Diphoton production in hadronic collisions

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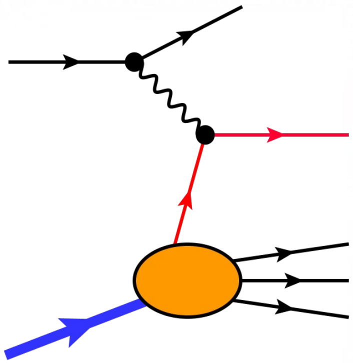
Outline of the talk

- Introduction of TMDs
- Drell-Yan lepton pair production and photon pair production
- The Sivers effect:
  Fit to data, Prediction for photon pairs
- Drell-Yan and Diphoton production at high q_T
- The double spin asymmetry A_{TT}

k_T-dependent Parton Distributions (TMDs)

Collinear PDFs $f_1(x,\mu), g_1(x,\mu), h_1(x,\mu)$

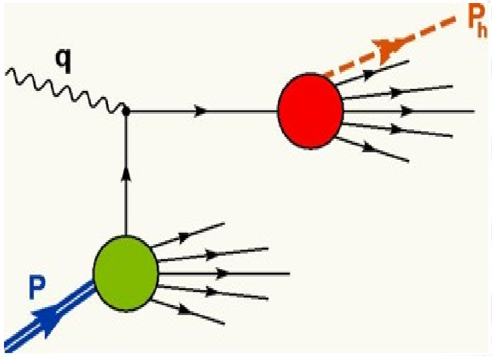


- **Theory well-understood,**
- **delivers a one-dimensional picture of nucleon structure**
- **Measurable in DIS (but not sensitive to transversity...)**

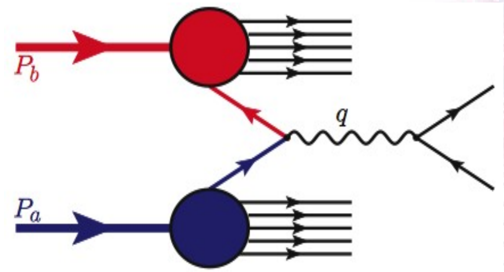
↕

TMDs (small transv. deviations):

- **measurable in semi-inclusive processes at small final state transverse momenta** $\Lambda_{QCD} \sim q_T \ll Q$
- **provides 3-dim. momentum picture**
- **Theory more complicated**



8 leading twist TMDs

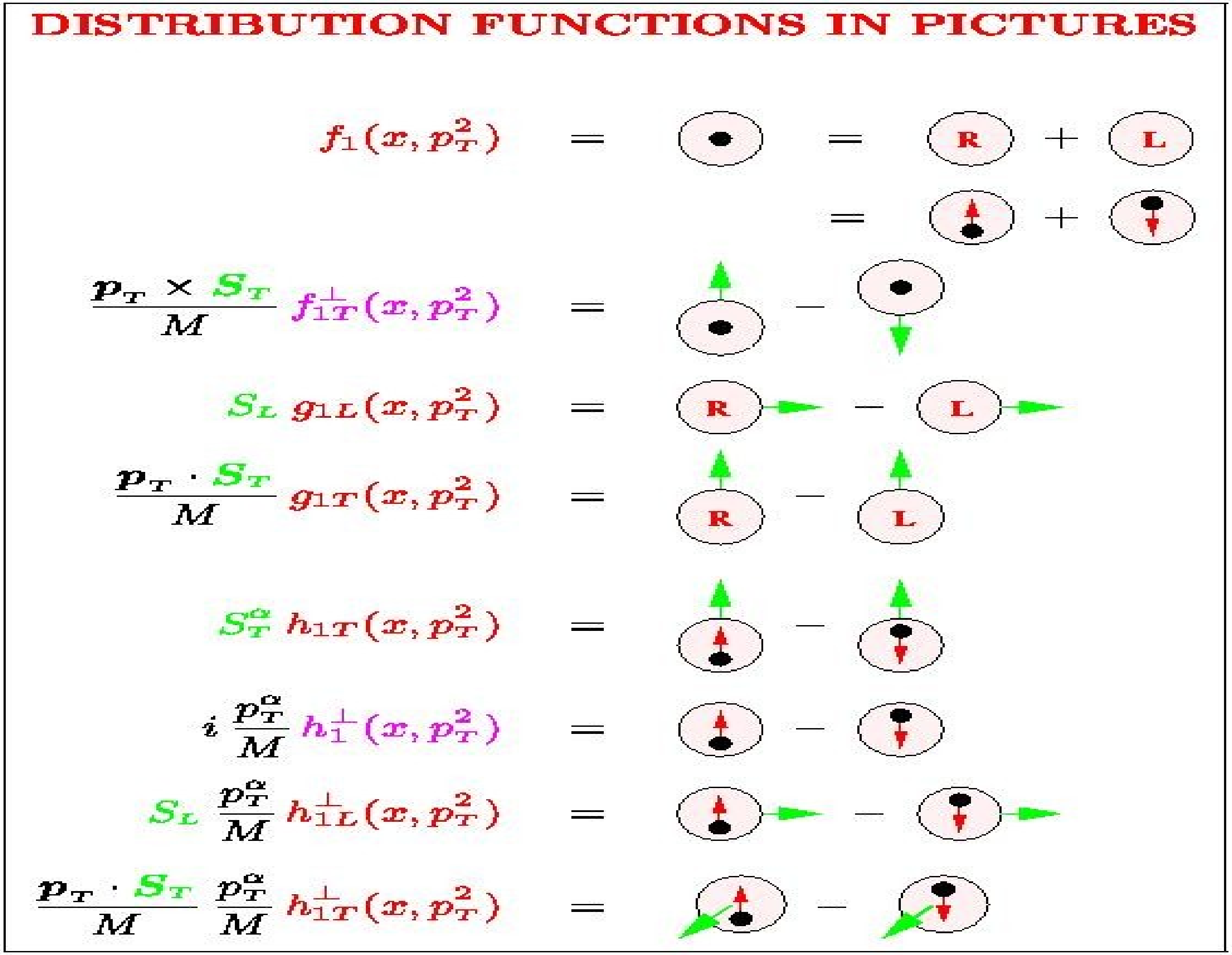


unpolarized: $(f_1\ ,\ f_{1T}^{\perp})(x,\vec{k}_T^2)$

longitudinally: $(g_{1L}\ ,\ g_{1T})$

transversely [chirally-odd]: $(h_1\ ,\ h_{1T}^{\perp}\ ,\ h_{1L}^{\perp}\ ,\ h_1^{\perp})$

Appear in SIDIS and DY !



"unpolarized" → f_1

"Sivers"

"helicity" → g_1

"wormgear"

"transversity" → h_1

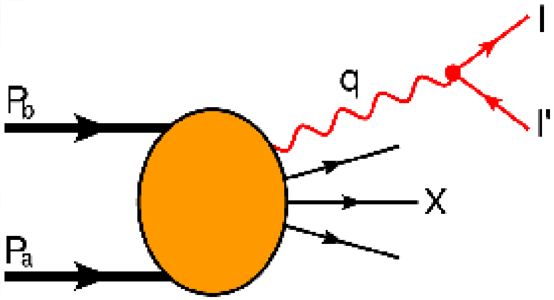
"Boer-Mulders"

"pretzelosity"

Sivers / Boer-Mulders ⟶ "naive" time-reversal odd (T-odd) ⟶ Single-Spin Asymmetries

The Drell-Yan process

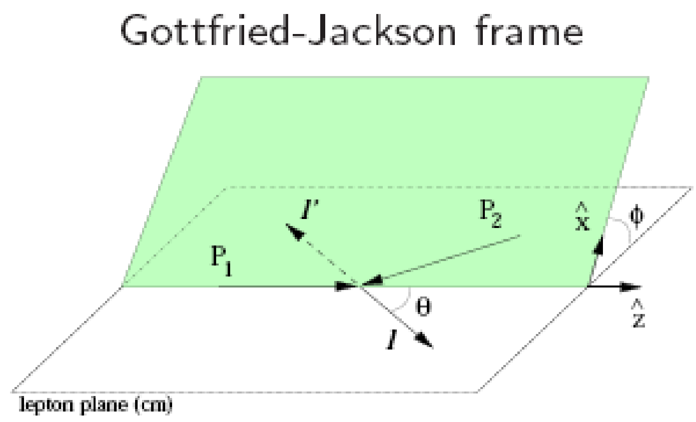
Kinematics (lepton pair produced by one decaying gauge boson):

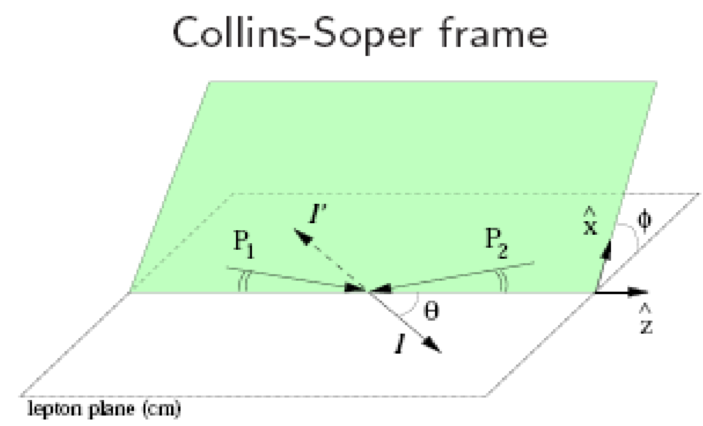


$$\frac{d\sigma}{d^4l\,d^4l'} = \frac{d\sigma}{d^4q\,d^4l} \propto \frac{\delta^+(l^2)\delta^+((q-l)^2)}{4F} \sum_X |M|^2 \delta^{(4)}(P_a + P_b - q - P_X)$$

Disentangling the δ-functions → Dilepton rest frame

Gottfried-Jackson frame and Collins-Soper frame:





Lepton angles:

$$d^4l \rightarrow d\Omega = d\phi\, d\cos\theta$$

Diff. CS including angular dependences:

$$\frac{d^6\sigma}{d^4q\,d\Omega} = 2\frac{d^6\sigma}{dy\,dQ^2\,d^2\vec{q}_T\,d\Omega}$$

Angular structure functions

Separation of the leptonic part (generated by one photon):

$$\frac{d\sigma}{d^4q\,d\Omega} \propto L_{\mu\nu} W^{\mu\nu}$$

with: $L_{\mu\nu} = 4\Big(l_\mu l'_\nu + l_\nu l'_\mu - \frac{Q^2}{2} g_{\mu\nu}\Big)$ → **Limited number of structure function**

Hadronic Tensor:

$$W^{\mu\nu}(P_a, S_a; P_b, S_b; q) = \int \frac{d^4x}{(2\pi)^4}\, e^{iq\cdot x} \langle a, b | J^\mu(0) J^\nu(x) | a, b\rangle$$

Parameterization constraint by current conservation, hermiticity and parity

Decomposition into 4 + 8 +8 + 28 = 48 structure functions $F(x_a, x_b, q_T^2, Q^2)$

[Arnold, Metz, M.S., PRD 79, 034005] **e.g. unpolarized Drell-Yan**

$$\frac{d\sigma_{UU}}{dx_a\, dx_b\, d^2q_T\, d\Omega} = \frac{\alpha^2 s}{2Q^2 F}\Big((1+\cos^2\Theta) F_{UU}^1 + (1-\cos^2\Theta) F_{UU}^2 + \sin 2\Theta \cos\phi F_{UU}^{\cos\phi} + \sin^2\Theta \cos 2\phi F_{UU}^{\cos 2\phi}\Big)$$

Classification of structure functions helpful for data analysis

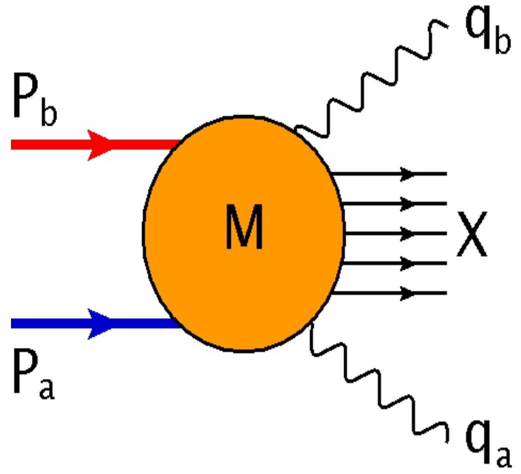
→ *Parton model*: 24 leading twist structure functions

$$
\begin{aligned}
\frac{d\sigma}{d^4q\,d\Omega} = \frac{\alpha_{\rm em}^2}{Fq^2}\{&((1+\cos^2\theta)F^1_{UU} + (1-\cos^2\theta)F^2_{UU} + \sin2\theta\cos\phi F^{\cos\phi}_{UU} + \sin^2\theta\cos2\phi F^{\cos2\phi}_{UU}) \\
&+ S_{aL}(\sin2\theta\sin\phi F^{\sin\phi}_{LU} + \sin^2\theta\sin2\phi F^{\sin2\phi}_{LU}) + S_{bL}(\sin2\theta\sin\phi F^{\sin\phi}_{UL} + \sin^2\theta\sin2\phi F^{\sin2\phi}_{UL}) \\
&+ |\vec{S}_{aT}|[\sin\phi_a((1+\cos^2\theta)F^1_{TU} + (1-\cos^2\theta)F^2_{TU} + \sin2\theta\cos\phi F^{\cos\phi}_{TU} + \sin^2\theta\cos2\phi F^{\cos2\phi}_{TU}) \\
&+ \cos\phi_a(\sin2\theta\sin\phi F^{\sin\phi}_{TU} + \sin^2\theta\sin2\phi F^{\sin2\phi}_{TU})] + |\vec{S}_{bT}|[\sin\phi_b((1+\cos^2\theta)F^1_{UT} + (1-\cos^2\theta)F^2_{UT} \\
&+ \sin2\theta\cos\phi F^{\cos\phi}_{UT} + \sin^2\theta\cos2\phi F^{\cos2\phi}_{UT}) + \cos\phi_b(\sin2\theta\sin\phi F^{\sin\phi}_{UT} + \sin^2\theta\sin2\phi F^{\sin2\phi}_{UT})] \\
&+ S_{aL}S_{bL}((1+\cos^2\theta)F^1_{LL} + (1-\cos^2\theta)F^2_{LL} + \sin2\theta\cos\phi F^{\cos\phi}_{LL} + \sin^2\theta\cos2\phi F^{\cos2\phi}_{LL}) \\
&+ S_{aL}|\vec{S}_{bT}|[\cos\phi_b((1+\cos^2\theta)F^1_{LT} + (1-\cos^2\theta)F^2_{LT} + \sin2\theta\cos\phi F^{\cos\phi}_{LT} + \sin^2\theta\cos2\phi F^{\cos2\phi}_{LT}) \\
&+ \sin\phi_b(\sin2\theta\sin\phi F^{\sin\phi}_{LT} + \sin^2\theta\sin2\phi F^{\sin2\phi}_{LT})] + |\vec{S}_{aT}|S_{bL}[\cos\phi_a((1+\cos^2\theta)F^1_{TL} + (1-\cos^2\theta)F^2_{TL} \\
&+ \sin2\theta\cos\phi F^{\cos\phi}_{TL} + \sin^2\theta\cos2\phi F^{\cos2\phi}_{TL}) + \sin\phi_a(\sin2\theta\sin\phi F^{\sin\phi}_{TL} + \sin^2\theta\sin2\phi F^{\sin2\phi}_{TL})] \\
&+ |\vec{S}_{aT}||\vec{S}_{bT}|[\cos(\phi_a+\phi_b)((1+\cos^2\theta)F^1_{TT} + (1-\cos^2\theta)F^2_{TT} + \sin2\theta\cos\phi F^{\cos\phi}_{TT} + \sin^2\theta\cos2\phi F^{\cos2\phi}_{TT}) \\
&+ \cos(\phi_a-\phi_b)((1+\cos^2\theta)\bar{F}^1_{TT} + (1-\cos^2\theta)\bar{F}^2_{TT} + \sin2\theta\cos\phi \bar{F}^{\cos\phi}_{TT} + \sin^2\theta\cos2\phi \bar{F}^{\cos2\phi}_{TT}) \\
&+ \sin(\phi_a+\phi_b)(\sin2\theta\sin\phi F^{\sin\phi}_{TT} + \sin^2\theta\sin2\phi F^{\sin2\phi}_{TT}) \\
&+ \sin(\phi_a-\phi_b)(\sin2\theta\sin\phi \bar{F}^{\sin\phi}_{TT} + \sin^2\theta\sin2\phi \bar{F}^{\sin2\phi}_{TT})]\}.
\end{aligned}
$$

: Leading twist in TMD – parton model $F = F(y, Q^2, q_T^2)$

- p – p scattering: relations between structure functions, e.g. $A_{UT} = -A_{TU}$
- p – _ scattering: no double polarization
- Integration over CS-angles: 8 structure functions survive

Diphoton production



Two highly energetic real photons produced with

$$q \equiv q_a + q_b$$

$$\frac{d\sigma}{d^4q_a\, d^4q_b} = \frac{d\sigma}{d^4q\, d^4q_a} \propto \frac{\delta^+(q_a^2)\delta^+((q-q_a)^2)}{2\times 4F} \sum_X |M|^2 \delta^{(4)}(P_a + P_b - q - P_X)$$

Convenient choice: Diphoton rest frame → **Collins-Soper frame** $\frac{d^6\sigma}{dy\, dQ^2\, d^2\vec{q}_T d\Omega_a}$

Unfortunately: No separation into ***hadronic – photonic*** parts possible!
→ *all* angular modulations are allowed, in principle.

$$\frac{d^6\sigma}{dy\, dQ^2\, d^2\vec{q}_T\, d\Omega_a} = \sum_{l=0}^{\infty} \sum_{m=-l}^{l} C_{lm}(y, Q^2, q_T^2)\, Y_{lm}(\Omega_a)$$

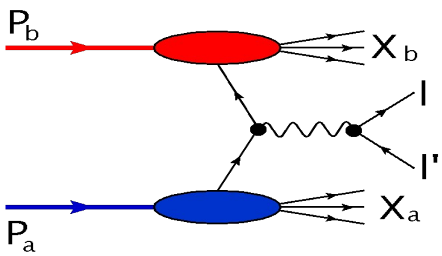
$$C_{00} = \frac{d^4\sigma}{dy\, dQ^2\, d^2q_T}, \ldots$$

However, we can calculate the cross section in the parton model.

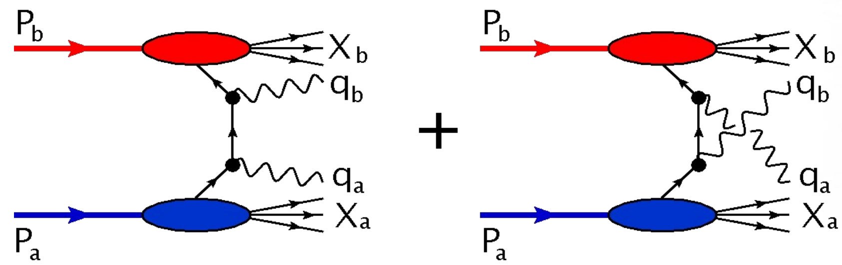
TMD tree-level formalism

Parton model tree-level at $O(\alpha_s^0)$:

Drell-Yan dilepton production:



Diphoton production:



Only relevant at very small q_T: $\Lambda_{QCD} \sim q_T \ll Q$

$$\left(\frac{d\sigma}{d^4q\, d\Omega}\right) \propto \int d^2k_{aT} \int d^2k_{bT}\, \delta^{(2)}(\vec{k}_{aT} + \vec{k}_{bT} - \vec{q}_T)\, \mathrm{Tr}\left[\Phi(x_a, \vec{k}_{aT})\, H(x_a, x_b, q_a, q_b)\, \bar{\Phi}(x_b, \vec{k}_{bT})\, H^\dagger\right] + \mathcal{O}(\tfrac{M}{Q})$$

k_T - correlator: $$\Phi_{ij}(x, \vec{k}_T) = \int \frac{dz^-\, d^2z_T}{(2\pi)^2}\, \mathrm{e}^{ik\cdot z} \langle P, S|\, \bar{q}_j(0)\, \mathcal{W}^{?/DY}[0\,;\, z]\, q_j(z)\, |P, S\rangle\Big|_{z^+=0}$$

→ can be parameterized in terms of TMDs according to quark / nucleon spin

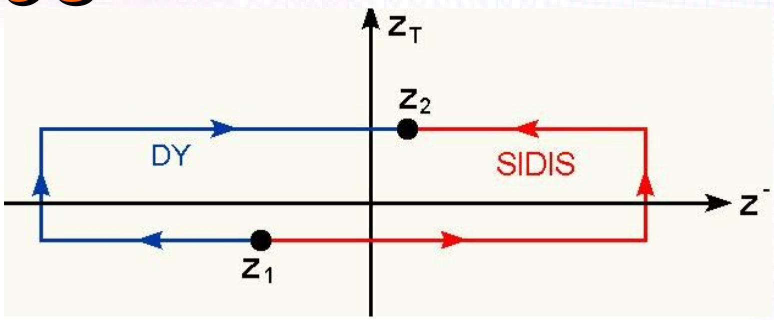
Main result of the TMD tree-level formalism:

$$\left(\frac{d^6\sigma^{hh\to\gamma\gamma X}}{dy\, dQ^2\, d^2q_T\, d\Omega}\right)(\Lambda \sim q_T \ll Q) = \frac{2}{\sin^2\theta}\left(\frac{d\sigma^{hh\to l^+l^-X}}{dy\, dQ^2\, d^2q_T\, d\Omega}\right)(\Lambda \sim q_T \ll Q\,|\, e_q \to e_q^2)$$

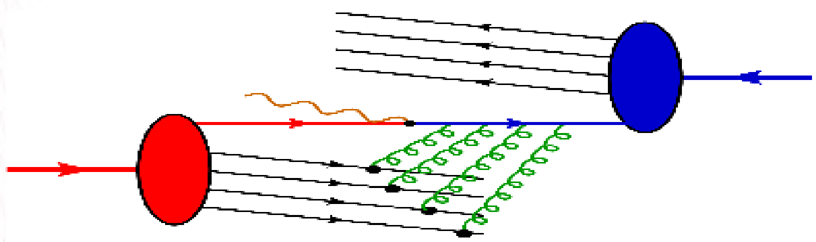
Wilson lines

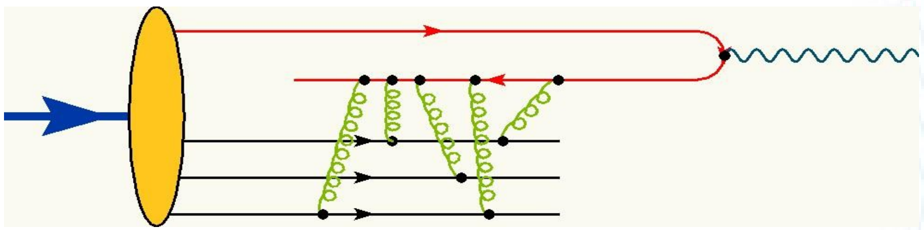
Wilson line process-dependent in DY/SIDIS:

$$\mathcal{W}[z_1; z_2] = \mathcal{P}\mathrm{e}^{-ig\int_{z_1}^{z_2} ds\cdot A(s)}$$

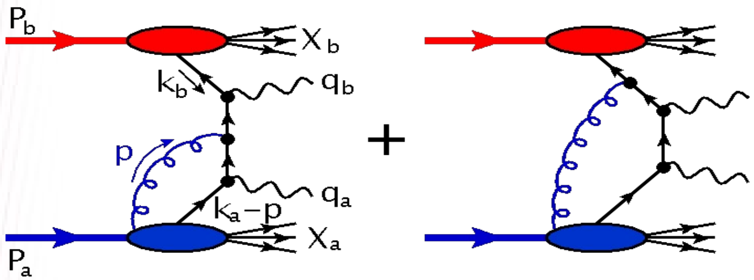


Physics: Initial / Final state interactions





Wilson line in diphoton production:



+crossed

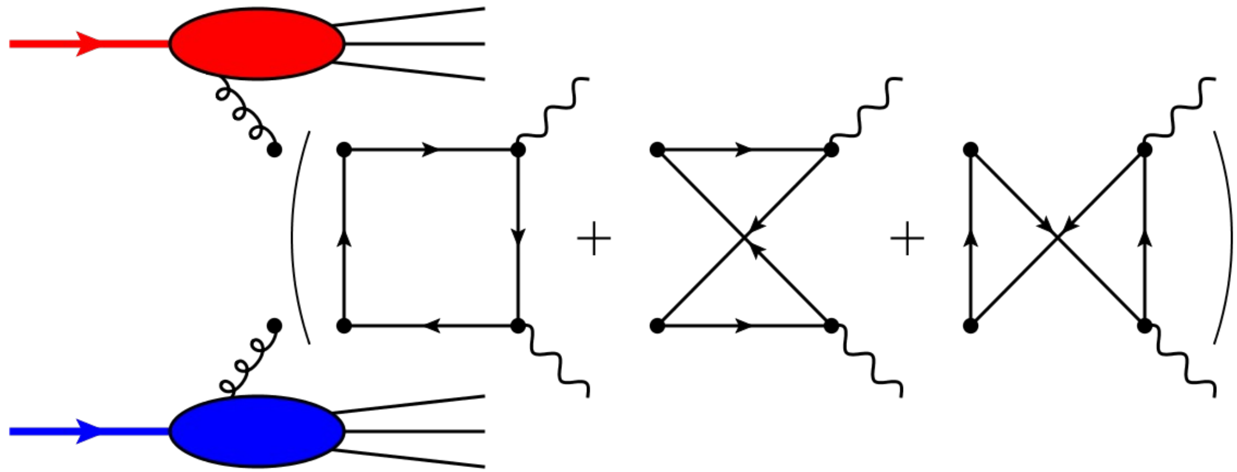
Check for $A^+,\ A_T^i(z^- = -\infty)$

Diagrams topologically different to DY, *but* cancellations between diagrams

$$\mathcal{W}^{\gamma\gamma}[0;z]\Big|_{z^+=0} = 1 - ig\int_0^{-\infty} d\lambda\, A^+(\lambda n) - ig\int_{0_T}^{z_T} d\vec{y}_T\cdot\vec{A}_T(-\infty,0,\vec{y}_T) - ig\int_{-\infty}^{0} d\lambda\, A^+(\lambda n + z_T) + \mathcal{O}(g^2) = \mathcal{W}^{DY}[0;z]\Big|_{z^+=0}$$

Gluon TMDs

Unique feature of diphoton production → direct sensitivity to gluon TMDs at O($_s^2$)



- Current conservation → ”boxes” are IR – and UV-finite → effectively ”tree-level”
- Large gluon distribution at smaller x compensates $_s^2$ suppression → competing process to quark – antiquark generated diphotons
- Polarized gluon TMDs at smaller x → possible contributions feasible at RHIC
- Background process for Higgs production at LHC → possible information on unpolarized gluon TMDs from LHC data

The Sivers effect

k_T – correlator for unpolarized quarks:

$$\frac{1}{2}\mathrm{Tr}[\Phi(x,\vec{k}_T)\,\gamma^+] = f_1(x,\vec{k}_T^2) - \frac{\epsilon_T^{ij}\,k_T^i\,S_T^j}{M}\,f_{1T}^\perp(x,\vec{k}_T^2)$$

Sivers function → time-reversal odd → sign switch:

$$f_{1T}^\perp\Big|_{DIS} = -f_{1T}^\perp\Big|_{DY}$$

Can be determined from SIDIS data of a transverse target SSA (HERMES, COMPASS):

$$A_{UT}^{Siv} \sim \frac{f_{1T}^\perp \otimes D_1}{f_1 \otimes D_1}$$

k_T – deconvolution through Gaussian ansatz

$$f(x,\vec{k}_T^2) = f(x)\exp\left[-\vec{k}_T^2/\langle k_T^2\rangle\right]$$

Fit of the Sivers function to data:

[Anselmino et al., EPJA 39, 89],

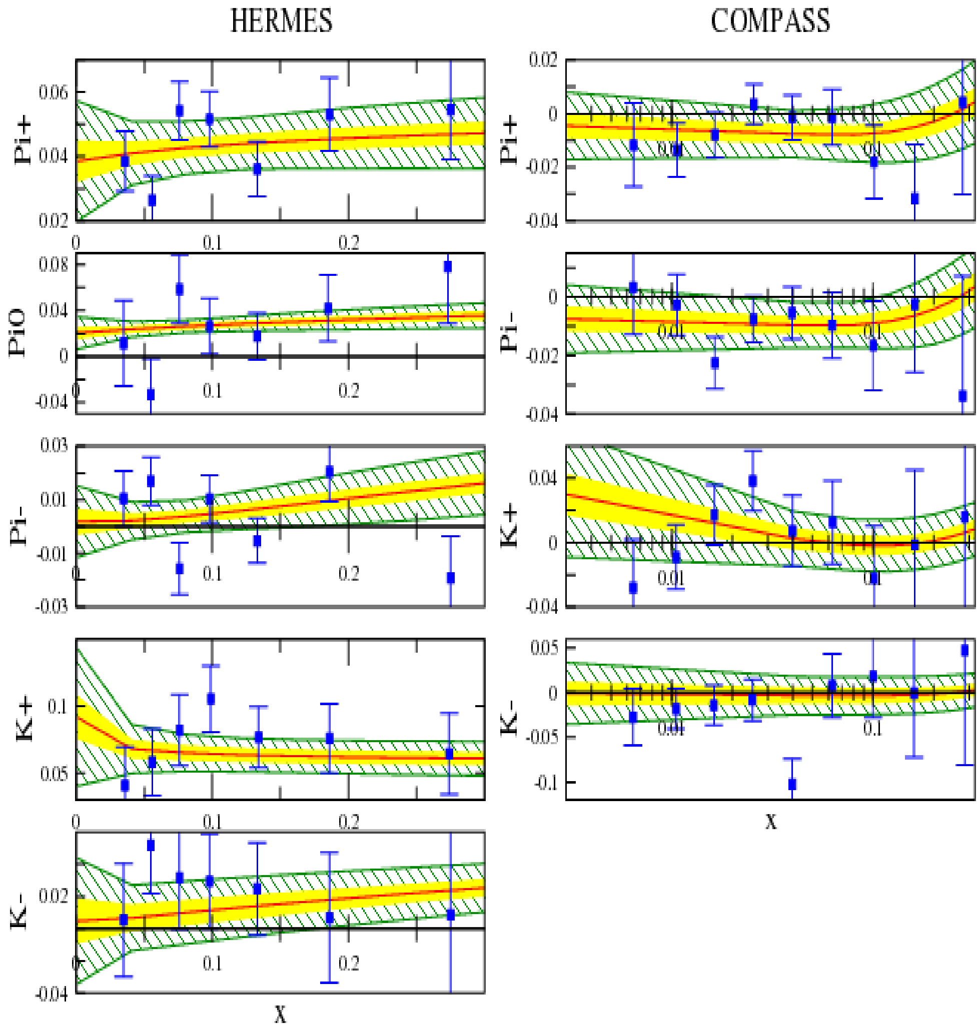
[Schweitzer, M.S., 0805.2137 and in prep.]

$$f_{1T}^{\perp,q}(x) = A^q\,f_1^q(x)$$

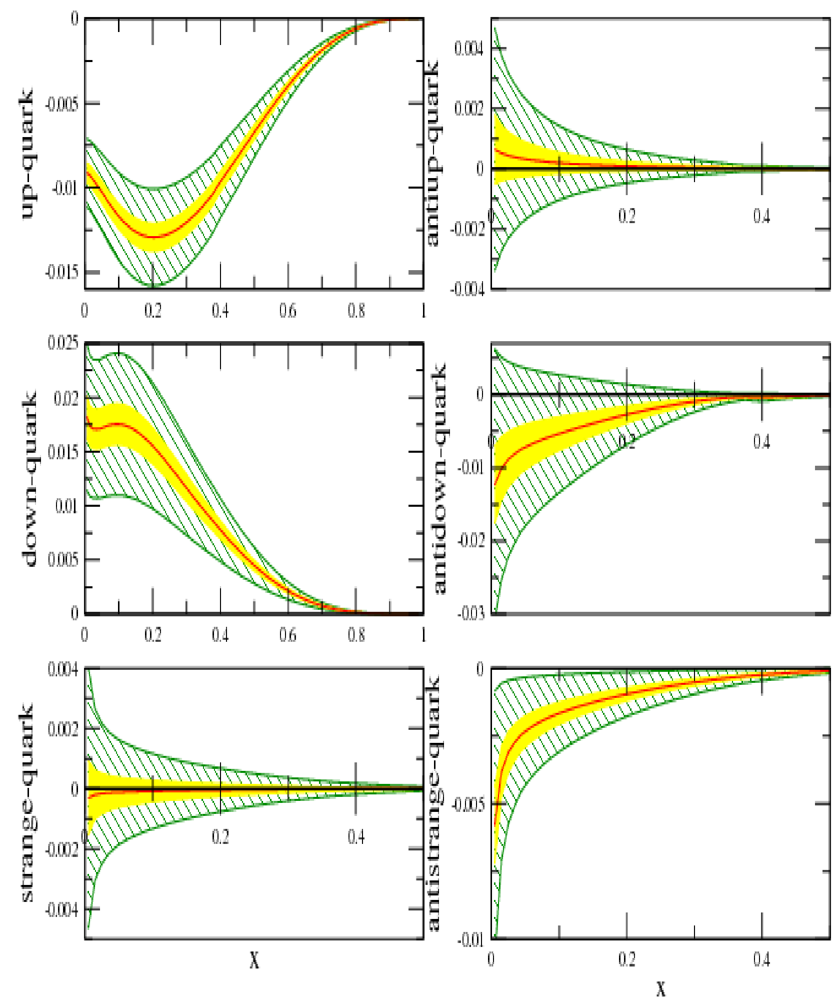
- non-zero sea-quark Sivers functions.
- Take into account finalized HERMES proton data and COMPASS deuteron data
- small statistical errors, χ^2 / d.o.f. ~ 1.07

- u- and d-Sivers roughly equal, but opposite sign
- Fits not constraint for x > 0.4...
  → (future) Jlab data, also COMPASS proton data

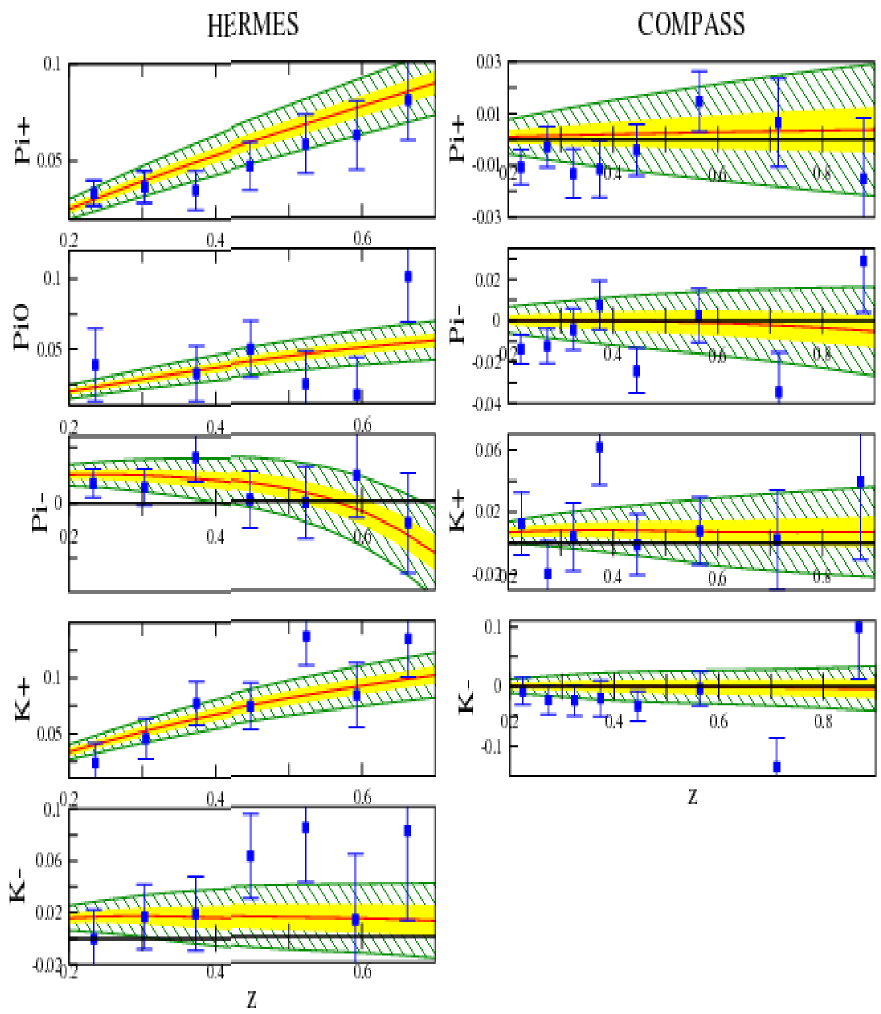
The Sivers Asymmetry plotted vs. x



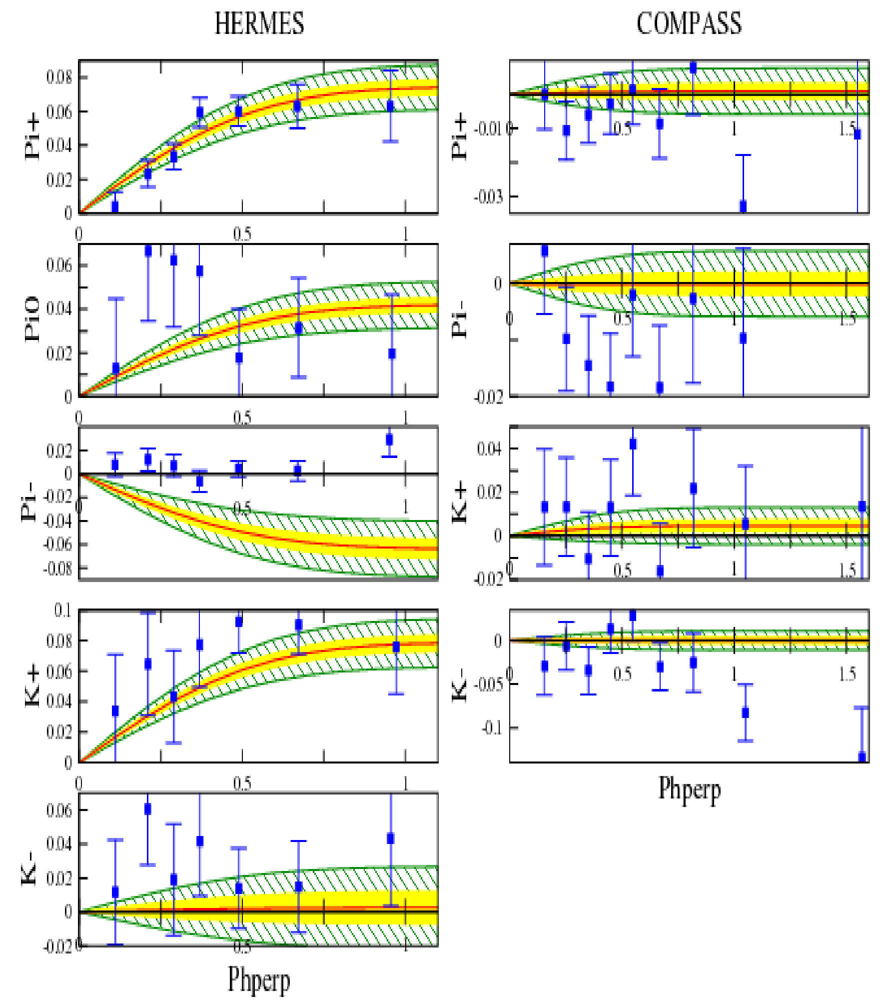
First transverse Moment of Sivers functions



The Sivers Asymmetry plotted vs. z



The Sivers Asymmetry plotted vs. Phperp



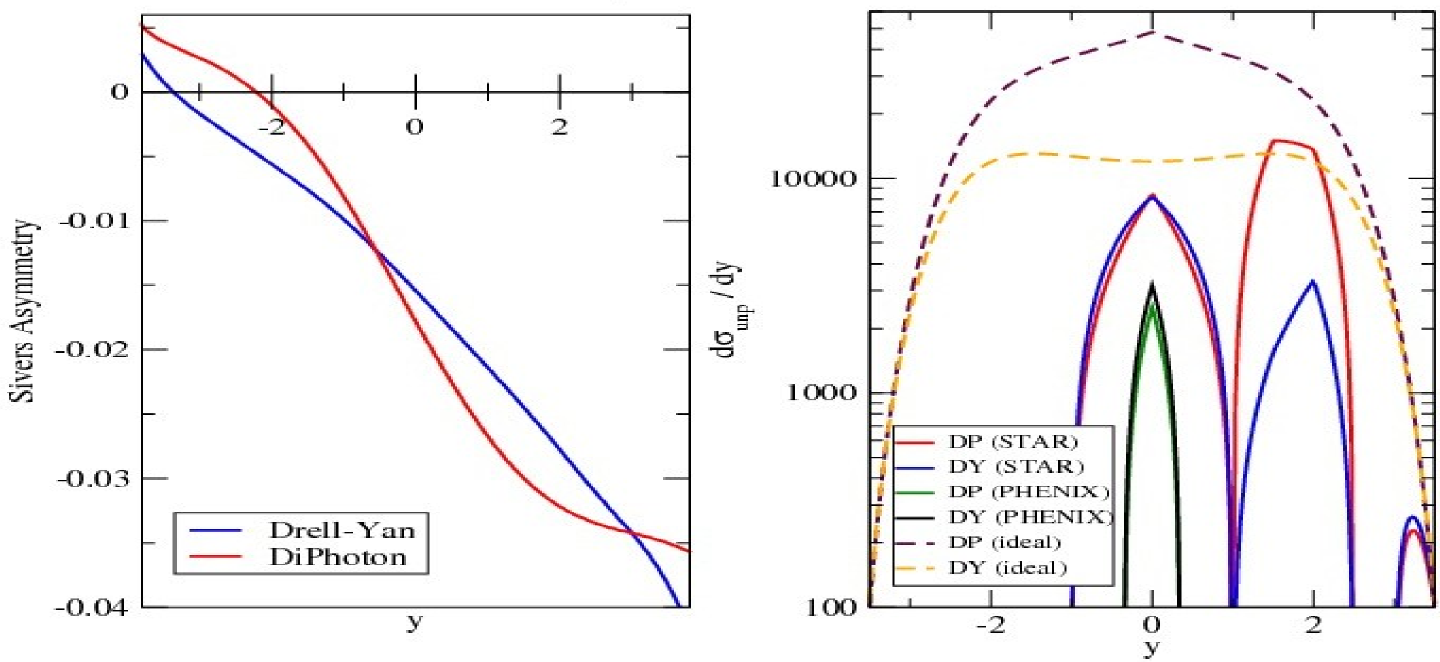
Sivers effect in photon pair production

$$\int_0^{2\pi} d\phi \, \frac{d\sigma_{TU}^{DP/DY}}{d^4q\, d\Omega} = \frac{\alpha^2}{2SQ^2}|\vec{S}_{aT}|\sin\phi_a \left[\frac{2}{\sin^2\theta}\right](1+\cos^2\theta)F_{TU}^{DP/DY} + \mathcal{O}(M/Q)$$

$$F_{TU}^{DP/DY} = -\sum_{q,\bar{q}} e_q^{4/2}\frac{1}{N_c}\int d^2k_{aT}\int d^2k_{bT}\,\delta^{(2)}(\vec{k}_{aT}+\vec{k}_{bT}-\vec{q}_T)\,\frac{\vec{q}_T\cdot\vec{k}_{aT}}{|\vec{q}_T|M}\, f_{1T}^{\perp,q}(x_a,\vec{k}_{aT}^2)\, f_1^{\bar{q}}(x_b,\vec{k}_{bT}^2)$$

Sivers Asymmetry vs. pair rapidity $y = (\eta_a + \eta_b)/2$

Bins[GeV]: $4 < Q < 10$, $0 < q_T < 1$, $|\eta| < 1$ and $3 < \eta < 4$ (STAR), $|\eta| < 0.35$ (PHENIX)



Sivers Asymmetry roughly equal in DY and DP

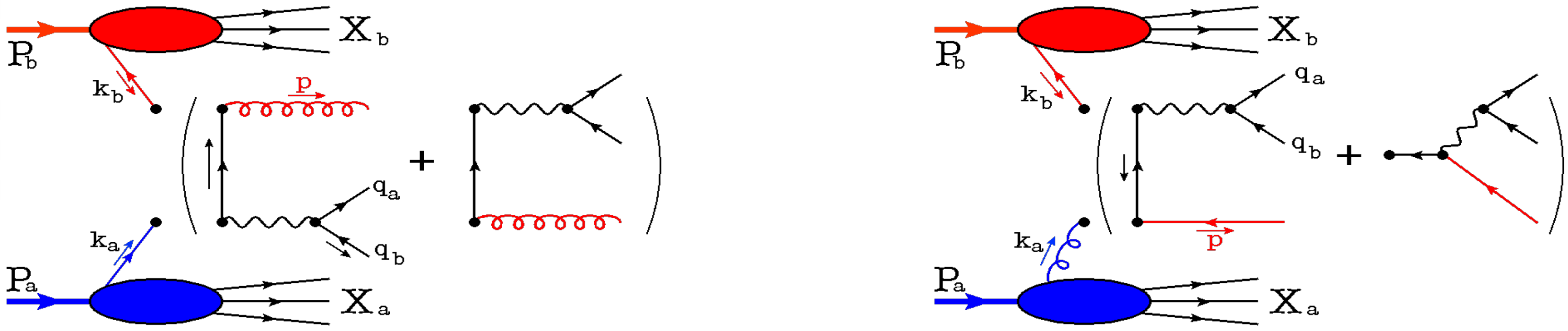
Photon pair production rate up to 5 times larger for large rapidity differences

$e_q^2 \rightarrow e_q^4$ u-quark dominance

Rapidity enhancement seems to cancel in SSA

High - q_T behaviour

At large $q_T \sim Q \rightarrow$ transverse momentum generated by gluon radiation



Unpolarized angular dependencies in Drell-Yan:

$$\frac{d\sigma_{UU}}{dx_a\,dx_b\,d^2q_T\,d\Omega} = \frac{\alpha^2 s}{2Q^2 F}\Big((1+\cos^2\Theta)F^1_{UU} + (1-\cos^2\Theta)F^2_{UU} + \sin 2\Theta\cos\phi F^{\cos\phi}_{UU} + \sin^2\Theta\cos 2\phi F^{\cos 2\phi}_{UU}\Big)$$

Collinear parton model applicable [Boer, Vogelsang, PRD74, 014004]

$$\frac{F^i}{x_a x_b} \sim \int\frac{d\xi_a}{\xi_a}\int\frac{d\xi_b}{\xi_b}\,\delta\Big((\xi_a - x_a)(\xi_b - x_b) - \frac{q_T^2}{s}\Big)\sum_{q,\bar{q}} e_q^2\Big(f_1^q(\xi_a)f_1^{\bar{q}}(\xi_b)\hat{F}^i_{q\bar{q}} + f_1^q(\xi_a)f_1^g(\xi_b)\hat{F}^i_{qg} + f_1^g(\xi_a)f_1^{\bar{q}}(\xi_b)\hat{F}^i_{g\bar{q}}\Big)$$

Partonic structure functions automatically obey angular decomposition

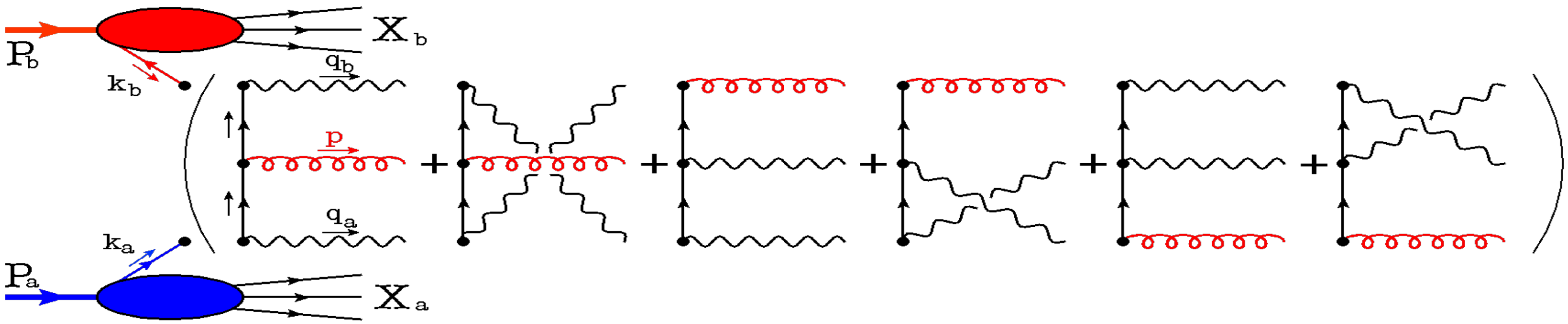
Lam-Tung relation in pQCD $\quad F^2_{UU} = 2F^{\cos 2\phi}_{UU} + \mathcal{O}(\alpha_s^2)$

Similar to Callan-Gross relation in DIS

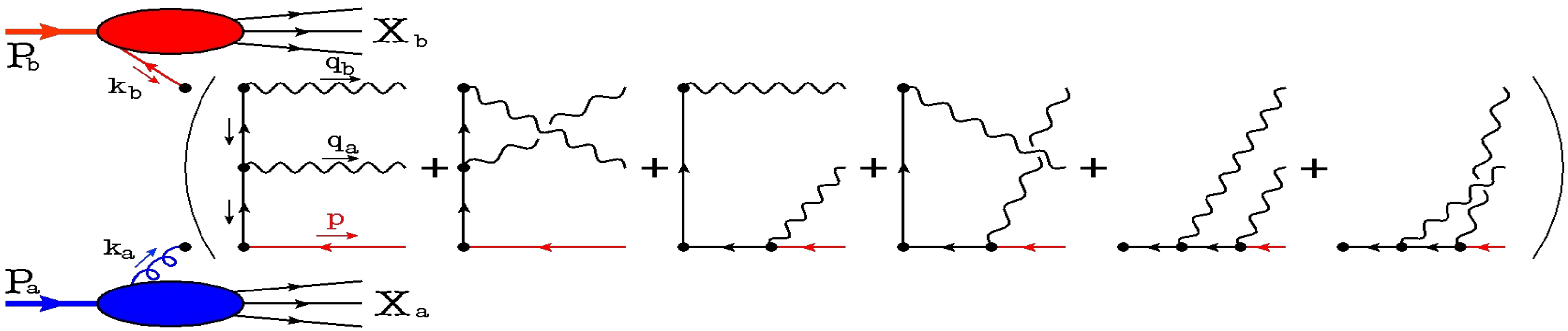
High - q_T of the photon pair

Same strategy as for DY:

quark – antiquark scattering:



quark – gluon scattering:



However: No model-independent angular decomposition!

Diphoton angles enter the partonic cross section in numerator and denominator
→ All angular depedencies are allowed.

Analytical results

What happens if q_T becomes smaller? → Expansion in $1/q_T$...

Drell-Yan:

$$d\sigma_{UU} \sim \left((1+\cos^2\Theta)F^1_{UU} + (1-\cos^2\Theta)F^2_{UU} + \sin 2\Theta\cos\phi F^{\cos\phi}_{UU} + \sin^2\Theta\cos 2\phi F^{\cos 2\phi}_{UU}\right)$$

Order $1/q_T^{\,2}$:

$$F^1_{UU} \propto \frac{\alpha_s}{q_T^2}\left[-C_F(2\ln\frac{q_T^2}{Q^2}+3)q(x_1)\bar{q}(x_2) + q(x_1)(P_{qq}\otimes\bar{q} + P_{qg}\otimes g)(x_2) + \{x_1 \leftrightarrow x_2\}\right]$$

Order $1/q_T$:

$$F^{\cos\phi}_{UU} \propto \frac{\alpha_s}{q_T}\left[q(x_1)(\tilde{P}_{qq}\otimes\bar{q} + \tilde{P}_{qg}\otimes g)(x_2) - \{x_1 \leftrightarrow x_2\}\right]$$

Order $1/q_T^{\,0}$:

$$F^2_{UU} = 2F^{\cos 2\phi}_{UU} = -C_F(2\ln\frac{q_T^2}{Q^2}+3)q(x_1)\bar{q}(x_2) + q(x_1)(P_{qq}\otimes\bar{q} + P'_{qg}\otimes\bar{q})(x_2) + \{x_1 \leftrightarrow x_2\}$$

DiPhoton production:

leading order follows "TMD - rule"

$$\sigma^{DP} = \frac{2}{\sin^2\theta}\sigma^{DY}(e_q \to e_q^2) + \mathcal{O}(1/q_T)$$

Order $1/q_T$:

$$\sigma^{DP} \sim (\sin 2\theta\cos\phi)\frac{\alpha_s}{q_T}\left[\frac{4}{\sin^4\theta}q(x_1)(\tilde{P}_{qq}\otimes\bar{q} + \tilde{P}_{qg}\otimes g)(x_2) + \frac{2}{\sin^2\theta}q(x_1)(\tilde{P}_{qq}\otimes\bar{q} + \tilde{P}^a_{qg}\otimes g)(x_2) - \{x_1 \leftrightarrow x_2\}\right]$$

Order $1/q_T^{\,0}$:

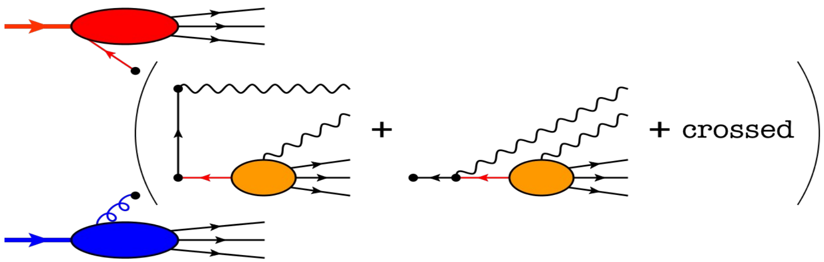
quark – antiquark contr. to diphoton production

$$\sigma^{DP}_{q\bar{q}} \propto \frac{(4-\cos^2\theta\sin^2\theta)\cos 2\phi + (3\sin^2\theta + 2\cos^2\theta)}{\sin^4\theta}F^{2,DY}_{UU,q\bar{q}}$$

quark – gluon scattering → collinearly divergent → need photon fragmentation function

Isolation of direct photons

Hide collinear divergence in photon fragmentation function:



- Potentially endangers TMD-factorization
- Photon FF unknown

Circumvent the problem → Isolation [Frixione PLB 429,369; Frixione, Vogelsang NPB 568, 60]

Define "cone" in rapidity – azimuthal angle space:

$$\mathcal{C}_\gamma(R_0) \equiv \left\{ (\eta,\phi) \,|\, \sqrt{(\eta-\eta_\gamma)^2 + (\phi-\phi_\gamma)^2} \le R_0 \right\}$$

1. "Traditional" Criterium: allow certain percentage of hadronic energy inside the cone

$$E_T(R_0) \le \epsilon q_{T\gamma}$$

- Boost-invariant criterium.
- Infra-red safe.
- Allows certain contribution from fragmentation photons.

2. "Improved" Criterium: dynamically generated cone $R < R_0$

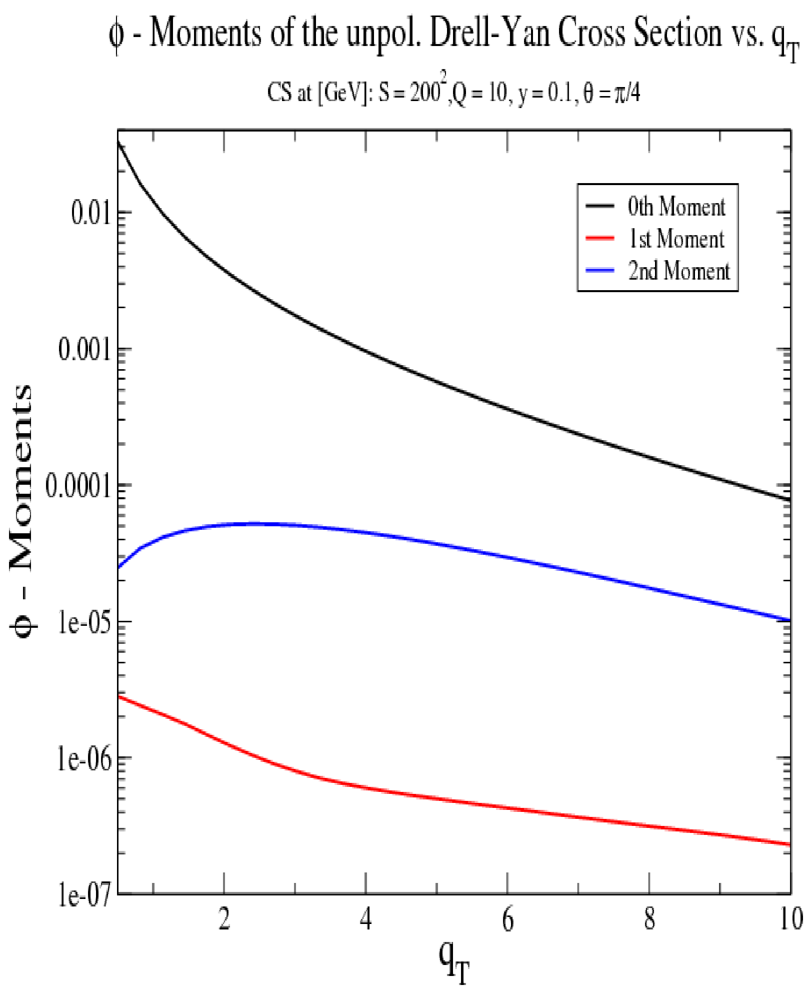
$$E_T(R) \le \epsilon_\gamma \, q_{T\gamma} \, f(R)$$

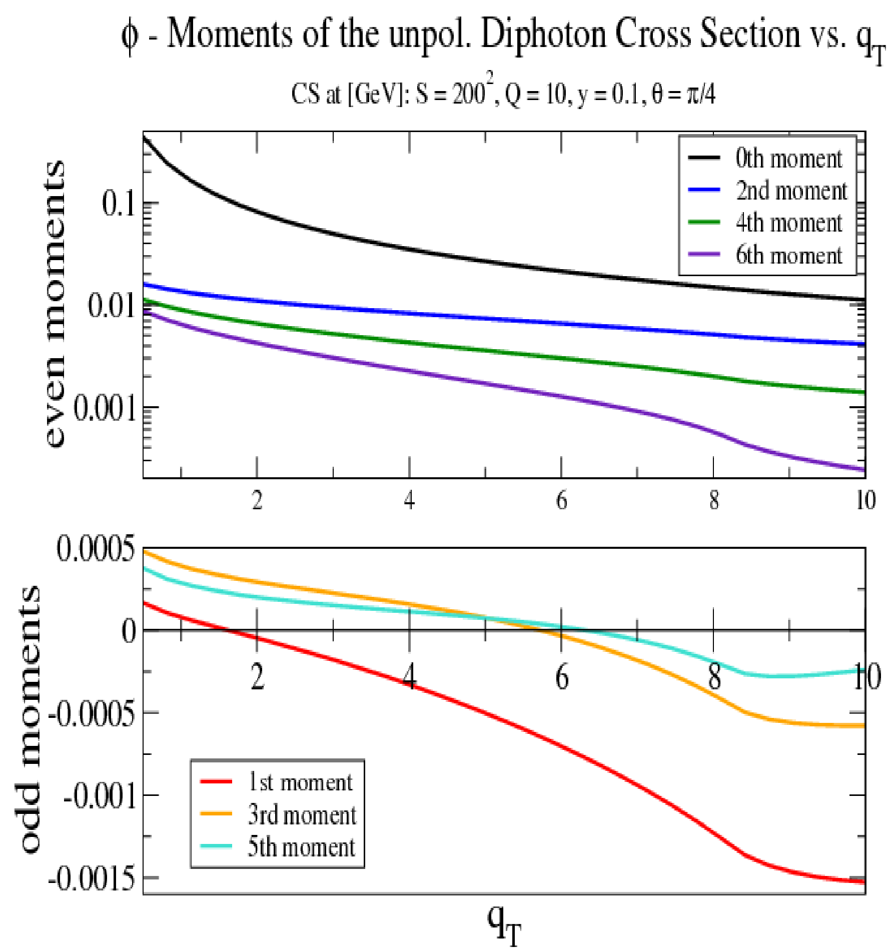
$$\lim_{R\to 0} f(R) = 0$$

- Boost-invariant criterium.
- Infra-red safe.
- Cuts out *all* fragmentation photons.
- Experimentally harder→ needs high resolution in η and ϕ.

Define phi moments:

$$\langle \cos(n\phi) \rangle = \int_0^{2\pi} d\phi \, \cos(n\phi) \frac{d\sigma}{dy\, dQ^2\, d^2q_T\, d\Omega}$$

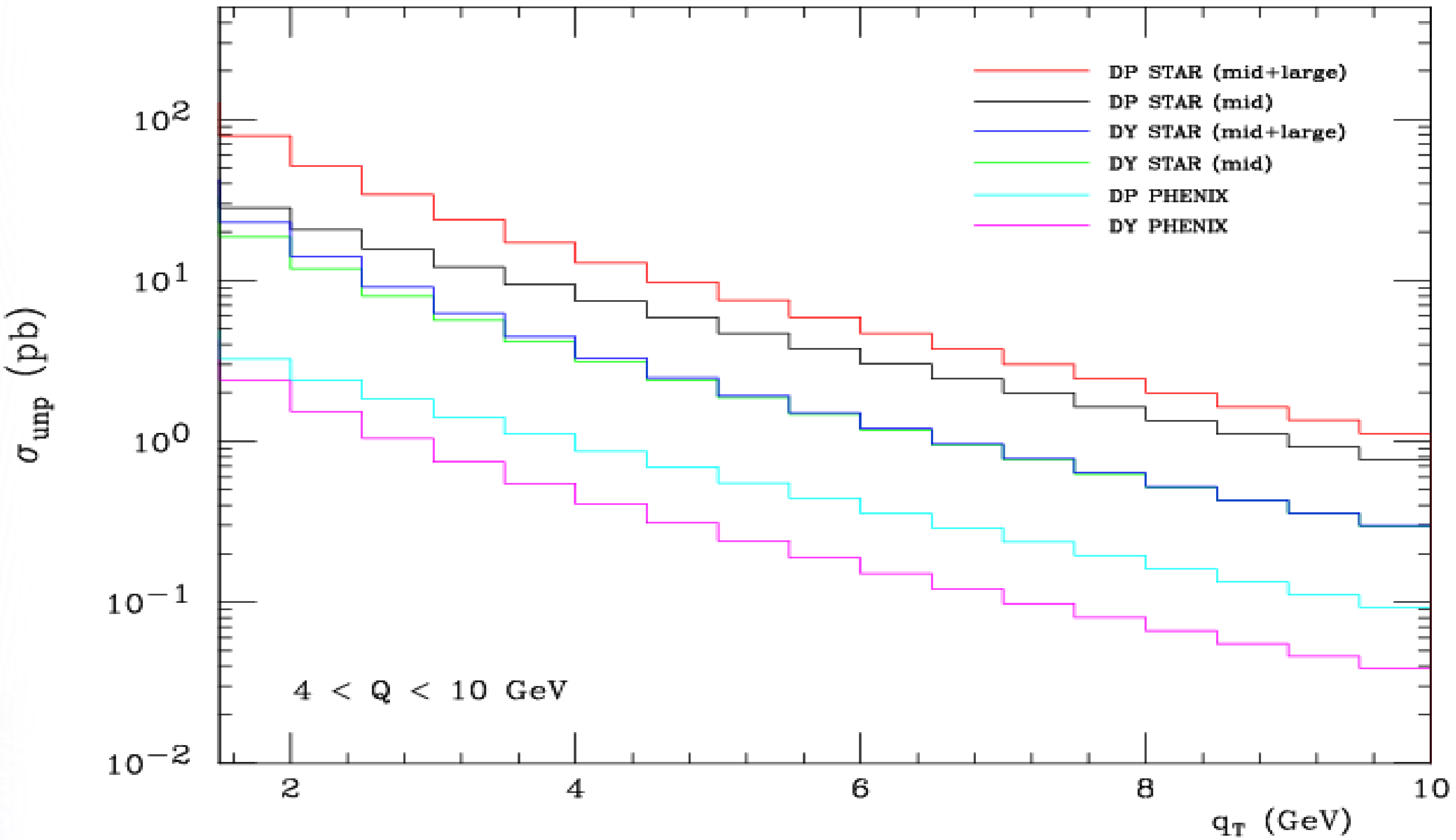




Numerical results

Predictions for the q_T-tail for STAR and PHENIX including isolation:

$$\sigma_{\rm unp} = \int_{\rm cuts} dy\, dQ^2\, dq_T\, d\varphi_q\, d\Omega\, \frac{d\sigma}{dy\, dQ^2\, dq_T\, d\varphi_q\, d\Omega}$$



Also at larger qT → Diphoton production rate about 5 - 10 times larger than Drell-Yan

The double spin asymmetry A_{TT}

The "golden" observable to measure the transversity distribution

$$S_T^i h_1^q(x) = S_T^i \Delta q(x) = \int \frac{dz^-}{2(2\pi)} e^{ixP^+z^-} \langle P, S_T |\, \bar{q}(0)\, i\sigma^{i+}\gamma_5\, [0;z^-]\, q(z^-)\, | P, S_T \rangle$$

- Non-hadronic final states (DY, Diphoton)
  → direct access to transversity, no input from other processes needed, however: production rates small
  → dream process: proton – antiproton DY in the valence region

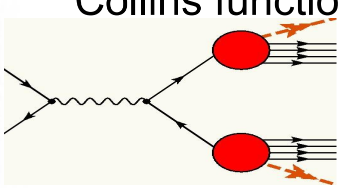
- Hadronic final states (single pion, single jet, dijets, ...)
  → high production rates, but small asymmetries (no gluon transversity)

So far: Extraction from combined e^+e^- and SIDIS data [Anselmino et al., PRD75,054032]

Collins effect in SIDIS (TMD-formalism)

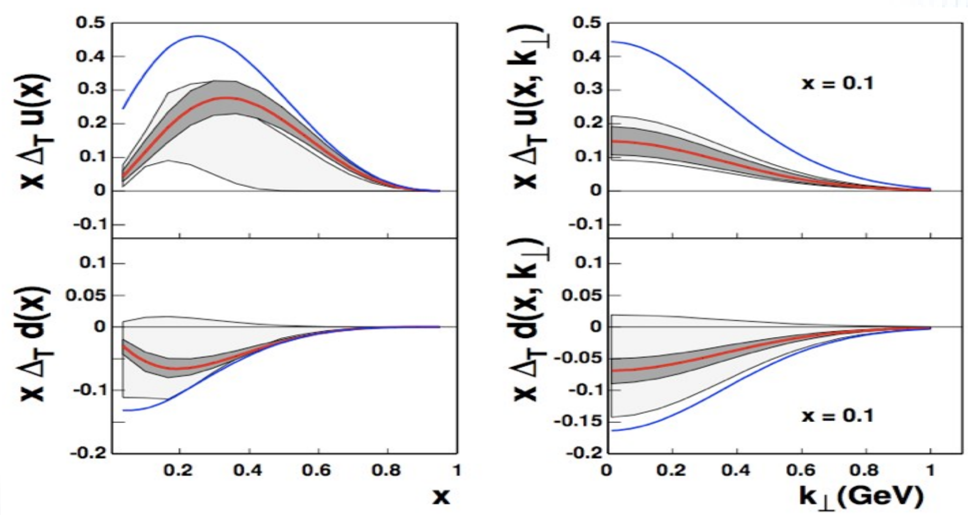
$$A_{UT}^{\sin(\phi+\phi_s)} \sim \frac{h_1 \otimes H_1^\perp}{f_1 \otimes D_1}$$

Collins function from BELLE e^+e^- data



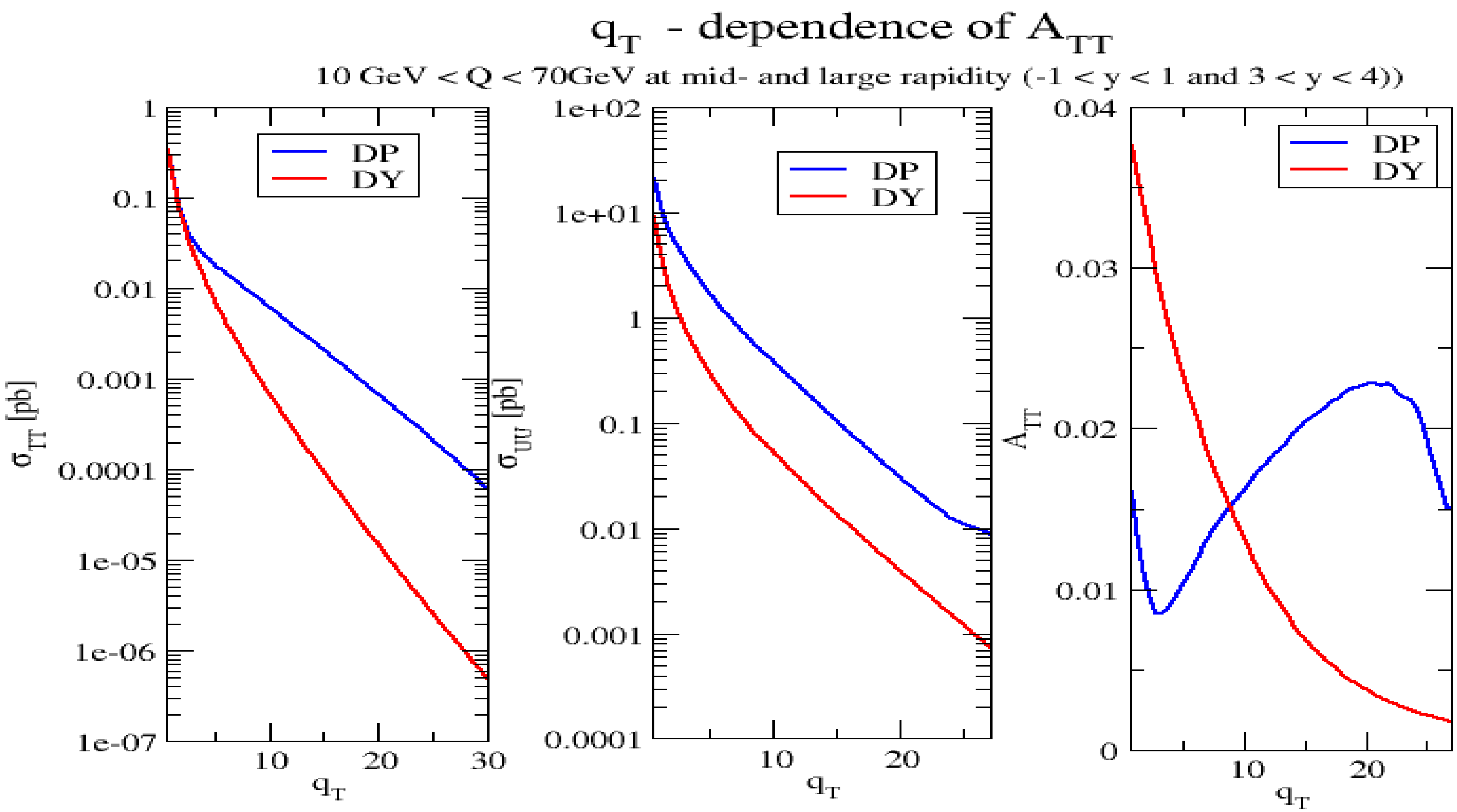
$$\sigma^{e^+e^-} \sim H_1^{\perp, q/H_1} \otimes H_1^{\perp, \bar{q}/H_2}$$

Extraction relies of Gaussian ansatz



A_{TT} in diphoton production

$$A_{TT} \sim \frac{\int h_1^q(x_1)\, h_1^{\bar{q}}(x_2) d\hat{\sigma}_{TT}}{\int f_1^q(x_1)\, f_1^{\bar{q}}(x_2)\, d\hat{\sigma}_{UU}}$$



- Saturation of Soffer bound assumed
  → implementation of transversity extraction in progress...
- Asymmetry is of the same size as for Drell-Yan (1 - 2 %)
- Event rate is larger at higher q_T

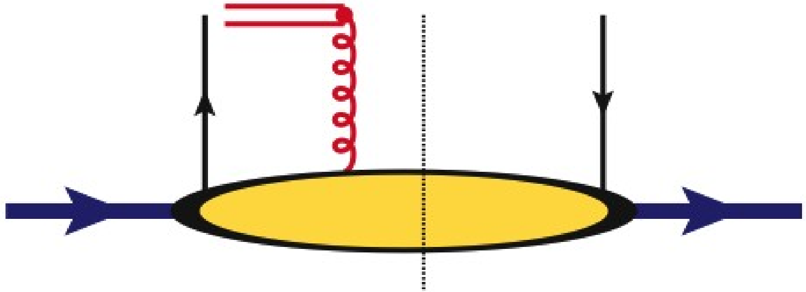
Summary:

- Drell-Yan cross section can be decomposed model-independently into angular structure function, not possible for photon pair production
- TMD-factorization at low q_T: Photon pair production similar to Drell-Yan
- Sivers effect similar in Photon pair production, but higher production rate → simultaneous measurement
- Collinear factorization at larger q_T: all azimuthal modulations possible for photon pair production in contrast to lepton pair production
- Expansion to smaller q_T: Azimuthal behaviour partly recovered → photon fragmentation or Isolation needed.
- Double Transverse Spin Asymmetry A_{TT} revisited: also higher production rate for the diphoton production

Model for the Sivers function

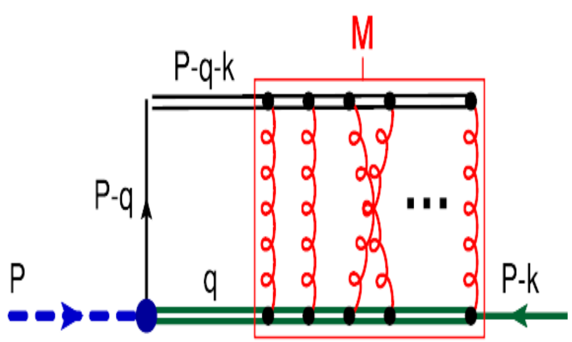
[Gamberg, MS, PLB 685, 95; in prep.]

- **Final State Interactions (Sivers-effect) mostly modeled by a One-Gluon Exchange:**



Example Diquark-spectator:
Sivers function ∝ α_s
Sivers effect at HERMES ≈ 5%
⇨ *α_s ≈ 0.2 - 0.3*

- **Eikonal methods: Non-perturbative, field-theoretic treatment of FSI.**



- **Models reflect factorization of the Sivers effect into FSI & Distortion of spatial transverse distribution**

$$f_{1T}^{\perp(1),q} \sim \mathcal{I} \otimes \frac{\partial}{\partial b_T^2} \mathcal{E}^q$$

***if:* Number of Spectators match in intermediate states**

- **Work in the diquark spectator framework (Lensing function identifyable)**

$$I^i(x, \vec{q}_T) = \int \frac{d^2 p_T}{(2\pi)^2} (2p_T - q_T)^i \Im M_{bc}^{ab}(|\vec{p}_T|) \Big((2\pi)^2 \delta^{ac} \delta^{(2)}(\vec{p}_T - \vec{q}_T) + \Re M_{da}^{cd}(|p_T - q_T|) \Big)$$

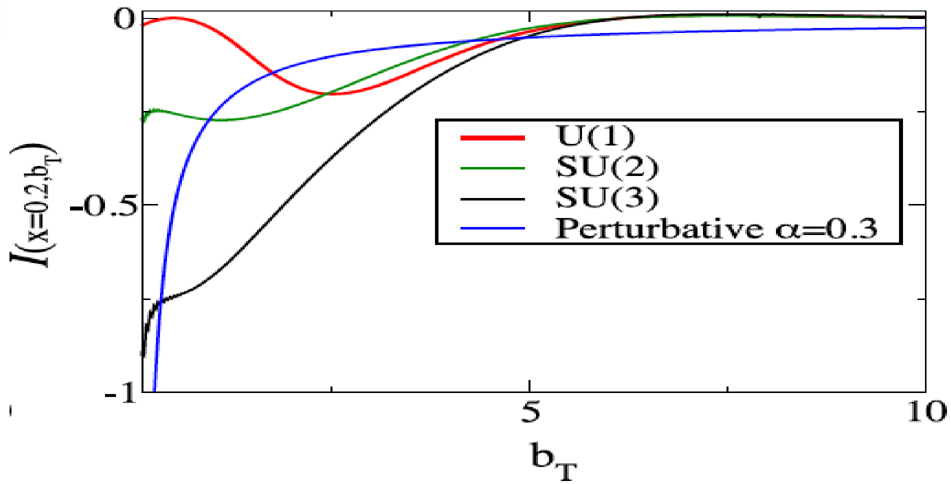
Scattering amplitude of two highly energetic particles at small momentum transfer:

<ins>Summation of gluons possible if:</ins>

1) Particles are eikonalized
   (not even an appr. for quark...)

2) Generalized Ladder Approximation

3) IR-finite gluon propagator
   → Dyson-Schwinger approach



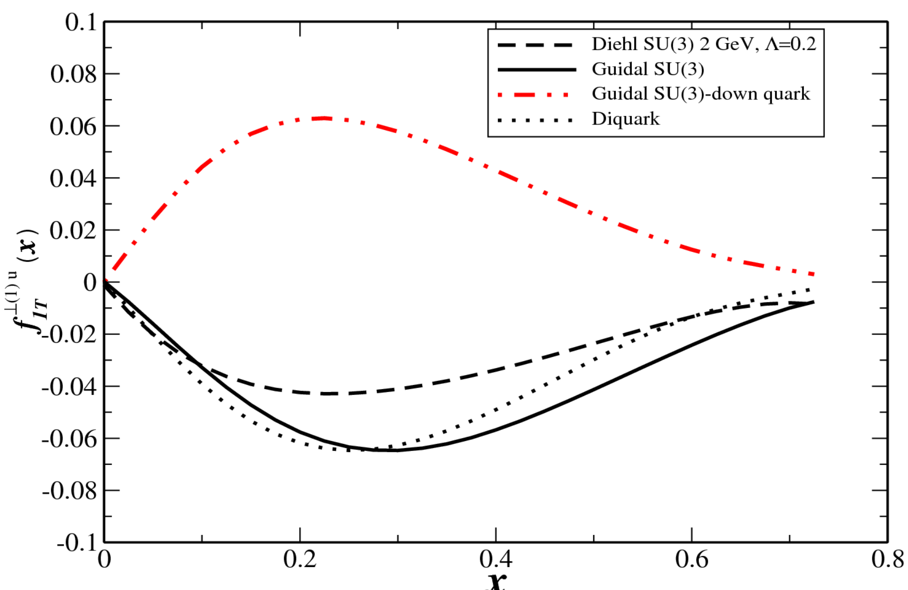
GPD parameterizations:

[Diehl et al., EPJ C39 (2005) 1-39]

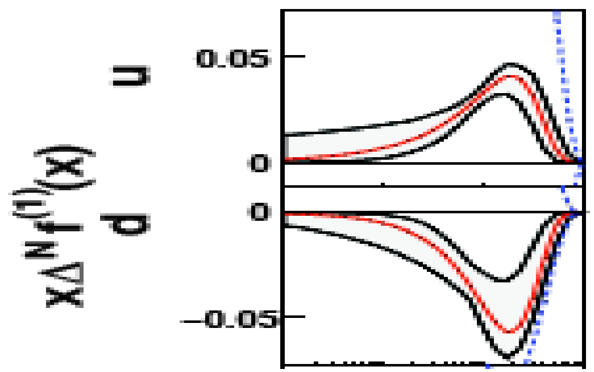
$$E_v^u(x,0,t) = (N^u \kappa^u x^{-\alpha}(1-x)^\beta) \mathrm{e}^{t g^u(x)}$$

[Guidal et al., PRD72, 054013]

$$E_v^q(x,0,t) = \frac{\kappa^q (1-x)^{\eta_q} q_v(x)}{\int_0^1 dx\,(1-x)^{\eta_q} q_v(x)}\, x^{-\alpha'(1-x)t}$$



Extraction by Torino-Group



$$\Delta^N f^{(1)}(x) = -f_{1T}^{\perp}(x)$$