

2017年大学院後期授業

# 宇宙論特論

暗黒物質優勢宇宙における構造形成

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(Kyoto Univ. Yukawa Institute for Theoretical Physics)

# Overview

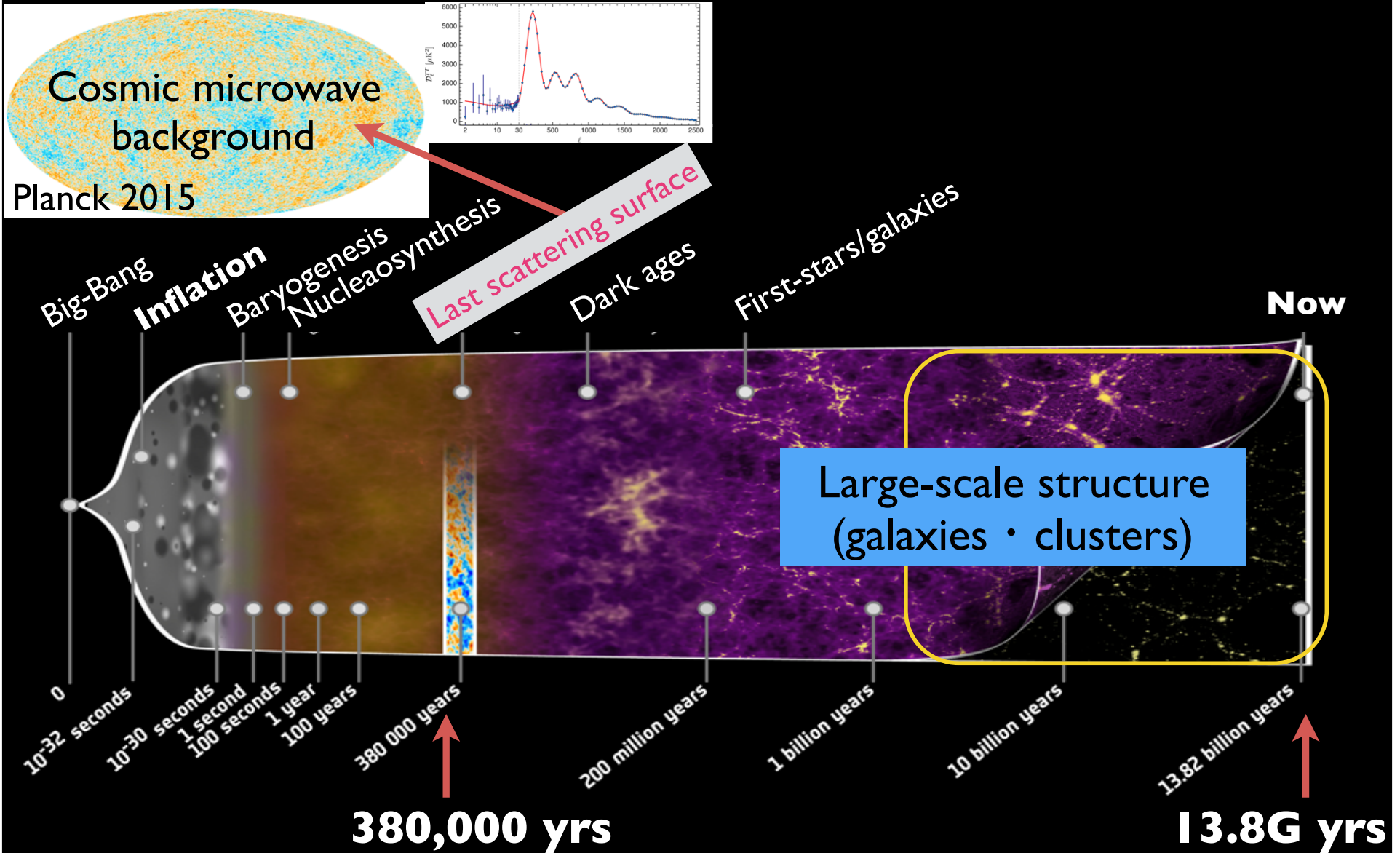
# Large-scale structure

Spatial matter inhomogeneities over Mpc  $\sim 10^3$  Mpc

Mpc =  $10^6$  parsec  $\sim 3 \cdot 10^6$  light years  
(c.f., 40kpc for size of Milky Way)

- Hierarchical clustering of matter distribution:  
galaxy  $\subset$  group / cluster  $\subset$  supercluster
- Contain rich cosmological information
  - primordial fluctuations,
  - structure formation
  - dynamics of cosmic expansion
- Traditionally traced by galaxy redshift surveys  
(other LSS probes are gravitational lensing, Lyman-alpha forest)

# Timeline of the Universe



# Observing large-scale structure

Intensive use of telescope is necessary

8.2m



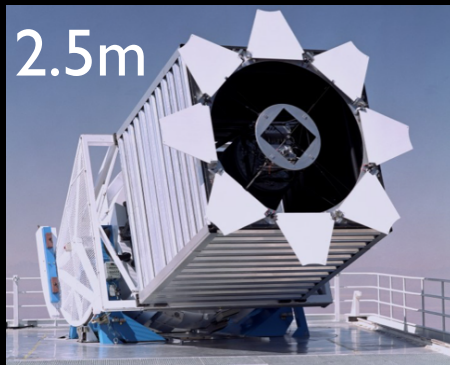
Very Large Telescope (Chile)

8.2m



Subaru Telescope (Hawaii)

2.5m



Sloan Digital Sky Survey  
@ APO (New Mexico)

3.6m



Canada-France-Hawaii  
Telescope (Hawaii)

4m



Blanco telescope  
@ CTIO (Chile)

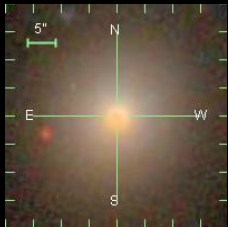
[https://en.wikipedia.org/wiki/Very\\_Large\\_Telescope](https://en.wikipedia.org/wiki/Very_Large_Telescope)  
<http://www.sdss.org/instruments/>  
<http://subarutelescope.org/Information/Download/DImage/index.html>  
<http://www.cfht.hawaii.edu/en/news/CFHT30/#wallpaper>  
<http://www.darkenergysurvey.org/DECam/index.shtml>

# Redshift

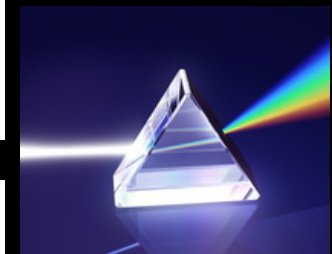
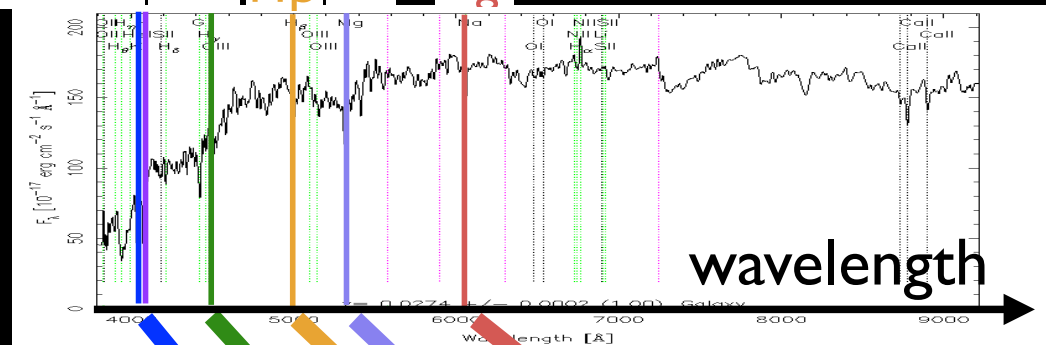
A key measurement to probe 3D view of large-scale structure

Distant galaxies look **redder** than nearby galaxies  
due to **cosmic expansion**

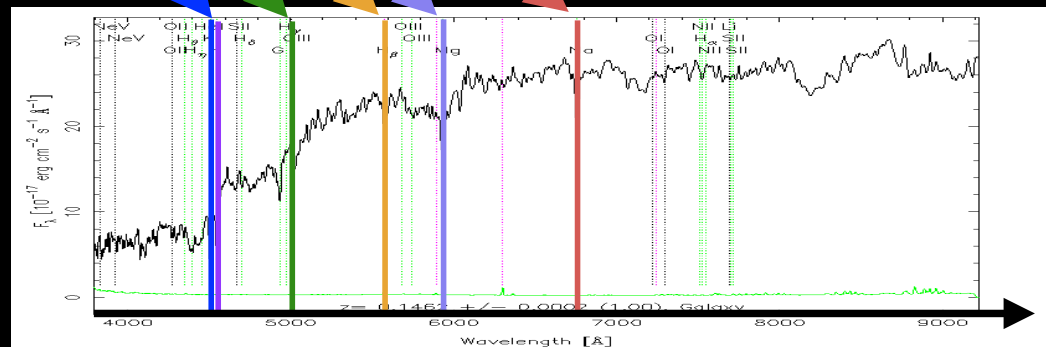
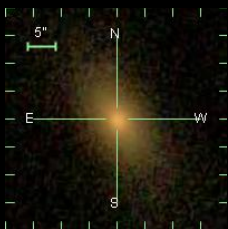
**Nearby galaxy**



Ca H & K   O III   H $\beta$    Na   Mg



**Distant galaxy**



SDSS SkyServer

# Redshift

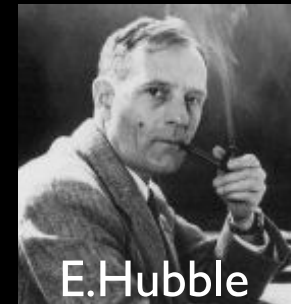
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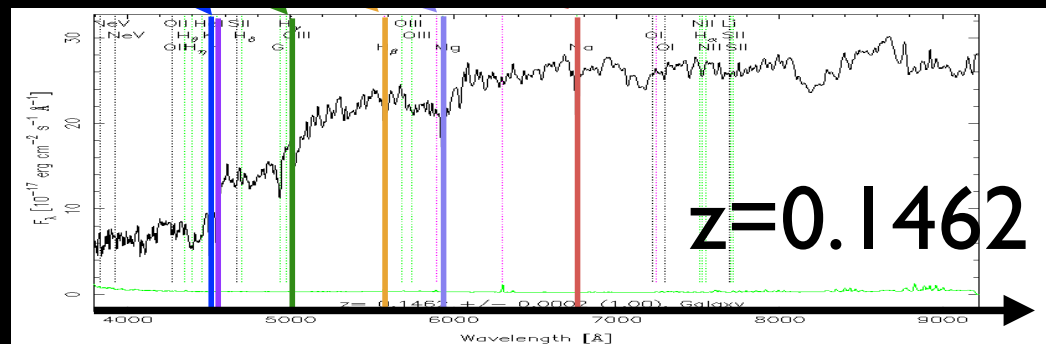
Redshift parameter  $z = \Delta\lambda/\lambda$

Hubble law

recession 'velocity'  $v = \underline{H} d$  distance to galaxy  
(=  $cz$ ) Hubble parameter



Distant galaxy

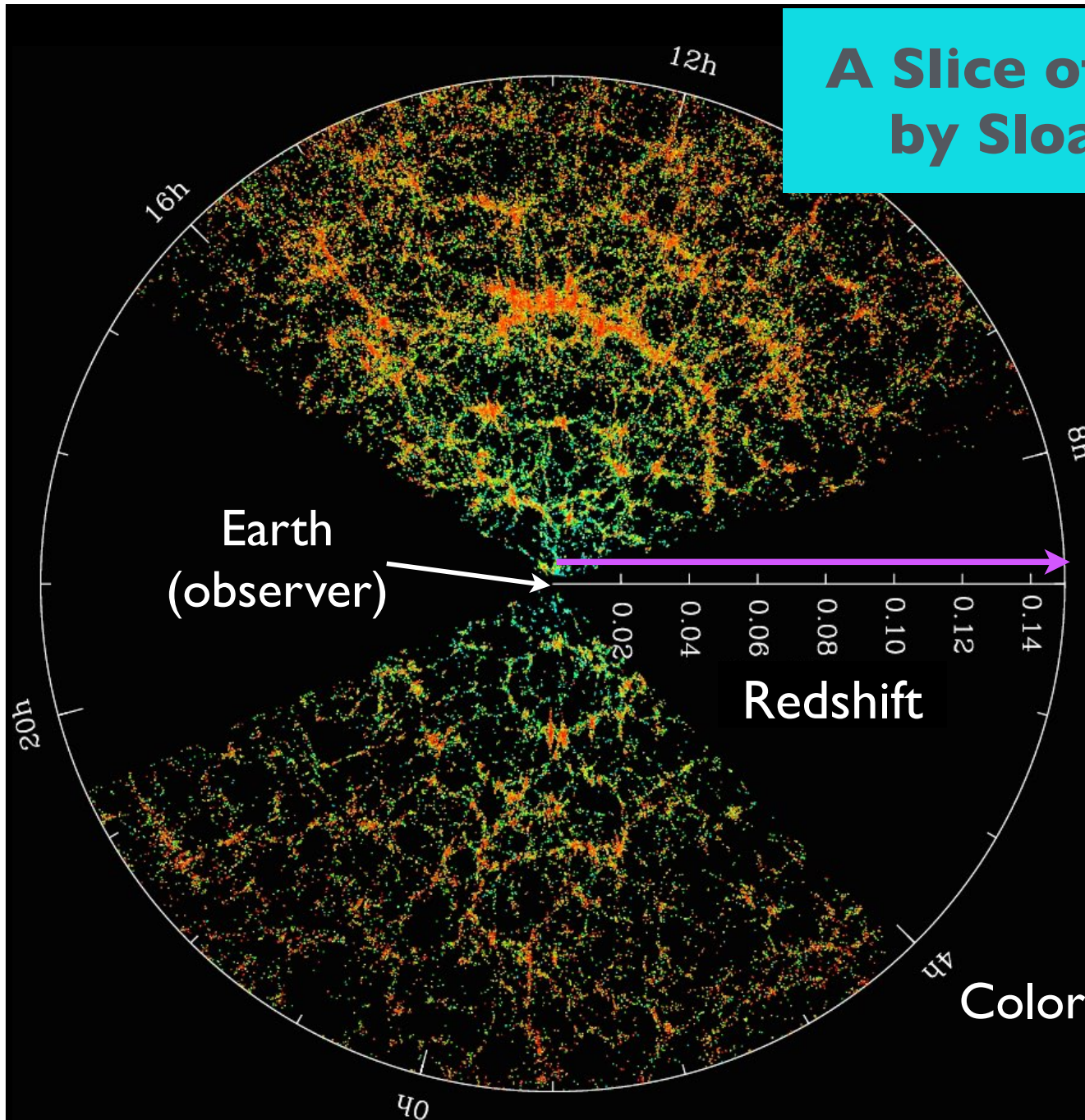


SDSS SkyServer

# A Slice of galaxy catalog by Sloan Digital Sky

finished in 2008

2 G yrs  
(look back time)



Color indicates age of galaxy

Blue : young

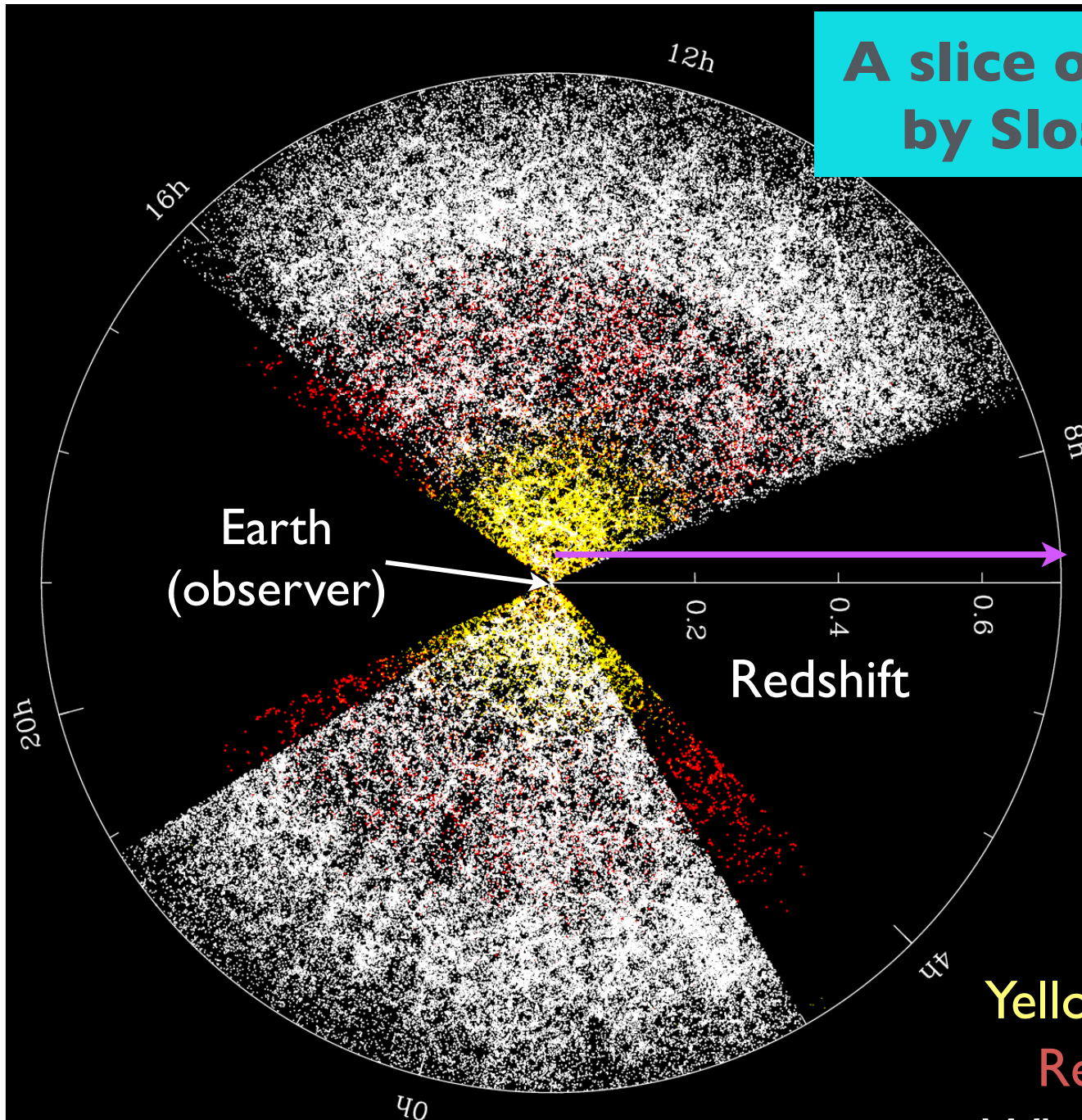
Red : old



# A slice of galaxy catalog by Sloan Digital Sky

finished in 2014

6 G yrs  
(look back time)

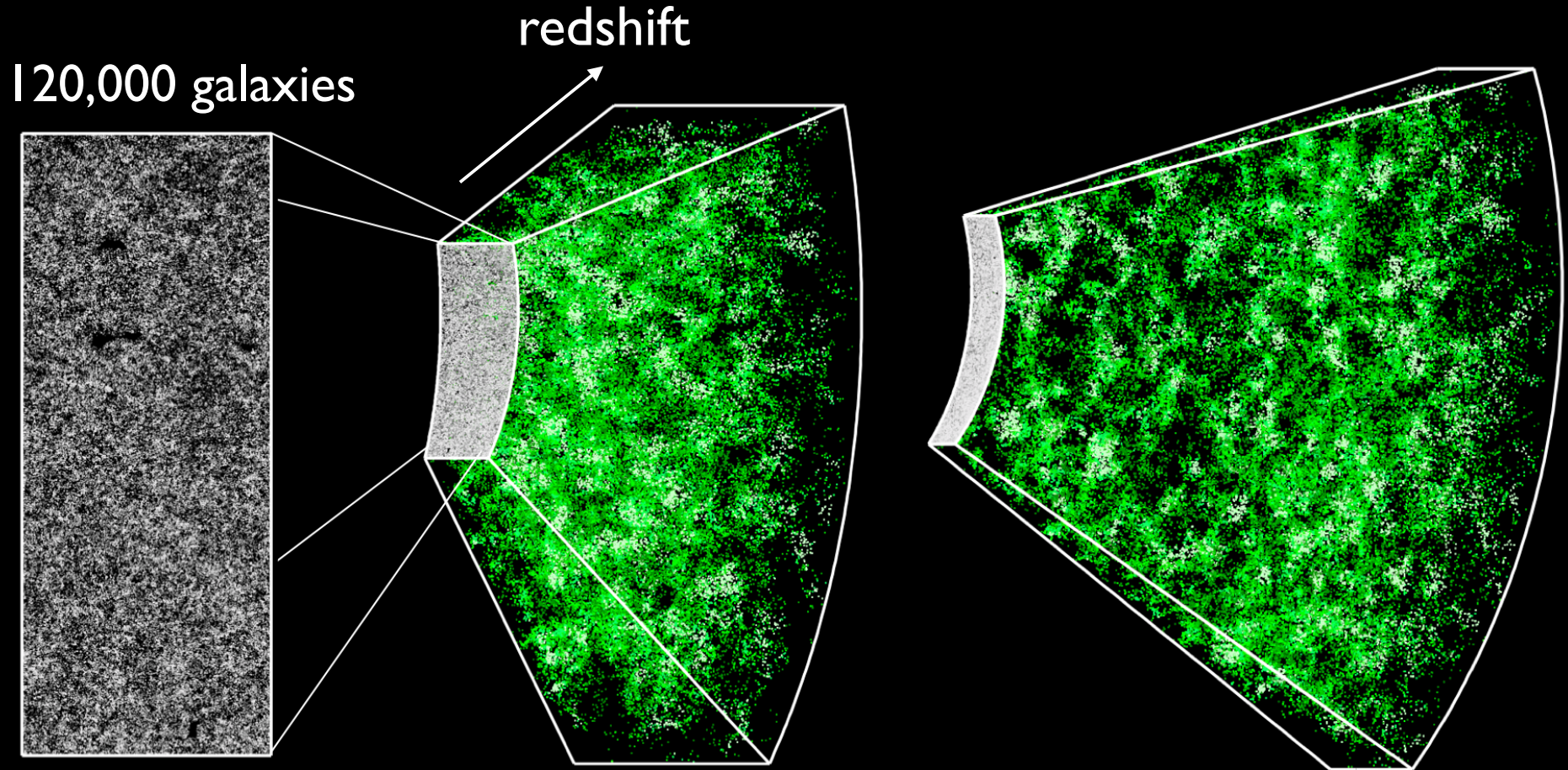


Yellow : SDSS-II main

Red : SDSS-II LRG

White : SDSS-III CMASS

# A section of 3D map



<http://www.sdss.org/press-releases/astronomers-map-a-record-breaking-1-2-million-galaxies-to-study-the-properties-of-dark-energy/>

# 3D Map of galaxies



## Sloan Digital Sky Survey

Miguel A Aragon (JHU), Mark Subbarao (Adler P.), Alex Szalay (JHU)

Sloan Digital Sky Survey III  
Baryon Oscillation Spectroscopic Survey

<https://www.sdss3.org/press/dr9.php>

# 3D Map of galaxies



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# Cosmology with galaxy 3D map

## Statistical properties

- Initial conditions for primordial fluctuations (cosmic inflation)
- Growth of structure
- Matter contents of the Universe

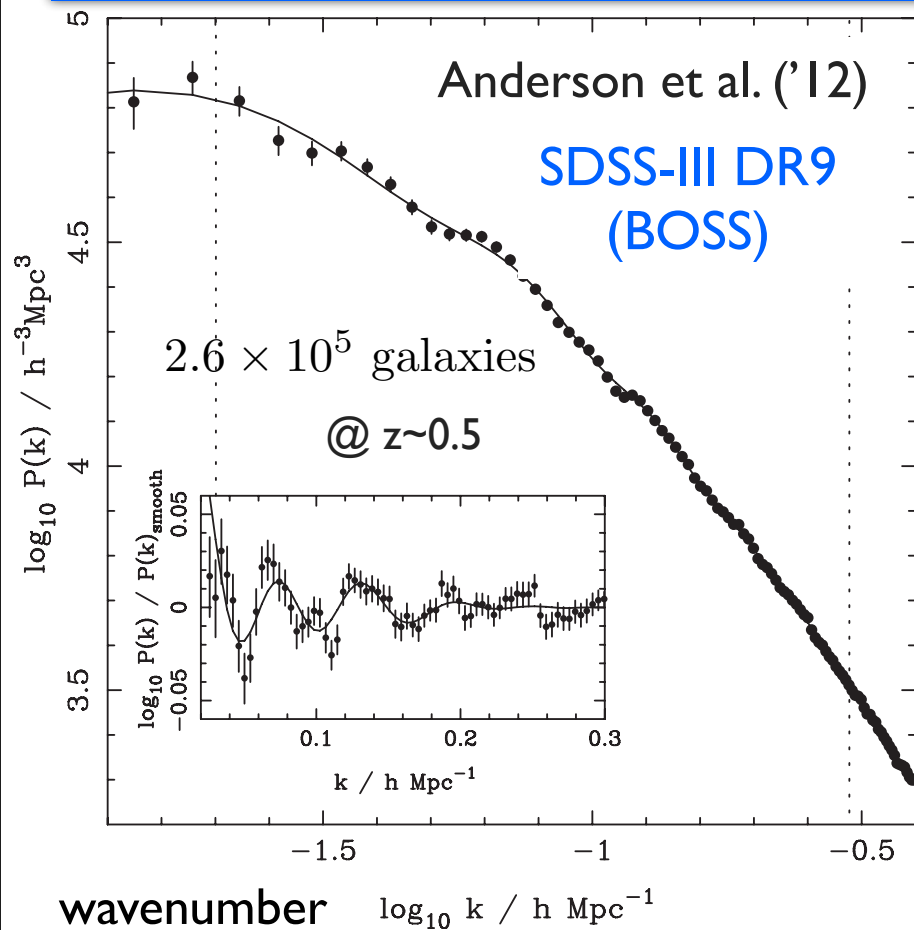
## Gauging the scales of large-scale structure



# Power spectrum of matter fluctuations

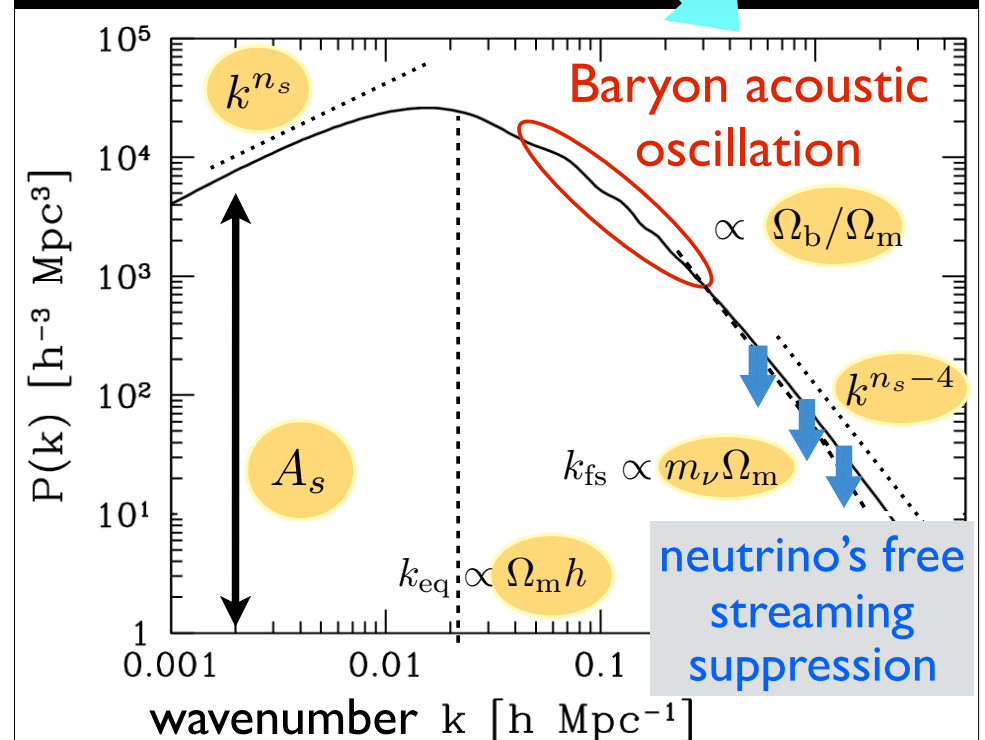
$$\delta(\vec{x}) \equiv \frac{\delta\rho_m(\vec{x})}{\bar{\rho}_m} = \frac{1}{\sqrt{V}} \sum_{\vec{k}} \delta(\vec{k}) e^{i\vec{k}\cdot\vec{x}}$$

$$P(k) = \frac{1}{N_k} \sum_{|\vec{k}|=k} |\delta(\vec{k})|^2$$



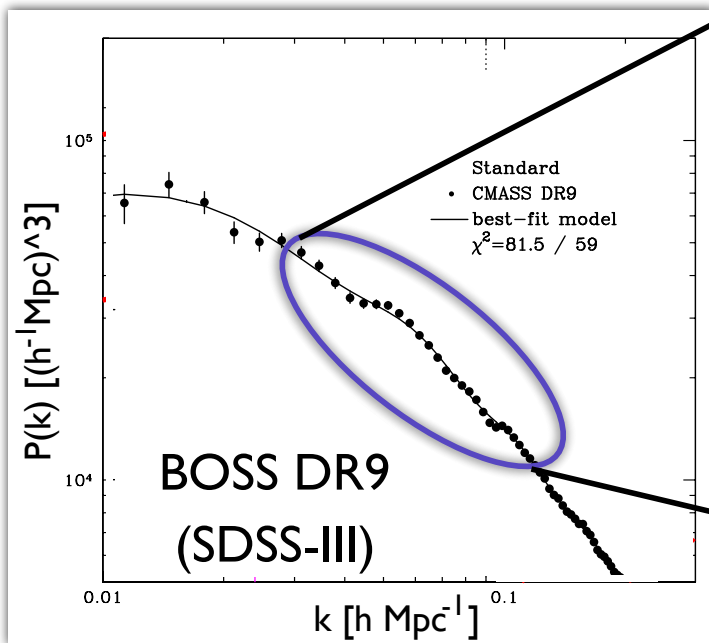
Observation

Linear theory

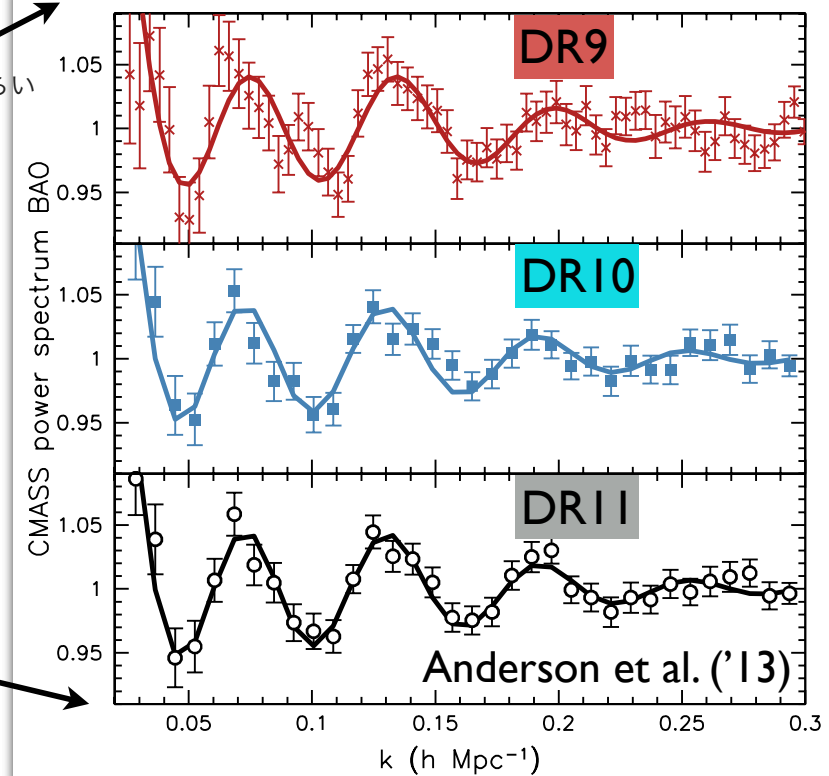


# Baryon acoustic oscillations (BAO)

- Characteristic scale of primeval baryon-photon fluid ( $\sim 150\text{Mpc}$ )  
( $\Leftrightarrow$  acoustic signal in CMB anisotropies)
- Can be used as standard ruler to measure cosmic expansion  
(theoretical prior)

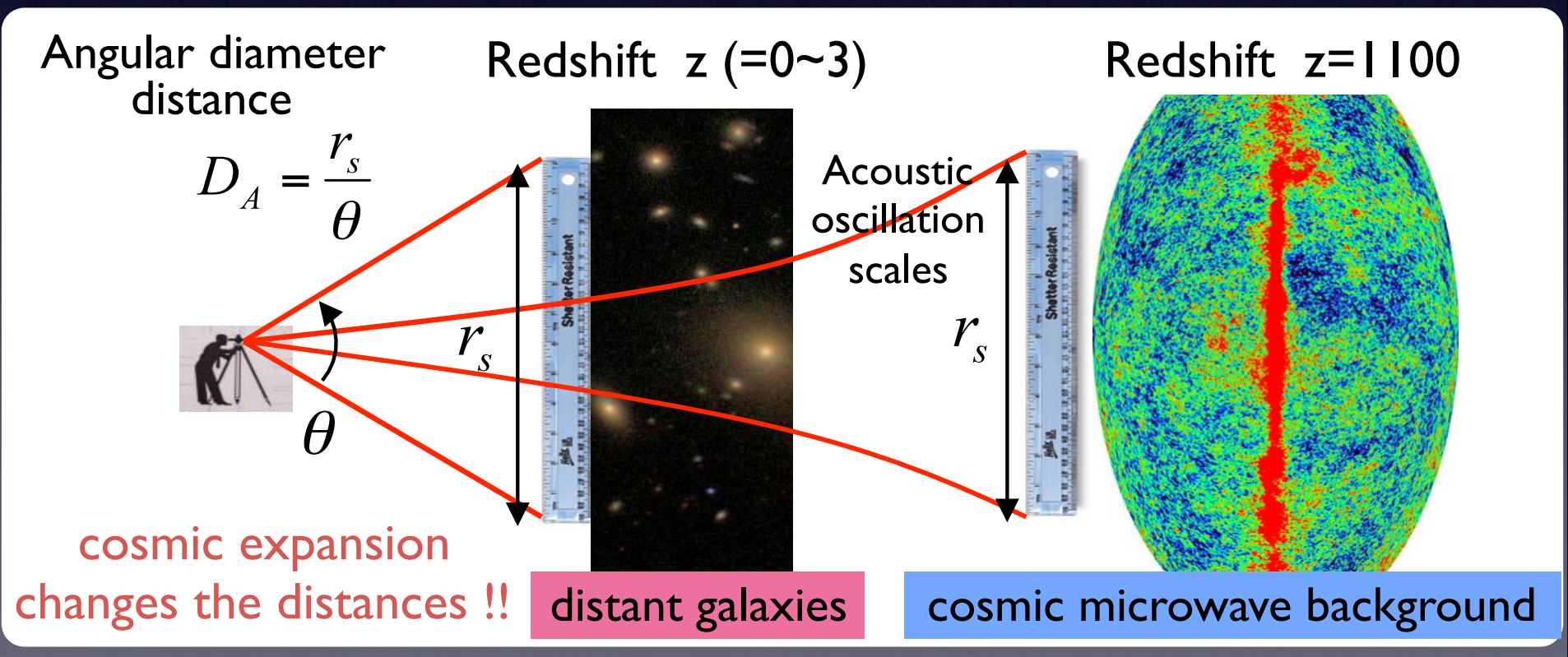


50倍くらい



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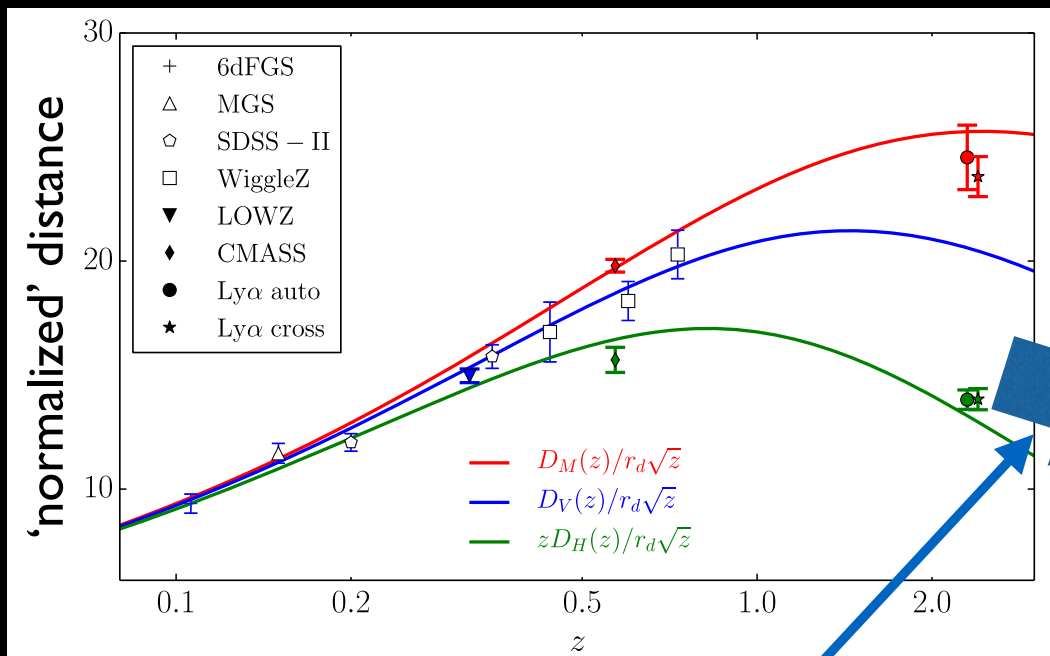




# Cosmological constraints from BAO

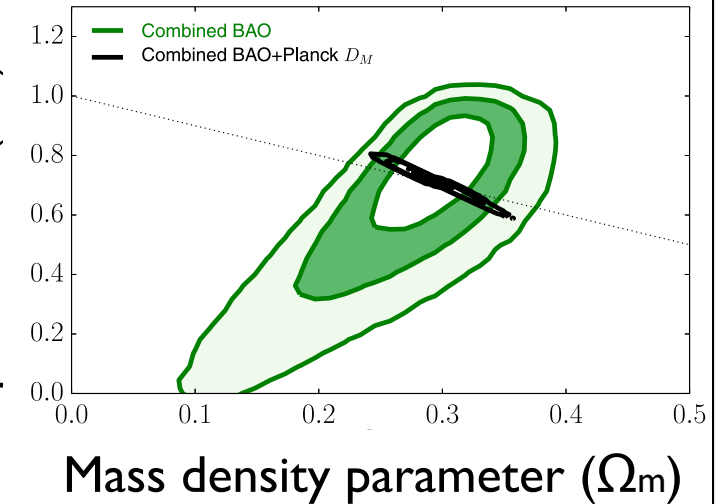
Aubourg et al. '15

Distance-redshift relation from  
BAO measurement

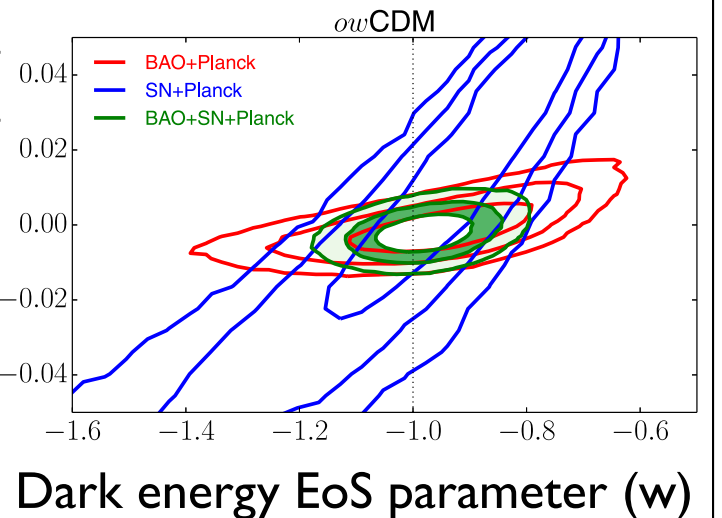


Combining CMB  
measurement by Planck

Dark energy density  
parameter ( $\Omega_\Lambda$ )



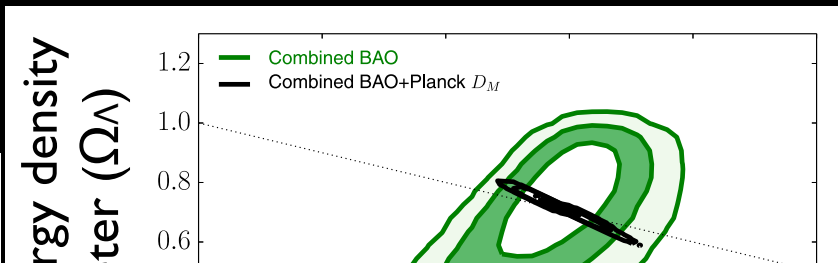
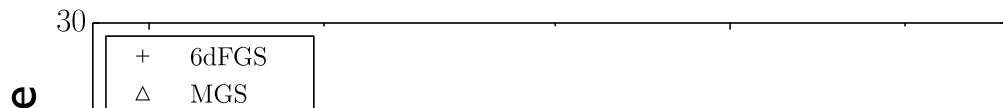
Curvature parameter  
of the Universe ( $\Omega_K$ )



# Cosmological constraints from BAO

Aubourg et al. '15

Distance-redshift relation from  
BAO measurement



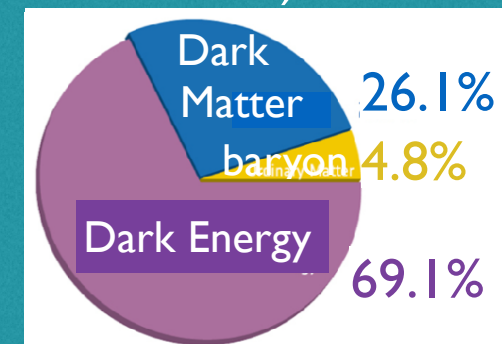
$\Lambda$ CDM model (standard cosmological model)

flat universe filled with mysterious energy/matter components :

- dark matter → structure formation
- dark energy → late-time cosmic acceleration

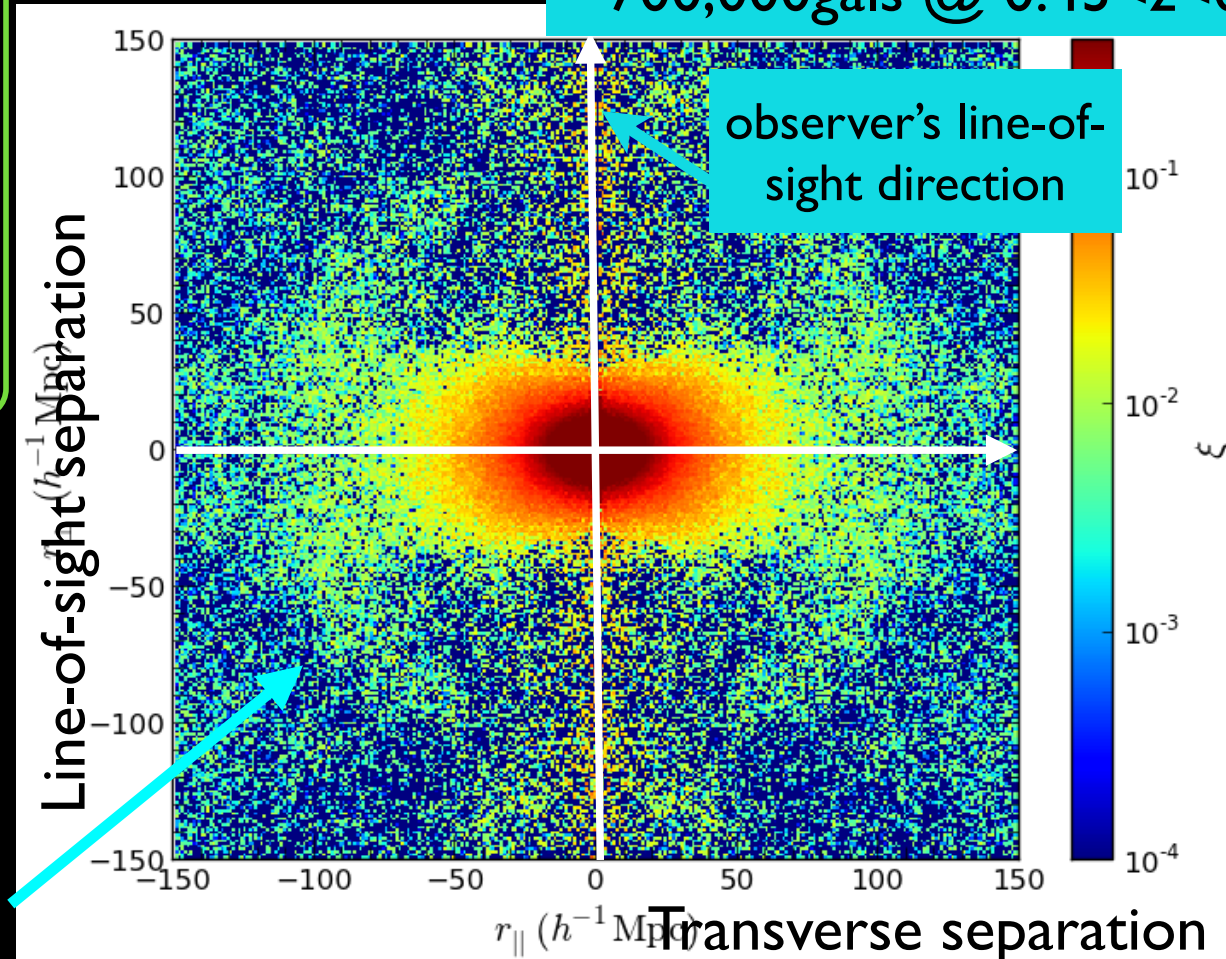
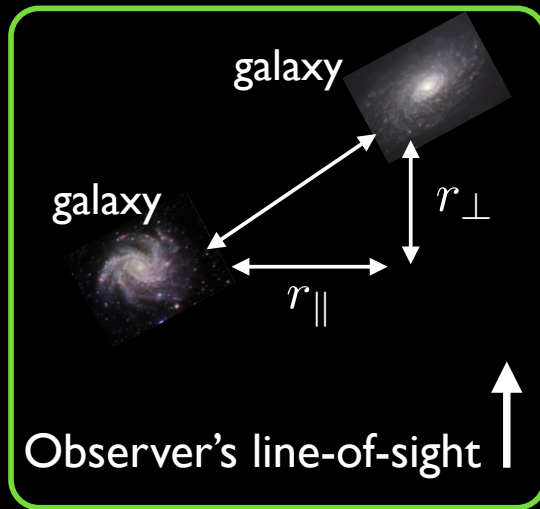
(In  $\Lambda$ CDM model, dark energy=cosmological constant,  $\Lambda$ )

Origin & nature of these components are largely unknown. Need further observations !!



# Two-point correlation function

BOSS DR11, CMASS samples  
700,000gals @  $0.43 < z < 0.7$



**Baryon acoustic oscillation (ridge)**

# RSD as a probe of gravity

Kaiser  
formula

(Kaiser '87)

$$\delta^{(S)}(\mathbf{k}) = (1 + f \mu_k^2) \delta(\mathbf{k}) ;$$

$$f \equiv \frac{d \ln D_+}{d \ln a}$$

Linear growth  
factor

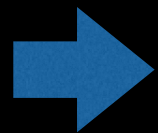
scale factor

*This parameter tells us*

how the nature of gravity affects the growth of structure

*Importantly,*

This Kaiser formula holds irrespective of gravity theory



probe of gravity (general relativity) on cosmological scales

- Untested hypothesis in  $\Lambda$ CDM model
- Hint for cosmic acceleration

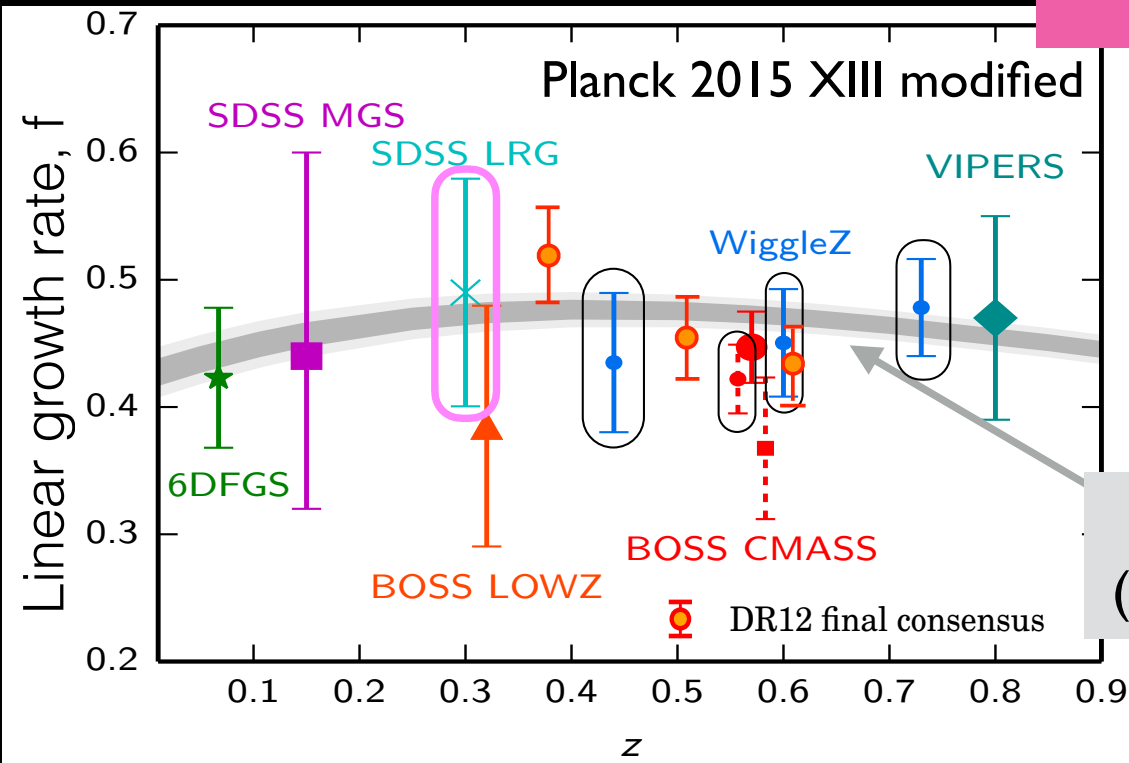
e.g., Linder ('08); Guzzo et al. ('08); Yamamoto et al. ('08); Percival & White ('09)

# Consistency test of GR

*In practice*

Testing gravity needs a nonlinear RSD model assuming underlying theory of gravity

A blind fit of growth rate based on GR-based template



Based on perturbation theory template

Oka, Saito, Nishimichi, AT & Yamamoto ('14)

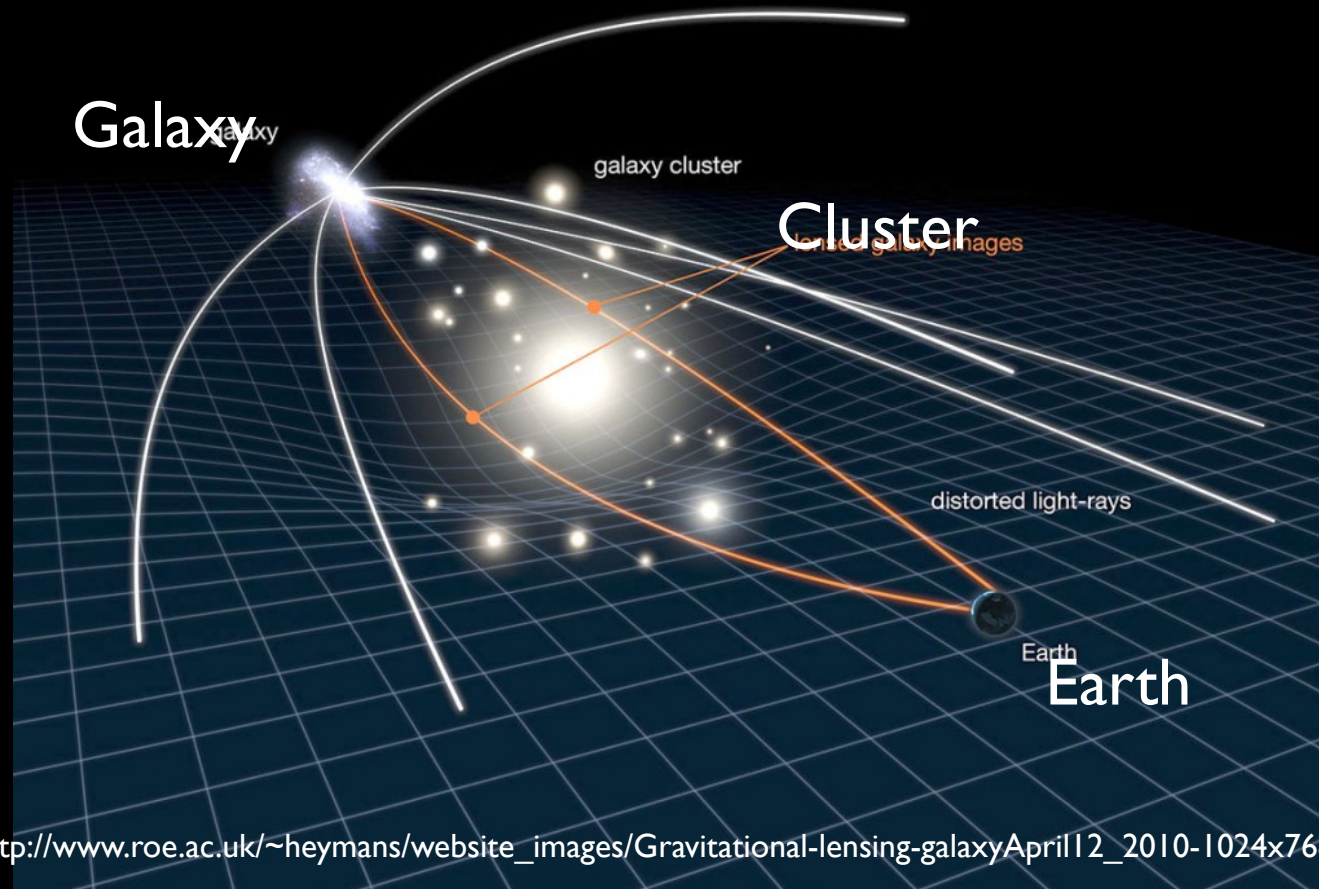
Planck  $\Lambda$ CDM (General relativity)

No strong evidence of deviation from GR

(See also Beutler, Seo, Saito et al. '16 for latest BOSS DR12)

# Gravitational lensing effect

Light bending phenomena caused by gravity induced by massive objects such as galaxy and star

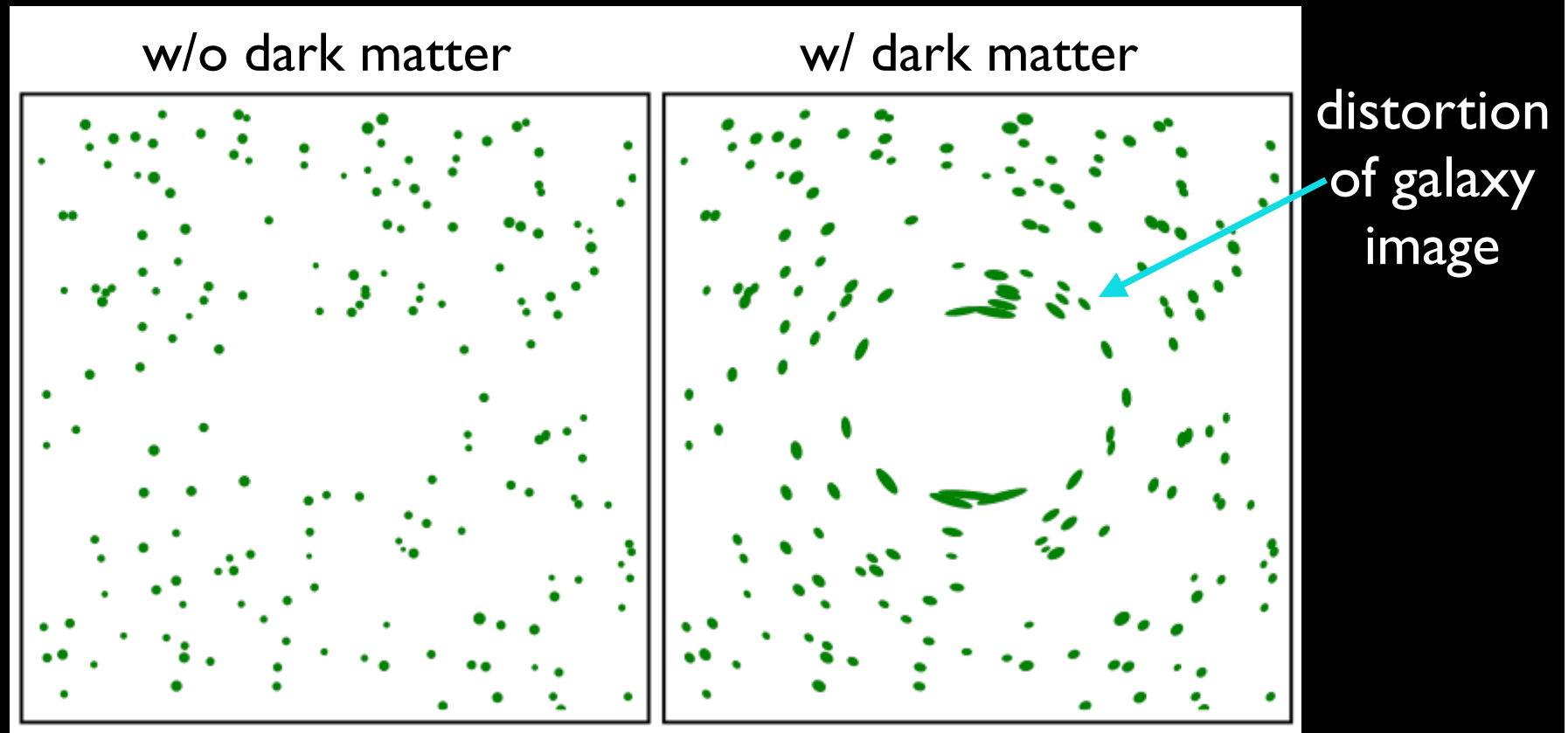


[http://www.roe.ac.uk/~heyman/website\\_images/Gravitational-lensing-galaxyApril12\\_2010-1024x768.jpg](http://www.roe.ac.uk/~heyman/website_images/Gravitational-lensing-galaxyApril12_2010-1024x768.jpg)

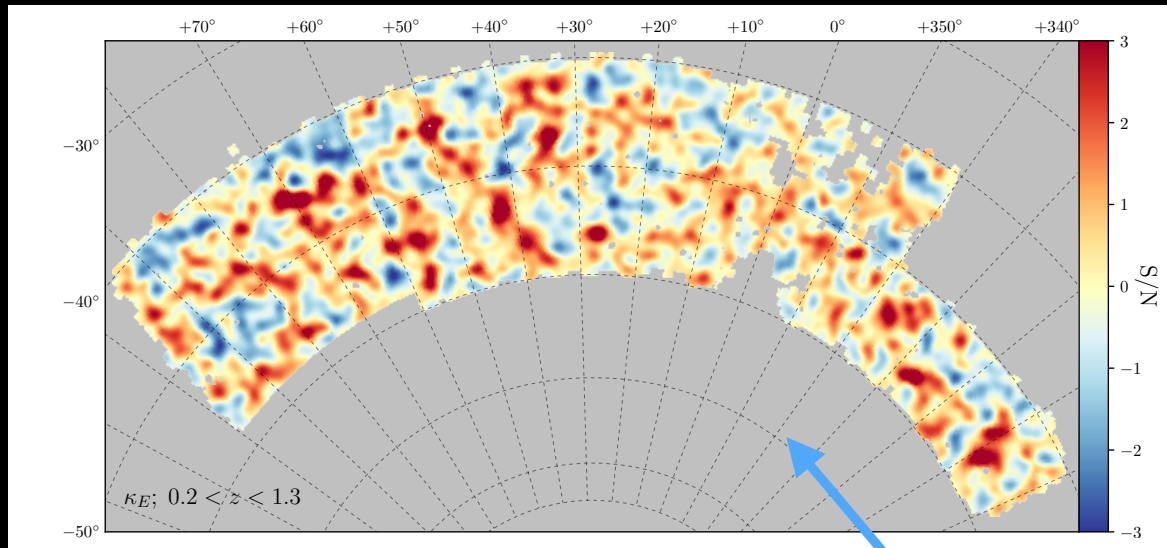
Observer will see distorted or multiple images of distant objects

# Mapping dark matter with weak lensing effect

Gravitational lensing effect can be powerful to probe invisible mass distribution (dark matter)

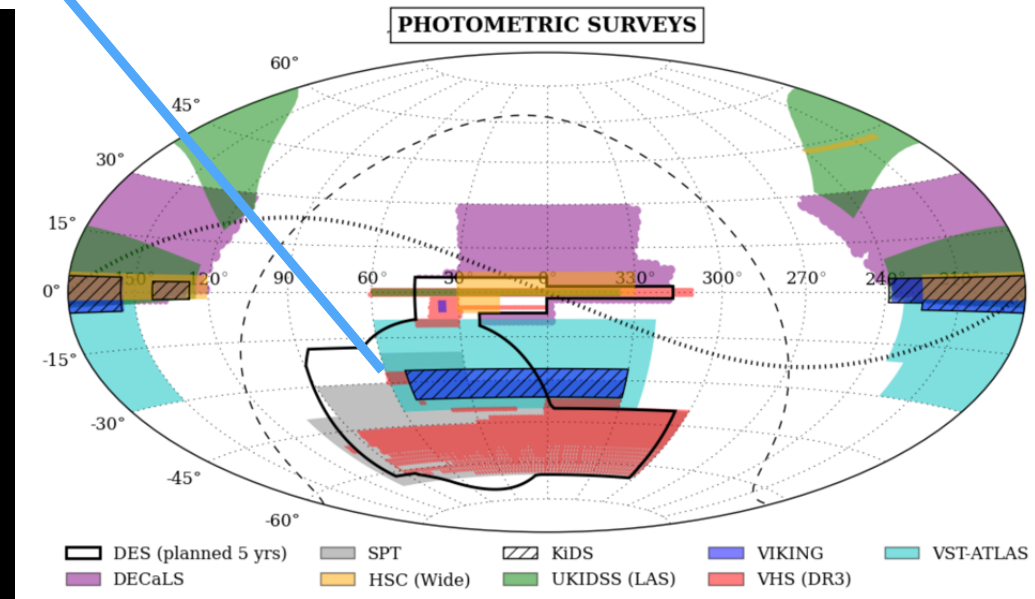


# Projected mass map

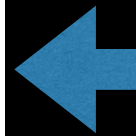
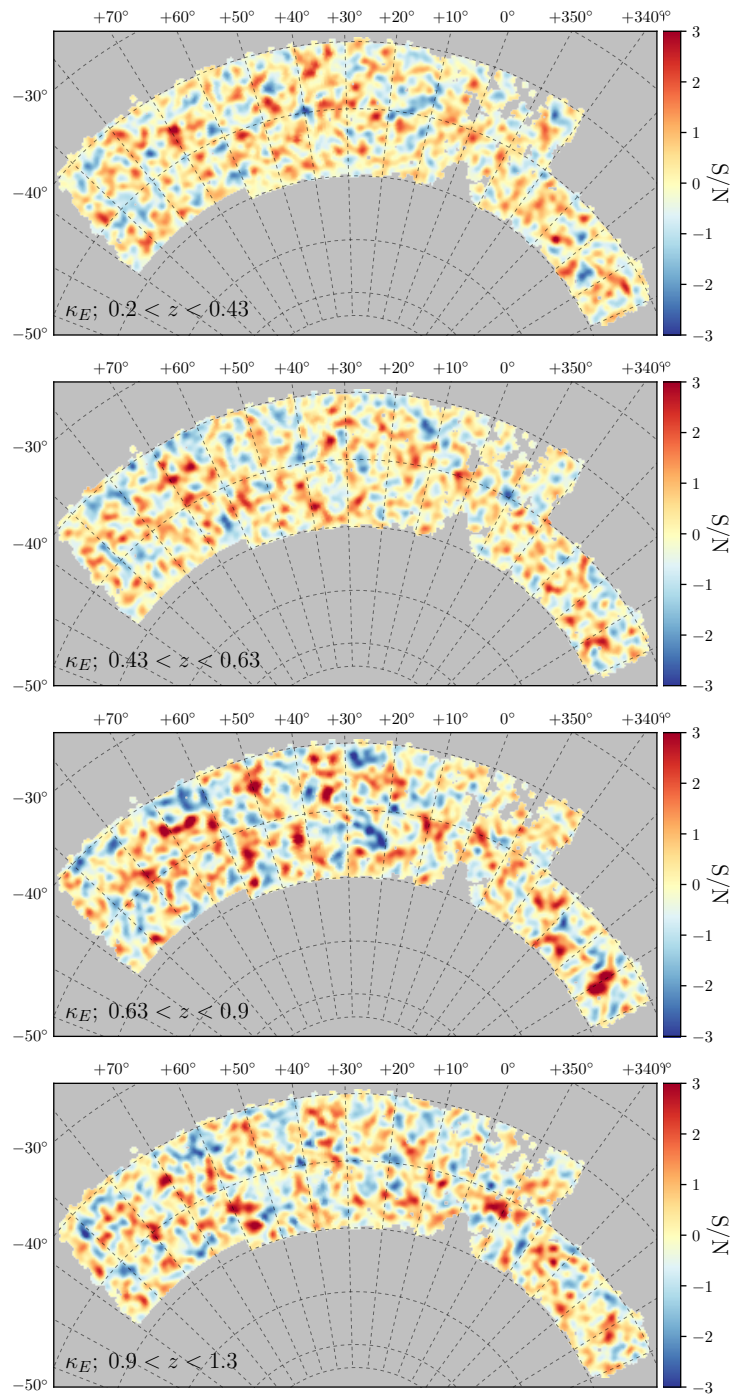


Dark Energy Survey  
1st year result  
 $\sim 1,500 \text{ deg}^2$

(Chang et al. '17)





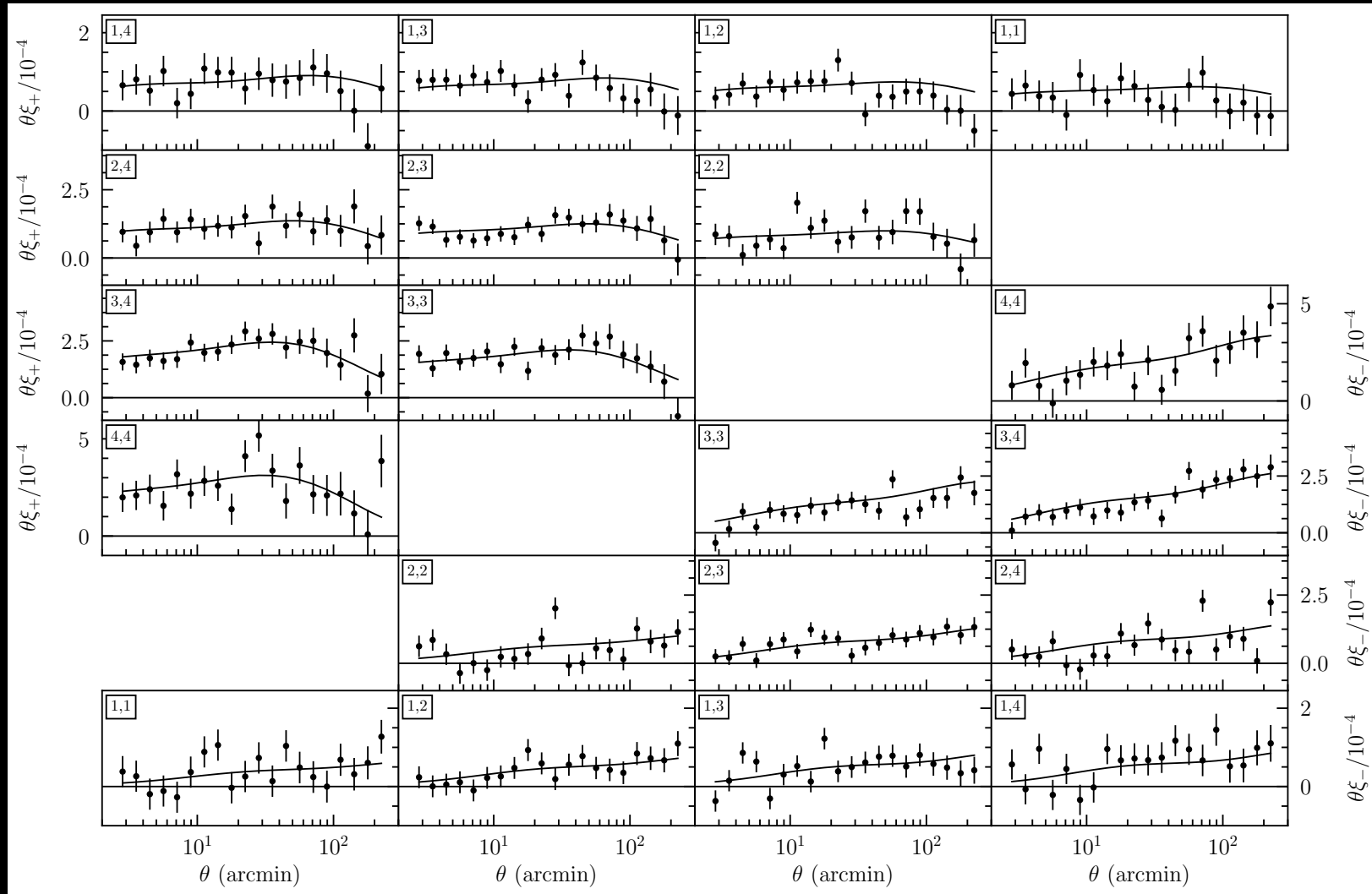


## Tomographic maps

using photo-z information of source galaxies, projected mass maps are obtained from several redshift bins

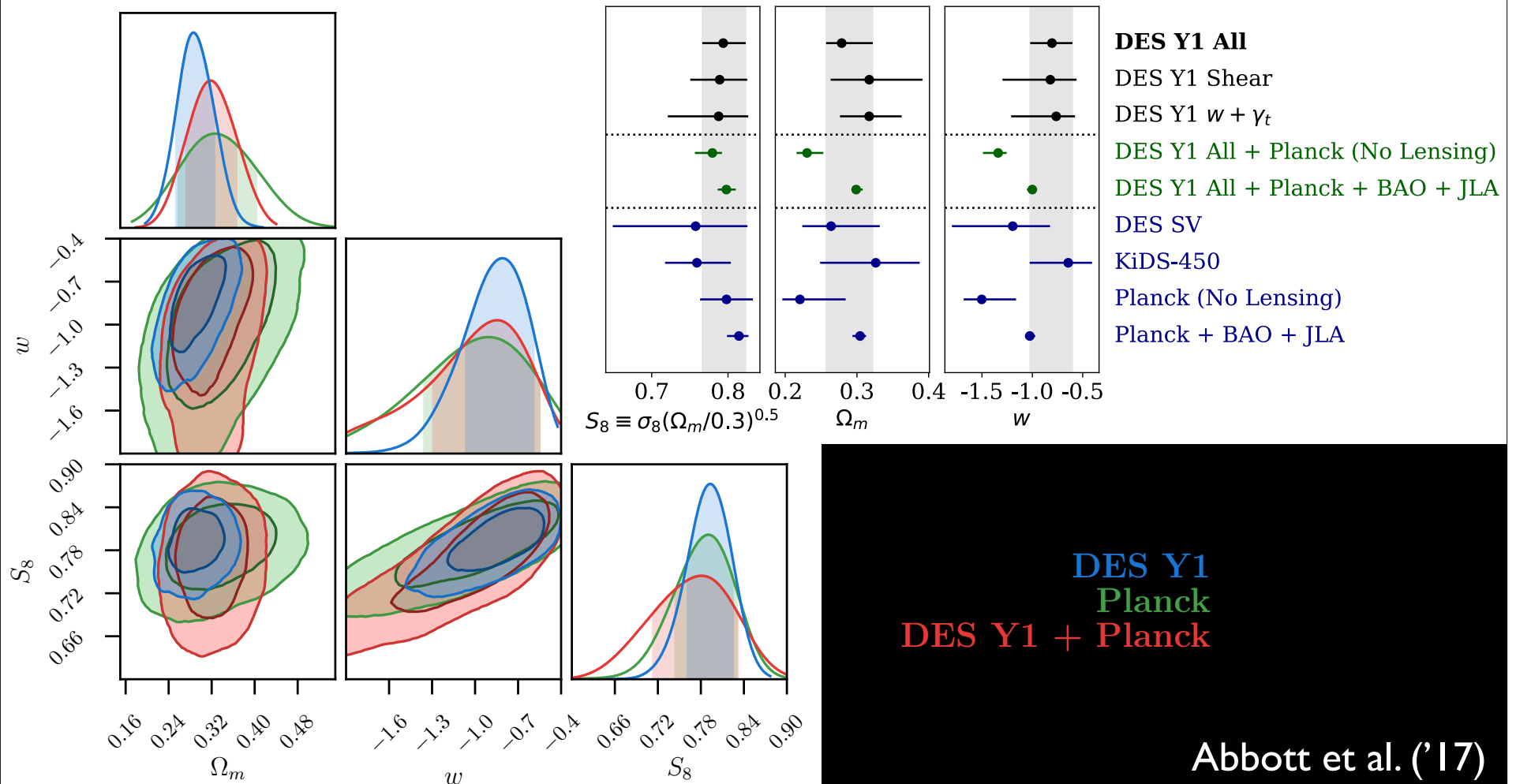
(Chang et al. '17)

# Shear correlation function



# Cosmological results

DES Y1r (cosmic shear + galaxy clustering)



DES Y1  
Planck  
DES Y1 + Planck

Abbott et al. ('17)

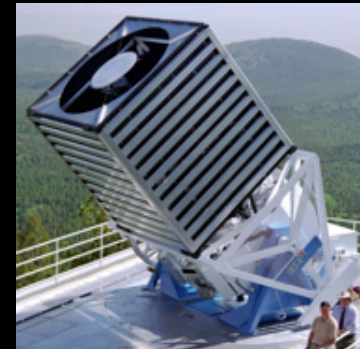
# Upcoming/on-going projects

Multi-purpose ground- & space-based experiments

DES (2013~)

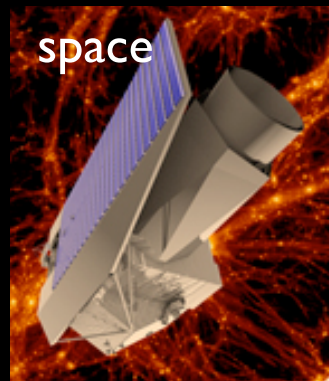


HETDEX (2016+)



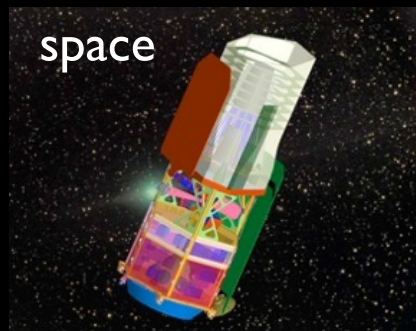
DESI  
(2018+)

WFIRST  
(2024++)



eBOSS (2014~)

Euclid (2020)



LSST  
(2022++)

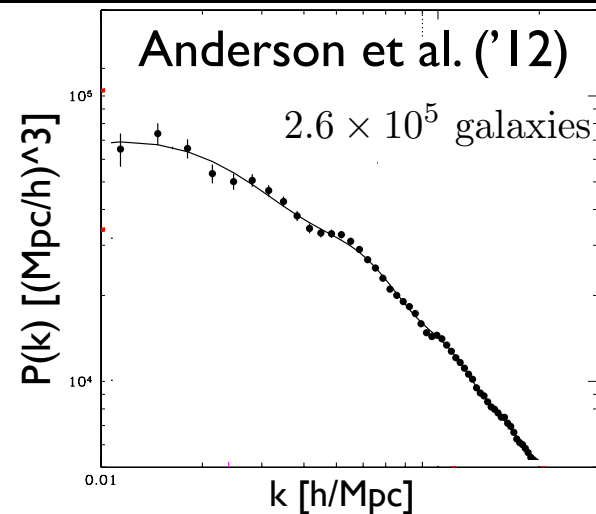
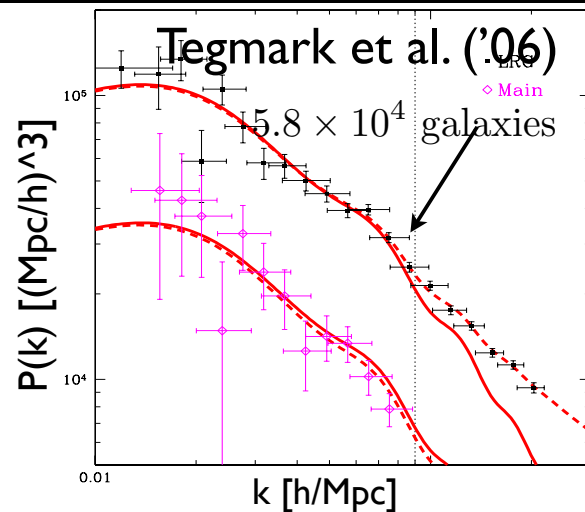
SuMIRe  
(2014~)



subaru

# LLS as precision cosmological tools

Large data set will reveal statistical properties of LSS at an unprecedented precision level ( $\rightarrow$  **precision cosmology**)



$10^7 \sim 10^9$  galaxies  
 $\sim 1\%$  precision

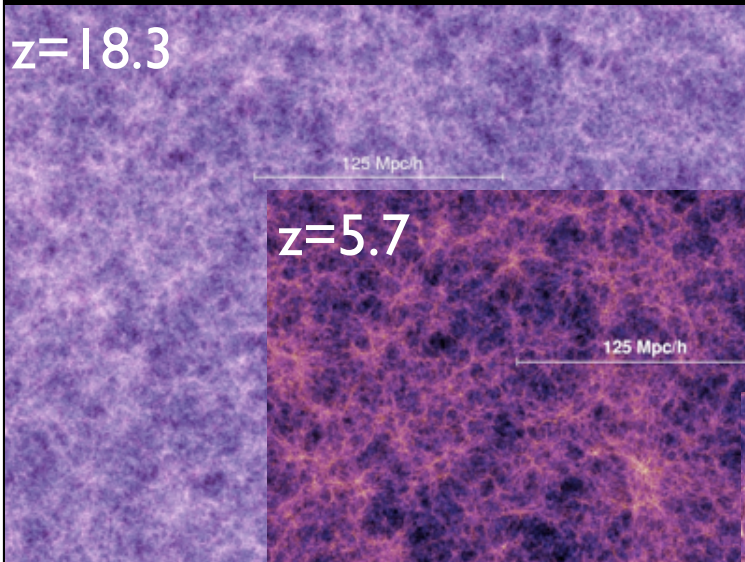
*New opportunity & scientific synergy :*

- Clarifying nature of dark energy (cosmic acceleration)
- Testing general relativity on cosmological scales
- Weighing total mass of neutrinos

Accurate theoretical description for LSS needs to be developed

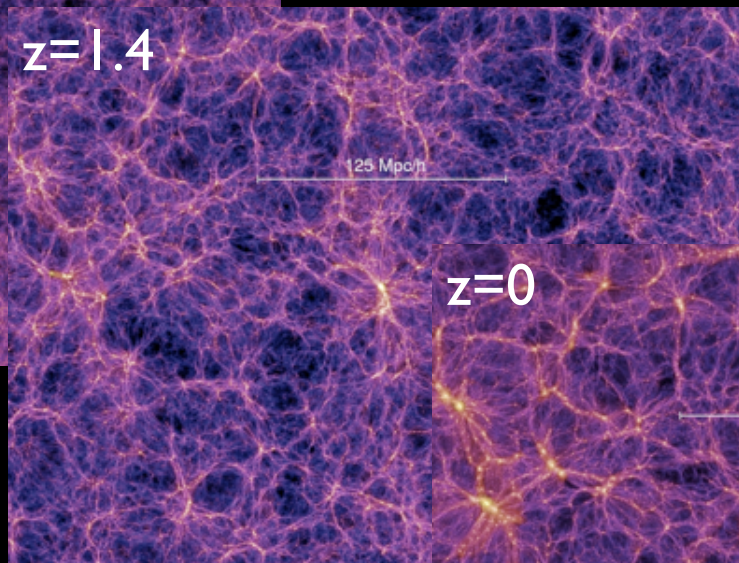
# Cosmological N-body simulation

$z=18.3$

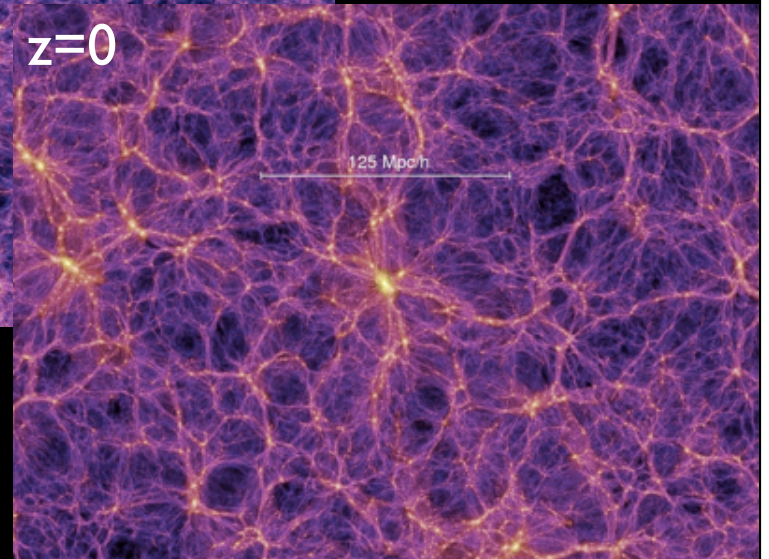


$z=5.7$

$z=1.4$



$z=0$



Self-gravitating many-body system  
in an expanding universe

$N \rightarrow \infty$

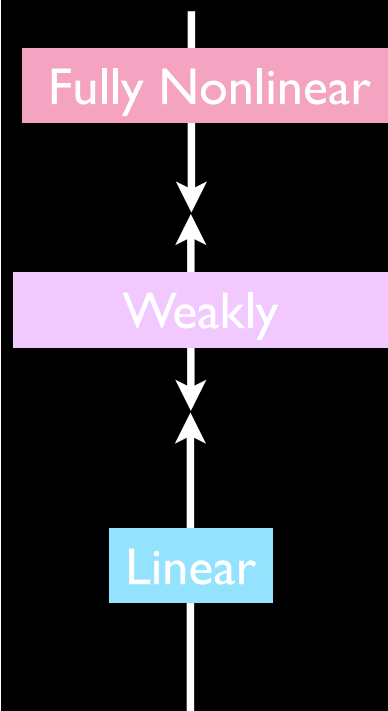
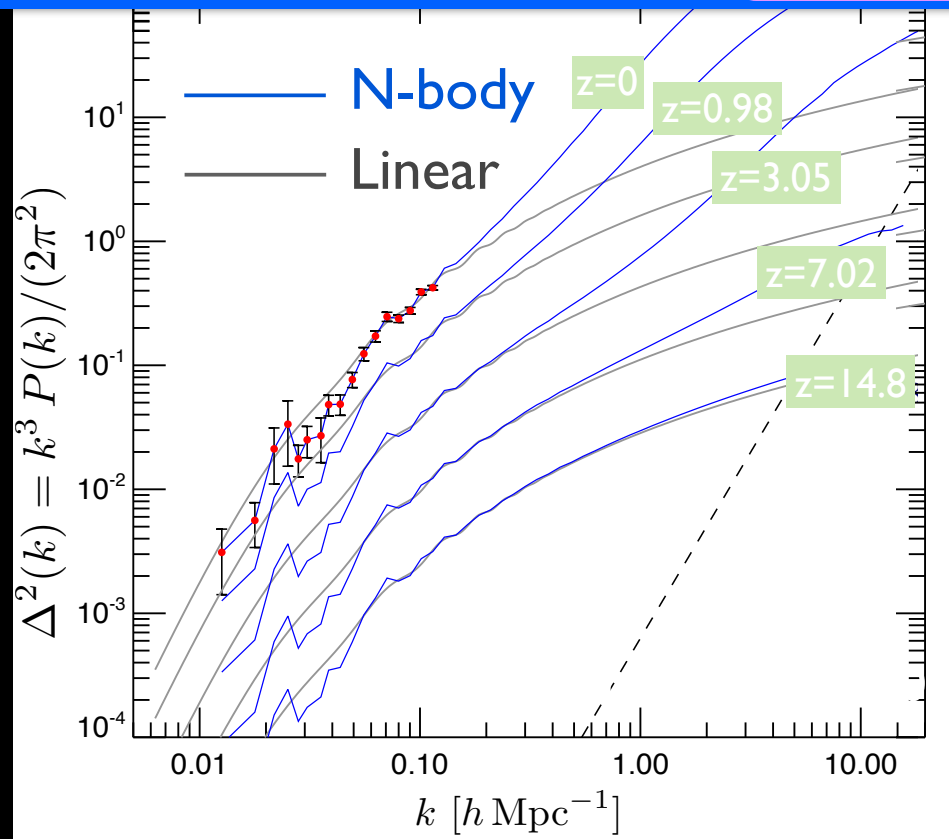
$$\frac{\vec{p}_i}{dt} = -\frac{Gm^2}{a} \sum_{j \neq i}^N \frac{\vec{x}_i - \vec{x}_j}{|\vec{x}_i - \vec{x}_j|^3} \quad \vec{p}_i = ma^2 \frac{d\vec{x}_i}{dt}$$

$(i = 1, 2, \dots, N)$

Formation of halos and  
filamentary structure

# Nonlinear power spectrum

$$\delta(\vec{x}) \equiv \frac{\delta\rho_m(\vec{x})}{\bar{\rho}_m} = \frac{1}{\sqrt{V}} \sum_{\vec{k}} \delta(\vec{k}) e^{i\vec{k}\cdot\vec{x}} \quad \rightarrow \quad P(k) = \frac{1}{N_k} \sum_{|\vec{k}|=k} |\delta(\vec{k})|^2$$



To what extent we can quantitatively understand statistical properties of large-scale structure?

# Goal of this lecture

Understanding of large-scale structure (LSS)  
as cosmology probe

- Theoretical basis of formation & evolution of LSS
  - Structure formation Standard model ( $\Lambda$ CDM)
  - Cosmological information imprinted in LSS
- Theoretical tools to confront with precision observations of LSS  
(mainly focusing on galaxy surveys)
  - Perturbation theory of LSS



# Plan

- Summary of background cosmology
- Linear theory of structure formation
- Observational effects:  
    Redshift-space & geometric distortions
- Analytic approaches to nonlinear structure formation
- Selected topics on statistics and dynamics of large-scale structure

# Note and supplements

Lecture note and supplemental materials (PDF files) are found in:

<http://www2.yukawa.kyoto-u.ac.jp/~atsushi.taruya/lecture.html>

## 宇宙論特論

日時: 2017年後期 水曜日 14:45--16:10

場所: 基礎物理学研究所 研究棟 K202

- 講義ノート: [PDF](#)
- 資料
  - 概観: [PDF](#)