

Higher spin holography and Higgs phenomenon

Yasuaki Hikida (Ritsumeikan University)

Ref. YH,arXiv:1601.01784

(Cf. YH-Rønne,JHEP1507(2015)125;Creutzig-YH,JHEP1510(2015)164)

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4 Day Conference "holography and quantum information"

Higher spin gauge theory

- Higher spin gauge theory

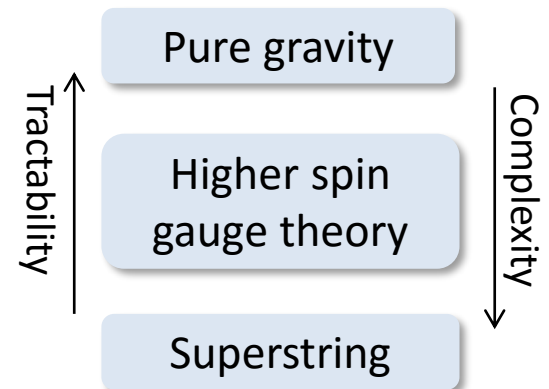
- A totally symmetric rank- s field

$$\varphi_{\mu_1 \dots \mu_s} \sim \varphi_{\mu_1 \dots \mu_s} + \partial_{(\mu_1} \xi_{\mu_2 \dots \mu_s)}$$

- Natural extension of electromagnetism ($s=1$) and gravity ($s=2$)
- **Vasiliev theory** is famous as a non-trivial theory on AdS

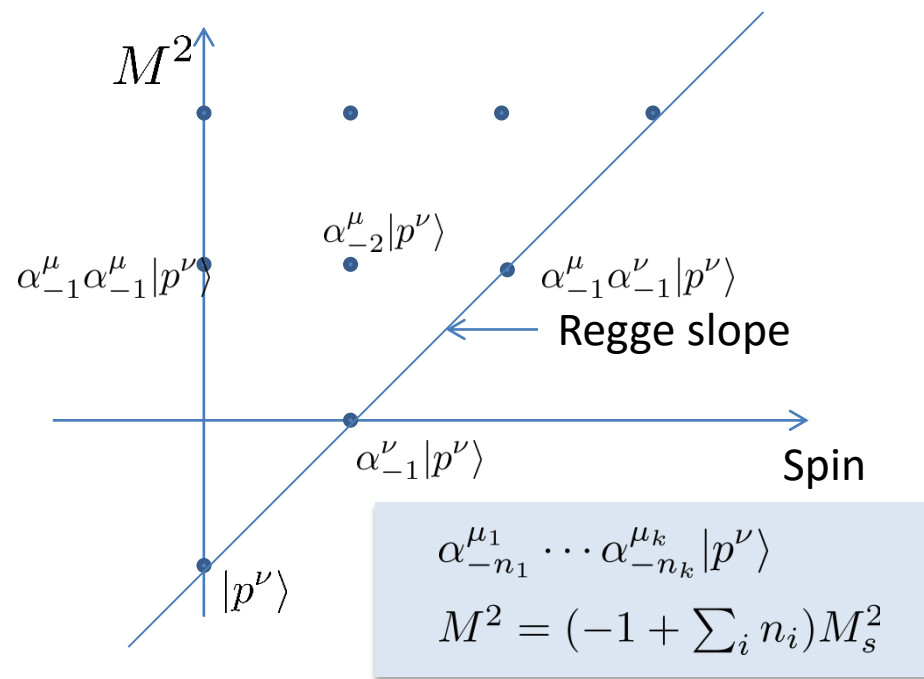
- Applications

- Simplified version of **AdS/CFT correspondence**
 - More tractable than using superstring theory
- Higher spin excitations of **superstring theory**
 - Higher spin gauge theory may be regarded as a toy model for superstring theory

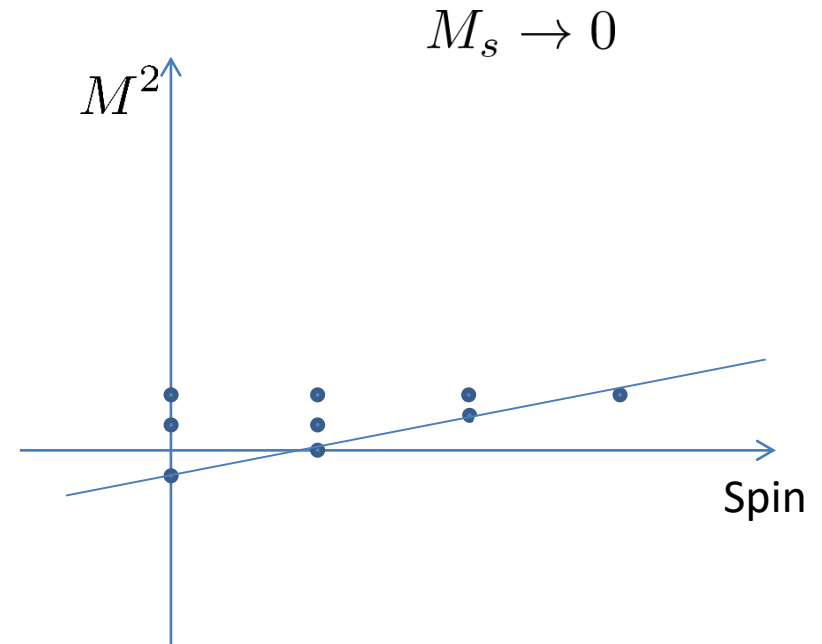


Strings \Leftrightarrow Higher spin fields

- String spectrum



- Tensionless limit



- \rightarrow {
 - Higher spin gauge symmetry may appear at the tensionless limit
 - Superstrings could be described by **breaking** higher spin symmetry [Gross '88]

Higgs phenomenon

- The aim of this talk
 - To understand the mechanism of **higher spin symmetry breaking** as a generalization of Higgs mechanism for spin 1 gauge theory
 - To examine the relation to superstring theory
- 4d Vasiliev theory
 - We examine 4d Vasiliev theory dual to 3d **critical** $O(N)$ vector model
 - The anomalous dimensions of dual higher spin currents were already computed from purely CFT method
 - We reproduce them with the bulk Witten diagram to understand the mechanism from **the bulk** viewpoints [YH '16]
- 3d Vasiliev theory
 - We compute masses for 3d Vasiliev theory and discuss the relation to superstring theory [YH-Rønne, Creutzig-YH '15]

Plan

0. Introduction
1. Higher spin holography
2. Breaking of higher spin symmetry (AdS_4)
3. Relation to superstrings (AdS_3)
4. Conclusion

1. HIGHER SPIN HOLOGRAPHY

Higher spin gauge theory

- Higher spin gauge theory

- Higher spin gauge transformation

$$\delta\varphi_{\mu_1\dots\mu_s} = \partial_{(\mu_1}\xi_{\mu_2\dots\mu_s)}, \quad \varphi_{\lambda\sigma\mu_3\dots\mu_s}^{\lambda\sigma} = 0, \quad \xi_{\lambda\mu_3\dots\mu_s}^{\lambda} = 0$$

- Equations of motion [Fronsdal '78]

$$\square\varphi_{\mu_1\dots\mu_s} - \partial_{(\mu_1}\partial^{\lambda}\varphi_{|\mu_2\dots\mu_s)\lambda} + \partial_{(\mu_1}\partial_{\mu_2}\varphi_{\mu_3\dots\mu_s)\lambda}^{\lambda} = 0$$

- No-go theorems [e.g. Weinberg '64] **forbid non-trivial interactions** consistent with higher spin gauge symmetry (with some assumptions)

- Non-trivial theories on AdS

- **Vasiliev theory**: Only equations of motion are known
- Higher spin AdS₃ gravity: Topological theory (Chern-Simons description)

Higher spin holography

- Klebanov-Polyakov proposal '02

4d Vasiliev theory \longleftrightarrow 3d $O(N)$ vector model

$$\varphi_{\mu_1 \dots \mu_s}$$

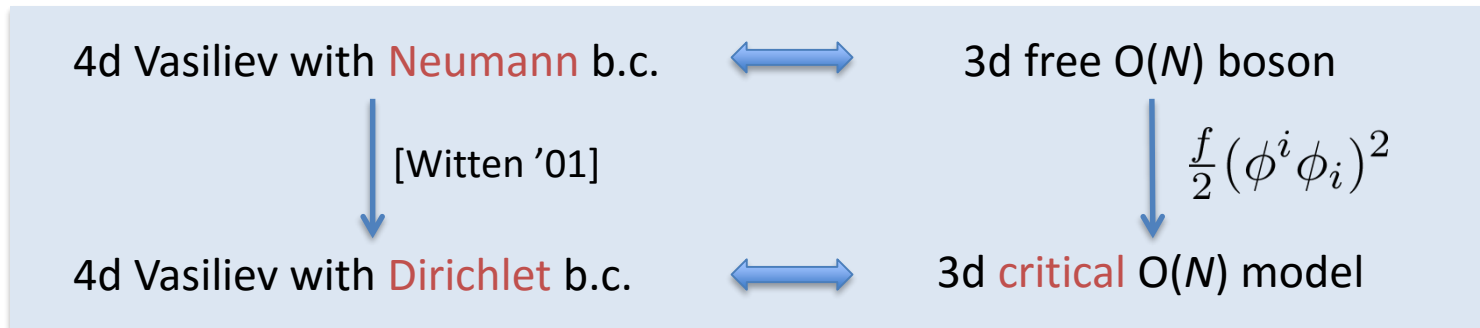
$$J_{a_1 \dots a_s} = \phi_i \partial_{(a_1} \dots \partial_{a_s)} \phi^i$$

- CFT **correlators** are reproduced from Vasiliev theory [Giombi-Yin '09-'10]
- Further developments
 - Role of higher spin symmetry is clarified [Maldacena-Zhiboedov '11-'12]
 - Concrete relations between superstrings and higher spin fields via AdS/CFT (ABJ triality) [Chang-Minwalla-Sharma-Yin '12]
 - Lower dimensional duality (3d Vasiliev \leftrightarrow 2d W_N minimal model) [Gaberdiel-Gopakumar '10]

2. BREAKING OF HIGHER SPIN SYMMETRY

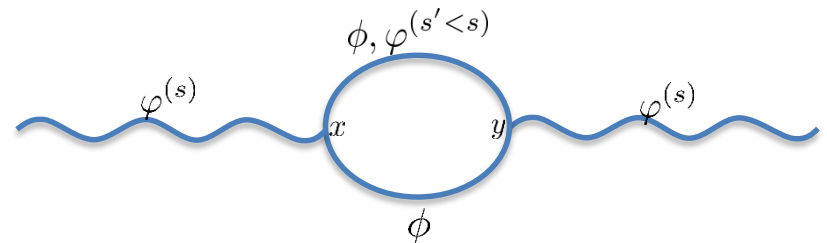
Symmetry breaking

- Klebanov-Polyakov duality



- Higher spin symmetry breaking

- CFT side: Symmetry is broken at the order of $1/N$
- HS side: Gauge fields become massive because of
 - The change of boundary condition for scalar field
 - One-loop effect
- We want to confirm this bulk interpretation **quantitatively**



Short v.s. long multiplet

[Girardello-Porrati-Zaffaroni '02]

- Fields on AdS_4 are classified by representations of $\text{so}(4,1)$
 - Δ : scaling dimension, s : spin ($\Delta \geq s + 1$)
- Shortening of representation

$$\lim_{\Delta \rightarrow s+1} D(\Delta, s) \rightarrow D(s+1, s) \oplus D(s+2, s-1)$$

Short representation: $\partial \cdot J^{(s)} = 0$

- Goldstone modes from bound states with $(S, n) = (s - s' - 1, 0)$

$$D(s' + 1, s') \otimes D(2, 0) = \bigoplus_{S=0}^{\infty} \bigoplus_{n=0}^{\infty} D(s' + S + n + 3, s' + S)$$

- A remark: spin 2 currents are kept conserved

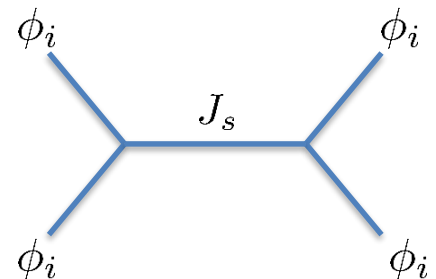
Masses from anomalous dimensions

- AdS/CFT dictionary
 - The masses from the **anomalous dimensions** of dual currents

$$M_s^2 = \Delta_s(\Delta_s - 3) - (s + 1)(s - 2)$$

- The anomalous dimensions from the critical model
 - They were obtained purely from the CFT [Ruhl '04] (see also [Skvortsov '15, Giombi-Kirilin '16])

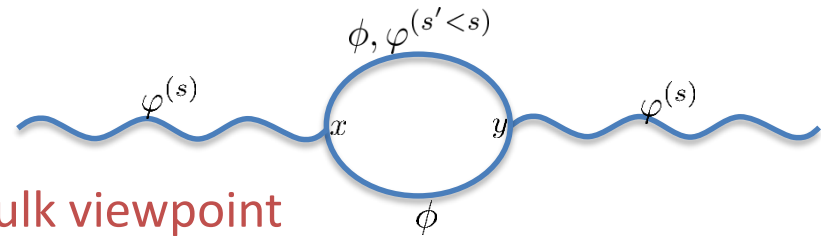
$$\begin{aligned}\tau_s \equiv \Delta_s - s - 1 &= \frac{16(s - 2)}{3\pi^2 N(2s - 1)} + \mathcal{O}\left(\frac{1}{N^2}\right) \\ \Rightarrow M_s^2 &= \frac{16(s - 2)}{3\pi^2 N} + \mathcal{O}\left(\frac{1}{N^2}\right)\end{aligned}$$



Anomalous dimensions from bulk

- Goal

- To reproduce the masses from **the bulk viewpoint**

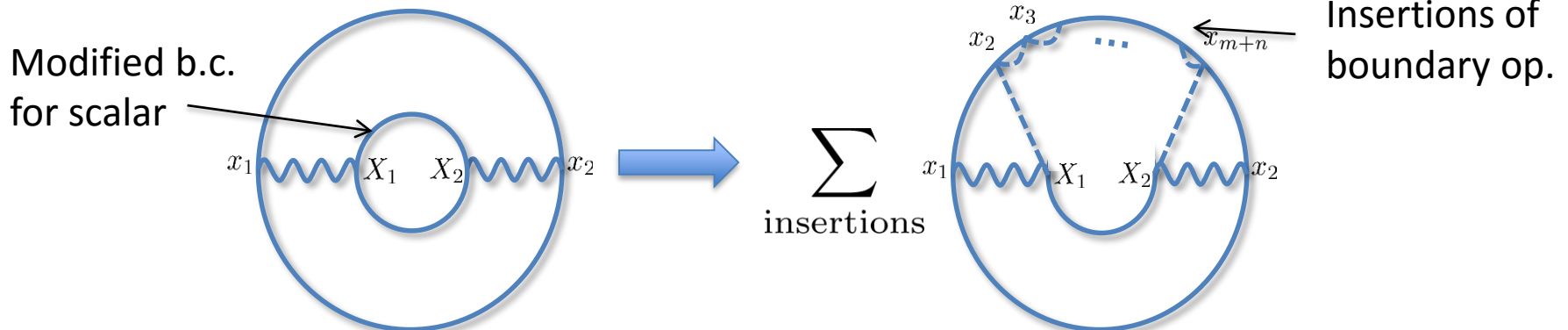


- Methods

- Trick 1: Compute 2-pt function of currents using **the bulk Witten diagram**

$$\langle J_s(x_1) J_s(x_2) \rangle_{f \rightarrow \infty} = \frac{N_s P_s(x_{12})}{|x_{12}|^{2s+2+2\tau_s}}$$

- Trick 2: Rewrite the scalar propagator with modified b.c. with the **insertions of boundary operators**

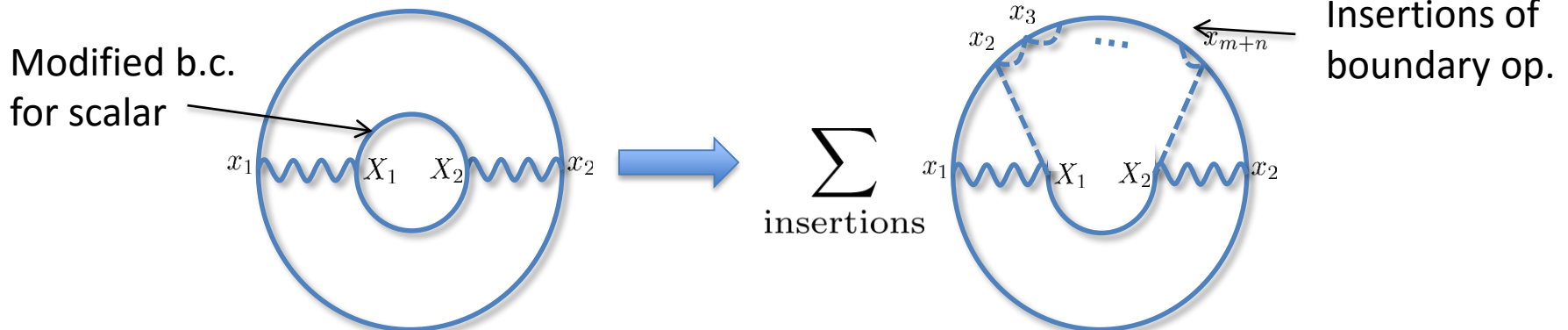


Anomalous dimensions from bulk

- Bulk **Witten diagram** \rightarrow Boundary **conformal perturbation theory**

$$\left\langle \prod_{i=1}^n \Phi_i(x_i) \right\rangle_f = \frac{\langle \prod_{i=1}^n \Phi_i(x_i) e^{-\Delta S} \rangle_0}{\langle e^{-\Delta S} \rangle_0}$$

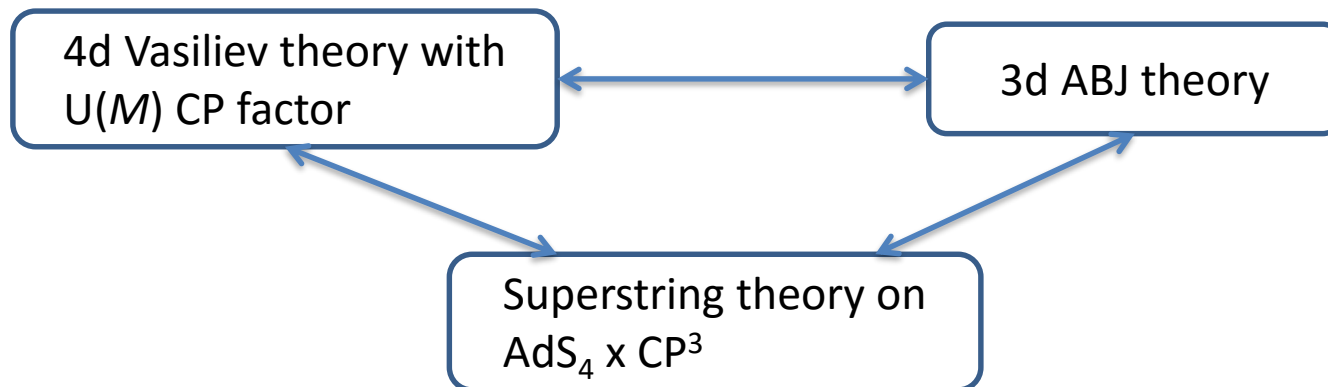
- The anomalous dimensions are reproduced in the conformal perturbation theory [YH '16]
 - The result confirm quantitatively **the bulk picture** that the breaking is a one loop effect and due to the change of boundary condition
 - The Goldstone modes cannot be identified with this method



3. RELATION TO SUPERSTRINGS

ABJ triality

- Klebanov-Polyakov proposal '02
 - 4d Vasiliev theory \Leftrightarrow 3d $O(N)$ vector model
- ABJ triality [Chang-Minwalla-Sharma-Yin '12]
 - HS side: 4d extended Vasiliev theory with $U(M)$ Chan-Paton factor
 - CFT side: 3d $U(N)_k \times U(M)_{-k}$ Chern-Simons-Matter theory (ABJ theory)
 - String side: Superstring theory on $AdS_4 \times CP^3$



Lower dimensional triality

- Gaberdiel-Gopakumar proposal '10
 - 3d Vasiliev theory \Leftrightarrow 2d W_N minimal model
- More degrees of freedom [CHR '13] (c.f. [Gaberdiel-Gopakumar '13] for $M=2$)
 - HS side: 3d Vasiliev theory with $U(M)$ CP factor
 - CFT side: 2d coset-type model at a large N limit $\frac{\mathfrak{su}(N+M)_k \oplus \mathfrak{so}(2NM)_1}{\mathfrak{su}(N)_{k+M} \oplus \mathfrak{u}(1)}$
 - Evidence: **One-loop partition function** agrees
- Extended supersymmetry [CHR '14, HR '15]
 - $N=3$ SUSY at $k=N+M$
 - ➔ Superstrings on $AdS_3 \times M^7$ ($M^7 = SO(5)/SO(3)$ or $SU(3)/U(1)$)
 - Evidence: **BPS spectrum** agrees (cf. [Argurio-Giveon-Shomer '00])
 - Similar proposals with $N=4$ [Gaberdiel-Gopakumar '13-'15]

Symmetry breaking

- Turning on string tension
 - The 2d coset model is dual to 3d Vasiliev with exact higher spin symmetry
 - Higher spin symmetry for 2d CFT is broken by deformation **preserving $N=3$ superconformal symmetry**
- The masses of higher spin fields
 - Leading in G_N , all order in deformation parameter f [YH-Rønne, Creutzig-YH '15]

$$\begin{cases} M_{(s)}^2 = 0 & (\text{so}(3)_R \text{ singlet}) \\ M_{(s)}^2 = \frac{8G_N(s-1)f^2}{(1+f^2)^2} & (\text{so}(3)_R \text{ triplet}) \end{cases}$$

- $M^2 = 0$ (symmetry is preserved at the order)
- $M^2 \propto s-1$ (like Regge spectrum in flat space-time)
- Need to examine M/N -effects

4. CONCLUSION

Conclusion

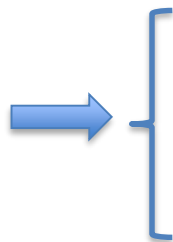
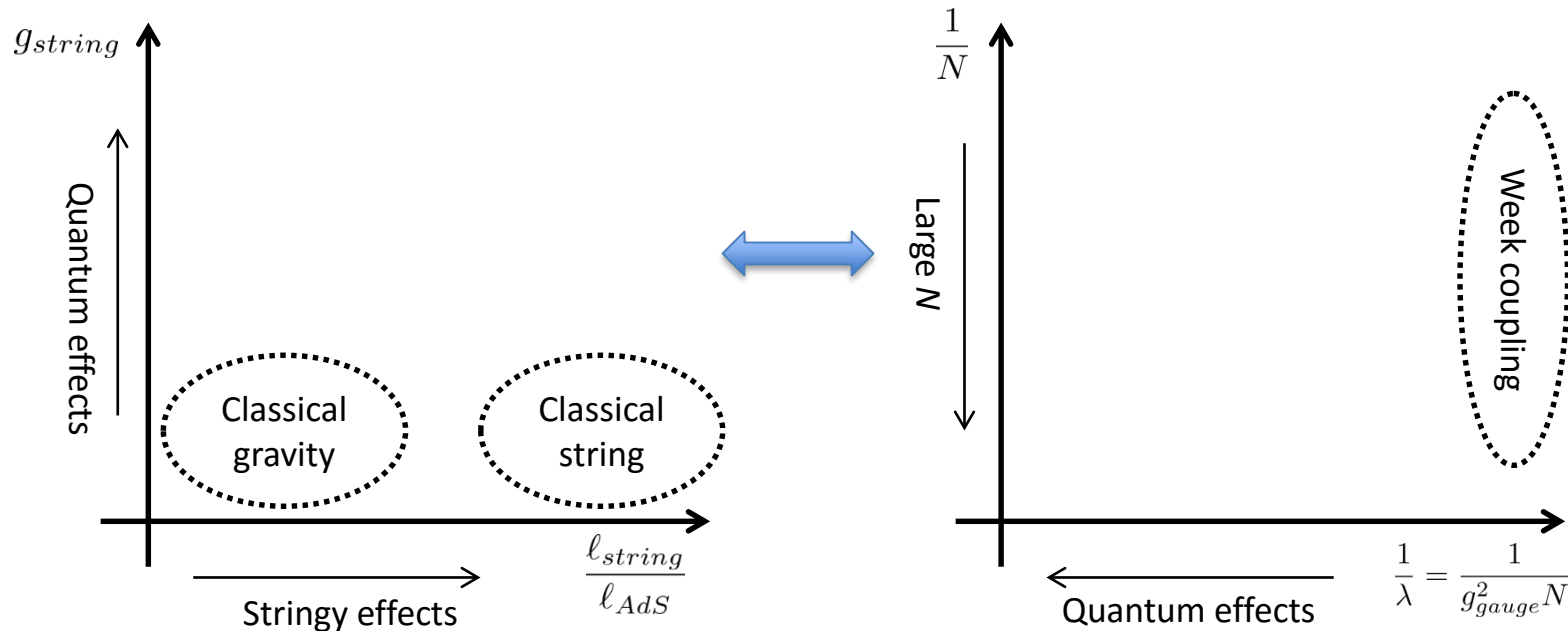
- The symmetry breaking in 4d Vasiliev theory
 - Masses of higher spin fields are reproduced in **conformal perturbation theory**
 - **Bulk interpretation** is (partially) confirmed via the relation between the bulk Witten diagrams and boundary conformal perturbation theory
- Relation to superstring theory
 - AdS_4 : need to introduce supersymmetry and coupling to gauge fields In order to see the relation to ABJ triality
 - AdS_3 : M/N -corrections should be included to relate to superstring theory
 - Other works on Higgsing for higher spin fields on AdS [Gaberdiel-Peng-Zadeh '15, Gwak-Joung-Mkrtchyan-Rey '15, Gwak-Kim-Rey '16]

5. APPENDICES

The map of AdS/CFT

- Superstrings on $AdS_5 \times S^5$

- 4d $U(N)$ gauge theory



- Tensionless limit of string theory (**higher spin gauge theory**) can be dual to a perturbative region of gauge theory
- Higher spin gauge theory is easier to solve than string theory

ABJ triality

- 3d ABJ theory
 - Bi-fundamentals under $U(N) \times U(M)$ gauge symmetry

$$A_i^\alpha, B_\beta^j \quad (i, j = 1, 2, \dots, N, \quad \alpha, \beta = 1, 2, \dots, M)$$

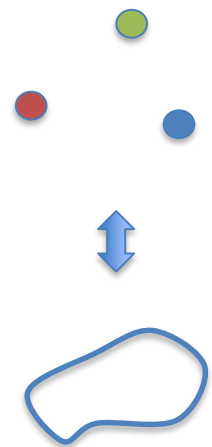
- Higher spin region: $M \ll N$
 - 't Hooft parameter is stronger for $U(N)$ than $U(M)$

$U(N)$ invariant currents

Higher spin fields

$$[J_{a_1 \dots a_s}]_\beta^\alpha = A_i^\alpha \partial_{(a_1} \dots \partial_{a_s)} B_\beta^i \quad \longleftrightarrow \quad [\varphi_{\mu_1 \dots \mu_s}]_\beta^\alpha$$

- String region: $M \approx N \gg 1$
 - $\text{tr}[ABAB \dots AB] \Leftrightarrow$ strings
 - Single-string state \Leftrightarrow Multi-particle state of higher spin fields



Boundary condition & RG flow

- Scalar field in 4d Vasiliev theory

- Behavior of bulk scalar near the boundary ($z=0$)

$$\varphi \sim az + bz^2 \Rightarrow \begin{cases} a = 0 \text{ (Dirichlet b.c.)} \Leftrightarrow \Delta_+ = 2 \\ b = 0 \text{ (Neumann b.c.)} \Leftrightarrow \Delta_- = 1 \end{cases}$$

$$\left(\Delta_{\pm} = \frac{3}{2} \pm \sqrt{\frac{9}{4} + m^2} = 2 \text{ or } 1 \right)$$

- RG flow by $\delta\mathcal{L} = \frac{f}{2}(\phi^i\phi_i)^2$

- Free theory at UV fixed pt.

- Dimension of dual scalar operator $[\phi_i\phi^i] = 1 \Leftrightarrow$ Neumann b.c.

- Critical theory at IR fixed pt.

[Witten '01]

- Deformation by double trace like op. \Leftrightarrow Change of bulk b.c.