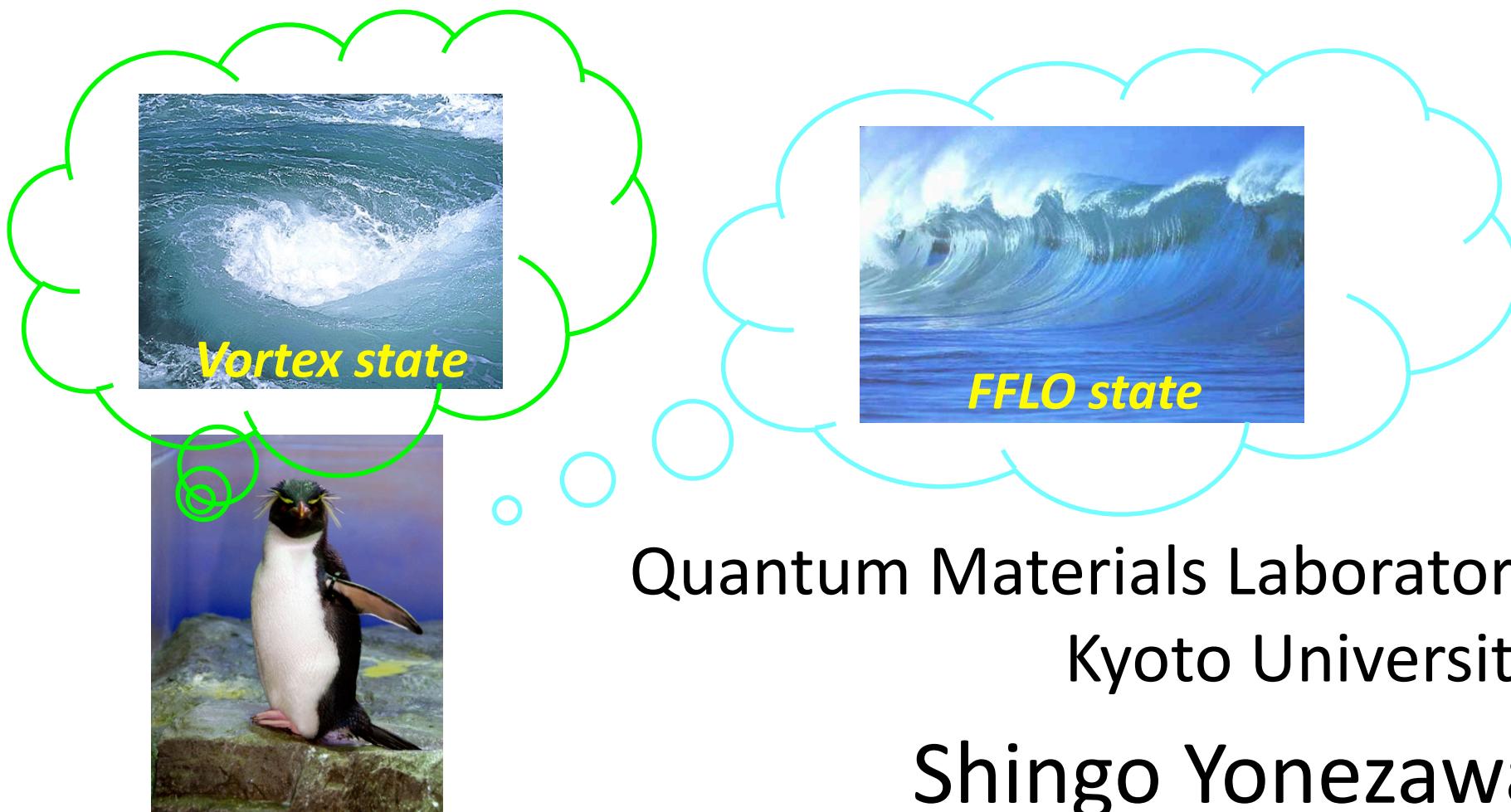
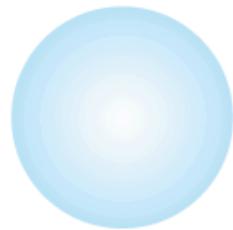


Superconductivity and magnetic fields

- competition and interplay -



Overview



Broken U1 gauge symmetry

Spin-Singlet Superconductor

?

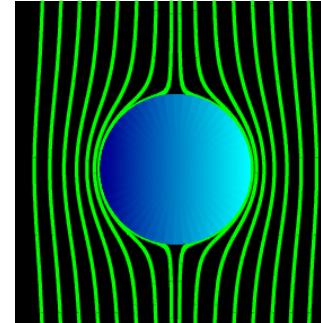
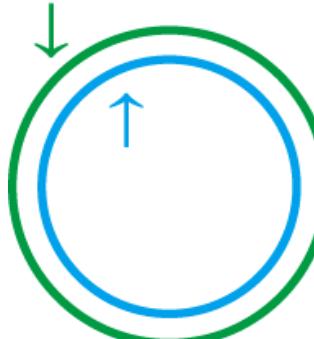


Spatially homogenous at $H = 0$

*What happens if a magnetic field is applied to
a singlet superconductor?*

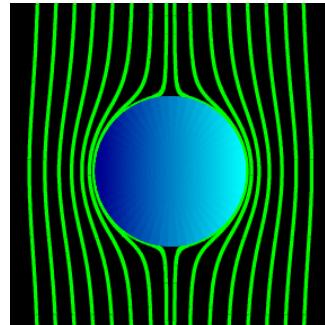
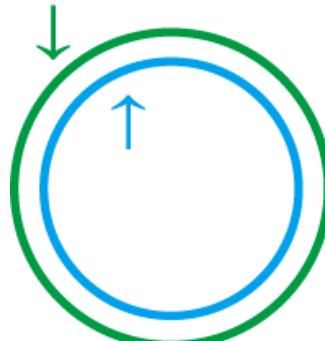
Overview

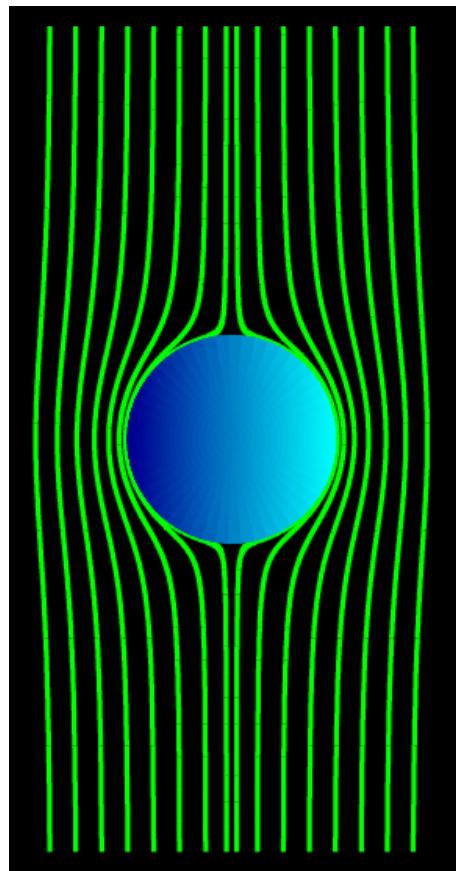
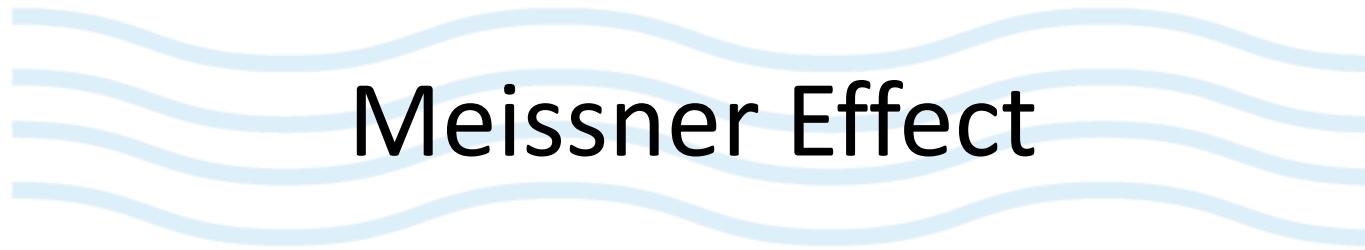
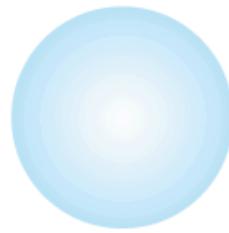
~ Competition and Interplay ~

	<i>Competition</i>	<i>Interplay</i>
Flux Expulsion	<p>Meissner Effect</p> 	
Spin Polarization	<p>Zeeman Effect</p> 	

Overview

~ Competition and Interplay ~

	<i>Competition</i>	<i>Interplay</i>
Flux Expulsion	<p>Meissner Effect</p> 	
Spin Polarization	<p>Zeeman Effect</p> 	



Meissner Effect

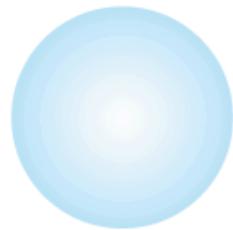
Meissner Effect:
Expelling magnetic flux inside a superconductor



Energy is required.

$$(1/2)\mu_0 H^2 / \text{unit volume}$$

When this energy is equal to
the condensation energy U_c ,
superconductivity is broken.



Meissner Effect

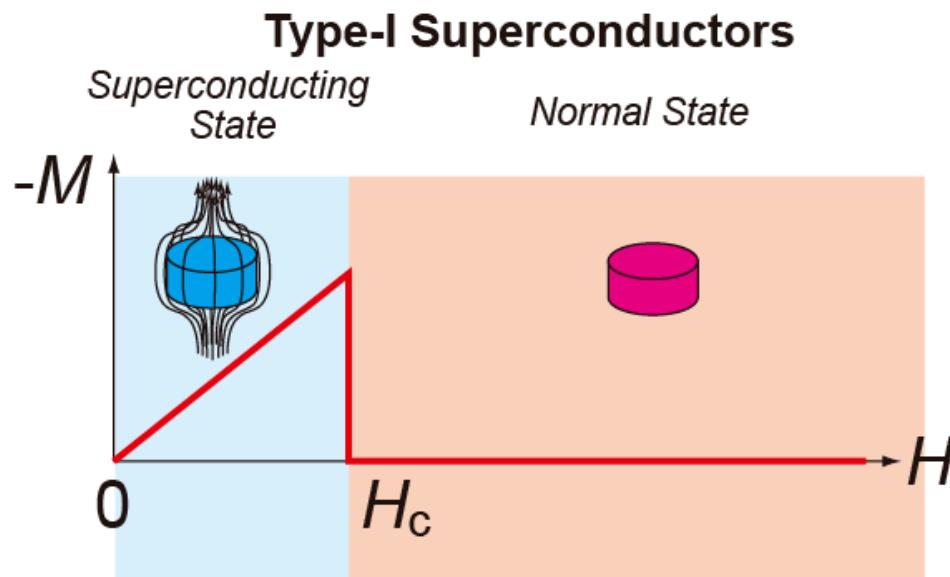


Meissner Effect:
Expelling magnetic flux inside a superconductor



Energy is required.

$$(1/2)\mu_0 H^2 / \text{unit volume}$$



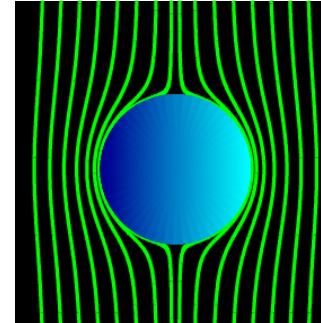
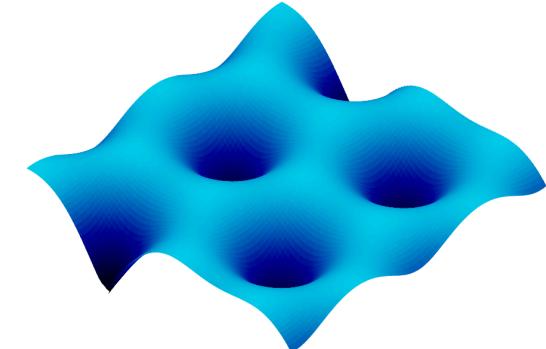
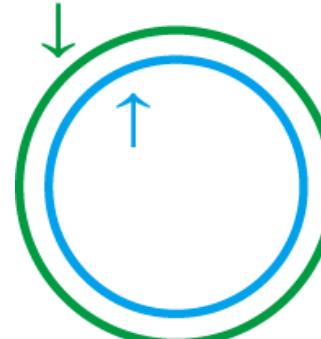
When this energy is equal to the condensation energy U_c , superconductivity is broken.

The critical field: H_c

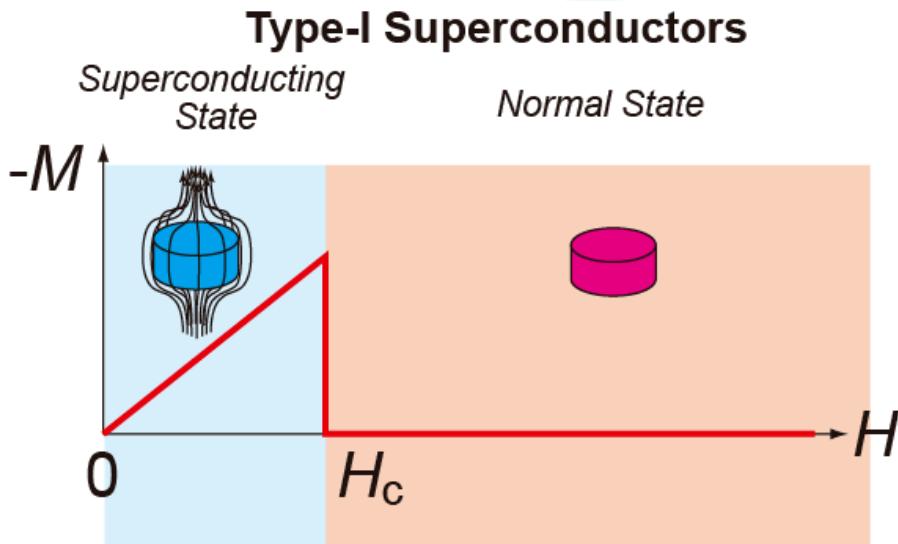
$$U_c = (1/2)\mu_0 H_c^2$$

Overview

~ Competition and Interplay ~

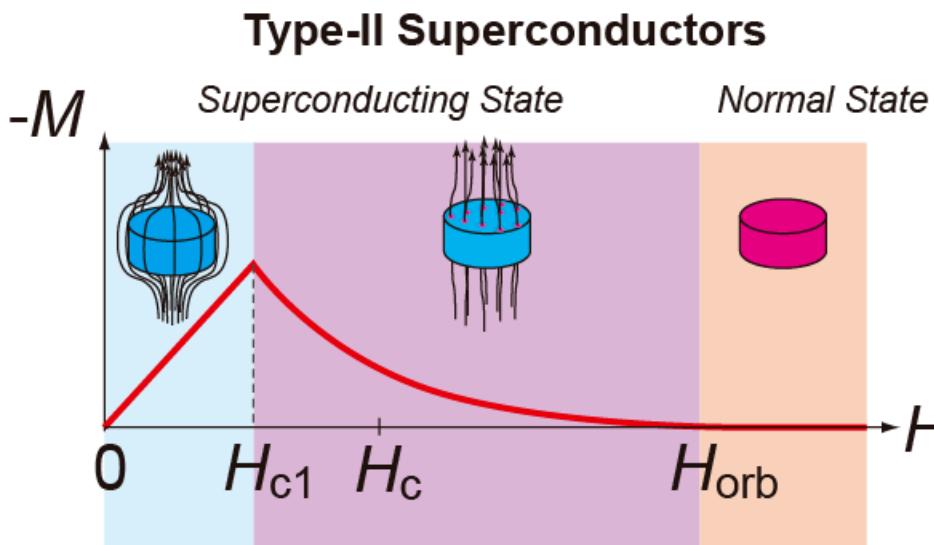
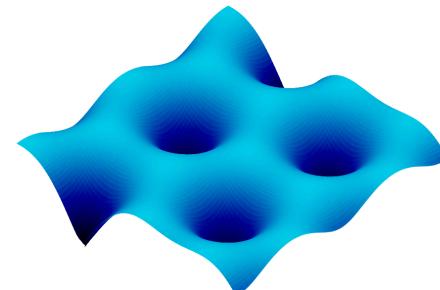
	<i>Competition</i>	<i>Interplay</i>
Flux Expulsion	Meissner Effect 	Vortex State 
Spin Polarization	Zeeman Effect 	

Vortex State



A. A. Abrikosov, Sov. Phys. JETP 5, 1174(1957).

Type-II superconductors:
Vortices penetrate above H_{c1}

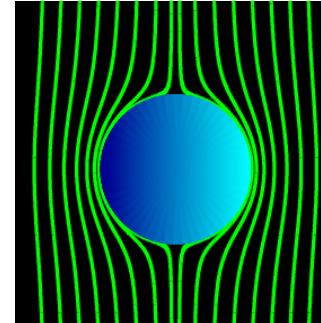
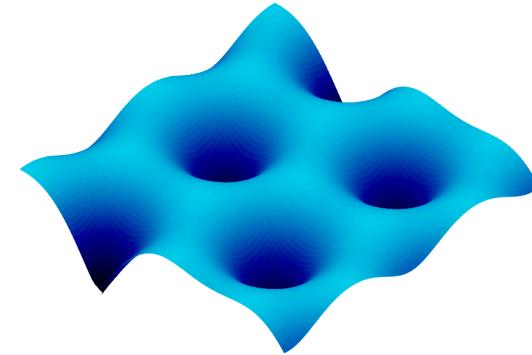
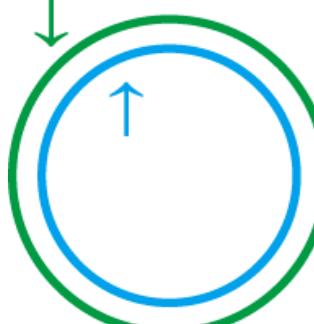


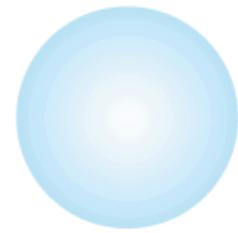
Superconductivity can survive
up to much higher field H_{orb}

$$H_{\text{orb}}(T=0) = \Phi_0 / (2\pi\xi^2)$$

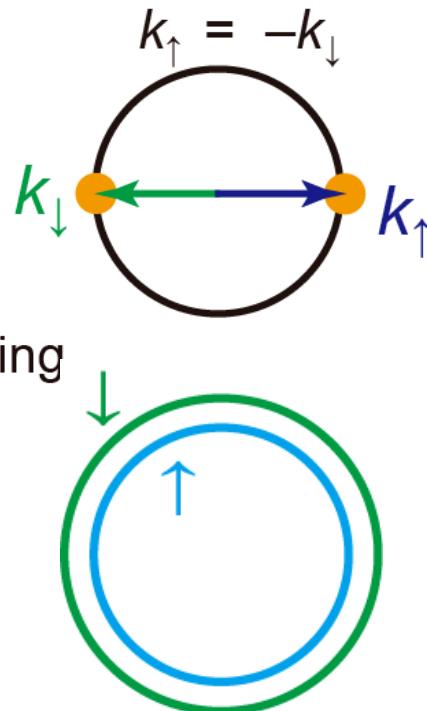
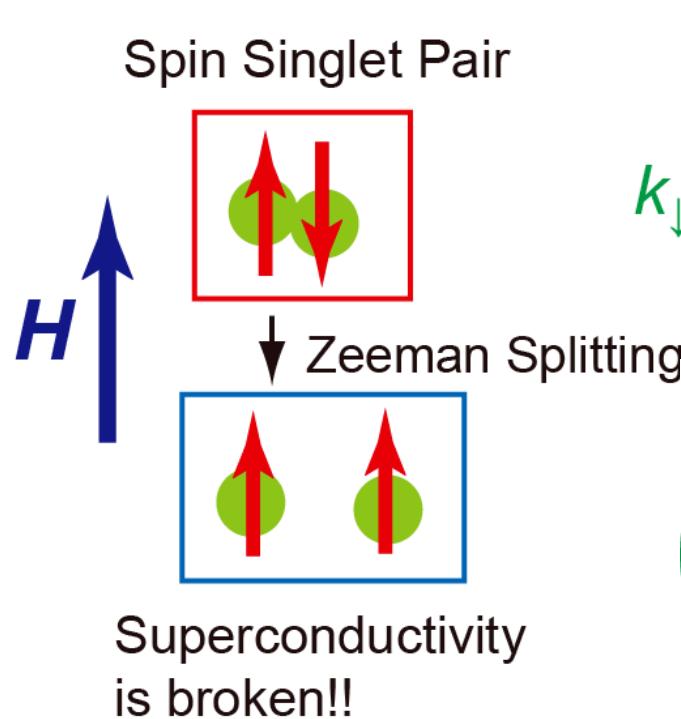
Overview

~ Competition and Interplay ~

	<i>Competition</i>	<i>Interplay</i>
Flux Expulsion	Meissner Effect 	Vortex State 
Spin Polarization	Zeeman Effect 	



Zeeman (Pauli) effect



Singlet pairs become unstable against the Zeeman splitting

Pauli limiting field H_p :

$$U_c = (1/2)\chi_p H_p^2$$

χ_p : Spin susceptibility in the normal state

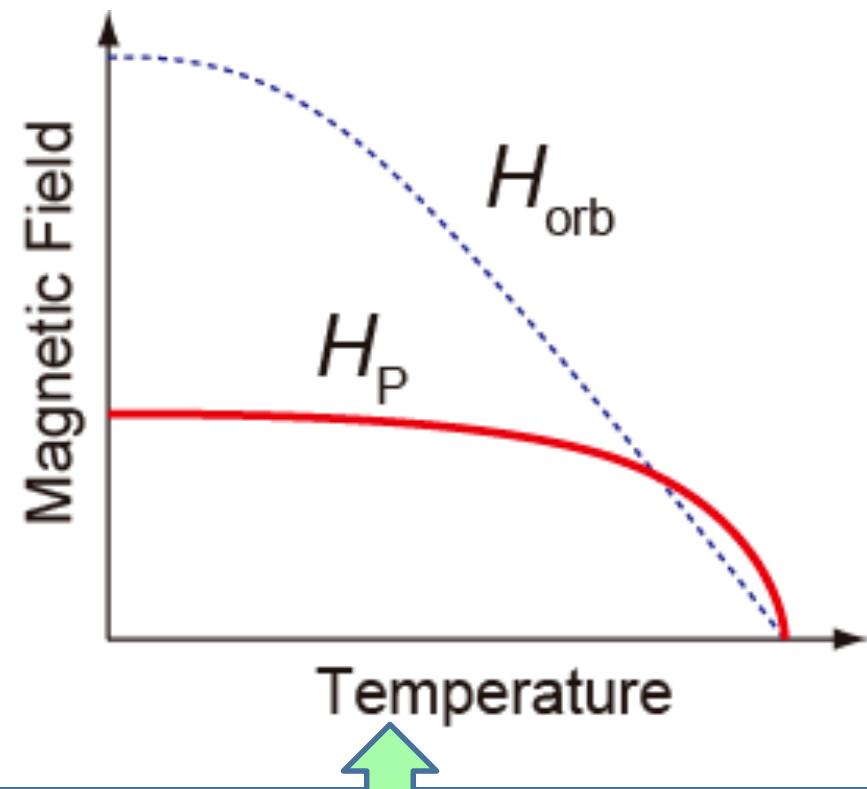
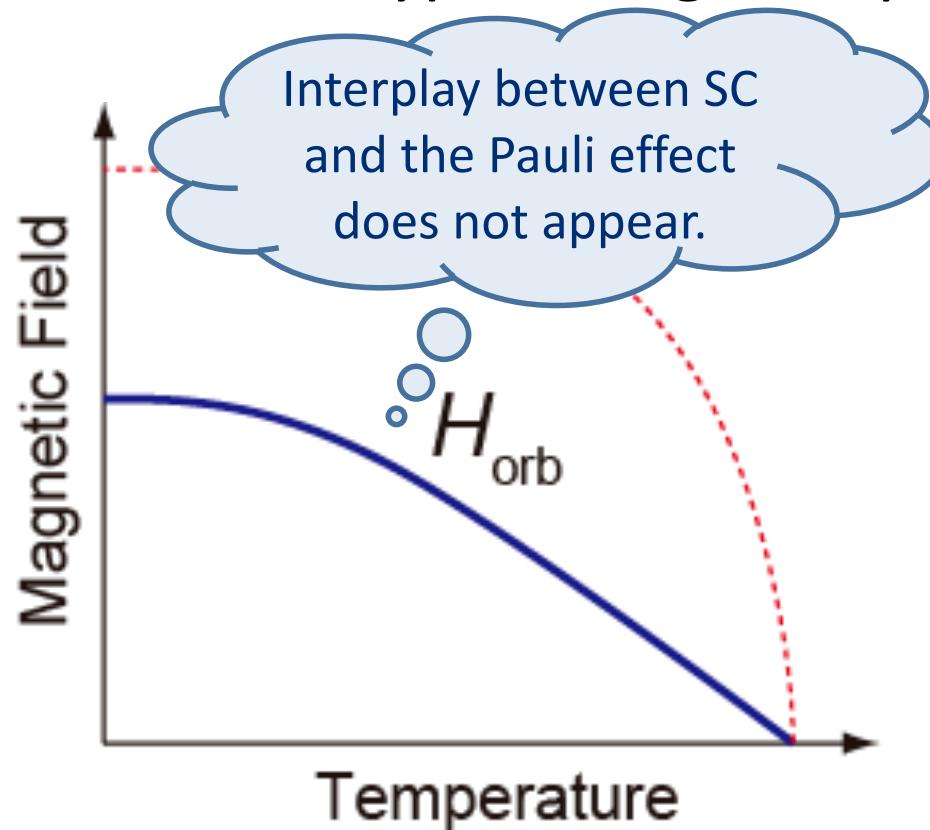
More useful relation:

$$H_p / T_c \sim 1.84 \text{ T/K}$$

A. M. Clogston, Phys. Rev. Lett. **9**, 266 (1962).

Comparison between H_{orb} and H_{P}

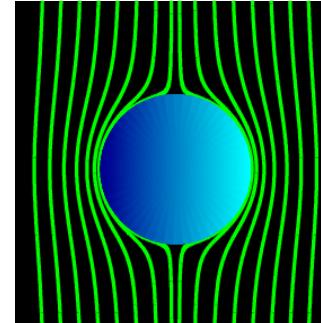
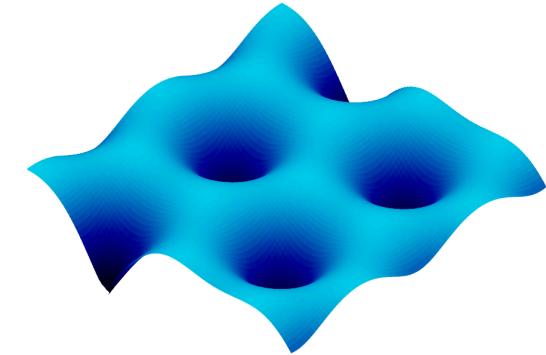
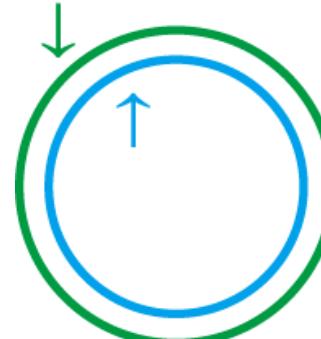
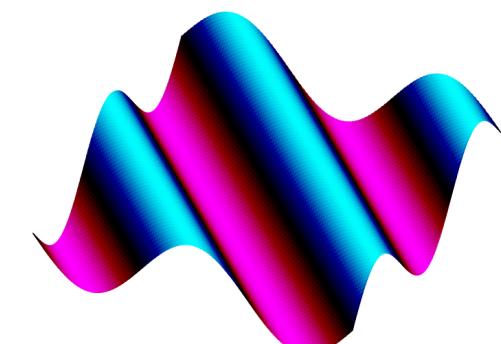
In most type-II singlet superconductors, $H_{\text{orb}} \ll H_{\text{P}}$

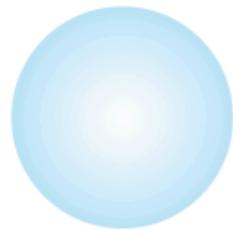


What happens in this situation?

Overview

~ Competition and Interplay ~

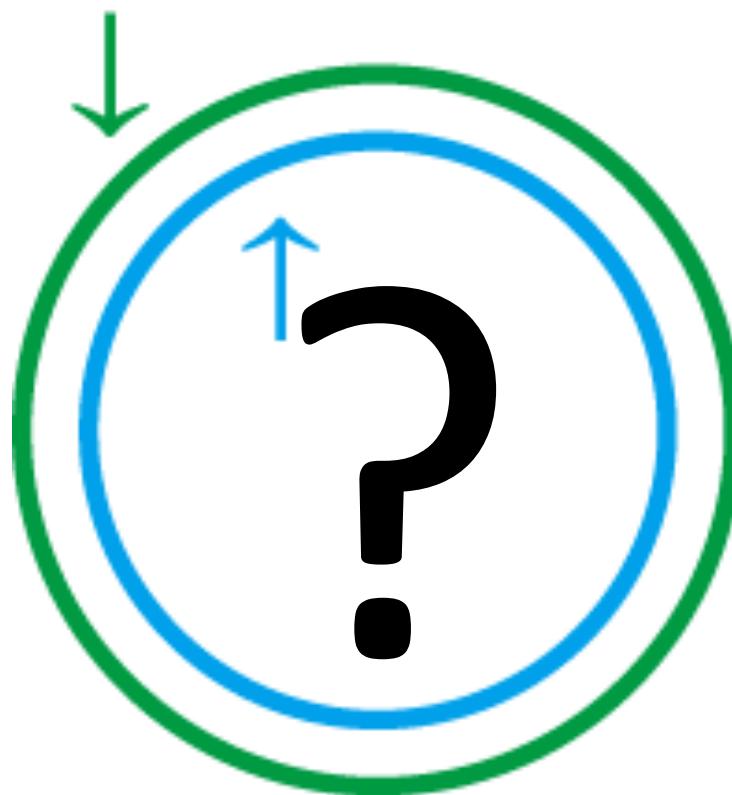
	<i>Competition</i>	<i>Interplay</i>
Flux Expulsion	Meissner Effect 	Vortex State 
Spin Polarization	Zeeman Effect 	FFLO State 

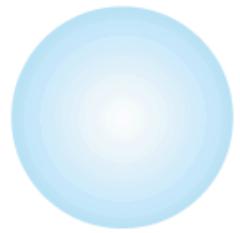


FFLO state

Question:

Can pair be formed on Zeeman-split Fermi surfaces??





FFLO state

1964, Fulde & Ferrell [Phys. Rev. **135**, A550]
Larkin & Ovchinnikov [Sov. Phys. JETP **20**, 762]

PHYSICAL REVIEW

VOLUME 135, NUMBER 3A

3 AUGUST 1964

Superconductivity in a Strong Spin-Exchange Field*

PETER FULDE AND RICHARD A. FERRELL

University of Maryland, College Park, Maryland

(Received 23 December 1963; revised manuscript received 17 April 1964)

SOVIET PHYSICS JETP

VOLUME 20, NUMBER 3

MARCH, 1965

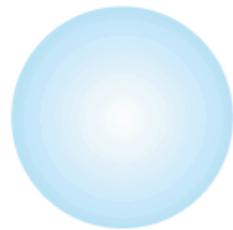
INHOMOGENEOUS STATE OF SUPERCONDUCTORS

A. I. LARKIN and Yu. N. OVCHINNIKOV

Moscow Physico-technical Institute

Submitted to JETP editor April 16, 1964

J Exptl. Theoret. Phys. (U.S.S.R.) 47, 1136-1146 (September, 1964)



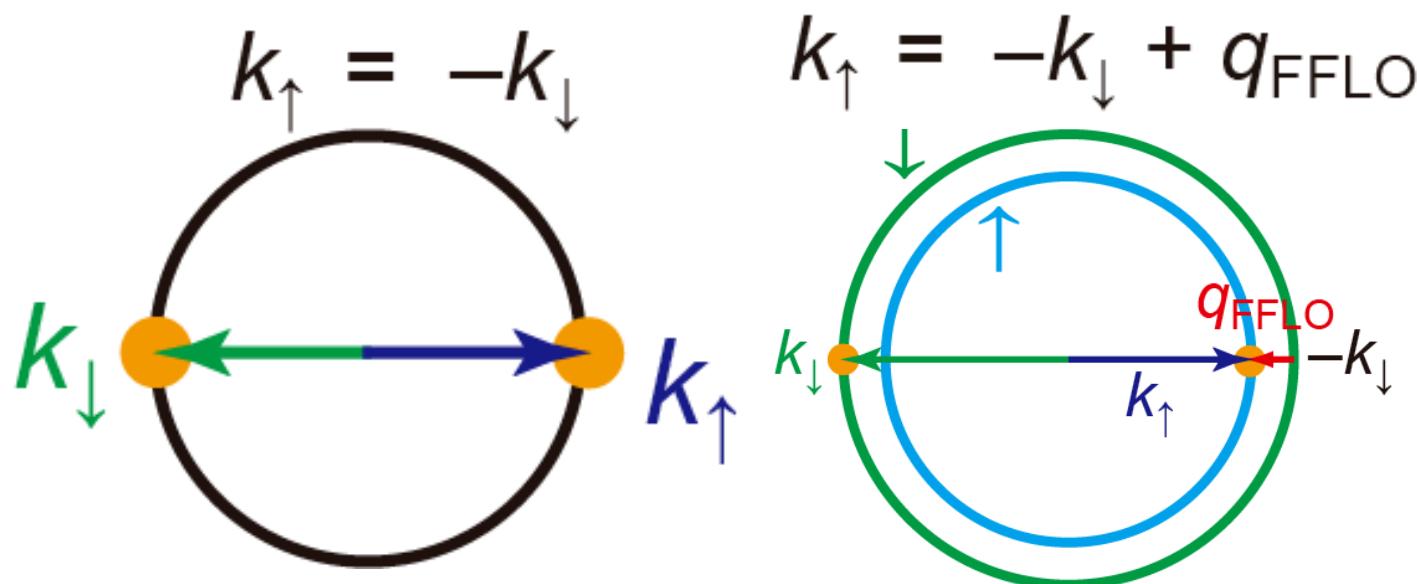
FFLO state



Question:

Can pair be formed on Zeeman-split Fermi surface??

Answer: Theoretically possible! But not usual BCS state.

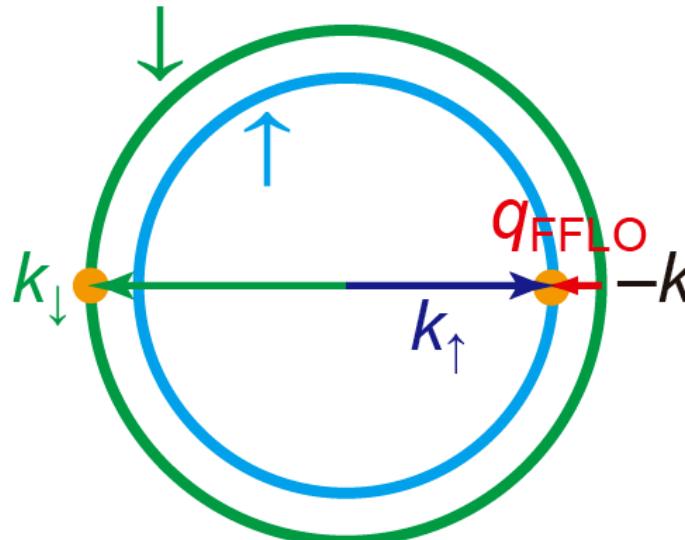


The center-of-mass momentum of the pair is non-zero

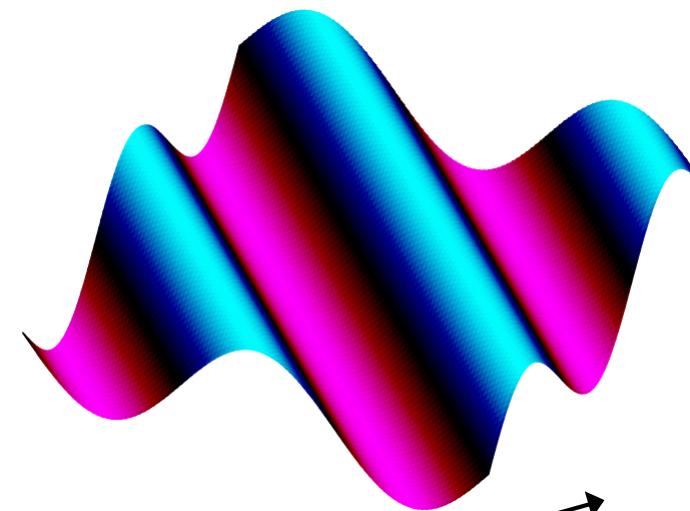
Fulde & Ferrell, Phys. Rev. **135**, A550 (1964).

Larkin & Ovchinnikov, Sov. Phys. JETP **20**, 762 (1964).

FFLO state: Spatial modulation



$$k_\uparrow = -k_\downarrow + q_{\text{FFLO}}$$



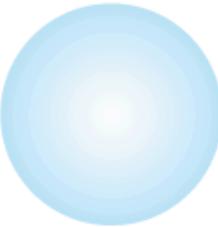
Spatial modulation of the order parameter $\Delta(r)$

$$\Delta(\mathbf{r}) = \Delta_0 \exp(i\mathbf{q}_{\text{FFLO}} \cdot \mathbf{r}) \quad [\text{Fulde \& Ferrell}]$$

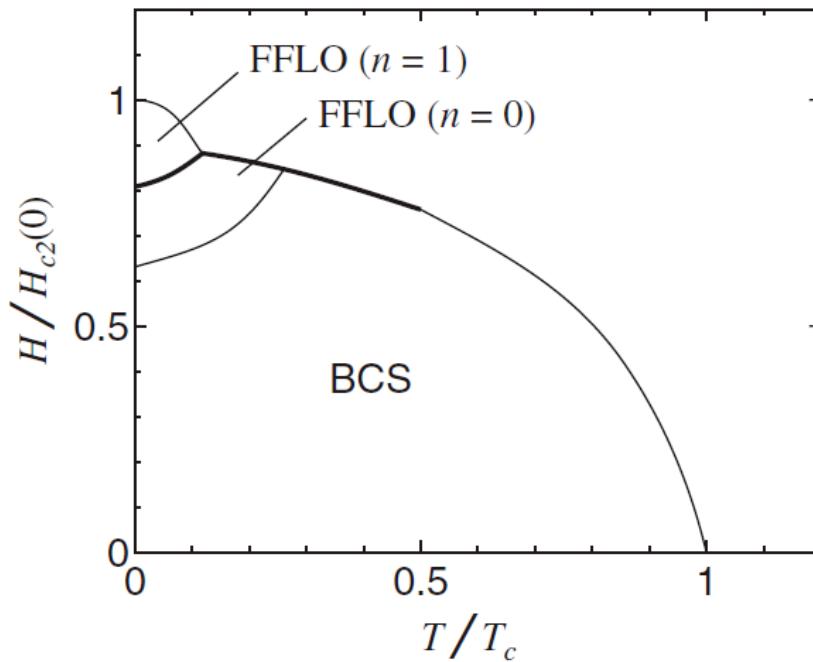
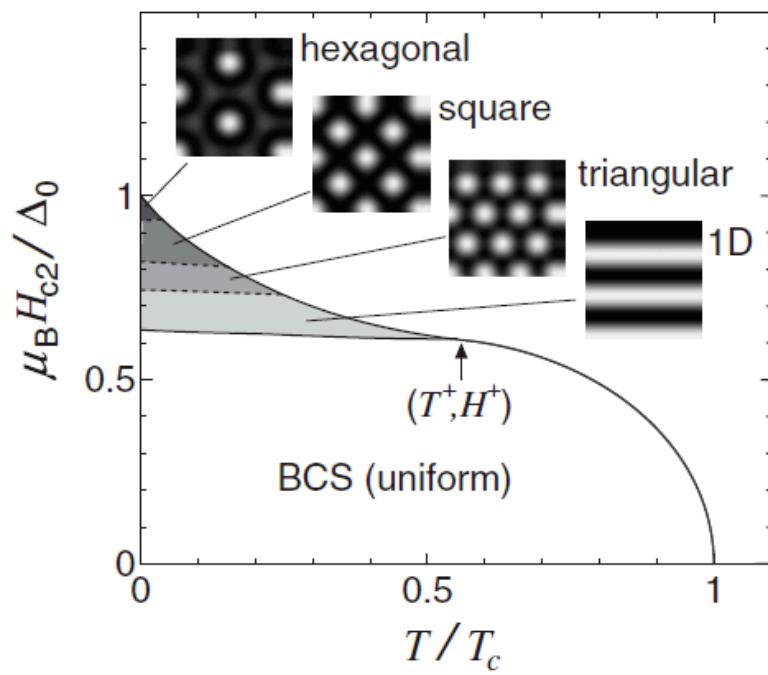
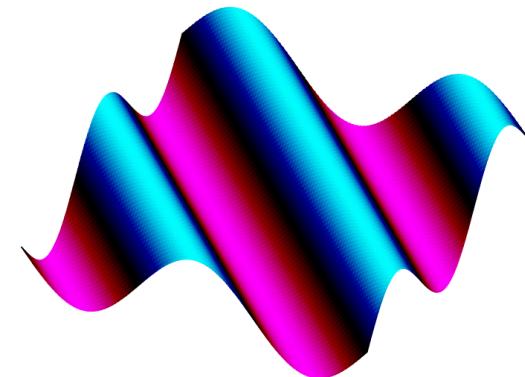
$$\text{or } \Delta_0 \cos(\mathbf{q}_{\text{FFLO}} \cdot \mathbf{r}) \quad [\text{Larkin \& Ovchinnikov}]$$

$$q_{\text{FFLO}} \sim 2\mu_B H / \hbar v_F$$

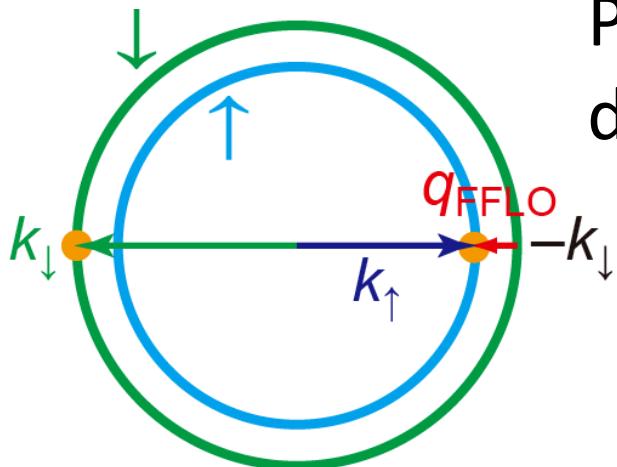
FFLO state: Phase Diagram



FFLO state locates
high-field low-temperature region
of the superconducting phase

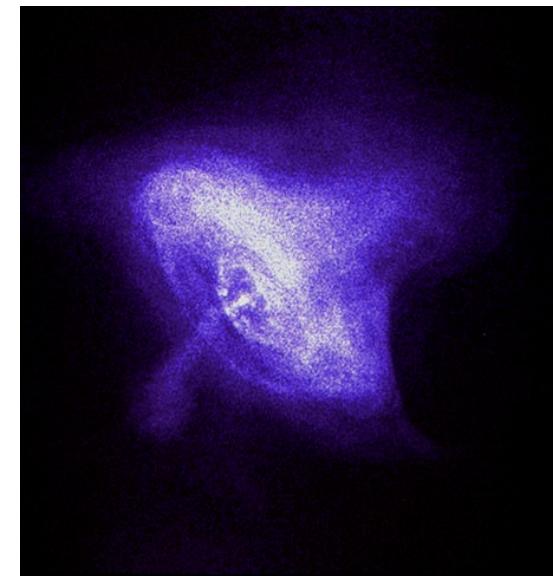
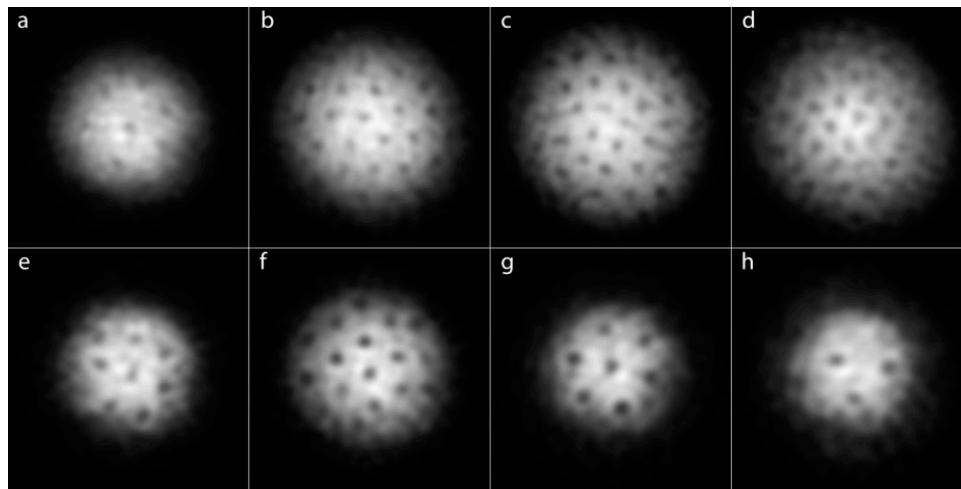


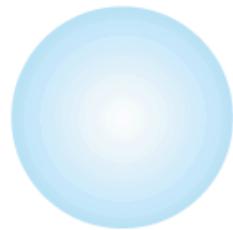
FFLO-related physics in other research fields



Pairing state of particles with different chemical potentials

- \uparrow Spin- \downarrow Spin Imbalanced Atomic Gas
- Color Superconductivity in pulsars





Required conditions for FFLO states

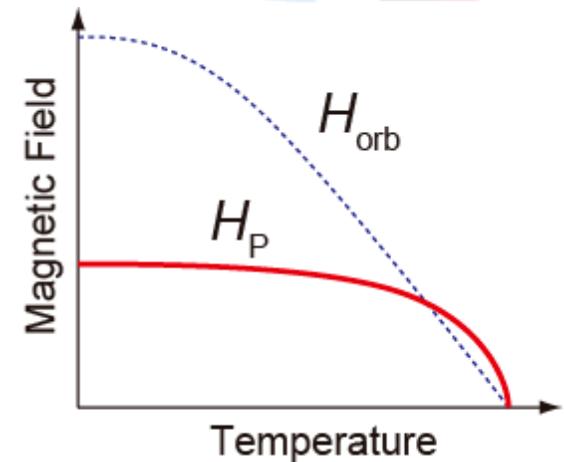


1. $H_P < H_{\text{orb}}$

Maki parameter:

$$\alpha \equiv \sqrt{2}H_{\text{orb}} / H_P > 1.8$$

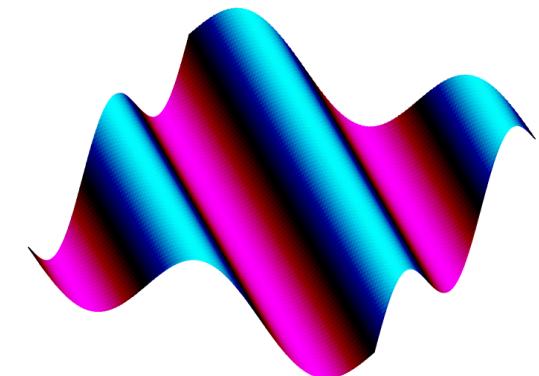
Accurate field alignment is often required.



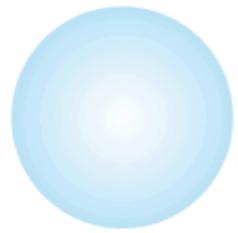
2. Very clean material

Mean free path \gg coherence length

Very clean sample is required.



Despite long history and much effort devoted,
FFLO state had not been observed for nearly 40 years!!



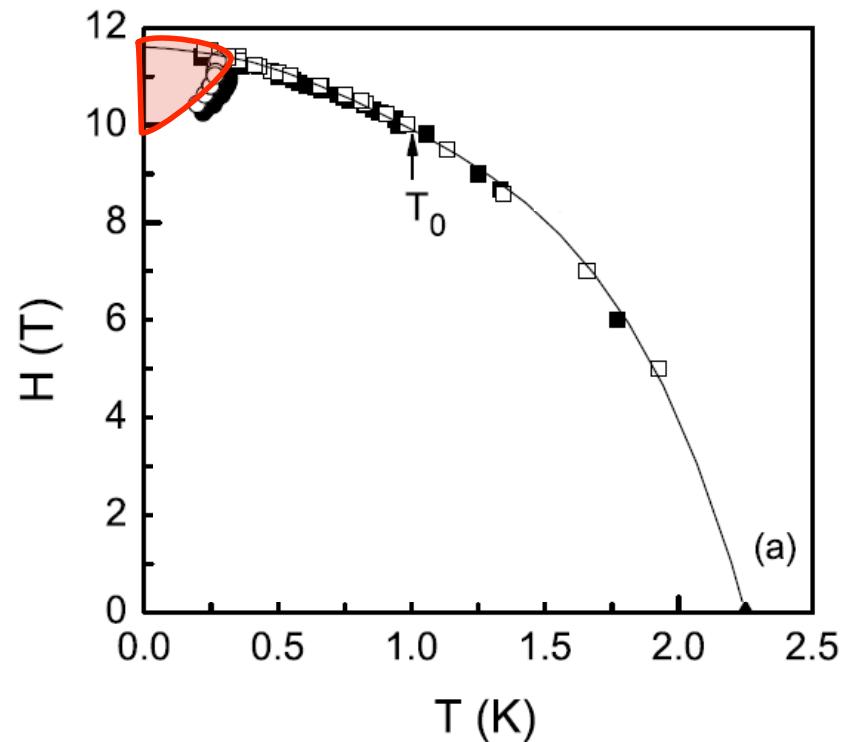
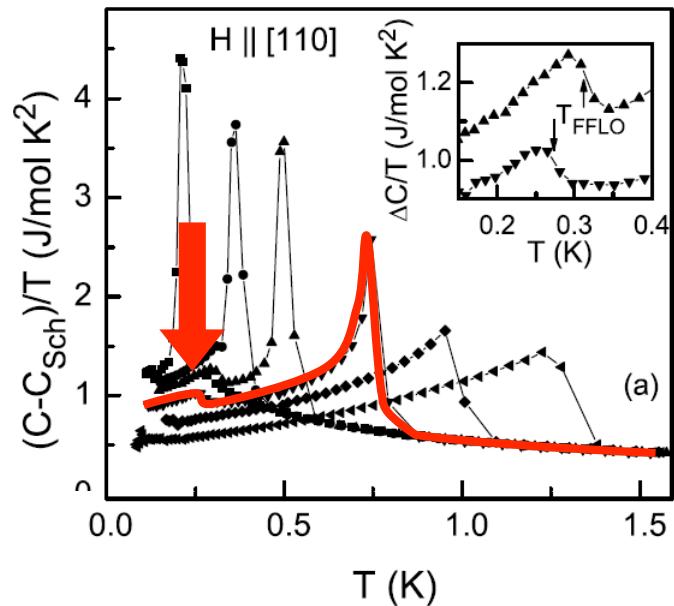
Candidate for FFLO states (1)

Heavy-Fermion CeColn₅

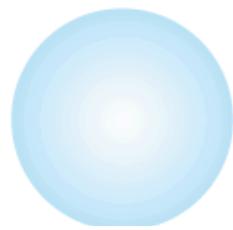


Heavy Fermion superconductor CeColn₅

$$\alpha = \sqrt{2} H_p / H_{\text{orb}} \sim 4.5$$

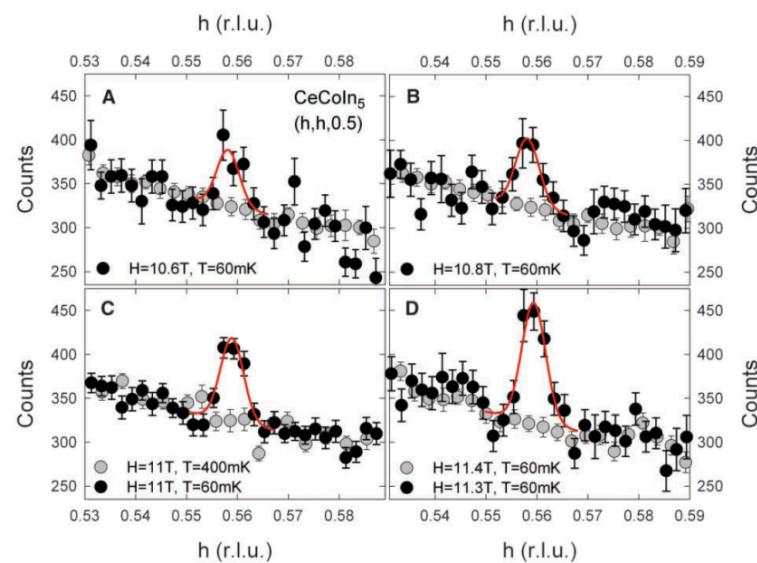
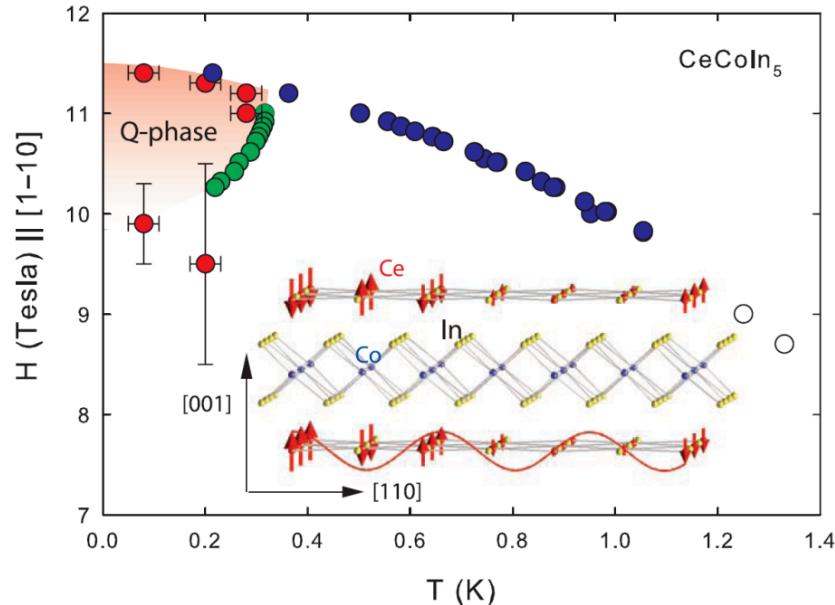


At high field,
another SC phase is observed!



Candidate for FFLO states (1)

Heavy-Fermion CeCoIn₅



However....

Recent experiments revealed
that antiferromagnetic order
coexists with the "FFLO" state.

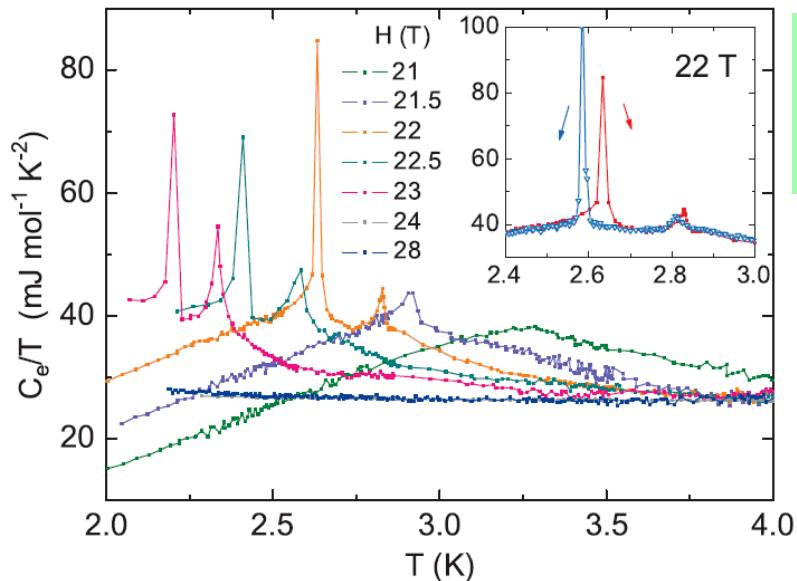
M. Kenzelmann *et al.*, Science 321, 5896 (2008)

The "FFLO" state is not
a text-book like modulated state.

Quantum criticality is involved??

Candidate for FFLO states (2)

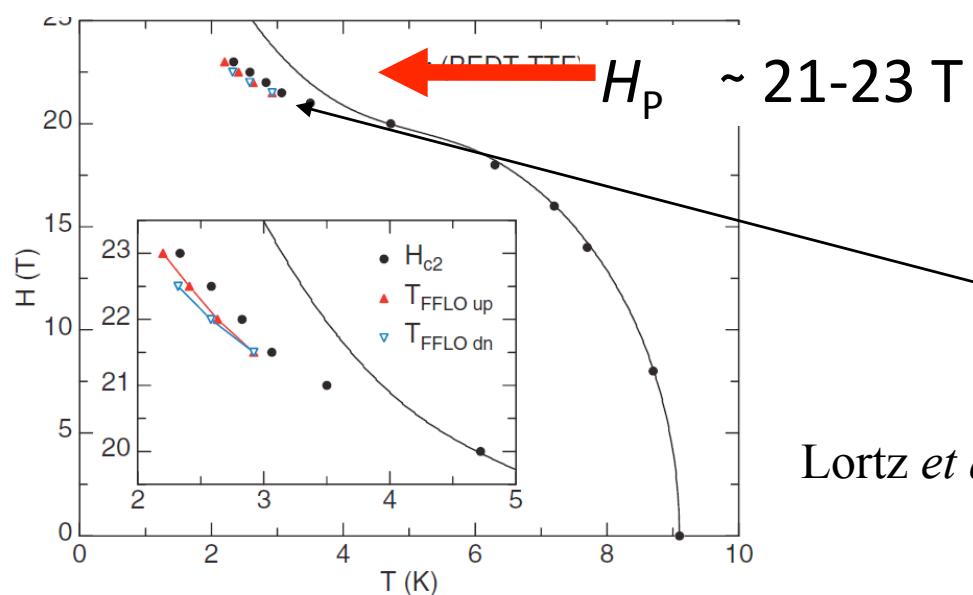
Q2D Organic Superconductor



Quasi-two-dimensional organic superconductor κ -(BEDT-TTF)₂Cu(NCS)₂

● $\alpha = \sqrt{2}H_p / H_{\text{orb}} \sim 8$

$H //$ conductive plane



Two phase transitions in high fields

FFLO state??

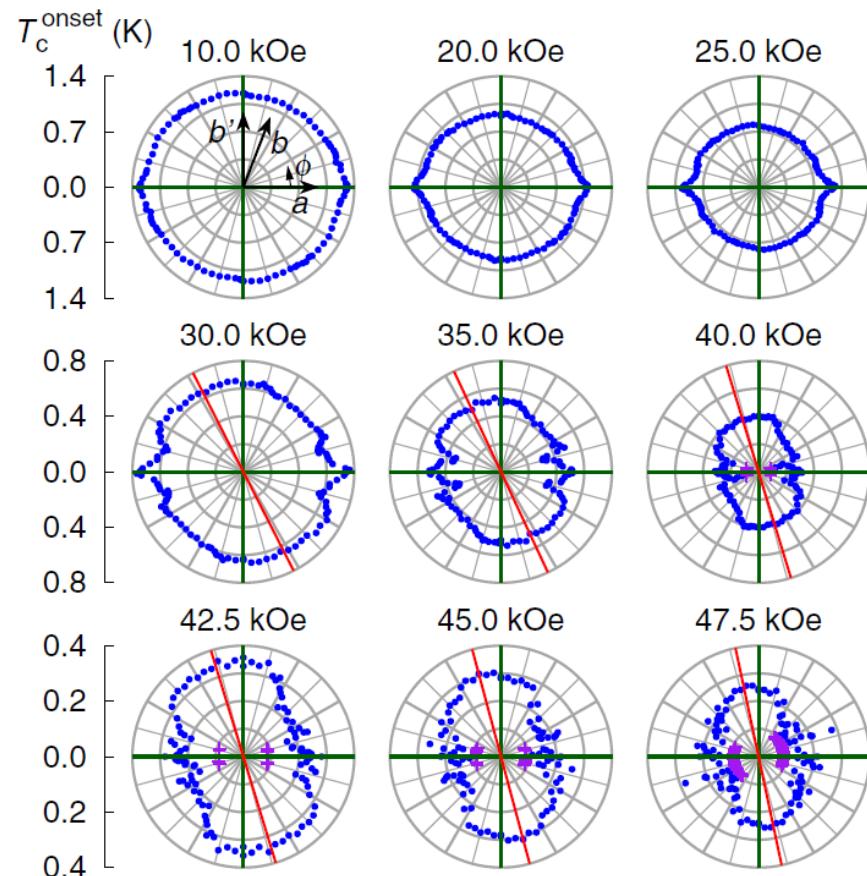
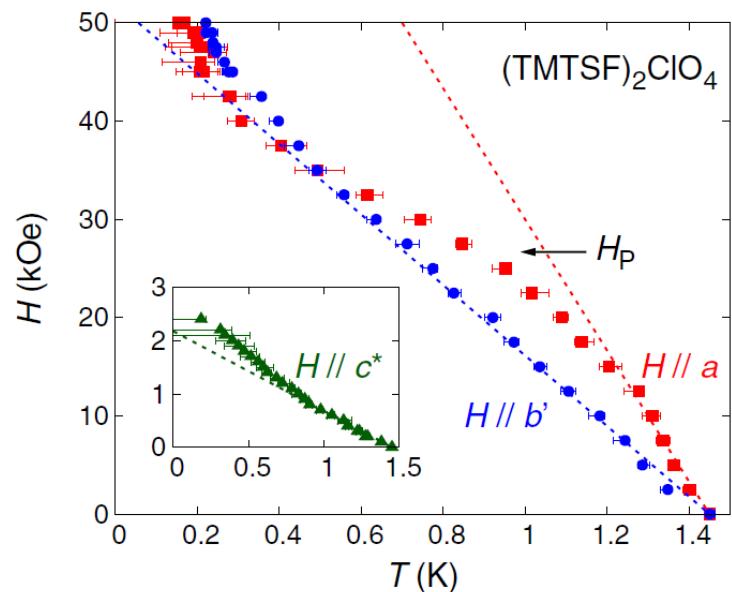
Lortz *et al.*, Phys. Rev. Lett. **99**, 187002 (2007).

Candidate for FFLO states (3)

Q1D Organic Superconductor



Quasi-one-dimensional organic superconductor $(\text{TMTSF})_2\text{ClO}_4$



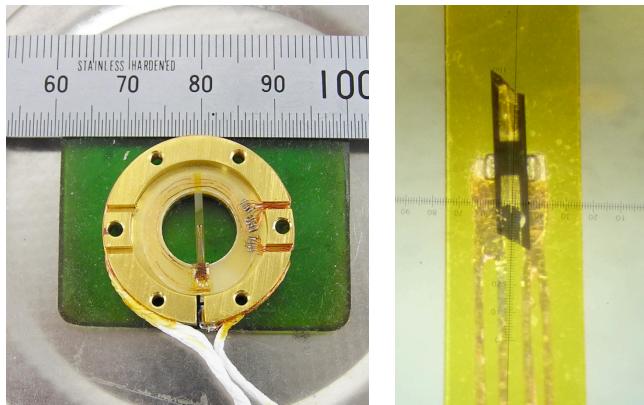
- $\alpha = \sqrt{2}H_p / H_{\text{orb}} \sim 3.7$ ($H \parallel a$)
- Resistivity onset T_c^{onset} remains finite in high fields.
- Unusual in-plane field angle dependence of T_c^{onset}

S. Yonezawa *et al.*, Phys. Rev. Lett. **100**, 117002 (2008).

Our recent specific-heat study on $(\text{TMTSF})_2\text{ClO}_4$

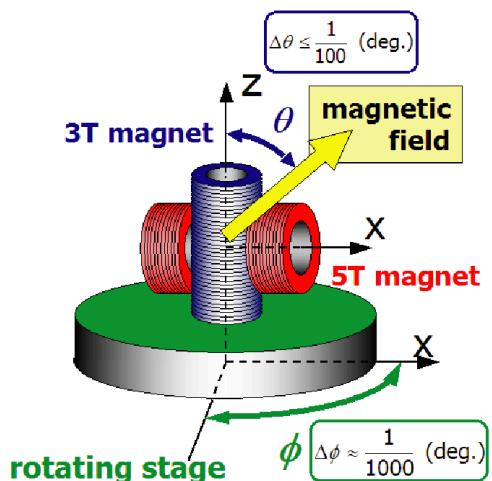


Sensitive calorimeter for further studies of the high-field SC state



mass: 0.102 mg

$$\rightarrow \Delta C / T_c = 1.7 \text{ nJ/K}^2$$



Phase Diagram of $(\text{TMTSF})_2\text{ClO}_4$

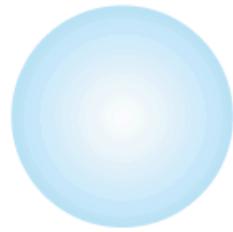


Summary

~ Competition and Interplay ~

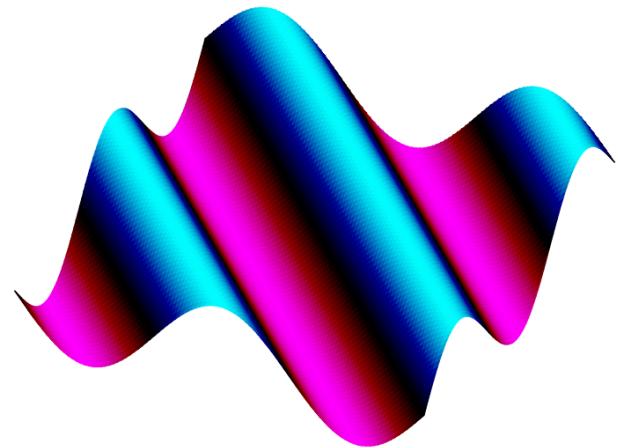


	<i>Competition</i>	<i>Interplay</i>
Flux Expulsion	Meissner Effect Quantum Criticality & Magnetism ?	Vortex State
Spin Polarization	Zeeman Effect Low Dimensionality and Fluctuations ?	FFLO State



Concluding Remark

We are almost catching the "FFLO wave",
40 years after the first prediction,



But....



We need more effort to really enjoy it!