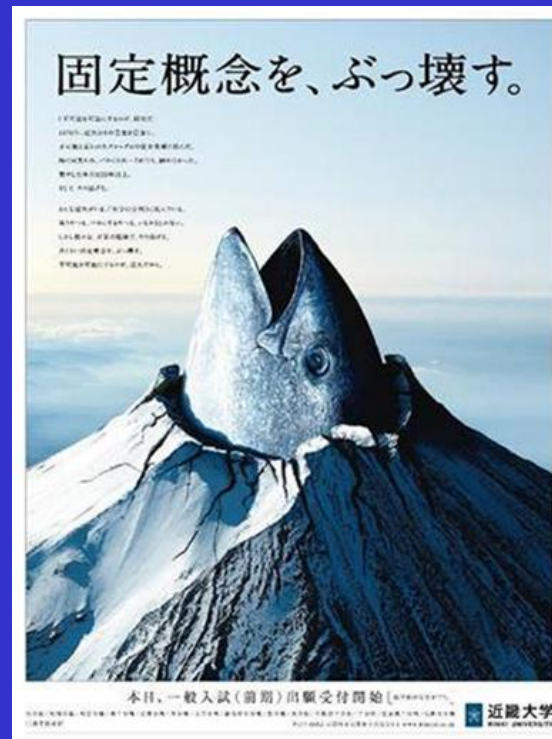


Dynamical Approach to Synthesis of Superheavy Elements

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*Long-term workshop on
“Computational Advances in Nuclear
and Hadron Physics” (CANHP2015)
YITP, Kyoto, Japan, 1st October 2015*



Topics

Structure

Light Nuclei

Reaction

Superheavy Nuclei

Key Words

1. Shell Correction Energy
Two-Center **Shell Model**
2. Dynamical Approach

Contents

1. Introduction

- Super Heavy Elements
- Stability of Nuclei, Shell effects
- Synthesis of SHE

2. Experimental methods

3. Theoretical calculation

- Dynamical model (Fluctuation Dissipation model)
- Langevin equation

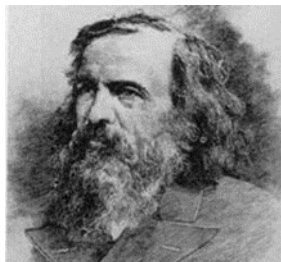
4. Calculation results

- fusion-fission process

5. Further study

Periodic Table

1	Hydrogen 1 H	2				
2	Lithium 3 Li	Beryllium 4 Be				
3	Sodium 11 Na	Magnesium 12 Mg	3	4	5	6
4	Potassium 19 K	Calcium 20 Ca	Scandium 21 Sc	Titanium 22 Ti	Vanadium 23 V	Chromium 24 Cr
5	Rubidium 37 Rb	Strontium 38 Sr	Yttrium 39 Y	Zirconium 40 Zr	Niobium 41 Nb	Molybdenum 42 Mo
6	Cesium 55 Cs	Barium 56 Ba	Lanthanum* 57 La*	Hafnium 72 Hf	Tantalum 73 Ta	Tungsten 74 W
7	Francium 87 Fr	Radium 88 Ra	Actinium** 89 Ac**	Rutherfordium 104 Rf	Dubnium 105 Db	Seaborgium 106 Sg



						18 Helium 2 He
	13 Boron 5 B	14 Carbon 6 C	15 Nitrogen 7 N	16 Oxygen 8 O	17 Fluorine 9 F	Neon 10 Ne
	Aluminum 13 Al	Silicon 14 Si	Phosphorus 15 P	Sulfur 16 S	Chlorine 17 Cl	Argon 18 Ar
	Gallium 31 Ga	Germanium 32 Ge	Arsenic 33 As	Selenium 34 Se	Bromine 35 Br	Krypton 36 Kr
	Indium 49 In	Tin 50 Sn	Antimony 51 Sb	Tellurium 52 Te	Iodine 53 I	Xenon 54 Xe
	Thallium 81 Tl	Lead 82 Pb	Bismuth 83 Bi	Polonium 84 Po	Astatine 85 At	Radon 86 Rn
2	113	114	115	116	117	118

Менделеев(1834-1907)
1869

May 2012 IUPAC

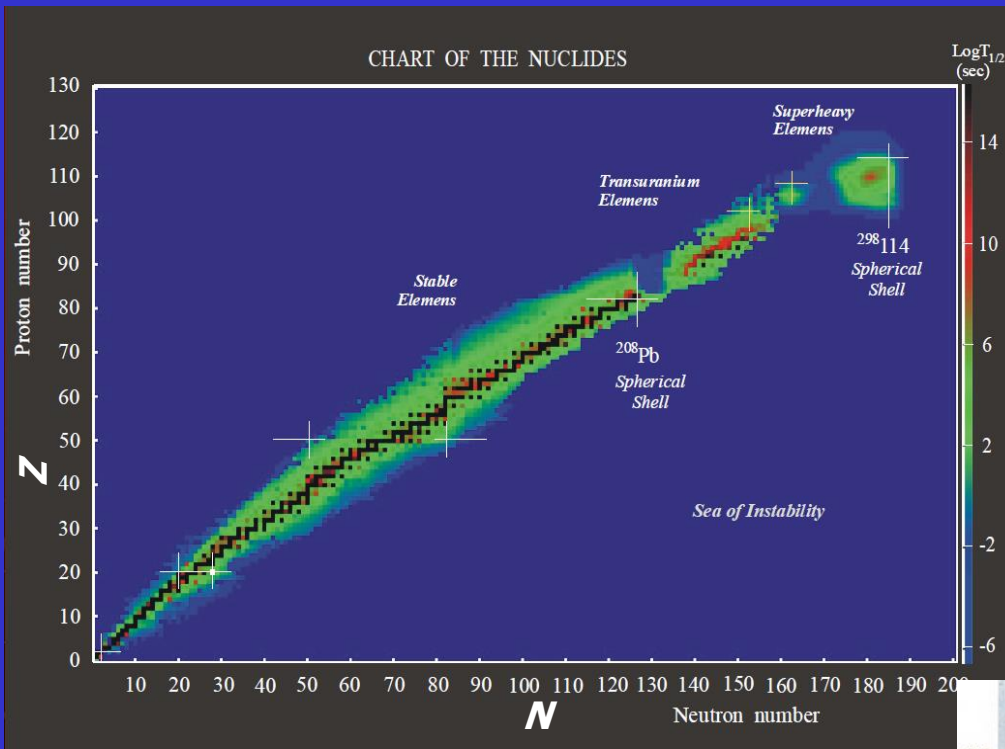
↑
Fl
flerovium

↑
Lv
livermorium

La*	Lanthanides	Lanthanum 57 La	Cerium 58 Ce	Praseodymium 59 Pr	Neodymium 60 Nd	Promethium 61 Pm	Samarium 62 Sm	Europium 63 Eu	Gadolinium 64 Gd	Terbium 65 Tb	Dysprosium 66 Dy	Holmium 67 Ho	Erbium 68 Er	Thulium 69 Tm	Ytterbium 70 Yb	Lutetium 71 Lu
Ac**	Actinides	Actinium 89 Ac	Thorium 90 Th	Protactinium 91 Pa	Uranium 92 U	Neptunium 93 Np	Plutonium 94 Pu	Americium 95 Am	Curium 96 Cm	Berkelium 97 Bk	Californium 98 Cf	Einsteinium 99 Es	Fermium 100 Fm	Mendelevium 101 Md	Nobelium 102 No	Lawrencium 103 Lr

Super Heavy Elements → less stable

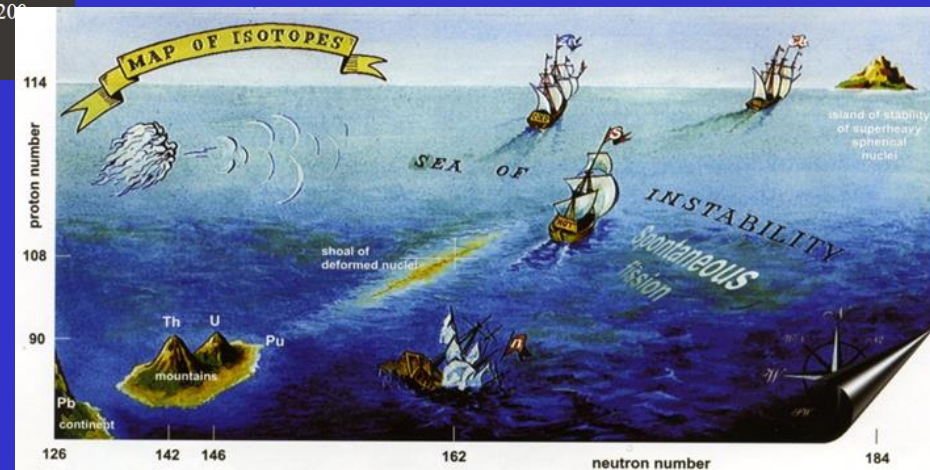
1. Introduction



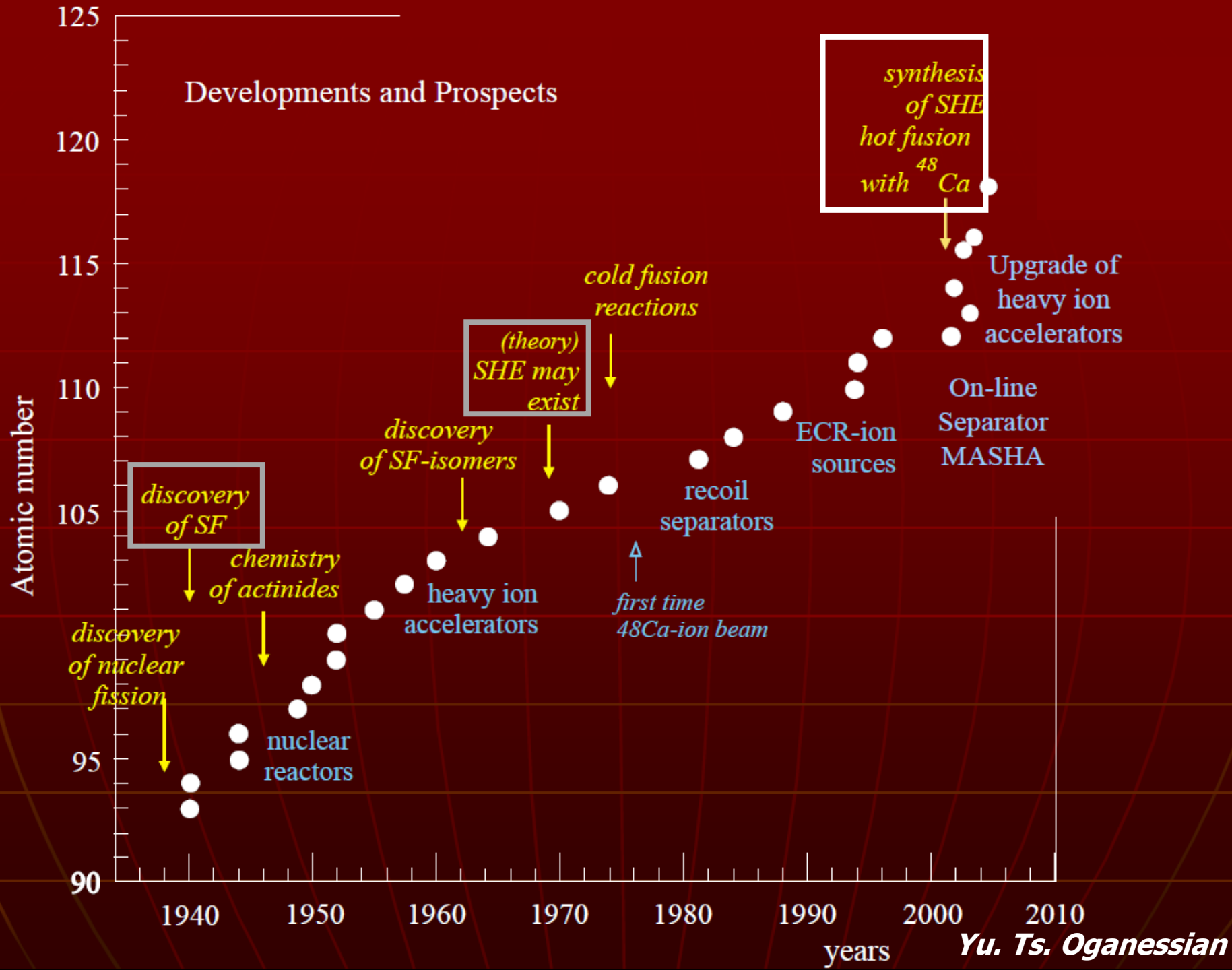
Nuclear Chart
Stability of nuclei

Our Interest

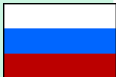
- Next magic number $\leftarrow Z=82, N=126$
- Verification of 'Island of Stability' (predicted by macroscopic-microscopic model in 1960's)
- Synthesis of new elements

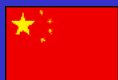


Developments and Prospects

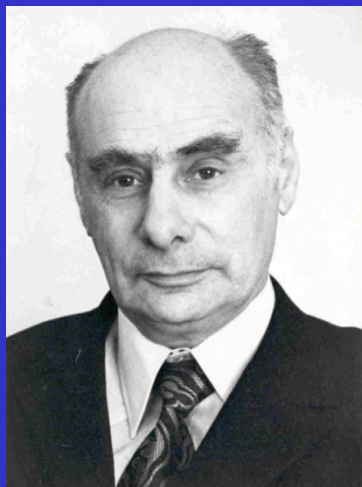


Experimental setup for synthesis of SHE

Lab	Country	City	Accelerator	Separator
FLNR	Russia 	Dubna	U400 U400M	DGFRS VASSILISSA
GSI	Germany 	Darmstadt	UNILAC	SHIP TASCA
RIKEN	Japan 	Wako	RILAC	GALIS
LBNL	USA 	Berkeley	88-inch Cyclotron	BGS
GANIL	France 	Caen	<i>SPIRAL2's LINAC accelerator</i>	<i>S3 (Super Separator Spectrometer)</i>



FLNR (Russia)



**G.N. Flerov
(1913 -1990)**



**Yu.Ts. Oganessian
(1933-)**

GSI (Germany)



Scanned at the American
Institute of Physics

**P. Armbruster G. Muenzenberg
(1931-) (1940-)**



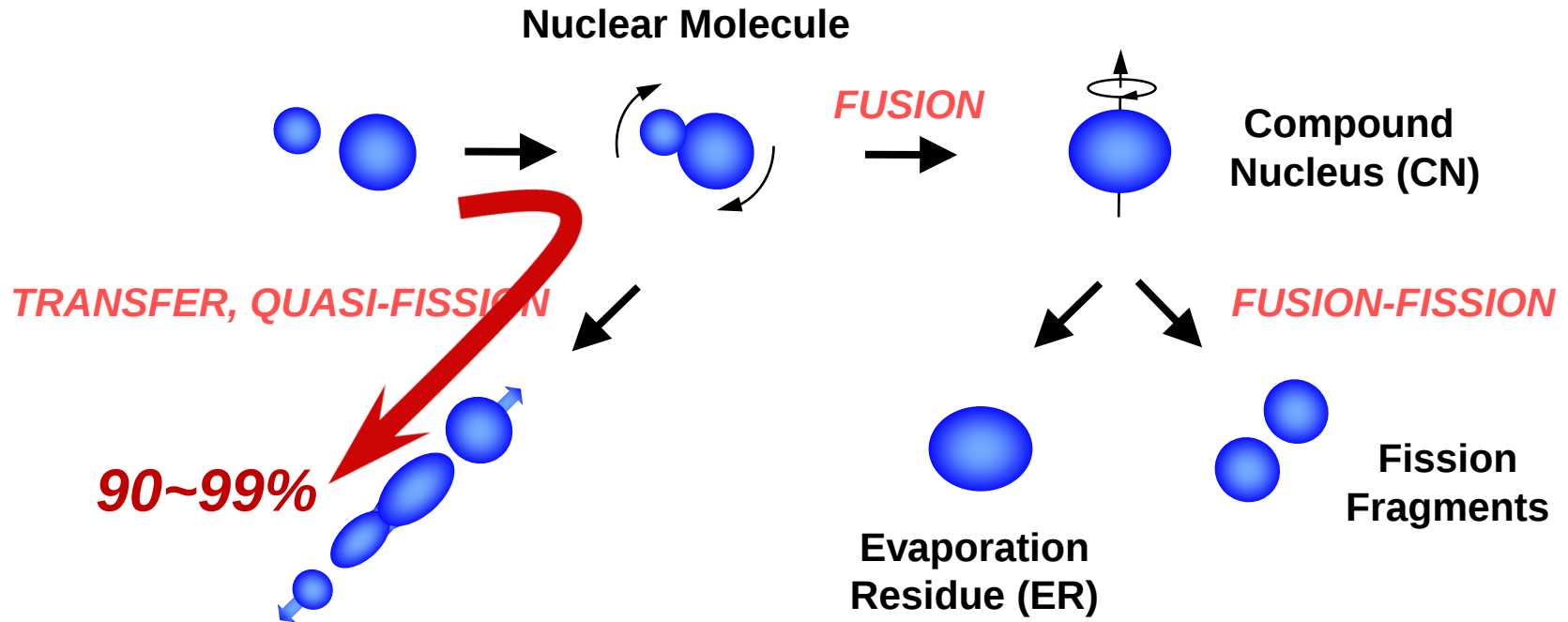
**S. Hofmann
(1943-)**

RIKEN (Japan)



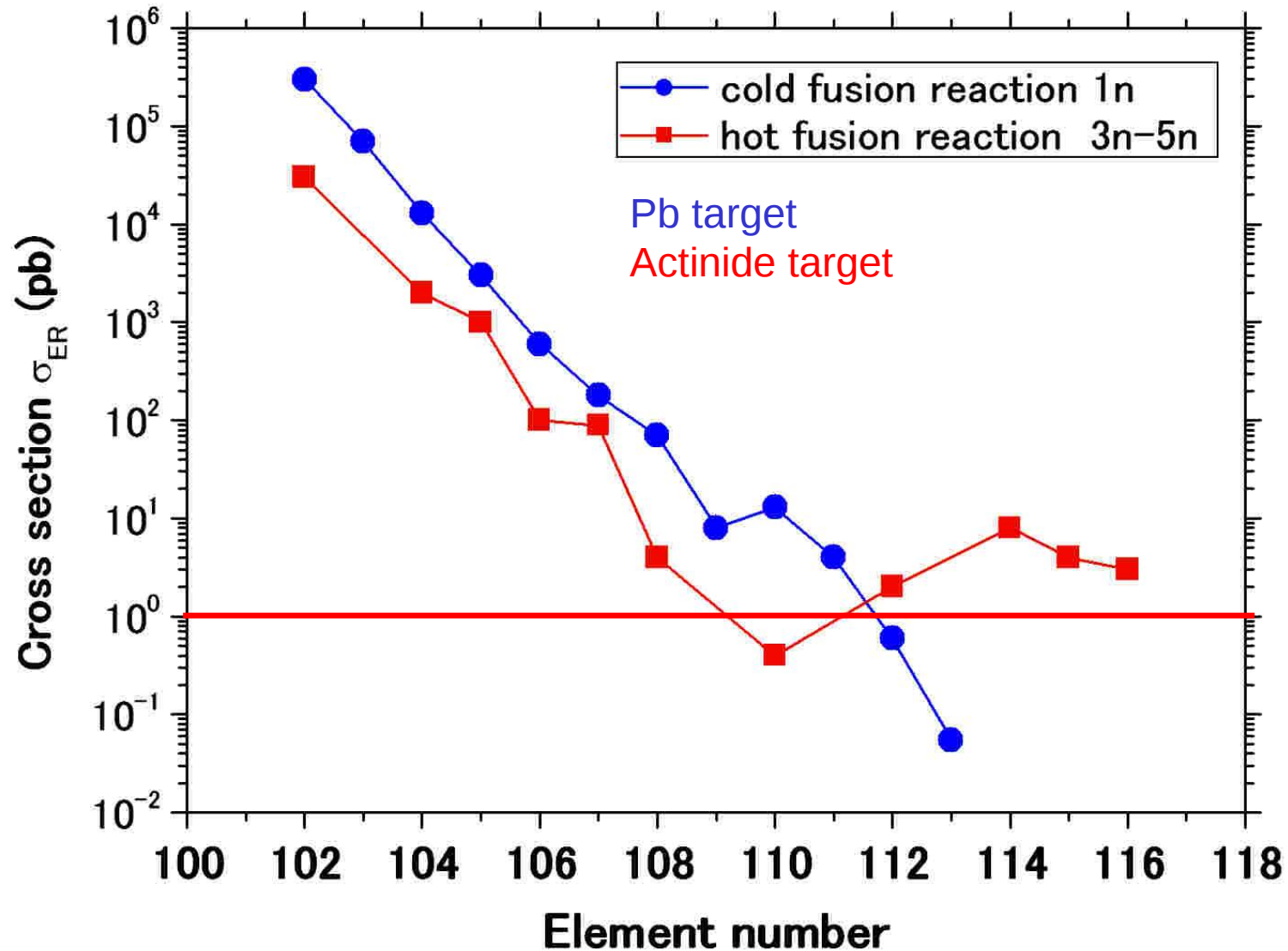
**K. Morita
(1957-)**

Fusion process in Superheavy mass region

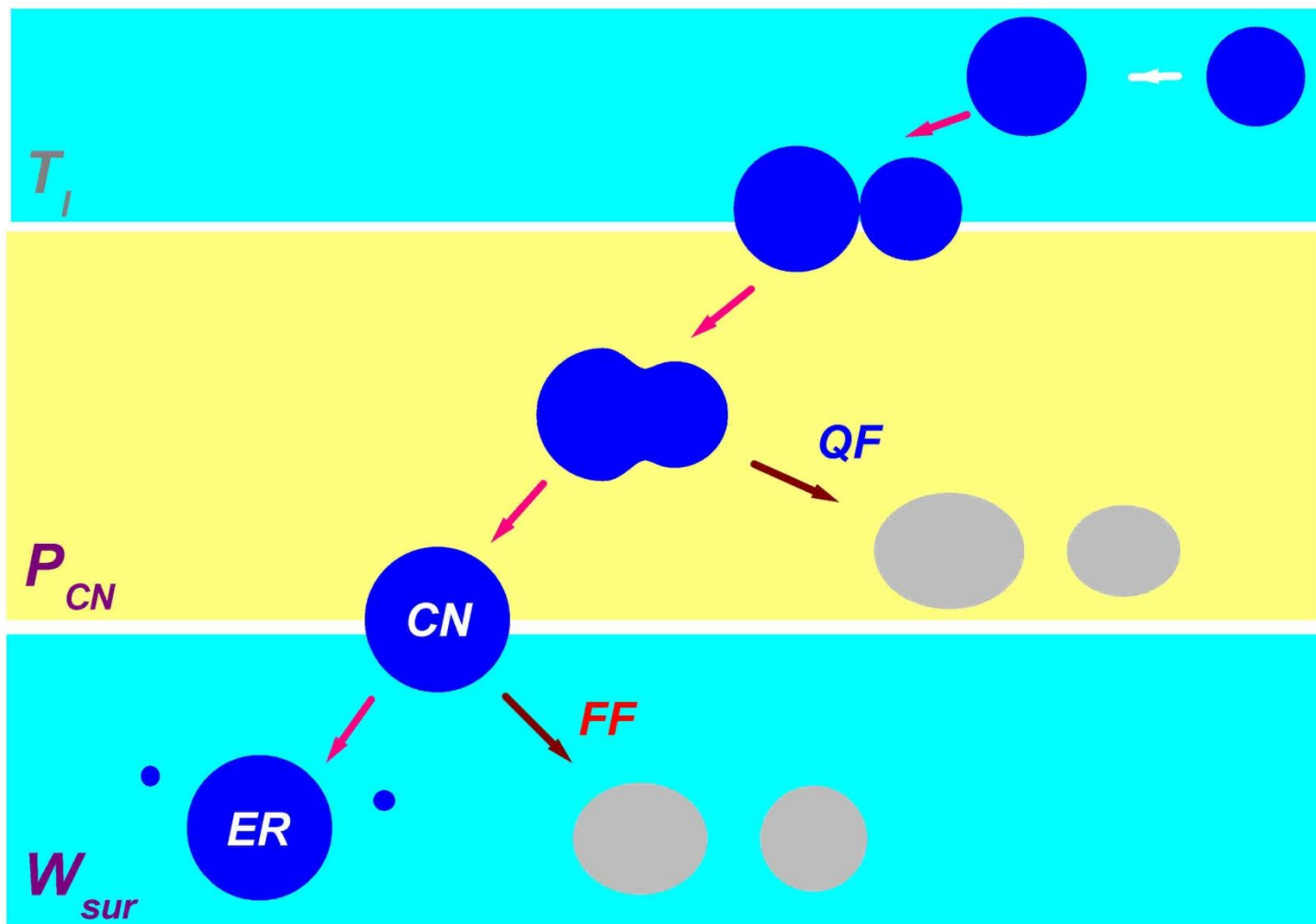


Experimental data

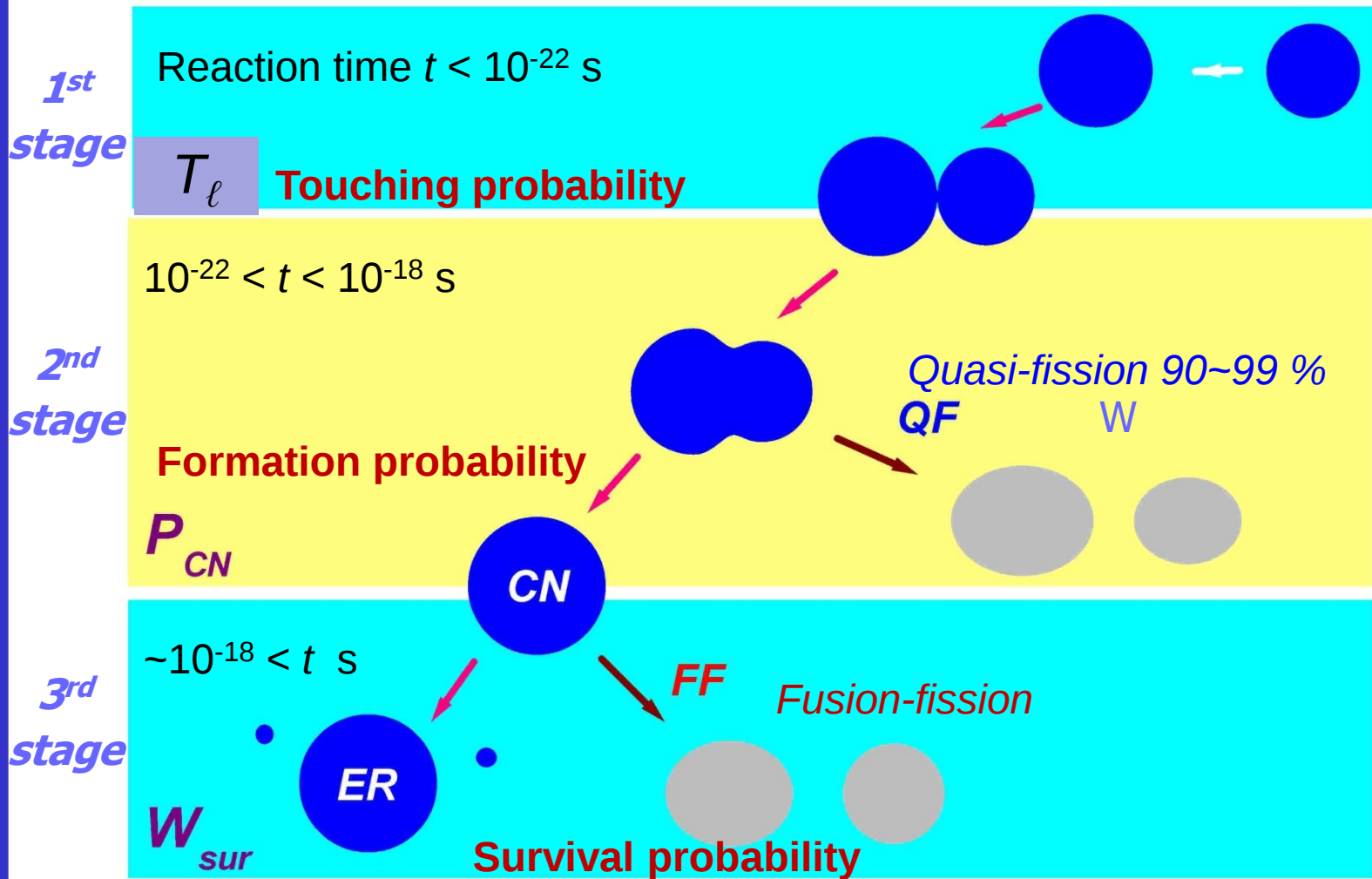
Evaporation residue cross sections



$$\sigma_{ER} = \frac{\pi \hbar^2}{2\mu_0 E_{cm}} \sum_{\ell=0}^{\infty} (2\ell + 1) T_{\ell}(E_{cm}, \ell) P_{CN}(E^*, \ell) W(E^*, \ell)$$



$$\sigma_{ER} = \frac{\pi \hbar^2}{2\mu_0 E_{cm}} \sum_{\ell=0}^{\infty} (2\ell + 1) T_{\ell}(E_{cm}, \ell) P_{CN}(E^*, \ell) W(E^*, \ell)$$



Synthesis of New Elements

Reports of new elements

Heavy ion reaction

Cold fusion reaction Hot fusion reaction

1994



1996



1999



2000



2002



2003

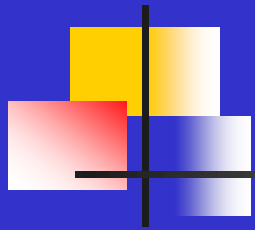


2004



2010





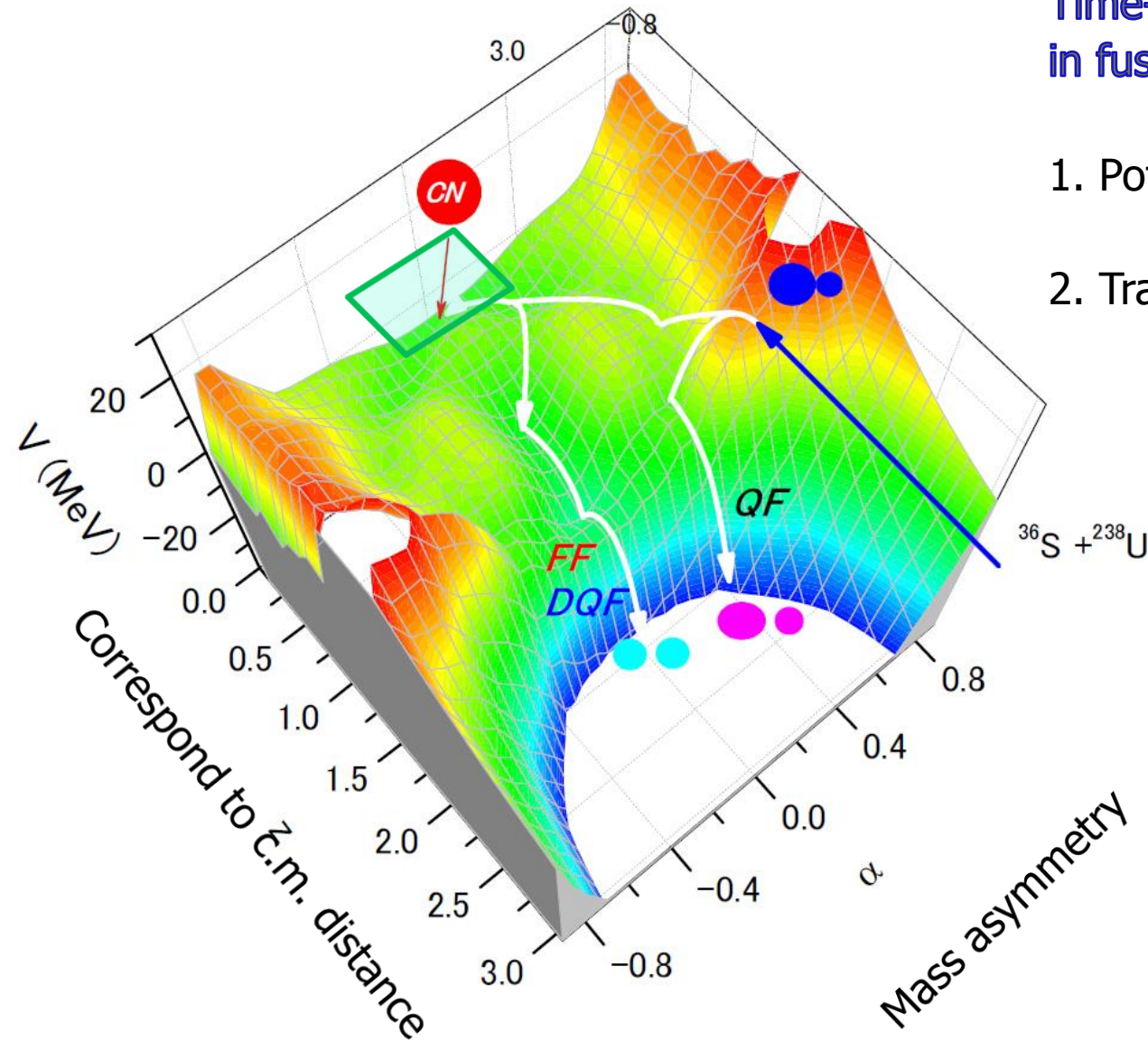
2. Model

- 2-1. Estimation of cross sections
- 2-2. Dynamical Equation

Overview of Dynamical Process in reaction $^{36}\text{S} + ^{238}\text{U}$

Time-evolution of nuclear shape in fusion-fission process

1. Potential energy surface
2. Trajectory $\rightarrow$ described by equations



Nuclear shape

two-center parametrization (z, δ, α)

(Maruhn and Greiner,
Z. Phys. 251(1972) 431)

$$q(z, \delta, \alpha)$$

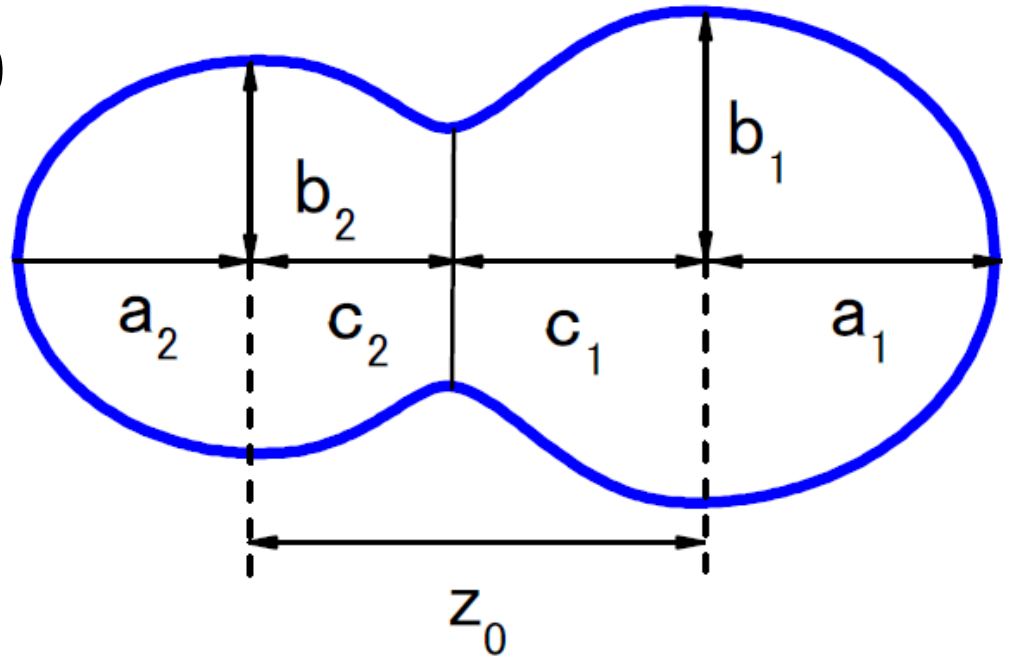
$$z = \frac{z_0}{BR}$$

$$B = \frac{3 + \delta}{3 - 2\delta}$$

R : Radius of the spherical compound nucleus

$$\delta = \frac{3(a - b)}{2a + b} \quad (\delta_1 = \delta_2)$$

$$\alpha = \frac{A_1 - A_2}{A_{CN}}$$

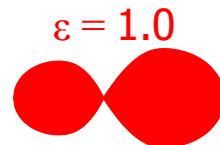


Two Center Shell Model

$$\hat{H} = -\frac{\hbar^2}{2m_0} \nabla^2 + V(\mathbf{r}) + V_{LS}(\mathbf{r}, \mathbf{p}, \mathbf{s}) + V_{L^2}(\mathbf{r}, \mathbf{p}).$$

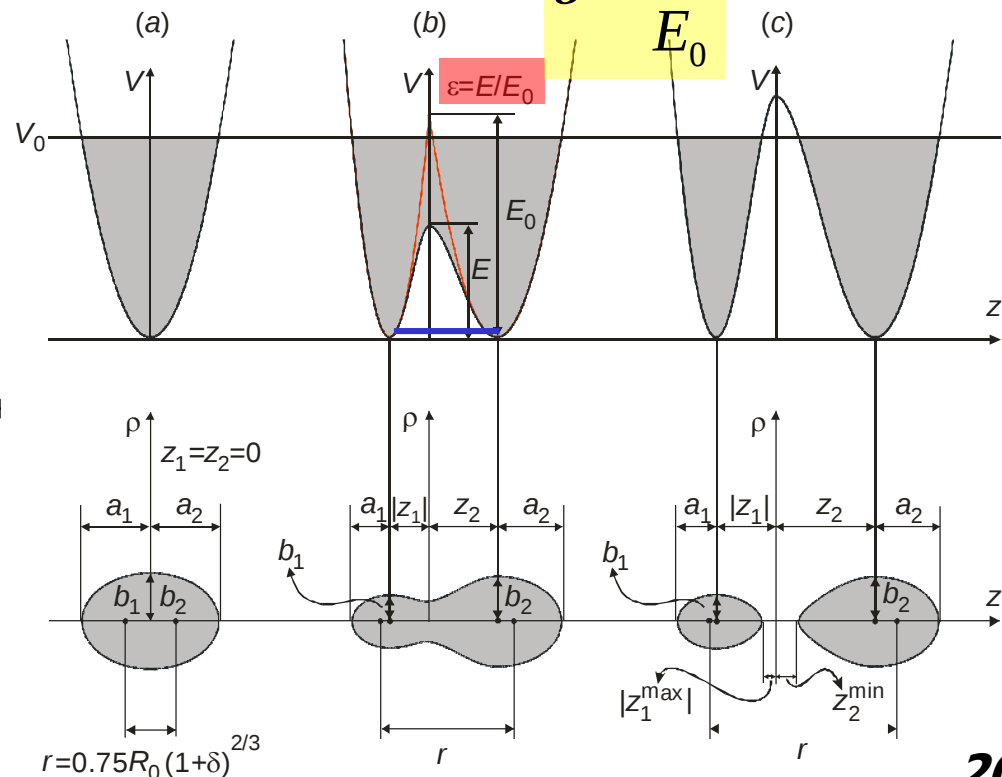
$$V(\rho, z) = \frac{1}{2} m_0 \begin{cases} \omega_{z1}^2 z'^2 + \omega_{\rho1}^2 \rho^2, & z < z_1 \\ \omega_{z1}^2 z'^2 (1 + c_1 z' + d_1 z'^2) + \omega_{\rho1}^2 (1 + g_1 z'^2) \rho^2, & z_1 < z < 0 \\ \omega_{z2}^2 z'^2 (1 + c_2 z' + d_2 z'^2) + \omega_{\rho2}^2 (1 + g_2 z'^2) \rho^2, & 0 < z < z_2 \\ \omega_{z2}^2 z'^2 + \omega_{\rho2}^2 \rho^2, & z > z_2, \end{cases}$$

$$z' = \begin{cases} z - z_1 & z < 0 \\ z - z_2 & z > 0 \end{cases}$$



Neck parameter is the ratio of smoothed potential height to the original one where two harmonic oscillator potential cross each other

$$\varepsilon = \frac{E}{E_0}$$



Potential Energy

$$V(q, \ell, T) = V_{DM}(q) + \frac{\hbar^2 \ell(\ell+1)}{2I(q)} + V_{SH}(q, T)$$

$$V_{DM}(q) = E_S(q) + E_C(q)$$

$$V_{SH}(q, T) = E_{shell}^0(q) \Phi(T)$$

T : nuclear temperature

$E^* = aT^2$ a : level density parameter

Toke and Swiatecki

E_S : Generalized surface energy (finite range effect)

E_C : Coulomb repulsion for diffused surface

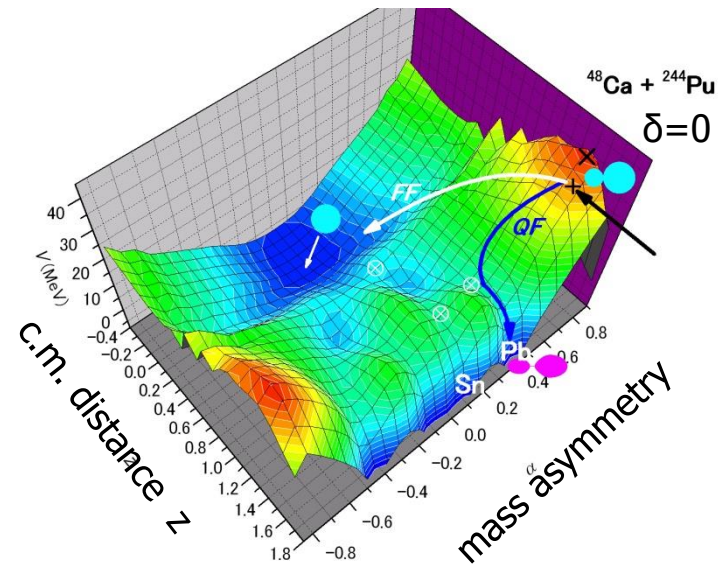
E_{shell}^0 : Shell correction energy at $T=0$

I : Moment of inertia for rigid body

$\Phi(T)$: Temperature dependent factor

$$\Phi(T) = \exp \left\{ - \frac{aT^2}{E_d} \right\}$$

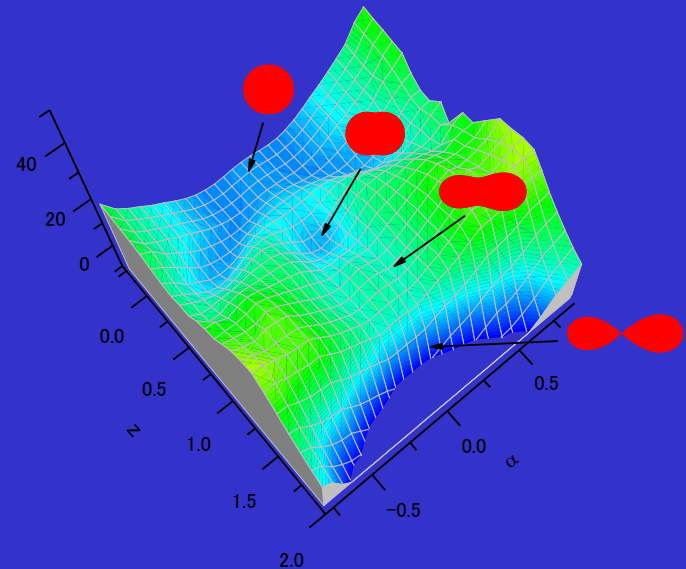
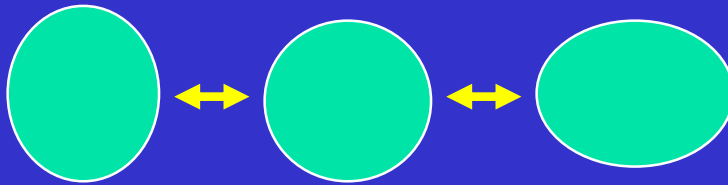
$$E_d = 20 \text{ MeV}$$



Taking into account the fluctuation around the mean trajectory

Thermal fluctuation of nuclear shape

→ thermal fluctuation of collective motion



Multi-dimensional Langevin Equation

$$\frac{dq_i}{dt} = (m^{-1})_{ij} p_j$$

$$\frac{dp_i}{dt} = -\frac{\partial V}{\partial q_i} - \frac{1}{2} \frac{\partial}{\partial q_i} (m^{-1})_{jk} p_j p_k - \underbrace{\gamma_{ij} (m^{-1})_{jk} p_k}_{\text{Friction dissipation}} + \underbrace{g_{ij} R_j(t)}_{\text{Random force fluctuation}}$$

Newton equation
ordinary differential equation

$\langle R_i(t) \rangle = 0$, $\langle R_i(t_1) R_j(t_2) \rangle = 2\delta_{ij} \delta(t_1 - t_2)$: white noise (Markovian process)

$$\sum_k g_{ik} g_{jk} = T \gamma_{ij}$$

Einstein relation

Fluctuation-dissipation theorem

q_i : deformation coordinate

(nuclear shape)

two-center parametrization (z, δ, α)

(Maruhn and Greiner, Z. Phys. 251(1972) 431)

p_i : momentum

m_{ij} : Hydrodynamical mass

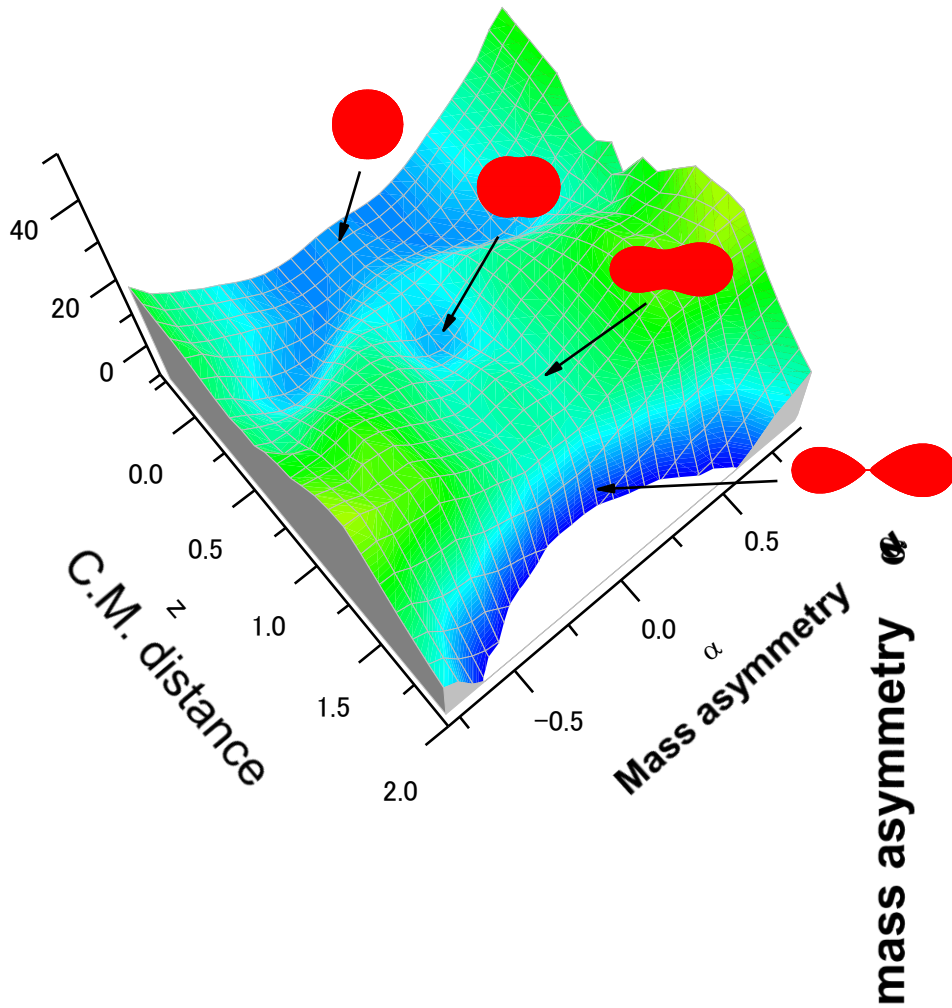
(inertia mass)

γ_{ij} : Wall and Window (one-body) dissipation (friction)

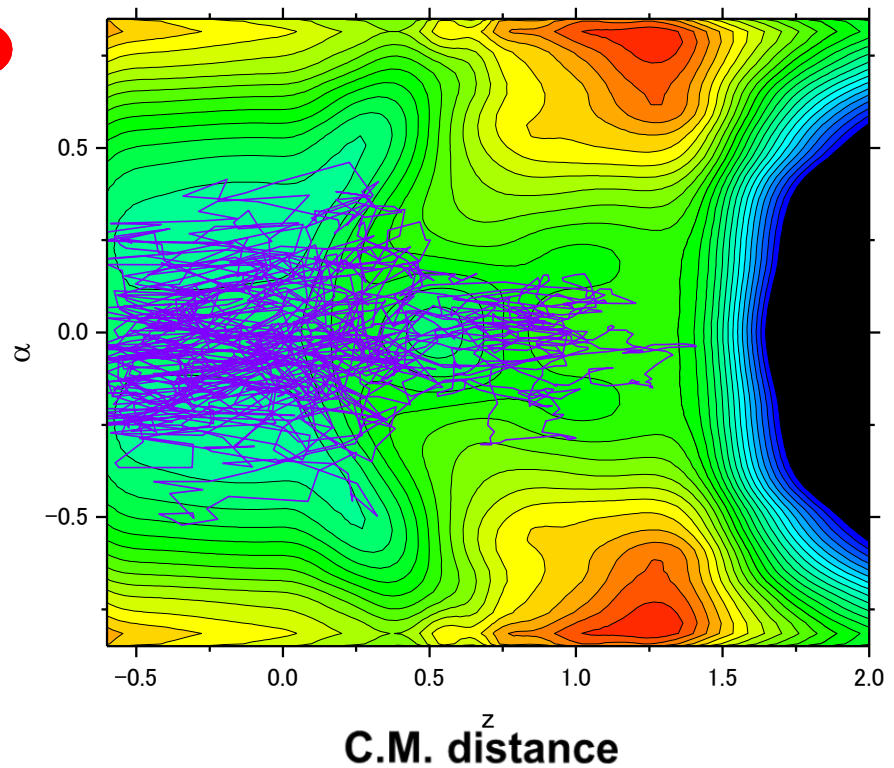
$$E_{\text{int}} = E^* - \frac{1}{2} (m^{-1})_{ij} p_i p_j - V(q)$$

E_{int} : intrinsic energy, E^* : excitation energy

Fission process ^{240}U $E^* < 20 \text{ MeV}$



Trajectory on potential energy surface

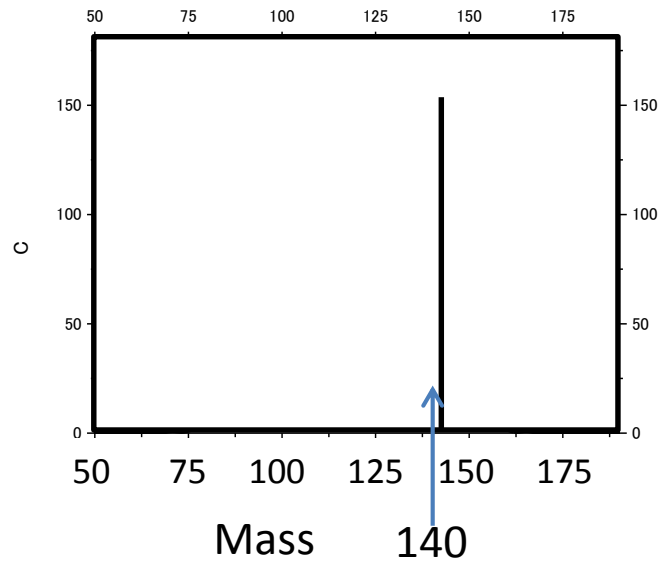
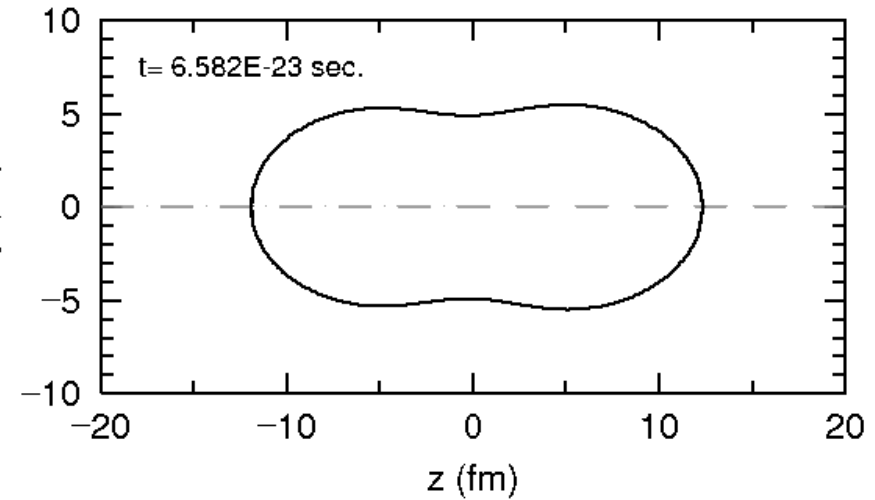
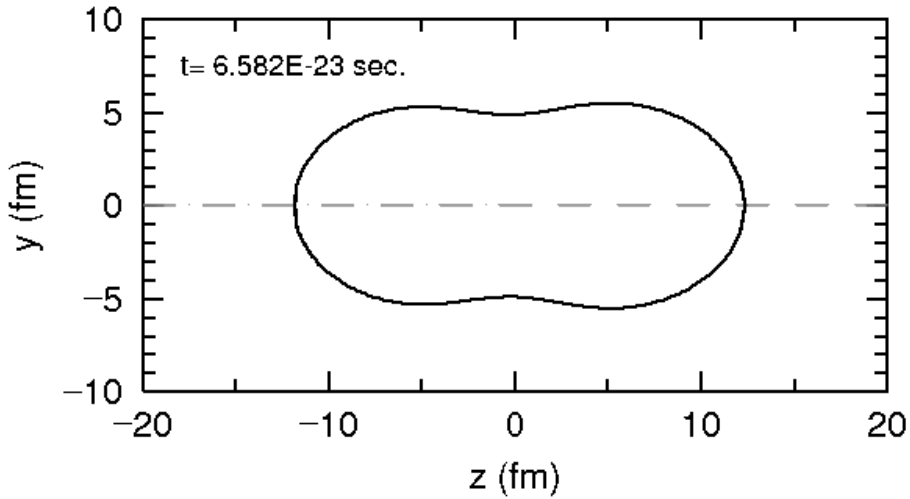


^{236}U $E^*=20$ MeV

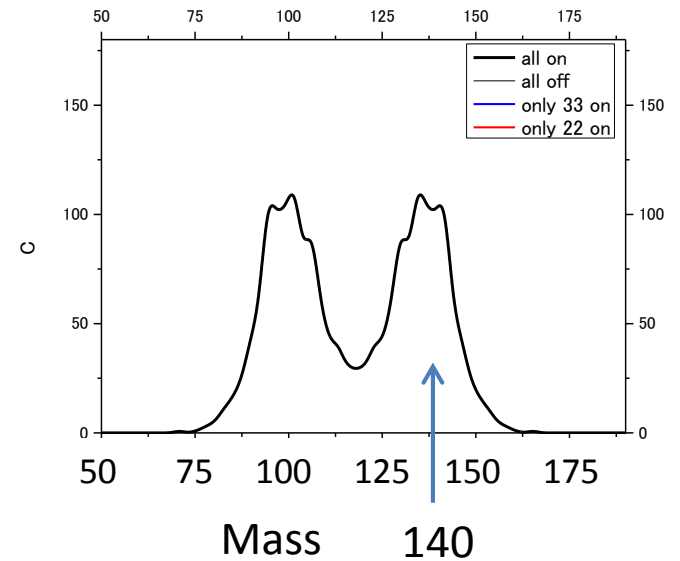
揺動項なし Newton Eq

分裂過程

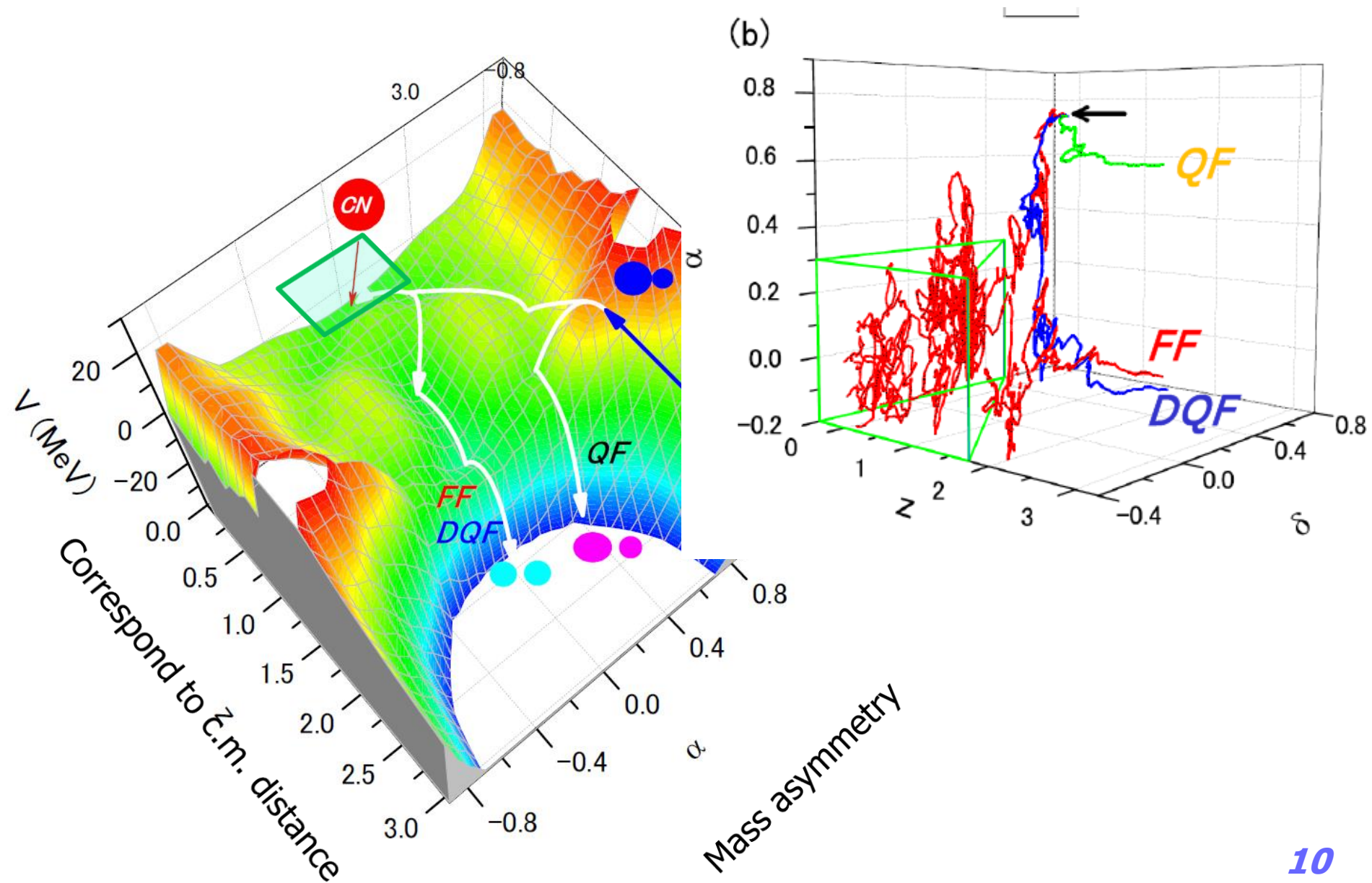
揺動項あり Langevin Eq.



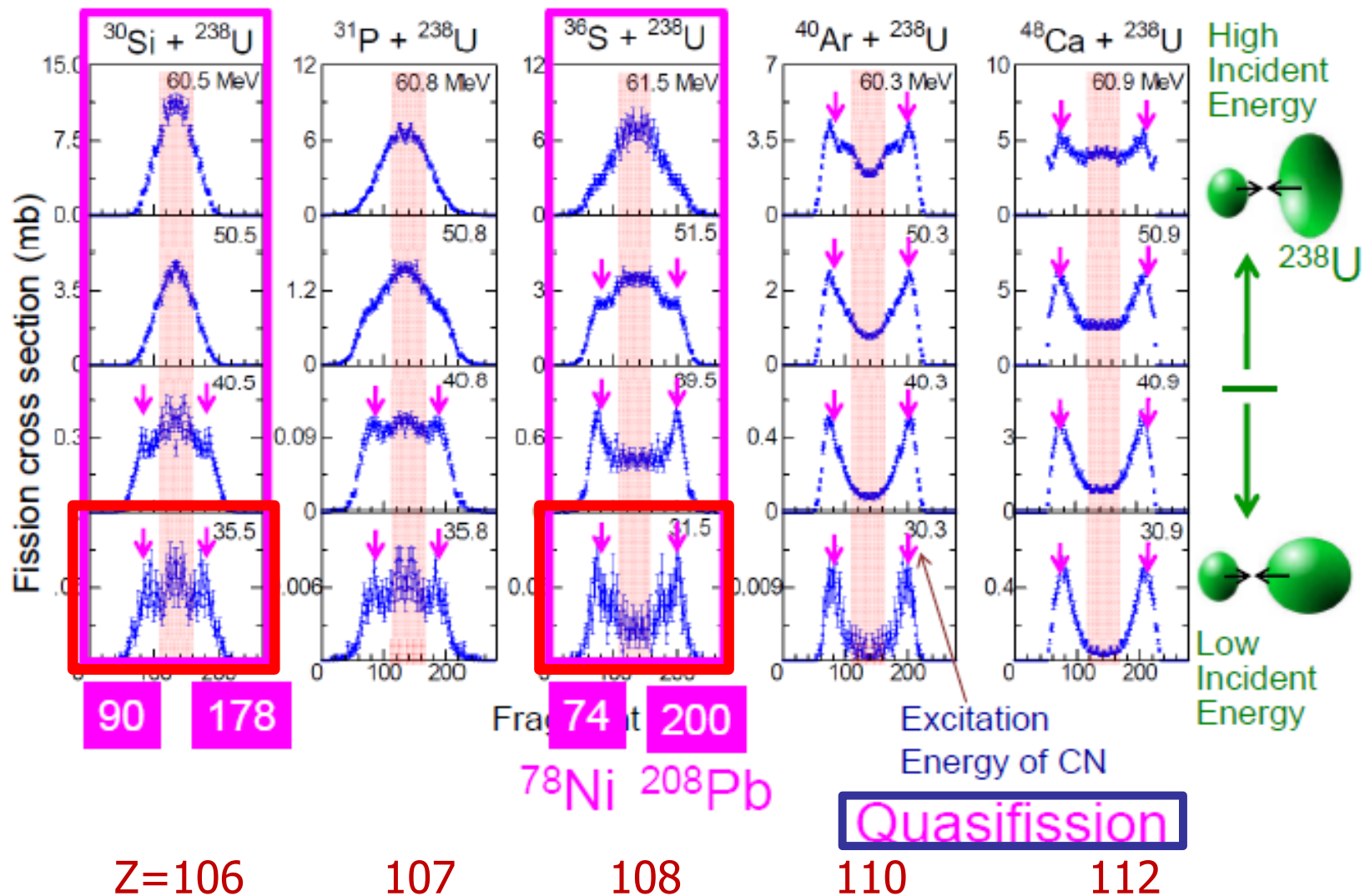
質量分布



Overview of Dynamical Process in reaction $^{36}\text{S}+^{238}\text{U}$

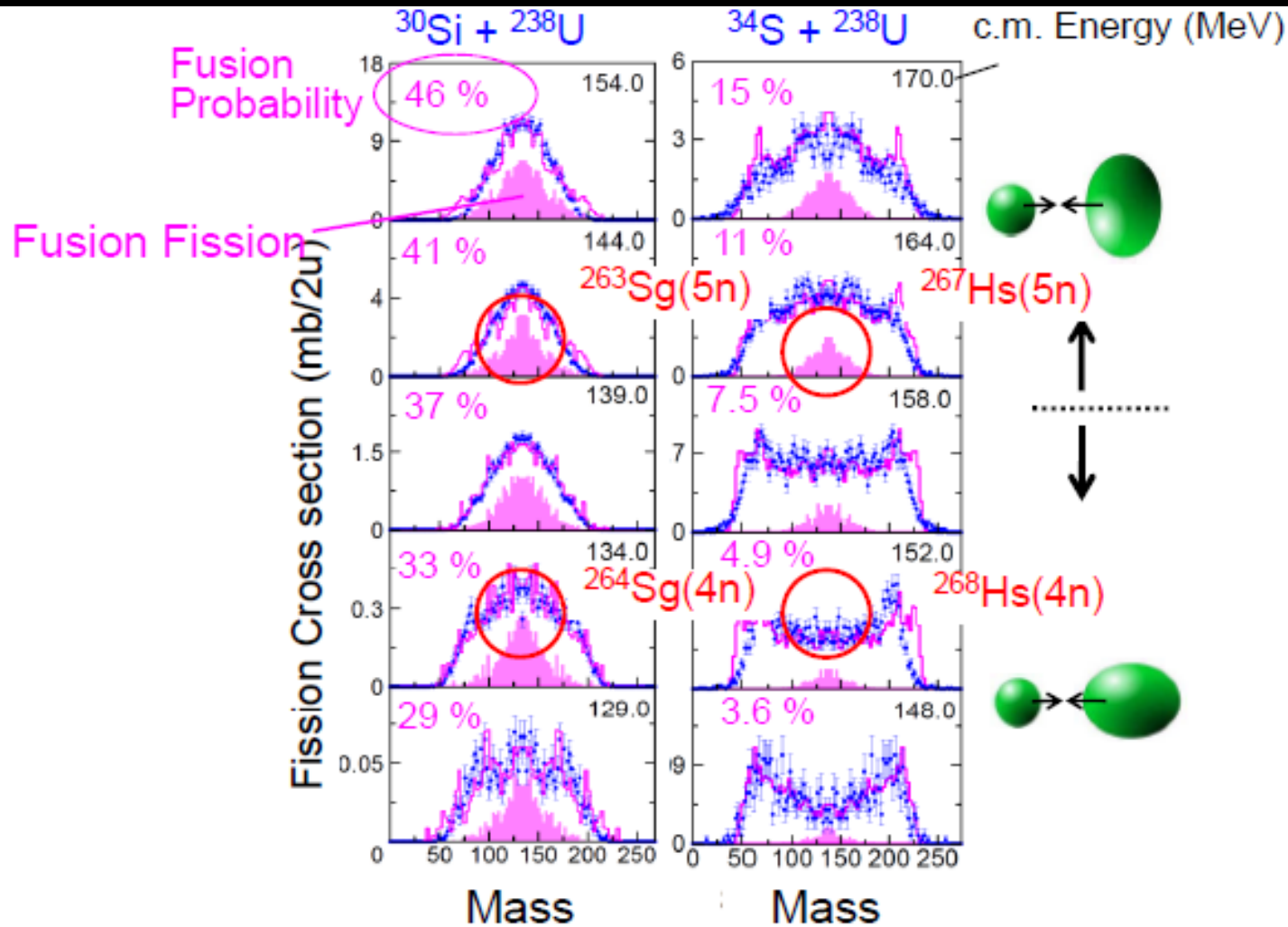


Projectile dependence of fragment mass distributions



Experiments by K. Nishio et al. (JAEA)

Calculated spectra for fusion-fission and quasi-fission

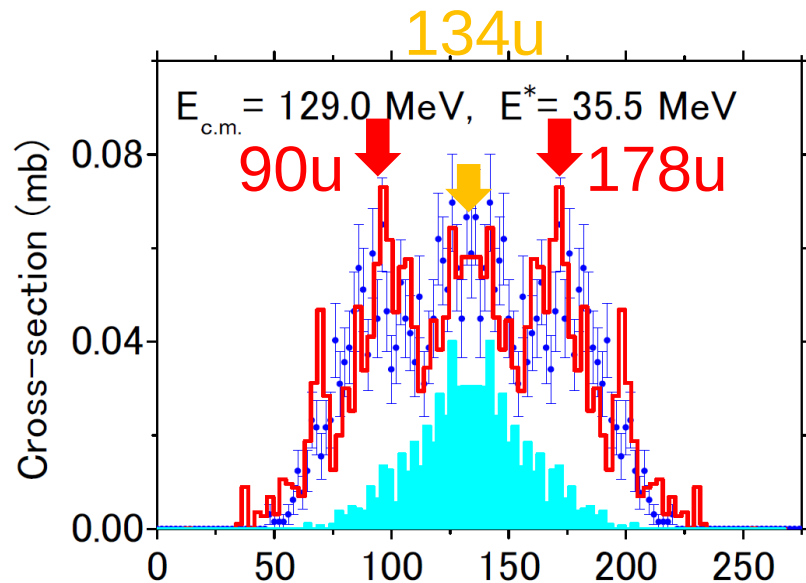


Experiments by K. Nishio et al. (JAEA)

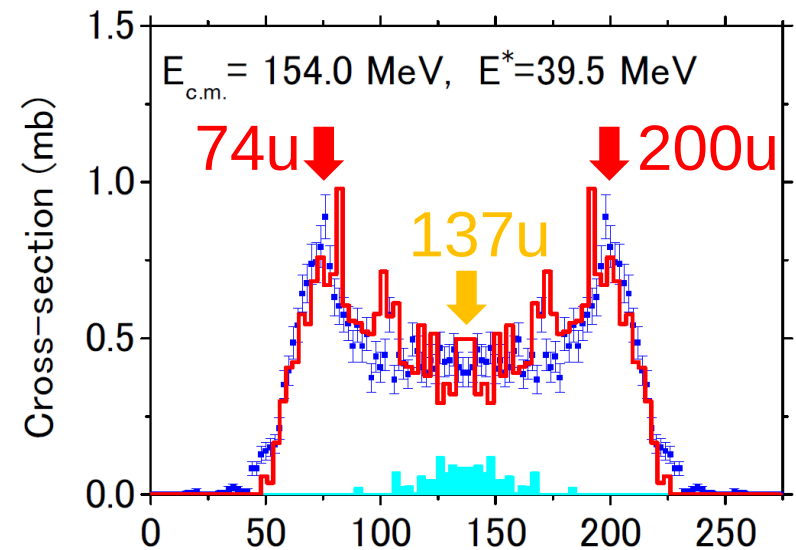
4. Mechanism of Dynamical process

MDFF at Low incident energy

$^{30}\text{Si}+^{238}\text{U}$



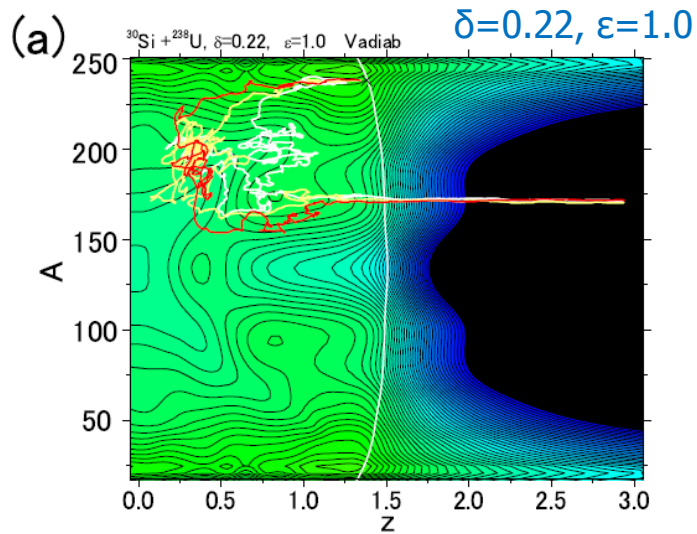
$^{36}\text{S}+^{238}\text{U}$



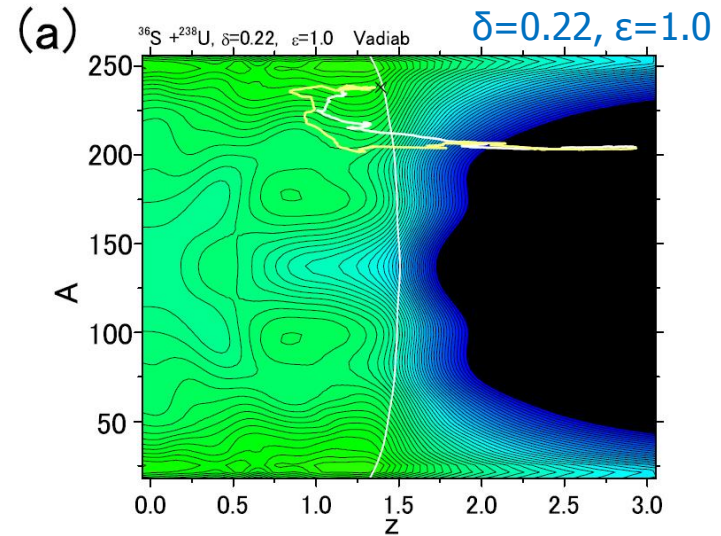
Clarify the origin of the difference

(b) Trajectory Analysis on Potential Energy Surface z-A plane

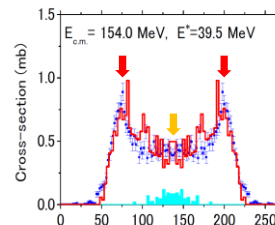
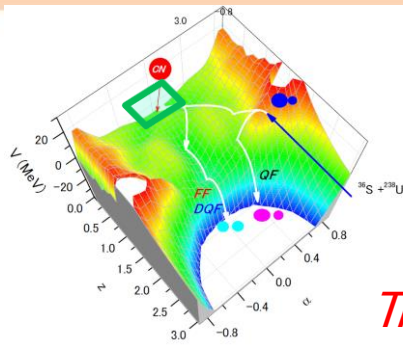
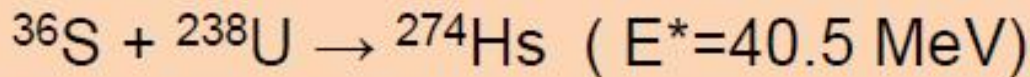
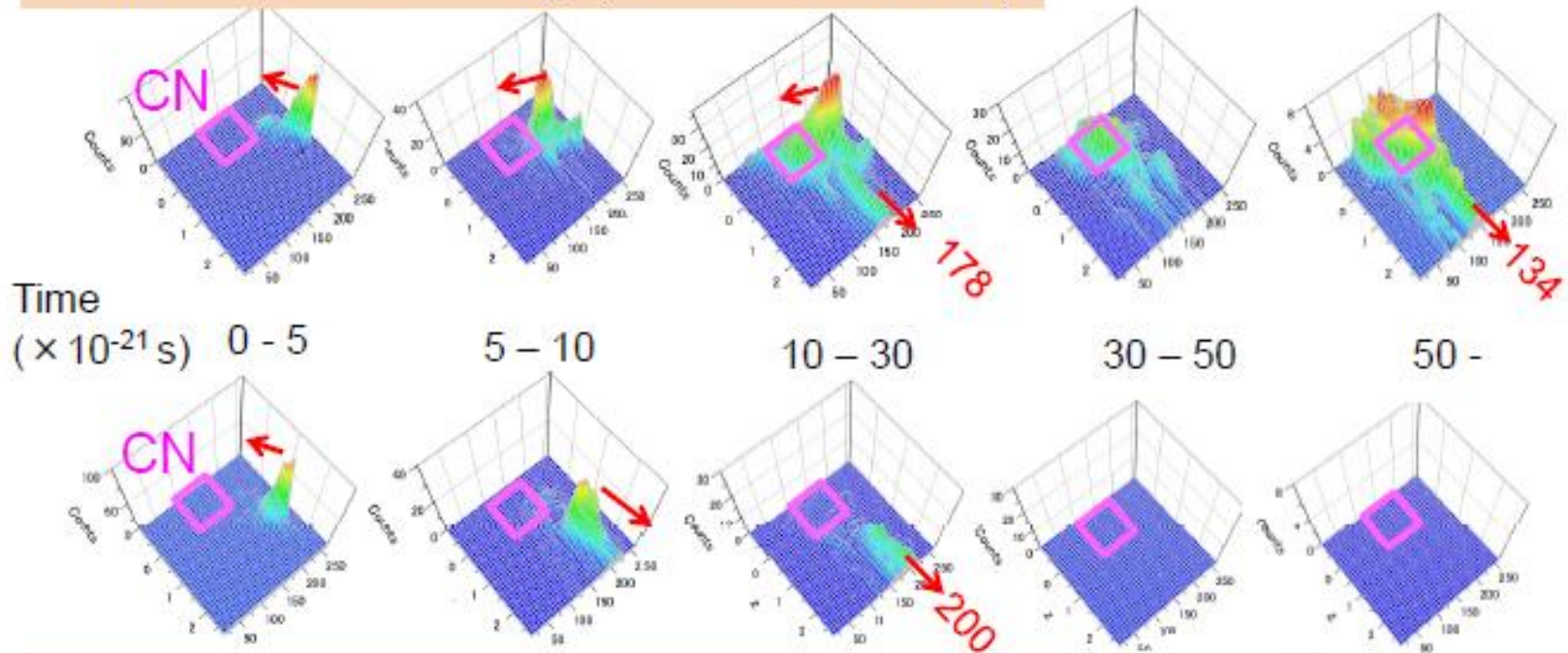
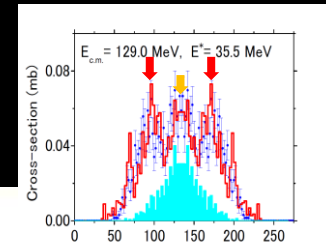
$^{30}\text{Si} + ^{238}\text{U}$ $E^* = 35.5$ MeV
 $L=0, \theta=0$



$^{36}\text{S} + ^{238}\text{U}$ $E^* = 39.5$ MeV
 $L=0, \theta=0$



Time evolution of probability distribution

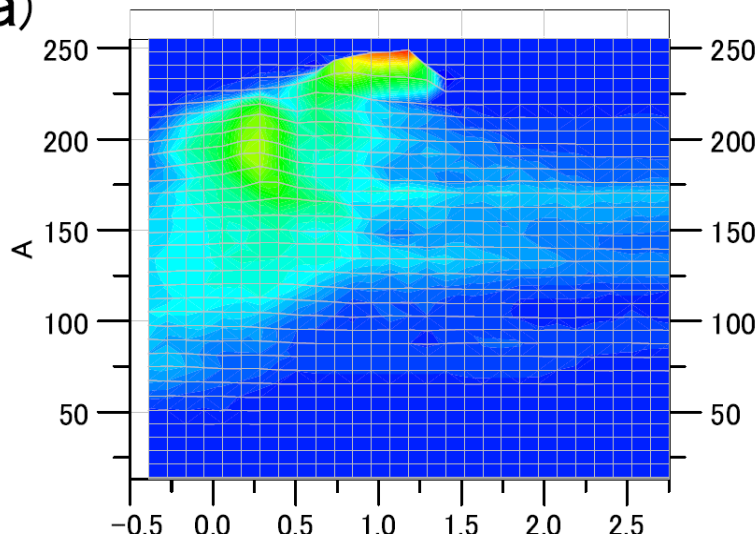


Mass Asymmetry: α
Charge Center Distance: Z

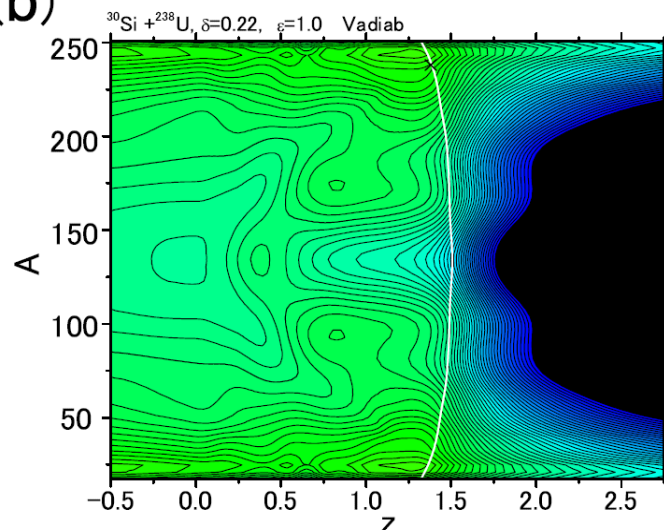
Try to clarify the origin of difference between the both cases →

Probability distribution on the z-A plane

(a)

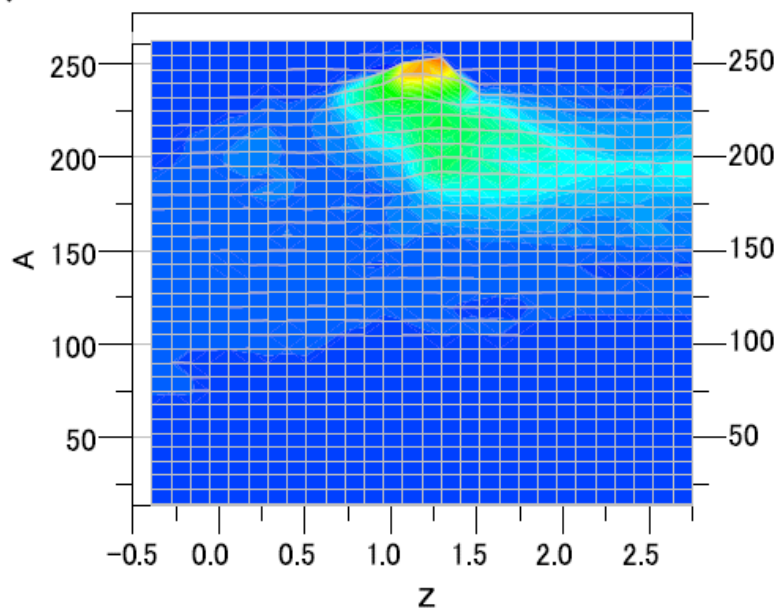


(b)

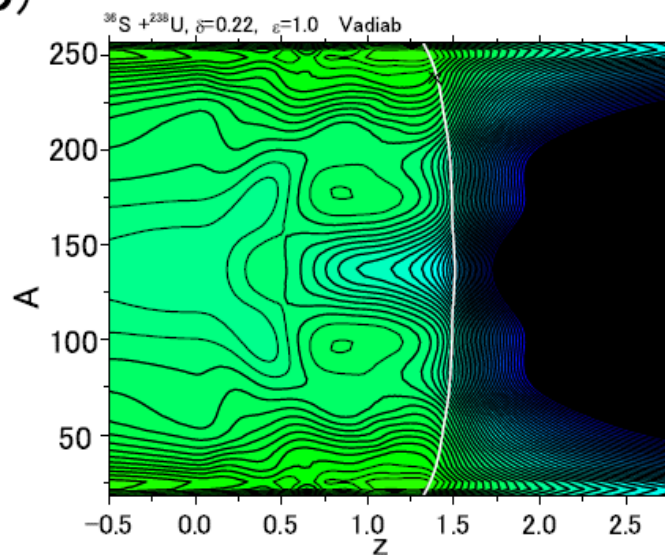


$^{30}\text{Si} + ^{238}\text{U}$

(a)



(b)

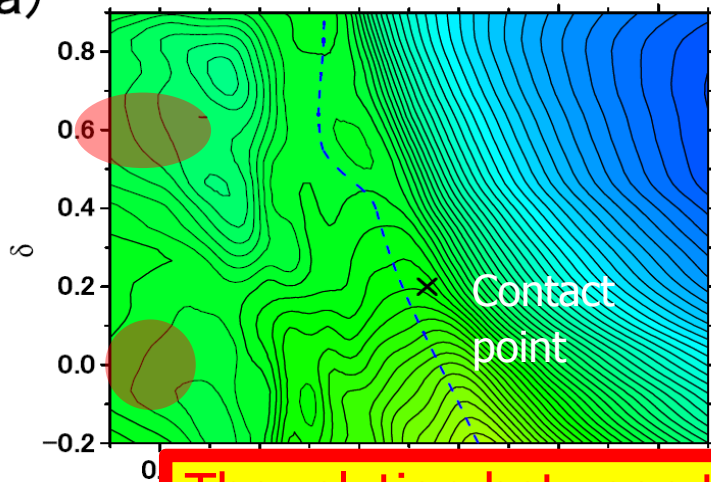


$^{36}\text{S} + ^{238}\text{U}$

Probability distribution of total time on the z - δ plane

$^{30}\text{Si} + ^{238}\text{U}$, $E^* = 35.5$ MeV

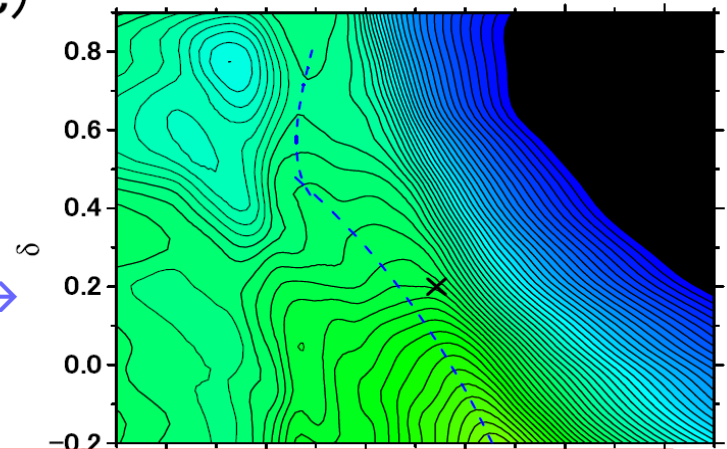
(a)



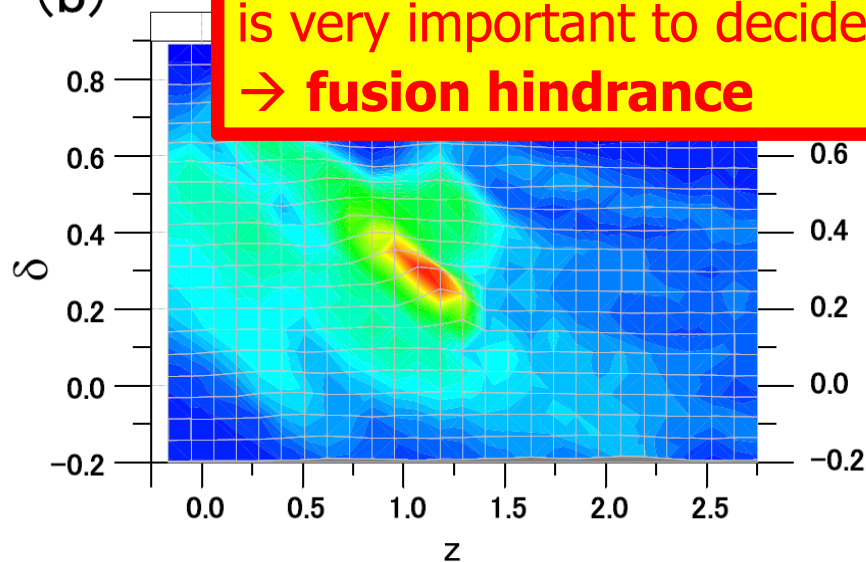
Ridge line
← steep
gentle →

$^{36}\text{S} + ^{238}\text{U}$, $E^* = 39.5$ MeV

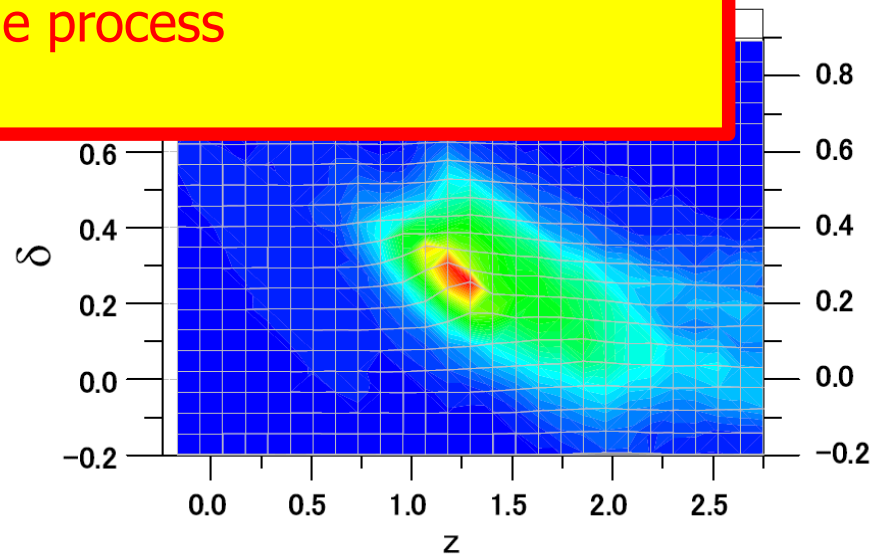
(c)



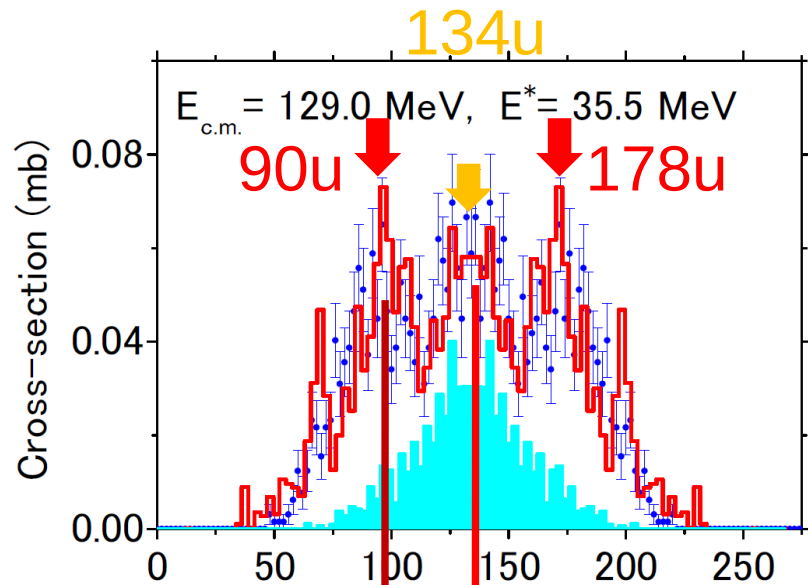
(b)



The relation between the touching point and the ridge line is very important to decide the process
→ **fusion hindrance**



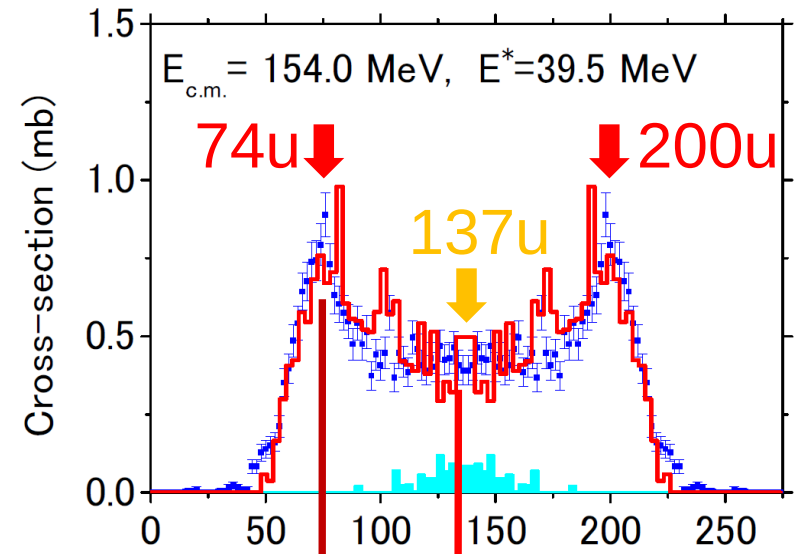
$^{30}\text{Si} + ^{238}\text{U}$



FF and DQF
 $t > 50 \times 10^{-21} \text{ sec}$
 $-0.2 < \delta < 0.2$ (peak 0)

QF via mono-nucleus
 $t < 30 \times 10^{-21} \text{ sec}$
 $0.2 < \delta < 0.5$ (peak 0.4)

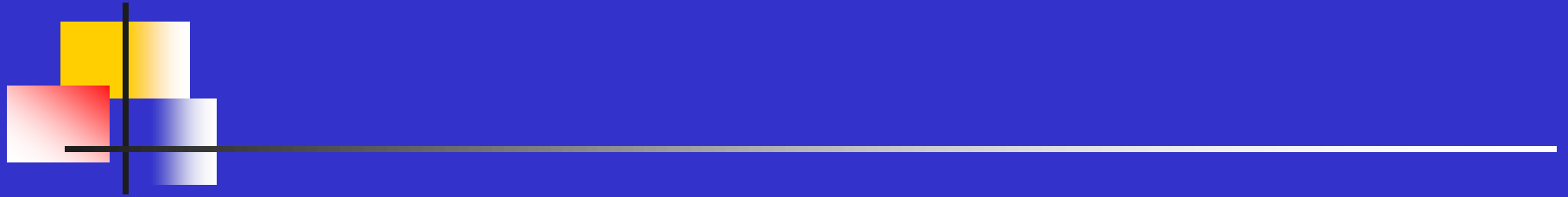
$^{36}\text{S} + ^{238}\text{U}$



FF and DQF
 $t < 30 \times 10^{-21} \text{ sec}$
 $0 < \delta < 0.4$ (peak 0.2)

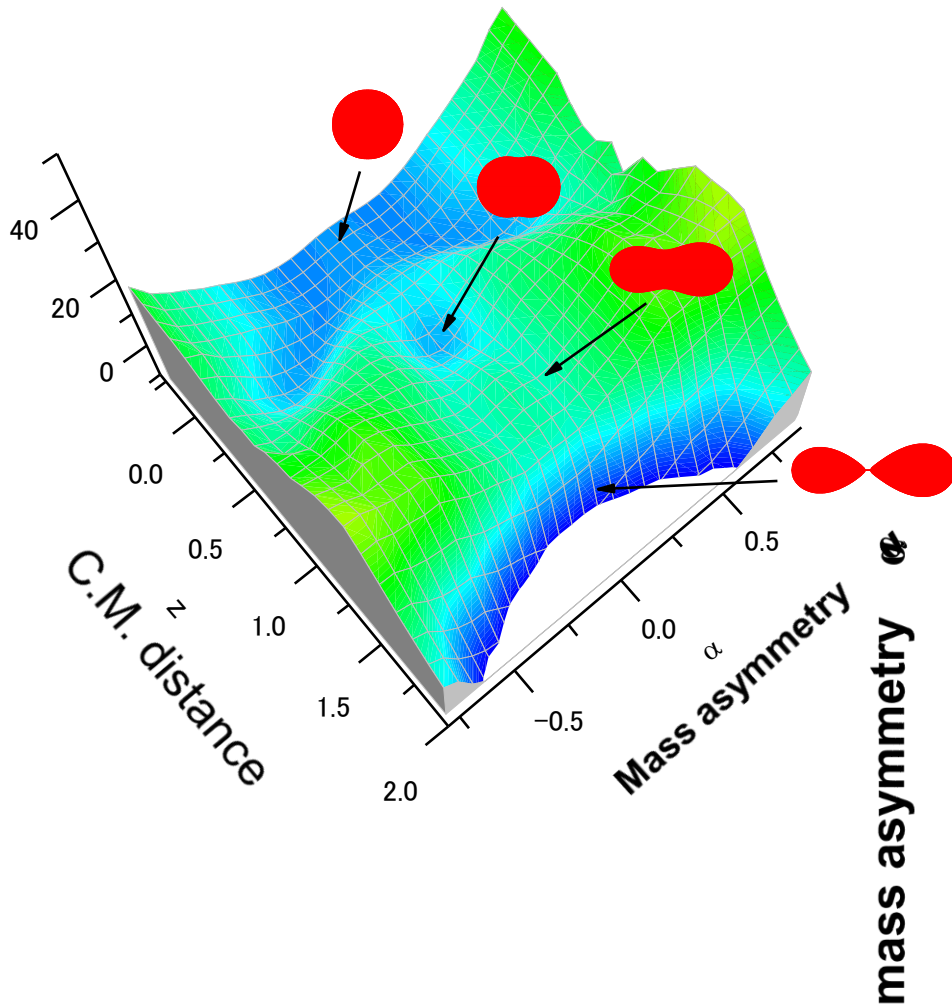
QF
 $t < 10 \times 10^{-21} \text{ sec}$
 $0 < \delta < 0.2$ (peak 0)

- (1) Origin of the reaction process
- (2) Building times
- (3) Deformation of fragments

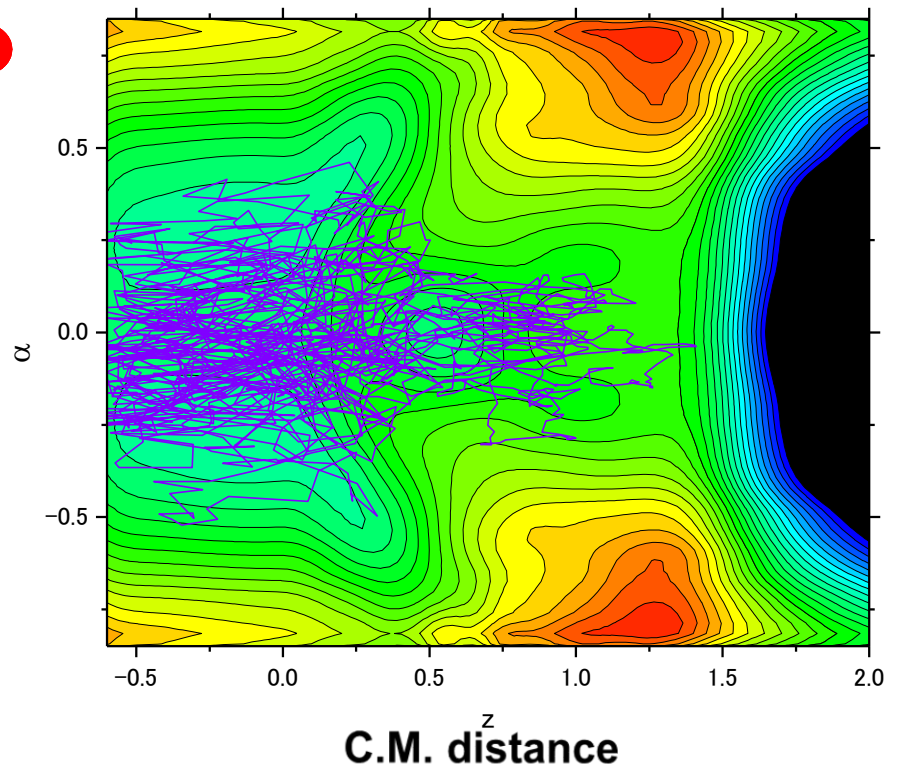


Fission Process

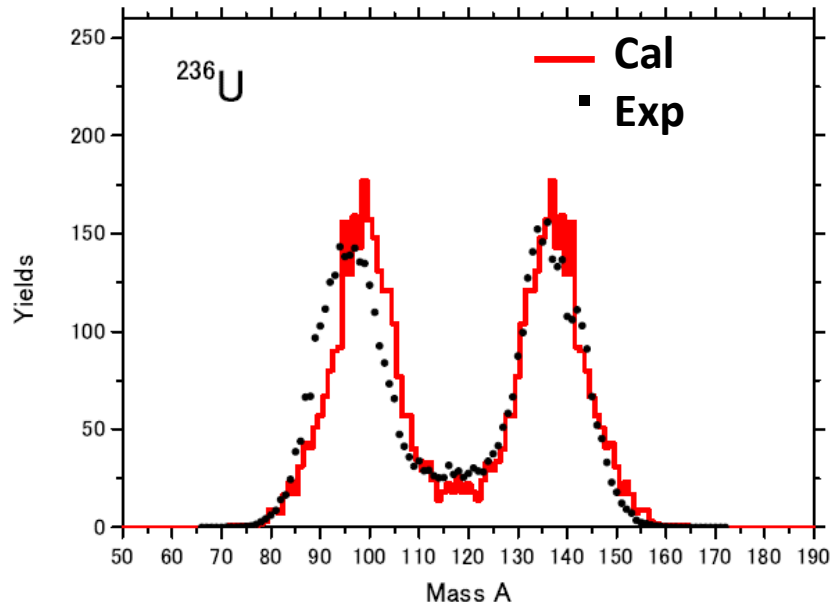
Fission process ^{240}U $E^* < 20 \text{ MeV}$



Trajectory on potential energy surface

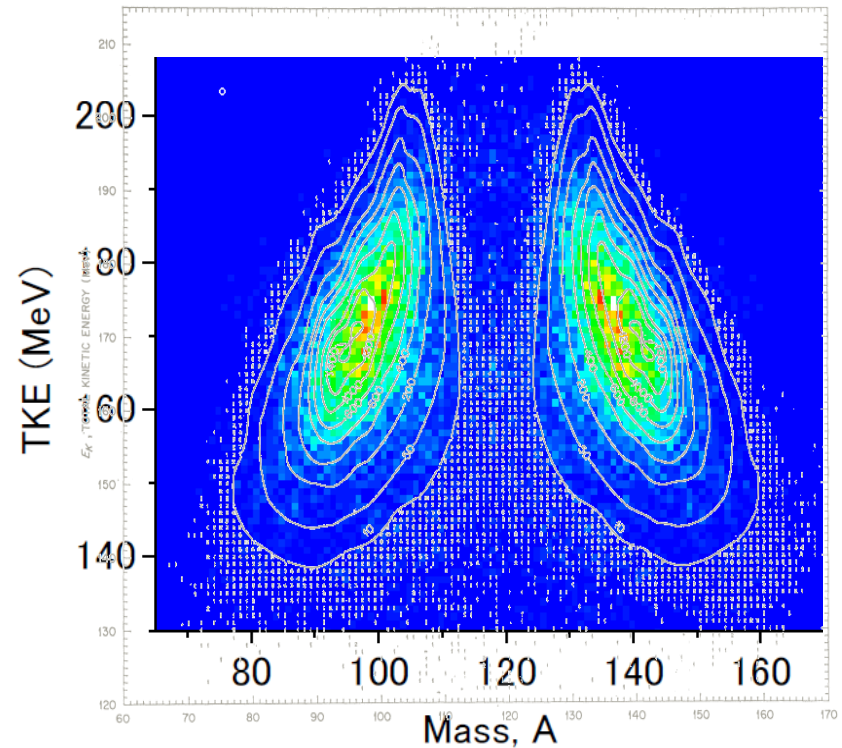


$^{236}\text{U}^*$ ($E^* = 20\text{MeV}$)



Experiment J.Katakura, JENDL FP Decay Data File 2011 and Fission Yields

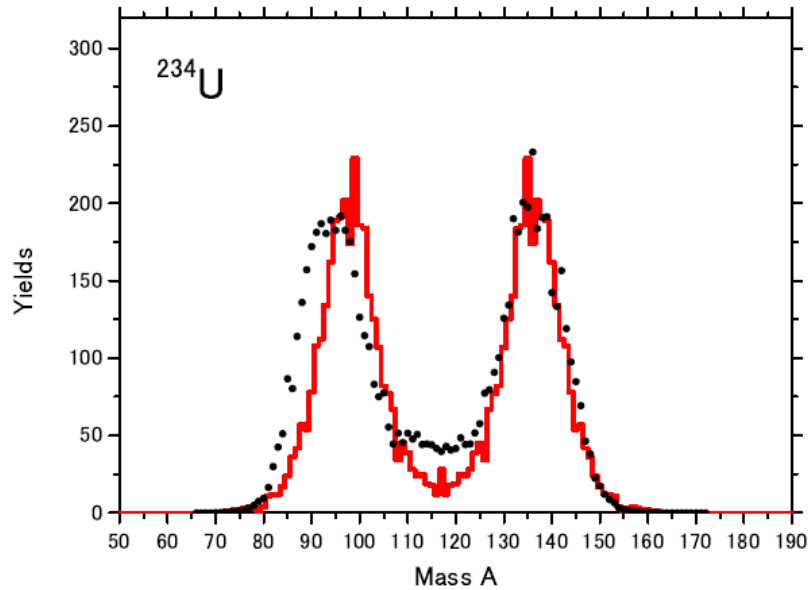
calculation Y. Aritomo and S. Chiba, PRC 88, 044614(2013)



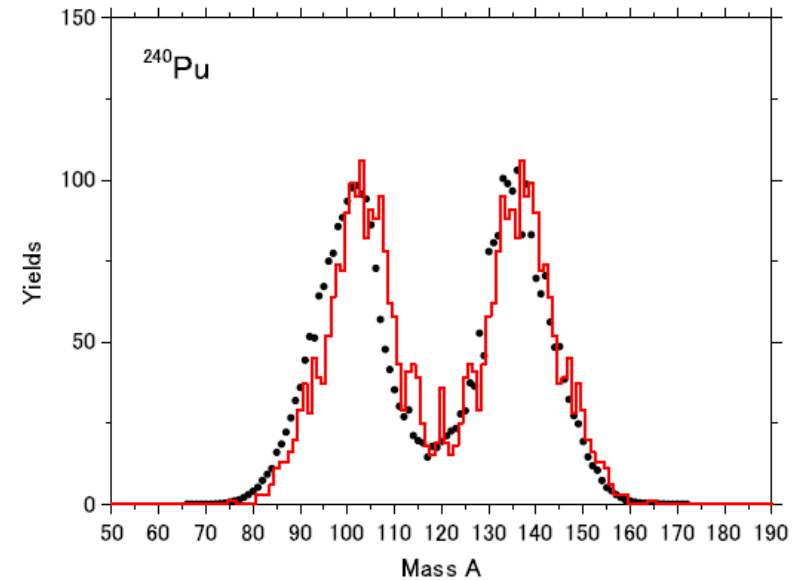
Exp. Phys.Rev. **141**(1966)1146

Mass distribution of fission fragments $E^* = 20 \text{ MeV}$

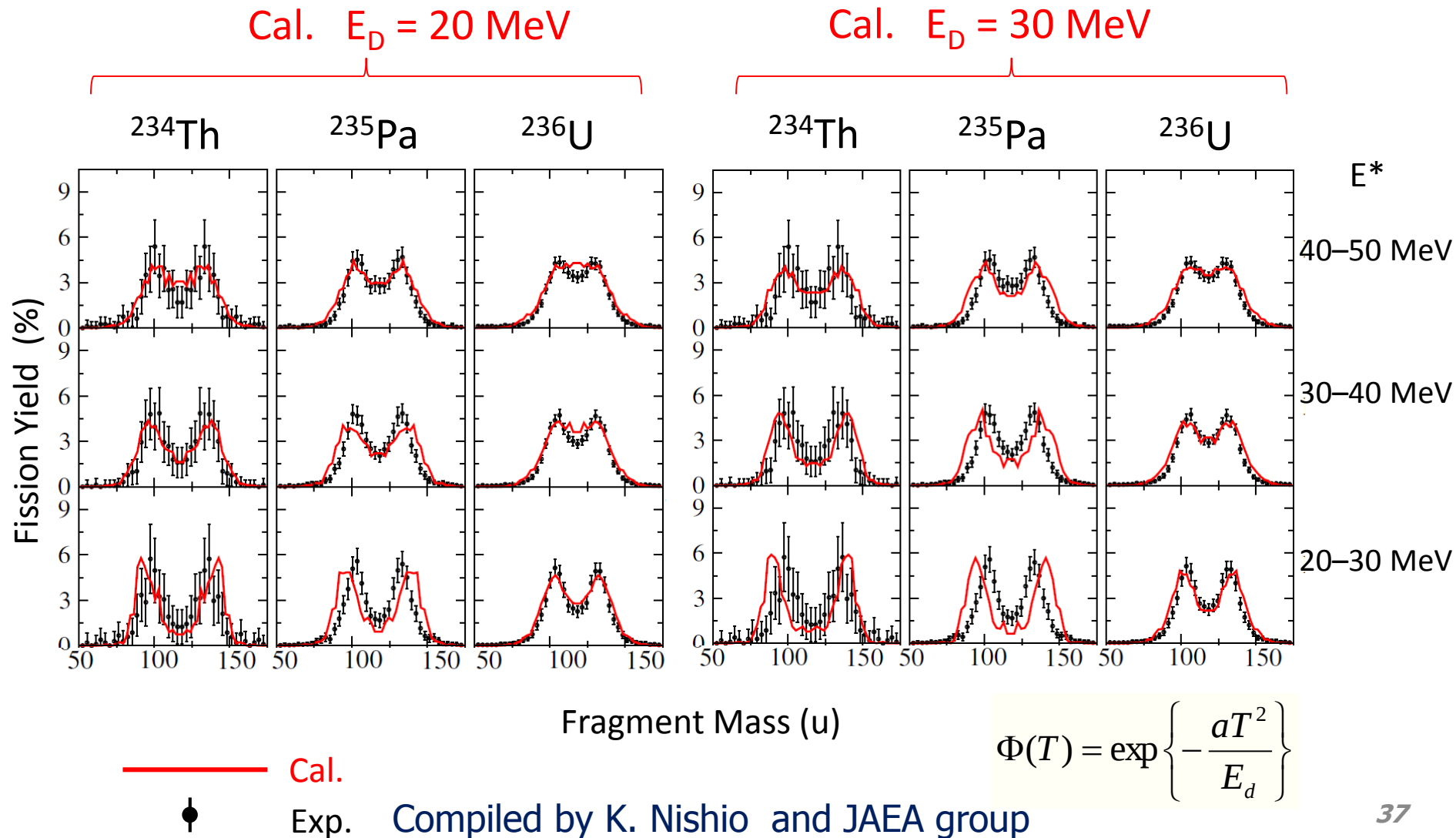
^{234}U



^{240}Pu



Comparison between Cal. and Exp.



5. Summary

1. In order to analyze the fusion-fission process in superheavy mass region, we apply the Couple channels method + Langevin calculation.
2. Incident energy dependence of mass distribution of fission fragments (MDFF) is reproduced in reaction $^{36}\text{S}+^{238}\text{U}$ and $^{30}\text{Si}+^{238}\text{U}$.
3. The shape of the MDFF is analyzed using *probability distribution*
4. The relation between the touching point and the ridge line is very important to decide the process → fusion hindrance

And....

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