# Testing consistency of the LCDM model with Planck data

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# Statistics of CMB

CMB Anisotropy Sky map => Spherical Harmonic decomposition



$$\Delta T(\theta,\phi) = \sum_{l=2}^{\infty} \sum_{m=-l}^{l} a_{lm} Y_{lm}(\theta,\phi)$$

$$\langle a_{lm} a^*_{l'm'} \rangle = C_l \delta_{ll'} \delta_{mm'}$$

Gaussian Random field => Completely specified by angular power spectrum  $l(l+1)C_l$ :

Power in fluctuations on angular scales of  $\sim \pi/l$ 



Sensitivity of the CMB acoustic temperature spectrum to four fundamental cosmological parameters. **Total density Dark Energy** Baryon density and Matter density.

From Hu & Dodelson, 2002





Testing deviations from an assumed model (without comparing different models)

**Gaussian Processes:** 

Modeling of the data around a mean function searching for likely features by looking at the the likelihood space of the hyperparameters.

**Bayesian Interpretation of Crossing Statistic:** 

Comparing a model with its own possible variations.

# Gaussian Process

Efficient in statistical modeling of stochastic variables
 Derivatives of Gaussian Processes are Gaussian
 Processes

Provides us with all covariance matrices

**Mean Function** 

Data

Shafieloo, Kim & Linder, PRD 2012 Shafieloo, Kim & Linder, PRD 2013







### Detection of the features in the residuals











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### GP Reconstruction of Planck TT, TE, EE spectra



### GP Reconstruction of Planck TT, TE, EE spectra

excellent agreement between Planck data and the best-fit LCDM



# **Crossing Statistic**

- To deal with unknown uncertainties/ systematics in the data
- To go beyond averaging nature of Chi square statistic (as a core metric in most statistical analysis) extracting more information from the data.

Shafieloo et al JCAP 2011 Shafieloo, JCAP 2012a Shafieloo, JCAP 2012b

# What if the actual size of the error bars are not known?



$$\chi^2 = \sum_{i}^{N} \frac{(\mu_i^t - \mu_i^e)^2}{\sigma_i^2},$$
  
$$\sigma_i^2 = \sigma_{i(data)}^2 + \sigma_{(sys)}^2$$

$$P(\chi^2; N) = \frac{2^{-N/2}}{\Gamma(N/2)} \chi^{N-2} e^{-\chi^2/2}$$

Constitution Supernovae data (2009)

$$Prob(\chi^2;N) = \int_{\chi^2}^\infty P(\chi^2;N) d\chi'^2.$$

# Equal in being probable?!





$$\chi^2 = \sum_i^N \frac{(\mu_i^t - \mu_i^e)^2}{\sigma_i^2},$$



## **Crossing Statistic**

If a proposed model is different than the actual model, then they cross each other at one or two or three or ... N points.



A. Shafieloo, T. Clifton & P. Ferreira, 2010



# One point Crossing: T1

- 1. Assume a model
- 2. Construct the normalized residuals
- 3. Finding the crossing point and calculating T1 by maximizing T(n1):
- 4. Comparing the results with Monte Carlo simulations.

$$q_i(z_i) = \frac{\mu_i(z_i) - \bar{\mu}(z_i)}{\sigma_i(z_i)}.$$

$$T(n_1) = Q_1(n_1)^2 + Q_2(n_1)^2$$

$$Q_1(n_1) = \sum_{i=1}^{n_1} q_i(z_i)$$
$$Q_2(n_1) = \sum_{i=n_1+1}^{N} q_i(z_i),$$

# Two points Crossing: T2

1-2.....
3. Finding the crossing points and calculating T2 by maximizing T(n1,n2):

$$q_i(z_i) = \frac{\mu_i(z_i) - \bar{\mu}(z_i)}{\sigma_i(z_i)}.$$

$$T(n_1, n_2) = Q_1(n_1, n_2)^2 + Q_2(n_1, n_2)^2 + Q_3(n_1, n_2)^2$$

4. Comparing the results with Monte Carlo simulations.

And so on we can derive T3, T4,...

$$Q_1(n_1, n_2) = \sum_{i=1}^{n_1} q_i(z_i)$$
$$Q_2(n_1, n_2) = \sum_{i=n_1+1}^{n_2} q_i(z_i)$$
$$Q_3(n_1, n_2) = \sum_{i=n_2+1}^{N} q_i(z_i).$$

# **Important Features:**

For N data points, the last mode of Crossing Statistic is T(N-1) which is identical to Chi Square Statistic

$$T_{N-1} = \sum_{i}^{N} (q_i)^2 = \chi^2$$

# The zero mode of Crossing Statistic is similar to Median Statistic

not only should the whole sample of residuals have a Gaussian distribution around the mean, but so should any continuous subsample.

$$T_0 = (\sum_i^N q_i)^2$$



Assumed model is consistent with the data using chi square

Data: Flat LCDM  $\Omega_{0m}^{true} = 0.27$ Assumed Model:

Flat LCDM  $\Omega_{0m}^{erroneous} = 0.22$ 

Assumed model is ruled out at 99% CL using T1

## **Comparing Two Statistics**

	T1	Chi Square
Ruling out by 99% CL	1% (Correct Model) 28.5% (Incorrect Model)	1% (Correct Model) 1.9% (Incorrect Model)
Ruling out by 99% CL Assuming extra (0.05) intrinsic dispersion	0.5% (Correct Model) 26.4% (Incorrect Model)	0% (Correct Model) 0% (Incorrect Model)

$$\sigma_i^2 = \sigma_{i(data)}^2 + \sigma_{(sys)}^2$$

Correct Model: Flat LCDM with  $\Omega_{0m}^{true} = 0.27$ 

Incorrect Model: Flat LCDM with  $\Omega_{0m}^{erroneous} = 0.22$ 

Simulated data similar to Constitution compilation

**Bayesian Interpretation of Crossing Statistics** 

### Theoretical Model

### **Crossing Function**

$$\mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\mathrm{modified}}^{N} = \mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\Omega_{\mathrm{b}}, \Omega_{\mathrm{CDM}}, \mathrm{H}_{0}, \tau, \mathrm{A}_{\mathrm{s}}, \mathrm{n}_{\mathrm{s}}} \times T_{N}(C_{0}, C_{1}, C_{2}, ..., C_{N}, \ell).$$

$$\begin{split} T_0(C_0,x) &= C_0 \\ T_{\rm I}(C_0,C_1,x) &= T_0(C_0,x) + C_1 \ x \\ T_{\rm II}(C_0,C_1,C_2,x) &= T_{\rm I}(C_0,C_1,x) + C_2(2x^2-1) \\ T_{\rm III}(C_0,C_1,C_2,C_3,x) &= T_{\rm II}(C_0,C_1,C_2,x) + C_3(4x^3-3x) \\ T_{\rm IV}(C_0,C_1,C_2,C_3,C_4,x) &= T_{\rm III}(C_0,C_1,C_2,C_3,x) + C_4(8x^4-8x^2+1) \\ T_{\rm V}(C_0,C_1,C_2,C_3,C_4,C_5,x) &= T_{\rm IV}(C_0,C_1,C_2,C_3,C_4,x) + C_5(16x^5-20x^3+5x) \end{split}$$

$$x = \ell/\ell_{\text{max}}$$
  $\ell_{\text{max}} = 2500.$ 

Shafieloo et al JCAP 2011 Shafieloo, JCAP 2012a Shafieloo, JCAP 2012b

*Chebychev polynomials* have the properties of orthogonality and convergence within the limited range of -1 < x < 1.







Data	ΛCDM	$T_0$	$T_{\rm I}$	$T_{\rm II}$	$T_{\rm III}$	$T_{\rm IV}$	$T_{\rm V}$
Planck low- $\ell$ ( $\ell$ =2-49)	-6.3	-7	-8.5	-8.6	-9.8	-9.7	-9.7
Planck high- $\ell$ ( $\ell$ =50-2500)	7794.9	7793.8	7793.8	7789.6	7785.9	7785.7	7784.7
Total	7788.6	7786.8	7785.3	7781	7776.1	7776	7775
$\chi^2_{ m Model}$ - $\chi^2_{ m \Lambda CDM}$	-	-1.8	-3.3	-7.6	-12.5	-12.6	-13.6

### **Theoretical Model**

### **Crossing Function**

 $\mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\mathrm{modified}}^{N} = \mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\Omega_{\mathrm{b}}, \Omega_{\mathrm{CDM}}, \mathrm{H}_{0}, \tau, \mathrm{A}_{\mathrm{s}}, \mathrm{n}_{\mathrm{s}}} \times T_{N}(C_{0}, C_{1}, C_{2}, ..., C_{N}, \ell).$ 



Data suggests substantial suppressions are required at both low and high multiples.

Hazra & Shafieloo, JCAP 2014

#### **Theoretical Model**

### **Crossing Function**

 $\mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\mathrm{modified}}^{N} = \mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\Omega_{\mathrm{b}}, \Omega_{\mathrm{CDM}}, \mathrm{H}_{0}, \tau, \mathrm{A}_{\mathrm{s}}, \mathrm{n}_{\mathrm{s}}} \times T_{N}(C_{0}, C_{1}, C_{2}, ..., C_{N}, \ell).$ 



Cosmological parameters while considering Crossing functions.

Hazra & Shafieloo, JCAP 2014

# Crossing Statistic (Bayesian Interpretation)

Theoretical model

**Crossing function** 

$$\mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\mathrm{modified}}^{N} = \mathcal{C}_{\ell}^{\mathrm{TT}} \mid_{\Omega_{\mathrm{b}}, \Omega_{\mathrm{CDM}}, \mathrm{H}_{0}, \tau, \mathrm{A}_{\mathrm{S}}, \mathrm{n}_{\mathrm{S}}, \ell} \times T_{i}(C_{0}, C_{1}, C_{2}, ..., C_{N}, \ell).$$

Confronting the concordance model of cosmology with Planck data Consistent only at 2~3 sigma CL





Dates







Published 28 January 2014







Test of consistency between temperature and polarization data from Planck 2015



Best fit (LCDM) TT power spectrum to EE data using 3<sup>rd</sup> anf 5<sup>th</sup> order Crossing functions







Test of consistency between temperature and polarization data from Planck 2015







Two data are consistent considering large uncertainties of the EE data.

There seems to be an amplitude shift (seen also in GP analysis).

Test of consistency between temperature and polarization data from Planck 2015





Crossing parameters marginalized over cosmological parameters fitting TT data

Test of consistency between LCDM model and Planck 2015 data

5 0.0

-1.6

1.6

0.8

0.0 U

0.8

-1.6

1.6

0.8

-1.6









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### Planck 2015: No feature but interesting effect on background parameters.

## Crossing Statistics



Shafieloo & Hazra, JCAP 2017

### Planck 2015: No feature but interesting effect on background parameters.

## Crossing Statistics

Planck polarization data and local H0 measurements seems having irresolvable tension. Maybe either or both have systematics? If not, new physics might be the answer.



Shafieloo & Hazra, JCAP 2017



No clear tension between Planck temperature and polarization data. There is a small amplitude shift.

No tension between Planck data and concordance LCDM model.

Even by allowing additional flexibility, Planck polarization data restrain to allow larger values of H0.