

# Behind the Scenes of High Temperature Superconductivity: Cuprates and Iron Pnictides

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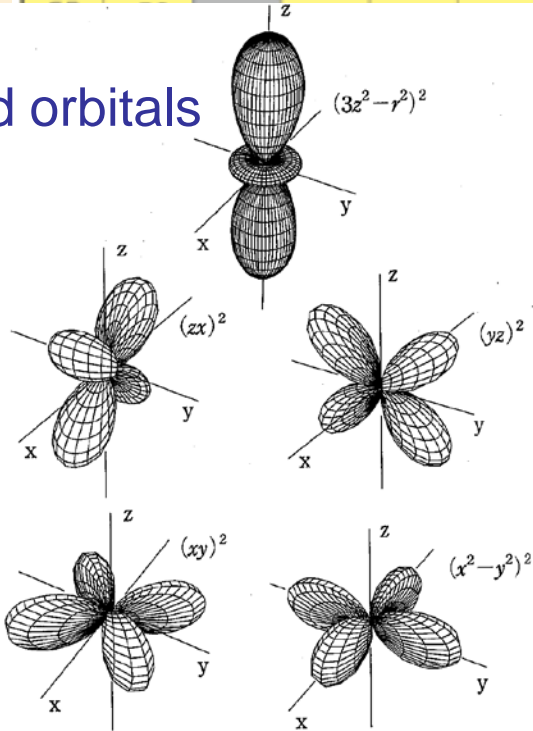
Eiji Kaneshita

Takao Morinari

# 3d transition-metal compounds

1																	18	
1 H													13	14	15	16	17	2
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne	
11 Na	12 Mg	3	4	5	6	7	8	9	10	11	12	13 Al	14 Si	15 P	16 S	17 Cl	18 Ar	
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr	
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe	
75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn							
107 Bh	108 Hs	109 Mt																

3d orbitals



Localized and itinerant natures compete.



Complicated interactions among the internal degrees of freedom of electrons:  
**charge, spin, orbital**

# Cuprate superconductors

1																						18
1	2												5	6	7	8	9	10				2
H	Li												B	C	N	O	F	Ne				He
3	4												13	14	15	16	17	18				
Li	Be												Al	Si	P	S	Cl	Ar				
11	12	3	4	5	6	7	8	9	10	11	12											
Na	Mg	21	22	23	24	25	26	27	28	29	30											
19	20	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn											
K	Ca																					
37	38	39	40	41	42	43	44	45	46	47	48											
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd											
55	56	57~	72	73	74	75	76	77	78	79	80											
Cs	Ba	71	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg											
87	88	89~	104	105	106	107	108	109	110	111	112											
Fr	Ra	103	Rf	Db	Sg	Bh	Hs	Mt														

1986 High-temperature superconductivity

$T_c \sim 160\text{K}$  under pressure

Oxides, two-dimensionality → superconductivity

# Iron-pnictide superconductors

1																		18
1	2												5	6	7	8	9	10
H	He												B	C	N	O	F	Ne
3	4												13	14	15	16	17	18
Li	Be												Al	Si	P	S	Cl	Ar
11	12												31	32	33	34	35	36
Na	Mg	3	4	5	6	7	8	9	10	11	12		Ga	Ge	As	Se	Br	Kr
19	20	21	22	23	24	25	26	27	28	29	30		49	50	51	52	53	54
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn		In	Sn	Sb	Te	I	Xe
37	38	39	40	41	42	43	44	45	46	47	48		81	82	83	84	85	86
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd		Tl	Pb	Bi	Po	At	Rn
55	56	57~	72	73	74	75	76	77	78	79	80							
Cs	Ba	71	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg							
87	88	89~	104	105	106	107	108	109	110	111	112							
Fr	Ra	103	Rf	Db	Sg	Bh	Hs	Mt										

2008 Hosono's Group at TIT

$$T_c \sim 55\text{K}$$

Fe: typical magnetic metal → superconductivity

# OUTLINE

## Motivation

Similarity and difference between cuprate and iron-pnictide superconductors

## Cuprates

- Ionic material
- doped Mott insulator

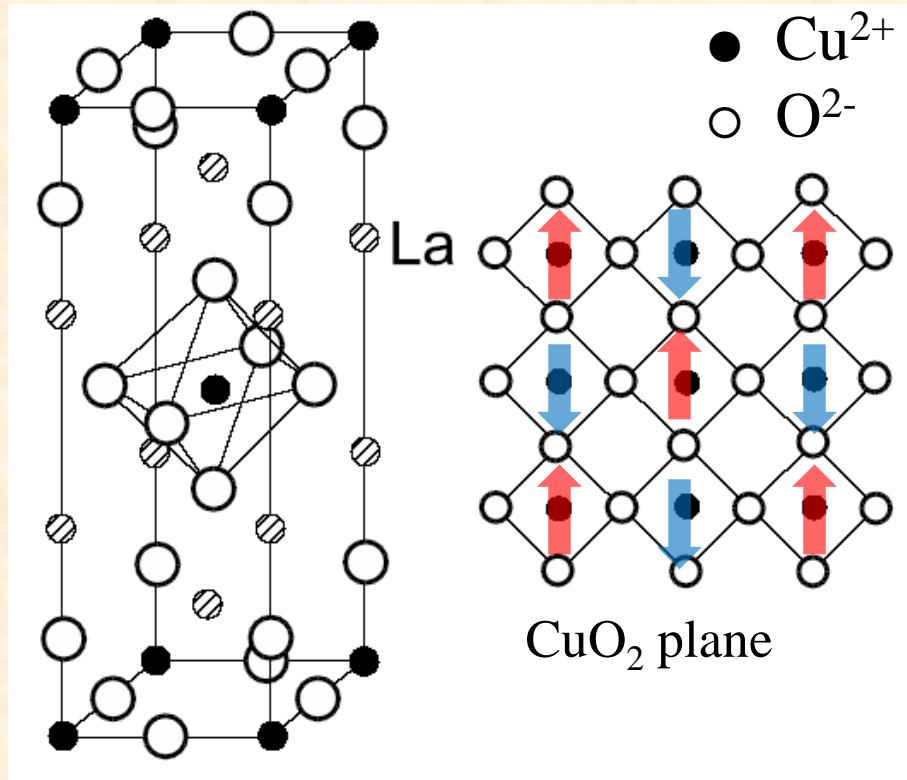
## Iron pnictides

- band material
- spin-density wave (SDW)

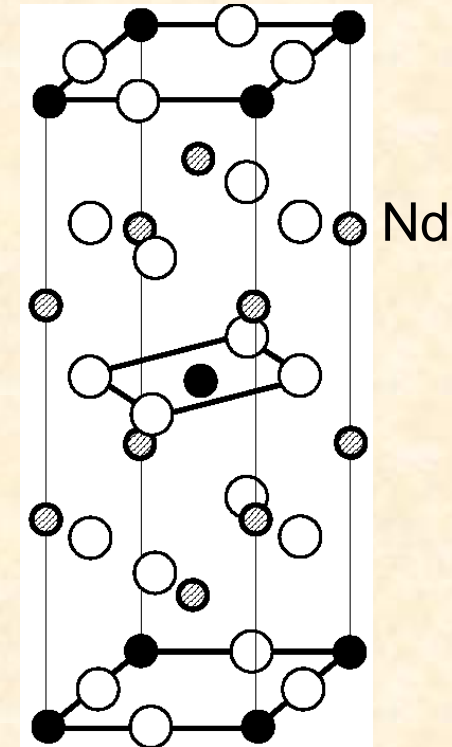
## Summary and perspectives

# Crystal structure of high $T_c$ cuprates

$\text{La}_2\text{CuO}_4$  (hole-doping)



$\text{Nd}_2\text{CuO}_4$  (electron-doping)



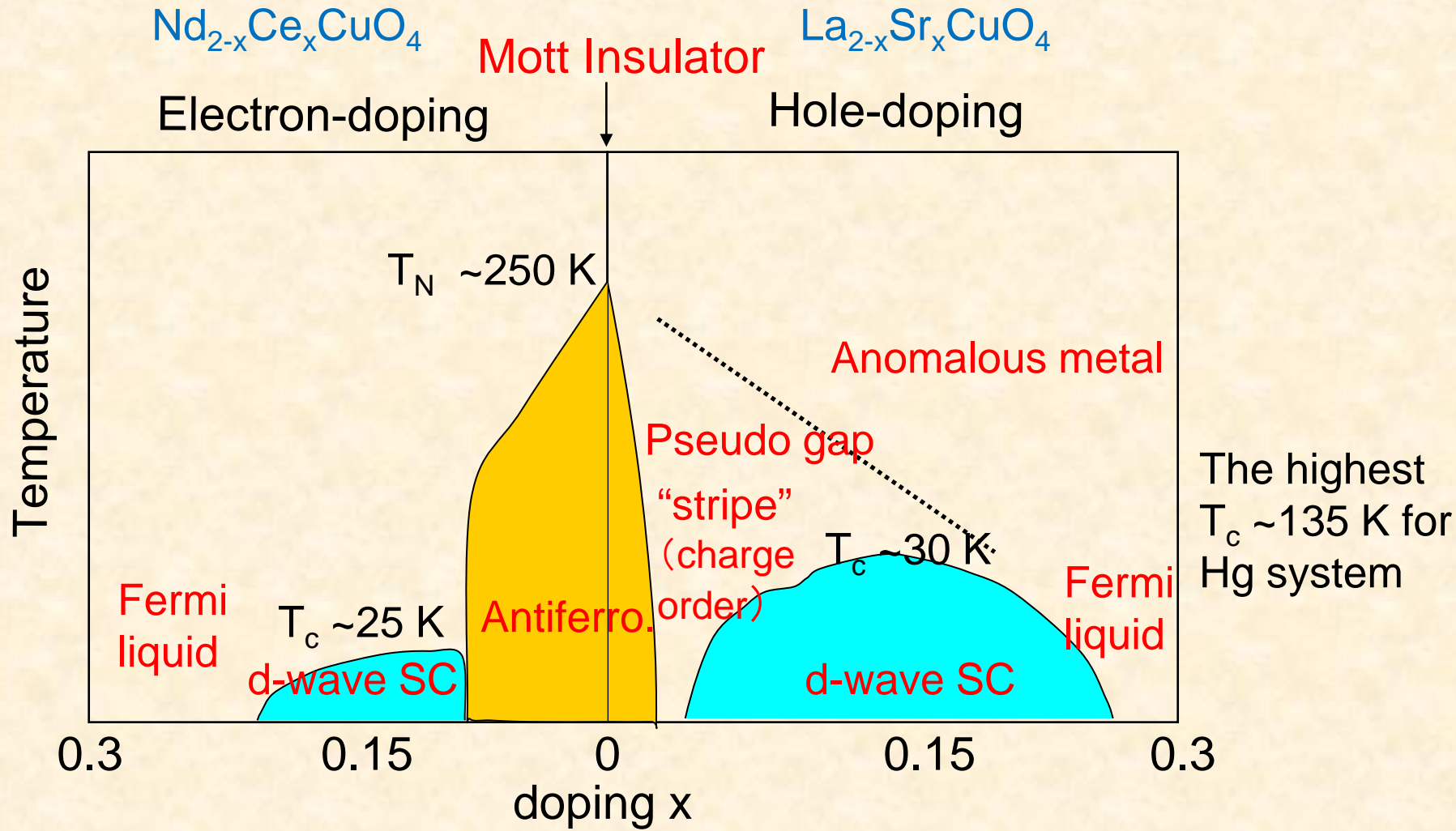
$\text{Cu}^{2+}$   $3d^9$   $S=1/2$  hole on each  $x^2-y^2$  orbital

Strong local Coulomb interaction  $\rightarrow$  **Mott insulator**

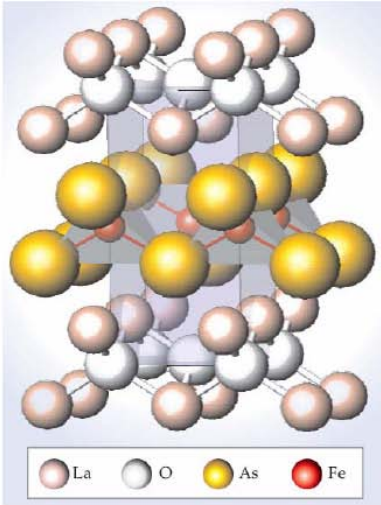
localized spin  $\rightarrow$  **antiferromagnetic exchange interaction**

$J \sim 1400\text{K}$

# Phase diagrams

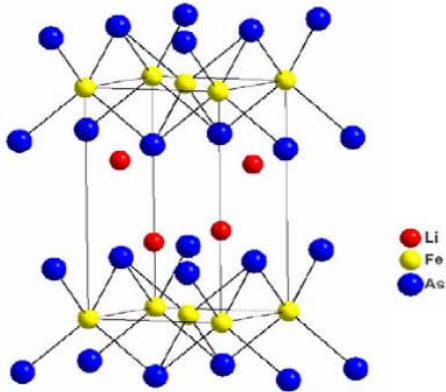


# Crystal structure of high $T_c$ iron pnictides



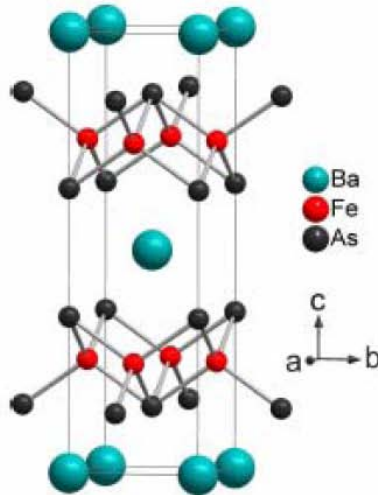
**LnFeAsO (1111)**

$T_c \sim 55$  K



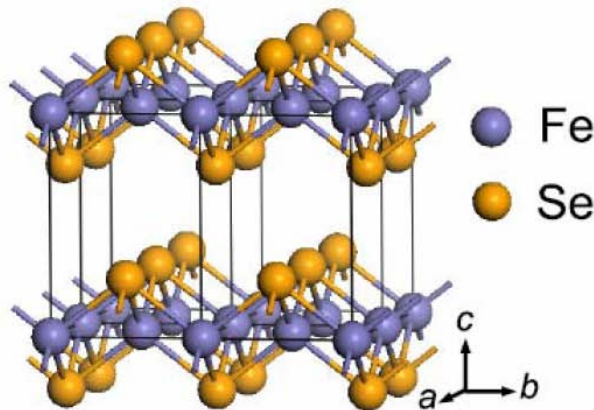
**LixFeAs (111)**

$T_c \sim 33$  K



**BaFe<sub>2</sub>As<sub>2</sub> (122)**

$T_c \sim 37$  K



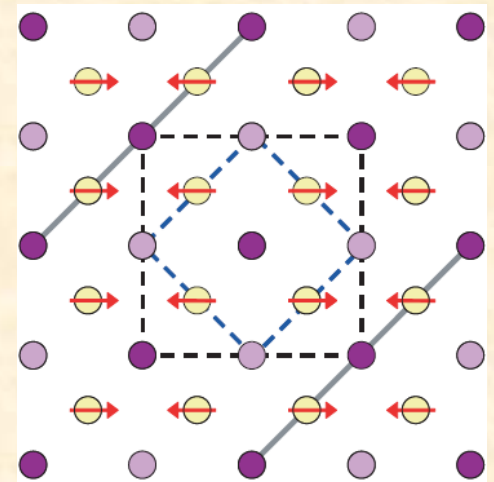
**FeSe (11)**

$T_c \sim 37$  K (under press.)

Layered structures

Fe-As layer

Quasi-2D system



$Q = (\pi, 0)$

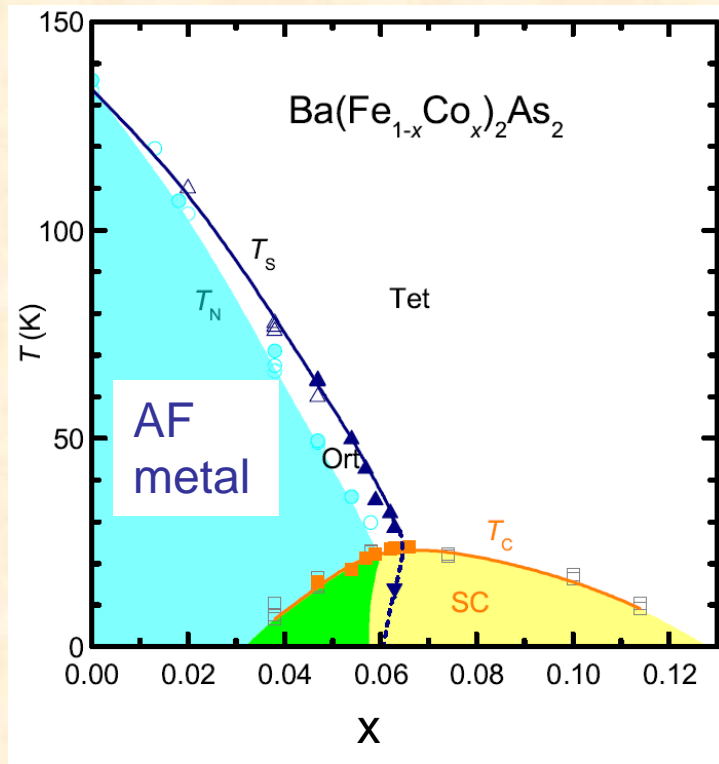
"Stripe" order



# Phase diagram of high- $T_c$ iron pnictides



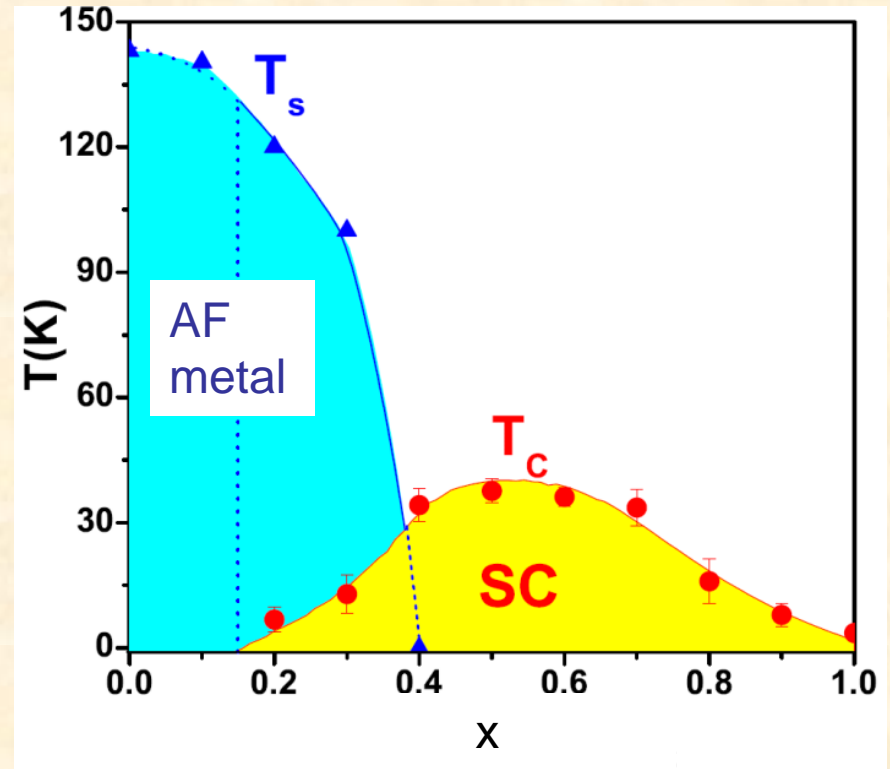
Electron “doping”



S. Nandi *et al.*, PRL **104**, 057006 (2010)



Hole “doping”



H. Chen *et al.*, Europhys. Lett. **85**, 17006 (2009)

# Cuprates and iron pnictides

Similarity

Superconductivity next to magnetism

Difference

cuprates

iron pnictides

electronic structure

crystal-field,  $3d^9$   
single band ( $x^2-y^2$ )

hybridization,  $3d^6$   
multi band (five orbitals)

magnetism

Antiferro.  
insulator

Antiferro.  
metal

super-conductivity

carrier doping

carrier doping  
pressure

super-conductivity

$d_{x^2-y^2}$  symmetry

sign-reversed or preserved s  
anisotropic s, d ??

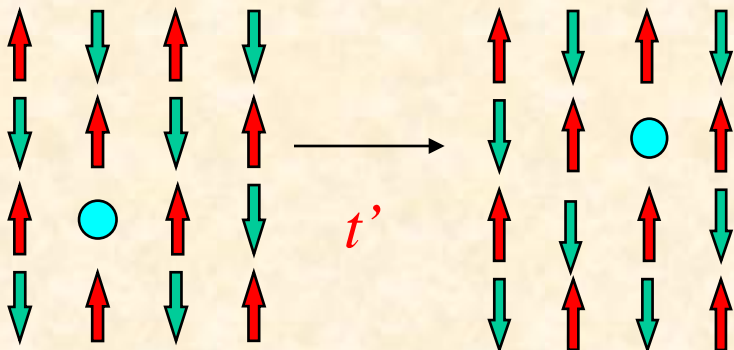
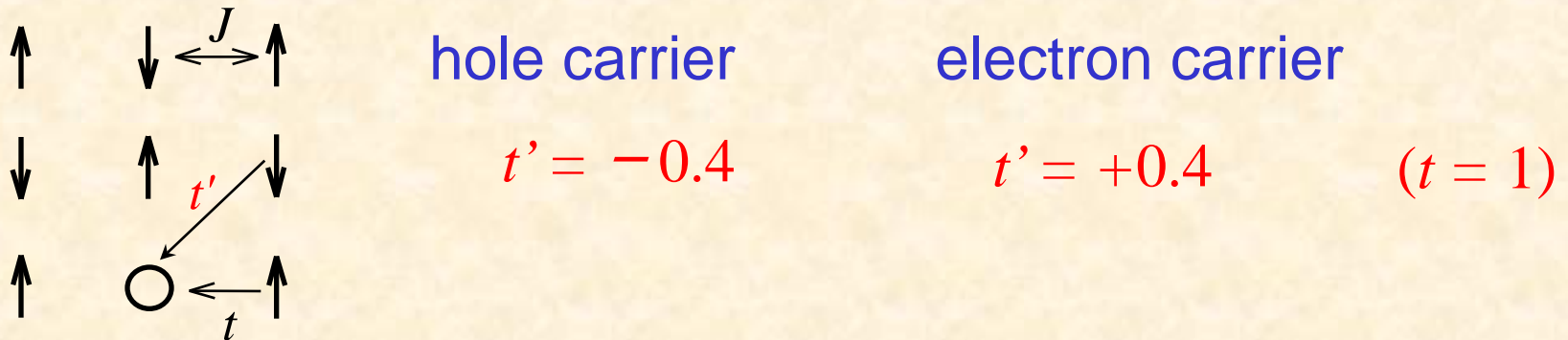
approaches from  
ionic picture and  
doped Mott insulator

approaches from  
band picture and  
spin-density wave

# Origin of the electron-hole asymmetry in cuprates

- low-energy effective model:  $t$ - $J$  model
- Introduction of the second nearest-neighbour hopping  $t'$

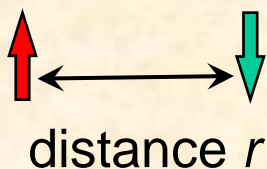
$$H_{tJ} = -t \sum_{\langle i,j \rangle_1, \sigma} \tilde{c}_{i,\sigma}^+ \tilde{c}_{j,\sigma} + J \sum_{i\delta} \mathbf{S}_i \cdot \mathbf{S}_{i+\delta} - t' \sum_{\langle i,j \rangle_2, \sigma} \tilde{c}_{i,\sigma}^+ \tilde{c}_{j,\sigma}$$



No change of spin configuration by  $t'$

The magnitude of the self-energy of this configuration is dependent of the sign of  $t'$

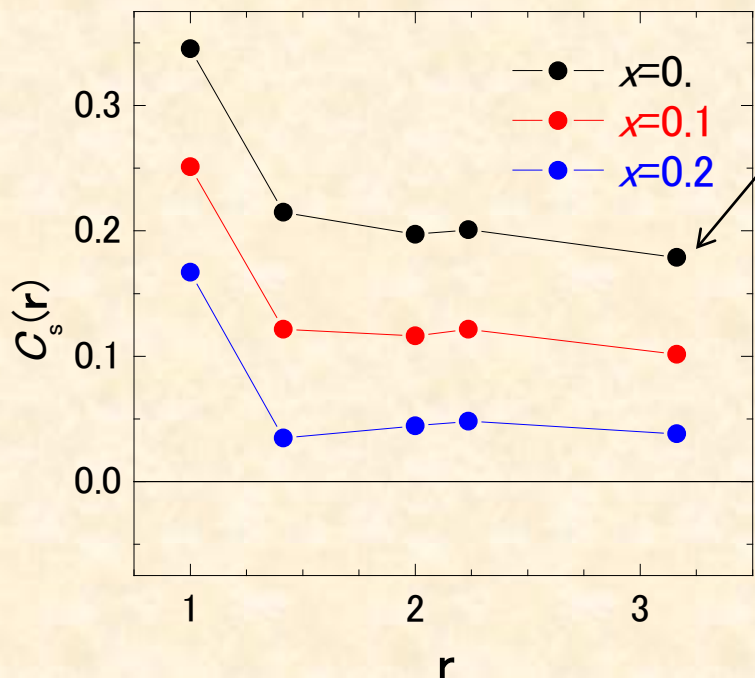
# Asymmetry of spin-spin correlation function



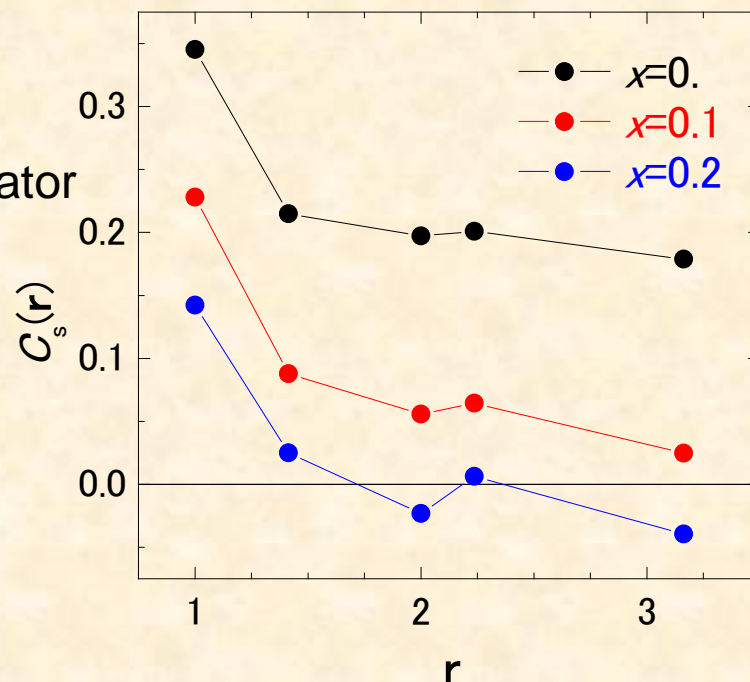
Exact results for a  
20-site t-t'-J model

$x$  : carrier density

Electron carrier

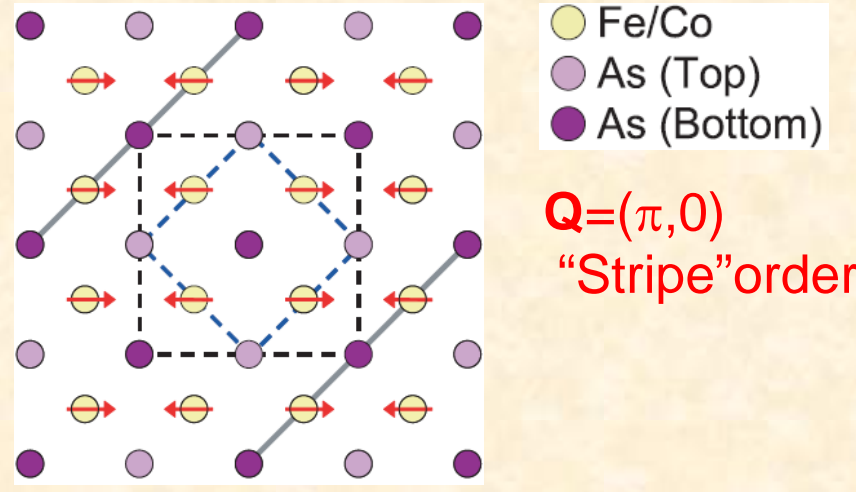
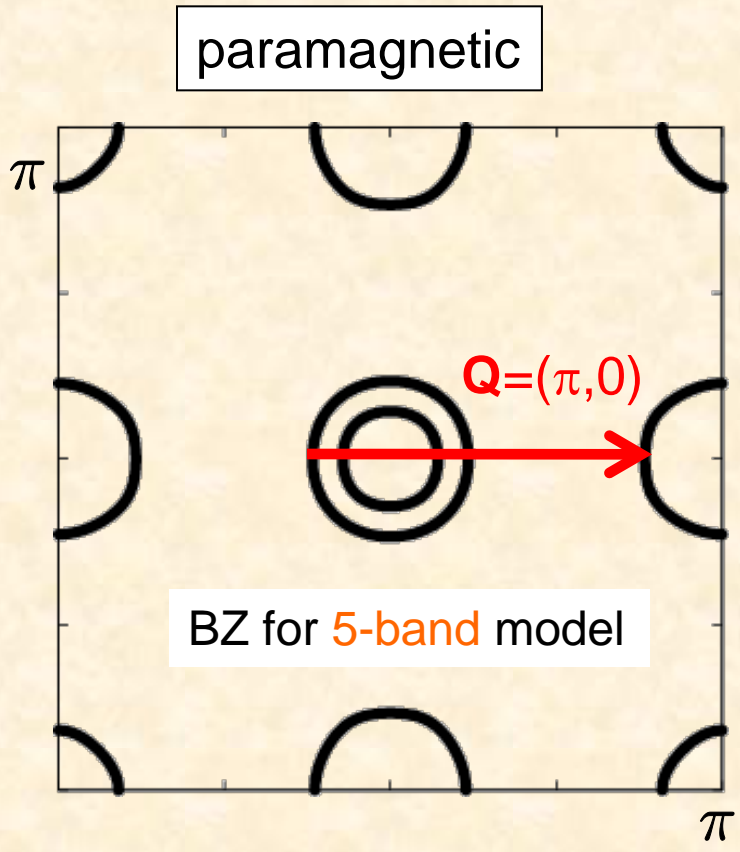


Hole carrier



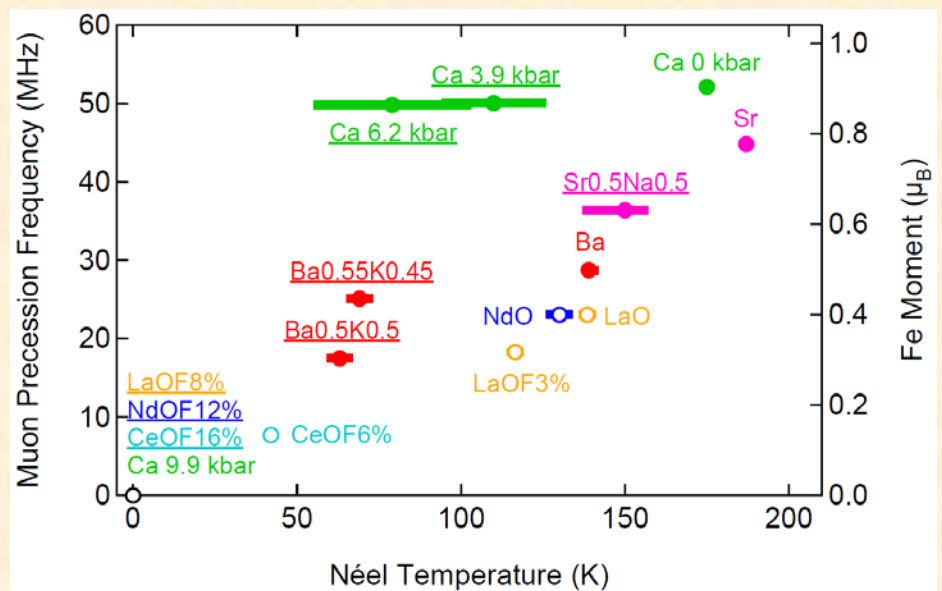
Antiferromagnetic correlation survives for the electron carrier.

# Antiferromagnetic phase of iron pnictides



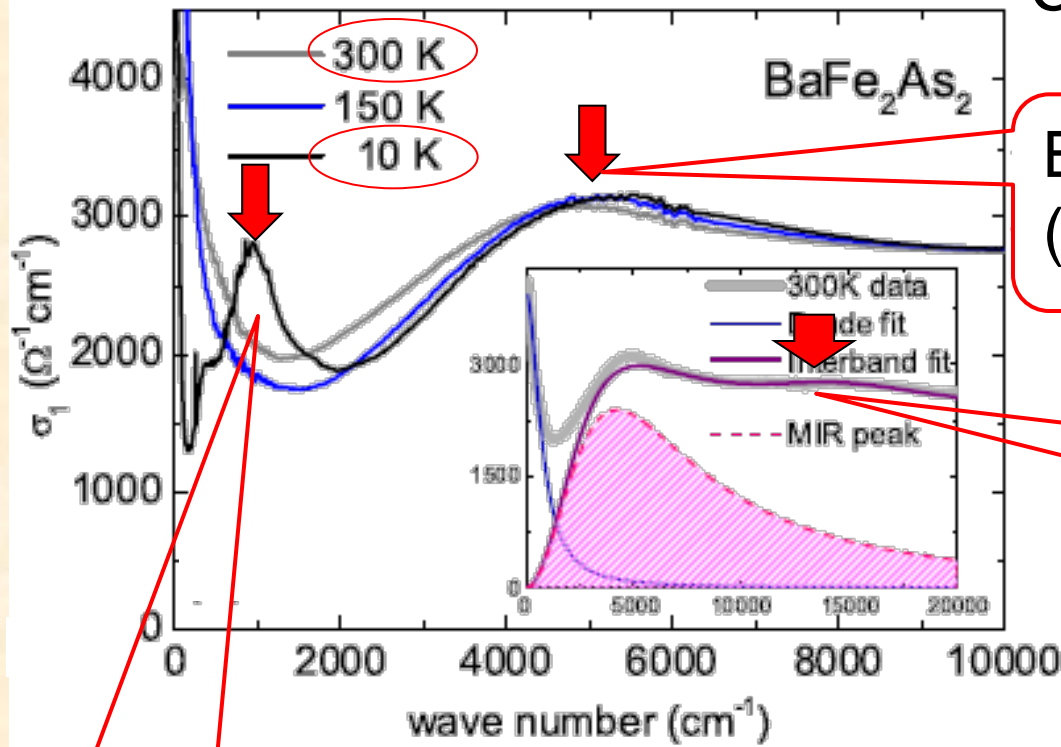
5-band tight-binding model  
 [K. Kuroki *et al.*, PRL 101, 087004 (2008)]

spin-density wave (SDW) ?



T. Goko *et al.*, PRB 80, 024508 (2009);  
 arXiv:0808.1425

# Characteristics of optical conductivity



grey

black

Compare PM and AF data

Broad excitation structure ( $\sim 0.5\text{eV}$ ) slightly shifted

Unchanged in high energies

AF gap ( $\sim 0.1\text{eV}$ )

W. Z. Hu *et al.*, PRL **10**, 257005 (2008)

# Mean-field calculation of the stripe AF state

Five-band model for the Fe square lattice

$$H = H_0 + H_I$$

$$H_0 = \sum_{\mathbf{k}, \mu, \nu, \sigma} \left[ \sum_{\Delta} t(\Delta_x, \Delta_y; \mu, \nu) e^{i\mathbf{k} \cdot \Delta} + \epsilon_{\mu} \delta_{\mu, \nu} \right] c_{\mathbf{k}\mu\sigma}^{\dagger} c_{\mathbf{k}\nu\sigma}$$

K. Kuroki *et al.*, Phys. Rev. Lett. **101**, 087004 (2008)

$$H_I = U \sum_{i, \mu} n_{i\mu\uparrow} n_{i\mu\downarrow} + \frac{2U - 5J}{4} \sum_{i, \mu \neq \nu, \sigma, \sigma'} n_{i\mu\sigma} n_{i\nu\sigma'}$$

$$+ J \sum_{i, \mu \neq \nu} (c_{i\mu\uparrow}^{\dagger} c_{i\nu\uparrow} c_{i\mu\downarrow}^{\dagger} c_{i\nu\downarrow} - \mathbf{S}_{i\mu} \cdot \mathbf{S}_{i\nu})$$

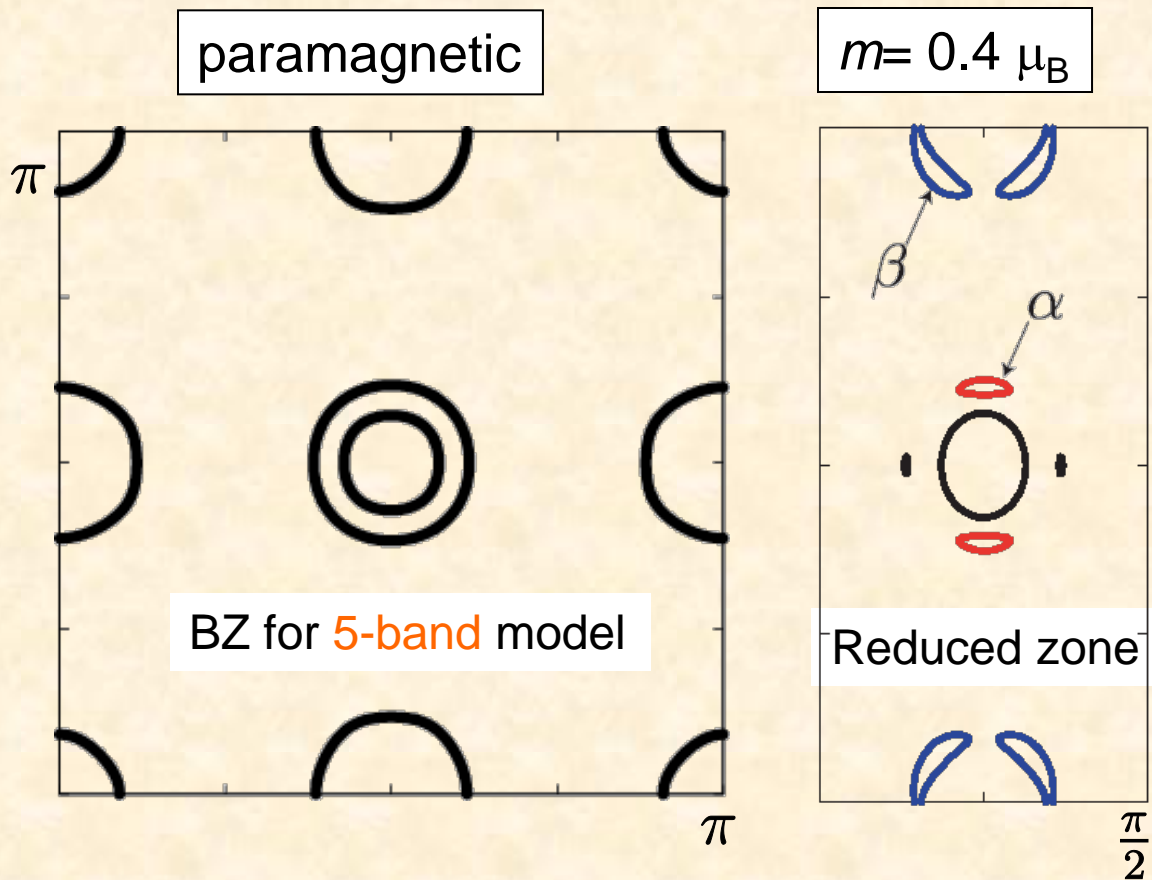
Striped AF order

Order parameter

$$\langle n_{\mathbf{Q}\mu\nu\sigma} \rangle = \frac{1}{N} \sum_{\mathbf{k}} \langle c_{\mathbf{k}+\mathbf{Q}\mu\sigma}^{\dagger} c_{\mathbf{k}\nu\sigma} \rangle$$

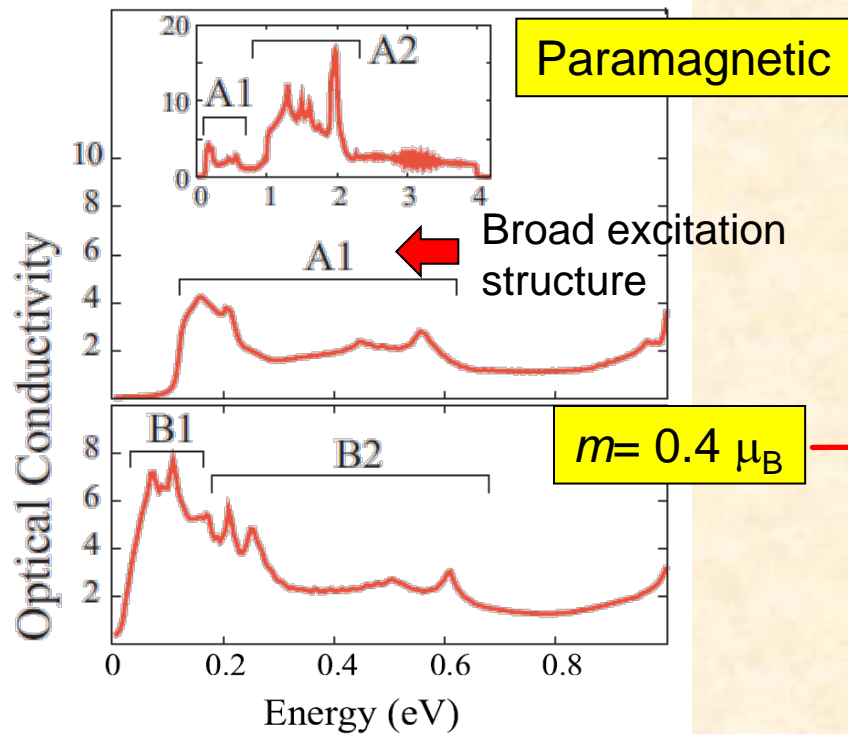
$$m = 0.4 \mu_B$$

# Fermi surfaces





# Calculated optical conductivity (Interband transitions)



- #1: SDW gap state ( $\sim 0.1\text{eV}$ ) (B1)
- #2: Small shift of broad structure (A1  $\rightarrow$  B2)
- #3: No change in high energy  $> 0.5\text{eV}$  (Similar DOS)

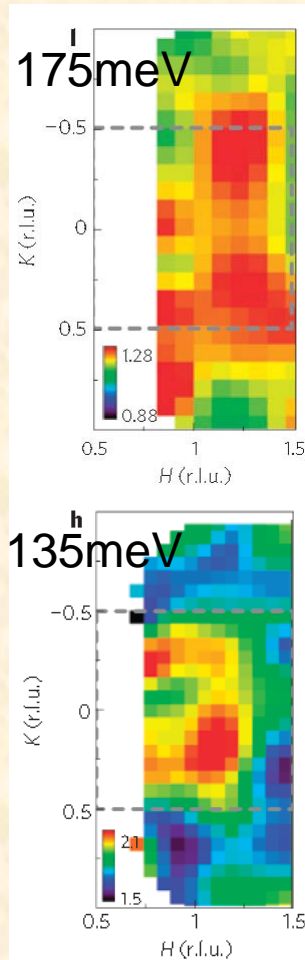
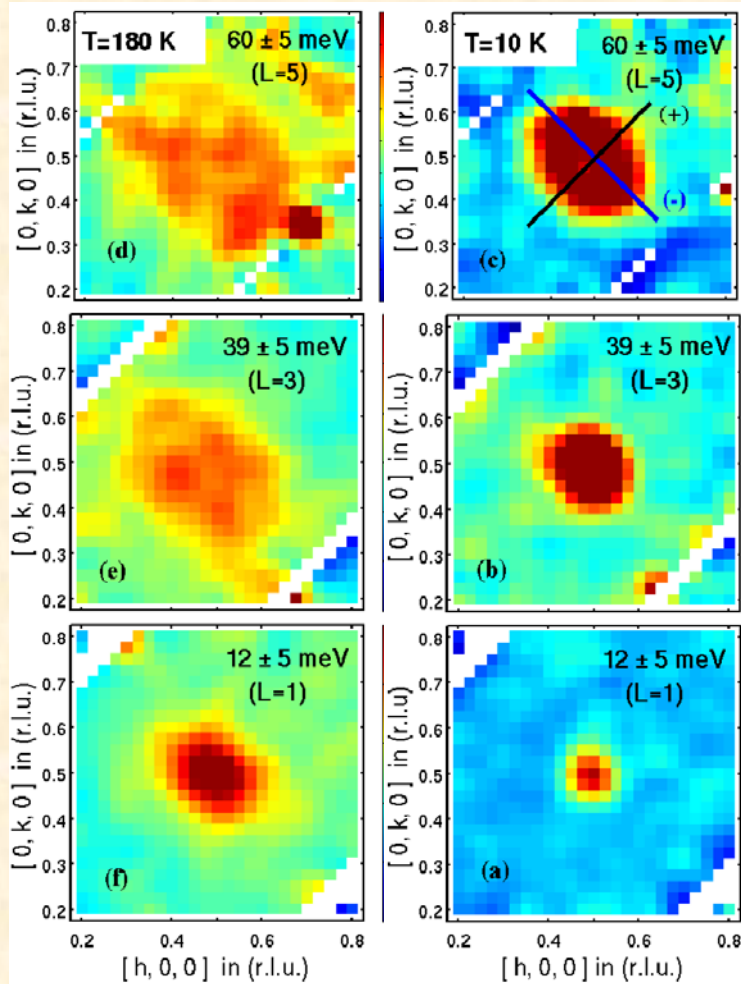
The AF state exhibits optical conductivity consistent with experiments.

E. Kaneshita, T. Morinari, T.T., PRL **103**, 224519 (2009)

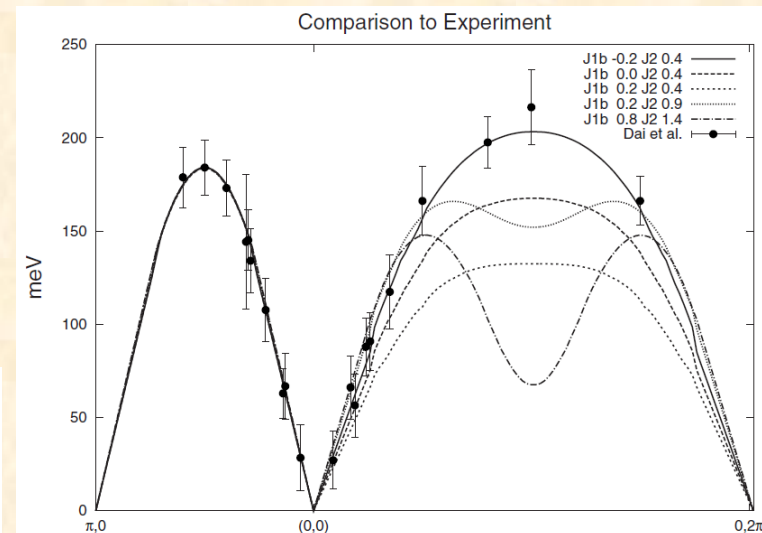
# Spin excitation of $\text{CaFe}_2\text{As}_2$ Experiment

Para.

AFM



dispersion



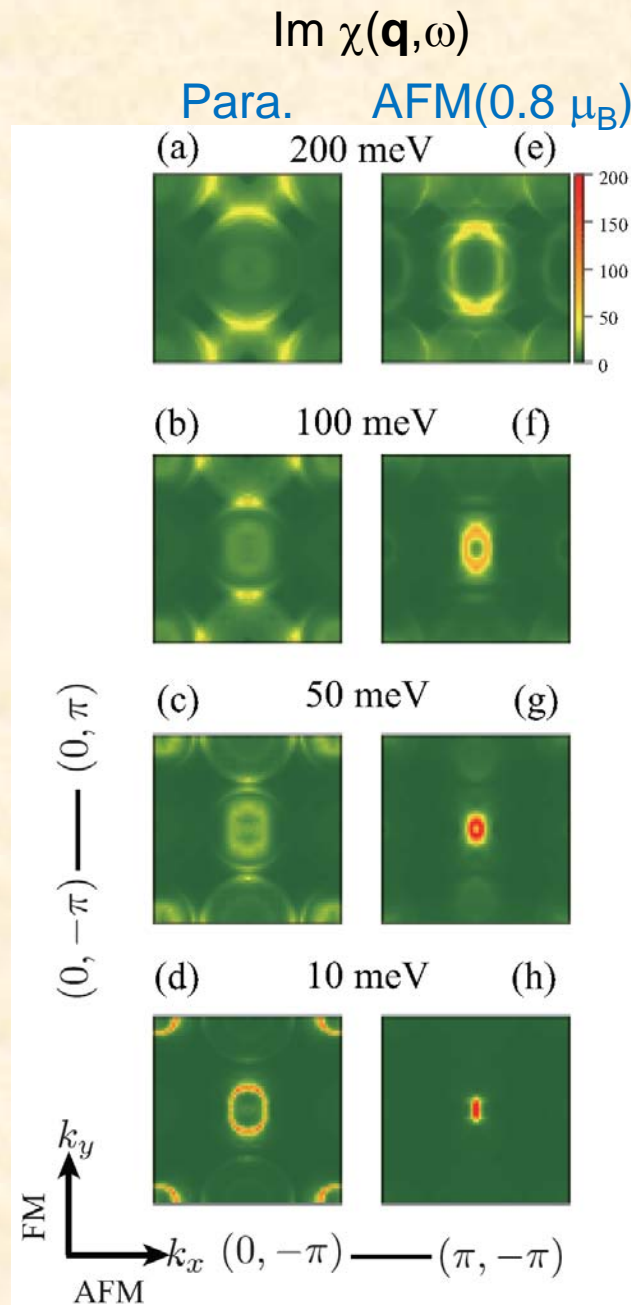
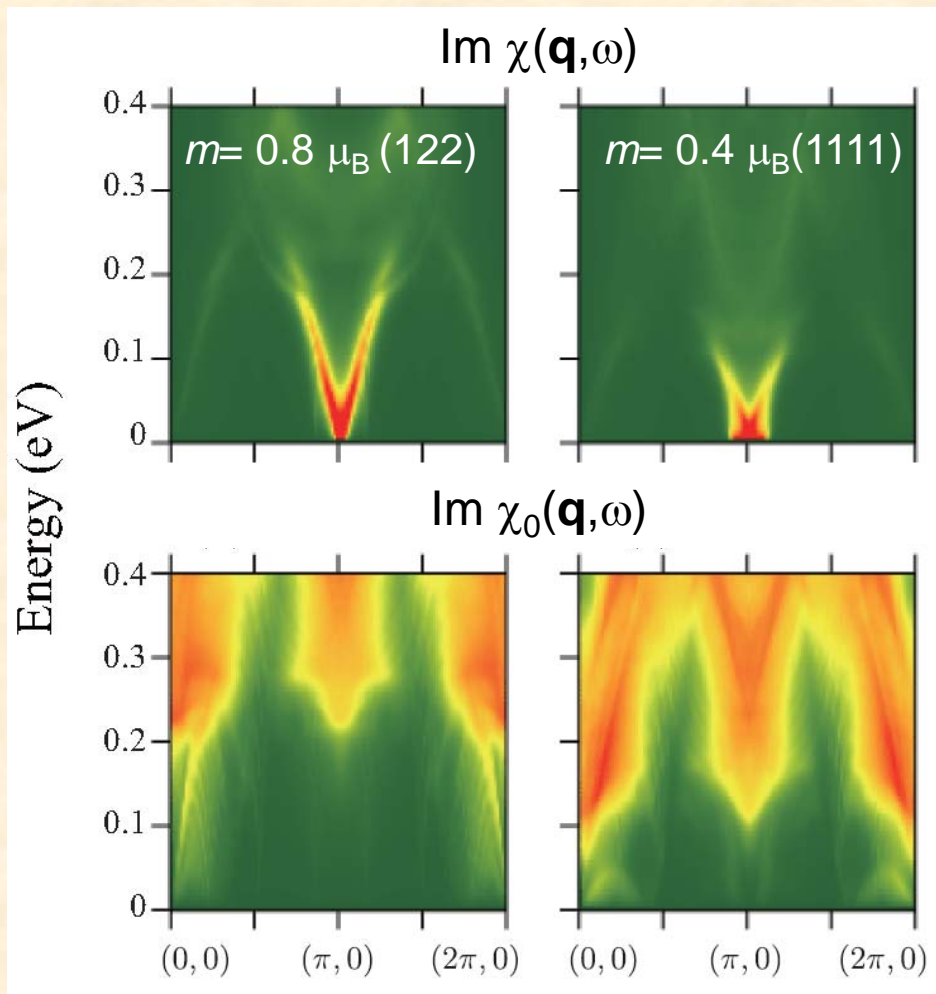
J. Zhao *et al.*, Nat. Phys.  
5, 555 (2009)

Localized spin model

# Spin excitation for AF metal Theory

E. Kaneshita and T.T., arXiv:1002.2701

Five band + mean-field  $\mathbf{Q}=(\pi,0)$  "Stripe" order  
 Random phase approximation



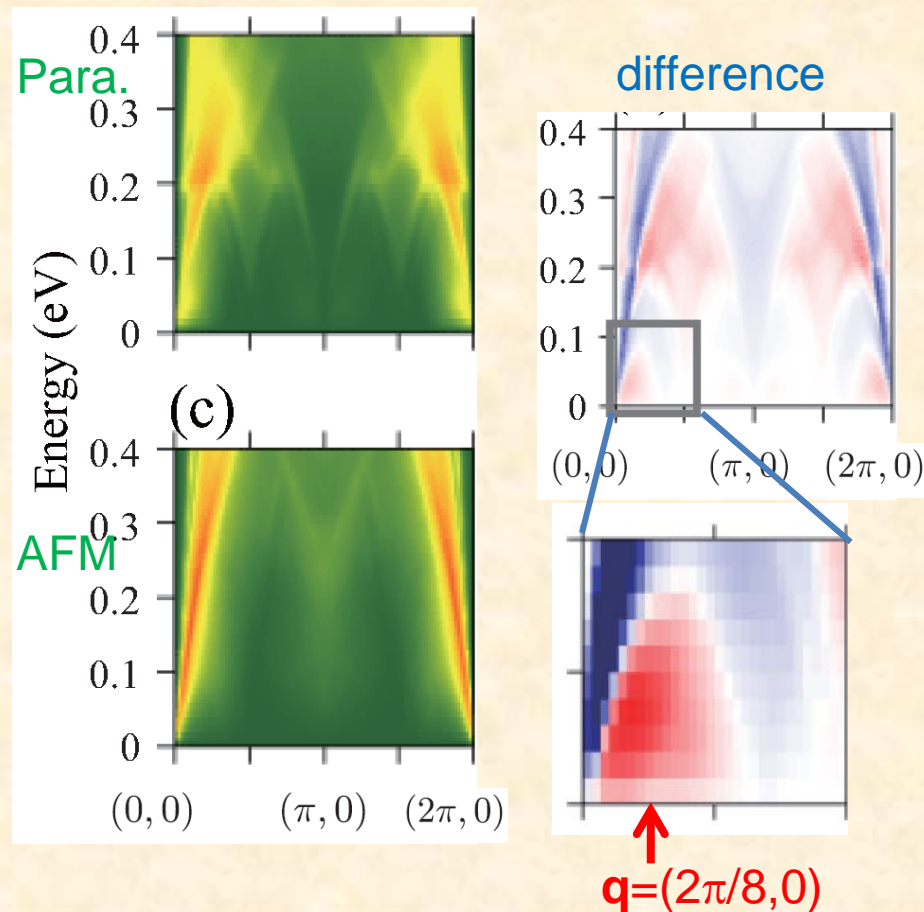
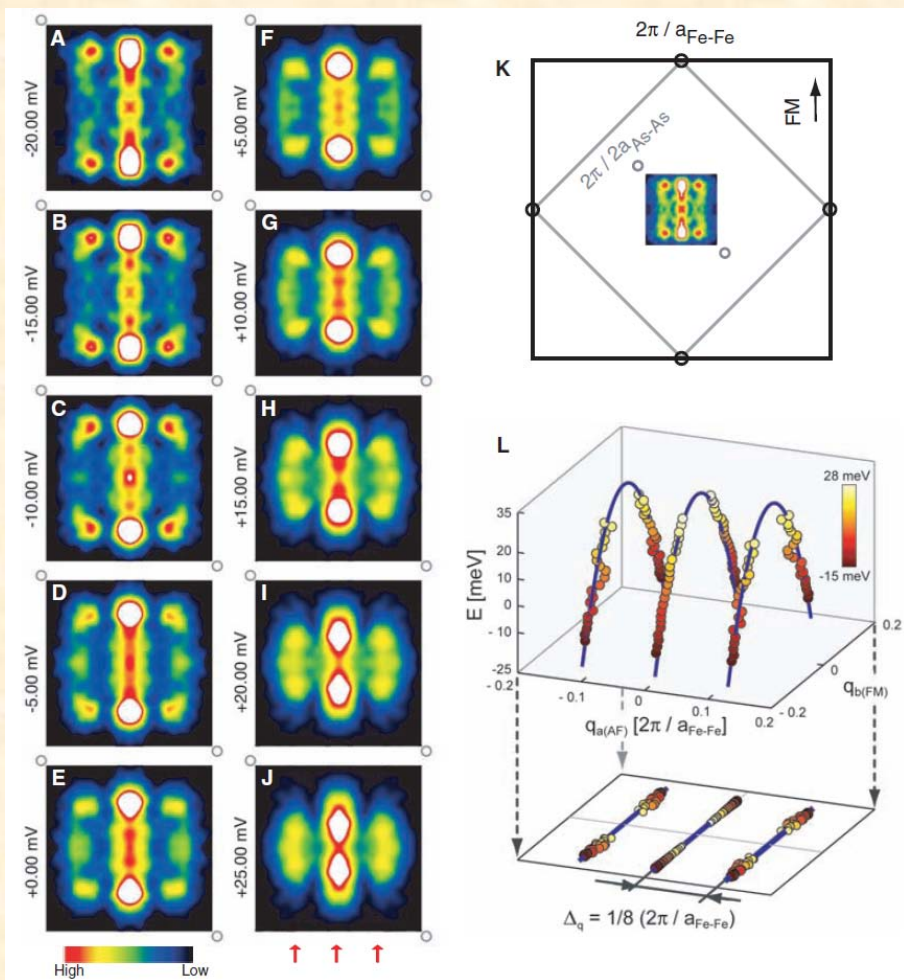
# “Nematic” electronic nanostructure seen in AF metal

STM for  $\text{CaFe}_{1.94}\text{Co}_{0.06}\text{As}_2$

T.-M. Chuang *et al.*, Science **327**, 181 (2010)

Charge response function

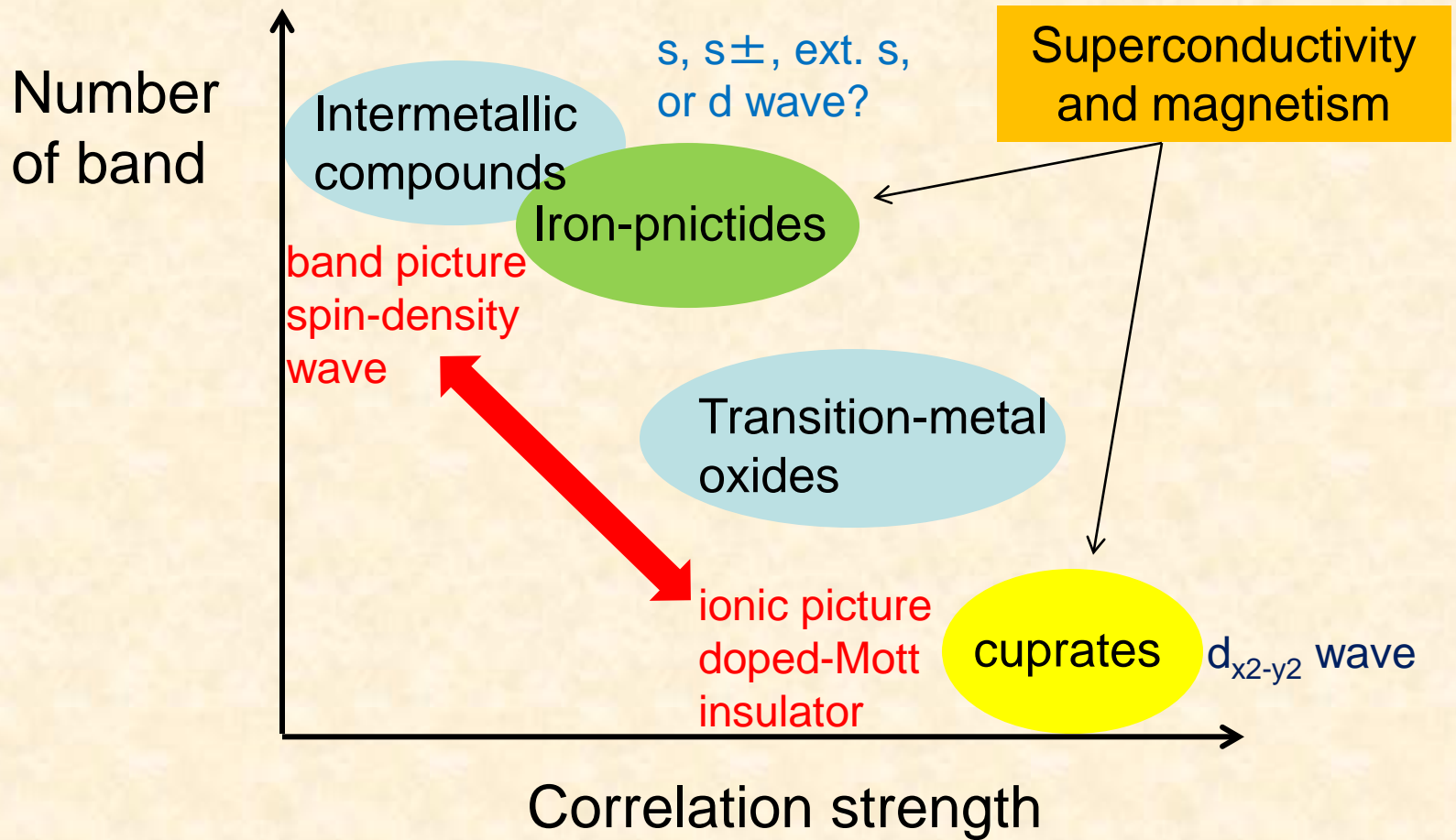
E. Kaneshita and T.T., arXiv:1002.2701



Charge fluctuations from residual Fermi surfaces

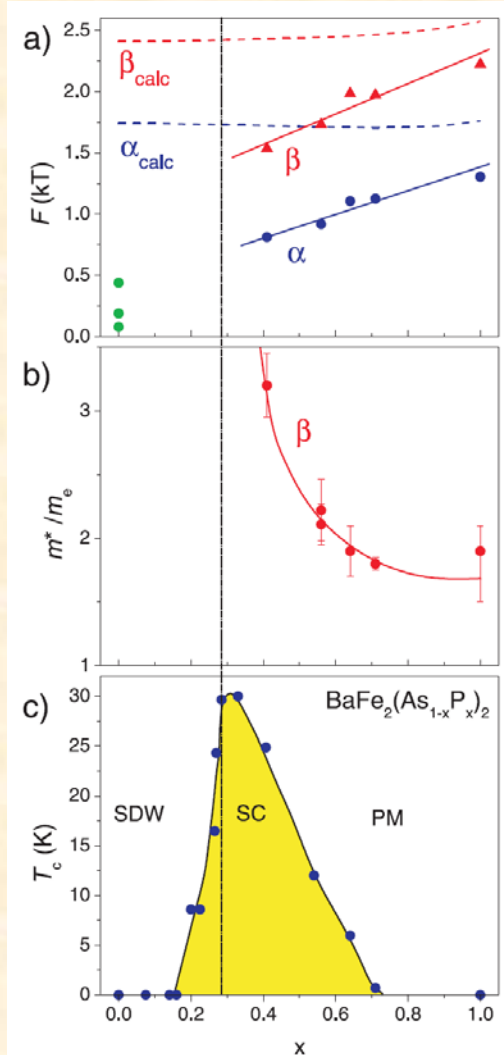
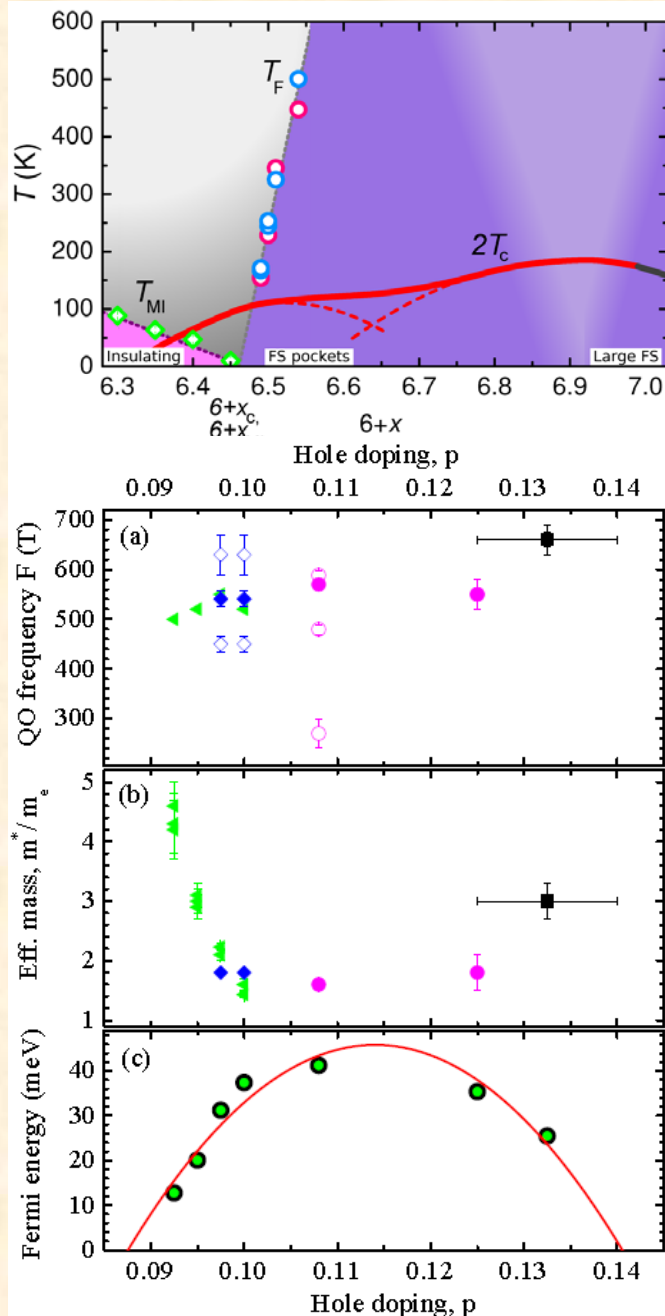
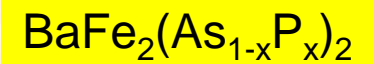
charge modulation with 8 Fe-Fe distance

# Summary





Perspective: Quantum oscillations



H. Shishido *et al.*,  
PRL **104**, 057008  
(2010)

- Multiple Fermi surfaces
  - Divergence of the effective mass
- Similar to iron-pnictides?

S. E. Sebastian *et al.*, arXiv:0910.2359

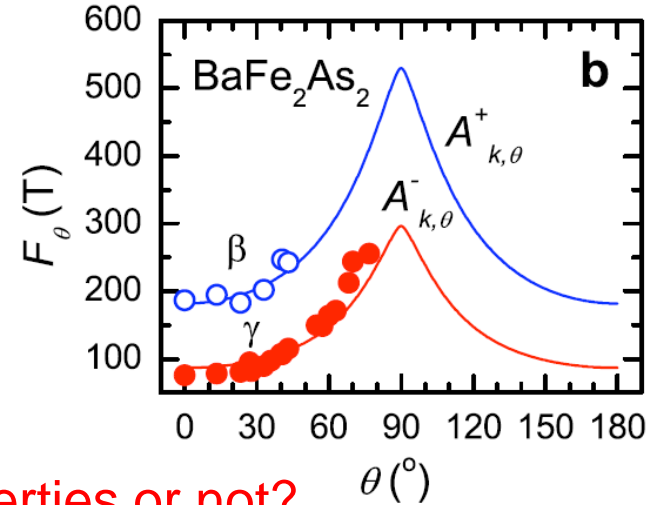
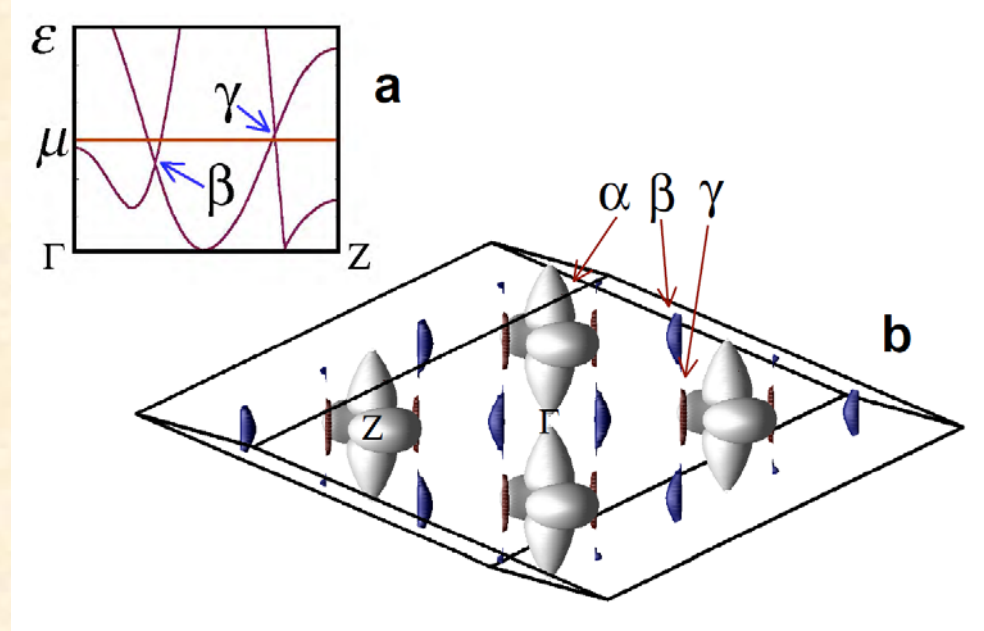
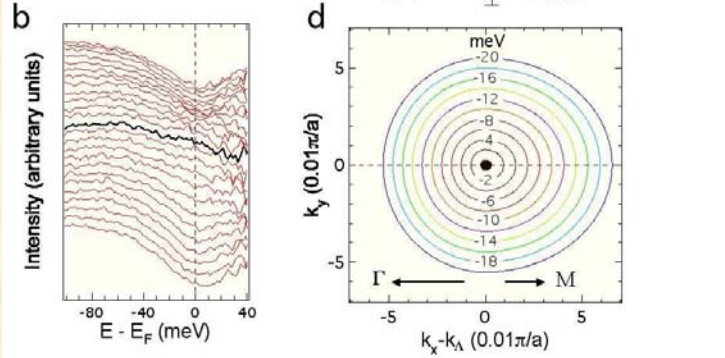
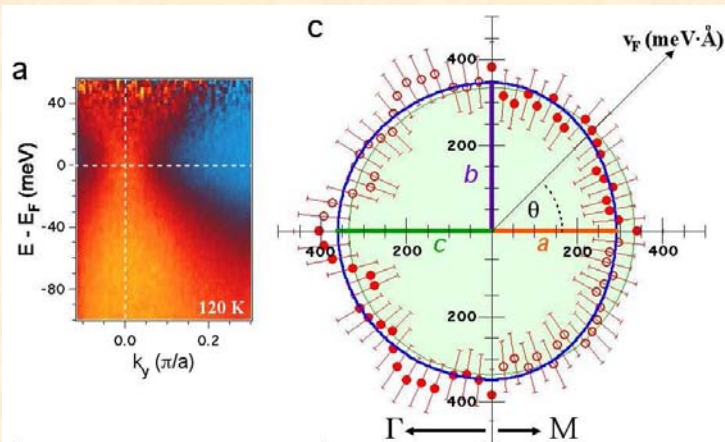
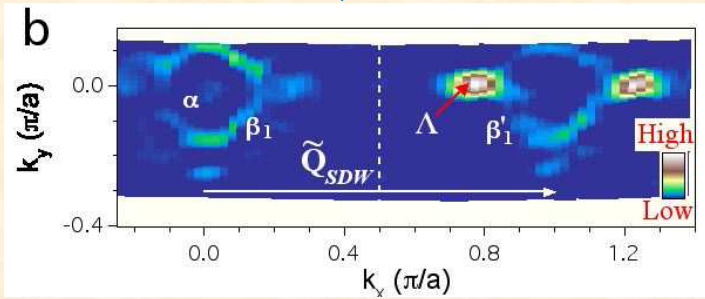
J. Singleton *et al.*, arXiv:0911.2745

# Perspective for iron-pnictides

## Dirac particles in band dispersions of AFM BaFe<sub>2</sub>As<sub>2</sub>

P. Richard *et al.*, arXiv:0909.0574

N. Harrison and S. E. Sebastian, arXiv:0910.4199



Real effect on transport properties or not?