

Neutrino-induced meson productions

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Analysis of $\gamma N, \pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$ data

→ baryon resonance properties extracted

Extension to $\nu N \rightarrow \bar{l} X$ ($X = \pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$)

★ Results for $\nu N \rightarrow \bar{l} X$

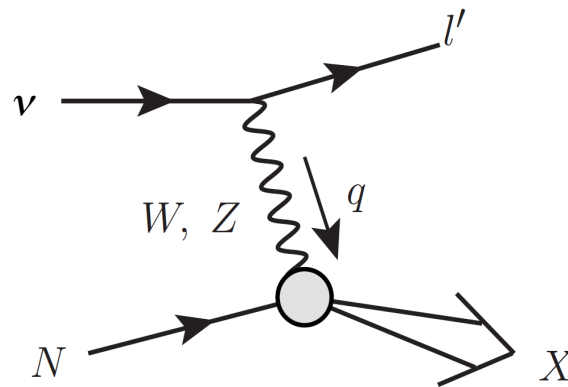
Introduction

Neutrino-nucleus scattering for ν -oscillation experiments

Next-generation exp. \rightarrow leptonic CP , mass hierarchy

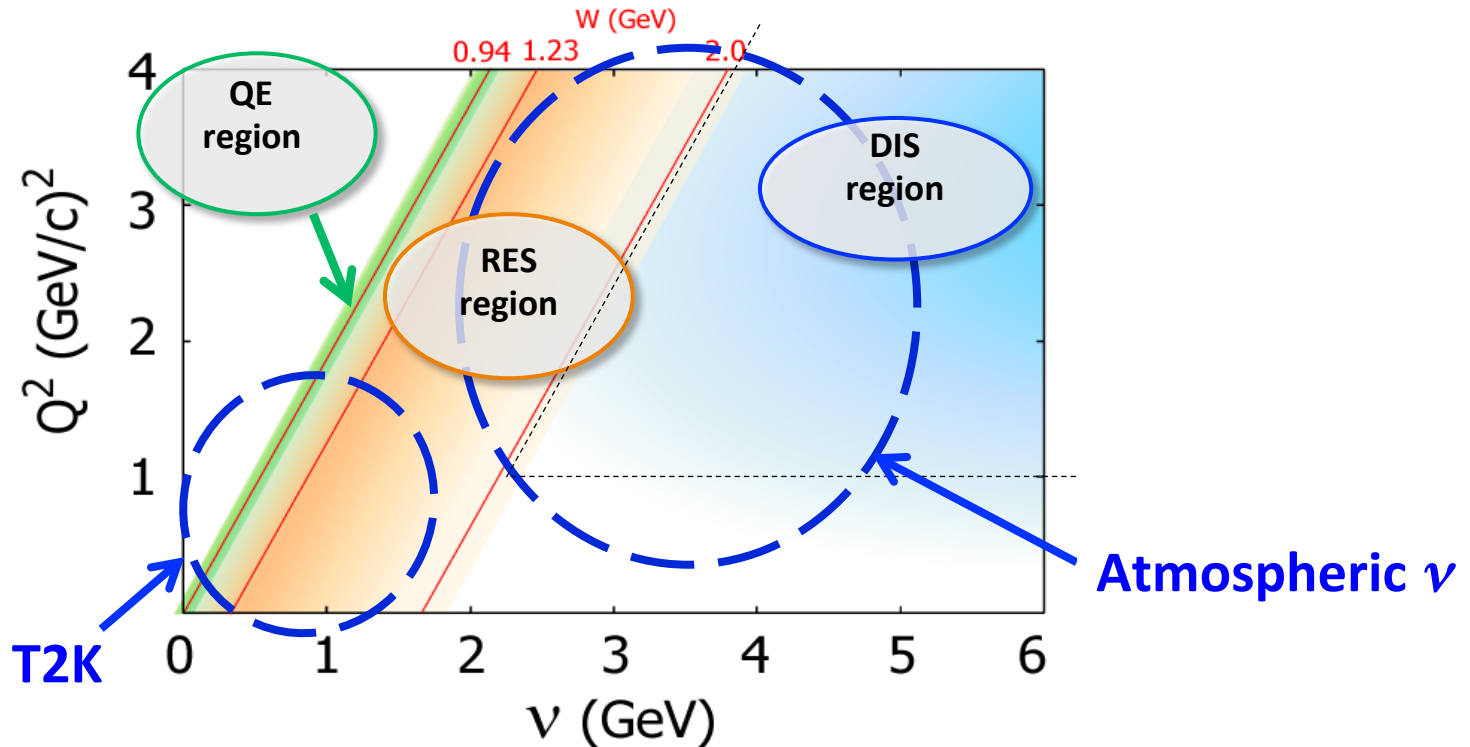
ν -nucleus scattering needs to be understood more precisely

All ν -oscillation experiments measure ν -flux through ν -nucleus interaction



Neutrino-nucleus scattering for ν -oscillation experiments

Next-generation exp. \rightarrow leptonic CP , mass hierarchy

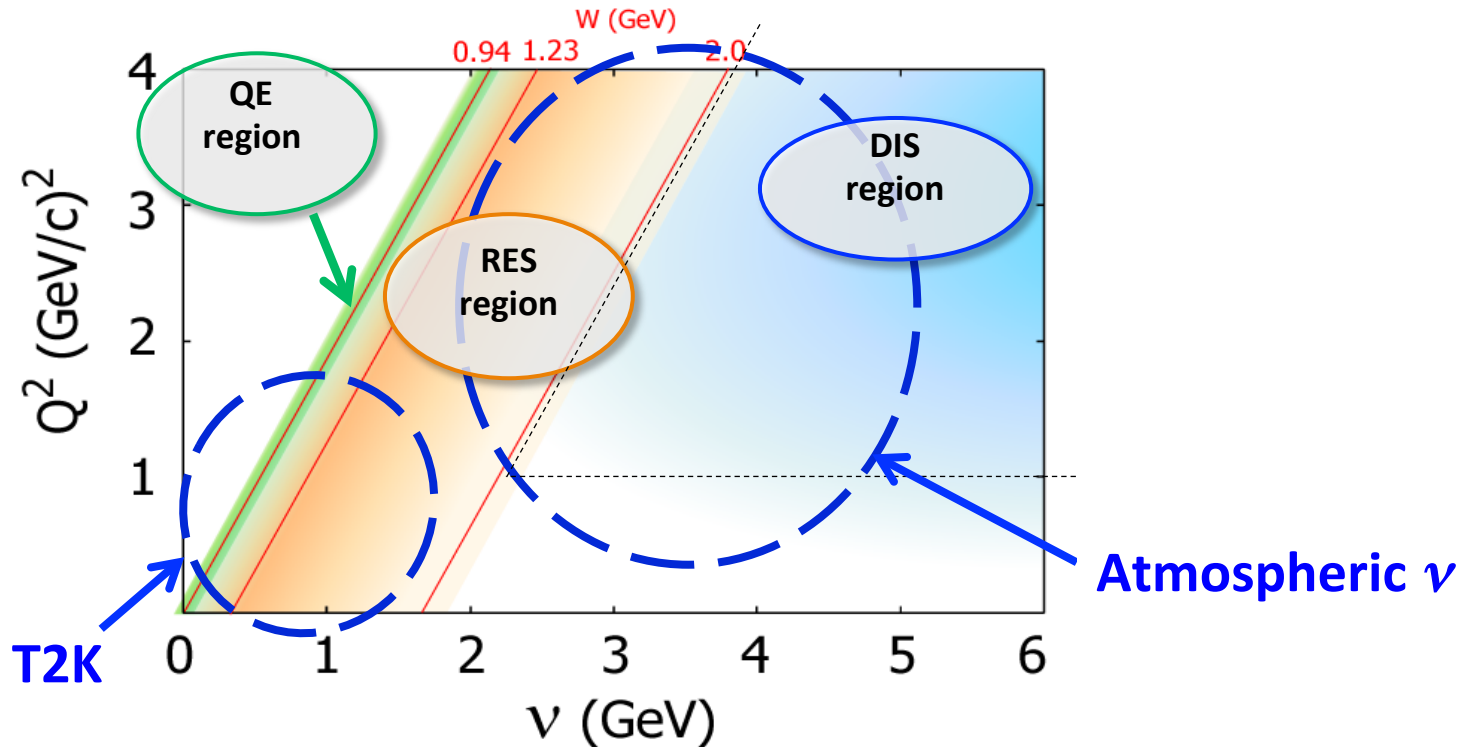


Wide kinematical region with different characteristic

\rightarrow Combination of different expertise is necessary

Neutrino-nucleus scattering for ν -oscillation experiments

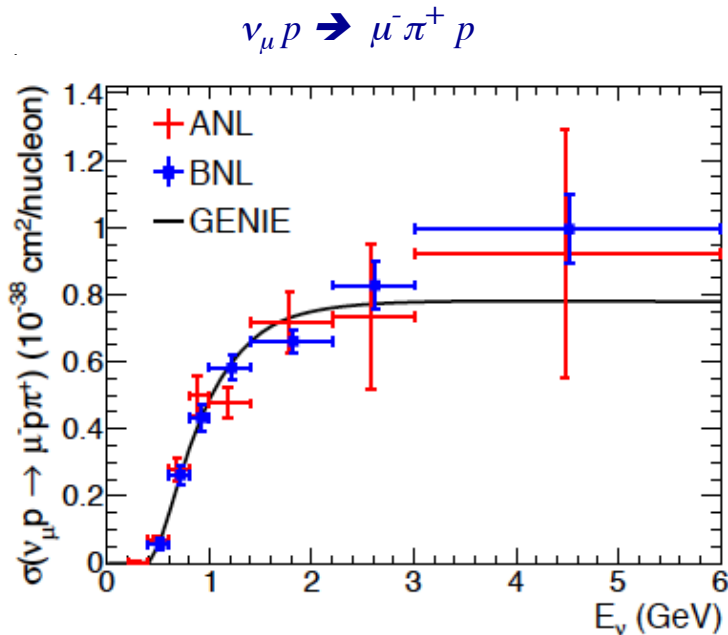
Next-generation exp. \rightarrow leptonic CP , mass hierarchy



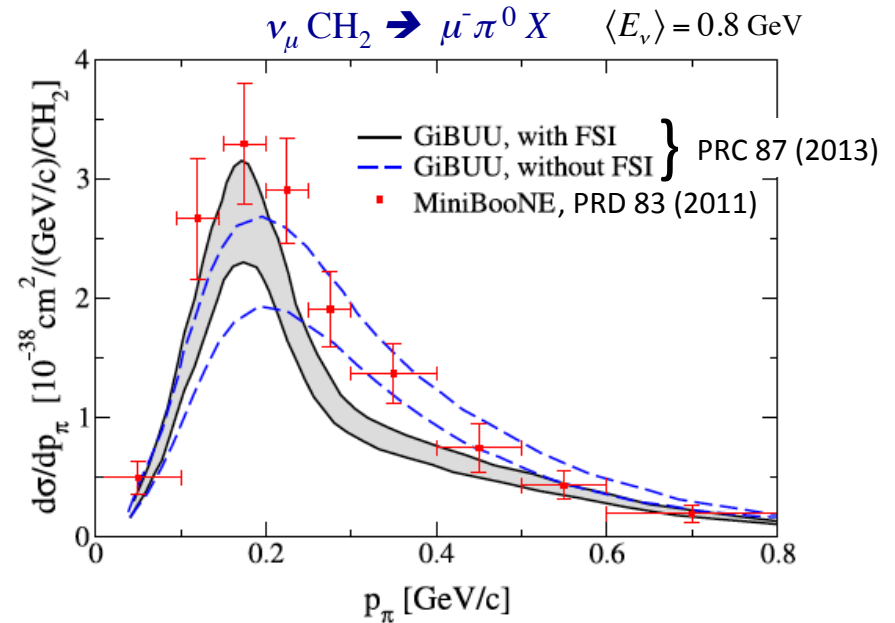
Collaboration at J-PARC Branch of KEK Theory Center

<http://j-parc-th.kek.jp/html/English/e-index.html>

Neutrino interaction data in resonance region



- Data to fix nucleon axial current ($g_{AN\Delta}$)
- Discrepancy between BNL & ANL data
- Recent reanalysis of original data
→ discrepancy resolved (!?)
PRD 90, 112017 (2014)

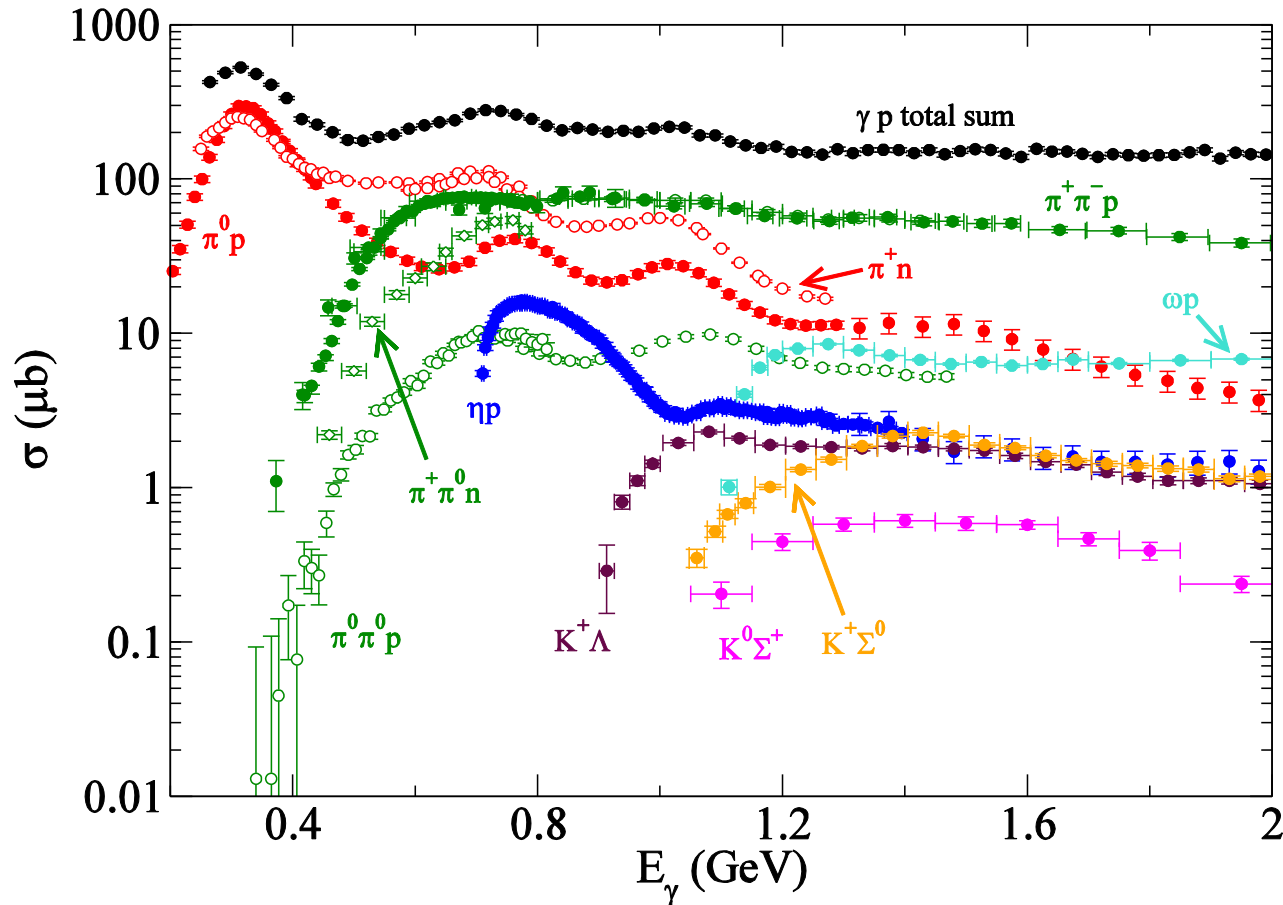


- Final state interaction (FSI) changes
charge, momentum, number of π
- Cross section shape is worse described with FSI
- MINERvA data (arXiv:1406.6415) favor FSI
 $\langle E_\nu \rangle = 4.0$ GeV

More data are coming → better understanding of neutrino-nucleus interaction

Resonance region (single nucleon)

$\gamma N \rightarrow X$



Multi-channel reaction

- 2π production is comparable to 1π
- η, K productions (ν case: background of proton decay exp.)

GOAL : Develop νN -interaction model in resonance region

Problems in previous models

- (multi-channel) **Unitarity** is missing
- Important **2π production** model is missing

Our strategy to overcome the problems...

We develop a **Unitary coupled-channels** model

- ★ Dynamical coupled-channels (DCC) model for $\gamma N, \pi N \rightarrow \pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$
- ★ Extension to $\nu N \rightarrow l^- X$ ($X = \pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$)

Dynamical Coupled-Channels model for meson productions

DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

Kamano et al., PRC 88, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$

$$\{a, b, c\} = \pi N, \eta N, \pi\pi N, \pi\Delta, \sigma N, \rho N, K\Lambda, K\Sigma$$

Coupled-channel unitarity is fully taken into account

In addition, $\gamma N, W^\pm N, ZN$ channels are included perturbatively

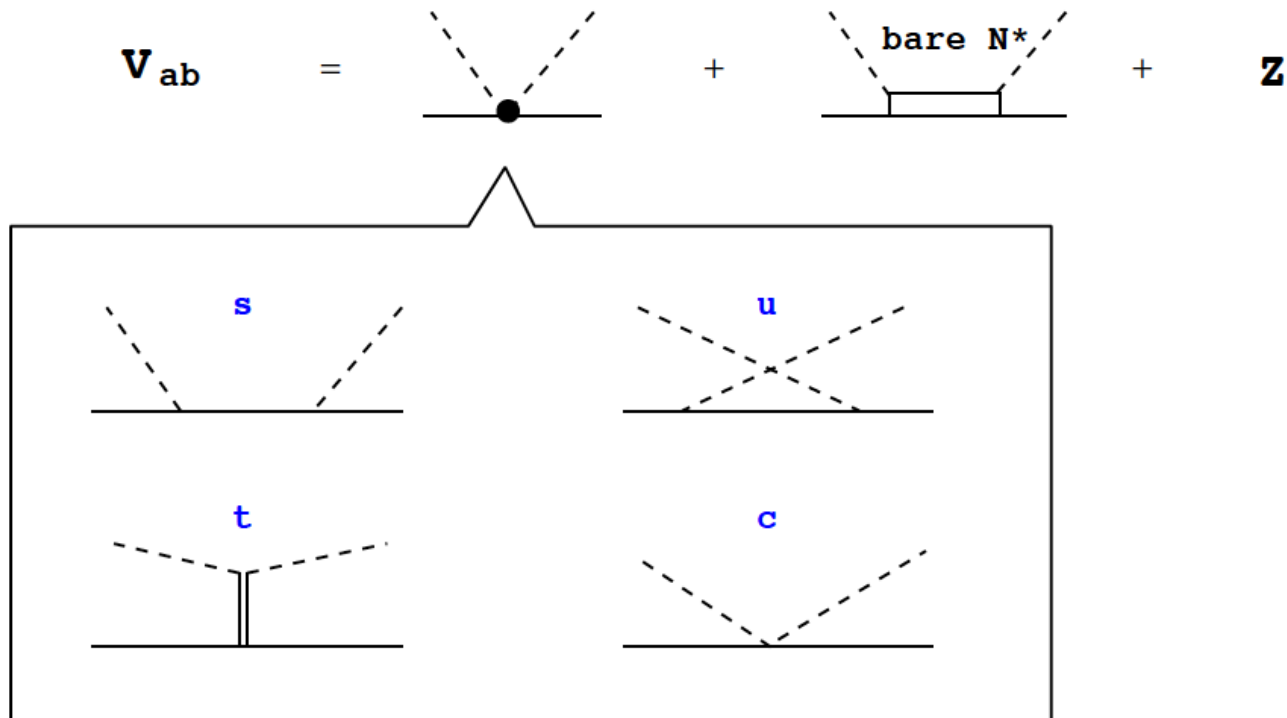
DCC (Dynamical Coupled-Channel) model

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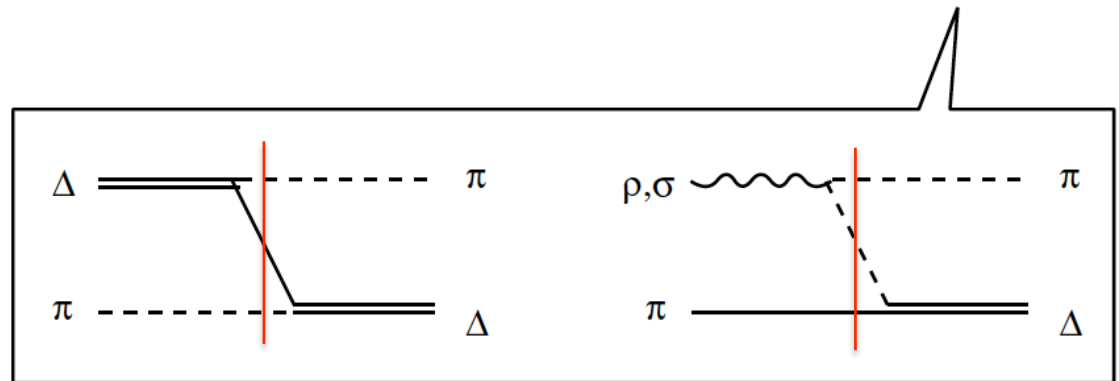
Matsuyama et al., Phys. Rep. **439**, 193 (2007)

Kamano et al., PRC 88, 035209 (2013)

Coupled-channel Lippmann-Schwinger equation

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$

$$\mathbf{V}_{ab} = \text{[diagram 1]} + \text{[diagram 2]} + \mathbf{Z}$$



essential for three-body unitarity

DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

Kamano et al., PRC 88, 035209 (2013)

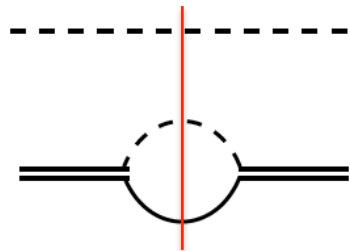
Coupled-channel Lippmann-Schwinger equation

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$

$G_c =$



for stable channels



for unstable channels

DCC analysis of meson production data

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

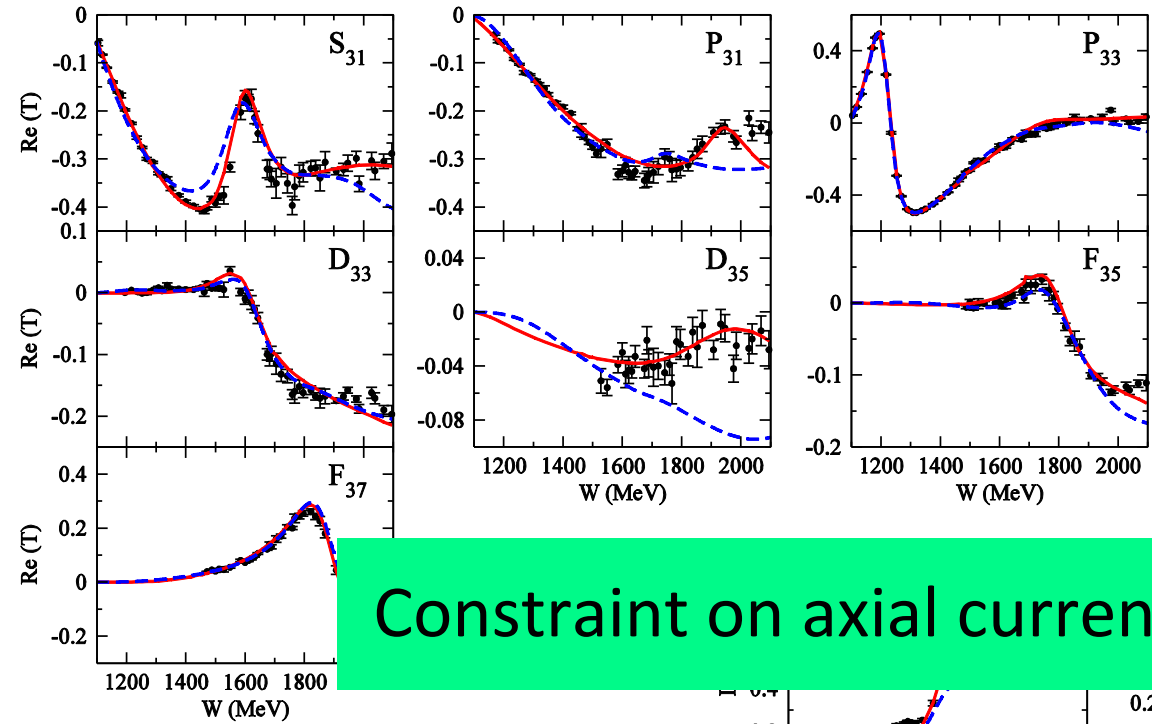
Fully combined analysis of $\gamma N, \pi N \rightarrow \pi N, \eta N, K\Lambda, K\Sigma$ data

$d\sigma / d\Omega$ and polarization observables ($W \leq 2.1$ GeV)

~ 20,000 data points are fitted

by adjusting parameters (N^* mass, $N^* \rightarrow MB$ couplings, cutoffs)

Partial wave amplitudes of πN scattering



Real part

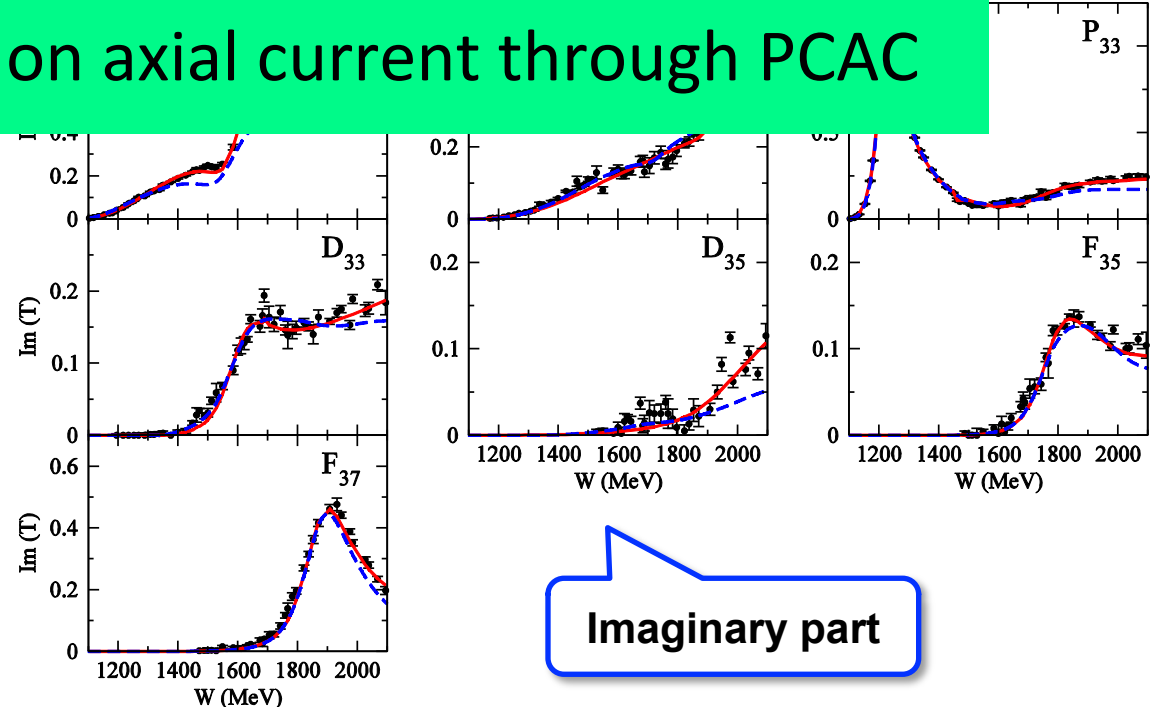
$$I = \frac{3}{2}$$

Constraint on axial current through PCAC

— Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

- - - Previous model (fitted to $\pi N \rightarrow \pi N$ data only) [PRC76 065201 (2007)]

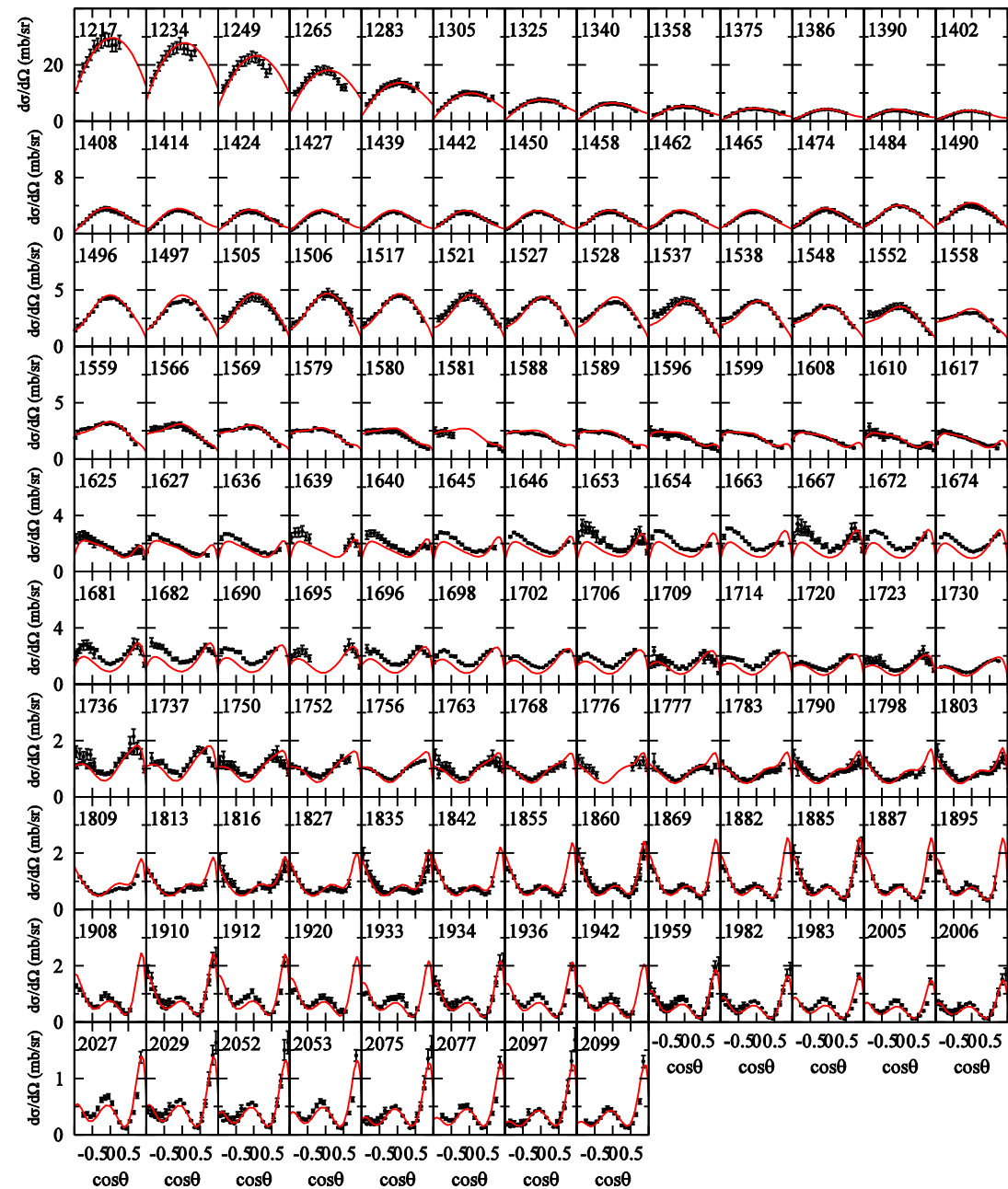
Data: SAID πN amplitude



Imaginary part

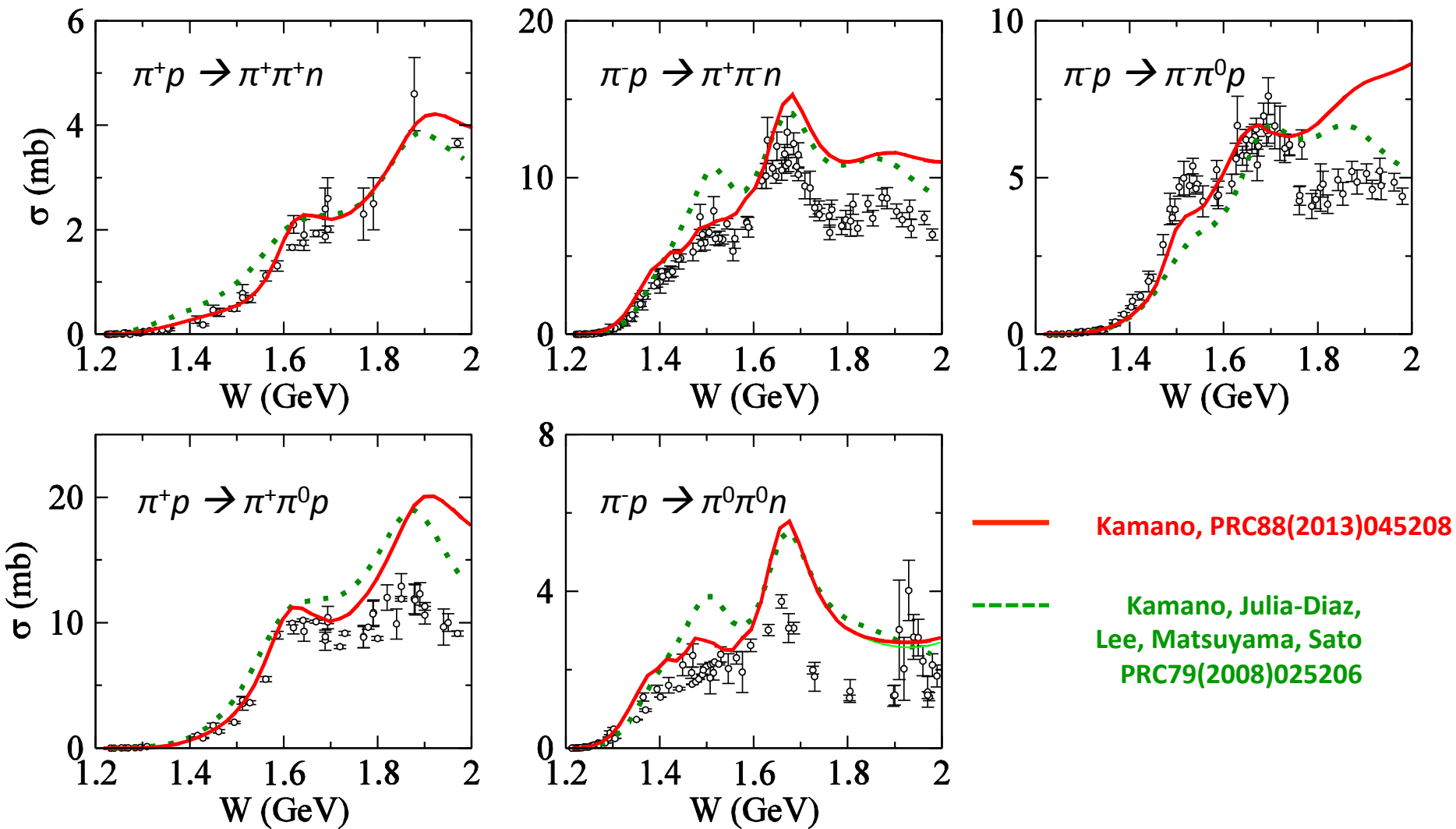
$\gamma p \rightarrow \pi^0 p$ $d\sigma/d\Omega$ for $W < 2.1$ GeV

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)

Vector current ($Q^2=0$) for 1π

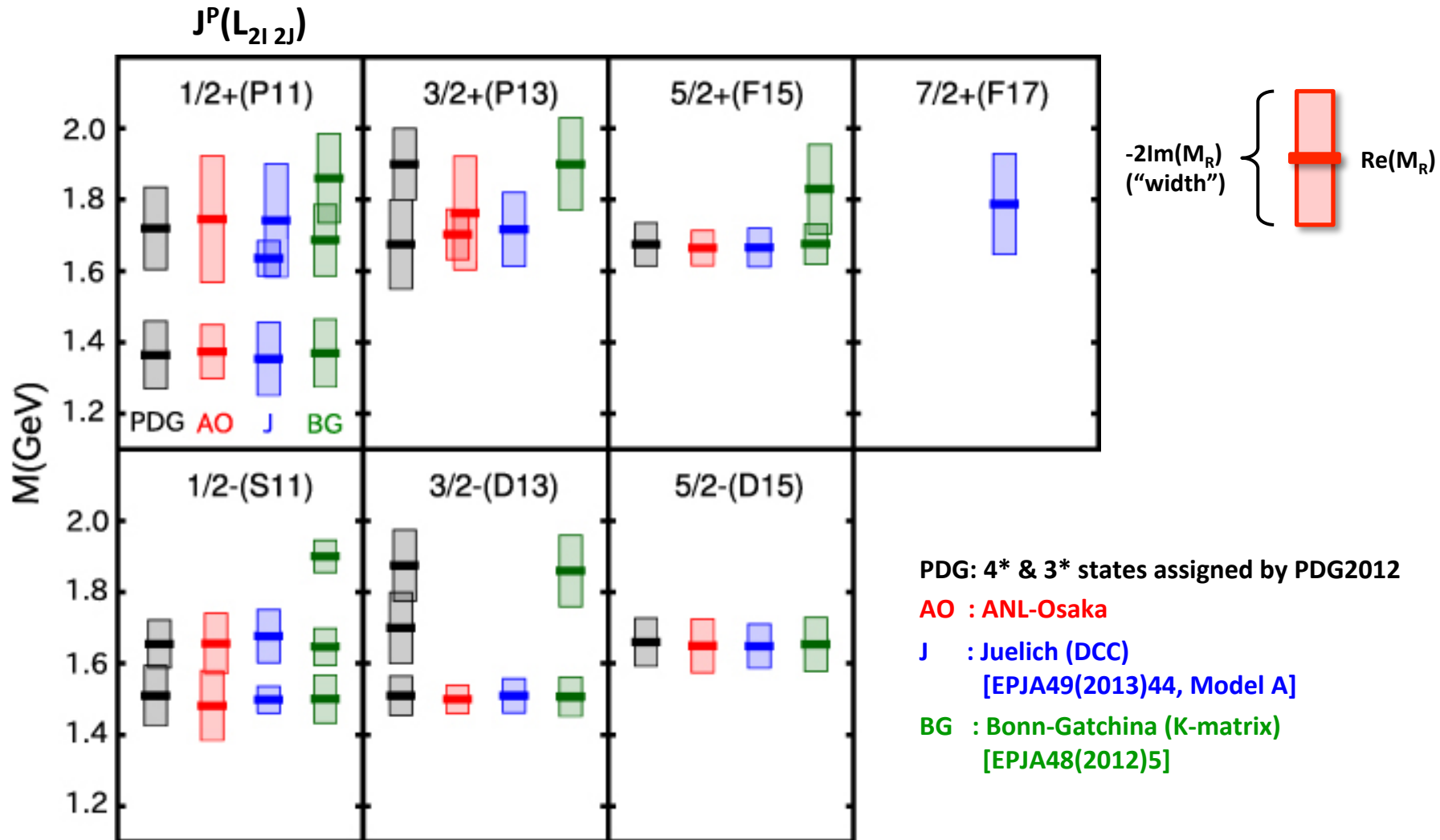
Production is well-tested by data

Predicted $\pi N \rightarrow \pi\pi N$ total cross sections with our DCC model



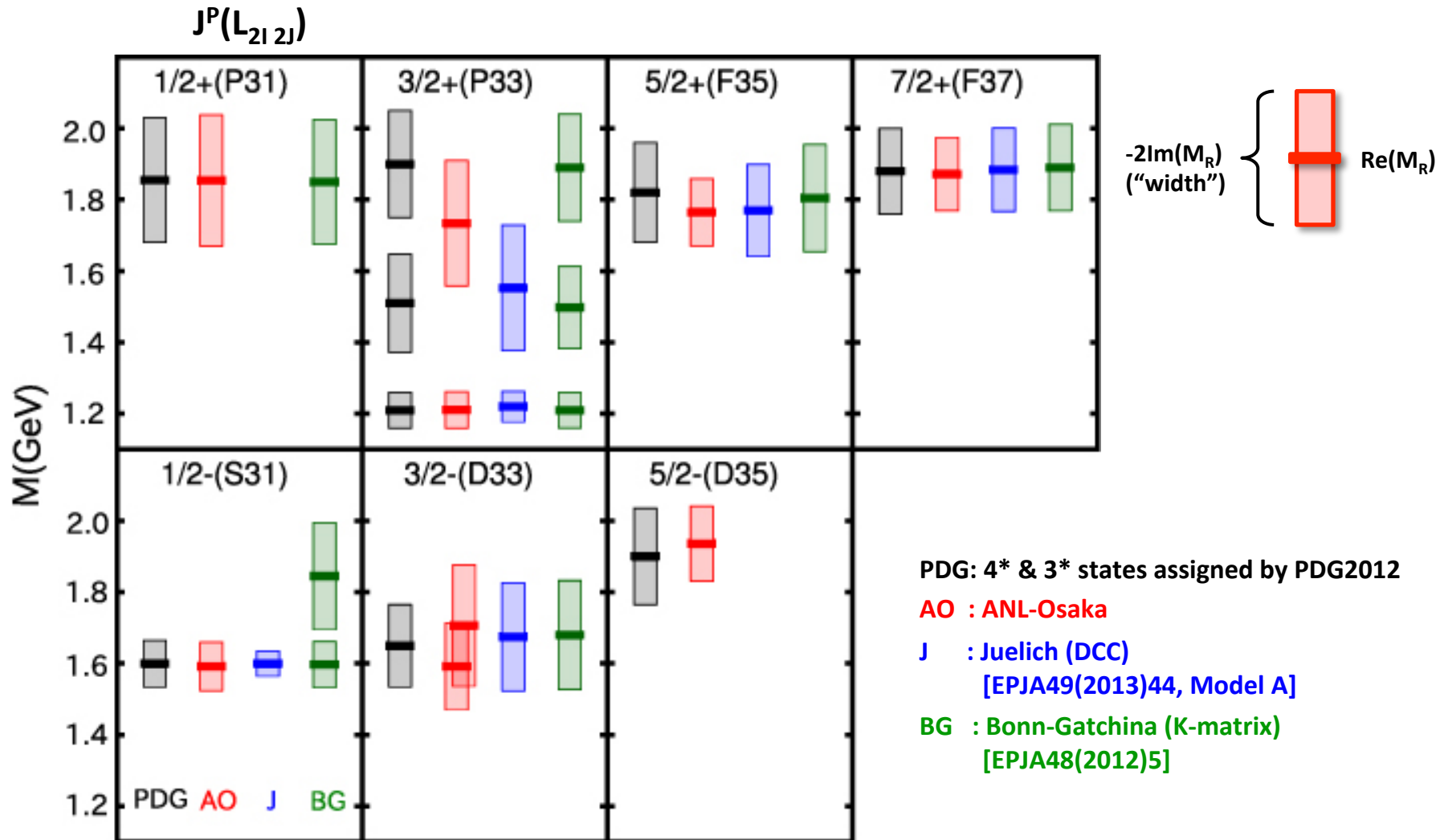
“N” resonances ($I=1/2$)

Kamano, Nakamura, Lee, Sato, PRC 88 (2013)



“ Δ ” resonances ($I=3/2$)

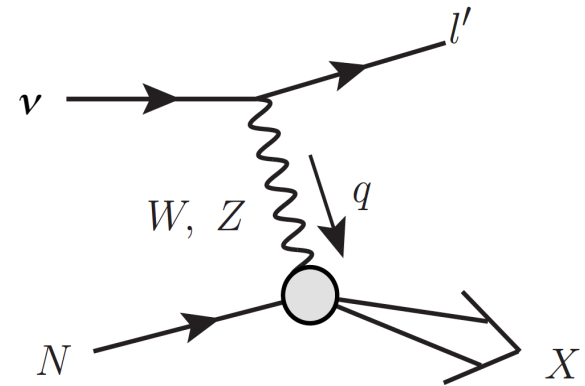
Kamano, Nakamura, Lee, Sato, PRC 88 (2013)



DCC model for neutrino interaction

Extension to full kinematical region $Q^2 \neq 0$

→ Model for **vector & axial currents** is necessary



DCC model for neutrino interaction

Vector current

$Q^2=0$

$\gamma p \rightarrow MB$

$\gamma n \rightarrow \pi N$

\rightarrow isospin separation

necessary for calculating ν -interaction

$Q^2 \neq 0$ (electromagnetic form factors for $N-N^*$ transitions)

obtainable from $(e, e' \pi)$, $(e, e' X)$ data analysis

We've done first analysis of all these reactions $\rightarrow VNN^(Q^2)$ fixed \rightarrow neutrino reactions*

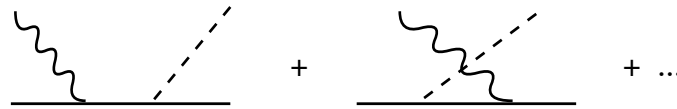
DCC model for neutrino interaction

Axial current

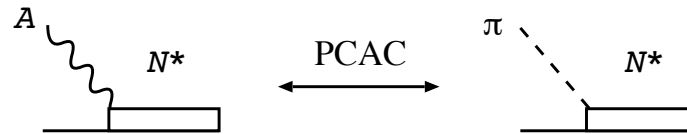
$Q^2=0$

non-resonant mechanisms

$$\partial_\mu \pi \rightarrow f_\pi A_\mu^{external}$$



resonant mechanisms



Interference among resonances and background can be made under control within DCC model

Caveat : phenomenological axial currents are added to maintain PCAC relation

$$q \cdot A_{AN \rightarrow \pi N} \sim i f_\pi T_{\pi N \rightarrow \pi N}$$

to be improved in future

DCC model for neutrino interaction

Axial current

$Q^2 \neq 0$ $F_A(Q^2)$: axial form factors

non-resonant mechanisms $F_A(Q^2) = \left(\frac{1}{1 + Q^2 / M_A^2} \right)^2$ $M_A = 1.02 \text{ GeV}$

resonant mechanisms $F_A(Q^2) = (1 + aQ^2) \exp(-bQ^2) \left(\frac{1}{1 + Q^2 / M_A^2} \right)^2$ Sato et al. PRC 67 (2003)

More neutrino data are necessary to fix axial form factors for ANN^*

Neutrino cross sections will be predicted with this axial current for this presentation

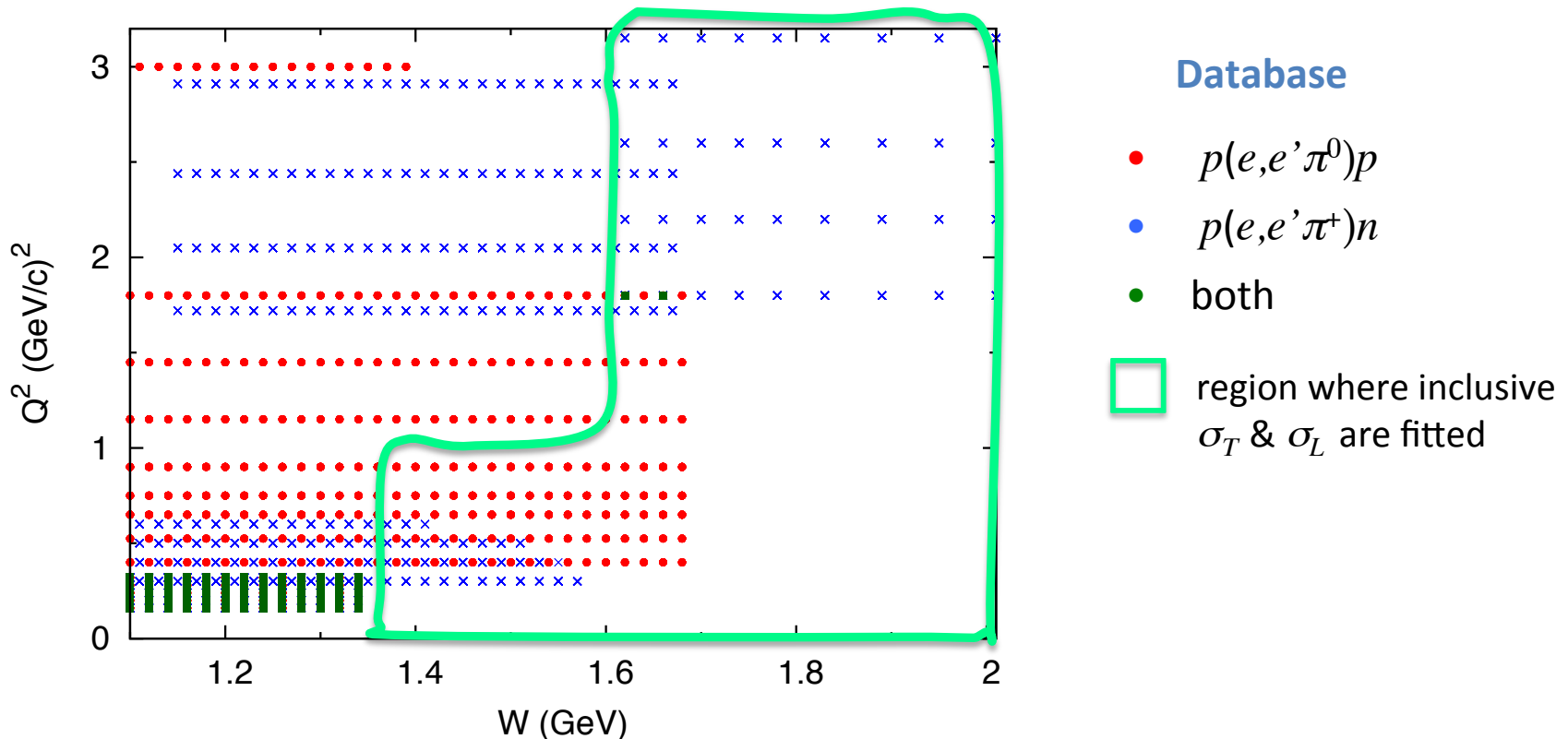
Analysis of electron scattering data

Analysis of electron-proton scattering data

Purpose : Determine Q^2 -dependence of vector coupling of p - N^* : $V_{pN^*}(Q^2)$

Data : * 1π electroproduction

* Empirical inclusive inelastic structure functions σ_T, σ_L ← Christy et al, PRC 81 (2010)

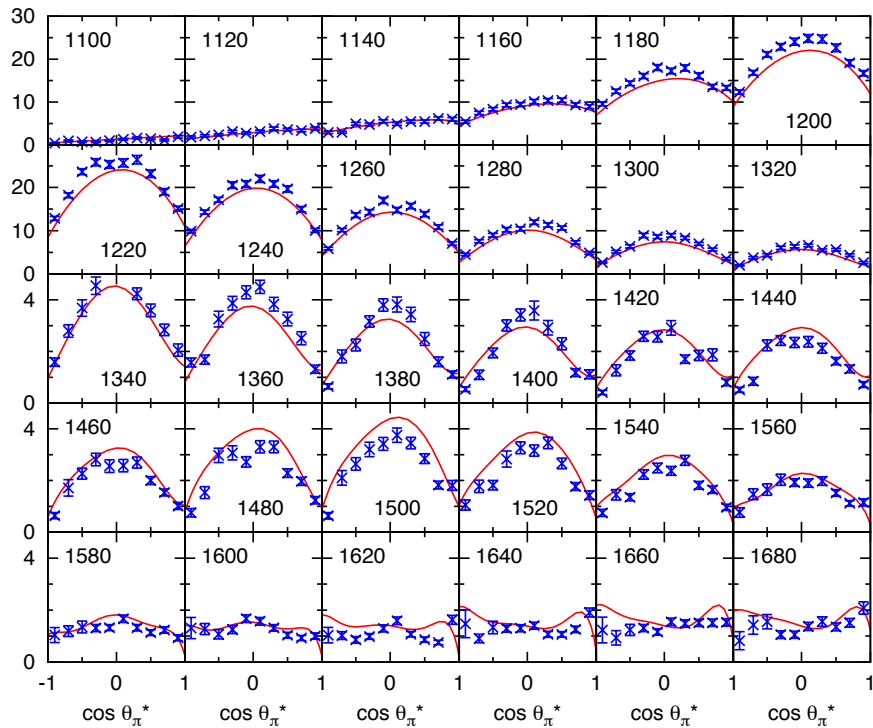


Analysis result (single π)

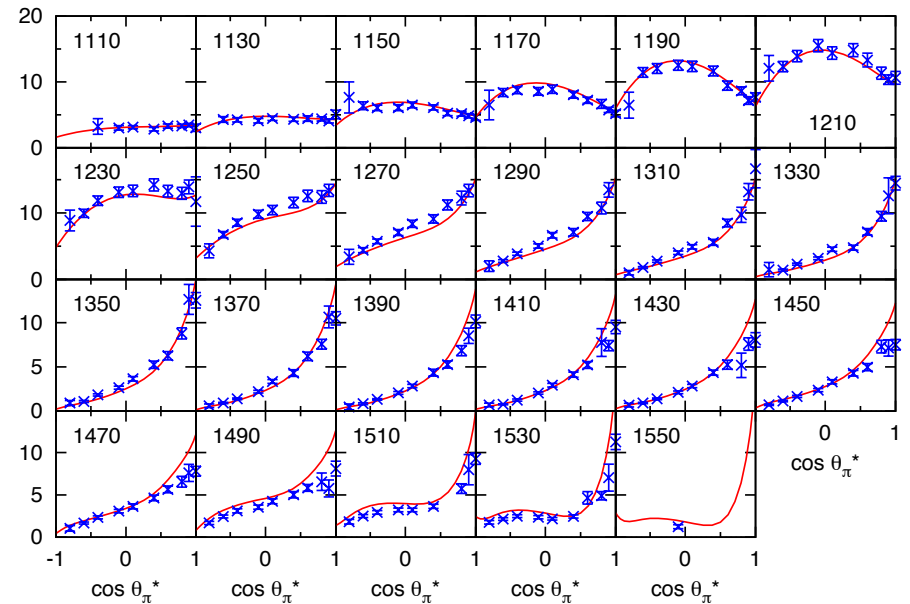
$$Q^2=0.40 \text{ (GeV/c)}^2$$

$\sigma_T + \varepsilon \sigma_L$ for $W=1.1 - 1.68 \text{ GeV}$

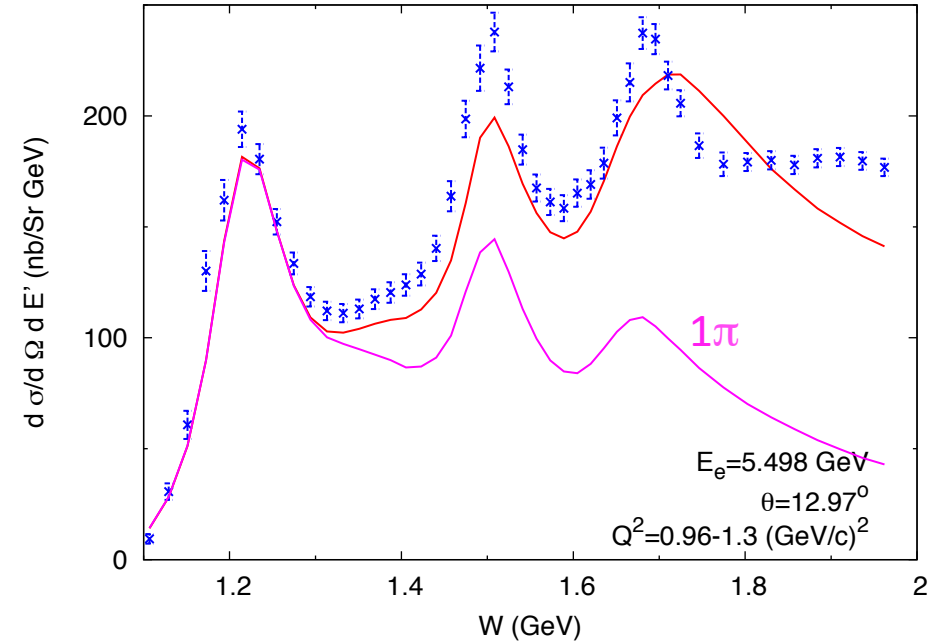
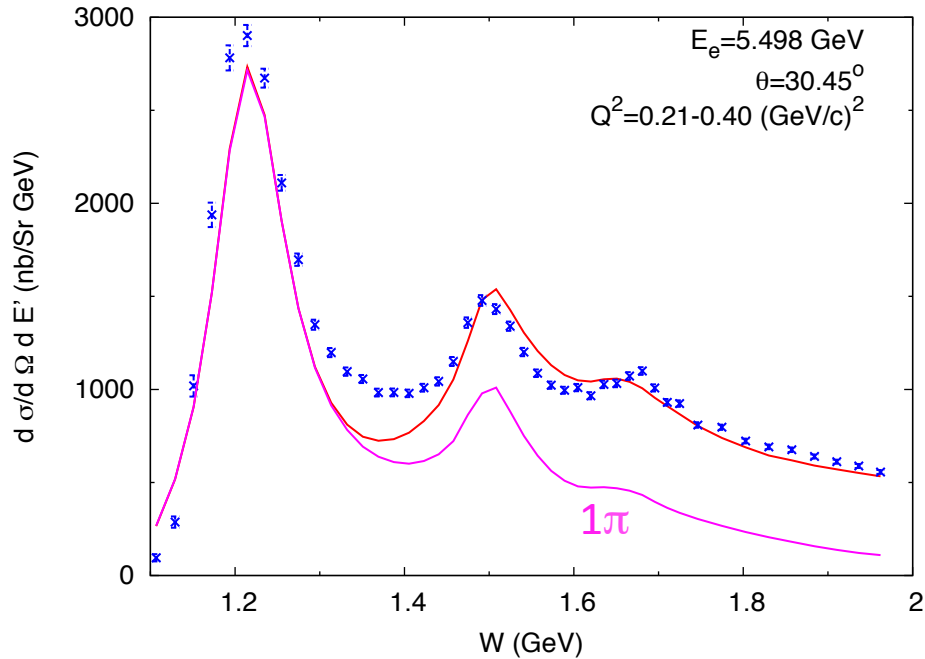
$p(e, e' \pi^0) p$



$p(e, e' \pi^+) n$



Analysis result (inclusive)



Data: JLab E00-002 (preliminary)

- Reasonable fit to data for application to neutrino interactions
- Important 2π contributions for high W region

Analysis of electron-'neutron' scattering data

Purpose : Vector coupling of neutron- N^* and its Q^2 -dependence : $VnN^*(Q^2)$ ($I=1/2$)
 $I=3/2$ part has been fixed by proton target data

Data : * 1π photoproduction ($Q^2=0$)

* Empirical inclusive inelastic structure functions σ_T, σ_L ($Q^2 \neq 0$)

← Christy and Bosted, PRC 77 (2010), 81 (2010)

Done

*DCC vector currents has been tested by data for whole kinematical region
relevant to neutrino interactions of $E_\nu \leq 2$ GeV*

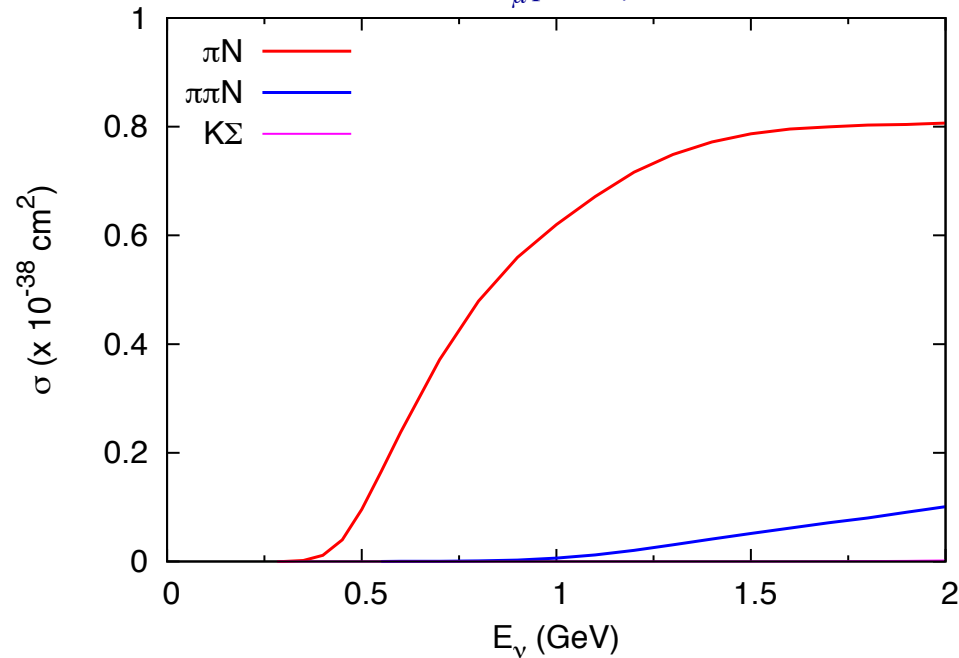
Neutrino Results

Caveat

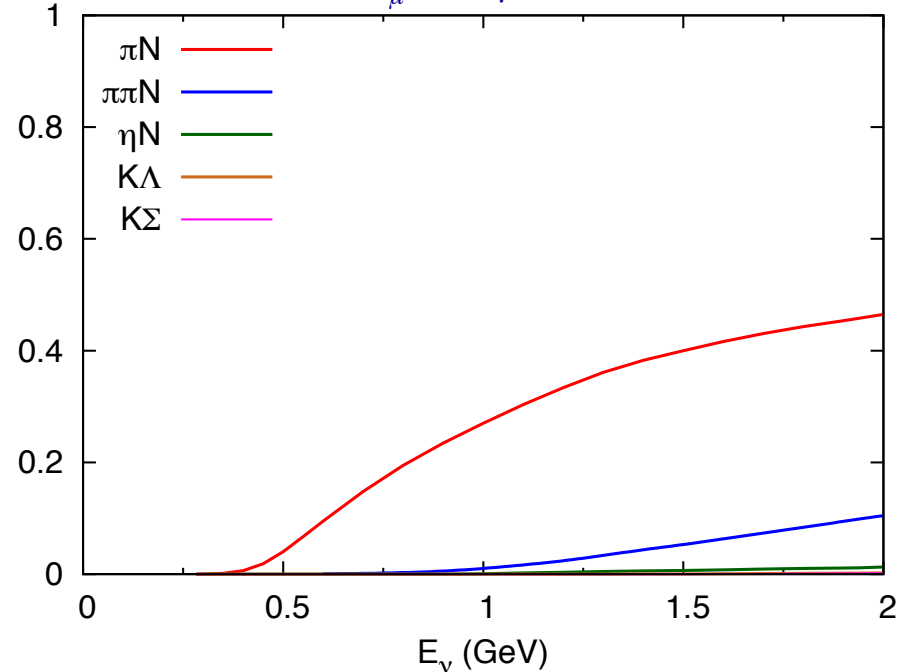
- Results presented here are still preliminary
- Careful examination needs to be made to obtain a final result

Cross section for $\nu_\mu N \rightarrow \mu^- X$

$\nu_\mu p \rightarrow \mu^- X$

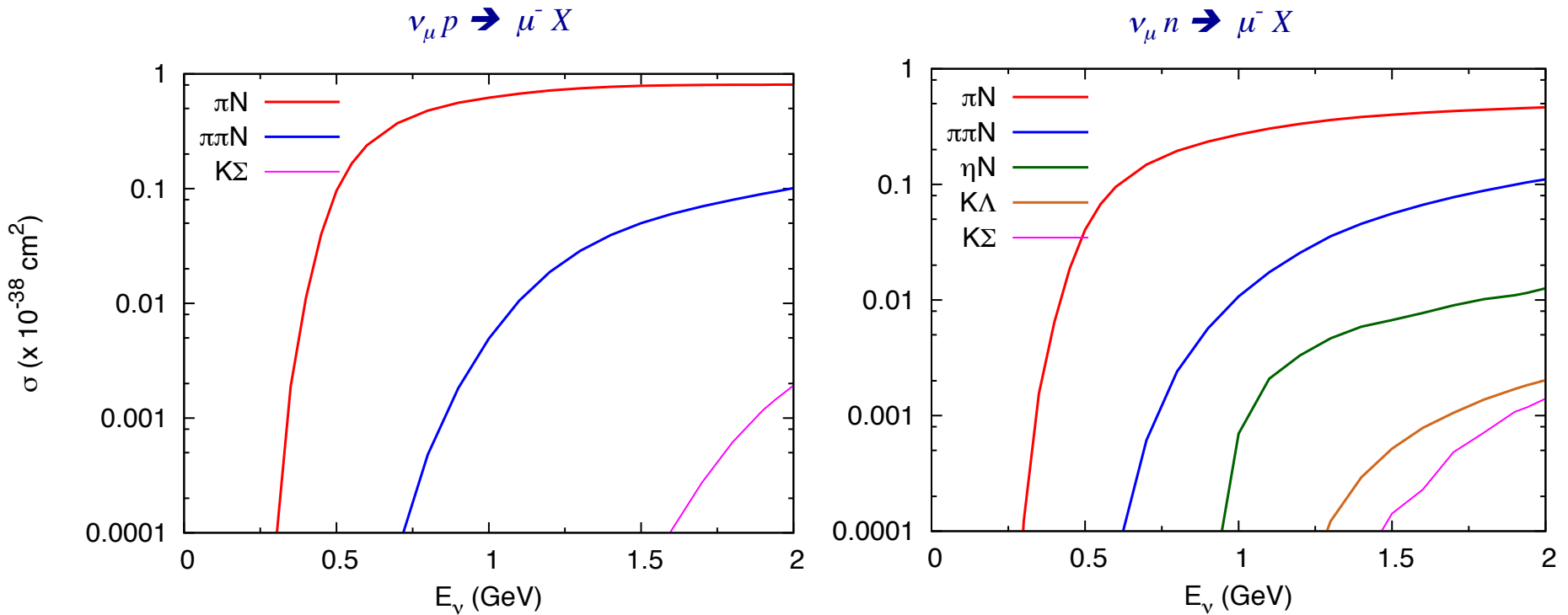


$\nu_\mu n \rightarrow \mu^- X$



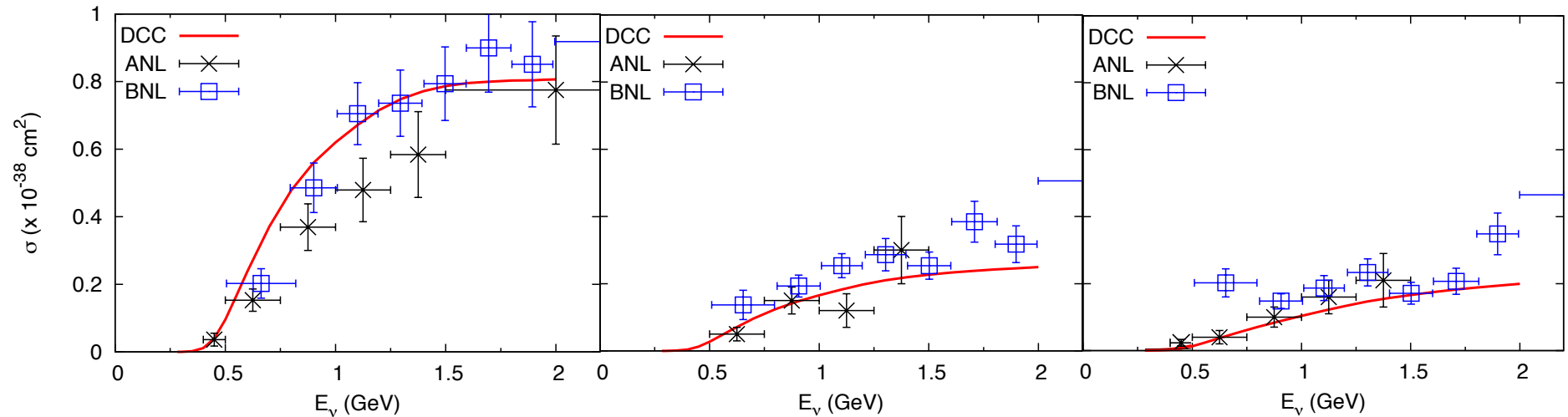
- πN & $\pi\pi N$ are main channels in few-GeV region
- DCC model gives predictions for all final states
- ηN , KY cross sections are $10^{-1} - 10^{-2}$ smaller

Cross section for $\nu_\mu N \rightarrow \mu^- X$



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- DCC model gives predictions for all final states
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Comparison with single pion data



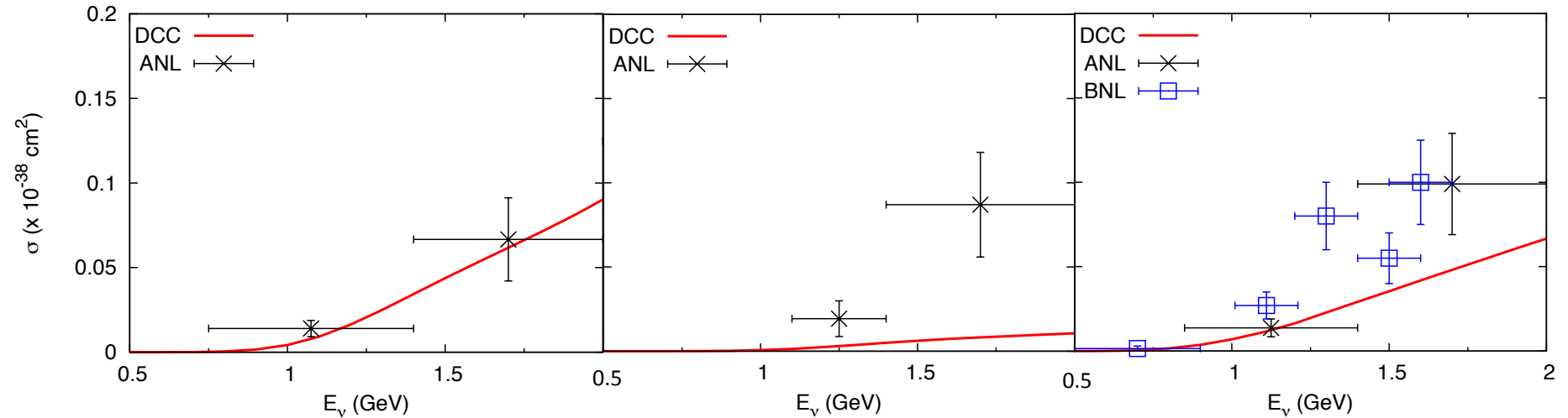
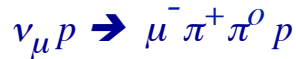
DCC model prediction is consistent with data

ANL Data : PRD **19**, 2521 (1979)

BNL Data : PRD **34**, 2554 (1986)

- DCC model has flexibility to fit data ($ANN^*(Q^2)$)
- Data should be analyzed with nuclear effects
(Wu et al. , arXiv:1412:2415)

Comparison with double pion data



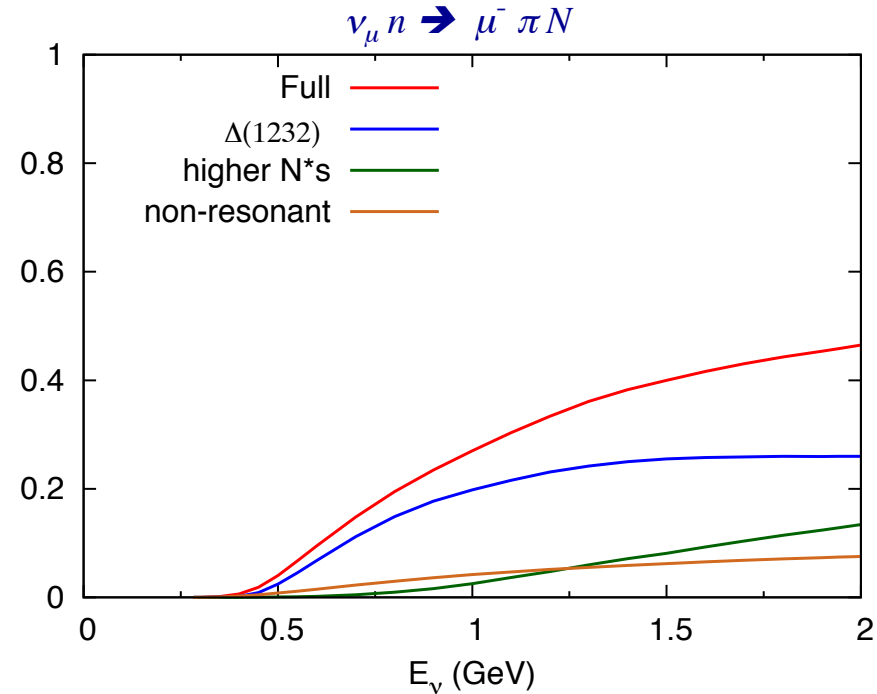
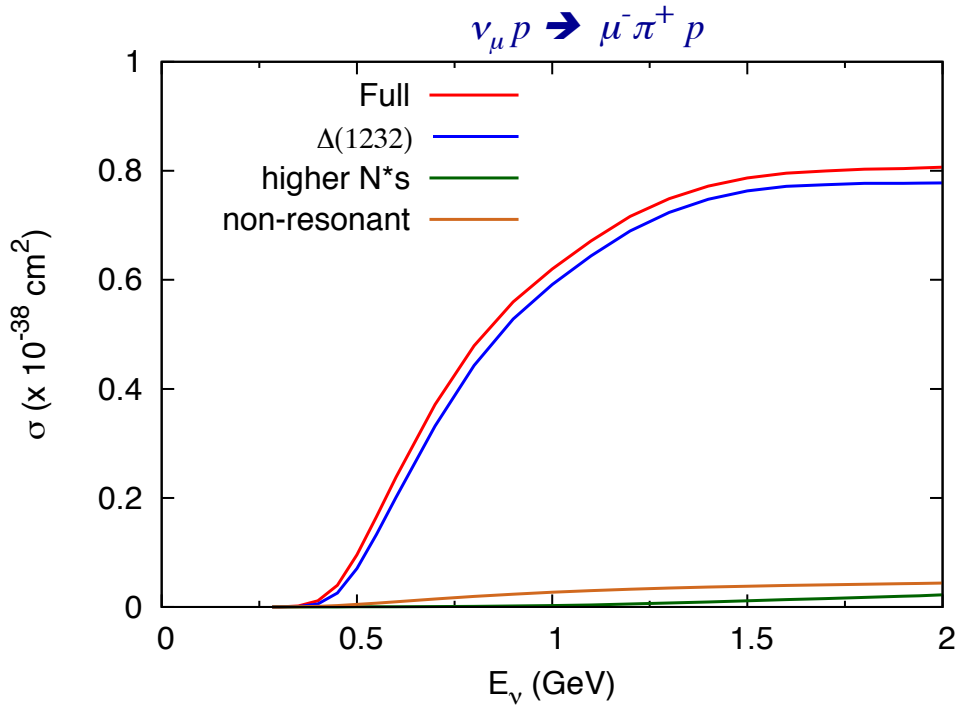
Fairly good DCC predication

ANL Data : PRD **28**, 2714 (1983)

BNL Data : PRD **34**, 2554 (1986)

- First microscopic model for 2 π production in resonance region
- 2 π production model is becoming available

Mechanisms for $\nu_\mu N \rightarrow \mu^- \pi N$



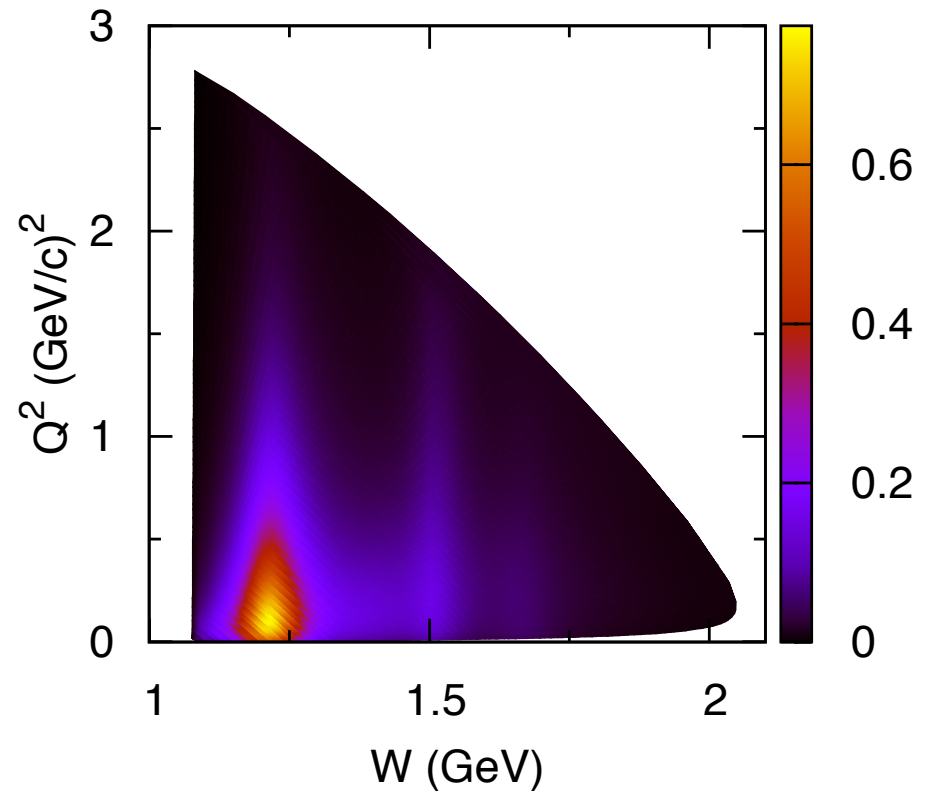
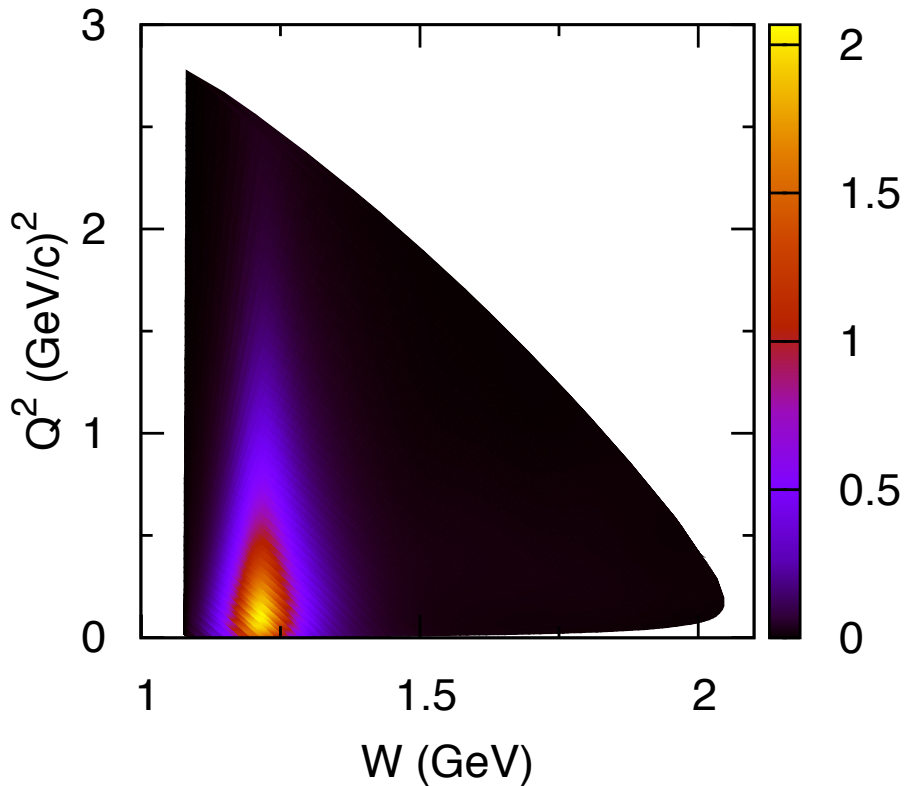
- $\Delta(1232)$ dominates for $\nu_\mu p \rightarrow \mu^- \pi^+ p$ ($I=3/2$) for $E_\nu \leq 2$ GeV
- Non-resonant mechanisms contribute significantly
- Higher N^* s becomes important towards $E_\nu \approx 2$ GeV for $\nu_\mu n \rightarrow \mu^- \pi N$

$$d\sigma / dW dQ^2 \quad (\times 10^{-38} \text{ cm}^2 / \text{ GeV}^2)$$

$$E_\nu = 2 \text{ GeV}$$

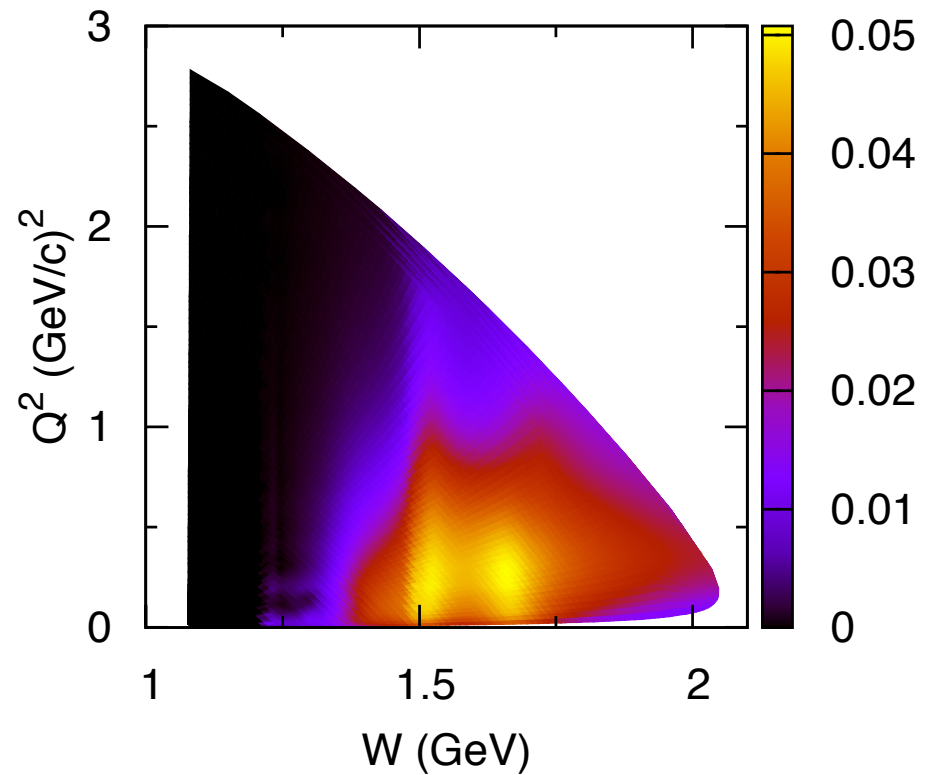
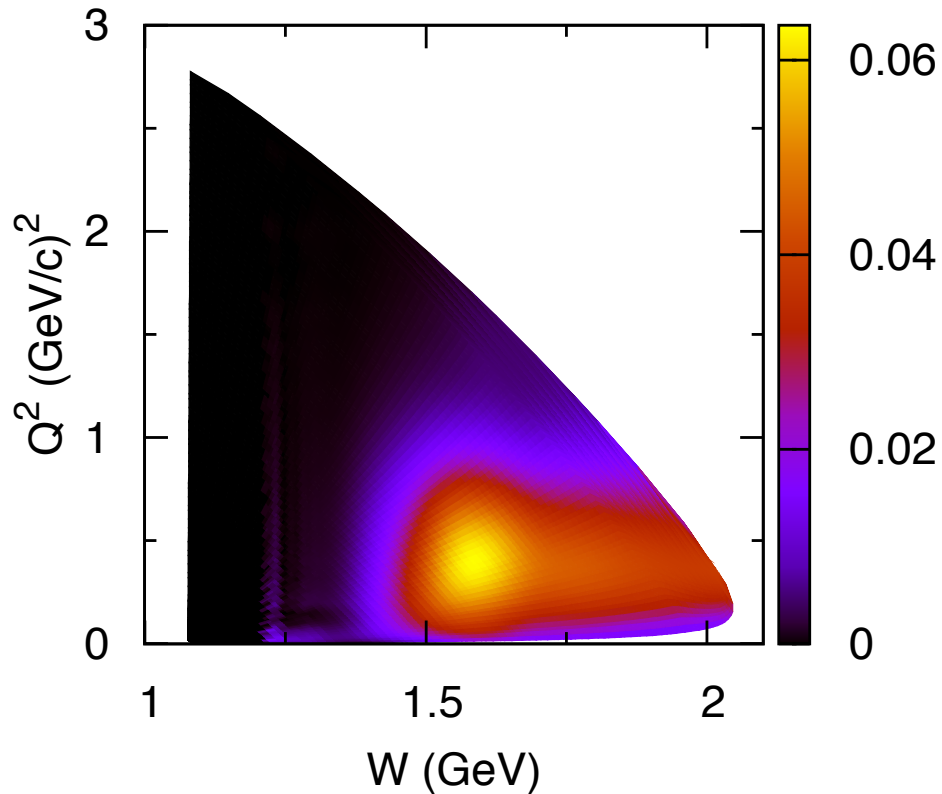
$$\nu_\mu p \rightarrow \mu^- \pi^+ p$$

$$\nu_\mu n \rightarrow \mu^- \pi\pi N$$



$$d\sigma / dW dQ^2 \quad (\times 10^{-38} \text{ cm}^2 / \text{GeV}^2)$$

$$E_\nu = 2 \text{ GeV}$$



Conclusion

Development of DCC model for νN interaction in resonance region

Start with DCC model for $\gamma N, \pi N \rightarrow \pi N, \pi\pi N, \eta N, K\Lambda, K\Sigma$

- extension of vector current to $Q^2 \neq 0$ region, isospin separation through analysis of $e^- - p$ & $e^- - n$ data for $W \leq 2 \text{ GeV}$, $Q^2 \leq 3 (\text{GeV}/c)^2$
- Development of axial current for νN interaction; PCAC is maintained

Conclusion

- πN & $\pi\pi N$ are main channels in few-GeV region
- DCC model prediction is consistent with BNL data
- Δ, N^* s, non-resonant are all important in few-GeV region (for $\nu_\mu n \rightarrow \mu X$)
 - essential to understand interference pattern among them
 - DCC model can do this; consistency between π interaction and axial current