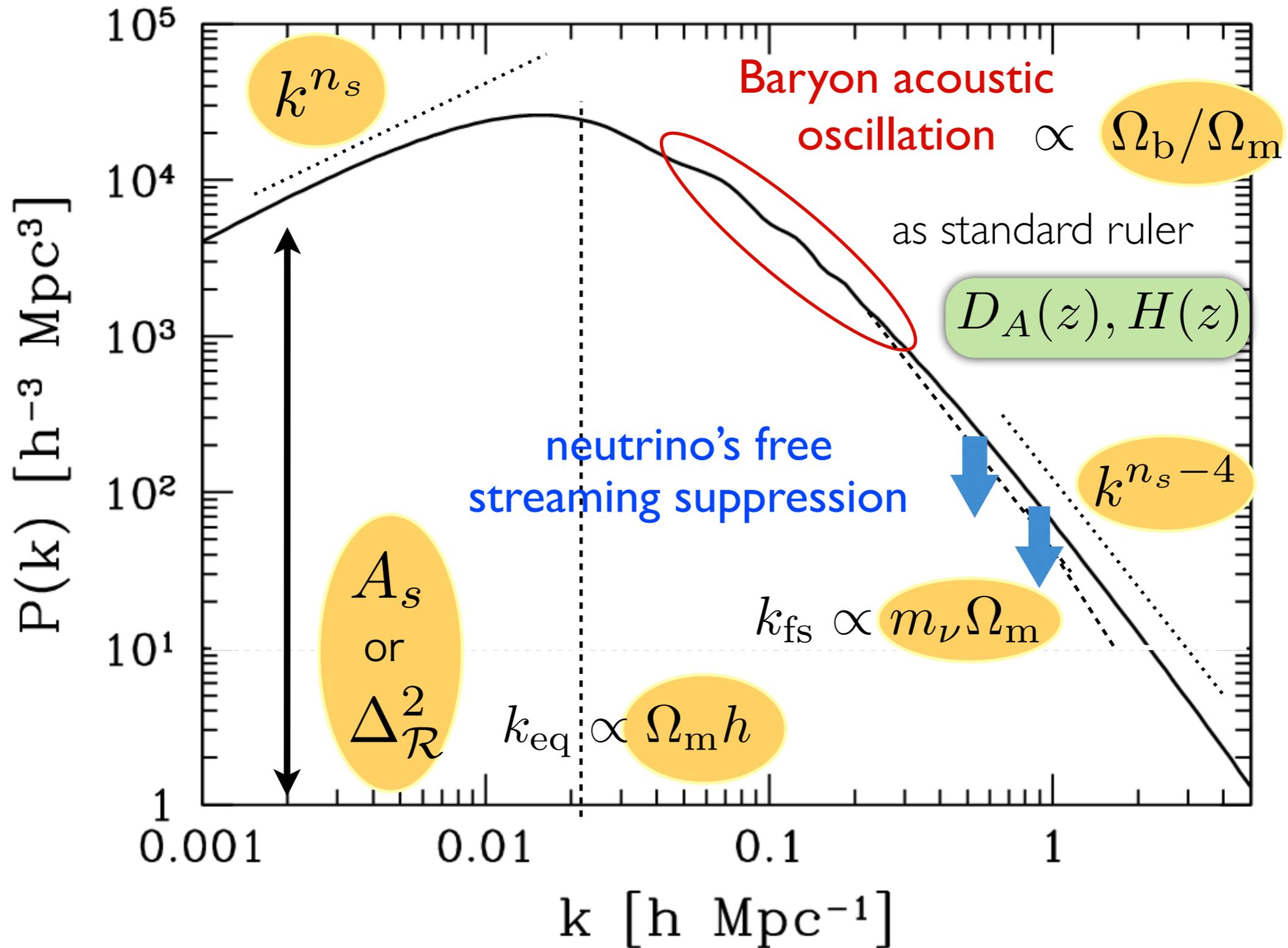


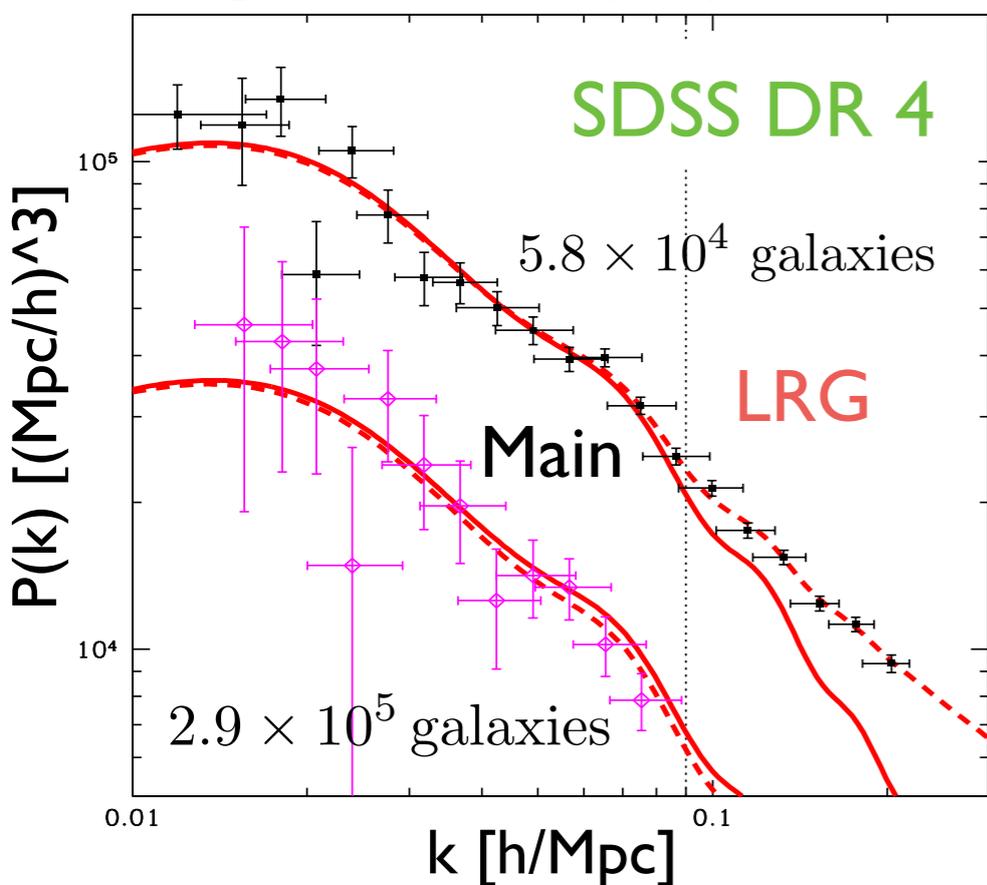
# Linear theory of structure formation

# (Linear) matter power spectrum

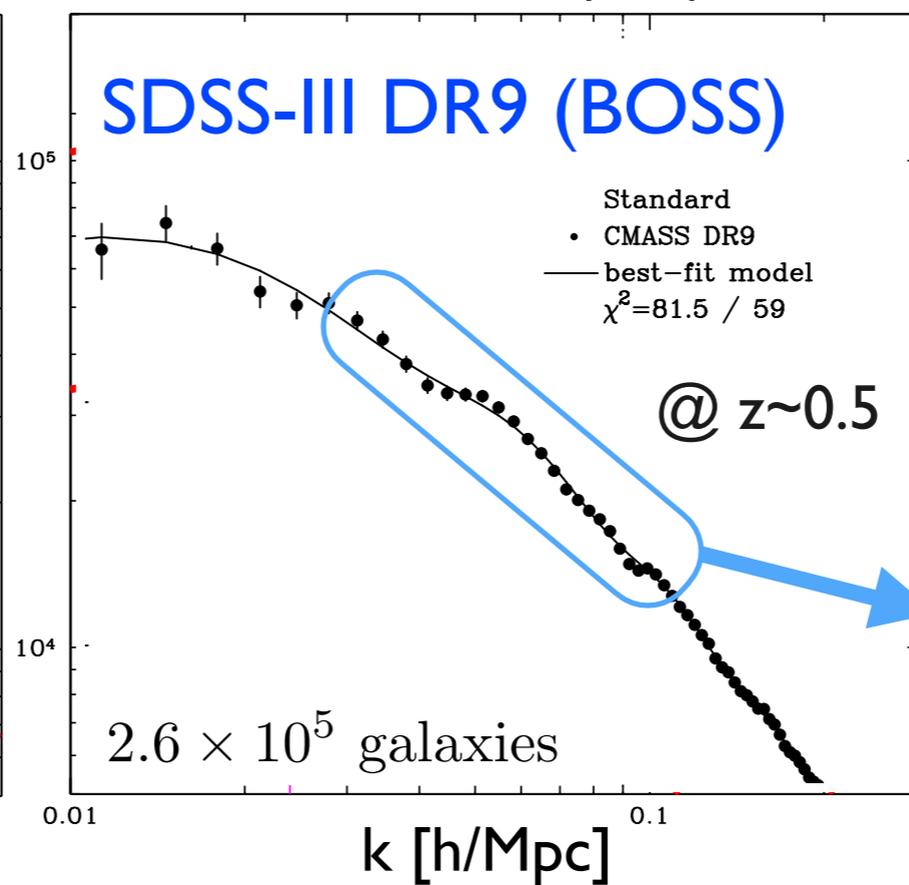


# Galaxy power spectrum

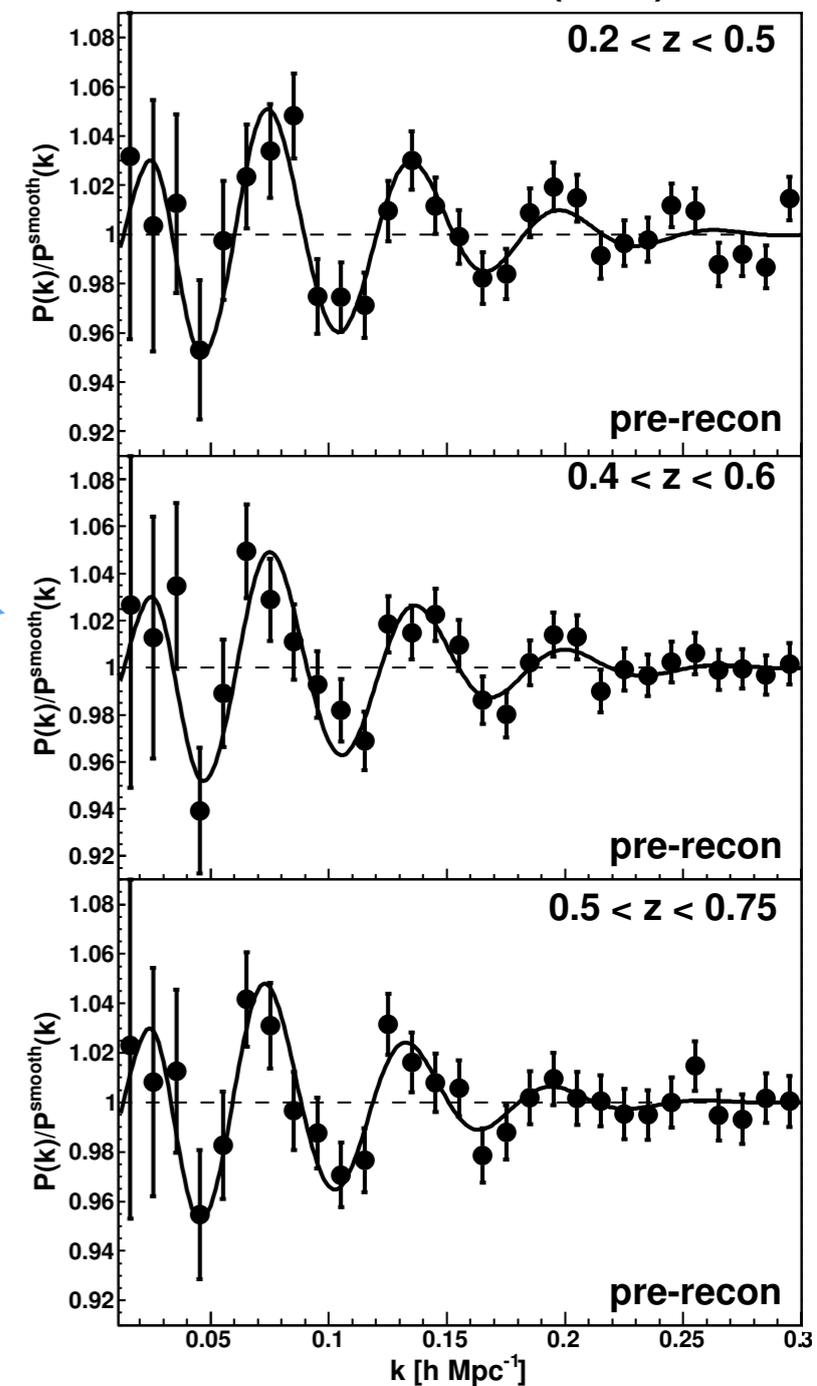
Tegmark et al. ('06)



Anderson et al. ('12)



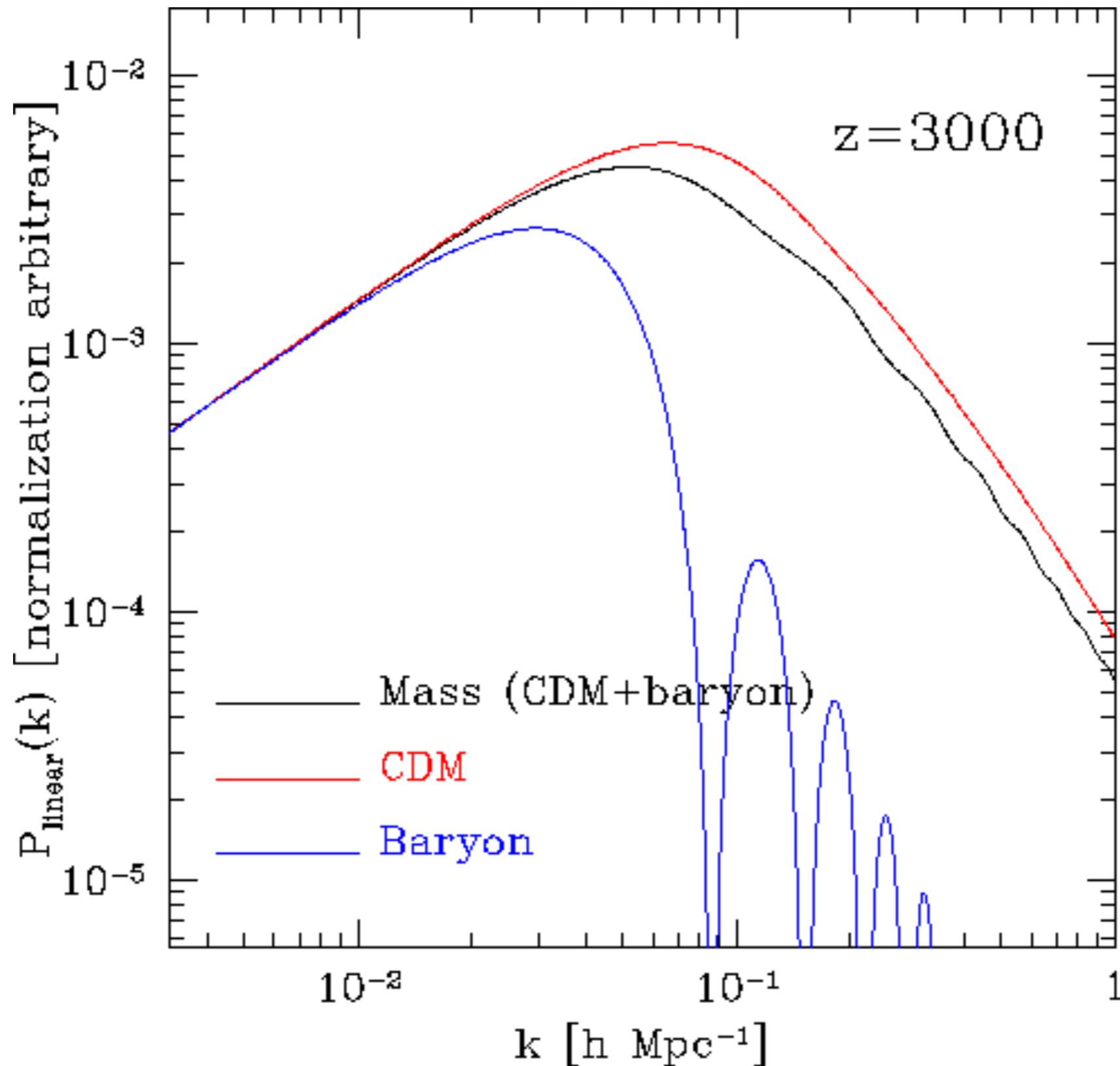
Beutler et al. ('16)



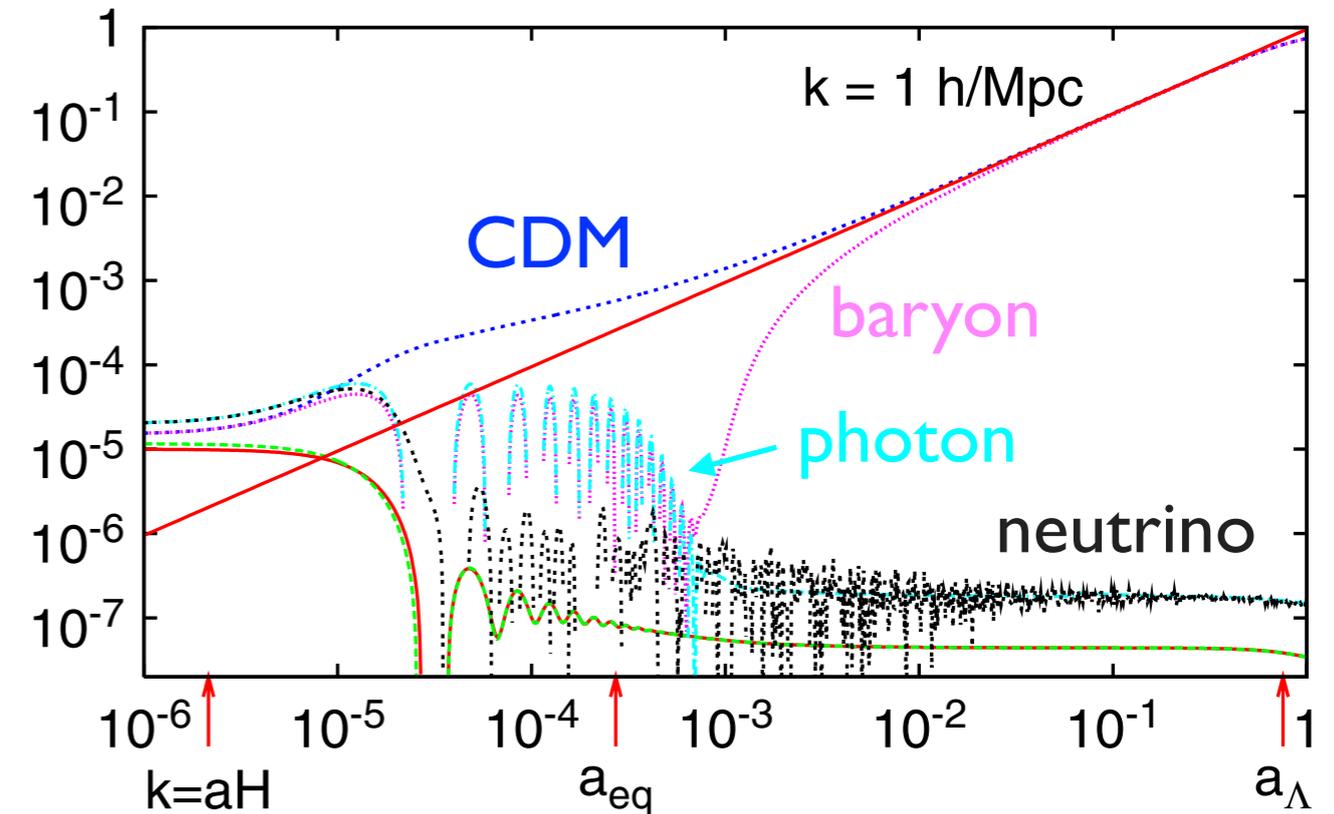
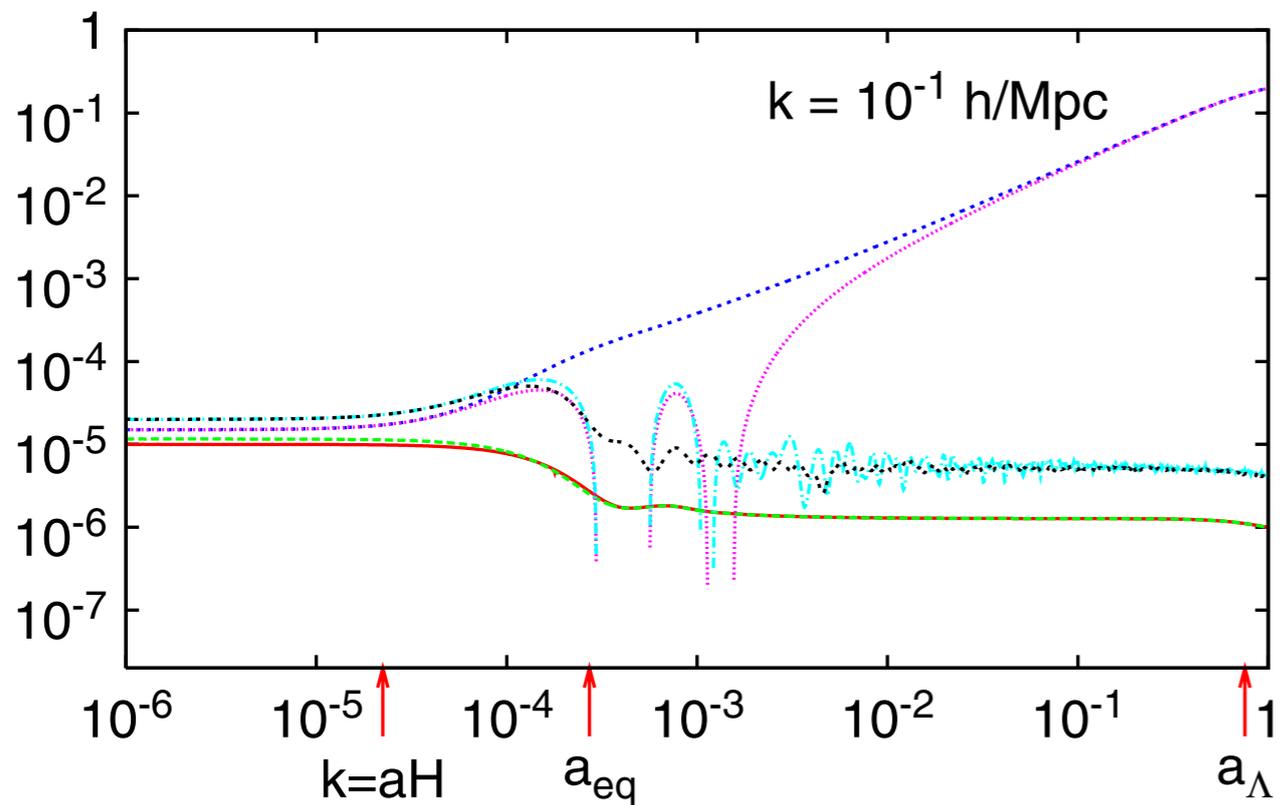
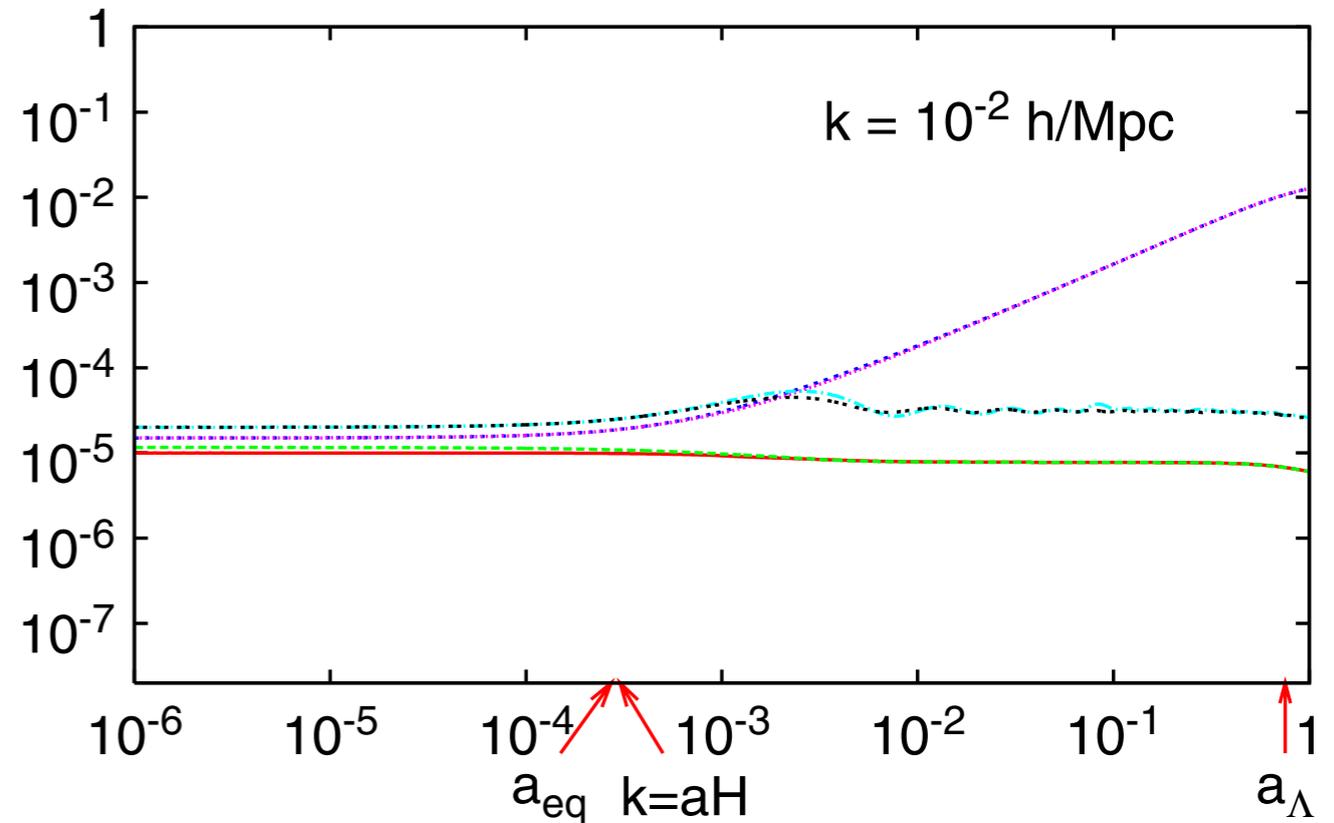
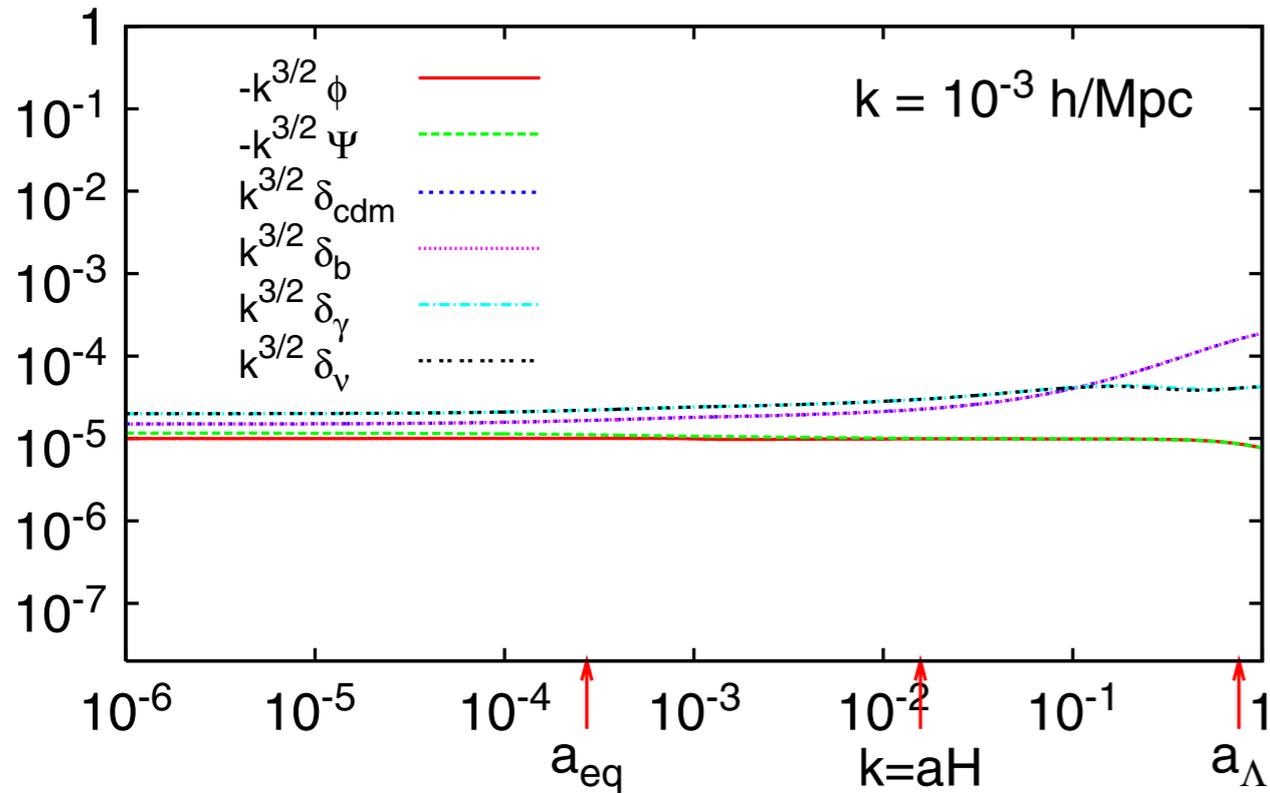
SDSS-III DR12 (BOSS)

$1.2 \times 10^6$  galaxies

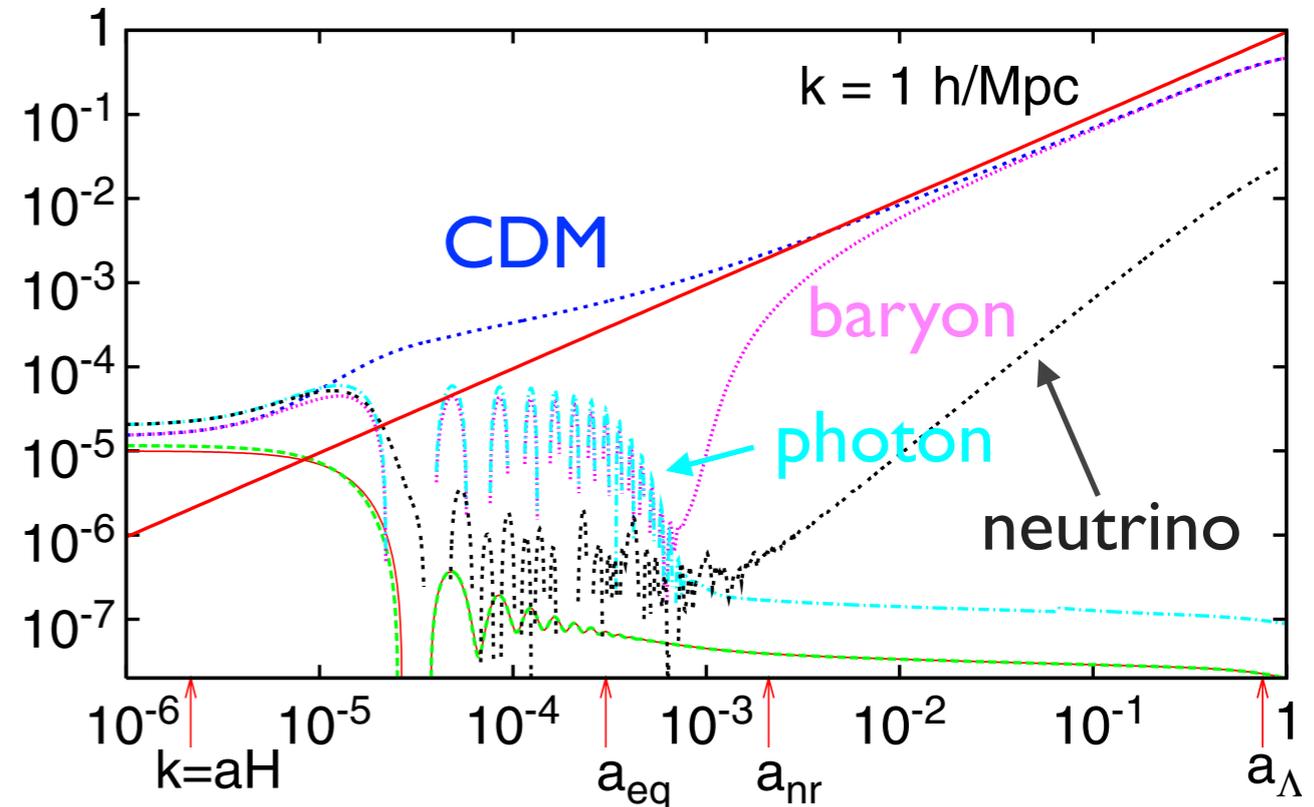
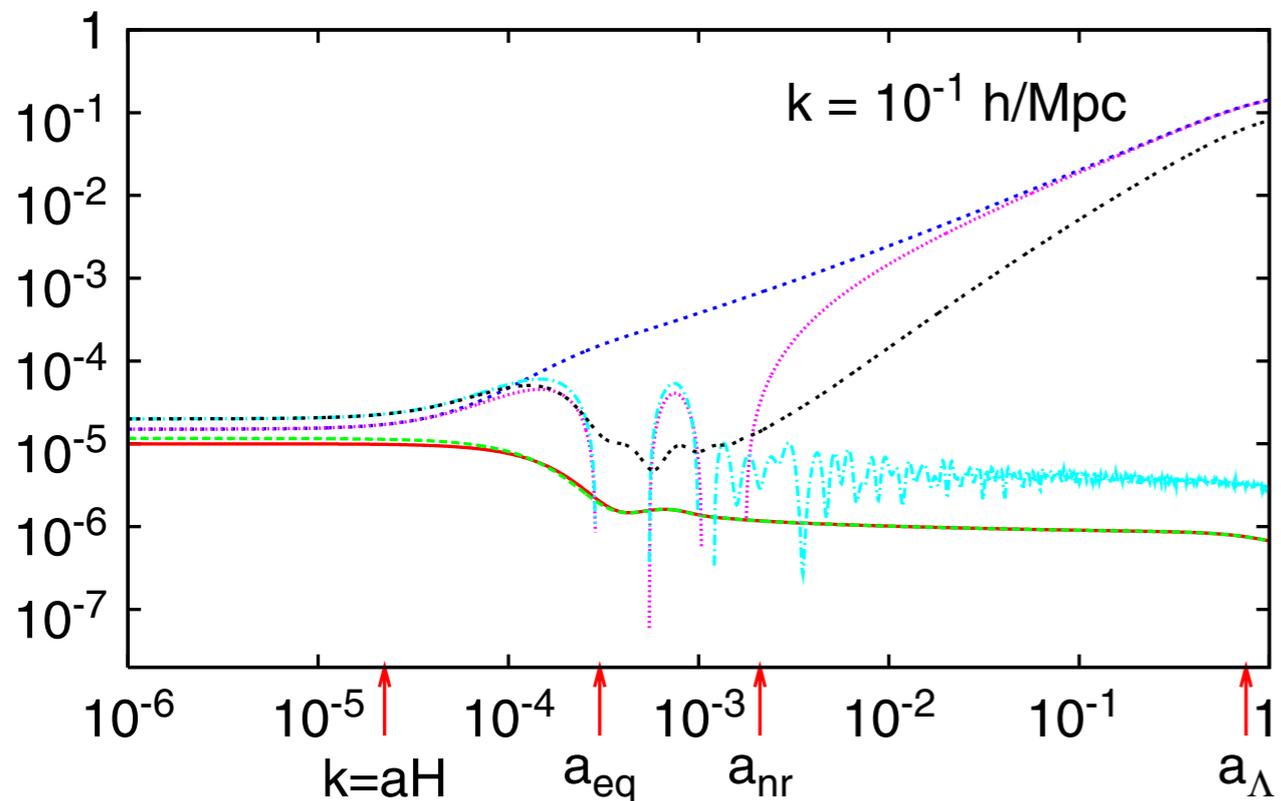
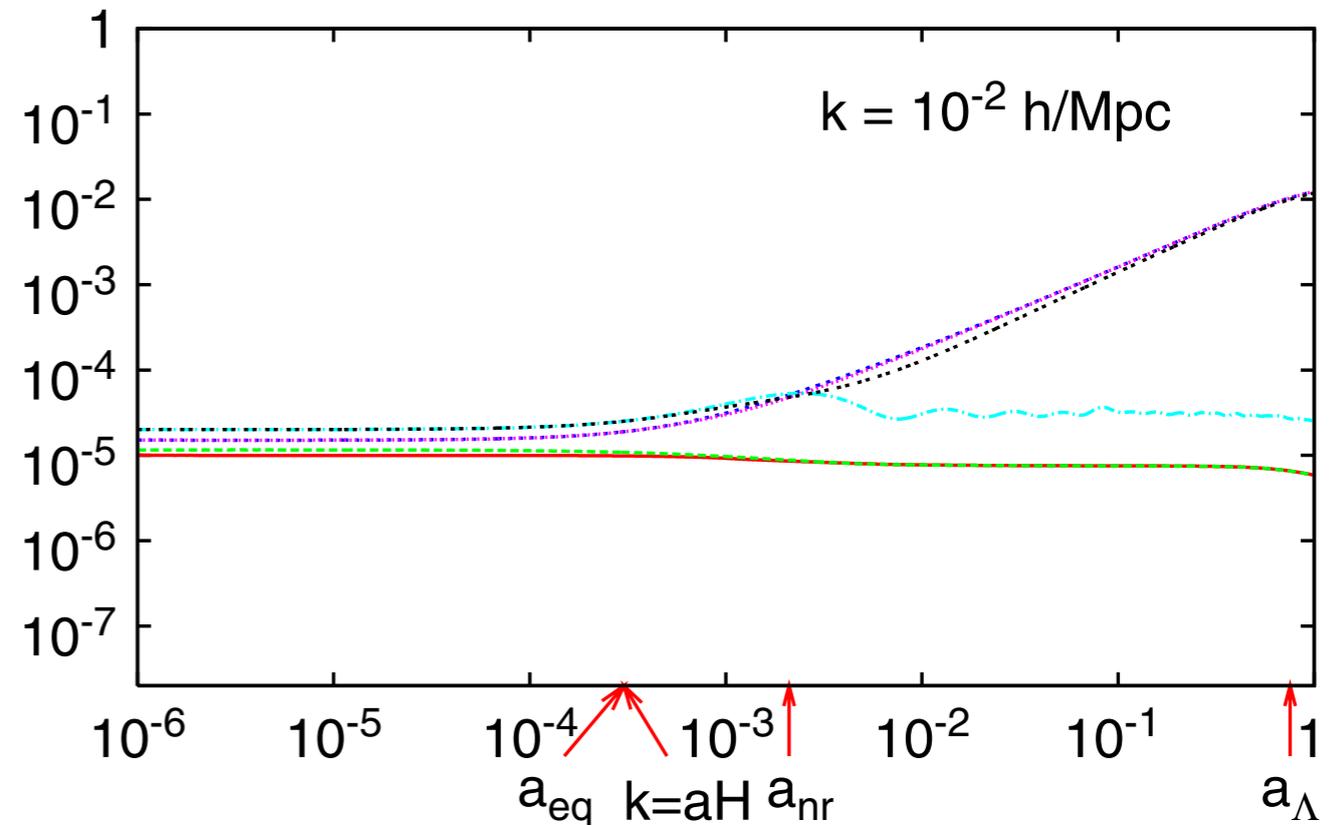
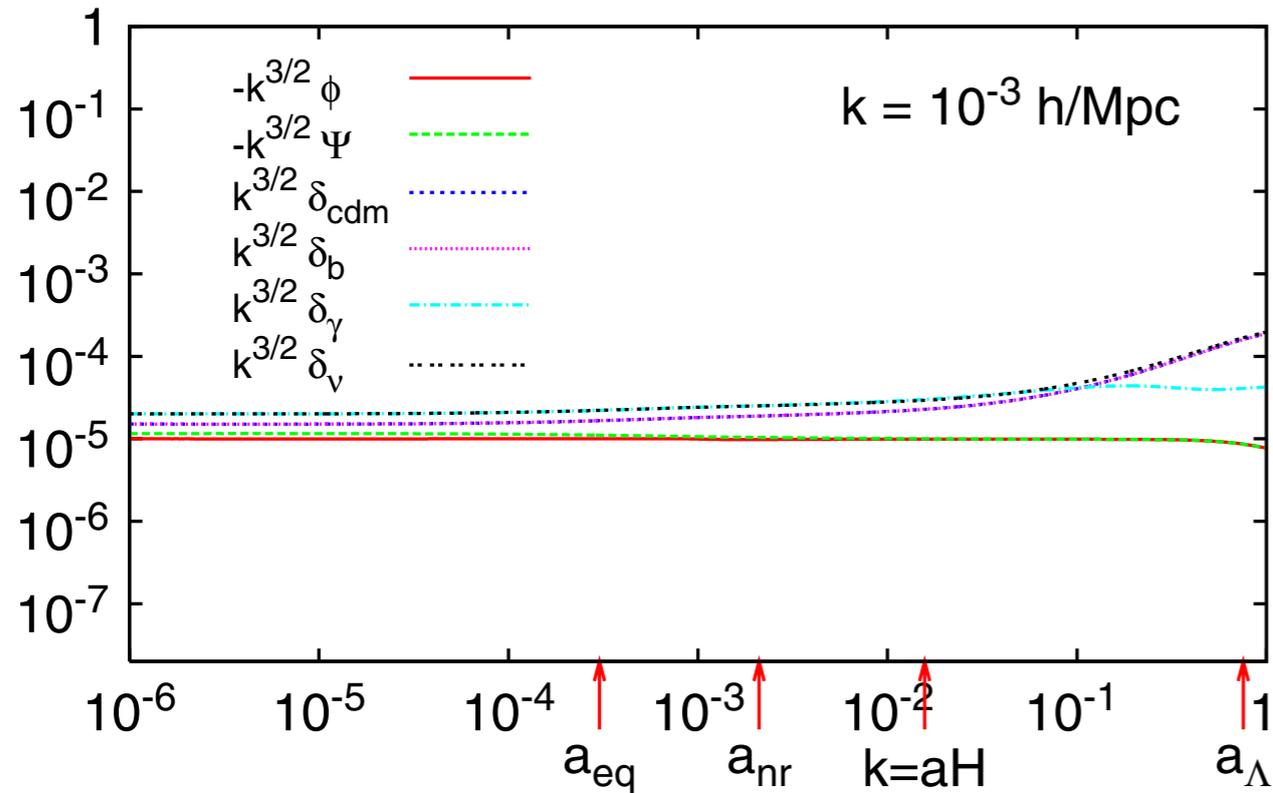
# Evolution of power spectrum



# $\Lambda$ CDM (massless neutrino)



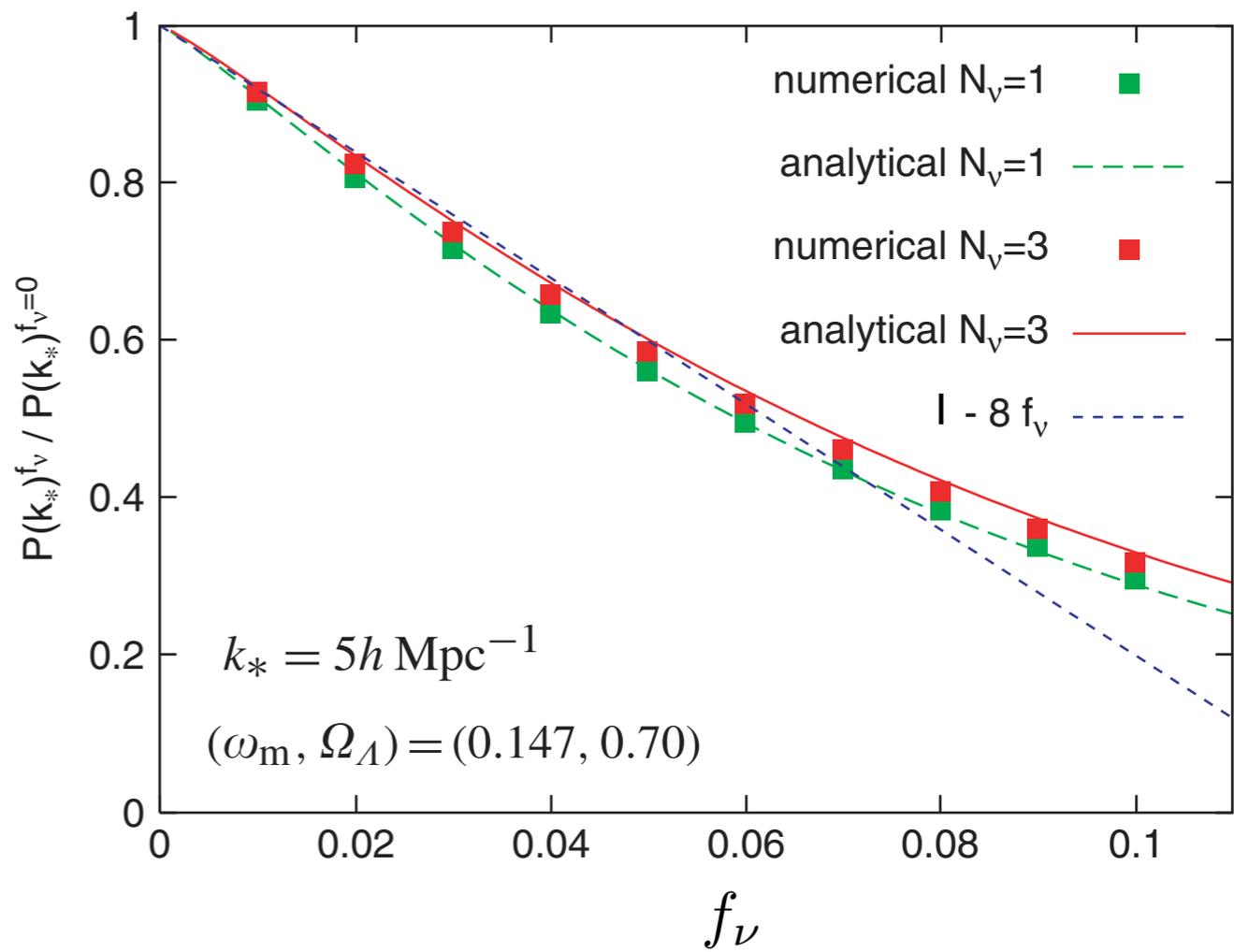
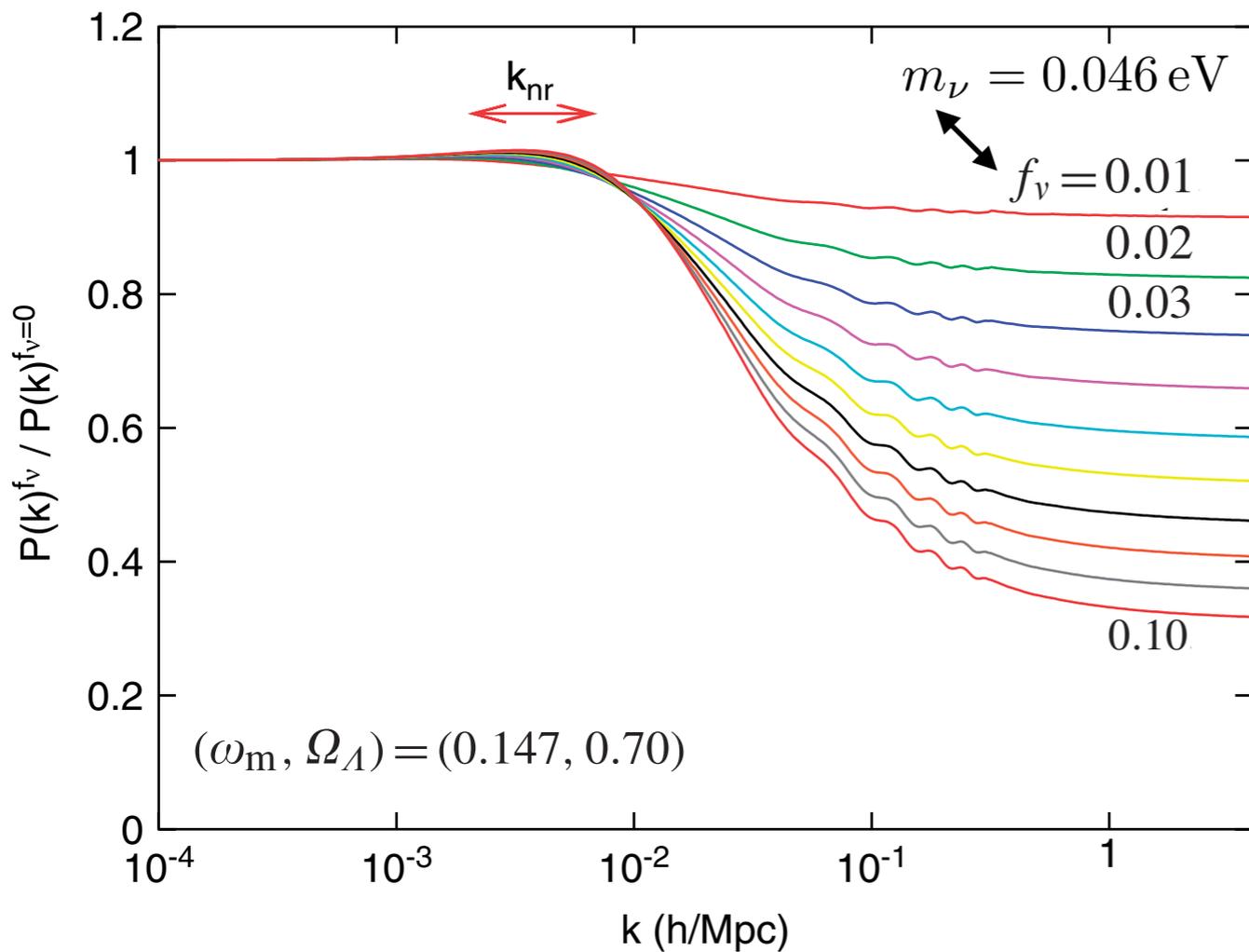
# $\Lambda$ CDM (massive neutrino) ( $f_\nu = 0.1$ )



# $\nu$ 's free-streaming suppression

$$k_{\text{FS}} = \frac{0.677}{(1+z)^2} \frac{m_\nu}{1 \text{ eV}} \sqrt{\Omega_{\text{m},0}(1+z)^3 + \Omega_\Lambda} h \text{ Mpc}^{-1}$$

$$\frac{P(k)|_{f_\nu \neq 0}}{P(k)|_{f_\nu = 0}} = (1 - f_\nu)^3 \left\{ 1.9 \times 10^5 \frac{\Omega_{\nu,0} h^2}{N_{\text{eff}}} \frac{D_1(a)}{a} \right\}^{-(6/5)f_\nu}$$



# Impact on large-scale structure

N-body simulations

massless limit

1e-28

massive neutrinos

$$\sum m_\nu = 0.95\text{eV}$$

$$\Omega_\nu = 0.02$$

1e-28

1e-29

massive neutrinos

$$\sum m_\nu = 1.9\text{eV}$$

$$\Omega_\nu = 0.04$$

1e-28

1e-29

1e-30

1e-31

Density ( $\text{g}/\text{cm}^3$ )

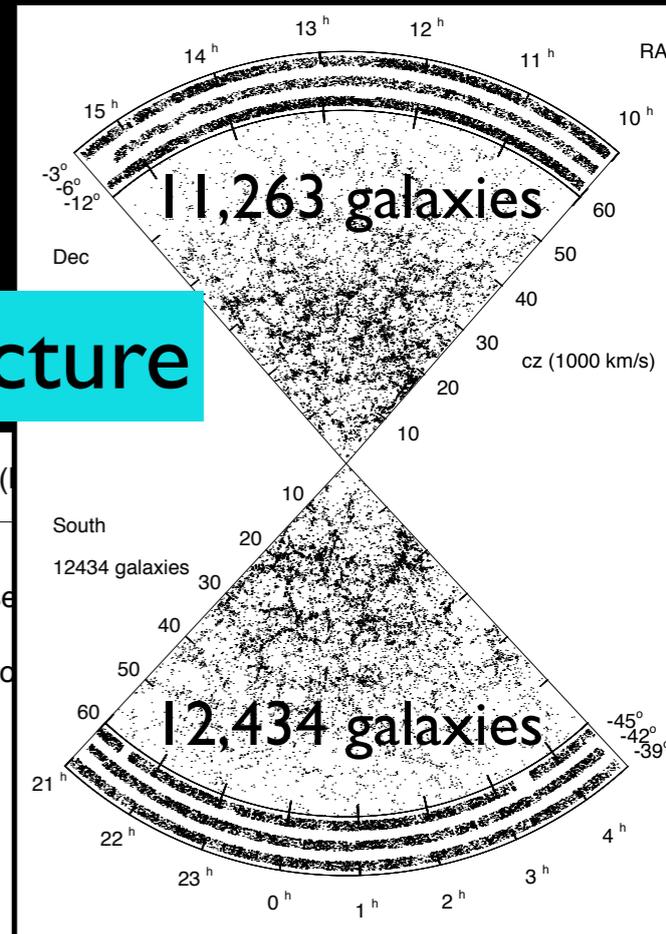
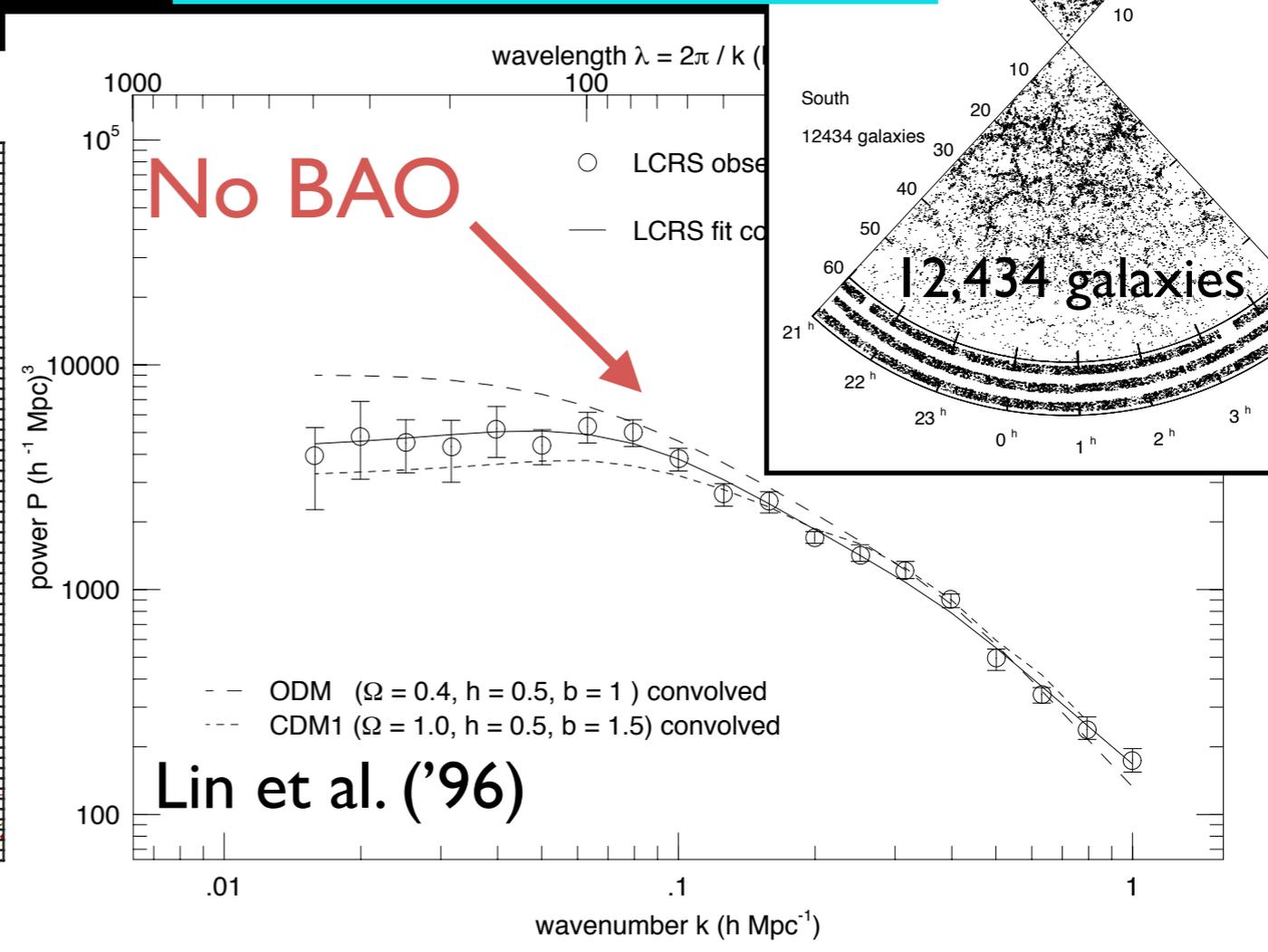
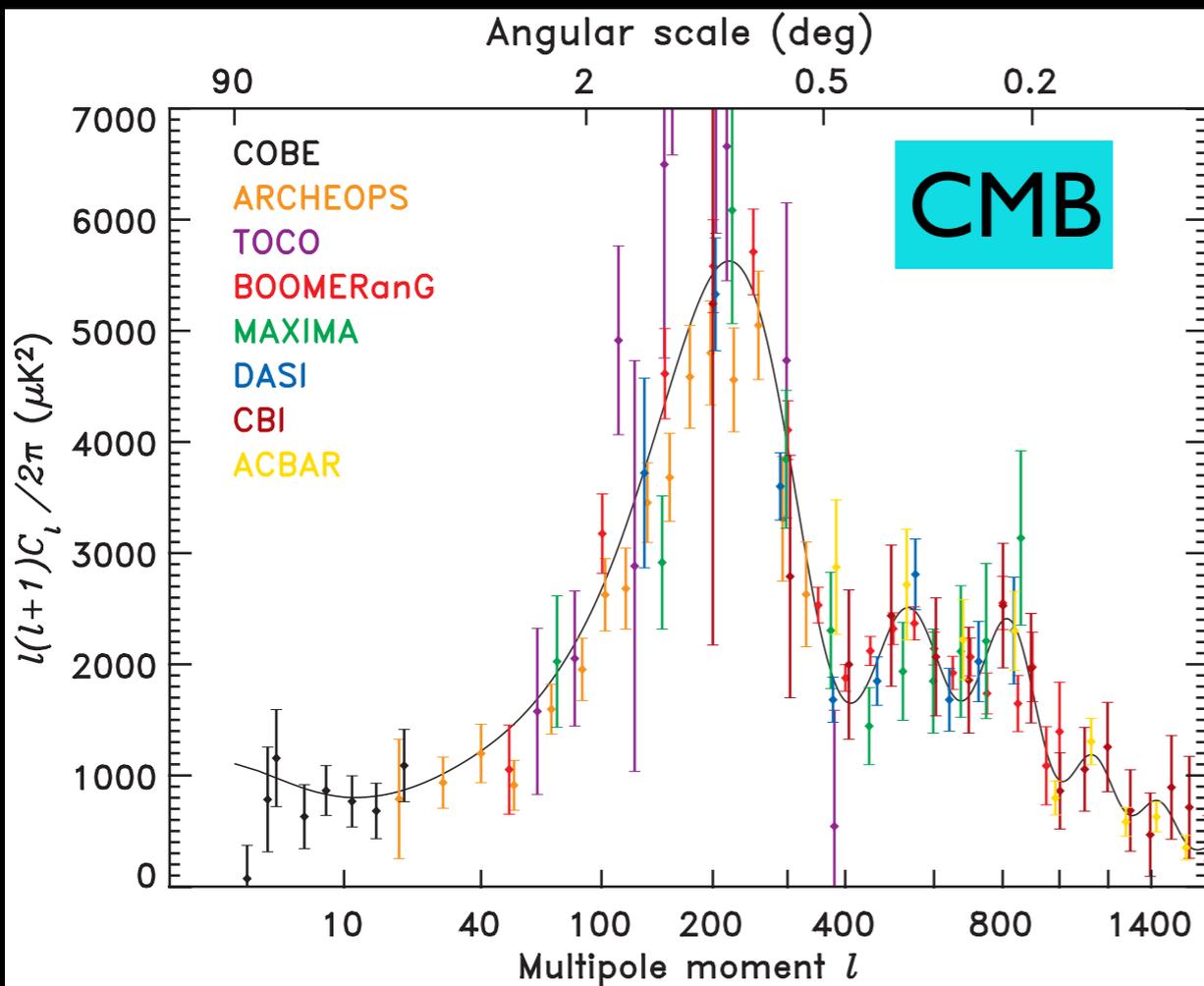
$$\begin{aligned}\Omega_m &= \Omega_{\text{cdm}} + \Omega_b + \Omega_\nu \\ &= 0.266\end{aligned}$$

200 Mpc/h

# Pre-precision cosmology era

No full-sky & high-resolution CMB measurements

Large-scale structure



Hinshaw et al. ('01)

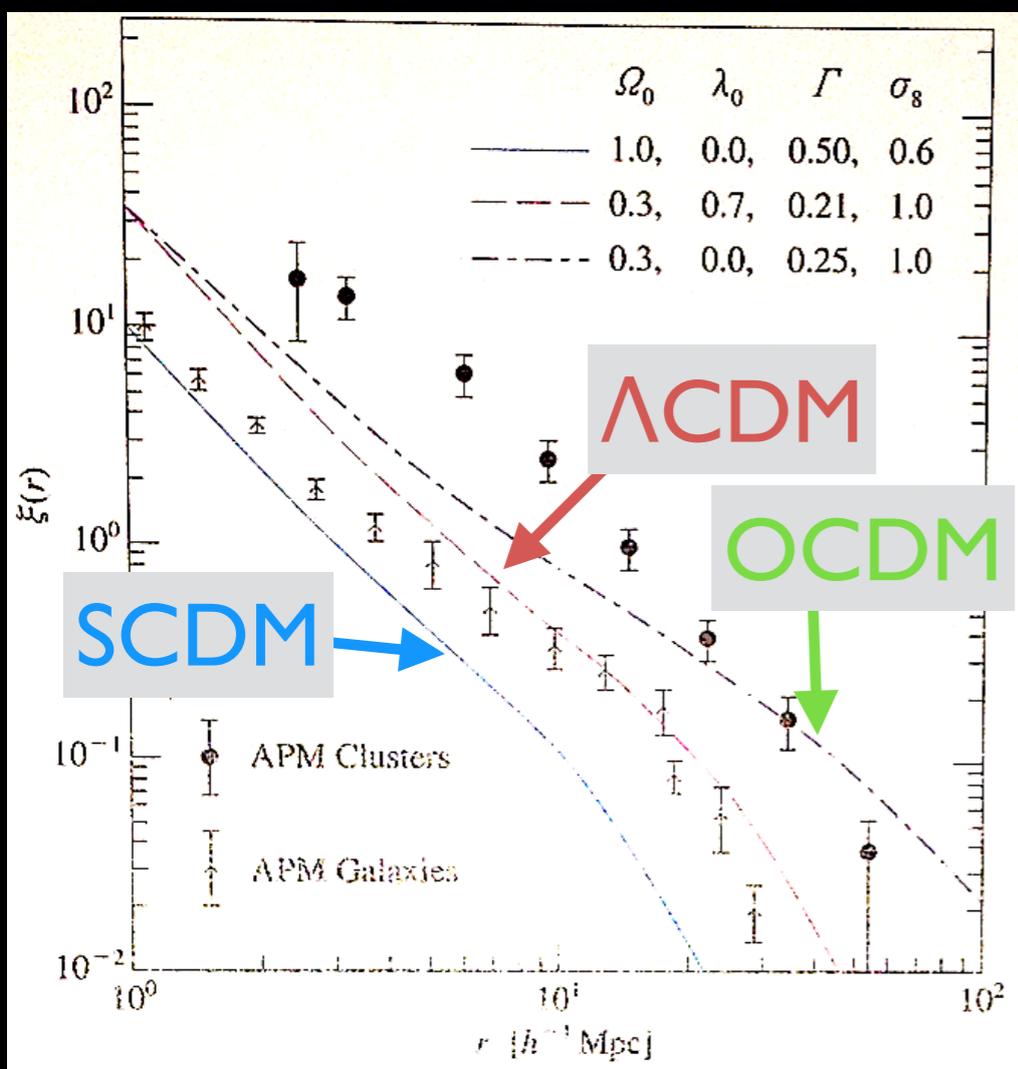
Las Campanas redshift survey  
(largest survey before SDSS/2dF)

# Standard model candidates

**SCDM (Standard CDM)** ( $\Omega_m = 1, \Omega_{DE} = 0, h \simeq 0.5, \sigma_8 \simeq 0.6$ )

**OCDM (Open CDM)** ( $\Omega_m \simeq 0.3, \Omega_{DE} = 0, h \simeq 0.8, \sigma_8 \simeq 1.0$ )

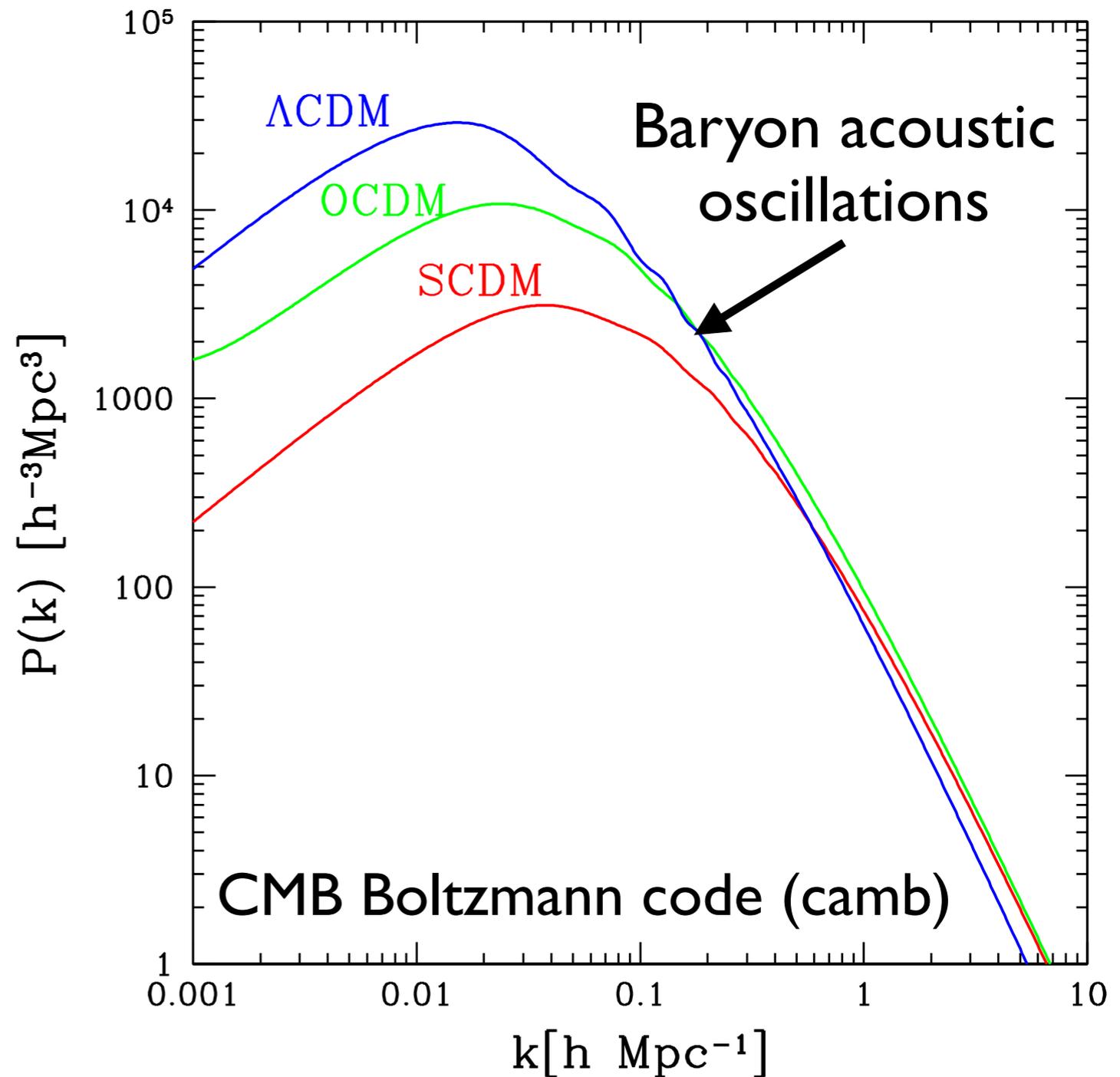
**$\Lambda$ CDM (Lambda CDM)** ( $\Omega_m \simeq 0.3, \Omega_{DE} \simeq 0.7, h \simeq 0.7, \sigma_8 \simeq 1.0$ )



Hard to distinguish between each other with limited cosmological observations

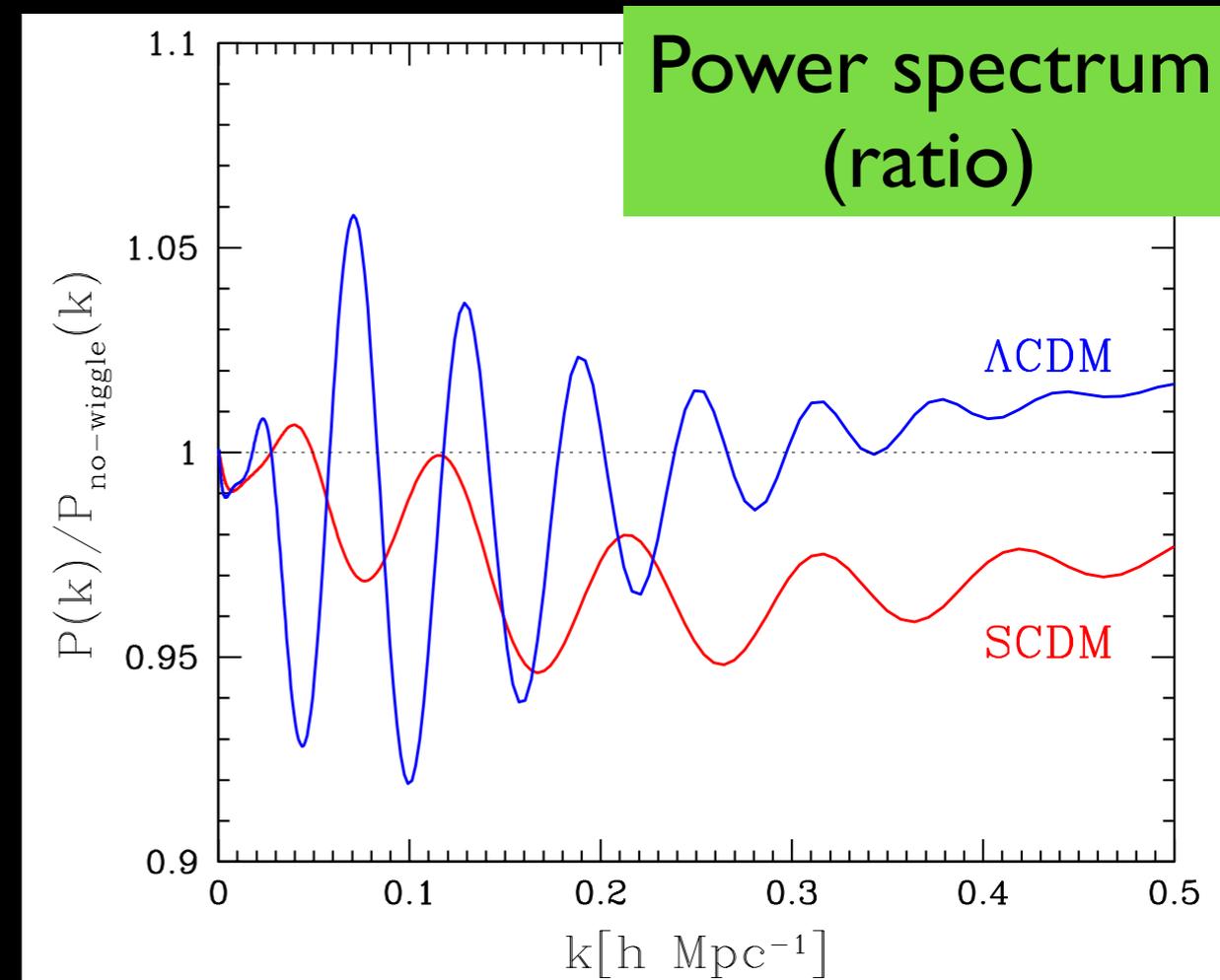
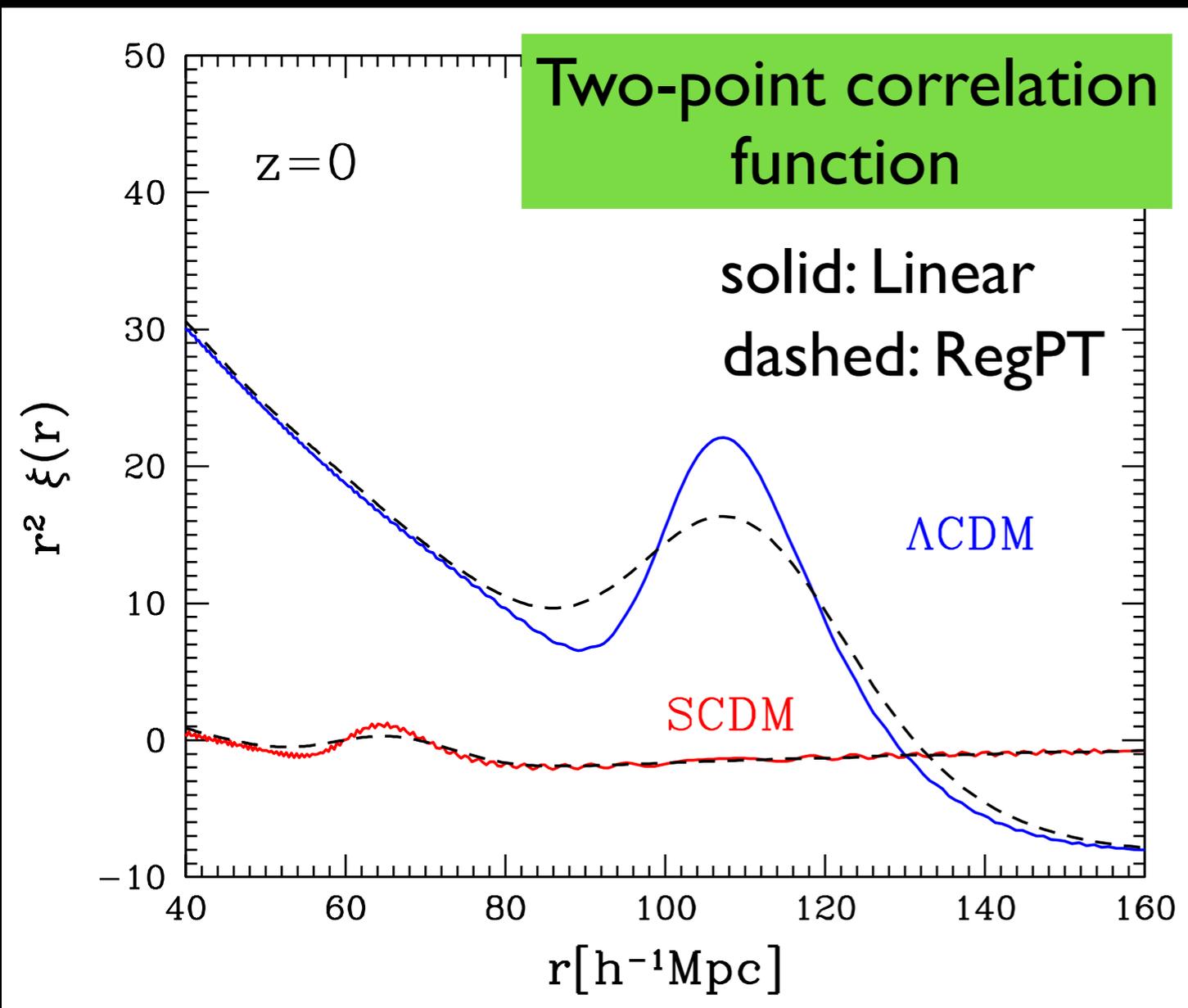
# Linear power spectrum

- SCDM** ( $\Omega_m = 1, \Omega_\Lambda = 0, \sigma_8 = 0.59$ )
- $\Lambda$ CDM** ( $\Omega_m = 0.272, \Omega_\Lambda = 0.728, \sigma_8 = 0.81$ )
- OCDM** ( $\Omega_m = 0.45, \Omega_\Lambda = 0, \sigma_8 = 0.80$ )



# Baryon acoustic oscillations in SCDM model

BAO signal can be too much  
small to detect !!



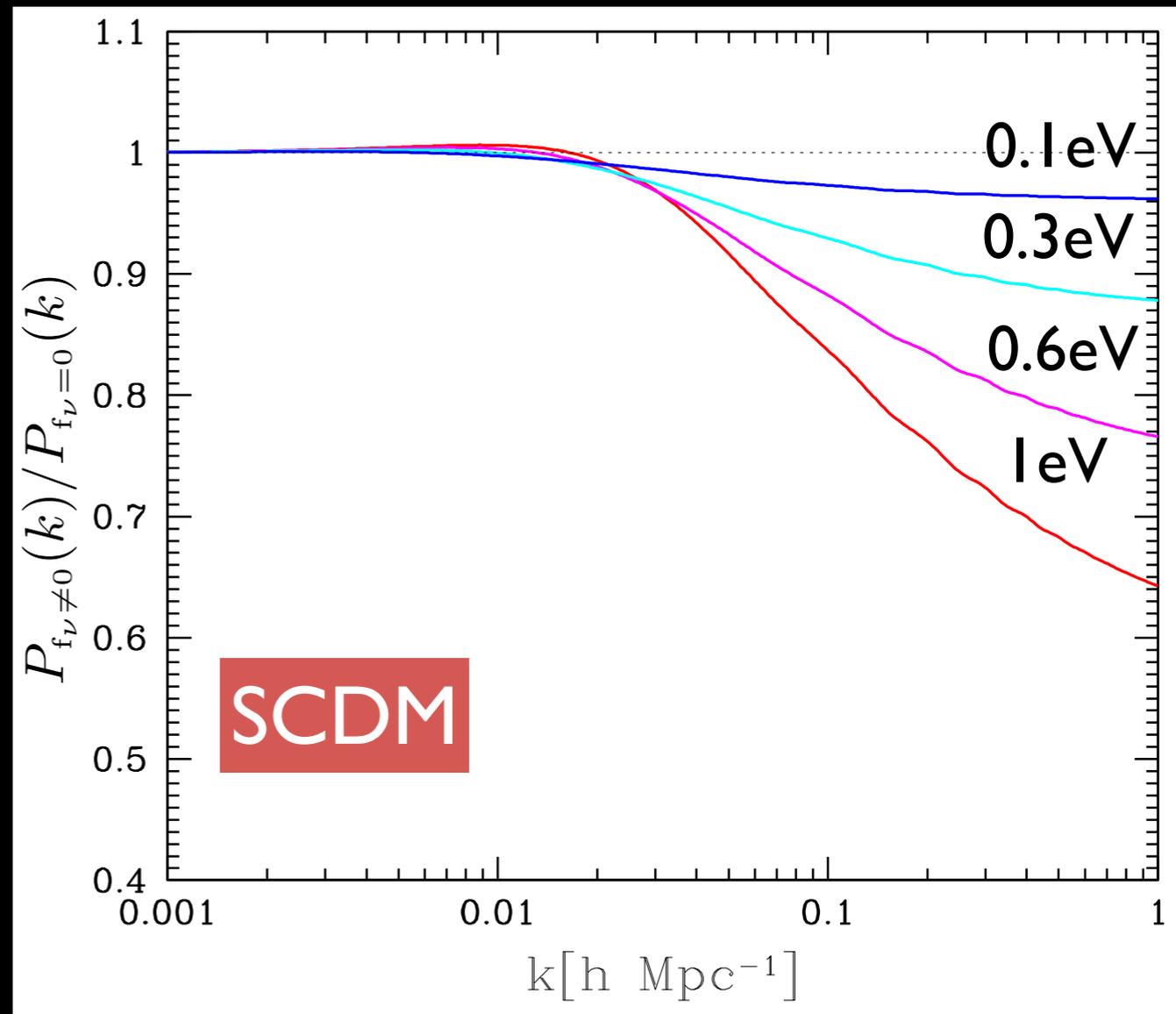
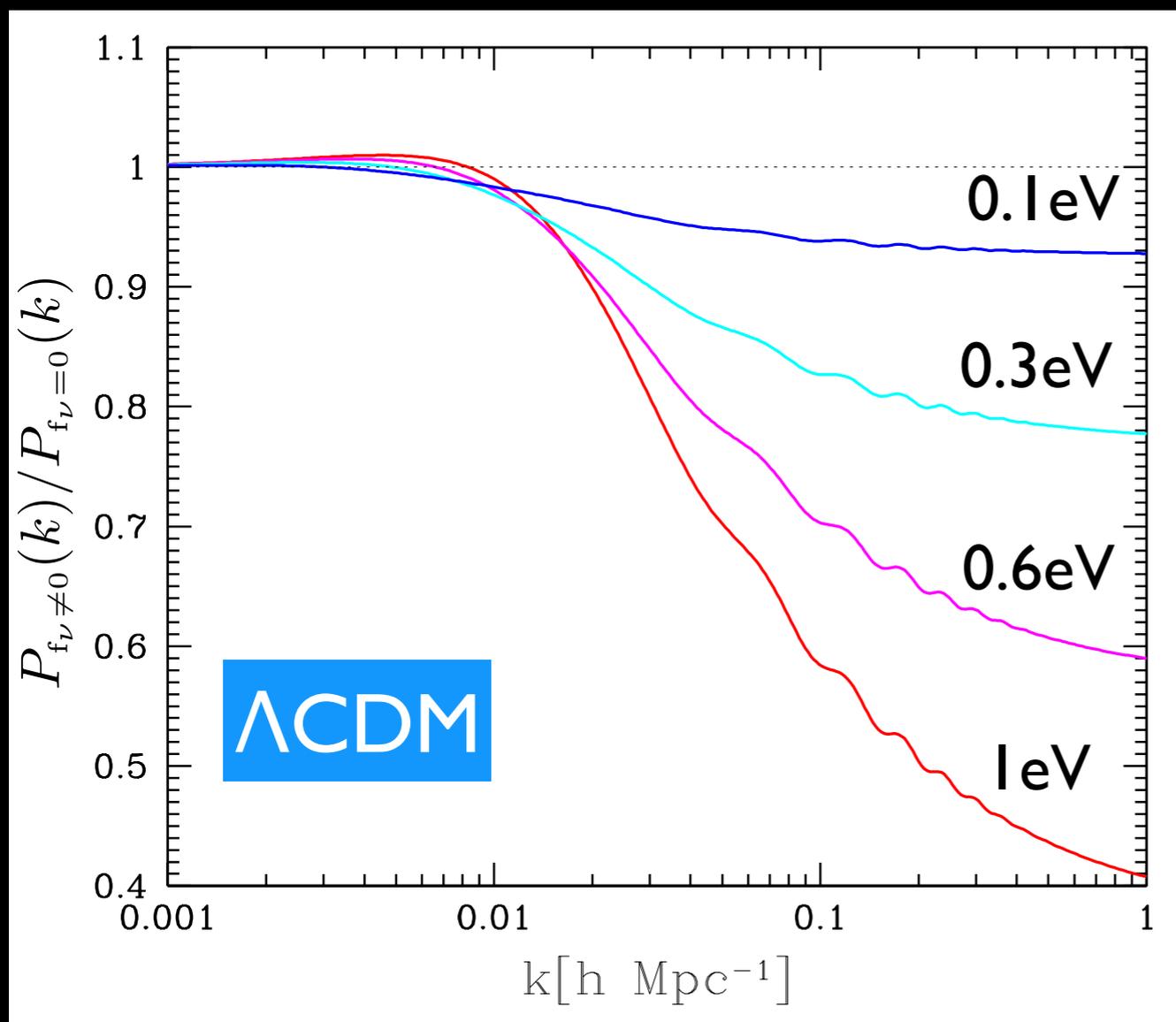
With a small signal of BAO,  
accurate measurement of  
cosmic expansion is difficult

# $\nu$ 's free-streaming suppression

$$\frac{P_{f_\nu \neq 0}(k)}{P_{f_\nu = 0}(k)} \simeq 1 - 8 f_\nu \quad ; \quad f_\nu = \frac{\Omega_\nu}{\Omega_m}$$

in  $\Lambda$ CDM model

(e.g., Hu et al. '98)

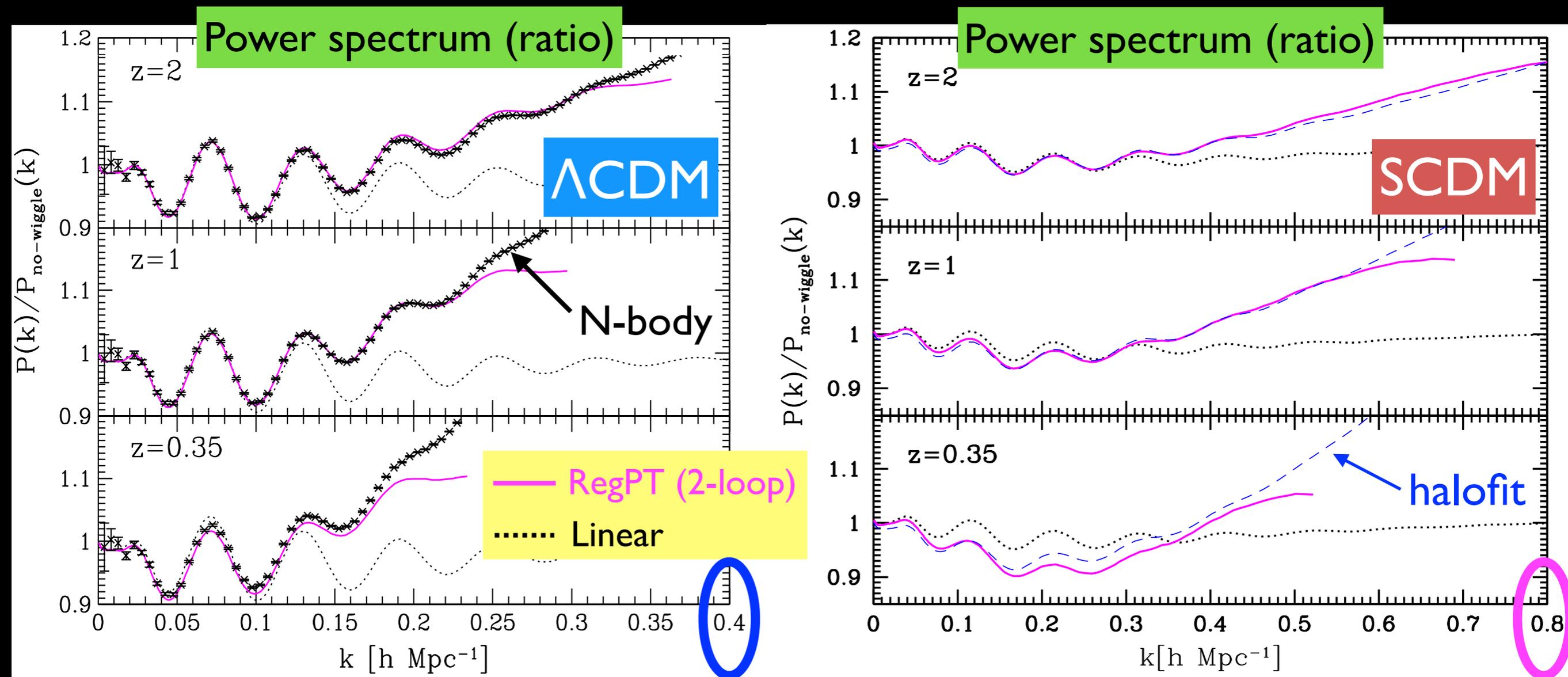


Suppression effect diminishes in SCDM

# Nonlinear gravitational evolution

Perturbation theory (PT) calculation can do a great job at high- $z$   
(but soon becomes worse at low- $z$ )

Even the standard PT would be much more powerful and accurate



# Large-scale structure in SCDM

~summary~

- **BAO** : signal is tiny, and even the detection is challenging
- **$\nu$ 's free-streaming suppression** : more difficult to measure  $\nu$ -mass
- **Nonlinear evolution** : standard PT does work well. No chance to develop resummation/renormalization technique ?
- **Redshift-space distortions** : Test of gravity may get in trouble

size of RSD

$$\propto f(z) \equiv \frac{d \ln D_+(z)}{d \ln a} \simeq \{\Omega_m(z)\}^\gamma \xrightarrow{\text{in SCDM}} 1$$

Development of precision cosmology will never happen in SCDM...  
 $\Lambda$ CDM (also OCDM) may be the best suited for precision cosmology !!