

Antikaon-nucleon interaction and $\Lambda(1405)$ in chiral SU(3) dynamics



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2015, Feb. 19th 1

Contents



Introduction: experimental developments

- precise **kaonic hydrogen** measurement
- new $\pi\Sigma$ **spectra** from various reactions



$\bar{K}N$ - $\pi\Sigma$ interaction from chiral SU(3) dynamics

Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881 98 (2012)



Current status of $\Lambda(1405)$



Y. Ikeda



W. Weise

\bar{K} meson and $\bar{K}N$ interaction

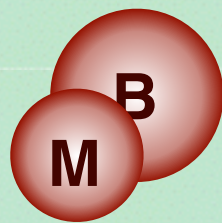
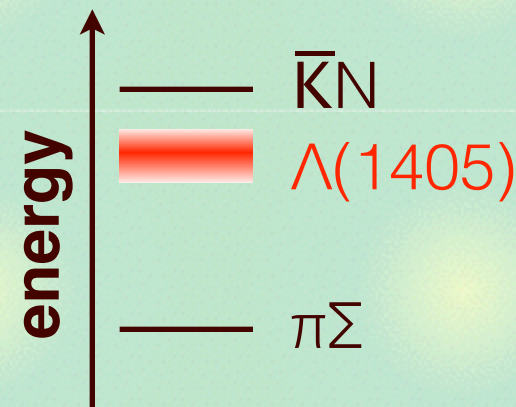
Two aspects of $K(\bar{K})$ meson

- **NG boson** of chiral $SU(3)_R \otimes SU(3)_L \rightarrow SU(3)_V$
- **massive** by strange quark: $m_K \sim 496$ MeV
- > **spontaneous/explicit** symmetry breaking

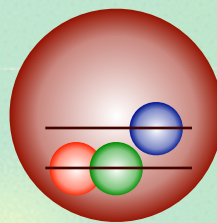
$\bar{K}N$ interaction ...

T. Hyodo, D. Jido, Prog. Part. Nucl. Phys. 67, 55 (2012)

- is coupled with $\pi\Sigma$ channel
- generates $\Lambda(1405)$ below threshold



molecule



three-quark

- is fundamental building block for \bar{K} -nuclei, \bar{K} in medium, ...₃

\bar{K} in nuclei

$\bar{K}N$ interaction

- strong attraction
- no repulsive core?

	$l=0$	$l=1$
NN	deuteron (2 MeV)	attractive
$\bar{K}N$	$\Lambda(1405)$ (15-30 MeV)	attractive

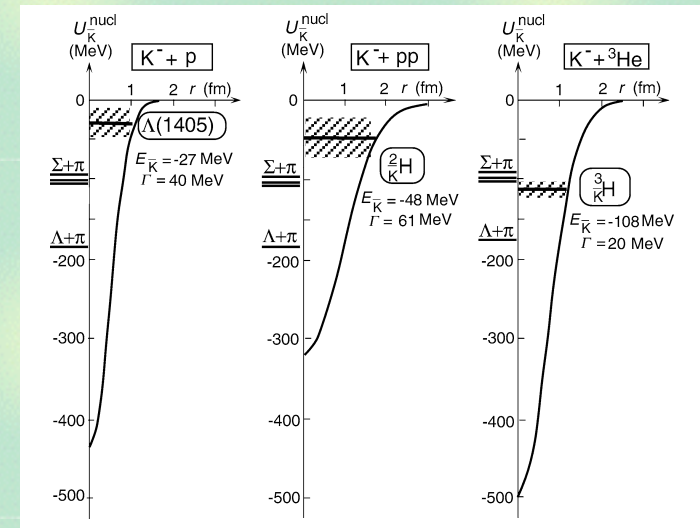
Possible (quasi-)bound \bar{K} in nuclei

- deep binding, high density?

Y. Nogami, Phys. Lett. 7, 288, (1963);

T. Yamazaki, Y. Akaishi, Phys. Lett. B535, 70 (2002);

A. Dote, *et al.*, Phys. Lett. B590, 51 (2004)



Rigorous calculations (2007-)

- bound states in few-nucleon systems
- binding energy depends on the employed $\bar{K}N$ interaction

—> We need a **realistic $\bar{K}N$ interaction.**

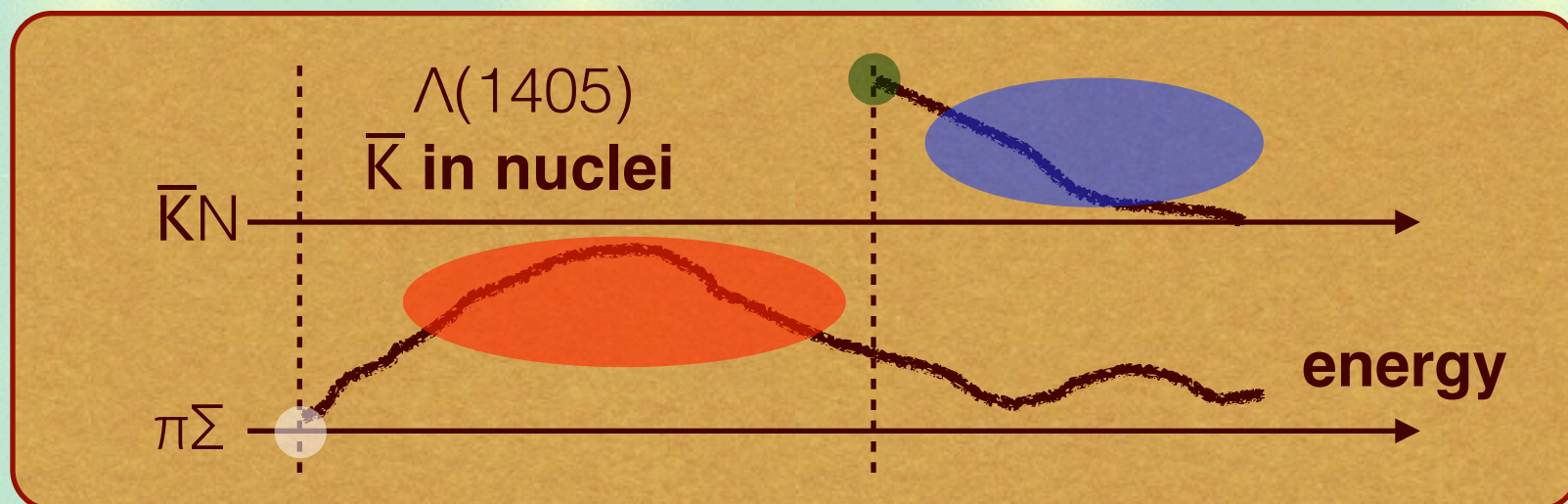
Experimental constraints for the $\bar{K}N$ interaction

Above the $\bar{K}N$ threshold:

- K - p total cross sections (old data)
- $\bar{K}N$ threshold branching ratios (old data)
- K - p scattering length (new data: SIDDHARTA) ←

Below the $\bar{K}N$ threshold:

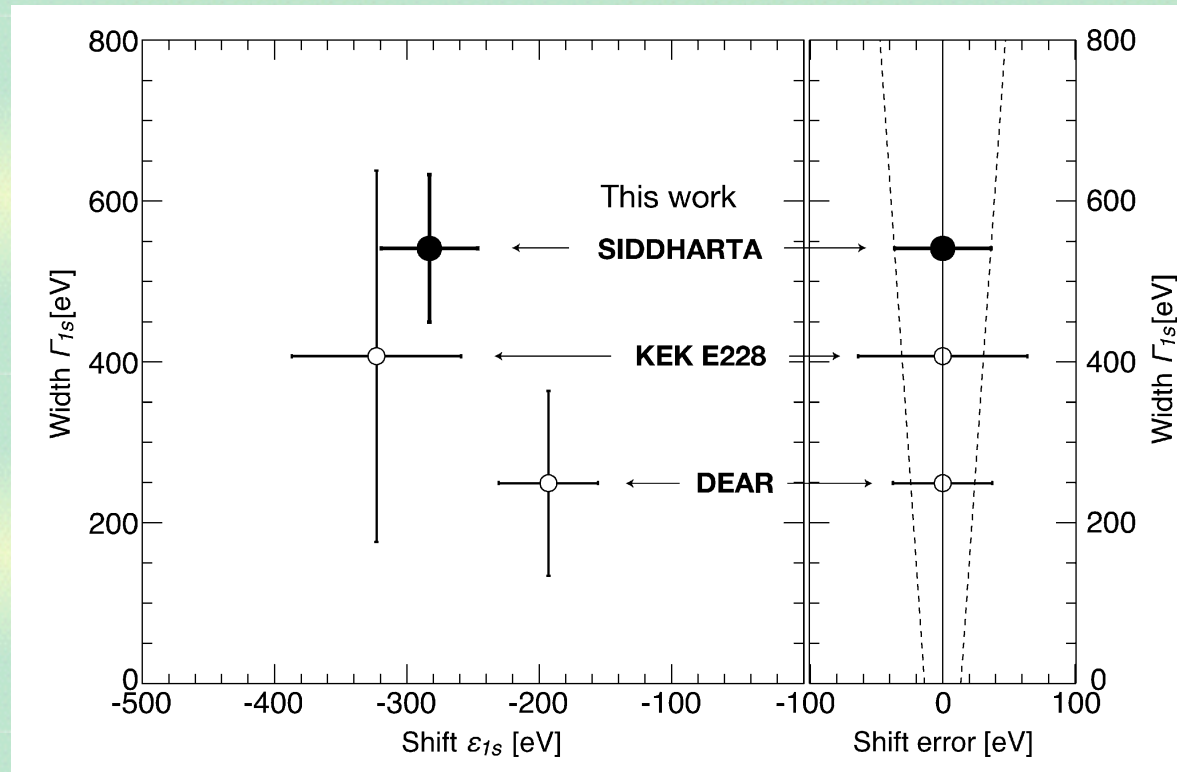
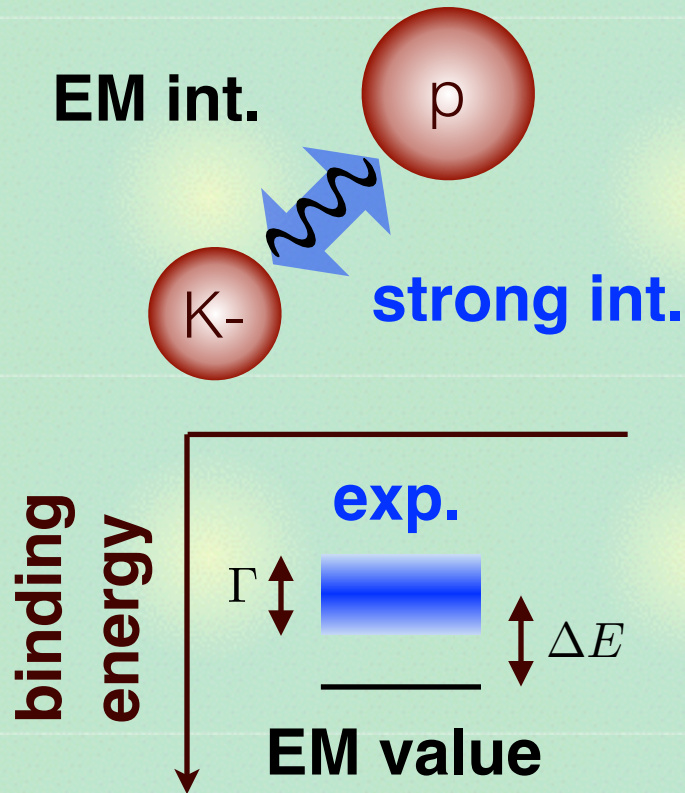
- $\pi\Sigma$ mass spectra (new data: LEPS, CLAS, HADES,...) ←
- $\pi\Sigma$ scattering length (no data at present)



SIDDHARTA measurement

Precise measurement of the kaonic hydrogen X-rays

M. Bazzi, *et al.*, Phys. Lett. B704, 113 (2011); Nucl. Phys. A881, 88 (2012)



- shift and width of atomic state \longleftrightarrow K^-p scattering length

U.-G. Meissner, U. Raha, A. Rusetsky, Eur. Phys. J. C35, 349 (2004)

Direct constraint on the $\bar{K}N$ interaction at fixed energy

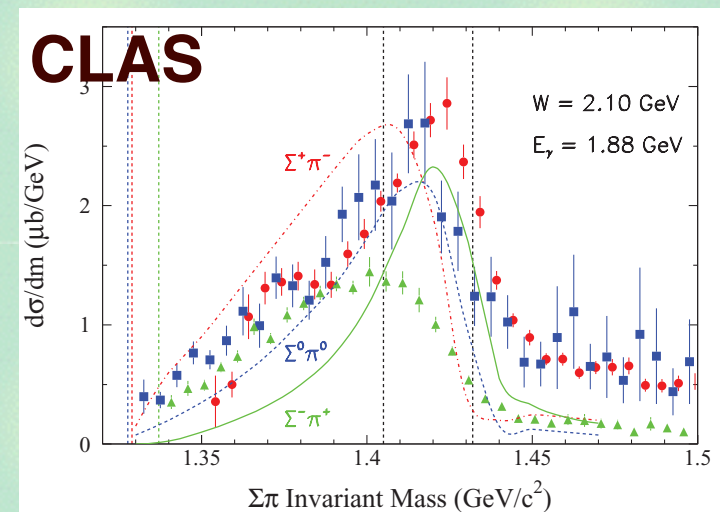
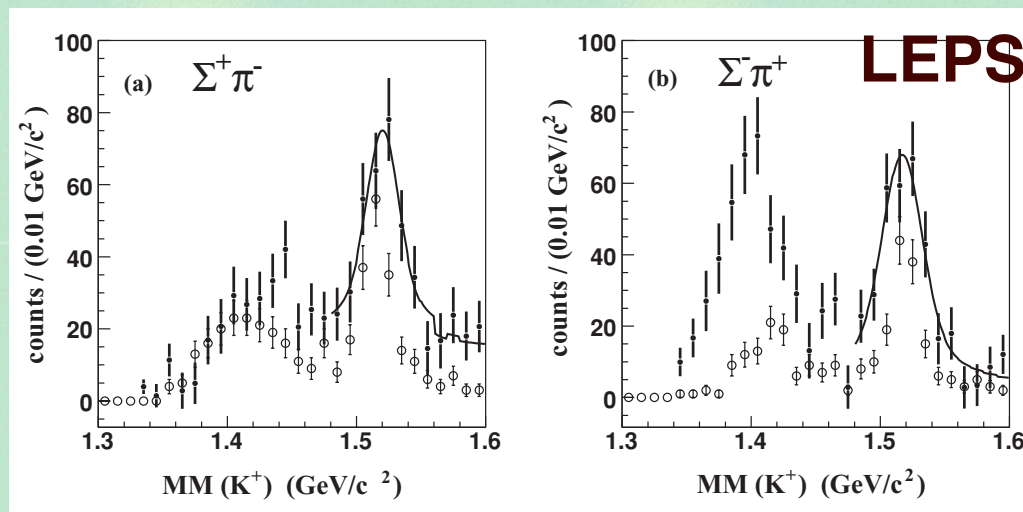
New $\pi\Sigma$ spectra

Photoproduction experiments: $\gamma p \rightarrow K^+(\pi\Sigma)^0$

- **LEPS@** $1.5 < E_\gamma < 2.4$ GeV, **CLAS@** $1.56 < E_\gamma < 3.83$ GeV

M. Niiyama, *et al.*, Phys. Rev. C78, 035202 (2008);

K. Moriya, *et al.*, Phys. Rev. C87, 035206 (2013)



Hadron-induced reactions:

- **HADES:** $pp \rightarrow K^+p(\pi\Sigma)^0$

G. Agakishiev, *et al.*, Phys. Rev. C87, 025201 (2013)

- **J-PARC E31(planned):** $K^-d \rightarrow n(\pi\Sigma)^0$

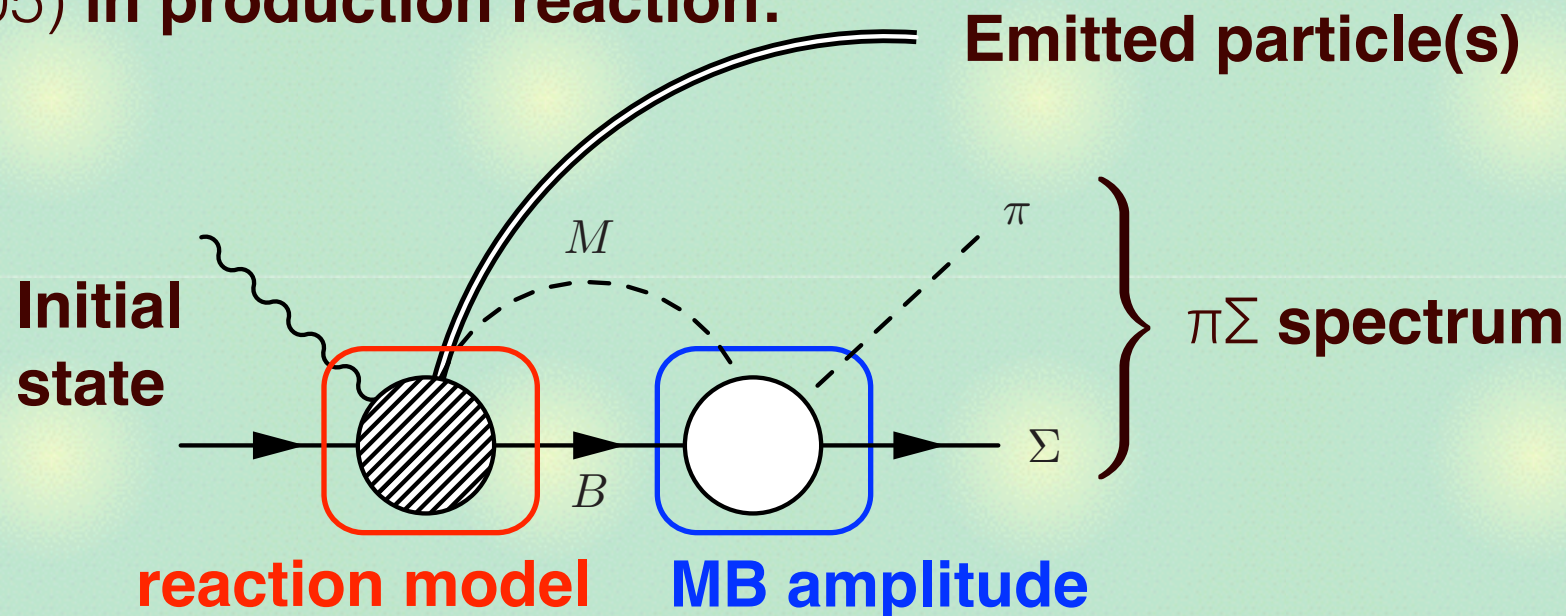
New and precise spectra are being available.

$\pi\Sigma$ spectra and $\bar{K}N$ interaction

Can spectra constrain the **MB amplitude** ($\bar{K}N$ interaction)?

- **Not directly.**




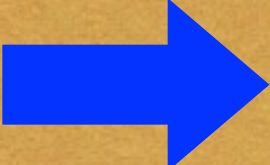
$\Lambda(1405)$ in production reaction:



- Spectra depend on the reaction (ratio of $\bar{K}N/\pi\Sigma$ in the intermediate state, interference with $l=1, \dots$).

—> Detailed **model analysis** for each reaction

Short summary of introduction

-  **$\bar{K}N$ interaction** is important both for hadron physics (structure of $\Lambda(1405)$ resonance) and for nuclear physics (\bar{K} in nuclei).
 -  Precise **K-p scattering length** by SIDDHARTA
—> quantitative **constraint** on $\bar{K}N$ interaction
 -  New **$\pi\Sigma$ spectra** from various reactions
—> reliable **reaction model** required
-  **Construct realistic $\bar{K}N$ scattering model based on a reliable framework.**

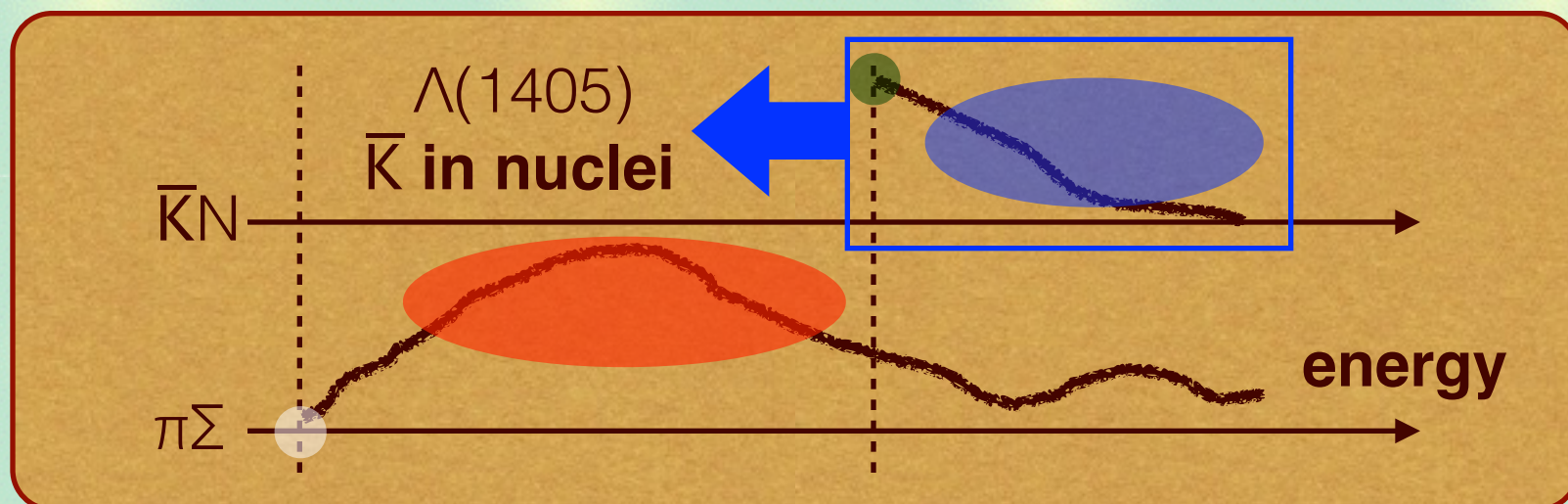
Strategy for $\bar{K}N$ interaction

Above the $\bar{K}N$ threshold:

- K - p **total cross sections** (old data)
- $\bar{K}N$ **threshold branching ratios** (old data)
- K - p **scattering length** (new data: SIDDHARTA)

Below the $\bar{K}N$ threshold:

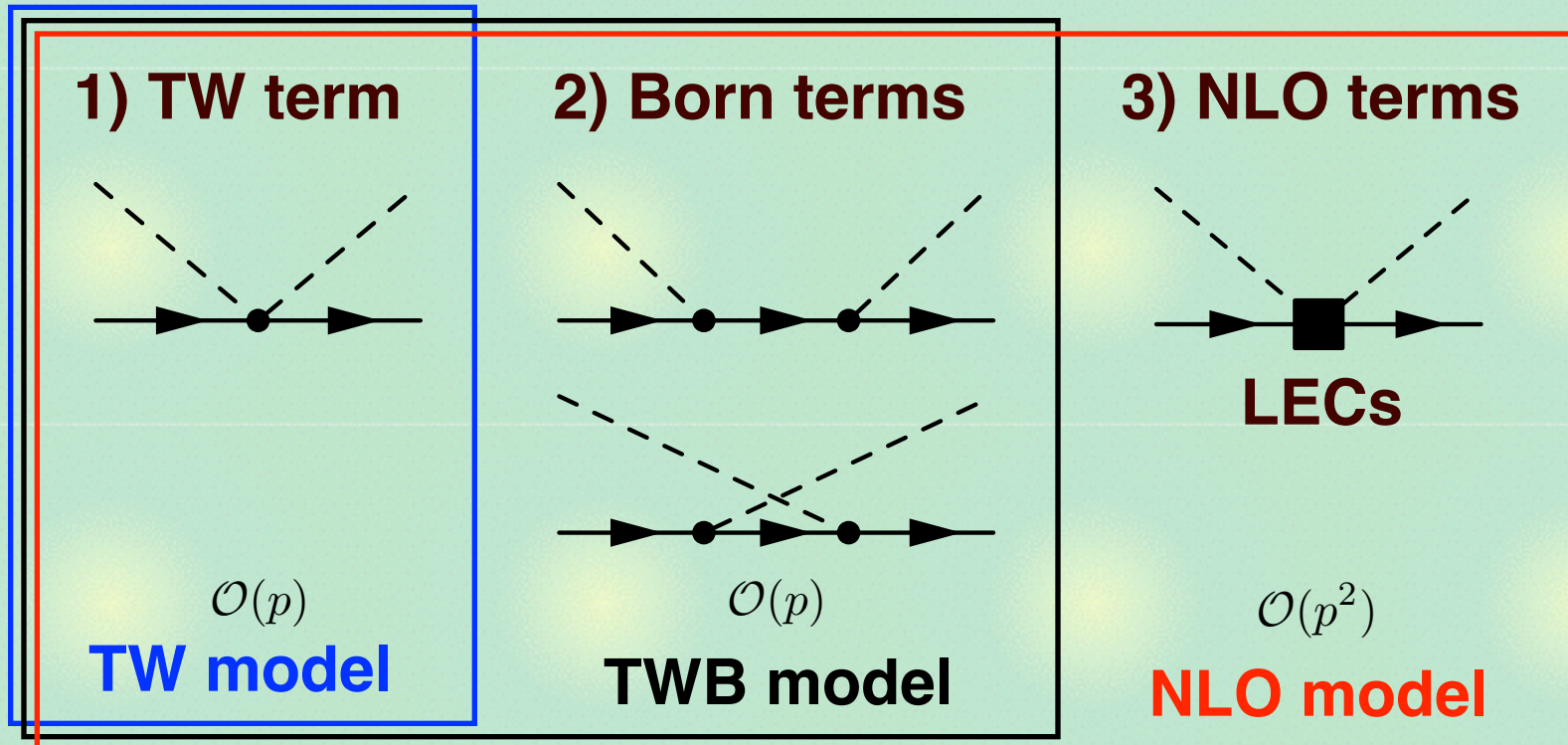
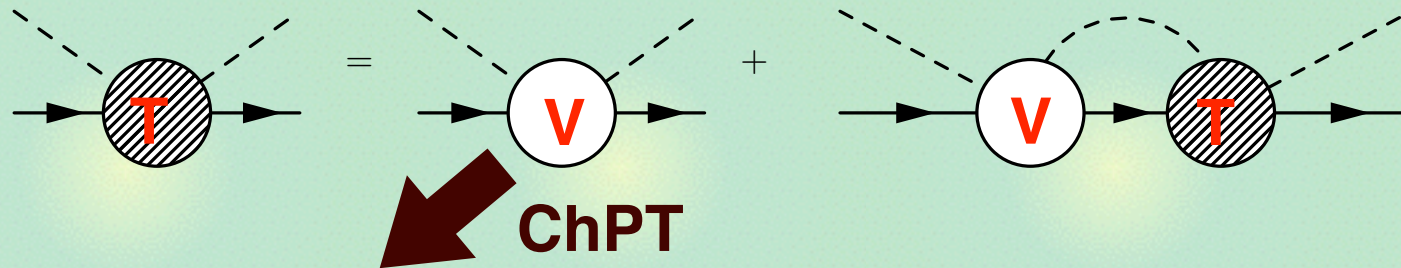
- $\pi\Sigma$ **mass spectra** (new data: LEPS, CLAS, HADES,...)
- $\pi\Sigma$ scattering length (no data at present)



Construction of the realistic amplitude

Chiral coupled-channel approach with systematic χ^2 fitting

Y. Ikeda, T. Hyodo, W. Weise, Phys. Lett. B706, 63 (2011); Nucl. Phys. A881 98 (2012);



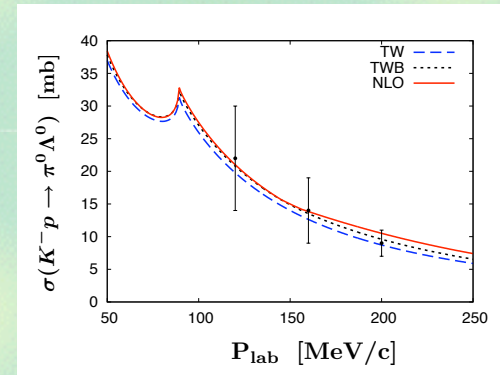
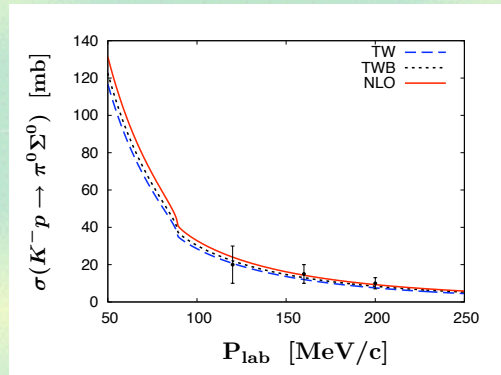
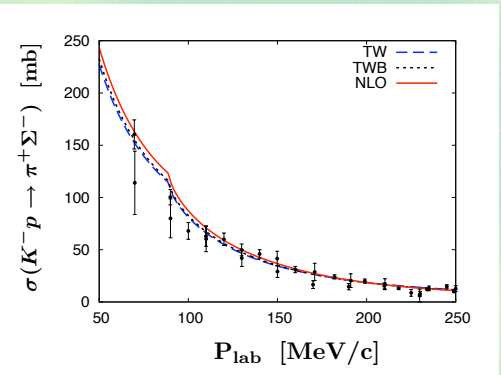
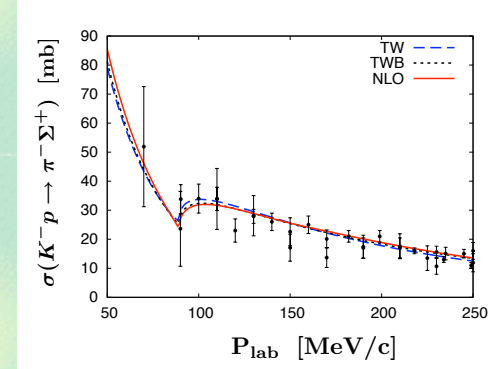
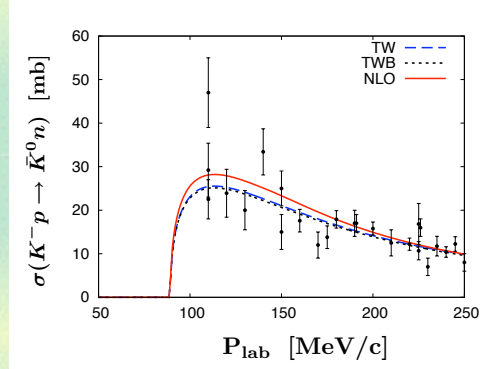
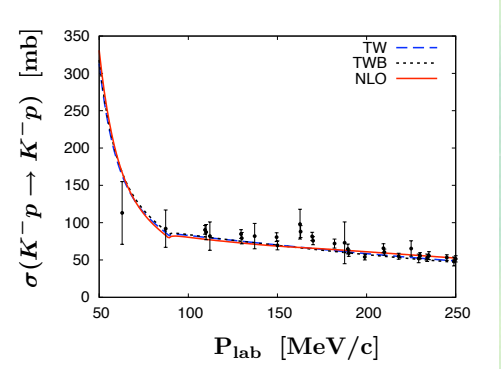
Best-fit results

SIDDHARTA

Branching ratios

	TW	TWB	NLO	Experiment
ΔE [eV]	373	377	306	$283 \pm 36 \pm 6$ [10]
Γ [eV]	495	514	591	$541 \pm 89 \pm 22$ [10]
γ	2.36	2.36	2.37	2.36 ± 0.04 [11]
R_n	0.20	0.19	0.19	0.189 ± 0.015 [11]
R_c	0.66	0.66	0.66	0.664 ± 0.011 [11]
$\chi^2/\text{d.o.f}$	1.12	1.15	0.96	

cross sections

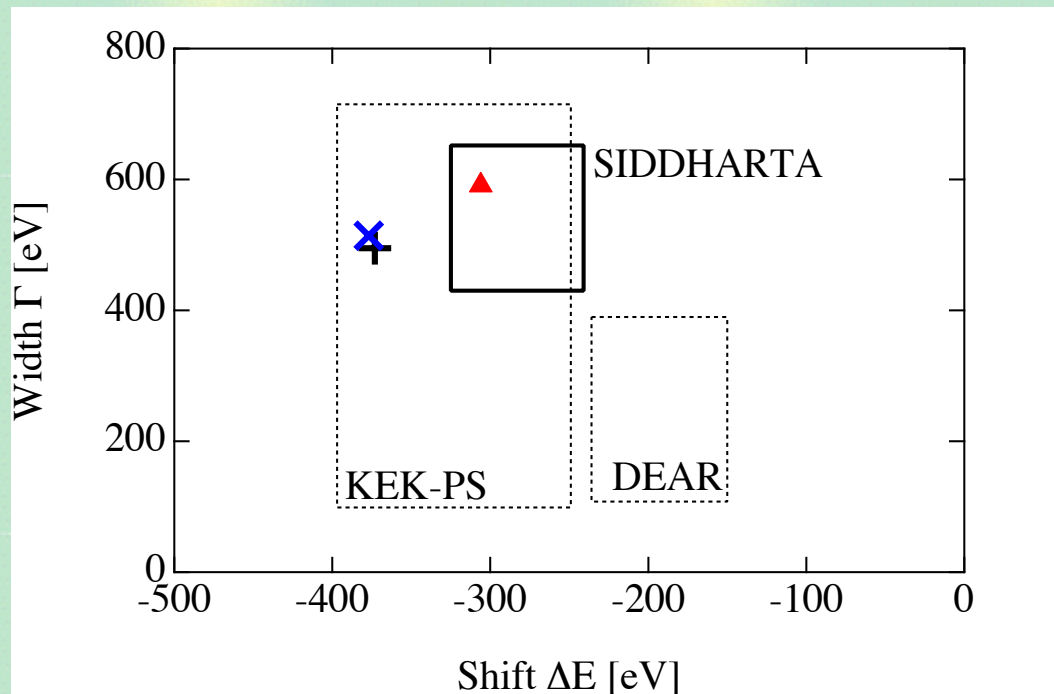


SIDDHARTA is consistent with cross sections

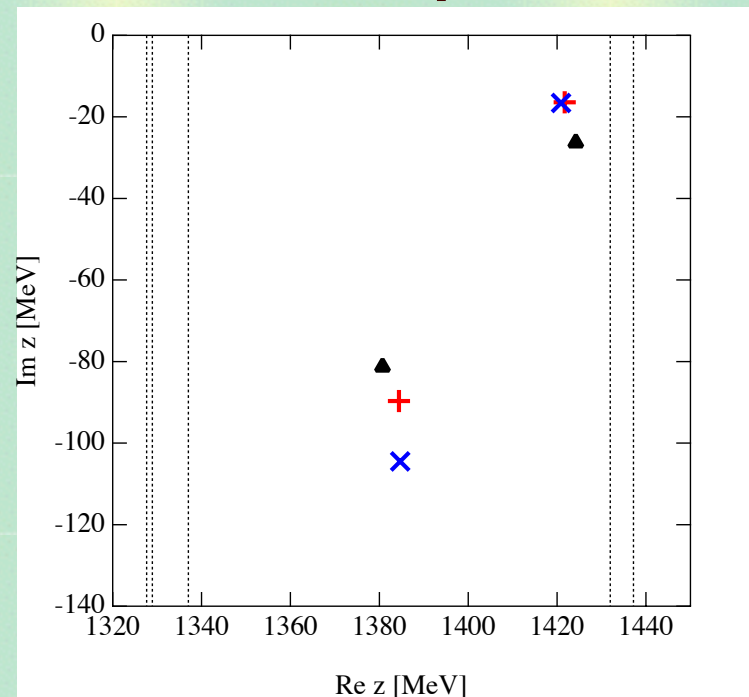
Shift, width, and pole positions

	TW	TWB	NLO
$\chi^2/\text{d.o.f.}$	1.12	1.15	0.957

Shift and width



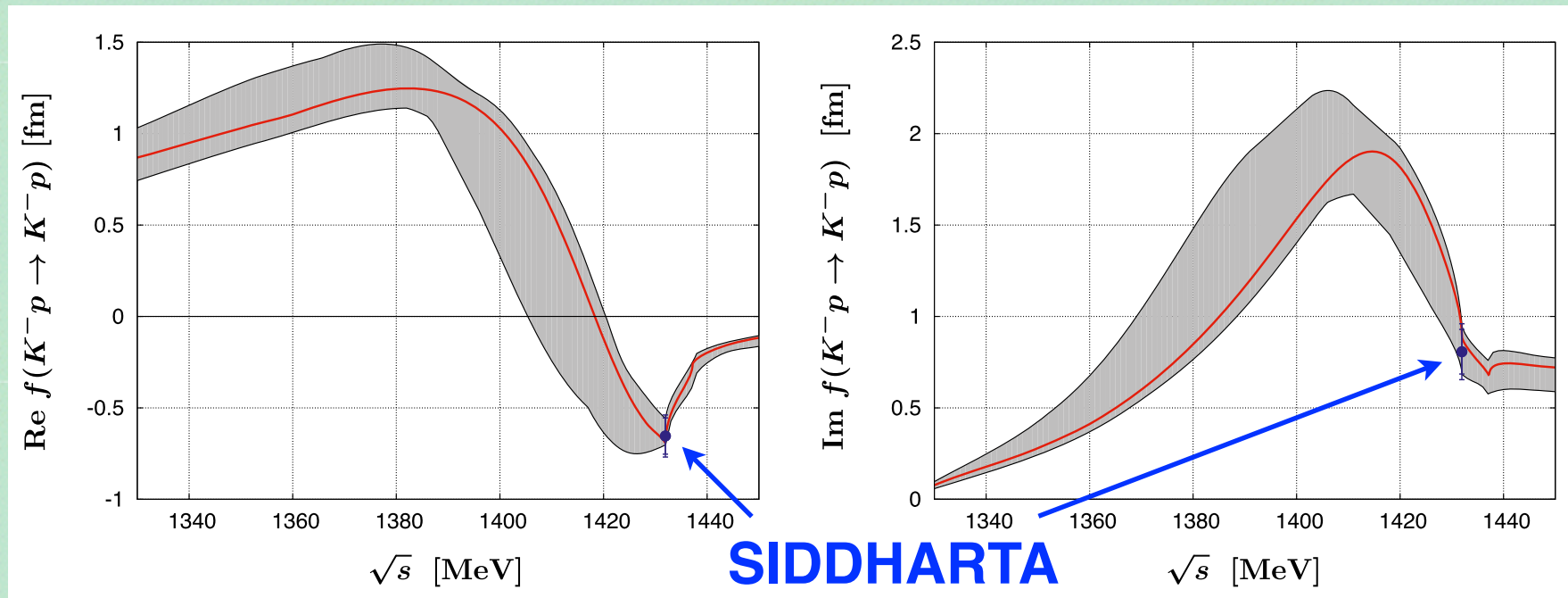
$\Lambda(1405)$ Pole positions



TW and **TWB** are reasonable, while best-fit requires **NLO**. Pole positions are now converging.

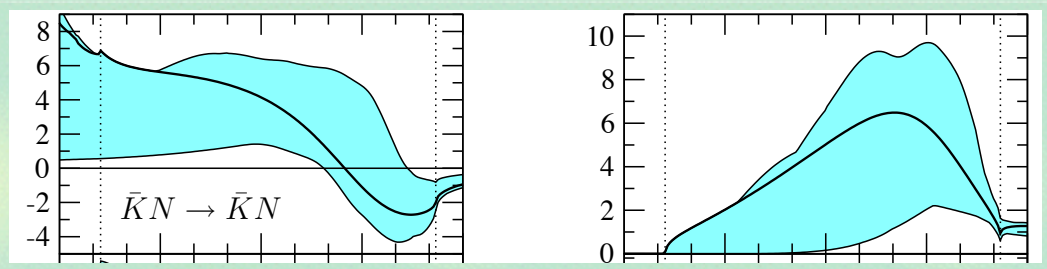
Subthreshold extrapolation

Behavior of $K^-p \rightarrow K^-p$ amplitude below threshold



- c.f. $\bar{K}N \rightarrow \bar{K}N$ ($I=0$) without SIDDHARTA

R. Nissler, Doctoral Thesis (2007)



Subthreshold extrapolation is now well controlled.

Remaining ambiguity

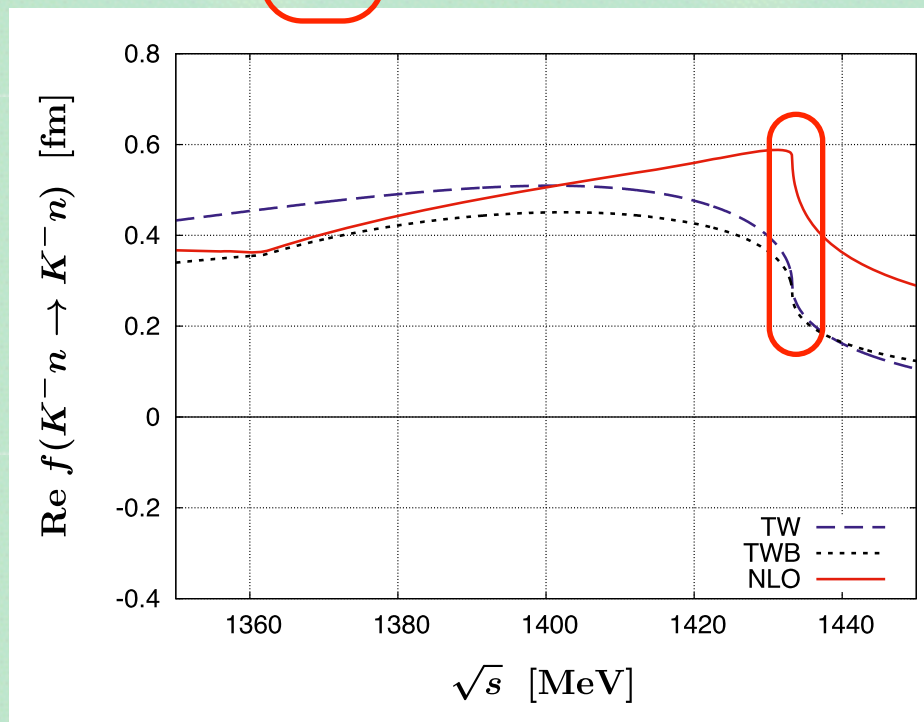
For \bar{K} -nucleon interaction, we need both K-p and K-n.

$$a(K^-p) = \frac{1}{2}a(I=0) + \frac{1}{2}a(I=1) + \dots, \quad a(K^-n) = a(I=1) + \dots$$

$$a(K^-n) = 0.29 + i0.76 \text{ fm (TW) ,}$$

$$a(K^-n) = 0.27 + i0.74 \text{ fm (TWB) ,}$$

$$a(K^-n) = 0.57 + i0.73 \text{ fm (NLO) .}$$



Some deviation: constraint on K-n (\leftarrow kaonic deuterium?)

Summary: chiral SU(3) dynamics

We perform systematic χ^2 analysis for the $\bar{K}N-\pi\Sigma$ interaction in chiral coupled-channel approach.

With accurate kaonic hydrogen data, we can construct realistic $\bar{K}N-\pi\Sigma$ interaction. **Ambiguity** in the subthreshold extrapolation for $\Lambda(1405)$ energy region **is significantly reduced**.

Pole position of $\Lambda(1405)$ is converging.

$$z_1 = (1424_{-23}^{+7} - i26_{-14}^{+3}) \text{ MeV}, \quad z_2 = (1381_{-6}^{+18} - i81_{-8}^{+19}) \text{ MeV}$$

Remaining ambiguity: **$l=1$ channel**
← kaonic deuterium measurement.

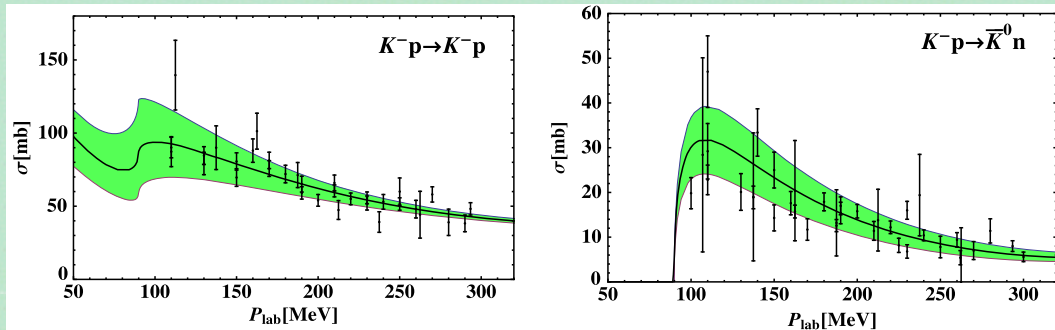
Y. Ikeda, T. Hyodo, W. Weise, PLB 706, 63 (2011); NPA 881 98 (2012)

Analyses by other groups

NLO interaction + χ^2 analysis + SIDDHARTA data

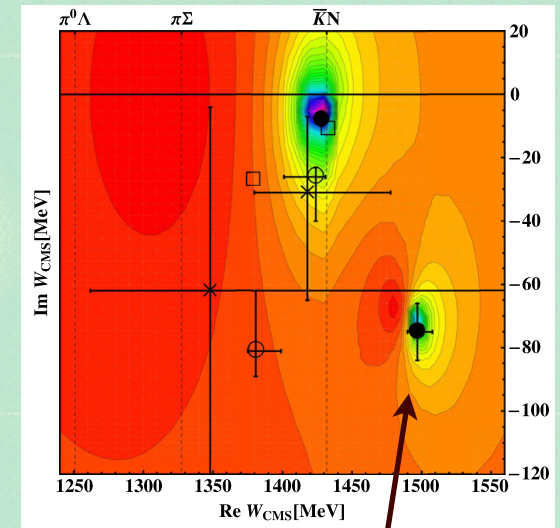
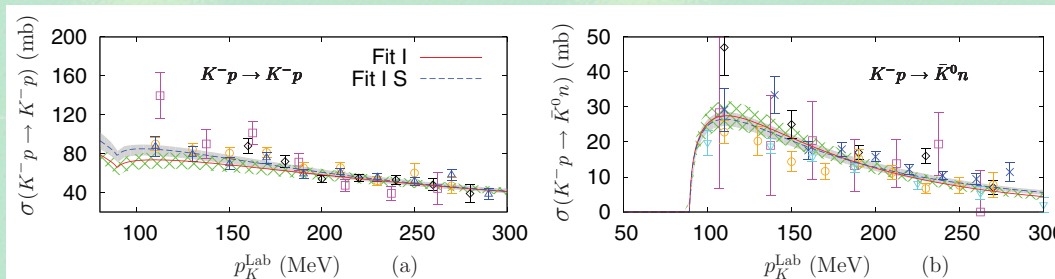
- Bonn group

M. Mai, U.-G. Meissner, Nucl. Phys. A900, 51 (2013)



- Murcia group

Z.H. Guo, J.A. Oller, Phys. Rev. C87, 035202 (2013)



~13 parameters \rightarrow several local minima

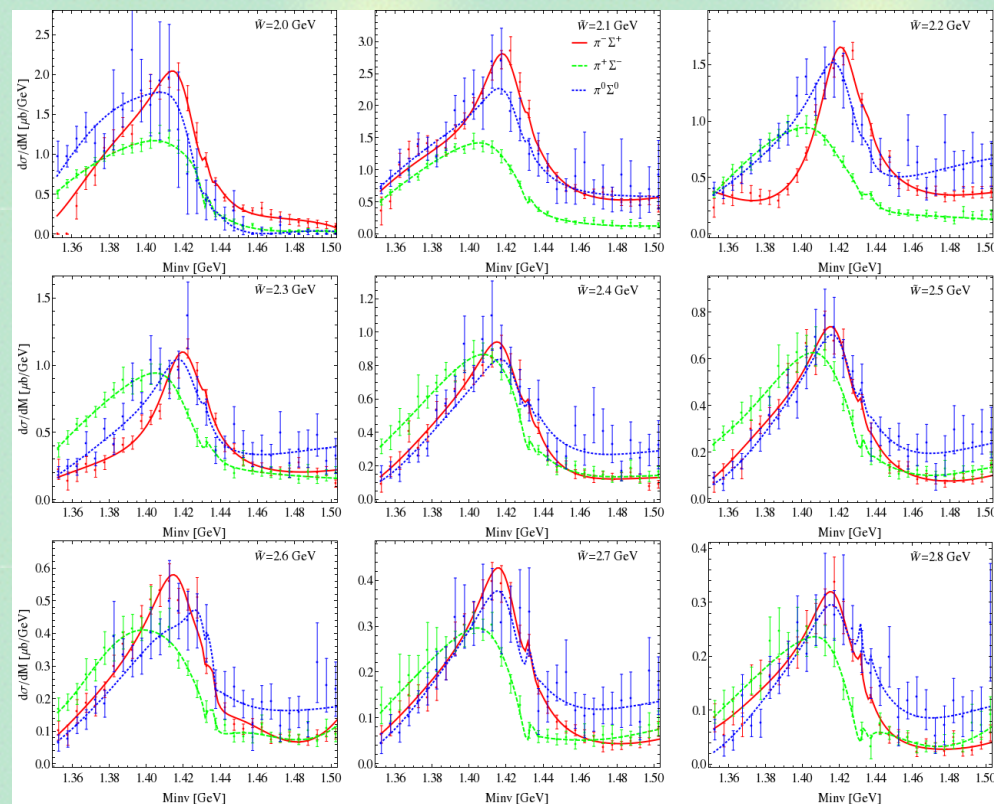
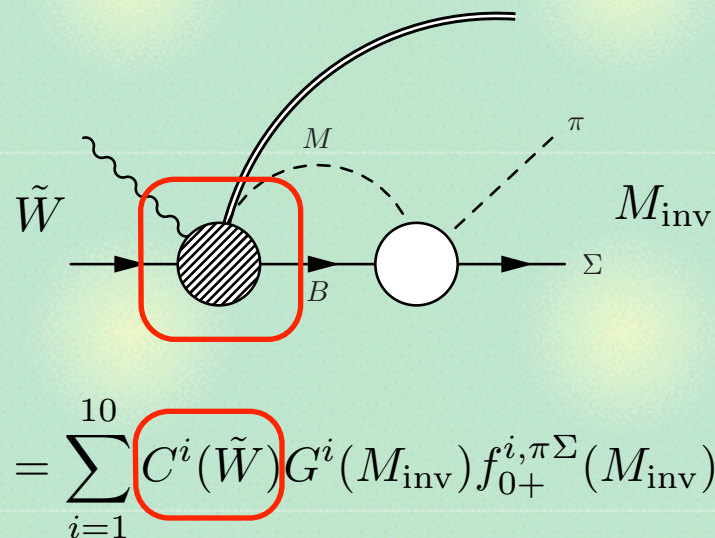
Another “exotic” solution (second pole above $\bar{K}N$)?

Constraints from the $\pi\Sigma$ spectrum

Combined analysis of scattering data + $\pi\Sigma$ spectrum

M. Mai, U.-G. Meissner, arXiv:1411.7884 [hep-ph]

- a simple model for the photoproduction $\gamma p \rightarrow K^+(\pi\Sigma)^0$
- CLAS data of the $\pi\Sigma$ spectrum



→ The “exotic” solution is excluded.

Pole positions of $\Lambda(1405)$

Mini-review prepared for PDG

Pole structure of the $\Lambda(1405)$

Ulf-G. Meißner, Tetsuo Hyodo

February 4, 2015




The $\Lambda(1405)$ resonance emerges in the meson-baryon scattering amplitude with the strangeness $S = -1$ and isospin $I = 0$. It is the archetype of

[11,12] Ikeda-Hyodo-Weise, [14] Murcia, [15] Bonn (updated)

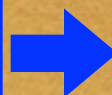
approach	pole 1 [MeV]	pole 2 [MeV]
Ref. [11, 12] NLO	$1424_{-23}^{+7} - i26_{-14}^{+3}$	$1381_{-6}^{+18} - i81_{-8}^{+19}$
Ref. [14] Fit I	$1417_{-4}^{+4} - i24_{-4}^{+7}$	$1436_{-10}^{+14} - i126_{-28}^{+24}$
Ref. [14] Fit II	$1421_{-2}^{+3} - i19_{-5}^{+8}$	$1388_{-9}^{+9} - i114_{-25}^{+24}$
Ref. [15] solution #2	$1434_{-2}^{+2} - i10_{-1}^{+2}$	$1330_{-5}^{+4} - i56_{-11}^{+17}$
Ref. [15] solution #4	$1429_{-7}^{+8} - i12_{-3}^{+2}$	$1325_{-15}^{+15} - i90_{-18}^{+12}$

still some deviations

Summary of current status of $\Lambda(1405)$

-  To avoid “exotic” solutions, we need to check the consistency with $\pi\Sigma$ spectra.
-  Different analyses show pole 1 (close to the $\bar{K}N$ threshold) is well determined. There is still ambiguity in pole 2 (with large imaginary part).
-  Future direction:

NLO chiral interaction
 χ^2 error analysis
reliable reaction model



$\bar{K}N$ scattering data
K-p scattering length
 $\pi\Sigma$ spectrum