

Collective aspects of microscopic mean-field evolution along the fission path

Yusuke Tanimura¹, Denis Lacroix¹ and
Guillaume Scamps²

¹IPN Orsay, ²Tohoku University

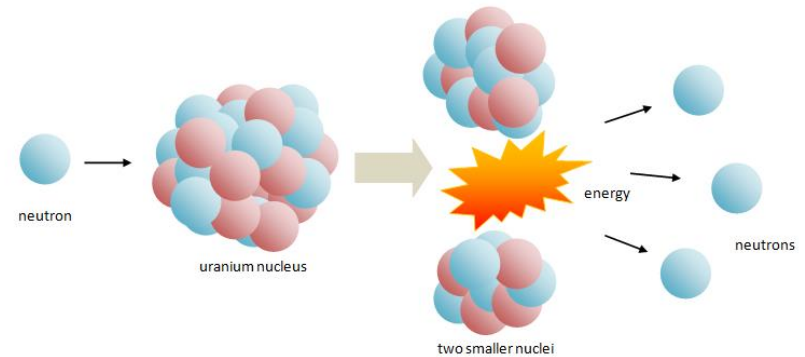
Y. Tanimura, D. Lacroix, and G. Scamps, Phys. Rev. C**92**, 034601(2015)



Nuclear fission

- **Importance**

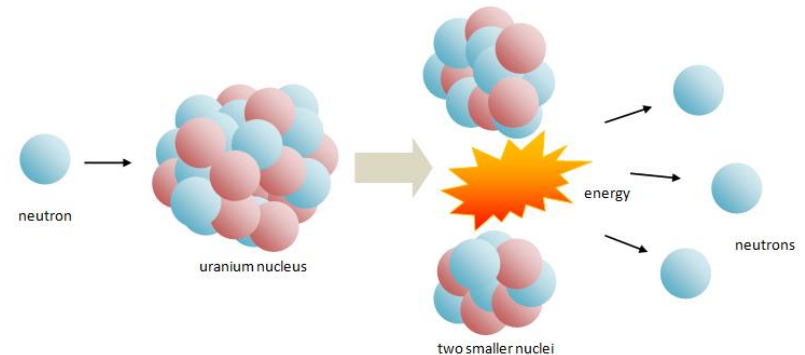
- Energy production
- Synthesis of super heavy elements
- Astrophysical process
- Production of radioactive isotopes



Nuclear fission

- **Importance**

- Energy production
- Synthesis of super heavy elements
- Astrophysical process
- Production of radioactive isotopes

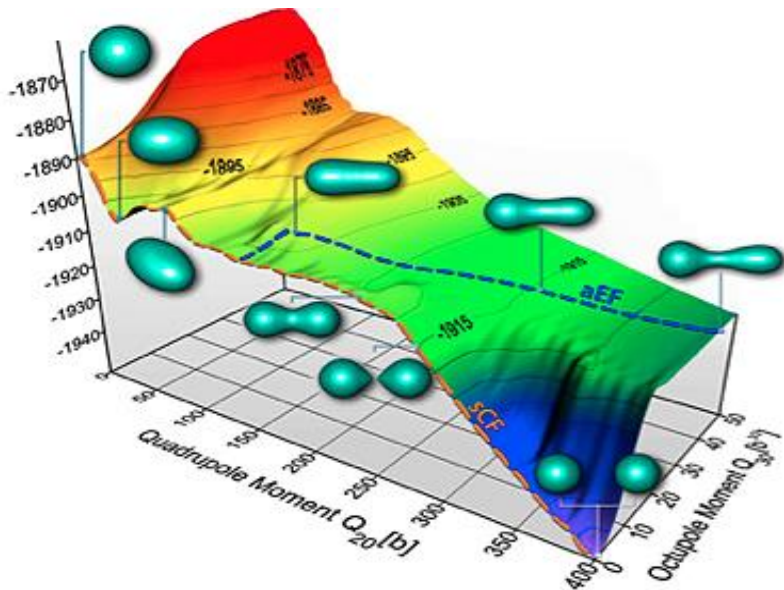


- **Theoretical challenges**

- **Phenomenological models** in terms of a few **macroscopic** degrees of freedom (elongation, mass asymmetry,...) have been developed
- Successful **microscopic models** are still under development
- Complicated dynamical process of quantum many-body system
 - Quantal treatments for both single-particle and collective DOFs
 - Dynamical and non-adiabatic effects
 - Different time scales

Microscopic models for fission

Static approach



- With energy density functional (EDF) theories (Skyrme, Gogny, RMF)
- Fission paths on the **potential energy surface**
- **Adiabatic (no excitation)**
- **Dynamics is poorly treated**

Our motivation:

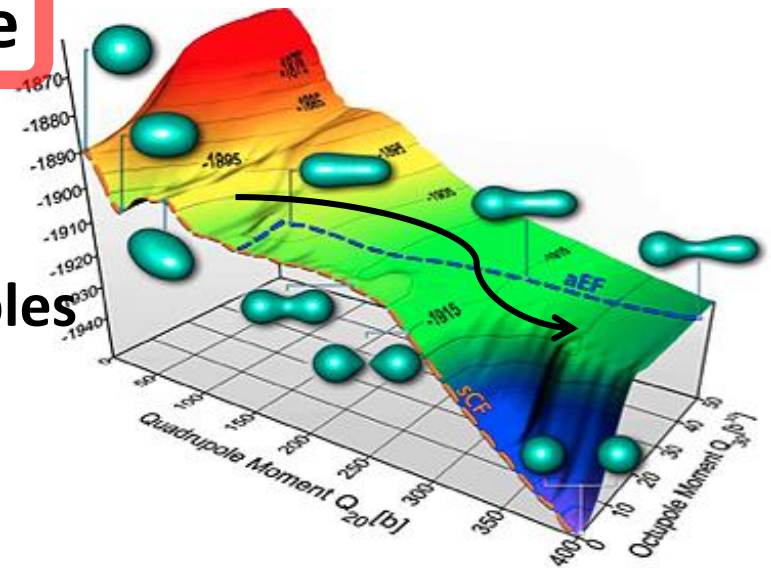
- Dynamical approach to fission based on **time-dependent energy density functional (TD-EDF)** theory
- Mapping TD-EDF trajectory onto a selected set of collective variables

TD-EDF \leftrightarrow collective space

✓ Momenta

✓ Masses

for a given set of collective variables



To Bridge TD-EDF and collective motion

Collective variable(s): \hat{Q}_α
ex: $\hat{Q}_2 = 2z^2 - x^2 - y^2$



Mass and **conjugate momentum**
associated with Q_α ?

To Bridge TD-EDF and collective motion

Collective variable(s): \hat{Q}_α
ex: $\hat{Q}_2 = 2z^2 - x^2 - y^2$



Mass and conjugate momentum
associated with Q_α ?

... We demand that

$$\frac{d\langle \hat{Q}_\alpha \rangle}{dt} = \frac{\langle \hat{P}_\alpha \rangle}{M_\alpha}$$

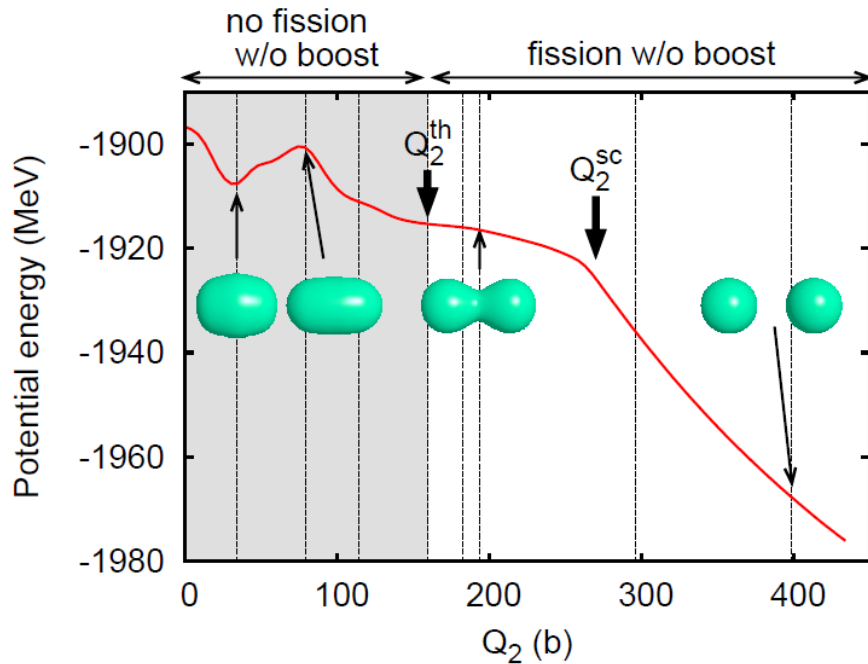
$$\text{Tr}(\rho(t) [\hat{Q}_\alpha, \hat{P}_\alpha]) = i\hbar$$



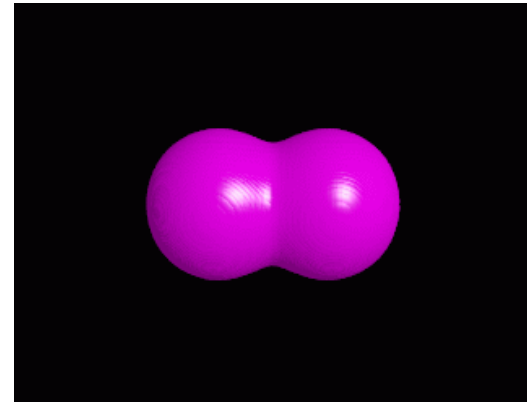
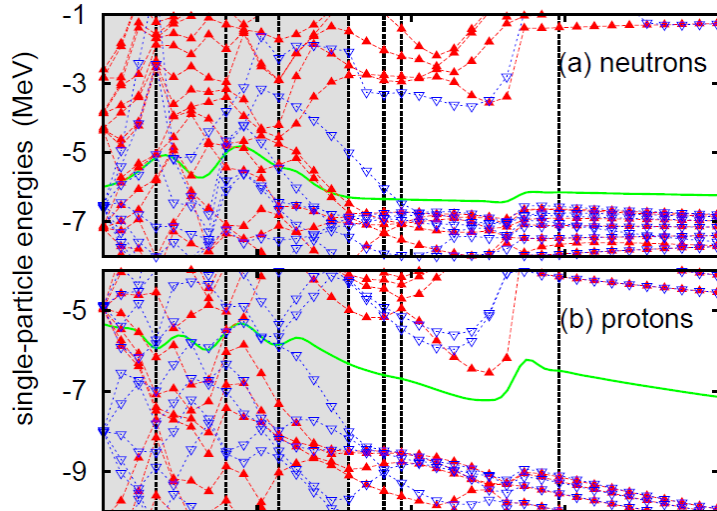
$$\frac{m_N}{M_\alpha} = \text{Tr}[\rho(t) \nabla Q_\alpha \cdot \nabla Q_\alpha]$$

$$P_\alpha = \frac{\hbar}{2i} \frac{M_\alpha}{m_N} [(\nabla Q_\alpha) \cdot \nabla + \nabla \cdot (\nabla Q_\alpha)]$$

Application to ^{258}Fm

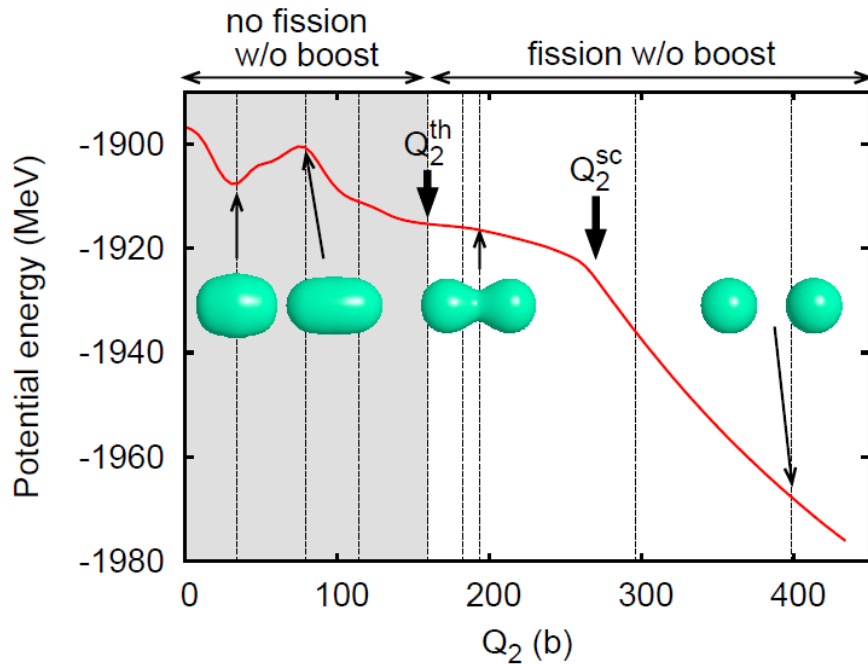


- TDHF + BCS
(Sly4d + constant pairing)
- Starting from a point on PEC
- No spontaneous fission
for $Q_2(t=0) < 160$ b

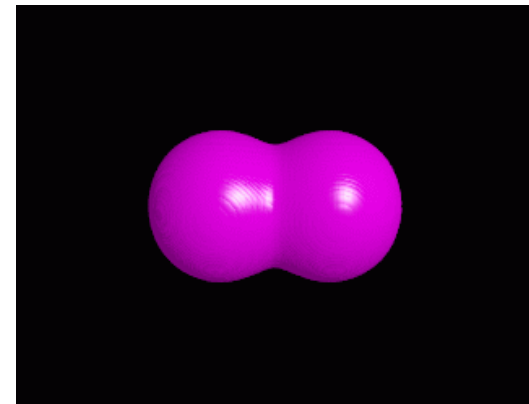
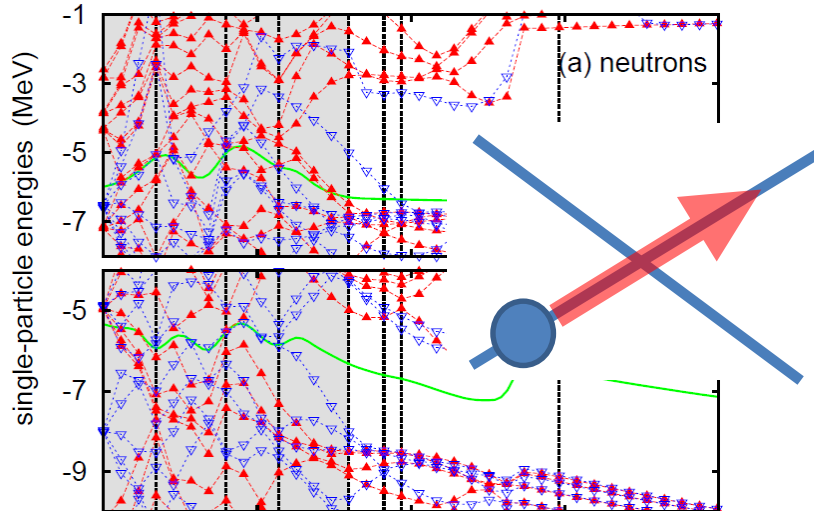


Symmetric fission of ^{258}Fm
with TDHF + BCS

Application to ^{258}Fm

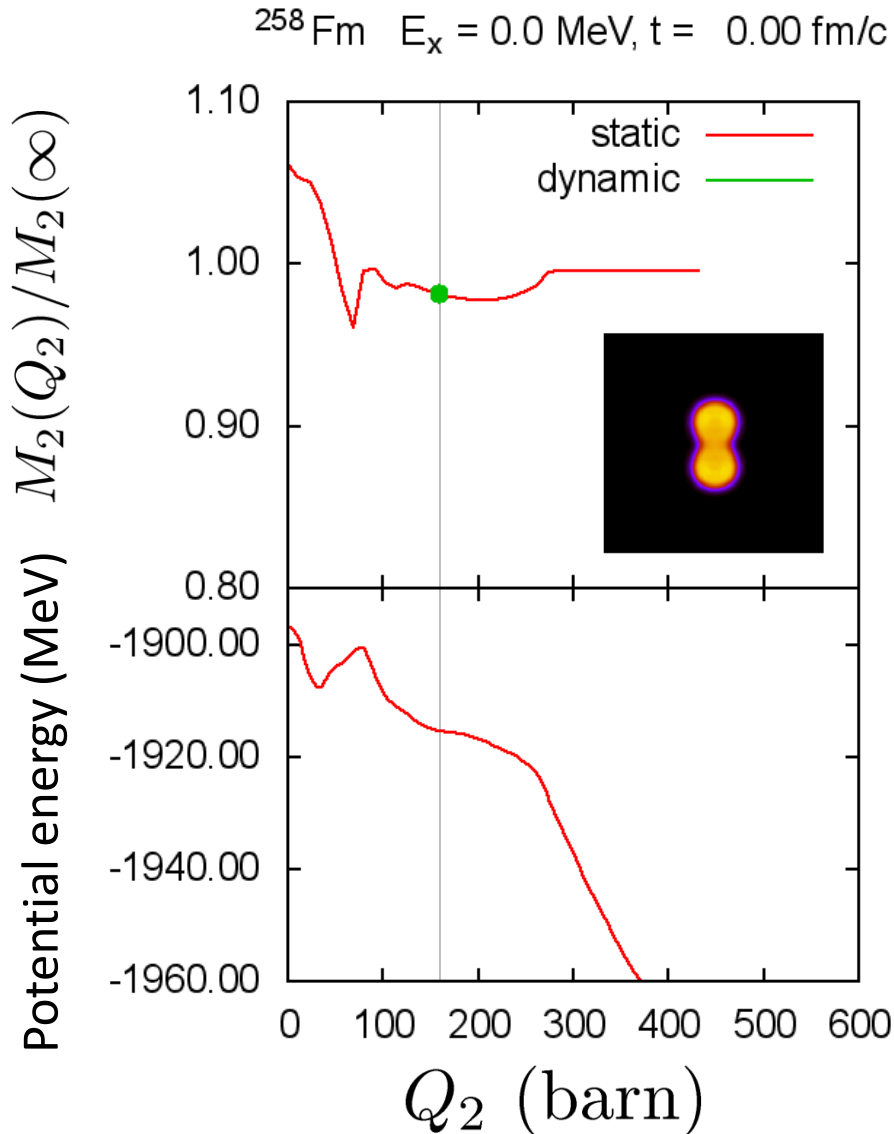


- TDHF + BCS
(Sly4d + constant pairing)
- Starting from a point on PEC
- No spontaneous fission
for $Q_2(t=0) < 160$ b



Symmetric fission of ^{258}Fm
with TDHF + BCS

1. Collective mass and momentum

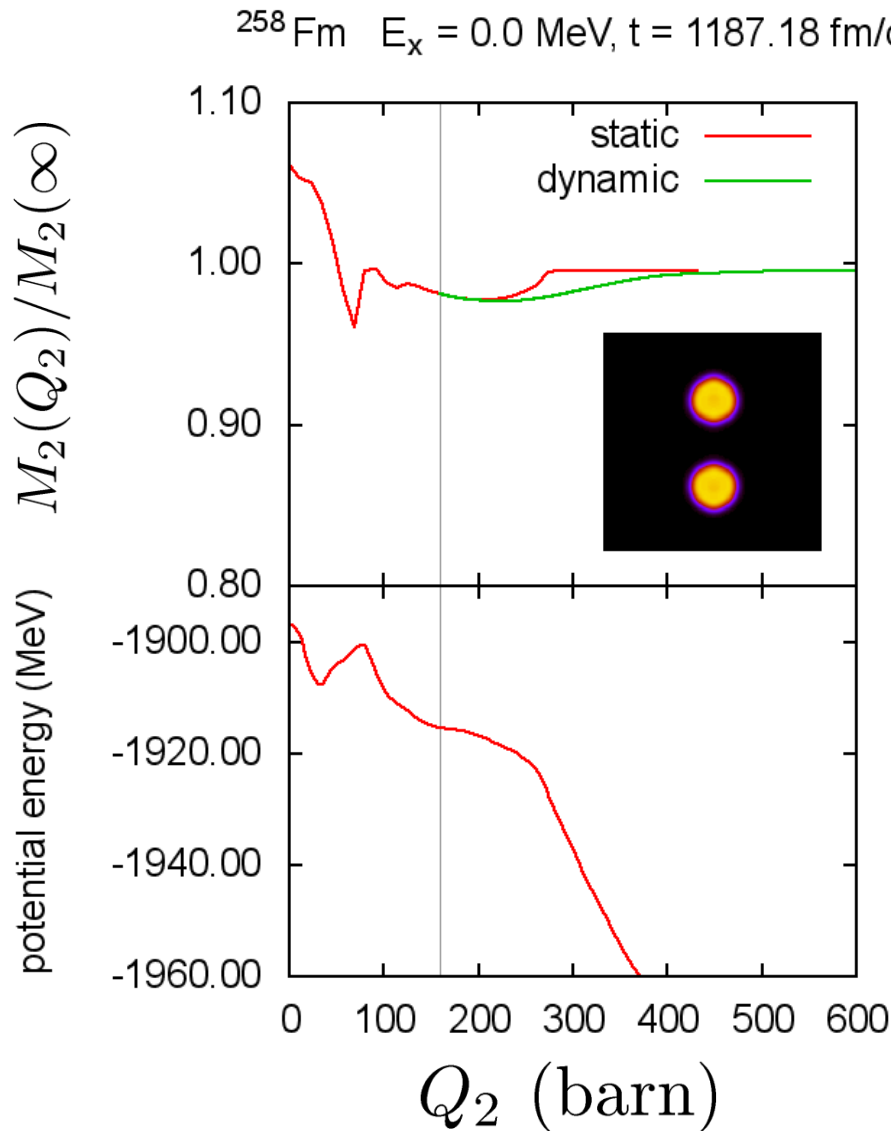


← Q_2 mass on dynamical path

- Deviation from static one around scission
- Scission happens more smoothly

$$\frac{m_N}{M_\alpha} = \text{Tr}[\rho \nabla Q_\alpha \cdot \nabla Q_\alpha]$$

1. Collective mass and momentum



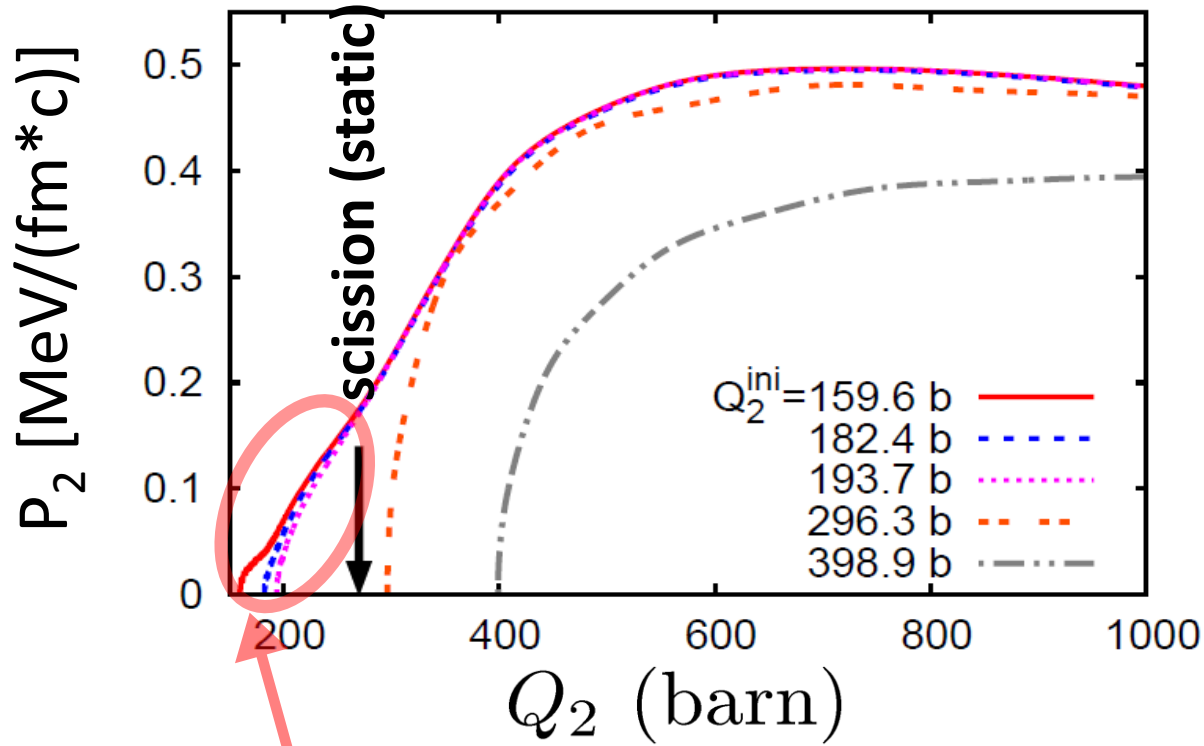
← Q_2 mass on dynamical path

- Deviation from static one around scission
- Scission happens more smoothly

$$\frac{m_N}{M_\alpha} = \text{Tr}[\rho \nabla Q_\alpha \cdot \nabla Q_\alpha]$$

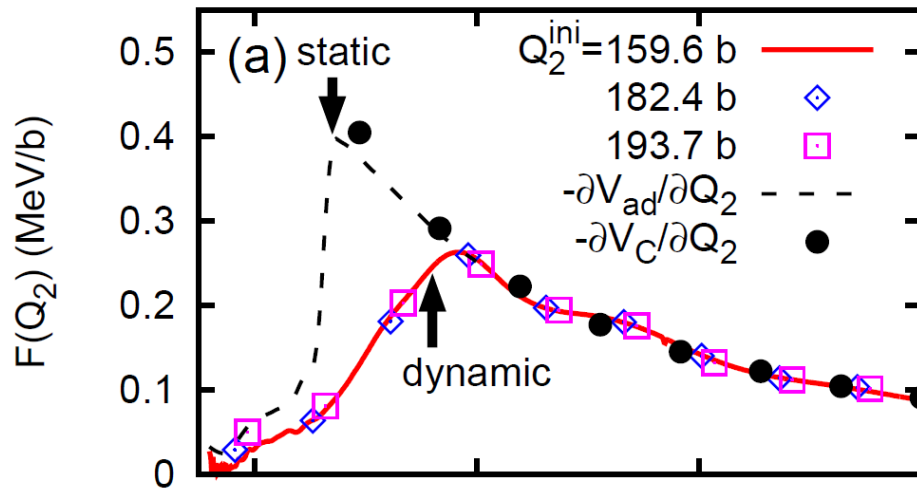
1. Collective mass and momentum

$$P_2 = M_2(dQ_2/dt)$$



**Dissipation
before the scission**

2. More analysis of the motion in Q_2 space



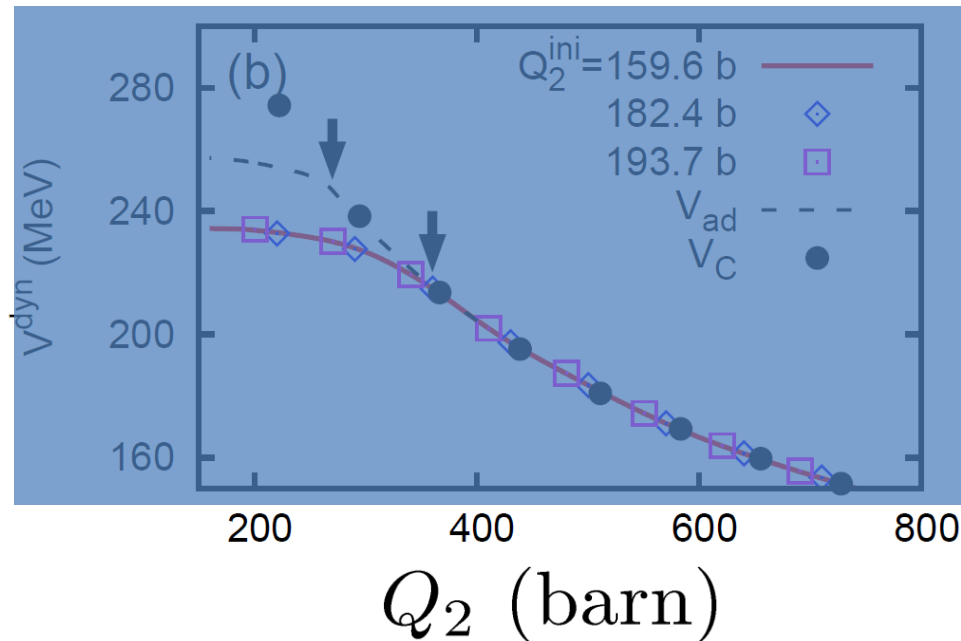
Assume a classical motion with dissipative force
cf. K. Washiyama and D. Lacroix, PRC78, 024610 ('08)

$$\dot{Q}_2 = \frac{P_2}{M_2}$$

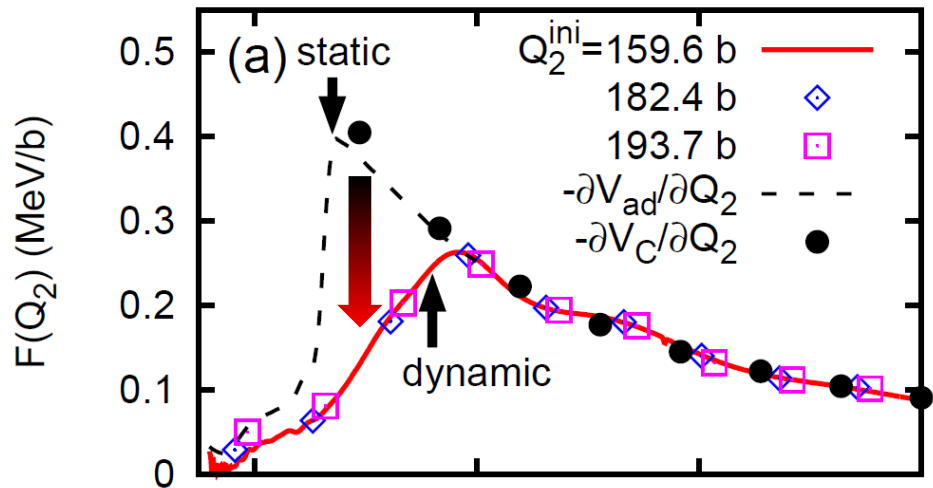
$$\dot{P}_2 = -\frac{\partial V_{\text{coll}}}{\partial Q_2} + \frac{1}{2} \frac{\partial M_2}{\partial Q_2} \dot{Q}_2^2 + \gamma(Q_2) \dot{Q}_2$$

$$\underbrace{\dot{P}_2 - \frac{1}{2} \frac{\partial M_2}{\partial Q_2} \dot{Q}_2^2}_{F(Q_2)} = -\frac{\partial V_{\text{coll}}}{\partial Q_2} + \gamma(Q_2) \dot{Q}_2$$

$F(Q_2) \sim$ force coming from
dynamical potential
and friction

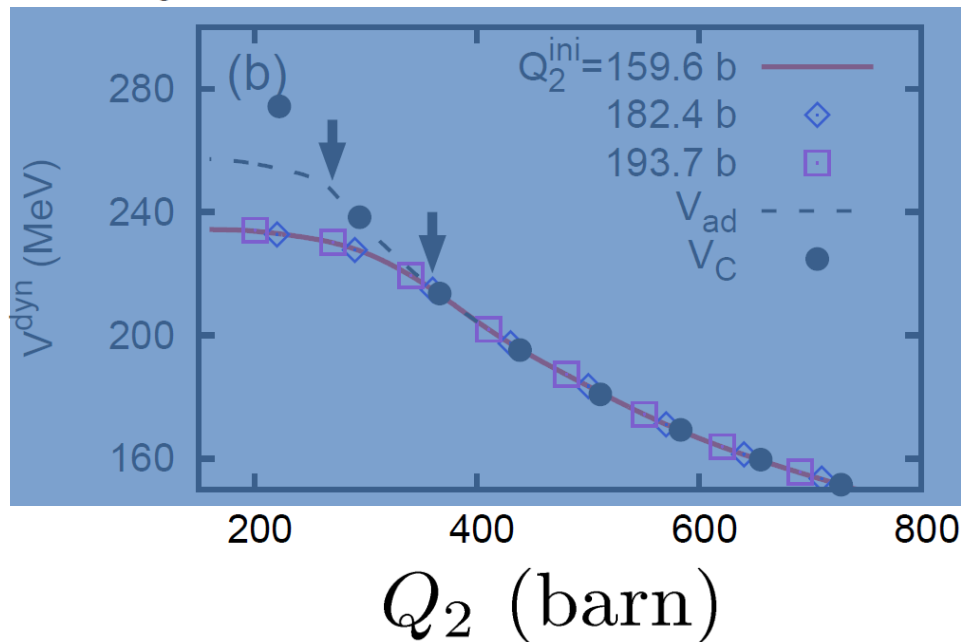


2. More analysis of motion in Q_2 space



$$\underbrace{\dot{P}_2 - \frac{1}{2} \frac{\partial M_2}{\partial Q_2} \dot{Q}_2^2}_{F(Q_2)} = -\frac{\partial V_{\text{coll}}}{\partial Q_2} + \gamma(Q_2) \dot{Q}_2$$

$F(Q_2) \sim$ force coming from
dynamical potential
and friction



- Reduction of outward force compared to the static path

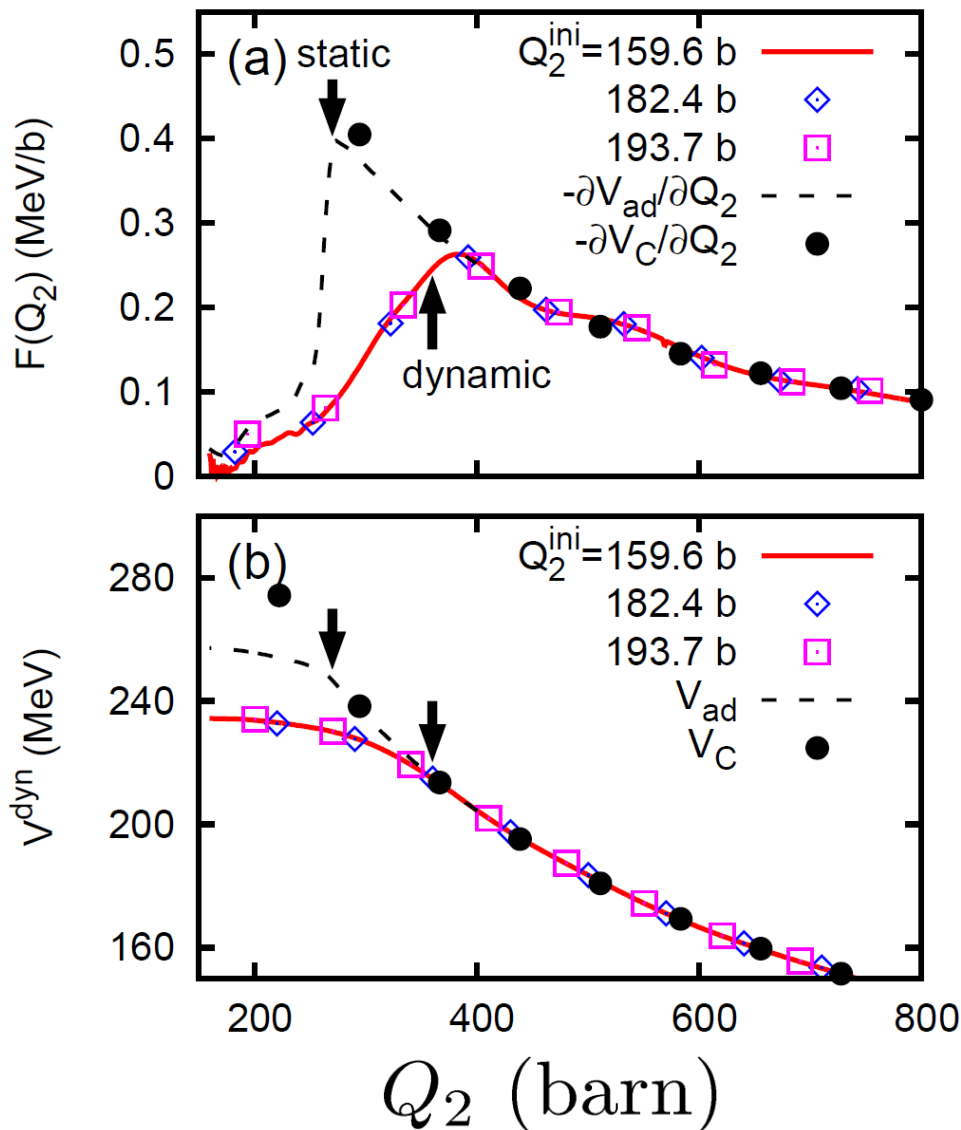
✓ fragments stick together more

and/or

✓ friction against separation (dissipation)

- Dissipation occurs before scission

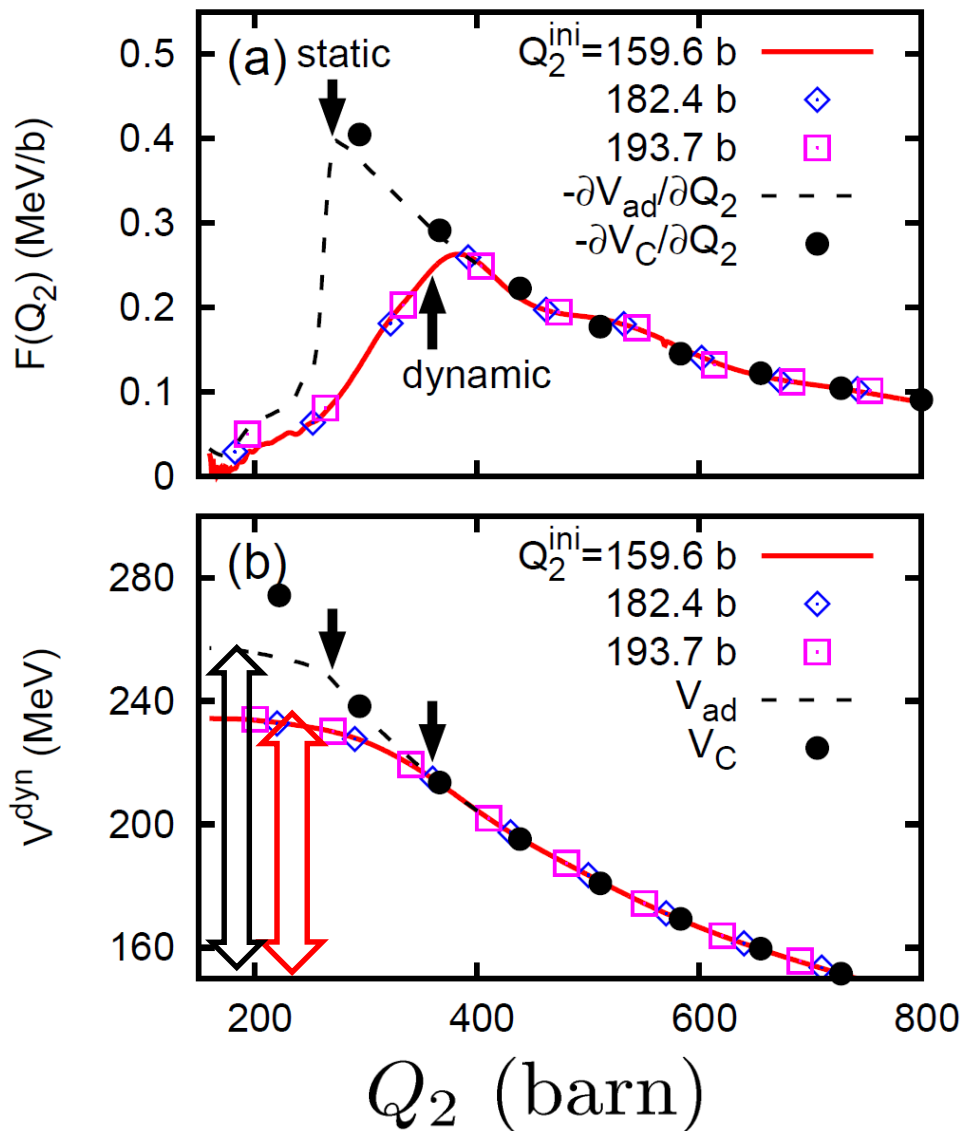
2. More analysis of motion in Q_2 space



Define
 “dynamical potential”
 (work done by F on Q_2)

$$V^{\text{dyn}}(Q_2) \equiv V_C(Q_2^{\text{max}}) + \int_{Q_2}^{Q_2^{\text{max}}} dQ'_2 F(Q'_2)$$

2. More analysis of motion in Q_2 space



Define
 “dynamical potential”
 (work done by F on Q_2)

$$V^{\text{dyn}}(Q_2) \equiv V_C(Q_2^{\text{max}}) + \int_{Q_2}^{Q_2^{\text{max}}} dQ'_2 F(Q'_2)$$

Potential along adiabatic path
Work by F along dynamic path
Difference = Dissipated Energy

3. Generalization to several DOFs

Diagonalize the inertia tensor:

$$\frac{m_N}{M_{\alpha\beta}} = \text{Tr}[\rho \nabla Q_\alpha \nabla Q_\beta]$$

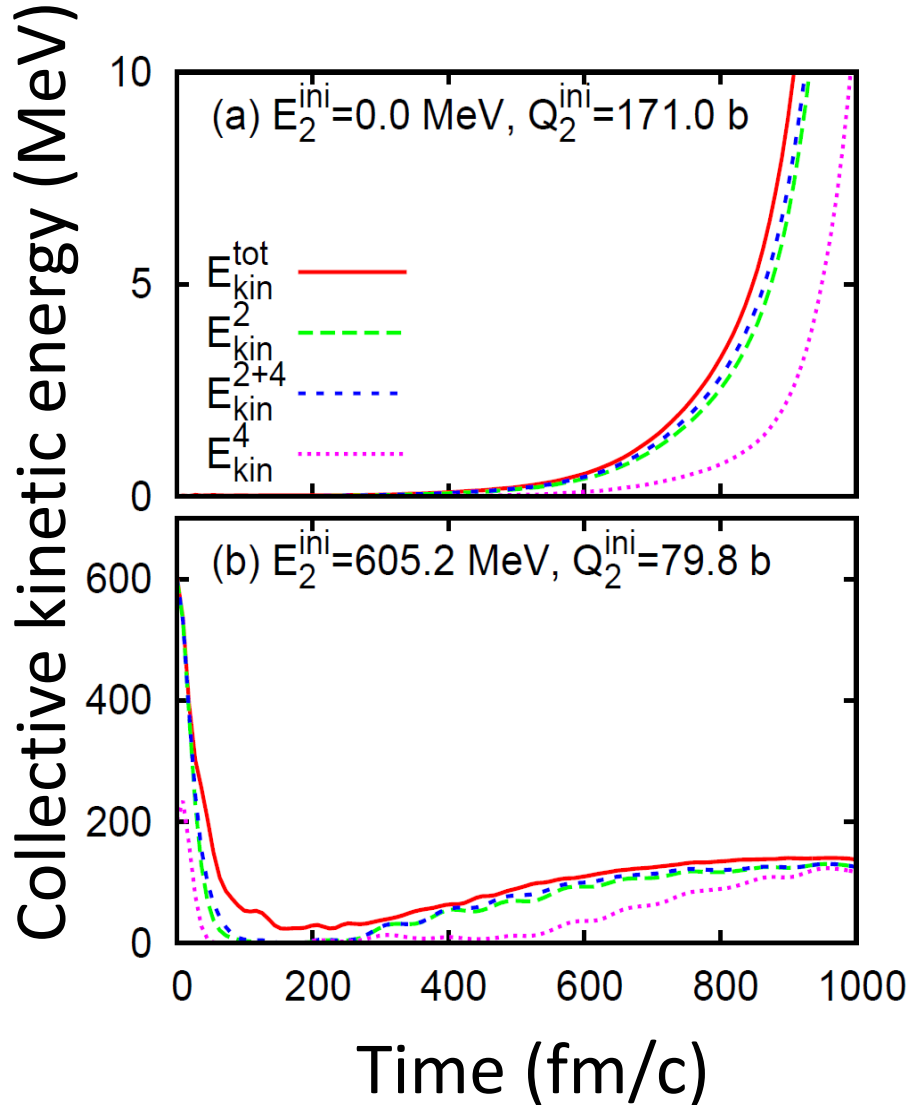
$$\frac{1}{M} \rightarrow \frac{1}{M'} = W \frac{1}{M} W^T$$

$$Q' \rightarrow WQ$$

$$(P/M)' \rightarrow W(P/M)$$

$$\Rightarrow \langle [Q'_\alpha, P'_\beta] \rangle = \delta_{\alpha\beta} i\hbar$$

3. Generalization to several DOFs



Diagonalize the inertia tensor:

$$\frac{m_N}{M_{\alpha\beta}} = \text{Tr}[\rho \nabla Q_\alpha \nabla Q_\beta]$$

$$\frac{1}{M} \rightarrow \frac{1}{M'} = W \frac{1}{M} W^T$$

$$Q' \rightarrow WQ$$

$$(P/M)' \rightarrow W(P/M)$$

Collective kinetic energy

$$E_{\text{kin}}^{\{\alpha\}} = \sum_{\alpha} \frac{P_\alpha'^2}{2M'_\alpha} \quad \text{selected set}$$

$$E_{\text{kin}}^{\text{tot}} = \int d^3r \frac{\mathbf{j}^2}{\rho} \quad \text{total}$$

Summary and perspectives

- We have developed a method to extract information in collective space from TD-EDF theory
- Our goal: **unified microscopic approach for fission**
- Next steps
 - beyond-mean-field effects with configuration mixing
 - mapping onto $\{Q_\alpha, P_\alpha\}$ space
 - quantum/thermal fluctuation of collective DOFs
 - obtain physical observables
 - ✓ fragment mass/charge distribution
 - ✓ kinetic energy of fragments
 - ✓ ...
 - compare them with data and other theoretical approaches

