# The Gong Show

The preview show by the 40 poster presenters



YKIS-2016

# Instantons and Entanglement Entropy

Arpan Bhattacharyya and Ling-Yan Hung Department of Physics and Center for Field Theory and Particle Physics, Fudan University

based on work with Charles -Melby Thomson and P.C.H Lau, Arxiv:- 1606.xxxxx

# Decay of False Vacuum and Entanglement Entropy



# Decay of False Vacuum in spin Chain and Growth of Entanglement Entropy

Transverse Ising Model:

$$\begin{split} H &= -J\sum_{i}\sigma_{i}^{z}\sigma_{i+1}^{z} + h\Sigma_{i}\sigma_{i}^{x} + b\sum_{i}\sigma_{i}^{z}\\ \text{Study the time evolution of the wave function which appears}\\ \text{like false vacuum}\\ |\Psi(t) > = e^{iHT}|0> \end{split}$$

|0> +1 eigenstate of  $\sigma_z$ 

We find the growth of entropy is bounded by the area law

Satisfy Lieb-Robinson Bound

# Gauge Theory

Generic gauge groups the background pure gauge configuration can be classified by different topological sectors.

These backgrounds cannot be related by small gauge transformation. True vacuum is the sum of all these. A Vacuum.

Instanton tunnels between these pure Gauge backgrounds



# Modelling *θ*-Vacuum

One more classic example is 1+1 dimensional Schwinger model:

$$S_{schwinger} = \int d^2x \, \bar{\psi} \gamma^{\mu} (i\partial_{\mu} - e \, A_{\mu}) \psi - \frac{1}{4} F^{\mu\nu} F_{\mu\nu}$$
  
Vacuum (in temporal Gauge) :

θ

$$\begin{aligned} |\theta \rangle &= \sum_{N} \exp^{iN\theta} f_0(N,\lambda) \prod_{n>0} exp^{-t_n(\tilde{j}_{\pm n}^{\dagger} \tilde{j}_{\pm n}^{\dagger} - \tilde{j}_{-n} \tilde{j}_{-n})} |N \rangle \\ \tilde{j}_{n,\pm} &= \cosh \gamma_n j_{n,\pm} + \sinh \gamma_n j_{n,\pm}^{\dagger}, j_{\pm} = \bar{\psi} \gamma_{\pm} \psi \end{aligned}$$
Bogoliubov transformation

Too complicated, we will consider a toy model where we just focus on the (weighted) sum of the Fermi-surfaces.

$$|\Psi\rangle = \sum_{N=1}^{L} f(N,\lambda) \prod_{k_i}^{N} c_{k_i}^{\dagger} |0\rangle$$
$$c_{k_1} = \frac{1}{\sqrt{L}} \sum_{j} c_j e^{-ik_i x_j}, c_j = (\prod_{i < j} \sigma_i^z) \sigma_j^{+}$$

Entanglement entropy for this case cannot scale as "Volume".



#### **Entanglement Entropy and Conformal Interfaces**

Enrico Brehm, Ilka Brunner, Daniel Jaud, Cornelius Schmidt-Colinet

Arnold Sommerfeld Center, Ludwig Maximilian Universität München

June 15th 2016



E. Brehm Entanglement Entropy and Conformal Interfaces

Measure of choice: Entanglement Entropy

$$S_A = -\operatorname{Tr} \rho_A \log \rho_A = - \frac{\partial}{\partial n} \operatorname{Tr} \rho_A^n$$

Method:



Result:

$$S_I = \sigma_I \frac{c}{3} \log L + s(I) \, .$$



# Equivalence of Emergent de Sitter Spaces from Conformal Field Theory

Claire Zukowski C. T. Asplund, N. Callebaut, CZ [1604.02687]

Two proposals for a dS space emergent from entanglement entropy:

### 1) <u>Kinematic Space</u>





 $\begin{array}{l} (b) \\ \mathrm{KS} = & \mathrm{Space} \ \mathrm{of} \ \mathrm{boundary} \\ \mathrm{intervals} \ \mathrm{in} \ \mathrm{CFT}_2 \ /\mathrm{spacelike} \\ \mathrm{Ryu-Takayanagi} \ \mathrm{geodesics} \ \mathrm{on} \\ \mathrm{a} \ \mathrm{bulk} \ \mathrm{slice}_{\mathrm{threlike}} & \mathrm{dS}_3 \\ \mathrm{null} \end{array}$ 

$$ds^2 = \frac{\partial^2 S(u,v)}{\partial u \partial v} du dv$$

 $\Rightarrow$  Global dS<sub>2acelike</sub>

Czech, Lamprou, McCandlish, Sully (2015a)

### 2) <u>Auxiliary de Sitter Proposal</u>

Modular Hamiltonian for ball-shaped regions for  $CFT_d$  in vacuum:

$$H_{\rm mod} = 2\pi \int_B \mathcal{P}T_{00}$$

 $\mathcal{P} = \text{boundary-to-bulk } dS_d$ propagator

 $\Rightarrow \delta S = \langle H_{\rm mod} \rangle \text{ satisfies a dS}$  Klein-Gordon equation

de Boer, Heller, Myers, Neiman (2015)

### Our Results

**<u>Goal</u>**: Provide support for the equivalence of these emergent spacetimes in the vacuum case and beyond



### <u>Our Results</u>:

• <u>Thermal Case</u>: KS for BTZ black string is the hyperbolic patch of  $dS_2$ . Perturbations of EE satisfy a wave equation on KS.

• <u>Quotient Spaces</u>: For e.g. BTZ black hole/conical singularity, phase transitions in EE introduce defects in KS.

• <u>Causal Structure</u>: KS of locally  $AdS_3$  spaces is generically globally hyperbolic.

Equivalence  $\Leftrightarrow$  Modular Hamiltonian from EE?

Kinematic space K (1.0) = space of CFT<sub>2</sub> intervals / AdS<sub>3</sub> geodesics [Czech, Lamprou, McCandlish, Sully JHEP 1510 (2015) 175]



K = auxiliary de Sitter of [de Boer, Heller, Myers, Neiman Phys.Rev.Lett. 116 (2016) no.6, 061602]

EE perturbations propagate on K

K of quotiented geometries raises questions on propagating fields on K

> [Asplund, NC, Zukowski 1604.02687]

Kinematic space K (1.0) = space of CFT<sub>2</sub> intervals / AdS<sub>3</sub> geodesics [Czech, Lamprou, McCandlish, Sully JHEP 1510 (2015) 175]



K = auxiliary dS for any locally AdS<sub>3</sub> geometry, by recognizing K as Liouville metric with the EE the Liouville field

[NC, Verlinde - in preparation]



### Emergent Geometry from Redundancy-Constrained States and Bulk Entanglement Gravity

ChunJun Cao and Sean Carroll, *California Institute of Technology* Prepared for YKIS 2016





#### Entanglement Entropy in a Holographic Kondo Model

#### Mario Flory

Max-Planck-Institut für Physik





#### Quantum Matter, Spacetime and Information YITP, 15.06.2016 Based on 1410.7811 and 1511.03666

MARIO	FLORY
Minuo	T DOIG

YKIS 2016

#### Entanglement entropy in the Kondo effect



MARIO FLORY

2/2



### A holographic dual to the Bose-Hubbard Model

- □ Bose-Hubbard model as the effective theory on an optical lattice, including the hopping term + Short-range repulsive interactions U
  - $\diamond$  The extension to the *SU(N)* Bose–Hubbard model

Conjecture of MF-Harrison-Karch-Meyer-Paquette, JHEP04(2015)068



$$H = -w \sum_{\langle ij \rangle} (b_{ai}^{\dagger} b_{aj} + b_{aj}^{\dagger} b_{ai})$$

$$-\mu \sum_{j} n_{j} + \frac{U}{2} \sum_{j} n_{j} (n_{j} - 1), n_{i} = b_{ai}^{\dagger} b_{ai}$$

To compute the VEV of the hopping term in both sides of the duality concretely and compare them, Work in progress of MF-Meyer-Sumiran-Tezuka





### Main results and comparision



□ (c): Comparision of  $dF/dt_{hop}$ : the result of  $SU(N_c)$  Bose–Hubbard model fits the result of the gravity dual at small hopping well (Dashed lines are the field theory result)





## Fractional quantum Hall states of dipolar fermions in a strained optical lattice Hiroyuki Fujita, ISSP. Univ. Tokyo

Aim: Quantum simulation of strongly entangled phase of matter



Synthetic magnetic field

in a strained honeycomb optical lattice



Fermionic dipolar molecule e.g. NaRb



Realization of FQHE states in ultra-cold gases?

# Method: Exact diag. in a spherical geometry in lowest LL Result:

#### Various valley-polarized FQHE states found



$\widetilde{\nu}$	$N = \widetilde{\nu}(N_{\rm orb} + \delta)$	p	n
1/3	$N = \frac{1}{3}(N_{\rm orb} + 2)$	1	1
2/5	$N = \frac{2}{5}(N_{\rm orb} + 3)$	1	2
1/5	$N = \frac{1}{5}(N_{\rm orb} + 4)$	2	1
1/7	$N = \frac{1}{7}(N_{\rm orb} + 6)$	3	1
2/7	$N = \frac{2}{7}(N_{\rm orb} + 1)$	2	-2
2/9	$N = \frac{2}{9}(N_{\rm orb} + 5)$	2	2

$$N = \frac{n}{2np+1}(N_{\rm orb} + 2p + n - 1)$$

Energy scale estimation for 
$$\,
u=rac{1}{3}\,$$
 Laughlin state of  $\,{}^{23}\mathrm{Na}^{87}\mathrm{Rb}$ 

Discussion on its experimental realization



Shape Dependence of Holographic Rényi entropies. Damián A. Galante (UWO/PI)

Work in progress in collaboration with L. Bianchi, S. Chapman, X. Dong, M. Meineri and R. Myers

Lots of conjectures have been made recently about universal features of Rényi entropies of deformed entangling surfaces...

For 4d CFTs  $f_b(n) = f_c(n)$ 

Cone Contributions to Rényi Entropies  $\sigma_n^{(d)} \propto rac{h_n}{n-1}$ 

Displacement conjecture in general dimensions

$$C_D(n) = d\Gamma\left(\frac{d+1}{2}\right)\left(\frac{2}{\sqrt{\pi}}\right)^{d-1}h_n$$

There has been a proof around n=1 [Faulkner, Leigh, • Parrikar], but for general n...

### Shape Dependence of Holographic Rényi entropies. Damián A. Galante (UWO/PI) Work in progress in collaboration with L. Biand

Work in progress in collaboration with L. Bianchi, S. Chapman, X. Dong, M. Meineri and R. Myers

In 4d holographic CFTs  $f_b(b) \neq f_c(n)$ 



In holographic CFTs in d dimensions



What is  $C_D$ ? How to compute it in holographic theories? What is the result? How different is it from the conjecture? Come see my poster



#### Dyonic extremal Black hole entropy for $\mathcal{N} = 8$ gauged supergravity

Prieslei Goulart - IFT/UNESP - Sao Paulo, Brazil - MPI - Munich, Germany

- Motivation: obtain the black hole entropy for supergravity theories with a non-trivial dilaton potential;
- Sen's entropy function: Near horizon metric is AdS<sub>2</sub> × S<sup>2</sup>:

$$ds^{2} = v_{1} \left( -r^{2} dt^{2} + \frac{dr^{2}}{r^{2}} \right) + v_{2} (d\theta^{2} + \sin^{2} \theta d\phi^{2}), \qquad (1)$$

where the constants  $v_1$  and  $v_2$  are the  $AdS_2$  radius and the  $S^2$  radius respectively. Entropy function:

$$\mathcal{E}(\vec{u},\vec{v},\vec{e},\vec{q},\vec{p}) \equiv 2\pi [e_A q^A - \int d\theta d\phi \sqrt{-\det g} \mathcal{L}].$$
(2)

Attractor equations:

$$\frac{\partial \mathcal{E}}{\partial u_s} = 0, \quad \frac{\partial \mathcal{E}}{\partial v_1} = 0, \quad \frac{\partial \mathcal{E}}{\partial v_2} = 0, \quad \frac{\partial \mathcal{E}}{\partial e_A} = 0 , \quad (3)$$

At the extremum (3) the entropy function is the black hole entropy:

$$S_{BH} = \mathcal{E}(\vec{u}, \vec{v}, \vec{e}, \vec{q}, \vec{p}).$$
(4)

- ∢ ⊒ →

Prieslei Goulart

• We obtain the dyonic black hole entropy  $\mathcal{N} = 8$  gauged supergravity:

$$S = \int d^{4}x \sqrt{-g} \left[ R - \frac{3}{8} \left( \sum_{l=1}^{4} (\partial_{\mu}\lambda_{l})^{2} - 2\sum_{l < J} \partial_{\mu}\lambda_{l} \partial^{\mu}\lambda_{J} \right) - \frac{1}{4} \sum_{l=1}^{4} X_{l}^{2} (F_{\mu\nu}^{l})^{2} - V \right],$$
(5)
$$F_{\mu\nu}^{l} = \partial_{\mu}A_{\nu}^{l} - \partial_{\nu}A_{\mu}^{l}, \quad V(X) = -\frac{g^{2}}{4} \sum_{l < I} \frac{1}{X_{l}X_{J}}, \quad X_{1}X_{2}X_{3}X_{4} = 1.$$
(6)

► The entropy is written as

$$\mathcal{E} = 2\pi \left(\sum_{l=1}^{4} q^{l} p_{l}\right) \left[\frac{1}{2} \left(1 + \sqrt{1 - \frac{g^{2}}{2} \left(\sum_{l=1}^{4} q^{l} p_{l}\right) \left(\sum_{J < K} \sqrt{\frac{p_{J} p_{K}}{q^{J} q^{K}}}\right)}\right)\right]^{-1/2}.$$
(7)

The entropy can also be written as

$$\mathcal{E} = \frac{1}{2} \left( \sum_{l=1}^{4} q^{l} p_{l} \right) \left( \frac{q^{1} q^{2} q^{3} q^{4}}{p^{1} p^{2} p^{3} p^{4}} \right)^{1/4}.$$
 (8)

- ∢ ≣ ▶

▶ We also how the entropy changes under electric-magnetic duality.



### String theory is not even wrong?



### Not really; we will make it FALSIFIABLE!



LIGO



### Today we propose yet another approach: an experimental realization of a quantum black hole



Make them from atoms and lasers!

# Experimental Quantum Gravity with Cold Atoms



I. Danshita, M. Hanada, M. Tezuka

Let's make a black hole in your lab and see how it behaves!


Hayata, Hidaka, MH, Noumi, Phys. Rev. D 92, 065008

**MH** in preparation (2016)

# Emergent curved spacetime from locally thermalized matter



### Masaru Hongo

iTHES Research group, RIKEN

Quantum Matter, Spacetime and Information, 2016/6/15, Kyoto University,

## **Thermal Field Theory**



Gibbs distribution: 
$$\hat{\rho}_G = \frac{e^{-\beta(\hat{H}-\mu\hat{N})}}{Z} = e^{-\beta(\hat{H}-\mu\hat{N})-\Psi[\beta,\nu]}$$

## Local Thermal Field Theory



$$\Psi[\bar{t};\lambda] \equiv \log \operatorname{Tr} \exp\left[\int d\Sigma_{\bar{t}\nu} \left(\beta^{\mu}(x)\hat{T}^{\nu}_{\ \mu}(x) + \nu(x)\hat{J}^{\nu}(x)\right)\right]$$

 $\Psi[\lambda]$  is written in terms of QFT in curved spacetime  $ds^2 = -e^{2\sigma}(d\tilde{t} + a_{\bar{i}})dx^{\bar{i}} + \gamma'_{\bar{i}\bar{j}}dx^{\bar{i}}dx^{\bar{j}}$ Symmetry = Spatial diffeomorphism + Kaluza-Klein gauge

Consistent with [Banerjee et al.(2012), Jensen et al.(2012) ...]



#### Crofton's formula



$$\frac{\sigma(\gamma)}{4G} = \frac{1}{4} \int_{\gamma \cap \Gamma \neq \varnothing} N(\gamma \cap \Gamma) \ \epsilon_{\mathcal{K}}$$

The length  $\sigma(\gamma)$  of a curve  $\gamma$  can be expressed in terms of an integral over the geodesics  $\Gamma$  that have nonvanishing intersection number  $N(\gamma \cap \Gamma)$  with  $\gamma$ 

The measure  $\epsilon_{\mathcal{K}}$  is given by the second derivative of the entanglement entropy

$$\epsilon_{\mathcal{K}}(u,v) = \tfrac{\partial^2 S(u,v)}{\partial u \partial v} \mathrm{d} u \wedge \mathrm{d} v$$

Hence we can obtain the geometry from the entanglement structure of the field theory on the boundary

#### Kinematic space of geodesics in general dimensions

#### XH and Lin 2015



$$\epsilon_{\mathcal{K}} = \frac{1}{4G} \det \left[ \frac{\partial^2 S(\vec{x}_1, \vec{x}_2)}{\partial \vec{x}_1 \partial \vec{x}_2} \right] \prod_{i=1}^{d-1} \mathrm{d} x_2^i \wedge \mathrm{d} x_1^i$$

Crofton's formula in higher dimensions:

$$\sigma_d(M^d) \sim \int_{M^{d-1} \cap \Gamma \neq \varnothing} N(M^d \cap \Gamma) \ \epsilon_{\mathcal{K}}$$

which says that the area is equal to flux of geodesics

- The volume form follows from second derivative of *S* and is a new type of measure of two-point correlation (entanglement contour)
- *S* is no longer related to entropy even though it can be computed from field theory





## Coupled Wire Construction and generalized Wilson line

YKIS2016

Yukihisa Imamura and Keisuke Totsuka (arXiv:1605.09235)

Coupled Wire Construction :

A new method of systematically constructing topological phases



many-body hopping interaction

(Abelian) Laughlin state chiral spin liquid

(Non-Abelian) Moore-Read state Read-Rezayi state etc.

CFT (Luttinger liquid)



## Coupled Wire Construction and generalized Wilson line

YKIS2016

Yukihisa Imamura and Keisuke Totsuka (arXiv:1605.09235)

The bulk theory of the Laughlin state

= the Chern-Simons gauge theory

### How emerging in the coupled wire construction?

The ground state has some redundancy related to a gauge and a chiral transformation

generalized Wilson line :

$$\bar{\psi}_{j+1} \exp\left[i\int_{ja}^{(j+1)a} dy\left(\frac{e}{\hbar}A_y + a_y\gamma_5\right)\right]\psi_j$$

Chern-Simons gauge field



#### Topological phase transition in QCD

described by using imaginary chemical potential

<u>K.K.</u> and A. Ohnishi, PLB 750 (2015) 282. <u>K.K.</u> and A. Ohnishi, arXiv: 1602.06037, to be published in PRD.

We propose a new determination of the confinement-deconfinement transition in QCD



This determination may have direct relations with the entanglement entropy and the Uhlmann phase



## Distinguishability of countably many states

Ryuitiro Kawakubo and Tatsuhiko Koike, Department of Physics, Keio University

Theme:

State discrimination (We want to distinguish each state in a given set of states).

Problem:

What kind of states can be distinguishable by a single measurement? More precisely, in our discussion distinguishability of states is to be understood as the possibility of an unambiguous measurement on them.

- An unambiguous measurement is allowed to answer "'?" or "do not know".
- An unambiguous measurement distinguishes the inputs with certainty unless "?" is detected.

\* Condition for distinguishability

We obtained

countable pure states to be distinguishable.



## Distinguishability of countably many states Ryuitiro Kawakubo and Tatsuhiko Koike, Department of Physics, Keio University

\* Distinguishability of von Neumann lattices

A von Neumann lattice is a family of states which corresponds to the lattice in the classical phase space. The distinguishability of a von Neumann lattice depends only on the area of its fundamental region S. It is indistinguishable when S is sufficiently small and distinguishable when S is sufficiently large. The threshold is exactly the Planck constant, which is the unit of area of the phase space as in Bohr-Sommerfeld quantum condition.





distinguishable

S





### Holographic Entanglement Entropy of Anisotropic Minimal Surfaces in LLM Geometries

YKIS2016 Quantum Matter, Spacetime and Information June 13-June 17, 2016 YITP, Kyoto University, Japan

In collaboration with Chanju Kim, O-Kab Kwon

Based on arXiv1605.00849 (accepted in PLB) Previous related works Phys.Rev. D90 (2014) 4, 046006 , Phys.Rev. D90 (2014) 12, 126003 (with O. Kwon, C. Park and H. Shin.)

Kyung Kiu Kim (Yonsei University)  $\text{ABJM} \sim \text{AdS}_4 \times \text{S}^7 / Z_k$ 

ABJM + mass term  $\rightarrow$  mass deformed ABJM theory

mABJM ~ A Class of LLM solutions with SO(2,1)×SO(4)×SO(4) (Asymptotically  $AdS_4 \times S^7/Z_k$ )

 $ds^{2} = |G_{tt}|(-dt^{2} + dw_{1}^{2} + dw_{2}^{2}) + G_{xx}\left(dx^{2} + dy^{2}\right) + G_{\theta\theta}ds^{2}_{S^{3}/\mathbb{Z}_{k}} + G_{\tilde{\theta}\tilde{\theta}}ds^{2}_{\tilde{S}^{3}/\mathbb{Z}_{k}},$ 

Vacuum structure

Continuous Vacua Discrete Vacua

• Entanglement Entropy ?

 $\rho = |\psi\rangle\langle\psi|$  s = Tr ( -  $\rho_A \log \rho_A$  )

• An infinite number of entanglement entropies

 We consider all the entanglement entropies corresponding to all the vacua through a holographic approach(Ryu-Takayanagi Formula).

 $|\psi_1\rangle$ 

1/1/2

 $|\psi_4\rangle$ 

1 1/3

 $|\psi_5\rangle$ 

For small mass deformation

 $|\psi_0\rangle$ 

$$S_{\text{disk}} = \frac{\pi^5 R^9}{24G_N k} \left\{ \frac{l}{\epsilon} - 1 - \mu_0^2 l^2 \left[ \frac{4}{3} + \frac{1}{24} (C_3 - 3C_1 C_2 + 2C_1^3)^2 \right] \right\} + \mathcal{O}(\mu_0^3).$$

 This result should correspond to the corresponding field theory calculation with small mass perturbation.

$$\rho_i = |\psi_i\rangle\langle\psi_i| \quad s = Tr(-\rho_i \log \rho_i)$$

 There are many interesting structures (Droplet picture, Yong diagam, H c-theorem). Please visit my poster presentation ! Thank you !



#### Dynamic correlation of Kitaev's honey-comb model

Shinji Koshida

Department of Basic Science, The University of Tokyo

June 15, 2016



• By mapping the Kitaev's honey-comb model to Majorana fermions coupled to  $\mathbb{Z}_2\text{-gauge fields},$ 

$$\tilde{H} = \frac{i}{4} \sum_{x,y \in \Lambda} A_{xy} a_x^4 a_y^4$$

acting on an extended Hilbert space, it is "solved".



- The action of quantum spin operators is not clear.
- I derived matrix elements of quantum spin operators with respect to energy eigenstates.

$$\begin{split} \langle \phi_{\mathfrak{I}}^{\sigma'}, \tilde{S}_{x}^{\mu} \phi_{0}^{\sigma} \rangle \\ &= C^{\sigma\sigma'} \left( \sum_{i \in I \setminus \mathfrak{I}} (-1)^{\ell(\mathfrak{I},i)} R_{xi}^{\sigma'} \mathrm{Pf} Z_{\mathfrak{I} \cup \{i\}}^{\sigma\sigma'} + \sum_{i \in \mathfrak{I}} (-1)^{\ell(\mathfrak{I},i)} \overline{R_{xi}^{\sigma'}} \mathrm{Pf} Z_{\mathfrak{I} \setminus \{i\}}^{\sigma\sigma'} \right) \end{split}$$



## Time-evolution of Holographic Entanglement Entropy and Metric perturbations

Jung Hun Lee (Kyung Hee Univ.) Based on (arXiv:1512.02816) with Nakwoo Kim (Kyung Hee Univ.)

 Entanglement Entropy has holographic descriptions of quantum gravity by AdS/CFT correspondence. [Ryu,Takayanagi 06]



- The motivation is to see how small excitations in the gravity side manifest itself in HEE.
- We consider the small cap-like surfaces in the bulk and compute HEE perturbatively in deformed AdS vacuum. (ex. AdS-BHs, AdS-scalar systems)

## Time-evolution of Holographic Entanglement Entropy and Metric perturbations

Jung Hun Lee (Kyung Hee Univ.) Based on (arXiv:1512.02816) with Nakwoo Kim (Kyung Hee Univ.)

- We found that the metric perturbation around the AdS vacuum does not effect the divergent terms and the change is in the finite part.
- We have computed the entanglement temperature by using the methods of holographic renormalisation. [Bhattacpatya,Nozaki,Takayanagi,Ugajin 13]
  [Fefferman,Graham 85][Myers 99]
- We have checked that the entanglement temperature is proportional to the inverse size of the system and has the same value for the systems considered in our paper.

Thank you for listening!



### Quantum Entanglement in Topological Phases on a Torus

#### <u>Zhu-Xi Luo</u><sup>1</sup>, Yu-Ting Hu<sup>1</sup>, Yong-Shi Wu<sup>1-3</sup>

#### ArXiv: 1603.01777

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- 3. Collaborative Innovation Center of Advanced Microstructures, Fudan University, China

#### Quantum Entanglement in Topological Phases on a Torus

- 1. Phases with intrinsic topological order have (among other features),
  - 1) ground state degeneracy on nontrivial manifolds;
  - 2) bulk-edge correspondence;
  - 3) long-range entanglement.
- 2. What does entanglement for such phases look like on nontrivial manifolds?

How do these degenerate ground states enter?

What other information is involved?

3. These questions have been partially studied before[1] using Chern-Simons

theory. We focus on a general set of non-chiral theories: string-net model[2].

[1] Dong, Shiying, et al. *Journal of High Energy Physics* 2008.05 (2008): 016.

[2] Levin, Michael A., and Xiao-Gang Wen. *Physical Review B* 71.4 (2005): 045110.



4. By partitioning a torus into two cylinders, we derive

$$\overline{\rho}_{A} = \sum_{\mathcal{J}} |c_{\mathcal{J}}|^{2} \left\{ \sum_{j \in I} \frac{d_{j}}{d_{\mathcal{J}}} M_{\mathcal{J}j} \left[ \frac{D}{d_{j}} P_{j} \left( \alpha^{\otimes L_{1}} \right) \times \frac{D}{d_{j}} P_{j} \left( \alpha^{\otimes L_{2}} \right) \right] \right\}.$$

$$S = aL - \gamma, \quad \gamma = -\sum_{k} \frac{d_k^2}{D} \log \frac{d_k^2}{D} + 2\log D - \sum_{\mathcal{J}} |c_{\mathcal{J}}|^2 \log d_{\mathcal{J}} + \sum_{\mathcal{J}} |c_{\mathcal{J}}|^2 \tilde{S_{\mathcal{J}}} - \tilde{S'}$$

5. A decomposition matrix M enters the expression which describes how bulk topological charges of the

ground states decompose into boundary degrees of freedom.

$$\mathcal{J} \to \bigoplus_j M_{\mathcal{J}j}j.$$

- 6. We generalize the Minimally Entangled States[3] to Minimally Entangled Sectors.
- 7. Examples from abelian & non-abelian finite groups and modular tensor category are discussed.



## Spectral Weight in Holographic Superfluids

### Victoria Martin Stanford University

arXiv:xxxx.xxxx Gouteraux, VM See also: arXiv:1210.1590 Anantua, Hartnoll, VM, Ramirez



**Quantum Matter, Spacetime and Information** 

June 15, 2016



#### Charge behind horizon



$$G^R_{J_\perp J \perp}(\omega,k) \sim \frac{\delta A_{(1)}}{\delta A_{(0)}}$$

### Low energy spectral weight at nonzero momentum



$$\sigma_{\perp}(k) = \lim_{\omega \to 0} \frac{\operatorname{Im} G^R_{J_{\perp}J_{\perp}}(\omega, k)}{\omega}$$












- 1) How should we interpret low energy spectral weight that exists independently of charge?
- 2) What other degrees of freedom could this weight represent?
- 3) To what extent do bulk charge distribution properties represent those of the boundary charge?







Discussion :

What a relation between the entanglement and the de Sitter spacetime structure ?



### Holographic Entanglement Entropy (HEE) and Field Redefinition Invariance (FRI)

### M. R. Mohammadi Mozaffar

arXiv: 1603.05713

in collaboration with A. Mollabashi, M.M. Sheikh-Jabbari, M.H. Vahidinia IPM (School of Physics)

June 2016

### Field Redefinition Invariance

• Physical observables must be invariant under the field reparametrization

(change of basis in the Hilbert space)

Example: Path Integral in QFT

$$Z = \int D\Phi(x) \ e^{-I[\Phi(x)]} = \int D\tilde{\Phi}(x) \ e^{-\tilde{I}[\tilde{\Phi}(x)]}$$

 $\Phi(x) \to \tilde{\Phi}(x) = \tilde{\Phi}[\Phi(x)]$  non-zero Jacobian

• A one-to-one correspondence between physical observables

Question

Can we find HEE functional for higher derivative gravity theories using FRI?

• Our Strategy



#### Achievements

- FRI extracts the new HEE functionals from the RT functional, so
  - **1** It gives both the HEE functional and the corresponding hypersurface
  - 2 It has simple generalization to time dependent cases
  - **③** Different entanglement inequalities satisfied



### Field Space Entanglement: Scalar Fields

### Ali Mollabashi

School of Physics

Institute for Research in Fundamental Sciences (IPM), Theran

Based on JHEP 03 (2016) 015 (arXiv: 1509.03829),

in collaboration with M.R. Mohammadi-Mozaffar

• Consider a local QFT with N number of fields  $\mathcal{L} = \mathcal{L}_1 \left[ \phi_1(x) \right] + \mathcal{L}_2 \left[ \phi_2(x) \right] + \dots + \mathcal{L}_N \left[ \phi_N(x) \right] + \mathcal{L}_{\text{int.}} \left[ \phi_i(x) \right]$ 

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• Explicit models

$$S = \frac{1}{2} \int d^d x \left[ \sum_{i=1}^N \left( \partial_\mu \phi_i \right)^2 + \lambda \sum \partial_\mu \phi_i \partial^\mu \phi_j \right]$$

### Our (Gaussian) Models



### Our (Gaussian) Models



- Renyi & Araki-Lieb inequalities and SSA are satisfied
- *n*-partite information  $\geq 0$  (checked for  $n \leq 5$ )
- In particular  $I^{(3)} \ge 0$  (existence holographic dual?)
- Infinite-Range model in  $\lambda \to 0$  limit

$$S^{\text{reg.}}(m) = \frac{\lambda^2 m(N-m)}{32} \left[ 1 - \log \frac{\lambda^2 m(N-m)}{32} \right] + \mathcal{O}(\lambda^3)$$



# The Gibbs paradox revisited from the fluctuation theorem with absolute irreversibility

<sup>1</sup>University of Tokyo, <sup>2</sup>RIKEN CEMS

Yûto Murashita<sup>1</sup>, Masahito Ueda<sup>1,2</sup>

The Gibbs paradox from gas mixing



The Gibbs paradox has three faces

Gibbs (1875) GP-I GP-II GP-II GP-II GP-III Ehrenfest&Trkal (1921) GP-III Classical) statistical mechanics

The three faces are resolved in the thermodynamic limit

van Kampen (1984) Jaynes(1992)

15th June, 2016

However, GP-II is partially open in small systems!

**YKIS** Conference

# The Gibbs paradox revisited from the fluctuation theorem with absolute irreversibility

<sup>1</sup>University of Tokyo, <sup>2</sup>RIKEN CEMS

Yûto Murashita<sup>1</sup>, Masahito Ueda<sup>1,2</sup>

Theme of GP-II  $S(T, V, N) = S^{\text{stat}}(T, V, N) + k_{\text{B}}f(N)$ **Removing the ambiguity** f(N)\*The quantum resolution is irrelevant in this context In the thermodynamic limit **Extensivity** S(T, qV, qN) = qS(T, V, N)  $\Leftrightarrow f(N) = -N \ln N + N \text{const.}$  $-\ln N! \ (N \to \infty)$ In a small thermodynamic system Fluctuation theorem with absolute irreversibility  $\Leftrightarrow f(N) = -\ln N! + N \text{const.}$  $\langle e^{-\beta(W-\Delta F)} \rangle = 1 - \lambda$ 

YKIS Conference

15th June, 2016

#26

Flux quench in a system of interacting spinless fermions in one dimension Yuya Nakagawa (ISSP, Univ. of Tokyo)

Nakagawa, Misguich, Oshikawa, arXiv:1601.06167

- Quantum quench of the flux piercing an interacting spinless fermion chain
- Numerical calculation of <u>the dynamics of particle current</u> <u>after the quench</u>







## Quantum Annealing with Hyperpolarized Nuclear Spins M. Negoro @ Eng. Sci., Osaka Univ.

Proposal for nuclear ferro or anti-ferro @ room temperature





Entanglement dynamics of Majorana fermions Takumi Ohta *Yukawa Institute for Theoretical Physics, Kyoto University* With Shu tanaka, Ippei Danshita, and Keisuke Totsuka Reference: Phys. Rev. B 93, 165423 (2016)

Dynamical properties of Majorana fermions

• Sweep dynamics with OBC

Sweep from C phase to C\* phase  $H(t) = -J^{XZX} \sum_{i=1}^{N} \sigma_i^x \sigma_{i+1}^z \sigma_{i+2}^x + J(t) \sum_{i=1}^{N} \sigma_i^y \sigma_{i+1}^z \sigma_{i+2}^y$ 



 $J(t)/J^{XZX} = 2t/ au, \quad 0 \leq t \leq au \qquad au$  : Sweep time

Physical quantities

String correlation functions (SCFs)

entanglement entropy (EE), spectrum (ES)

## **Digest of Dynamics**



Oscillating and splitting structures in time





### Universality of Black Hole Quantum Computing

#### **Benedikt Richter**

Physics of Information and Quantum Technologies Group, IT, Lisboa

IST, Universidade de Lisboa

ASC, Ludwig-Maximilians-Universität München

joint work with

Gia Dvali (LMU, MPP, NYU) Cesar Gomez (LMU, UAM-CSIC) Dieter Lüst (LMU, MPP) Yasser Omar (IT, IST)

based on arXiv: 1605.01407









Doctoral Programme in the Physics and Mathematics of Information www.dp-pmi.org

### Black Hole Quantum Computing

By analyzing the key properties of black holes, we derive a model-independent picture of black hole quantum computing.



 $t_{gate} \sim t_{decoh} \sim t_{life-time}$ 

⇒ maximal circuit depth is trivial,

⇔ Trade-off between memory and information processing capacity





"QUANTUM MATTER, SPACETIME AND INFORMATION", JUNE, 13-17, 2016

PAOLA RUGGIERO

### THE ENTANGLEMENT NEGATIVITY IN RANDOM SPIN CHAINS

WITH V. ALBA, P. CALABRESE ARXIV:1605.00674



### ENTANGLEMENT NEGATIVITY IN MANY BODY SYSTEMS

$$\mathcal{E}_{A_1: A_2} = \ln Tr |\rho^{T_2}|$$

$$\langle e_i, e_j | \rho_A^{T_2} | e_k e_l \rangle = \langle e_i, e_l | \rho_A | e_k e_j \rangle$$

$$\mathcal{B} \qquad A_2$$

$$A_1$$

### <u>"GOOD MEASURE" OF ENTANGLEMENT:</u> PURE STATES MIXED STATES

### **QFT** METHODS: [CALABRESE, CARDY, TONNI, 2011]

Replica Approach: 
$$\mathcal{E} = \lim_{n_e \to 1} \ln Tr(\rho^{T_2})^{n_e}$$

EXACT RESULTS AVAILABLE IN CFT:

 $tr(\rho_A^{T_2})^n = \mathcal{N}\langle \mathcal{T}(u_1, 0)\tilde{\mathcal{T}}(v_1, 0)\tilde{\mathcal{T}}(u_2, 0)\mathcal{T}(v_2, 0)\rangle$ 



### NEGATIVITY IN REANDOM SPIR CHAINS B2








# Entanglement Entropy of Scattering Particles

Shigenori Seki

This poster presentation is based on the work:

R. Peschanski (IPhT, CEA-Saclay) and SS,

"Entanglement entropy of scattering particles", Phys. Lett. B758 (2016) 89.

### QUESTION

Let us consider a scattering process of two particles.



What is the entanglement entropy between the particles in the two-particle final state?

### **OUR ANSWER**

There are elastic and inelastic channels:  $A + B \rightarrow A + B$  "elastic"  $A + B \rightarrow X$  "inelastic" (multi-particle)

By using partial wave expansions, we calculate the entanglement entropy;

$$S_{\rm EE} = -\ln \frac{\left|\sum_{\ell} (2\ell+1)s_{\ell}\right|^{2}}{\sum_{\ell,\ell'} (2\ell+1)(2\ell'+1)|s_{\ell}|^{2}}$$

$$\stackrel{\vec{p}}{\longrightarrow} \qquad \frac{\vec{p}}{-\vec{k}} \stackrel{\vec{p}}{=} \frac{\pi k}{E_{A\vec{k}} + E_{B\vec{k}}} \langle\!\langle \vec{p} | \mathbf{s} | \vec{k} \,\rangle\!\rangle = \sum_{\ell} (2\ell+1)s_{\ell}P_{\ell}(\cos\theta)$$

$$s_{\ell} = 1 + 2i\tau_{\ell}, \quad \mathrm{Im}\tau_{\ell} = |\tau_{\ell}|^{2} + \frac{1}{2}f_{\ell} \quad \text{(unitarity)}$$

By introducing the physical Hilbert space, we obtain the formula that describes the entanglement entropy in terms of physical observables;

$$S_{\rm EE} = -\ln K$$
,  $K \sim 1 - \frac{\sigma_{\rm el} - \frac{1}{R^2} \frac{d\sigma_{\rm el}}{dt} \Big|_{t=0}}{4\pi R^2 - \sigma_{\rm inel}}$ 

 $\sigma_{\rm el}$ : integrated elastic cross section  $\frac{d\sigma_{\rm el}}{dt}$ : differential elastic cross section  $\sigma_{\rm inel}$ : integrated inelastic cross section R: maximal impact parameter



### Z4 topological crystalline insulators and superconductors

Ken Shiozaki, University of Illinois at Urbana Champaign

KS, M. Sato, K. Gomi, arXiv:1511.01463

- Topological insulators + nonsymmorphic space group
- Periodic table from K-theory
- Glide + Time-reversal symmetry  $\rightarrow$  Z4 phase



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#### Sudden Death and Birth of Topological Entanglement in 1D Fermions at Finite Temperature





# A few examples for Holography vs. experiment

### Sang-Jin Sin (HYU) 2016.06.15@Kyoto



### Anomalous Hall coefficient Rs

$$\rho_H \equiv R_H H + R_s M_0,$$

For Intrinsic deflection/  $R_s \sim \rho_{xx}^2$ . Side jump

#### For skew scattering

 $R_s \sim \rho_{xx}.$ 



#### <u>arXiv:1512.08916</u> Phys.Lett. B759 (2016) 104-109 KY. Kim, KK.Kim, Y.Seo + sj

$$2\kappa^{2}S = \int d^{4}x \sqrt{-g} \left\{ R + \frac{6}{L^{2}} - \frac{1}{4}F^{2} - \sum_{I=1,2} \frac{1}{2}(\partial\chi_{I})^{2} \right\} - \frac{1}{16} \int q_{\chi}(\partial\chi_{I})^{2}F \wedge F + R_{s} = \frac{3}{r_{0}\mu} \frac{1}{\theta^{2} + (1 + \mu^{2}/\beta^{2})^{2}} \qquad \rho_{xx} = \frac{1 + \mu^{2}/\beta^{2}}{\theta^{2} + (1 + \mu^{2}/\beta^{2})^{2}}$$



FIG. 2. Extraordinary Hall constant as a function of resistivity. The shown fit has the relation  $R_s \sim \rho^{1.9}$ . From Kooi, 1954.

#### Theory vs. experiment in Dirac Fluid of graphene

#### Science 11 Feb 2016

#### Observation of the Dirac fluid and the breakdown of the Wiedemann-Franz law in

**graphene** Jesse Crossno, Jing . Shi, Ke Wang, Xiaomeng Liu,

Subir Sachdev, Philip Kim,\*, Takashi Taniguchi, Kenji Watanabe, Thomas A. Ohki5, Kin Chung Fong,\*



Holography (HYU) to appear U(1) x U(1) #35

# Fidelity approach to Adiabatic Quantum Computation of hard problems Jun Takahashi (Univ. of Tokyo)



Annealing parameter  $\lambda$ 

# Fidelity approach to Adiabatic Quantum Computation of hard problems Jun Takahashi (Univ. of Tokyo)



# Q.

When AQC is applied to an **NP-hard** problem, what is the *physical mechanism* that causes the exponentially small gap?

# Fidelity approach to Adiabatic Quantum Computation of hard problems Jun Takahashi (Univ. of Tokyo)



# Q.

When AQC is applied to an **NP-hard** problem, what is the *physical mechanism* that causes the exponentially small gap?

# A. (so far)

1st order phase transition (-like) phenomena



# Main Question

# The 1st-order phase transitions are actually *strongly sample dependent*.

Can we understand them as a whole? (e.g. a non self-averaging behavior within a spin glass phase?)



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# Method



fix: Maximum Independent Set as a NP-complete problem Stochastic Series Expansion (SSE) + Replica Exchange ( $\lambda$  direction)

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fix: Maximum Independent Set as a NP-complete problem Stochastic Series Expansion (SSE) + Replica Exchange ( $\lambda$  direction)

Our study suggests that fidelity susceptibility is so far the best way to see the sample-averaged phase transition





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### Numerical study of real-time correlation function

### Comparison with analytical results, random-matrix limit





#### Fixed Point Matrix Product States and 1+1D Topological Quantum Field Theory

#### Alex Turzillo

California Institute of Technology Based on work with Anton Kapustin and Minyoung You

June 14, 2016

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#### Idea

- Matrix Product States (MPS) efficiently approximate ground states of 1D gapped local Hamiltonians. Each gapped phase of these Hamiltonians corresponds to a Fixed Point MPS.
- Lattice TQFT also describes gapped systems at fixed points.
- Idea: build a dictionary between these two frameworks.
  - both are classified by the same algebraic data
  - MPS and parent Hamiltonians arise from the state-sum



#### Generalizations

- ► The algebraic data that classifies these theories makes sense in other categorical contexts ⇒ generalizations
- Idea: passing structured (*ie* not strictly topological) field theories through the dictionary returns variants of MPS.
- ► Equivariant TQFT → Symmetric MPS
  - describes gapped symmetric phases: SPTs/SETs
  - twisted sectors and symmetry breaking
- ► Spin TQFT → Fermionic MPS
  - describes fermionic phases, eg the nontrivial Majorana chain

related to symmetric MPS by bosonization





## Holographic duality from random tensor arxiv:1601.01694

### Construction



Every vertex:



=  $\sum_{abcde} T_{abcde}$  |abcde> Haar random state in the product Hilbert space  $\otimes_{i=1}^{5} \mathcal{H}_{i}$ 

## Holographic duality from random tensor arxiv:1601.01694

### Properties

- RT formula & bulk correction Hawking-Page transition
- Quantum error correction
- Correlation spectrum









# **Engineering Holographic Superconductor Phase Diagrams**

Presented by Yun-Long Zhang

CTS-NTU (Center for Theoretical Sciences, National Taiwan University) — zhangyunlong001@gmail.com 2016-06-15 @ YITP

$$\mathcal{L}_{M} = \sum_{i=1,2} \mathcal{L}_{\psi_{i}} + \mathcal{L}_{\phi} + \mathcal{L}_{int}, \qquad g_{M}^{2} \mathcal{L}_{\psi_{i}} = -\frac{1}{2} \left( \partial \psi_{i} \right)^{2} - V(\psi_{i}), \qquad V(\psi_{i}) = \frac{1}{2} m_{i}^{2} \psi_{i}^{2} + \frac{1}{4} \lambda_{i} \psi_{i}^{4}, \\ g_{M}^{2} \mathcal{L}_{int} = -\frac{1}{2} \sum_{i=1,2} F_{i}(\phi) \psi_{i}^{2}, \qquad g_{M}^{2} \mathcal{L}_{\phi} = -\frac{1}{2} \left( \partial \phi \right)^{2} - V(\phi), \qquad V(\phi) = \frac{1}{2} m_{\phi}^{2} \phi^{2} + \frac{1}{4} \lambda_{\phi} \phi^{4},$$



arXiv: <u>1603.08259</u> Jiunn-Wei Chen, Shou-Huang Dai, Debaprasad Maity, Yun-Long Zhang



## **Constraints in Rindler Fluid & AdS Cutoff Fluid**

#### arXiv: 1207.5309 & 1401.7792 & 1408.6488



Presented by Yun-Long Zhang (zhangyunlong001@gmail.com)