Possible compositeness of the 125 GeV Higgs boson

M. Zubkov

ITEP (Moscow) & UWO (Canada)

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Abstract

The modification of the top – quark condensation model is suggested.

Higgs boson is composed of all quarks and leptons of the SM.

$$M_h = m_t / \sqrt{2} \approx 125 \, \mathrm{GeV}$$

The low energy effective action is calculated using zeta – regularization.



- 1. Nambu sum rules.
- 2. Conventional models of top quark condensation
- 3. Modification of top quark condensation scenario
- 4. Effective action and the Higgs boson mass
- 5. Experimental constraints
- 6. Effective U(12)xO(4) model at small distances

Nambu sum rules in BCS models

Energy gaps of scalar excitations (composed of the given fermion) are related to the energy gap of this fermion

$$\sum M_{H,i}^2 \approx 4M_f^2,$$



Example: BCS model of He-3 B

Cooper pairs are classified by the total momentum J. For each J = 0,1,2:

 $E_1^{(0)} = 0, \quad E_2^{(0)} = 2\Delta \qquad [E_u^{(J)}]^2 + [E_v^{(J)}]^2 = 4\Delta^2$ $E_1^{(1)} = 0, \quad E_2^{(1)} = 2\Delta$ $E_1^{(2)} = \sqrt{2/5} (2\Delta), \quad E_2^{(2)} = \sqrt{3/5} (2\Delta)$

P. N. Brusov and V. N. Popov, "Nonphonon branches of the Bose spectrum in the B phase of systems of the He3 type", JETP 51, 1217–1222 (1980).

Example 2: BCS model of QCD Sigma meson mass is related to the dynamical quark mass

 $M_{\sigma} \approx 2M_{quark}$



Conventional top quark condensation model

Weinberg – Salam model. Higgs particles are condensed (world trajectories of Higgs particles)



Top quark ----> composite Higgs boson



Top quark condensation – superconductivity dictionary

Standard model	S-wave superconductivity
Weinberg — Salam model	Ginzburg — Landau model
$L = \frac{1}{2} \int \left[\left(\partial_{\mu} - 2iA_{\mu} \right) H \right]^{+} \left(\partial^{\mu} - 2iA^{\mu} \right) H d^{3}x - \frac{\lambda}{4} \int \left(H ^{2} - v^{2} \right)^{2} d^{3}x$	$L = \frac{1}{2} \int \left[\left(\partial_{\mu} - 2iA_{\mu} \right) H \right]^{+} \left(\partial^{\mu} - 2iA^{\mu} \right) H d^{3}x - \frac{\lambda}{4} \int \left(H ^{2} - v^{2} \right)^{2} d^{3}x$
$A \in SU(2) \otimes U(1); H = \begin{pmatrix} 1 \\ h_2 \end{pmatrix}$	
Top — quark condensation model	BCS model
$S'_{I} = \frac{1}{M^{2}} \int d^{4}x \left(\bar{L}^{(tb)A}_{aK} t^{A}_{B,K} \right) \left(\bar{t}^{B}_{B,N} L^{(tb)B}_{aN} \right)$	$L = \int \bar{\psi} \left(i \left(\partial_{\mu} - iA_{\mu} \right) \gamma^{\mu} - m + \mu \gamma^{0} \right) \psi d^{3} x + L_{I}$
$M_{I}^{2} J \qquad (an - h, h) (h, h) (h$	$L_{I} = \frac{g^{2}}{M^{2}} \int (\bar{\psi} i\gamma_{5} C \bar{\psi}^{T}) (\psi^{T} i\gamma_{5} C \psi) d^{3}x; C = i\gamma^{0}\gamma^{2}$
Composite Higgs boson	Cooper pair

Weinberg – Salam model/Ginzburg – Landau Model Higgs – bosons/Cooper pairs are condensed (world trajectories)



Weinberg – Salam model $L = \frac{1}{2} \int \left[\left(\partial_{\mu} - 2iA_{\mu} \right) H \right]^{+} \left(\partial^{\mu} - 2iA^{\mu} \right) H d^{3}x - \frac{\lambda}{4} \int \left(|H|^{2} - v^{2} \right)^{2} d^{3}x$ $A \in SU(2) \otimes U(1); H = \begin{pmatrix} h_{1} \\ h_{2} \end{pmatrix}$

Ginzburg – Landau Model

 $L = \frac{1}{2} \int \left[\left(\partial_{\mu} - 2iA_{\mu} \right) H \right]^{+} \left(\partial^{\mu} - 2iA^{\mu} \right) H d^{3}x - \frac{\lambda}{4} \int \left(|H|^{2} - v^{2} \right)^{2} d^{3}x$

Top quark condensation model = analogue of BCS model for s-wave superconductor Top quarks ----> Higgs bosons 350 GeV Nambu sum rule $M_H^2 = 4m_t^2$ $S_{I}' = \frac{1}{M_{\tau}^{2}} \int d^{4}x \left(\bar{L}_{aK}^{(tb)A} t_{R,K}^{A} \right) \left(\bar{t}_{R,N}^{B} L_{aN}^{(tb)B} \right)$ $L_{aK}^{(tb)A} = \begin{pmatrix} t_{L,K}^{A} \\ b_{L,K}^{A} \end{pmatrix}$ $H_a \sim \bar{t}^B_{R,N} L^{(tb)B}_{aN}$ V.A. Miransky, Masaharu Tanabashi, and Koichi Yamawaki, Mod. Phys. Lett. A 4, 1043--1053 (1989); Bardeen 1990

New version of top quark condensation model

Four – fermion interaction with the non – trivial form – factors



All leptons and all quarks ----> composite Higgs boson







New version of the top quark condensation model Modified Nambu Sum rule. All quarks and leptons ----> Higgs bosons 125 GeV

 $N_{\rm total}M_H^2 = 4N_c m_t^2$

 $N_{\text{total}} = 2 \times (N_c + 1) \times N_g = 24, N_c = 3$ $N_g = 3$

- 1. The four fermion interaction involves all quarks and leptons
- 2. The four fermion interaction in nonlocal
- **3. At small distances it is highly symmetric**

4. At large distances it is complicated and produces different masses for different fermions

M.A.Zubkov, Phys. Rev. D 89 (2014), 075012

The fermions of the Standard Model

quarks

$$L^{1} = \begin{pmatrix} u_{L} \\ d_{L} \end{pmatrix}, \quad L^{2} = \begin{pmatrix} c_{L} \\ s_{L} \end{pmatrix}, \quad L^{3} = \begin{pmatrix} t_{L} \\ b_{L} \end{pmatrix}$$
$$R^{1}_{U} = u_{R}, \quad R^{2}_{U} = c_{R}, \quad R^{3}_{U} = t_{R}$$
$$R^{1}_{D} = d_{R}, \quad R^{2}_{D} = s_{R}, \quad R^{3}_{D} = b_{R}$$

leptons

$$\mathcal{L}^{1} = \begin{pmatrix} \nu_{L} \\ e_{L} \end{pmatrix}, \quad \mathcal{L}^{2} = \begin{pmatrix} \nu_{\mu L} \\ \mu_{L} \end{pmatrix}, \quad \mathcal{L}^{3} = \begin{pmatrix} \nu_{\tau L} \\ \tau_{L} \end{pmatrix}$$
$$\mathcal{R}^{1}_{N} = \nu_{R}, \quad \mathcal{R}^{2}_{N} = \nu_{\mu R}, \quad \mathcal{R}^{3}_{N} = \nu_{\tau R}$$
$$\mathcal{R}^{1}_{E} = e_{R}, \quad \mathcal{R}^{2}_{E} = \mu_{R}, \quad \mathcal{R}^{3}_{E} = \tau_{R}$$

Non – local four – fermion interaction



$$S_{I} = \frac{V}{M_{I}^{2}} \sum_{\mathbf{a}} \sum_{q=p-k=p'-k'} \left(\bar{L}_{b}^{\mathbf{a}}(p) R_{U}^{\mathbf{a}}(k) G_{U}^{\mathbf{a}}(p,k) + \bar{\mathcal{L}}_{b}^{\mathbf{a}}(p) \mathcal{R}_{N}^{\mathbf{a}}(k) G_{N}^{\mathbf{a}}(p,k) \right. \\ \left. + \bar{R}_{D}^{\mathbf{a}}(p) L_{c}^{\mathbf{a}}(k) \epsilon_{bc} G_{D}^{\mathbf{a}}(p,k) + \bar{\mathcal{R}}_{E}^{\mathbf{a}}(p) \mathcal{L}_{c}^{\mathbf{a}}(k) \epsilon_{bc} G_{E}^{\mathbf{a}}(p,k) \right) \\ \left. \left(\bar{G}_{D}^{\mathbf{a}}(p',k') \bar{L}_{d}^{\mathbf{a}}(k') R_{D}^{\mathbf{a}}(p') \epsilon_{bd} + \bar{G}_{E}^{\mathbf{a}}(p',k') \bar{\mathcal{L}}_{d}^{\mathbf{a}}(k') \mathcal{R}_{E}^{\mathbf{a}}(p') \epsilon_{bd} \right. \\ \left. + \bar{G}_{U}^{\mathbf{a}}(p',k') \bar{R}_{U}^{\mathbf{a}}(k') L_{b}^{\mathbf{a}}(p') + \bar{G}_{N}^{\mathbf{a}}(p',k') \bar{\mathcal{R}}_{N}^{\mathbf{a}}(k') \mathcal{L}_{b}^{\mathbf{a}}(p') \right),$$

Formfactor for all fermions except for the top quark

$$\begin{array}{rcl} G^{\mathbf{a}}_{a}(p,k) &=& g^{\mathbf{a}}_{a}(q^{2},p^{2},k^{2}) \rightarrow 1 \\ && (|q^{2}|,|p^{2}|,|k^{2}| \sim M_{Z}^{2} \sim [90\,\mathrm{GeV}]^{2}) \\ G^{\mathbf{a}}_{a}(p,k) &=& g^{\mathbf{a}}_{a}(q^{2},p^{2},k^{2}) \rightarrow 0 \quad (|q^{2}|,|p^{2}|,|k^{2}| \ll M_{Z}^{2}) \end{array}$$

for the top quark $G_t(p,k) \equiv G_U^3(p,k) \approx 1$

Distances ~ 1/100 GeV; momenta transfer ~ 100 GeV

$$S_{I} = -V \sum_{\mathbf{a}} \sum_{q=p-k} \left[\bar{L}_{b}^{\mathbf{a}}(p) R_{U}^{\mathbf{a}}(k) H^{b}(q) + \bar{\mathcal{L}}_{b}^{\mathbf{a}}(p) \mathcal{R}_{N}^{\mathbf{a}}(k) H^{b}(q) + (h.c.) \right]$$
$$-V \sum_{\mathbf{a}} \sum_{q=p-k} \left[\bar{L}_{c}^{\mathbf{a}}(k) R_{D}^{\mathbf{a}}(p) \bar{H}^{b}(q) \epsilon_{bc} + \bar{\mathcal{L}}_{c}^{\mathbf{a}}(k) \mathcal{R}_{E}^{\mathbf{a}}(p) \bar{H}^{b}(q) \epsilon_{bc} + (h.c.) \right]$$
$$\left(\left| (p-k)^{2} \right|, \left| p^{2} \right|, \left| k^{2} \right| \sim M_{Z}^{2} \right)$$

The field of composite Higgs boson H

$$S = -V \sum_{p} H^+(p) H(p) M_I^2$$

Effective four – fermion interaction is obtained after the integration over H

Distances >> 1/100 GeV; momenta transfer << 100 GeV

$$S_I' = -\int d^4x \left(\bar{L}_{aK}^{(tb)A} t_{R,K}^A H^a + (h.c.) \right)$$
$$L_{aK}^{(tb)A} = \begin{pmatrix} t_{L,K}^A \\ b_{L,K}^A \end{pmatrix}, \quad t_{R,K}^A$$



Effective action (leading 1/Nc order) using zeta – **regularization** *M.A.Zubkov, Phys. Rev. D 89 (2014), 075012* **Quadratic divergences are absent ; the same for the dimensional** *regularization ; ordinary cutoff regularization gives different result*

$$S[H] = \int d^4x \left(Z_h^2 H^+(x) (-D^2 w (D^2)) H(x) - \frac{1}{8} (|H|^2 - v^2)^2 \right)$$

$$D = \partial + iB$$
 with $B = B^a_{SU(2)}\sigma^a + YB_{U(1)}$

$$Z_h^2 \approx \frac{N_{\text{total}}}{16\pi^2} \log \frac{\mu^2}{m_t^2} \qquad N_{\text{total}} = 2 \times (N_c + 1) \times N_g = 24, N_c = 3$$
$$w(-p^2) \to 1 \left(|p^2| \sim [90 \,\text{GeV}]^2 \right);$$
$$w(-p^2) \to N_c/N_{\text{total}} = 1/8 \left(|p^2| \ll [90 \,\text{GeV}]^2 \right)$$
$$M_H^2 \approx 4N_c m_t^2/N_{\text{total}} = m_t^2/2$$

Scale of the hidden interaction $\mu \sim 5 \text{ TeV}$

Effective potential for the gauge field $||B||^2 = -(1,0)B^2(1,0)^T = -((B^3_{SU(2)} - B_{U(1)})^2 + [B^1_{SU(2)}]^2 + [B^2_{SU(2)}]^2).$

$$V_B \approx \frac{N_{\text{total}}}{16\pi^2} m_t^2 \log \frac{\mu^2}{m_t^2} w(\|B\|^2) \|B\|^2$$

 $w(M_Z^2) \approx 1$

$$S_B \approx \frac{\eta^2}{2} \|B\|^2 \approx \frac{N_{\text{total}}}{16\pi^2} m_t^2 \log \frac{\mu^2}{m_t^2} \|B\|^2$$

 $\eta^2 \approx 2Z_h^2 v^2 = \frac{2N_{\text{total}}}{16\pi^2} m_t^2 \log \frac{\mu^2}{m_t^2}$ η should be equal to $\approx 246 \text{ GeV}$

Scale of the hidden interaction $\mu \sim 5$ TeV

Branching ratios and Higgs production cross sections $h \rightarrow gg, \gamma\gamma, ZZ, WW, \bar{b}b, \bar{c}c, \bar{\tau}\tau$ $L_{eff} = \frac{2m_W^2}{\eta}hW_{\mu}^+W_{\mu}^- + \frac{m_Z^2}{\eta}hZ_{\mu}Z_{\mu} + c_g\frac{\alpha_s}{12\pi\eta}hG_{\mu\nu}^aG_{\mu\nu}^a$ $+c_\gamma\frac{\alpha}{\pi\eta}hA_{\mu\nu}A_{\mu\nu} - c_b\frac{m_b}{\eta}h\bar{b}b - c_c\frac{m_c}{\eta}h\bar{c}c - c_\tau\frac{m_\tau}{\eta}h\bar{\tau}\tau$ SM gives $c_q \simeq 1.03, c_\gamma \approx -0.81$

For the particular form of the form factors (all but the t quark)

$$G_a^{\mathbf{a}}(p,k) = g_a^{\mathbf{a}}(q^2, p^2, k^2) = \begin{cases} 1 \text{ for } |q^2|, |p^2|, |k^2| > M_0^2 \\ \kappa_a^{\mathbf{a}} << 1 \text{ otherwise} \end{cases}$$

for the top quark

 $G_t(p,k) \equiv G_U^3(p,k) \approx 1$

 $c_b \approx g(M_H^2, m_b^2, m_b^2) / \kappa_D^3$ $c_c \approx g(M_H^2, m_c^2, m_c^2) / \kappa_U^2$ $c_b \approx g(M_H^2, m_\tau^2, m_\tau^2) / \kappa_E^3$

Branching ratios and Higgs production cross sections

For the particular form of the form factors (all but the t quark)

 $G_a^{\mathbf{a}}(p,k) = g_a^{\mathbf{a}}(q^2, p^2, k^2) = \begin{cases} 1 \text{ for } |q^2|, |p^2|, |k^2| > M_0^2 \\ \kappa_a^{\mathbf{a}} << 1 \text{ otherwise} \end{cases}$ corrections $\delta c_g^{(f)} = \frac{2m_f}{M_H} \delta r_g^{(f)} \qquad \delta c_{\gamma}^{(b,c,\tau)} = \left(3(1/3)^2 m_b + 3(2/3)^2 m_c + m_\tau\right) \frac{2}{6M_H} \delta r_g$ $\delta r_g^{(f)} \approx \frac{3\sqrt{2}}{\tau_0} \left(\tau_0 - \frac{\tau_0 - 1}{4} \left[\log \left| \frac{\sqrt{1 - 1/\tau_0} + 1}{\sqrt{1 - 1/\tau_0} - 1} \right| \right]^2 \right)$ $\tau_0 = \frac{M_H^2}{4M_e^2}$ $-1.0 < c_a/c_a^{(SM)} < +1.0$ $M_0 = 35 \text{ GeV}.$ $M_0 = 10 {\rm ~GeV}$ $1.4 > c_{\gamma}/c_{\gamma}^{(SM)} > 1.0$

Branching ratios and Higgs production cross – sections (ATLAS) Phys. Lett. B 726 (2013) 88



Branching ratios and Higgs production cross – sections (CMS) JHEP 06 (2013) 081



Effective theory at small distances ~1/100GeV

At small distances (large momenta transfer)

$$S_{I} = -\int d^{4}x \Big(\bar{L}_{1i}^{\mathbf{a}A} R_{1i}^{\mathbf{a}A} h + \bar{R}_{2i}^{\mathbf{a}A} L_{2i}^{\mathbf{a}A} h + (h.c.) \Big)$$

For example, for the quarks of the first generation:

$$S_I^{(ud)} = -\int d^4x \left(\bar{u}_L^A u_R^A h + \bar{d}_R^A d_L^A h + (h.c.) \right)$$

All leptons and all quarks ----> composite Higgs boson All fermions interact in an equal way



Standard Model fermions as components of Majorana spinor Nambu – Gorkov spinor

$$\mathbf{L}_{aiU}^{\mathbf{a}A} = \begin{pmatrix} L_{ai}^{\mathbf{a}A} \\ \bar{L}_{c'i}^{\mathbf{a}B} \epsilon_{c'a} \epsilon^{BA} \end{pmatrix}, \ \mathbf{R}_{aiU}^{\mathbf{a}A} = \begin{pmatrix} \bar{R}_{bi}^{\mathbf{a}B} \epsilon_{ba} \epsilon^{BA} \\ R_{a,i}^{\mathbf{a}A} \end{pmatrix}$$

Spinor representation of O(4) = SU(2)xSU(2)

$$\Psi_{i}^{\mathbf{a}} = \begin{pmatrix} \mathbf{L}_{ai}^{\mathbf{a}} \\ \mathbf{R}_{ai}^{\mathbf{a}} \end{pmatrix} \qquad \bar{\Psi}_{i}^{\mathbf{a}} = \left(\Psi_{i}^{\mathbf{a}}\right)^{T} i\gamma^{2}\gamma^{5}\gamma^{0}\Gamma^{4}\Gamma^{2}\Gamma^{5}$$

$$\bar{\mathbf{L}}_{ai}^{\mathbf{a}} = \epsilon_{ab} \left(\mathbf{L}_{bi}^{\mathbf{a}} \right)^T i \gamma^2 \gamma^5 \gamma^0, \ \bar{\mathbf{R}}_{ai}^{\mathbf{a}} = \epsilon_{ab} \left(\mathbf{R}_{bi}^{\mathbf{a}} \right)^T i \gamma^2 \gamma^5 \gamma^0$$

The Standard Model gauge group

$$e^{i\theta} \in U(1)_Y \subset SU(2)_R, \ U^{(L)} \in SU(2)_L$$
$$U^{(R)} = \begin{pmatrix} e^{i\theta} & 0\\ 0 & e^{-i\theta} \end{pmatrix} \in SU(2)_R \qquad Q \in SU(3)$$
$$V = \begin{pmatrix} Qe^{i\theta/3} & 0\\ 0 & e^{-i\theta} \end{pmatrix} \in SU(4)_{\text{Pati Salam}} \subset U(12)$$

Action on the spinor

$$\Psi_i^{\mathbf{a}} \to \left(V_{ij} \frac{1 + \Gamma^5 \gamma^5}{2} + \bar{V}_{ij} \frac{1 - \Gamma^5 \gamma^5}{2} \right) \left(\begin{array}{cc} U^{(L)} & 0\\ 0 & U^{(R)} \end{array} \right) \Psi_j^{\mathbf{a}}$$

Global symmetry group is O(4)xU(12) = SU(2)xSU(2)xU(12)

Distances ~ 1/100 GeV; momenta transfer ~ 100 GeV

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Unitary gauge fixing $\bar{\Psi}_{i}^{\mathbf{a}} = \left(\Psi_{i}^{\mathbf{a}}\right)^{T} i\gamma^{2}\gamma^{5}\gamma^{0}\Gamma^{4}\Gamma^{2}\Gamma^{5}$ $S_{I} = \frac{1}{2} \int d^{4}x \left(\bar{\Psi}_{i}^{\mathbf{a}}\gamma^{5}\Gamma^{5}\mathbf{H}\Psi_{i}^{\mathbf{a}}\right)$ $S_{I} = -\frac{1}{2} \int d^{4}x \left(\bar{L}_{bi}^{\mathbf{a}A}R_{ai}^{\mathbf{a}A}H_{ab} + \bar{R}_{ci}^{\mathbf{a}A}L_{c'i}^{\mathbf{a}A}\epsilon_{c'b}\epsilon_{ca}H_{ab} + (h.c.)\right)$

The field of composite $H_{ab} = \mathbf{h}^4 \delta_{ab} + i \sum_{K=1,2,3} \mathbf{h}^K \tau_{ab}^K = H U_{\mathbf{h}}$ Higgs boson

$$L_{ai}^{\mathbf{a}A} \to \begin{bmatrix} U_{\mathbf{h}} \end{bmatrix}_{ab} L_{bi}^{\mathbf{a}A} \qquad U_{\mathbf{h}} = \begin{bmatrix} \hat{\mathbf{h}}^{4}\mathbf{1} + i \sum_{K=1,2,3} \hat{\mathbf{h}}^{K} \tau^{K} \end{bmatrix}_{ab} \in SU(2)$$

$$\begin{aligned} H_{ab} &= H\delta_{ab} \\ H &= v + h \in \mathcal{R} \end{aligned} \qquad H = \sqrt{\sum_{k=1,2,3,4} \mathbf{h}_k^2}, \quad \hat{\mathbf{h}}^K = \frac{1}{H} \mathbf{h}^K \end{aligned}$$

Effective interaction between fermions and the h - boson

$$S_{I} = -\int d^{4}x \Big(\bar{L}_{1i}^{\mathbf{a}A} R_{1i}^{\mathbf{a}A} h + \bar{R}_{2i}^{\mathbf{a}A} L_{2i}^{\mathbf{a}A} h + (h.c.) \Big)$$

Due to the unknown strong dynamics the Higgs boson is composed of the known leptons and quarks

The interaction between the composite Higgs boson and the SM fermions is U(12)xO(4) symmetric at small distances ~ 1/[100GeV]

$$M_h = m_t / \sqrt{2} \approx 125 \, \mathrm{GeV}_t$$

(cancellation of quadratic divergences is required) At large distances the new interaction is complicated and results in the hierarchy of fermion masses

More detailed view of how this unknown hidden interaction might look like

