

Hadrons and Hadron interactions in QCD 2015
Yukawa Institute for Theoretical Physics, Kyoto Univ.,
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Hadron properties at finite density and spectroscopies of mesic nuclei



Hideko NAGAHIRO (Nara Women's University)



H. Nagahiro, D.Jido, H. Fujioka, K.Itahashi, S. Hirenzaki, PRC87(13)045201 [(p,d) theo.]

Itahashi, Fujioka, Geissel, Hayano, Hirenzaki, Itoh, Jido, Metag, Nagahiro, Nanova, Nishi,
Okochi, Outa, Suzuki, Tanaka, Weick, PTP128(12)601, [(p,d) exp. @GSI]



H. Nagahiro, S. Hirenzaki, E. Oset, A. Ramos, PLB709(12)87, [chiral unitary, (π ,N)]

D. Jido, H. Nagahiro, S. Hirenzaki, PRC85(12)032201(R) [χ sym vs. $m_{\eta'}$, (π ,N)]

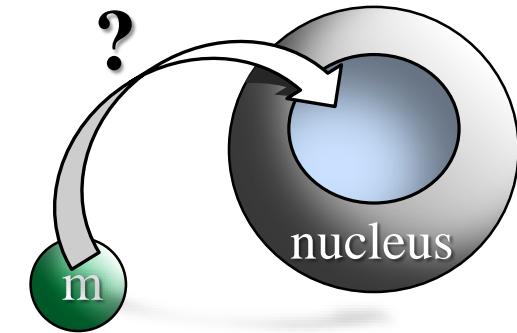
H.Nagahiro, M.Takizawa, S. Hirenzaki, PRC74(06)045203 [NJL, (γ ,p)]

H. Nagahiro, S. Hirenzaki, PRL94(05)232503 [(γ ,p)]

Introduction

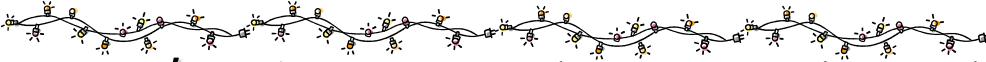


✓ Interests of meson bound systems : **mesic nuclei**



- exotic many body systems
- energy **eigenstates** with **definite quantum numbers**
 - selection by choosing an appropriate kinematics in the formation reaction
- important info. on **in-medium hadron properties** and QCD symmetries
 - » **π atom** ... deeply bound state / χ -sym. restoration
 - » **η -mesic nuclei** ... strong coupling to $N^*(1535)$ resonance
 - χ -sym. for baryon resonance ?
 - » **$\eta'(958)$ -mesic nuclei** ... $U_A(1)$ anomaly effect in medium ?
- » **K -atom & nuclei** ... deeply bound nuclear states ? exotic few body ?
- » **ω -mesic nuclei** ... mass shift in medium ?
- » **D or \bar{D} nuclei** ... heavy quark in nuclei ?
 - :

heavy η' (958) mass



- η' (958) meson ... close connection to the $U_A(1)$ anomaly

» many theoretical works

› in vacuum / at finite temperature / at finite density

- » R. D. Pisarski, R. Wilczek, PRD29(84)338
- » T. Kunihiro, T. Hatsuda, PLB206(88)385 / T. Kunihi
- » V. Bernard, R.L.Jaffe and U.-G.Meissner, NPB308(1)
- » Y. Kohyama, K.Kubodera and M.Takizawa, PLB208
- » K. Fukushima, K.Onishi, K.Ohta, PRC63(01)045203
- » P. Costa *et al.*,PLB560(03)171, PRC70(04)025204, e

» poor experimental information at finite density

- $U_A(1)$ anomaly in medium from the viewpoint of “meson

» the η' properties, especially **mass shift**, at finite density

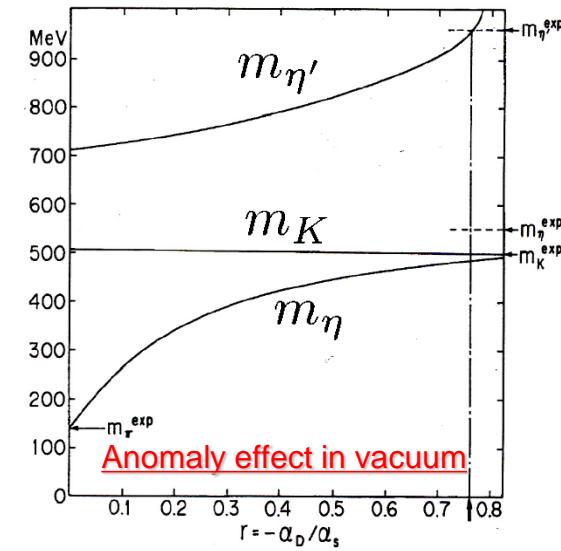
- **Nambu-Jona-Lasinio model** with the **KMT interaction**

$$\mathcal{L} = \bar{q}(i\cancel{\partial} - m)q + \frac{g_s}{2} \sum_a [(\bar{q}\lambda_a q)^2 + (i\bar{q}\lambda_a \gamma_5 q)^2]$$

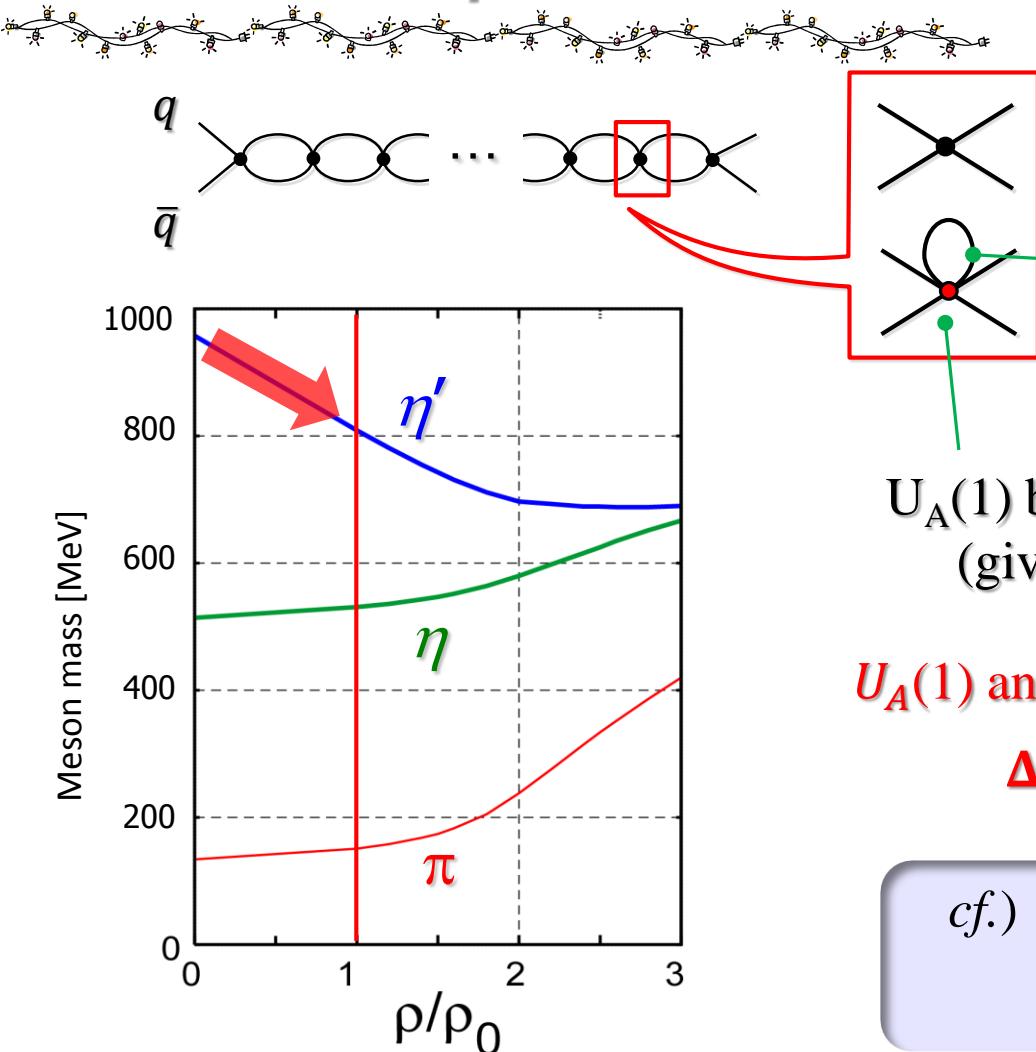
$$+ g_D [\det \bar{q}_i (1 - \gamma_5) q_j + h.c.]$$

explicit breaking the $U_A(1)$ sym.

Kunihiro, Hatsuda, PLB206(88)385



✓ in-medium η' mass reduction with NJL model



Kobayashi-Maskawa, PTP44(70)1422
 G. 't Hooft, PRD14(76)3432
 Kunihiro, Hatsuda, PLB206(88)385
 Costa et al., PLB560(03)171

$\langle \bar{q}q \rangle \rightarrow \text{small}$
partial restoration of chiral sym.

$U_A(1)$ breaking [KMT interaction]
 (giving heavier mass for η')

$U_A(1)$ anomaly effect \rightarrow small in medium

$$\Delta m_{\eta'} \sim -150 \text{ MeV @ } \rho_0$$

cf.) $\Delta m_{\eta'} \sim -40 - -80 \text{ MeV @ } \rho_0$

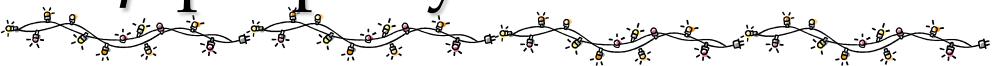
Quark-meson-coupling model,
 S.Bass, A.Thomas, PLB634(06)368

cf.) $\Delta m_{\eta'} \sim -80 \text{ MeV @ } \rho_0$

linear sigma model
 S.Sakai, D.Jido, PRC88(13)064906

Costa et al., PLB560(03)171,
 Nagahiro-Takizawa-Hirenzaki,
 PRC74(06)045203

η' property in medium



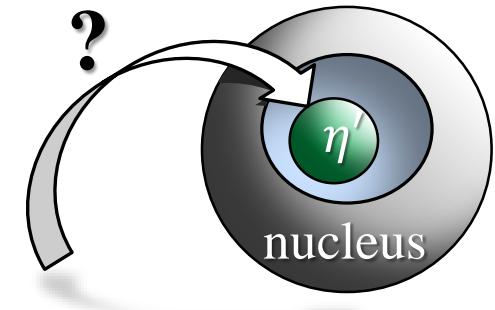
→ Phenomenologically poorly understood

✓ **small scattering length ?**

$$Re(a_{\eta' p}) = 0 \pm 0.43 \text{ fm}, \text{Im}(a_{\eta' p}) = 0.37^{+0.40}_{-0.16} \text{ fm} \quad \text{in free space}$$

[E. Czerwinski *et al.*, (COSY-11) PRL113(14)062004]

[estimated from FSI on $pp \rightarrow pp\eta'$ observed at COSY]

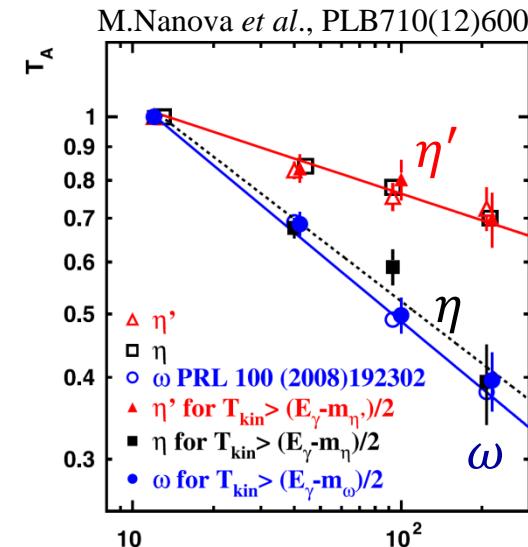


✓ **smaller absorption width in medium ?**

$$\Gamma_{\eta'}(\rho_0; \langle |\vec{p}_{\eta'}| \rangle \sim 1 \text{ GeV}/c) \sim 15 - 25 \text{ MeV} @ \rho_0,$$

CBELSA/TAPS [M.Nanova *et al.*, PLB710(12)600]

[estimated transparency ratio $\gamma A \rightarrow \eta' X$]



✓ **mass reduction in finite T/ρ?**

$$\Delta m \sim -150 \text{ MeV} @ \rho_0 \quad [\text{NJL model w/ KMT interaction}]$$

$$\Delta m \sim -200 \text{ MeV} ? \text{ in finite } T \quad [\text{in Au+Au collisions at RHIC}]$$

[experimentally observed enhanced production of soft pions]

Interpreted as mass reduction of η' in the hot medium [Csorgo *et al.*, PRL105(10)182301]]

Our strategy for studying the η' properties



■ Possible η' bound states and their formation

- » with missing mass spectroscopy : (γ, p) , (π, N) , (p, d) , ...
 - › H.N., S.Hirenzaki, PRL94 (05) 232503
 - › H.N., M.Takizawa, S.Hirenzaki, PRC74 (06)045203
 - › ... and references in title page !

→ $\Gamma_{\eta'}$ in-medium strongly affects its observation possibilities

Experimental information [CBELSA/TAPS [M.Nanova *et al.*, PLB710(12)600]

$$\Gamma_{\eta'}(\rho_0; \langle |\vec{p}_{\eta'}| \rangle \sim 1 \text{ GeV}/c) \sim 15 - 25 \text{ MeV} @ \rho_0$$

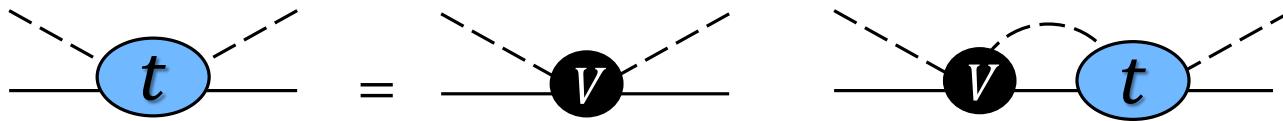
[estimated transparency ratio $\gamma A \rightarrow \eta' X$]

phenomenological approach [H.N., S. Hirenzaki, E. Oset, A. Ramos, PLB]

Based on : Coupled-channel calculation [Oset-Ramos, PLB704(11)334]

$$PB (\pi N, \eta N, K\Lambda, K\Sigma) + VB (K^*\Lambda, K^*\Sigma) + \eta_0 B$$

Unitarized scattering amplitude by coupled-channel BS eq.



Interaction kernel V

(1) Weinberg-Tomozawa interaction : pseudoscalar-baryon (PB) channel

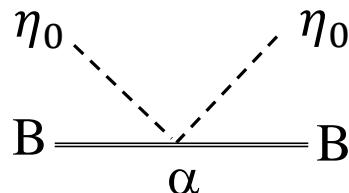
$\pi N, \eta N, K\Lambda, K\Sigma + \eta' N$ by the $\eta - \eta'$ mixing

their result : $|a_{\eta'N}| = 0.01$ fm $\Leftrightarrow |a_{\eta'N}| \sim 0.1 - 0.8$ fm [PLB'00]

(2) Vector meson-baryon (VB) channel ($K^*\Lambda, K^*\Sigma$)

their result : $|a_{\eta'N}| = 0.03$ fm

(3) **coupling of the singlet component of pseudoscalar to baryons**



$$\mathcal{L}_{\eta_0 B} \propto \eta_0^2 (\partial_\mu \bar{B} \gamma^\mu B - \bar{B} \gamma^\mu \partial_\mu B)$$

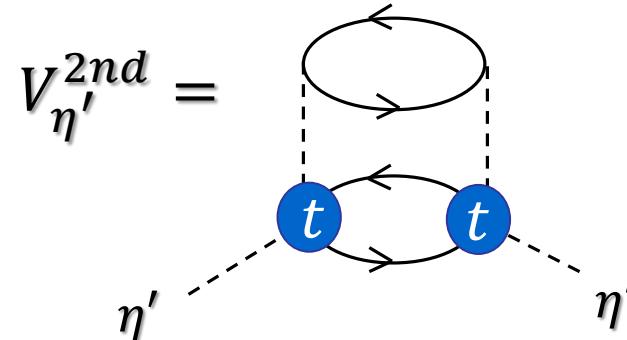
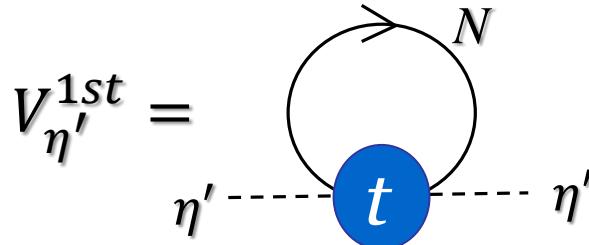
α ... free parameter $\rightarrow |a_{\eta'N}| = 0.1$ fm

Borasoy , PRD61(00)014011

Kawarabayashi-Ohta, PTP66(81)1789

phenomenological estimation for $V_{\eta'}^{opt}$

Optical potential $V_{\eta'}$ [H.N., S. Hirenzaki, E. Oset, A. Ramos, PLB709(12)87]



We consider only the **attractive** case & **energy-independent** potential.

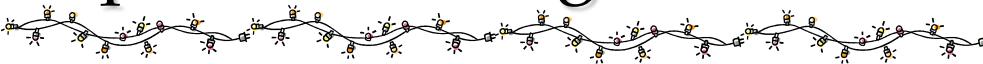
$\text{Re } V_{\eta'}$ and $\text{Im } V_{\eta'}$ with various α values

in unit of MeV

α	$ a_{\eta'N} \text{ fm}$	$V_{\eta'}^{1st}(\rho_0)$	$V_{\eta'}^{2nd}(\rho_0)$	$V_{\eta'}^{total}(\rho_0)$
-0.193	0.1	$-8.6 - 1.7i$	$-0.1 - 0.1i$	$-8.7 - 1.8i$
-0.834	0.3	$-26.3 - 2.1i$	$-0.6 - 0.9i$	$-26.8 - 3.0i$
-1.79	0.5	$-43.8 - 3.0i$	$-1.3 - 2.5i$	$-44.1 - 5.5i$
-9.67	1.0	$-87.7 - 6.9i$	$-4.1 - 10.4i$	$-91.8 - 17.2i$

$\text{Re } V \gg \text{Im } V$

phenomenological estimation for $V_{\eta'}^{opt}$

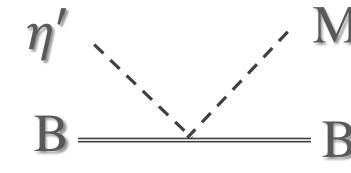
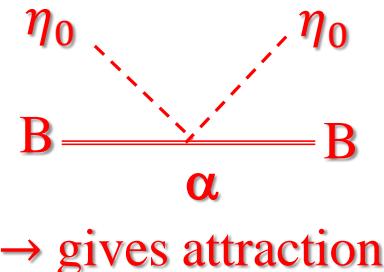


The reason why $\text{Re } V \gg \text{Im } V$ in coupled channel calculation

Kawarabayashi-Ohta, PTP66(81)1789

Borasoy , PRD61(00)014011

WT interaction for η'



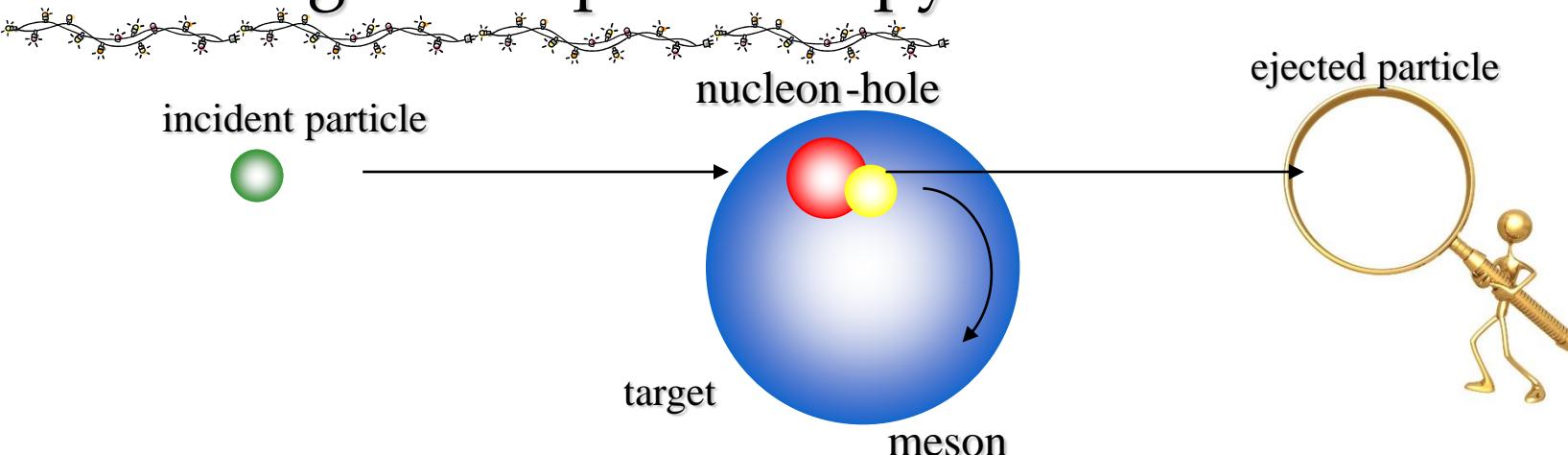
This interaction ...

- ✓ *resembles* that of the anomaly effect [S.Sakai, D.Jido, PRD88(13)064906]
- ✓ **dominate** the $\eta'N$ interaction
- ✓ contributes mostly to the **η' elastic channel** & barely to the **inelastic channel**

ongoing work [→ later]

- ✓ **energy-dependence of $V_{\eta'}$** :
we discuss over a wide energy range (deep bound state $\leftrightarrow a_{\eta'N}$ at threshold)
- ✓ possible **α** value evaluated from, ex.) $\pi N \rightarrow \eta'N$ cross section

Missing mass spectroscopy



one-nucleon pick up : recoil-free production for light meson (but not for η')

- » **(d,³He) reaction** ...established method π atom formation (96, 98, 01)
S.Hirenzaki, H.Toki, T.Yamazaki, PRC44(91)2472, K.Itahashi, *et al.*, PRC62(00)025202, ...
- » **(γ ,p) reaction** M.Kohno, H.Tanabe PLB231(89)219, E.Marco, W.Weise, PLB502(01)59
H.Nagahiro, D.Jido, S.Hirenzaki, Nucl. Phys. **A761** (2005) 92-119 etc..
- » **(π ,N) reaction** Chrien *et al.*, PRL60(1988)2595 / Liu, Haider, PRC34(1986)1845
H.Nagahiro, D.Jido, S.Hirenzaki, PRC80(2009)025205, ...
- » **(p,d) reaction** Nagahiro, Jido, Fujioka, Itahashi, Hirenzaki, PRC87(13)045201.
Itahashi, Fujioka, Geissel, Hayano, Hirenzaki, Itoh, Jido, Metag, Nagahiro, Nanova, Nishi, Okochi, Outa, Suzuki, Tanaka, Weick, PTP128(12)601. ...

formation by (p,d) reaction @ GSI (\rightarrow Y.K.Tanaka's talk)



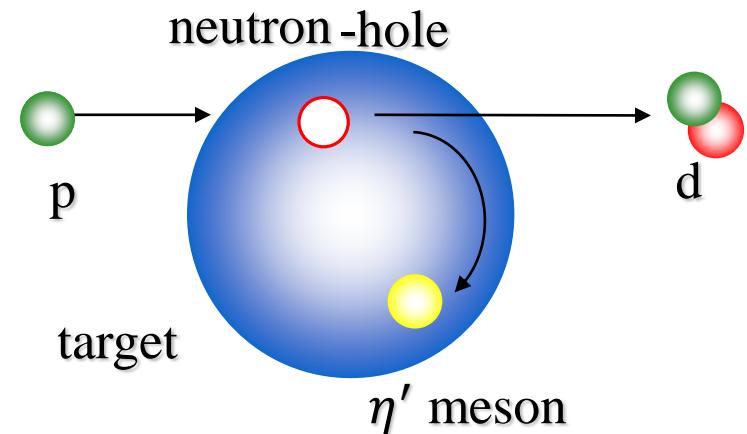
missing mass spectroscopy

K. Itahashi, H. Fujioka *et al.*, PTP128(12)601

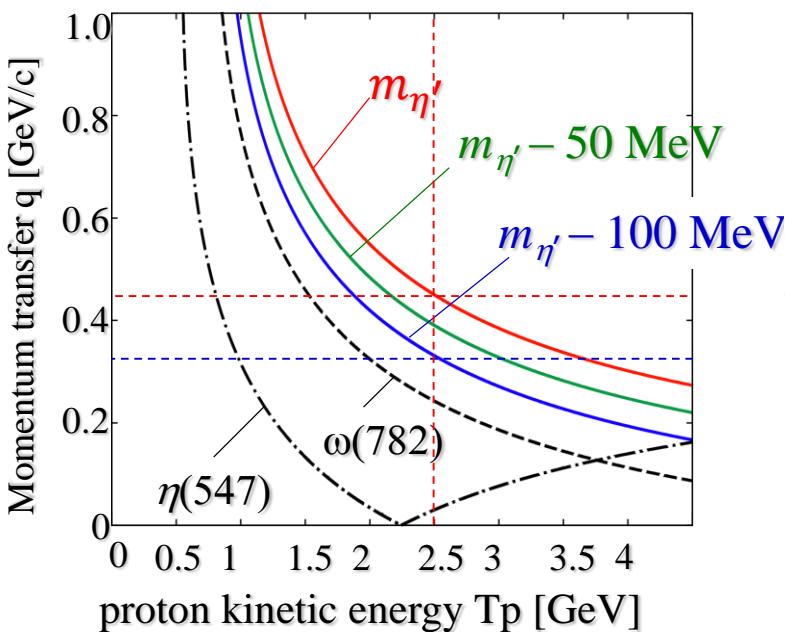
proton kinetic energy $T_p = 2.5 \text{ GeV}$

target : ^{12}C

forward reaction : $\theta_d = 0 \text{ deg.}$

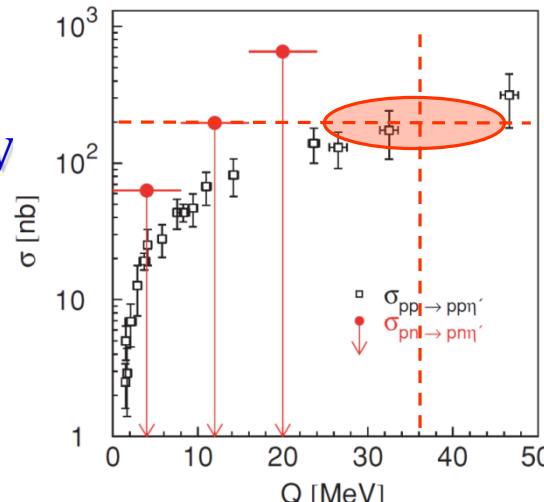


momentum transfer



elementary cross section $pn \rightarrow \eta' d$ **No information**

J.Klaja et al., PRC81(10)035209 (COSY)



$$\begin{array}{c} \sigma_{pp \rightarrow pp\eta'} \\ \downarrow \\ \text{assumptions} \\ \left(\frac{d\sigma}{d\Omega} \right)_{pn \rightarrow \eta'd}^{lab} = 30 \mu\text{b}/\text{sr} \end{array}$$

Itahashi *et al.*, PTP128(12)601
K.Nakayama in private comm.

formation spectra : Green's function method

Green's function method

O. Morimatsu, K. Yazaki, NPA435(85)727-737

impulse approximation

$$\left(\frac{d^2\sigma}{d\Omega dE} \right) = \left(\frac{d\sigma}{d\Omega} \right)_{n(p,d)\eta'}^{\text{Lab.}} \times S(E)$$

nuclear response function

$$S(E) = -\frac{1}{\pi} \text{Im} \sum_{\alpha} T_{\alpha}^* G_{\alpha}(E) T_{\alpha}$$

Green's function

$$G(E) = \langle n^{-1} | \phi_{\eta'} \frac{1}{E - H'_{\eta} + i\epsilon} \phi_{\eta'}^{\dagger} | n^{-1} \rangle$$

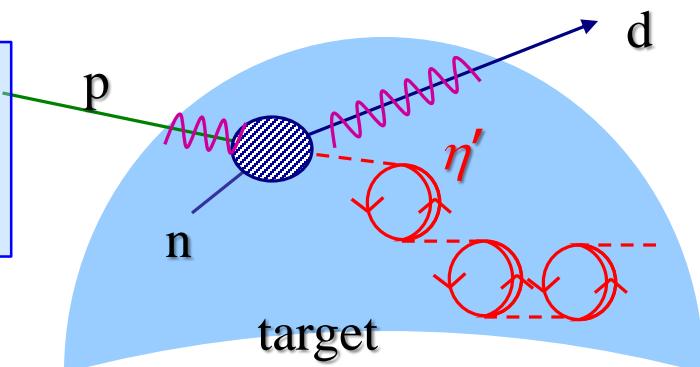
transition amplitude

$$T_{\alpha}(\mathbf{r}) = \chi_d^*(\mathbf{r}) \xi_{1/2, m_s}^* \left[Y_{l_{\eta'}}^*(\hat{r}) \otimes \psi_{j_n}(\mathbf{r}) \right]_{JM} \chi_p(\mathbf{r})$$

Distortion factor: flux reduction due to absorption

$$\chi_f^*(\mathbf{r}) \chi_i(\mathbf{r}) = \exp[i\mathbf{q} \cdot \mathbf{r}] F(b) \text{ eikonal approximation}$$

$$F(b) = \exp \left[-\frac{1}{2} \sigma_{iN} \int_{-\infty}^z dz' \rho_A(z', b) - \frac{1}{2} \sigma_{fN} \int_z^{\infty} dz' \rho_{A-1}(z', b) \right]$$



potential parameters

Energy independent optical potentials

$$V(r) = (V_0 + iW_0) \frac{\rho(r)}{\rho_0}$$

$V_0 \backslash W_0$	-150	-100	-50	0
-5	✓	✓	✓	
-10	✓	✓	✓	
-15	✓	✓	✓	
-20	✓	✓	✓	✓

in unit of MeV

cf.) NJL with KMT

$\Delta m_{\eta'} \sim -150 \text{ MeV} @ \rho_0$

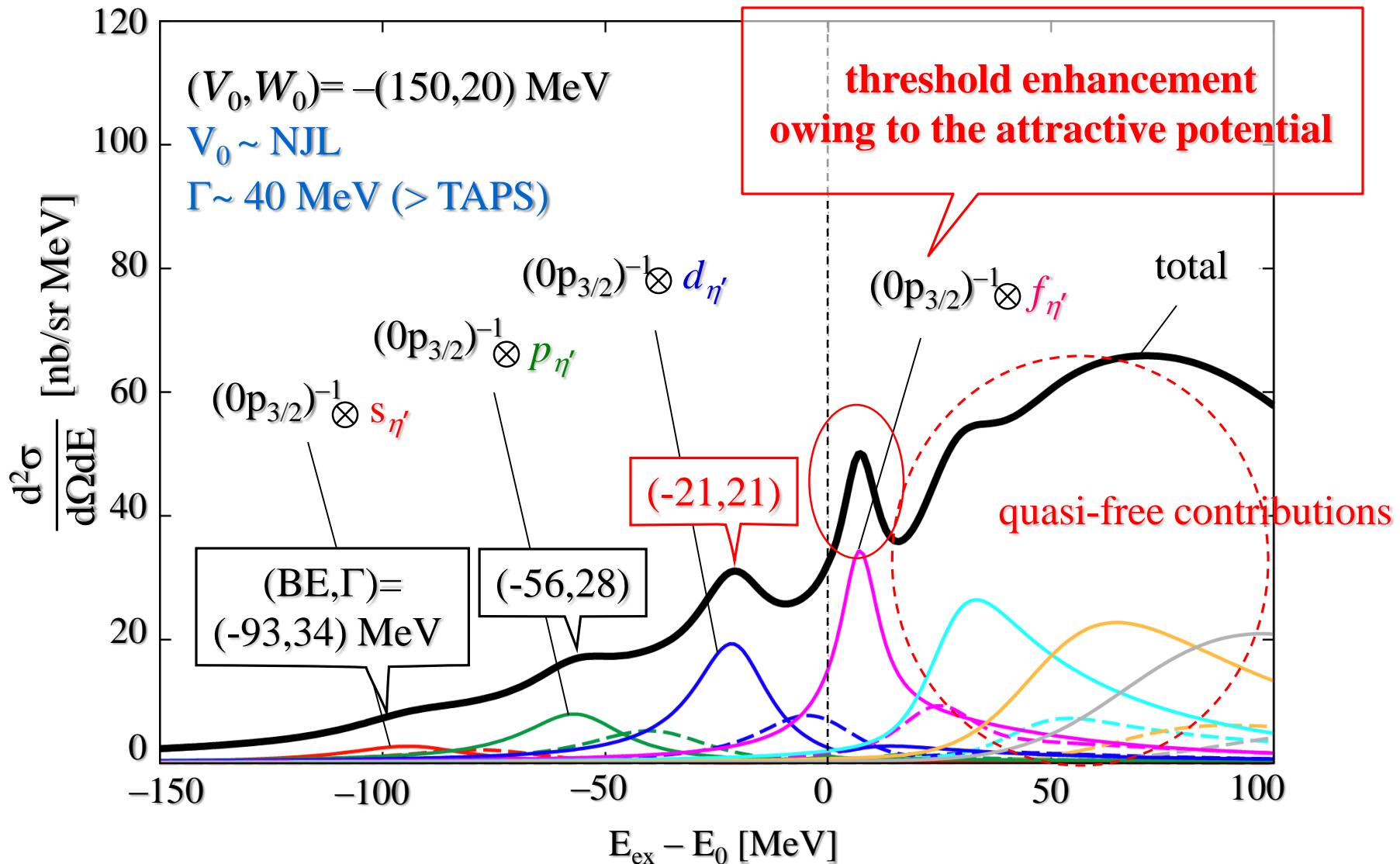
*cf.) coupled-channel
PLB709*

*cf.) CBELSA/TAPS
Transparency ratio*

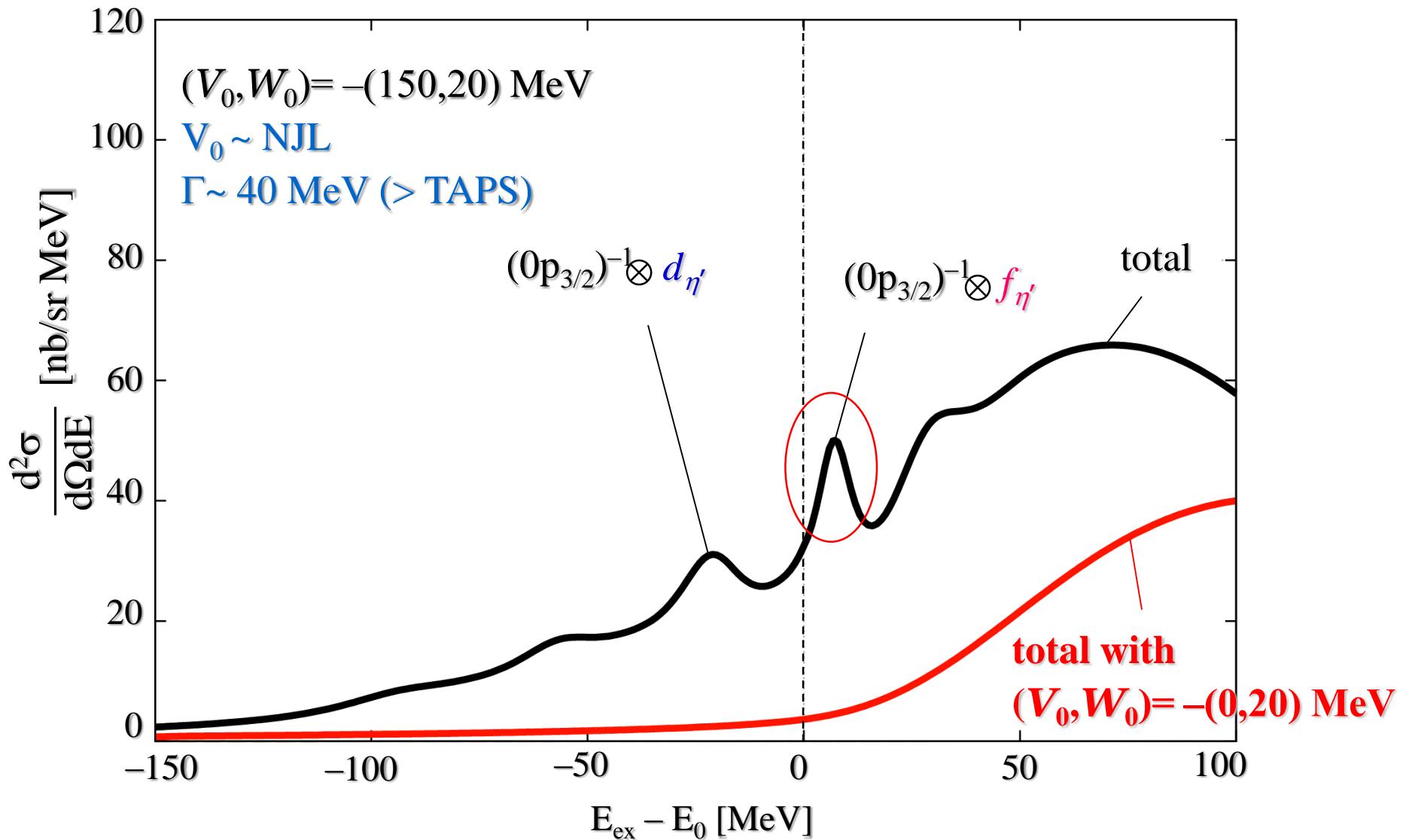
$\Gamma_{\eta'} \sim 10 - 25 \text{ MeV}$

To see observation feasibility, we consider various combinations of ReV and ImV.

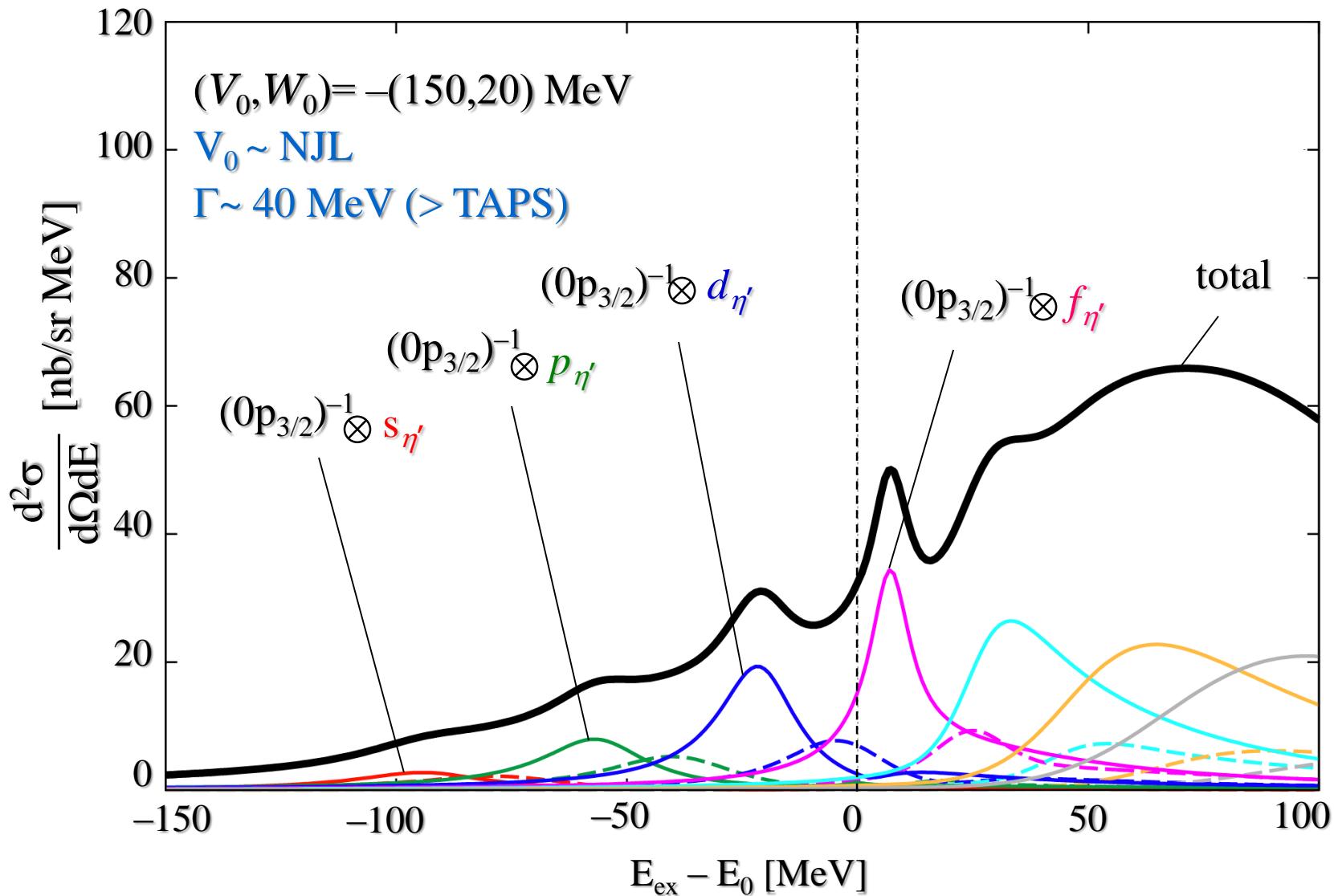
Numerical results : $-(150, 20)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



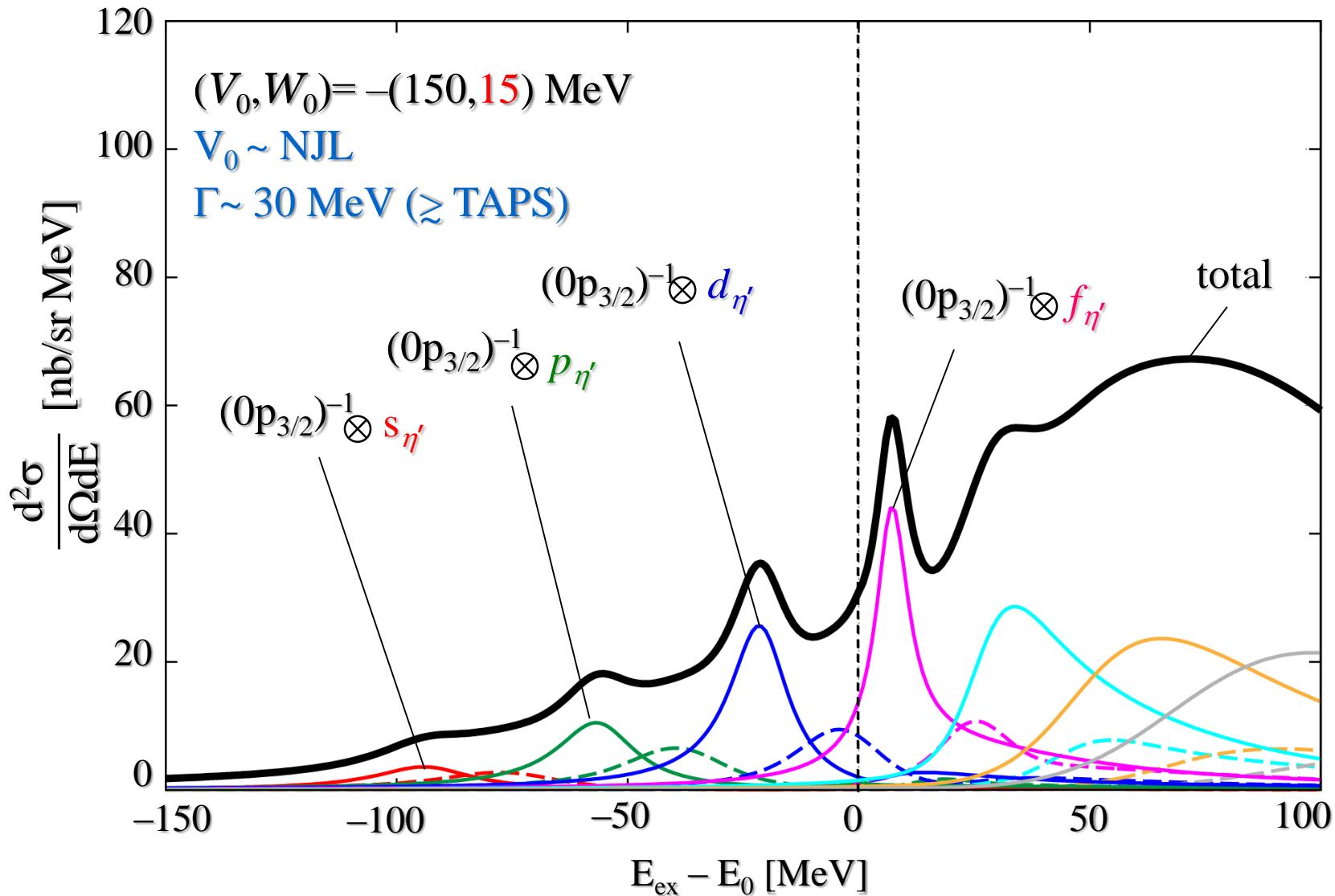
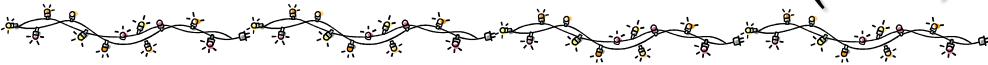
Numerical results : $-(150, 20)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



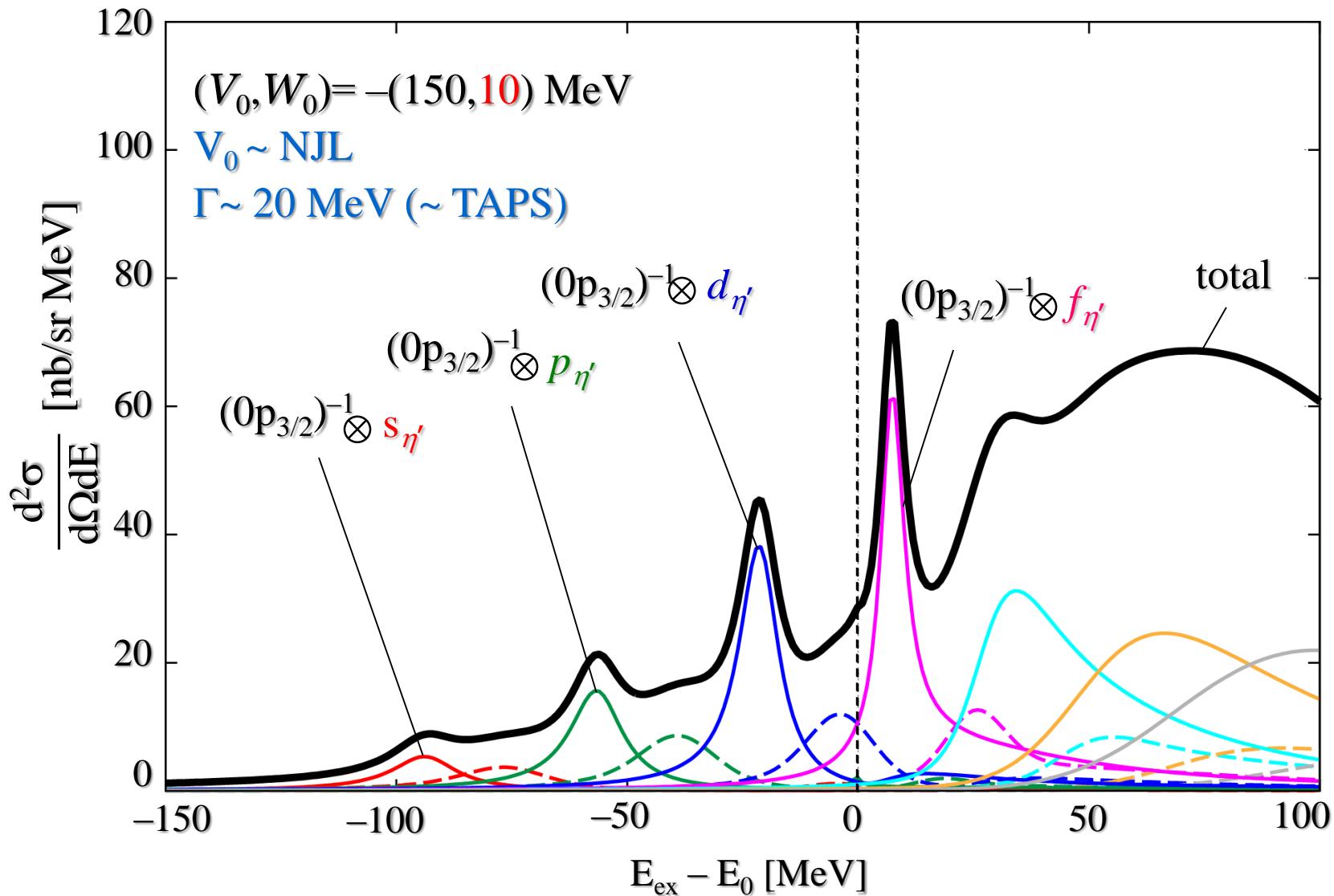
Numerical results : $-(150, 20)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



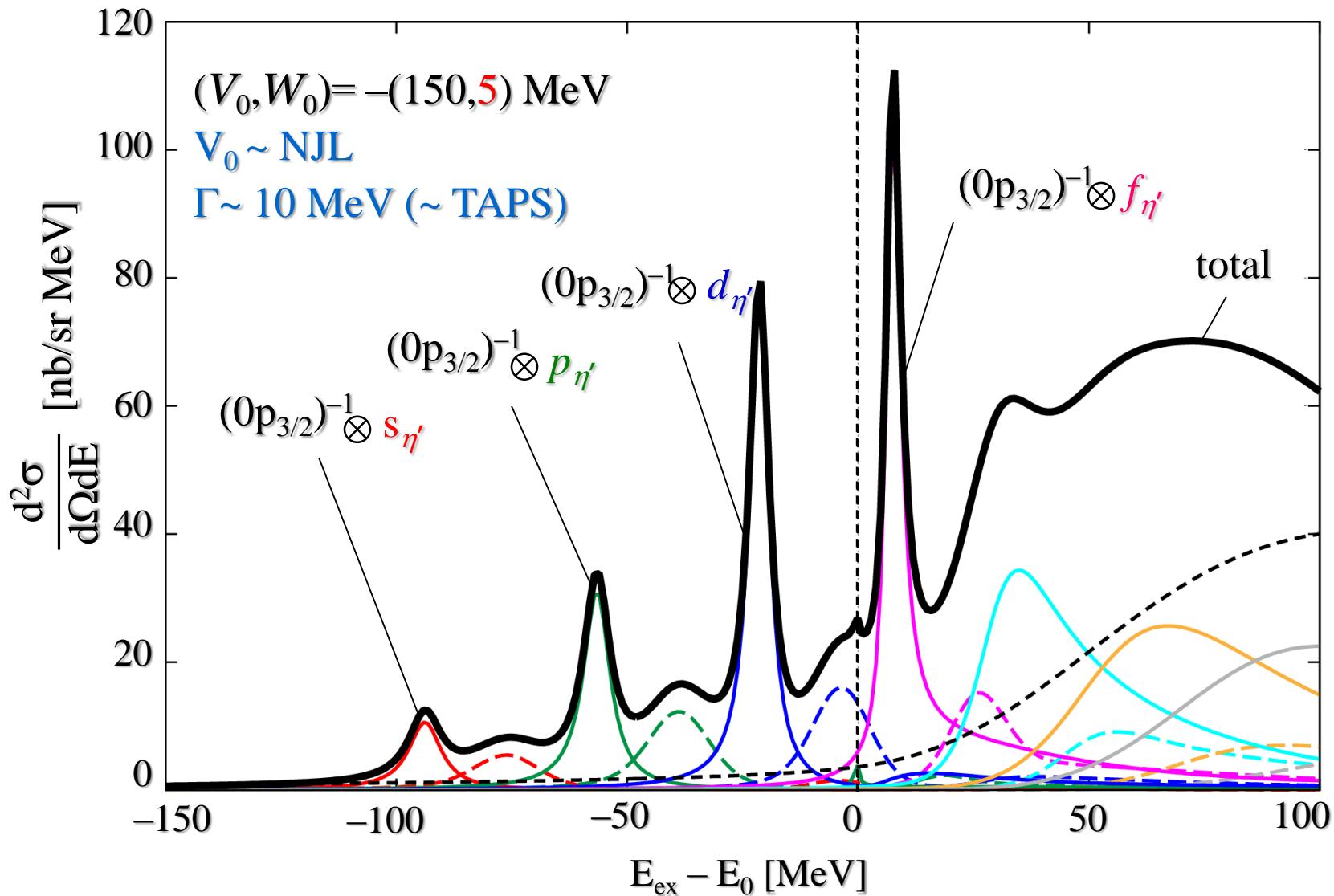
Numerical results : $-(150, 15)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



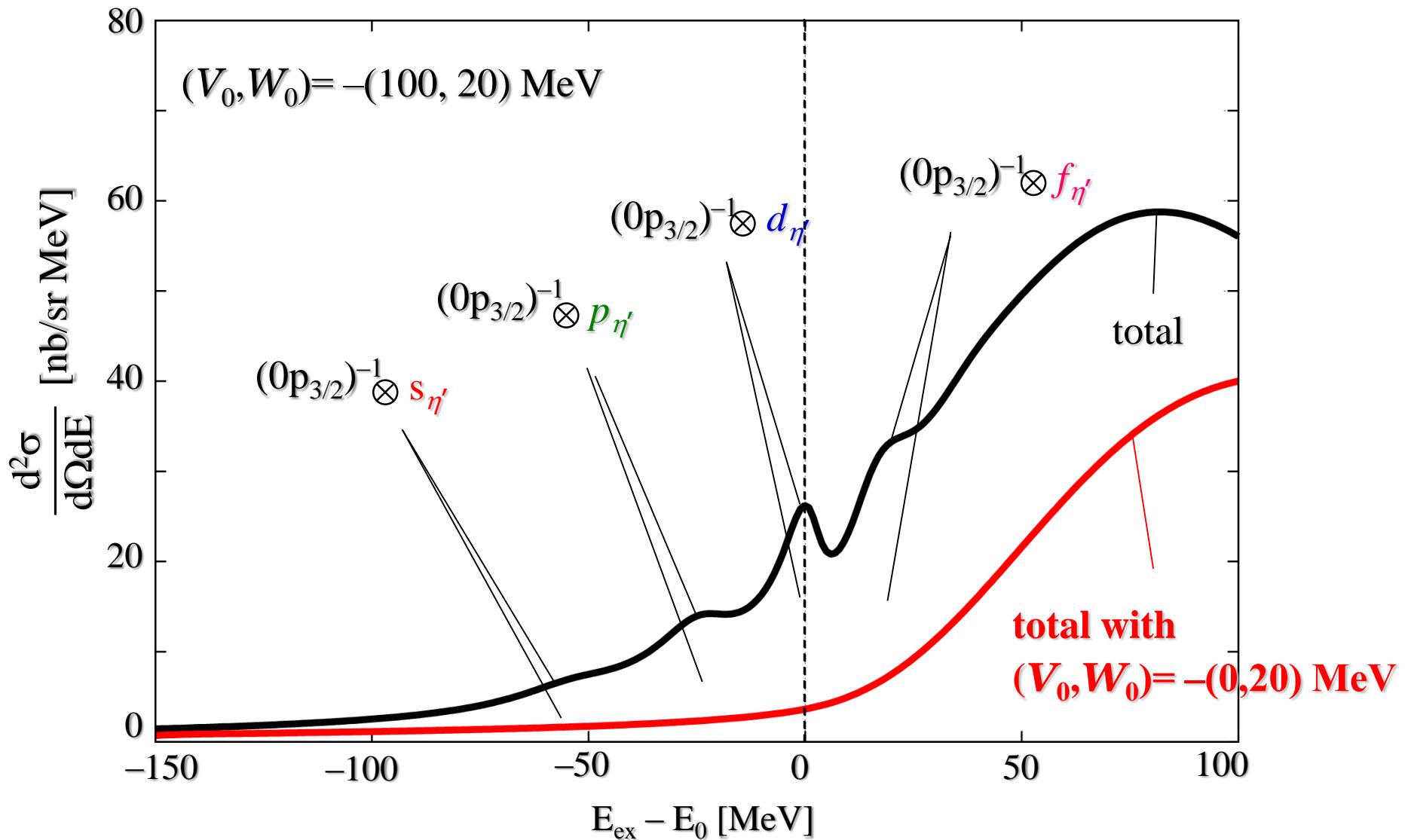
Numerical results : $-(150, 10)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



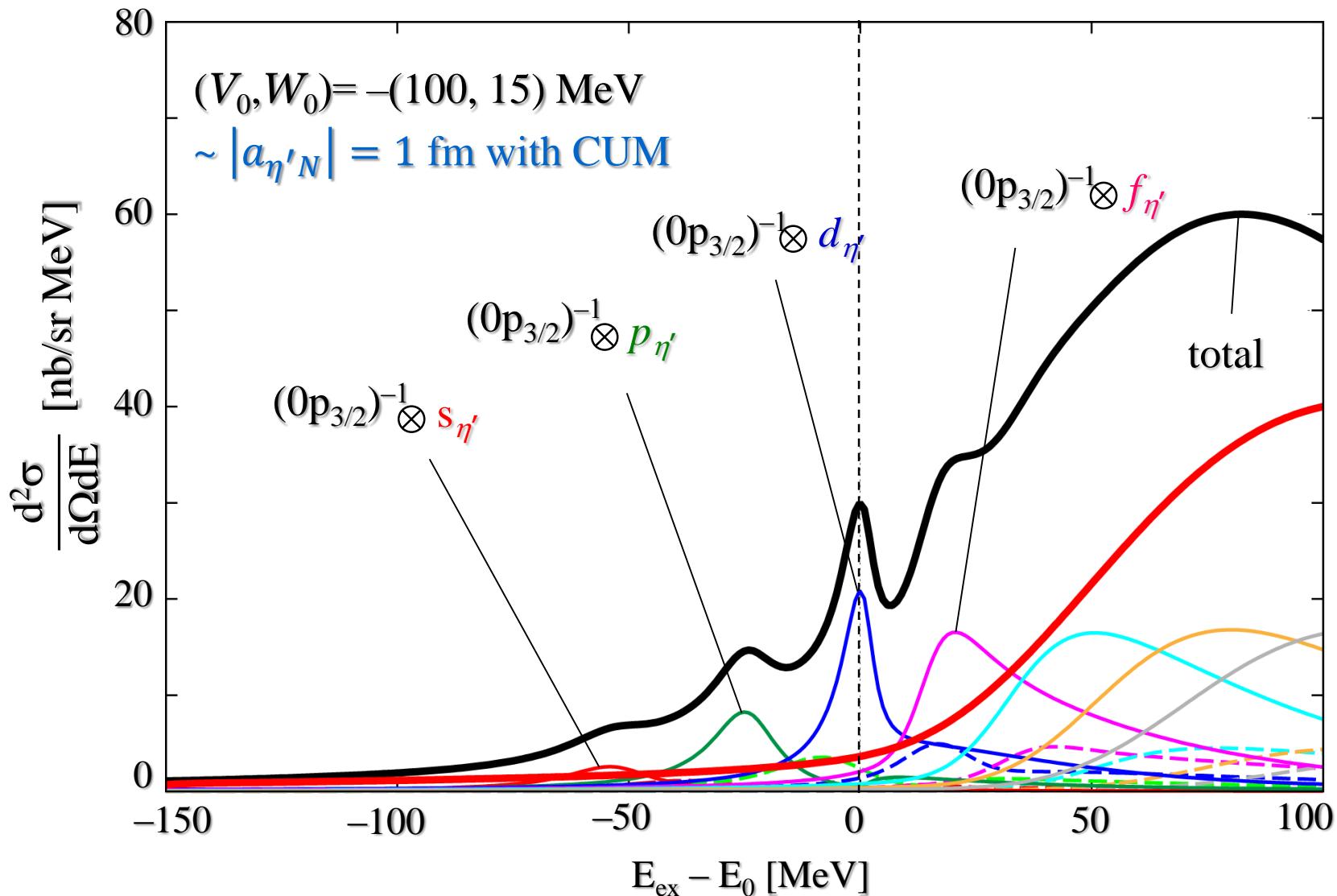
Numerical results : $-(150, 5)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



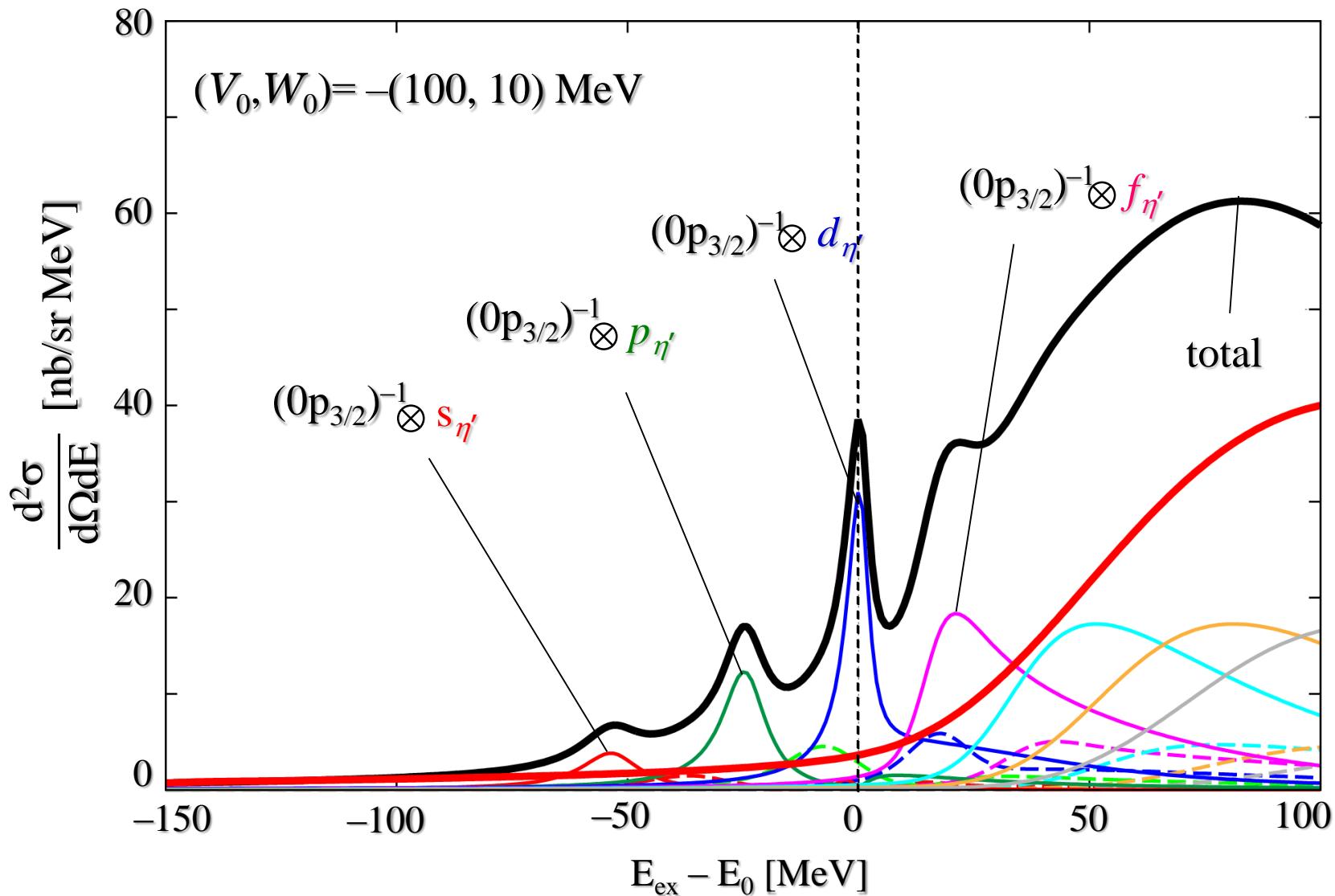
Numerical results : $-(100, 20)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



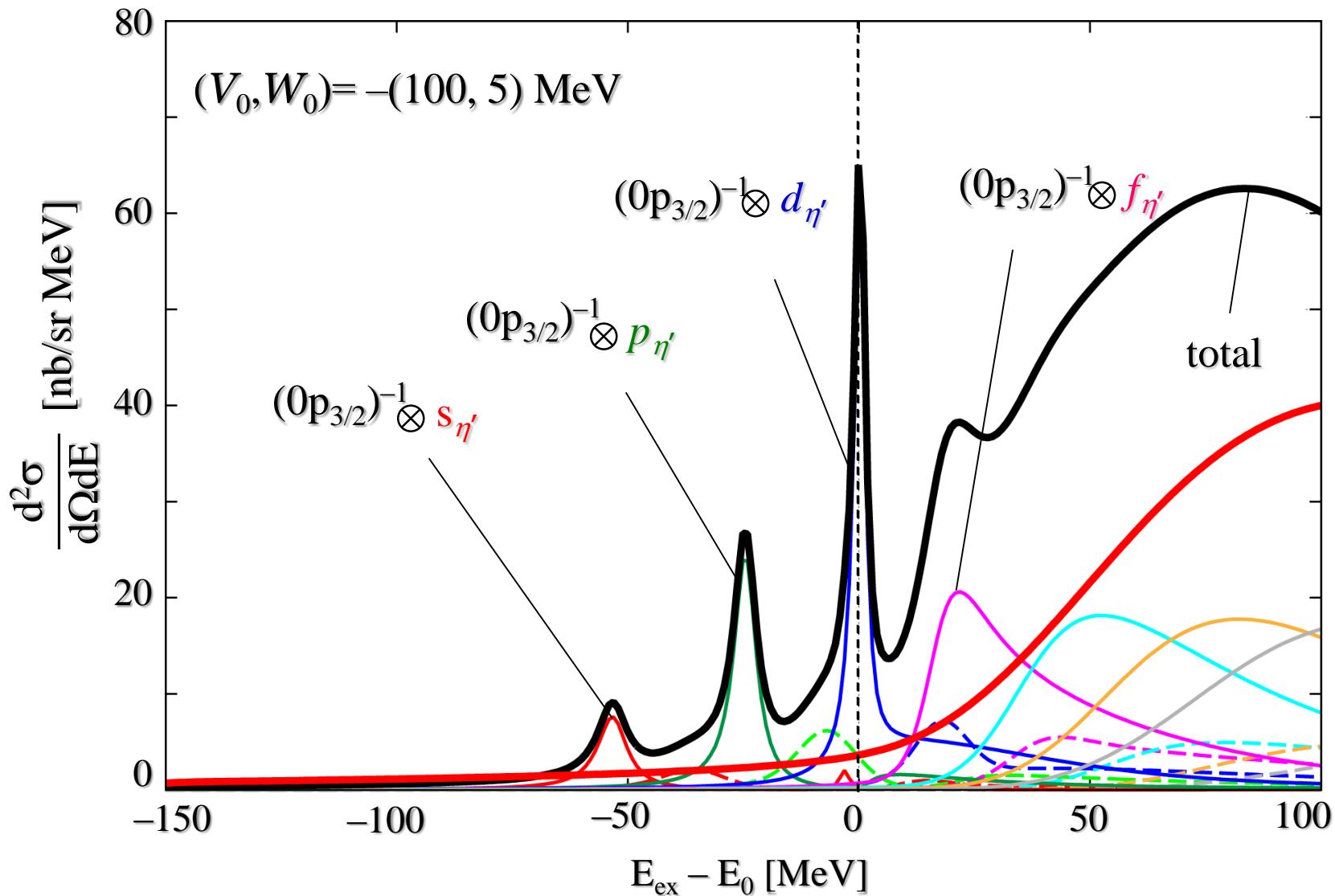
Numerical results : $-(100, 15)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



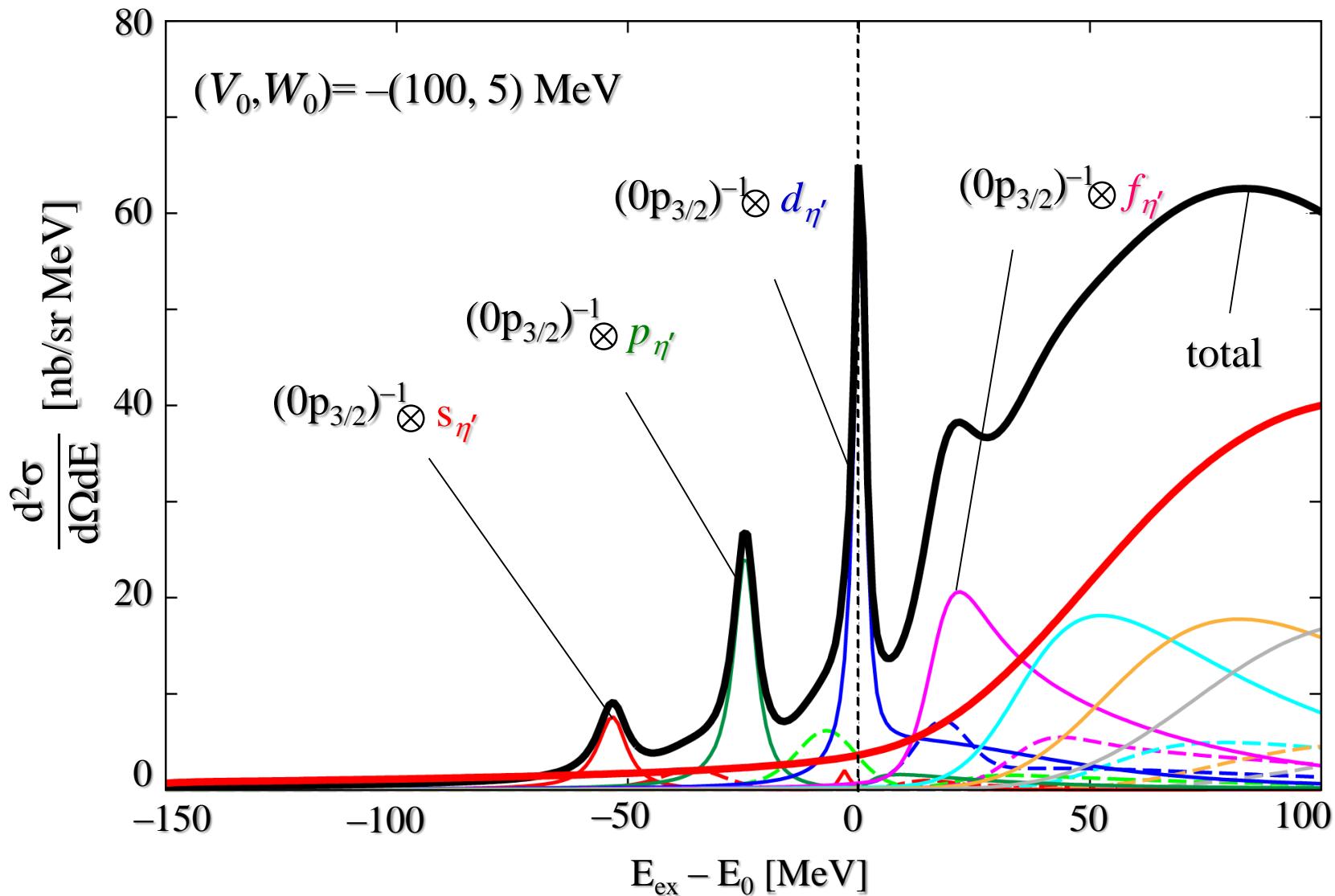
Numerical results : $-(100, 10)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



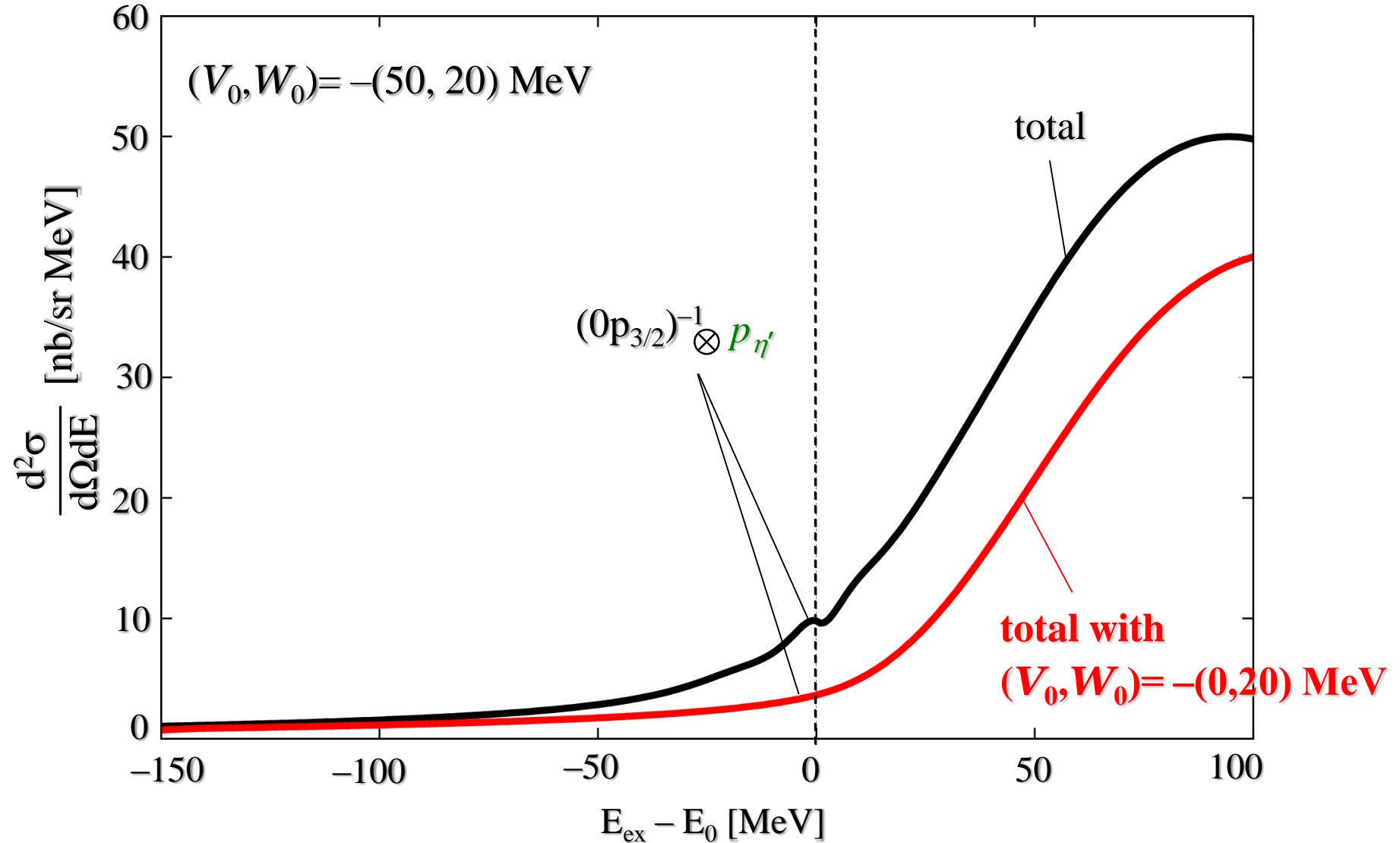
Numerical results : $-(100, 5)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



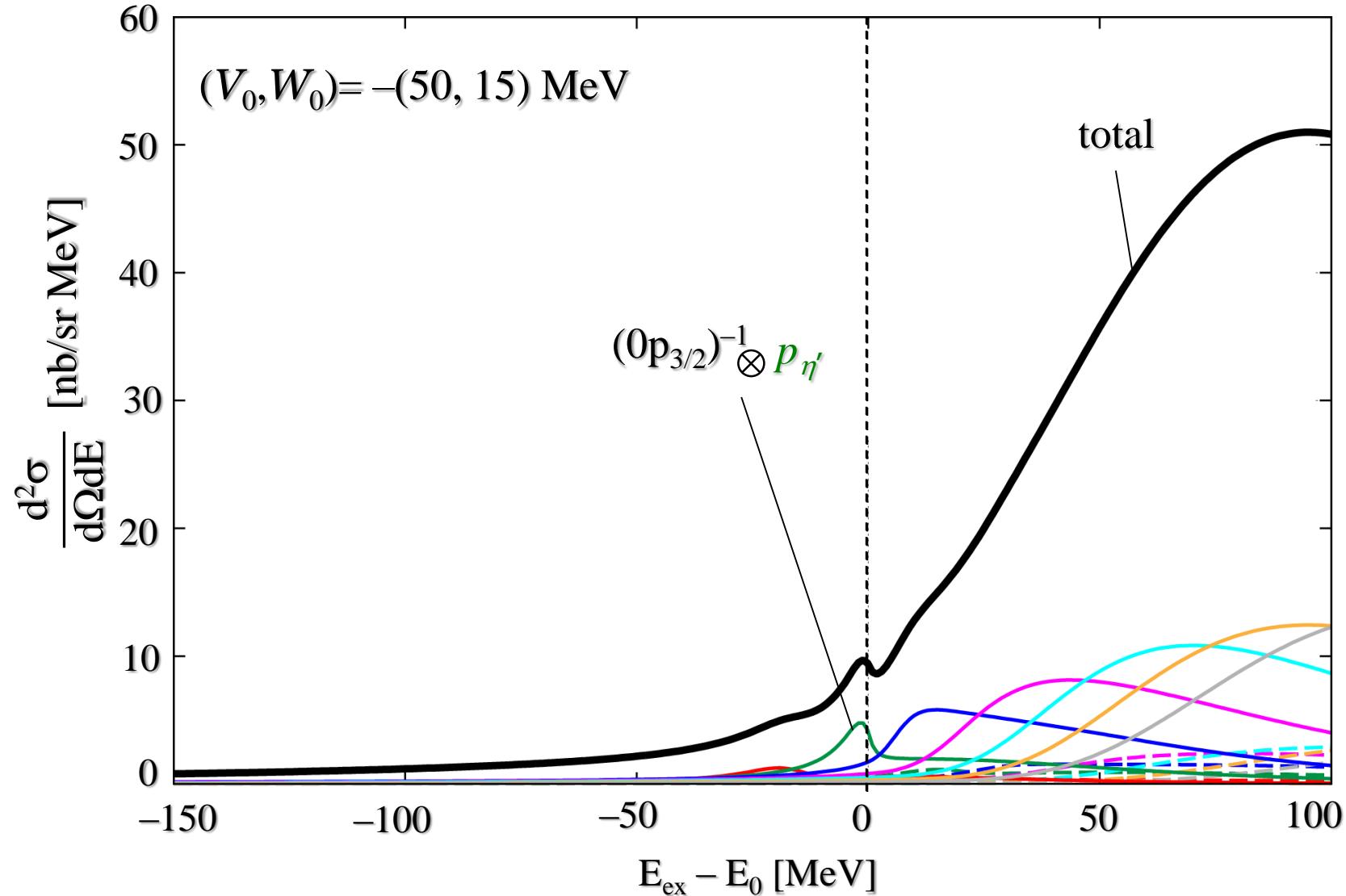
Numerical results : $-(100, 5)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



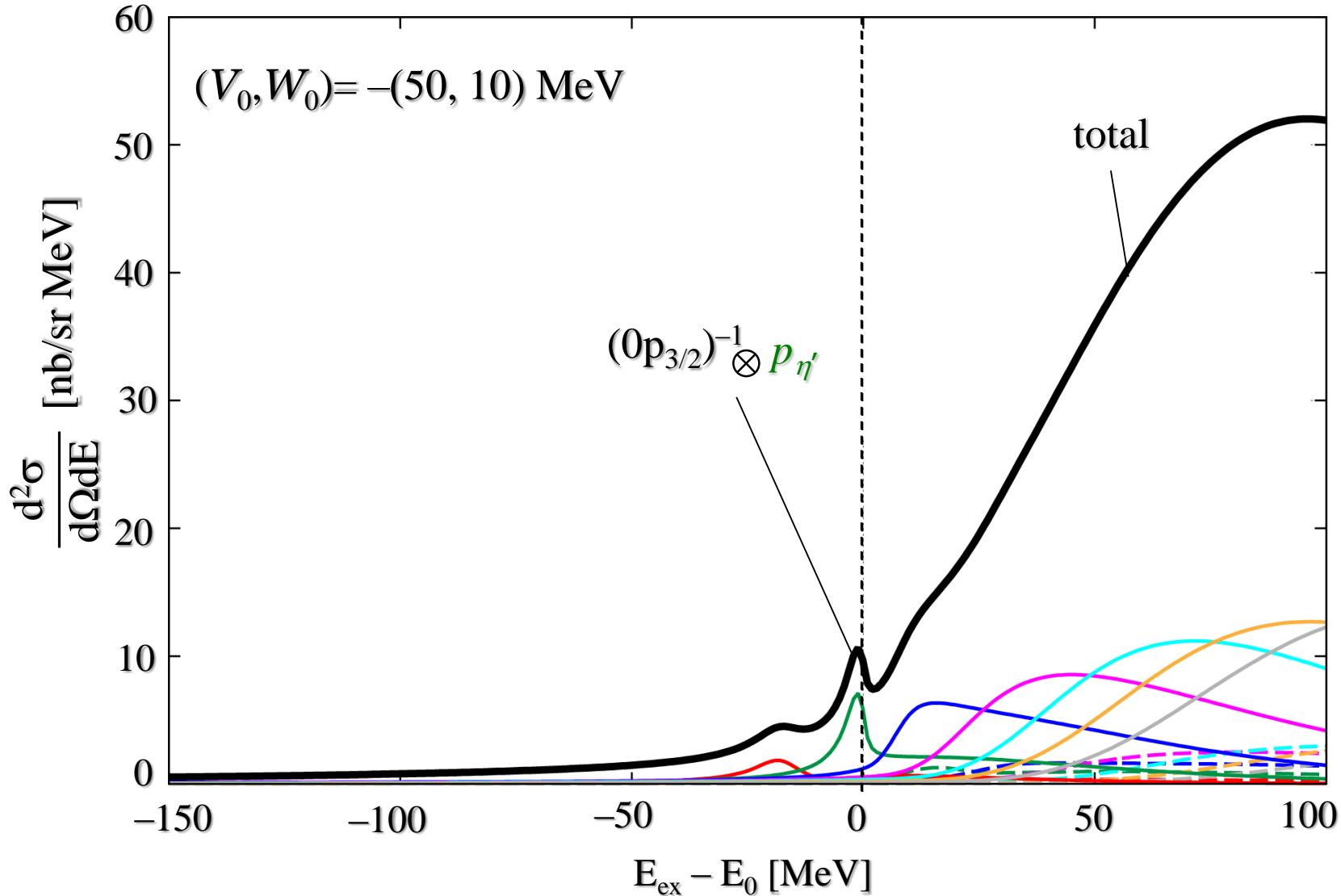
Numerical results : $-(50, 20)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



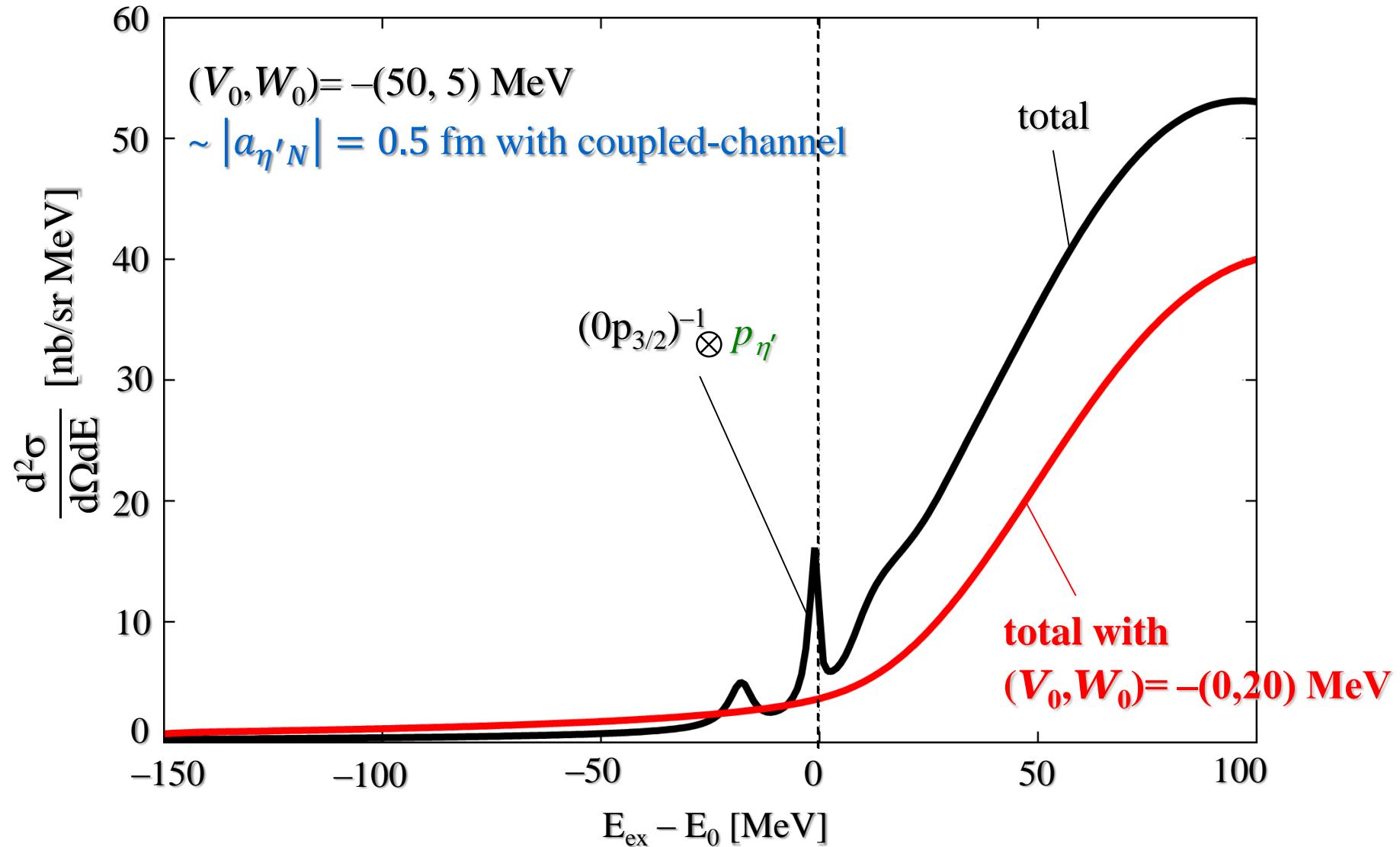
Numerical results : $-(50, 15)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$

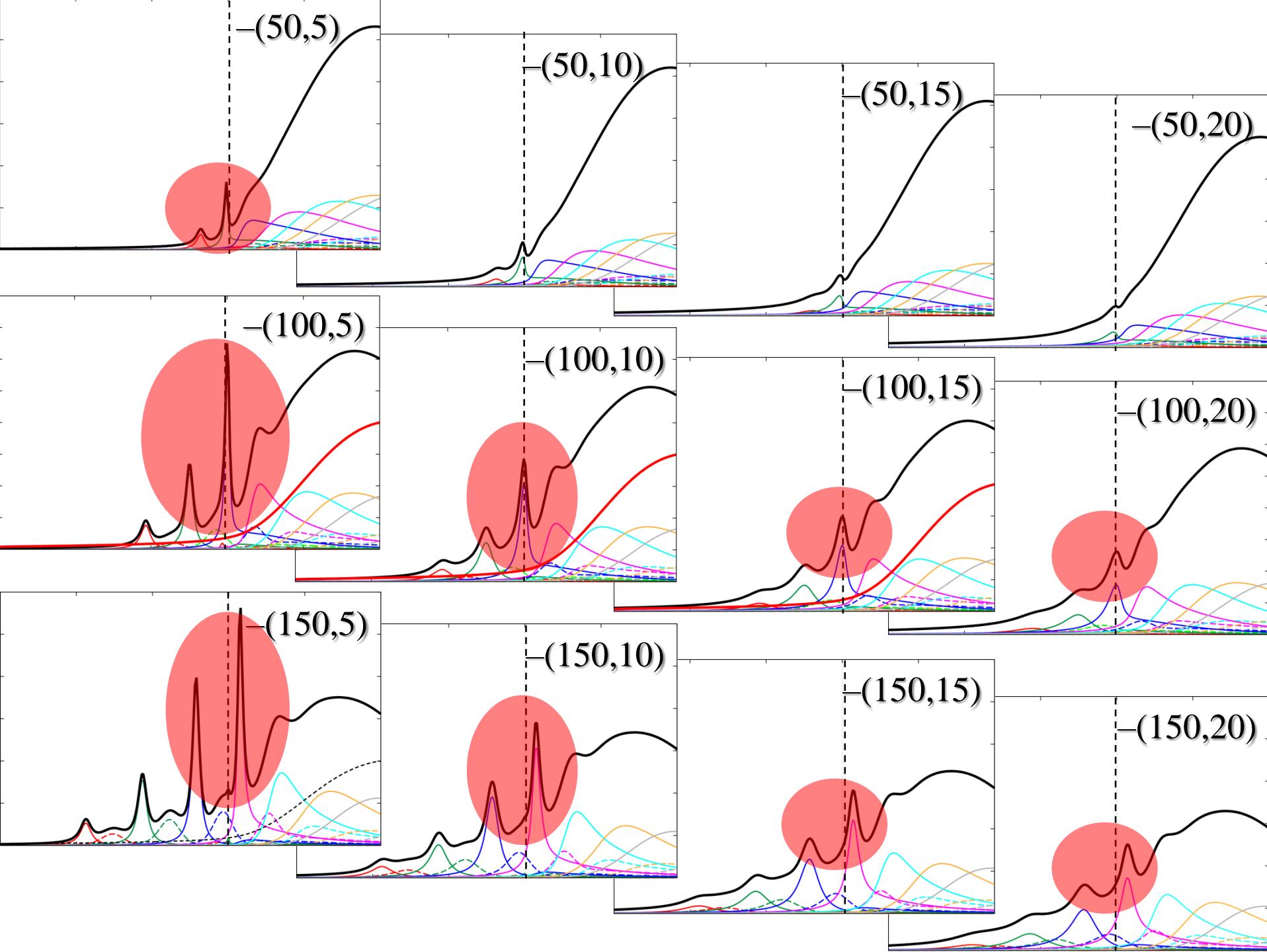


Numerical results : $-(50, 10)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$



Numerical results : $-(50, 5)$ MeV : $^{12}\text{C}(\text{p},\text{d})^{11}\text{C}_{\eta'}$

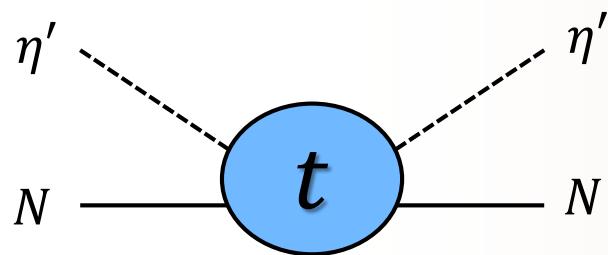




Revisiting $\eta'N$ scattering amplitude considering a **possible $\eta'N$ bound state**



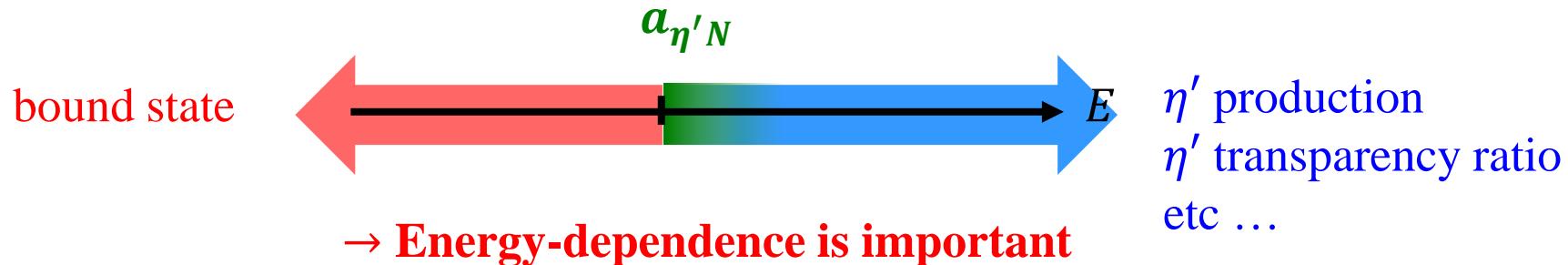
A. Hinata, A. Kiyomura, M. Sakamoto, H.N., S. Hirenzaki, in progress
(Nara Women's Univ.)



on-going theoretical works

We are now revisiting the $\eta'N$ scattering and η' -nucleus optical potential $V_{\eta'}$

- ✓ We have estimated $\text{Re}(V_{\eta'})$ and $\text{Im}(V_{\eta'})$ by using $T_{\eta'N \rightarrow \eta'N}$ [Oset-Ramos(2011)]
at $\eta'N$ threshold value



- ✓ different model for **vector-meson-baryon channel**

[K. P. Khemchandani, A. Martinez Torres H. N. and A. Hosaka, PRD88(13)114016]

- ✓ considering “possibility to have **$\eta'N$ bound state**”

→ subtraction const. positive → negative value ($\Lambda \sim 1\text{GeV}$)

(Oset-Ramos, PLB)

(Hinata *et al.*)

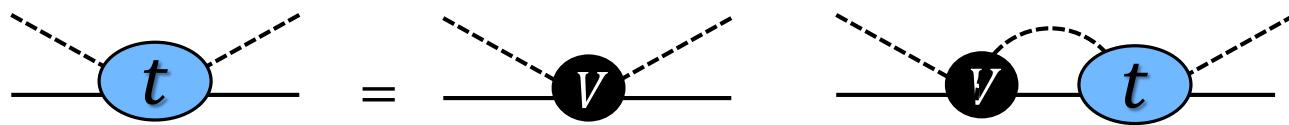
- ✓ trying to extract **possible α value**

→ $\eta'N$ scattering length, $\pi N \rightarrow \eta'N$ production, η' transparency ratio, ...
& also η' -mesic nuclei formation, ...

- ✓ different model for **vector-meson-baryon** channel

K. P. Khemchandani, A. Martinez Torres, H. N. and A. Hosaka, PRD88(13)114016

Unitarized scattering amplitude by coupled-channel BS eq.



Interaction kernel V

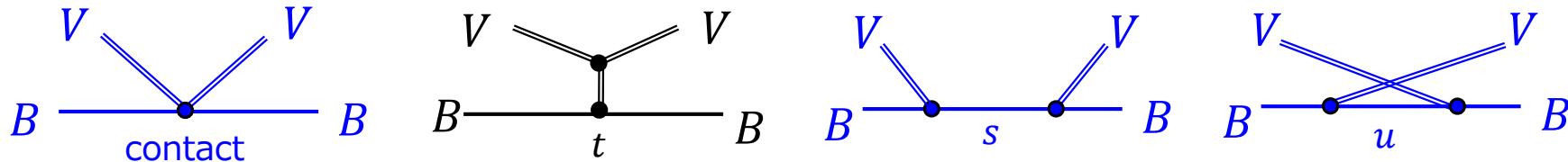
(1) Weinberg-Tomozawa interaction : pseudoscalar-baryon (PB) channel

$$\pi N, \eta N, K\Lambda, K\Sigma \quad \begin{array}{c} P \\ | \\ B \end{array} \quad \begin{array}{c} P \\ | \\ B \end{array}$$

V_{WT}

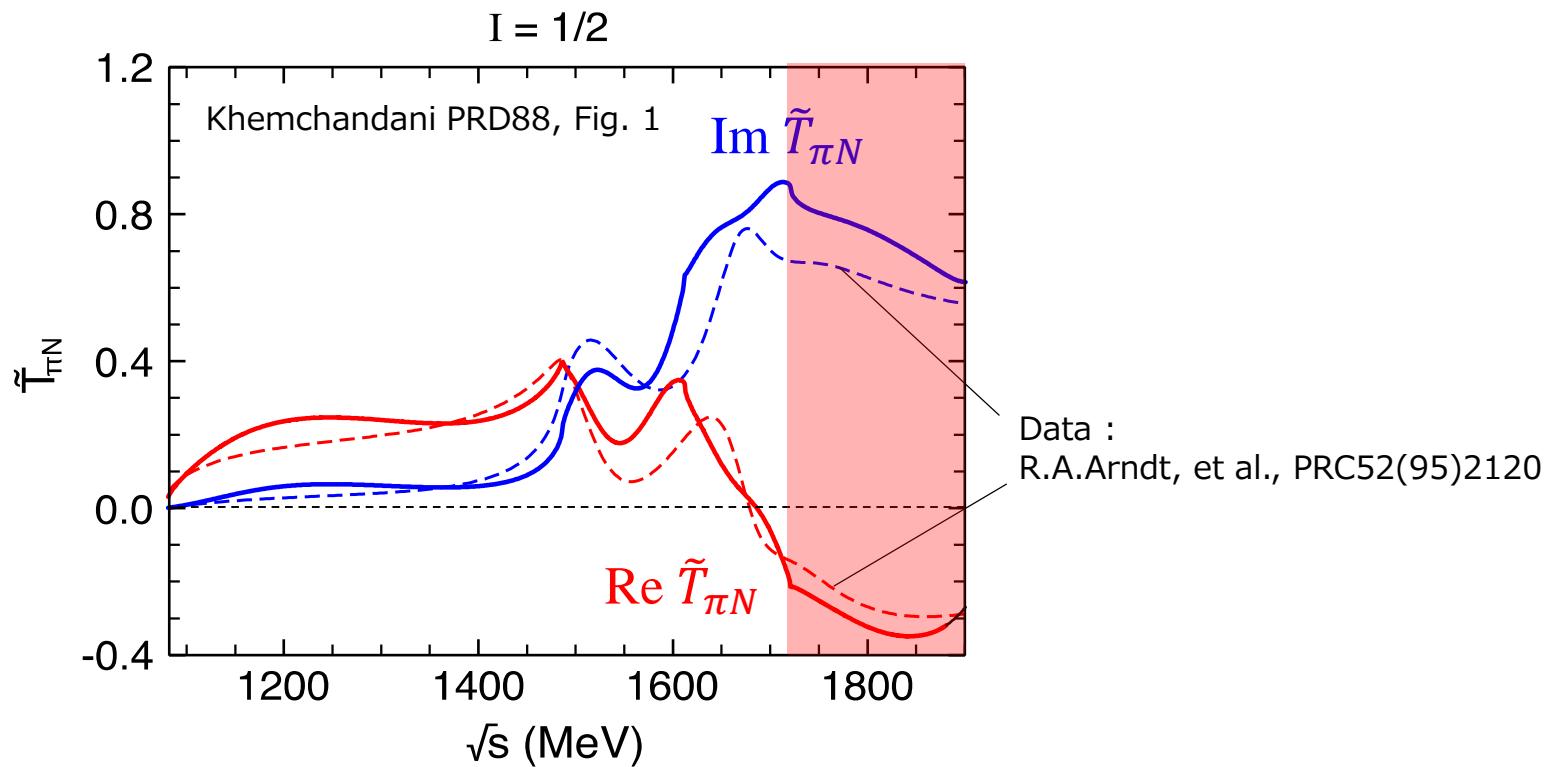
(2) Vector meson-baryon (VB) channel

$$\rho N, \omega N, \phi N, K^* \Sigma, K^* \Lambda$$



✓ different model for **vector-meson-baryon** channel

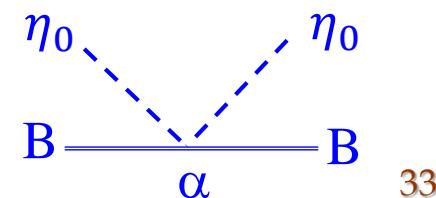
K. P. Khemchandani, A. Martinez Torres, H. N. and A. Hosaka, PRD88(13)114016



$\pi N \rightarrow \pi N$ scattering amplitude ... good agreement at $\sqrt{s} \sim 1.9$ GeV

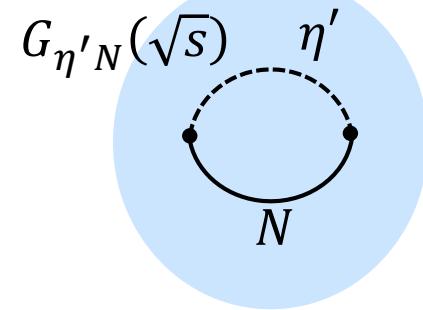
Hinata, Kiyomura, Sakamoto (Nara WU.)

→ we add $\eta'N$ channel in V_{WT} through $\eta\text{-}\eta'$ mixing
and $V_{\eta_0 B}$ (singlet- η Baryon interaction) as well



✓ considering “possibility to have $\eta'N$ bound state”

→ subtraction const. positive → negative value ($\Lambda \sim 1\text{ GeV}$)



subtraction constants for the loop function

[Oset-Ramos-PLB, and our previous work]

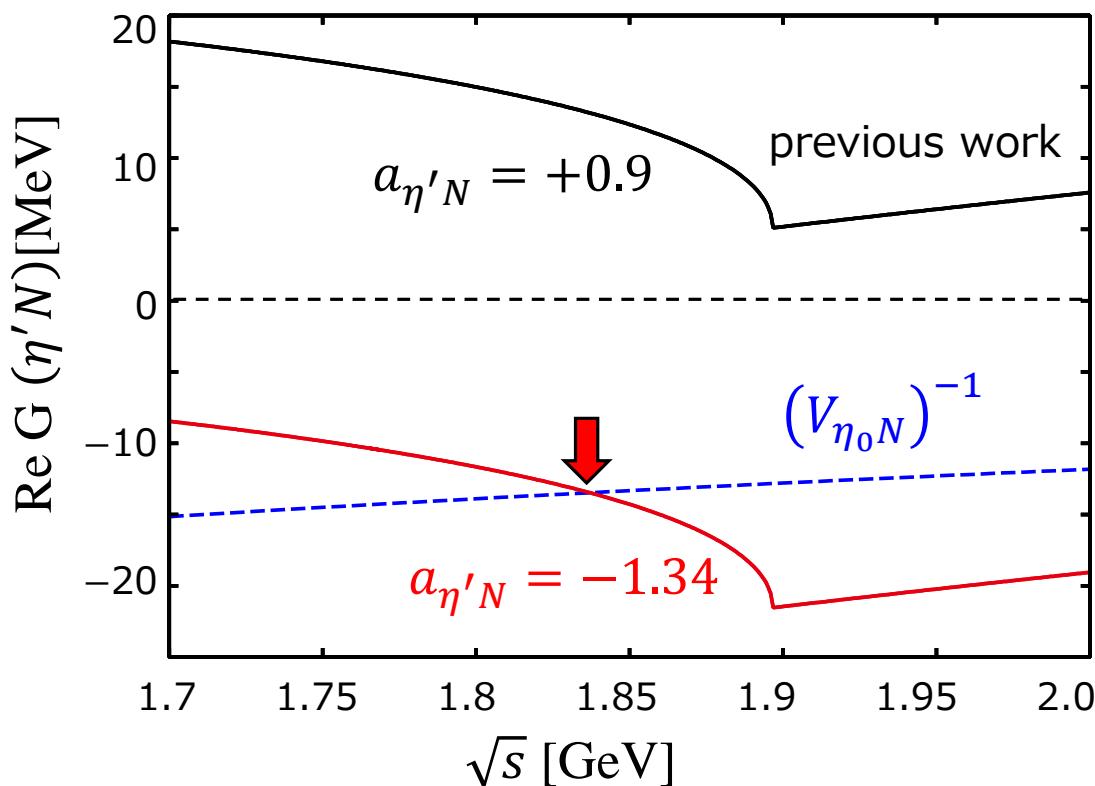
$$a_{\pi N}, a_{\eta N}, a_{K\Sigma}, a_{K\Lambda} \quad a_{\eta'N} = a_{\eta N} = 0.9$$



$$a_{\eta'N} = -1.34$$

→ to reproduce $N^*(1535)$ (Inoue et al., PRC65)

$\Lambda \sim 1\text{ GeV}/c$



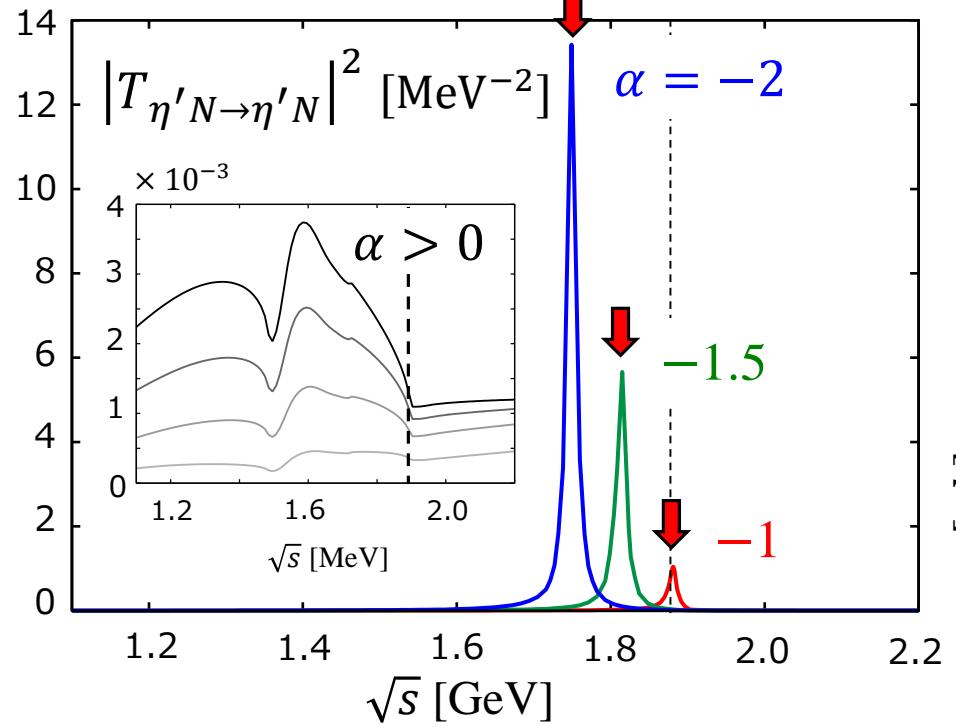
$$(V_{\eta_0 N})^{-1} - G(\sqrt{s}) = 0$$

→ $\eta'N$ bound state
due to $\eta_0 B$ coupling ?

$\eta'N$ bound state and $\sigma_{\pi N \rightarrow \eta'N}$

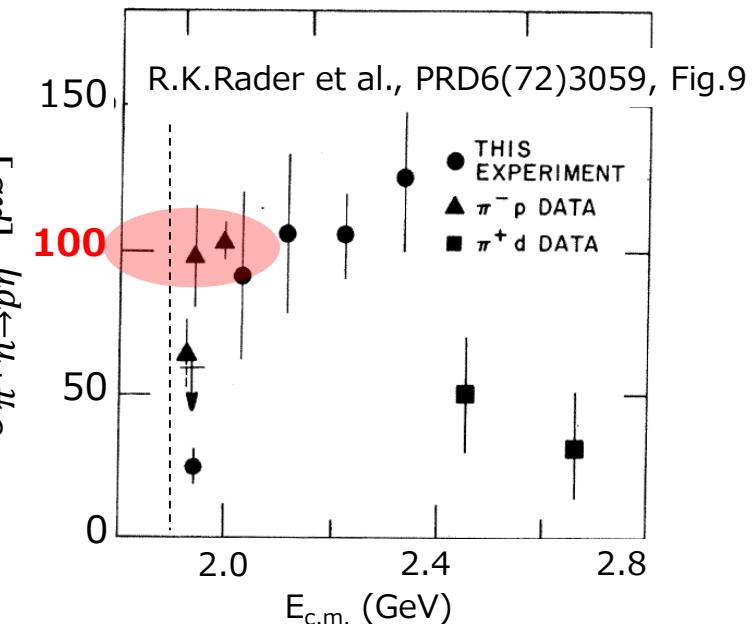
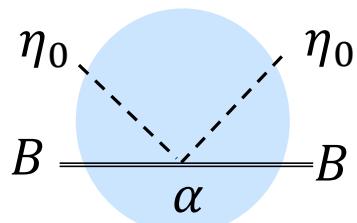
by Hinata, Kiyomura, Sakamoto [Nara WU.]

$\eta'N \rightarrow \eta'N$ scattering amplitude

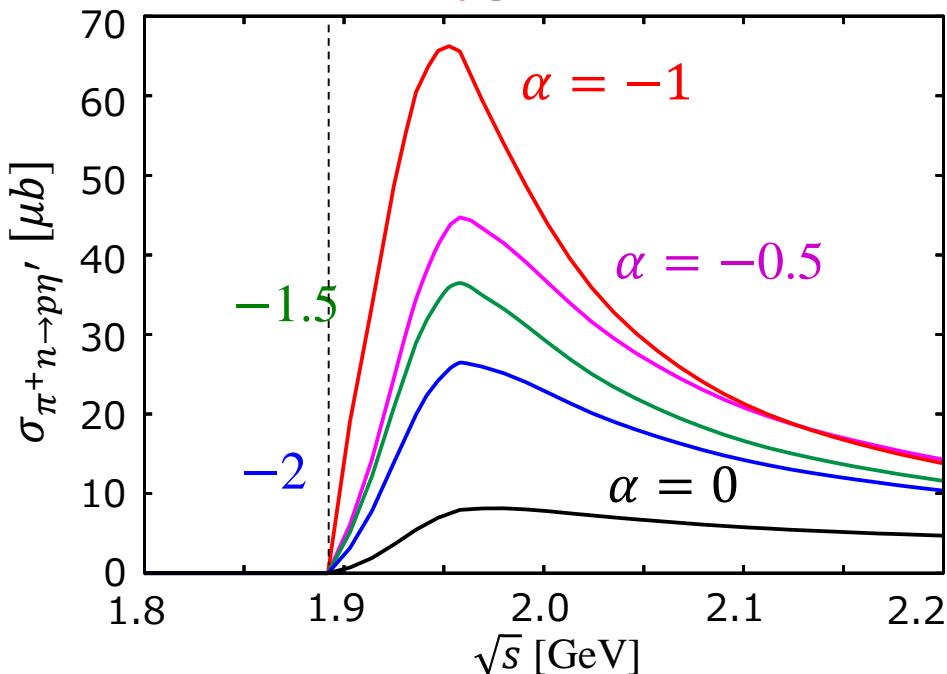


$\eta'N$ bound state

cf.) S. Sakai and D. Jido,
PRC88(13)064906,
based on linear σ model



$\pi^+ n \rightarrow \eta' p$ cross section

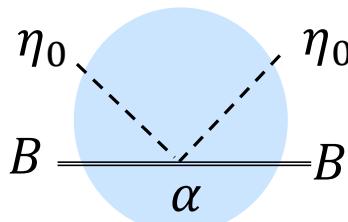
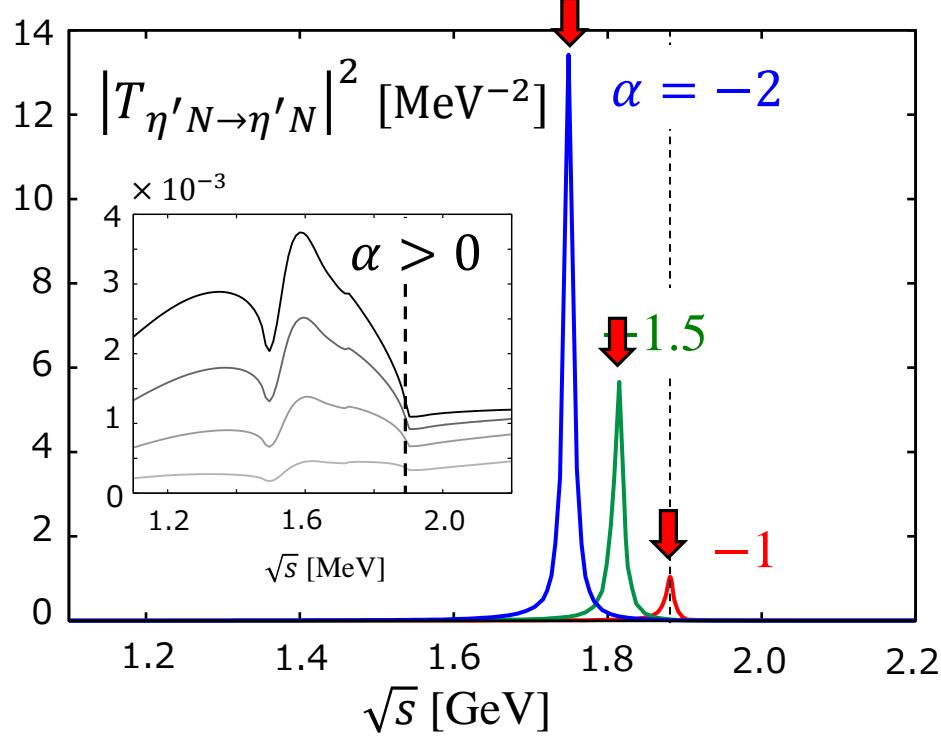


$\eta'N$ scattering length



✓ small scattering length

$\eta'N \rightarrow \eta'N$ scattering amplitude

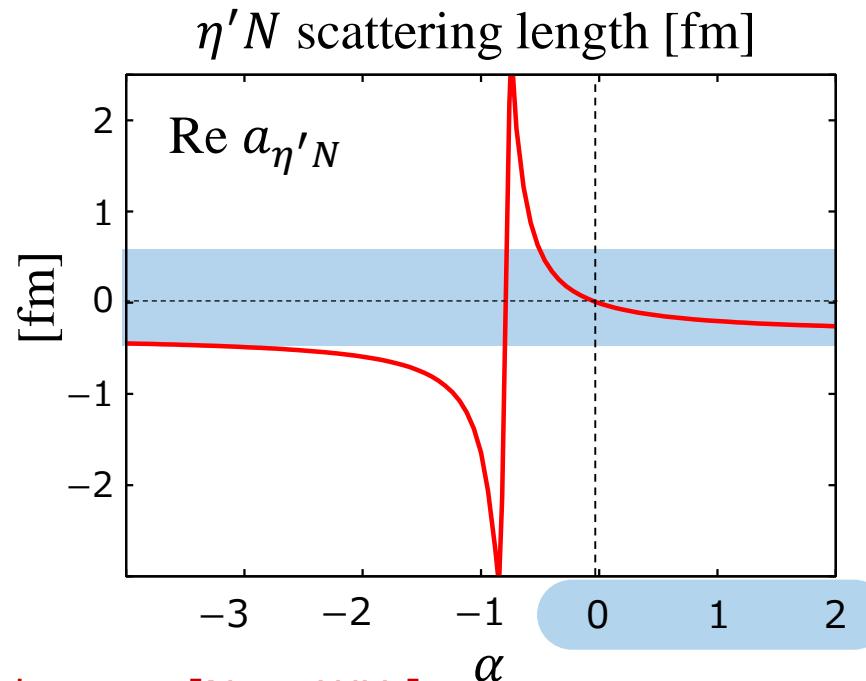


by Hinata, Kiyomura, Sakamoto [Nara WU.]

$$\text{Re}(a_{\eta'p}) = 0 \pm 0.43 \text{ fm}$$

$$\text{Im}(a_{\eta'p}) = 0.37 \begin{array}{l} +0.40 \\ -0.16 \end{array} \text{ fm}$$

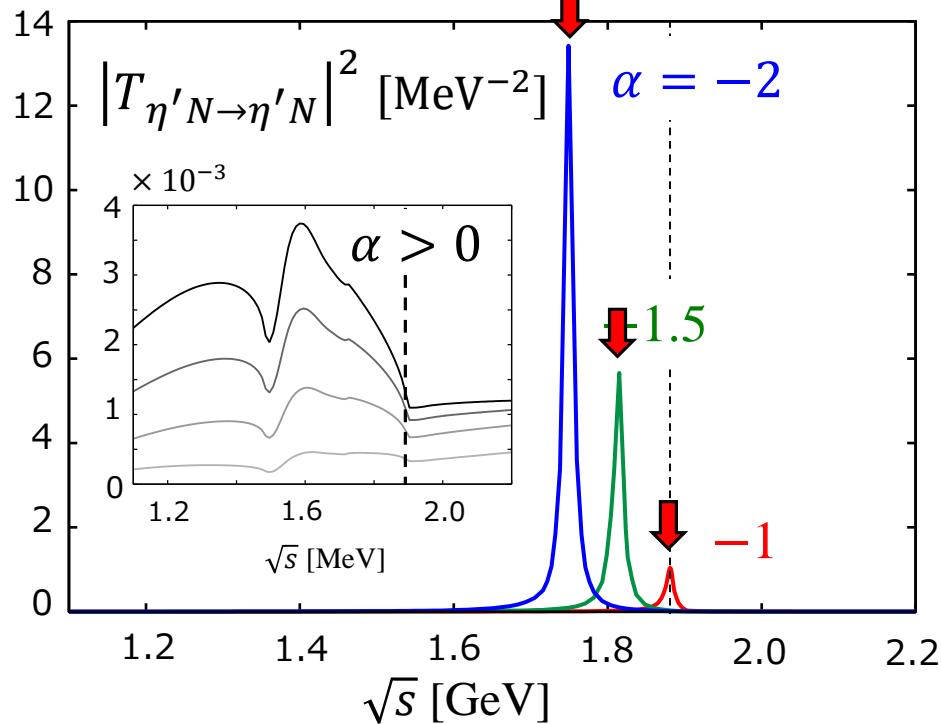
[E. Czerwinski *et al.*, (COSY-11),
PRL113(14)062004]



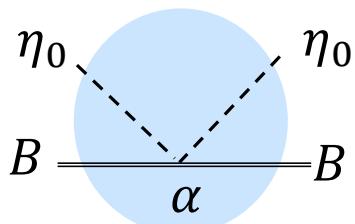
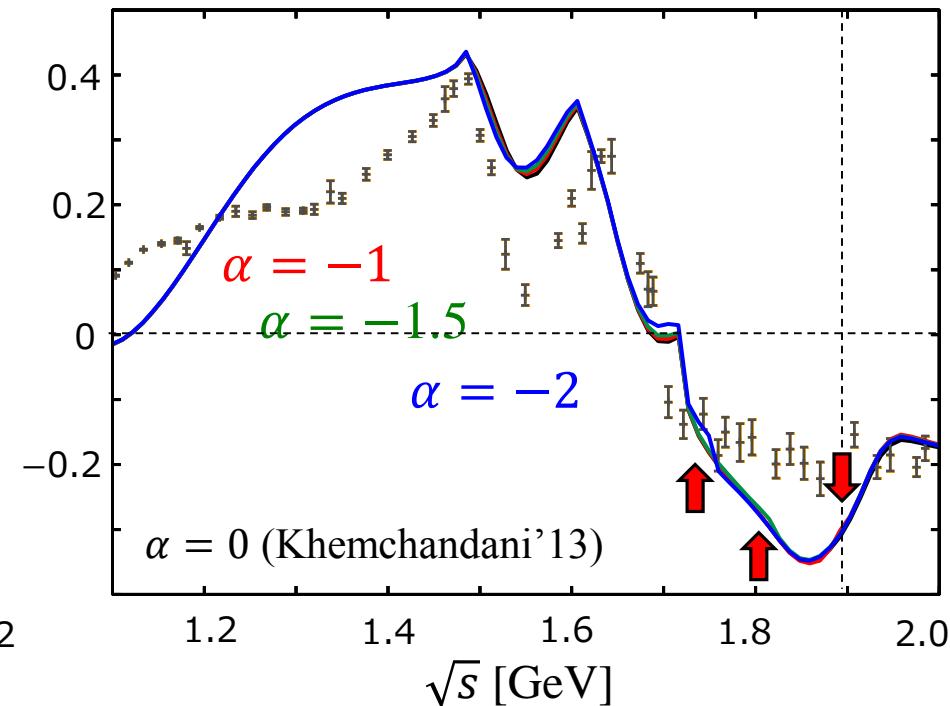
πN scattering amplitudes

by Hinata, Kiyomura, Sakamoto [Nara WU.]

$\eta' N \rightarrow \eta' N$ scattering amplitude



πN amplitude (real part)



such a “narrow N^* ” exists ??

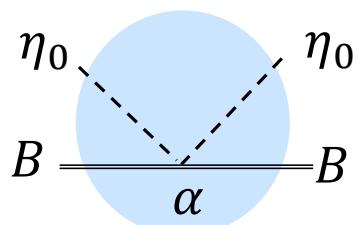
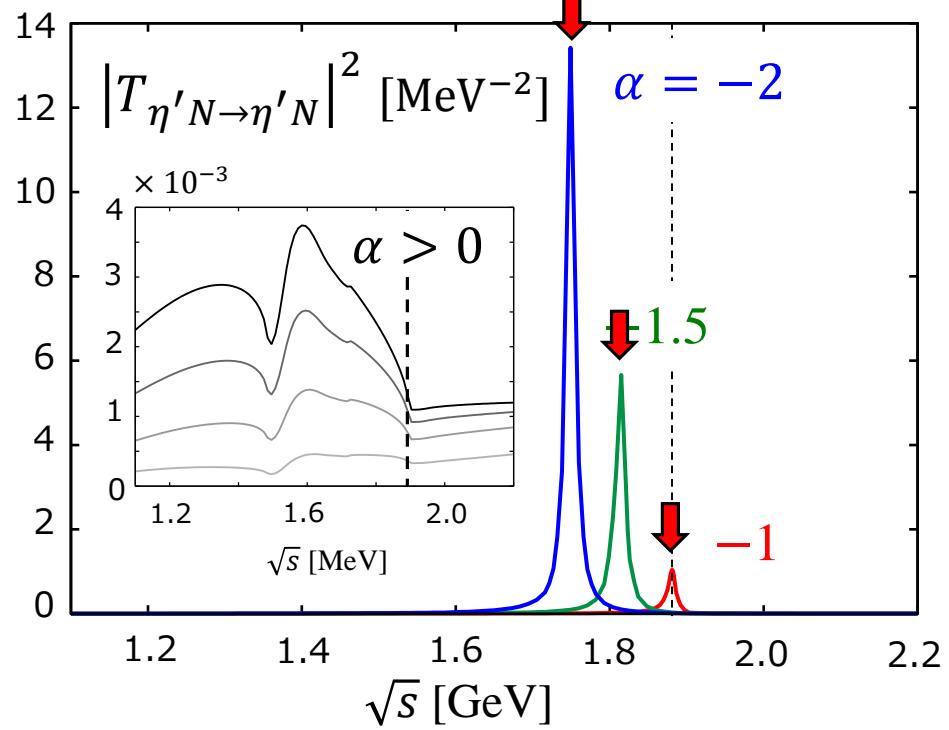
... at least it does not couple to πN due to its singlet char.

data : CNS, <http://gwdac.phys.gwu.edu/>

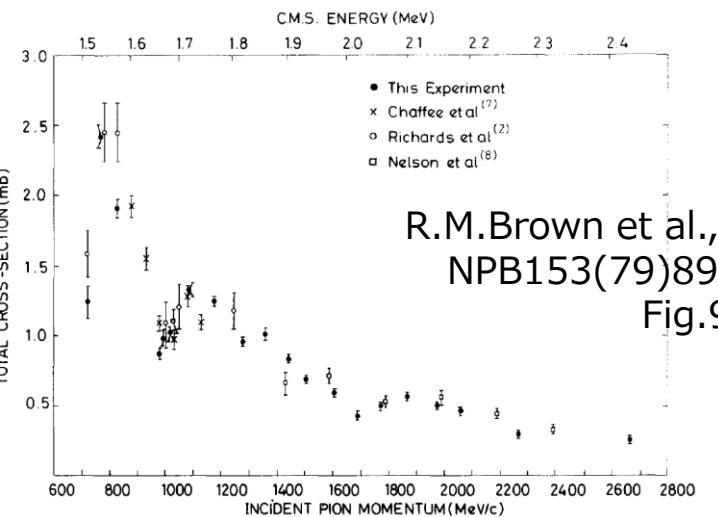
$\sigma_{\pi N \rightarrow \eta N}$ cross section

by Hinata, Kiyomura, Sakamoto [Nara WU.]

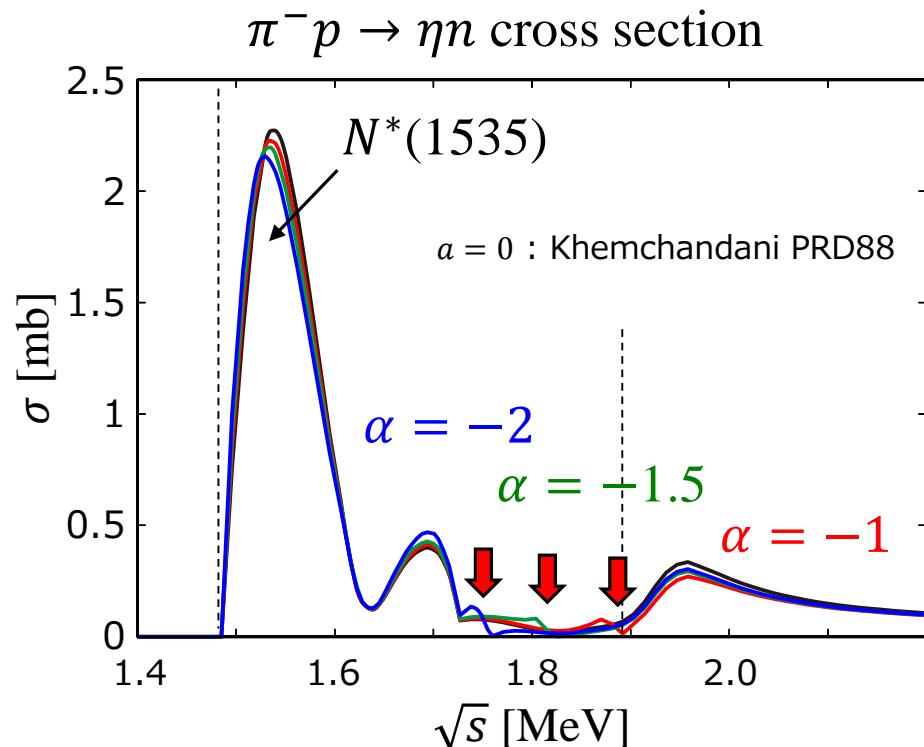
$\eta' N \rightarrow \eta' N$ scattering amplitude



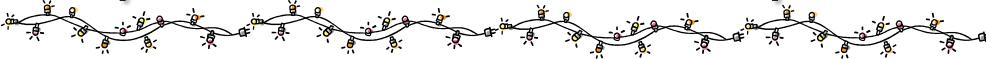
$\eta' N$ b.s. cannot be seen in η production



R.M.Brown et al.,
NPB153(79)89,
Fig.9



$\eta'N$ bound state $\Leftrightarrow \eta'$ -nucleus bound state ?



- ✓ $\pi N \rightarrow \eta'N$ is **sensitive** to V_{η_0B} interaction (α), where, however, the $\eta'N$ bound state **cannot be reached** (above the threshold)
- ✓ The $\eta'N$ bound state **does not appear** in the π or η production, because it couples to $\eta'N$ channel selectively due to its singlet character.
- ✓ The large $\pi N \rightarrow \eta'N$ production prefers the **attractive** V_{η_0B} , while the small scattering length prefers **zero or repulsive** V_{η_0B} .
- ✓ $\eta'N$ b.s. must play an **important role in η' -nucleus** optical potentials, which gives **strong energy dependence**.

$\eta'N$ b.s. can be found as (deeply) η' -nucleus bound state ?

Summary : η' (958)-meson-nucleus bound system

**Partial restoration of Chiral sym and $U_A(1)$ anomaly effect
in the viewpoint of mesic-nuclei**

(possible) large mass reduction **without** large absorption

$$\text{Re}V \gg \text{Im}V$$

- special feature of η'
- ✓ attraction from contact interaction
 - ✓ smaller inelastic channel

possibilities to observe bound state peaks

ongoing theoretical works in NaraWU

- ✓ Considering $\eta'N$ bound state
- ✓ estimate possible α (strength of singlet meson-baryon int.)
 - ↔ transparency ratio of η'
 - ↔ $\pi N \rightarrow \eta'N$ cross section
 - ↔ $\eta'N$ scattering length and so on...