

# Molecular dynamics study of the lifetime of nanobubbles on the substrate



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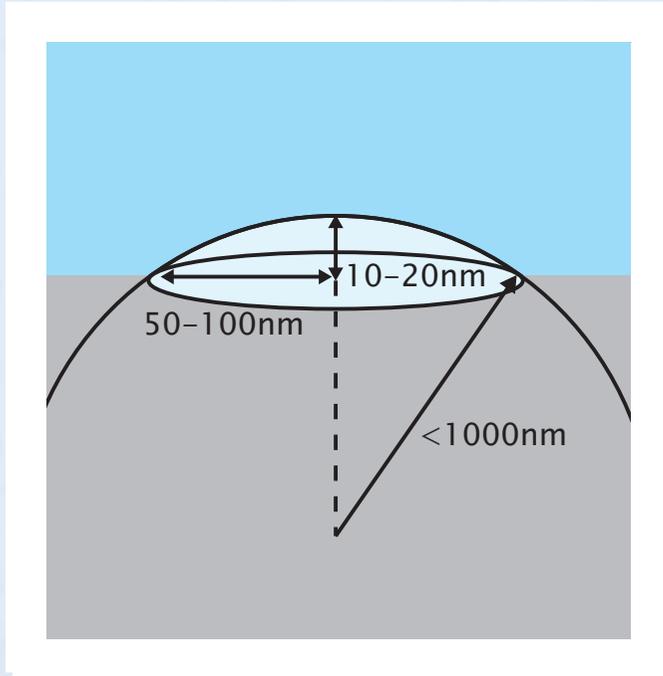
# Outline

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- Introduction
  - nanobubbles
  - stability of nanobubbles
  - preceding studies
  - purpose of this study
- Molecular dynamics simulations
- Numerical results
  - in the bulk liquid vs on the substrate
  - Knudsen gas ?
- Summary and remarks

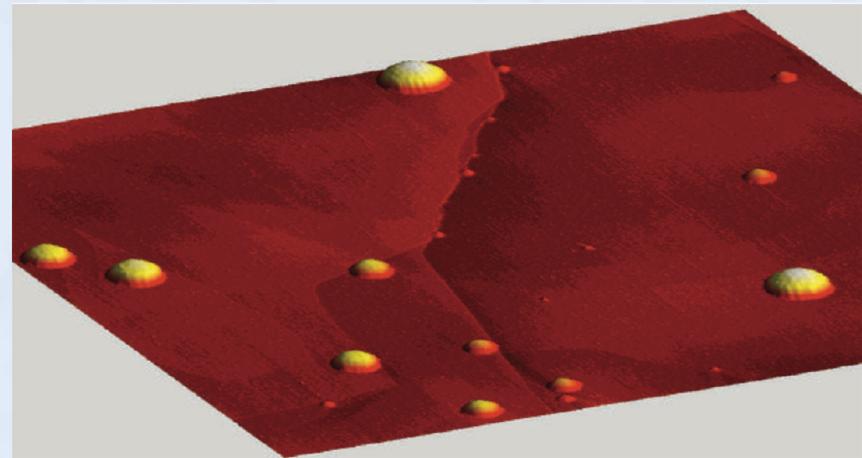
# Nanobubbles

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Schematic illustration of typical nanobubble on a substrate

- radius  $\sim < 1 \mu\text{m}$
- One cause of microscale behavior of fluids



Borkent et al.  
Langmuir, 26, 260 (2010)

- Observed in experiments using AFM or IR spectroscopy

# Nanobubbles are stable ?

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- Theoretical prediction
  - Nanobubbles are unstable

Young–Laplace equation

- High pressure in nanobubbles

$$\Delta p = \gamma \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$

--> Gas in nanobubbles dissolve immediately

lifetime < 100 $\mu$ s

(spherical bubble, diameter = 100nm)

cf. Ljunggren and Eriksson, Colloids Surf. A, 130, 151 (1997)

- In experiment
  - Nanobubbles are stable

lifetime > 4days

# Suggestions for stability

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1. Young–Laplace equation is NOT applicable to nanobubbles.
2. Young–Laplace equation IS applicable to nanobubbles. But surface tension is reduced and bubbles shrink slowly.
3. Gas atoms in the bubble do dissolve, but outflux is balanced by the influx in nonequilibrium state.

# Classical theory is applicable ?

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1. Classical diffusion theory is not applicable ?
  - MD simulations of nucleation of stable nanobubbles



surface tension

Young–Laplace equation is applicable to nanobubbles.  
( confirmed in many MD simulations of nucleation evaluating surface tension )

Nagayama et al. J. Heat. Mass. Trans., 49, 4437 (2006)

- single component  
    <-> real nanobubbles are filled with gas

# Why nanobubbles are stable ?

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## 2. Reduction of surface tension

- Theoretical model and experiments
- Impurities on gas-liquid interface
  - Reduce surface tension
  - Prevent dissolution of gas
- > Nanobubbles shrink slowly

Das et al. Phys. Rev. E, 82, 056310 (2010)

more than  $\times 10^9$  lifetime ? -> not enough

3. Nonequilibrium stabilizing mechanism  
: Outflux is balanced by an equivalent influx



# Purpose of this study

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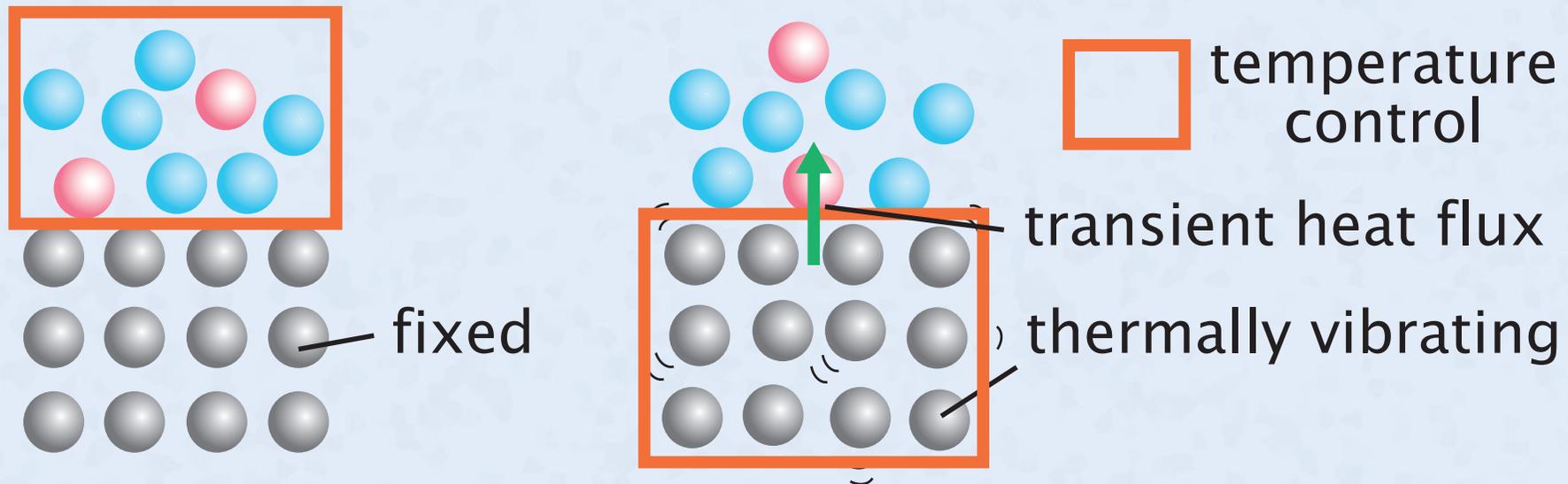
- Investigate dynamics of nanobubbles
  - > Molecular dynamics simulations
- Only a few MD simulations of nanobubbles in ternary systems ( liquid + gas + wall ) have performed.
  - > Create stable nanobubbles and survey shrinking nanobubbles
- Introduce nonequilibrium ( transient heat flux )
  - > Thermal wall

# Molecular Dynamics Simulations

- Interaction - Lennard-Jones 6-12 potential

$$U(r) = 4\epsilon_{ij} \left\{ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right\}$$

- $N, V, (T) = \text{const.}$
- Liquid and gas - Ar and Ne respectively
- Fixed wall and thermal wall



# Two Steps of Simulations

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Step1 : Creation of nanobubbles

$T = 85\text{K}$

- Nanobubbles are stable
- Bubble nucleation occurs spontaneously
- Negative system pressure ( stretched state )

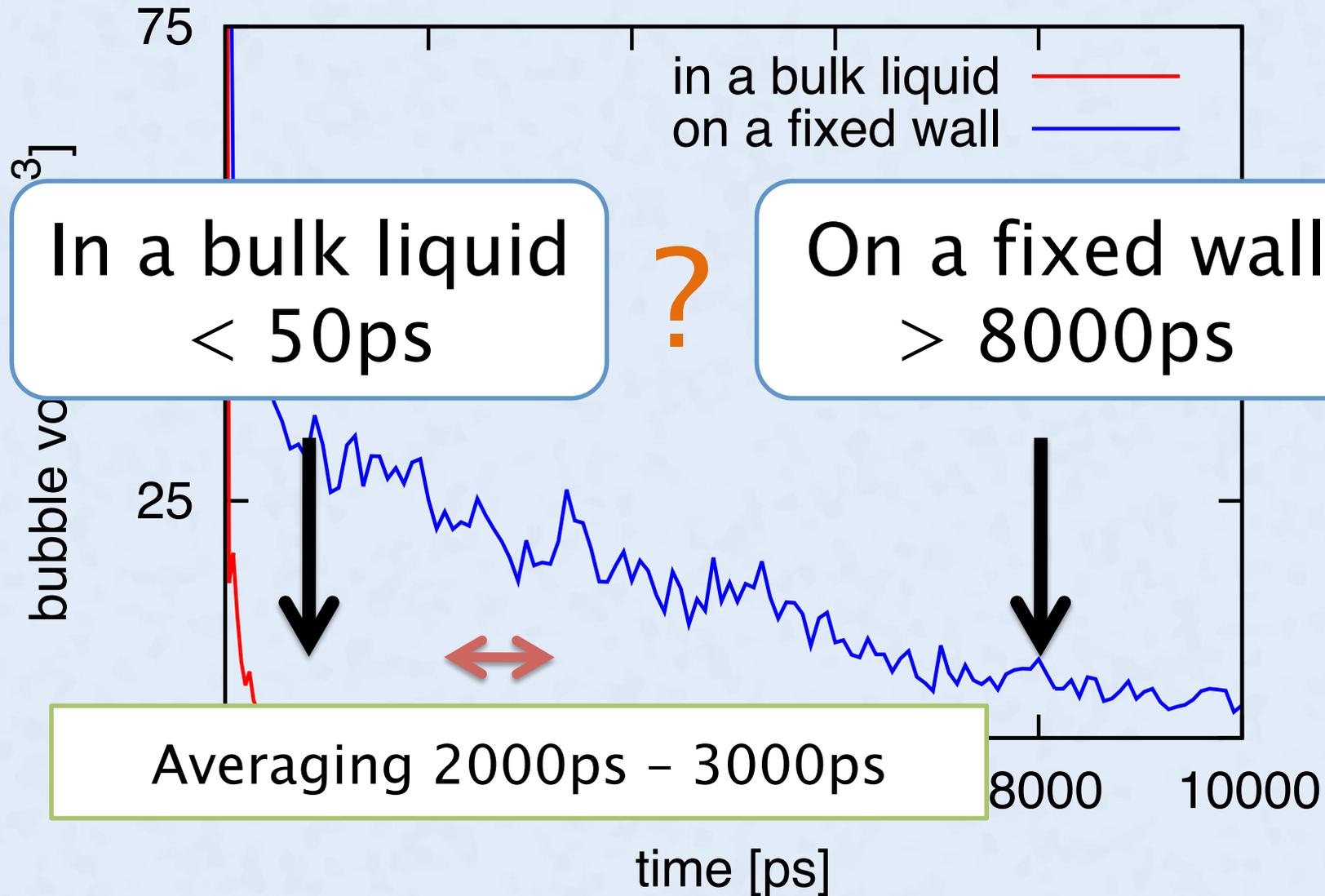
Step2  $\rightarrow$  Step1 : Quenching ( bubble nucleation )

Step2 : Simulations of shrinking nanobubbles

$T = 104\text{K}$

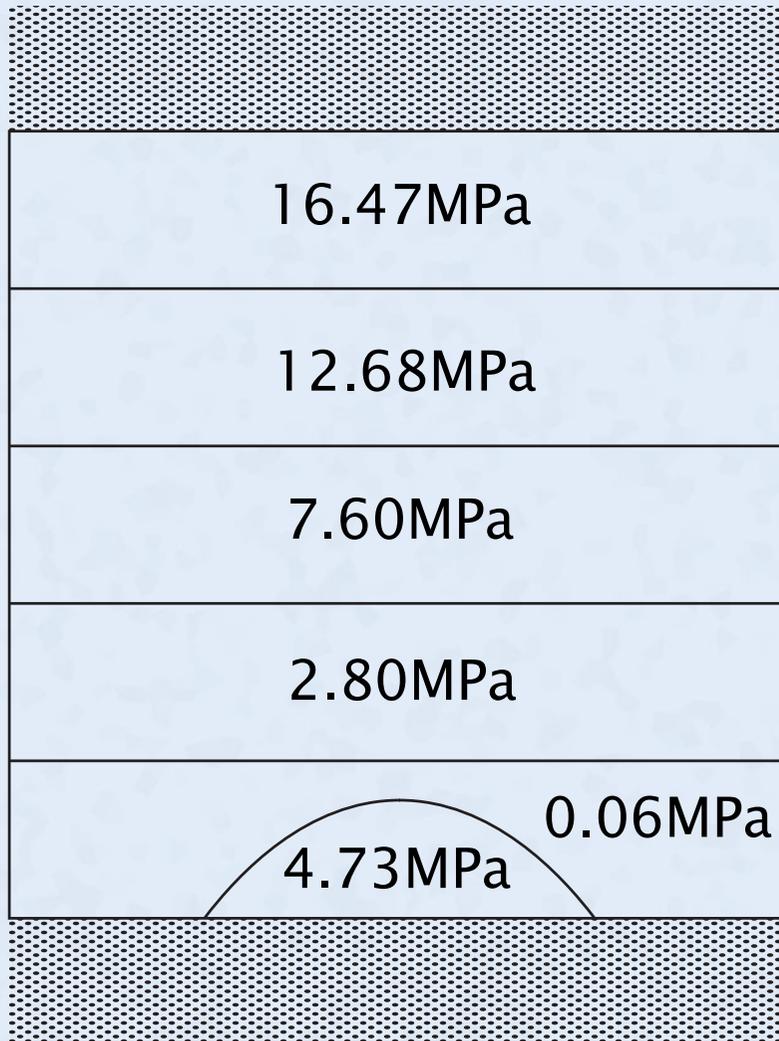
- Nanobubbles are unstable
- Bubble nucleation does not occur
- Positive system pressure

# Lifetime of Nanobubbles



# Inhomogeneity of the System

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Averaged pressure

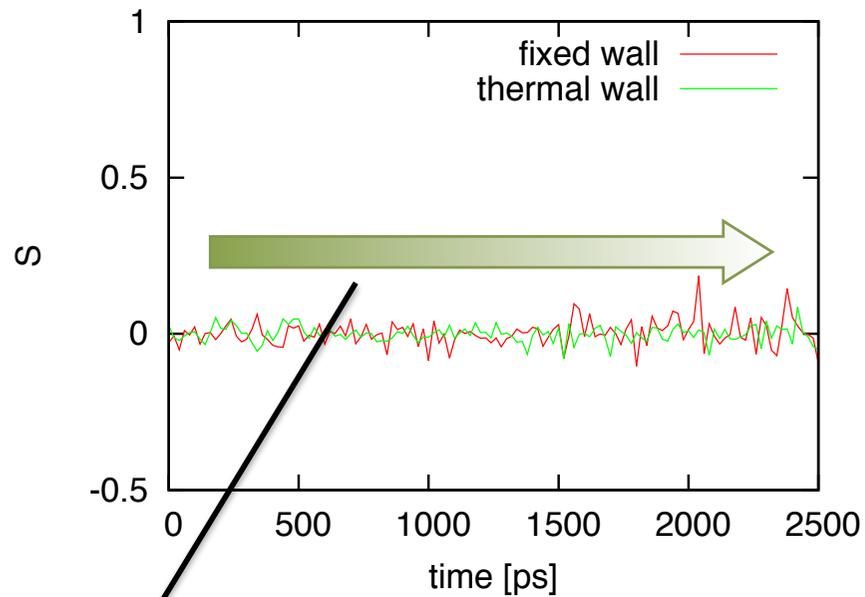
- 2000ps – 3000ps
- 5 regions parallel to the wall

Low pressure  
near the bubble

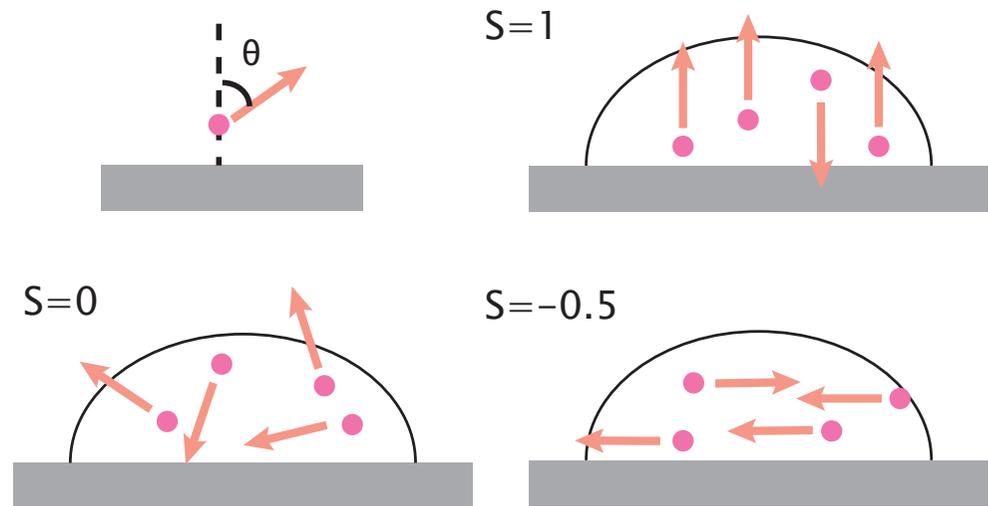


Increases lifetime of  
the bubble

# Knudsen Gas Behavior ?



transient heat flux exists :  
wall  $\rightarrow$  liquid & gas  
(thermal wall)



$$S = (3\langle \cos^2 \theta \rangle - 1) / 2$$

- No anisotropic motion of gas atoms observed

# Summary

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- Lifetime of nanobubbles on a substrate is more than 100 times longer than in a bulk liquid.
- Inhomogeneity of the system increases the lifetime of nanobubbles
- Lifetime of simulated nanobubbles was shorter than  $1\ \mu\text{s}$ . ( No stabilizing mechanism is implemented in simulations. )
- Thermal wall is also employed to realize transient nonequilibrium state.
- Knudsen gas behavior is not observed.

# Remarks

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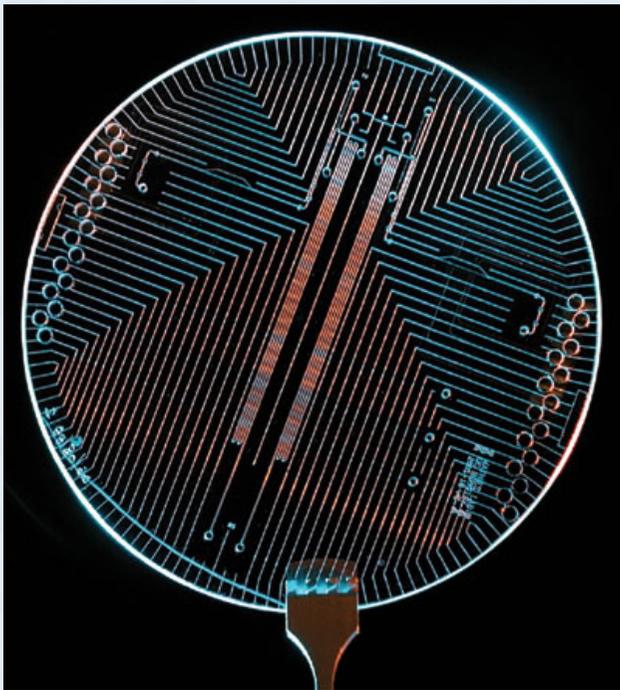
- Knudsen number in simulated nanobubble  $Kn \sim 2$  is slightly higher than proposed condition.  
→ Create lower density nanobubbles
- Simulated nanobubbles are smaller than real nanobubbles.  
→ Larger calculations
- More detailed analysis is needed to investigate flux of atoms.

# Microfluidics\*

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## Microscale behavior of fluids

- Apparent slip on walls
- Attractive force between walls



Lab on a chip for DNA sequencing  
diameter of the wafer = 100mm  
Nature 444, 985 (2006)

= differ from macroscale

Surface tension

Hydrophobicity of the wall

## Technological application

- Flow or mixing control  
in microfluidic devices  
...and more

# Molecular Dynamics Simulations

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- Solve equation of motion for each particle
- Interaction – Lennard–Jones 6–12 potential

$$U(r) = 4\epsilon_{ij} \left\{ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right\}$$

Interaction between different species  
– Berthelot–Lorentz law

$$\sigma_{\alpha\beta} = \frac{\sigma_{\alpha} + \sigma_{\beta}}{2}$$

$$\epsilon_{\alpha\beta} = \sqrt{\epsilon_{\alpha}\epsilon_{\beta}}$$

Cut off length = 2.24nm ( 6.58  $\epsilon_{\text{LiqLiq}}$  )

- NVT = const.

Motion of the center of mass is removed  
in order to avoid “flying ice cube”

# Particle Settings

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- Liquid and gas – Ar and Ne respectively

$$\sigma_{\text{LiqLiq}} = 0.3405\text{nm} \quad \sigma_{\text{GasGas}} = 0.2750\text{nm}$$

$$k_B \epsilon_{\text{LiqLiq}} = 119.8\text{K} \quad k_B \epsilon_{\text{GasGas}} = 35.05\text{K}$$

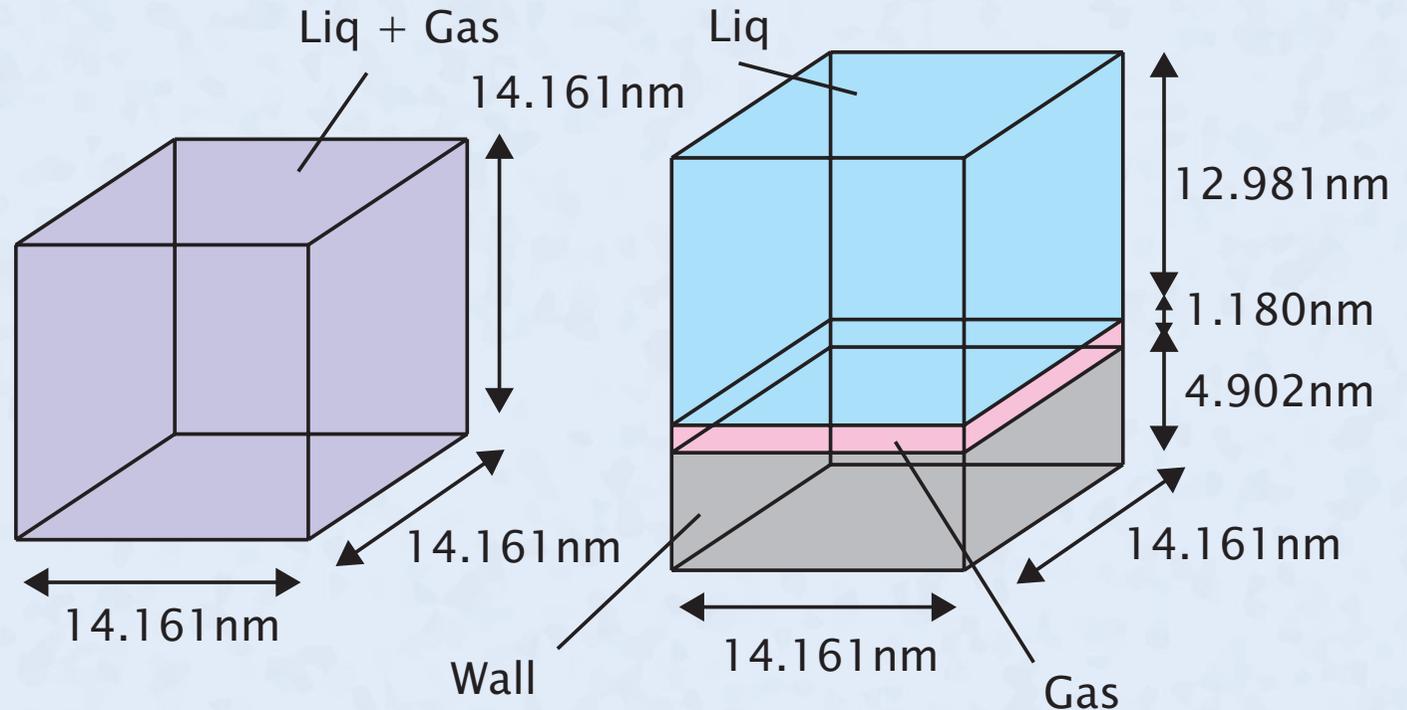
Baidakov and Protsenko, J. Chem. Phys., 26, 1701 (2008)

- Fixed wall – fixed to FCC lattice  
( Thermostat is applied to liquid and gas )
- Thermal wall
  - confined to FCC lattice by harmonic potential
  - behaves as a heat bath  
( Thermostat is applied only to wall particles )

# Simulations

## • Initial Conditions

Liq : 50688  
Gas : 4608  
Wall : 24336



## • System configurations

(I) In a bulk liquid

(III) On a thermal wall

(Temperature raised immediately)

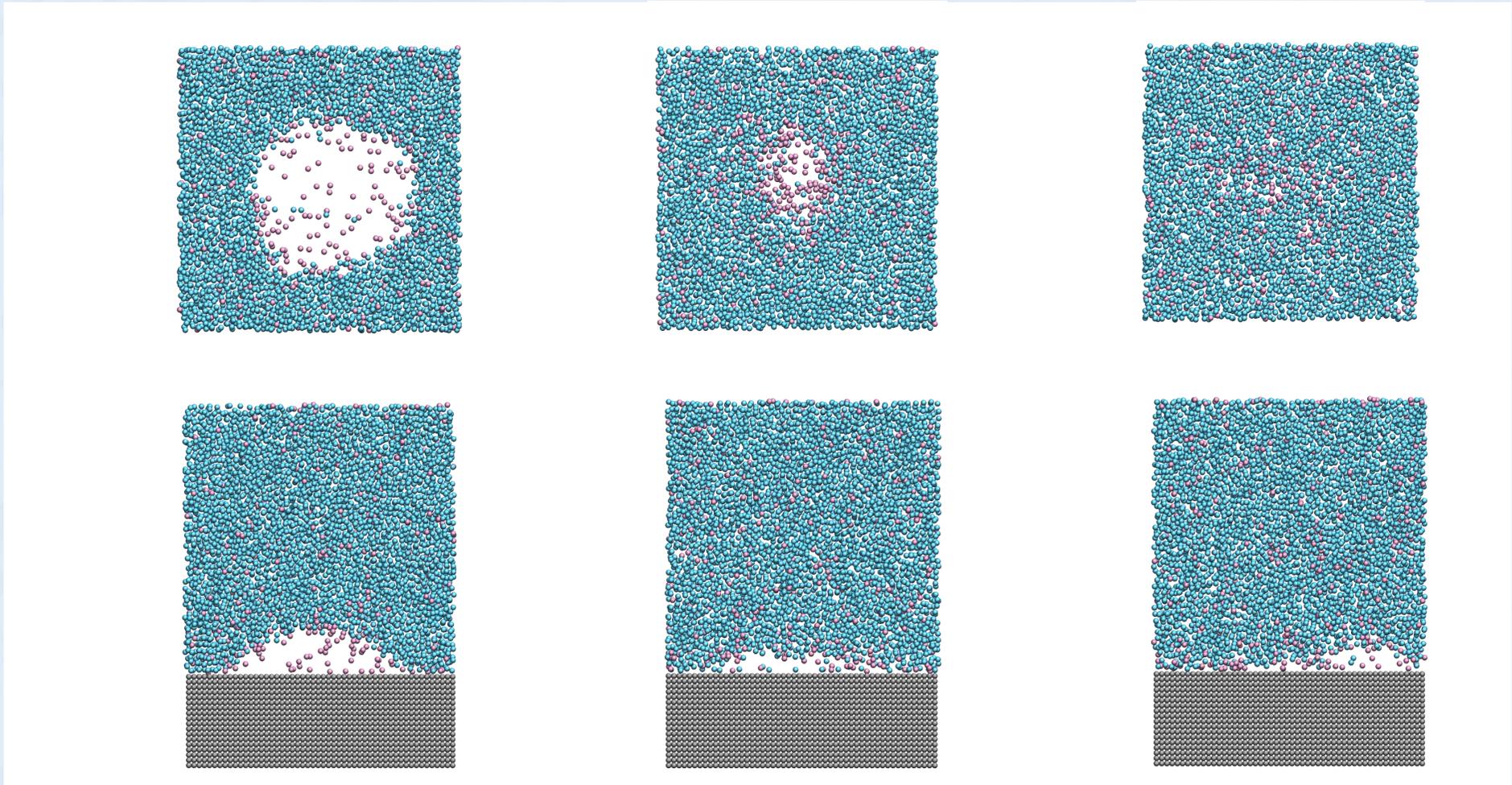
(II) On a fixed wall

(IV) On a thermal wall

(Temperature raised slowly)

# Visualized Shrinking Nanobubbles

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After temperature suddenly raised