## Supersymmetric Dark Matter or Not

1) With CMSSM-like models pushed to high mass scales, can we still guarantee Supersymmetry's discovery at the LHC. Viable dark matter models in the CMSSM tend to lie in strips (co-anninilation funhel focus point), how far up in energy do these strips extend?
2) Non-Supersymmetric $S O(10)$-gauge coupling unification; neutrino masses, AND DARK MATTER.

# $\Delta \chi^{2}$ map of $\mathrm{m}_{0}-\mathrm{m}_{1 / 2}$ plane 

Mastercode


- CMSSM

Buchmueller, Cavanaugh, De Roeck, Ellis, Flacher, Heinemeyer Isidori, Olive, Ronga, Weiglein

## Elastic scaterring cross-section

Mastercode


- CMSSM

Buchmueller, Cavanaugh, De Roeck, Ellis, Flacher, Heinemeyer Isidori, Olive, Ronga, Weiglein

## $\mathrm{m}_{1 / 2}$ - mo planes incl. LHC




## $\Delta x^{2}$ nap of $m_{0}-m_{1 / 2}$ plane

Mastercode
2015

## Low mass

 spectrum still observable at LHC$14 \mathrm{TeV} 3000 \mathrm{fb}^{-1}$
$\begin{array}{rlllllllll}500 & & & & & & & & & \\ 0 & 1000 & 2000 & 3000 & 4000 & 5000 & 6000\end{array}$ $m_{0}[\mathrm{GeV}]$

stau coann.
A/H funnel
hybrid
$\tilde{\chi}_{1}^{ \pm}$coann.
stop coann. focus point
h funnel
Z funnel

## Elastic scaterring cross-section



## The Strips:

* Stau-coannhilation Strip
$\because$ extends only out to 11 ieV


## Siau stirip (end poinis)




## The Strips:

* Stau-coannhilation Strip
- extends only out to 11 TeV
- Stop-coannihilation Strip


## Sitop strip




Buchmueller, Citron, Ellis, Guha, Marrouche, Olive, de Vries, Zheng

## Stop strip




$$
A=3 m_{0}, \Omega_{\chi} h^{2}=0.12, \tan \beta=20
$$

## The Strips:

* Stau-coannhilation Strip
" extends only out to 11 TeV
- Stop-coanninilation Strip
$\checkmark$ Funnel
- associated with high tan $\beta$, problems with $B \rightarrow \mu \mu$
$\checkmark$ Focus Point


## Focus Poinit




Buchmueller, Citron, Ellis, Guha, Marrouche, Olive, de Vries, Zheng

## Direct detiectabillity






## The Strips:

* Stau-coannhilation Strip
" extends only out to 11 TeV
- Stop-coannihilation Strip
$\omega$ Funnel
- associated with high tan $\beta$, problems with $B \rightarrow \mu \mu$
- Focus Point
- Gluino-coanninilation Strip


## Gluilno Surips $\left(M_{3} \neq \mathbb{M}_{1}=\mathbb{M}_{2} @ \operatorname{Mg}\right.$ @ur $)$



## Gluilno Stirips $\left(M_{3} \neq \mathbb{M}_{1}=\mathbb{M}_{2} @(\mathbb{M}\right.$ Gurv $)$




May require more general models which are concordant with LHC MET; Higgs; and $B_{s} \rightarrow \mu H$, and Dark Matter

## Other Possibilities



- uand/orma mree
- subGUTmodels:Mn MaU
- with or without mSUGRA


## Why Supersymmetry (stil))?

* Gauge Coupling Unification
* Gauge Hierarchy Problem
- Stabilization of the Electroweak Vacuin
- Radiative Electroweak Symmetry Breaking
- Dark Matter
-Improvement to low energy phenomenology?
but, mh $\sim 126 \mathrm{GeV}$, and no SUSY?


## So(10) GUT?

* Gauge Coupling Unification
$\because$ Stabilization of the Electroweak Vacuum?
- Dark Matter
- Improvement to low energy phenomenology?

Neutrino masses....

## Recipe for constructing an SO(10) DM model

## 0. Get a copy of Slansky's review (Phys Rep 79 (1981) 1) (or something equivalent)

$16 \times 10=16+144$
$16 \times 16=10_{5}+120_{3}+126_{3}$
$16 \times 16=1+45+210$
$45 \times 10=10+120+320$
$45 \times 16=16+1144+5560$
$45 \times 45=1_{\mathrm{s}}+45_{\mathrm{a}}+54_{\mathrm{s}}+210_{\mathrm{s}}+770_{\mathrm{s}}+9945_{\mathrm{s}}$
$54 \times 10=10+210^{\prime}+32$
$54 \times 16=144+720$
$54 \times 45=45+54+945+1386$
$\begin{aligned} 54 \times 54 & =1_{s}+45_{\mathrm{s}}+54_{\mathrm{s}}+660_{\mathrm{s}}+770_{\mathrm{s}}+1386_{s} \\ 120 \times 10 & =45+210+945\end{aligned}$
$120 \times 10=45+210+9945$
$120 \times \overline{16}=16+144+560+1 \frac{1200}{126}+320+1728+2970$
$120 \times 45=10+120+126+\overline{126}+320+1728+2970$
$120 \times 54=120+320+1728+4312$
$120 \times 120=1_{s}+45_{\mathrm{a}}+54 \mathrm{~s}+210_{\mathrm{s}}+210_{\mathrm{a}}+770_{\mathrm{s}}+945_{\mathrm{a}}+1050_{\mathrm{s}}+\overline{1050_{\mathrm{s}}}+4125_{\mathrm{s}}+5940_{\mathrm{s}}$
$126 \times 10=210+1050$
$\overline{126} \times \overline{16}=144+672+1200$
$126 \times \overline{16}=16+560+14440$
$126 \times 45=120+126+1728+3696$
$126 \times 54=\overline{126}+1728+4950$
$126 \times 120=45+210+945+1050+5940+6930$
$126 \times 126=54_{\mathrm{s}}+945_{\mathrm{s}}+1050_{\mathrm{s}}+2772_{\mathrm{s}}+4125_{\mathrm{s}}+6930_{\mathrm{s}}$
$126 \times 126=54_{\mathrm{s}}+94 \mathrm{~s}_{\mathrm{a}}+1055_{\mathrm{s}}+272_{\mathrm{s}}+412 \mathrm{~s}_{\mathrm{s}}$
126
$\frac{120}{144} \times 10=16+1144+560+720$
$\frac{144}{144} \times 16=45+54+210+945+1050$
$144 \times \frac{16}{144} \times \frac{16}{16}=10+54+2120+995+1050$
$=120+126+320+1728$
$144 \times 16=10+120+126+320+128$
$144 \times 45=16+144_{1}+144_{2}+560+720+1200+3696$
$144 \times 45=16+144_{1}+144_{2}+560+720+1200$
$144 \times 54=16+144+560+720+2640+3696^{\prime}$
$\frac{144 \times 54}{144 \times 120}=16+144+144_{1}+144_{2}+560_{1}+560_{2}+720+1200+1440+3696^{\prime}+8800$
$\overline{144} \times \underline{126}=144+560+720+1200+1440+5280+8800$
$\overline{144} \times \overline{126}=16+144+560+1200+1440+3696^{\prime}+11088$
$144 \times 144=10_{\mathrm{s}}+120_{\mathrm{a} 1}+120_{\mathrm{a} 2}+126_{\mathrm{s}}+\overline{126_{\mathrm{s}}}+210_{\mathrm{s}}^{\prime}+320_{\mathrm{s}}+320_{\mathrm{a}}+1728_{\mathrm{s}}+1728_{\mathrm{a}}+2970_{\mathrm{s}}+3696_{\mathrm{a}}+4312_{\mathrm{a}}+4950$
$144 \times 144=1+45_{1}+45_{2}+54+210_{1}+210_{2}+770+945_{1}+945_{2}+1050+\overline{1050}+1386+5940+8085$
$210 \times 10=120+126+126+1728$
$210 \times 16=16+144+560+1200+1440$
$210 \times 45=45+210_{1}+210_{2}+945+1050+\overline{1050}+5940$
$210 \times 54=210+945+\overline{1050}+1050+8085$
$210 \times 120=10+120_{1}+120_{2}+126+\overline{126}+320+1728_{1}+1728_{2}+2970+3696+\overline{3696}+10560$
$210 \times 126=10+120+126+320+1728+2970+3696+6930^{\prime}+10560$
$210 \times 144=16+144_{1}+144_{2}+560_{1}+560_{2}+672+720+1200_{1}+1200_{2}+1440+3696^{\prime}+8800+11088$

GROUP THEORY FOR UNIFIED MODEL BUILDING

Georgi, Nanopoulos; Vayonakis; Masiero; Shafi, Sondermann, Wetterich; del Aguila, Ibanez;
Mohapatra, Senjanovic; Mambrini, Nagata, Olive, Quevillon, Zheng; Nagata, Olive, Zheng

## Recipe for constructing an SO(10) DM model

0. Get a copy of Slansky's review (Phys Rep 79 (1981) 1) (or something equivalent)
1. Pick an Intermediate Scale Gauge Group
$R_{1}$

$$
\mathrm{SO}(10) \longrightarrow G_{\mathrm{int}}
$$

| $G_{\text {int }}$ | $R_{1}$ |
| :--- | :--- |
| $\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}$ | $\mathbf{2 1 0}$ |
| $\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \otimes D$ | $\mathbf{5 4}$ |
| $\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{U}(1)_{R}$ | $\mathbf{4 5}$ |
| $\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \otimes \mathrm{U}(1)_{B-L}$ | $\mathbf{4 5}$ |
| $\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \otimes \mathrm{U}(1)_{B-L} \otimes D$ | $\mathbf{2 1 0}$ |
| $\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{U}(1)_{R} \otimes \mathrm{U}(1)_{B-L}$ | $\mathbf{4 5 , 2 1 0}$ |
| $\mathrm{SU}(5) \otimes \mathrm{U}(1)$ | $\mathbf{4 5}, \mathbf{2 1 0}$ |
| Flipped $\mathrm{SU}(5) \otimes \mathrm{U}(1)$ | $\mathbf{4 5}, \mathbf{2 1 0}$ |

## Recipe for constructing an SO(10) DM model

0. Get a copy of Slansky's review (Phys Rep 79 (1981) 1) (or something equivalent)
1. Pick an Intermediate Scale Gauge Group
2. Use 126 to break $\mathrm{G}_{\text {int }}$ to SM

$$
\mathrm{SO}(10) \xrightarrow{\mathrm{R}_{1}} G_{\mathrm{int}} \xrightarrow{\mathrm{R}_{2}} G_{\mathrm{SM}} \otimes \mathbb{Z}_{2}
$$

$$
R_{2}=126+\ldots
$$

Neutrino see-saw: Majorana mass for $V_{\mathrm{R}}$ from $1616126 \rightarrow \mathrm{~m}_{\mathrm{vR}} \sim \mathrm{M}_{\text {int }}$

## Recipe for constructing an SO(10) DM model

0. Get a copy of Slansky's review (Phys Rep 79 (1981) 1) (or something equivalent)
1. Pick an Intermediate Scale Gauge Group
2. Use 126 to break $\mathrm{G}_{\text {int }}$ to SM
3. Pick DM representation and insure proper splitting within the multiplet, and pick low energy field content

## Remnant $Z_{2}$ symmetry

Fermions from 10,45, $54,120,126$, or 210 representations;

Scalars from 16, 144

Kadastik, Kannike, Raidal;
Frigerio, Hambye;
Mambrini, Nagata,
Olive, Quevillon, Zheng;
Nagata, Olive, Zheng

| Model | $B-L$ | $\mathrm{SU}(2)_{L}$ | $Y$ | $\mathrm{SO}(10)$ representations |
| :--- | :---: | :---: | :--- | :--- |
| $\mathrm{F}_{\mathbf{1}}^{0}$ |  | $\mathbf{1}$ | 0 | $\mathbf{4 5}, \mathbf{5 4}, \mathbf{2 1 0}$ |
| $\mathrm{~F}_{2}^{1 / 2}$ |  | $\mathbf{2}$ | $1 / 2$ | $\mathbf{1 0}, \mathbf{1 2 0}, \mathbf{1 2 6}, \mathbf{2 1 0}^{\prime}$ |
| $\mathrm{F}_{\mathbf{3}}^{0}$ |  | $\mathbf{3}$ | 0 | $\mathbf{4 5}, \mathbf{5 4}, \mathbf{2 1 0}$ |
| $\mathrm{~F}_{\mathbf{3}}^{1}$ | 0 | $\mathbf{3}$ | 1 | $\mathbf{5 4}$ |
| $\mathrm{~F}_{4}^{1 / 2}$ |  | $\mathbf{4}$ | $1 / 2$ | $\mathbf{2 1 0}$ |
| $\mathrm{~F}_{\mathbf{4}}^{3 / 2}$ |  | $\mathbf{4}$ | $3 / 2$ | $\mathbf{2 1 0} 0^{\prime}$ |
| $\mathrm{S}_{1}^{0}$ |  | $\mathbf{1}$ | 0 | $\mathbf{1 6}, \mathbf{1 4 4}$ |
| $\mathrm{~S}_{2}^{1 / 2}$ |  | $\mathbf{2}$ | $1 / 2$ | $\mathbf{1 6}, \mathbf{1 4 4}$ |
| $\mathrm{~S}_{\mathbf{3}}^{0}$ | 1 | $\mathbf{3}$ | 0 | $\mathbf{1 4 4}$ |
| $\mathrm{~S}_{\mathbf{3}}^{1}$ |  | $\mathbf{3}$ | 1 | $\mathbf{1 4 4}$ |
| $\widehat{\mathrm{~F}}_{\mathbf{1}}^{0}$ |  | $\mathbf{1}$ | 0 | $\mathbf{1 2 6}$ |
| $\widehat{\mathrm{~F}}_{2}^{1 / 2}$ | 2 | $\mathbf{2}$ | $1 / 2$ | $\mathbf{2 1 0}$ |
| $\widehat{\mathrm{~F}}_{\mathbf{3}}^{1}$ |  | $\mathbf{3}$ | 1 | $\mathbf{1 2 6}$ |

## Recipe for constructing an SO(10) DM model

0. Get a copy of Slansky's review (Phys Rep 79 (1981) 1) (or something equivalent)
1. Pick an Intermediate Scale Gauge Group
2. Use 126 to break $\mathrm{G}_{\text {int }}$ to SM
3. Pick DM representation and insure proper splitting within the multiplet, and pick low energy field content
4. Use RGEs to obtain Gauge Coupling Unification

## Recipe for constructing an SO(10) DM model

## 4. Use RGEs to obtain Gauge Coupling Unification

Fixes Mgut, $M_{\text {int }}$, agut


## Examples:

## Scalars

| Model | $R_{\text {DM }}$ | $\mathrm{S}_{\mathrm{n}}^{\mathrm{Y}}$ | $\mathrm{SO}(10)$ representation |
| :---: | :---: | :---: | :---: |
| $G_{\mathrm{int}}=\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}(\otimes D)$ |  |  |  |
| $\mathrm{SA}_{422 \text { (D) }}$ | 4, 1, 2 | $\mathrm{S}_{1}^{0}$ | 16, 144 |
| $\mathrm{SB}_{422 \text { (D) }}$ | 4, 2, 1 | $\mathrm{S}_{2}^{1 / 2}$ | 16, 144 |
| $\mathrm{SC}_{422 \text { (D) }}$ | 4, 2, 3 | $\mathrm{S}_{2}^{1 / 2}$ | 144 |
| $\mathrm{SD}_{422 \text { (D) }}$ | 4, 3, 2 | $\mathrm{S}_{3}^{1}$ | 144 |
| $\mathrm{SE}_{422 \text { (D) }}$ | 4, 3, 2 | $\mathrm{S}_{3}^{0}$ | 144 |
| $G_{\text {int }}=\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{U}(1)_{R}$ |  |  |  |
| $\mathrm{SA}_{421}$ | 4, 1, -1/2 | $\mathrm{S}_{1}^{0}$ | 16, 144 |
| $\mathrm{SB}_{421}$ | 4, 2, 0 | $\mathrm{S}_{2}^{1 / 2}$ | 16, 144 |
| $\mathrm{SC}_{421}$ | 4, 2, 1 | $\mathrm{S}_{2}^{1 / 2}$ | 144 |
| $\mathrm{SD}_{421}$ | 4,3,1/2 | $\mathrm{S}_{3}^{1}$ | 144 |
| $\mathrm{SE}_{421}$ | 4, 3, -1/2 | $\mathrm{S}_{3}^{0}$ | 144 |
| $G_{\mathrm{int}}=\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \otimes \mathrm{U}(1)_{B-L}(\otimes D)$ |  |  |  |
| $\mathrm{SA}_{3221 \text { (D) }}$ | 1, 1, 2, 1 | $\mathrm{S}_{1}^{0}$ | 16, 144 |
| $\mathrm{SB}_{3221 \text { (D) }}$ | 1,2,1, -1 | $\mathrm{S}_{2}^{1 / 2}$ | 16, 144 |
| $\mathrm{SC}_{3221 \text { (D) }}$ | 1,2,3, -1 | $\mathrm{S}_{2}^{1 / 2}$ | 144 |
| $\mathrm{SD}_{3221 \text { (D) }}$ | 1, 3, 2, 1 | $\mathrm{S}_{3}^{1}$ | 144 |
| $\mathrm{SE}_{3221(\mathrm{D})}$ | 1,3,2,1 | $\mathrm{S}_{3}^{0}$ | 144 |

## Examples:

## Scalars

## Higgs portal models <br> Inert Higgs doublet models

| Model | $\log _{10} M_{\mathrm{GUT}}$ | $\log _{10} M_{\mathrm{int}}$ | $\alpha_{\mathrm{GUT}}$ | $\log _{10} \tau_{p}\left(p \rightarrow e^{+} \pi^{0}\right)$ |
| :--- | :--- | :--- | :--- | :--- |
| $G_{\mathrm{int}}=\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}$ |  |  |  |  |
| $\mathrm{SA}_{422}$ | 16.33 | 11.08 | 0.0218 | $36.8 \pm 1.2$ |
| $\mathrm{SB}_{422}$ | 15.62 | 12.38 | 0.0228 | $34.0 \pm 1.2$ |
| $G_{\text {int }}=\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \otimes \mathrm{U}(1)_{B-L}$ |  |  |  |  |
| $\mathrm{SA}_{3221}$ | 16.66 | 8.54 | 0.0217 | $38.1 \pm 1.2$ |
| $\mathrm{SB}_{3221}$ | 16.17 | 9.80 | 0.0223 | $36.2 \pm 1.2$ |
| $\mathrm{SC}_{3221}$ | 15.62 | 9.14 | 0.0230 | $34.0 \pm 1.2$ |
| $G_{\mathrm{int}}=\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \otimes \mathrm{U}(1)_{B-L} \otimes D$ |  |  |  |  |
| $\mathrm{SA}_{3221 \mathrm{D}}$ | 15.58 | 10.08 | 0.0231 | $33.8 \pm 1.2$ |
| $\mathrm{SB}_{3221 \mathrm{D}}$ | 15.40 | 10.44 | 0.0233 | $33.1 \pm 1.2$ |

other models have MGut too low
mass splitting:

$$
\begin{aligned}
-\mathcal{L}_{\mathrm{int}} & =M^{2}\left|R_{\mathrm{DM}}\right|^{2}+\kappa_{1} R_{\mathrm{DM}}^{*} R_{\mathrm{DM}} R_{1}+\left\{\kappa_{2} R_{\mathrm{DM}} R_{\mathrm{DM}} R_{2}^{*}+\text { h.c. }\right\} \\
& +\lambda_{1}^{1}\left|R_{\mathrm{DM}}\right|^{2}\left|R_{1}\right|^{2}+\lambda_{2}^{1}\left|R_{\mathrm{DM}}\right|^{2}\left|R_{2}\right|^{2}+\left\{\lambda_{12}^{126}\left(R_{\mathrm{DM}} R_{\mathrm{DM}}\right)_{\mathbf{1 2 6}}\left(R_{1} R_{2}^{*}\right)_{\overline{\mathbf{1 2 6}}}+\text { h.c. }\right\} \\
& +\lambda_{1}^{\mathbf{4 5}}\left(R_{\mathrm{DM}}^{*} R_{\mathrm{DM}}\right)_{\mathbf{4 5}}\left(R_{1}^{*} R_{1}\right)_{\mathbf{4 5}}+\lambda_{1}^{210}\left(R_{\mathrm{DM}}^{*} R_{\mathrm{DM}}\right)_{\mathbf{2 1 0}}\left(R_{1}^{*} R_{1}\right)_{\mathbf{2 1 0}} \\
& +\lambda_{2}^{45}\left(R_{\mathrm{DM}}^{*} R_{\mathrm{DM}}\right)_{\mathbf{4 5}}\left(R_{2}^{*} R_{2}\right)_{\mathbf{4 5}}+\lambda_{2}^{\mathbf{2 1 0}}\left(R_{\mathrm{DM}}^{*} R_{\mathrm{DM}}\right)_{\mathbf{2 1 0}}\left(R_{2}^{*} R_{2}\right)_{\mathbf{2 1 0}},
\end{aligned}
$$

## Examples:

# SM Fermion Singlets: Produced thermally out of equilibrium $\Rightarrow$ Fermionic candidates (NETDM) 

Mambrini, Olive, Quevillon, Zaldivar

To aid in gauge coupling unification, DM should be a SM singlet but a non-singlet under the Intermediate gauge group. Requires splitting multiplets

| $G_{\text {int }}$ | $R_{\mathrm{DM}}$ | $\mathrm{SO}(10)$ |
| :--- | :--- | :--- |
| $\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}$ | $(\mathbf{1}, \mathbf{1}, \mathbf{3})$ | $\mathbf{4 5}$ |
|  | $(\mathbf{1 5}, \mathbf{1}, \mathbf{1})$ | $45, \mathbf{2 1 0}$ |
|  | $(\mathbf{1 0}, \mathbf{1}, \mathbf{3})$ | $\mathbf{1 2 6}$ |
|  | $(\mathbf{1 5}, \mathbf{1}, \mathbf{3})$ | $\mathbf{2 1 0}$ |
| $\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{U}(1)_{R}$ | $(\mathbf{1 5}, \mathbf{1}, 0)$ | $\mathbf{4 5}, \mathbf{2 1 0}$ |
|  | $(\mathbf{1 0}, \mathbf{1}, 1)$ | $\mathbf{1 2 6}$ |
| $\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \otimes \mathrm{U}(1)_{B-L}$ | $(\mathbf{1}, \mathbf{1}, \mathbf{3}, 0)$ | $45, \mathbf{2 1 0}$ |
|  | $(\mathbf{1}, \mathbf{1}, \mathbf{3},-2)$ | $\mathbf{1 2 6}$ |
| $\mathrm{SU}(3)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{U}(1)_{R} \otimes \mathrm{U}(1)_{B-L}$ | $(\mathbf{1}, \mathbf{1}, 1,-2)$ | $\mathbf{1 2 6}$ |

## Gauge Coupling Unification

## Also fix particle content below Mgut

$\left.\begin{array}{llccc}\hline \hline \mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R} \\ \hline R_{\mathrm{DM}} & R_{2} & \log _{10}\left(M_{\mathrm{int}}\right) & \log _{10}\left(M_{\mathrm{GUT}}\right) & g_{\mathrm{GUT}} \\ \hline(\mathbf{1}, \mathbf{1}, \mathbf{3})_{W} & (\mathbf{1 0}, \mathbf{1}, \mathbf{3})_{C} \\ (\mathbf{1}, \mathbf{1}, \mathbf{3})_{R}\end{array}\right)$


## Examples:

## SM Fermion Singlets: Produced thermally out of equilibrium $\Rightarrow$ Fermionic candidates (NETDM)

## For mass splittings:

$$
\begin{aligned}
& \mathcal{L}_{\text {int }}=-\frac{M_{45_{W}}}{2} \mathbf{4 5} 45_{W}-\frac{y_{54}}{2} 45_{W} 45_{W} 54_{R}-\frac{y_{210}}{2} 45_{W} 45_{W} 210_{R}+\text { h.c. }, \\
& 15=8+3+\overline{3}+1 \\
& M_{15} \sim M_{45 W}-y_{54} V_{54} \sim M_{\text {int }} ;
\end{aligned}
$$

$$
\begin{aligned}
& (10,1,3)_{C},(10,3,1)_{C} \in \mathbf{1 2 6 ;} ;(15,1,1)_{R} \in 210
\end{aligned}
$$

## Examples:

Non-Singlets: Fermions

|  |  |  |  |  |
| :--- | :---: | :---: | :--- | :--- |
|  |  |  |  |  |
| Model | $B-L$ | $\mathrm{SU}(2)_{L}$ | $Y$ | $\mathrm{SO}(10)$ representations |
| $\mathrm{F}_{1}^{0}$ |  | $\mathbf{1}$ | 0 | $\mathbf{4 5}, \mathbf{5 4}, \mathbf{2 1 0}$ |
| $\mathrm{~F}_{2}^{1 / 2}$ |  | $\mathbf{2}$ | $1 / 2$ | $\mathbf{1 0}, \mathbf{1 2 0}, \mathbf{1 2 6}, \mathbf{2 1 0}$ |
| $\mathrm{~F}_{3}^{0}$ |  | $\mathbf{3}$ | 0 | $\mathbf{4 5}, \mathbf{5 4}, \mathbf{2 1 0}$ |
| $\mathrm{~F}_{3}^{1}$ | 0 | $\mathbf{3}$ | 1 | 54 |
| $\mathrm{~F}_{4}^{1 / 2}$ |  | 4 | $1 / 2$ | $\mathbf{2 1 0}$ |
| $\mathrm{~F}_{4}^{3 / 2}$ |  | $\mathbf{4}$ | $3 / 2$ | $\mathbf{2 1 0}$ |


| $\mathrm{SO}(10)$ representation |  | $\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}$ |  |
| :---: | :---: | :---: | :---: |
| 45 |  | $(1,3,1)$ |  |
| 54 |  | iplets (Wino) $\quad(1,3,3)$ |  |
| 210 |  | $(15,3,1)$ |  |
| $\mathrm{SO}(10)$ representation | SU | (4) ${ }_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}$ | $B-L$ |
| 10, 120, 210 |  | (1,2) | 0 |
| 120, 126 |  | $(15,2,2)$ | 0 |
| $210 \quad \begin{aligned} & \text { SM Doublets } \\ & \text { (Higgsino) }\end{aligned}$ |  | $(\mathbf{0}, \mathbf{2}, \mathbf{2}) \oplus(\overline{\mathbf{1 0}}, \mathbf{2}, \mathbf{2})$ | $\pm 2$ |
| $210^{\prime}$ |  | (1,4,4) | 0 |
| 54, 210 |  | (1,1) | 0 |
| 45 <br> SM Singlets <br> for mixing |  | 1,3) | 0 |
| 45, 210 (Bino) |  | $(5,1,1)$ | 0 |
| 210 |  | ( 5, 1, 3) | 0 |
| 126 |  | (0, 1, 3) | 2 |

## Examples:

## Non-Singlets: Fermions

| $R_{\text {DM }}$ | Additio in | nal Higgs $R_{1}$ | $\log _{10} M_{\mathrm{int}}$ | $\log _{10} M_{\mathrm{GUT}}$ | $\alpha_{\text {GUT }}$ | $\log _{10} \tau_{p}$ | $\left.\rightarrow e^{+} \pi^{0}\right)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $G_{\text {int }}=\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}$ |  |  |  |  |  |  |  |
| $(15,1,3)$ |  |  |  |  |  |  |  |
| Model | $R_{\text {DM }}$ | $R_{\text {DM }}^{\prime}$ | Higgs | $\log _{10} M_{\text {int }}$ | $\log _{10} M_{\mathrm{GUT}}$ | $\alpha_{\text {GUT }}$ | $\log _{10} \tau_{p}$ |
| $G_{\text {int }}=\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{U}(1)_{R}$ |  |  |  |  |  |  |  |
| $\mathrm{FA}_{421}$ | $(\mathbf{1 , 2 , 1 / 2})_{D}$ | $(15,1,0)_{W}$ | $\begin{aligned} & (15,1,0)_{R} \\ & (15,2,1 / 2)_{C} \end{aligned}$ | $3.48$ |  | 0.0320 | $40.9 \pm 1.2$ |
| $G_{\text {int }}=\mathrm{SU}(4)_{C} \otimes \mathrm{SU}(2)_{L} \otimes \mathrm{SU}(2)_{R}$ |  |  |  |  |  |  |  |
| $\mathrm{FA}_{422}$ | $(1,2,2)_{W}$ | $(\mathbf{1}, \mathbf{3}, \mathbf{1})_{W}$ | $\begin{aligned} & (\mathbf{1 5}, \mathbf{1}, \mathbf{1})_{R} \\ & (\mathbf{1 5}, \mathbf{1}, \mathbf{3})_{R} \end{aligned}$ | 9.00 | 15.68 | 0.0258 | $34.0 \pm 1.2$ |
| $\mathrm{FB}_{422}$ | $(1,2,2)_{W}$ | $(\mathbf{1}, \mathbf{3}, \mathbf{1})_{W}$ | $\begin{aligned} & (\mathbf{1 5}, 1,1)_{R} \\ & (\mathbf{1 5}, 2,2)_{C} \\ & (\mathbf{1 5}, \mathbf{1}, \mathbf{3})_{R} \end{aligned}$ | $5.84$ | $17.01$ | 0.0587 | $38.0 \pm 1.2$ |

## Examples:

## Non-Singlets: Fermions

## Summary Plot



## Summary

* LHC susy and Higgs searches have pushed CMSSM位e models to "corners"

4 Though some phenomenological solutions are stil vable typically along strios in parameter space

- NUH models withow histil promising as are subGUT models PGM (with wino DM or Higgsino DM)
- Several possibilities in non-SUSY SO(10) models
- Challenge lies in detection strategies

