

YITP workshop: “Connecting high-energy astroparticle  
physics for origins of cosmic rays and future perspectives”  
@Kyoto University  
December 7–10

# **Systematic Study of Acceleration Efficiency in Young Supernova Remnants**

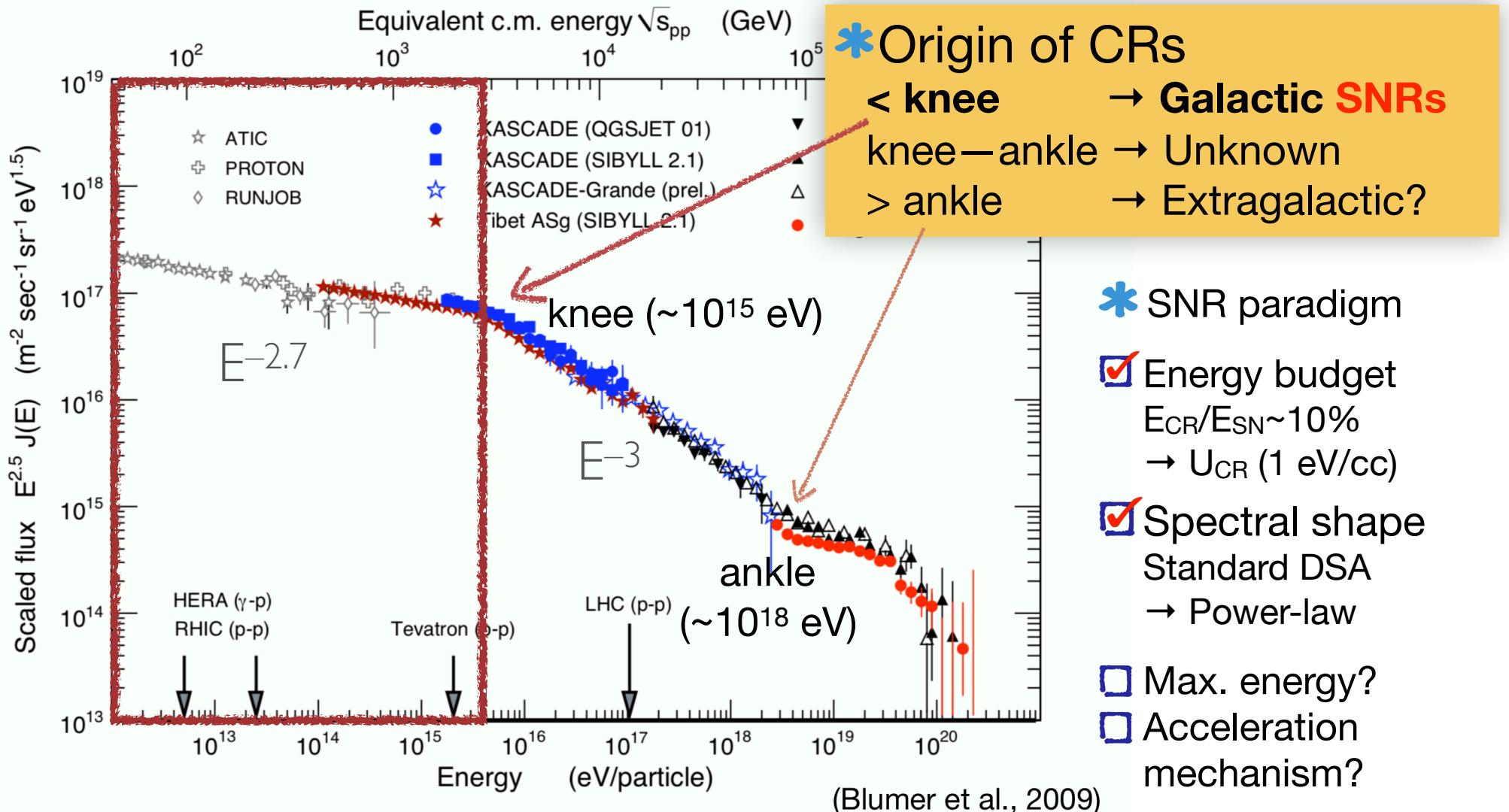
**(arxiv:2012.01047)**

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December 9, 2020  
Naomi Tsuji (RIKEN / iTHEMS)

# Cosmic Ray: CR

- High-energy particles in space
- Protons (~90%), He nuclei (~10%), electrons, and heavy nucleon...
- CR spectrum has two breaks; knee and ankle



# Acceleration efficiency

Acceleration timescale:  $t_{\text{acc}} \propto \frac{E\eta}{v_{\text{sh}}^2 B}$

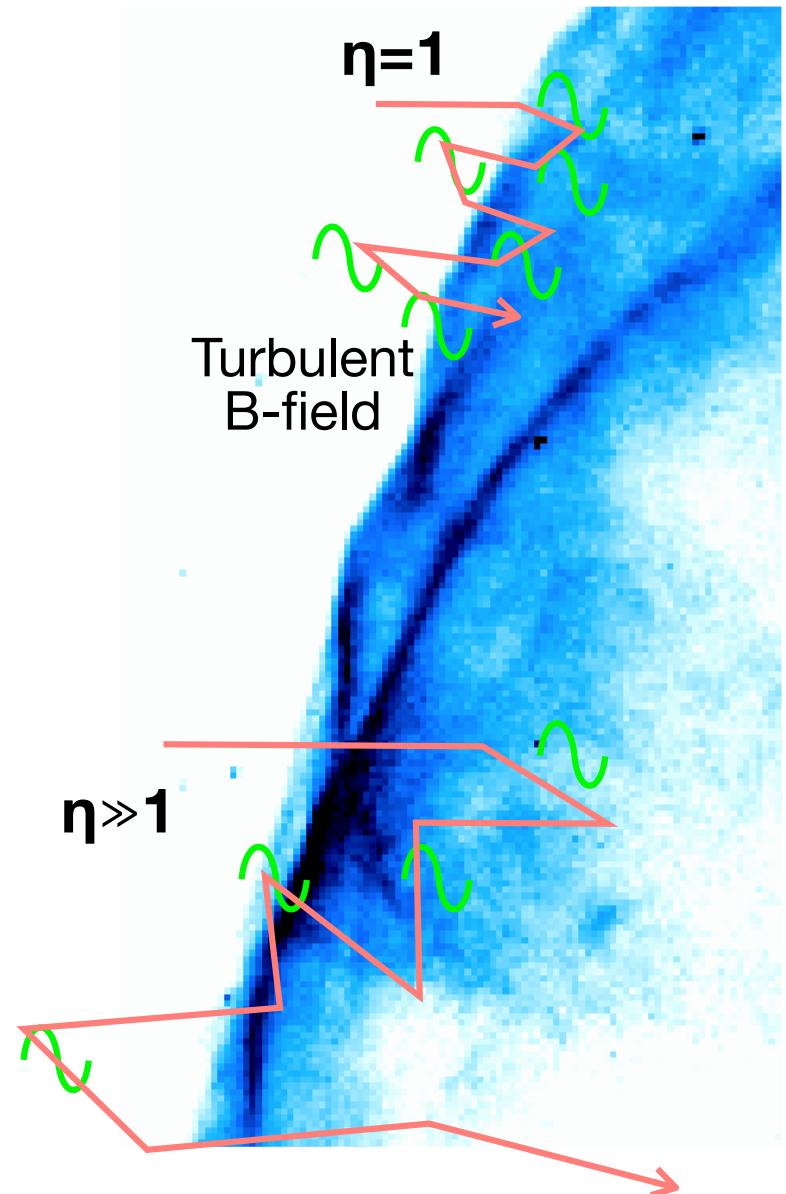
“Bohm factor”  $\eta$

Acceleration efficiency

$\eta = (\text{particle m.f.p.}) / (\text{gyroradius})$

$$\eta \sim (B_0 / \delta B)^2$$

|                  | $\eta=1$ (Bohm limit) | $\eta \gg 1$   |
|------------------|-----------------------|----------------|
| m.f.p.           | smallest              | large          |
| $t_{\text{acc}}$ | shortest              | long           |
| B-field          | turbulent             | less turbulent |
| Acceleration     | efficient!            | inefficient    |



# How to derive $\eta$ from observations?

Acceleration timescale:  $t_{\text{acc}} \propto \frac{E\eta}{v_{\text{sh}}^2 B}$

Cooling (synchrotron) timescale:  $t_{\text{synch}} \propto \frac{1}{EB^2}$

Cooling-limited acceleration:

$t_{\text{acc}} \approx t_{\text{synch}}$  gives cutoff energy

Electron cutoff:  $E_c \propto v_{\text{sh}} B^{-1/2} \eta^{-1/2}$

Synchrotron X-ray cutoff:  $\epsilon_c \propto E_c^2 B \propto v_{\text{sh}}^2 \eta^{-1}$

$$\boxed{\epsilon_0 \propto V_{\text{sh}}^2 / \eta}$$

If we measure **cutoff** and **shock speed**, we can obtain  $\eta$ !

Spectral fitting

Proper motion measurement

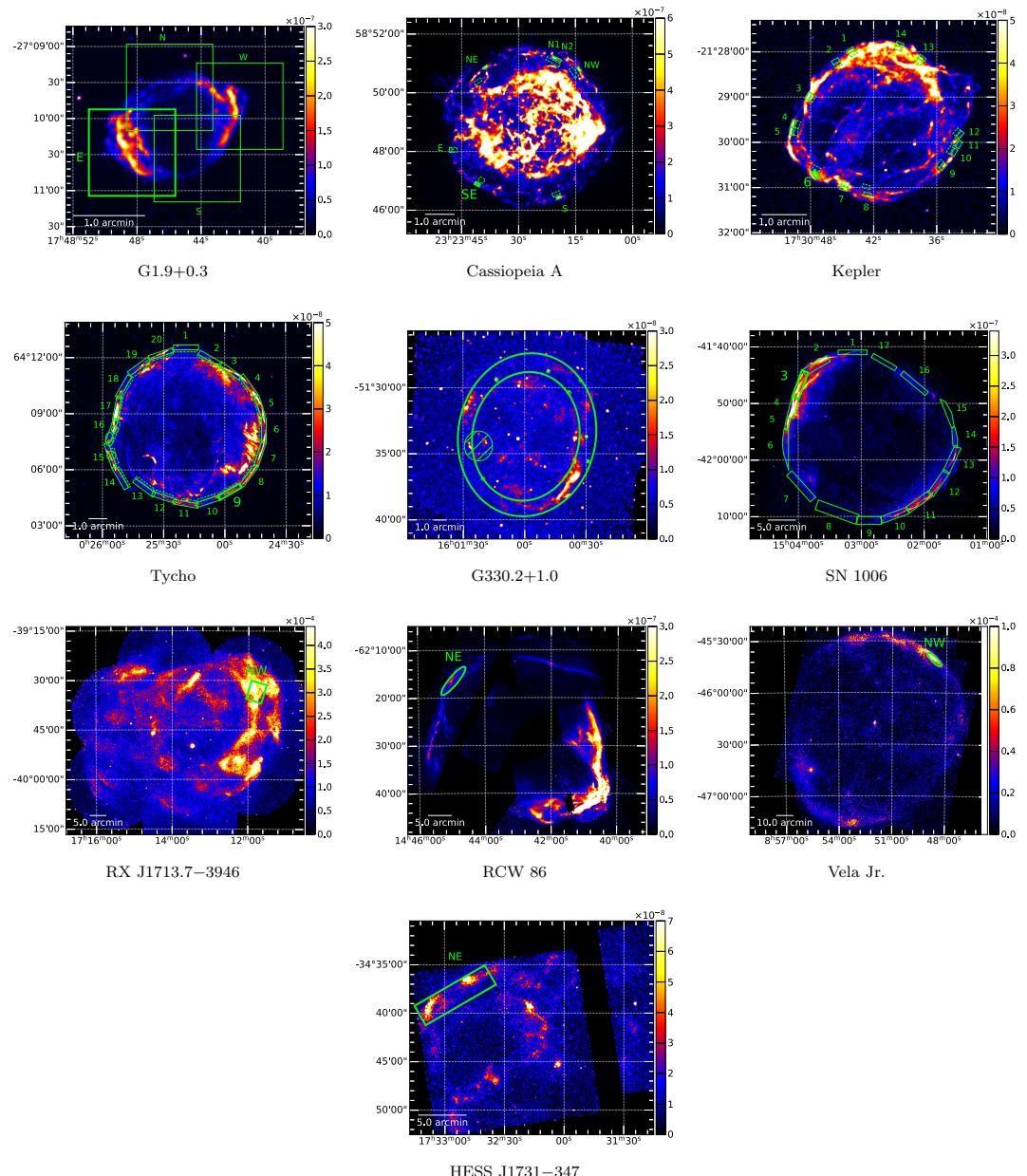
this work

\* More detailed analytical calculations are done by Zirakashvili & Aharonian 2007

# Young SNRs in X-ray

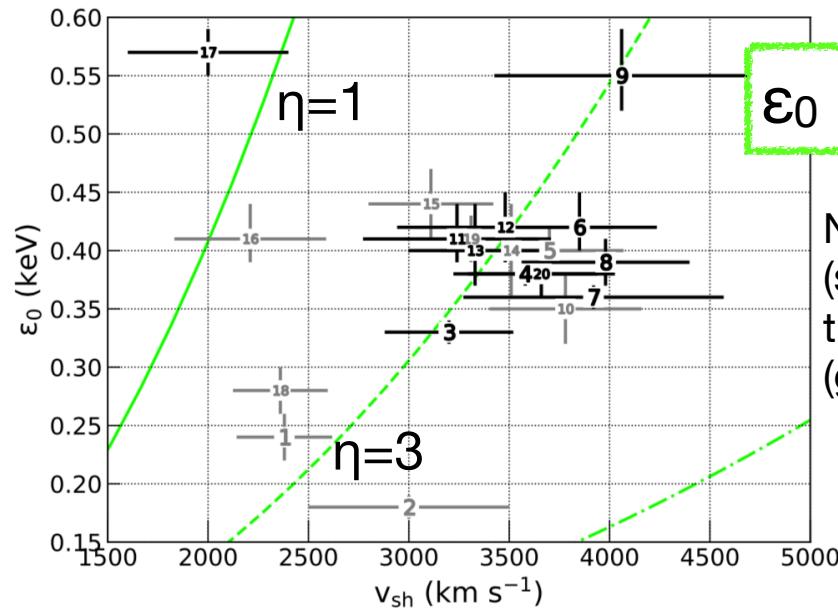
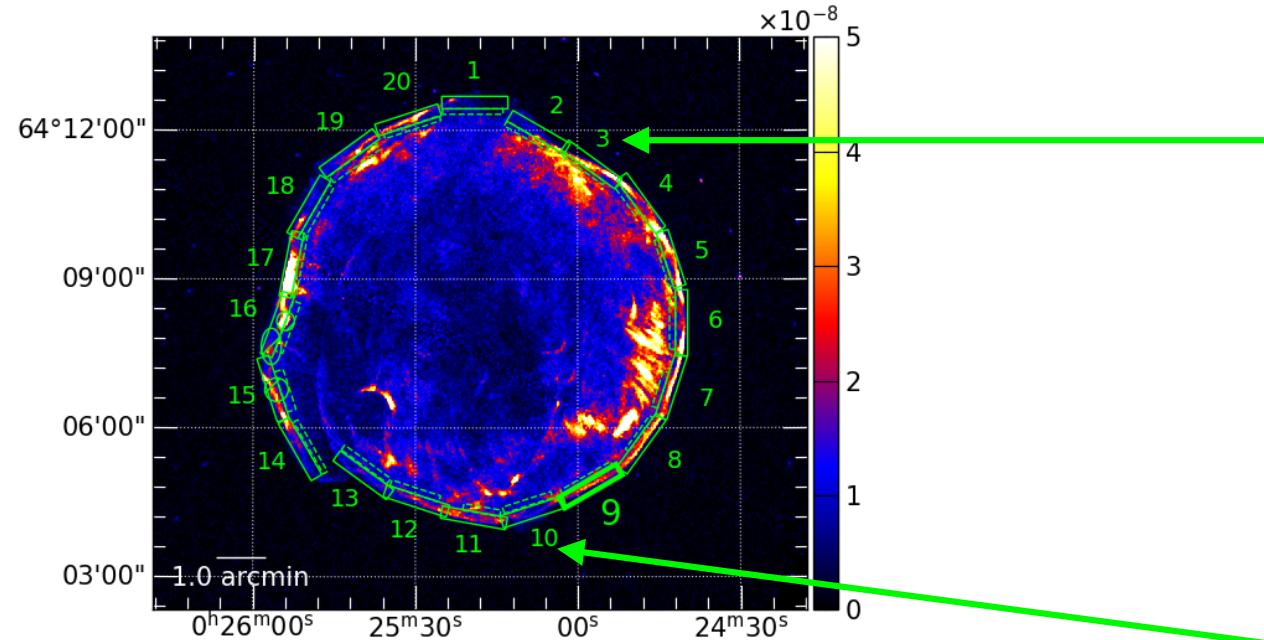
- Systematic analysis of young Galactic SNRs:
  - G1.9+0.3, Cassiopeia A, Kepler, Tycho, G330.2+1.0, SN1006, RX J1713.7–3946, RCW 86, Vela Jr., HESSJ 1731-347 (, SN 1987A)

Assume the hard continuum is synchrotron for SN1987A



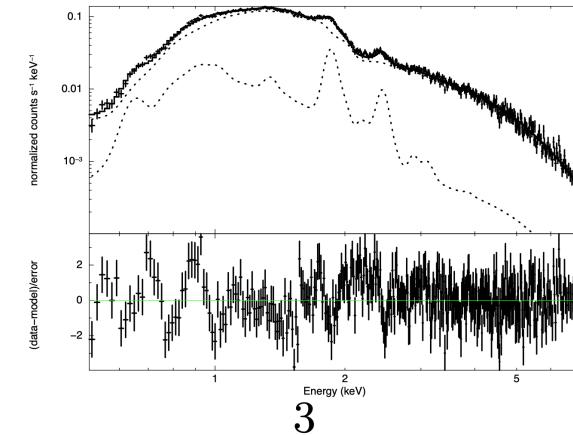
- Spectral fitting:
  - soft X-ray: Chandra/Suzaku
  - hard X-ray: NuSTAR
  - Model: ZA07
- Derived cutoff energy + known shock speed  
→ acceleration efficiency ( $\eta$ )

# Tycho

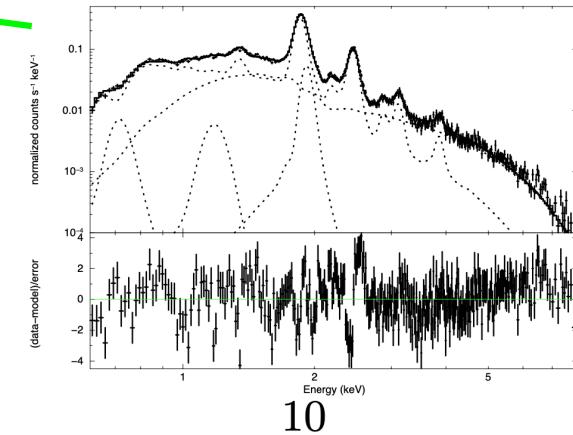


Nonthermal-dominated  
(shown in black)  
thermal-dominated  
(gray)

Nonthermal-dominated

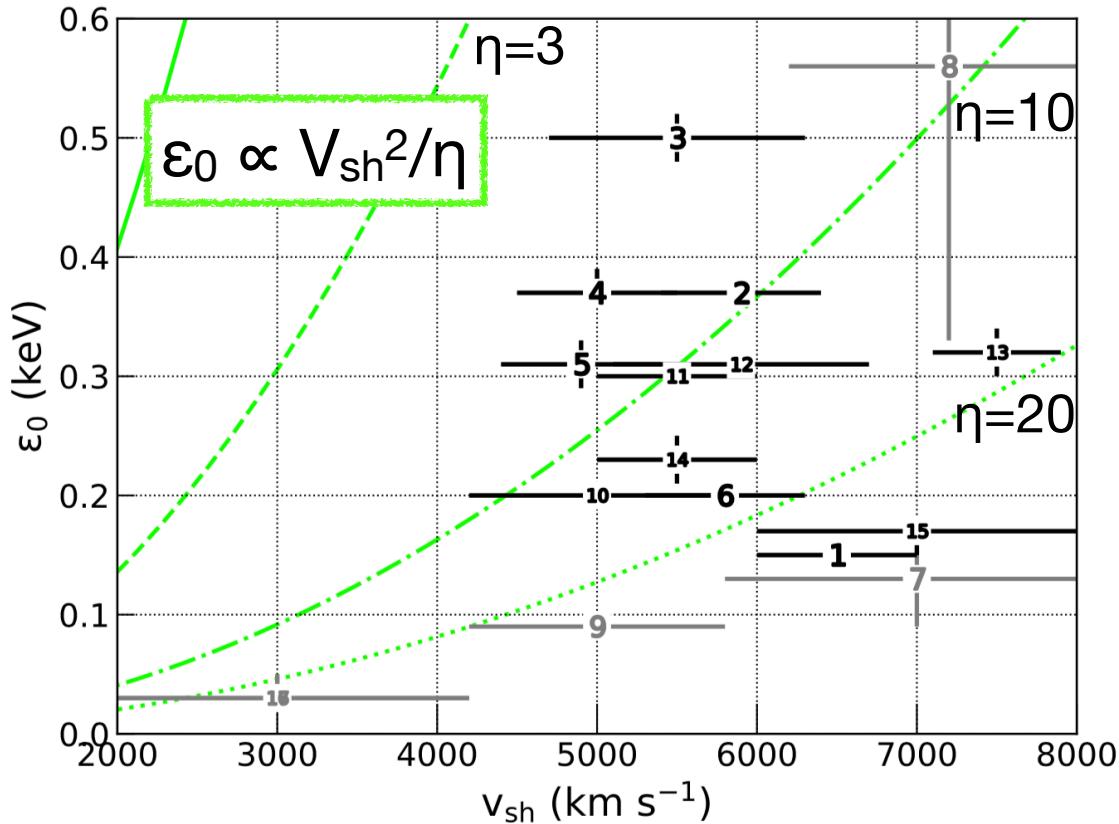


Thermal-dominated

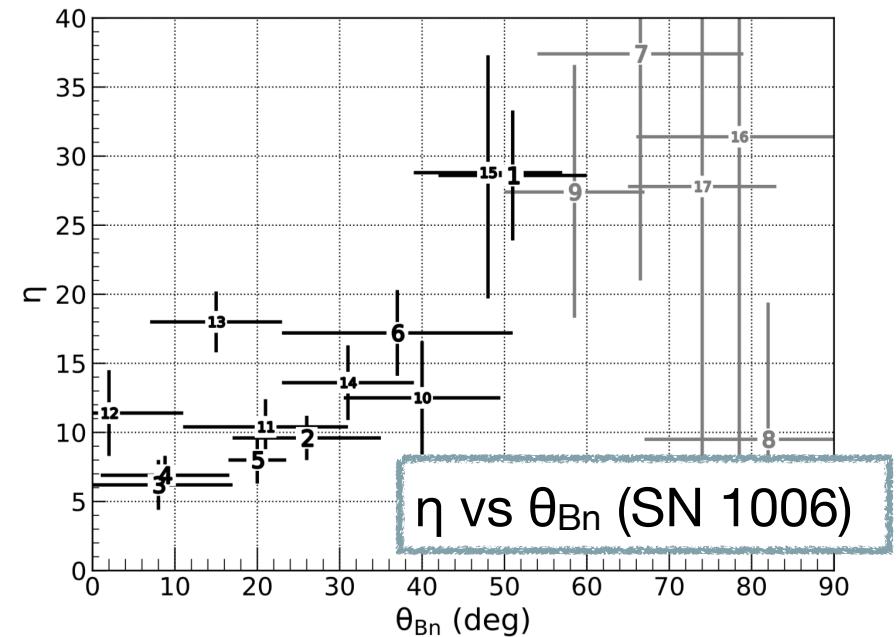
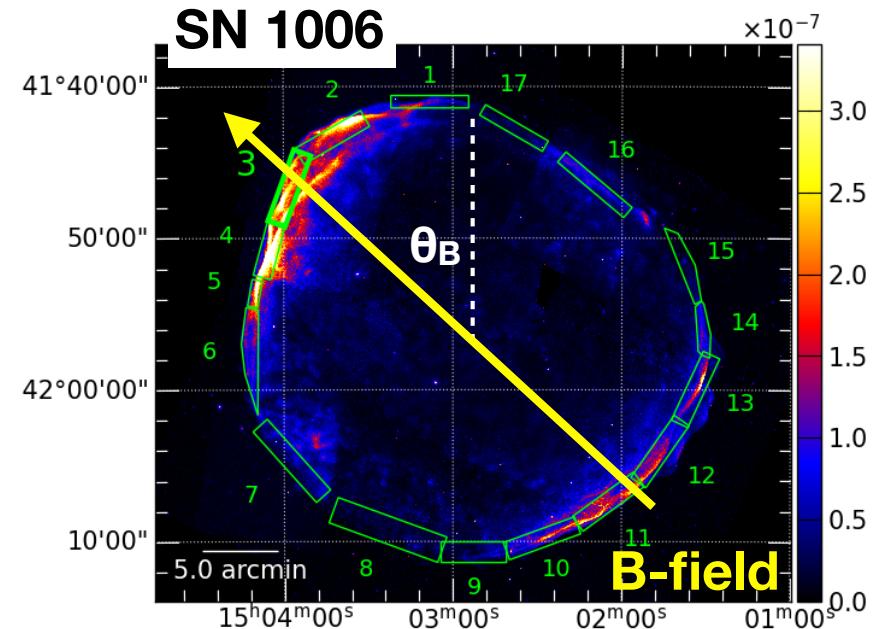


‘Standard’ acceleration with  
constant  $\eta = 3-5$

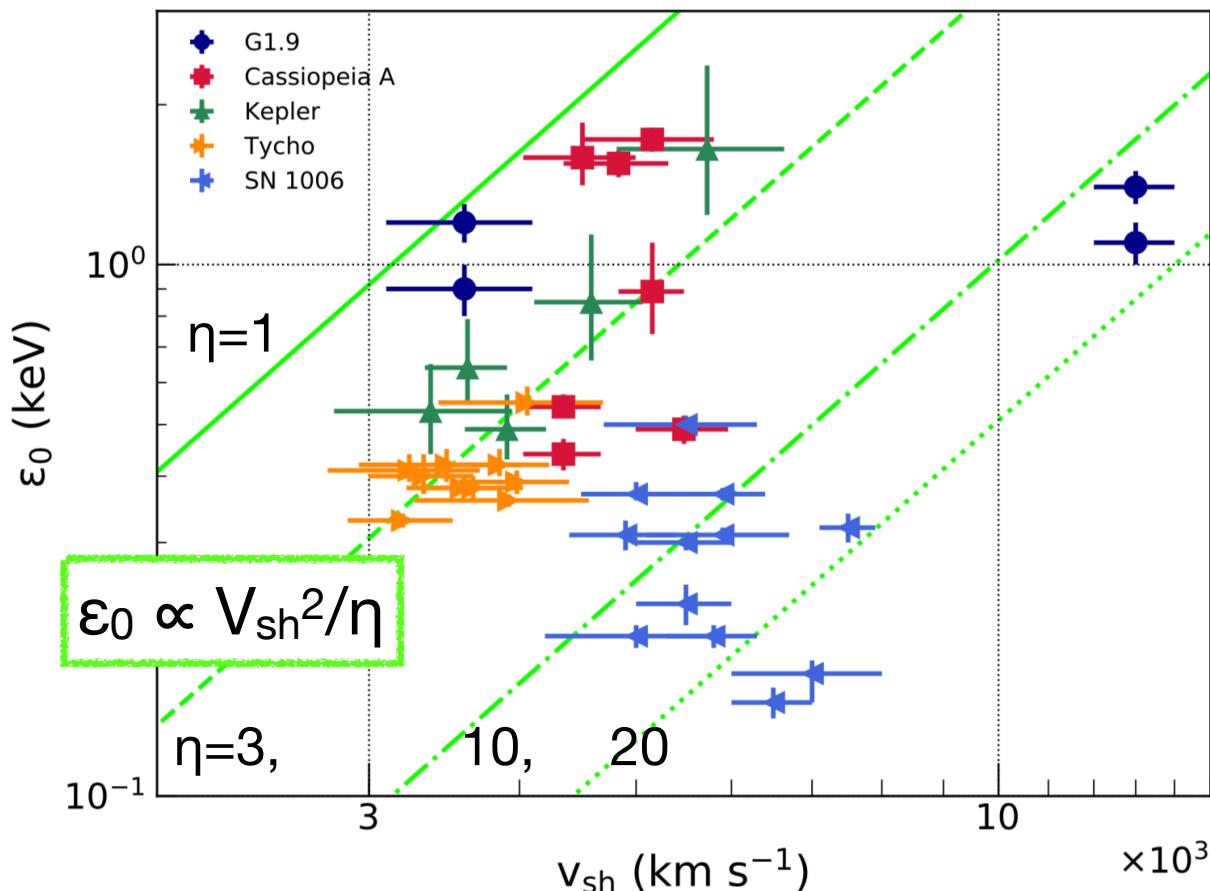
# SN 1006



- Inverse trend of the theoretical curve
- Acceleration affected by B-field; shock obliquity (e.g., Miceli+ 09)
- → Perpendicular shock is more efficient?



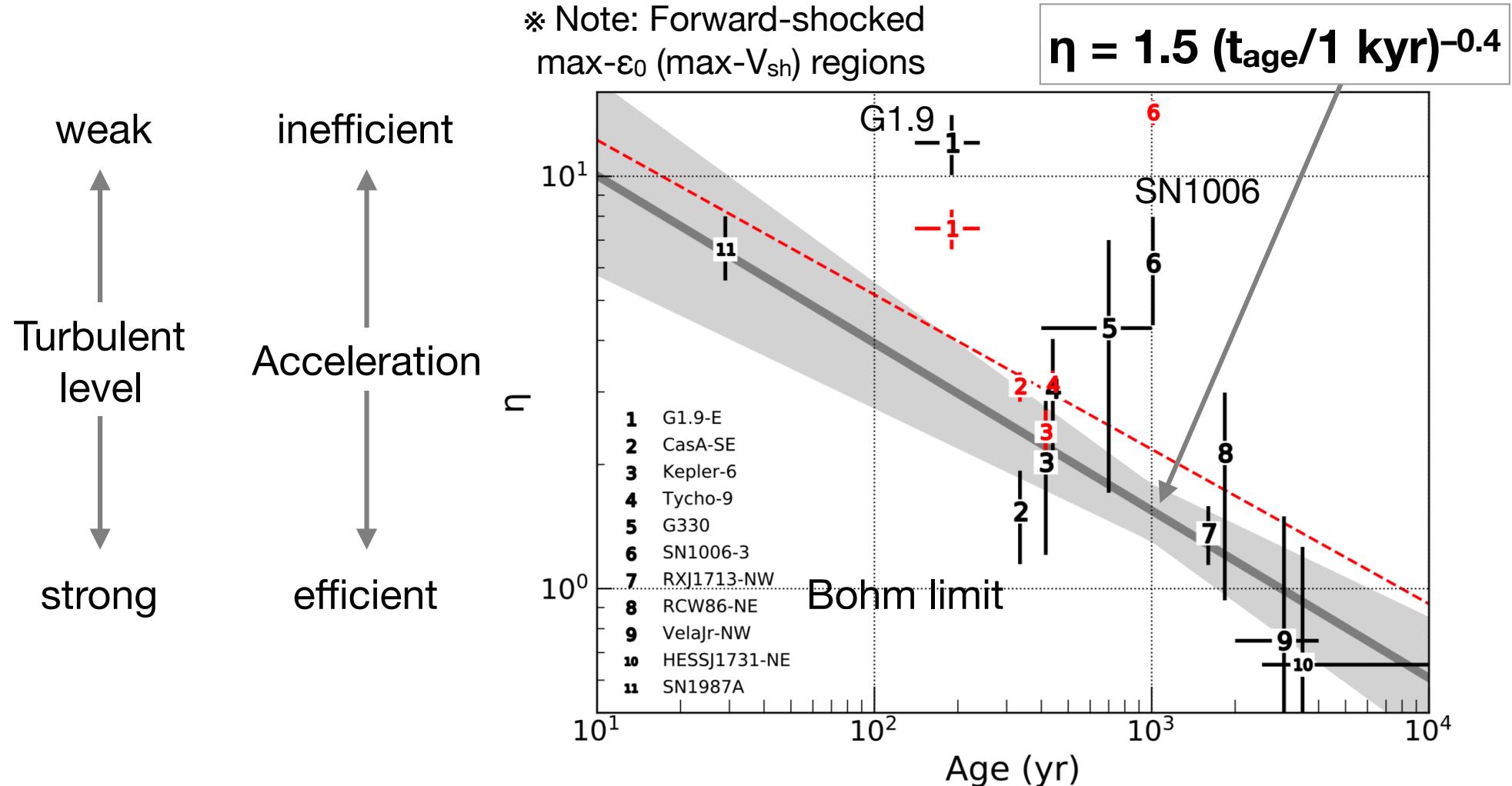
# $E_0$ v.s. $V_{sh}$ (summary)



- Kepler**  
Constant acc. efficiency
- Tycho**  
Constant acc. efficiency
- Cassiopeia A**  
Affected by ambient density
- SN 1006**  
Affected by B-field obliquity
- G1.9+0.3**  
Young accelerator

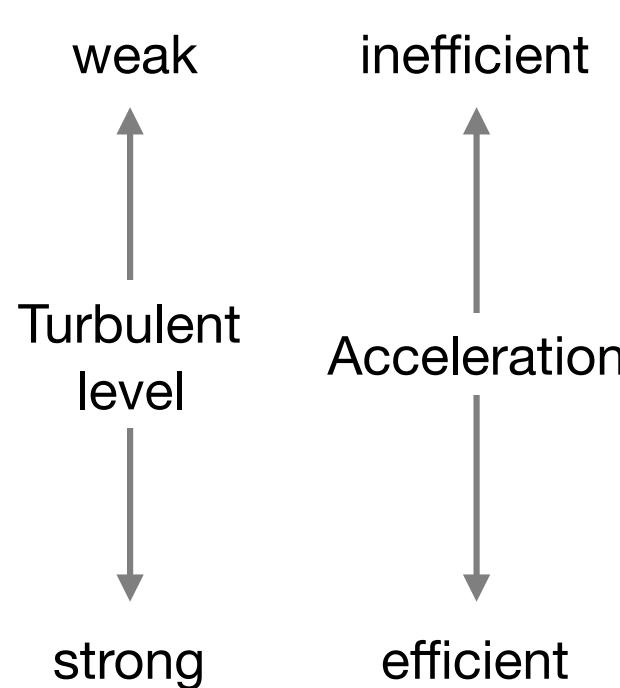
- Cutoff - shock speed relation
  - A variety (many kinds) of particle acceleration
  - See Tsuji+ 2020 for detail

# Acceleration efficiency in young SNRs



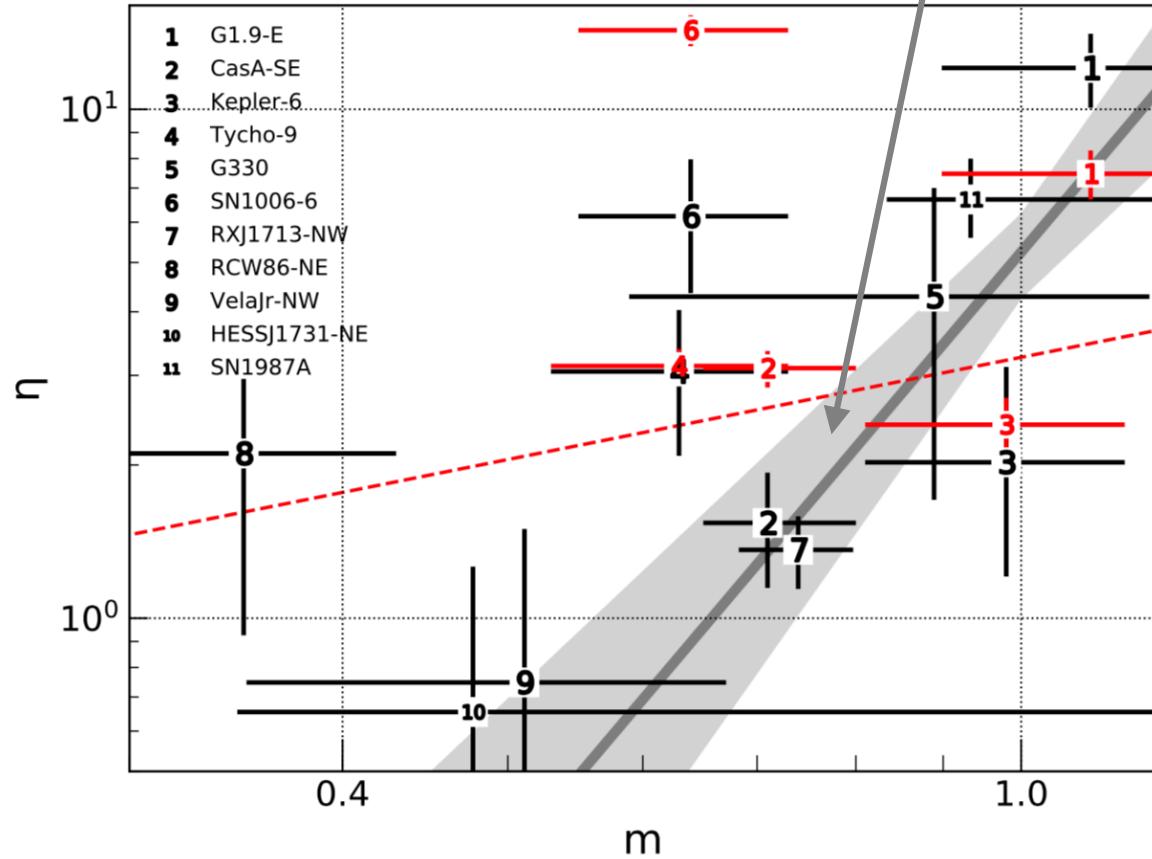
- Evolution of  $\eta$ :
  - Acceleration is more efficient (small  $\eta$ ) in older ( $\sim$ kyr) SNRs
  - could be related to turbulent production

# Acceleration efficiency in young SNRs



\* Note: Forward-shocked  
max- $\epsilon_0$  (max- $V_{sh}$ ) regions

$$\eta = 5.2 \text{ m}^{-4}$$

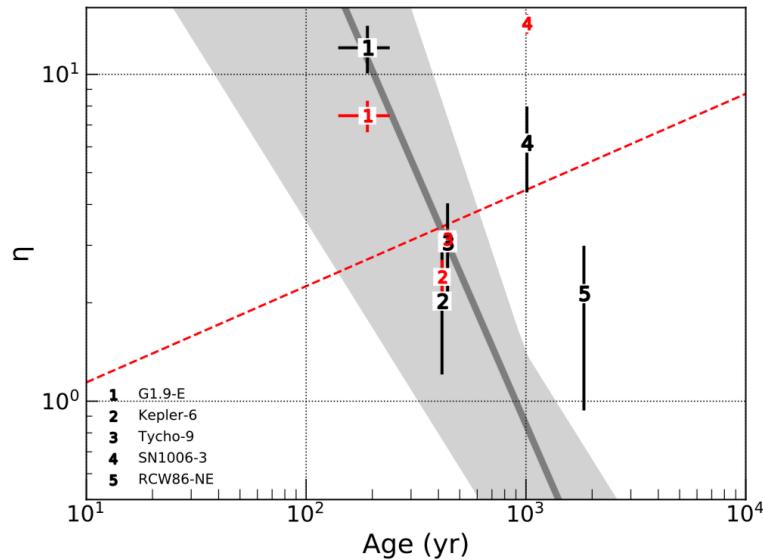


- Evolution of  $\eta$  (expansion parameter v.s.  $\eta$ ):
  - Acceleration is more efficient (small  $\eta$ ) in older ( $m \sim 0.4$ ) SNRs
  - could be related to turbulent production

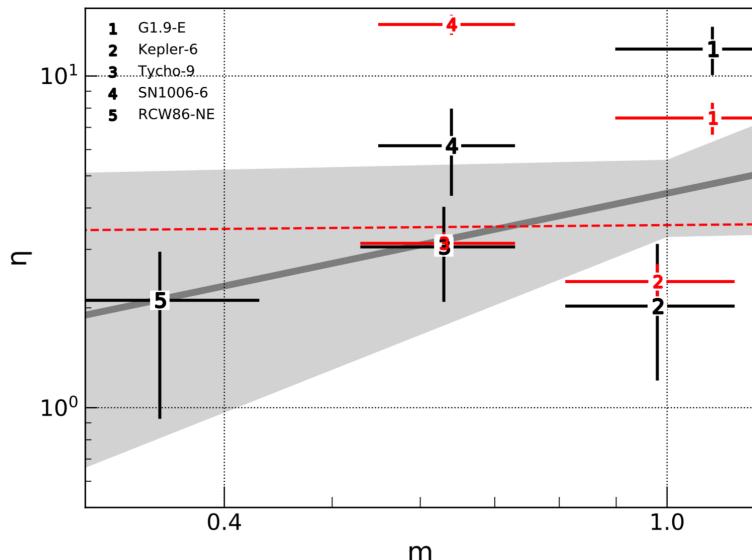
# Acceleration efficiency: type Ia & II

## Type Ia

G1.9, Kepler, Tycho, SN1006, RCW86



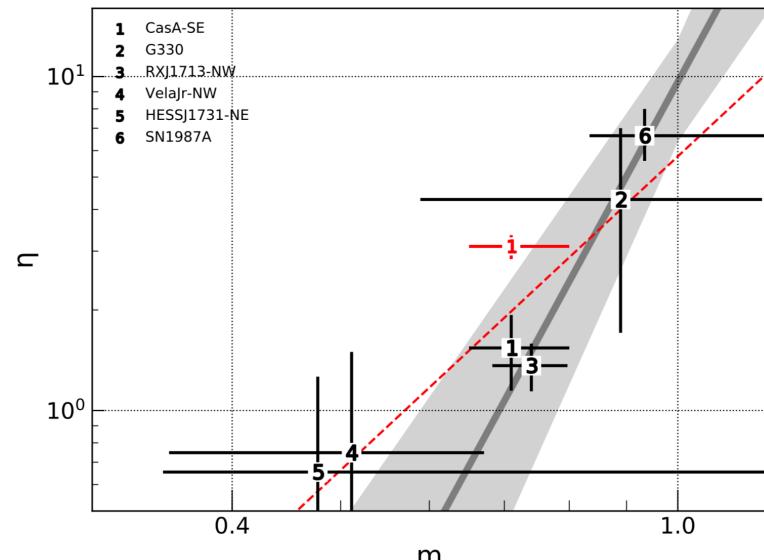
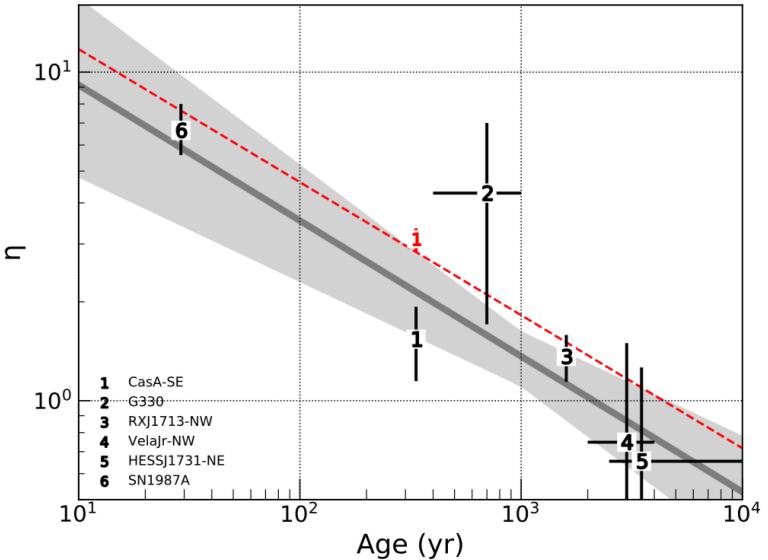
$\leftarrow \text{age}-\eta \rightarrow$



$\leftarrow m-\eta \rightarrow$

## Type II

Cas A, G330, RXJ1713, Vela Jr., HESS J1731,1987A



# Maximum energy

Age-limited maximum energy:  $E_{\max, \text{age}} = \frac{Zq}{c} tv_{\text{sh}}^2 B \eta^{-1}$

Shock speed:  $v_{\text{sh}} \propto \begin{cases} t^0 & \text{(Free-expansion phase)} \\ t^{-3/5} & \text{(Sedov-Taylor phase)} \end{cases}$

Magnetic field:  $B \propto t^{-\mu}$   
 $\mu = \begin{cases} 0 & \text{(Free-expansion)} \\ 0.55 - 0.9 & \text{(Sedov-Taylor)} \end{cases}$

(Bamba+ 2005; Volk+ 2005; Vink 2008)

Bohm factor:  $\eta \propto t^{-\delta}$  ( $\delta \sim 0.46$ ; this work)

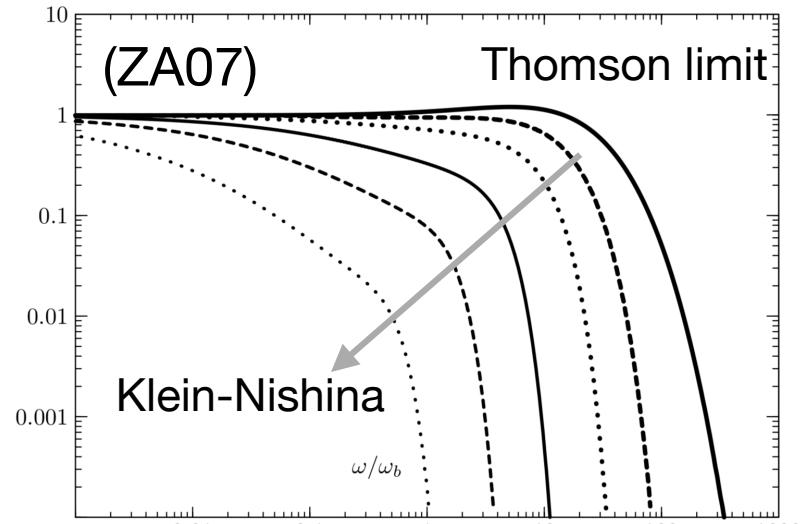
$E_{\max, \text{age}} \propto \begin{cases} t^{1-\mu+\delta} & \text{(Free-expansion)} \\ t^{-1/5-\mu+\delta} & \text{(Sedov-Taylor)} \end{cases}$

- Assume that  $\eta$  evolves as  $\eta \propto t^{-\delta}$  at free-expansion/ST stages before  $\eta=1$
- Max energy can be higher than expected before ( $\delta=0$ )

# Application to gamma-ray observation

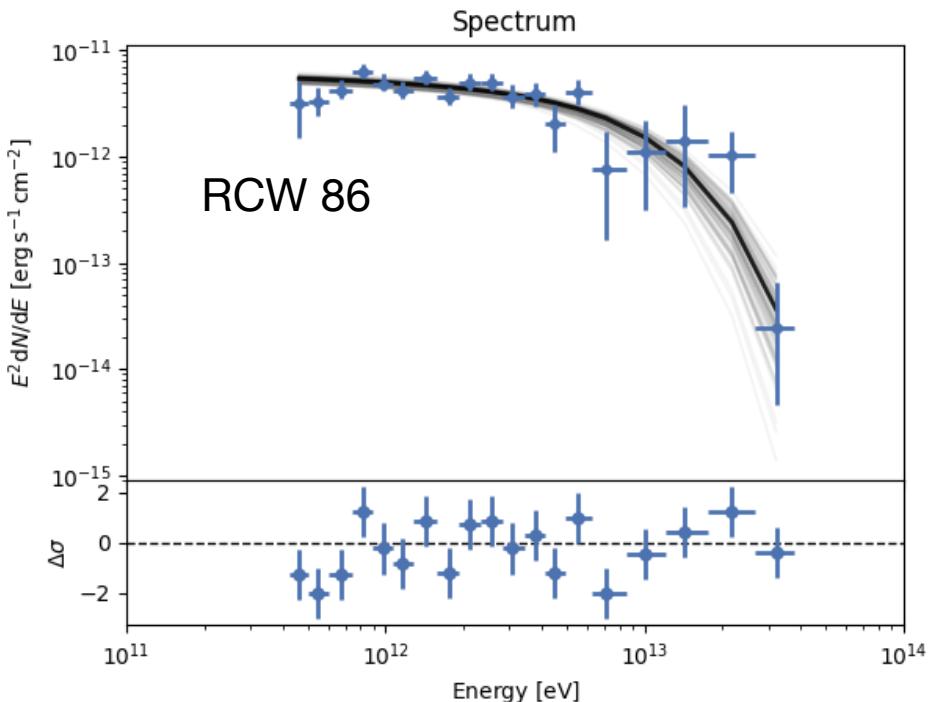
## Model (electron)

- SNR shock
- Zirakashvili & Aharonian 2007 (ZA07)
- Energy loss: synchrotron cooling
- Diffusion: Bohm type



## Model (gamma-ray)

Inverse Compton scattering  
(in KN regime using Naima)



## Observation

e.g.) RCW 86-whole (w/ H.E.S.S.)

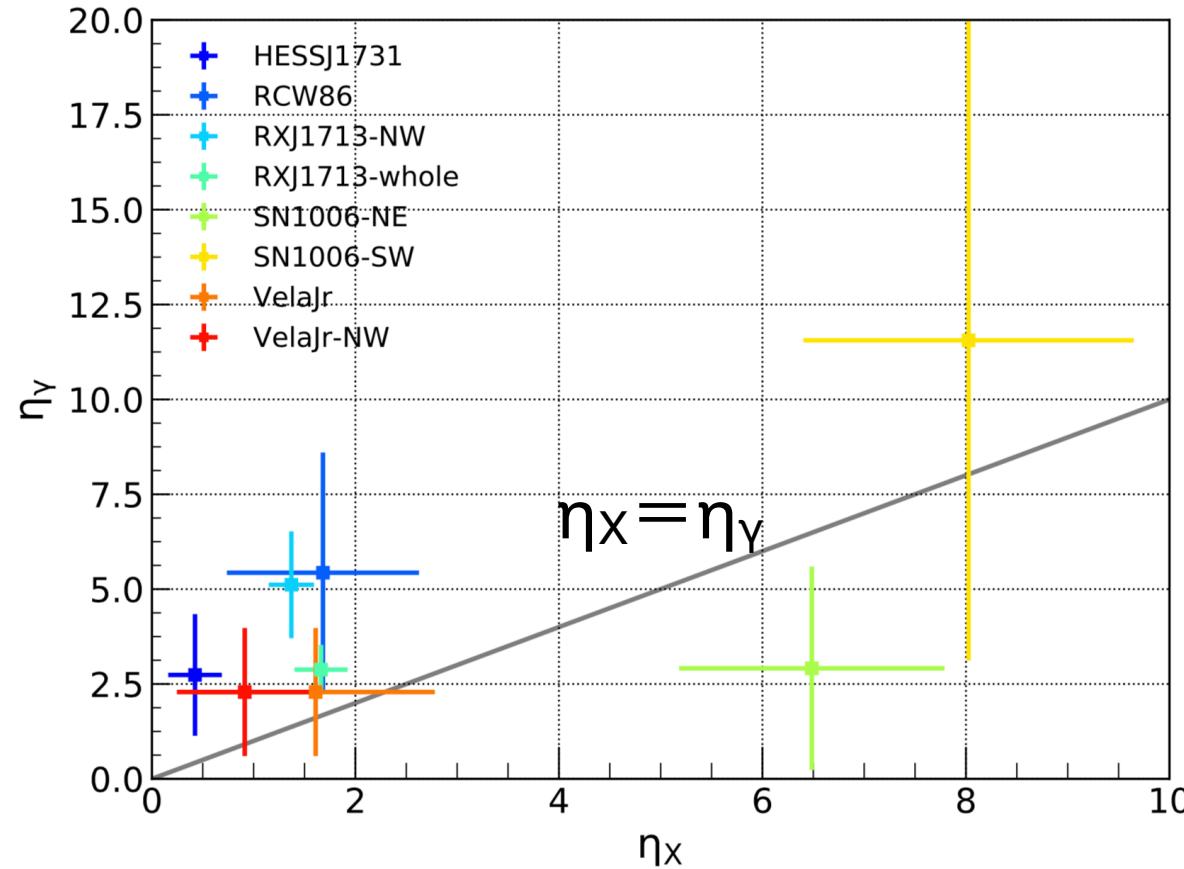
Cutoff energy (electron): 26 TeV

Shock speed: ~3000 km/s (Yamaguchi+ 16)

B-field: ~10 uG (Ajello+ 16)

→Bohm factor:  $\eta \sim 8$

# Bohm factor: X-ray and $\gamma$ -ray observations



- $\eta$  can also be estimated from gamma-ray spectra
- Issues: different regions for X-ray and gamma-ray spectra and/or assumption of leptonic origin
- More constrained with spatially resolved gamma-ray observations (Cherenkov Telescope Array; CTA)

# Summary

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- Particle acceleration in SNRs can be characterised by cutoff, shock speed, acceleration efficiency ( $\eta$ ; Bohm factor), etc.

## ❖ X-ray observations

- Systematic analysis of 11 young SNRs
  - Measurement of cutoff energy
  - Various types of cutoff-V<sub>shock</sub> relation
  - The more efficient acceleration for the older SNR

## ❖ Gamma-ray observations

- Measurement of cutoff energy
- Prospect for CTA