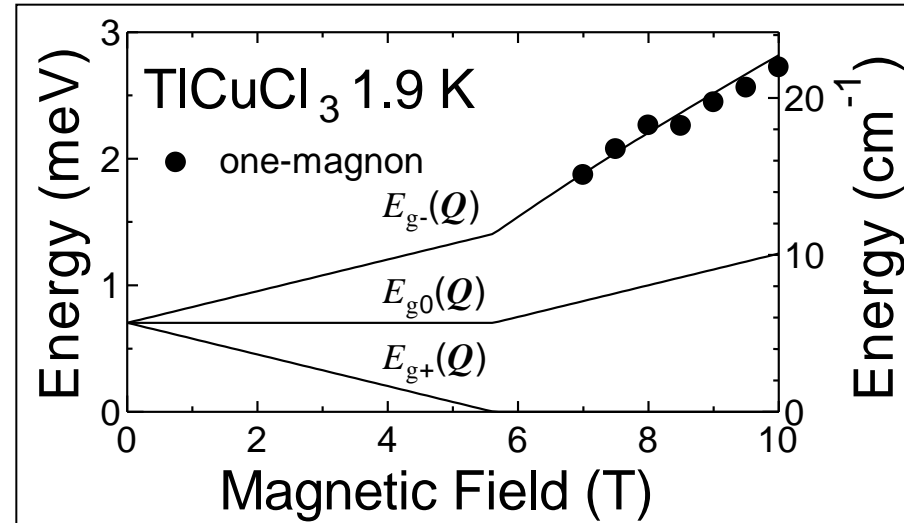
$$a_k, \alpha_k^+, \alpha_k^0, \alpha_k^-$$

Bogoliubov Transformation

$$\begin{pmatrix} \alpha_k^- \\ \alpha_k^+ \\ \alpha_k^{-\dagger} \\ \alpha_k^{+\dagger} \end{pmatrix} = \begin{pmatrix} u_{k^-}^- & u_{k^+}^- & v_{k^-}^- & v_{k^+}^- \\ u_{k^-}^+ & u_{k^+}^+ & v_{k^-}^+ & v_{k^+}^+ \\ v_{-k^-}^- & v_{-k^+}^- & u_{-k^-}^- & u_{-k^+}^- \\ v_{-k^-}^+ & v_{-k^+}^+ & u_{-k^-}^+ & u_{-k^+}^+ \end{pmatrix} \begin{pmatrix} b_{k^-} \\ b_{k^+} \\ b_{-k^-}^\dagger \\ b_{-k^+}^\dagger \end{pmatrix}$$

For Higgs and Goldstone Modes,
 we have

$$\begin{aligned} b_{Q^+} + b_{Q^+}^\dagger &= (u_{Q^+}^- - v_{Q^+}^-)^* \alpha_{Q^+}^- + (u_{Q^+}^- - v_{Q^+}^-) \alpha_{Q^+}^{-\dagger} \\ &\quad + \underbrace{(u_{Q^+}^+ - v_{Q^+}^+)^* \alpha_{Q^+}^+ + (u_{Q^+}^+ - v_{Q^+}^+) \alpha_{Q^+}^{+\dagger}}_{\text{zero}} \end{aligned}$$



Summary of Experimental Results:

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Summary of Experimental Results and Theoretical Consideration:

- ✓ We observe strong magnetic RS when the incident light is polarized along the direction of strong interdimer interaction;
- ✓ 1st Order magnetic RS never appears below H_c or below p_c ;
- ✓ Raman intensity is proportional to M_{xy}^2 ;
- ✓ Energy of the P1 peak is the same as that of the Higgs mode;
- ✓ Halfwidth of the P1 peak under high pressures is proportional to the P1-peak energy.

We conclude that

Magnetic RS detects the Higgs mode.