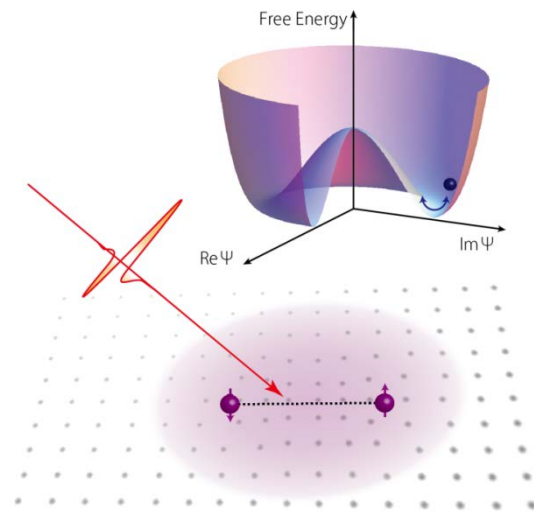


# Observation of Higgs mode in s-wave superconductors

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*Cryogenic Research Center,  
Department of Physics,  
The University of Tokyo*



# Outline

- (1) *Higgs mode in superconductors: previous works*
- (2) *Observation of Higgs mode in NbN  
by THz pump and THz probe experiments:  
**non-adiabatic excitation** with monocycle THz pulse*
- (3) *Coherent order parameter oscillation in the presence of  
multi-cycle THz pulse tuned below the superconducting gap:  
**coupling of Higgs mode with two-photon process.***
- (4) *Higher order harmonics generation from **the collective  
precession of Anderson's pseudospins***

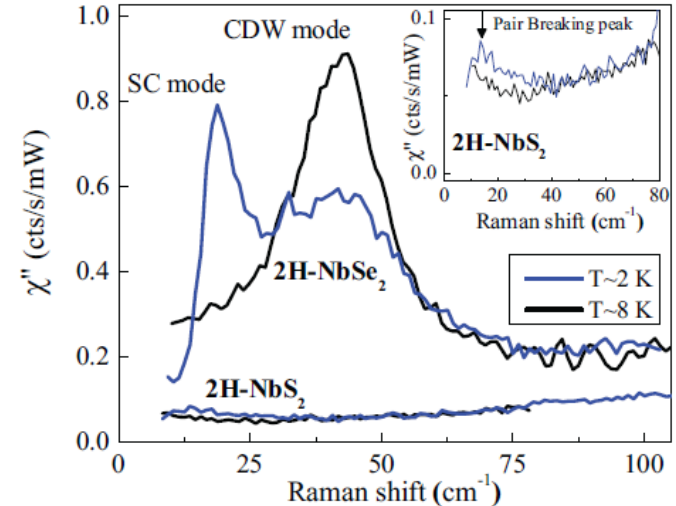
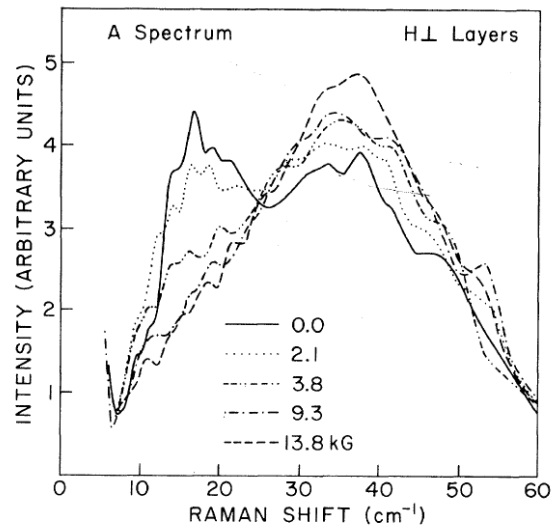
# Higgs mode in superconductors : previous works

## BCS-CDW coexistent compound $\text{NbSe}_2$

R. Sooryakumar and M. V. Klein, PRL **45**, 660 (1980).

P.B. Littlewood and C. M. Varma, PRL **47**, 811 (1982).

C. M. Varma, J. Low Temp. Phys. **126**, 901 (2002)



M.-A. Measson, et al., PRB **89**, 060503 (2014).

## Cf.) $p$ -wave superfluid $^3\text{He}$

For a review, e.g., Lee, J. Phys. Chem. Sol. **59**, 1682 (1998).

G. E. Volovik, and M. A. Zubkov, J. Low Temp. Phys. **175**, 486 (2014)

# Theoretical investigations: quench problem

Quenching the interaction  $U(t)$  much faster than

$$\tau_{\Delta} \sim \hbar/\Delta \quad (\Delta: \text{order parameter})$$

⇒ Emergence of order parameter oscillation (Higgs mode)

Theoretical studies for  
dynamics of nonequilibrium BCS  
state after *nonadiabatic*  
excitation

Volkov *et al.*, Sov. Phys. JETP **38**, 1018 (1974).

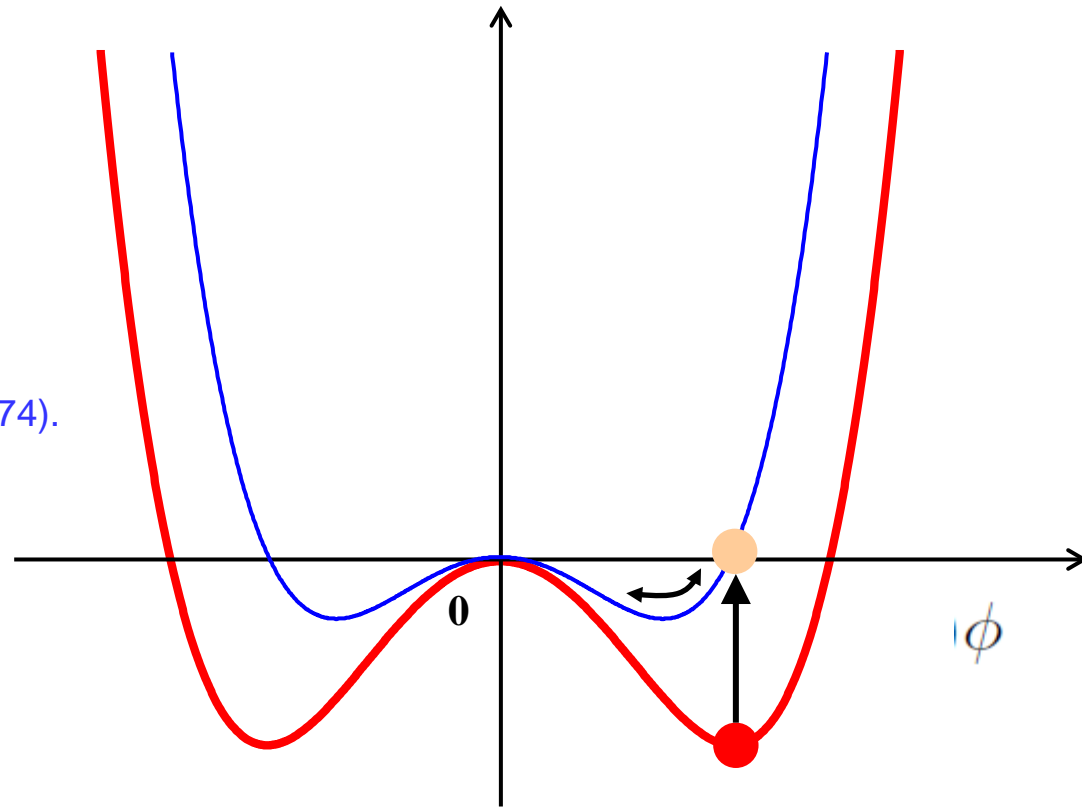
Barankov *et al.*, PRL **94**, 160401 (2004).

Barankov *et al.*, PRL **96**, 230403 (2006).

Yuzbashyan *et al.*, PRL **96**, 230404 (2006).

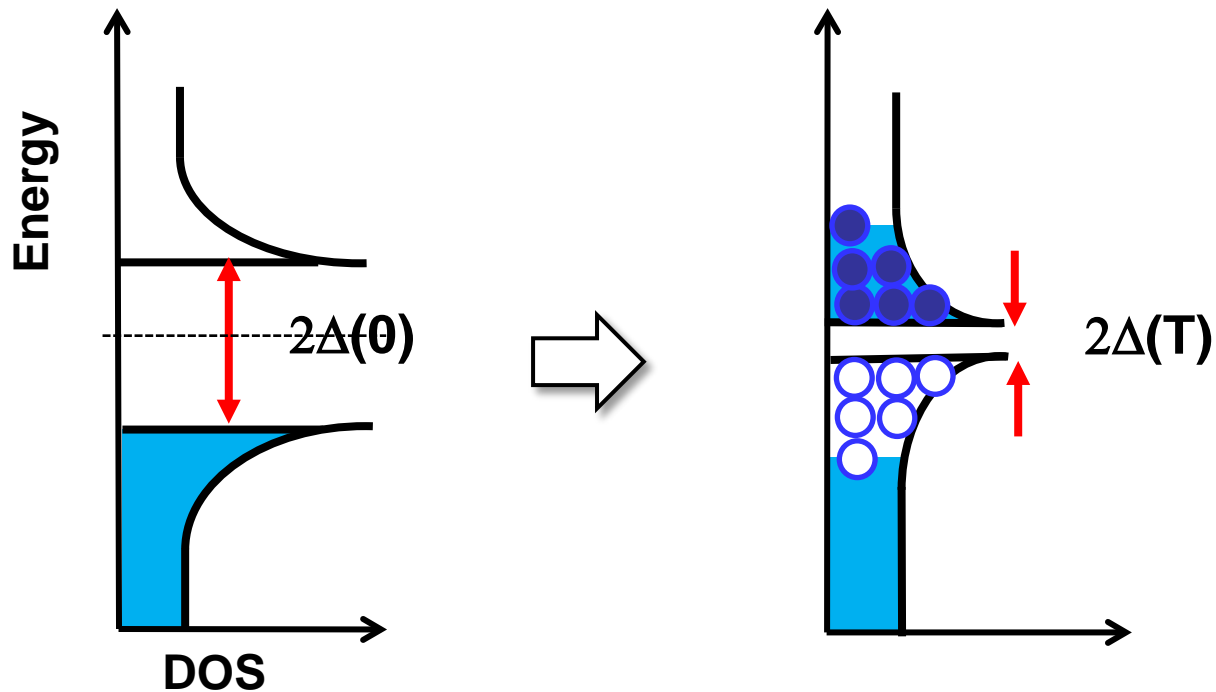
Gurarie *et al.*, PRL **103**, 075301 (2009).

Tsuji *et al.*, PRL **110**, 136404 (2013).

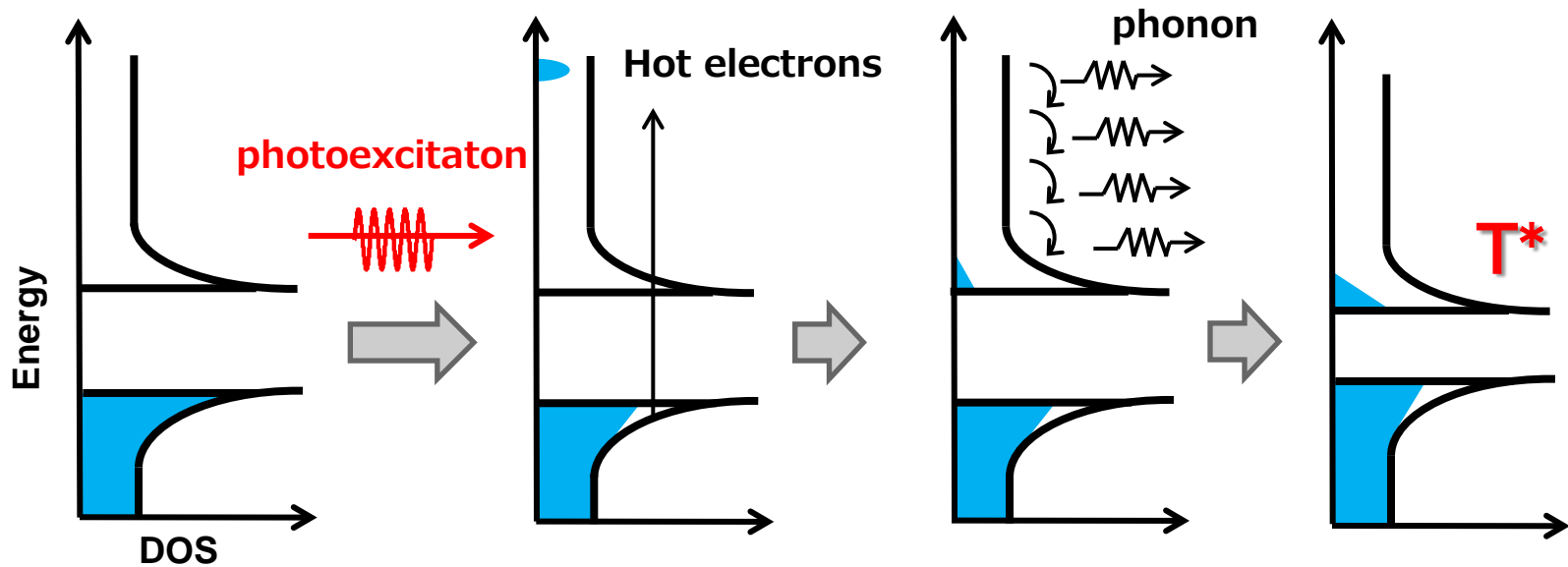


# Quench by Quasiparticle injection

$$\Delta = V \int_{\Delta}^{\hbar\omega_D} d\varepsilon \frac{\Delta}{\sqrt{\varepsilon^2 - \Delta^2}} [1 - 2f(\varepsilon)]$$



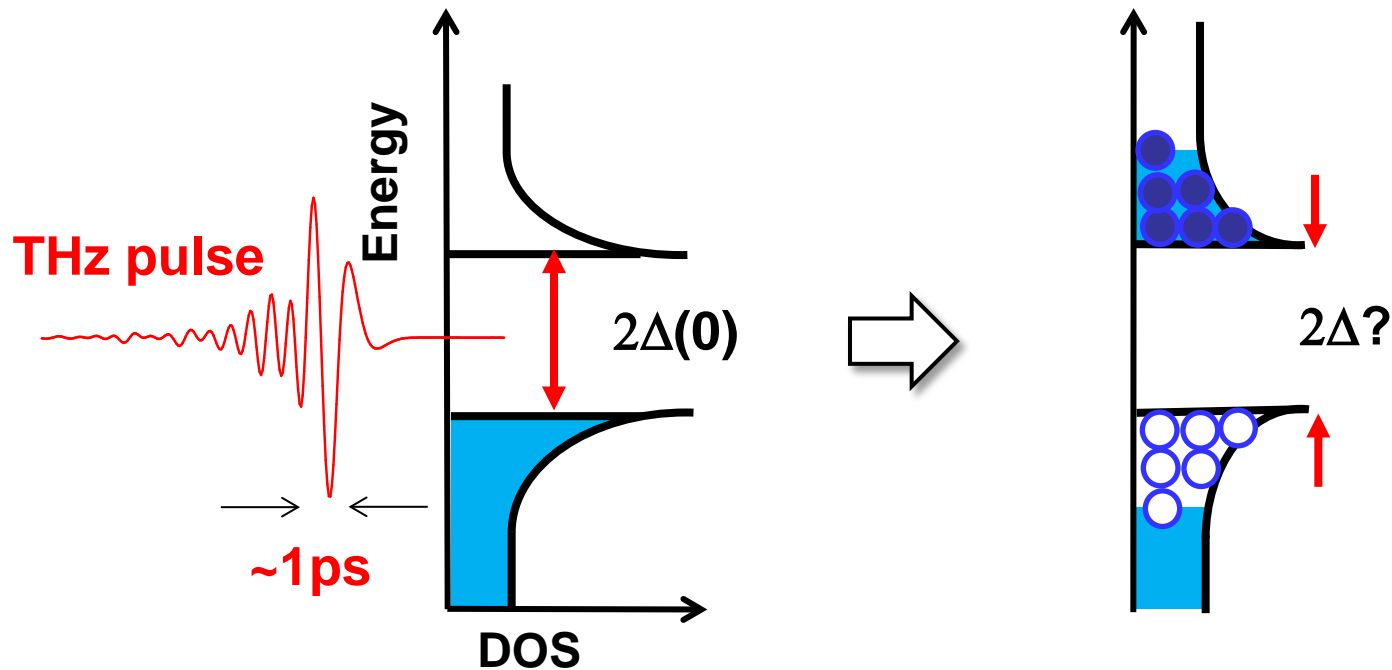
# Gap quenching dynamics after photoexcitation



M. Beck *et al.*, Phys. Rev. Lett. **107**, 177007 (2011).

- ① photoexcitation of hot electrons far above the SC gap
- ② phonon emission
- ③ pair breaking by emitted phonons
- ④ gradual reduction of the SC gap

# What happens if one create quasiparticle instantaneously, $\tau < \Delta^{-1}$

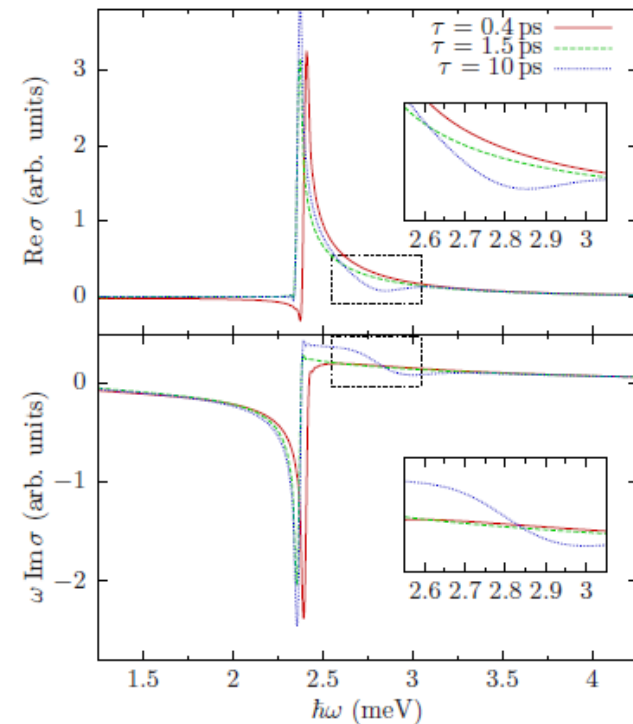
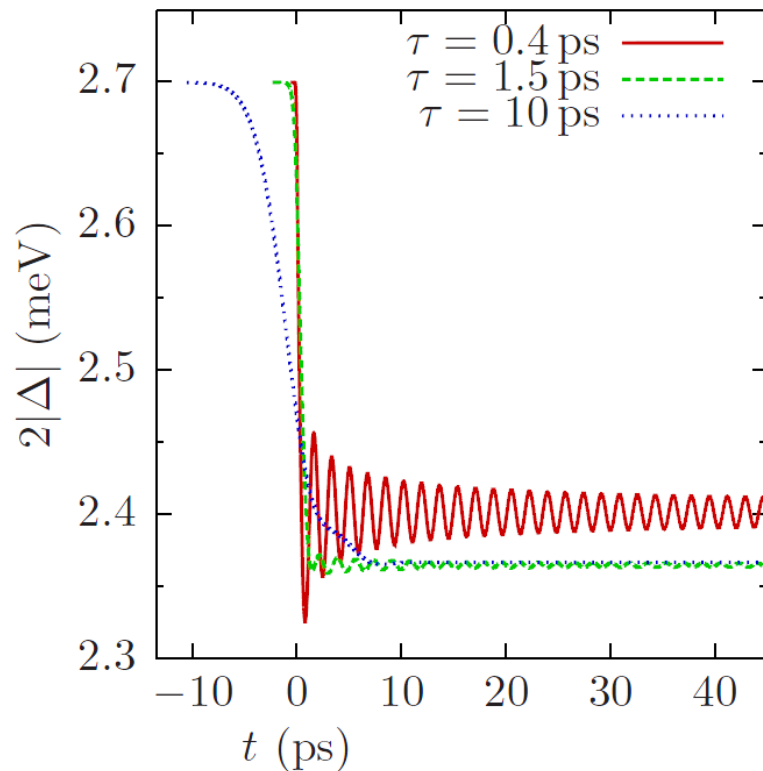


$2\Delta(0)$  in typical superconductors:  $\sim 1$  THz

We need an intense monocycle-like THz pulse, avoiding the injection of excess energy to the system that cause the phonon-induced pair breaking.

# Non-adiabatic excitation by light pulse

Papenkort *et al.*, PRB 76, 224522 (2007).



Invisible in  $\sigma(\omega)$  spectra?

See also, A. P. Schnyder, D. Manske, and A. Avella, Phys. Rev. B84, 214513 (2011)



# Sample and pump pulse

Sample



$\text{Nb}_{0.8}\text{Ti}_{0.2}\text{N}$  film (12nm)/Quartz

$T_C = 8.5$  K,

$2\Delta(T=4\text{ K}) = 3.0$  meV = 0.72 THz

**response time :  $\tau_{\Delta} = \Delta^{-1} \sim 2.8$  ps**

THz pump pulse

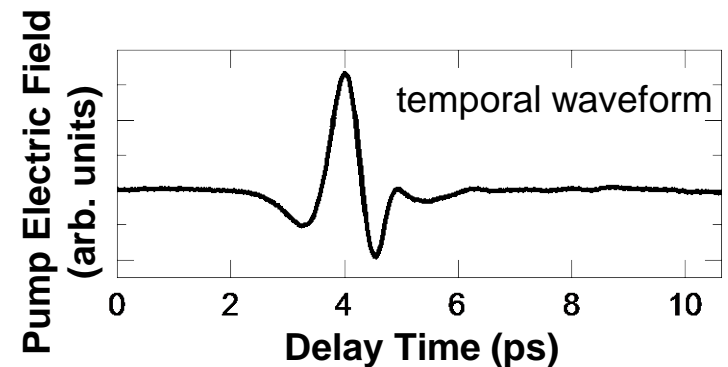
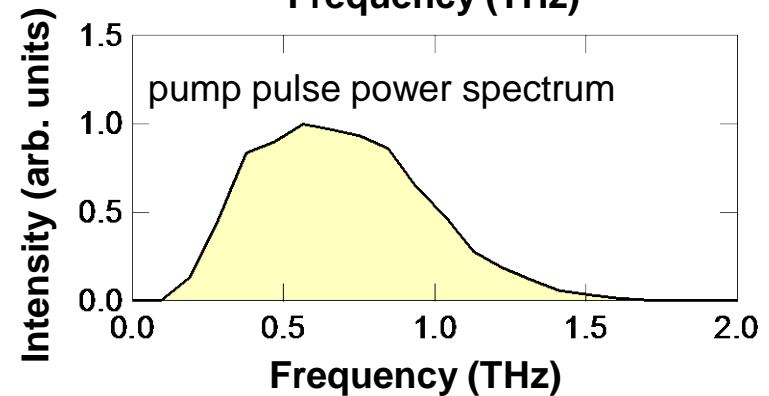
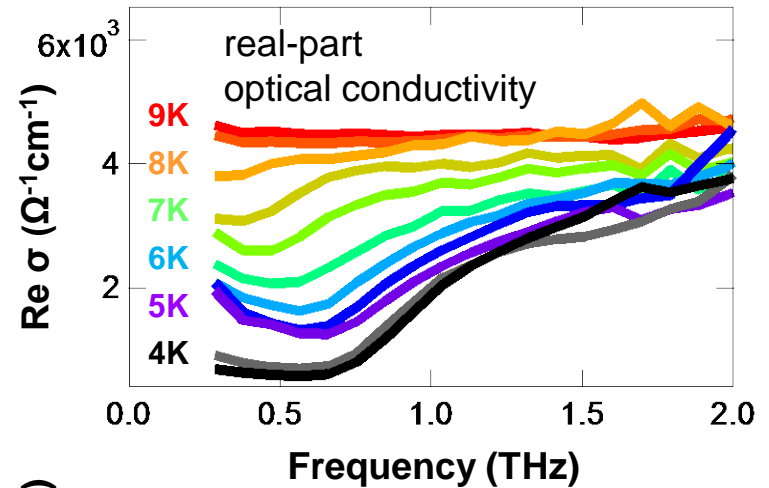
Center frequency 0.7THz  $\sim 2\Delta$

**pulse width:  $\tau_{\text{pump}} \sim 1.5$  ps**

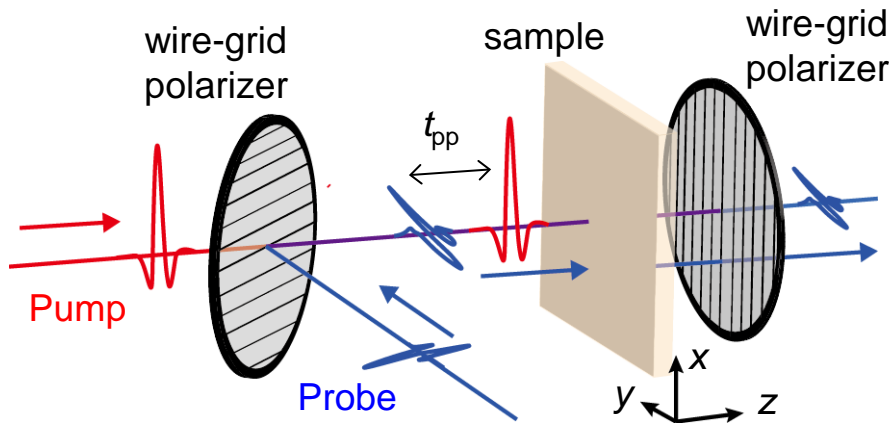
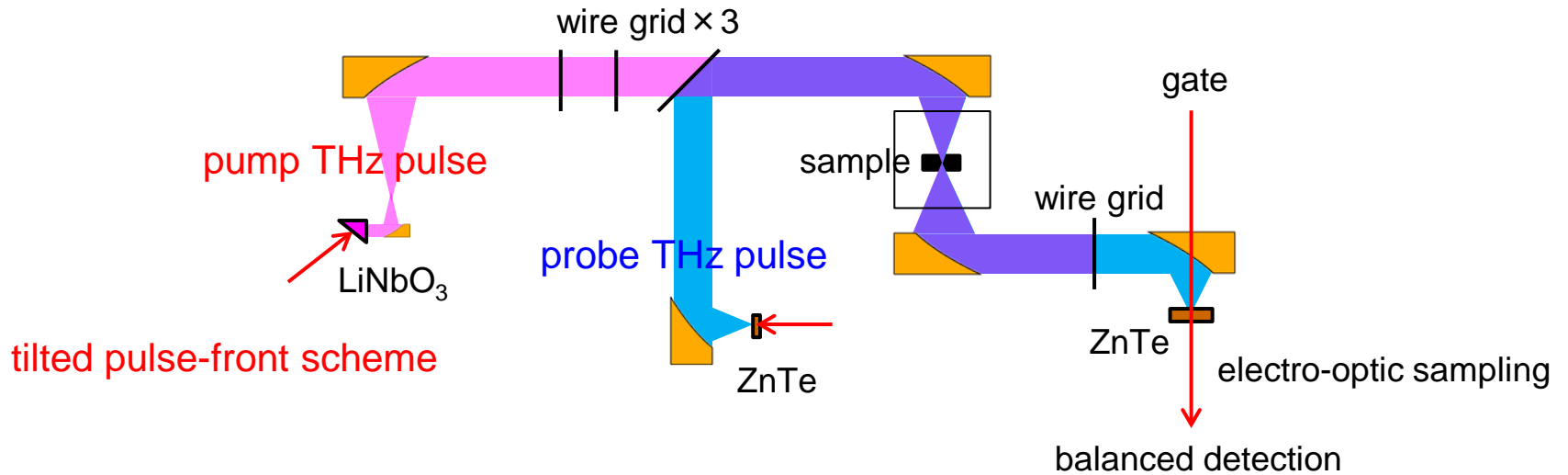
$\tau_{\text{pump}}/\tau_{\Delta} \sim 0.57 < 1$



**nonadiabatic excitation  
condition**



# THz pump and THz probe spectroscopy



Pump :  $E_{\text{pump}} // x$

Probe :  $E_{\text{probe}} // y$

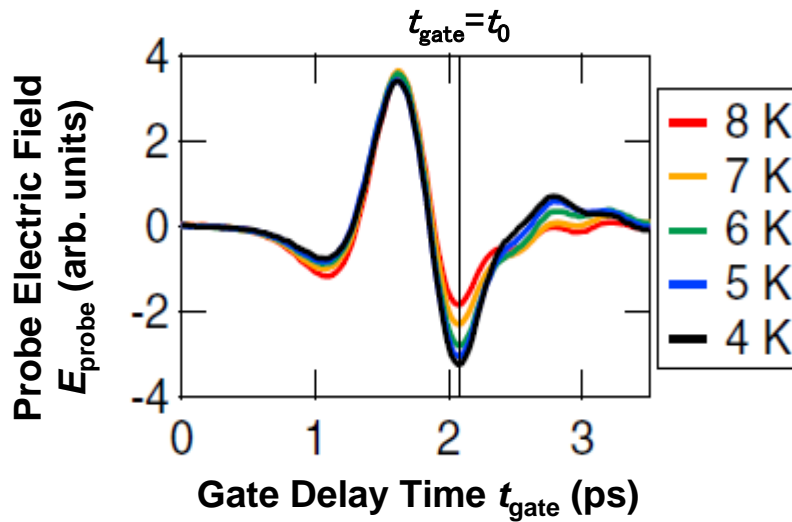
$t_{pp}$ : pump-probe delay

Transmitted probe THz electric field:

Free space EO sampling

10  $t_{\text{gate}}$ : gate pulse delay

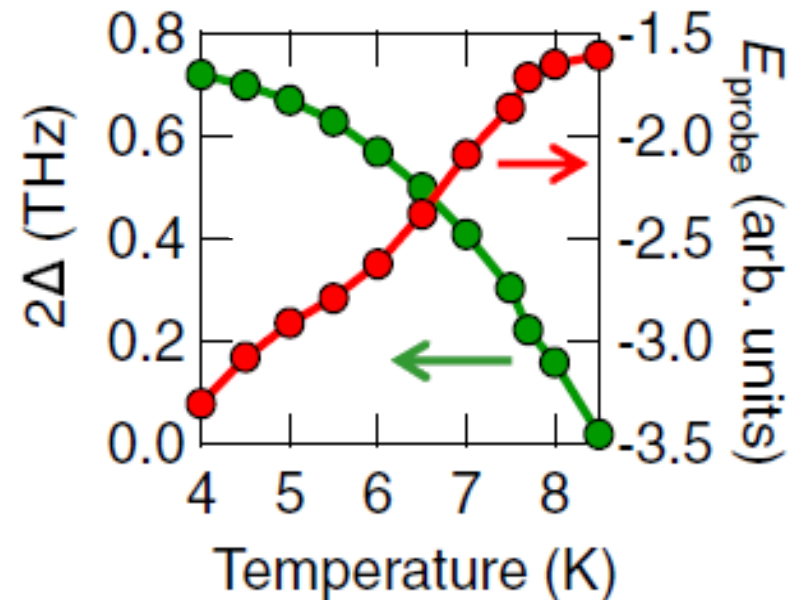
# Detection scheme of the Higgs mode



Temperature dependence of the probe E-field without pump  $E_{\text{probe}}(t_{\text{gate}})$

At  $t_{\text{gate}} = t_0$ , the change in  $E_{\text{probe}}$  is proportional to the change in the order parameter  $\Delta$ .

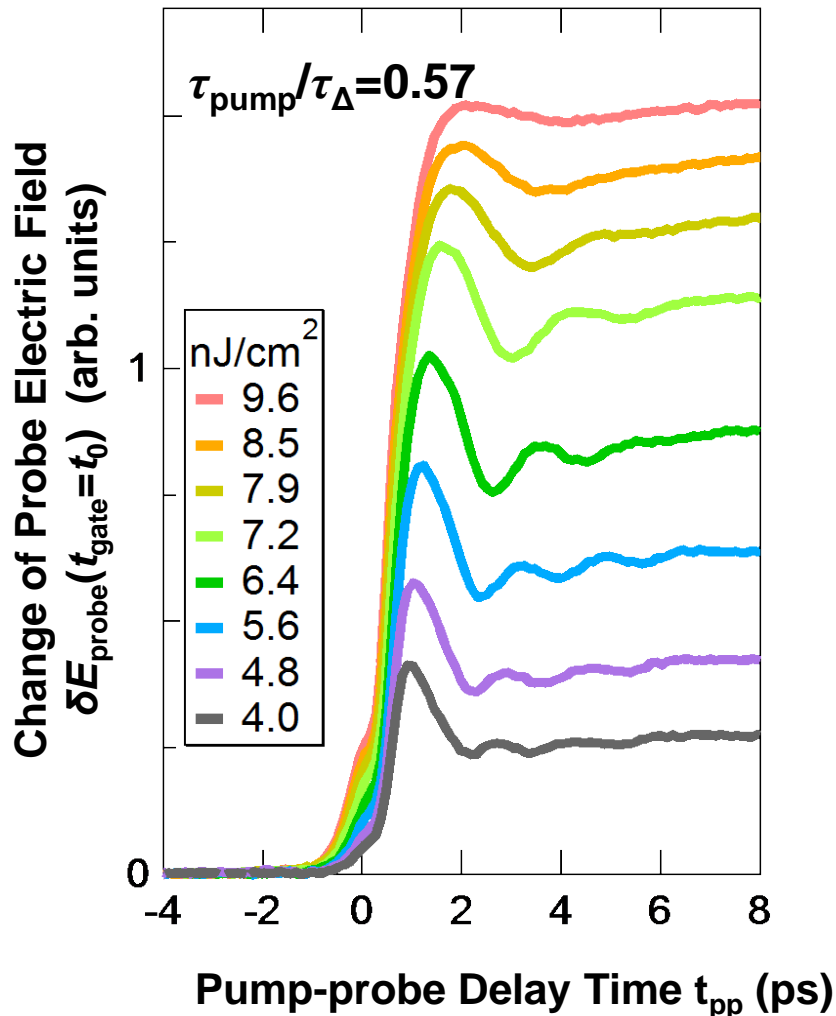
We fixed the gate delay at  $t_{\text{gate}} = t_0$  and measure the pump-probe delay dependence



# Dynamics after the THz pump pulse

Pump-induced change in the probe E-field

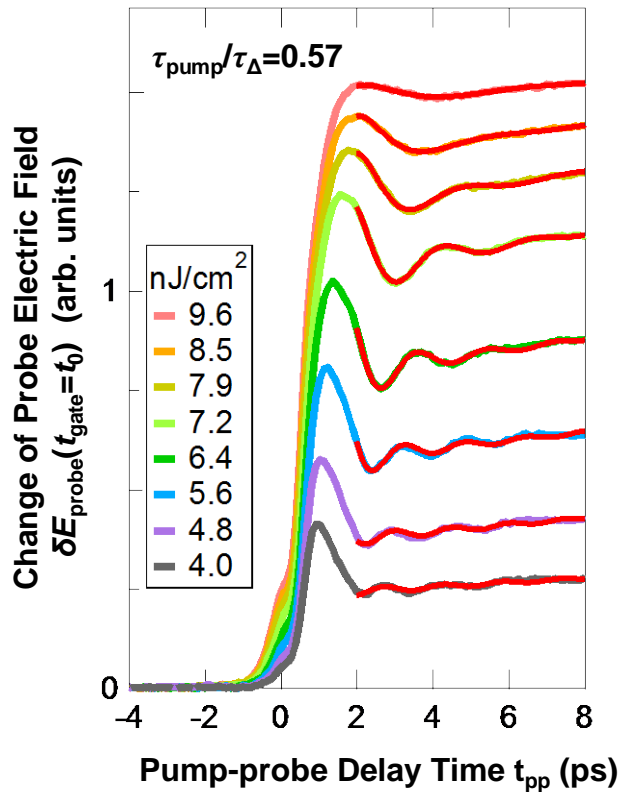
$$\delta E_{\text{probe}}(t_{\text{gate}}=t_0)$$



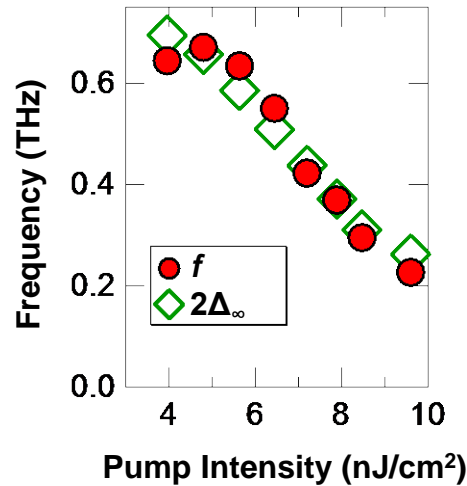
THz Pump irradiation ( $t_{\text{pp}} > 0$ )  
 $\Rightarrow$  rapid increase in  $E_{\text{probe}}$   
 $\Leftrightarrow$  reduction of  $\Delta$  due to the quasiparticle excitation

**A clear damped oscillation is observed**

# Oscillation frequency



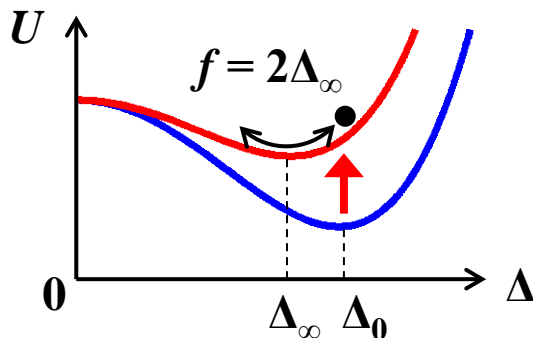
$$\delta E_{\text{probe}}(t_{\text{pp}}) = C_1 + C_2 t_{\text{pp}} + \frac{a}{(t_{\text{pp}})^b} \cos(2\pi f t_{\text{pp}} + \phi)$$



$2\Delta_{\infty}$ :  
asymptotic value of  
the order parameter  
estimated at  $t_{\text{pp}}=8\text{ps}$

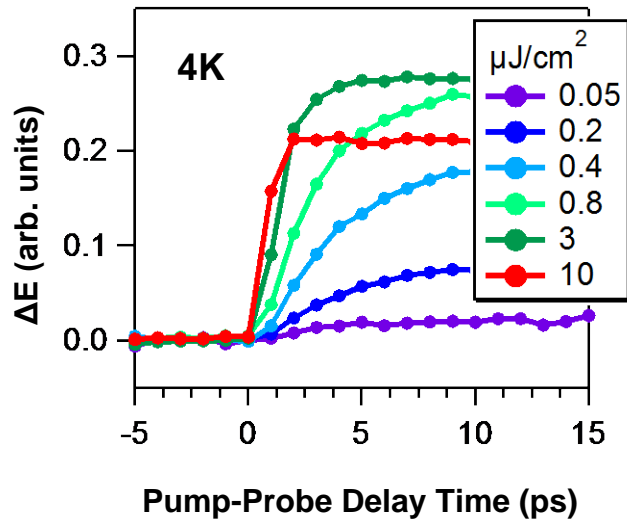
**oscillation frequency  $f = 2\Delta_{\infty}$**

characteristic to the Higgs mode behavior



R. Matsunaga, Y. Hamada, R. Shimano *et al.*,  
PRL **111**, 057002 (2013).

# Optical pump vs THz pump



## Optical Pump (800nm, 1.5eV 90fs)

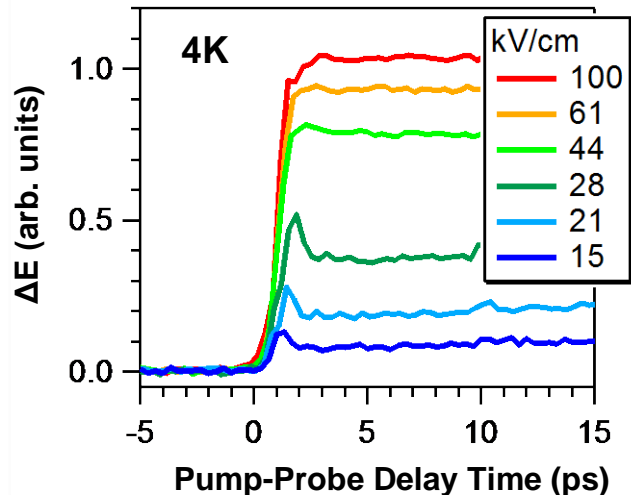
Slow rise , dependent of pump intensity

Photoexcitation of hot electron

⇒ phonon emission

⇒ pair breaking

⇒ reduction of order parameter

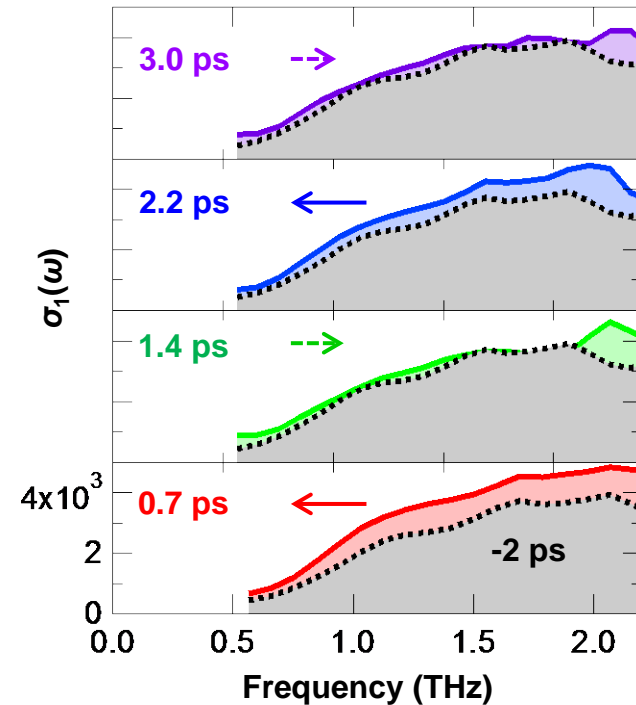
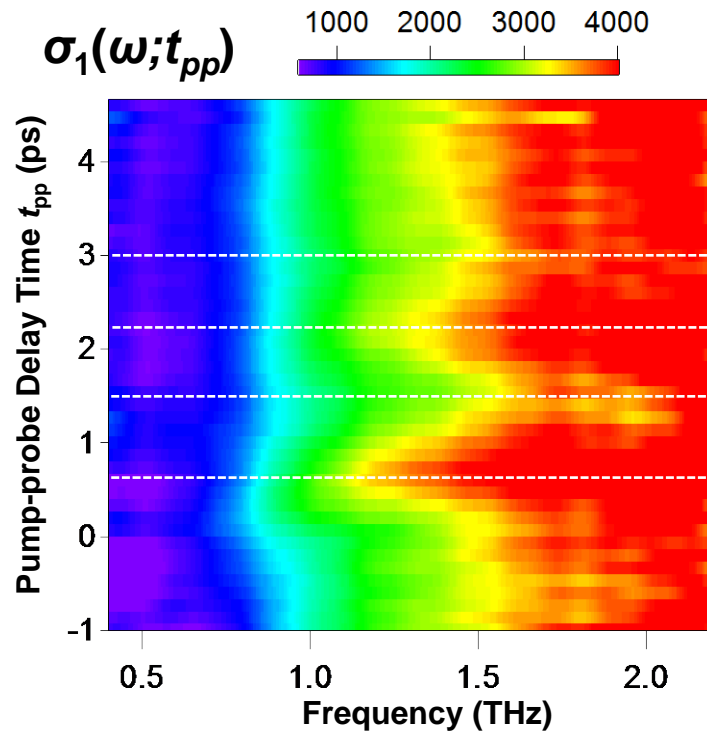


## THz pump

Fast rise, independent of pump intensity

Direct excitation of quasiparticle near the gap

# Time evolution of conductivity spectrum $\sigma_1(\omega; t_{pp})$

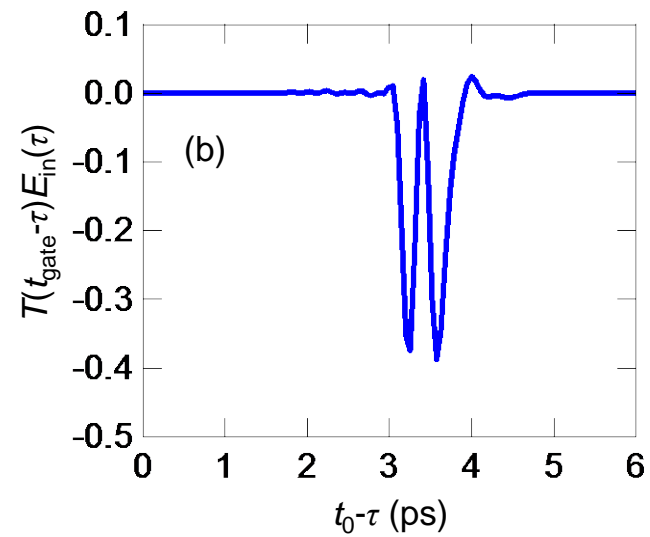
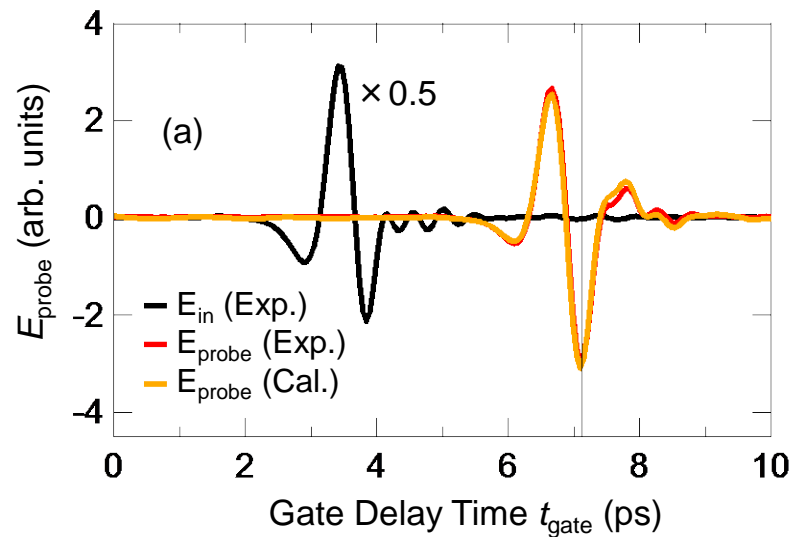


Temporal oscillation in the optical conductivity spectrum near the gap frequency

# Why the Higgs mode oscillation $(2\Delta)^{-1}$ is not smeared out in the probe transmittance?

$$T(\omega; \Delta) = \frac{1}{1 + n_{\text{sub}} + Z_0 d \sigma(\omega; \Delta)} \frac{4n_{\text{sub}} e^{i\Phi(\omega)}}{1 + n_{\text{sub}}}$$

$$E_{\text{probe}}(t_{\text{gate}}) = \int_{-\infty}^{t_{\text{gate}}} T(t_{\text{gate}} - \tau; \Delta) E_{\text{in}}(\tau) d\tau$$





# Samples with larger gaps

**Nb<sub>0.8</sub>Ti<sub>0.2</sub>N**

**12nm / Quartz**

$$2\Delta_0 = 0.72 \text{ THz}$$

$$\tau_{\text{pump}}/\tau_{\Delta} = 0.57$$

**Nb<sub>0.8</sub>Ti<sub>0.2</sub>N**

**30nm / Quartz**

$$2\Delta_0 = 1.1 \text{ THz}$$

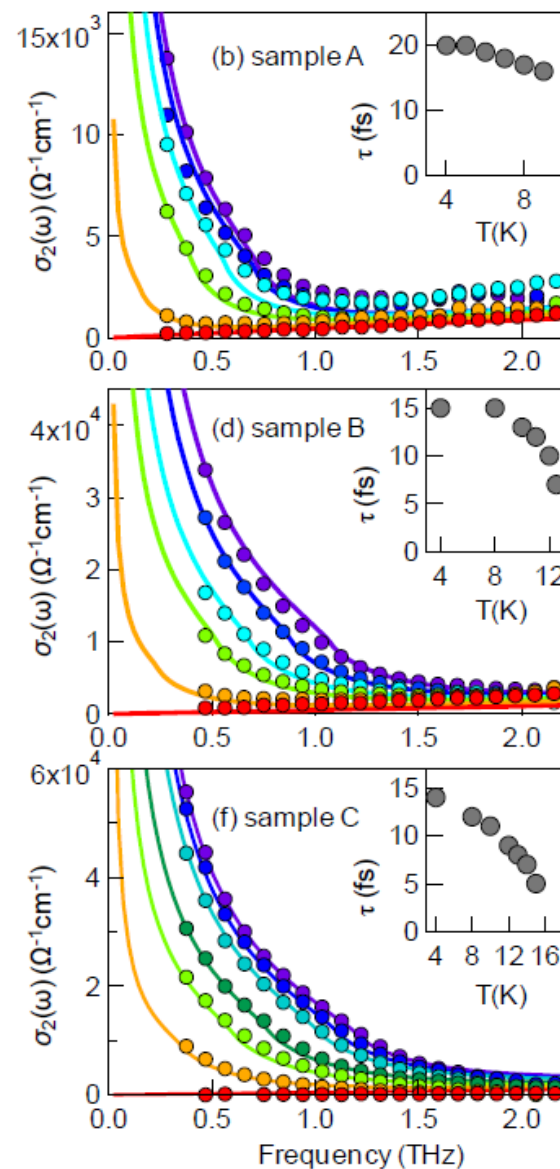
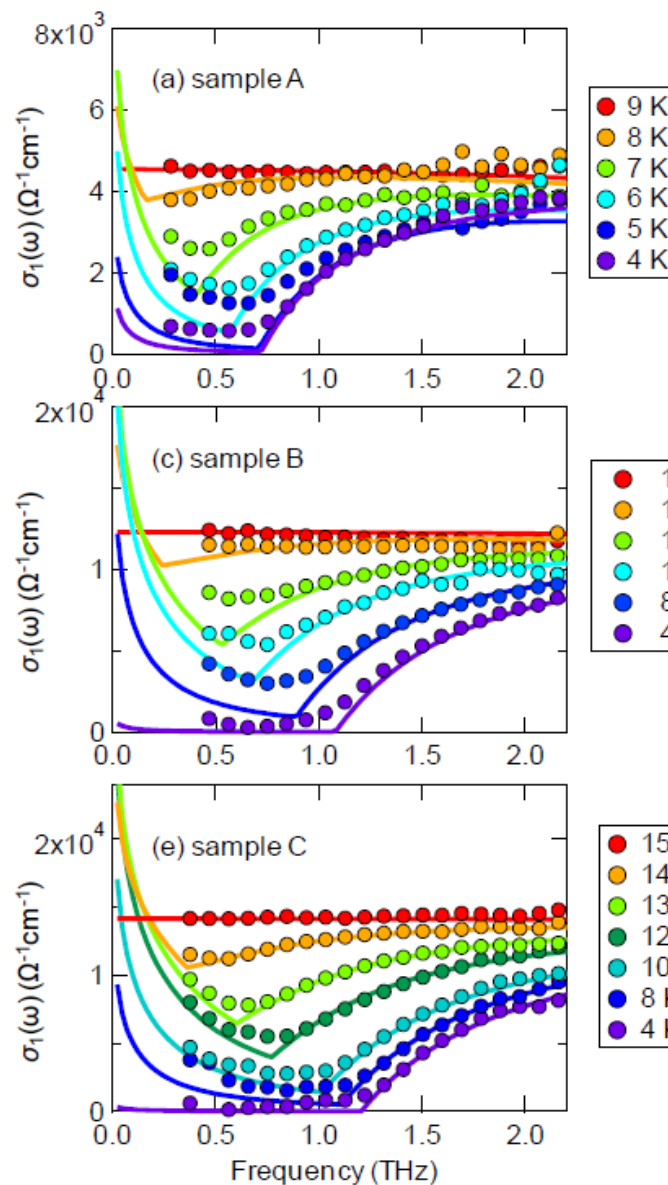
$$\tau_{\text{pump}}/\tau_{\Delta} = 0.81$$

**NbN**

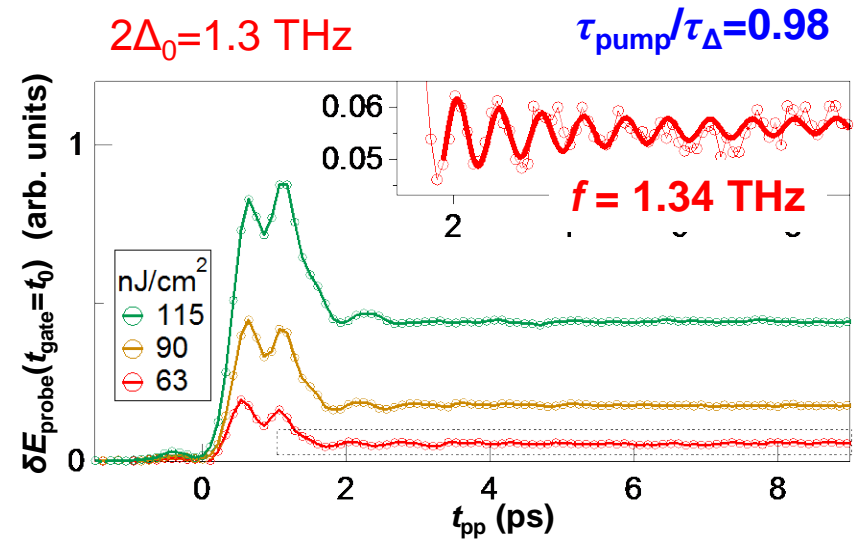
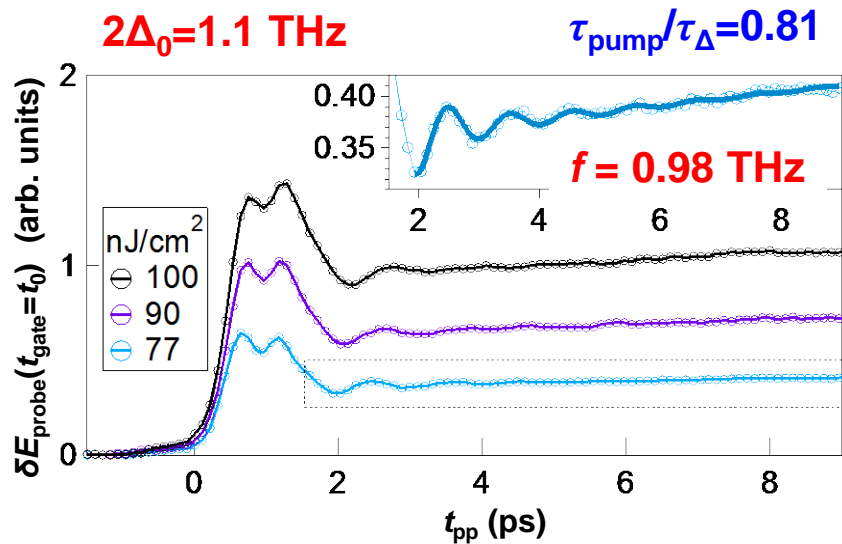
**24nm / MgO**

$$2\Delta_0 = 1.3 \text{ THz}$$

$$\tau_{\text{pump}}/\tau_{\Delta} = 0.98$$



# Higgs mode in larger gap samples $\tau_{\text{pump}}/\tau_{\Delta} \lesssim 1$

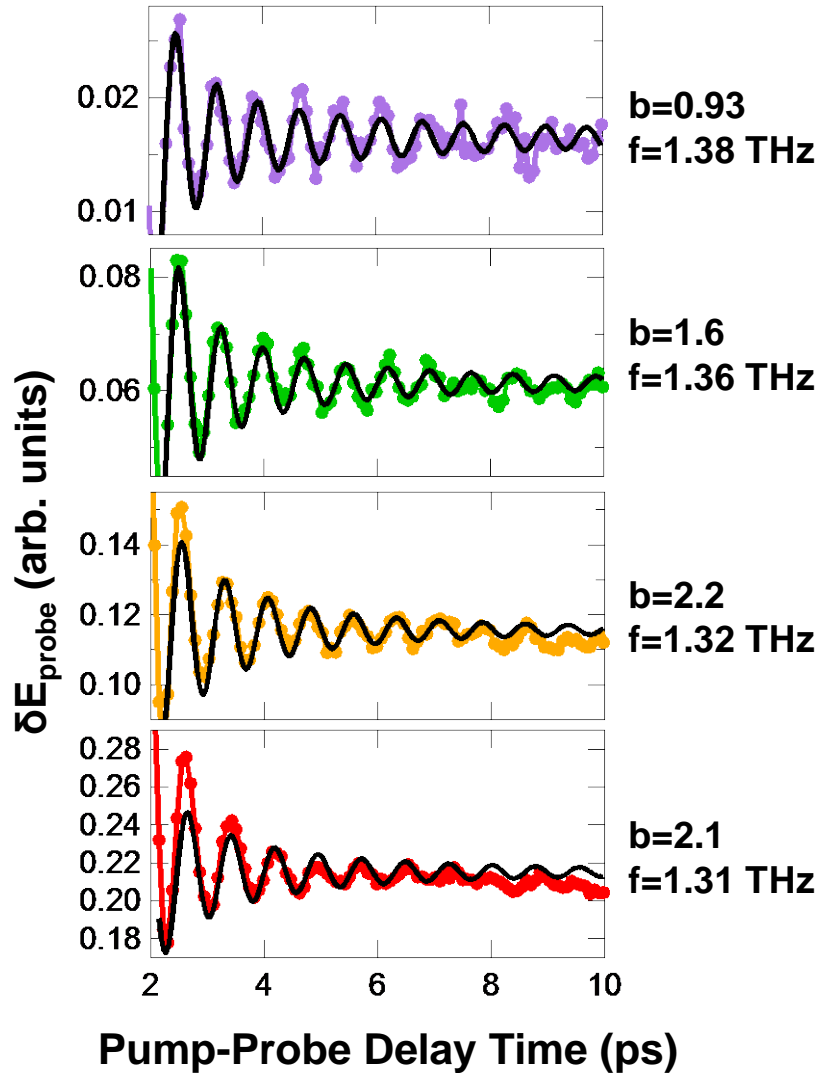


The Higgs mode is identified, although it is less prominent than the previous sample.

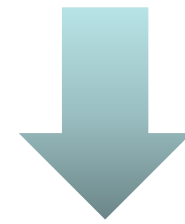
The oscillation frequency perfectly matches with the gap energy.

# Decay dynamics of Higgs mode

Weak  
excitation

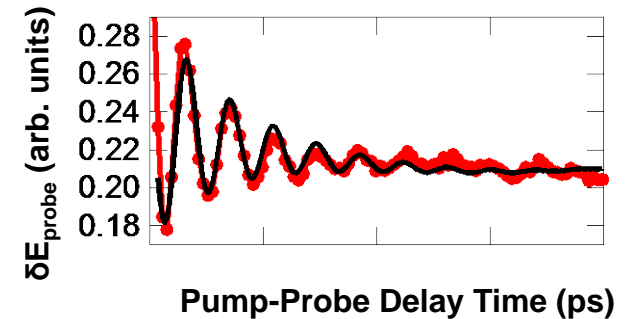


Power law decay

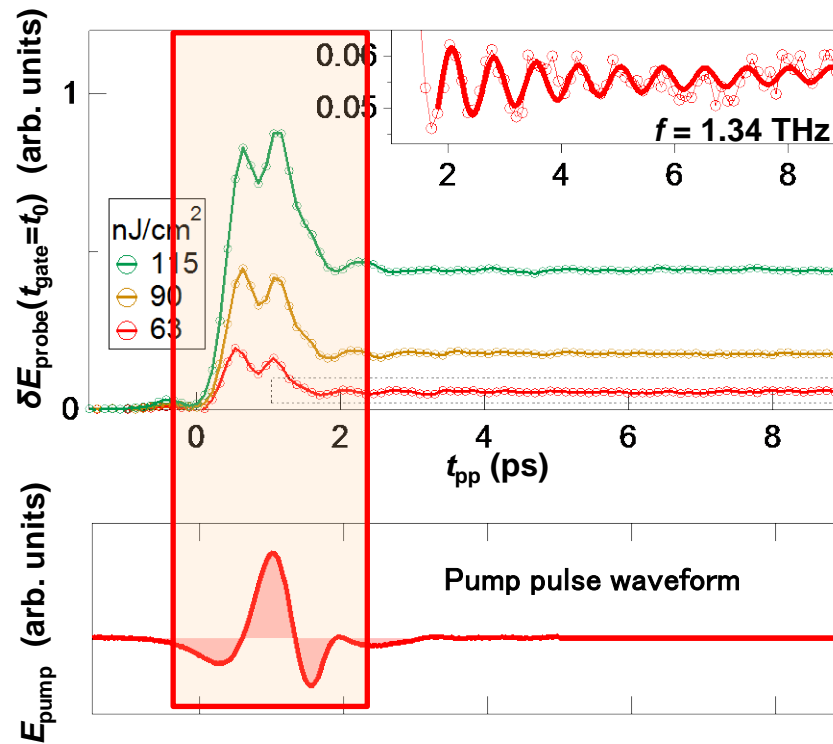


Exponential decay

Strong  
excitation



# Dynamics in the coherent excitation regime

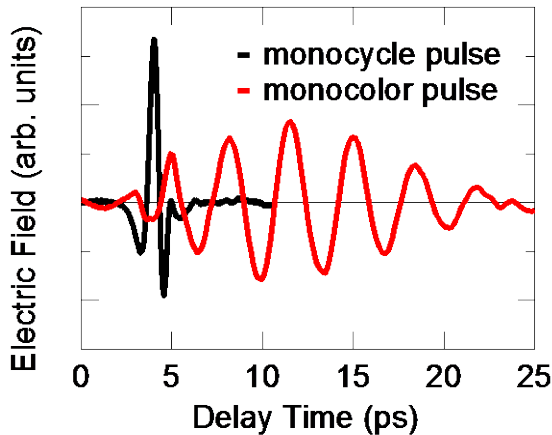


**What is happening during the irradiation of coherent pump field?**

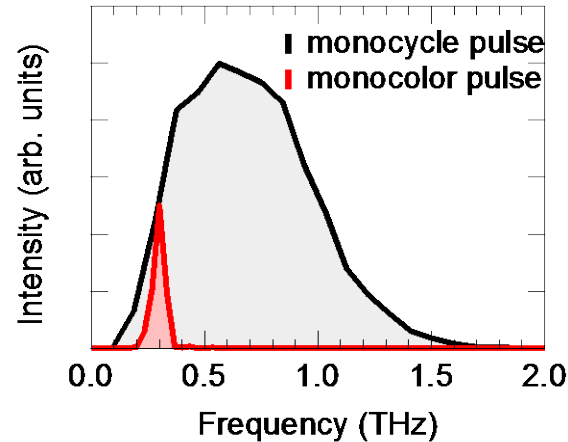
# Quasi-Monochromatic Excitation Experiments (Coherent Excitation Regime)

Quasi-monochromatic THz pulse ( $0.3\text{THz}$ , pulsewidth  $\sim 13\text{ps}$ )

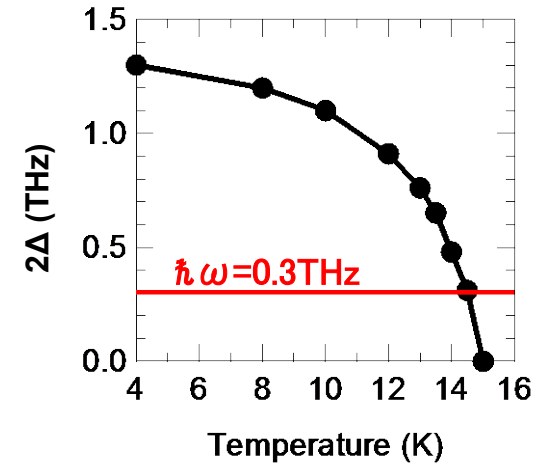
E-field waveform



Power Spectrum



Photon energy vs  
BCS gap

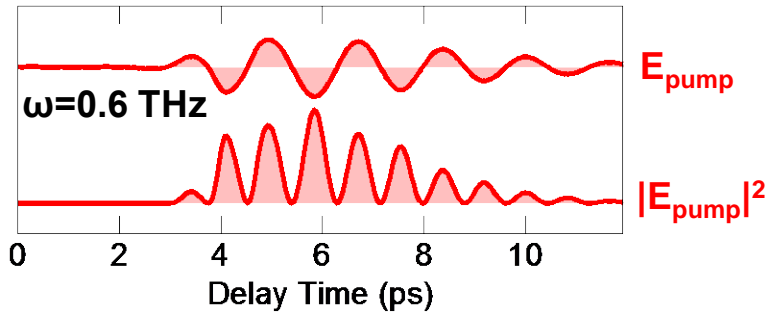


How does the BCS ground state respond to the strong electromagnetic field with  $\hbar\omega < 2\Delta$ ?

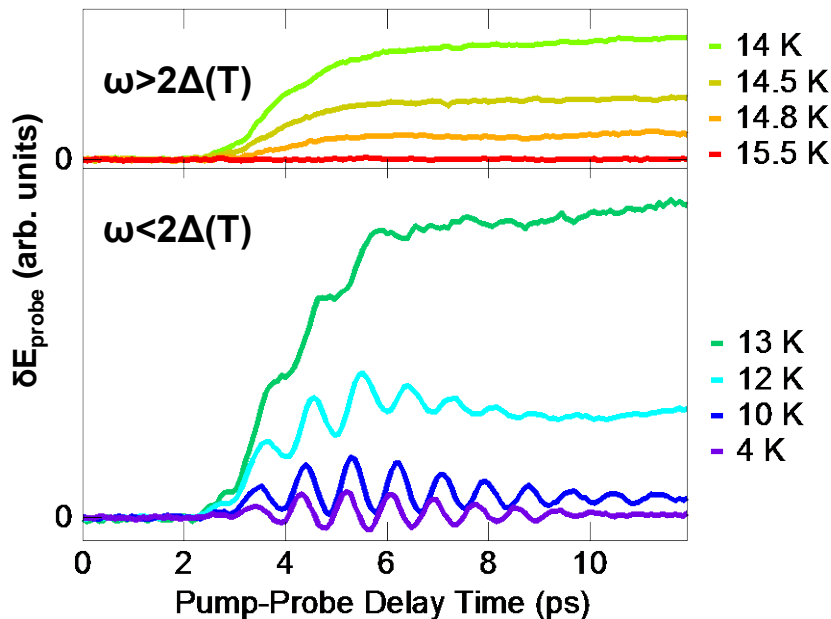
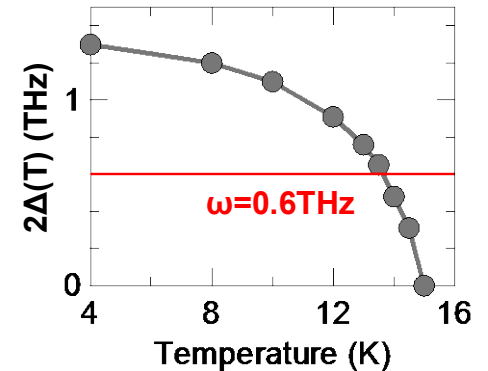
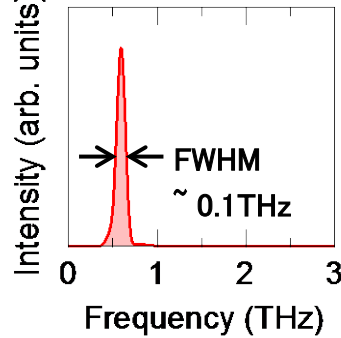
# Coherent Excitation Regime Experiments

$\omega=0.6\text{THz}$

3.5 kV/cm@peak



Pump power spectrum,



In case of  $\hbar\omega > 2\Delta(T)$

Reduction of order parameter  
due to QPs excitation

In case of  $\hbar\omega < 2\Delta(T)$

**$2\omega$  coherent oscillation of order  
parameter driven by the AC field of  $\omega$ ?**

# Anderson's pseudospin ( $\sigma_k$ ) representation

Anderson, Phys.Rev. **112**, 1900 (1958)

$$|\Psi_{\text{BCS}}\rangle = \prod_{\mathbf{k}} (u_{\mathbf{k}} + v_{\mathbf{k}} c_{\mathbf{k}\uparrow}^+ c_{-\mathbf{k}\downarrow}^+) |0\rangle$$

Pseudospin up :  $(k, -k)$  both empty

Pseudospin down:  $(k, -k)$  both occupied

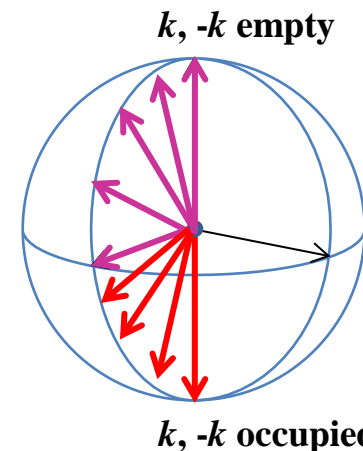
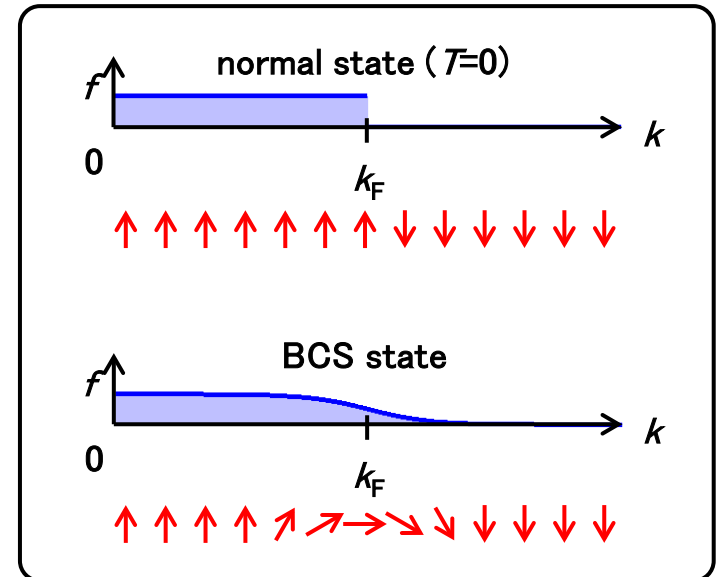
$$\mathcal{H}^{\text{BCS}} = \sum_{\mathbf{k}} \mathbf{b}_{\mathbf{k}}^{\text{eff}} \cdot \boldsymbol{\sigma}_{\mathbf{k}}$$

$$\mathbf{b}_{\mathbf{k}}^{\text{eff}} = (-\Delta', -\Delta'', \varepsilon_{\mathbf{k}})$$

: effective magnetic field for  $k$

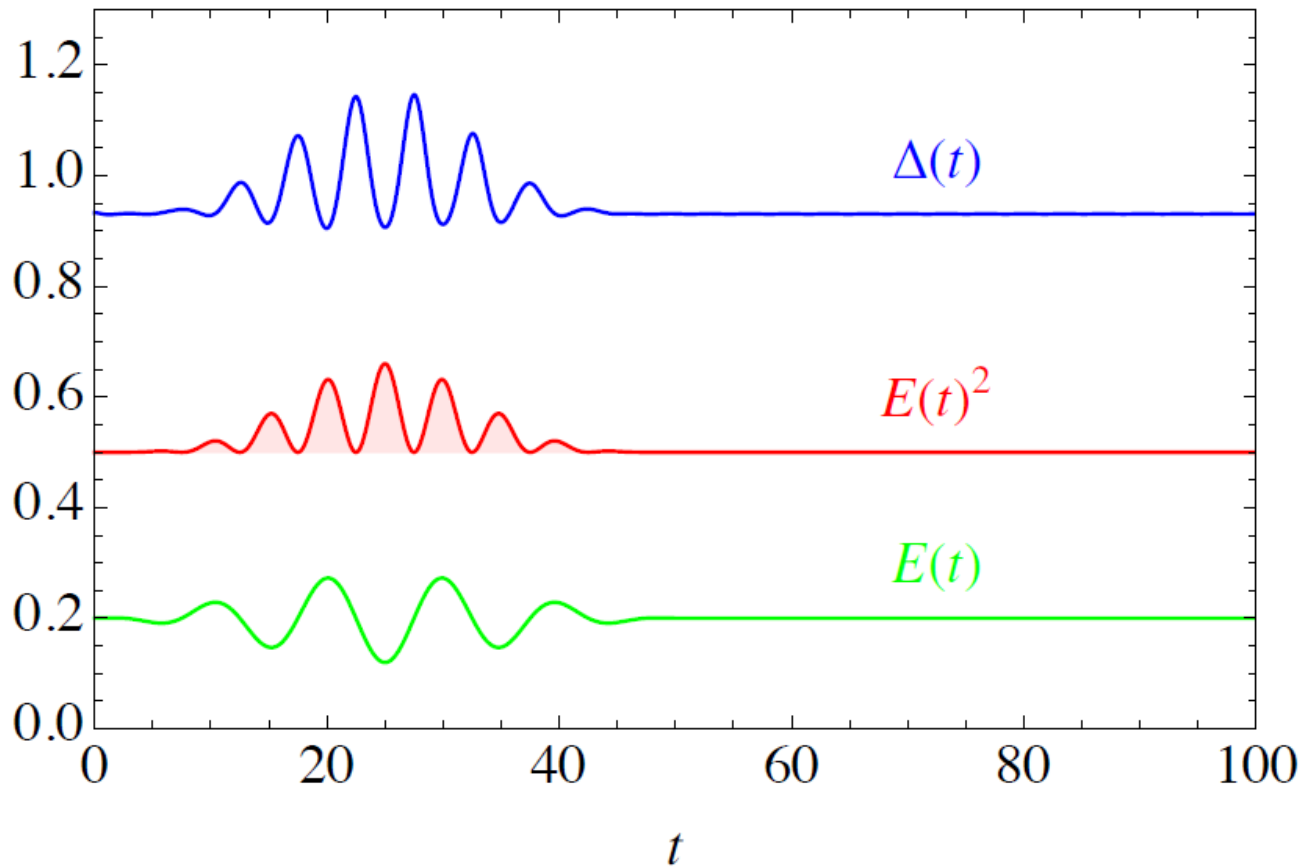
$$\Delta = \Delta' + i\Delta'' = U \sum_{\mathbf{k}} (\sigma_{\mathbf{k}}^x + i\sigma_{\mathbf{k}}^y)$$

$$\frac{d}{dt} \boldsymbol{\sigma}_{\mathbf{k}} = i[\mathcal{H}^{\text{BCS}}, \boldsymbol{\sigma}_{\mathbf{k}}] = 2\mathbf{b}_{\mathbf{k}}^{\text{eff}} \times \boldsymbol{\sigma}_{\mathbf{k}}$$



Time evolution of BCS state= motion of pseudospins under effective magnetic field

# Pseudospin dynamics : simulation with BdG equation



$$U = 3, \beta = 12, A = 0.2,$$
$$\Omega = 0.628, 2\Delta(0) = 1.87$$



# Summary

(1) We have observed the Higgs amplitude mode in s-wave superconductors NbTiN in a **non-adiabatic excitation regime with a monocycle THz pulse**.

R. Matsunaga, Y. Hamada, R. Shimano *et al.*, PRL **111**, 057002 (2013).

R. Matsunaga and R. Shimano, PRL **109**, 187002 (2012).

(2) Coherent  $2\omega$  oscillation of the order parameter was observed during the below-gap irradiation of multicycle THz pulse, which is well described by the precession of Anderson pseudospin.

(3) Strong THG is observed at  **$2\omega=2\Delta$**  (two-photon resonance of the Higgs mode).

R. Matsunaga *et al.*, to be published in Science

# Collaborators

## Experiment, Analysis & Simulation

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**Y. I. Hamada**

**A. Sugioka**

**H. Fujita**

## Theory

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**H. Aoki**

## Sample Fabrication

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**Y. Uzawa**

**H. Terai**

**Z. Wang**



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情報通信研究機構