

# Progress in microscopic shell model for medium-mass nuclei and nuclear matrix elements

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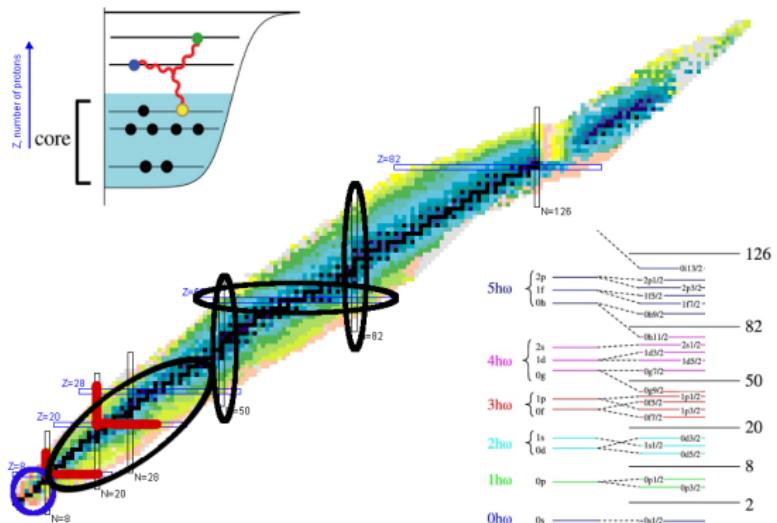
# Outline

- 1 Nuclear structure of medium-mass nuclei
- 2 Matrix elements for  $\beta\beta$  decay
- 3 Dark Matter scattering off nuclei

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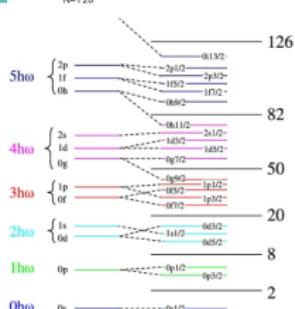
# Nuclear landscape



Big variety of nuclei in the nuclear chart,  $A \sim 2\ldots 300$

Systematic *ab initio* calculations only possible in the lightest nuclei

Hard many-body problem:  
approximate methods suited  
for different regions



Shell Model: Choose relevant degrees of freedom (valence space)

Interactions based on realistic nucleon-nucleon (NN) potentials  
phenomenological modifications  $\Rightarrow$  three-nucleon (3N) interactions

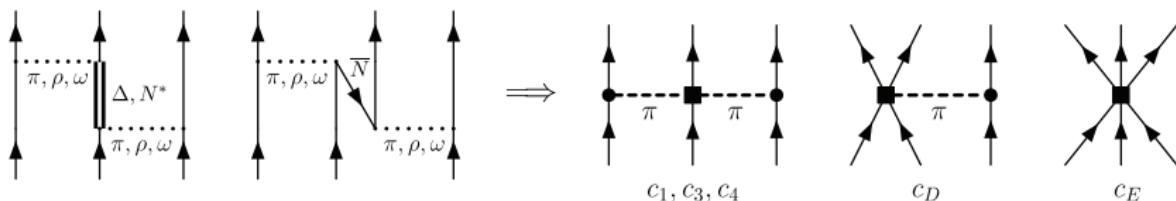
# Three-nucleon forces

3N forces known for a long time (also 2b currents)

Fujita and Miyazawa PTP17 (1957), Towner Phys. Rep. 155 (1987)...

3N forces originate in the elimination of degrees of freedom  
(N-body forces appear in any effective theory)

Bogner, Schwenk, Furnstahl PPNP65 94 (2010)



Difficult to constrain directly

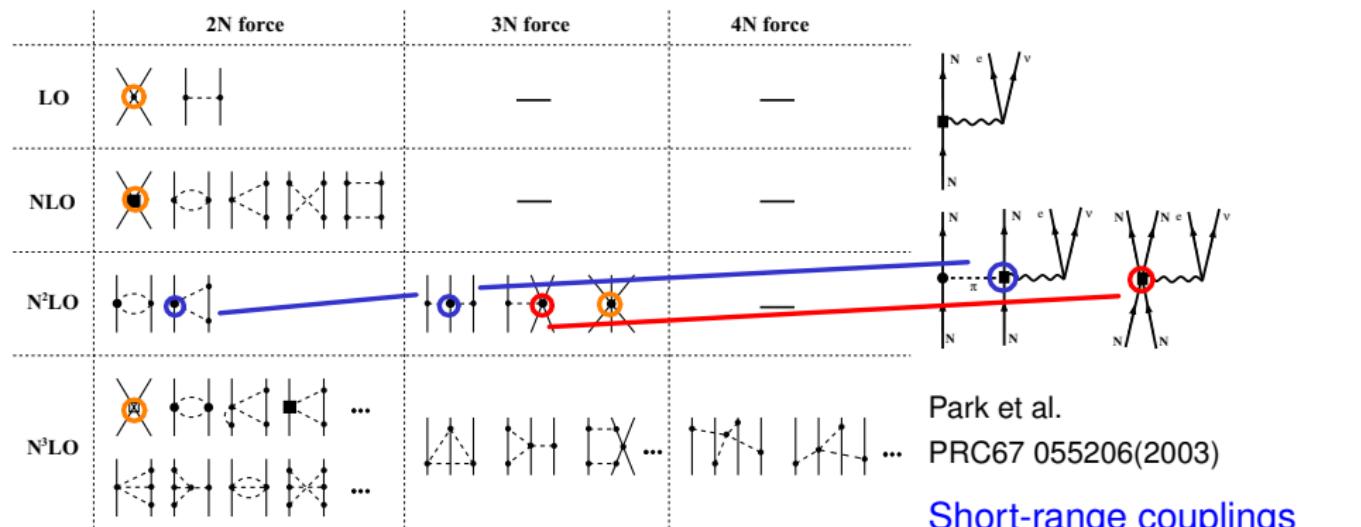
⇒ Chiral EFT, in a natural and systematic manner,  
treats 3N forces consistent with NN forces (same for 2b and 1b currents)

# Chiral Effective Field Theory

Chiral EFT: low energy approach to QCD, nuclear structure energies

Approximate chiral symmetry: pion exchanges, contact interactions

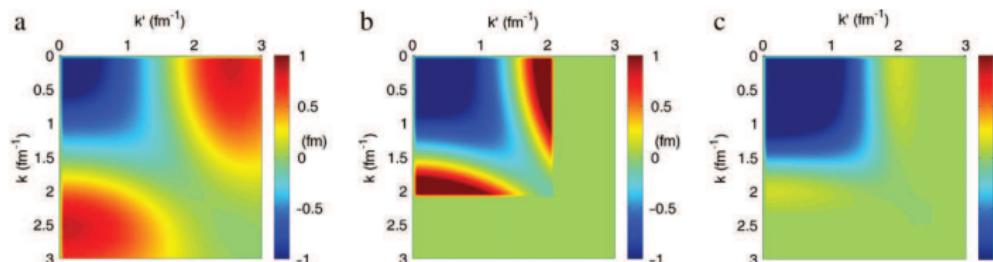
Systematic expansion: nuclear forces and electroweak currents



Weinberg, van Kolck, Kaplan, Savage, Weise, Epelbaum, Meißner...

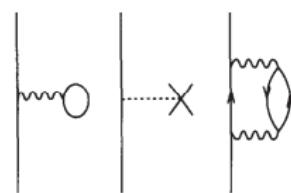
# Many Body Perturbation Theory

Better convergence of chiral forces after RG transformation

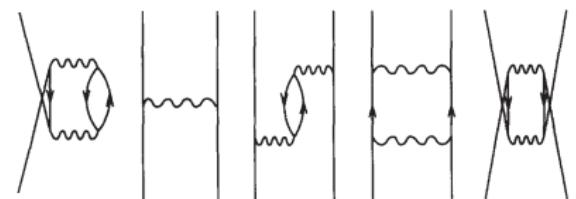


Many-body perturbation theory to third order:  
obtain effective  
Shell Model interaction  
in the valence space

Single Particle Energies



Two-Body Matrix Elements



Effective Hamiltonian in valence space:

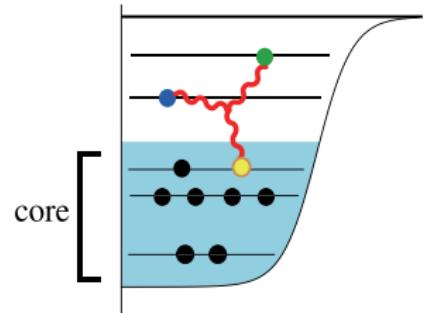
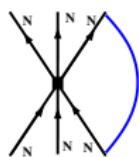
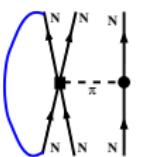
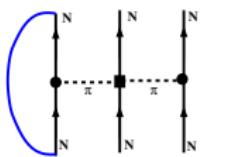
$$H |\Psi\rangle = E |\Psi\rangle \rightarrow H_{\text{eff}} |\Psi\rangle_{\text{eff}} = E |\Psi\rangle_{\text{eff}}$$

3N couplings  $c_D$ ,  $c_E$  fitted with evolved NN forces (induced + initial 3N forces)

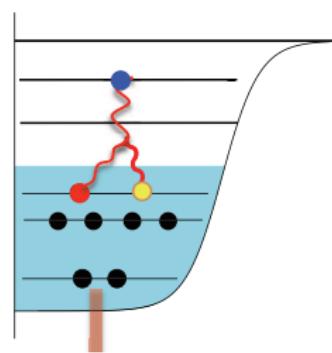
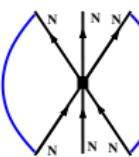
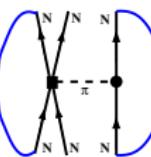
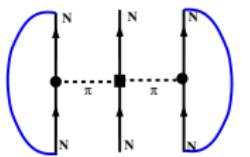
# 3N Forces: Normal ordering

3N forces in normal-ordering approximation:

normal-ordered 2B: 2 valence, 1 core particle  
⇒ Two-body Matrix Elements



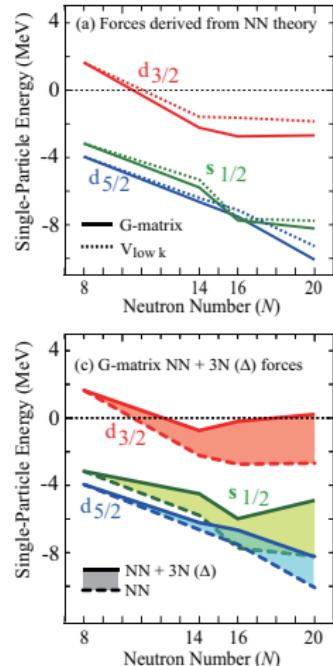
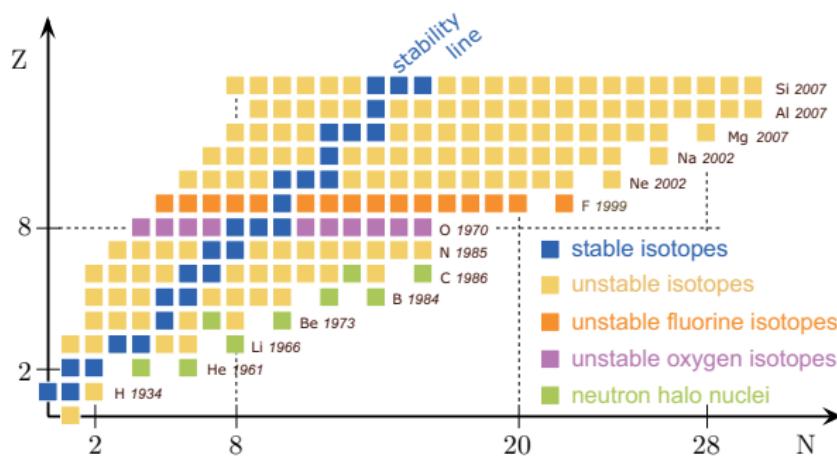
normal-ordered 1B: 1 valence, 2 core particles  
⇒ Single particle energies



3N forces in  $H_{\text{eff}}$  treated to third order in MBPT

# Oxygen dripline anomaly and 3N forces

O isotopes: 'anomaly' in the dripline at  $^{24}\text{O}$ , doubly magic nucleus



Calculations based on chiral NN+3N forces  
and MBPT correctly predict dripline at  $^{24}\text{O}$

Otsuka et al. PRL105 032501 (2010)

# Oxygen dripline in ab-initio calculations

Oxygen dripline including chiral NN+3N forces correctly reproduced confirmed in ab-initio calculations by different approaches, treating explicitly all nucleons as degrees of freedom

No-core shell model  
(Importance-truncated)

In-medium SRG

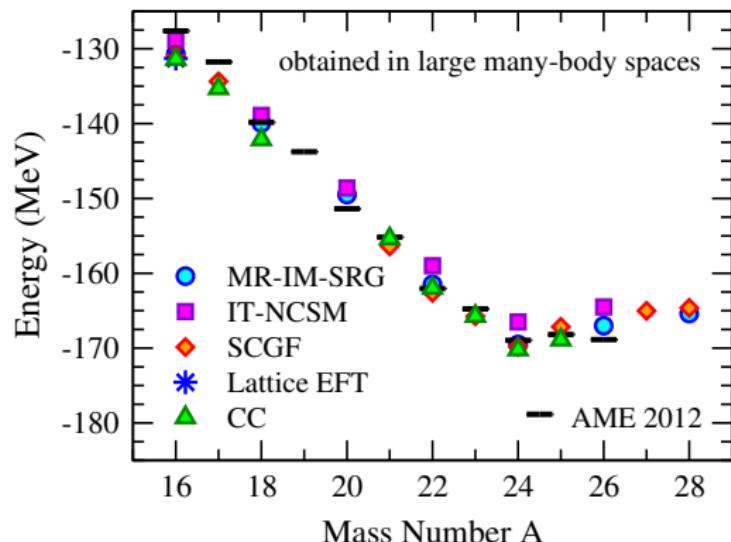
Hergert et al. PRL110 242501 (2013)

Self-consistent Green's function

Cipollone et al. PRL111 062501 (2013)

Coupled-cluster

Jansen et al. PRL113 142502 (2014)



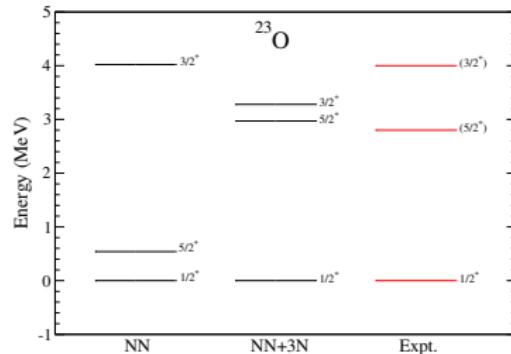
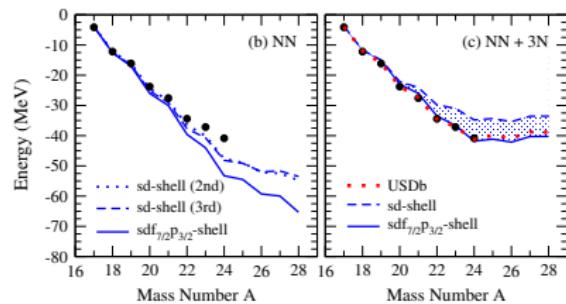
Benchmark with the same initial Hamiltonian

Sensitivity to the chiral interaction not systematically explored

# O isotopes: excitation spectra

NN+3N calculations good description of excitation spectra

Holt, JM, Schwenk EPJA49 39 (2013)

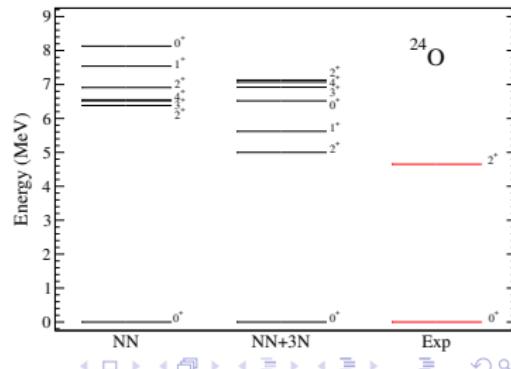


Spectroscopic factors for  $s_{1/2}$  orbital  
good agreement with experiment, closed  $^{24}\text{O}$



Kanungo et al.

PRL102 152501 (2010); PST152 014002(2013)

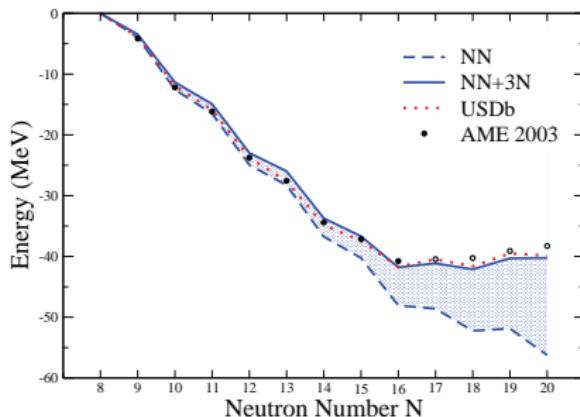
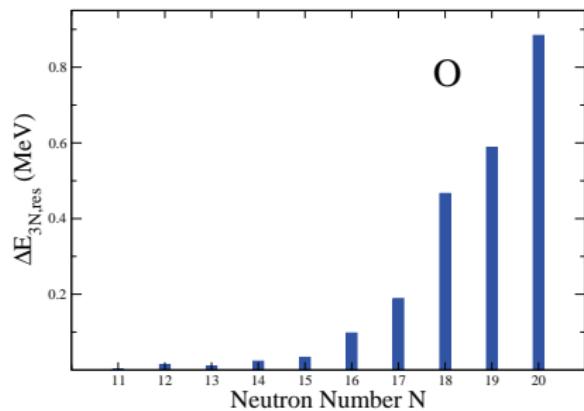
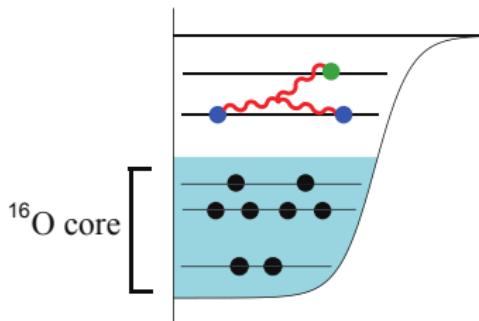


# Residual 3N Forces

Previous results with normal-ordered  
1b and 2b part of 3N forces

In extreme neutron-rich oxygen isotopes,  
3N forces between 3 valence neutrons  
can give a relevant contribution

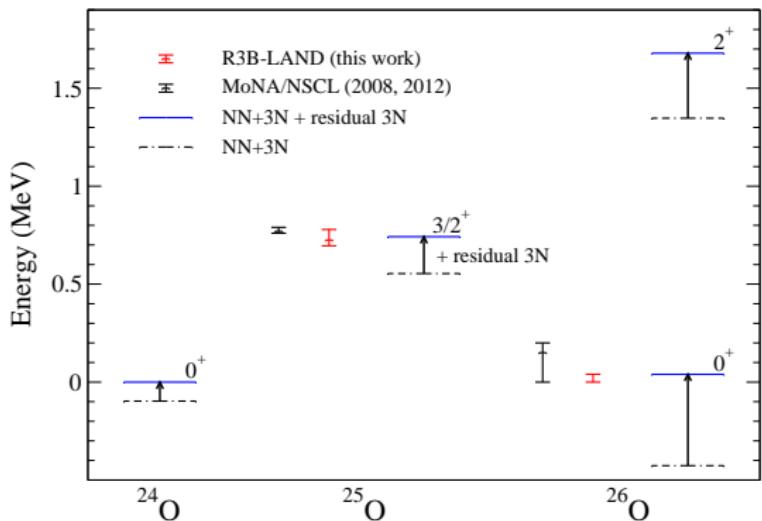
Evaluated perturbatively:  $\langle \Psi | V^{3N} | \Psi \rangle$



Residual 3N small and repulsive Caesar, Simonis et al. PRC88 034313 (2013)

# Beyond the oxygen dripline

Oxygen isotopes beyond the dripline can be accessed with residual 3N forces



Repulsive residual 3N contributions

Small compared to normal-ordered 3N force increase with  $N$

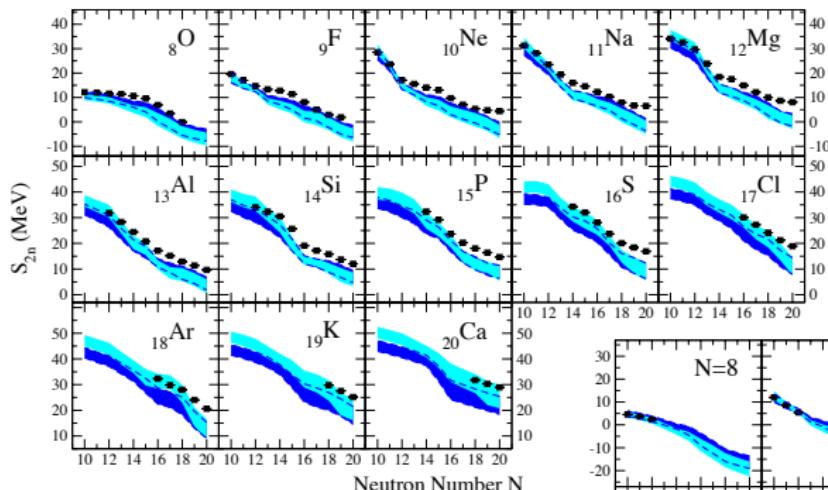
Very good agreement with resonances in  $^{25}\text{O}$  and  $^{26}\text{O}$

Caesar, Simonis et al.  
PRC88 034313 (2013)

Challenge: include continuum degrees of freedom in the calculation

Hagen et al. PRL108 242501 (2012)

# Full sd-shell calculation



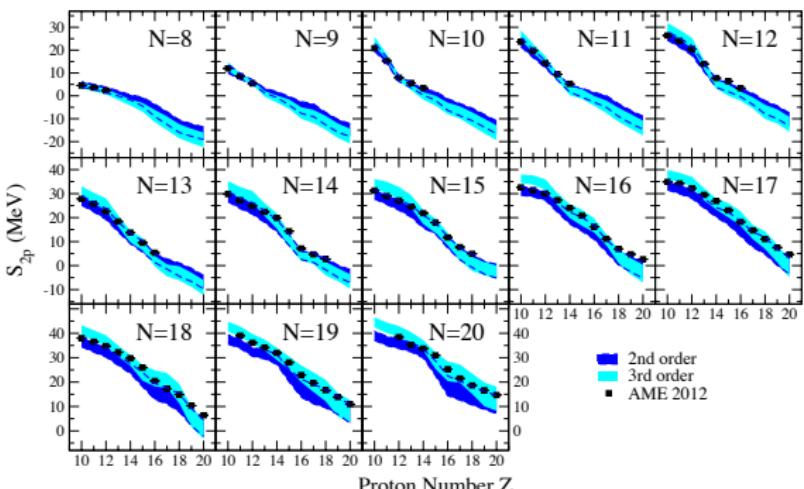
Uncertainty band including  
different SRG resolution scales  
and low-energy couplings

Second and third-order  
MBPT results

Typical uncertainties 5MeV,  
larger for neutron-rich systems

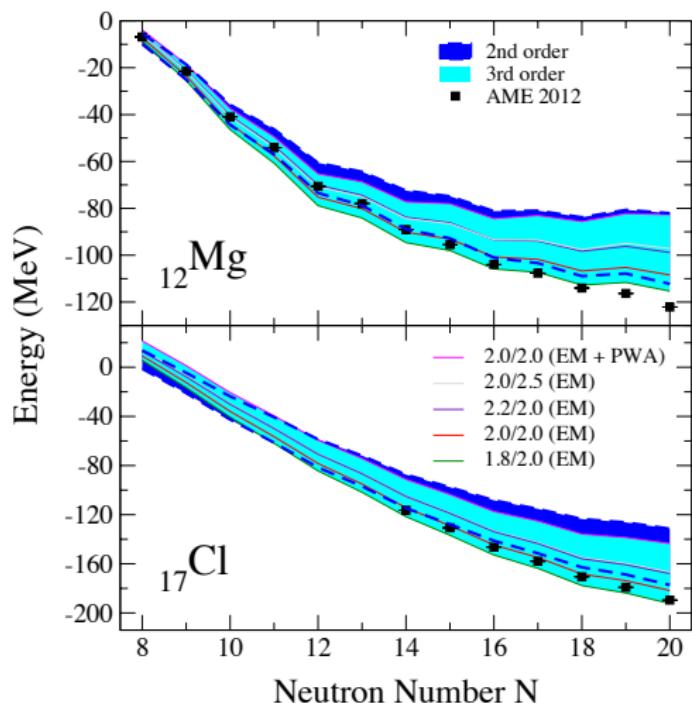
Full sd-shell calculation  
with chiral NN+3N forces

Fit only to two, three and  
four-body systems



# Nuclei in *sd* shell and theoretical uncertainties

Extend the study to *sd*-shell nuclei, proton-neutron interaction included



Explore the theoretical sensitivity:

Initial chiral Hamiltonian

RG evolution of NN, 3N forces

Convergence in MBPT

Use Hamiltonians with good nuclear saturation properties  
Hebeler et al. PRC 83 031301 (2011)

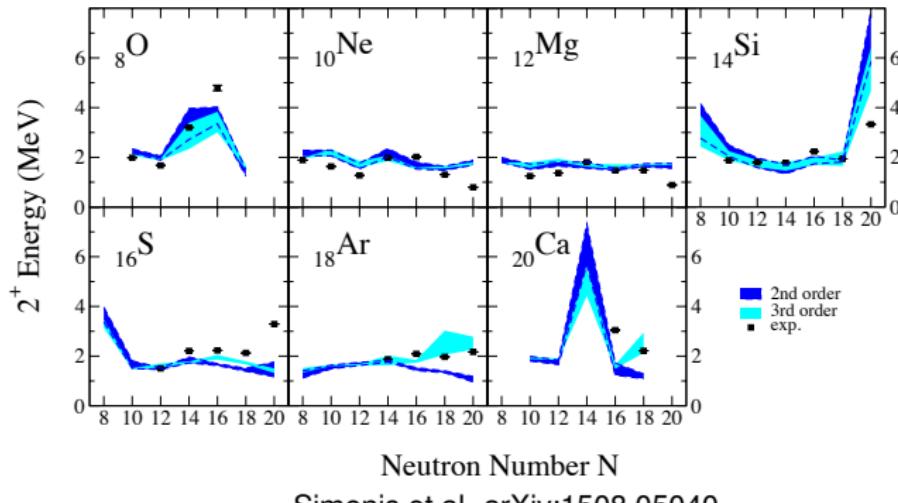
Magnesium ground-state energies underbound, Chlorine good agreement to experiment

Not enough neutron-neutron binding in *sd* shell

Uncertainties dominated by initial nuclear Hamiltonian

# $2^+$ energies in *sd*-shell nuclei

Energies of lowest  $2^+$  states less sensitive to the initial Hamiltonian



Simonis et al. arXiv:1508.05040

$2^+$  energies in *sd* shell reasonably well reproduced

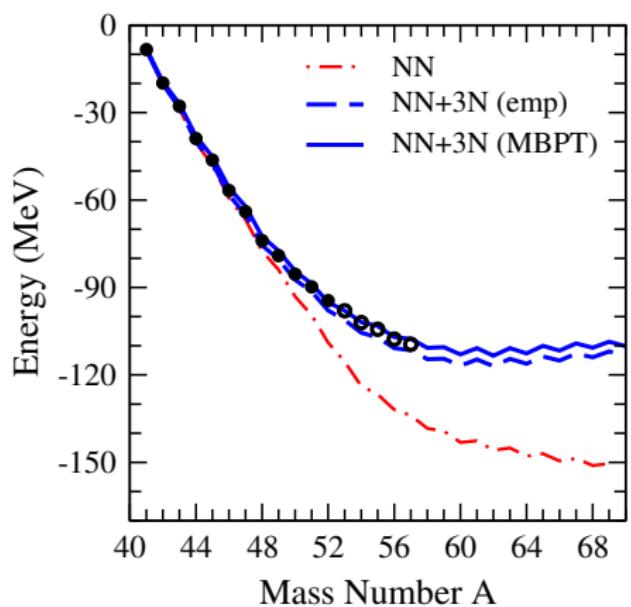
Typical uncertainties  $\sim 500$  keV,

MBPT convergence more important in semi-magic nuclei

Island-of-inversion states in Ne, Mg, not reproduced in *sd* shell calculation

# Ca isotopes: masses

Ca isotopes: explore nuclear shell evolution  $N = 20, 28, 32?, 34?$

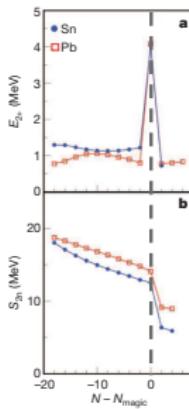


Ca measured from  $^{40}\text{Ca}$  core  
in  $\text{pf}g_{9/2}$  valence space

3N forces repulsive contribution,  
chiral NN-only forces too attractive

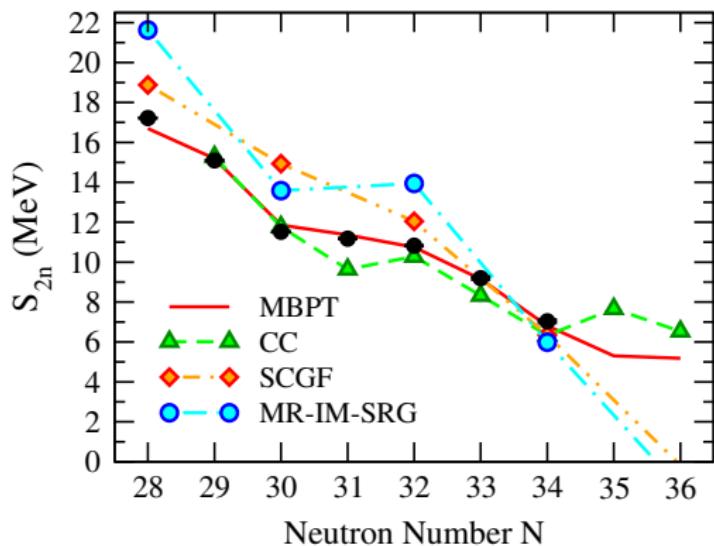
Probe shell  
evolution:  
Mass-differences  
 $2_1^+$  energies

Jones et al.  
Nature 465 454 (2010)



# Calcium two-neutron separation energies

Measurement of  $^{51,52}\text{Ca}$  at TRIUMF and  $^{53,54}\text{Ca}$  at ISOLDE



Excellent agreement of MBPT prediction with experiment

$S_{2n}$  evolution:  
 $^{52}\text{Ca}-^{54}\text{Ca}$  decrease  
similar to  $^{48}\text{Ca}-^{50}\text{Ca}$   
unambiguously establishes  
 $N = 32$  shell closure

Phenomenological interactions  
GXPF1A and KB3G  
also good description of  
experiment up to  $^{54}\text{Ca}$

Coupled-cluster, SCGF, IM-SRG  
reasonable agreement  
with experiment

Gallant et al. PRL 109 032506 (2012)

Wienholtz et al. Nature 498 346 (2013)

Hagen et al. PRL 109 032502 (2012)

Somà et al. PRC 89 061301 (2014)

Hergert et al. PRC 90 041302 (2014)

# Calcium $2_1^+$ energies

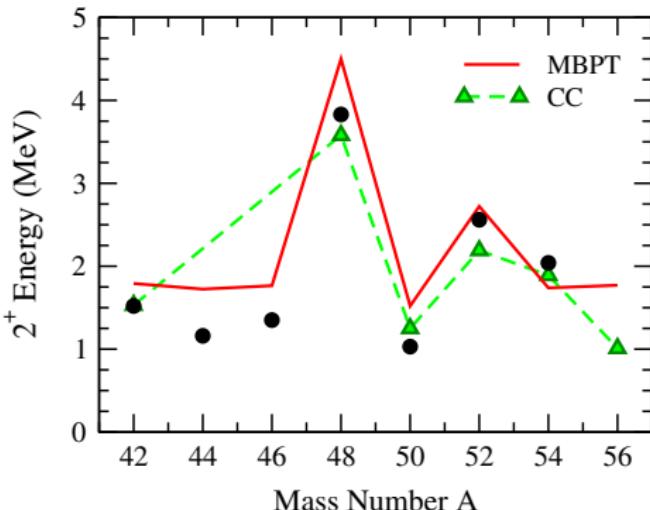
$2_1^+$  energies characterize shell closures

Correct closure at  $N = 28$   
when 3N forces are included

Holt et al. JPG39 085111 (2012)

Holt, JM, Schwenk, JPG40 075105 (2013)

Hagen et al. PRL 109 032502 (2012)

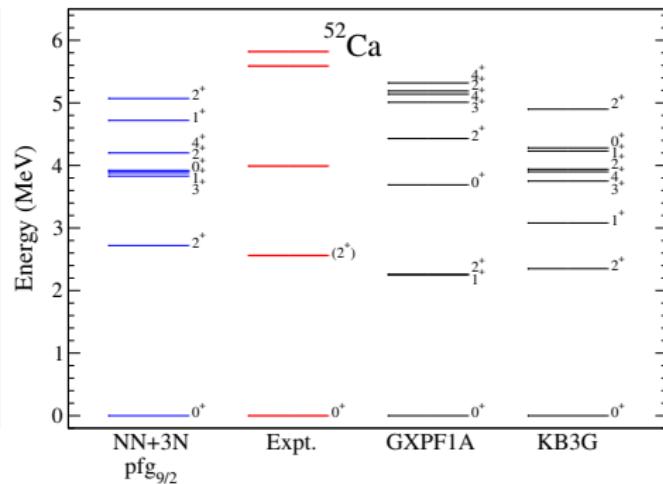
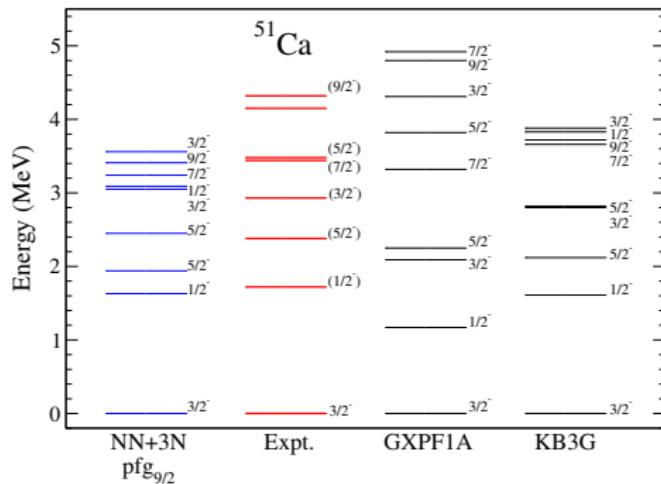


- High  $2^+$  in  $^{32}\text{Ca}$  related to closure at  $N = 32$
- Relatively high  $2^+$  in  $^{32}\text{Ca}$  measured at RIBF indicate closure at  $N = 34$   
to be confirmed in mass, B(E2) measurements  
Steppenbeck et al. Nature 502 207 (2013)



# Excitation spectra

## Spectra for neutron-rich calcium isotopes

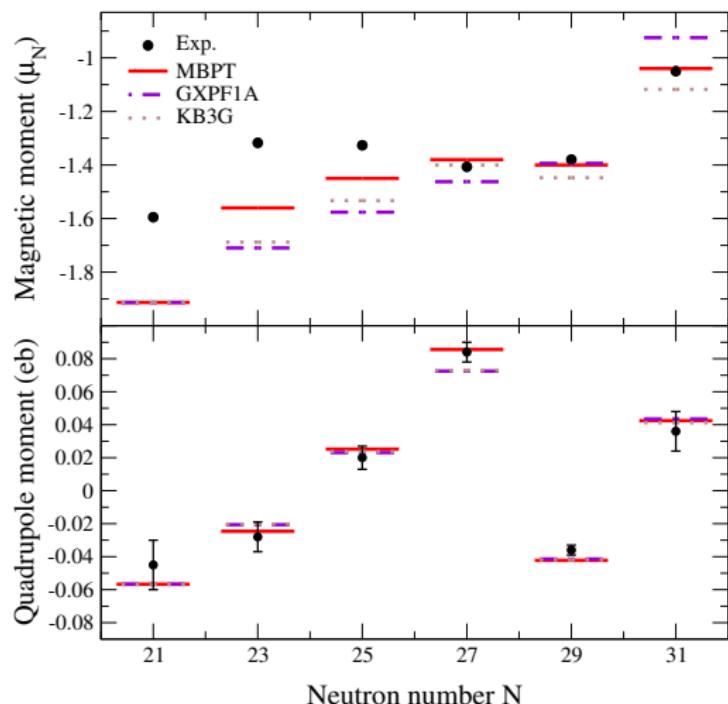


Good agreement with experiment, comparable to phenomenological interactions, and predictions given for heavier systems

Holt, JM, Simonis, Schwenk PRC90 024312 (2014)

# Calcium magnetic and quadrupole moments

Electric quadrupole moments and magnetic moments  
in ground states of calcium isotopes measured by COLLAPS at ISOLDE



Consistent description of  
ground-state masses  
and spectroscopy

Very good agreement to  
experiment,  
up to neutron-rich systems

Comparable to  
phenomenological interactions

Phenomenological effective  
charges  $q_n = 0.5e$ ,  
and bare g-factor  $g_s(\text{bare})$

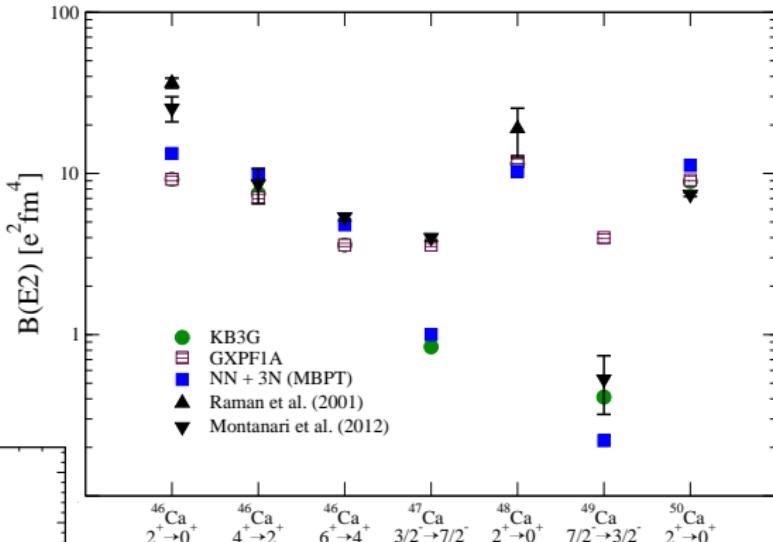
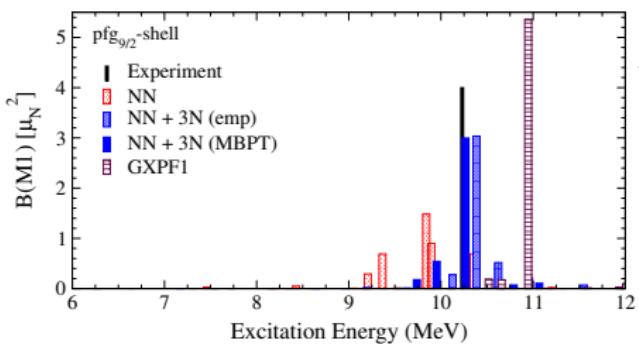
Garcia Ruiz et al.

PRC91 041304 (2015)

# Calcium electromagnetic transitions

B(E2)s in reasonable agreement  
with experiment  
span three orders of magnitude

Similar quality as  
phenomenological interactions



B(M1) strength in  $^{48}\text{Ca}$   
NN+3N good agreement  
experiment strength and energy  
quenched g-factor  $g_s = 0.75g_s(\text{bare})$

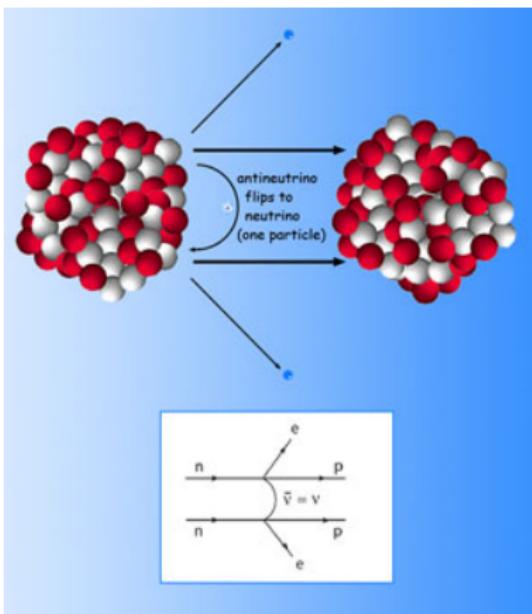
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# Neutrinoless $\beta\beta$ decay, Dark Matter detection



## Neutrinoless double-beta decay

Lepton number violation

Majorana / Dirac nature of neutrinos  
Neutrino masses and hierarchy



Dark matter scattering off nuclei

What is Dark Matter made of?

# Nuclear physics and fundamental symmetries

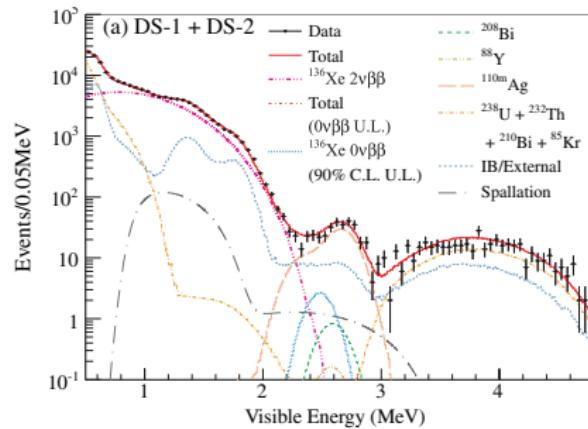
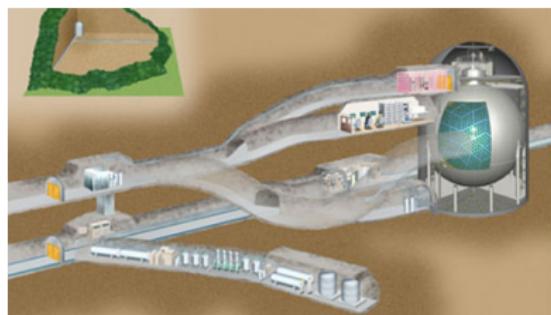
Neutrinos, Dark Matter can be studied with high-energy experiments

Nuclear physics offers an alternative:

Nuclei are abundant in huge numbers  $N_A = 6.02 \cdot 10^{23}$  nuclei in A grams!

Lots of material over long times provides access to detect  
very rare decays and very small cross-sections!

Isolate from other processes:  
very low background (underground)

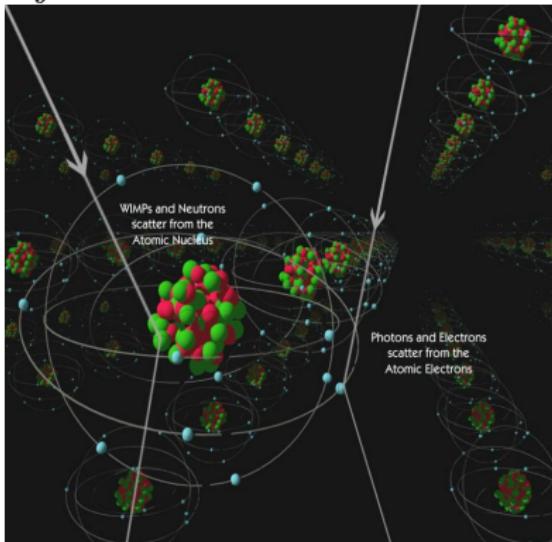


# Nuclear matrix elements

Nuclear matrix elements are needed to study fundamental symmetries

$$\langle \text{Final} | \mathcal{L}_{\text{leptons-nucleons}} | \text{Initial} \rangle = \langle \text{Final} | \int dx j^\mu(x) J_\mu(x) | \text{Initial} \rangle$$

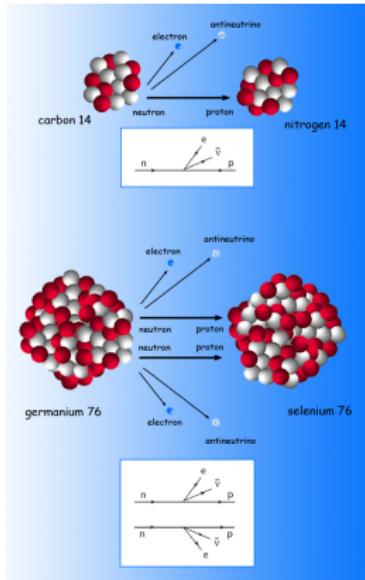
- Nuclear structure calculation of the initial and final states:  
Ab initio, shell model,  
energy density functional...
- Lepton-nucleus interaction:  
Evaluate (non-perturbative)  
hadronic currents inside nucleus:  
phenomenology, effective theory



CDMS Collaboration

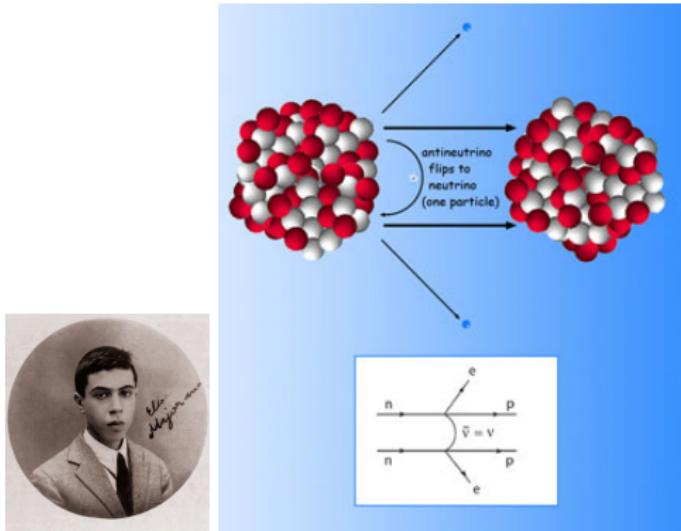
# Lepton-number conservation

Lepton number conserved  
in all processes observed to date



$\beta$  decay,  $2\nu\beta\beta$  decay...

Uncharged massive particles  
like Majorana neutrinos ( $\nu = \bar{\nu}$ )  
theoretically allow lepton number violation



Neutrinoless  $\beta\beta$  ( $0\nu\beta\beta$ ) decay

# Weak transitions in nuclei

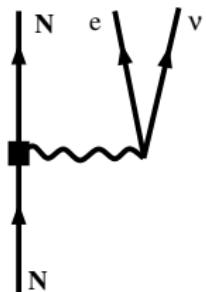
$\beta$  and  $\beta\beta$  decay processes driven by Weak interaction

$$\mathcal{L}_W = \frac{G_F}{\sqrt{2}} \left( j_{L\mu} J_L^{\mu\dagger} \right) + H.c.$$

$j_{L\mu}$  leptonic current (electron, neutrino)

$J_L^{\mu\dagger}$  hadronic current

Standard Model:  $J_L^{\mu\dagger}$  for quarks, need  $J_L^{\mu\dagger}$  for nucleons

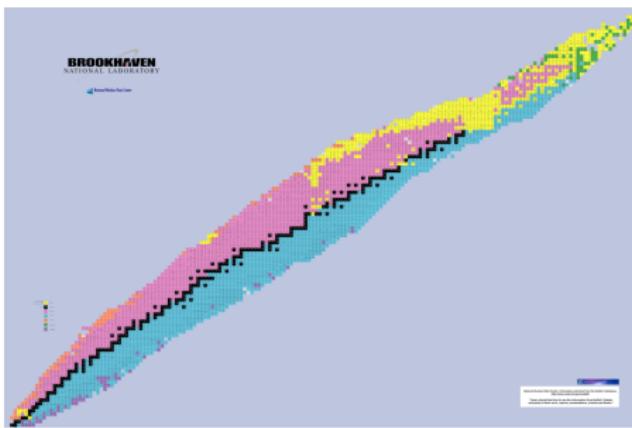


In nuclei (non-relativistic),  $\beta$  decay is

$$\langle F | \sum_i g_V \tau_i^- + g_A \sigma_i \tau_i^- | I \rangle$$

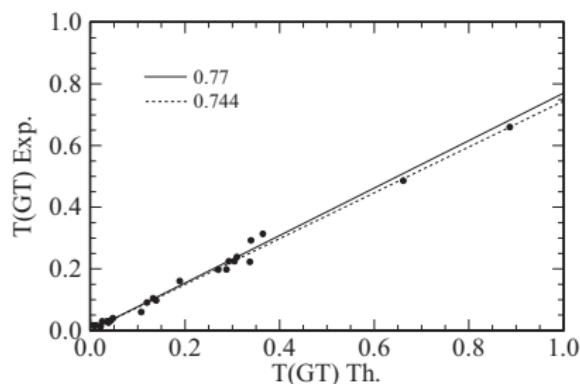
Fermi and Gamow-Teller transitions

corrections (forbidden transitions)  
expansion of the lepton current



# Gamow-Teller transitions

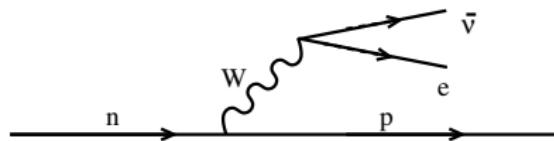
Single- $\beta$ ,  $2\nu\beta\beta$  decays well described by nuclear structure: shell model...



Martinez-Pinedo et al. PRC53 2602(1996)

$$\langle F | \sum_i g_A^{\text{eff}} \sigma_i \tau_i^- | I \rangle, \quad g_A^{\text{eff}} \approx 0.7 g_A$$

For agreement theory needs to  
“quench” Gamow-Teller operator



$$M^{2\nu\beta\beta} = \sum_k \frac{\langle 0_f^+ | \sum_n \sigma_n \tau_n^- | 1_k^+ \rangle \langle 1_k^+ | \sum_m \sigma_m \tau_m^- | 0_i^+ \rangle}{E_k - (M_i + M_f)/2}$$

Table 2

The ISM predictions for the matrix element of several  $2\nu$  double beta decays (in MeV $^{-1}$ ). See text for the definitions of the valence spaces and interactions.

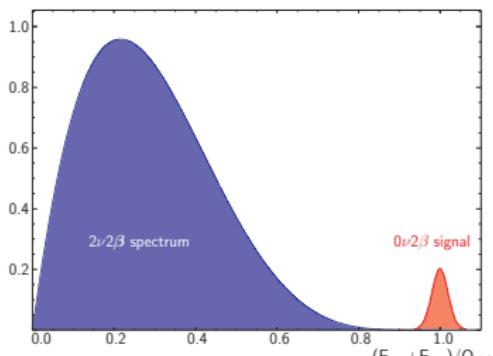
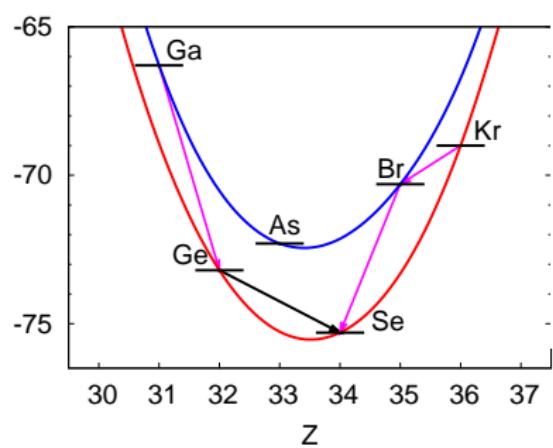
	M $^{2\nu}$ (exp)	q	M $^{2\nu}$ (th)	INT
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.047	kb3
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.048	kb3g
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.065	gxpfl
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140 \pm 0.005$	0.60	0.116	gcn28:50
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140 \pm 0.005$	0.60	0.120	jun45
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	$0.098 \pm 0.004$	0.60	0.126	gcn28:50
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	$0.098 \pm 0.004$	0.60	0.124	jun45
$^{128}\text{Te} \rightarrow ^{128}\text{Xe}$	$0.049 \pm 0.006$	0.57	0.059	gcn50:82
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	$0.034 \pm 0.003$	0.57	0.043	gcn50:82
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	$0.019 \pm 0.002$	0.45	0.025	gcn50:82

Caurier, Nowacki, Poves PLB711 62(2012)

# Neutrinoless double-beta decay

Neutrinoless double-beta decay ( $0\nu\beta\beta$ ):  
Lepton-number violation, Majorana nature of neutrinos

Second order process only observable if single- $\beta$ -decay  
is energetically forbidden or hindered by large  $\Delta J$



$$2\nu\beta\beta : E_{e_1} + E_{e_2} + E_{\bar{\nu}_1} + E_{\bar{\nu}_2} = Q_{\beta\beta}$$
$$0\nu\beta\beta : E_{e_1} + E_{e_2} = Q_{\beta\beta}$$

- $^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$
- $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$
- $^{82}\text{Se} \rightarrow ^{82}\text{Kr}$
- $^{96}\text{Zr} \rightarrow ^{96}\text{Mo}$
- $^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$
- $^{110}\text{Pd} \rightarrow ^{110}\text{Cd}$
- $^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$
- $^{124}\text{Sn} \rightarrow ^{124}\text{Te}$
- $^{130}\text{Te} \rightarrow ^{130}\text{Xe}$
- $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$
- $^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$

Lifetime limits:  $^{76}\text{Ge}$  (GERDA),  $^{136}\text{Xe}$  (EXO, KamLAND)  $T_{1/2}^{0\nu\beta\beta} > 10^{25}$  y!

# $0\nu\beta\beta$ decay nuclear matrix elements

$0\nu\beta\beta$  process needs massive Majorana neutrinos ( $\nu = \bar{\nu}$ )  
⇒ detection would proof Majorana nature of neutrinos

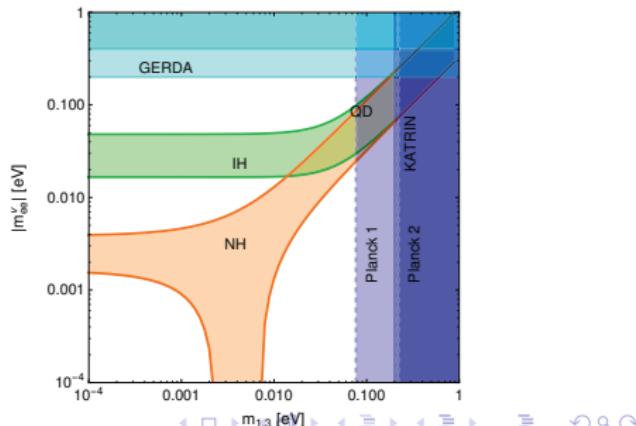
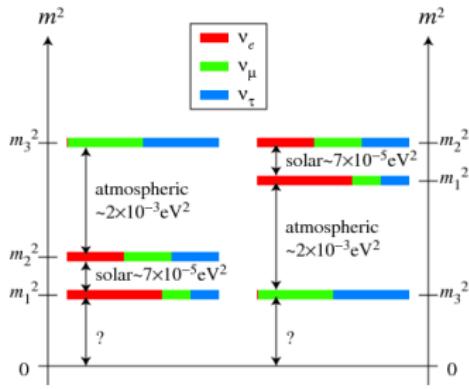


$$\left( T_{1/2}^{0\nu\beta\beta} (0^+ \rightarrow 0^+) \right)^{-1} = G_{01} |M^{0\nu\beta\beta}|^2 \left( \frac{m_{\beta\beta}}{m_e} \right)^2$$

$G_{01}$  is the phase space factor:  $Q_{\beta\beta}$ , electrons...

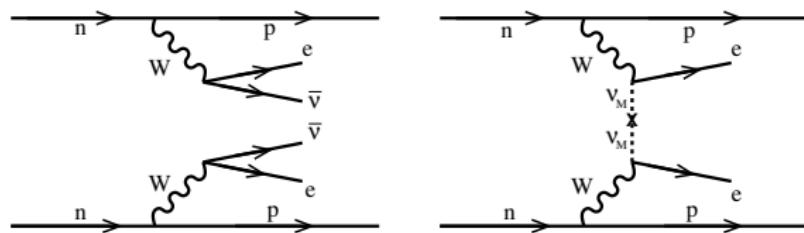
$M^{0\nu\beta\beta}$  is the nuclear matrix element

Identify best experimental isotopes, obtain neutrino mass  $m_{\beta\beta} = |\sum U_{ek}^2 m_k|$



# $\beta\beta$ decays and closure approximation

$\beta\beta$  decays are quite different processes



In  $2\nu\beta\beta$  decay, the momentum transfer limited by  $Q_{\beta\beta}$   
while for  $0\nu\beta\beta$  decay larger momentum transfers are permitted

In  $0\nu\beta\beta$  decay the Majorana neutrinos are part of the transition operator,  
via the so-called neutrino potential

Closure approximation, good to 90%, Sen'kov et al. PRC89 054304 (2014)

$$\sum_a \frac{\langle N_f | J_L^{\mu\dagger}(\mathbf{x}) | N_a \rangle \langle N_a | J_L^{\rho\dagger}(\mathbf{y}) | N_i \rangle}{p + E_a - \frac{1}{2}(E_i + E_f)} \simeq \frac{\langle N_f | J_L^{\mu\dagger}(\mathbf{x}) J_L^{\rho\dagger}(\mathbf{y}) | N_i \rangle}{p + \langle E \rangle - \frac{1}{2}(E_i + E_f)}$$

# Neutrinoless $\beta\beta$ decay matrix elements

The nuclear matrix element reads

$$M^{0\nu\beta\beta} = \langle 0_f^+ | \sum_{n,m} \tau_n^- \tau_m^- \sum_X H^X(r) \Omega^X | 0_i^+ \rangle$$

- $\tau_n^- \tau_m^-$  transform two neutrons into two protons

- $\Omega^X$  is the spin structure:

Fermi ( $\mathbb{1}$ ), Gamow-Teller ( $\sigma_1 \sigma_2$ ), Tensor  $\left( \left[ Y^2(\hat{r}) [\sigma_1 \sigma_2]^2 \right]^0 \right)$

- $H(r)$  is the neutrino potential

$$H^X(r) = \frac{2}{\pi} \frac{R}{g_A^2(0)} \int_0^\infty f^X(pr) \frac{h^X(p^2)}{\left( p + \langle E^m \rangle - \frac{1}{2}(E_i - E_f) \right)} q dq \sim \frac{R}{r}$$

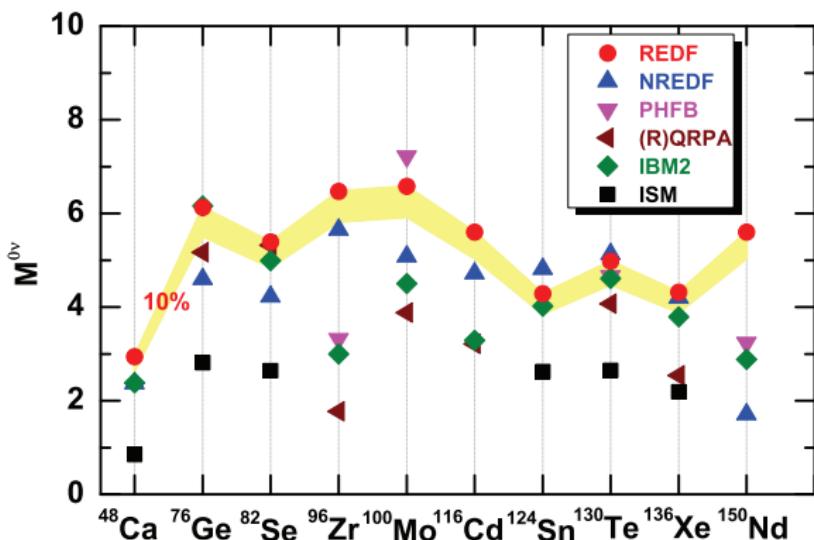
⇒ Virtual neutrinos,  $H(r)$ , allow all  $J^P$  in intermediate states

⇒ Momentum-transfer  $p \sim 100$  MeV, closure approximation

⇒  $H(r)$  breaks isospin invariance: three spin structures contribute, but Gamow-Teller part dominant  $\sim 85\%$  of total NME

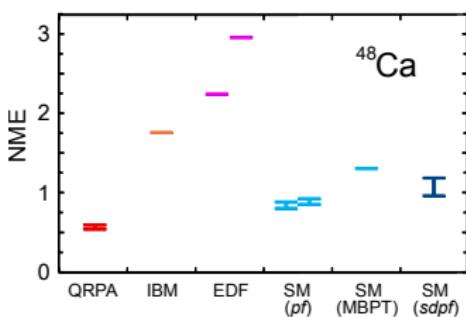
# Neutrinoless $\beta\beta$ decay matrix elements

Large difference in matrix element calculations, same transition operator



Yao et al. PRC91 024316 (2015)

EDF, IBM, QRPA  
large matrix elements:  
How well they include  
nuclear structure  
correlations?



Shell model small matrix elements:  
What is the effect of the small valence space?

# Shell model spectra and occupancies

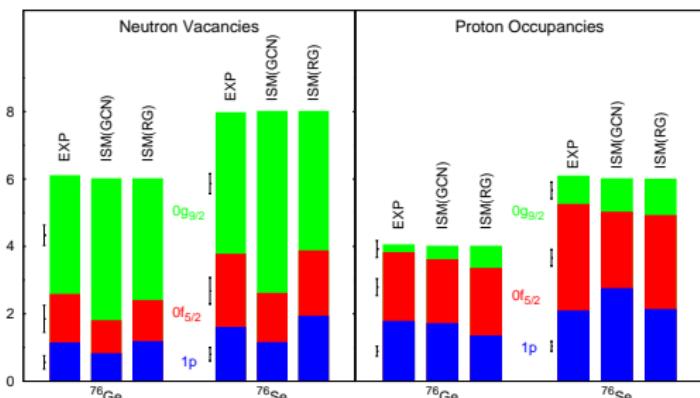
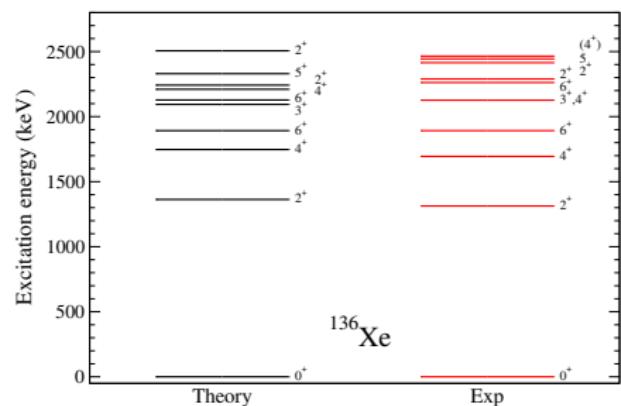
Shell model in one-major-shell spaces with phenomenological interactions

pf-shell, KB3G interaction:  $^{48}\text{Ca}$

$p_{3/2}, p_{1/2}, f_{5/2}, g_{9/2}$  space, GCN2850 interaction:  $^{76}\text{Ge}, ^{82}\text{Se}$

$d_{5/2}, s_{1/2}, d_{3/2}, g_{7/2}, h_{11/2}$  space, GCN5082 interaction:  $^{124}\text{Sn}, ^{130}\text{Te}, ^{136}\text{Xe}$

Experimental excitation spectra and occupancies well reproduced



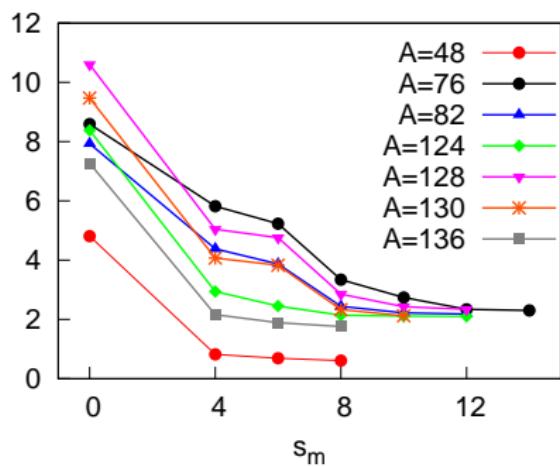
Exp: Schiffer et al. PRL100 112501(2009), Kay et al. PRC79 021301(2009)

Th: JM, Caurier, Nowacki, Poves PRC80 048501 (2009)

# Pairing correlations and $0\nu\beta\beta$ decay

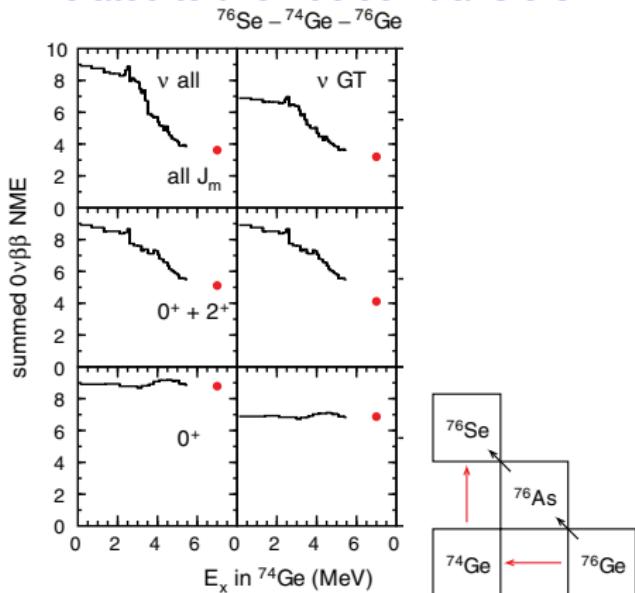
$0\nu\beta\beta$  decay is favoured by pairing correlations

Maximum between superfluid nuclei,  
reduced with high-seniorities



Caurier et al. PRL100 052503 (2008)

Related to two-nucleon transfers

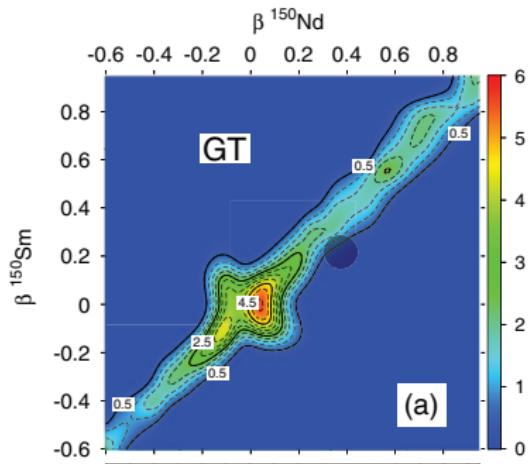


Brown et al. PRL113 262501 (2014)

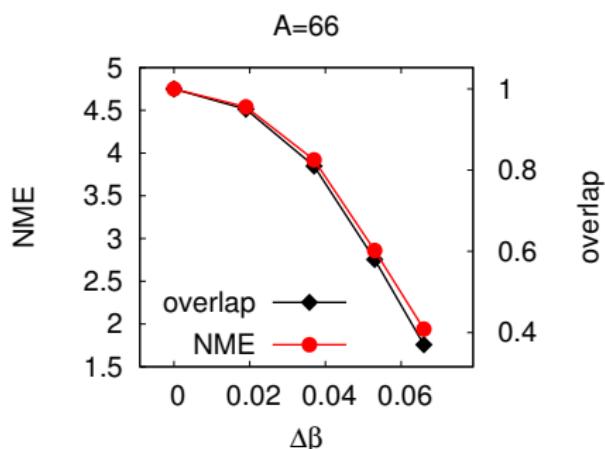
# Deformation and $0\nu\beta\beta$ decay

$0\nu\beta\beta$  decay is disfavoured by quadrupole correlations

$0\nu\beta\beta$  decay very suppressed when nuclei have different structure



Rodríguez, Martínez-Pinedo  
PRL105 252503 (2010)



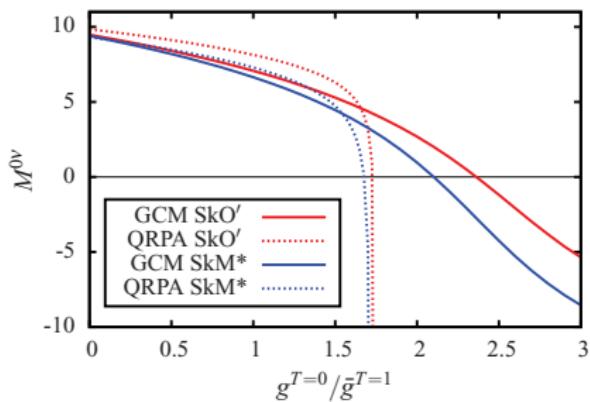
JM, Caurier, Nowacki, Poves  
JPCS267 012058 (2011)

Suppression also observed with QRPA Fang et al. PRC83 034320 (2011)

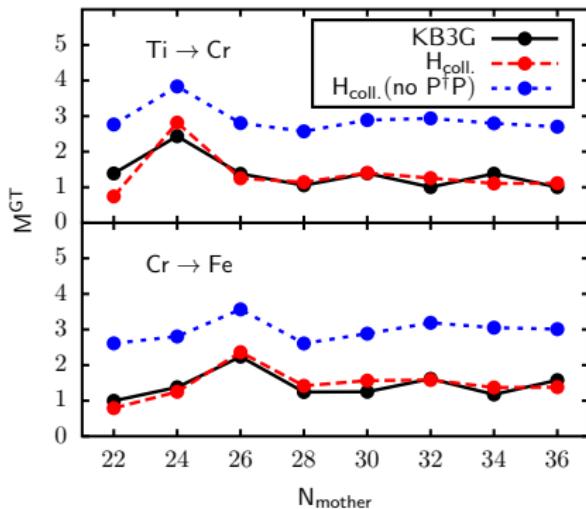
# Proton-neutron pairing and $0\nu\beta\beta$ decay

$0\nu\beta\beta$  decay very sensitive to proton-neutron (isoscalar) pairing

Matrix elements too large if proton-neutron correlations are neglected



Hinohara, Engel PRC90 031301 (2014)



JM, Hinohara, Rodriguez, Engel, Martínez-Pinedo

Related to approximate  $SU(4)$  symmetry of the  $0\nu\beta\beta$  decay operator

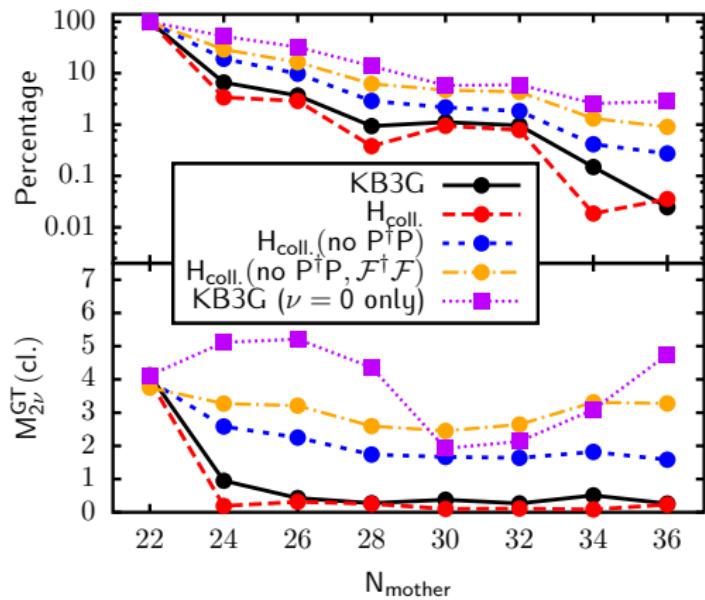
# SU(4) symmetry: small matrix elements

Exact SU(4) symmetry  $\Rightarrow M^{0\nu\beta\beta} = 0$

(mother and daughter nuclei in different SU(4) irreps)

SU(4) broken in nuclei  
(spin-orbit force...)  
but relatively small fraction  
of mother and daughter nuclei  
in same SU(4) irrep

When neutrino potential is omitted,  
 $0\nu\beta\beta$  operator exactly  
symmetric under SU(4):  
Matrix elements almost vanish

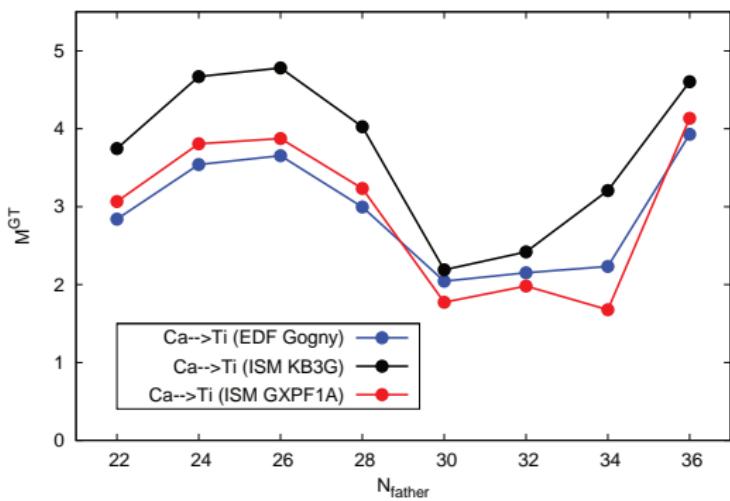


Missing correlations that break SU(4) symmetry, strong impact on  $\beta\beta$  decay

# $0\nu\beta\beta$ decay without correlations

Non-realistic spherical (uncorrelated) mother and daughter nuclei:

- Shell model (SM): zero seniority, neutron and proton  $J = 0$  pairs
- Energy density functional (EDF): only spherical contributions



In contrast to full  
(correlated) calculation  
SM and EDF NMEs agree!

NME scale set by  
pairing interaction

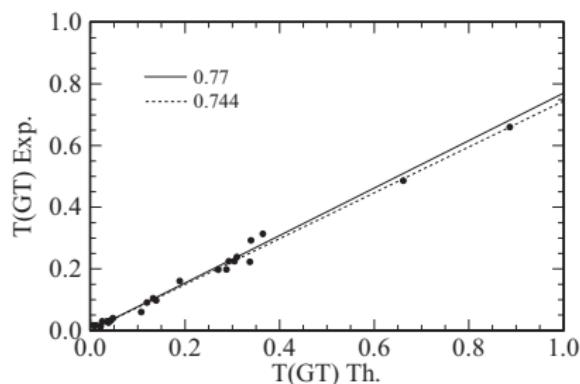
JM, Rodríguez, Martínez-Pinedo,  
Poves PRC90 024311(2014)

NME follows generalized  
seniority model:

$$M_{\text{GT}}^{0\nu\beta\beta} \simeq \alpha_\pi \alpha_\nu \sqrt{N_\pi + 1} \sqrt{\Omega_\pi - N_\pi} \sqrt{N_\nu} \sqrt{\Omega_\nu - N_\nu + 1}, \text{ Barea, Iachello PRC79 044301(2009)}$$

# Gamow-Teller transitions: quenching

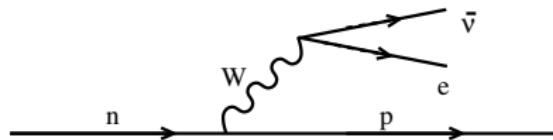
Single- $\beta$ ,  $2\nu\beta\beta$  decays well described by nuclear structure: shell model...



Martinez-Pinedo et al. PRC53 2602(1996)

$$\langle F | \sum_i g_A^{\text{eff}} \sigma_i \tau_i^- | I \rangle, \quad g_A^{\text{eff}} \approx 0.7 g_A$$

For agreement theory needs to  
“quench” Gamow-Teller operator



$$M^{2\nu\beta\beta} = \sum_k \frac{\langle 0_f^+ | \sum_n \sigma_n \tau_n^- | 1_k^+ \rangle \langle 1_k^+ | \sum_m \sigma_m \tau_m^- | 0_i^+ \rangle}{E_k - (M_i + M_f)/2}$$

Table 2

The ISM predictions for the matrix element of several  $2\nu$  double beta decays (in MeV $^{-1}$ ). See text for the definitions of the valence spaces and interactions.

	M $^{2\nu}$ (exp)	q	M $^{2\nu}$ (th)	INT
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.047	kb3
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.048	kb3g
$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$	$0.047 \pm 0.003$	0.74	0.065	gxpfl
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140 \pm 0.005$	0.60	0.116	gcn28:50
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$0.140 \pm 0.005$	0.60	0.120	jun45
$^{82}\text{Se} \rightarrow ^{82}\text{Kr}$	$0.098 \pm 0.004$	0.60	0.126	gcn28:50
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$^{128}\text{Te} \rightarrow ^{128}\text{Xe}$	$0.049 \pm 0.006$	0.57	0.059	gcn50:82
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	$0.034 \pm 0.003$	0.57	0.043	gcn50:82
$^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$	$0.019 \pm 0.002$	0.45	0.025	gcn50:82

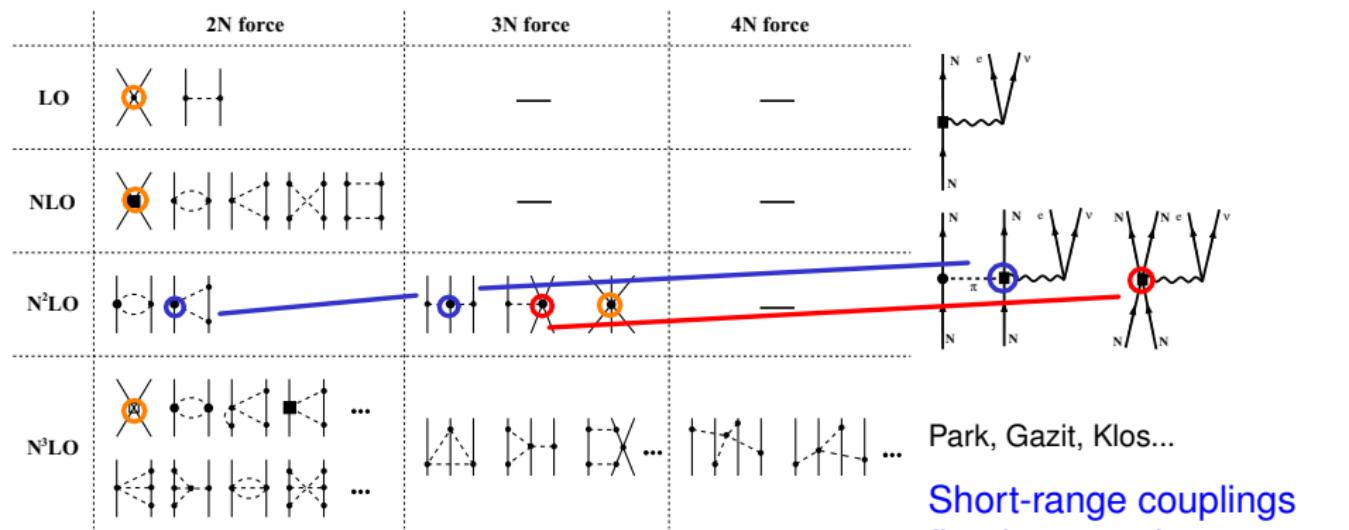
Caurier, Nowacki, Poves PLB711 62(2012)

# Chiral Effective Field Theory

Chiral EFT: low energy approach to QCD, nuclear structure energies

Approximate chiral symmetry: pion exchanges, contact interactions

Systematic expansion: nuclear forces and electroweak currents



Weinberg, van Kolck, Kaplan, Savage, Epelbaum, Kaiser, Meißner...

# 2b currents in light nuclei

2b currents (meson-exchange currents) tested in light nuclei:

$^3\text{H}$   $\beta$  decay

Gazit et al. PRL103 102502(2009)

$A \leq 9$  magnetic moments

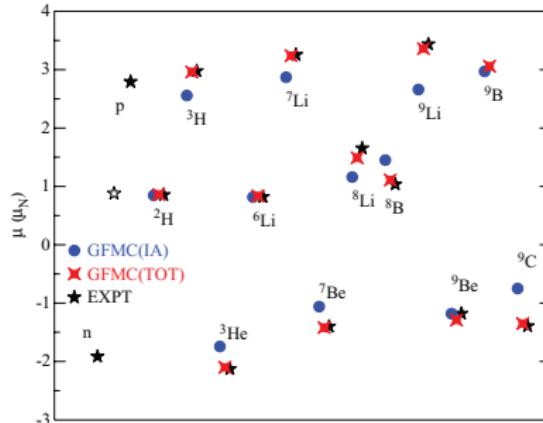
$^8\text{Be}$  EM transitions

Pastore et al. PRC87 035503(2013)

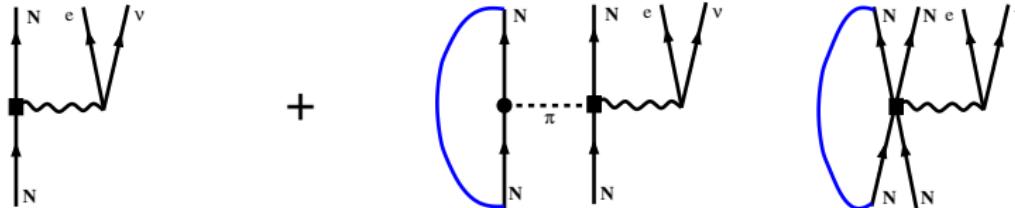
Pastore et al. PRC90 024321(2014)

$^3\text{H}$   $\mu$  capture

Marcucci et al. PRC83 014002(2011)



In medium-mass nuclei, chiral EFT 1b + 2b currents (normal ordering)

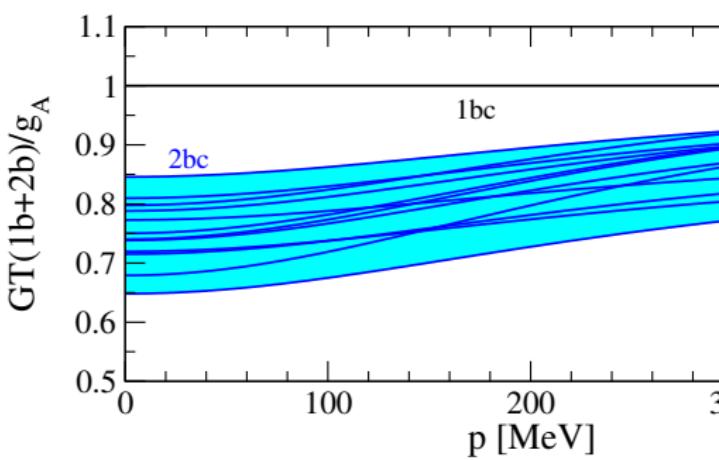
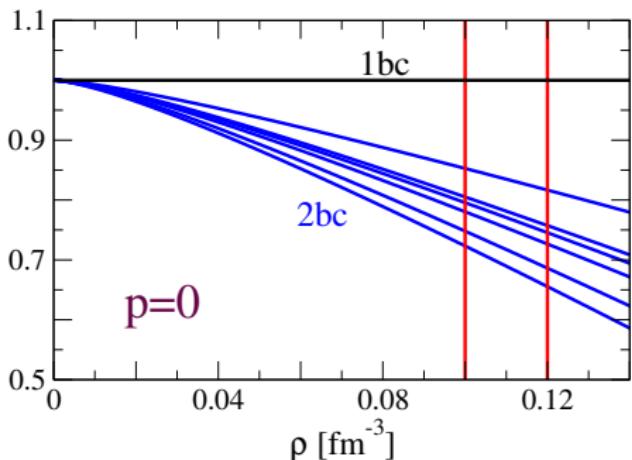
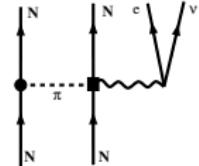


# 2b currents in medium-mass nuclei

Normal-ordered 2b currents modify GT operator

JM, Gazit, Schwenk PRL107 062501 (2011)

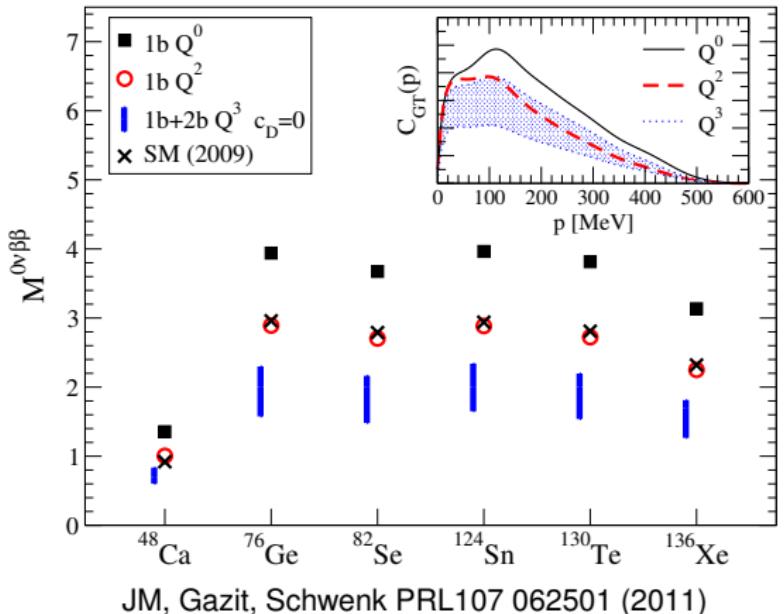
$$\mathbf{J}_{n,2b}^{\text{eff}} \simeq -\frac{g_A \rho}{f_\pi^2} \tau_n^- \sigma_n \left[ I(\rho, P) \frac{(2c_4 - c_3)}{3} \right] - \frac{g_A \rho}{f_\pi^2} \tau_n^- \sigma_n \frac{2}{3} c_3 \frac{\mathbf{p}^2}{4m_\pi^2 + \mathbf{p}^2},$$



2b currents predict  $g_A$  quenching  $q = 0.85 \dots 0.66$

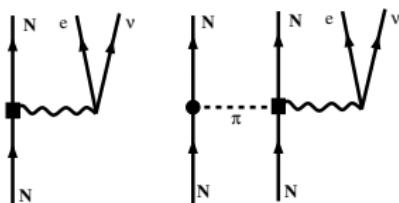
Quenching reduced at  $p > 0$ , relevant for  $0\nu\beta\beta$  decay where  $p \sim m_\pi$

# Nuclear matrix elements with 1b+2b currents



JM, Gazit, Schwenk PRL107 062501 (2011)

Order  $Q^0 + Q^2$  similar to phenomenological currents  
JM, Poves, Caurier, Nowacki  
NPA818 139 (2009)

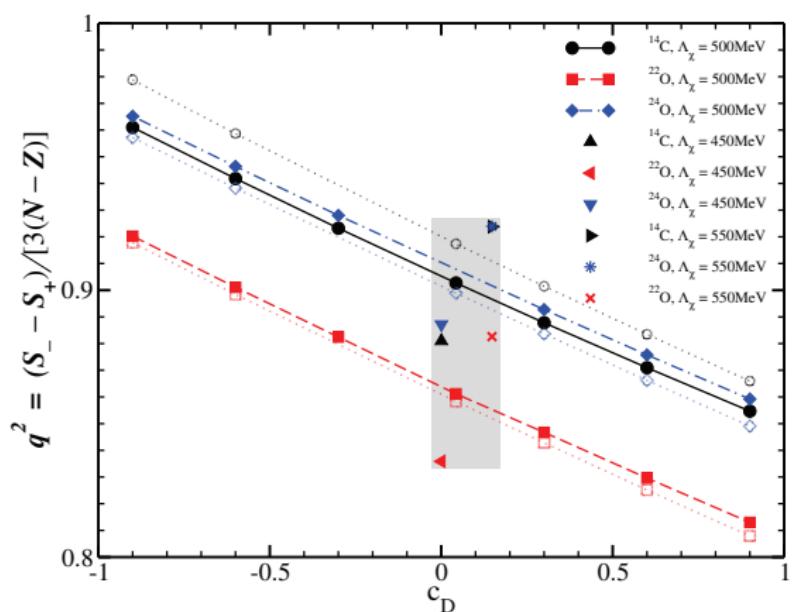


Order  $Q^3$  2b currents reduce NMEs  $\sim 15\% - 40\%$

Similar quenching obtained in QRPA calculations with same 2b currents  
Engel, Šimkovic, Vogel PRC89 064308 (2014)

# Contribution of 2b currents: Coupled-Cluster

Very recent Coupled-cluster calculations for single- $\beta$  decay (GT strengths) including chiral 1b and 2b currents in  $p$ , low- $sd$  nuclei  $^{14}\text{C}$ ,  $^{22}\text{O}$  and  $^{24}\text{O}$



Ekström et al. PRL113 262504 (2014)

Calculation with chiral NN+3N forces and currents

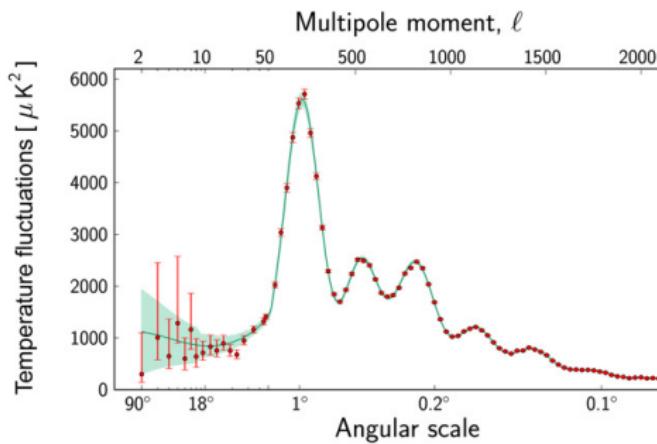
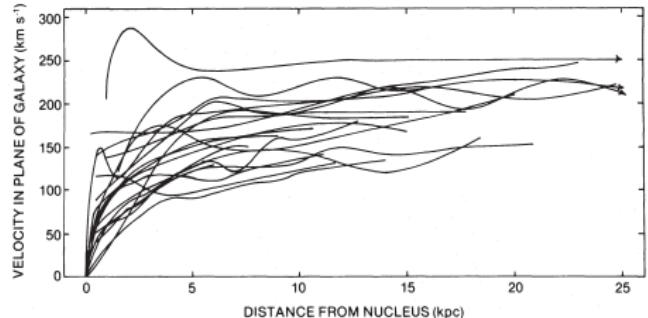
Dominant effect of 2b currents captured by normal-ordered 1b part with respect to Hartree-Fock state

From 2b currents predict small  $g_A$  quenching  
 $q = 0.96...0.92$

# Outline

- 1 Nuclear structure of medium-mass nuclei
- 2 Matrix elements for  $\beta\beta$  decay
- 3 Dark Matter scattering off nuclei

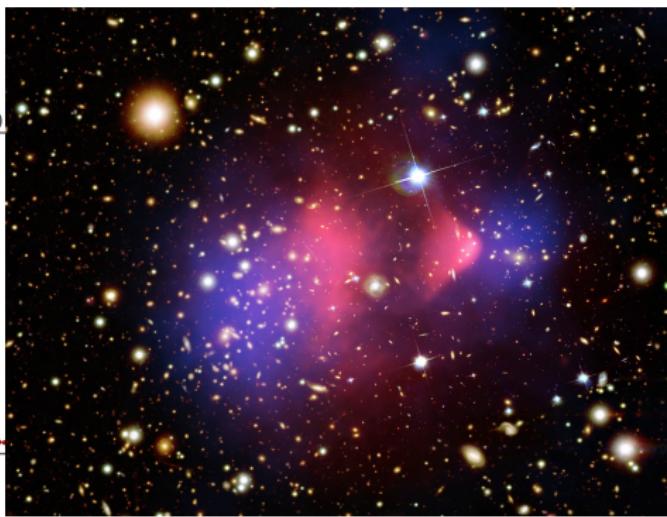
# Dark Matter: evidence



Solid evidence of Dark Matter  
in very different observations:

Rotation curves, Lensing, CMB...

Zwicky 1930's, Rubin 1970's..., Planck 2010's

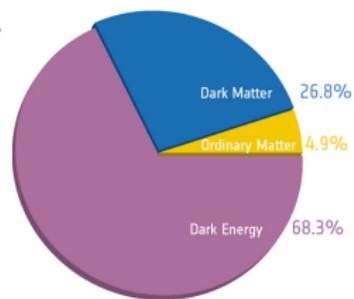


# What is Dark Matter made of?

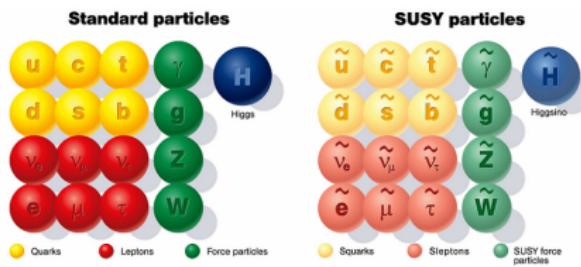
The composition of Dark Matter is unknown

High-energy physics: candidates proposed beyond Standard Model

- Weakly interacting massive particles (WIMPs)
- Sterile neutrinos
- Axions
- Gravitons
- ...



Lightest supersymmetric particles (usually neutralinos) predicted in SUSY extensions of the Standard Model



Expected WIMP-density agrees with observed Dark Matter density

# WIMP scattering off nuclei

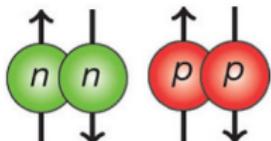
The challenge is direct Dark Matter detection

WIMPs interact with quarks  $\Rightarrow$  nuclei

Direct detection experiments: XENON100, LUX  
nuclear recoil from WIMP scattering off nuclei  
sensitive to Dark Matter masses  $\gtrsim 1$  GeV

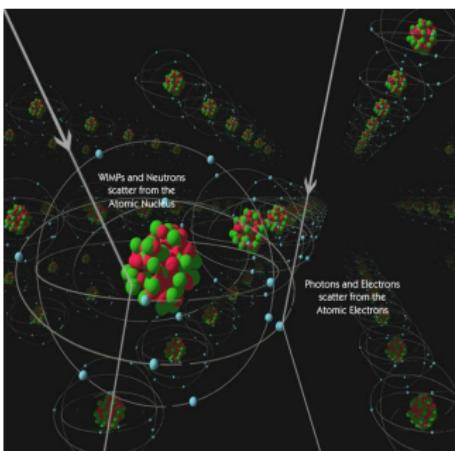
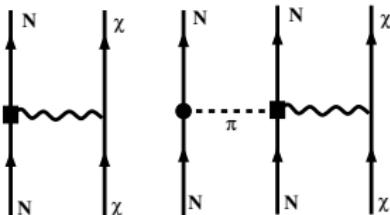
WIMPs couple to the nuclear density

For elastic scattering, coherent sum  
over nucleons and protons in the nucleus



WIMP spins couple to the nuclear spin

Pairing interaction: Two spins couple to  $S = 0$   
Only relevant in stable odd-mass nuclei



CDMS Collaboration

# WIMP-nucleon interactions

The WIMP-nucleus interaction is

Coupling to nuclear density: scalar-scalar, spin-independent

Coupling to the spin: axial-axial, spin-dependent

$$\mathcal{L}_\chi^{\text{SI}} + \mathcal{L}_\chi^{\text{SD}} = \frac{G_F}{\sqrt{2}} \int d^3\mathbf{r} [j(\mathbf{r})S(\mathbf{r}) + j^\mu(\mathbf{r})J_\mu^A(\mathbf{r})]$$

$j(\mathbf{r}) = \bar{\chi}\chi = \delta_{s_f s_i} e^{-i\mathbf{q}\mathbf{r}}$  is the leptonic (WIMP) scalar current

$S(\mathbf{r}) = c_0 \sum_{i=1}^A \delta^3(\mathbf{r} - \mathbf{r}_i)$  is the hadronic scalar current

$j^\mu(\mathbf{r}) = \bar{\chi}\gamma\gamma_5\chi e^{-i\mathbf{q}\mathbf{r}}$  is the leptonic (WIMP) axial current

$J_\mu^A(\mathbf{r}) = \sum_{i=1}^A J_{\mu,i}^A(\mathbf{r})\delta^3(\mathbf{r} - \mathbf{r}_i)$  is the hadronic axial current

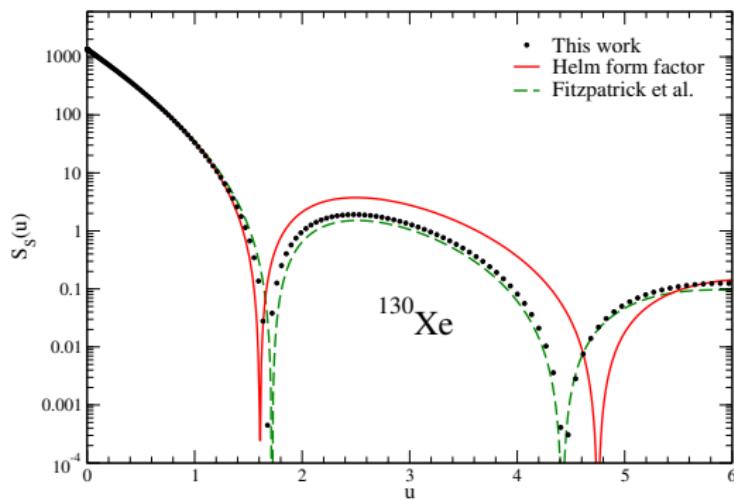
Matrix element of the dark matter scattering: structure factor

$$S_S(q) + S_A(q) = \frac{1}{4\pi G_F^2} \sum_{s_f, s_i} \sum_{M_f, M_i} |\langle J_f M_f | \mathcal{L}_\chi^{\text{SI}} + \mathcal{L}_\chi^{\text{SD}} | J_i M_i \rangle|^2$$

# Spin-independent structure factor for $^{130}\text{Xe}$

Coherent response at  $p = 0$ , lost at finite momentum transfers

$$S_S(q) = \sum_{L=0}^{\infty} \left| \langle J_f | c_0 \sum_{i=1}^A j_L(qr_i) Y_L(\mathbf{r}_i) | J_i \rangle \right|^2 \xrightarrow{q \rightarrow 0} \frac{c_0^2}{4\pi} (2J+1) A^2 ,$$



Plot as function of dimensionless  $u = p^2 b^2 / 2$   
b harmonic oscillator length

Only low-momentum transfers up to  $u \sim 2$  relevant for present experiments

Not very sensitive to nuclear structure details: similar results with model constant density + gaussian surface

# Spin-dependent hadronic currents

Calculate axial hadronic currents

Derive predicted currents within chiral EFT (similar to Weak transitions)

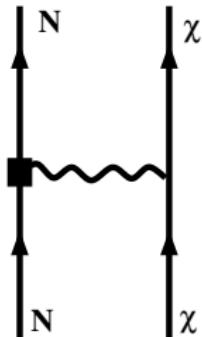
At lowest orders  $Q^0$  and  $Q^2$  in chiral EFT, 1b currents

$$Q^0 : \sum_{i=1}^A \mathbf{J}_{i,1b} = \sum_{i=1}^A \frac{1}{2} \left[ a_0 \sigma_i + a_1 \tau_i^3 \sigma_i \right],$$

isoscalar      isovector

$$Q^2 : \sum_{i=1}^A \mathbf{J}_{i,1b} = \sum_{i=1}^A \frac{1}{2} \left[ a_0 \sigma_i + a_1 \tau_i^3 \left( \frac{g_A(p^2)}{g_A} \sigma_i - \frac{g_P(p^2)}{2mg_A} (\mathbf{p} \cdot \sigma_i) \mathbf{p} \right) \right],$$

axial      pseudoscalar



Isoscalar and isovector (distinguish neutrons and protons) components

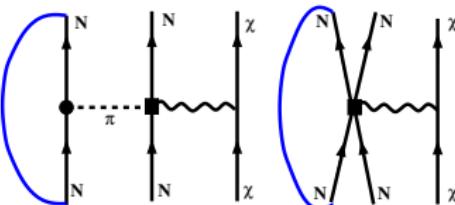
Isovector components have axial (dominant) and pseudoscalar term

# Spin-dependent 2b currents

## Leading $Q^3$ correction: 2b currents

Approximate in medium-mass nuclei: normal-ordered 1b part  
with respect to spin/isospin symmetric Fermi gas

$$\mathbf{J}_{12}^3 = -\frac{g_A}{4F_\pi^2} \frac{1}{m_\pi^2 + k^2} \left[ 2 \left( c_4 + \frac{1}{4m} \right) \mathbf{k} \times (\boldsymbol{\sigma}_X \times \mathbf{k}) \tau_X^3 + 4c_3 \mathbf{k} \cdot (\boldsymbol{\sigma}_1 \tau_1^3 + \boldsymbol{\sigma}_2 \tau_2^3) \mathbf{k} - \frac{i}{m} \mathbf{k} \cdot (\boldsymbol{\sigma}_1 - \boldsymbol{\sigma}_2) \mathbf{q} \tau_X^3 \right]$$



The leading (long-range) normal-ordered two-body currents are

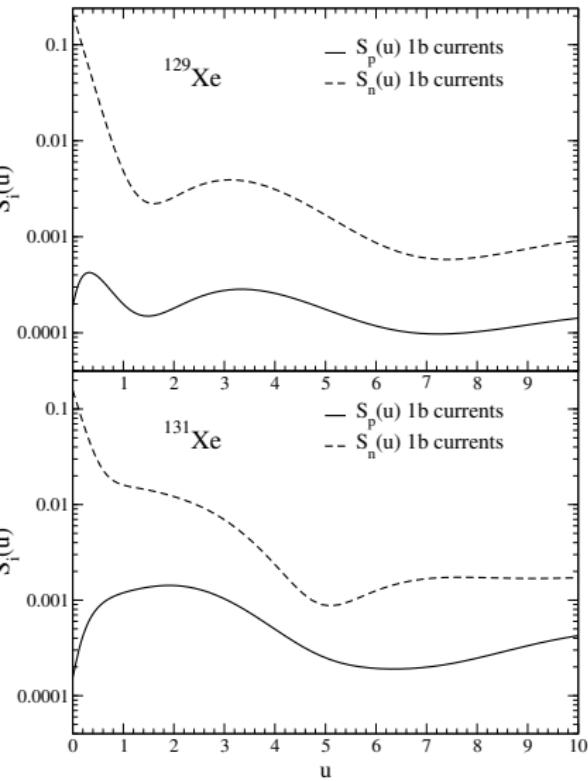
$$\mathbf{J}_{i,2b}^{\text{eff}} = \sum_{\sigma_j}^{FG} \sum_{\tau_j}^{FG} \int \frac{p_j^2 dp_j}{(2\pi)^3} \mathbf{J}_{i,j,2b} (1 - P_{ij})$$

$$\mathbf{J}_{i,2b}^{\text{eff}} = -g_A \frac{\tau_i^3}{2} \frac{\rho}{F_\pi^2} I(\rho, P=0) \left( \frac{1}{3} (2c_4 - c_3) \right) \boldsymbol{\sigma}_i = -g_A \frac{\tau_i^3}{2} \delta a_1 \boldsymbol{\sigma}_i$$

$$\mathbf{J}_{i,2b}^{\text{eff}, P} = -g_A \frac{\tau_i^3}{2} \frac{\rho}{F_\pi^2} 2c_3 \frac{1}{4m_\pi^2 + p^2} (\mathbf{p} \cdot \boldsymbol{\sigma}_i) \mathbf{p} = -g_A \frac{\tau_i^3}{2} \frac{\delta a_1^P(p^2)}{p^2} (\mathbf{p} \cdot \boldsymbol{\sigma}_i) \mathbf{p}$$

Renormalize isovector couplings: **reduce axial** and **enhance pseudoscalar**

# SD Structure Factors with 1b+2b currents

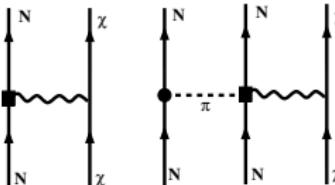


In  $^{129,131}_{54}\text{Xe}$   $\langle S_n \rangle \gg \langle S_p \rangle$ ,  
Neutrons carry most nuclear spin

Couplings sensitive more to  
protons ( $a_0 = a_1$ ) or neutrons ( $a_0 = -a_1$ )

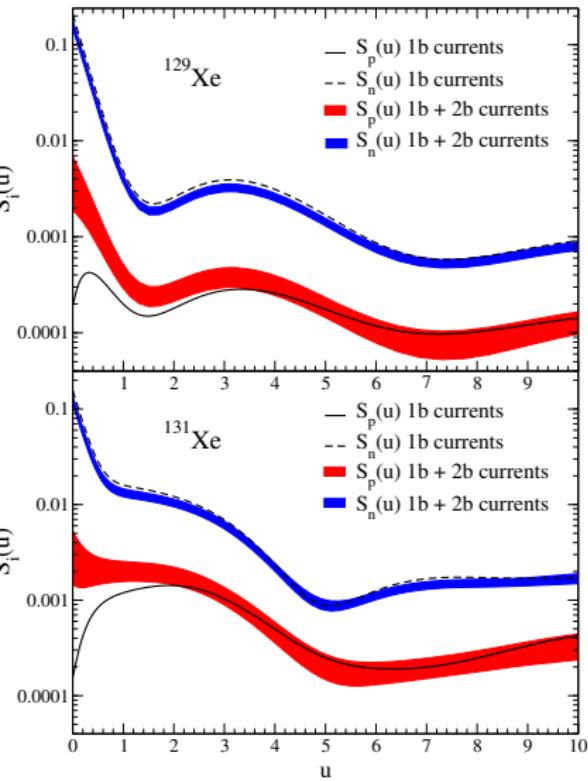
$$S(0) \propto \left| \frac{a_0+a_1}{2} \langle S_p \rangle + \frac{a_0-a_1}{2} \langle S_n \rangle \right|^2$$

2b currents involve neutrons + protons:



Neutrons always contribute with 2b  
currents, dramatic increase in  $S_p(u)$

# SD Structure Factors with 1b+2b currents

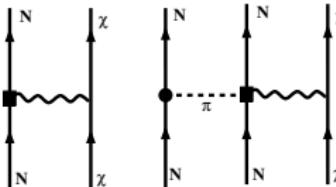


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$$S(0) \propto \left| \frac{a_0+a_1}{2} \langle S_p \rangle + \frac{a_0-a_1}{2} \langle S_n \rangle \right|^2$$

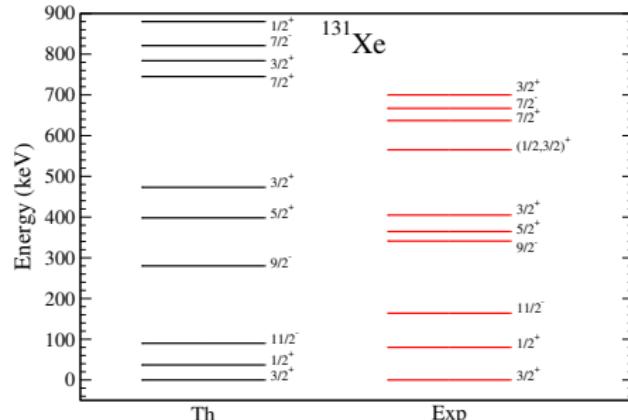
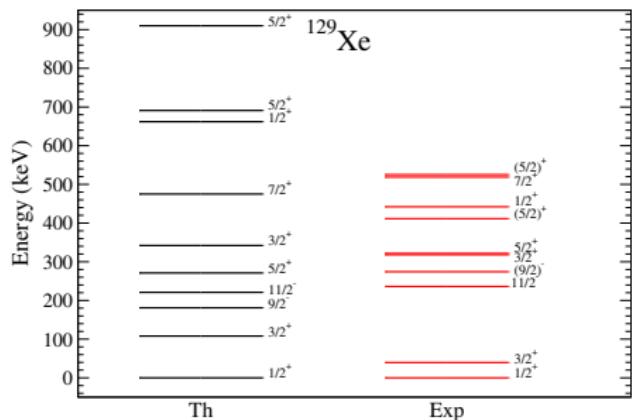
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# Inelastic scattering?

Can Dark Matter scatter exciting the nucleus to the first excited state?



Very low-lying first-excited states  $\sim 40, 80$

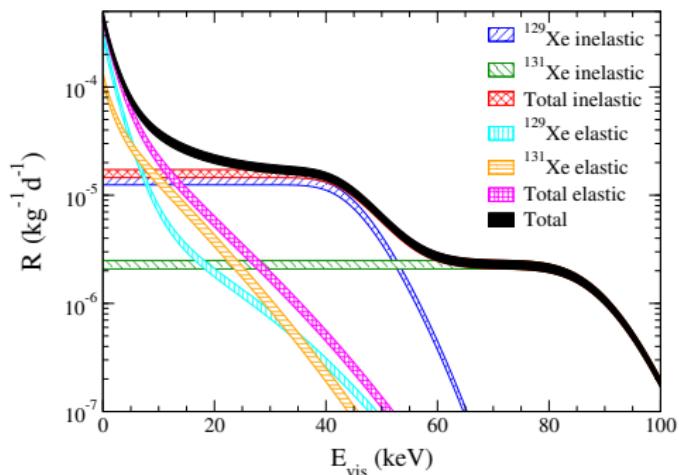
If WIMPs have enough kinetic energy  
inelastic scattering possible

$$p_{\pm} = \mu v_i \left( 1 \pm \sqrt{1 - \frac{2E^*}{\mu v_i^2}} \right)$$

# Spin-dependent inelastic WIMP scattering

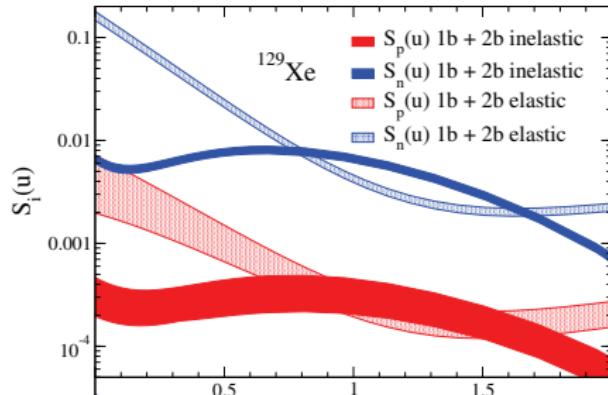
Inelastic structure factors

compete with elastic at  $p \sim 150$  MeV,  
in the kinematically allowed region



Inelastic scattering  $\Rightarrow$  spin coupling

Density coupling suppressed:  
coherence of all nucleons lost



Integrated spectrum for xenon  
shows expected signal from  
inelastic scattering including the  
gamma from excited state decay

One plateau per excited state

# Summary

Shell Model calculations based on chiral effective field theory including NN+3N forces and many-body perturbation theory

- 3N forces explain dripline in O, shell evolution in Ca, spectroscopy
- Theoretical uncertainties: initial Hamiltonian dominates many-body approach, limit predictive power of calculations

Neutrinoless double-beta decay key process to understand Majorana neutrino character and neutrino absolute mass and hierarchy

- Shell Model matrix elements smaller than other approaches, but only method to include full correlations in configuration space
- Correlations (deformation, proton-neutron pairing) have strong impact on (reducing) matrix elements
- 2b currents, analogue of 3N forces, modify nuclear matrix elements

WIMP scattering off nuclei for direct Dark Matter detection experiments

- Spin-Independent response coherent enhancement, no inelastic signal
- Spin-Dependent case sensitive to nuclear structure and 2b currents

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