

Plastic Flow and Dynamic Transitions of Vortex Solids in Superconductors



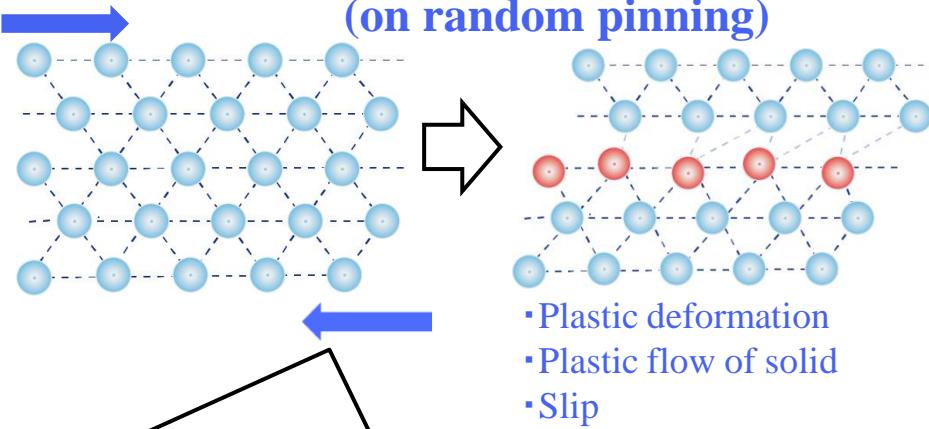
S. Okuma, Y. Kawamura, A. Motohashi, and S. Kaneko

Department of Physics, Tokyo Institute of Technology, Tokyo, Japan

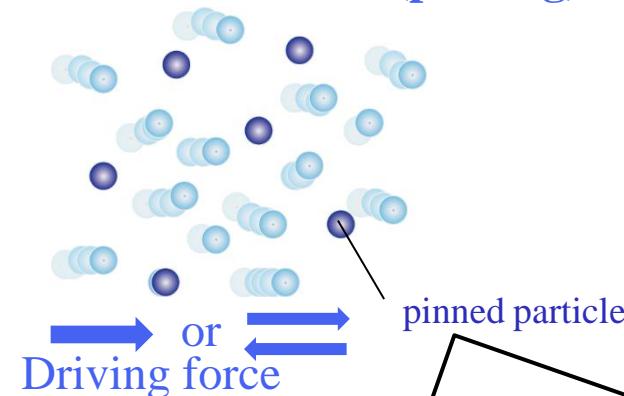
Acknowledgments: N. Kokubo, C. Reichhardt, K. Takeuchi

Introduction

Lattice subject to shearing force (on random pinning)



Interacting particles driven over a random substrate (pinning)



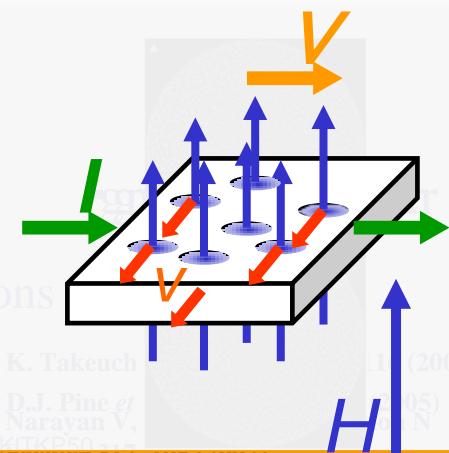
Elastic media responding to an external shearing force

- drift of earth plates
- avalanches

Non-equilibrium phenomena in many-particle systems

- turbulent fluids
- granular matter

A vortex system is a general model system for studying **plasticity of solids** and various **non-equilibrium phenomena in interacting many particle systems**



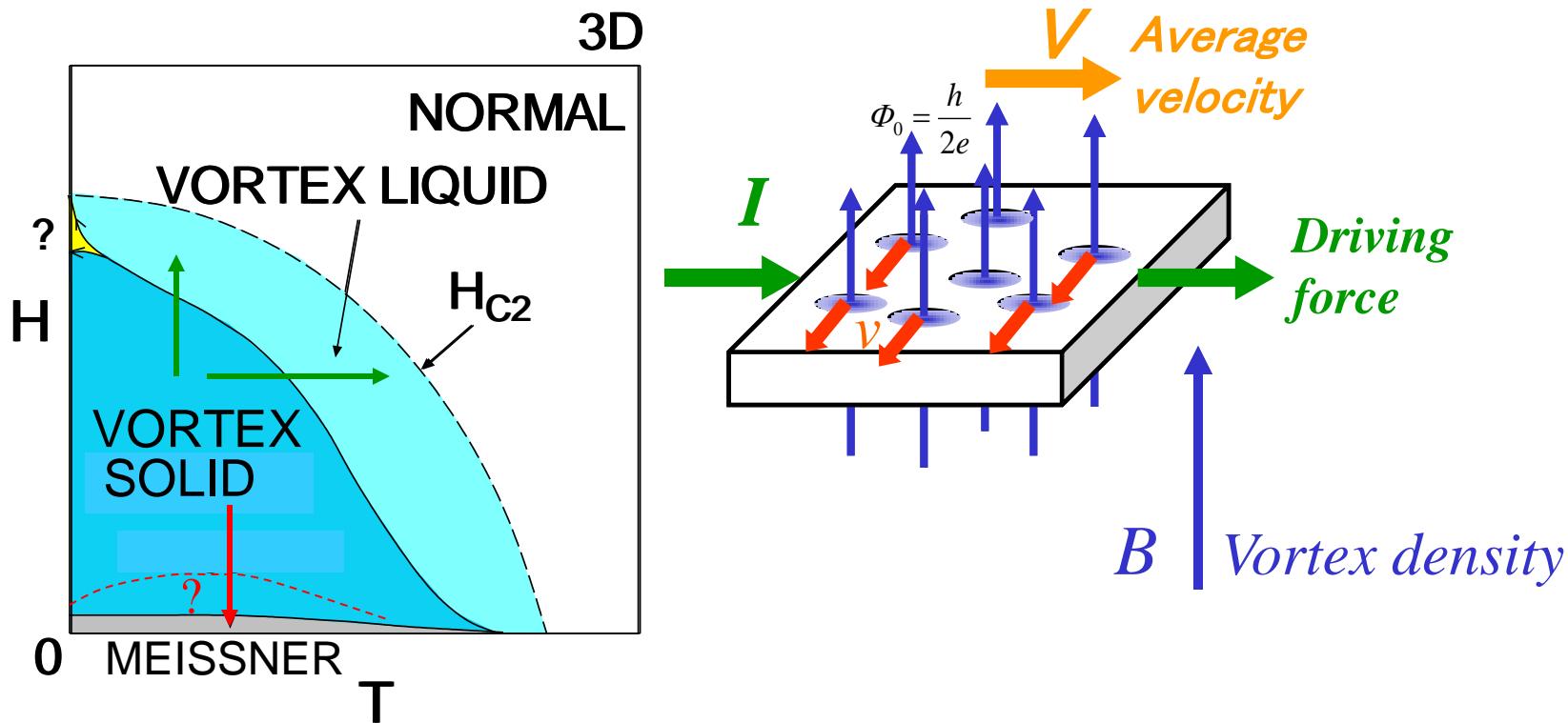
Introduction

Vortex states (phase diagram) in type-II superconductors

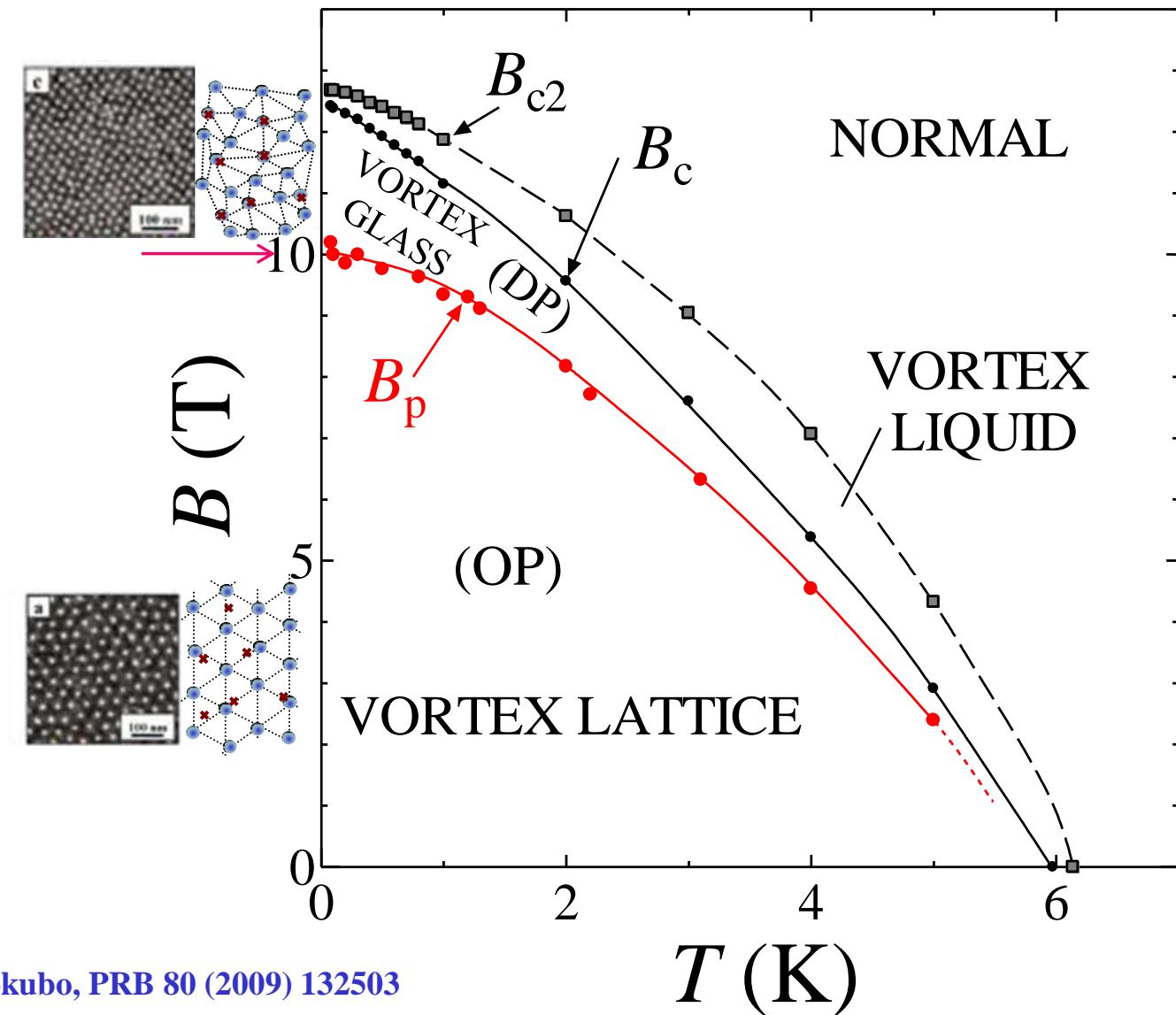
Solid-liquid (melting) transition

with increasing T / H (thermal fluctuations) or

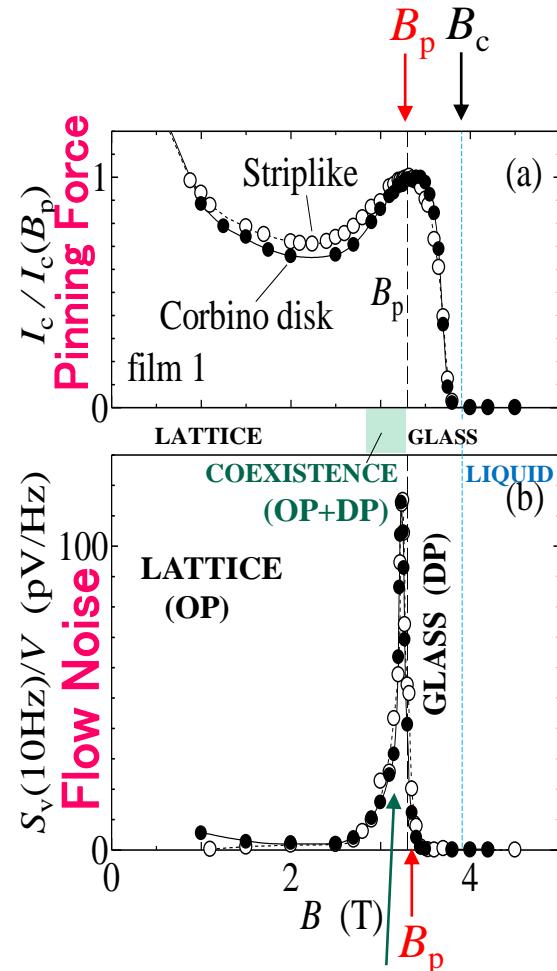
with decreasing H (vanishing shear modulus)



Static vortex phases for $a\text{-Mo}_x\text{Ge}_{1-x}$ film with weak random pinning

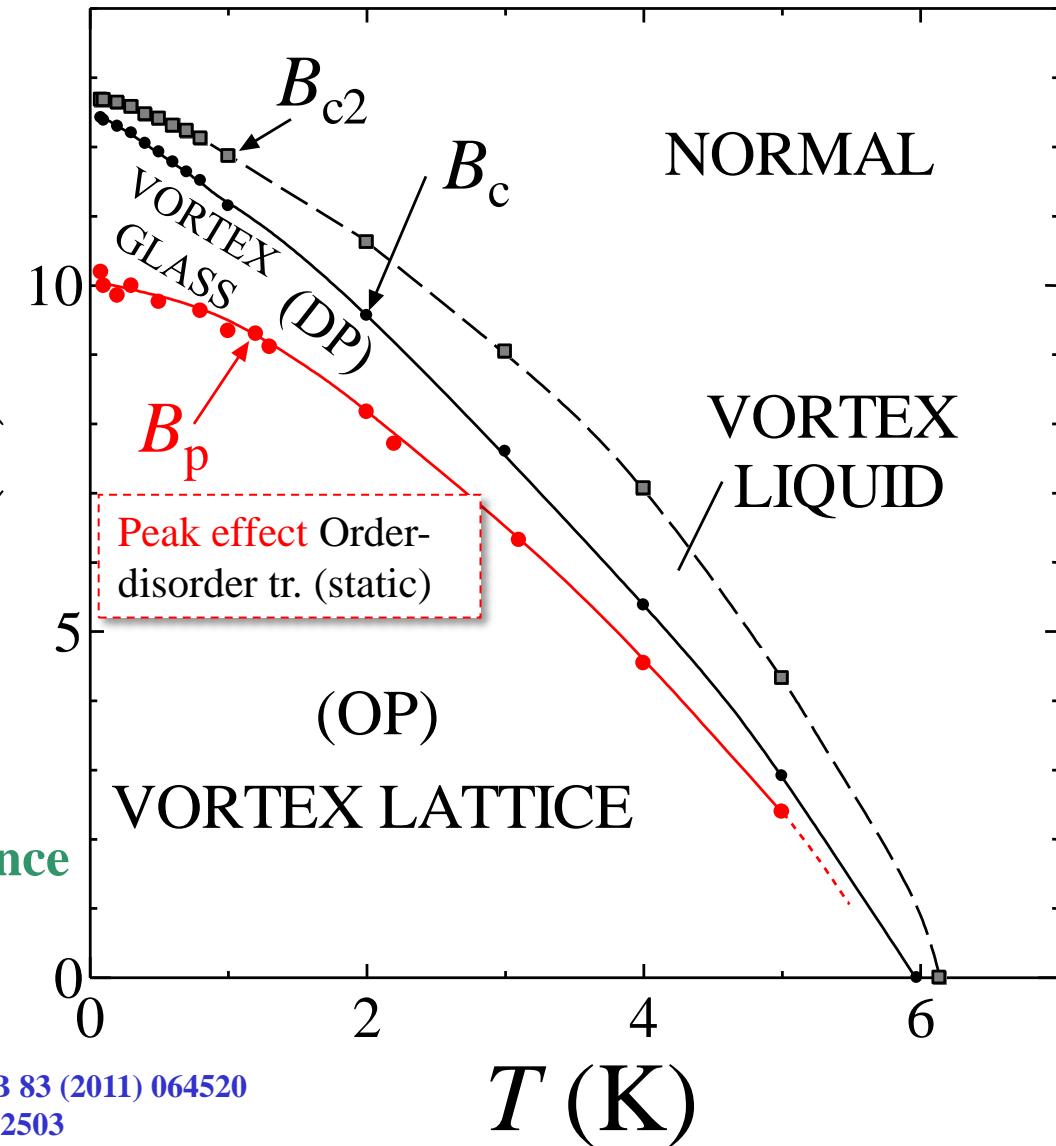


Order-disorder (OP-DP) transition at B_p



Largest noise at phase **coexistence**
OP+DP

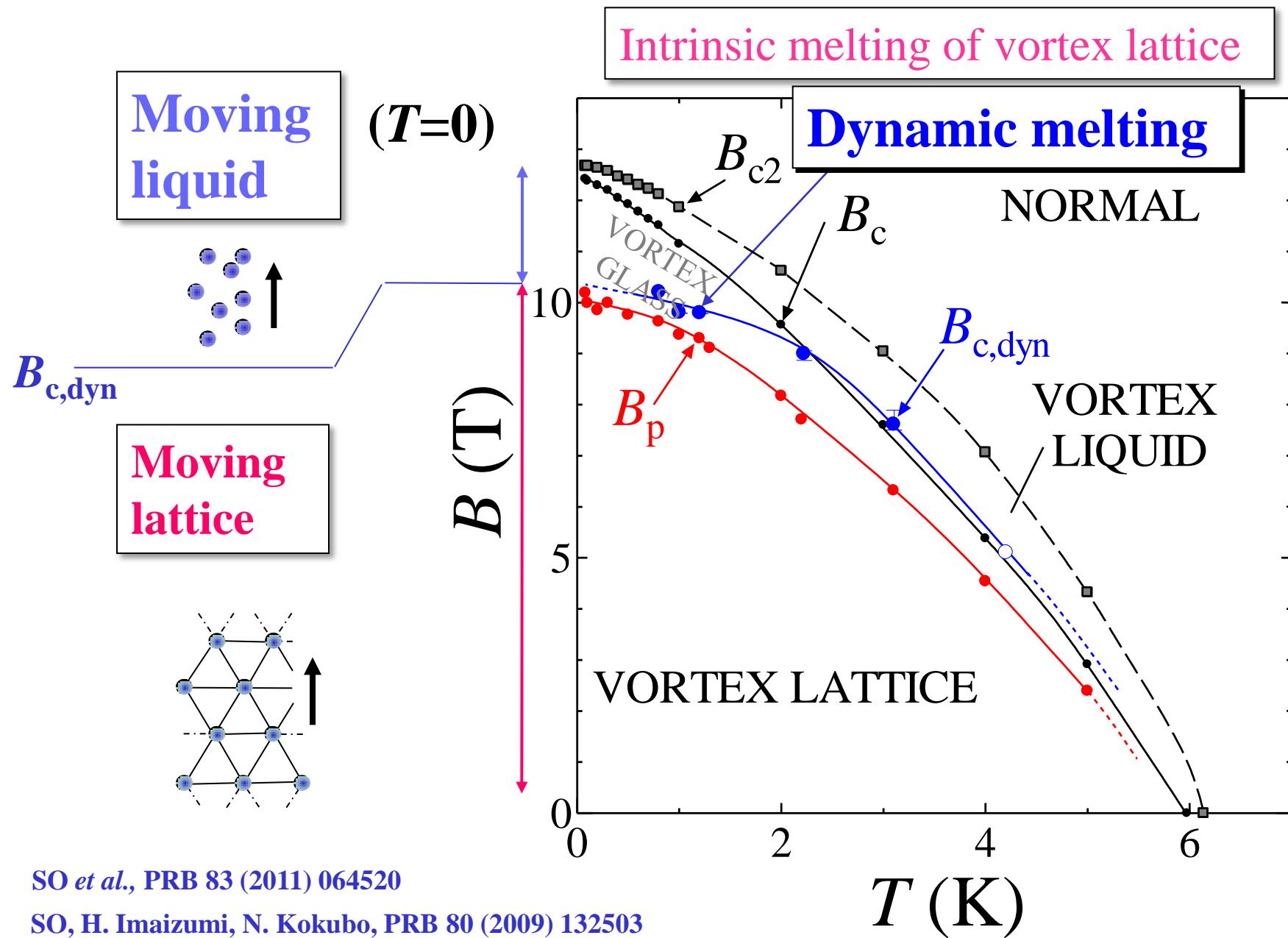
SO, Y. Suzuki, N. Kokubo, PRB 77 (2008) 212505



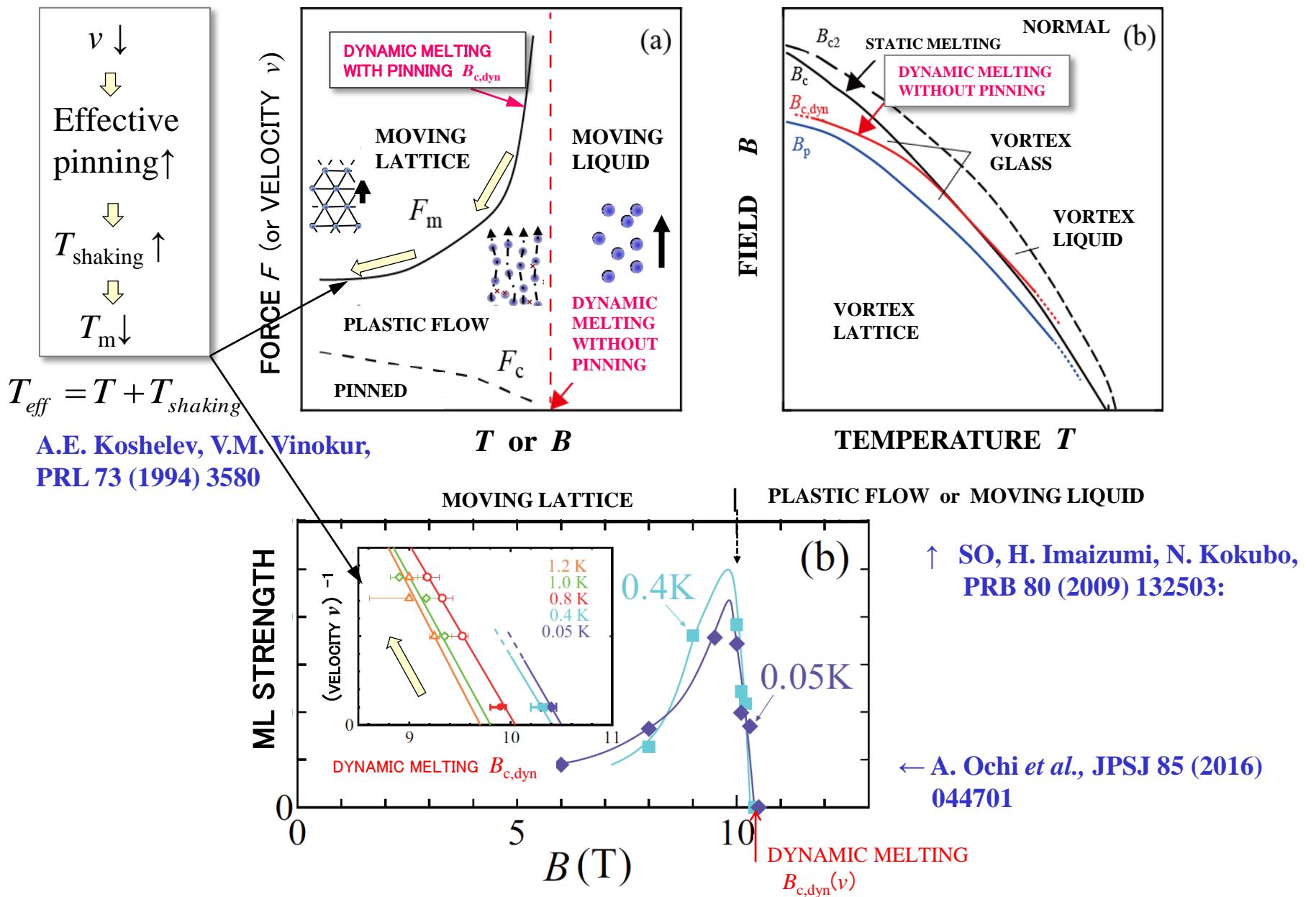
SO, H. Imaizumi, D. Shimamoto, N. Kokubo, PRB 83 (2011) 064520

SO, H. Imaizumi, N. Kokubo, PRB 80 (2009) 132503

Dynamic melting $B_{c,dyn}$ decoupled from pinning vs static melting B_c

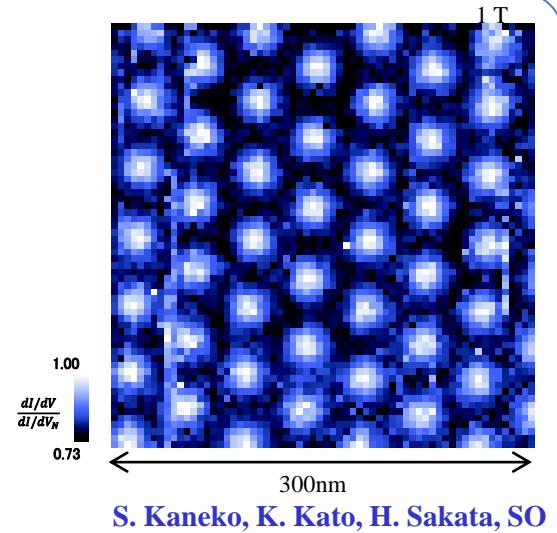


Suppression of $B_{c,dyn}$ by increased effective pinning (decreased ν)

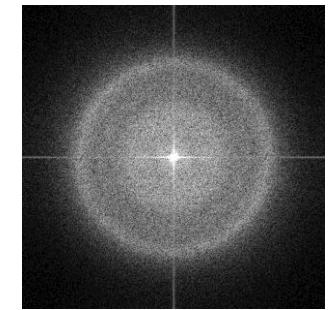


Vortex matter in type-II superconductors

- Exhibit **various phases** and **dynamic phase transitions** induced by motion, which are **not** largely dependent on materials



- $a\text{-Mo}_x\text{Ge}_{1-x}$ films with **weak pinning**
 - very uniform
 - random point pinning ~ 10 nm



Merits of vortex systems

- 1) We can conduct experiments **repeatedly** and **controllably**
- 2) readily **change** static vortex **structure**, *lattice, glass, liquid, ...*
only by changing B and T
- 3) **drive** the system by **dc**, **ac**, and **dc+ac** currents (**forces**)

Uniqueness of this work

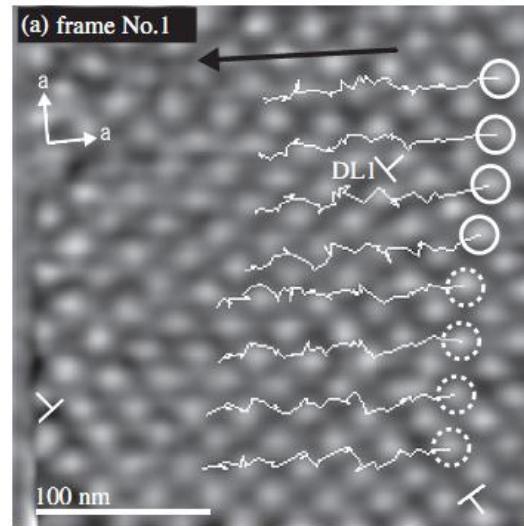
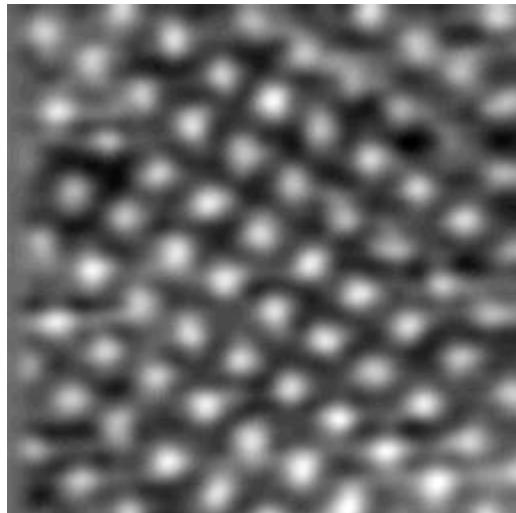
- 4) **global shear** (CD) as well as local shear (strip)
- 5) various non-equilibrium phenomena in **different ν regimes**
 - large ν* : **elastic to plastic** transformation with $\nu \downarrow$ (**pinning** \uparrow)
 - small ν* : **non-equilibrium transitions** in interacting many particles with $\nu \uparrow$ (**pinning** \downarrow)
 - **random organization** and reversible to irreversible transition (**RIT**)
 - plastic **depinning** transition

Vortex motion detected by STM/STS

Uchiyama, Kaneko, Sakata, Nishida *et al.*

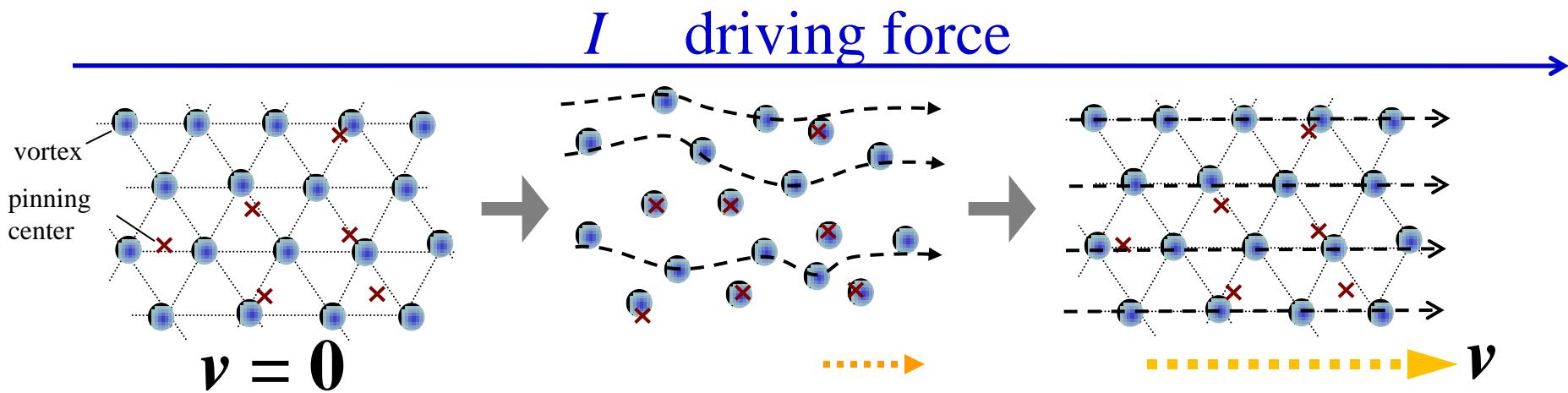
STM/STS High B (> 1 T)

$v_{\text{STM}} \sim 1$ nm/s (too slow)



Driving force for the vortex motion

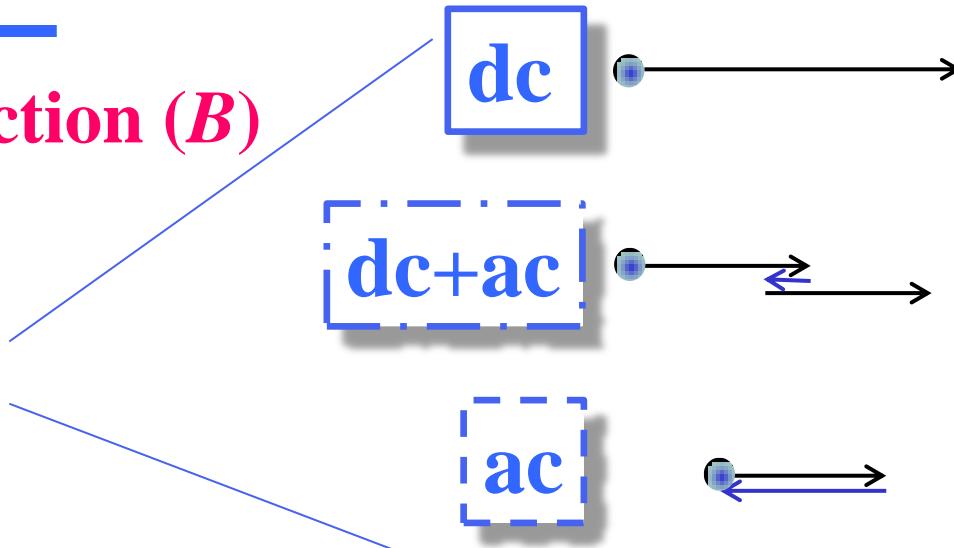
Forces acting on driven vortices



$$\eta \frac{d\mathbf{R}_i}{dt} = \mathbf{F}_i^{vv} + \mathbf{F}_i^p + \mathbf{F}^{ext}(t)$$

— — —

- **Vortex-vortex interaction (B)**
- **Pinning force (I_c)**
- **Lorentz force (I)**



(1) *Dynamics of moving lattices*

➡ Dynamic ordering of driven vortices

- lattice orientation, non-equilibrium SC

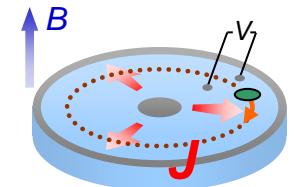
dc+ac

Dynamic melting of driven lattices

- intrinsic (quantum) melting

Plastic flow of solids

Fast



(2) *Dynamics of non-equilibrium many particles*

Novel dynamic transitions

ac

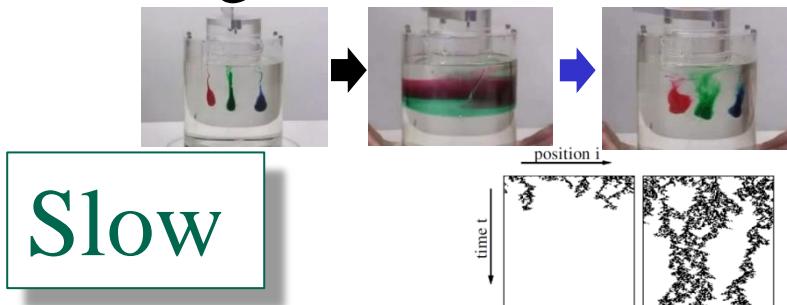
- rev-irreversible tr. and random organization

- absorbing tr.

- depinning tr.

dc

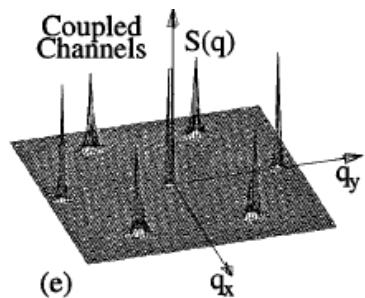
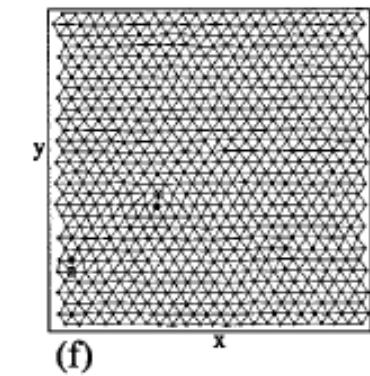
Slow



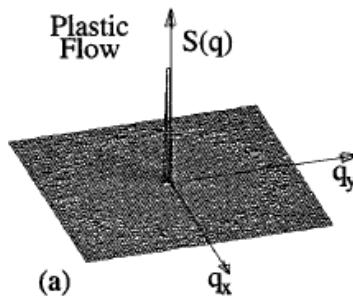
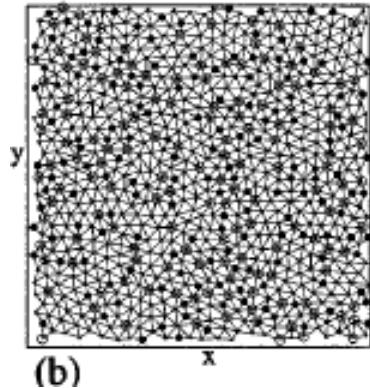
Dynamic ordering of driven vortices

Vortex configurations for *flux flow* and *plastic flow*

simulation

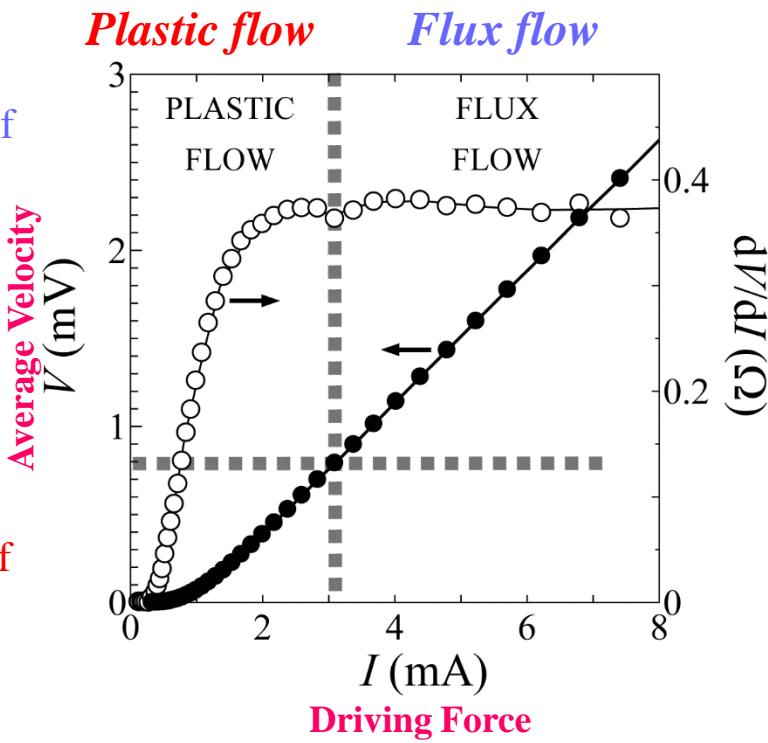


Flux flow
Small number of
dislocation



Plastic flow
Large number of
dislocation

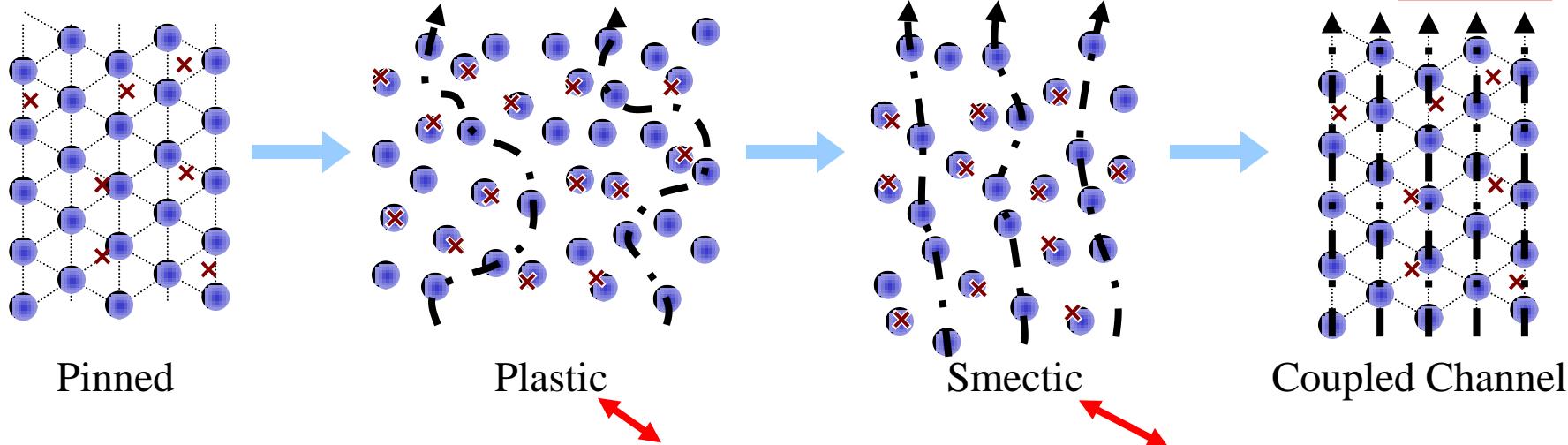
experiment



Vortex flow states and dynamic ordering

C. J. Olson, C. Reichhardt, F. Nori, PRL 81, 3757 (1998) 大熊哲, 井上甚, 小久保伸人, 固体物理 44, 1 (2009)

Current



Pinned

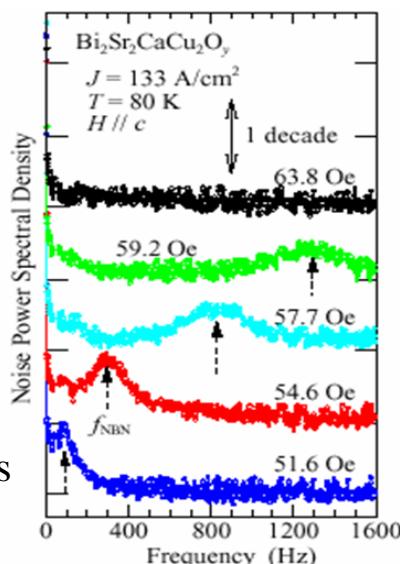
Plastic

Smectic

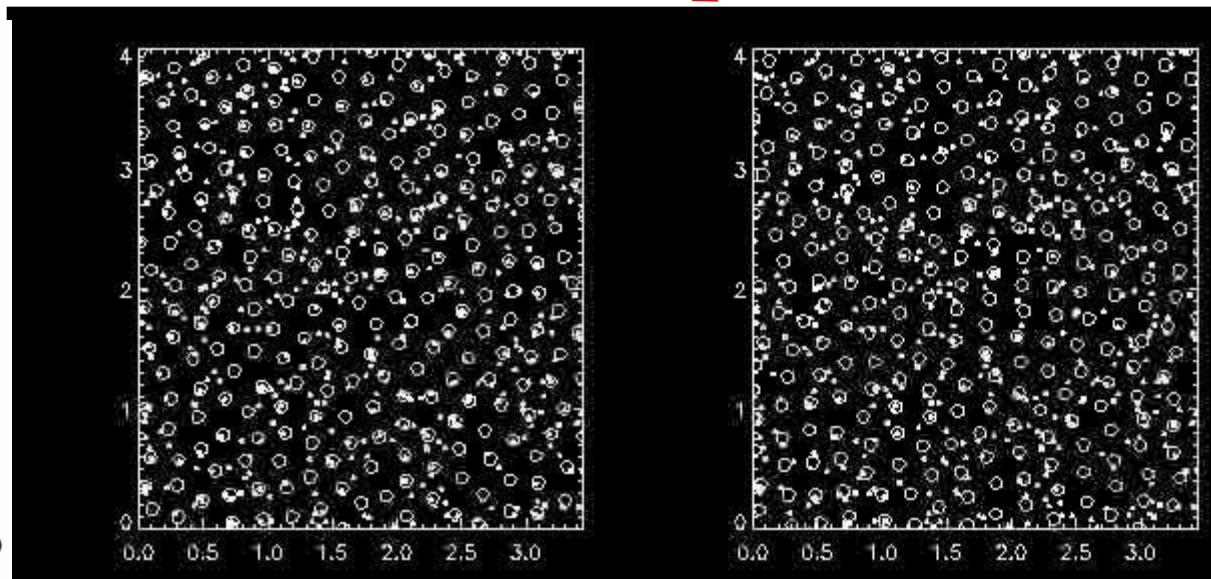
Coupled Channel

- Vortex
- ✗ Pinning

Narrow band
noise $S_V(f)$



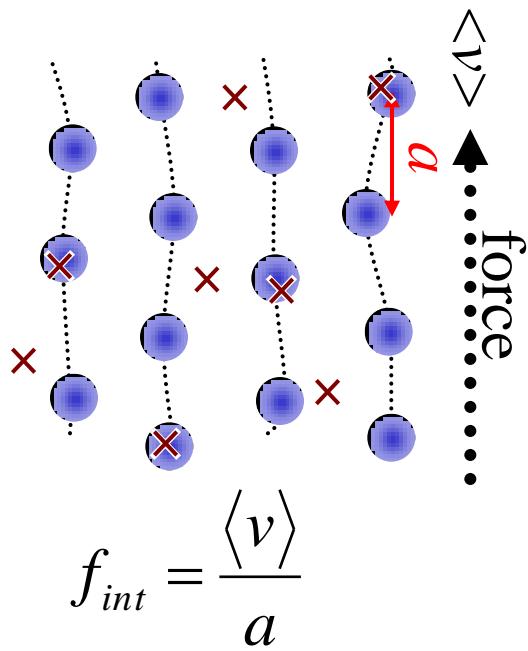
Y. Togawa, R. Abiru, K. Iwaya, H. Kitano,
A. Maeda, PRL 85 (2000) 3716



A. B. Kolton, D. Domínguez, N. G. Jensen

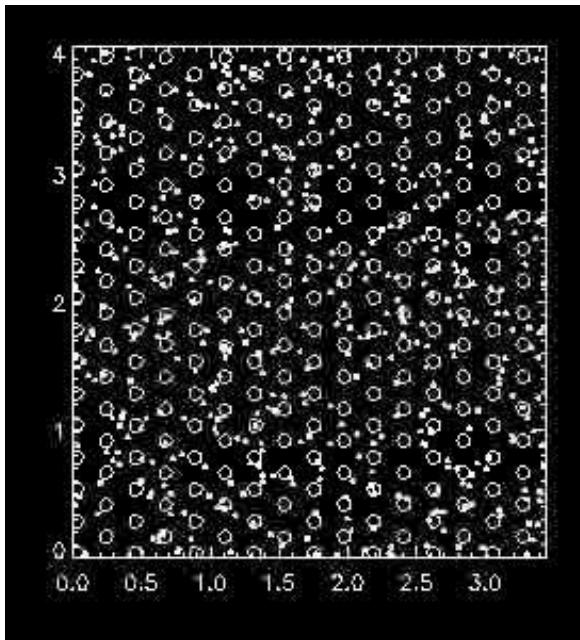
ML in uniform films with random pinning

Random pinning; dc + superimposed ac forces

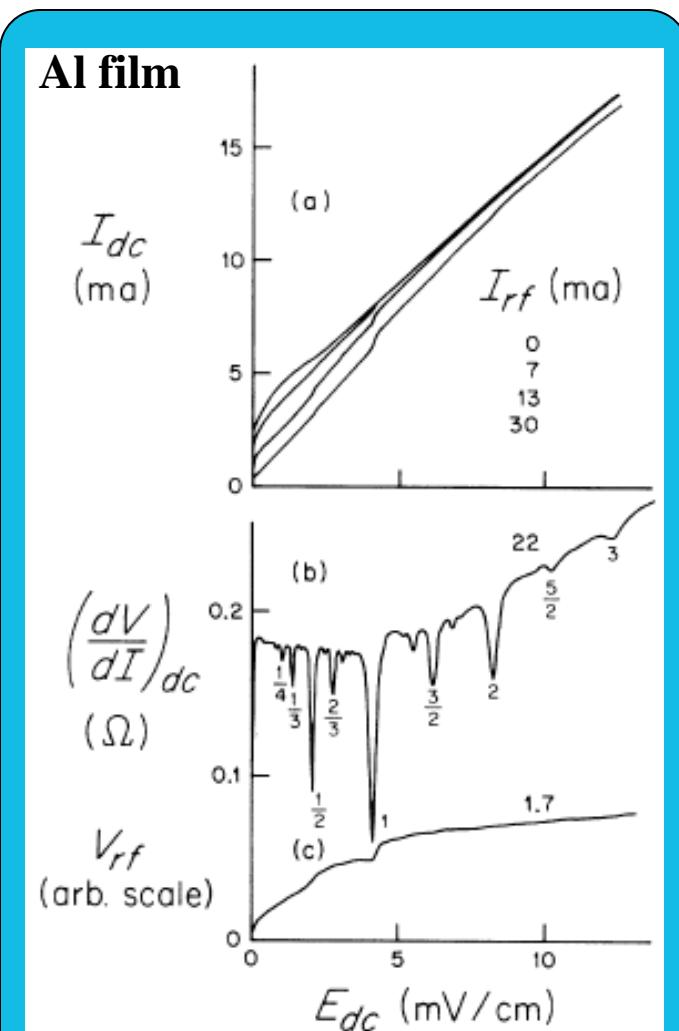


$$pf_{ext} = qf_{int} \quad (p, q : \text{integer})$$

- Coherent motion of a vortex lattice →
Periodicity can be induced dynamically
- At ML, the step-like structure analogous to
Shapiro steps appears in the I - V curves.



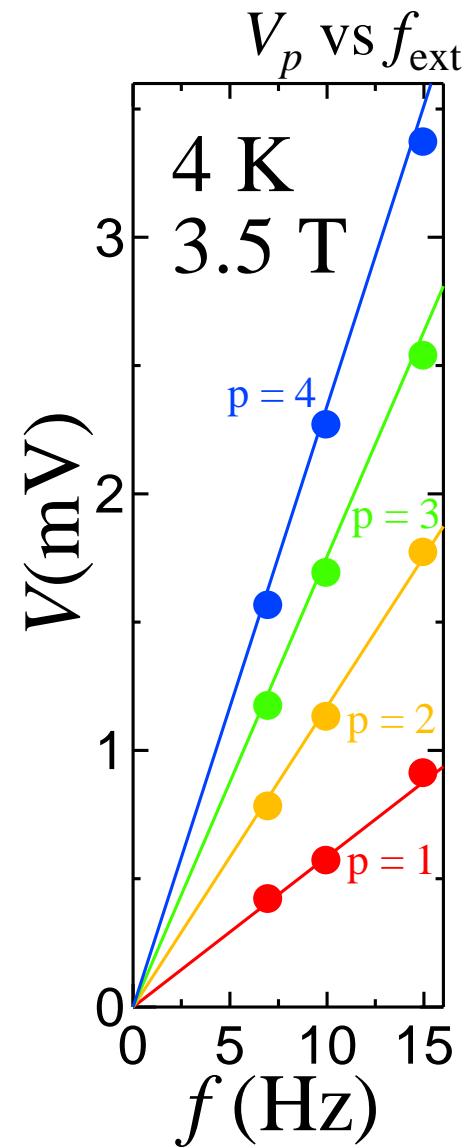
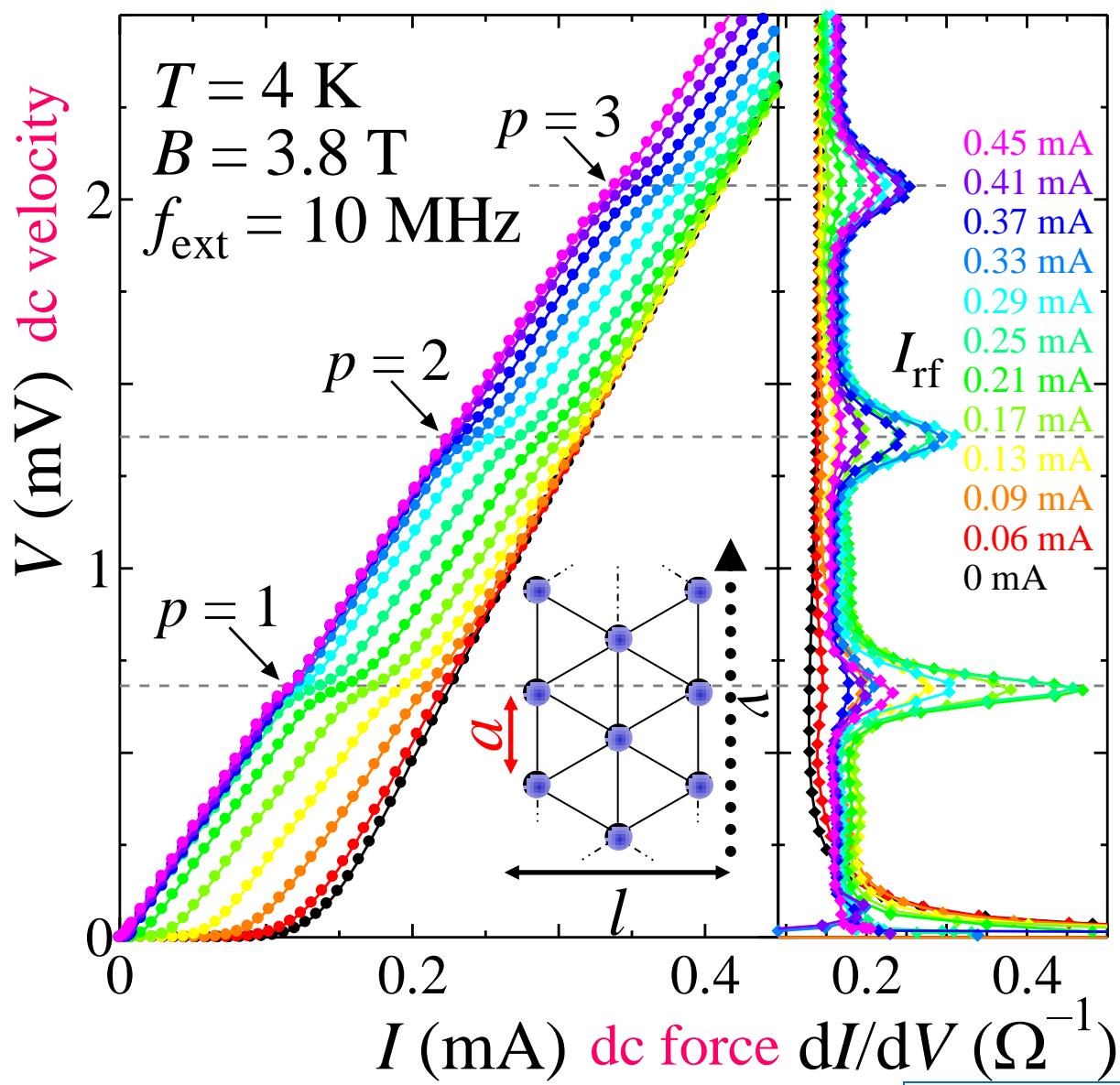
A. B. Kolton, D. Domínguez,
N. G. Jensen



$T = 1.36$ K, $H = 80$ G, $f = 96$ MHz

A. T. Fiory, PRL 27, 501 (1971)

ML steps in I - V curves



Plastic flow of solids
-Rotating vortex matter in CD

SUPERCONDUCTORS

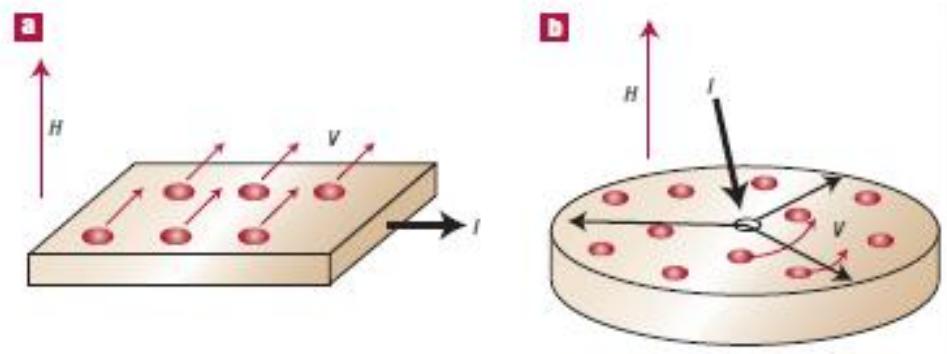
The mysteries of plastic motion

Understanding plastic motion of solids — in which atoms change their neighbours as they move — is complicated because it is discontinuous and does not conserve energy. An elegant study of vortex dynamics in superconductors provides new insights.

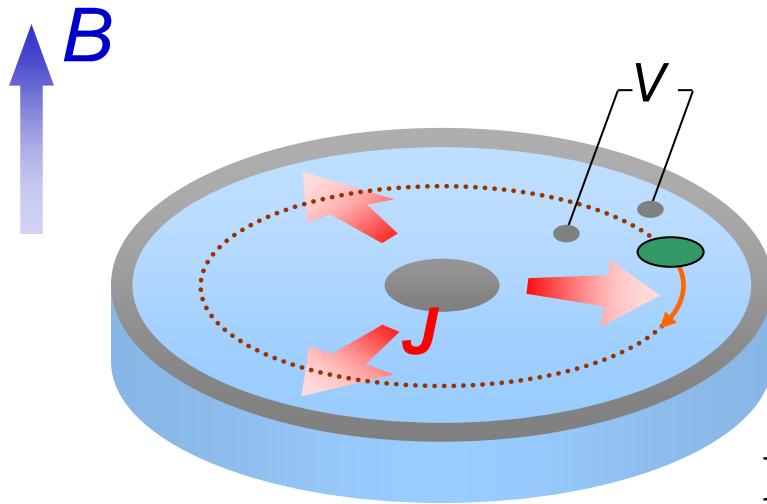
GEORGE W. CRABTREE is at the Materials Science Division, Argonne National Laboratory, 9700 South Cass Avenue, Argonne, Illinois 60439, USA.

e-mail: crabtree@anl.gov

Plastic motion of solids governs many processes in our physical world. On geological timescales, plastic motion is responsible for the topography of the landmasses of the Earth, for the drift of the continents, and for the regeneration of the Earth's crust from sources at the mid-ocean ridges. On shorter time scales, plastic motion produces cataclysmic events such



r dependence of velocity v (or V) in CD



$$J = \frac{I}{2\pi t} \frac{1}{r}$$

Frustrated Lorentz force
inversely proportional to r

SO, S. Morishima, M. Kamada, PRB 76, 224521 (2007)

$$v \propto r$$

($\omega = \text{const}$)

Elastic (rigid-disk-like)
rotation

$$v \propto 1/r$$

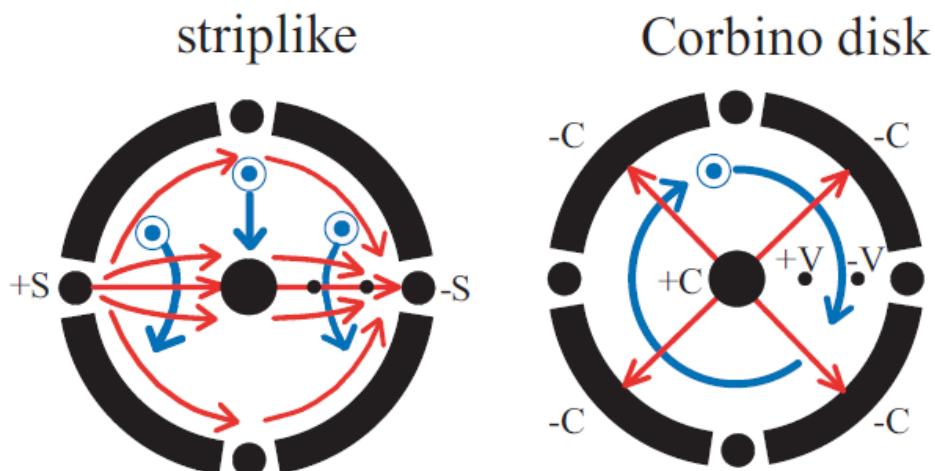
Liquid-like
rotation

Experiment

◆ Sample

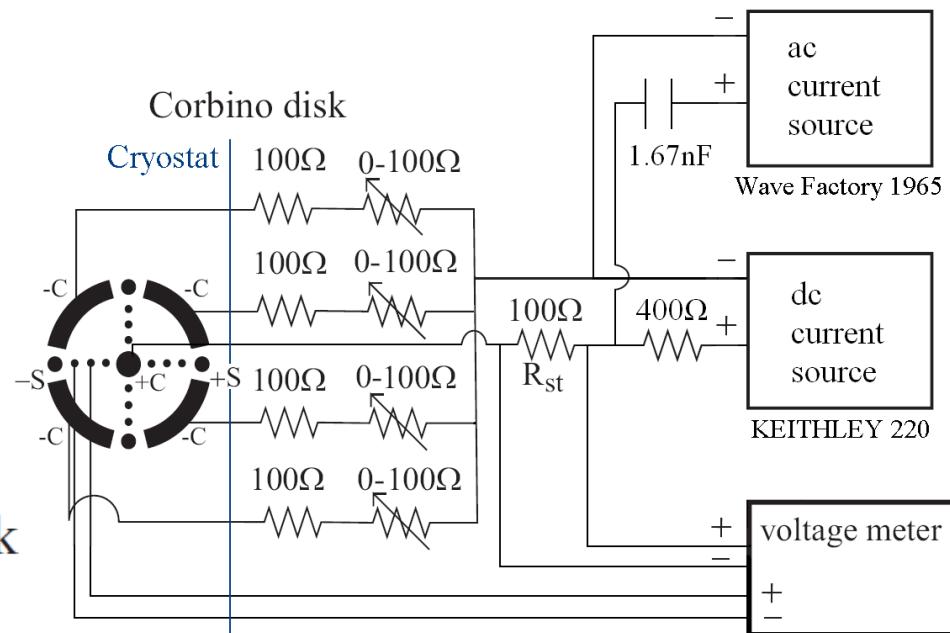
$a\text{-Mo}_x\text{Ge}_{1-x}$ film (CD)

- Thickness 330 nm
- x 0.78
- T_{c0} 6.3 K
- ρ_n $2.2 \mu\Omega\text{m}$
- Inner radius 0.8 mm

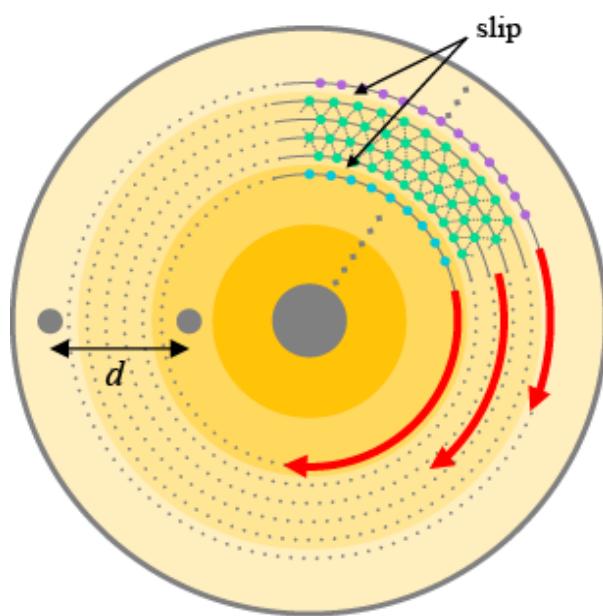
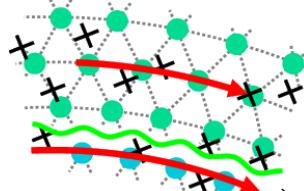
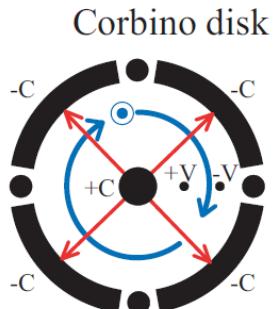


◆ Measurement

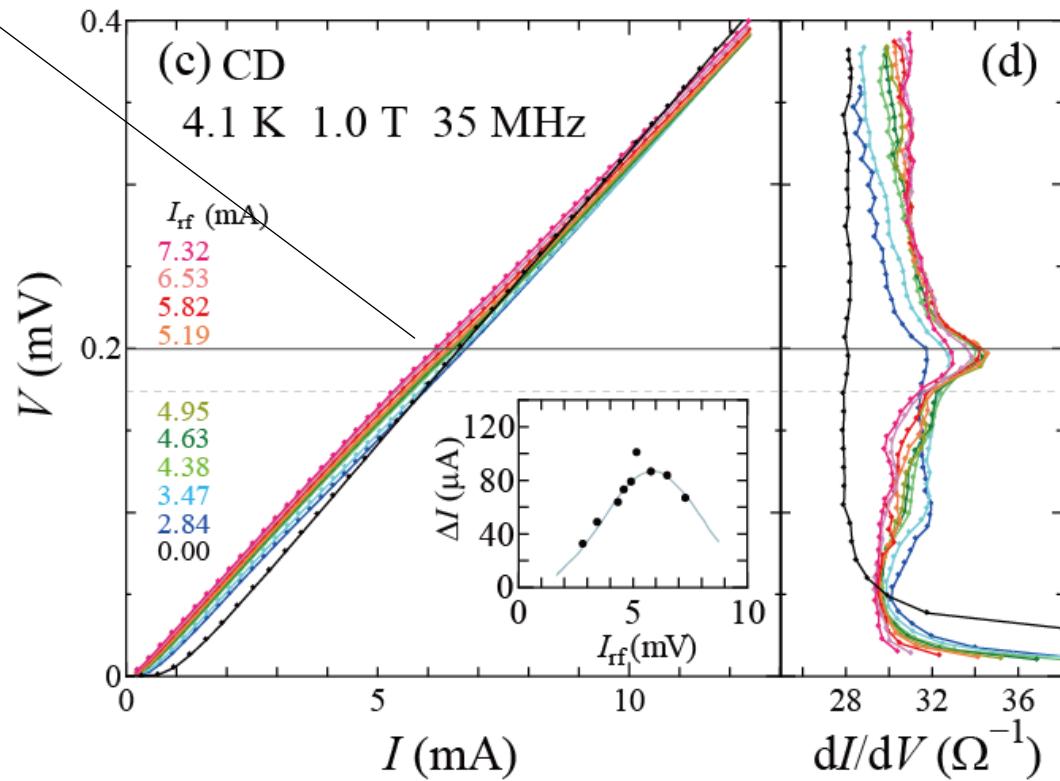
dc I - V with four-terminal method

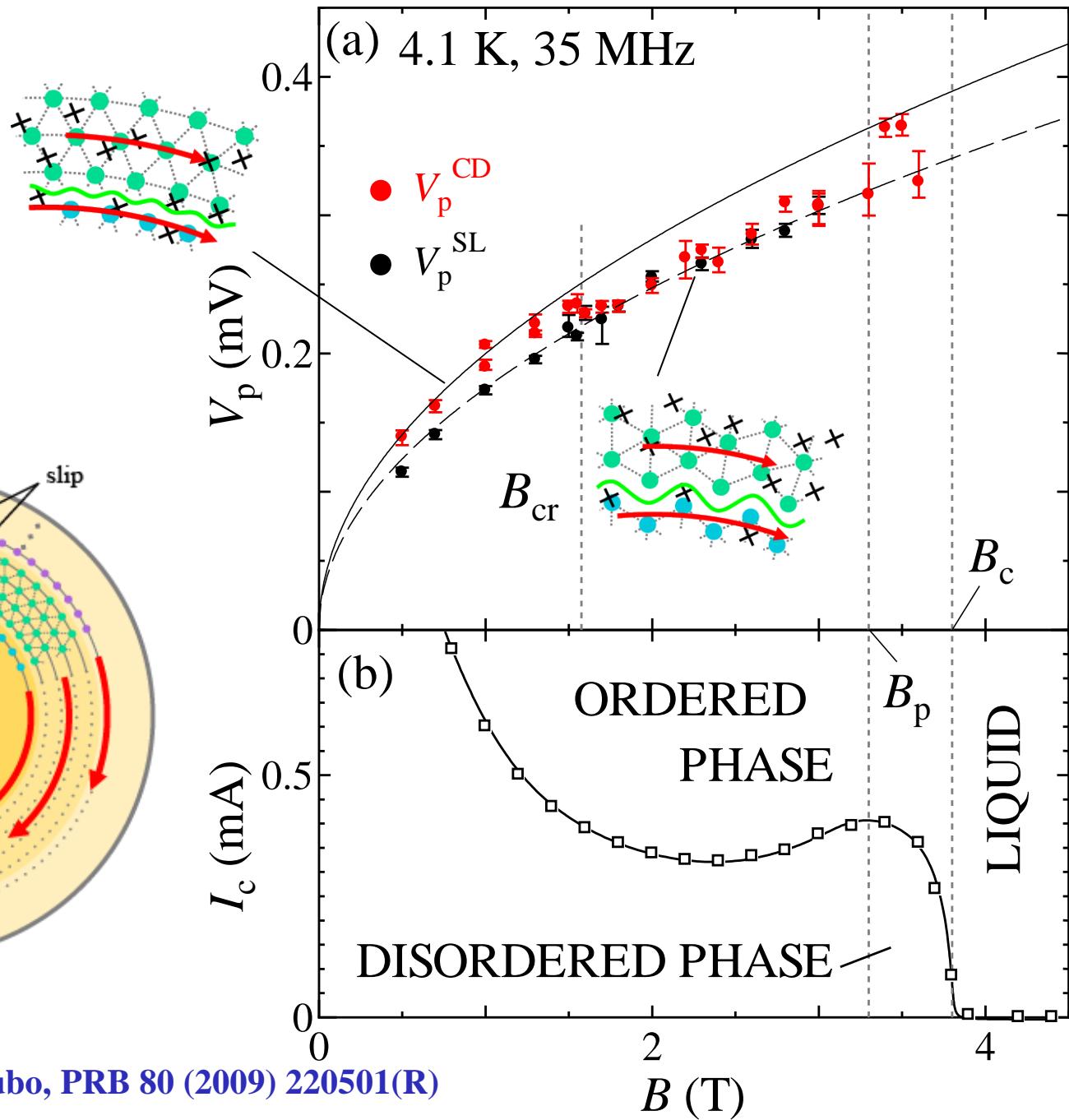
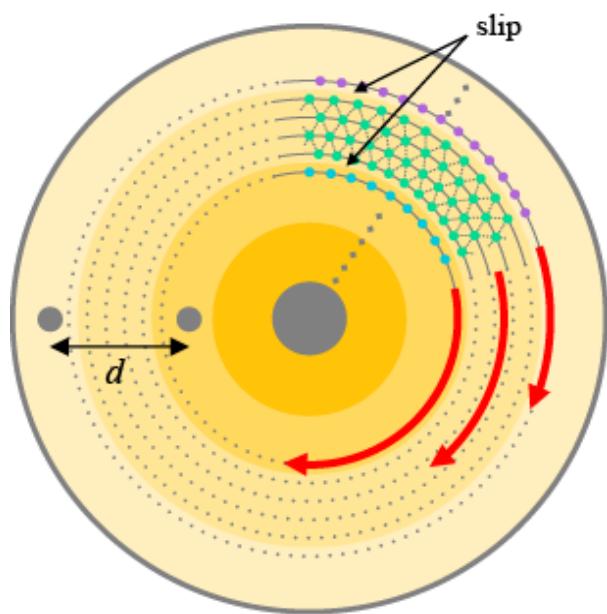
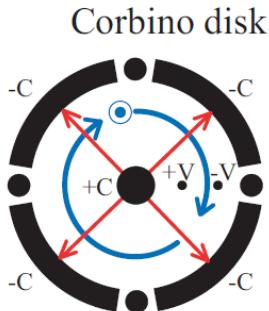


Observation of rotating lattice rings



ML resonance

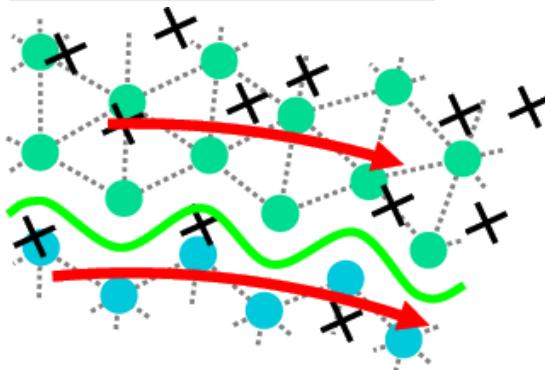




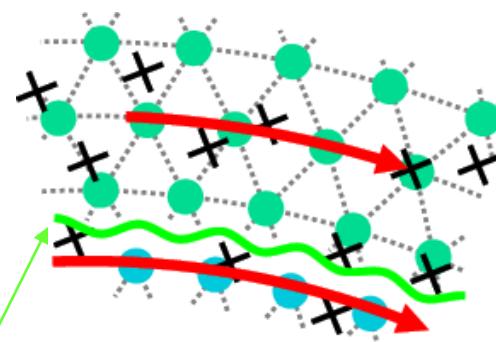
Change in lattice orientation of rotating rings at low B

Slip between adjacent rings

High B (perp.)

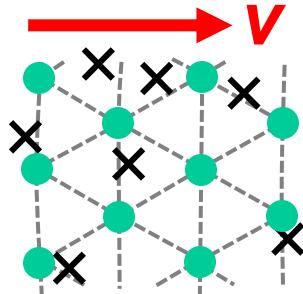


Low B (para.)



cf. Strip(like)

Any B measured
(perp.)

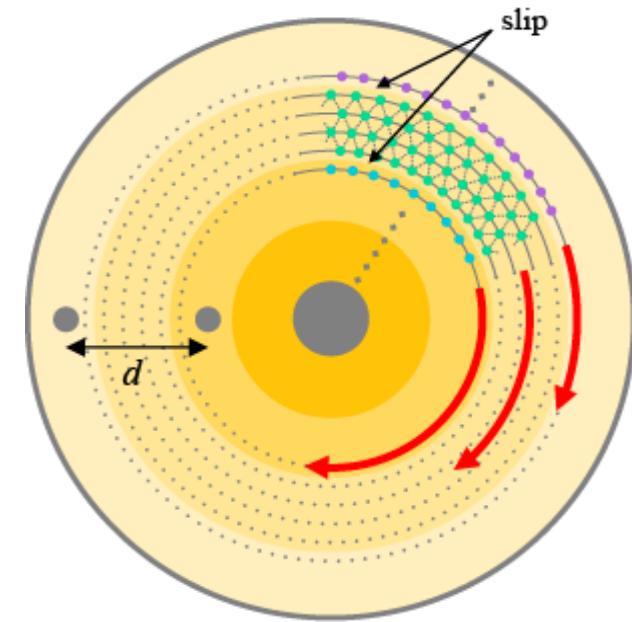


Change in lattice orientation at B^* ($\sim 0.3B_{c2}$)
may be due to the **change in elasticity** of
vortex arrays

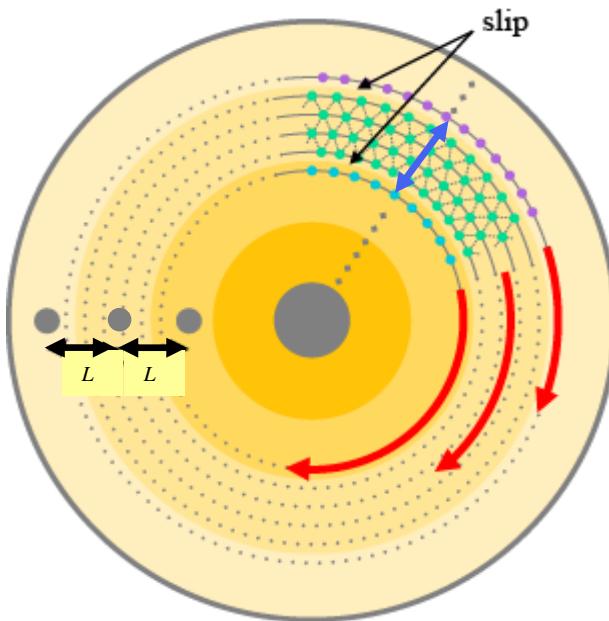
SO, Y. Yamazaki, N. Kokubo, PRB 80 (2009) 220501(R)

Simulation: Unusual vortex dynamics in Meso-CD

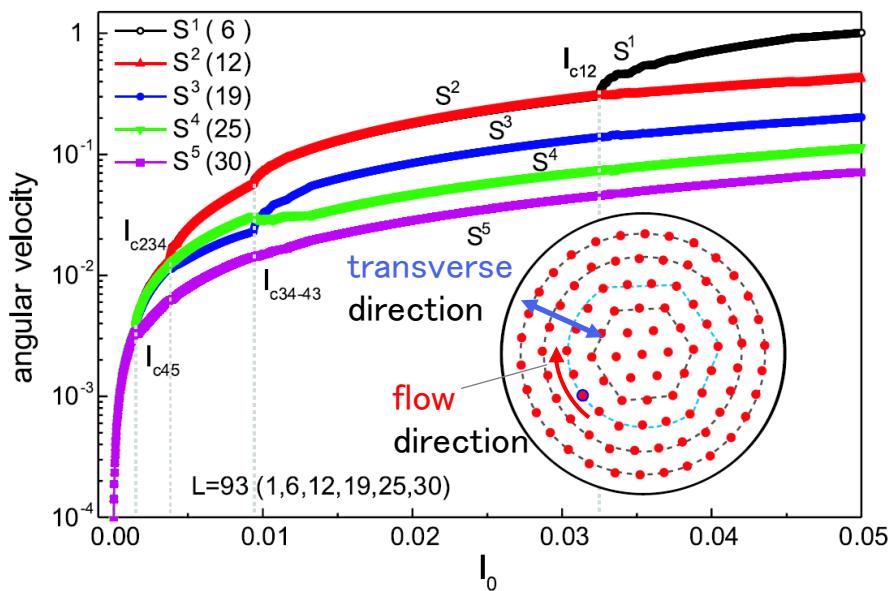
N.S. Lin, V.R. Misko, F.M. Peeters, PRL 102, 197003 (2009)



ML in CD can detect
→ coherence in the **flow** direction O
but cannot detect
coherence in the **transverse (radial)** direction X



Unconventional vortex dynamics in meso-size CD

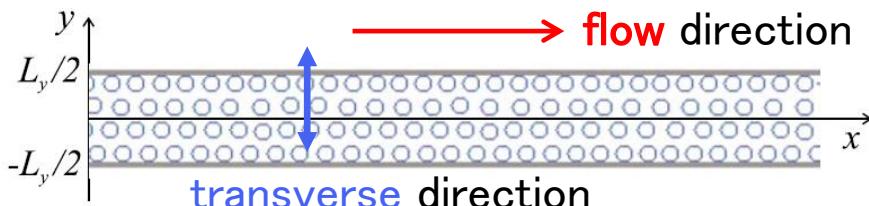


simulation

Inversion of shell velocities with respect to gradient driving force and angular melting propagating from shear minimum to center

N.S. Lin, V.R. Misko, F.M. Peeters, PRL 102, 197003 (2009)

Dynamics of colloids in a narrow channel driven by nonuniform force



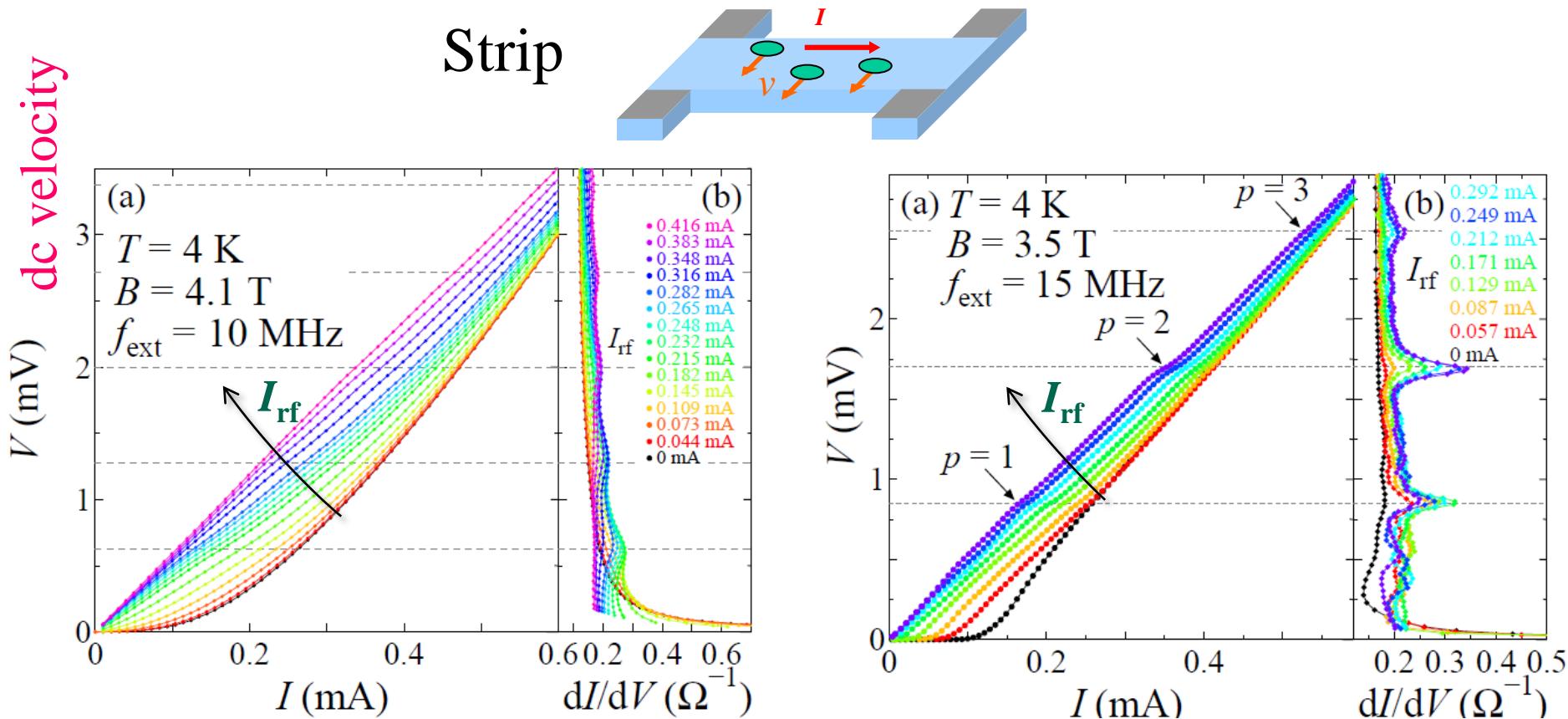
simulation

Shear-induced melting and onset of plasticity near the boundaries.

D. V. Tkachenko, V. R. Misko, and F. M. Peeters, PRB 80, 051401 (2009)

Unusual dc I - V characteristics
superimposed with ac I_{rf} in CD

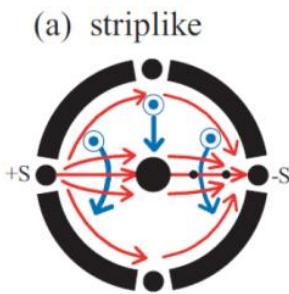
Dc I - V superimposed with I_{rf} in strip samples



I_{rf} -induced increase in $V(I) \rightarrow$ **Reduced pinning effects by increased I_{rf}** , leading to an **increase in dc velocity (V)**.

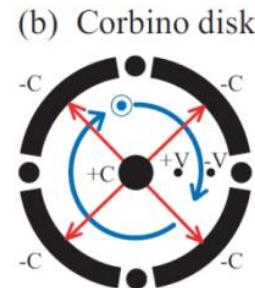
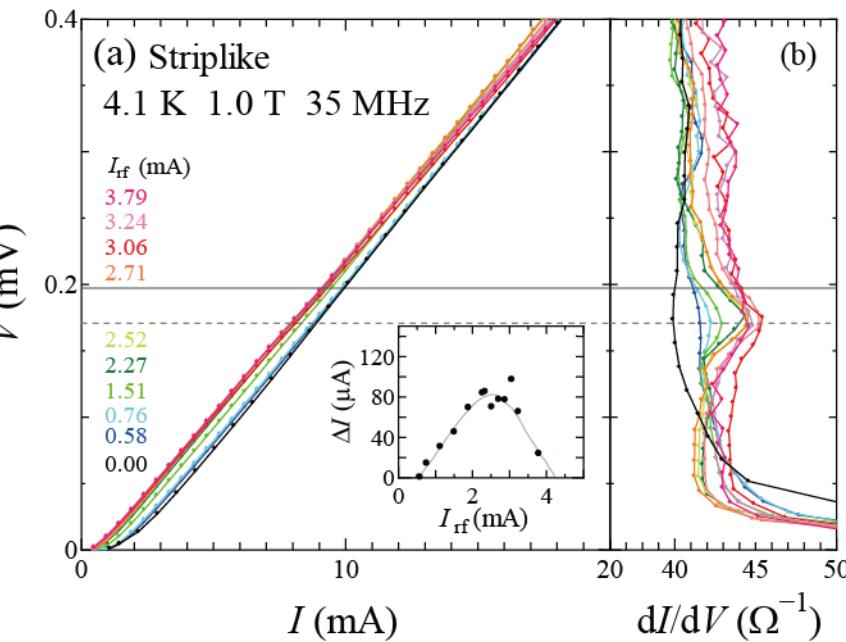
Unusual I - V superimposed with I_{rf} in CD

$f_{\text{rf}} = 35 \text{ MHz}$, $B = 1 \text{ T}$



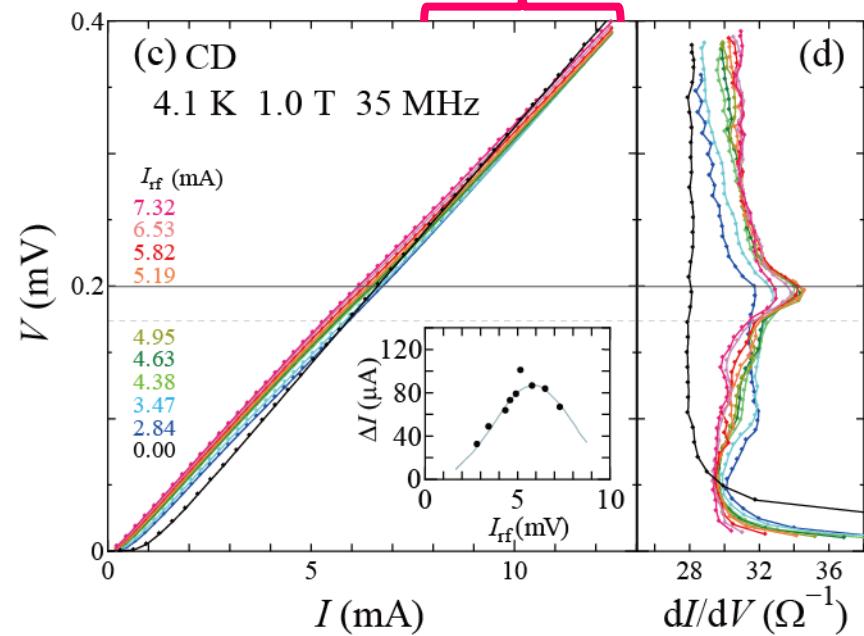
Striplike

I_{rf} -induced
increase in $V(I)$

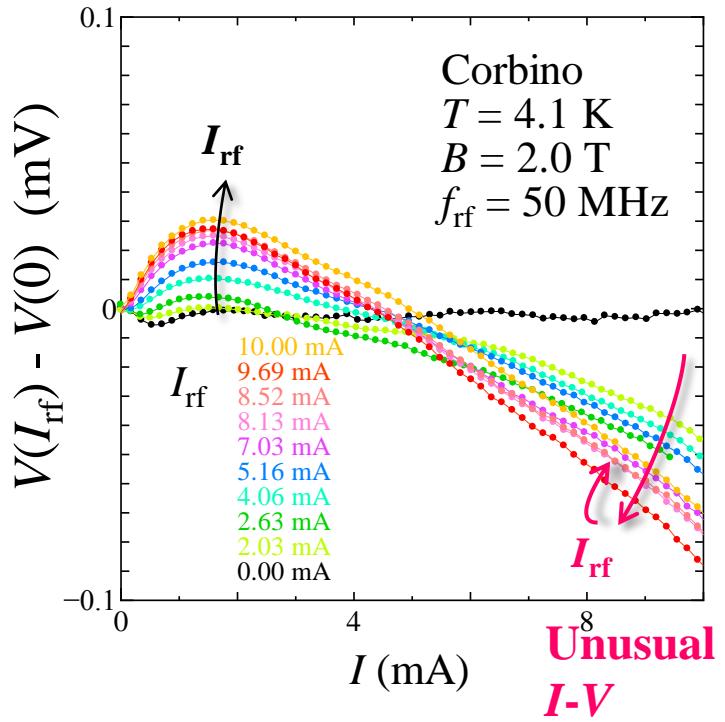
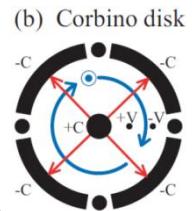
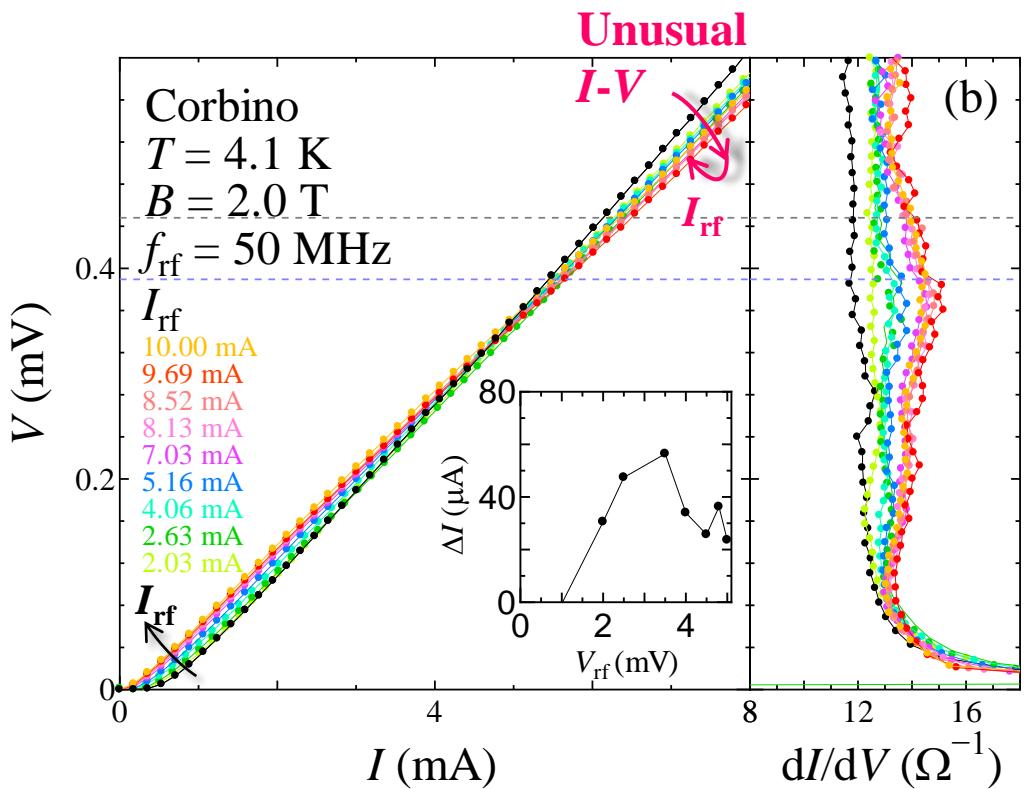


CD

Unusual decrease of
 $V(I)$ with increasing I_{rf}
for large I .

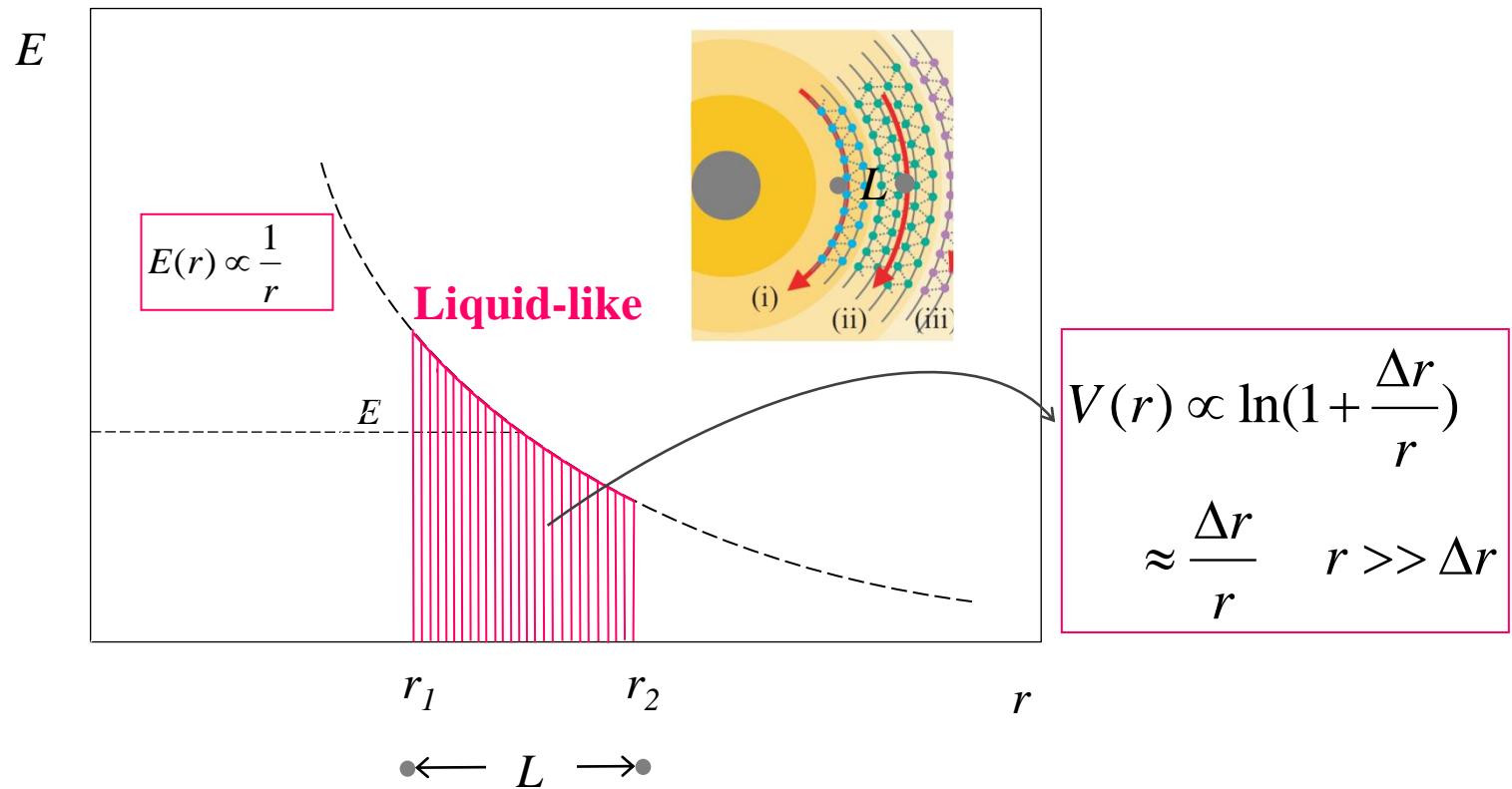


$f_{\text{rf}} = 50 \text{ MHz}, B = 2 \text{ T}$



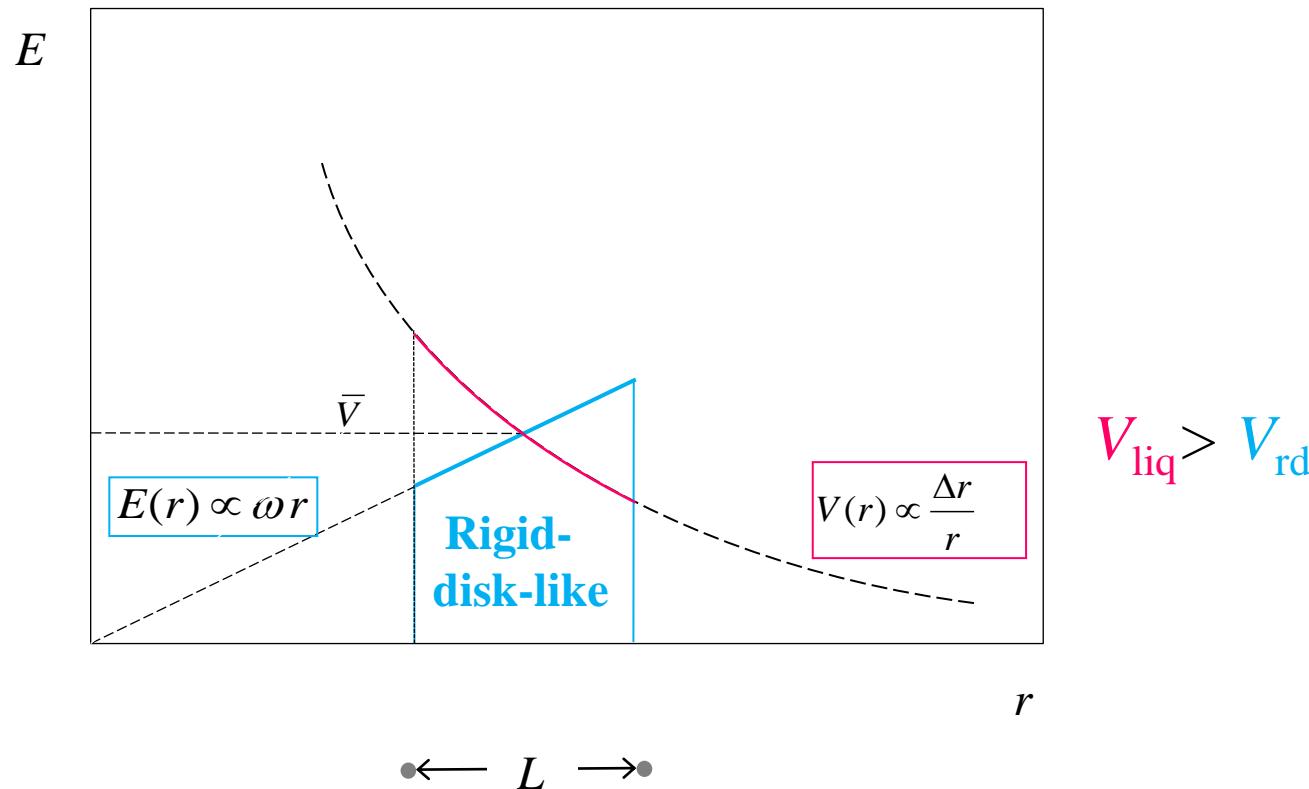
Unusual decrease of I - V curves with increasing I_{rf} is also observed at higher f_{rf} and more pronounced.

Explanation: V generated by rotating lattice rings with different width

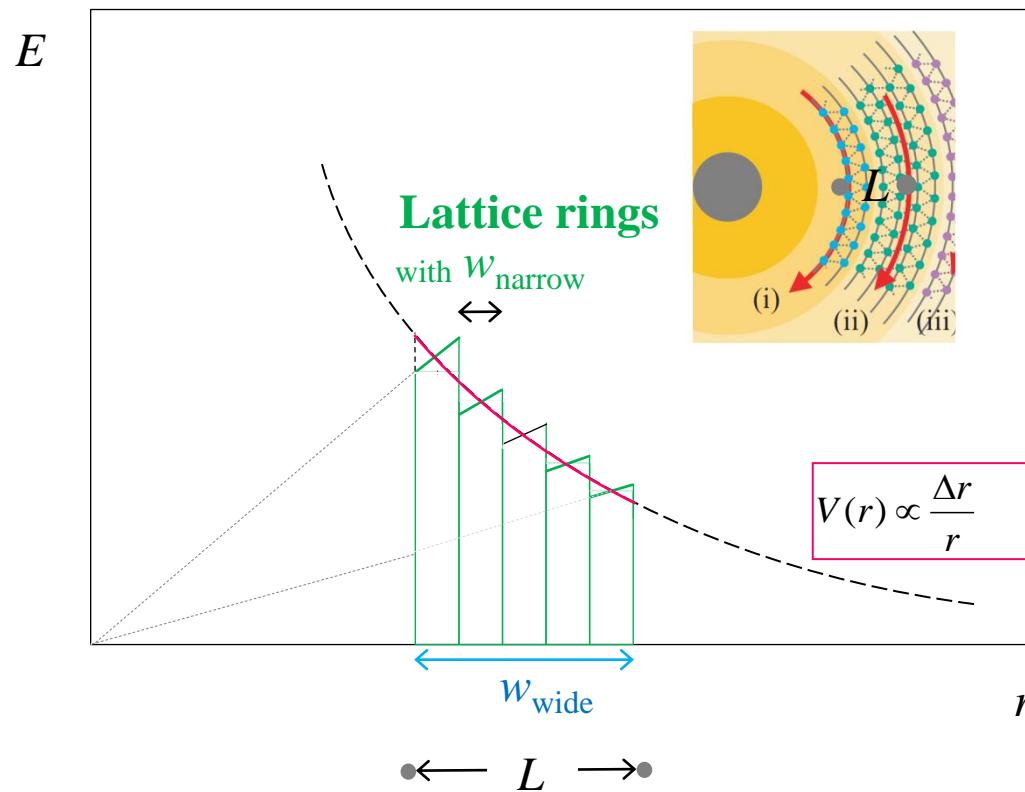


For liquid-like rotation, $E \propto 1/r$

Explanation: V generated by rotating lattice rings with different width



Explanation: V generated by rotating lattice rings with different width



$$V_{\text{liq}} > V_{\text{nar}} > V_{\text{wide}}$$

Wider rings generate smaller $V \rightarrow$

I_{rf} -induced decrease of I - V curves is attributed to growth of w , which occurs associated with enhanced ML

I_{rf} -induced growth in lattice-ring width

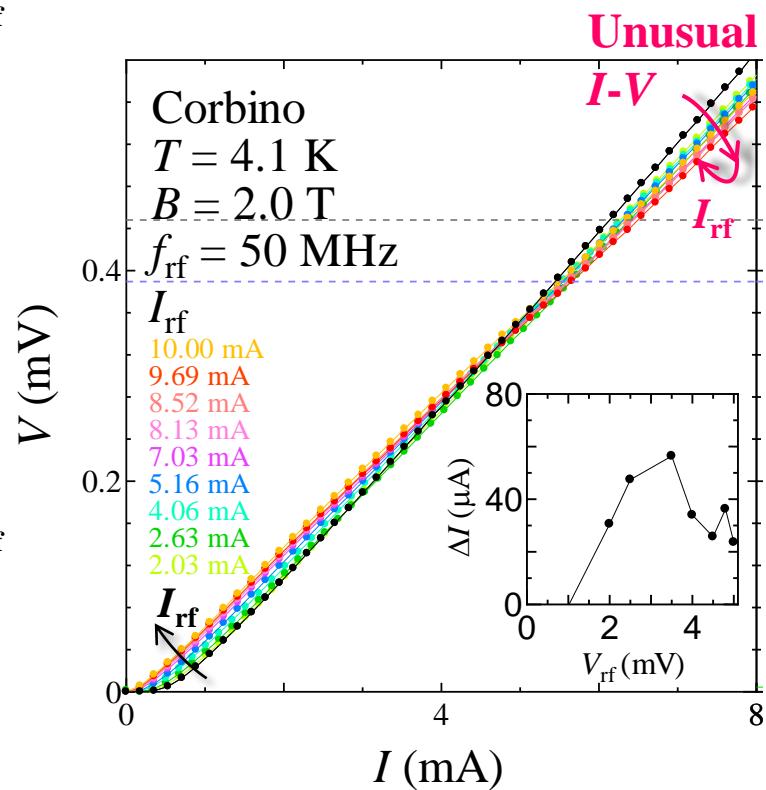
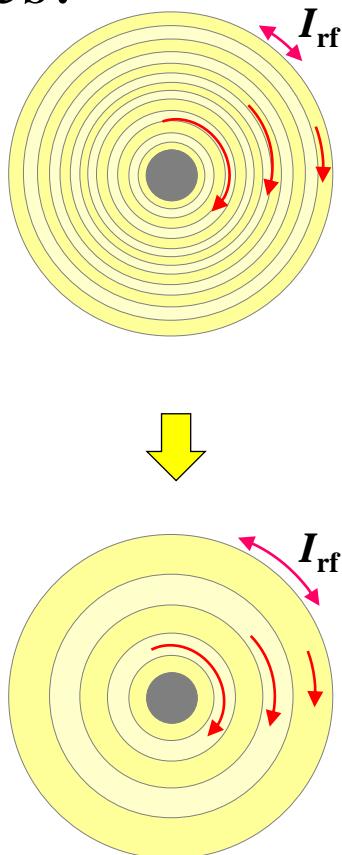
As ac force (I_{rf}) increases:

- effective **pinning**
(i.e., local shear)
and
 - **dislocation** number
decrease
- ⇒
- **healing** of lattice
 - enhanced ML



increase in:

- **transverse correlation**
- **width** of lattice rings



Summary 1

- We measure I - V and ML for vortex-lattice rings rotated by dc I superimposed with ac I_{rf} of different amplitudes in CD.
- As I_{rf} is increased from zero, **ML becomes more pronounced and the I - V curve in the large I region decreases.**
- This is **opposite to the usual behavior of vortex flow, in which I_{rf} -induced depinning leads to an increase in the flow voltage.**
- The result is explained in terms of the **I_{rf} -induced growth in the width of the rotating lattice rings**

(1) *Dynamics of moving lattices*

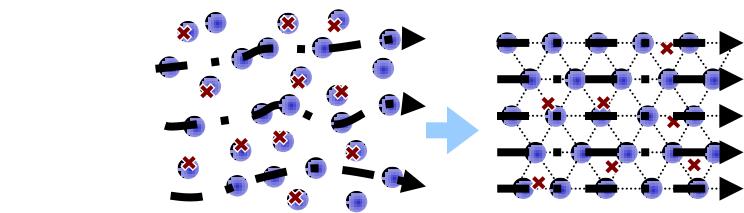
Dynamic ordering of driven vortices

- lattice orientation, non-equilibrium SC

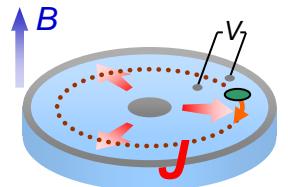
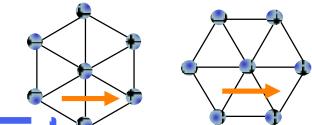
Dynamic melting of driven lattices

- intrinsic (quantum) melting

Plastic flow of solids



dc+ac



Fast

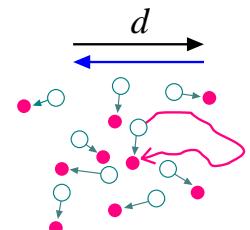
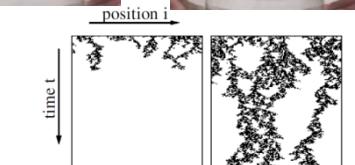
(2) *Dynamics of non-equilibrium many particles*

Novel dynamic transitions

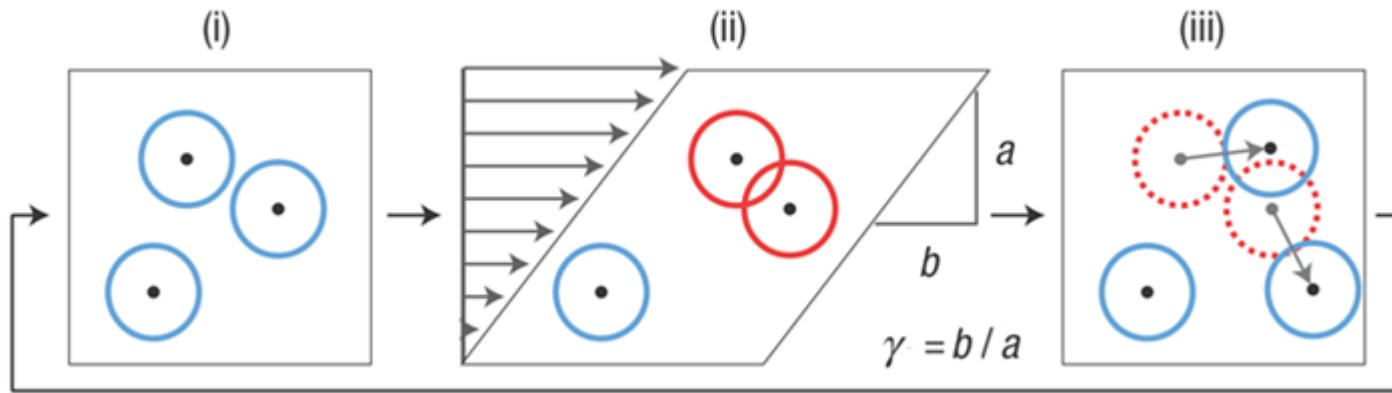
- ➡ - rev-irreversible tr. and random organization
- absorbing tr.
- depinning tr.

dc

Slow



Dynamics of many particles subject to periodic shear



γ : shear amplitude

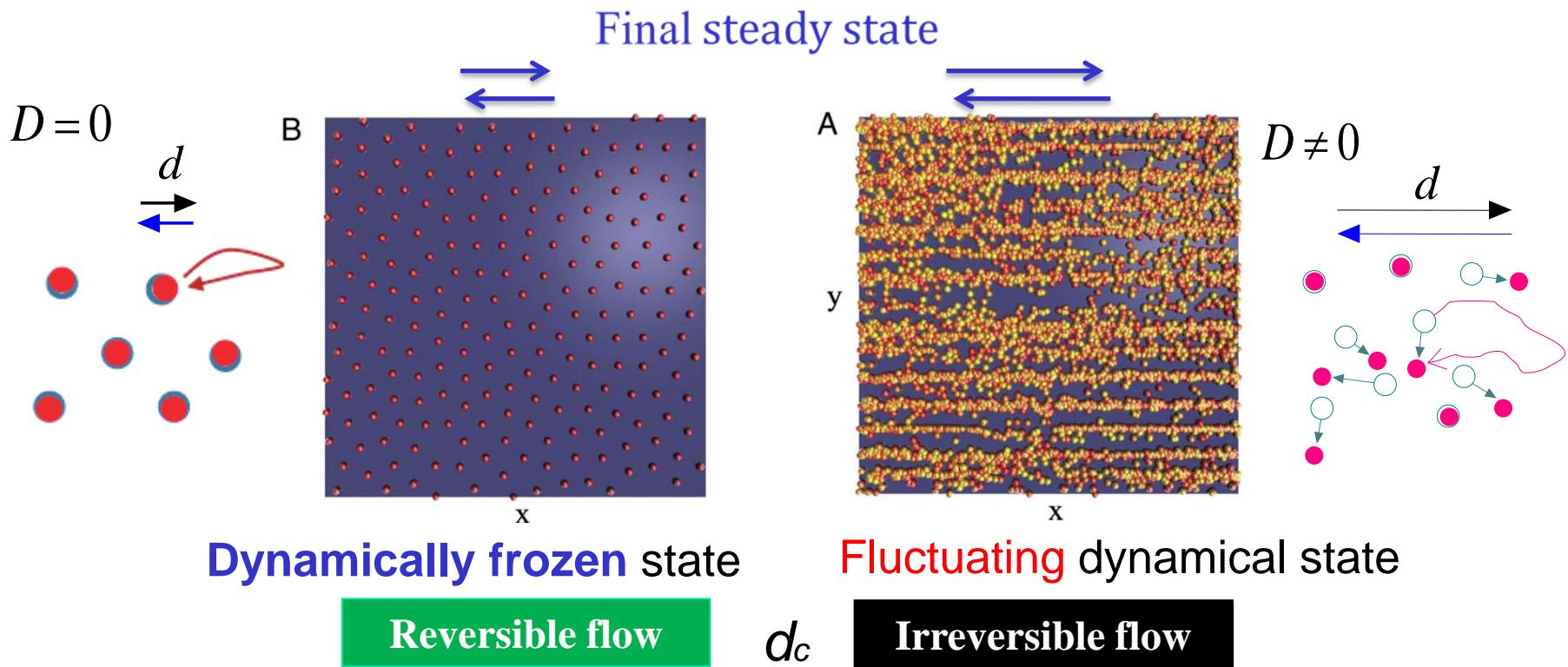
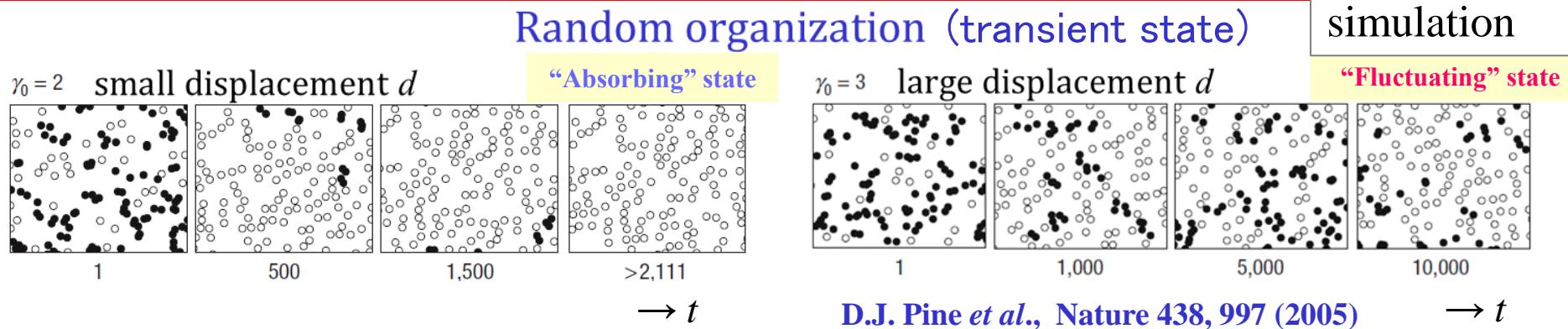
Application of periodic shear



Collided particles move in the random direction
with small distance

L. Corte *et al.*, Nat. Phys. **4**, 420 (2008)

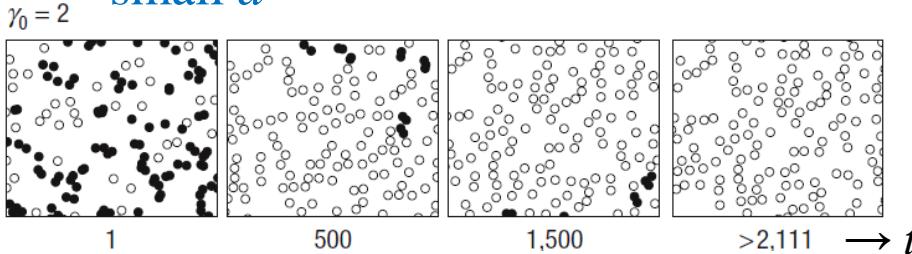
Random organization and Reversible-Irreversible Transition



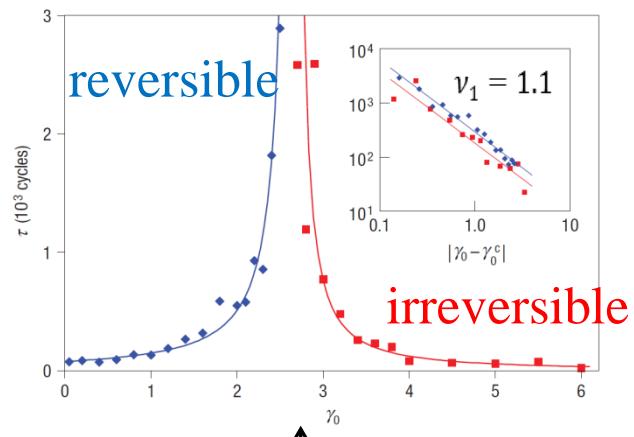
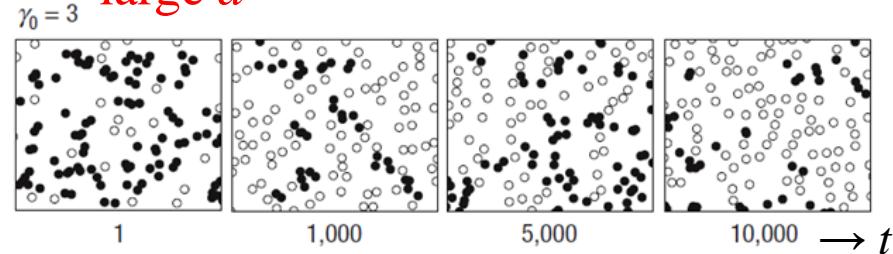
Critical behavior of RIT

simulation

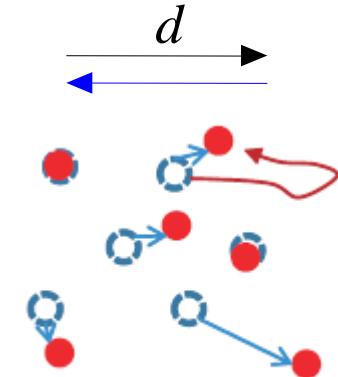
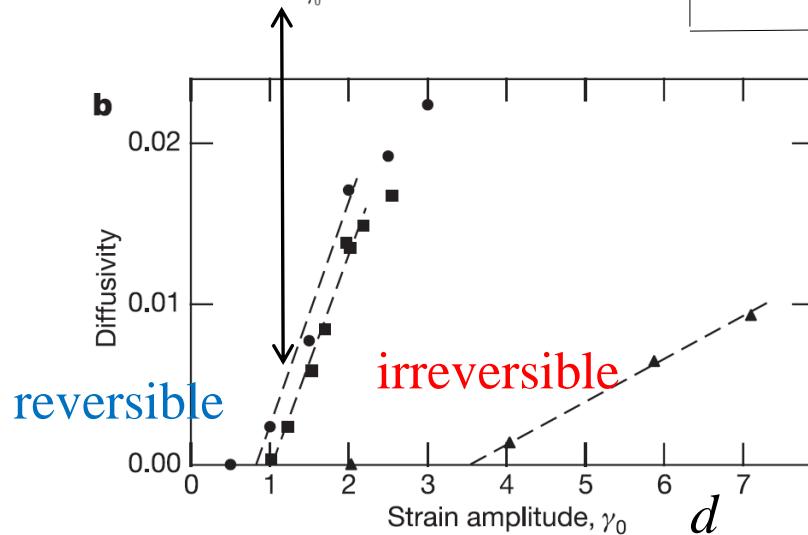
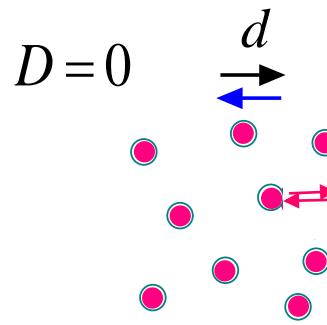
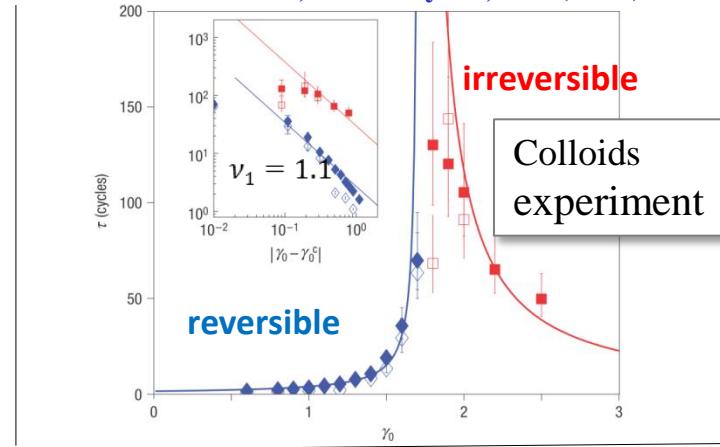
small d



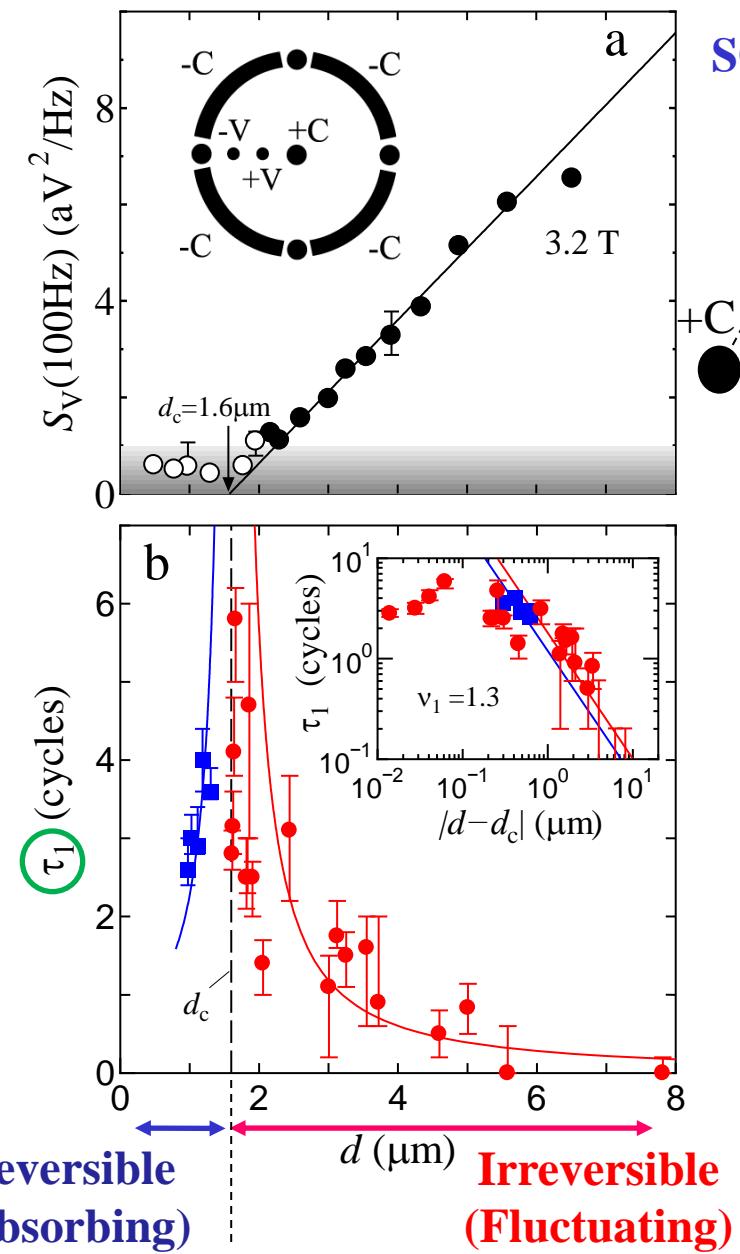
large d



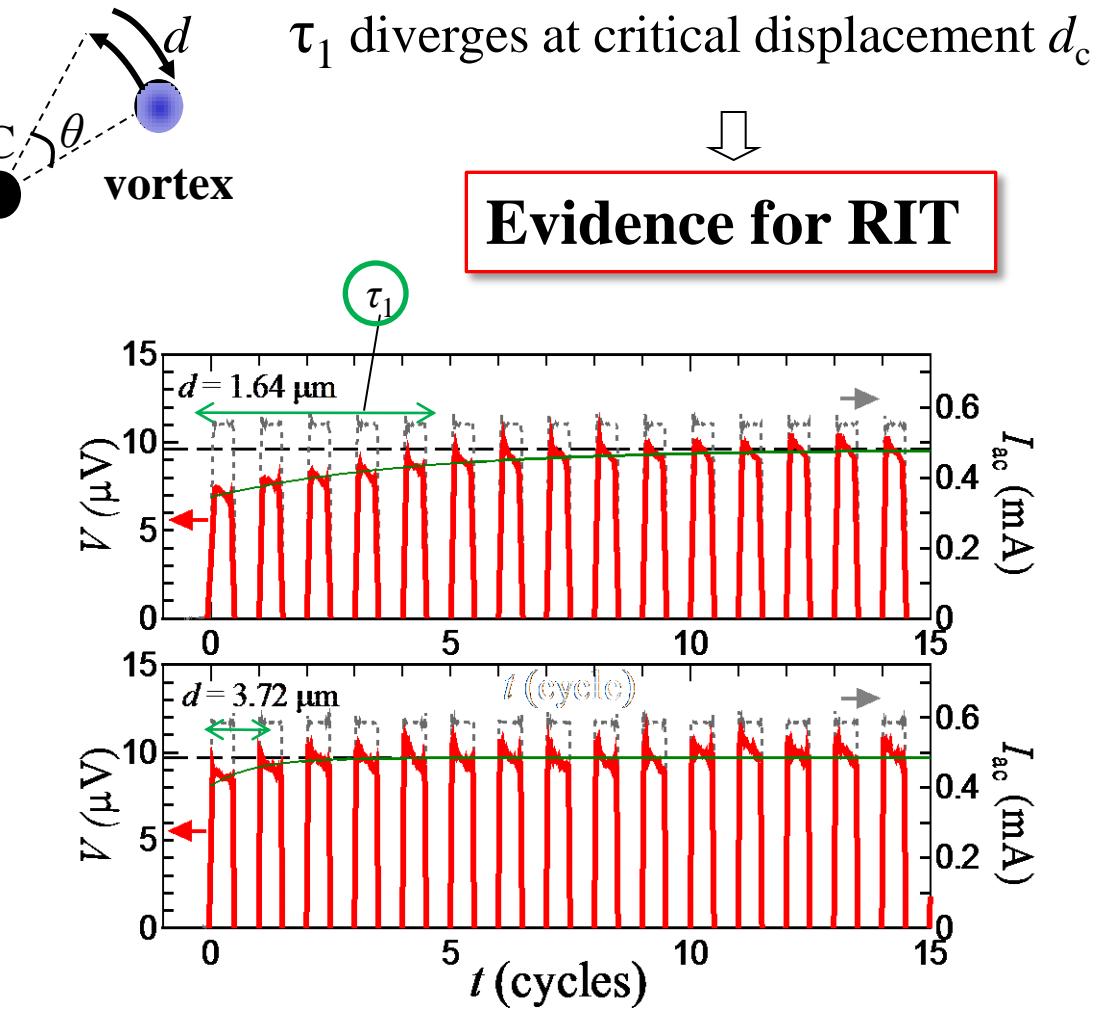
L. Corte et al., Nat. Phys. 4, 420 (2008)



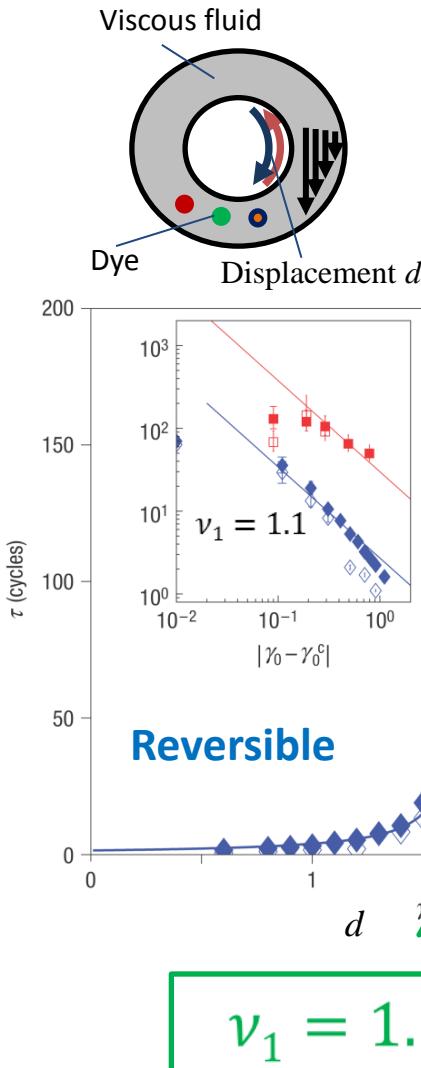
Random organization and RIT: Vortices CD experiment



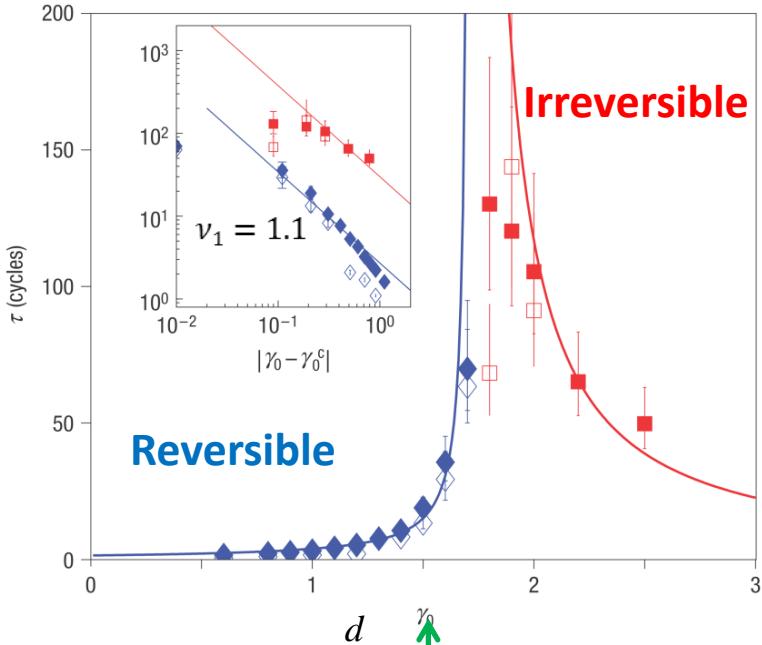
SO, Y. Tsugawa, A. Motohashi, PRB 83 (2011) 012503



Colloids experiment



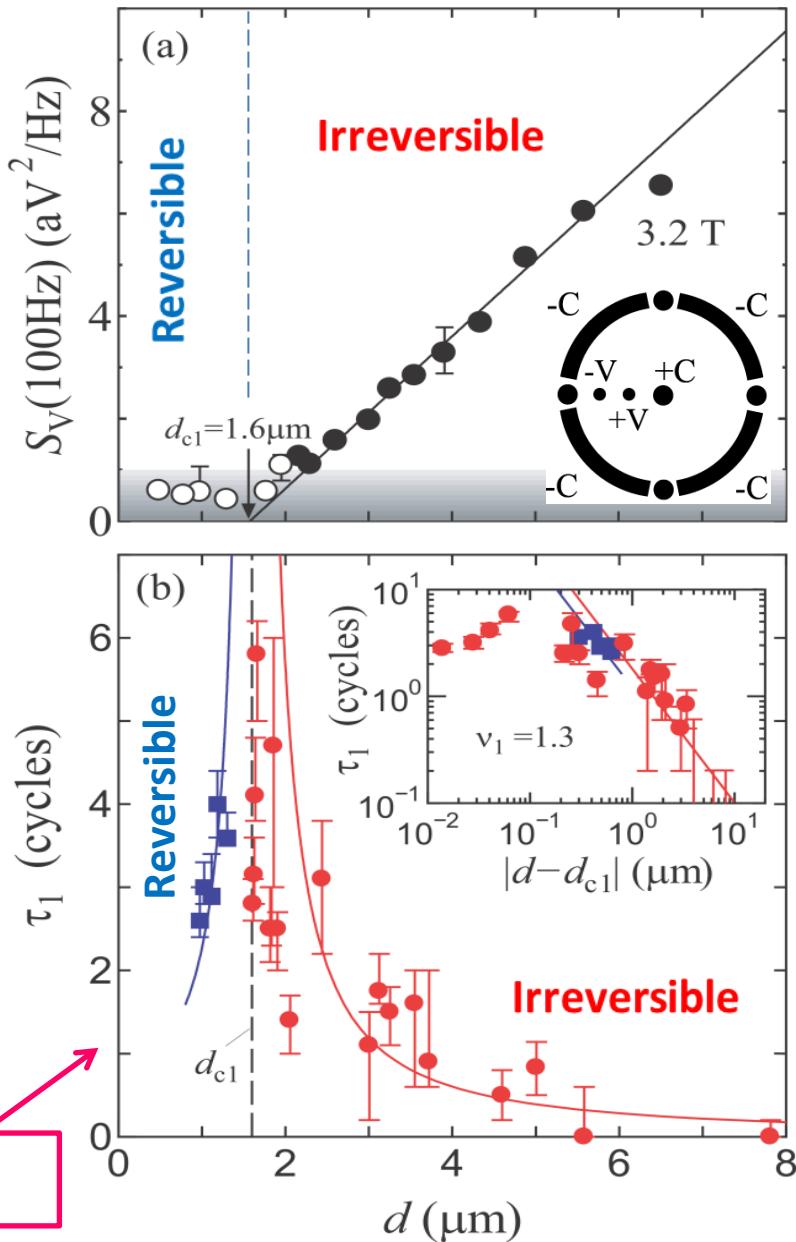
L. Corte *et al.*, Nat. Phys. 4, 420 (2008)



$$\nu_1 = 1.1 \quad (3D)$$

$\nu_1 = 1.3$ (2D)

Vortices experiment



Absorbing tr. Experiment

Random Fields at a Nonequilibrium Phase Transition

Hatem Barghathi and Thomas Vojta

Department of Physics, Missouri University of Science and Technology, Rolla, Missouri 65409, USA

(Received 19 June 2012; published 26 October 2012)

Finally, we turn to experiments. Although clear-cut realizations of absorbing state transitions were lacking for a long time [34], beautiful examples were recently found in turbulent liquid crystals [35], driven suspensions [36,37], and superconducting vortices [38].

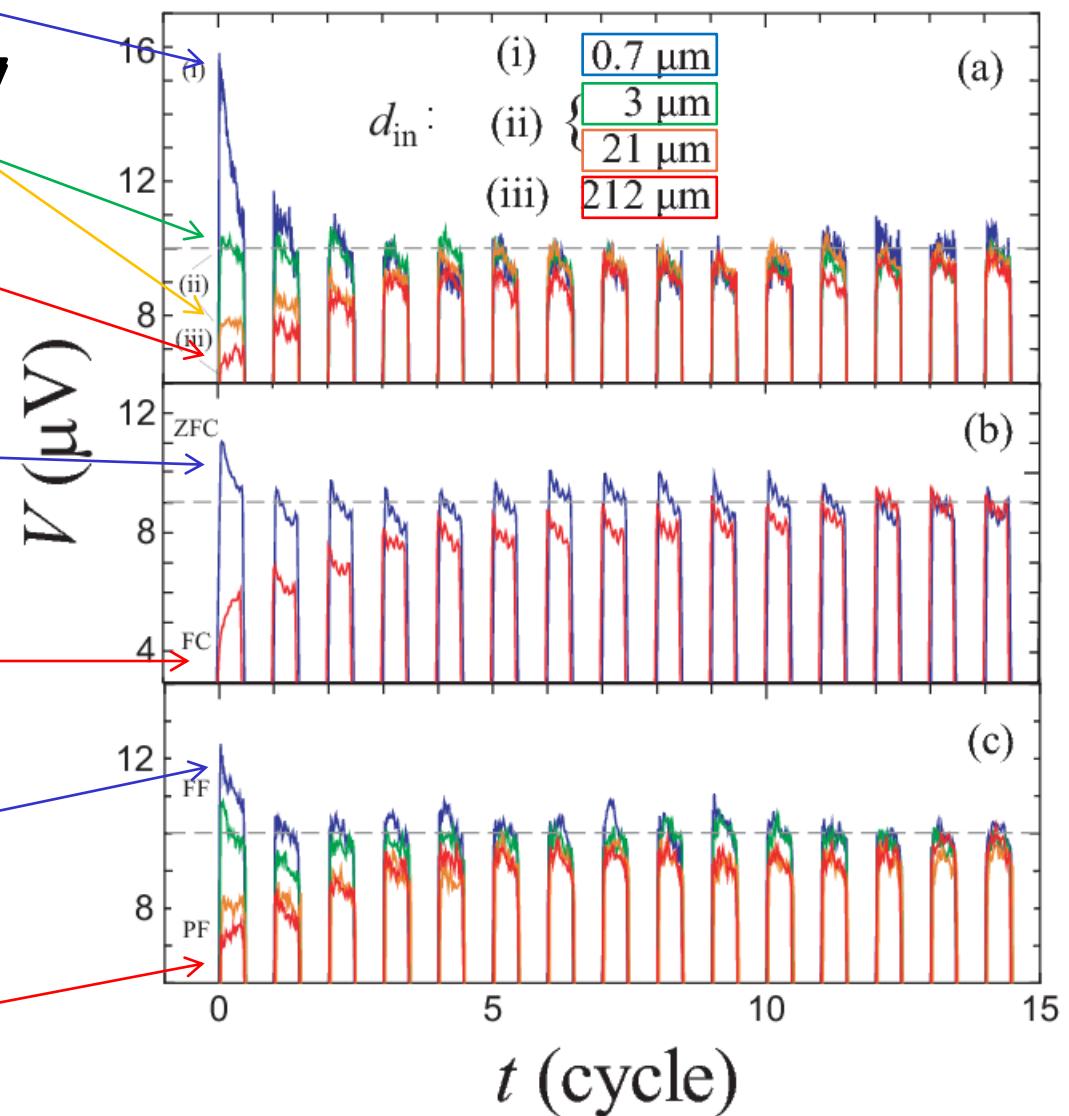
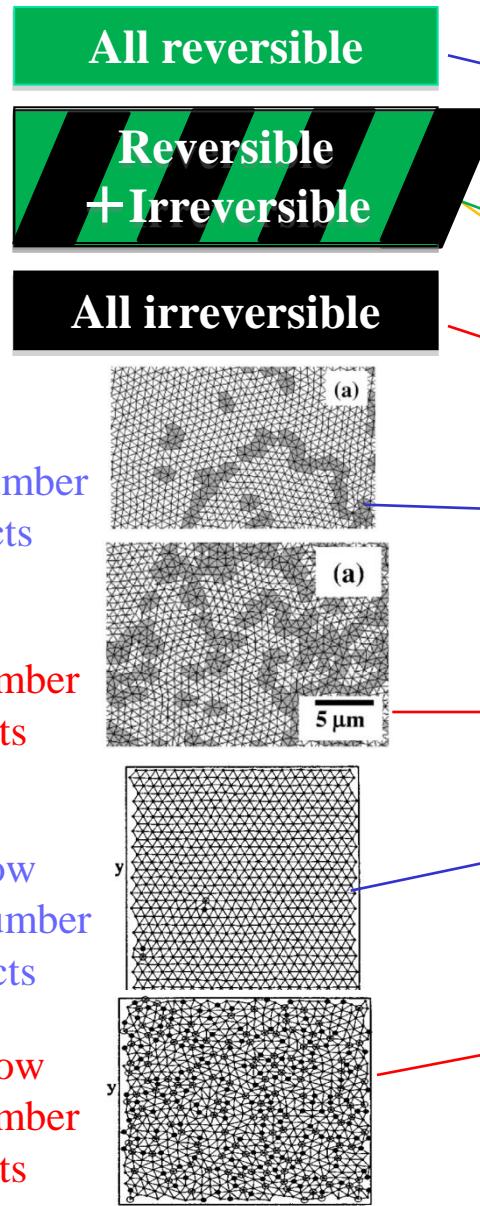
- [35] K. A. Takeuchi, M. Kuroda, H. Chate, and M. Sano, Phys. Rev. Lett. **99**, 234503 (2007).
- [36] L. Corte, P. M. Chaikin, J. P. Gollub, and D. J. Pine, Nat. Phys. **4**, 420 (2008).
- [37] A. Franceschini, E. Filippidi, E. Guazzelli, and D. J. Pine, Phys. Rev. Lett. **107**, 250603 (2011).
- [38] S. Okuma, Y. Tsugawa, and A. Motohashi, Phys. Rev. B **83**, 012503 (2011).

liquid
crystal

colloid

vortex

Vortex configurations in rev. and irrev. states



Y. Fasano *et al.*, PRB **66**, 020512 (2002)
C. J. Olson, C. Reichhardt, F. Nori, PRL **81**, 3757 (1998)

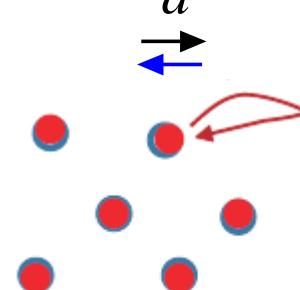
SO, Y. Kawamura, Y. Tsugawa, JPSJ **81**, 114718 (2012)
Y. Kawamura, SO, JPS Conf. Proc. **4** (2015) 011007.

Possible vortex configurations of the reversible flow state

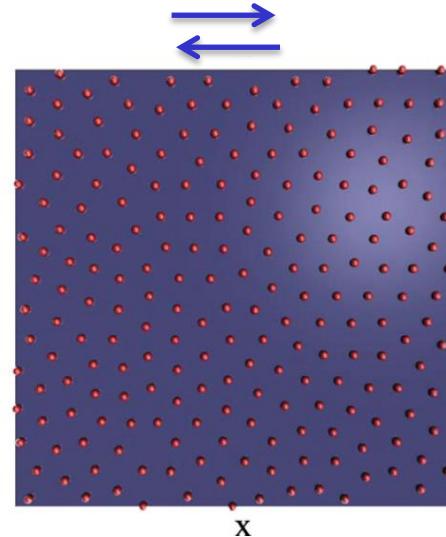


Our experiment

$$D = 0$$



B



Abrikosov lattice



Reversible flow

Dynamically frozen state

Reversible flow

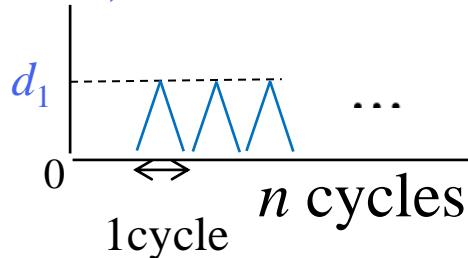
Simulation:

C. Reichhardt, C.J.O. Reichhardt, PNAS 108, 19099 (2011)

Memory effect of ac drive d in particle configurations (simulation)

Trial amplitude

d_1 (=fixed)

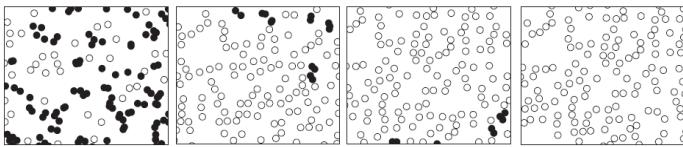


Readout
amplitude d

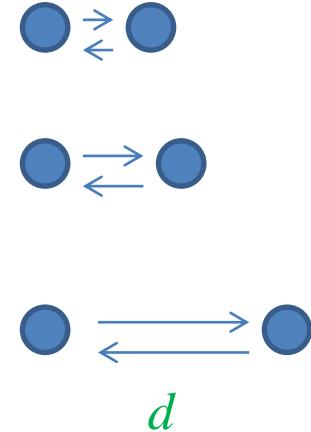


Number of cycles

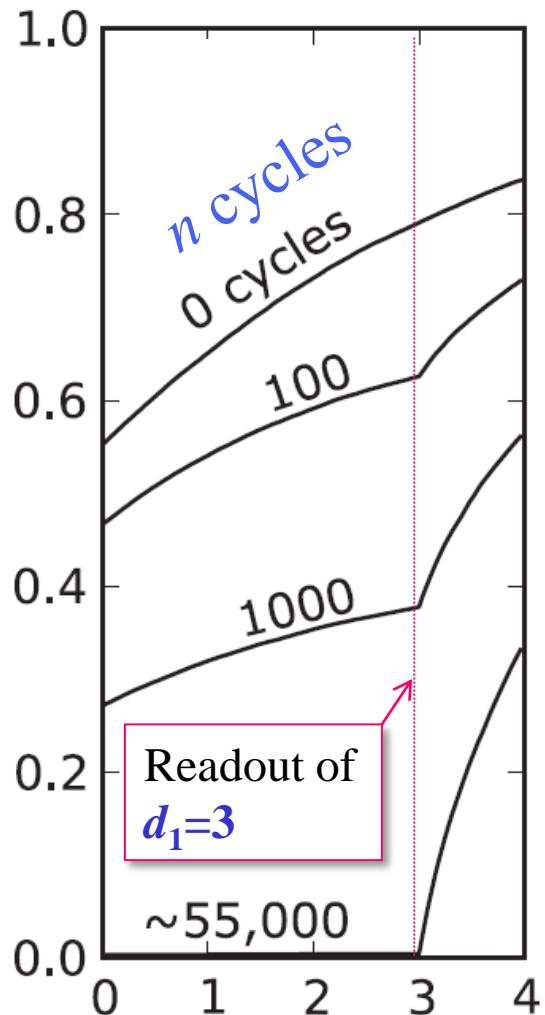
$n=1, \quad 100, \quad 1000, \quad 55,000$



$d_1=3=\text{fixed}$



Number of collided particles



Readout amplitude d

Memory effect of ac drive in the vortex configuration

(experiment)

Sorry, unpublished data

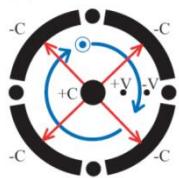
$a_1 = 5.0 \mu\text{m}$

Readout of $d_1=3 \mu\text{m}$

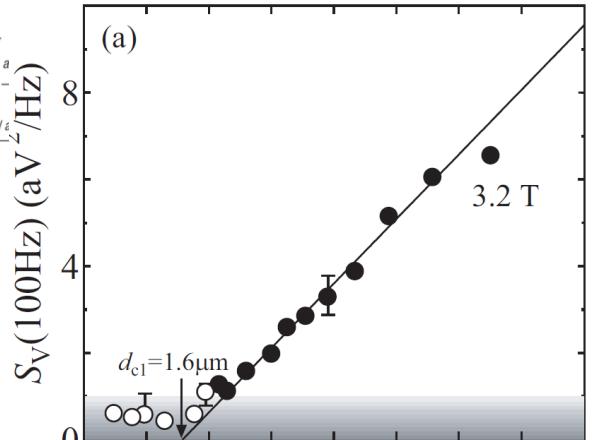
$d (\mu\text{m})$

RIT under local shear
and
RIT in the moving frame
with a constant velocity?

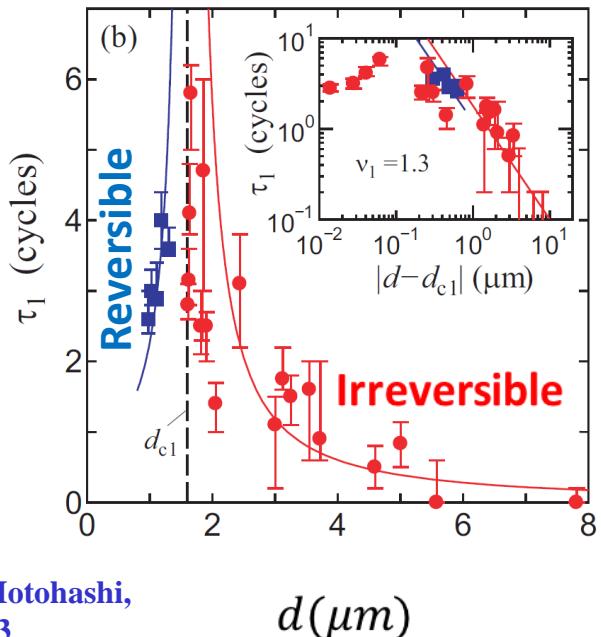
Vortices experiment on RIT (ac drive)



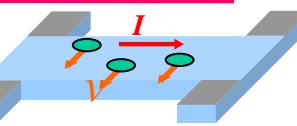
CD: strong *global* shear
weak pinning



$\nu_1 = 1.3$



Strip: weak *local* shear
stronger pinning

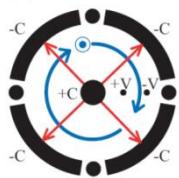


Simulation → RIT Yes

N. Mangan, C. Reichhardt, C. J. Olson Reichhardt,
PRL 100, 187002 (2008)

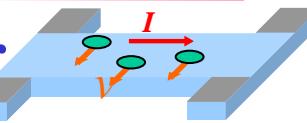
Sorry, unpublished data

Vortices experiment on RIT (ac drive)

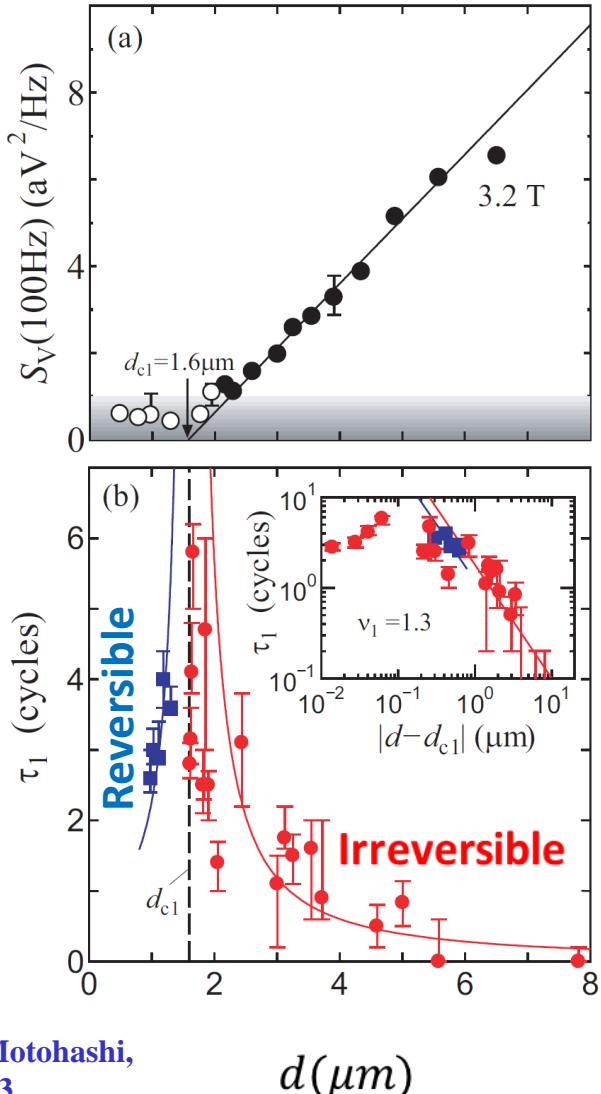


CD: strong *global* shear
weak pinning

Strip: weak *local* shear
stronger pinning



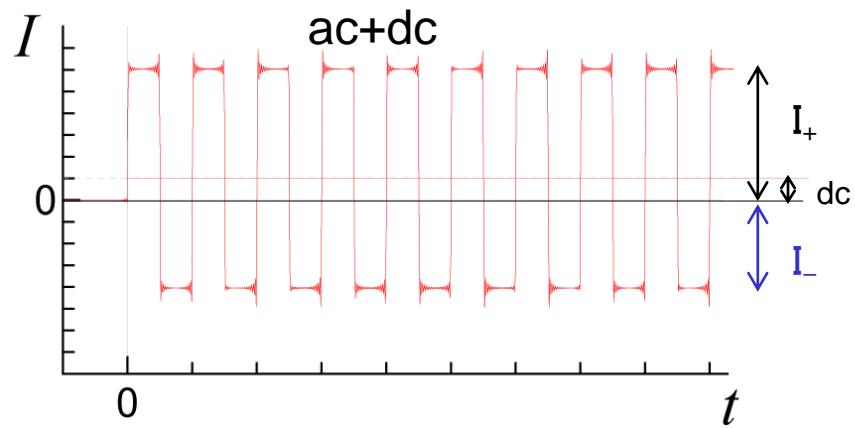
$\nu_1 = 1.3$



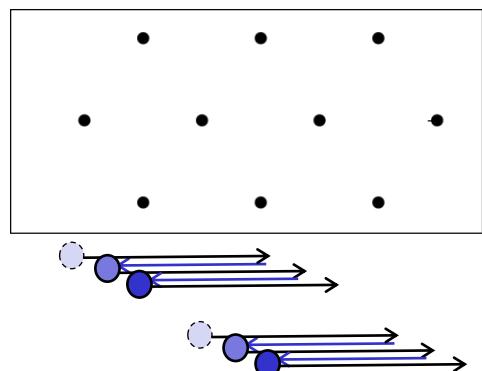
Sorry, unpublished data

Observation of “RIT” in the moving frame with v_{dc}

Our idea: Reduction of pinning forces
by driving the vortex system with v_{dc}
→ RIT in the moving frame?



Oscillation viewed from:
rest (lab) frame



moving frame

Sorry, unpublished data

Vortex matter in conventional type-II SC

— $a\text{-Mo}_x\text{Ge}_{1-x}$ films with weak pinning —

(1) Field-driven quantum phase transition

(2) Dynamics of moving lattices

-Dynamic ordering

dc + ac

-Plastic flow of solids -Strong shear: Corbino disk

(3) **Dynamics of non-equilibrium many particles and novel dynamic transitions**

- rev-irreversible tr. and random organization

- absorbing tr.

➡ - **depinning tr.**

ac

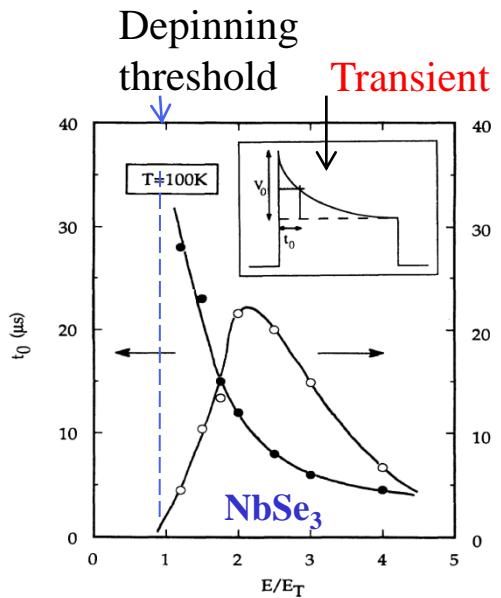
Exploring further dynamic transitions

dc

Depinning phenomena in various physical systems

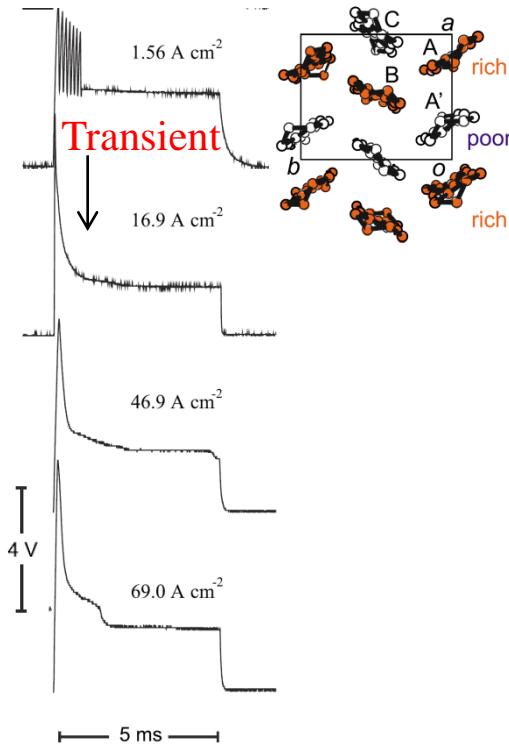
Colloids, Electron crystals, SC vortices, ... ,

CDW



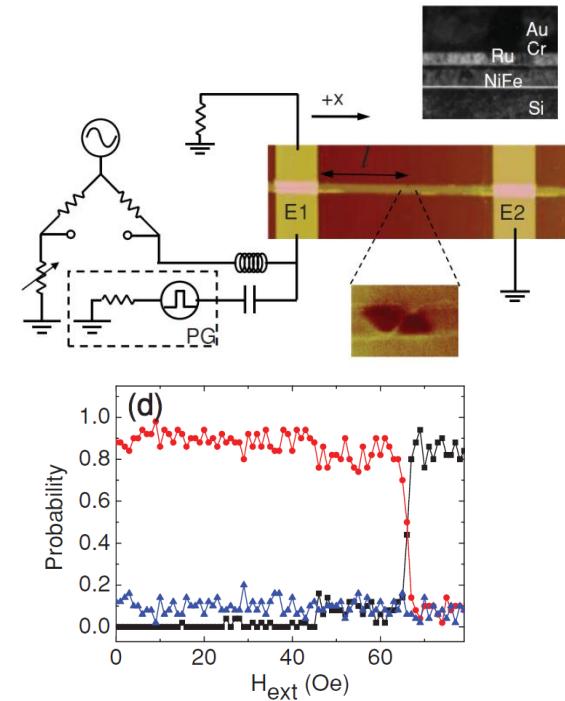
I.D. Parker, A. Zettl, PRB
45, 3260 (1992)

Charge-ordered org. cond.



K. Tamura, T. Mori *et al.*,
JAP 107, 103716 (2010)

Magnetic domain walls

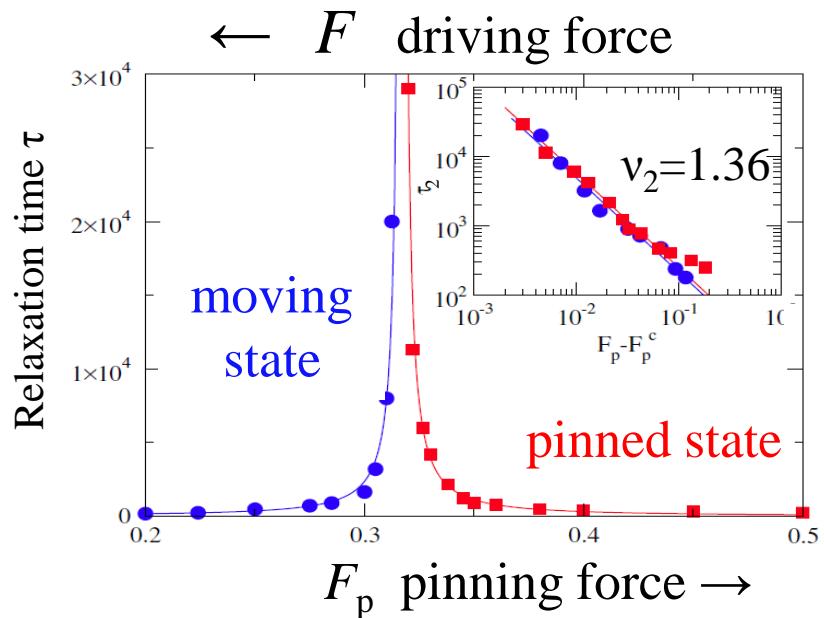
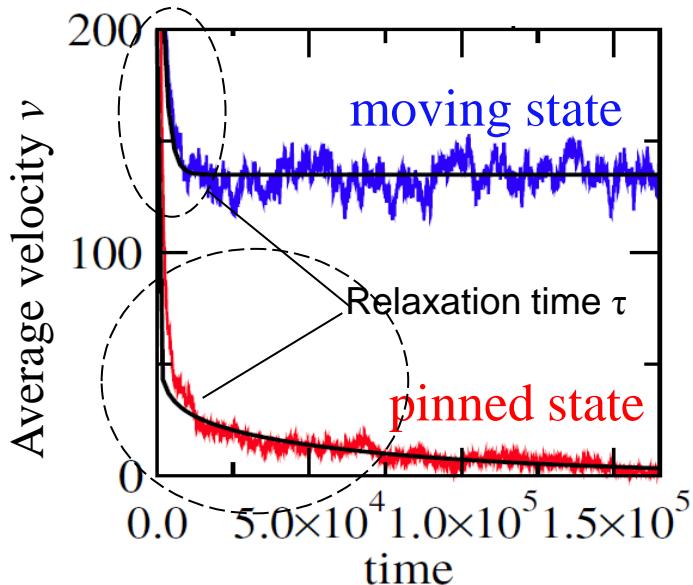
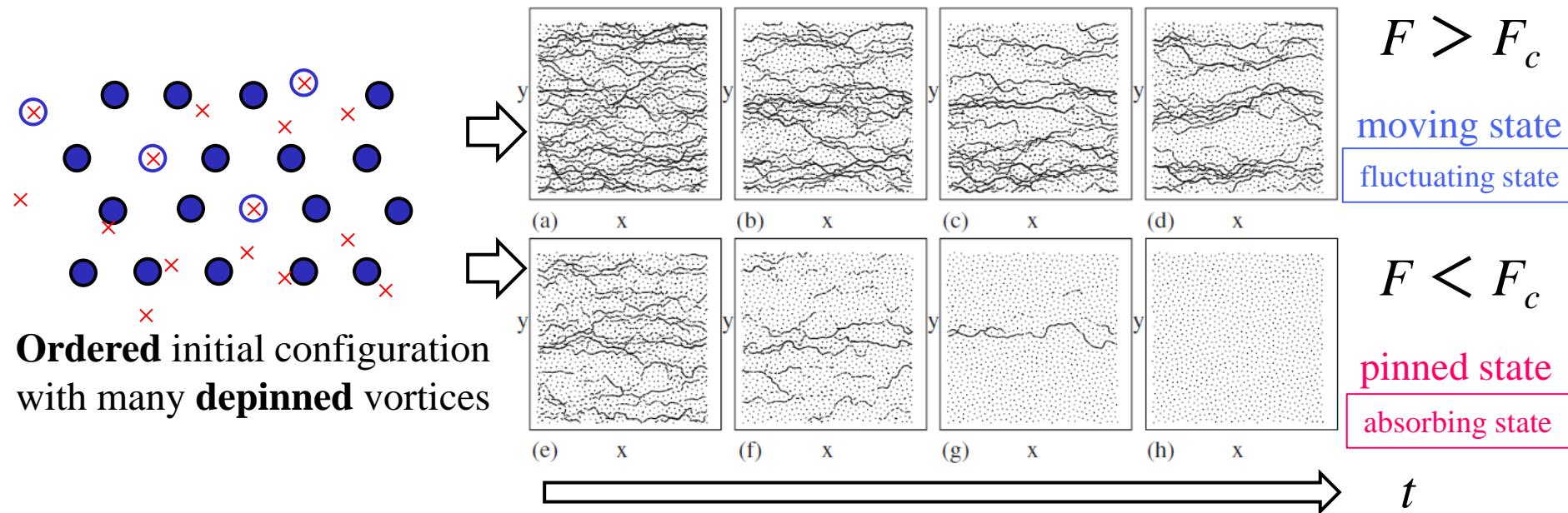


U.H. Pi *et al.*, PRB 84, 024426 (2011)

Importance of the depinning transition

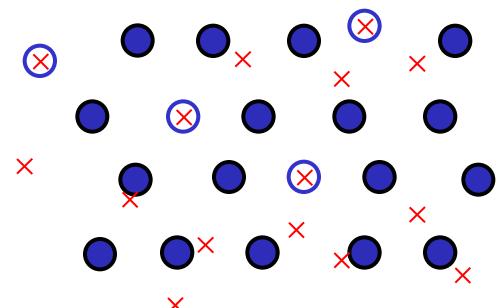
- Practical application of logic and memory devices in spintronic and flux-based SC circuits
- Fundamentally, a new **dynamic (nonequilibrium) phase transition**

Non-equilibrium depinning transition (simulation)



Dynamic disordering (pinning)

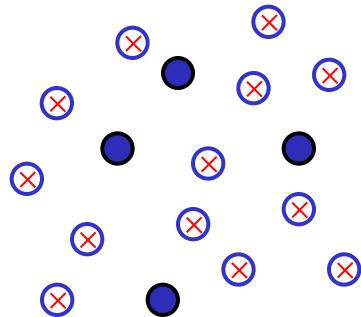
SO, Y. Tsugawa, A. Motohashi,
PRB 83 (2011) 012503



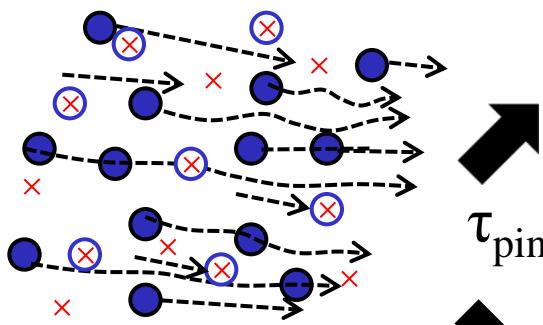
Ordered initial configuration
with many depinned vortices

Initial state

Application of F

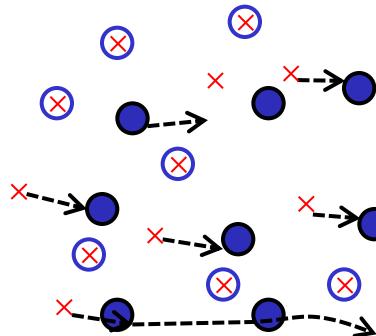


Disordered initial configuration
with many pinned vortices



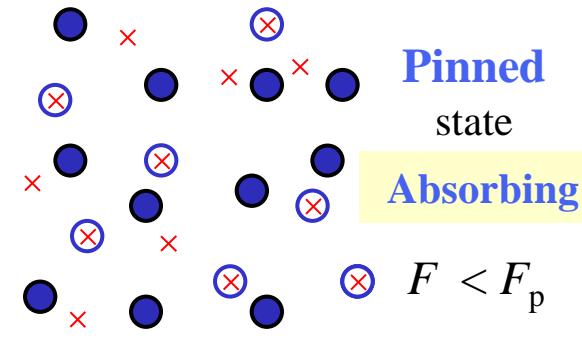
Driven vortices are
gradually pinned

Transient state



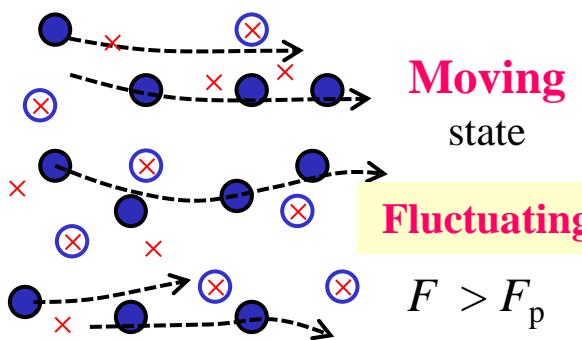
Pinned vortices are
gradually depinned

Dynamic ordering (depinning)



Pinned
state

Absorbing



Moving
state

Fluctuating

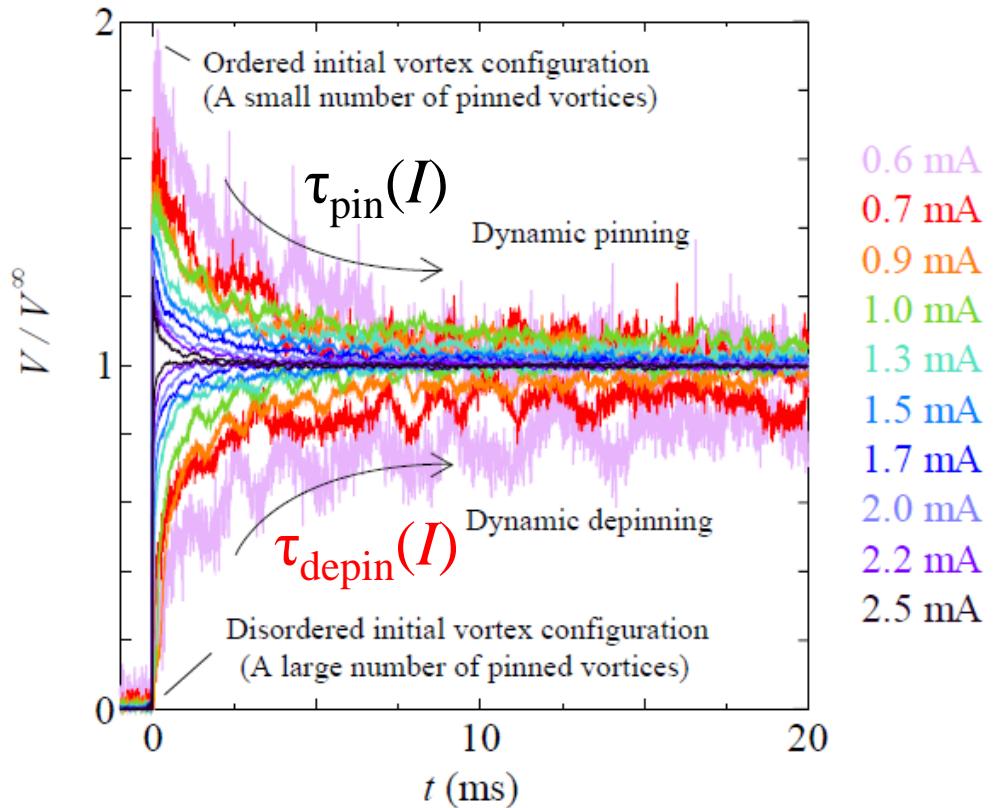


Steady state

- Mobile vortex
- Pinned vortex
- ✗ Pinning center

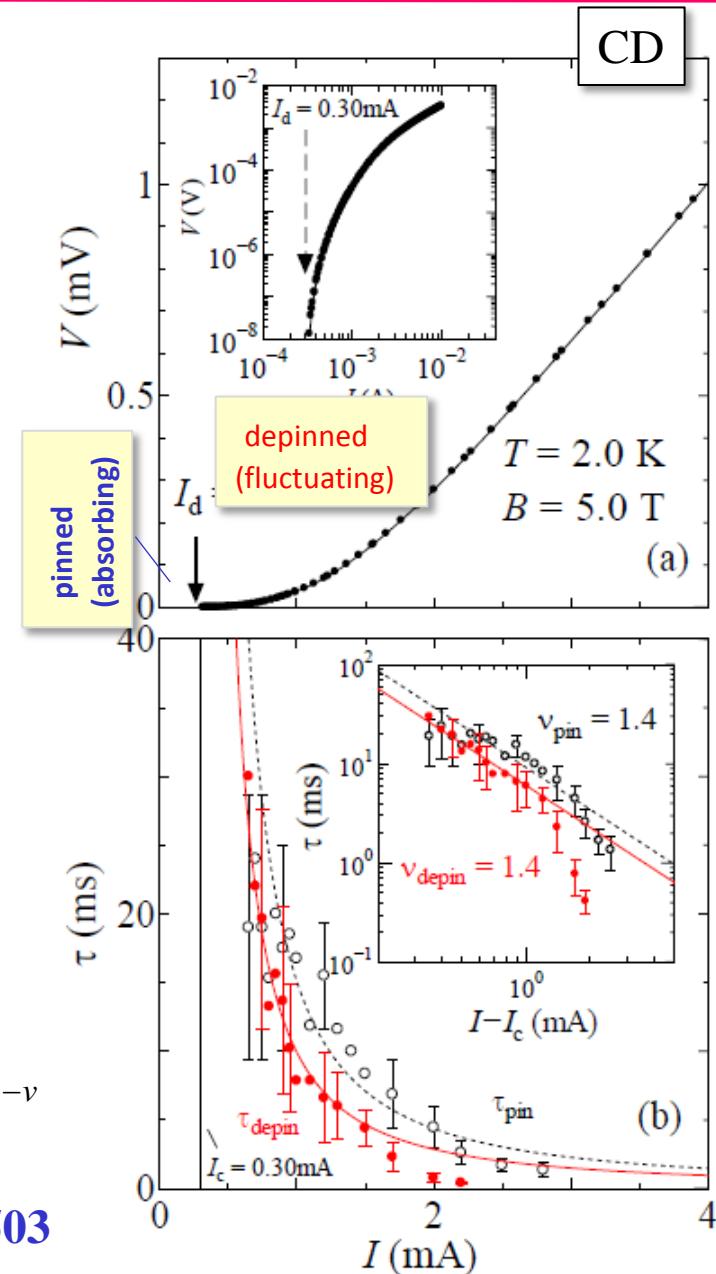
Evidence of plastic depinning transition: dynamic transition

SO, A. Motohashi, New J. Phys. 14 (2012) 123021

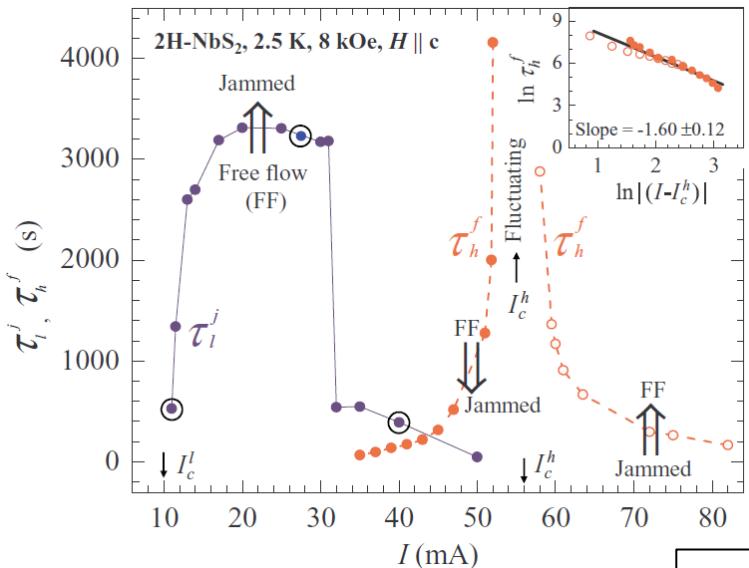


$$V(t) = \frac{(V^0 - V^\infty) \exp(-t/\tau)}{t^\alpha} + V^\infty \quad \tau \sim |I - I_c|^{-\nu}$$

SO, Y. Tsugawa, A. Motohashi, PRB 83 (2011) 012503
 Phys. Rev. Lett. 103, 168301 (2009).



Jammed(?) - FF in NbS₂



G. Shaw *et al.*, PRB **85**, 174517 (2012)

Critical behavior in pinned phase for $a\text{-Mo}_x\text{Ge}_{1-x}$

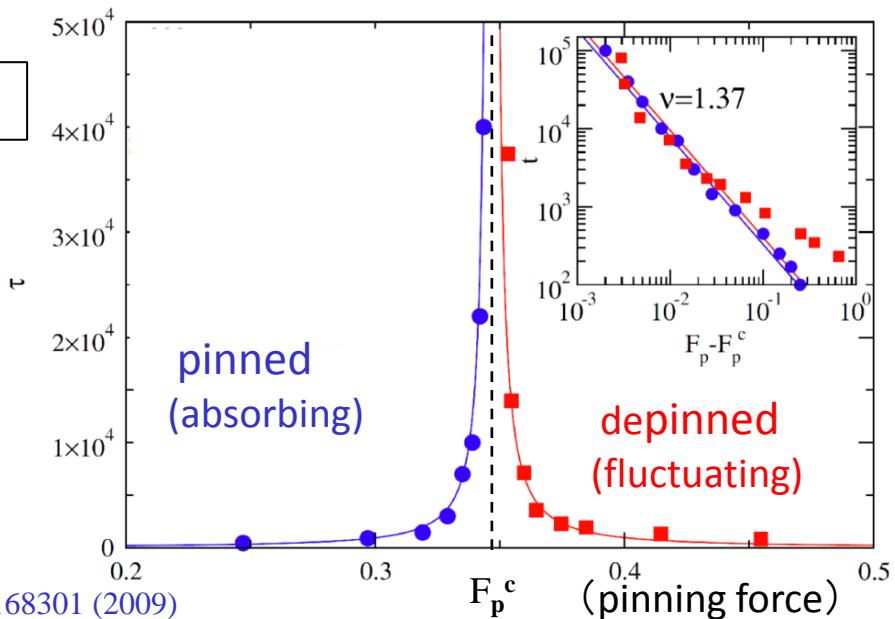
T. Kaj
(2015)

Sorry, unpublished data

Experiment

SO e

Simulation



C. Reichhardt, C.J. Olson Reichhardt, PRL **103**, 168301 (2009)

Summary 2

Non-equilibrium phenomena and phase transitions in a vortex system

(1) Reversible-irreversible transition (RIT)

- Rev. state is a **weakly disordered** (but not perfect) lattice
→ **Memory effect** of the input amplitude and its readout
- **RIT** occurs under **local** shear as well as global shear
- “**RIT**” occurs in the **moving frame**, but **v (=0.7)** is smaller

(2) Dynamic depinning transitions for ...

DC drive:

- Critical dynamics similar to that in the depinned phase is observed in the **pinned** phase
- In **coexistence** phase **v =1.0**, which **is smaller** than **v =1.3** in OP

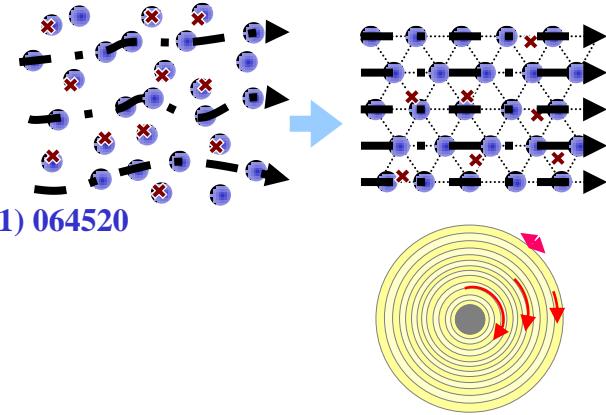
Plastic flow and dynamic transitions of vortex matter

(1) Dynamics of moving lattices

Dynamic ordering of driven vortices

- B and v -induced lattice reorientation

- [SO, H. Imaizumi, D. Shimamoto, N. Kokubo, PRB 83 (2011) 064520]
- [SO, D. Shimamoto, N. Kokubo, PRB 85 (2012) 064508]
- [D. Shimamoto, SO, N. Kokubo, JPCS 302 (2011) 012027]

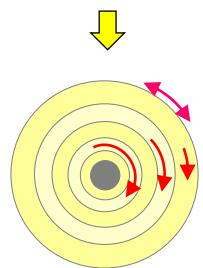


Dynamic melting of driven lattices

- [SO, H. Imaizumi, N. Kokubo, PRB 80 (2009) 132503]
- [A. Ochi et al., JPSJ 85 (2016) 044701; JPSJ 85 (2016) 034712]

Rotating lattice rings in CD: roles of effective pinning

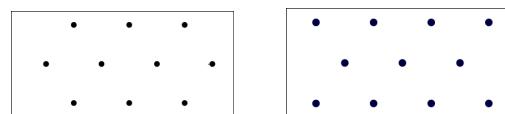
- [SO, Y. Yamazaki, N. Kokubo, PRB 80 (2009) 220501(R)]
- [Y. Kawamura et al., SUST 28 (2015) 045002]



(2) Dynamics of non-equilibrium many particles

Novel dynamic transitions

- RIT and random organization
- depinning tr.



- [SO, Y. Tsugawa, A. Motohashi, PRB 83 (2011) 012503]
- [Y. Kawamura, SO, JPS 4 (2015) 011007; 81 (2012) 114718]
- [SO, A. Motohashi, NJP 14 (2012) 123021]
- [SO, Y. Kawamura, Y. Tsugawa, SUST 26 (2013) 025013]

