

Kyoto, Feb. 12, 2014

Peculiar phenomena in the time-dynamics of condensed matter systems undergoing symmetry-breaking transitions.

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Jožef Stefan International Postgraduate School*



European Research Council
Established by the European Commission



Experiments:

(at JSI)

L. Stojchevska
I. Vaskivskiy
T. Mertelj
P. Kusar
R. Yusupov



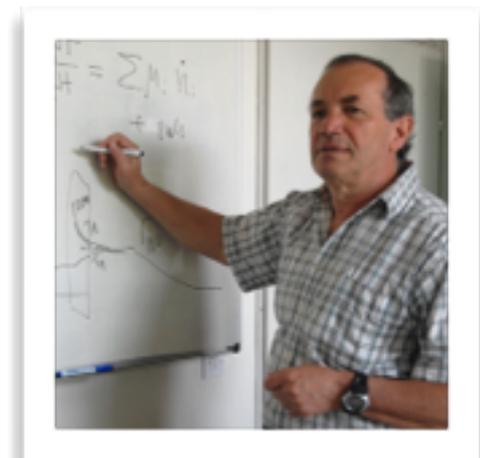
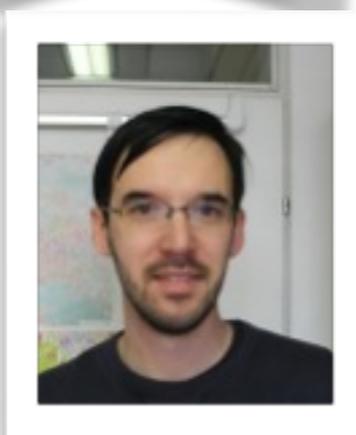
Samples+:

I. Fisher (Stanford)
P. Sutar (JSI)
L. Forro (EPFL)
H. Berger (EPFL)



Lithography:

D. Svetin (JSI)

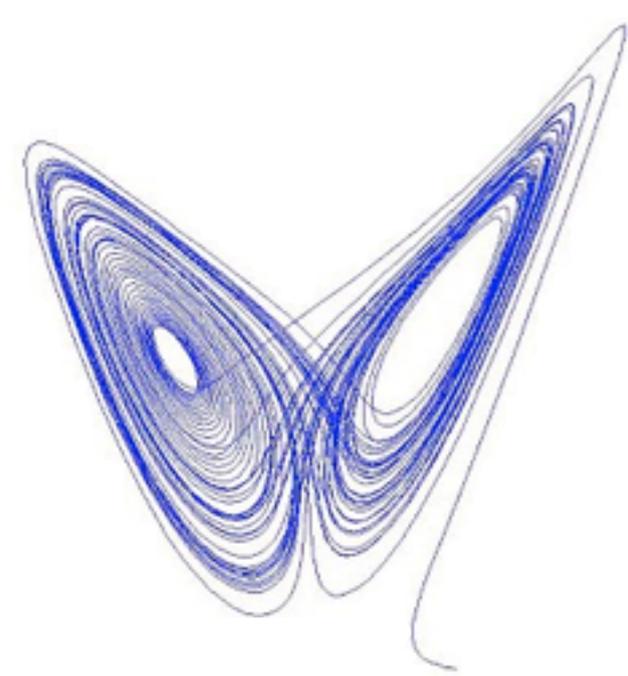


Theory

Serguei Brazovskii
(Univ. Paris Sud Orsay)

Viktor Kabanov
(JSI)





Our aim is to investigate trajectories of systems through symmetry-breaking transitions under nonequilibrium conditions, in real time.

Examples:

- HT Superconductors
- CDW transitions

Peculiar phenomena:

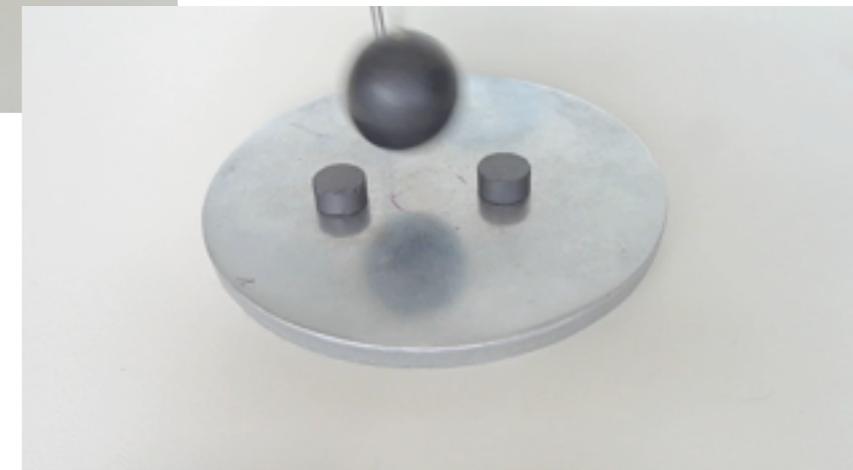
- Amplitude mode decay and creation from defect annihilation
- Coupling to collective modes from previous eons
- A transition to a **hidden state**: $1T$ -TaS₂



$$\psi(t) = A(t)e^{i\phi(t)}$$

(τ_1 and τ_2)

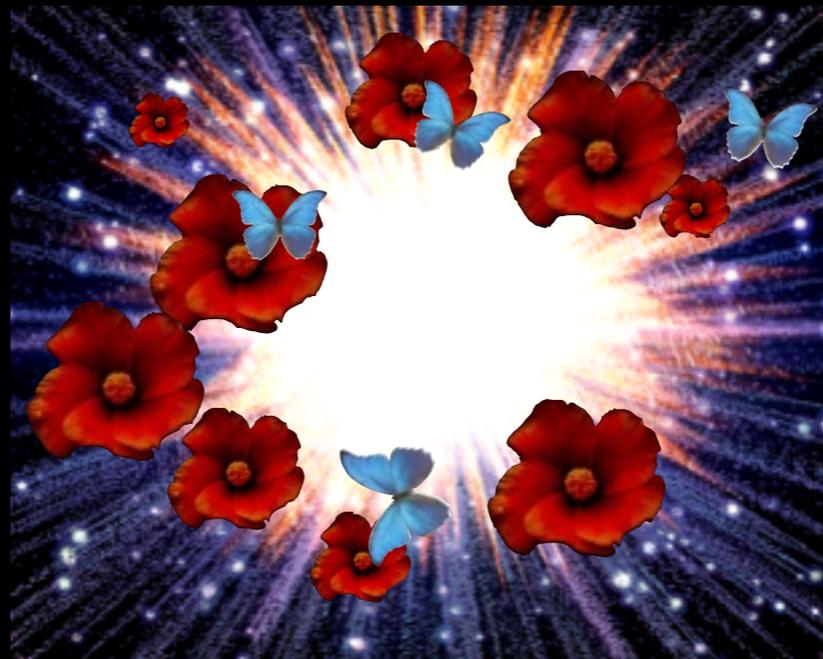
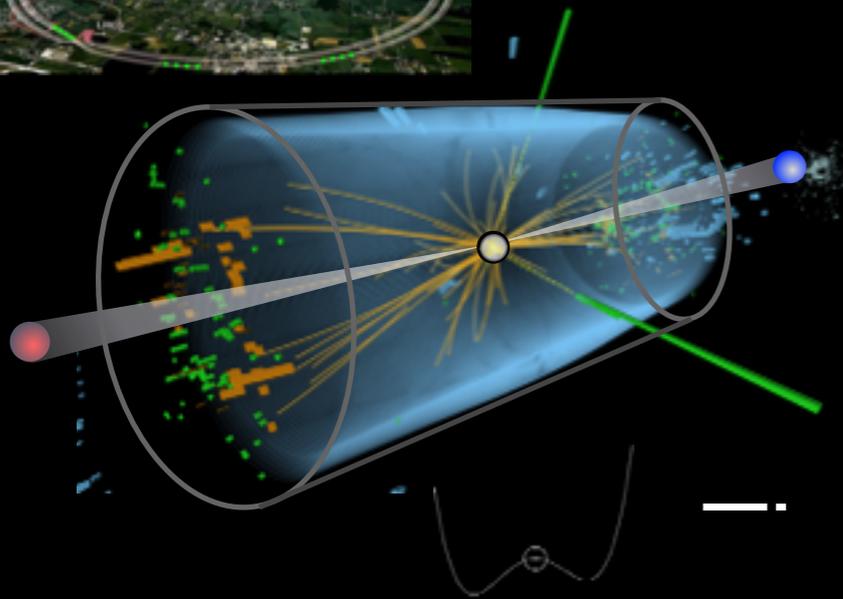
$$\psi(t) \simeq A(t) (\tau_1)$$





Transitions...

in time



The non-linear energy functional

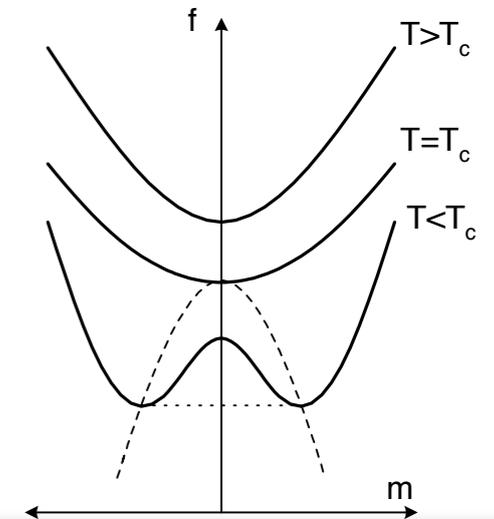


The Landau non-linear energy functional originally written to describe a structural phase transition:

$$F = \alpha\Psi^2 + \beta\Psi^4 + H\Psi \quad \text{where} \quad \alpha = \alpha_0(T - T_c)$$

leads to the Ginzburg-Landau equation for a superconductor:

$$F = F_0 + \alpha|\psi|^2 + \frac{\beta}{2}|\psi|^4 + \frac{1}{2m}|(-i\hbar\nabla - 2e\mathbf{A})\psi|^2 + \frac{|\mathbf{B}|^2}{2\mu_0}$$

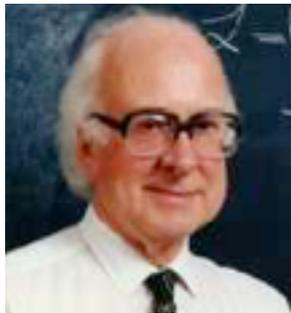


13, NUMBER 16 PHYSICAL REVIEW LETTERS 19 OCTOBER 1964

BROKEN SYMMETRIES AND THE MASSES OF GAUGE BOSONS

Peter W. Higgs

Tait Institute of Mathematical Physics, University of Edinburgh, Edinburgh, Scotland
(Received 31 August 1964)



Lagrangian density, includes K.E. term

$$L(\varphi) = \partial_\mu\varphi^*\partial^\mu\varphi - \alpha\varphi^*\varphi - \frac{\beta}{2}|\varphi^*\varphi|^2$$

J. Phys. A: Math. Gen., Vol. 9, No. 8, 1976. Printed in Great Britain. © 1976

Topology of cosmic domains and strings

T W B Kibble

Blackett Laboratory, Imperial College, Prince Consort Road, London



2. The phase transition

Although our discussion will be quite general, for illustrative purposes it is convenient to have a specific example in mind. Let us consider an N -component real scalar field ϕ with a Lagrangian invariant under the orthogonal group $O(N)$, and coupled in the usual way to $\frac{1}{2}N(N-1)$ vector fields represented by an antisymmetric matrix $B_{\mu\nu}$. We can take

$$L = \frac{1}{2}(D_\mu\phi)^2 - \frac{1}{8}g^2(\phi^2 - \eta^2)^2 + \frac{1}{8}\text{Tr}(B_{\mu\nu}B^{\mu\nu}) \quad (1)$$

with

$$D_\mu\phi = \partial_\mu\phi - eB_\mu\phi$$

$$B_{\mu\nu} = \partial_\nu B_\mu - \partial_\mu B_\nu + e[B_\mu, B_\nu].$$



The time-dependent GLT

The energy of the system can be described in terms of a time-dependent Ginzburg-Landau functional[†]:

$$F = \alpha \Psi^2 + \beta \Psi^4 + H \Psi$$

where instead of the usual temperature dependence $(T - T_c)$, the *first* term is time-dependent:

$$\alpha = \left[1 - \frac{T_e(t, \mathbf{r})}{T_c} \right]$$

“The quench process”

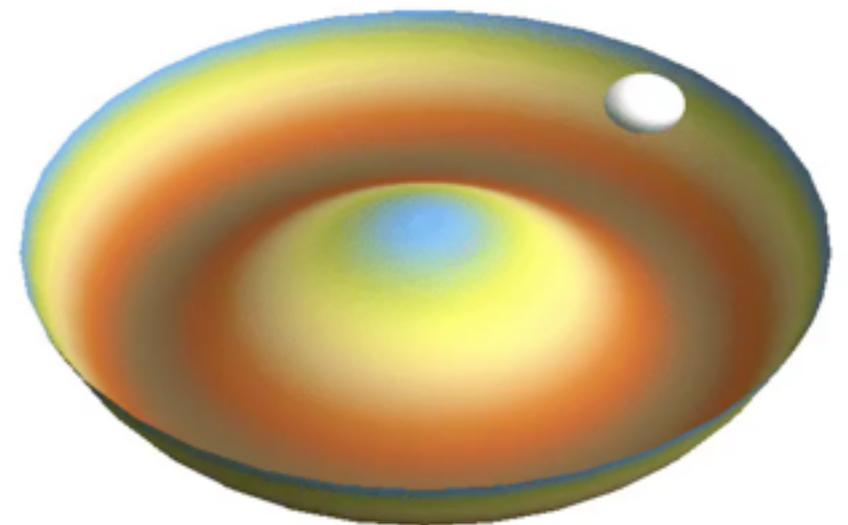
The equation of motion is obtained via the Euler-Lagrange theorem :

$$\frac{1}{\omega_0^2} \frac{\partial^2}{\partial t^2} A + \frac{\alpha}{\omega_0} \frac{\partial}{\partial t} A - (1 - \eta) A + A^3 - \xi^2 \frac{\partial^2}{\partial z^2} A = 0$$

The order parameter, $\psi(t) = A(t)e^{i\phi(t)}$

Yusupov et al, Nat Phys. (2010)

[†] Phase fluctuations are assumed to be slow.

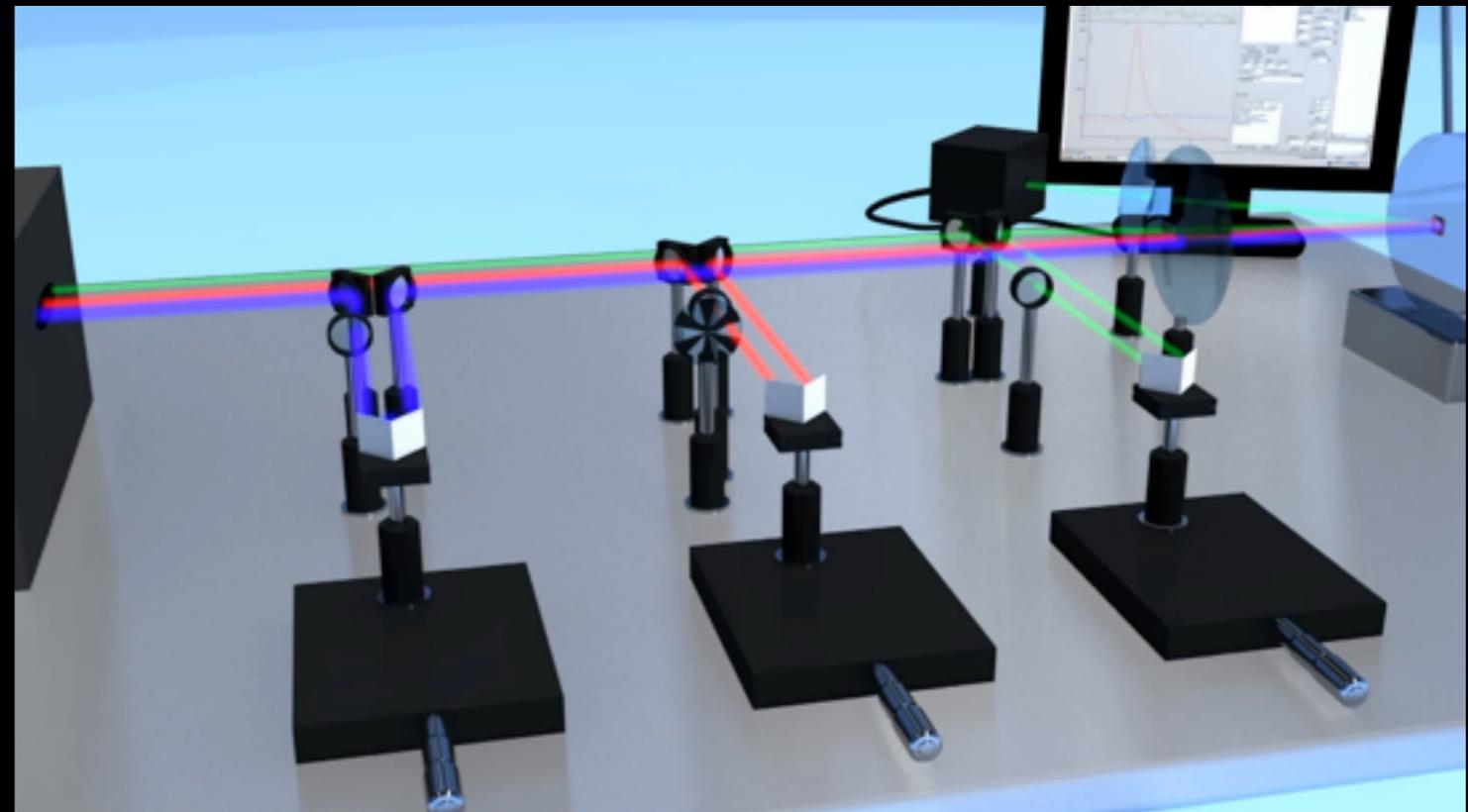


“Cosmic Quench” experiments

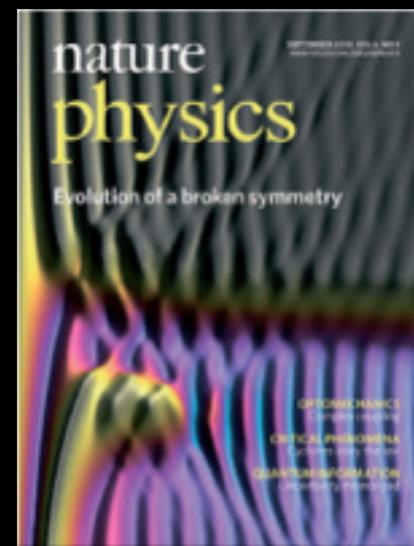
“Cosmology in $L^4\text{He}$ ”, Zurek (1985)

Optical experiments :

- offer high temporal resolution (easily to 7 fs)
- flexibility in probe wavelengths (THz - UV)
- we can probe the symmetry of different states

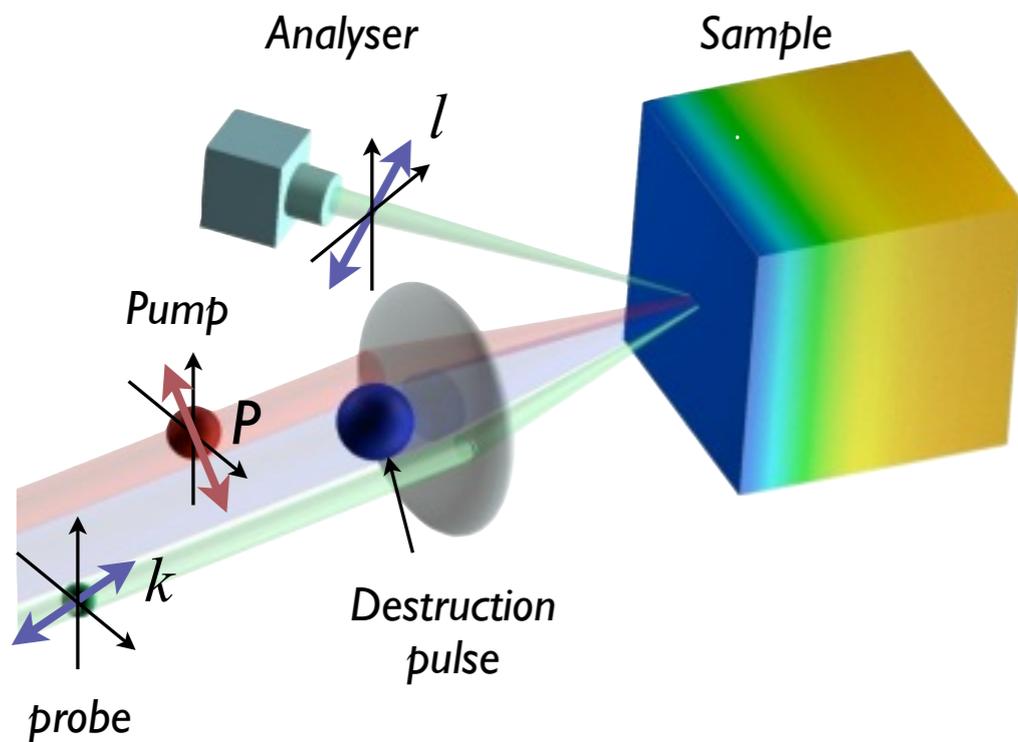


Yusupov, R. *et al. Nat Phys*
6, 681–684 (2010).

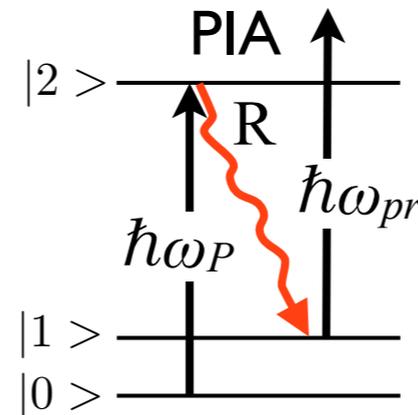


The response function is related to Raman-like processes

Toda et al., arXiv:1311.4719



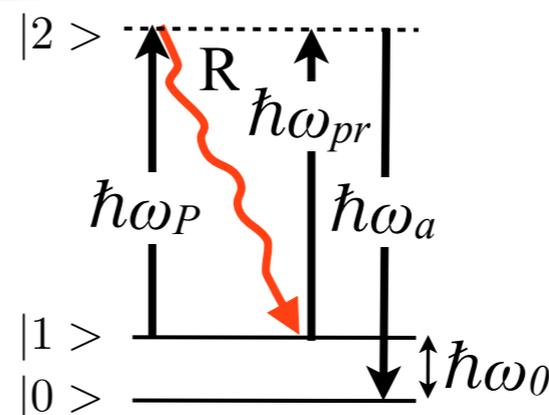
I. Photoinduced absorption (PIA):



The polarisation selection rules are determined by the dielectric tensor

1. Kabanov, V., Demsar, J., Podobnik, B. & Mihailovic, D. *Phys Rev B* **59**, 1497–1506 (1999).
2. Dvorsek, D. et al. *Phys Rev B* **66**, 020510 (2002).
3. Mihailovic, D., et al., *J Phys-Condens Mat* **25**, 404206 (2013).

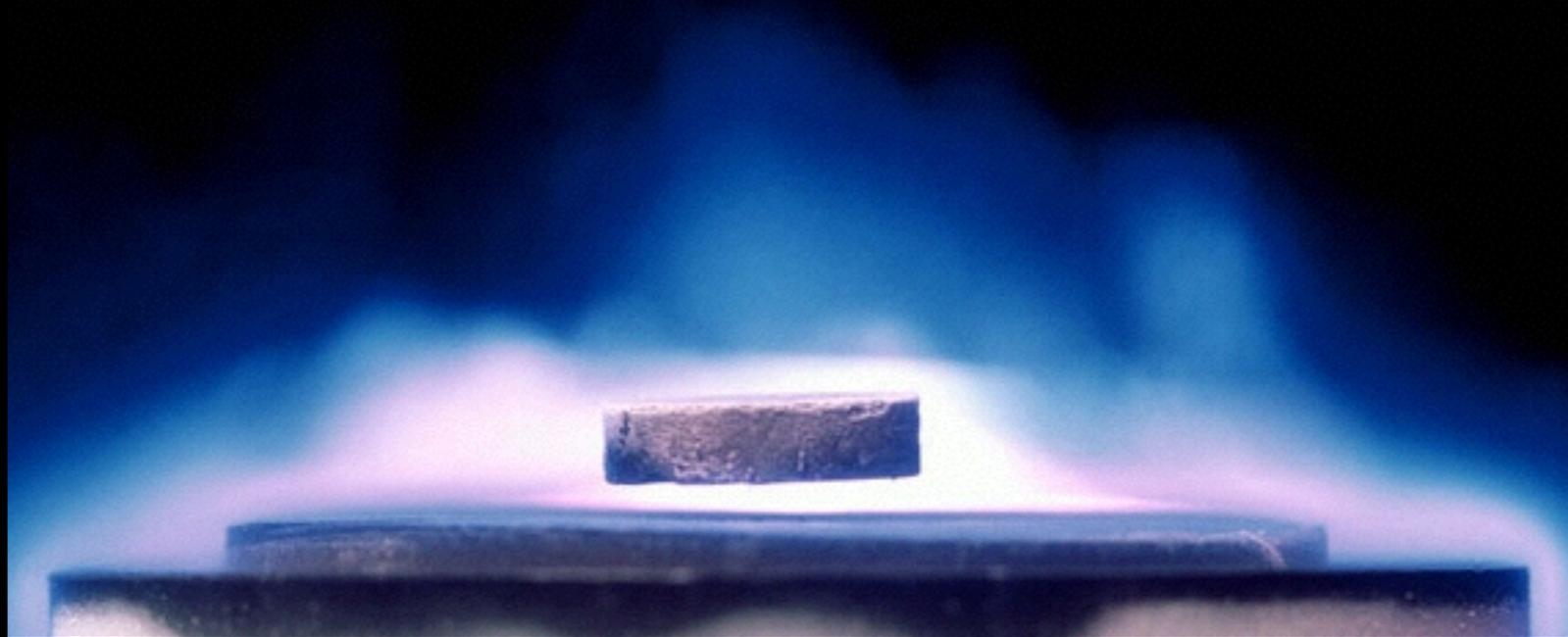
2. Coherent Raman-like (CRS) process:



The polarisation selection rules are governed by the Raman tensor χ_{kl}

1. Garrett, G., Albrecht, T., WHITAKER, J. & Merlin, R. *Phys Rev Lett* **77**, 3661–3664 (1996).
2. Stevens, T. E., Kuhl, J. & Merlin, R. *Phys Rev B* **65**, 144304 (2002).

CRS and PIA probe processes can be distinguished by polarisation selection rules



Dynamics of broken symmetry nodal and anti-nodal excitations in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ probed by polarized femtosecond spectroscopy

Y. Toda and F. Kawanokami

Department of Applied Physics, Hokkaido University, Sapporo 060-8628, Japan.

T. Kurosawa and M. Oda

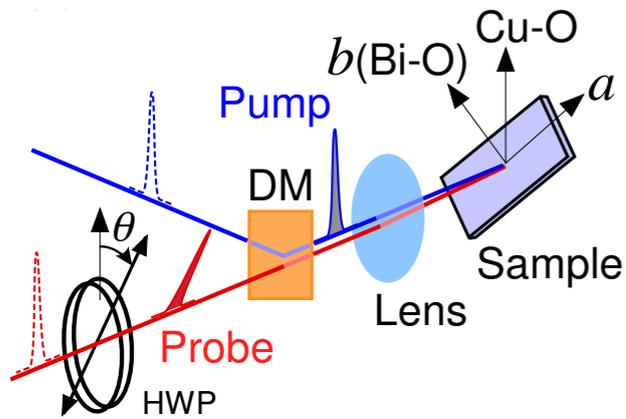
Department of Physics, Hokkaido University, Sapporo 060-0810, Japan.

arXiv: Toda et al., (2013)

I. Madan, T. Mertelj, V. V. Kabanov, and D. Mihailovic

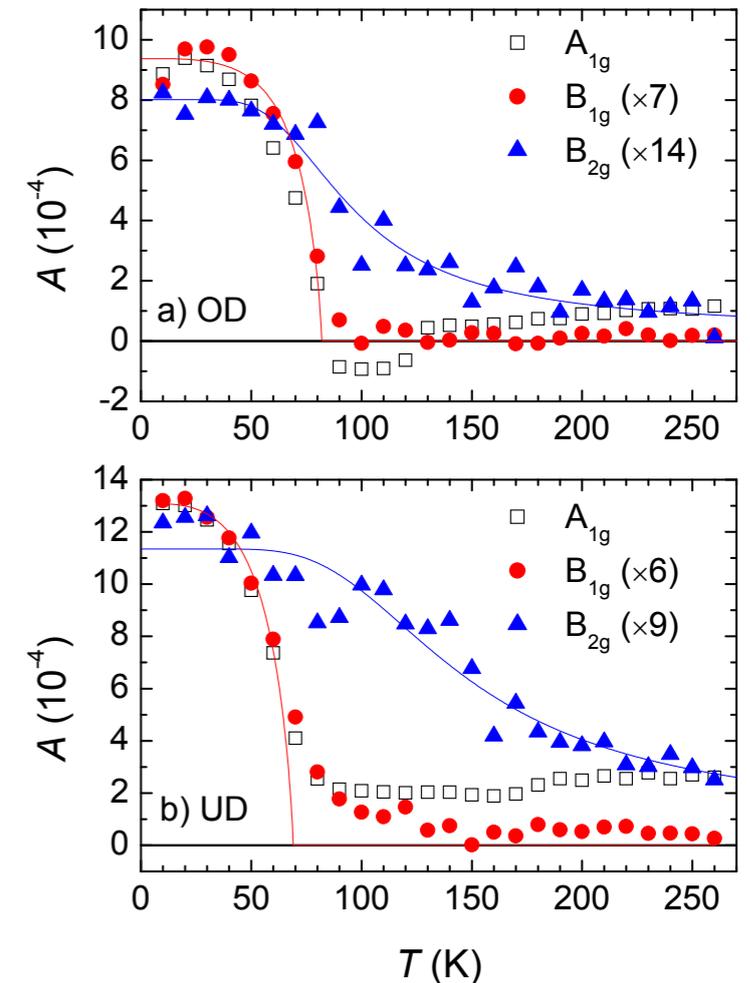
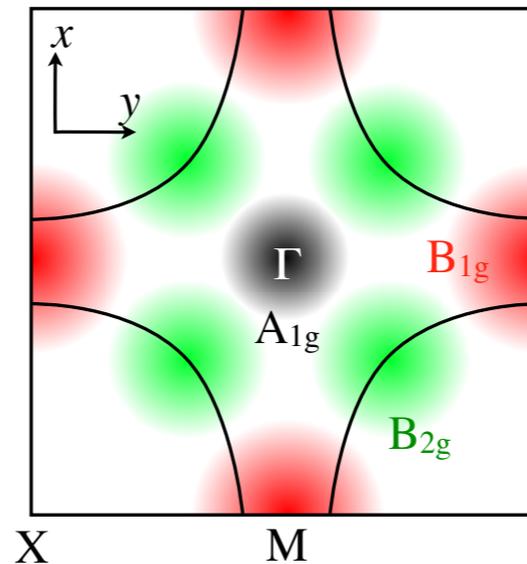
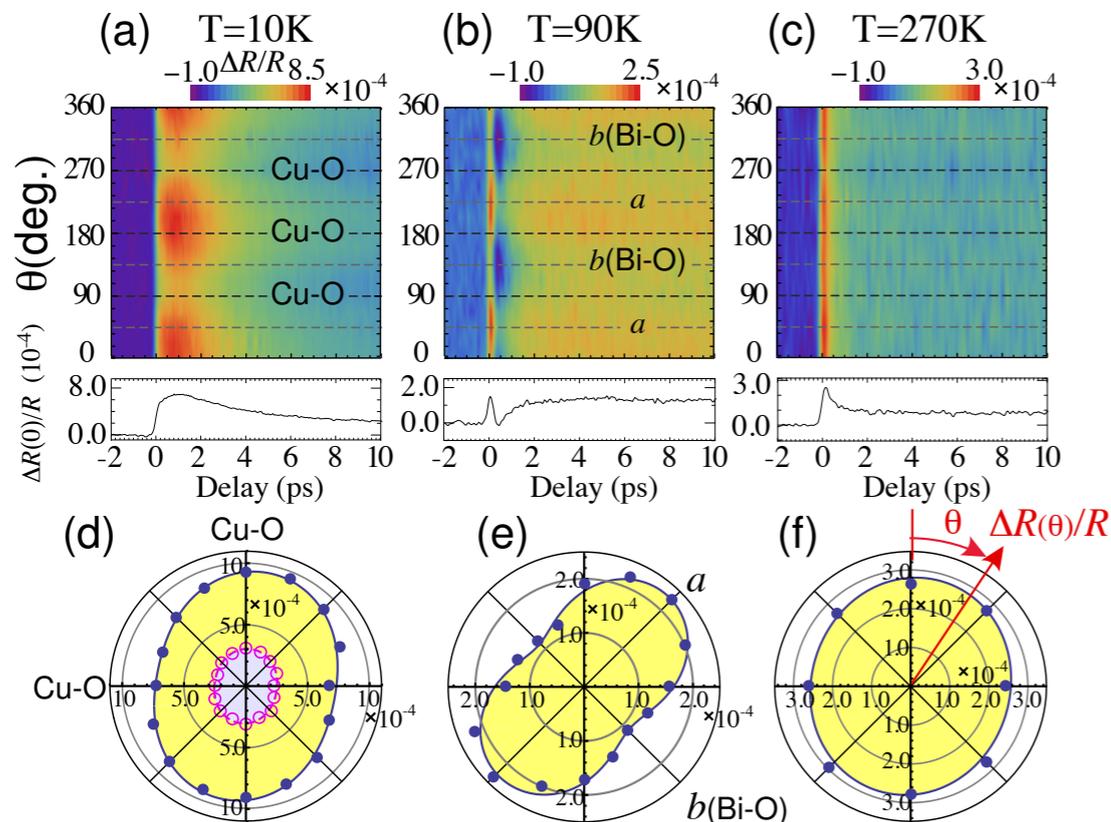
Complex Matter Dept., Jozef Stefan Institute, Jamova 39, Ljubljana, SI-1000, Slovenia

(Dated: January 29, 2014)



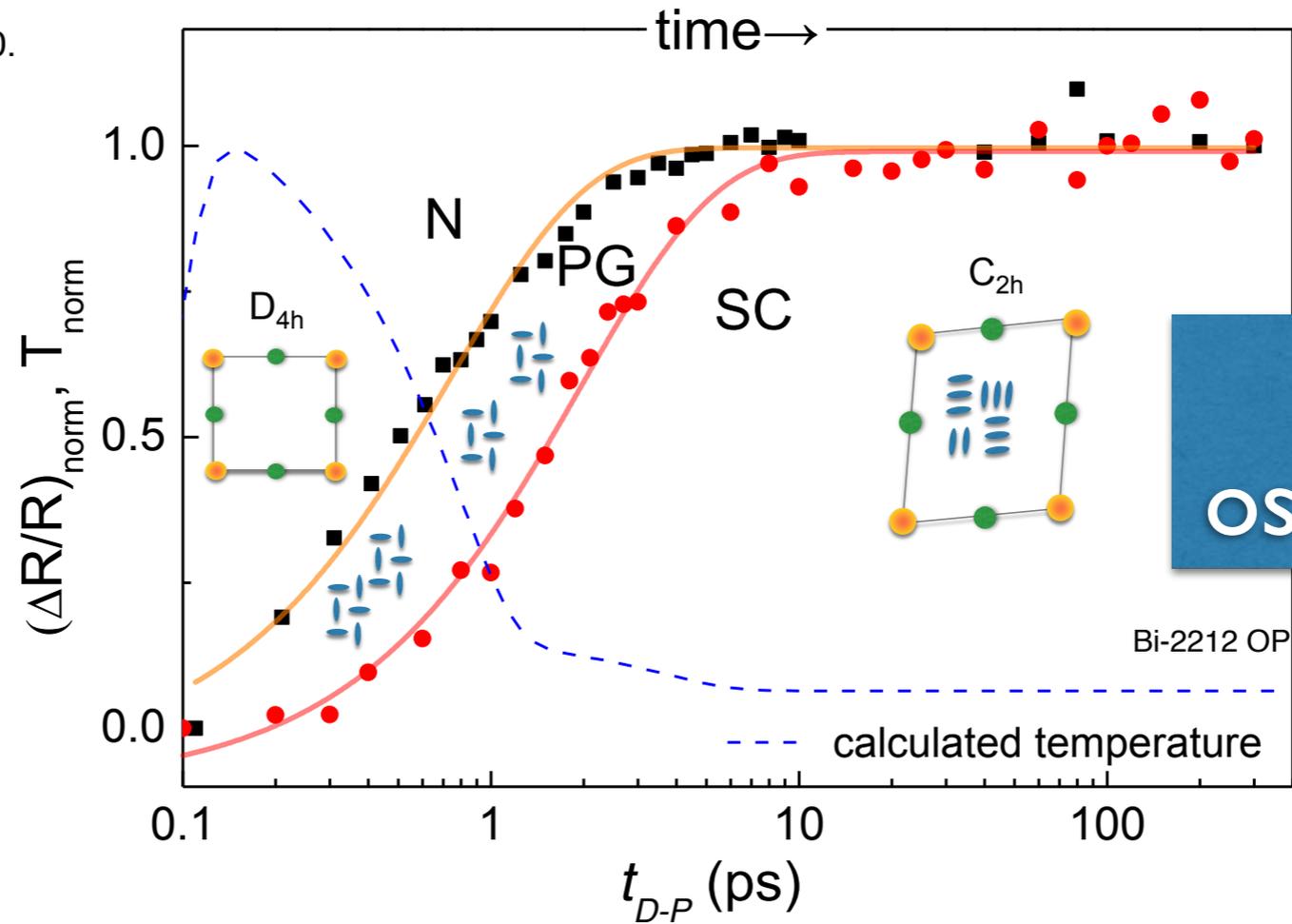
Temperature dependence of different symmetry components, A_{1g} , B_{1g} and B_{2g} :

$$\Delta R(\theta) = \frac{\partial R}{\partial \epsilon_1} \left[\Delta \epsilon_1^{A_{1g}} + \Delta \epsilon_1^{B_{1g}} \cos(2\theta) + \Delta \epsilon_1^{B_{2g}} \sin(2\theta) \right] + \frac{\partial R}{\partial \epsilon_2} \left[\Delta \epsilon_2^{A_{1g}} + \Delta \epsilon_2^{B_{1g}} \cos(2\theta) + \Delta \epsilon_2^{B_{2g}} \sin(2\theta) \right] \quad (2)$$



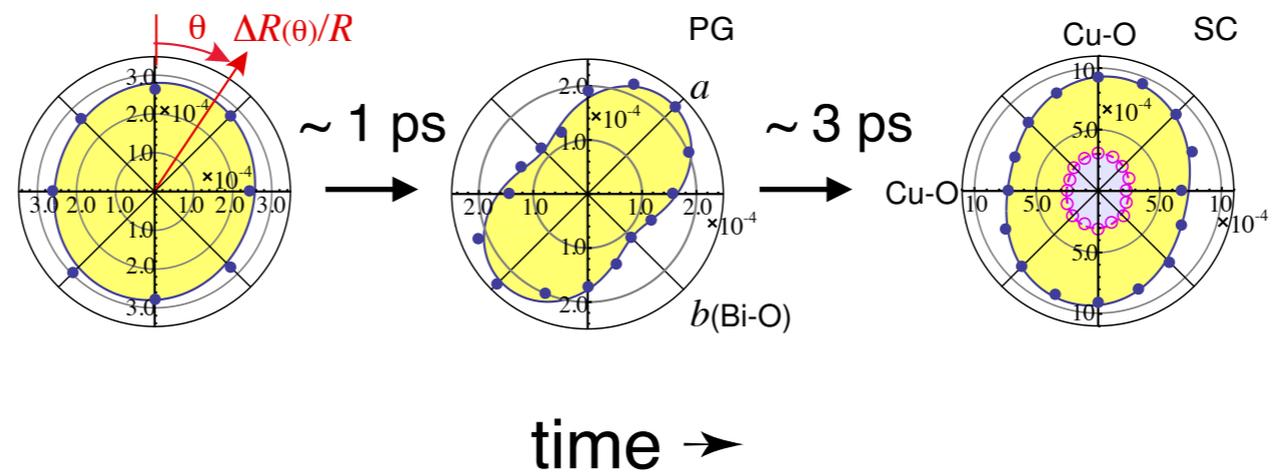
Time-dynamics of broken (rotational) symmetry in a high-Tc superconductor (Bi-2212-OP)

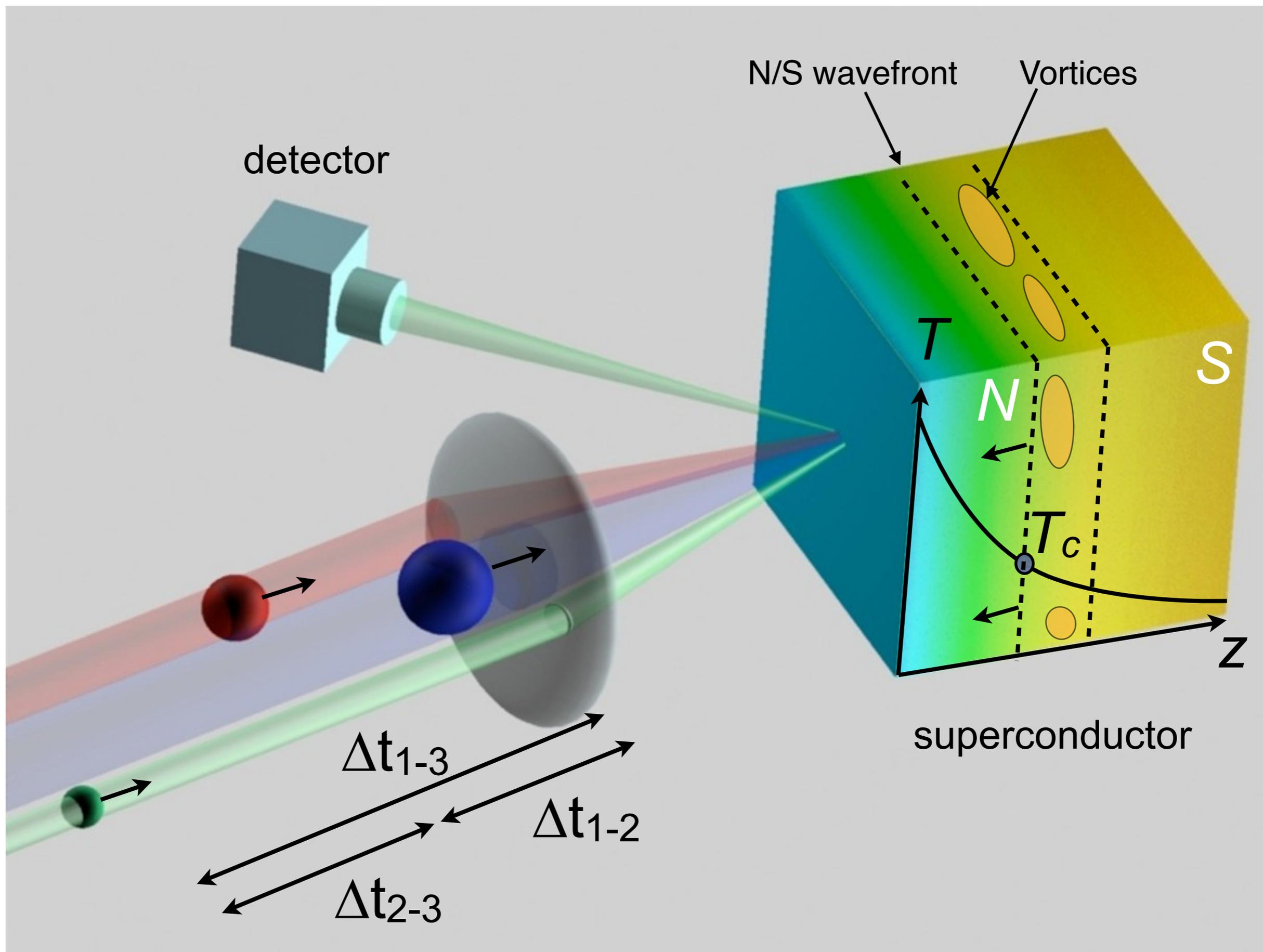
The D laser pulse is incident at $t = 0$.



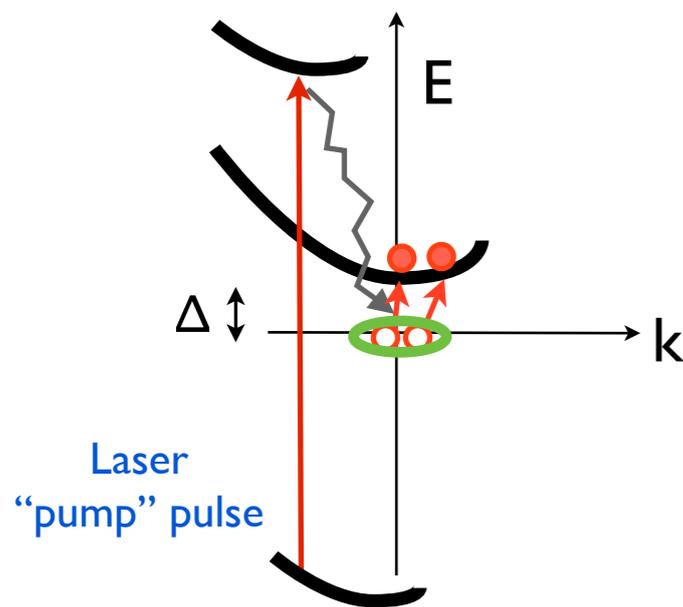
No oscillations!

Polarisation anisotropy changes with time





Laser vaporisation of the superconducting condensate

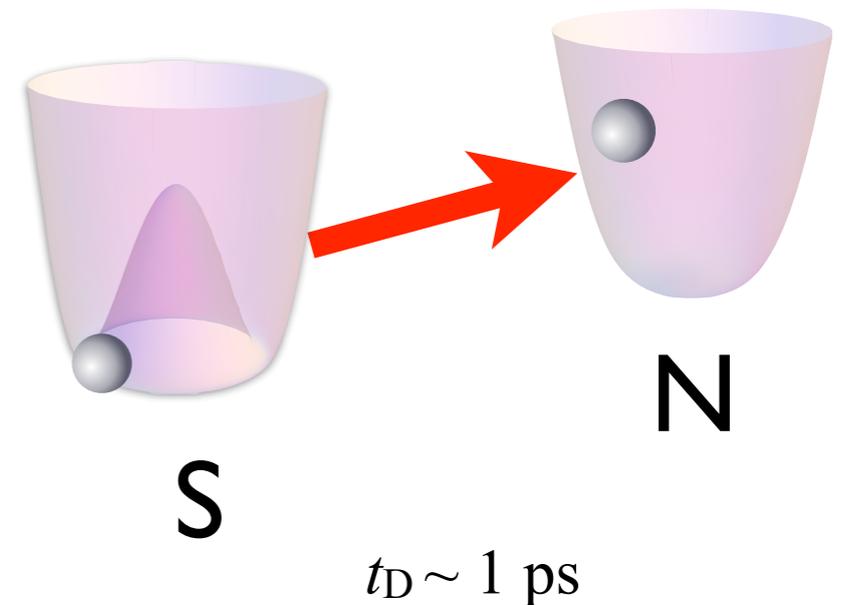


Single particle
(electron) energy
relaxation via boson
(phonon) emission

↓ $t_D \sim 1$ ps

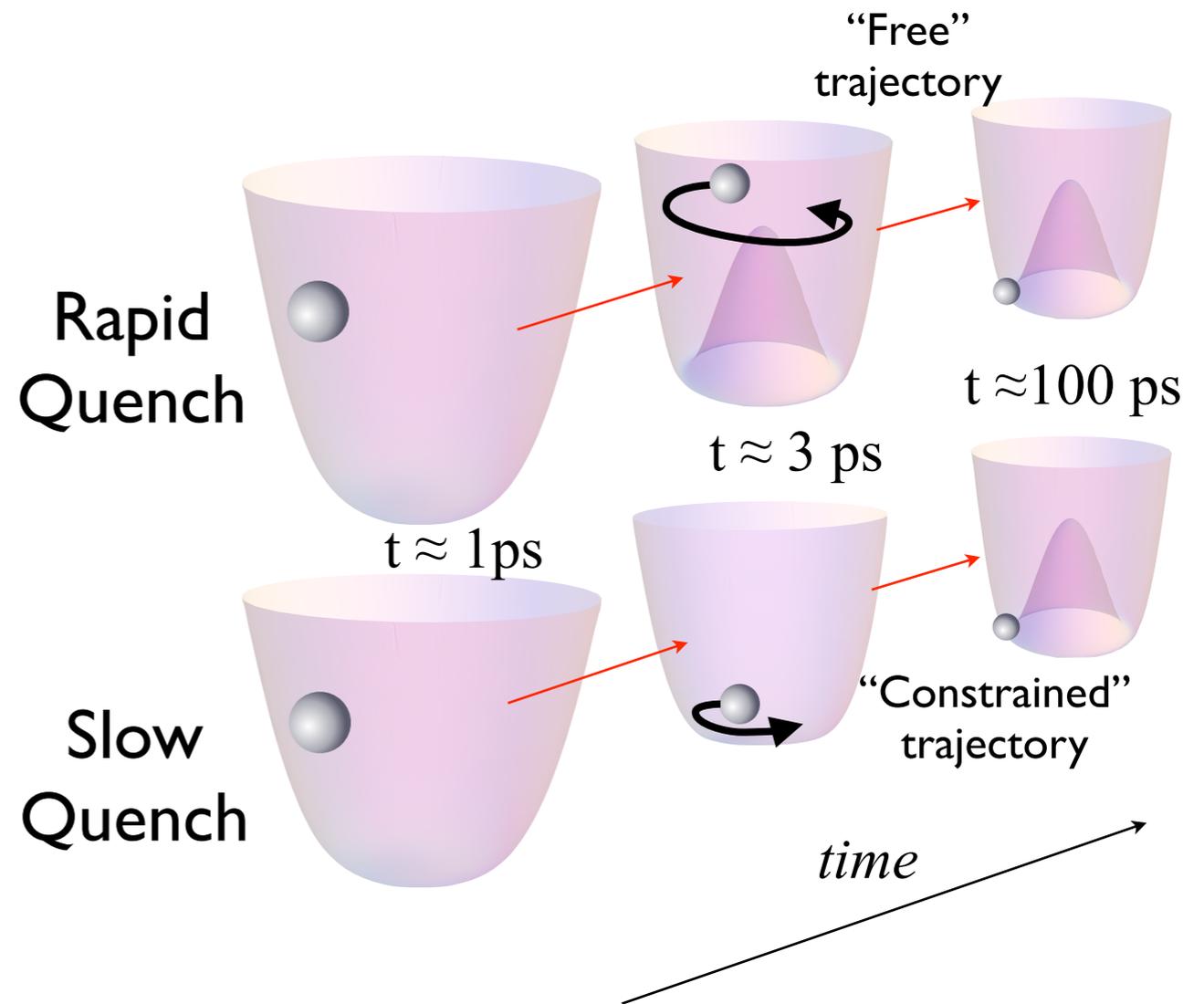
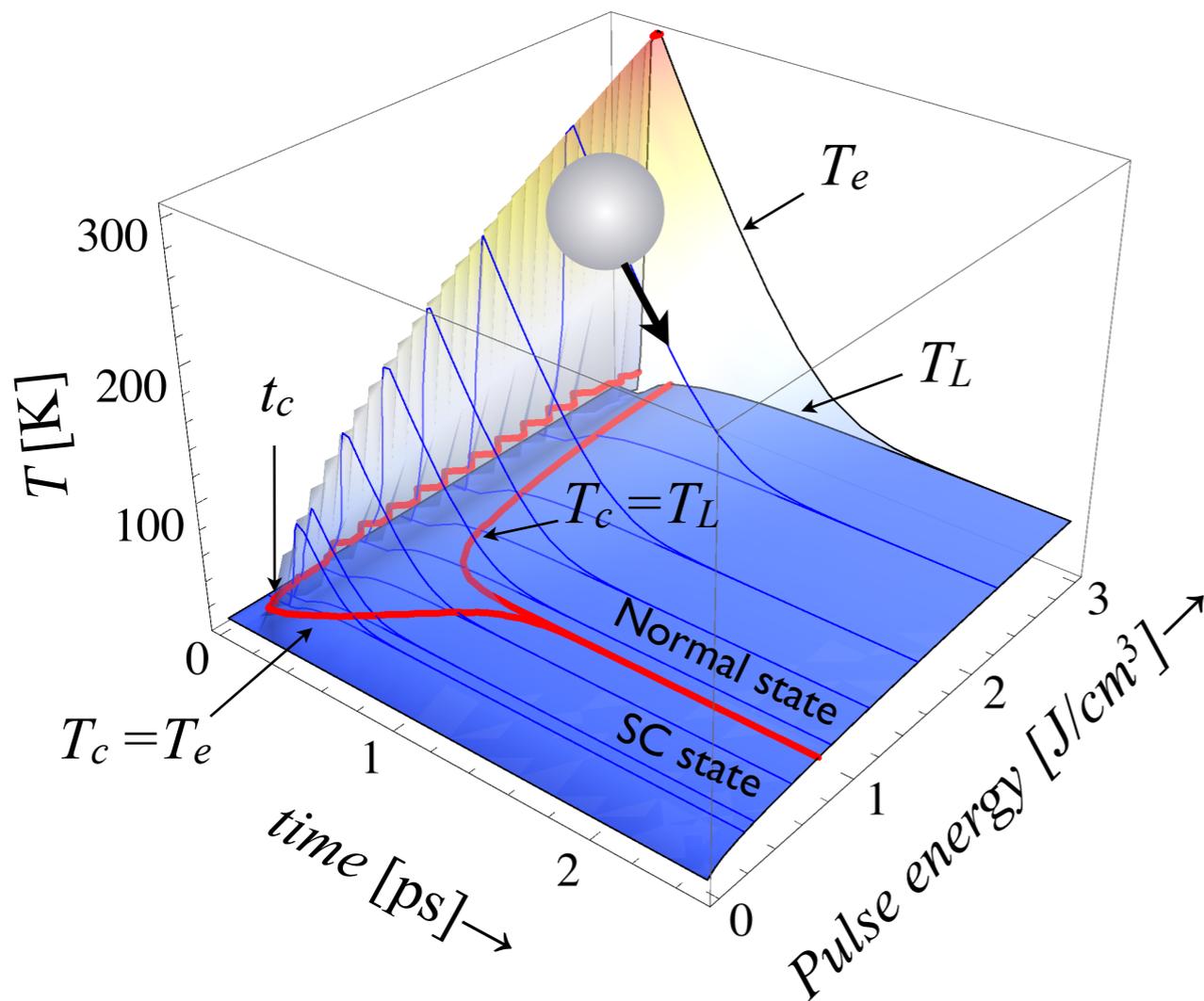
Bosons destroy pairs,
creating QPs

The SC condensate is
vaporised in less than 1 ps



1. Kugar, P., Kabanov, V., Demsar, J. & Mertelj, T. Controlled Vaporization of the Superconducting Condensate in Cuprate Superconductors by Femtosecond Photoexcitation. *Phys Rev Lett* **101**, 227001 (2008).
2. Stojchevska, L. *et al.* Mechanisms of nonthermal destruction of the superconducting state and melting of the charge-density-wave state by femtosecond laser pulses. *Phys Rev B* **84**, 180507(R) (2011).

The quench through T_c

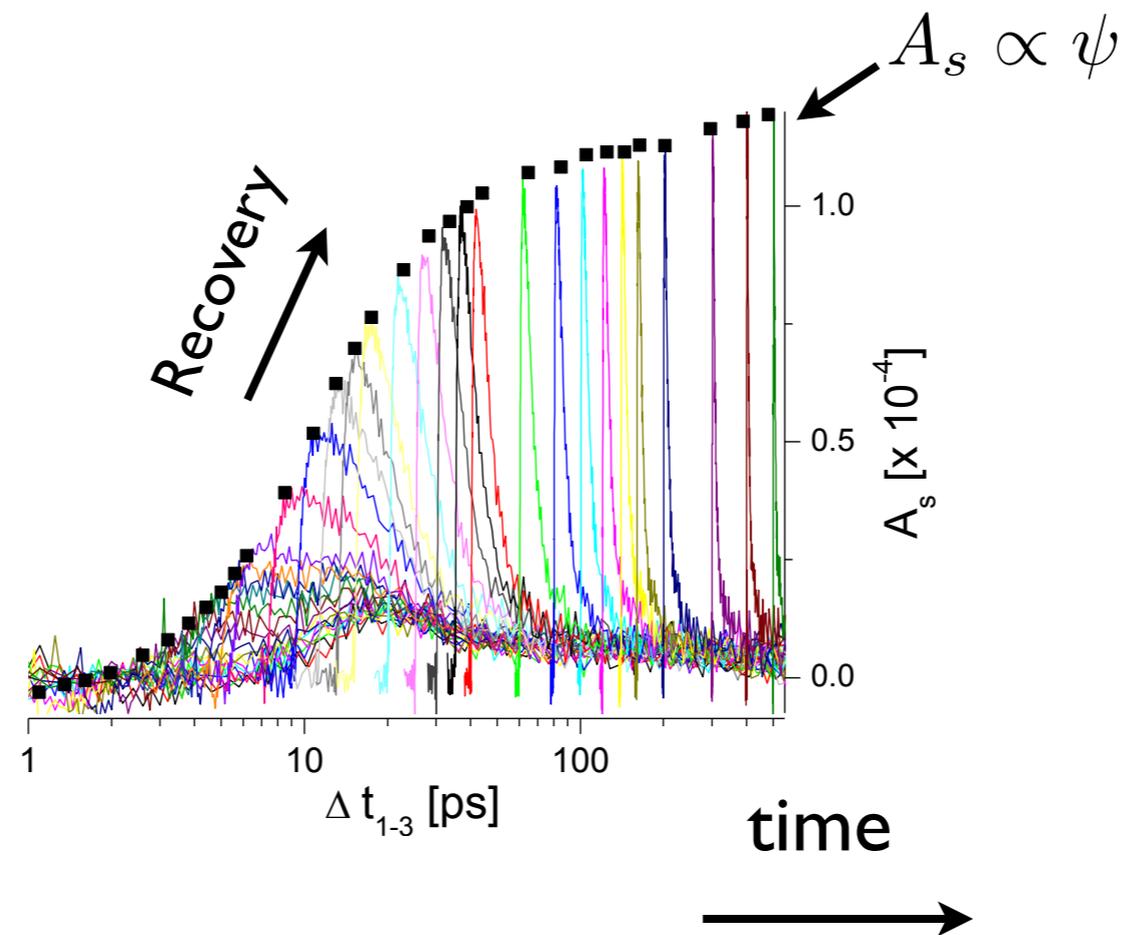


Higgs mode osc. period: $2\pi/\omega_H \sim 0.1$ ps

Quench time: $\tau_Q = 0.1 \sim 30$ ps

Ginzburg-Landau time: $\tau_{GL} = 1/\Delta_0 = 0.1 \simeq 5$ ps

Recovery of the superconducting state measured by the amplitude of the transient reflectivity $A_s(t)$

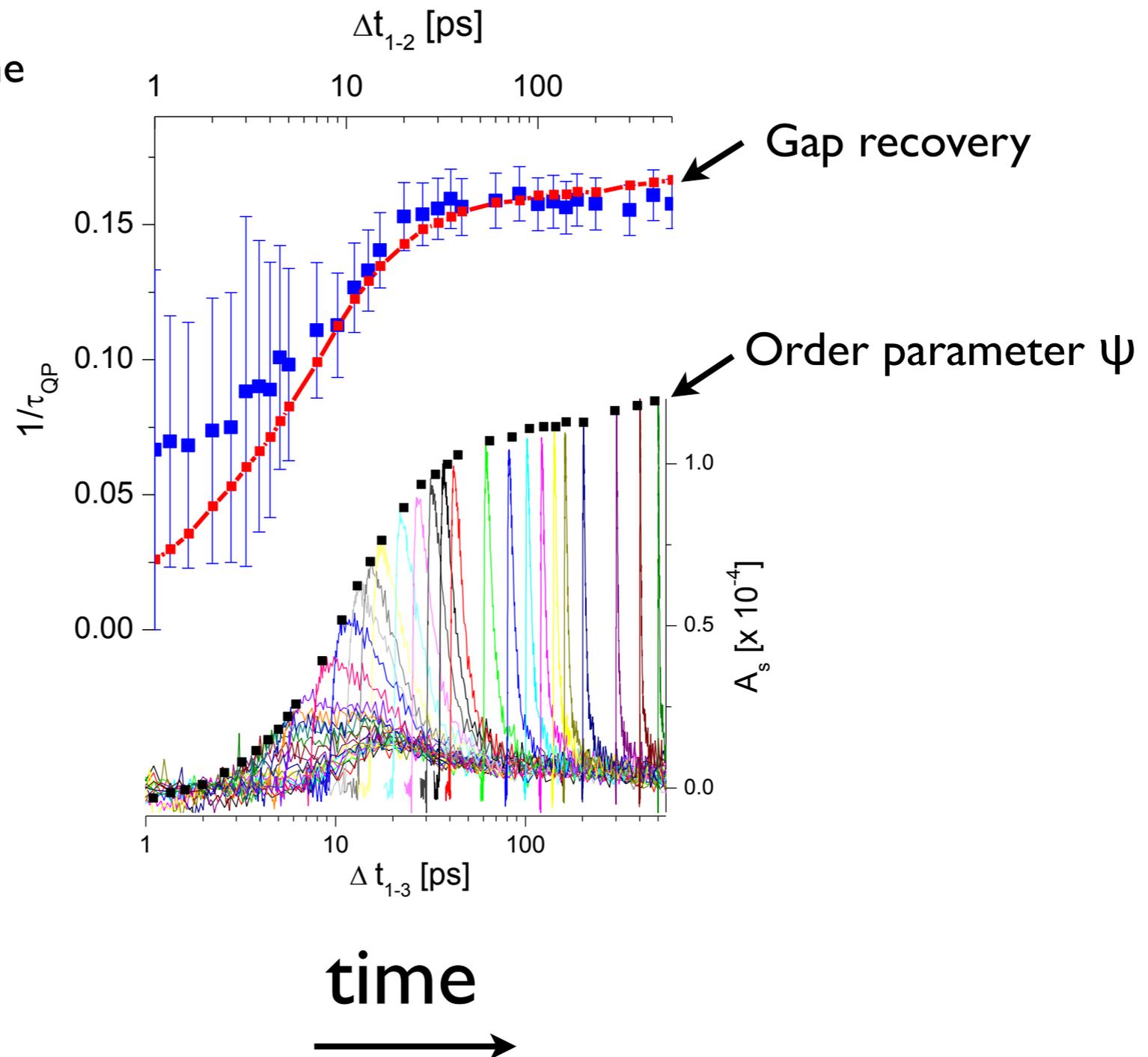
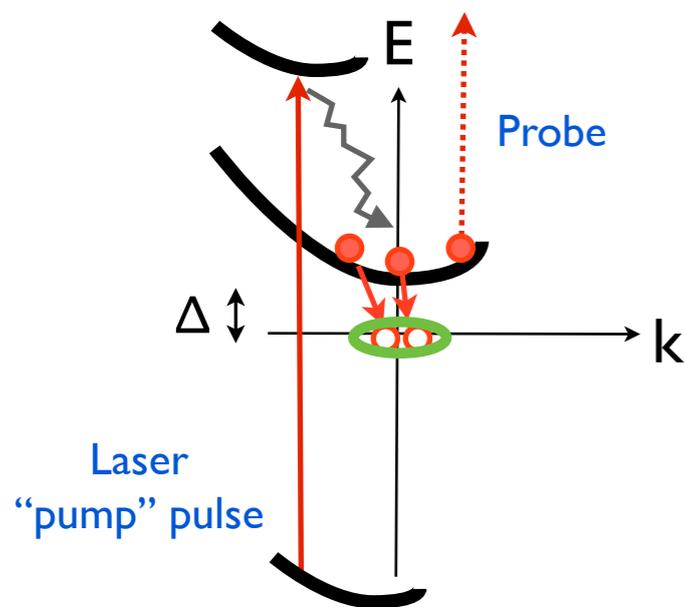


No Higgs oscillations observed in $A_s(t)$!

Superconducting gap recovery: QP recombination time compared with reflectivity amplitude

Quasiparticle recombination time

$$1/\tau_{QP} \sim \Delta(t)$$



time
→

Modelling of superconducting state recovery:

TDGL:
$$i \left(\frac{\partial \psi}{\partial t} + \cancel{i\Phi} \right) = -\alpha_r(t, z)\psi - \psi|\psi|^2 - (i\nabla + \cancel{\mathbf{a}})^2 \psi + \eta$$

$$\nabla^2 \Phi = -\nabla \left[\frac{i}{2} (\psi^* \nabla \psi - \psi \nabla \psi^*) + \mathbf{a} |\psi|^2 \right]$$

 no external field

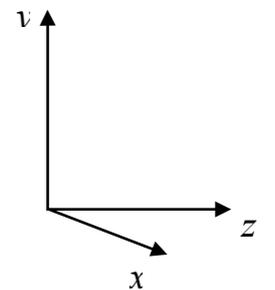
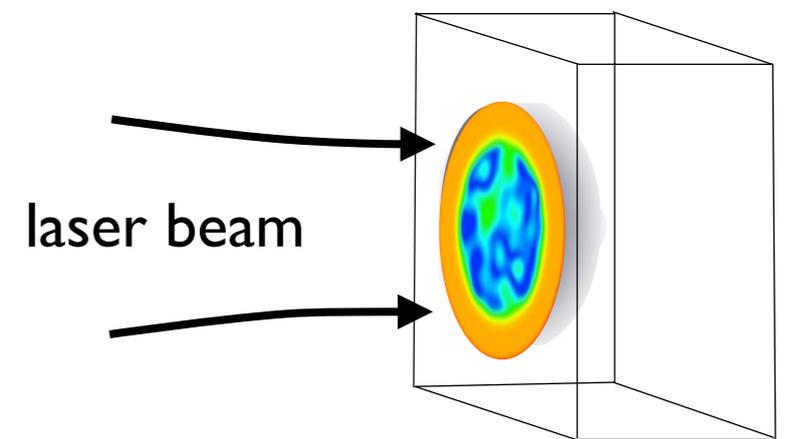
Diffusion:

$$\frac{\partial T_D(t, \mathbf{s})}{\partial t} = D \nabla^2 T_D$$

Photoexcited electron energy loss:

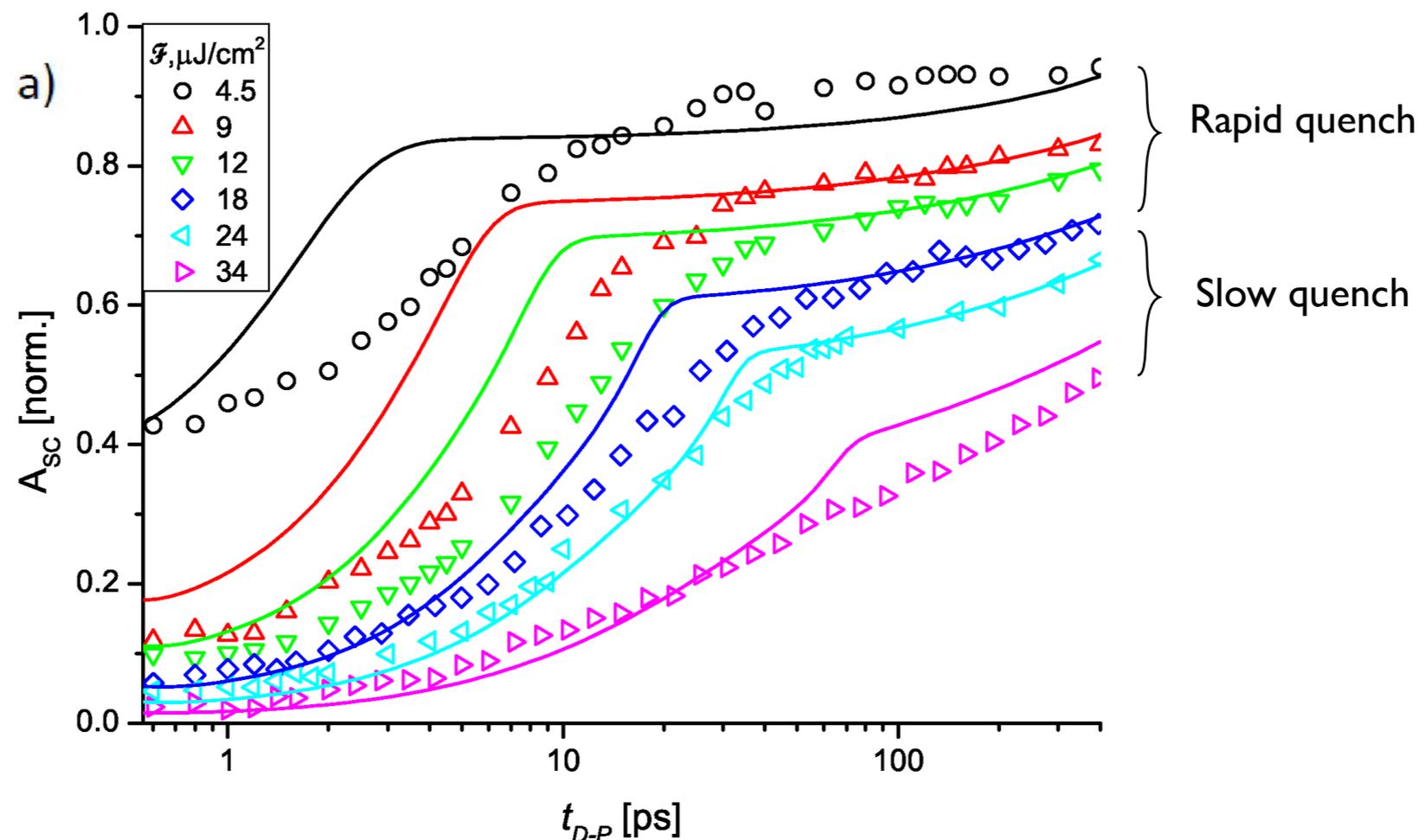
$$\gamma_e T_e \frac{dT_e}{dt} = -\gamma_L (T_e - T_L) + P(t)$$

$$C_L(T) \frac{dT_L}{dt} = \gamma_L (T_e - T_L)$$



Basic TDGL equation:
$$\frac{\partial \psi}{\partial t} = \alpha_r(t, z)\psi - \psi|\psi|^2 + \nabla^2 \psi + \eta$$

Boundary conditions:
$$\psi(0, z) = \begin{cases} 0 & , \mathcal{F}(z) > \mathcal{F}_T; \\ (1 - \frac{\mathcal{F}}{\mathcal{F}_T} e^{-z/\lambda}) \sqrt{1 - T(0, z)/T_c} & , \mathcal{F}(z) < \mathcal{F}_T. \end{cases}$$

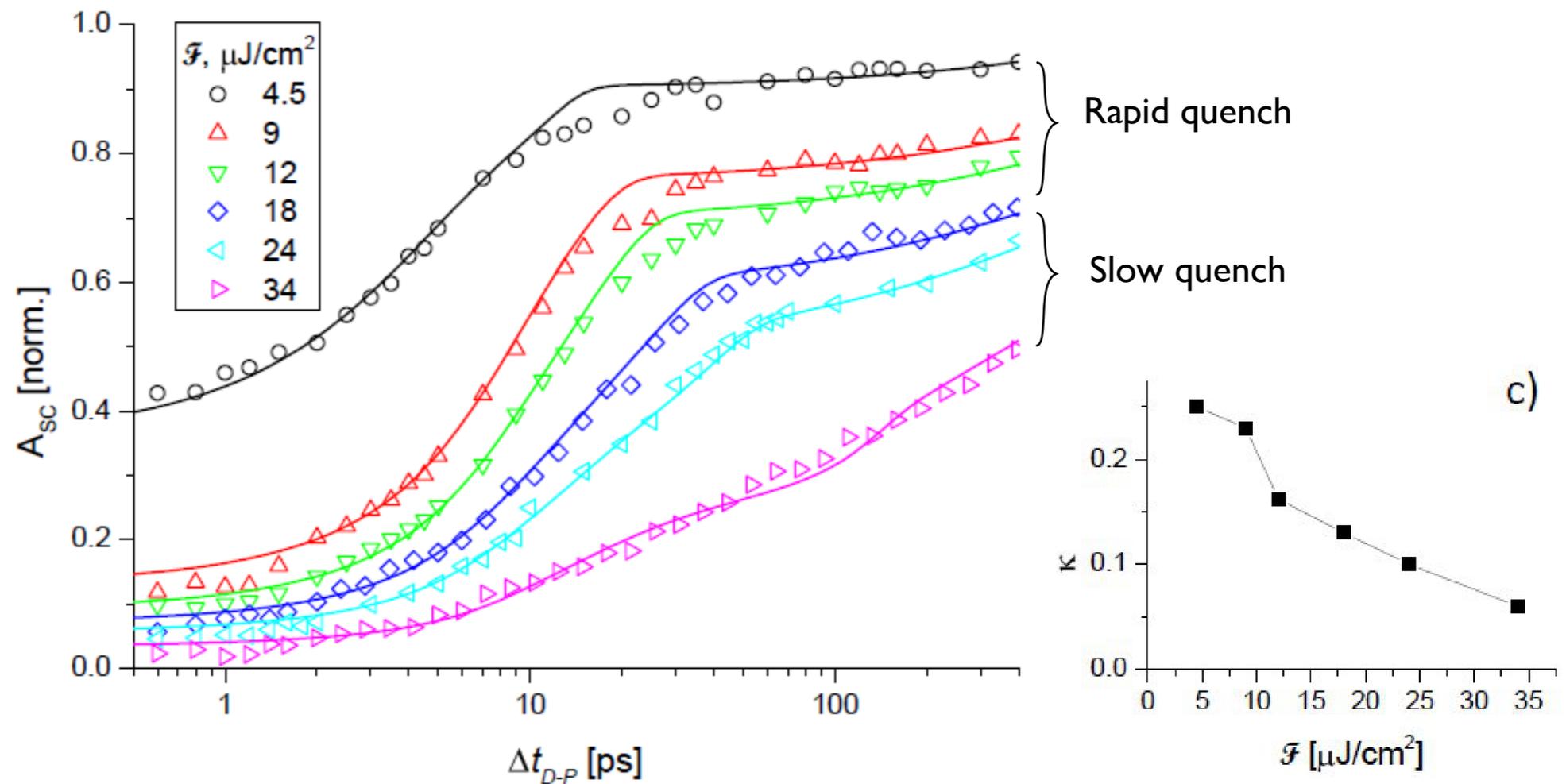


Doesn't work very well!

Basic TDGL equation: $\frac{\partial \psi}{\partial t} = \alpha_r(t, z)\psi - \psi|\psi|^2 + \nabla^2 \psi + \eta$

Boundary conditions: $\psi(0, z) = \begin{cases} 0 & , \mathcal{F}(z) > \mathcal{F}_T; \\ (1 - \frac{\mathcal{F}}{\mathcal{F}_T} e^{-z/\lambda}) \sqrt{1 - T(0, z)/T_c} & , \mathcal{F}(z) < \mathcal{F}_T. \end{cases}$

Introducing fluctuations at $t = 0$ (Volovik, 2000)[†]:
 $\psi(t = 0) = \kappa z$



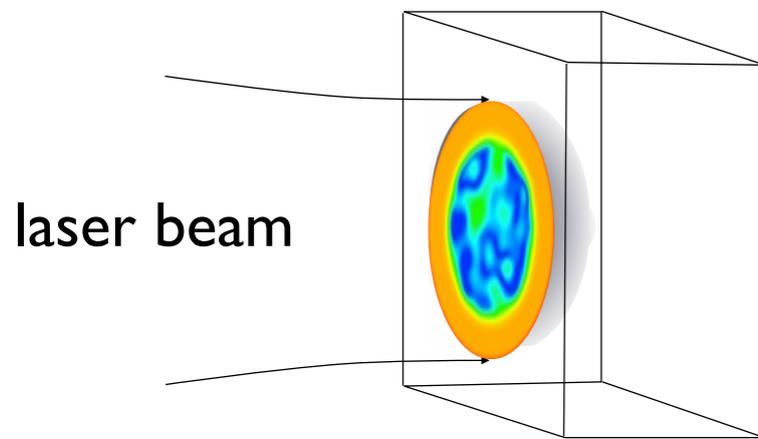
Much better

[†] G. E. Volovik, *Physica B* **280** 122-127 (2000).

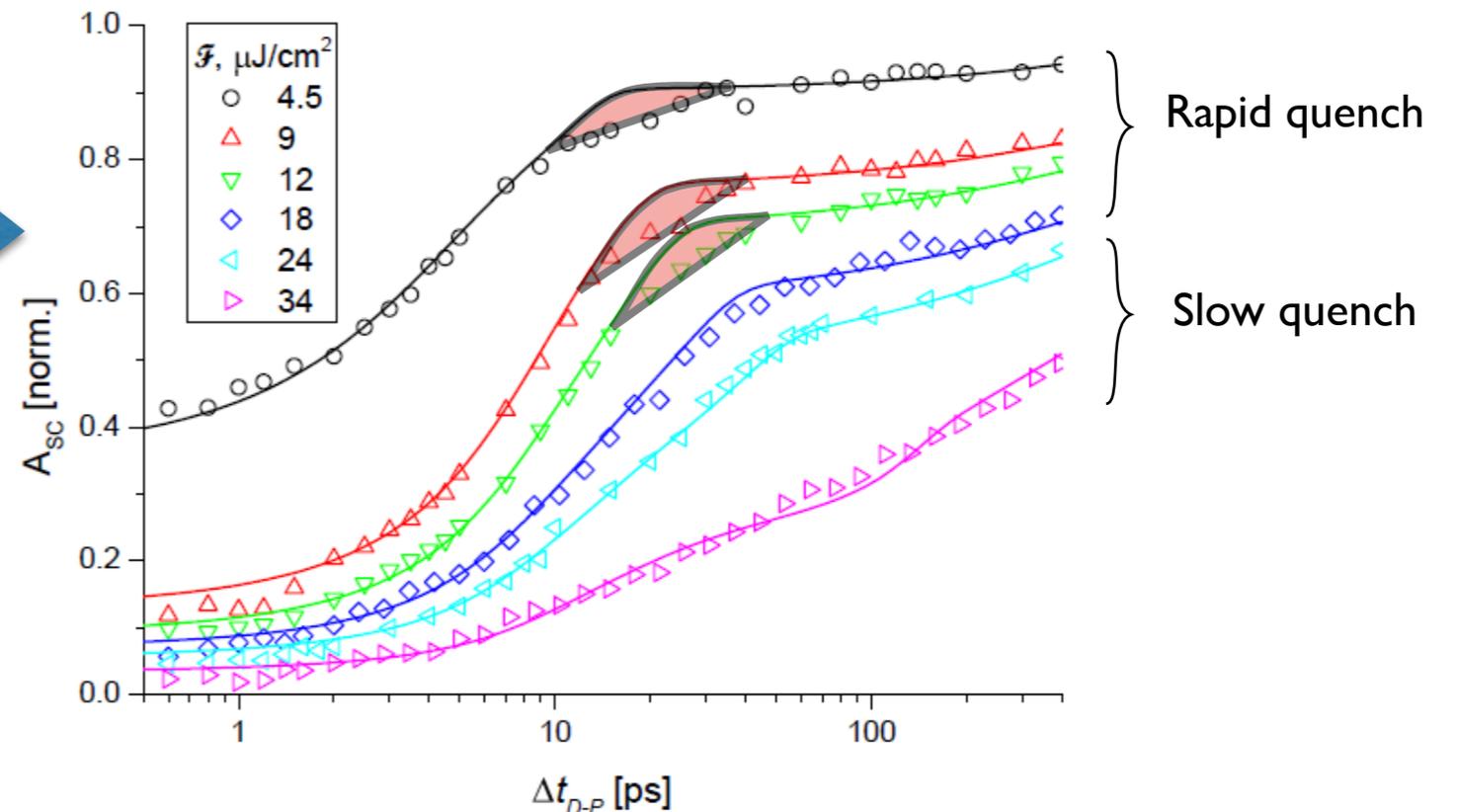
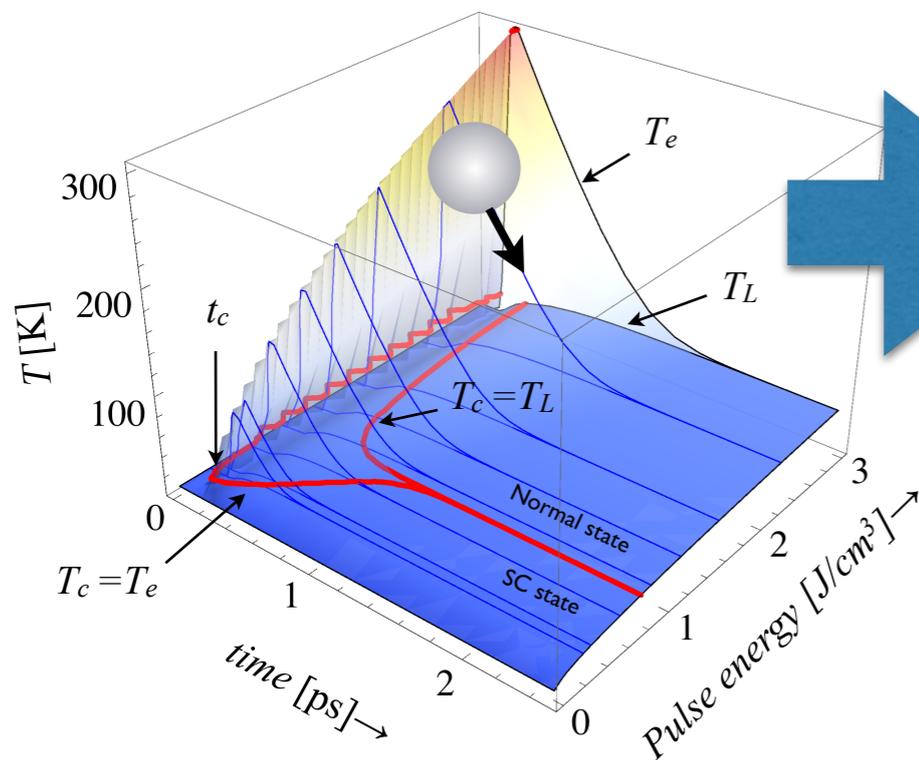
Kibble-Zurek mechanism: Evidence for vortex formation and annihilation on 10 ps timescale

Laser spot size: $d = 60\mu\text{m}$

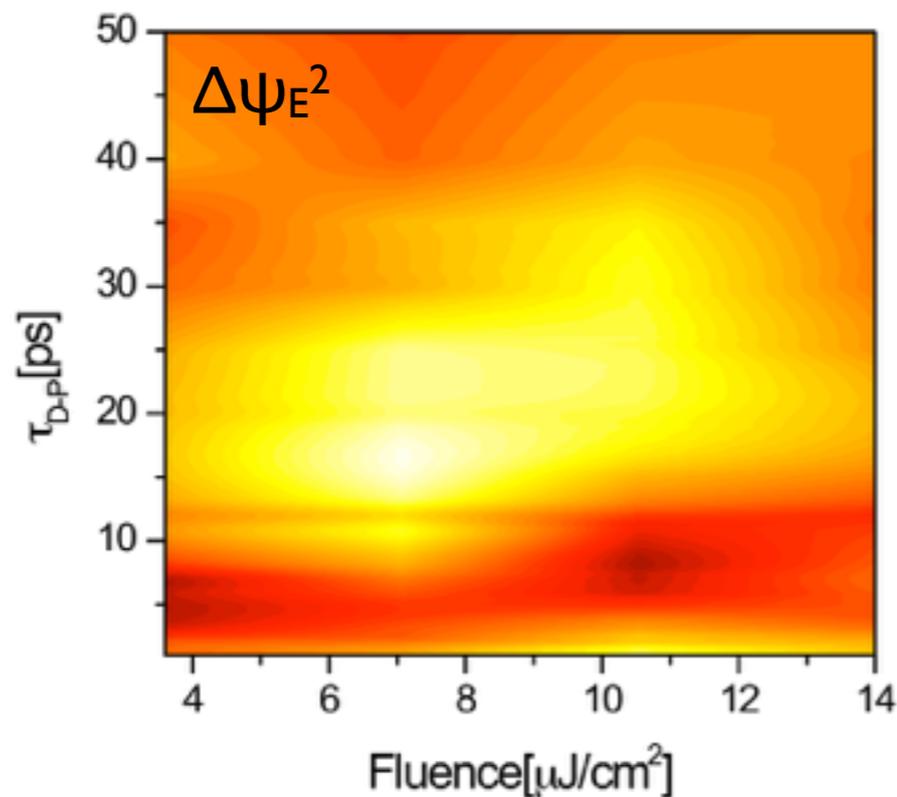
Coherence length: $\xi_{||} \simeq 2\text{nm}$



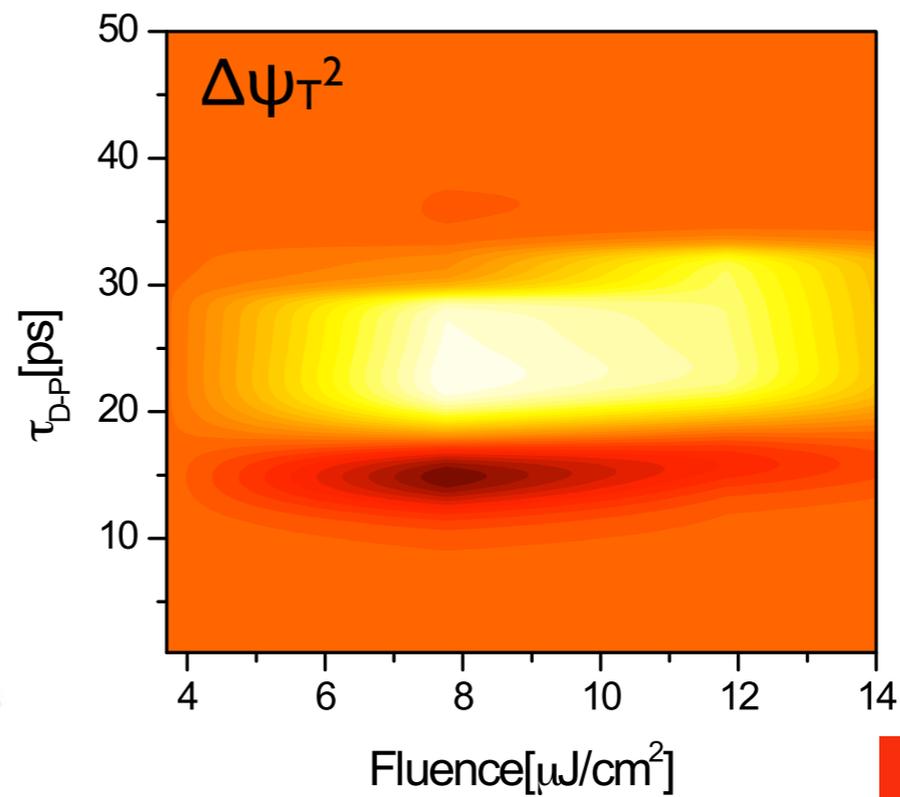
Regions are causally unconnected and evolve independently after the quench which causes the formation of topological defects.



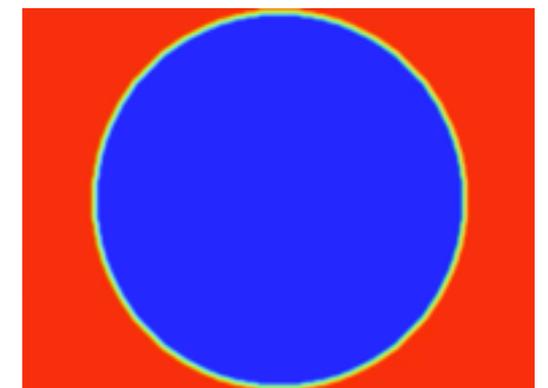
Vortices created in the quench annihilate on a timescale of 10-30 ps



Experiment

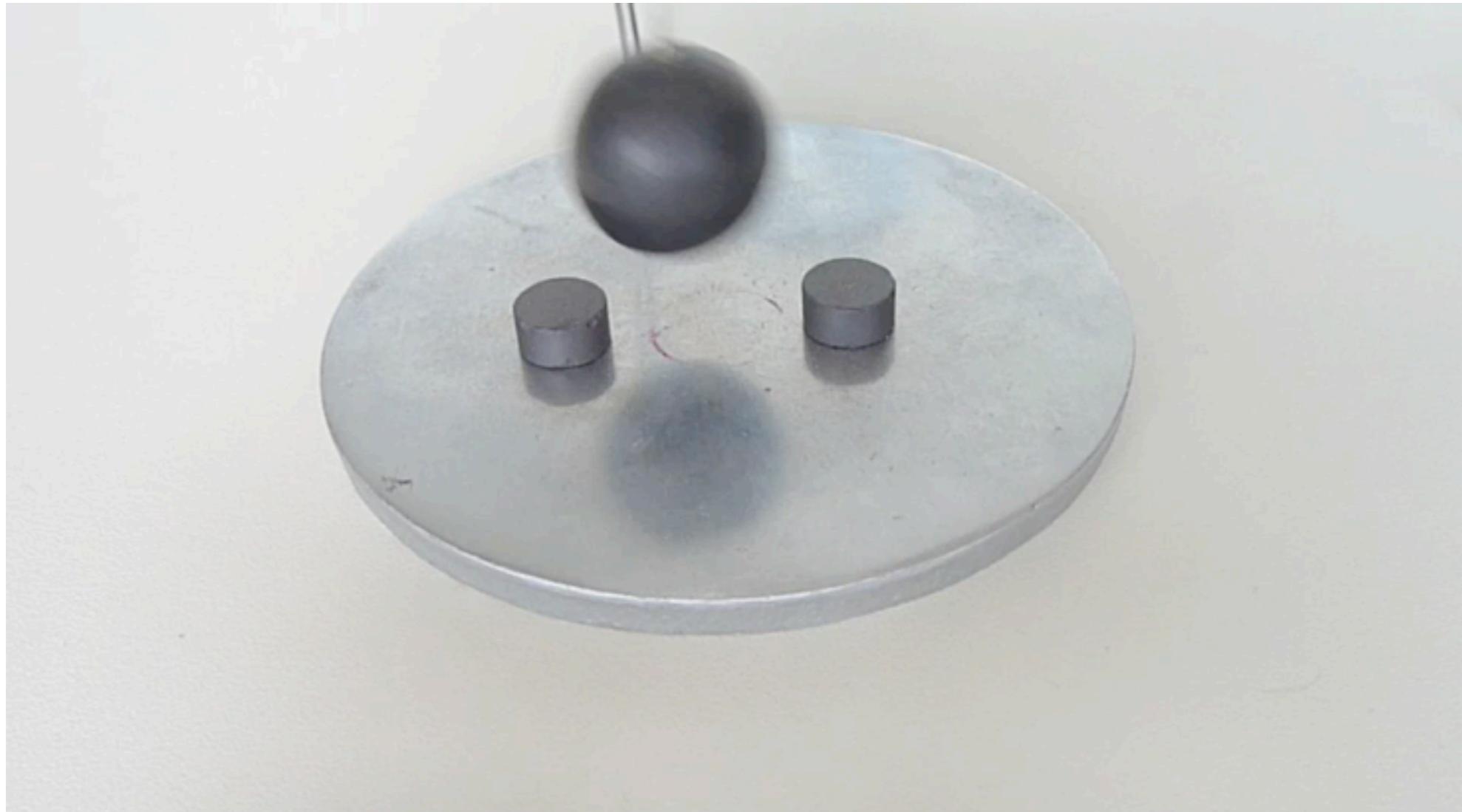


Theory
calculation



Laser spot

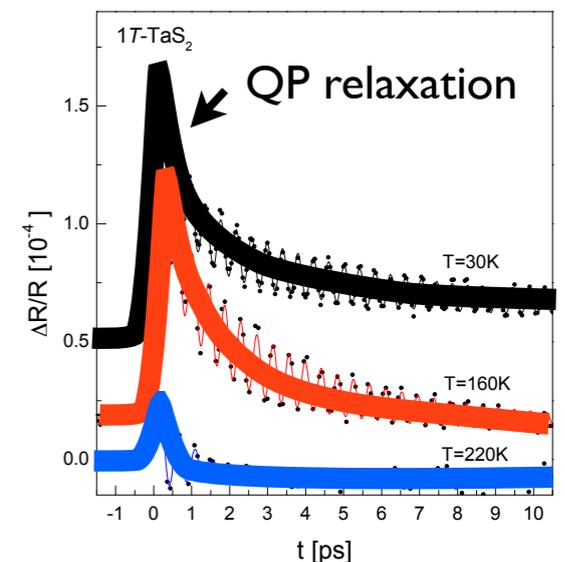
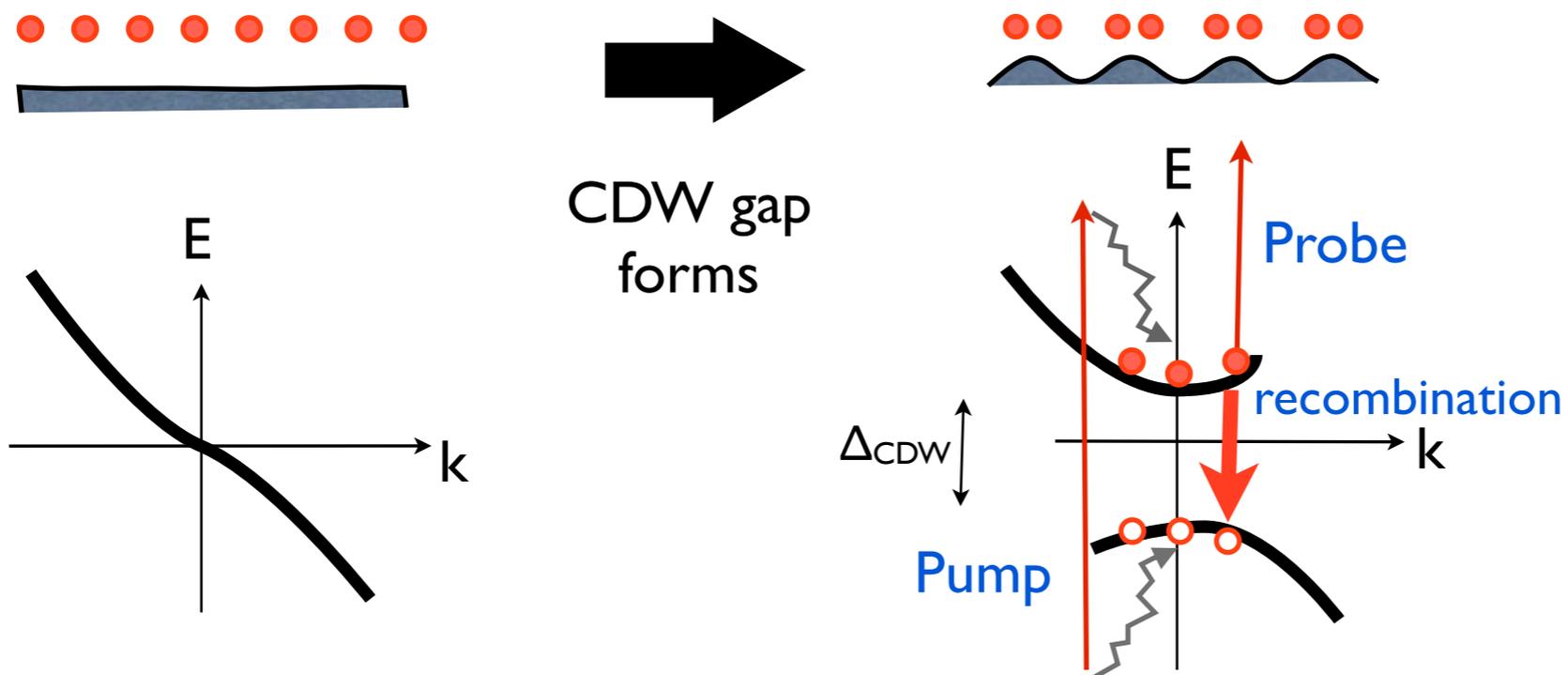
CDWs



For $\phi \ll 2\pi/\omega_{AM}$, $\psi(t) \simeq A(t)$

Detection of the onset of order in CDW systems: The elementary excitations

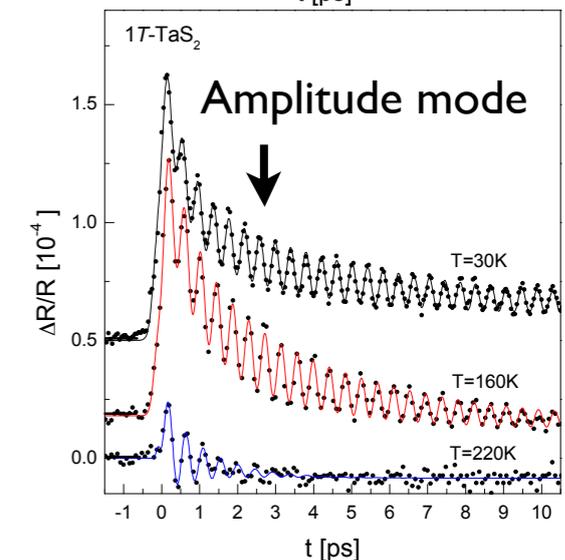
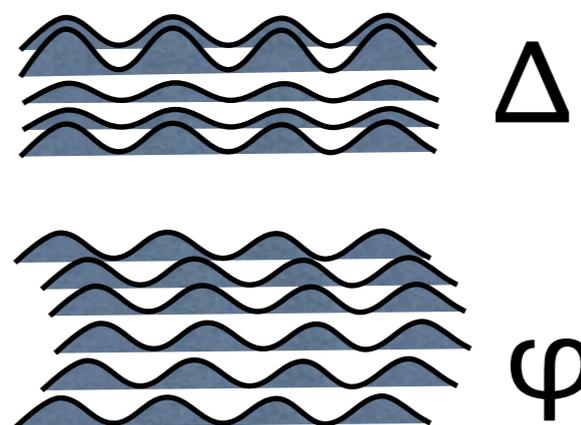
1. Detection of the gap through quasiparticle (fermionic) excitations



2. Collective mode (bosonic) excitations

The amplitude and phase modes

$$\Psi = \Delta e^{i\varphi}$$



Demsar et al., PRL **83**, 800 (1999).
 Demser, J., et al, PRB **66**, (2002).
 Demser, et al., PRB **82**, 4918 (1999).
 Kusar et al, PRL **101**, 227001 (2008)
 Yusupov et al., PRL **101**, 246402 (2008).

Coherent control and data processing using the Amplitude mode and Grover's superpositional search algorithm

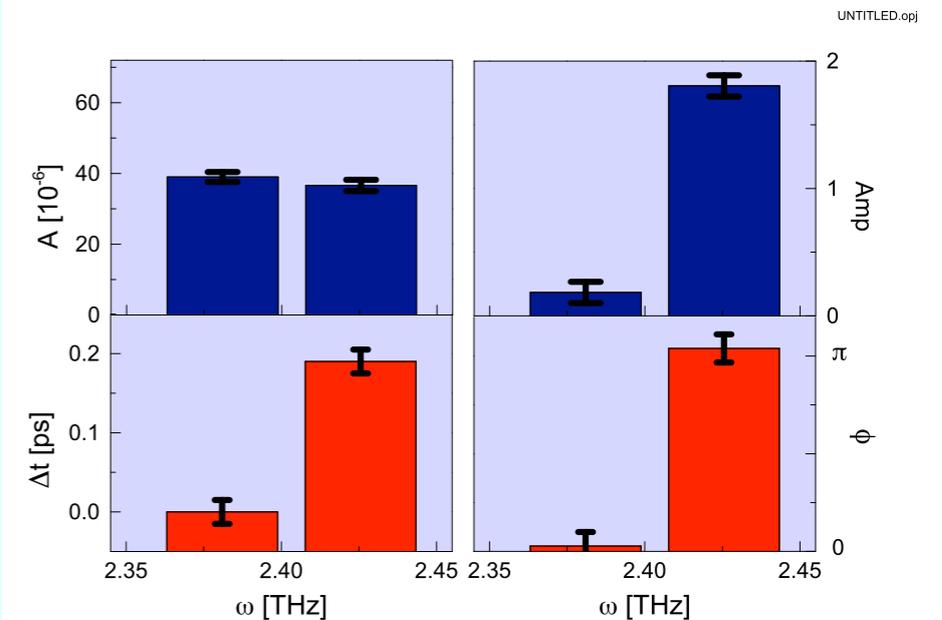
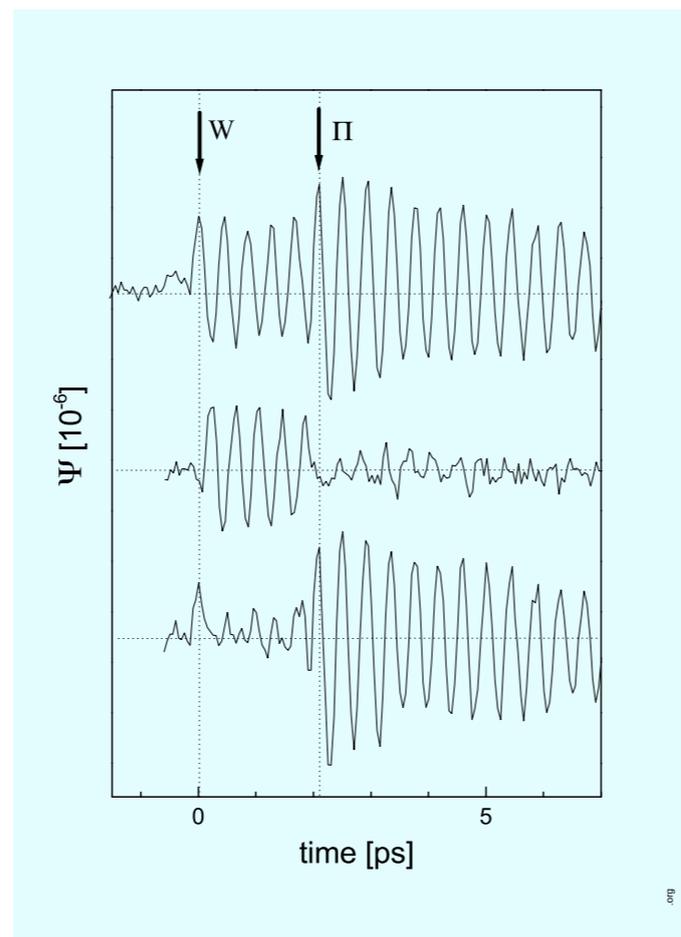
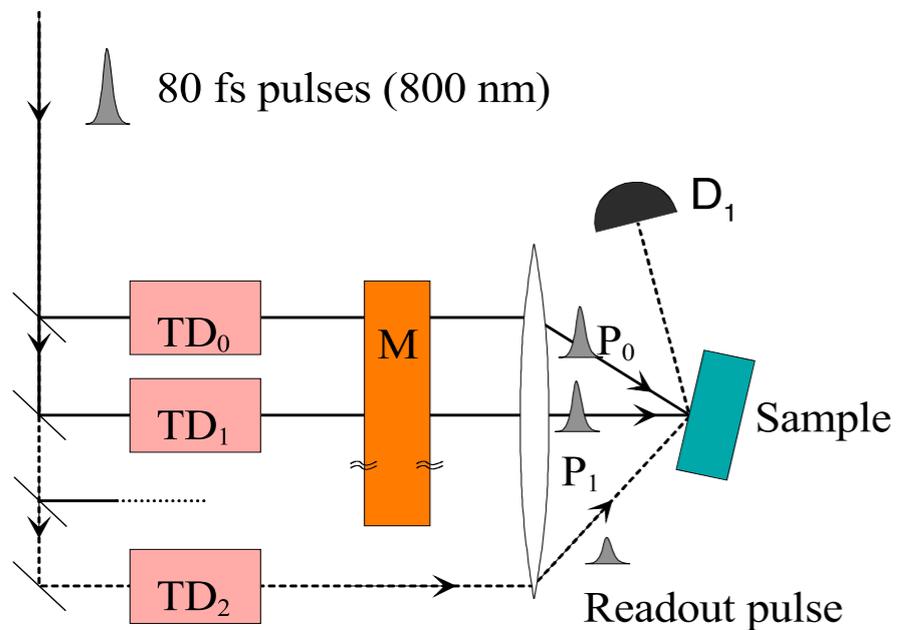
APPLIED PHYSICS LETTERS

VOLUME 80, NUMBER 5

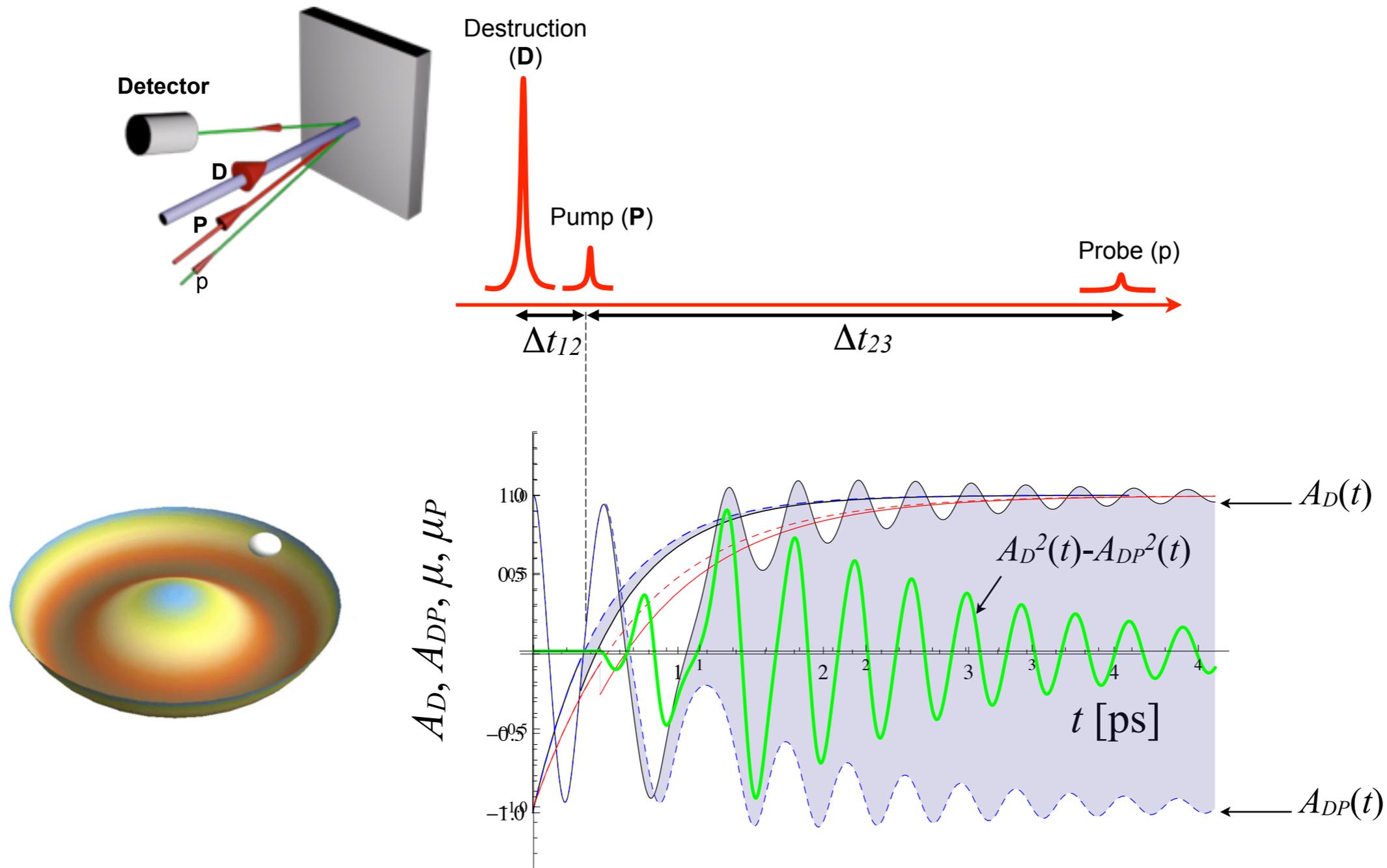
4 FEBRUARY 2002

Femtosecond data storage, processing, and search using collective excitations of a macroscopic quantum state

D. Mihailovic,^{a)} D. Dvorsek, V. V. Kabanov, and J. Demsar
Jozef Stefan Institute, Jamova 39, 1000 Ljubljana, Slovenia

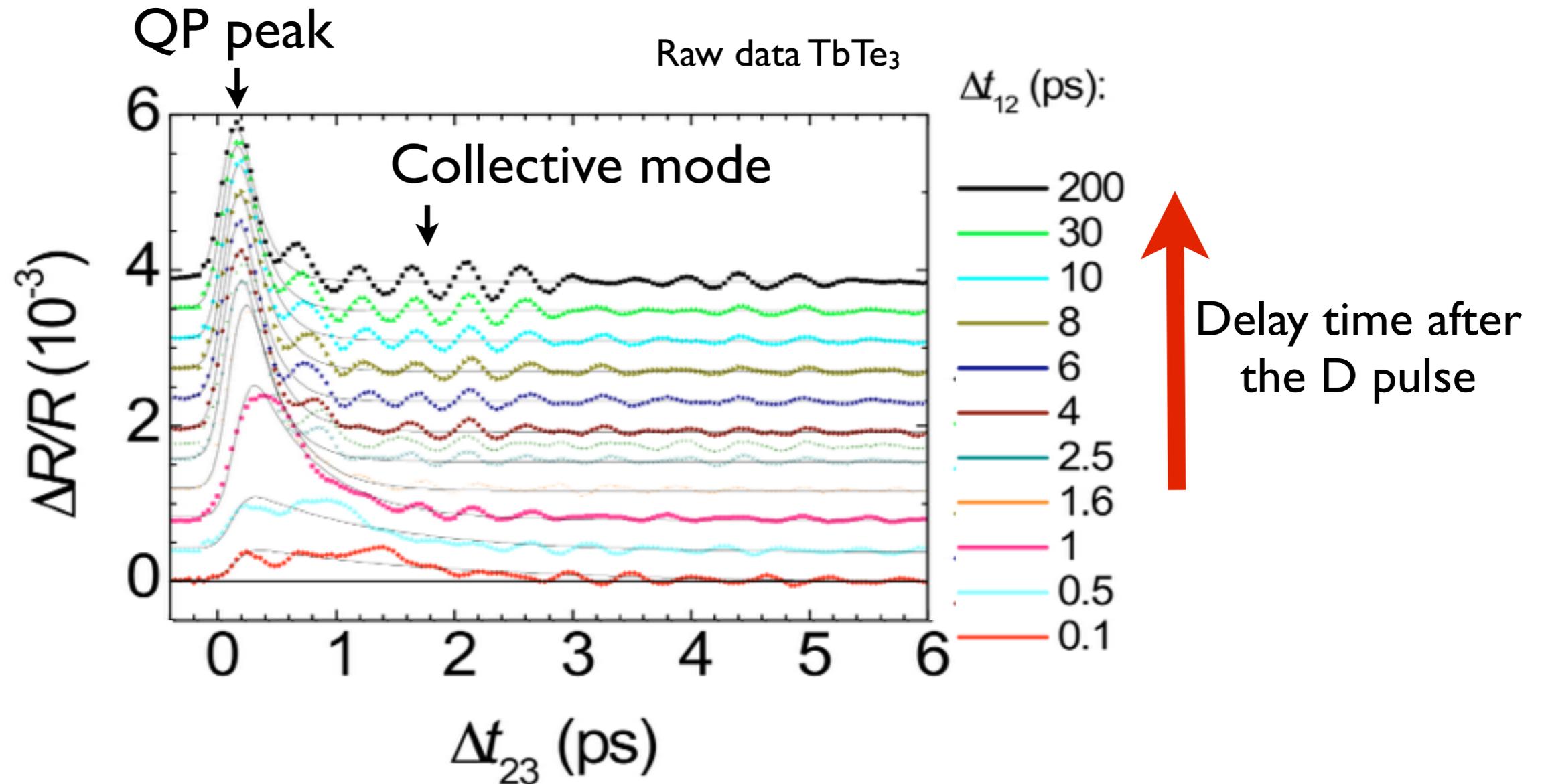


The calculated optical response of the collective mode after a quench

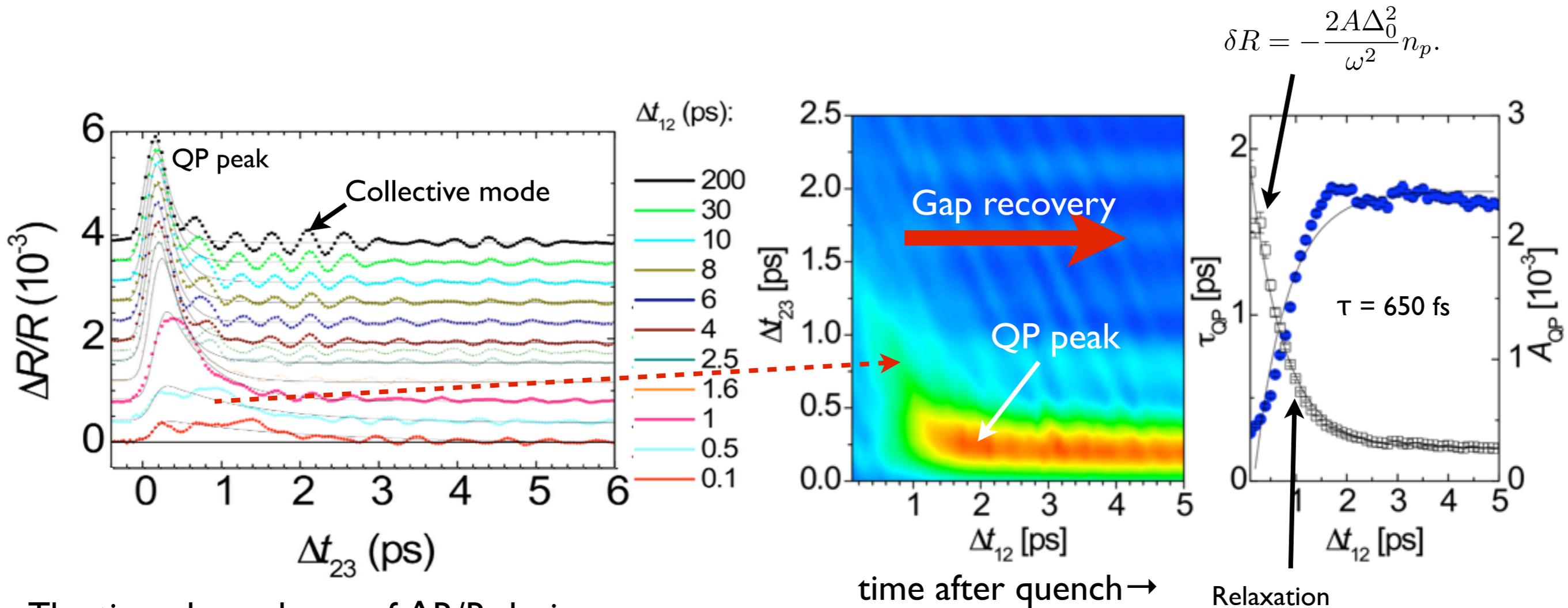


The reflectivity, $\Delta R(t) \propto \left(\frac{\partial R}{\partial \epsilon} \right) \Delta \epsilon \propto \int [A_{DP}^2(t, \mathbf{r}, \Delta t_{12}) - A_D^2(t, \mathbf{r})] e^{-z/\lambda} d^3 \mathbf{r}$.

The transient reflectivity $\Delta R/R$ after a quench at $\Delta t_{12}=0$



Quasi-particle (Fermion) kinetics: gap recovery



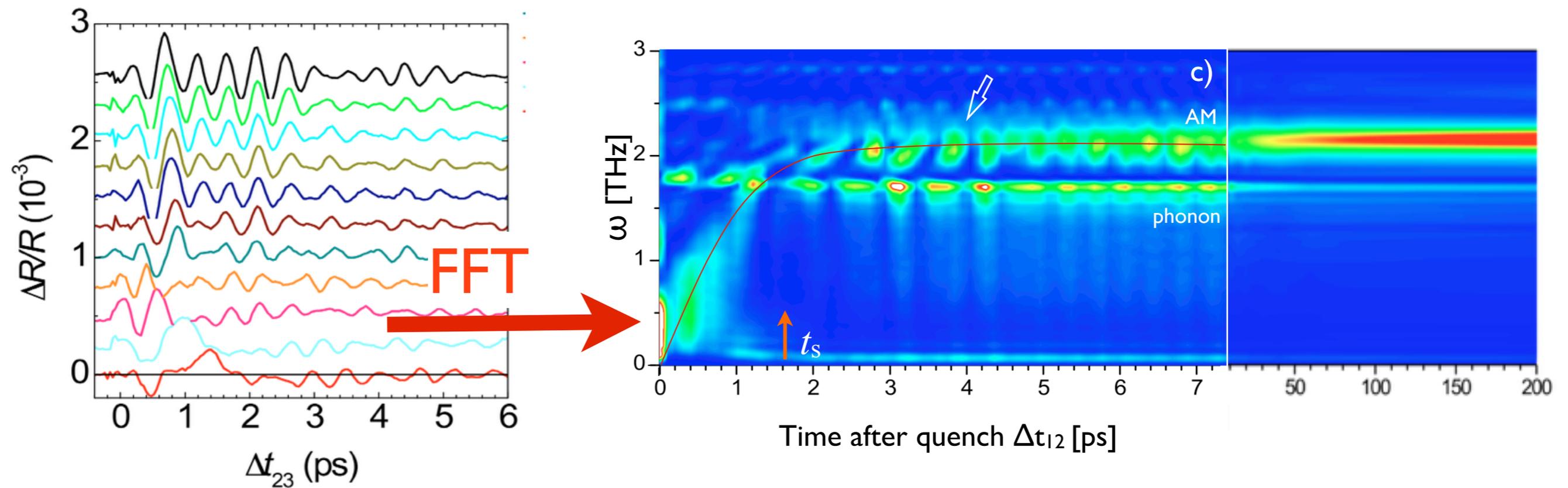
The time-dependence of $\Delta R/R$ during the recovery of ψ :

$$\delta R/R \propto \frac{1/(|\psi(t)| + T(t)/2)}{1 + B\sqrt{2T(t)/|\psi(t)|}\exp[-|\psi(t)|/T(t)]}$$

Relaxation time recovery

$$\tau \propto \frac{1}{\Delta}$$

The collective mode spectrum as a function of time after quench



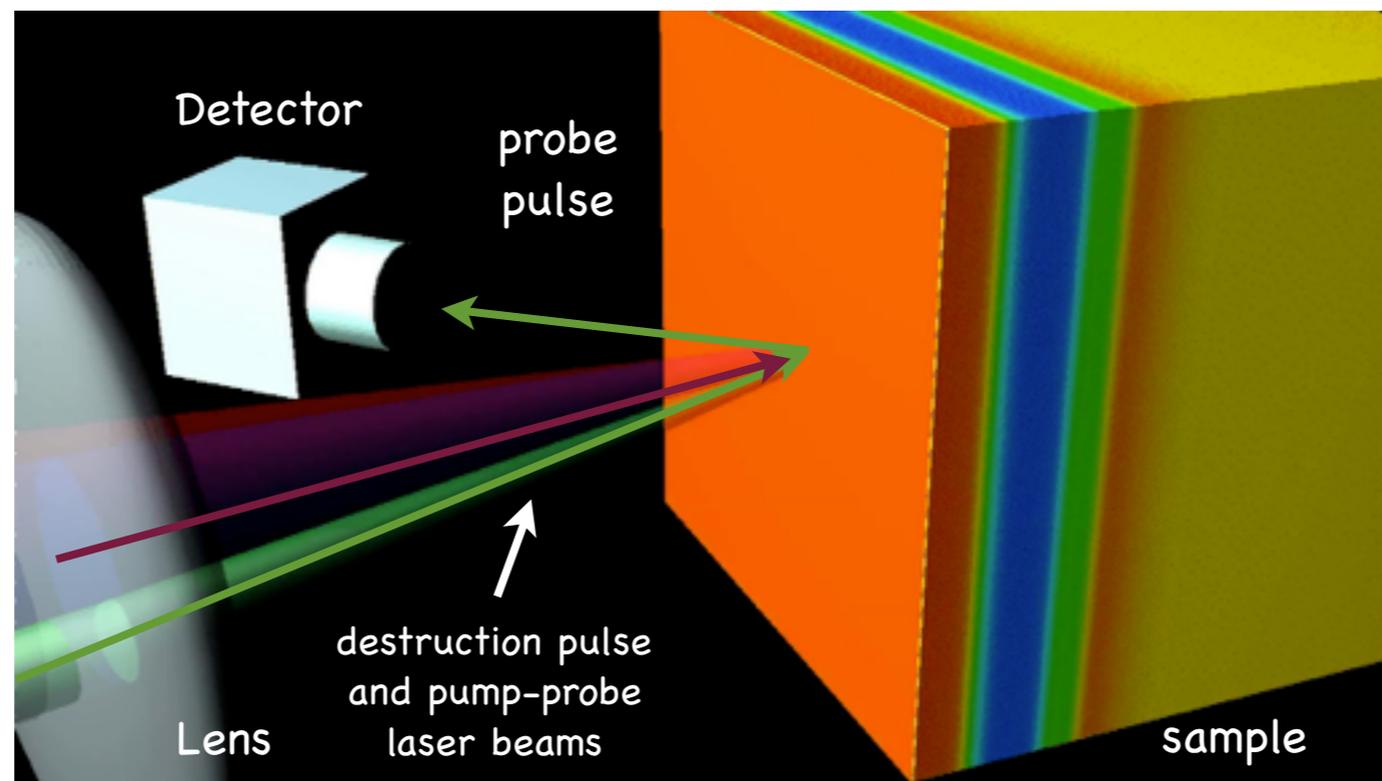
The most obvious feature:
oscillations of intensity of the collective mode

Order parameter calculation

The eq. of motion:

$$\frac{1}{\omega_0^2} \frac{\partial^2}{\partial t^2} A + \frac{\alpha}{\omega_0} \frac{\partial}{\partial t} A - (1 - \eta) A + A^3 - \xi^2 \frac{\partial^2}{\partial z^2} A = 0$$

Calculated $A(z,t)$ after quench:



Experimental parameters:

$$\tau_{QP} = 650 \text{ fs}$$

$$\omega_0/2\pi = 2.18 \text{ THz}$$

$$\eta = 2$$

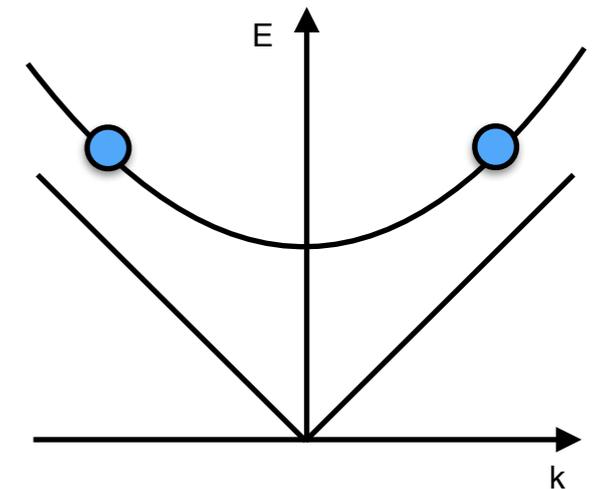
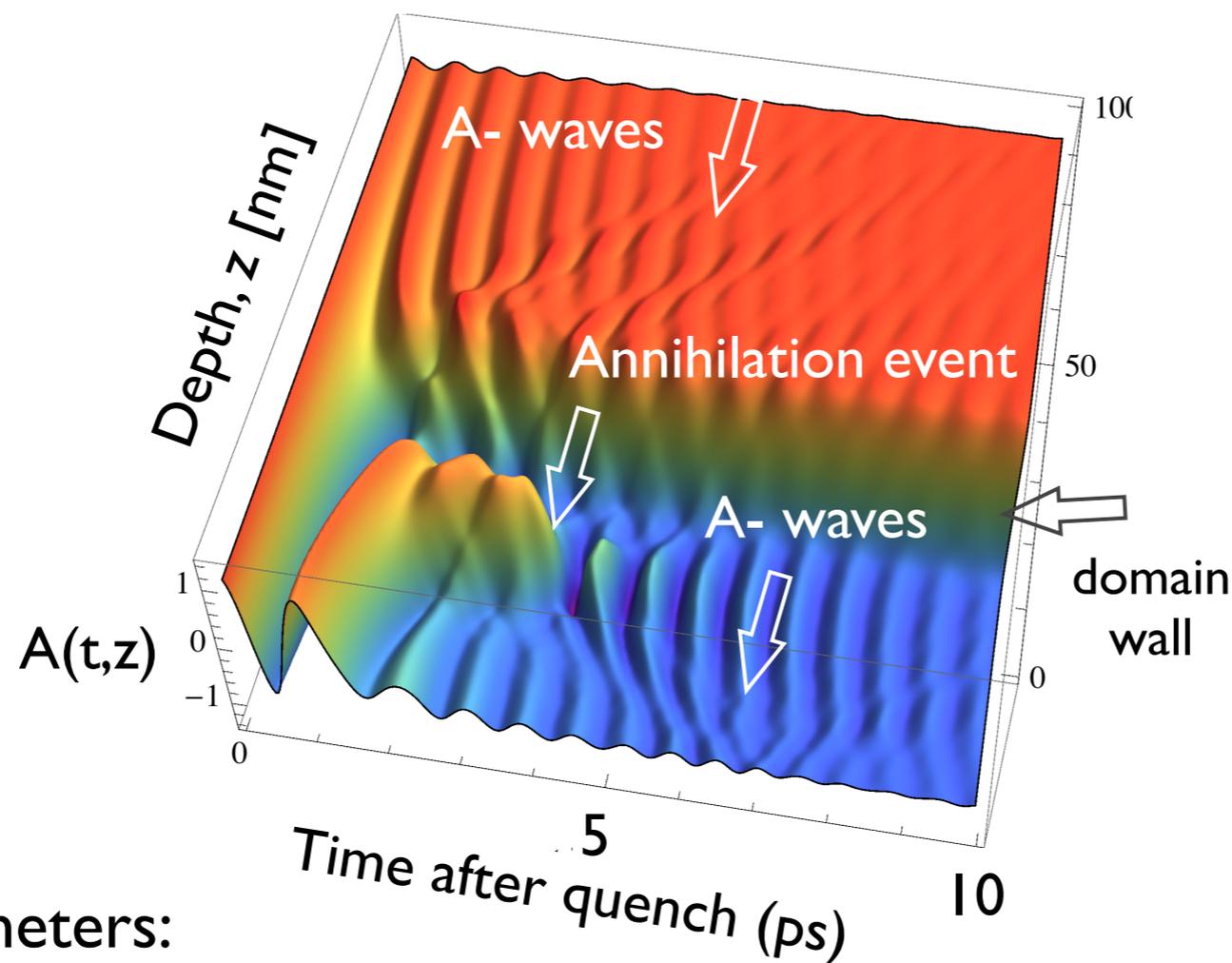
$$\alpha = 0.1$$

Order parameter calculation

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$$\frac{1}{\omega_0^2} \frac{\partial^2}{\partial t^2} A + \frac{\alpha}{\omega_0} \frac{\partial}{\partial t} A - (1 - \eta) A + A^3 - \xi^2 \frac{\partial^2}{\partial z^2} A = 0$$

Calculated $A(z,t)$ after quench:



Experimental parameters:

$$\tau_{QP} = 650 \text{ fs}$$

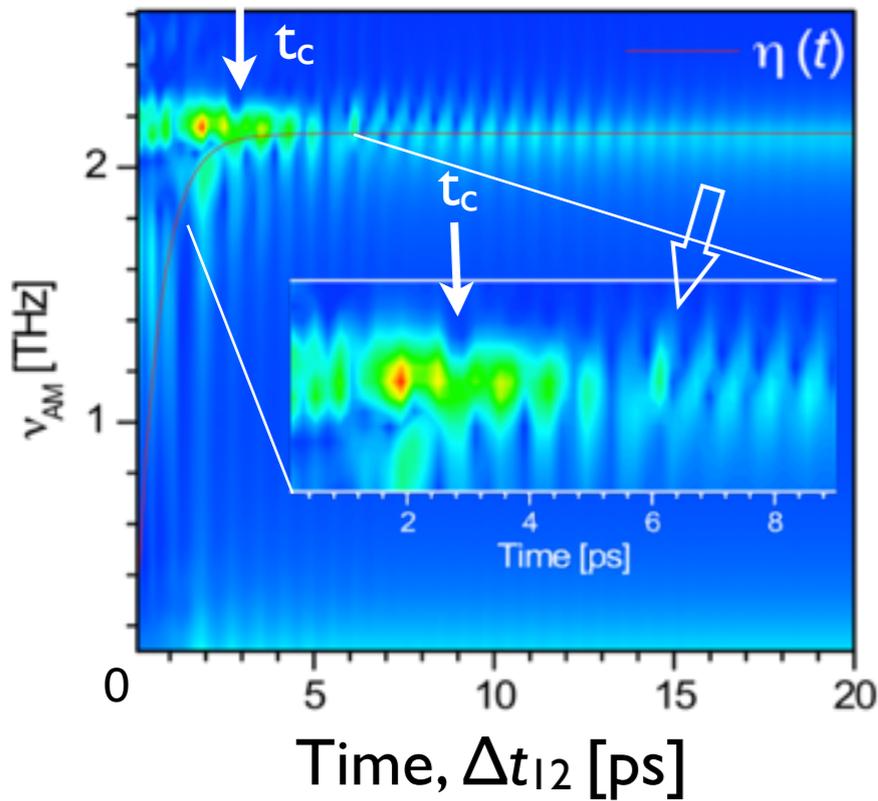
$$\omega_0/2\pi = 2.18 \text{ THz}$$

$$\eta = 2$$

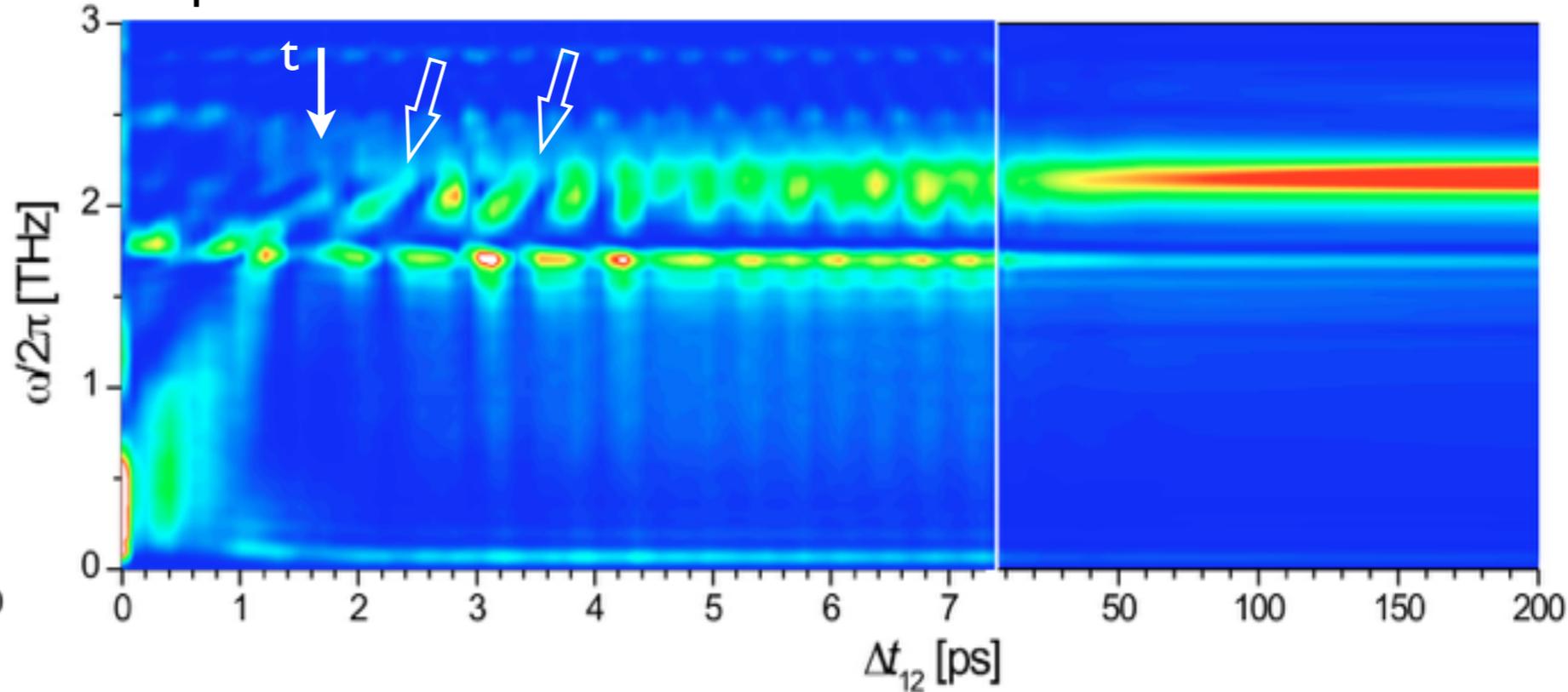
$$\alpha = 0.1$$

Order parameter dynamics: theory vs. expt.

Theory



Experiment

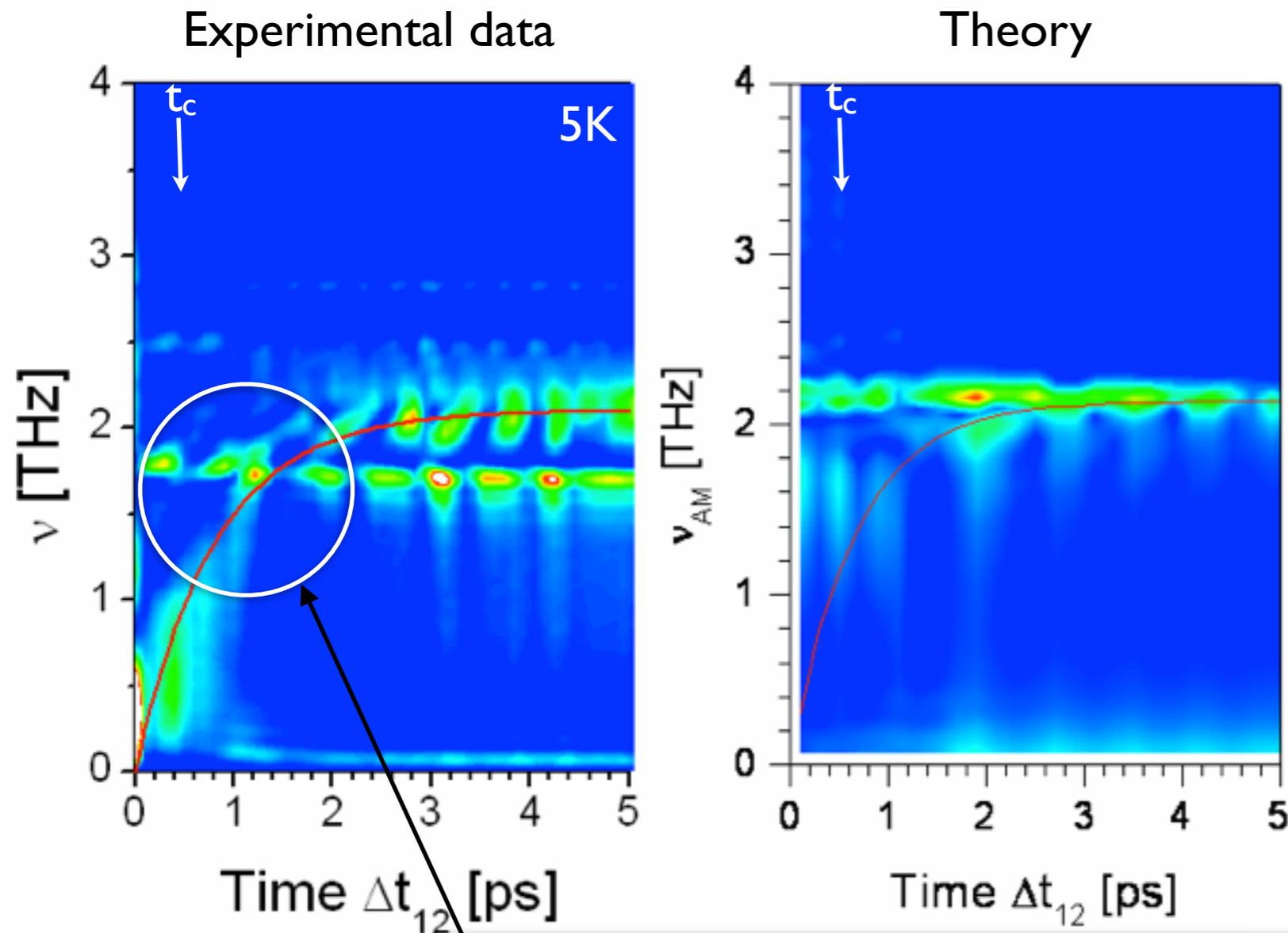


Theory predictions:

- Oscillations of Δ or $|\Psi|$
- Critical slowing down
- Collective mode softening
- Domain formation
- Ψ Higgs waves +

The first three picoseconds:

Critical dynamics as $t \rightarrow t_c$

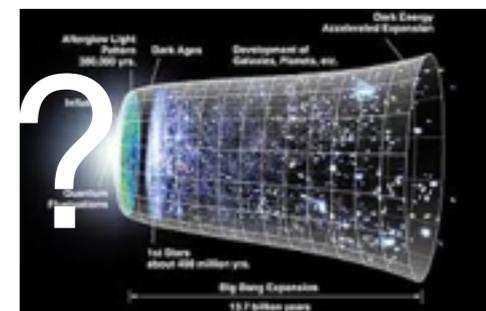


ISSUES NOT ADDRESSED:

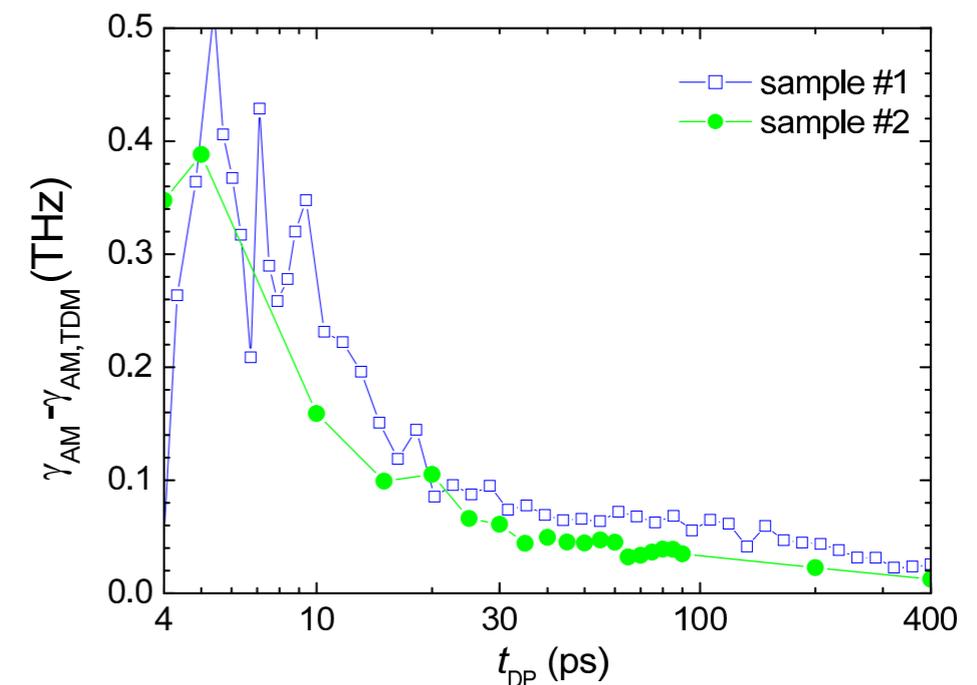
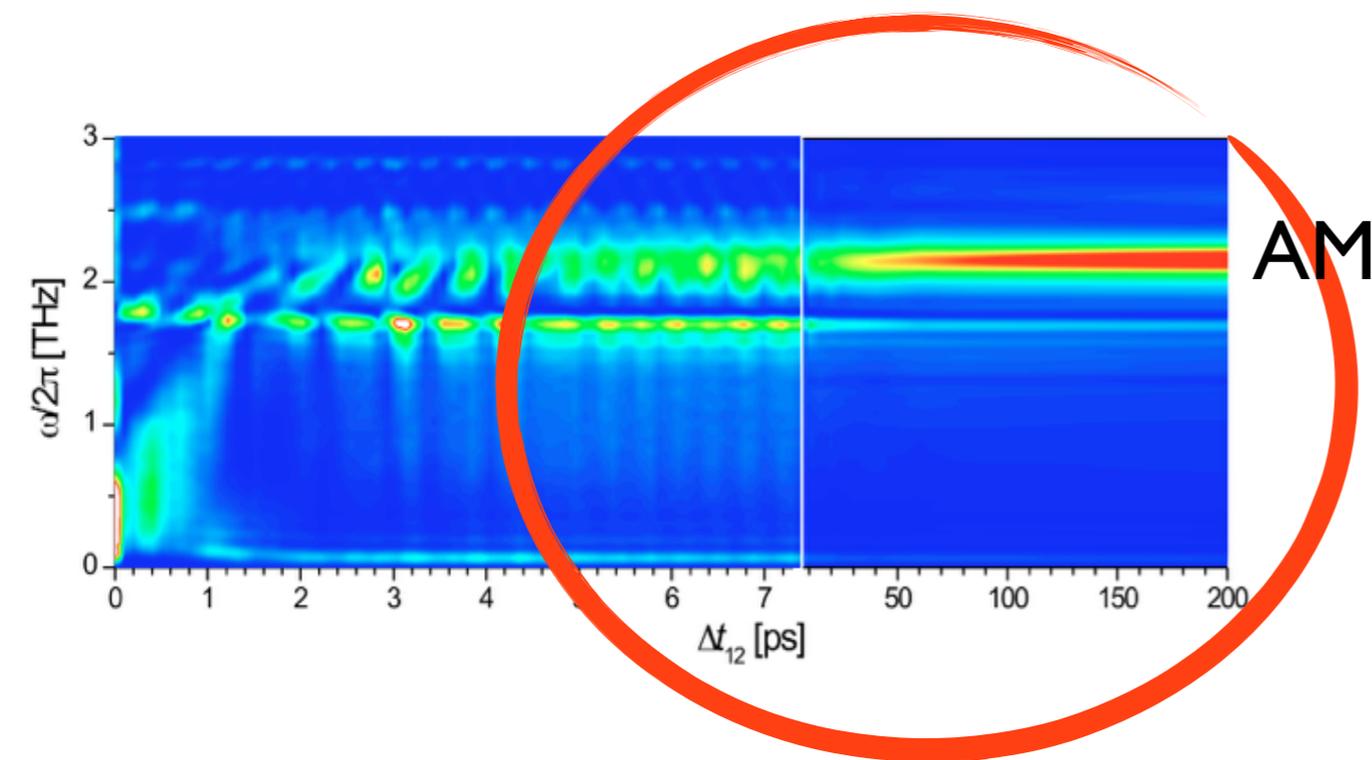
- Response selection rules: AM has A symmetry only $t > t_c$
- coupling to other pre-existing collective modes (phonons)
- initial energy relaxation
- fluctuation phenomena

Coupling of AM to a collective mode from a previous eon!

(Different from Penrose's eons. More like Littlewood-Varma-Klein NbSe₂ resonance)



Incoherent topological defect dynamics: collective mode broadening for $\Delta t_{12} > 7$ ps

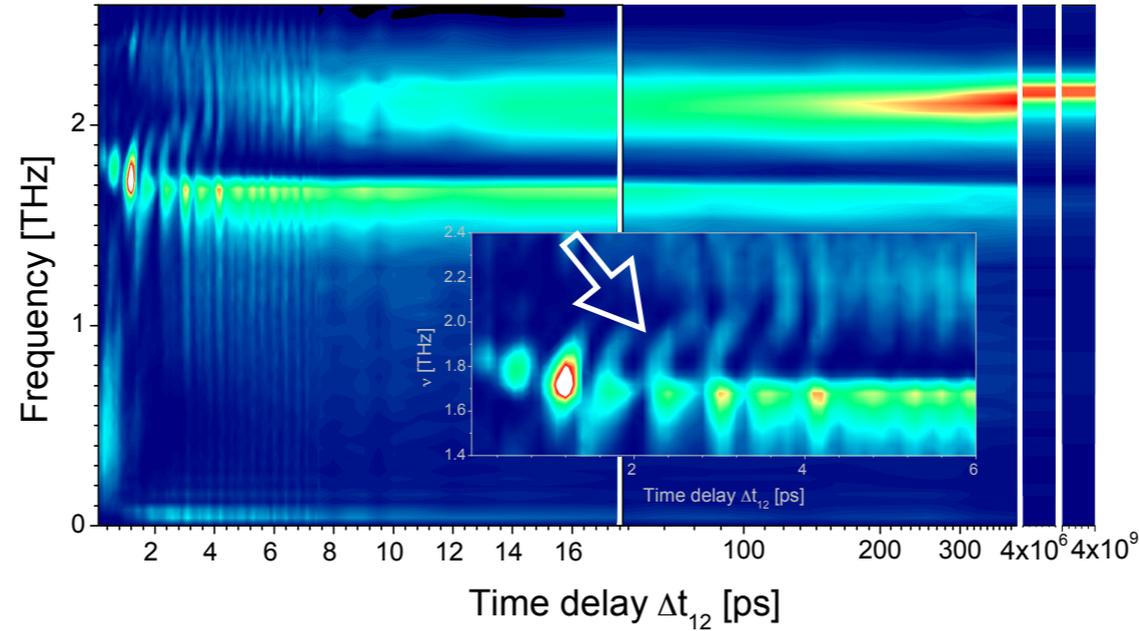
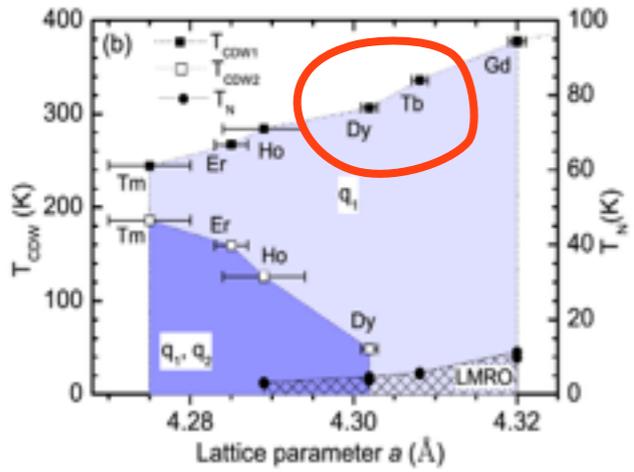


The collective mode linewidth reflects the presence of domain walls

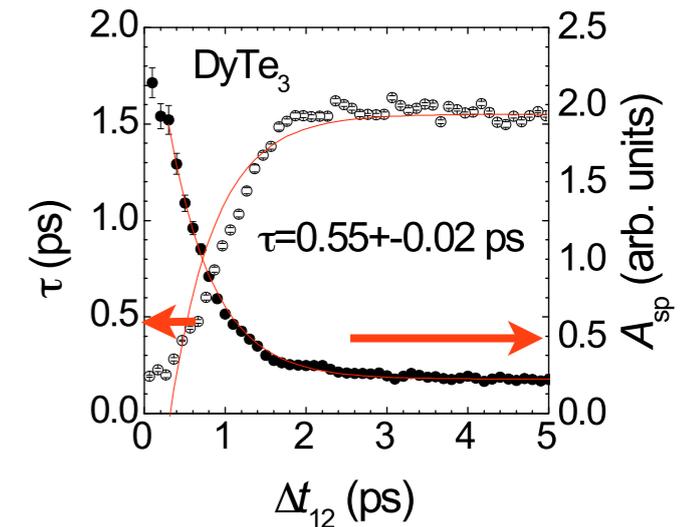


Related systems show (not so subtle) differences

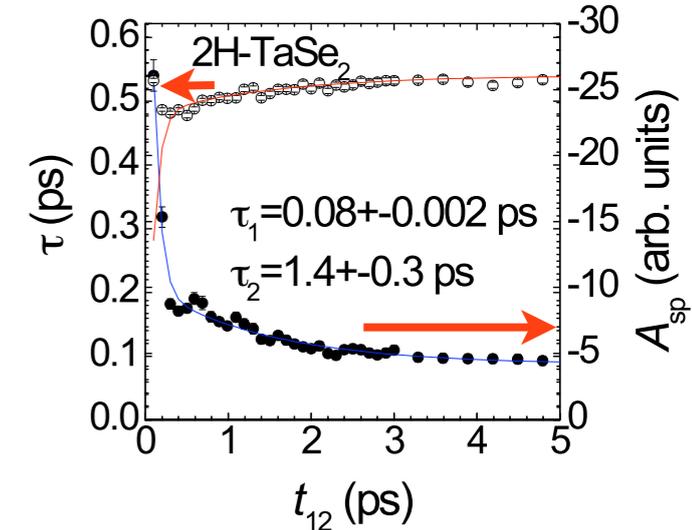
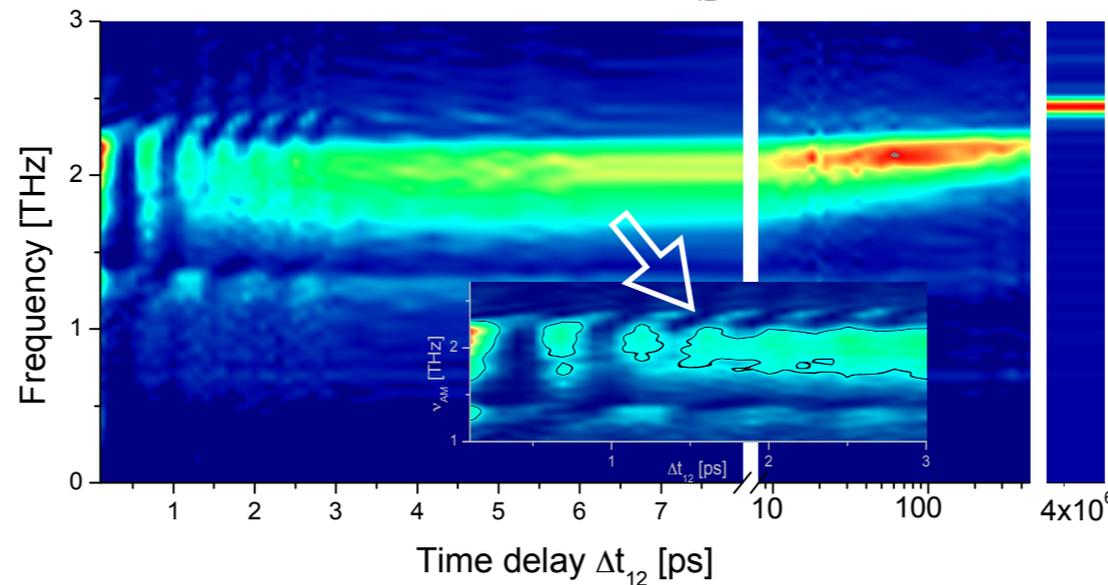
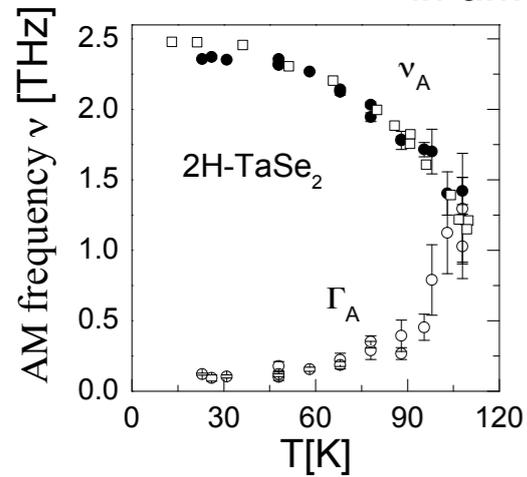
DyTe₃ Very similar to TbTe₃



Gap closure (QP dynamics)

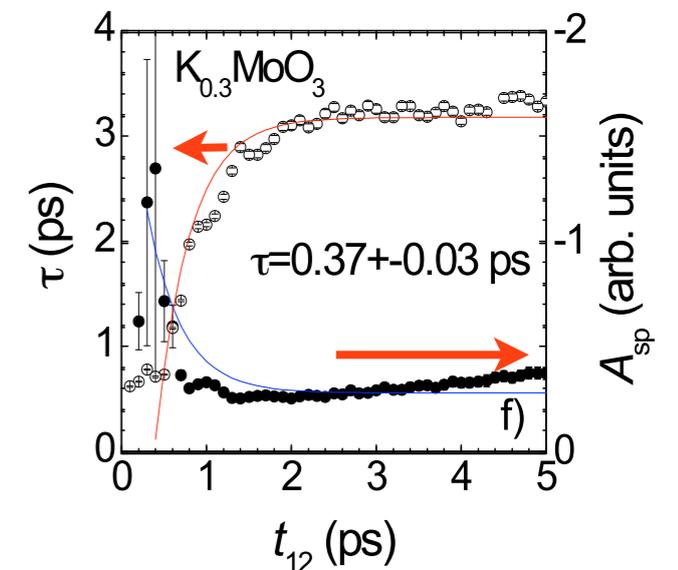
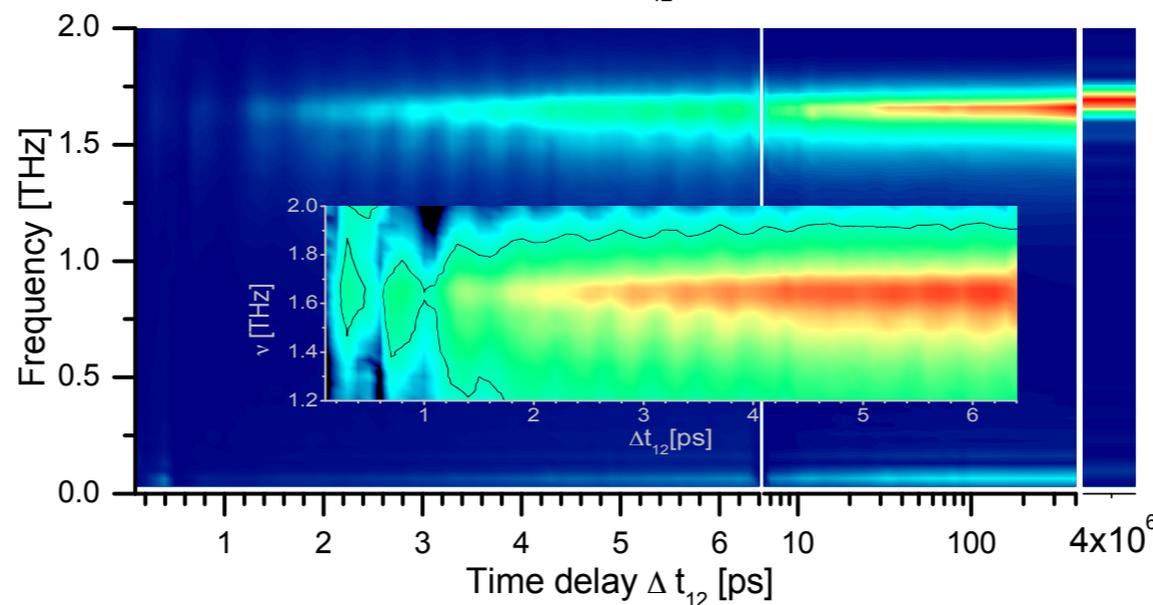


2H-TaSe₂ 2D system
No soft mode
in time



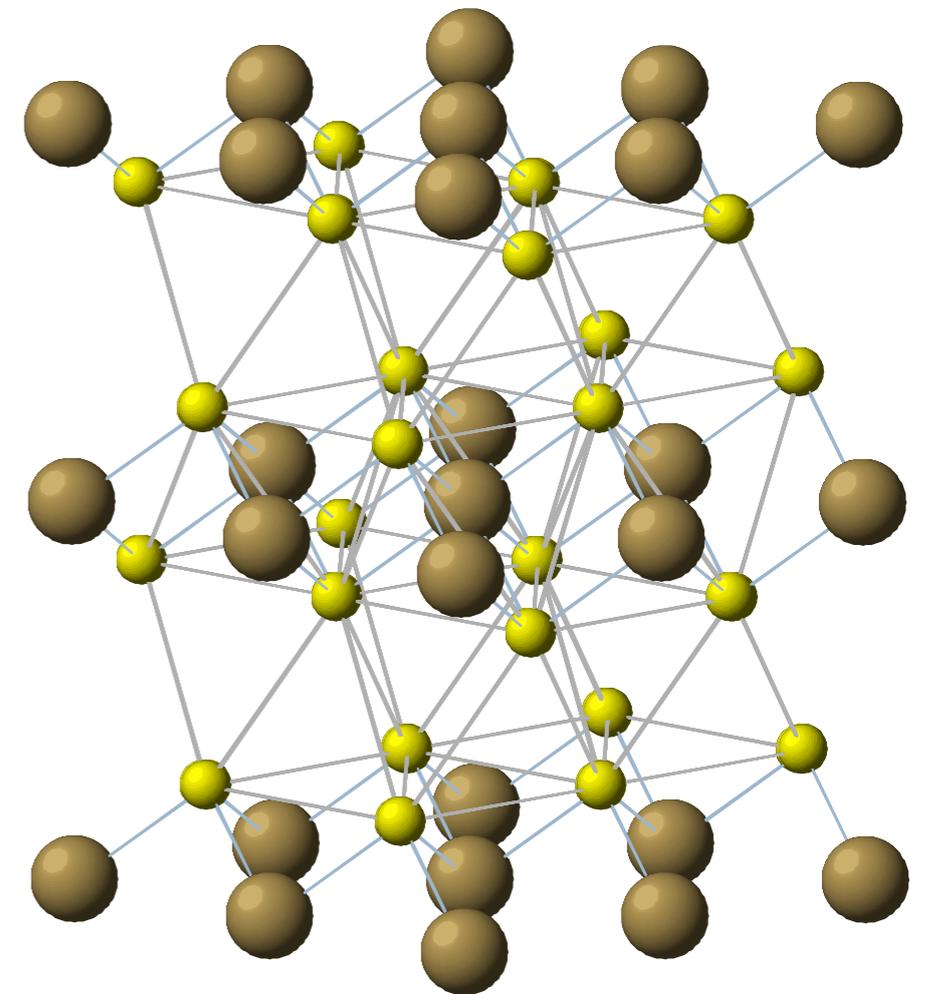
K_{0.3}MoO₃

1D chains
only 10% softening of the AM





The trajectory to a hidden state in *I*T-TaS₂

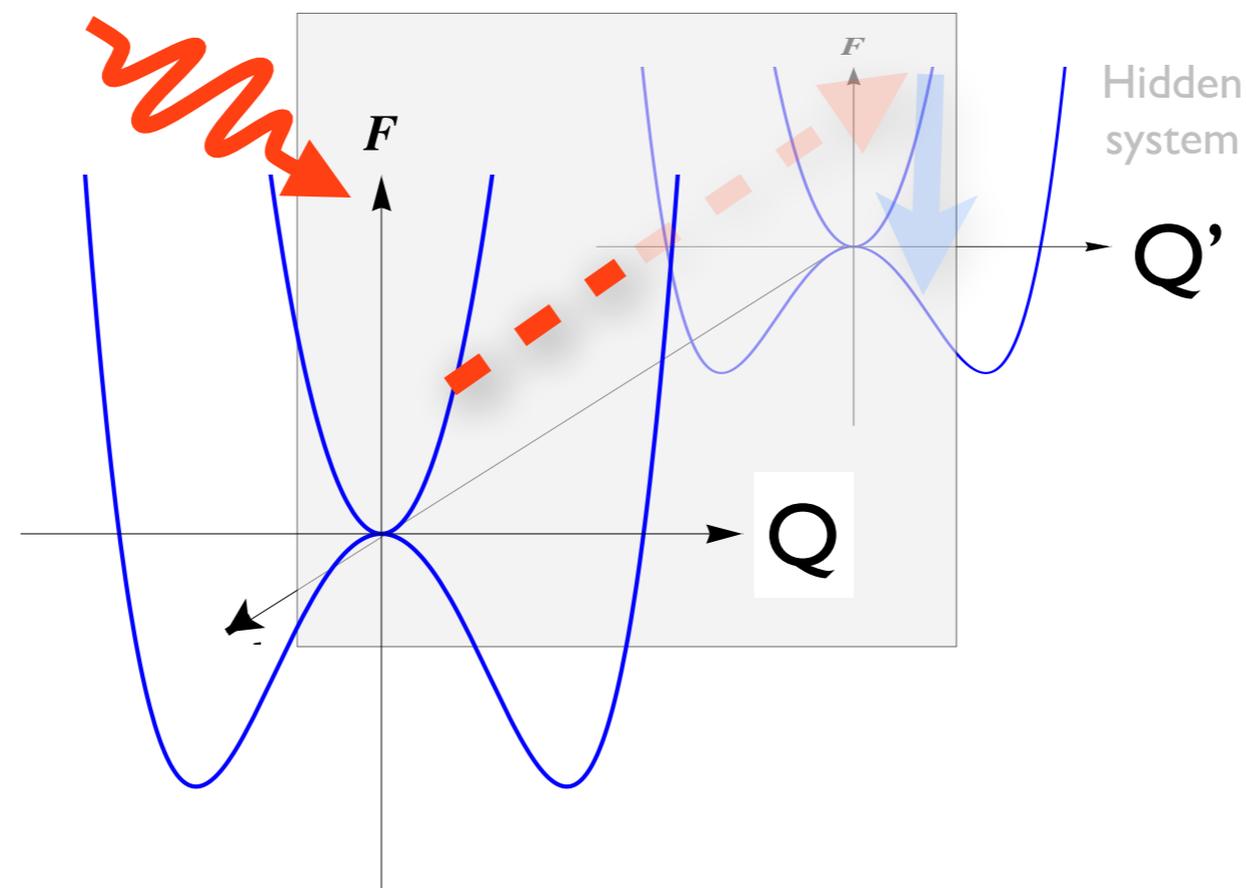


*I*T-TaS₂

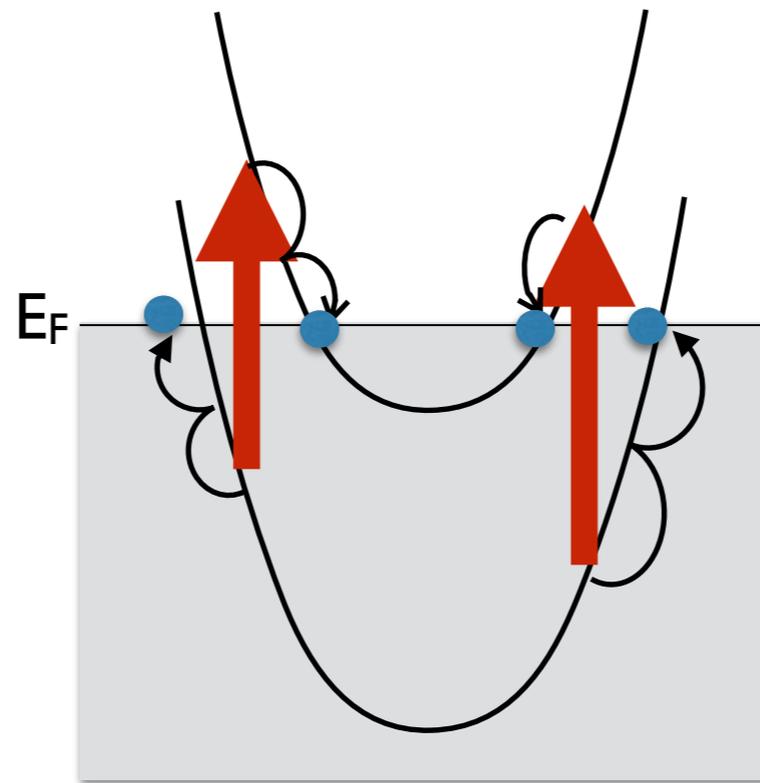
What is a hidden state?

It is a state of matter which cannot be reached under ergodic conditions, by slowly changing T , P , B -field, etc.

Switching to a hidden state can be achieved by a **non-thermal process** which occurs under highly non-equilibrium conditions of the underlying vacuum

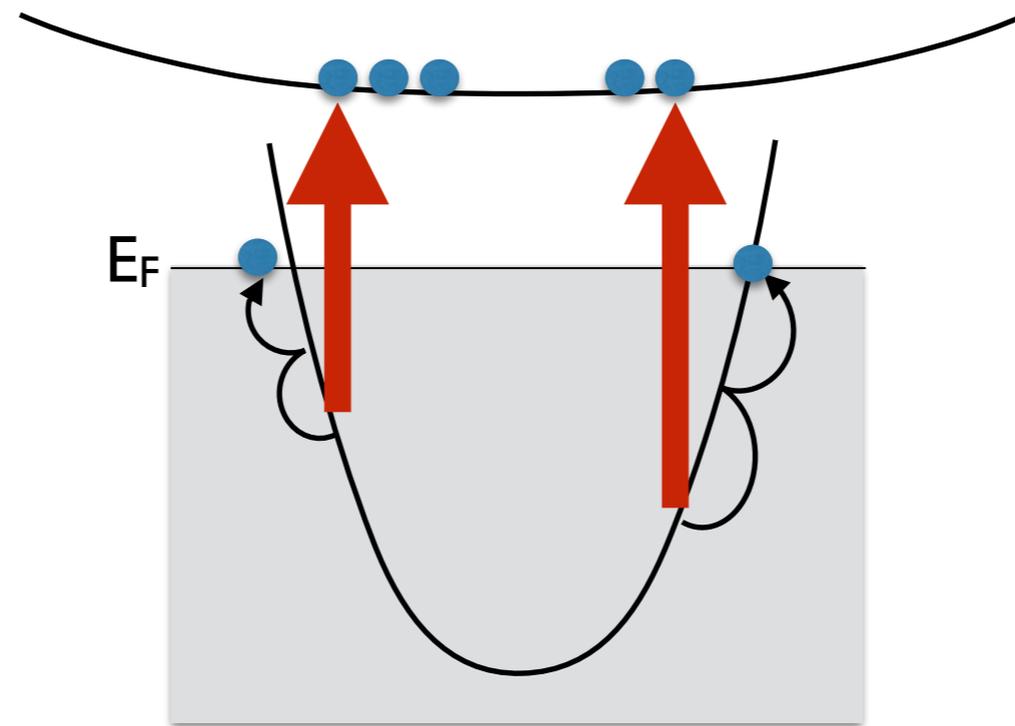


The importance of e-h (a)symmetry for creating photoinduced states

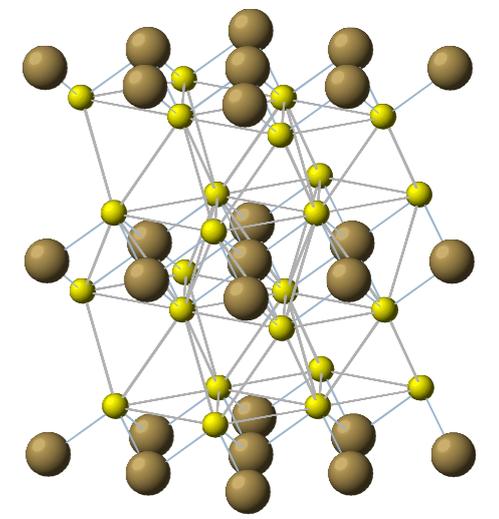


Just heating ($T_e^* = T_L^* = \dots$).
No doping.

The importance of e-h (a)symmetry for creating photoinduced states

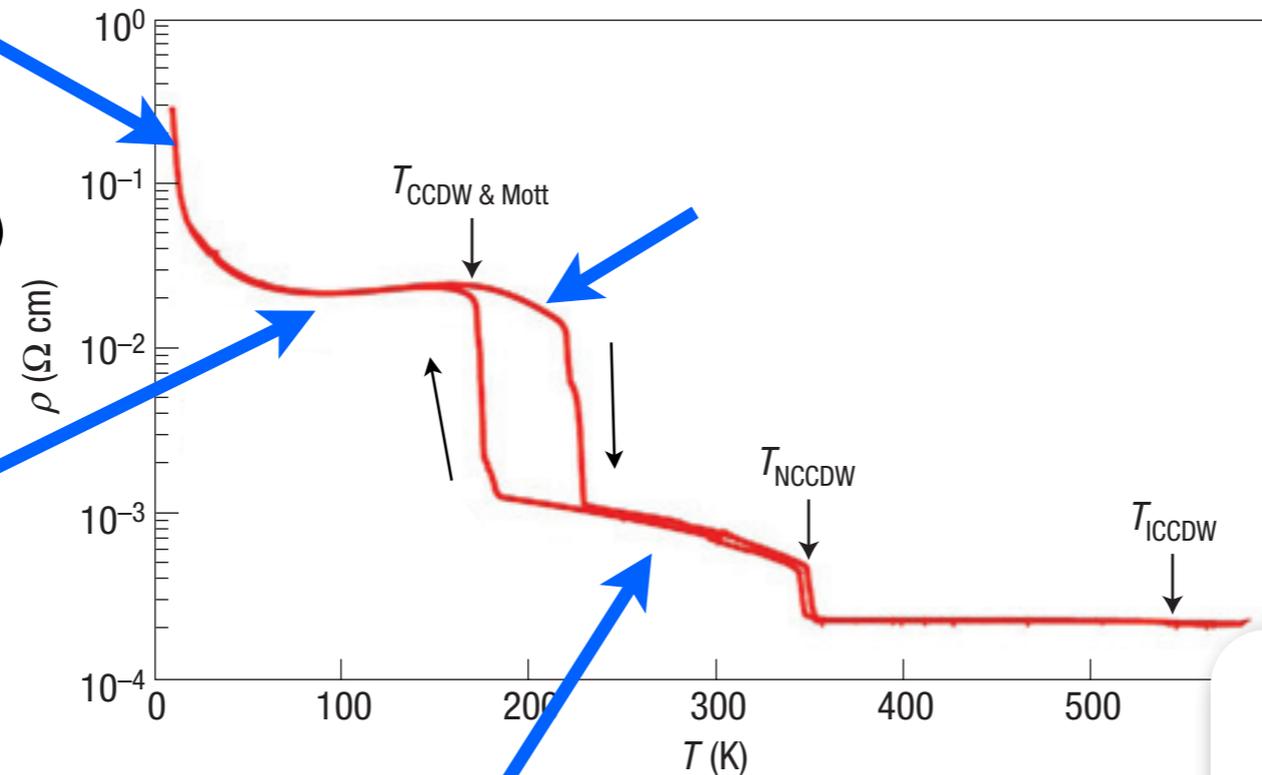


The competing states of $1T$ -TaS₂ under equilibrium conditions

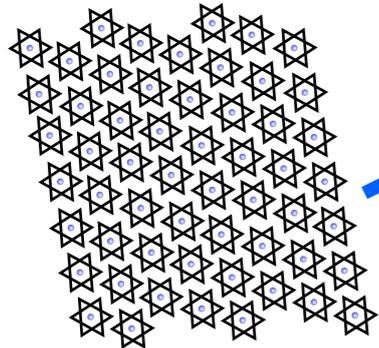


Mott state

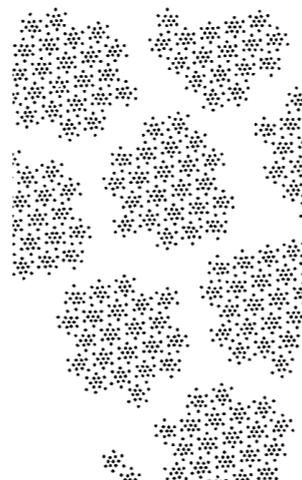
Resistivity of $1T$ -TaS₂



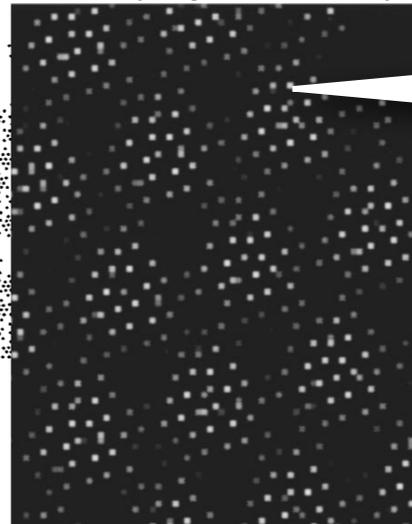
Honeycomb structure
(Commensurate CDW phase)
Tossati and Fazekas (1974)



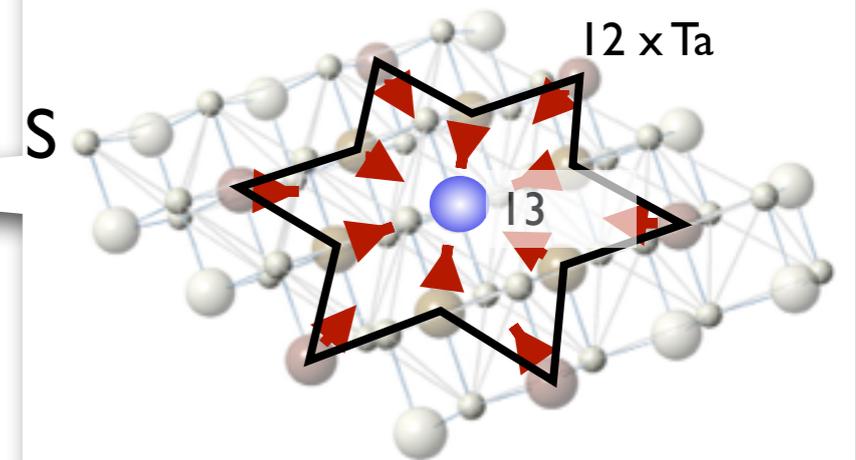
Stretched honeycomb structure of C phase
with domain walls in between
(Nearly Commensurate CDW phase)
Wilson et al



STM (experiments)

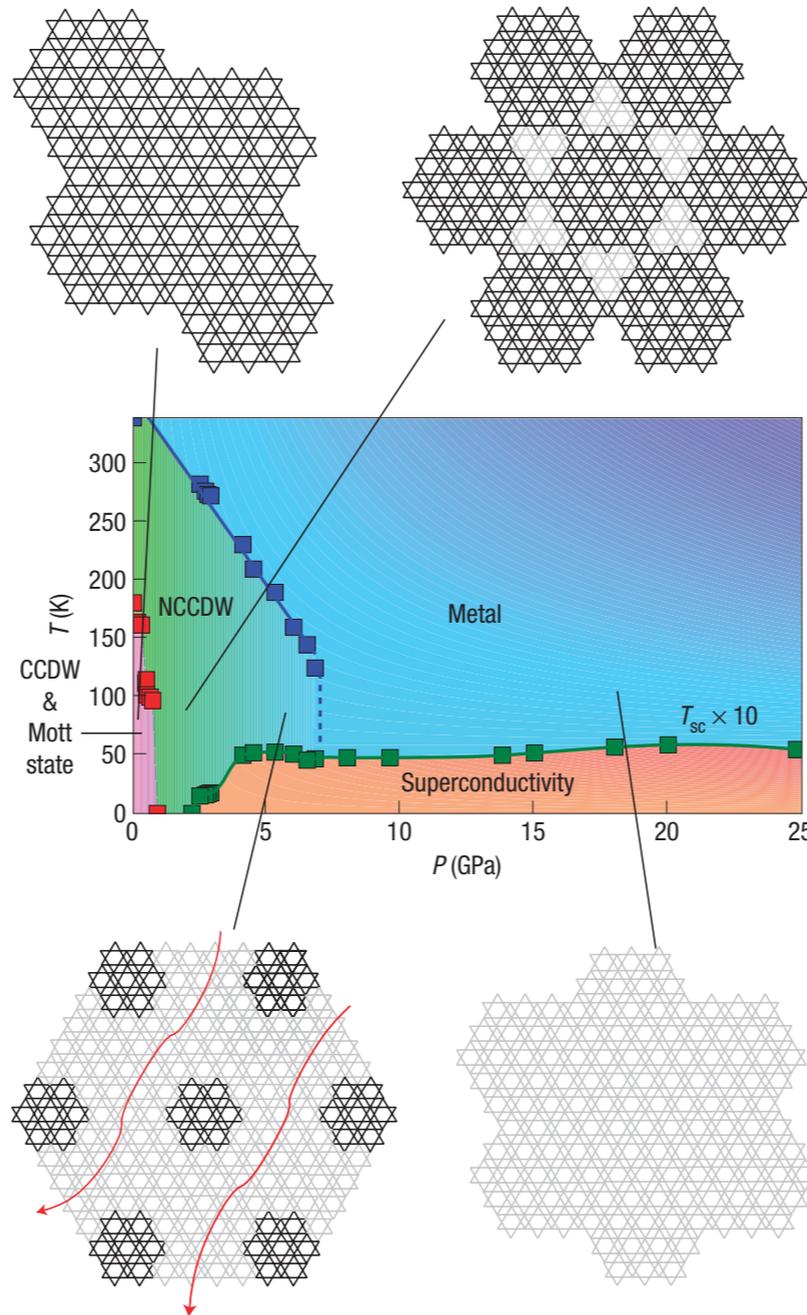
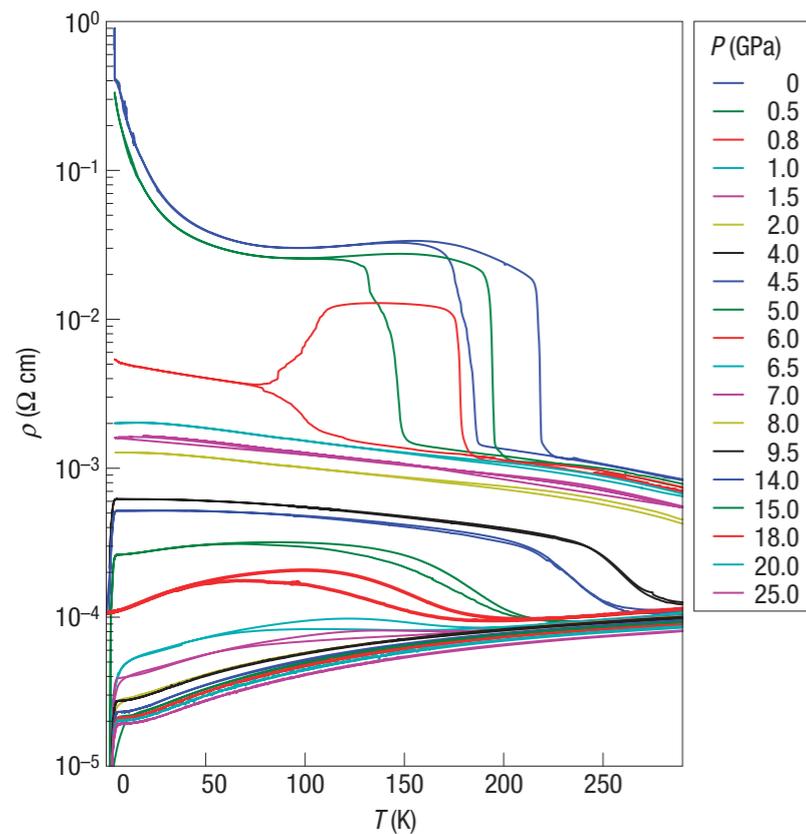


The polaron in $1T$ -TaS₂

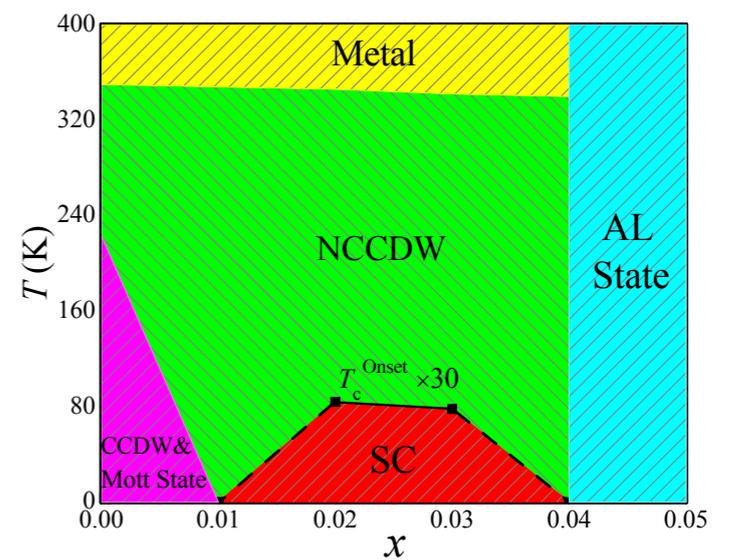
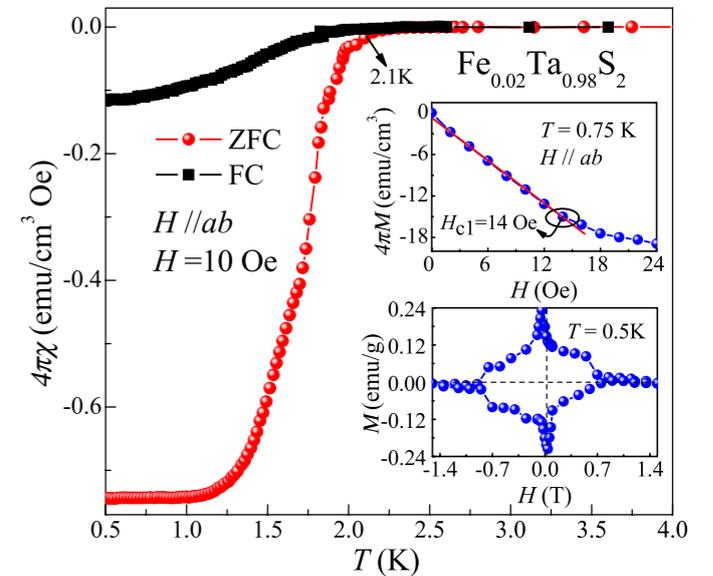


Other nearby states in 1T-TaS₂: Superconductivity under pressure, or Fe doping

Pressure:

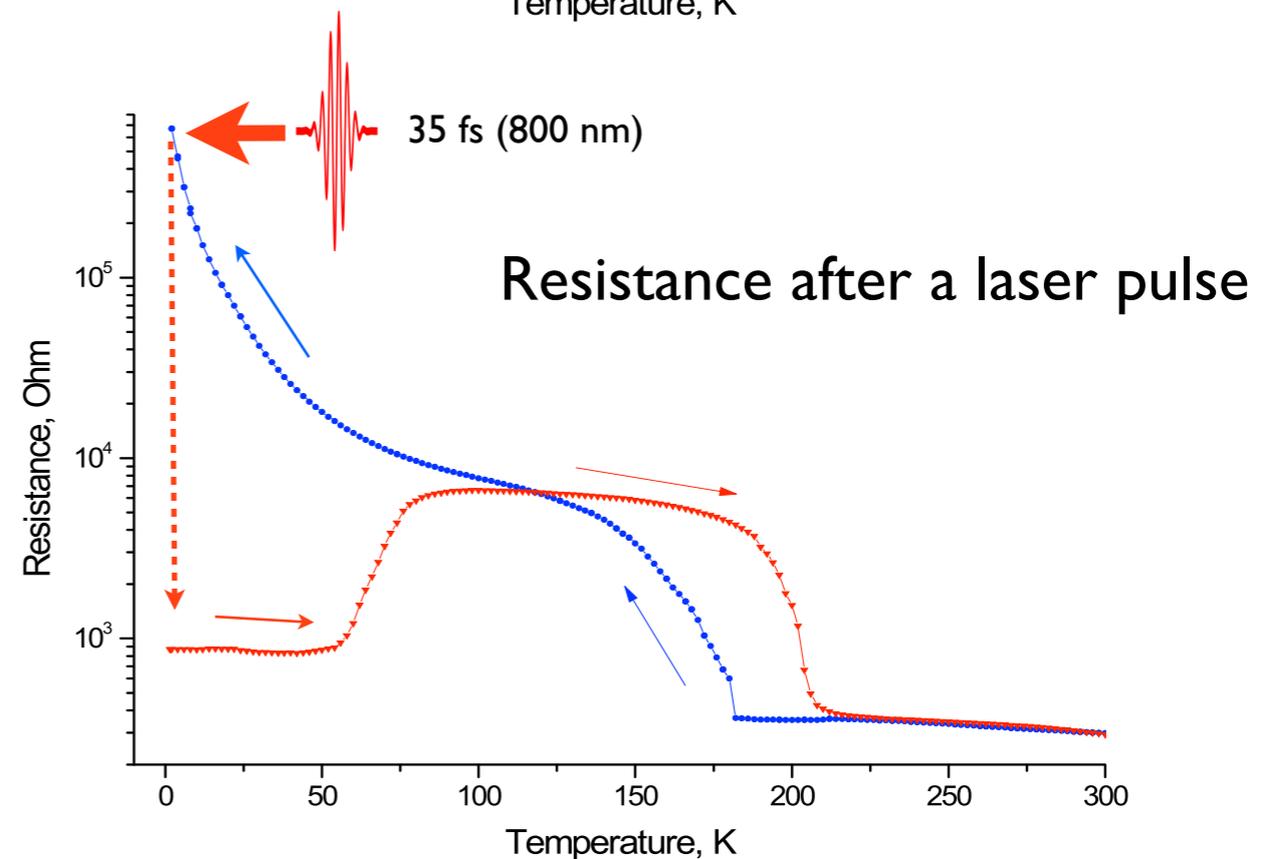
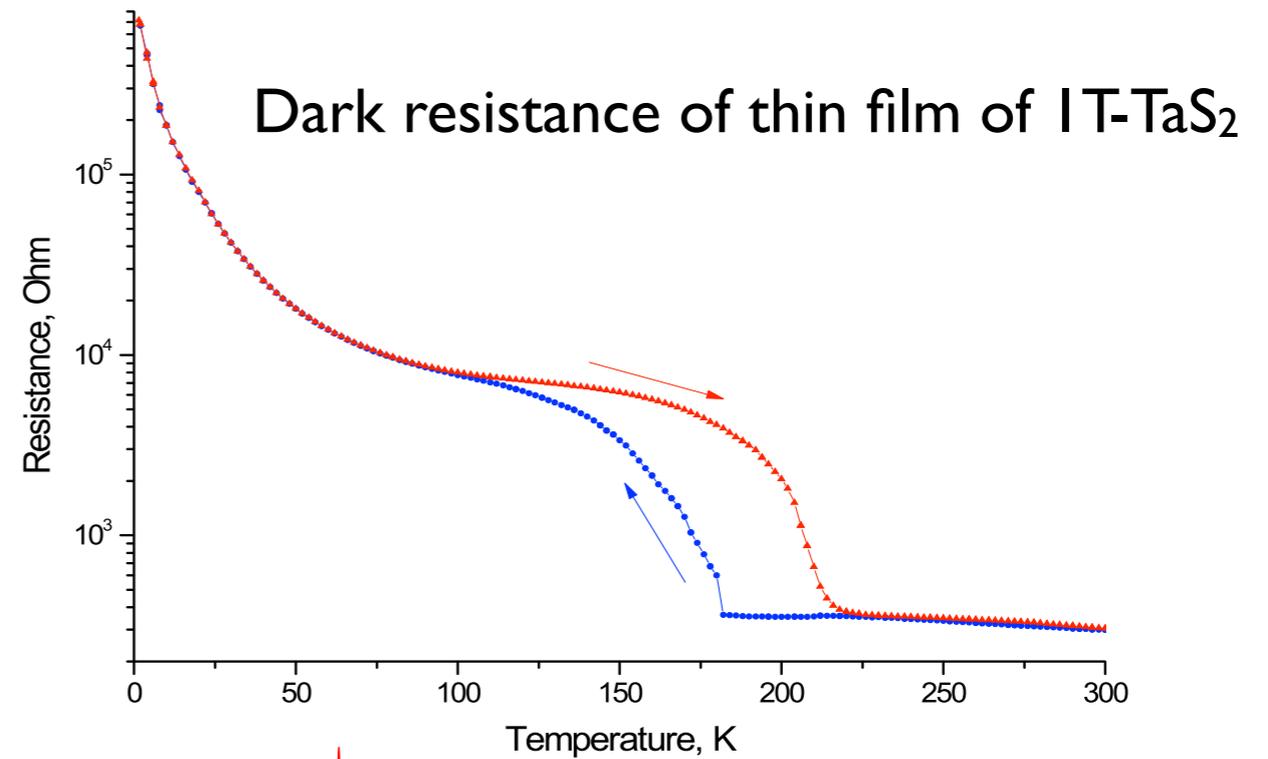
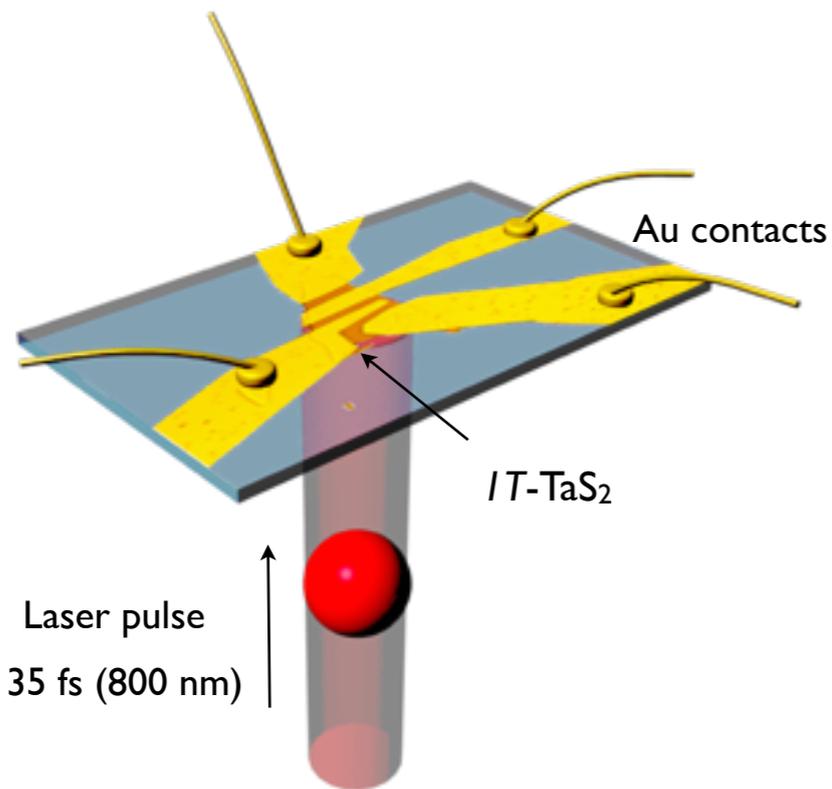


Fe doping:



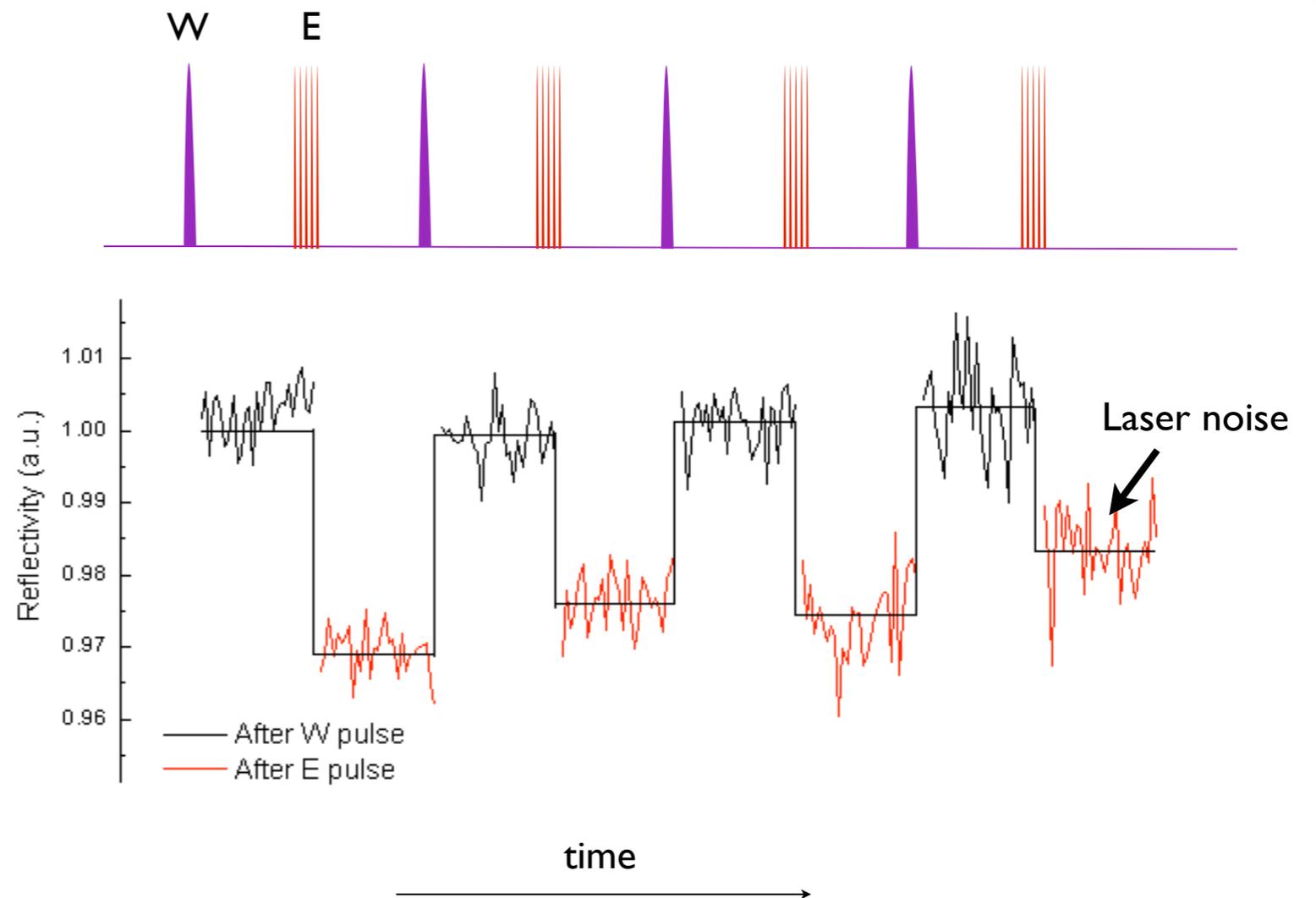
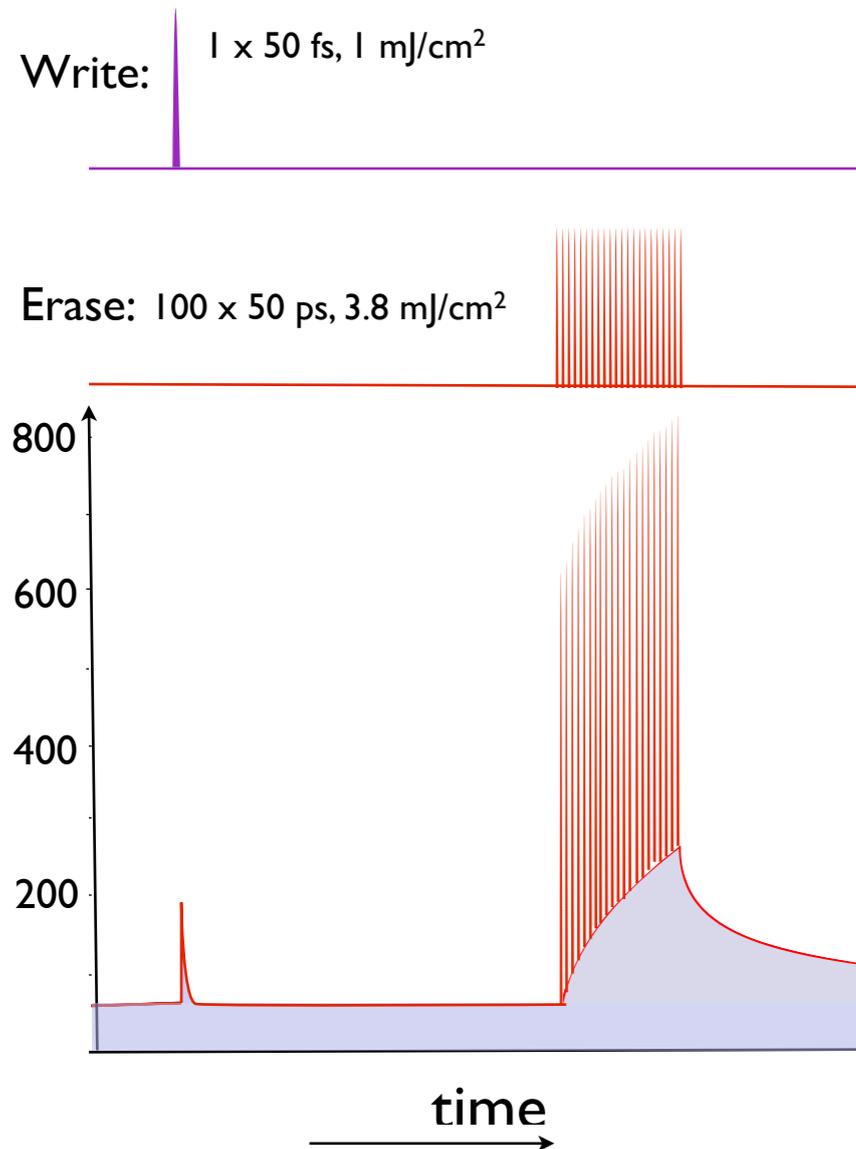
Switching to a hidden state in $1T\text{-TaS}_2$: Resistance change after a (single) 35 fs pulse

$1T\text{-TaS}_2$ single crystal, ~ 100 nm thick.
Au contacts by laser lithography (LPKF LDI).



Stojchevska et al, Science **344**, 177 (2014).

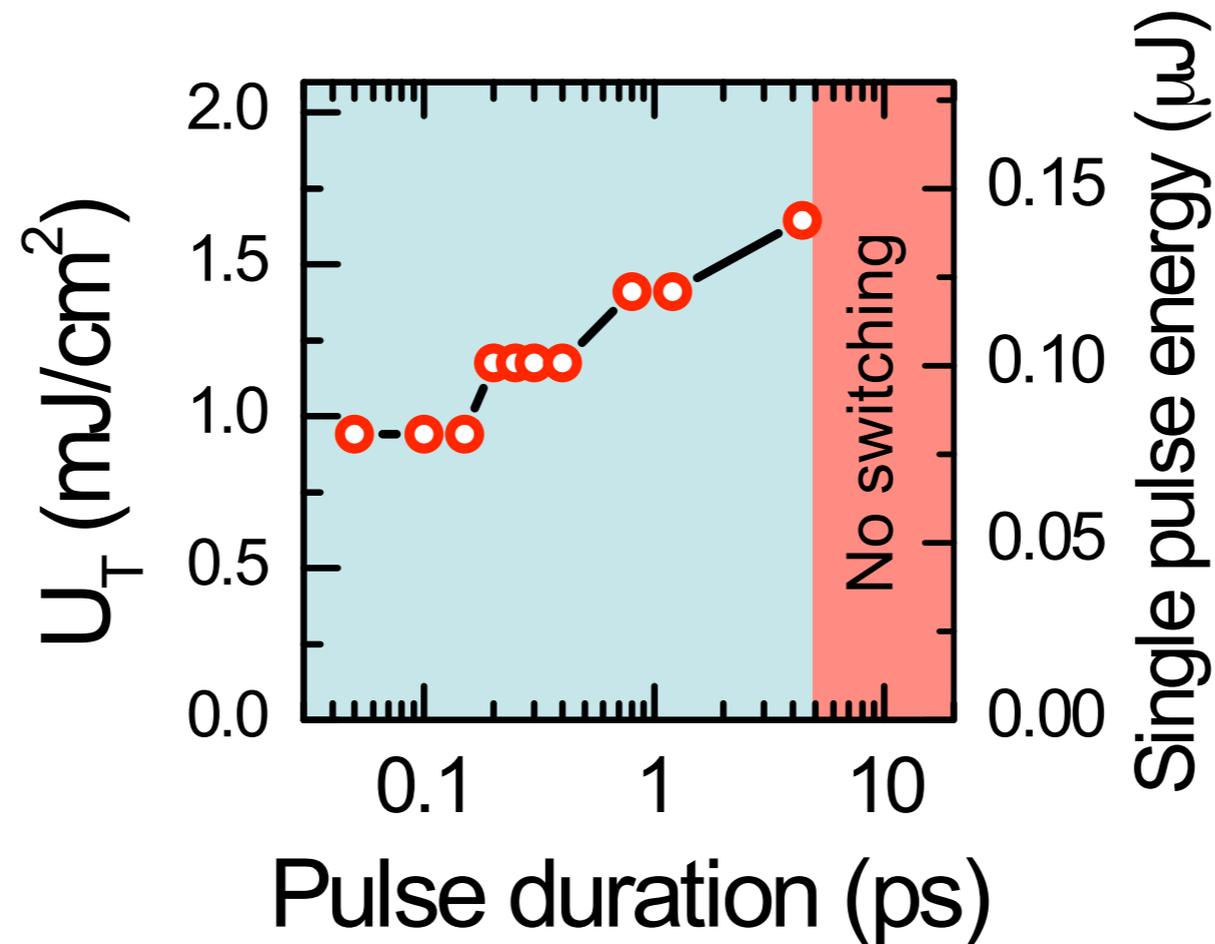
Reflectivity switching by laser pulses



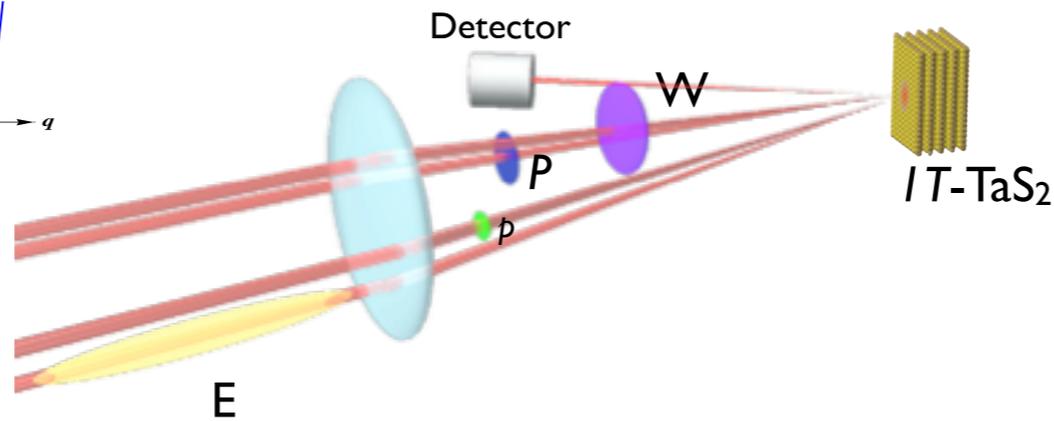
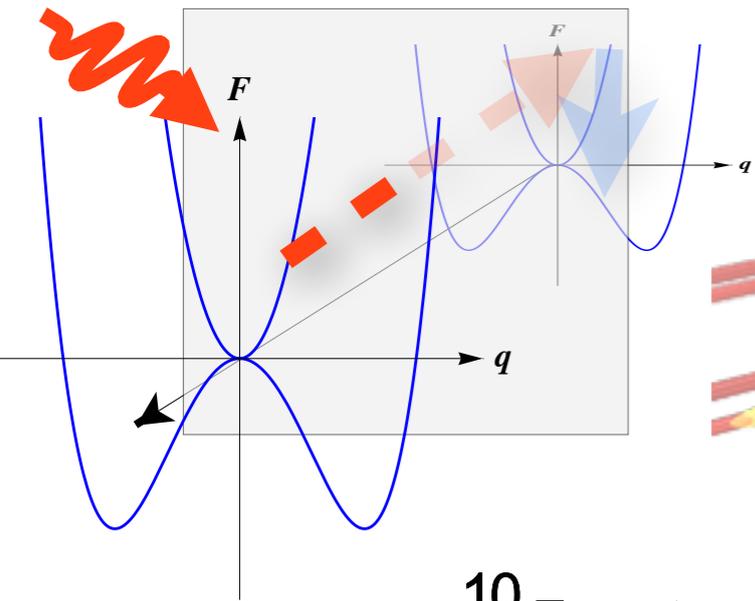
Switching is accompanied by a change in dielectric constant.

$$\Delta R = 5\% \text{ at } 800 \text{ nm (1.5 eV)}$$

Switching only occurs for short pulses $\tau_L < 4$ ps



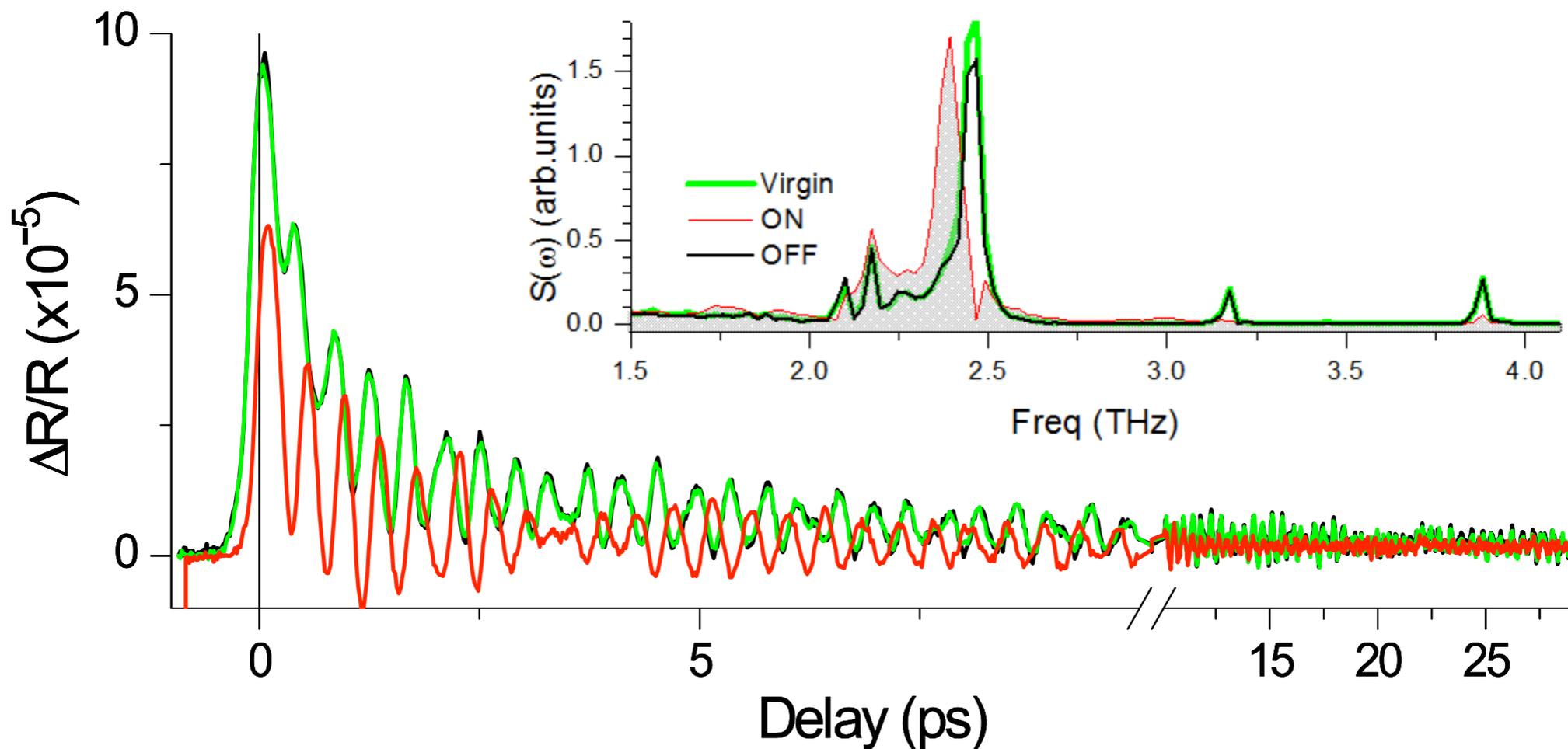
$1T$ -TaS₂: Collective mode switching



W = 50 fs “write”
E = 50 ps “erase”
P = “pump” (50 fs)
p = “probe” (50 fs)

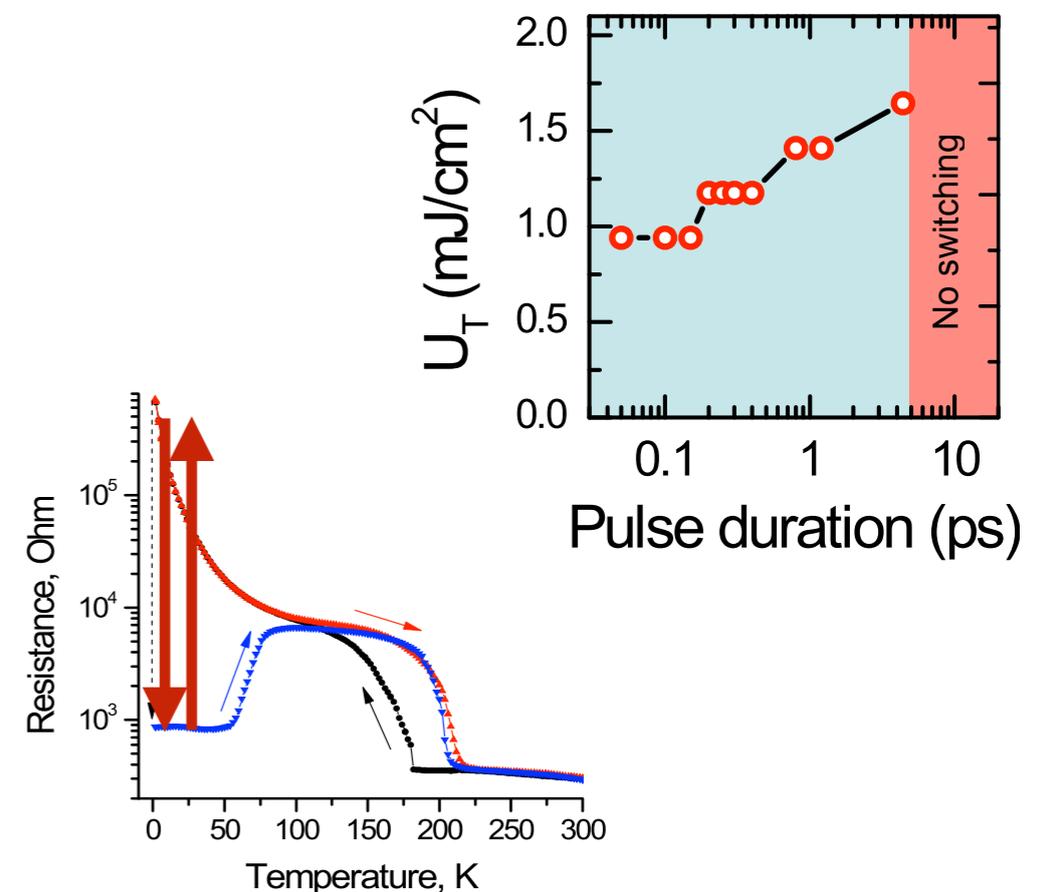
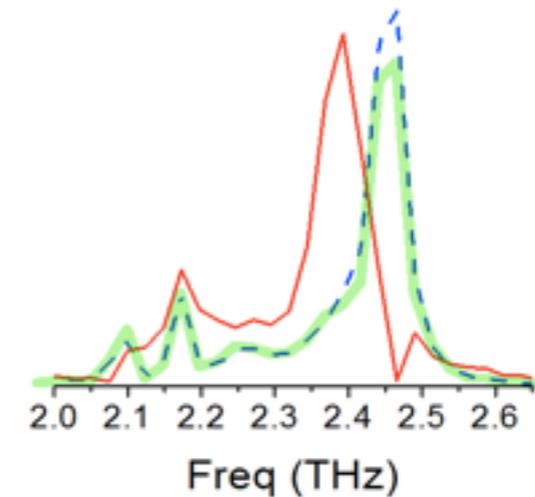


Ljupka Stojchevska



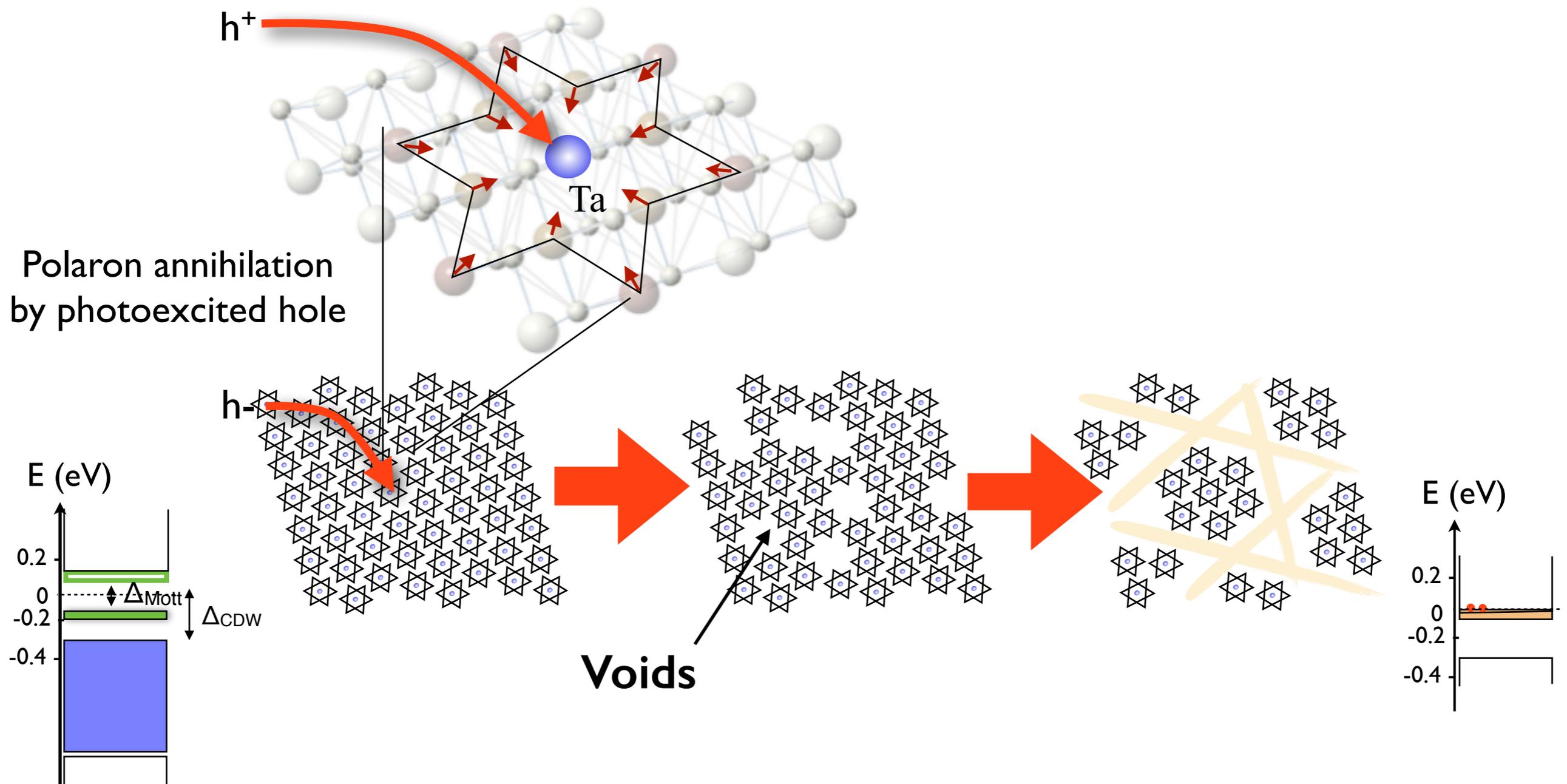
3 unusual characteristics of the hidden state

1. Narrow collective mode peak - implies long range order with no intermediate states, or inhomogeneity
2. Switching is achieved only with sub-5 ps pulses
3. Reproducible metal-Insulator bistability (not sample dependent)



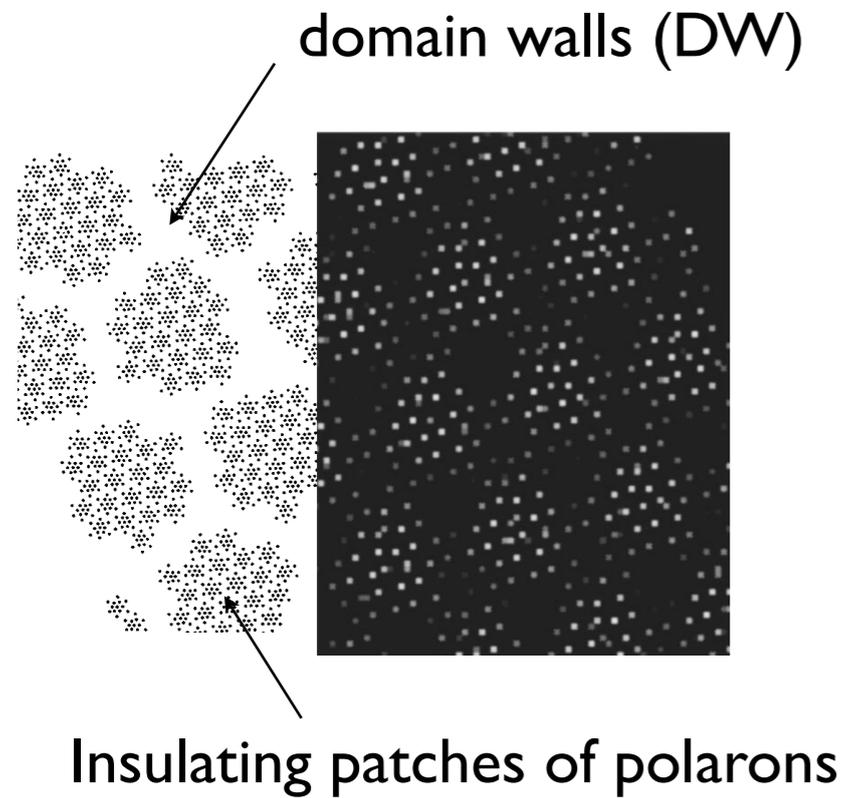
Photo''doping'' and ordering of voids

The addition of a h^+ to the C structure annihilates a polaron, creating a defect.



The nearly-commensurate state of $1T\text{-TaS}_2$

McMillan (1975), Nakanishi et al (1977), Serguei Brazovskii, (2013)

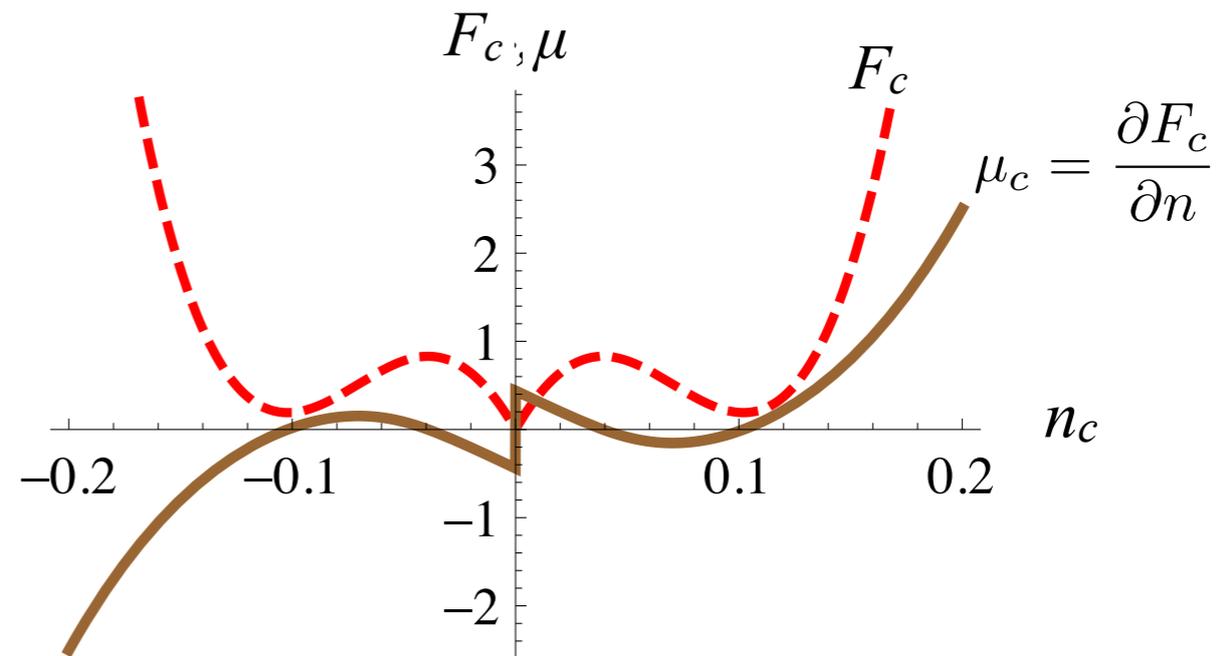


Free energy:

$$F_c(n_c) = E_{DW} \underbrace{(C_0|n_c| + C_1|n_c|e^{-1/(\xi|n_c|)})}_{\text{C - IC transition (MacMillan, 1975)}} - \underbrace{C_2\xi n_c^2}_{\text{Intersection of DW}} + \underbrace{C_4\xi^3 n_c^4}_{\text{Repulsion between DW crossings}}$$

Where $n_c = n_h - n_e$

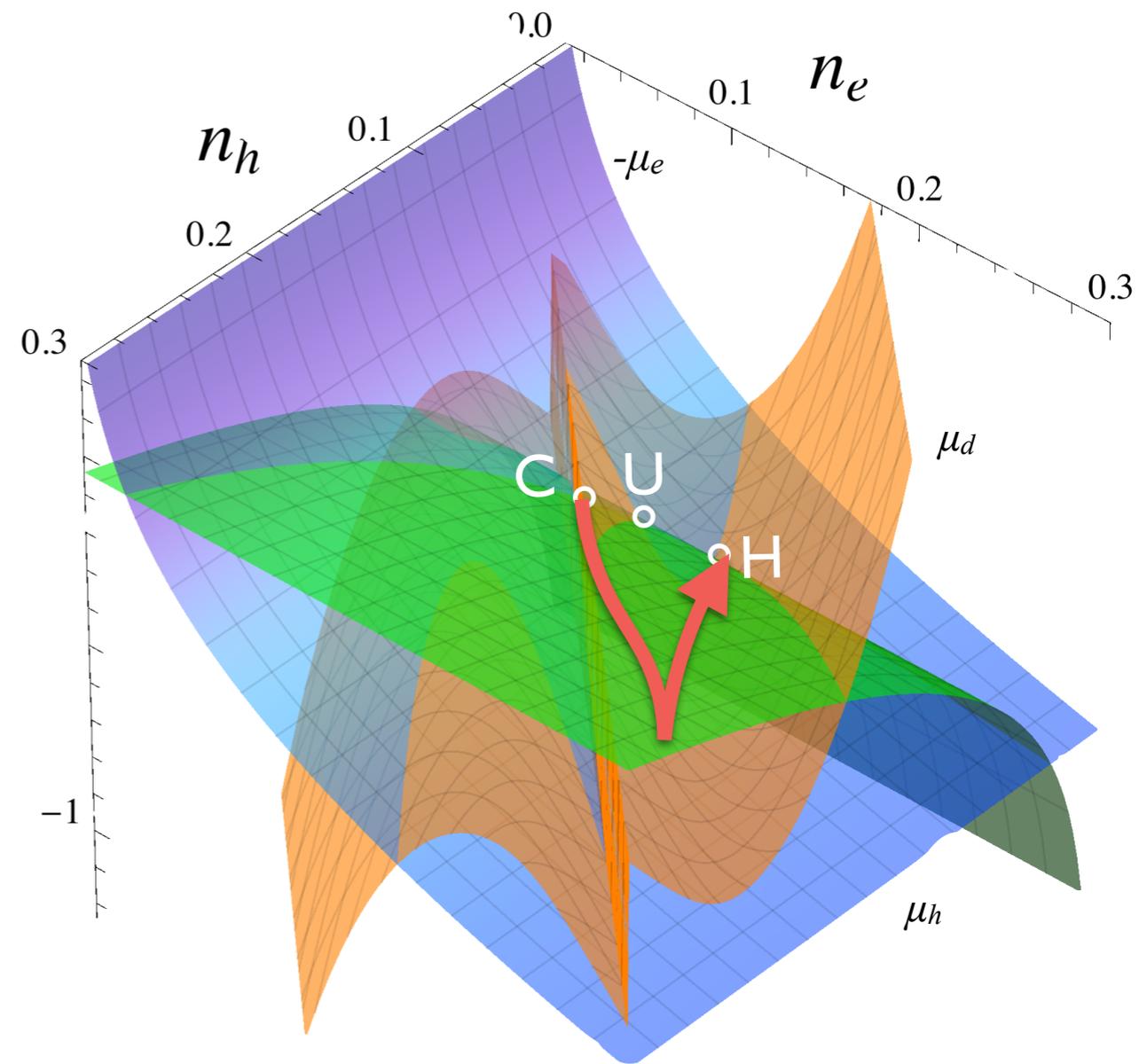
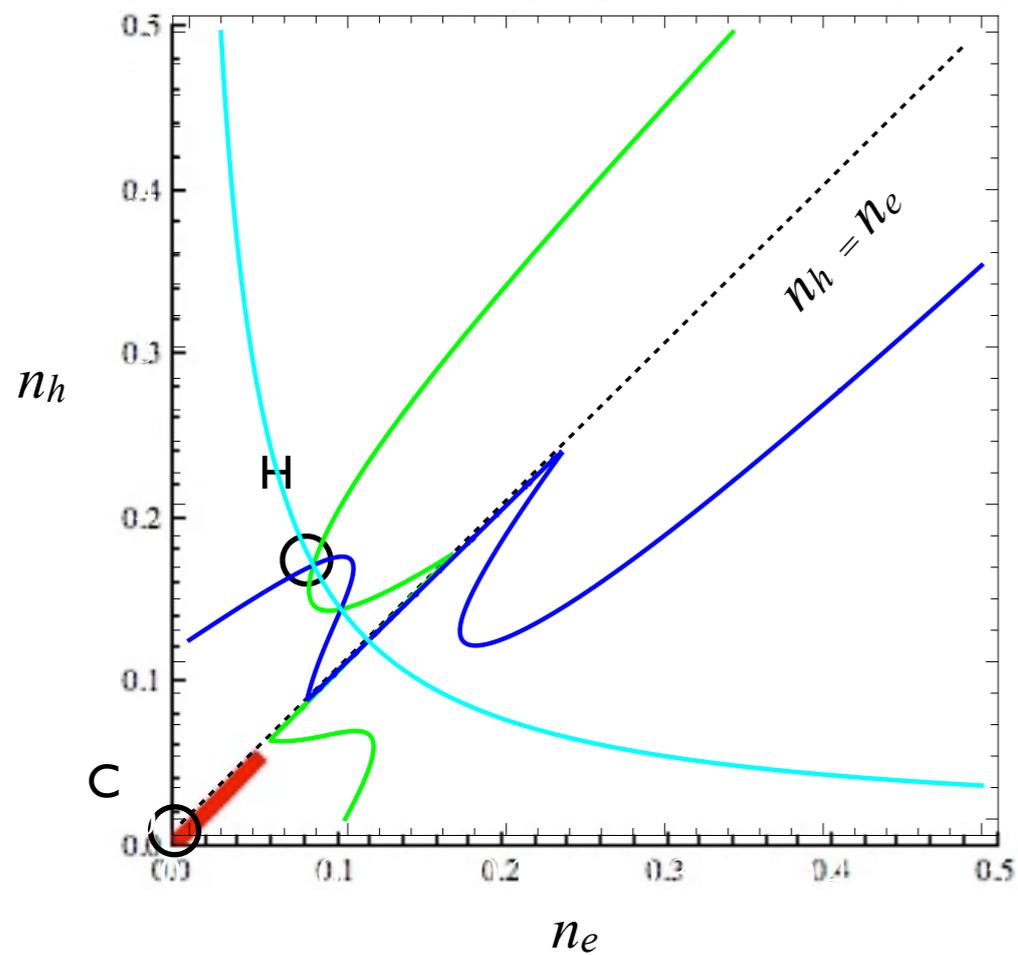
Free energy and chemical potential:



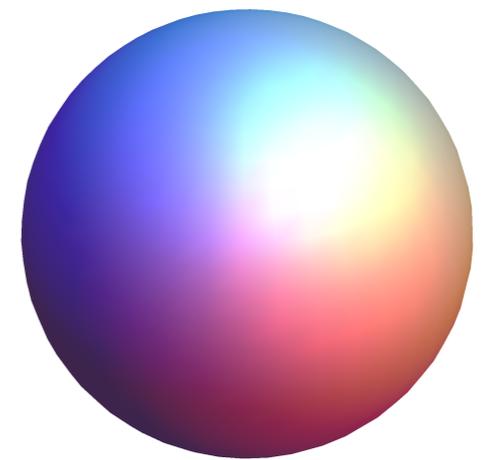
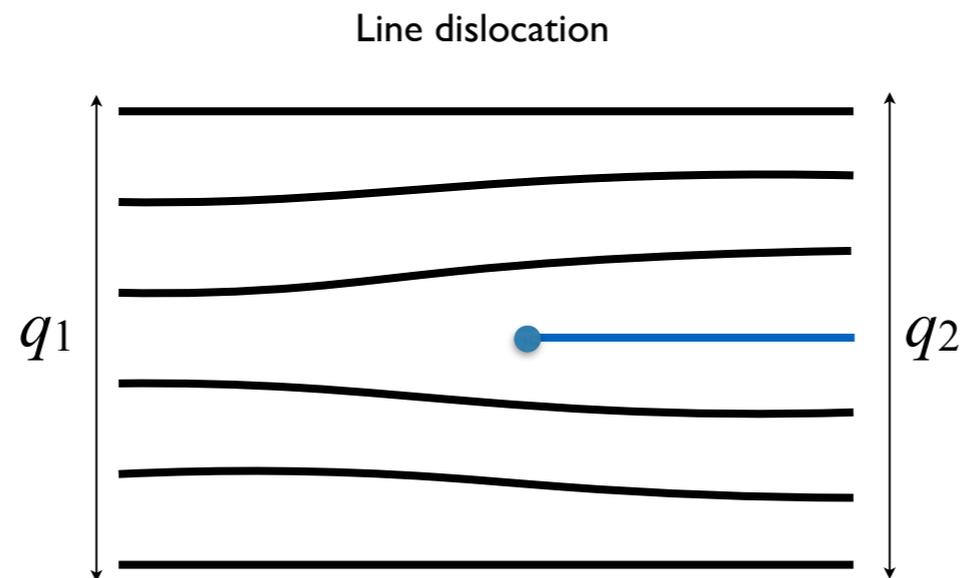
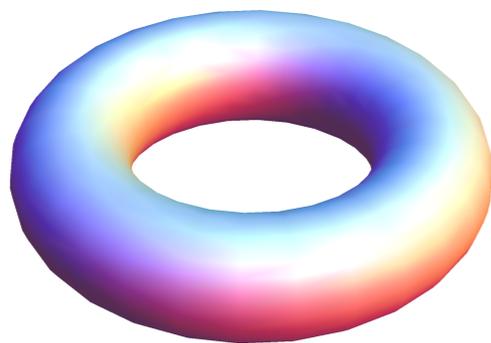
Calculated trajectory

Laser pulse energy above threshold ($U_W > U_T$):

System trajectory (parametric plot)

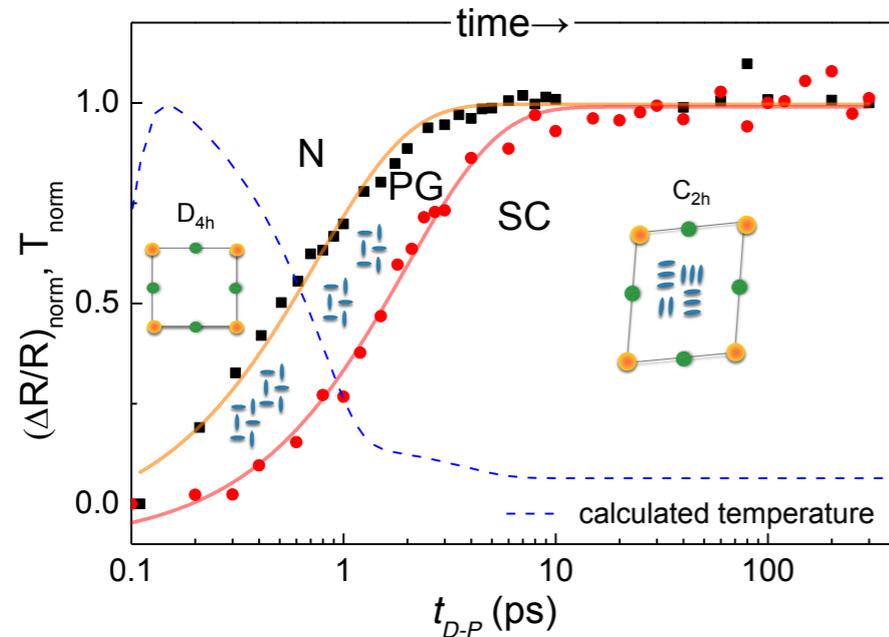


Why is the H state so stable?

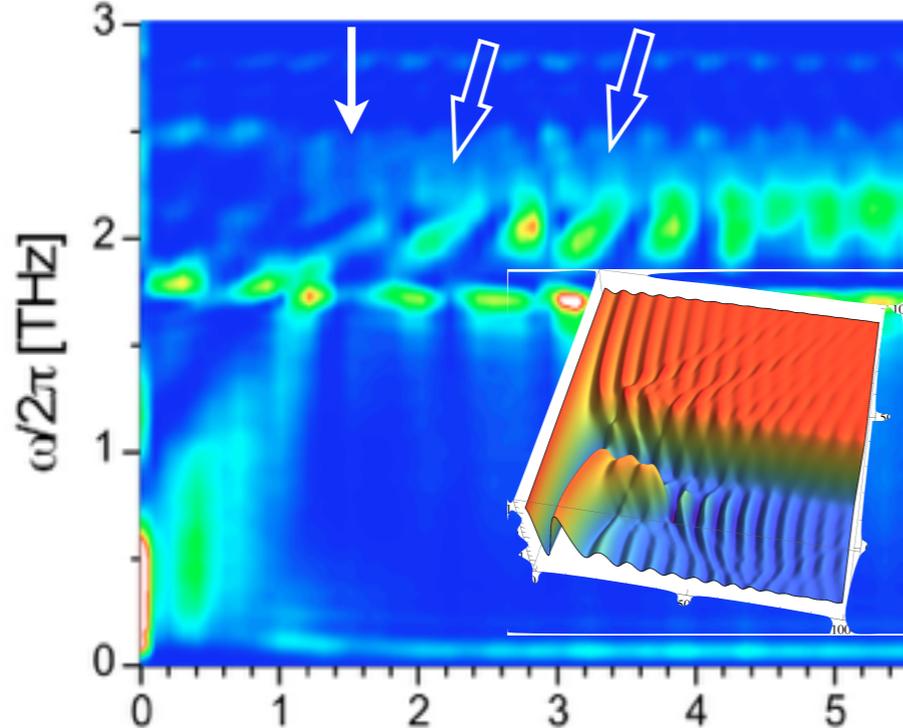


Conclusions

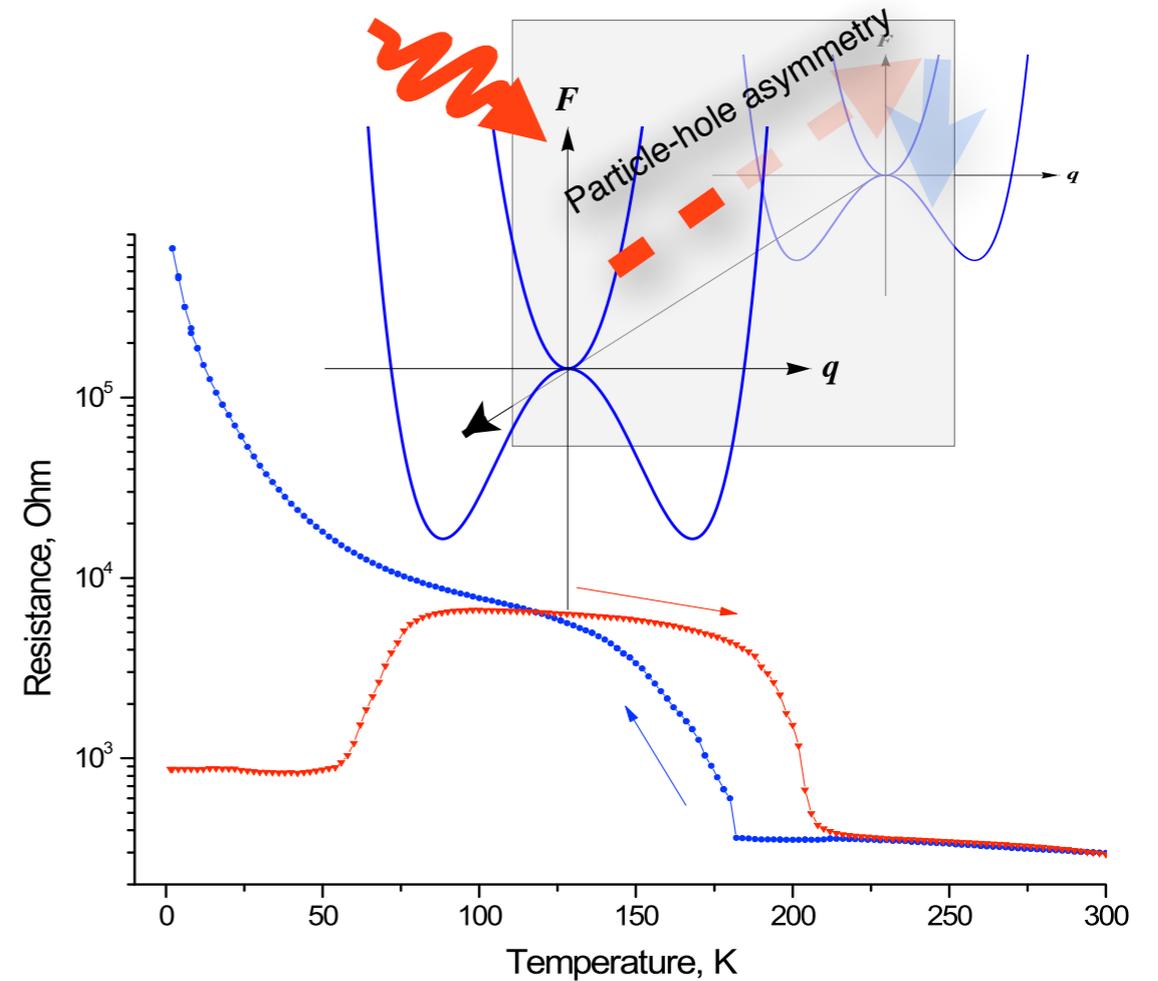
No Higgs oscillations in HTS



Plenty of amplitude modes in CDWs



Hidden states of matter



Stojchevska et al, Science **344**, 177 (2014).

Yusupov, R. et al. Nat Phys **6**, 681 (2010).

Mertelj, T. et al. Phys Rev Lett **110**, 156401 (2013).

Mihailovic et al., J Phys-Condens Mat **25**, 404206 (2013).