九州大学理学部物理学科 宇宙物理理論研究室コロキウム 2021/12/03

Primordial black holes

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Abstract

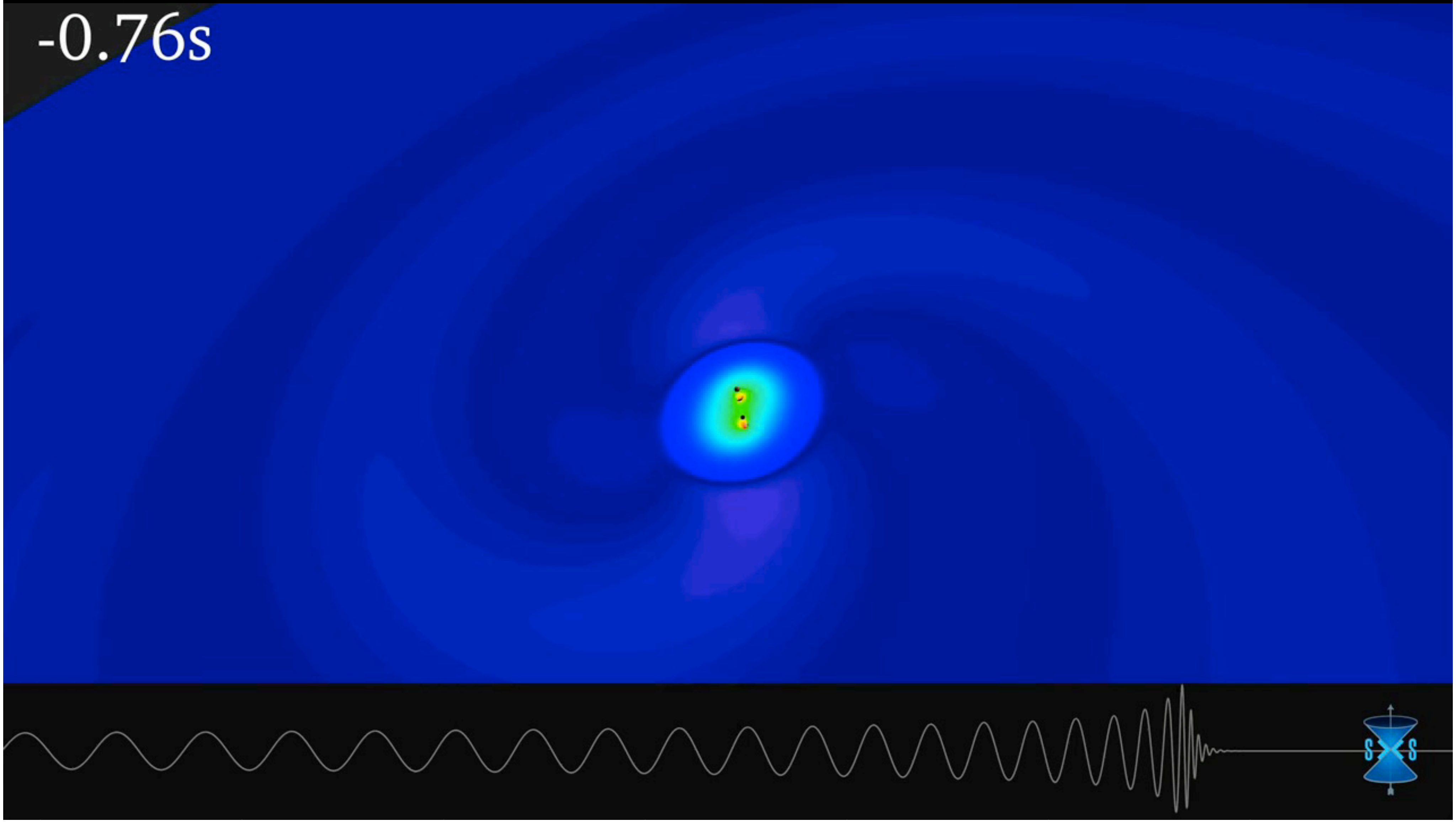
- Binary PBHs are good candidates for LIGO/Virgo events
- PBHs can be also produced both in the early radiation and matter dominated Universe
- We can probe high-energy physics, the early Universe, and gravity with PBHs
- The NANOGrav 12.5yr data can be fitted by secondary GWs induced by large curvature perturbation, which could have produced PBHs with $O(1)$ $M_{\odot}$ simultaneously
- We will be able to distinguish a model of PBH formations from others by future observations such as LIGO/Virgo/KAGRA or DECIGO/BBO and so on.

Why PBHs?

- We can probe high-energy physics, the early Universe, and gravity with PBHs through recent and future gravitational wave observations

LIGO and Virgo have detected gravitational wave signals from Binary Black Holes

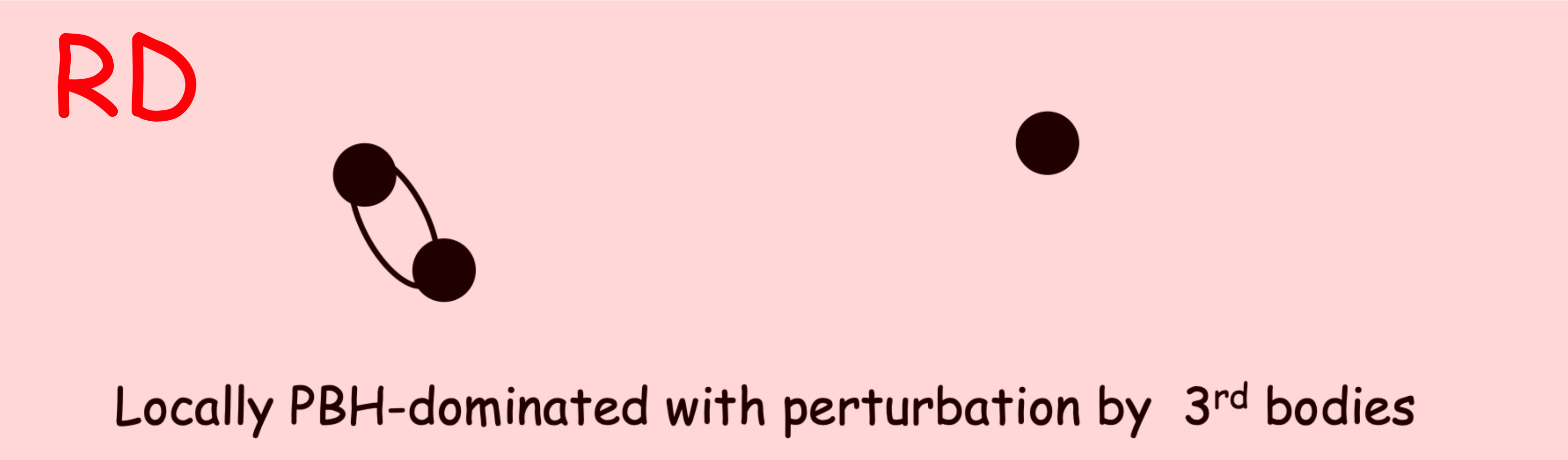
https://www.youtube.com/watch?v=1agm33iEAuo



Binary formations of PBHs in the radiation dominated epoch

M. Sasaki, T. Suyama, T. Tanaka and S. Yokoyama (2016).

- Three body effects are important



- Formation rate

$$\mathcal{R}_{\mathrm{PBH}}(z) = A_{\mathrm{PBH}} \left(\frac{t(z)}{\tau} \right)^{-\frac{34}{37}}$$

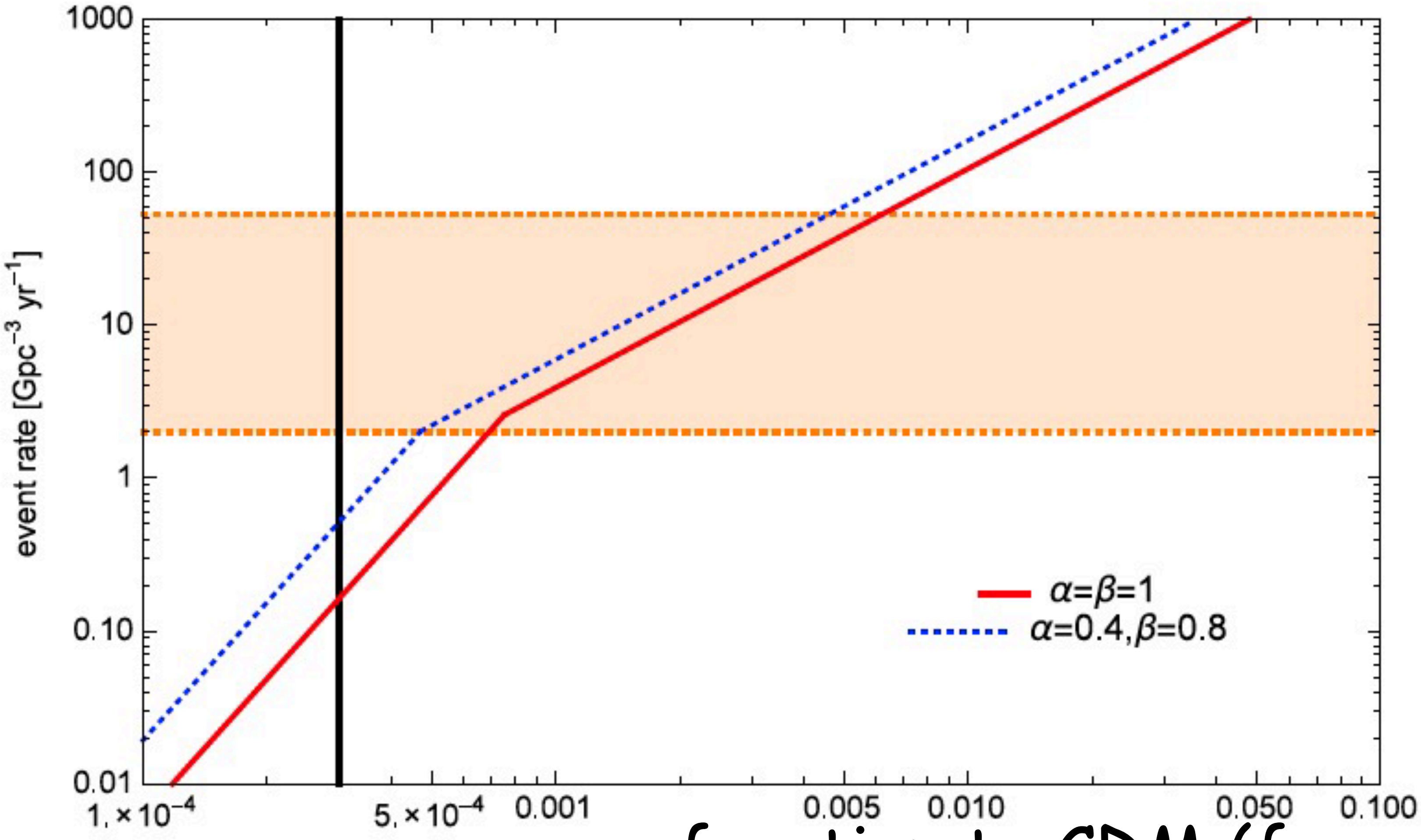
Z.-C. Chen and Q.-G. Huang, Astrophys. J. 864, 61 (2018), 1801.10327

GW150914 and its merger rates for 30 M_{solar} masses BBH

M. Sasaki, T. Suyama, T. Tanaka and S. Yokoyama (2016).

A 3-body effect is important for the BBH formations

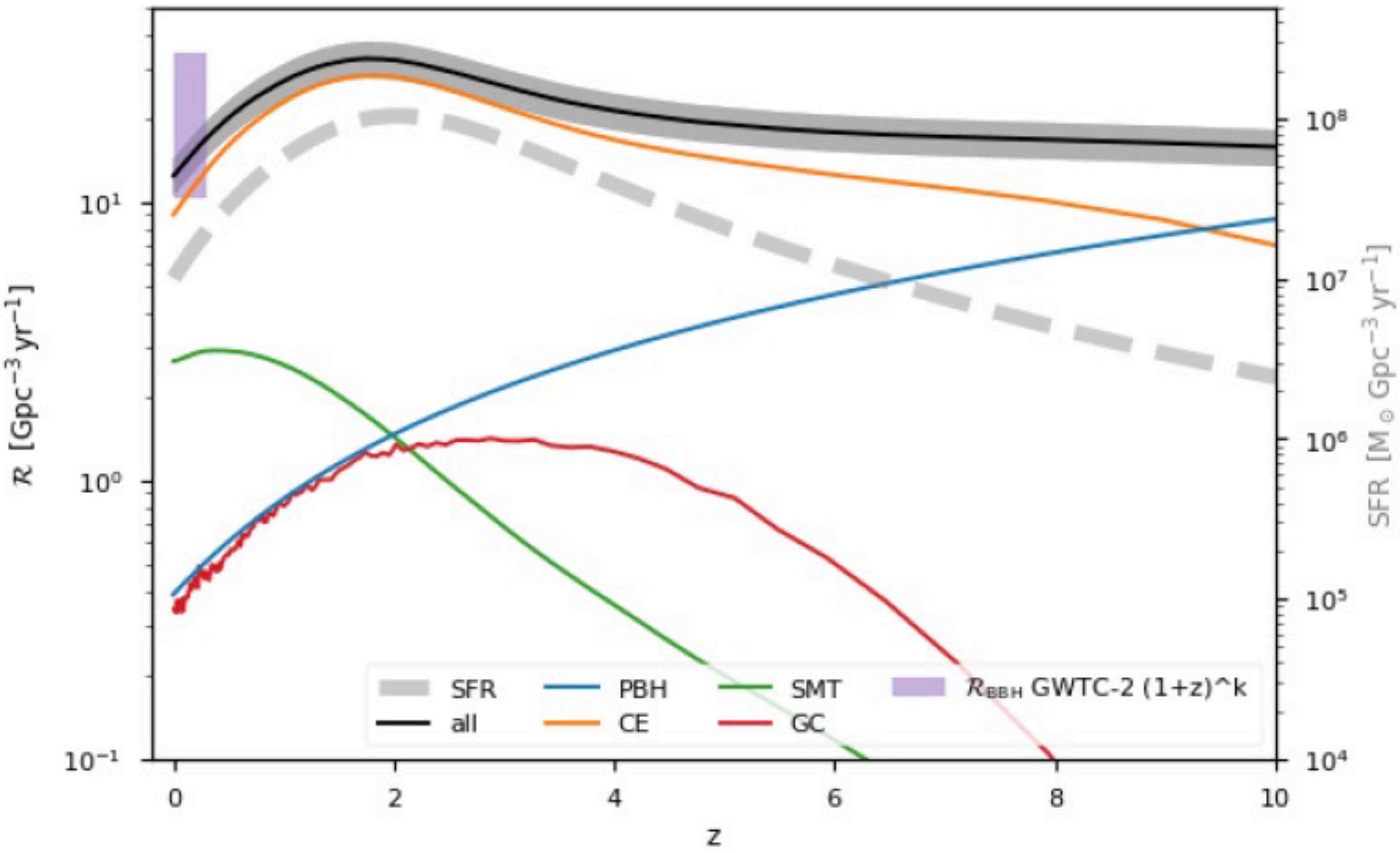
Rate of GW150914



fraction to CDM ($f_{fraction}$)

PBH mergers in the total merger rate

Simone S. Bavera, Gabriele Franciolini, Giulia Cusin, Antonio Riotto, Michael Zevin, Tassos Fragos, arXiv:2109.05836 [astro-ph.CO]



Evidence for primordial black holes in LIGO/Virgo gravitational-wave data

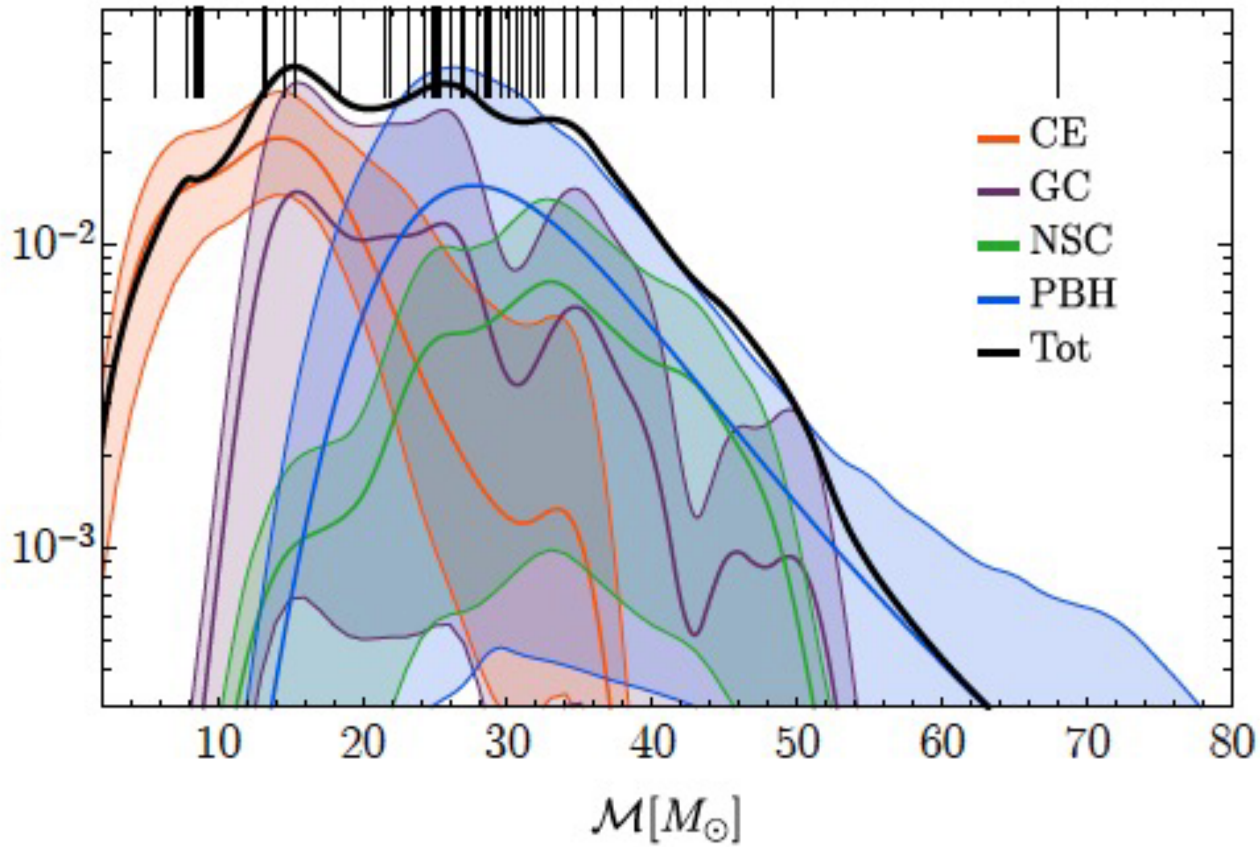
Gabriele Franciolini, Vishal Baibhav, Valerio De Luca, Ken K. Y. Ng, Kaze W. K. Wong, Emanuele Berti, Paolo Pani, Antonio Riotto, Salvatore Vitale, arXiv:2105.03349

a late-phase common envelope (CE)

nuclear star clusters (NSC)

old, metal-poor globular clusters (GC)

Distribution



How to produce the binary black holes (BBH) with masses of O(10) $M_\odot$?

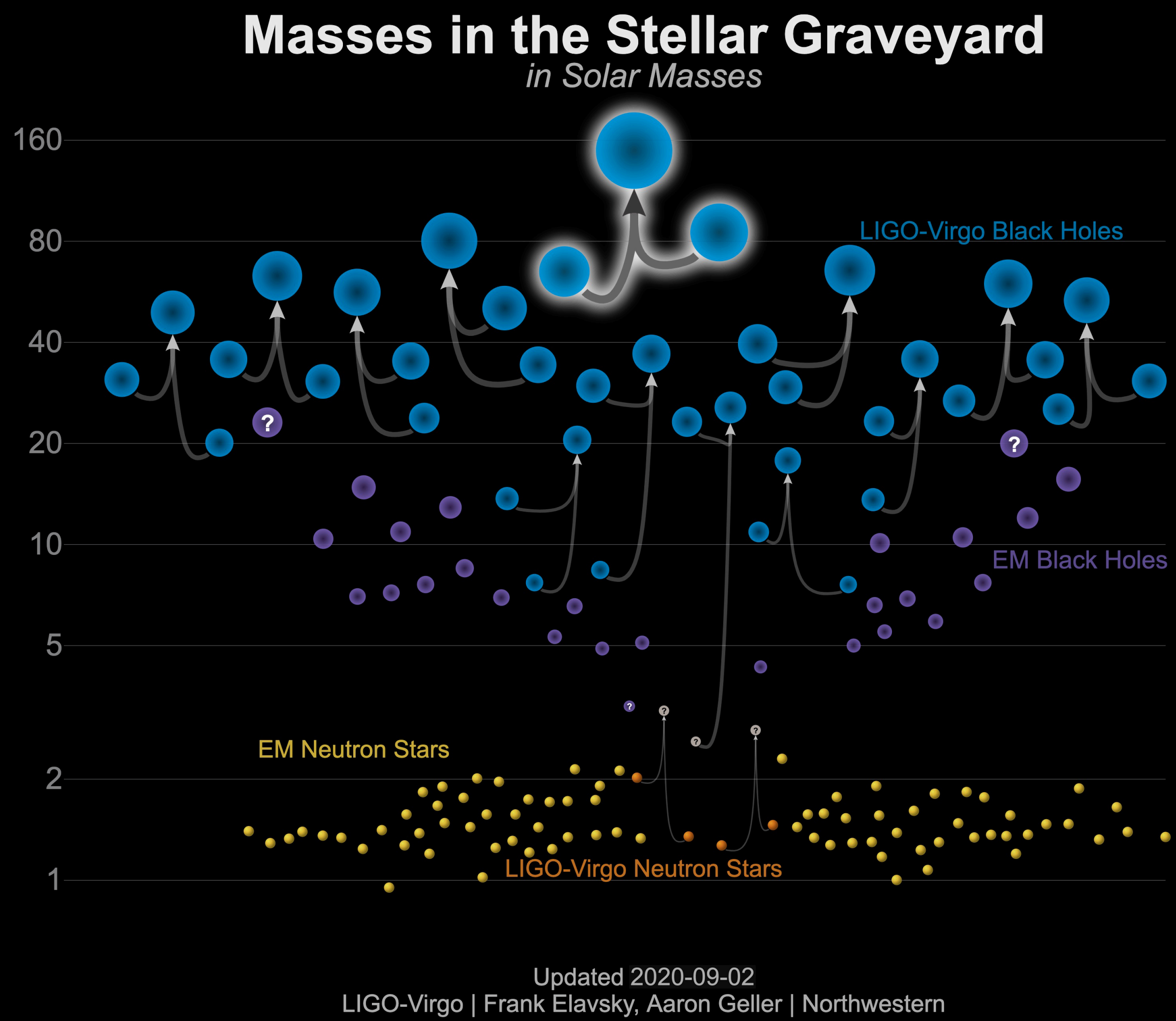
- Astrophysics: Large uncertainties on gravitational frictions through common envelope phases, mechanisms of supernovae (SNe) and appropriate kick velocities after SNe for Pop III/Pop II stars [astrophysically-model dependent]

- Cosmology: large uncertainties on numbers of PBHs, which depend on inflation models

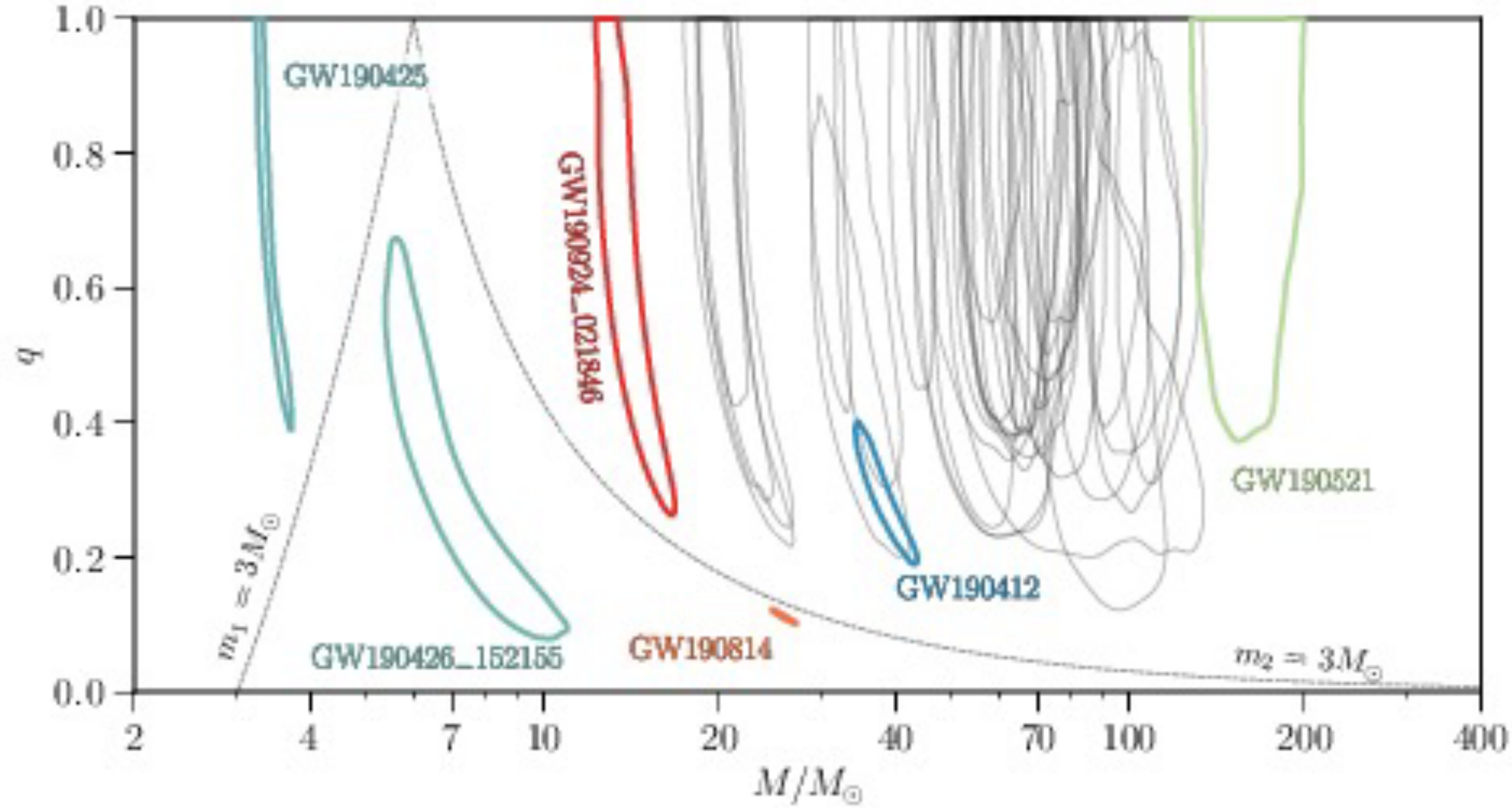
  [cosmologically-model dependent]

Mass Gap

M = 2 – 5 $M_\odot$ or M >> O(10) $M_\odot$ would be no longer neutron stars or astrophysical BHs



Mass ratio q v.s. total mass

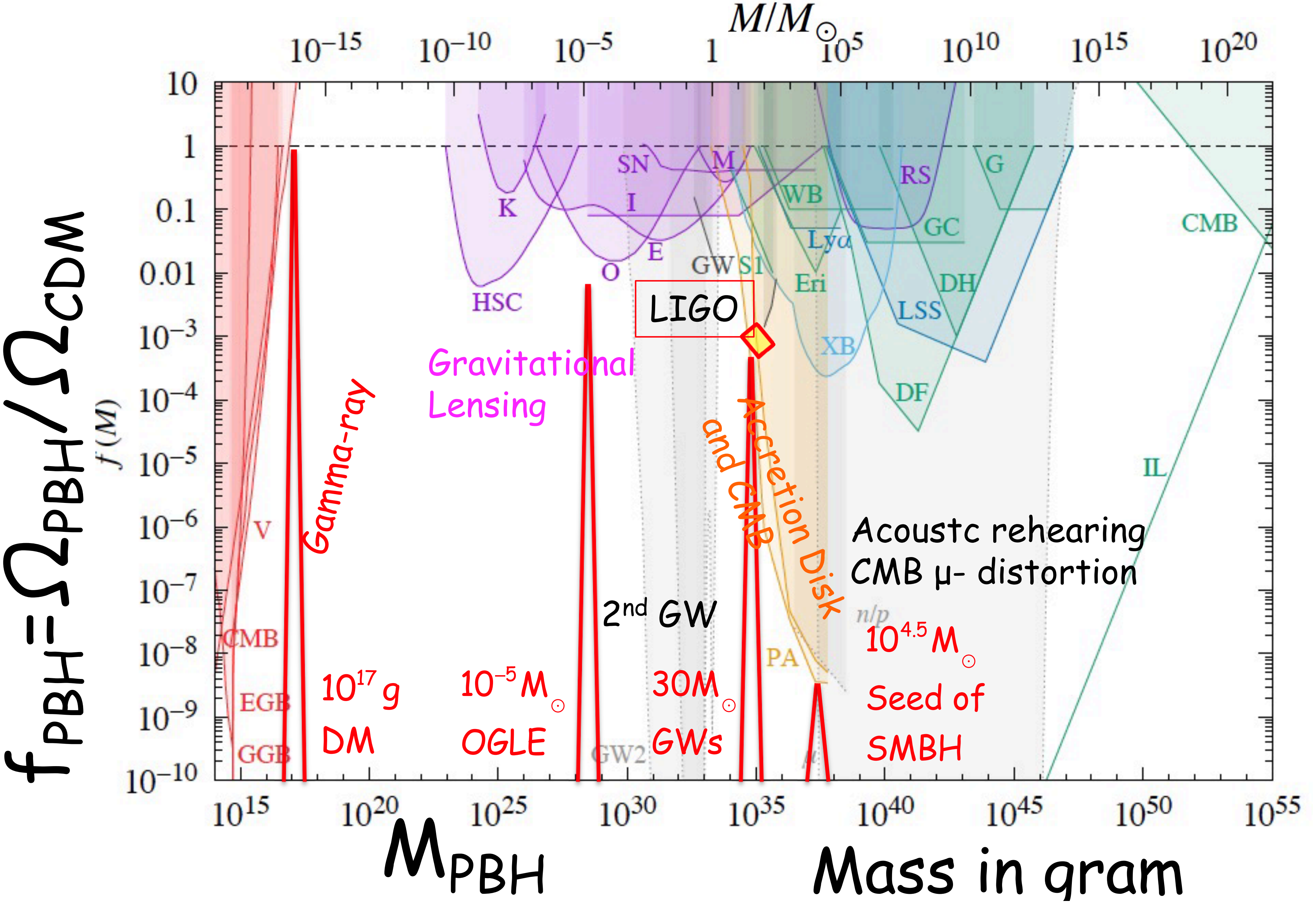


Credible region contours for all candidate events in the plane of total mass M and mass ratio q. Each contour represents the 90\% credible region for a different event. We highlight the previously published notable candidate events: \protect\NAME{GW190412A}, \protect\NAME{GW190425A}, \protect\NAME{GW190521A}\ and \protect\NAME{GW190814A}, the potential NSBH \protect\NAME{GW190426A}, and finally \protect\NAME{GW190924A}, which is most probably the least massive system with both masses >3\,\Msun. The dashed lines delineate regions where the primary/secondary can have a mass below 3\,\Msun. For the region above the m_2=3 \,\Msun line, both objects in the binary have masses above 3\,\Msun.

R. Abbott, et al, LSC P&P Committee, arXiv:2010.14527 [gr-qc]

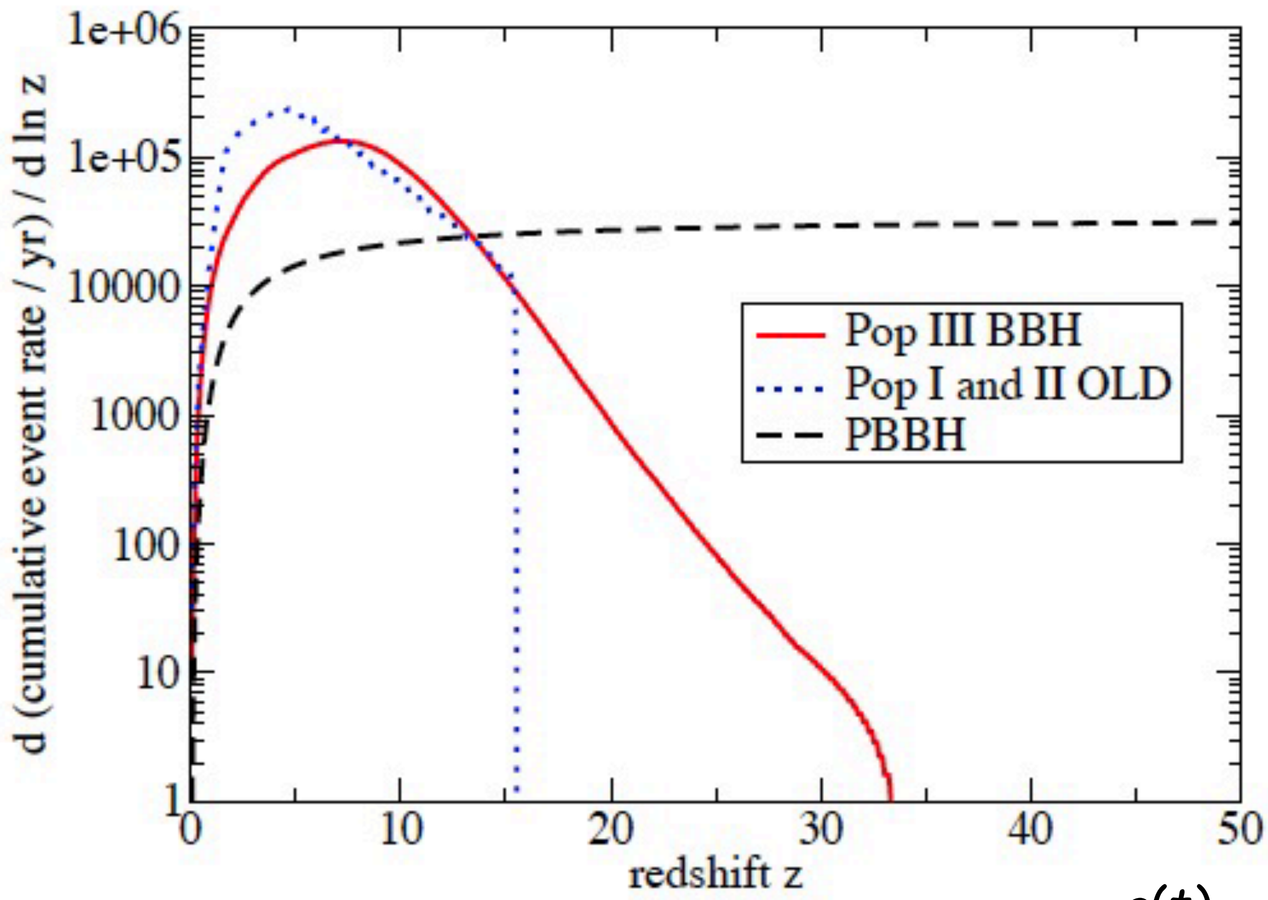
Upper bounds on the fraction to CDM

Carr, Kohri, Sendouda, J.Yokoyama (2009)(2020)



DECIGO discriminates BPBHs from the normal BBHs

Takashi Nakamura et al, arXiv:1607.00897 [astro-ph.HE]

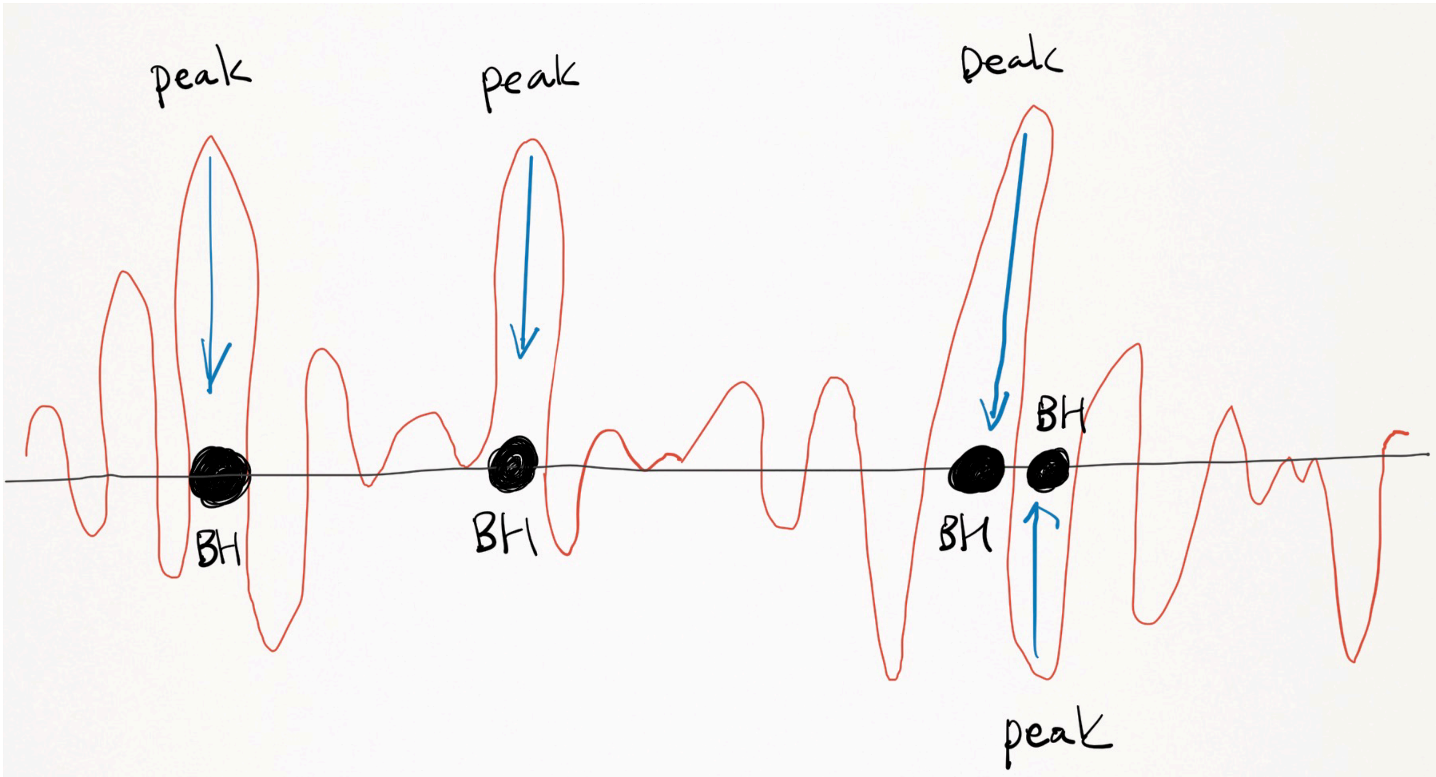


$$1/z \sim \frac{a(t)}{a(t_0)} \sim \left(t/10Gyr\right)^{2/3}$$

Formations of PBHs
(in the radiation dominated epoch)

Primordial Black Hole (PBH)

- Large perturbation at small scales was produced by Inflation at around $> 10^{-38}$ second



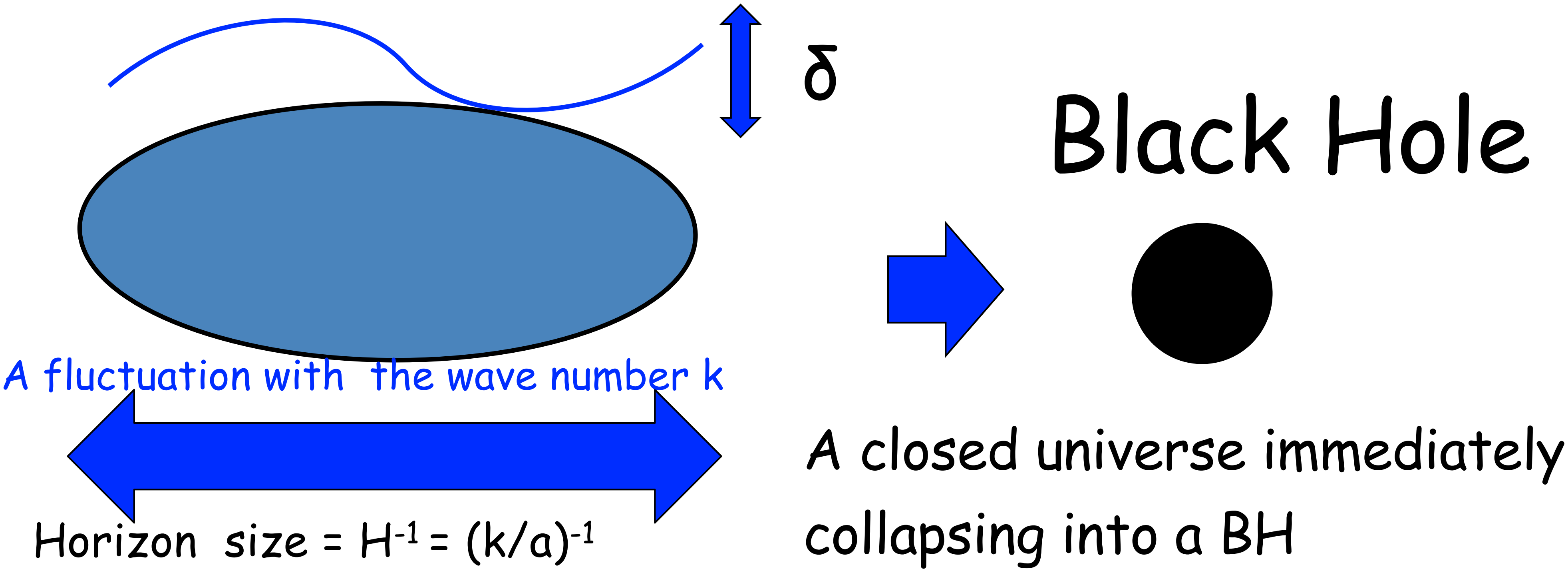
Conditions for a PBH formation in Radiation dominated (RD) Universe

Zel'dovich and Novikov (1967), Hawking (1971), Carr (1975)

Harada,Yoo and KK (2013)

- Gravity could be stronger than pressure

$$\delta > \delta_c \sim p / \rho \sim c_s^2 = w = 1/3$$



P_ζ (k) and PBH abundance β(M)

- Fraction of PBH to the total with Press Schechter formalism

For Peak Statistics,
e.g., see Yoo, Harada, KK et al (2018)(2020)

$$\beta(M) \equiv \frac{\rho_{\rm PBH}(M)}{\rho_{\rm tot}} = 2\int_{\delta_{\rm th}}^{\infty} d\delta \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{\delta^2}{2\sigma^2}\right) = {\rm erfc}\left(\frac{\delta_{\rm th}}{\sqrt{2}\sigma}\right)$$

$\delta_{\rm th} \sim 1/3 - 0.5$

For analytical derivations, see Harada, Yoo, KK (2013)

$\sigma \sim \overline{\delta\rho/\rho}$

- Relation between β and fluctuation σ (or β and Ω)

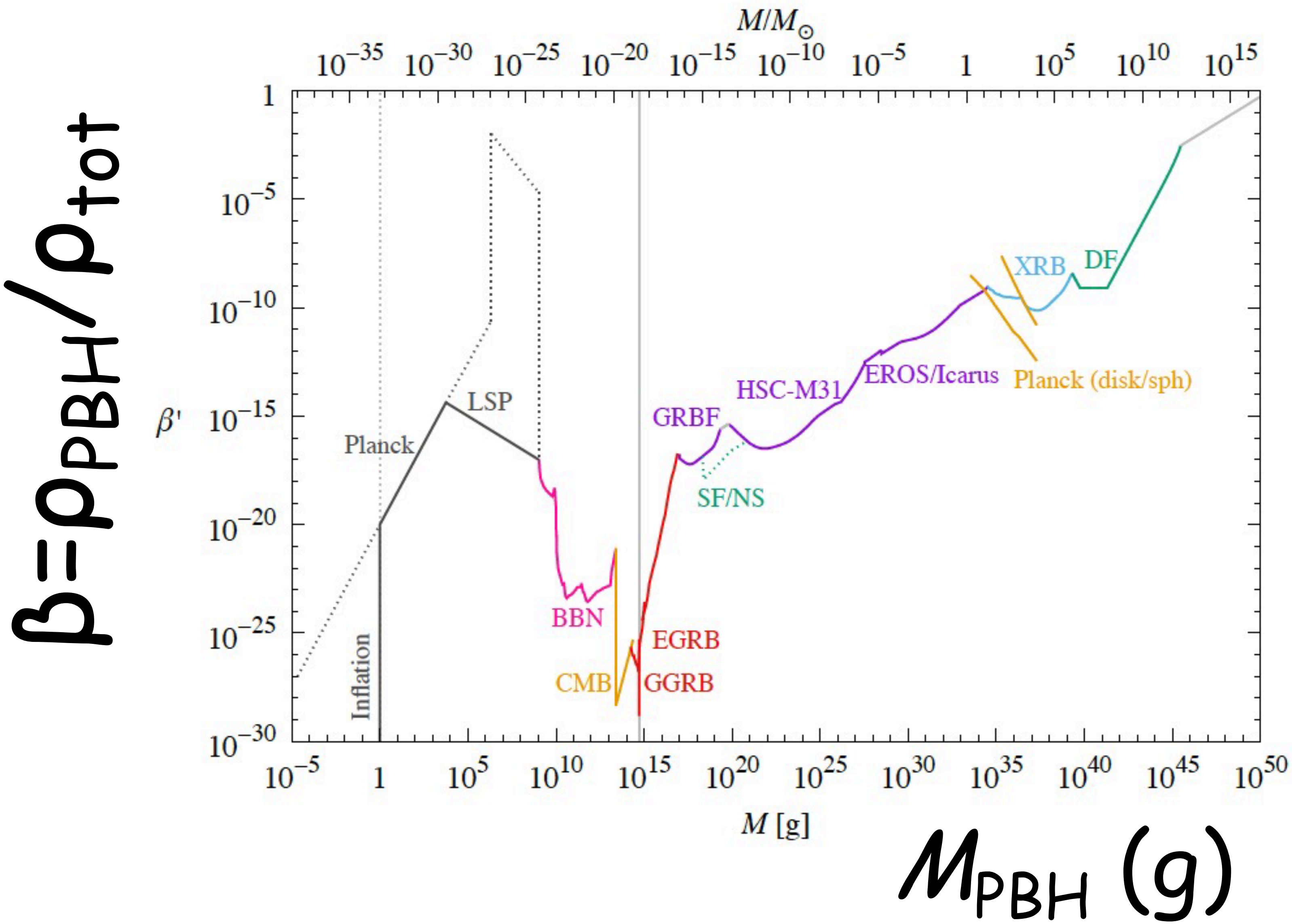
$$\beta(M) \sim {\rm erfc}\left(\frac{\delta_{\rm th}}{\sqrt{2}\sigma}\right) \simeq \sqrt{\frac{2}{\pi}}\frac{\sigma}{\delta_{\rm th}} \exp\left(-\frac{\delta_{\rm th}^2}{2\sigma^2}\right)$$

$$= 1.5 \times 10^{-18} \left(\frac{m_{\rm PBH}}{10^{15} g}\right)^{1/2} \left(\frac{\Omega_{\rm PBH} h^2}{0.1}\right)$$

$\sigma^2 \sim P_\zeta$

$\beta=\rho_{PBH}/\rho_{tot}$ vs M_{PBH}

Carr, Kohri, Sendouda, J.Yokoyama (2009)(2020)



Typical quantities of PBHs in RD

- Mass (horizon mass $=\rho(t_{form})\, H(t_{form})^{-3}$)

$$M_{PBH} \sim \rho(H_{form}^{-1})^3 \sim M_{pl}^2 t_{from} \sim \frac{M_{pl}^3}{T_{form}^2} \sim 10^{15} g \left(\frac{T_{form}}{3\times 10^8 GeV} \right)^{-2} \sim 30 M_\odot \left(\frac{T_{form}}{40 MeV} \right)^{-2}$$

- Lifetime

$$\tau_{PBH} \sim \frac{M_{PBH}^3}{M_{pl}^4} \sim 4\times 10^{17} sec \left(\frac{M_{PBH}}{10^{15} g} \right)^3 \sim 3\times 10^{68} yrs \left(\frac{M_{PBH}}{30 M_\odot} \right)^3$$

- Hawking Temperature

$$T_{PBH} \sim \frac{M_{pl}^2}{M_{PBH}} \sim 0.1 MeV \left(\frac{M_{PBH}}{10^{15} g} \right)^{-1} \sim 3\times 10^{-11} K \left(\frac{M_{PBH}}{30 M_\odot} \right)^{-1}$$

- Wave number of horizon length

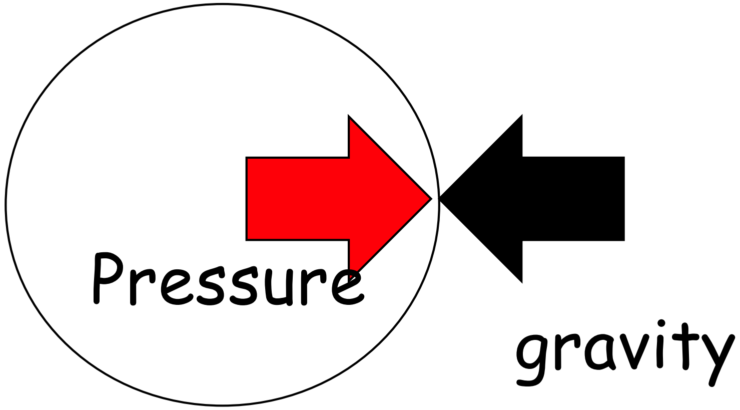
$$k = aH \sim 10^5 Mpc^{-1} \left(\frac{M_{PBH}}{10^4 M_\odot} \right)^{-1/2} \sim 10^5 Mpc^{-1} \left(\frac{T_{form}}{MeV} \right)^{+1}$$

- Fraction to CDM

$$f_{fraction} \equiv \frac{\Omega_{PBH}}{\Omega_{CDM}} \sim \left(\frac{\beta}{10^{-18}} \right) \left(\frac{M_{PBH}}{10^{15} g} \right)^{-1/2} \sim \left(\frac{\beta}{10^{-8}} \right) \left(\frac{M_{PBH}}{30 M_\odot} \right)^{-1/2} \sim 10^8 \left(\frac{M_{PBH}}{30 M_\odot} \right)^{-1/2} \sqrt{P_\delta} \exp\left[-\frac{1}{18 P_\delta} \right]$$

Features of PBH formations in RD

- Spherical due to radiation pressure



$(w \equiv p / \rho \sim 1/3)$

- Negligible evolutions of density perturbations
- Quite a small angular momentum

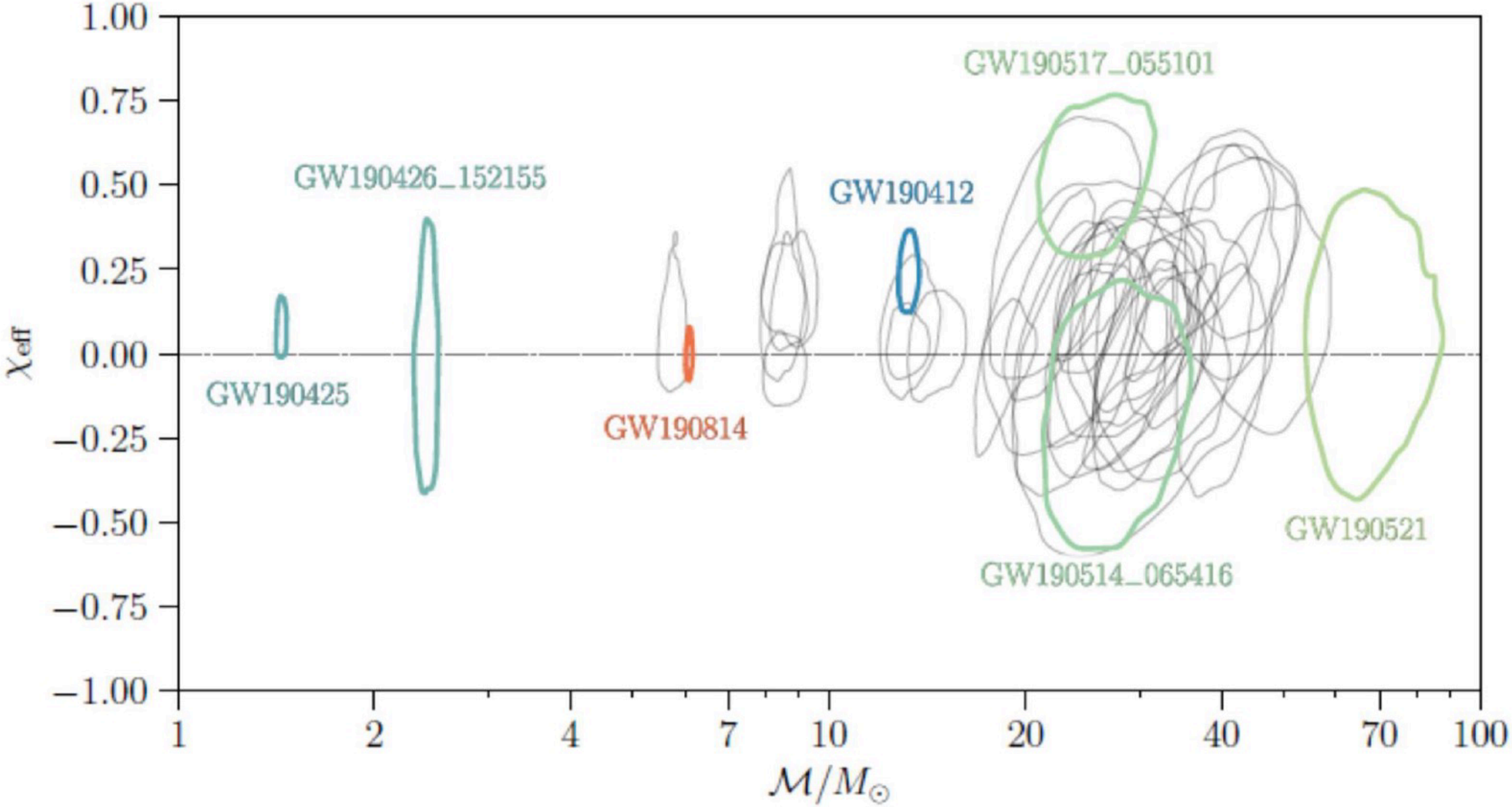
See, T.Chiba and S.Yokoyama, 2017
De Luca et al, 2019
Minxi He and Suyama, 2019
Harada, Yoo, Kohri, Koga and Monobe, 2020

(dimensionless Kerr parameter)

$$\sqrt{\langle a_*^2 \rangle} \simeq 6.5 \times 10^{-4} \left(\frac{M}{M_H} \right)^{-1/3}$$

Effective inspiral spin parameter of the observed BHs

$$\chi_{\rm eff} = \frac{m_1\chi_1\cos\theta_1 + m_2\chi_2\cos\theta_2}{m_1+m_2}$$

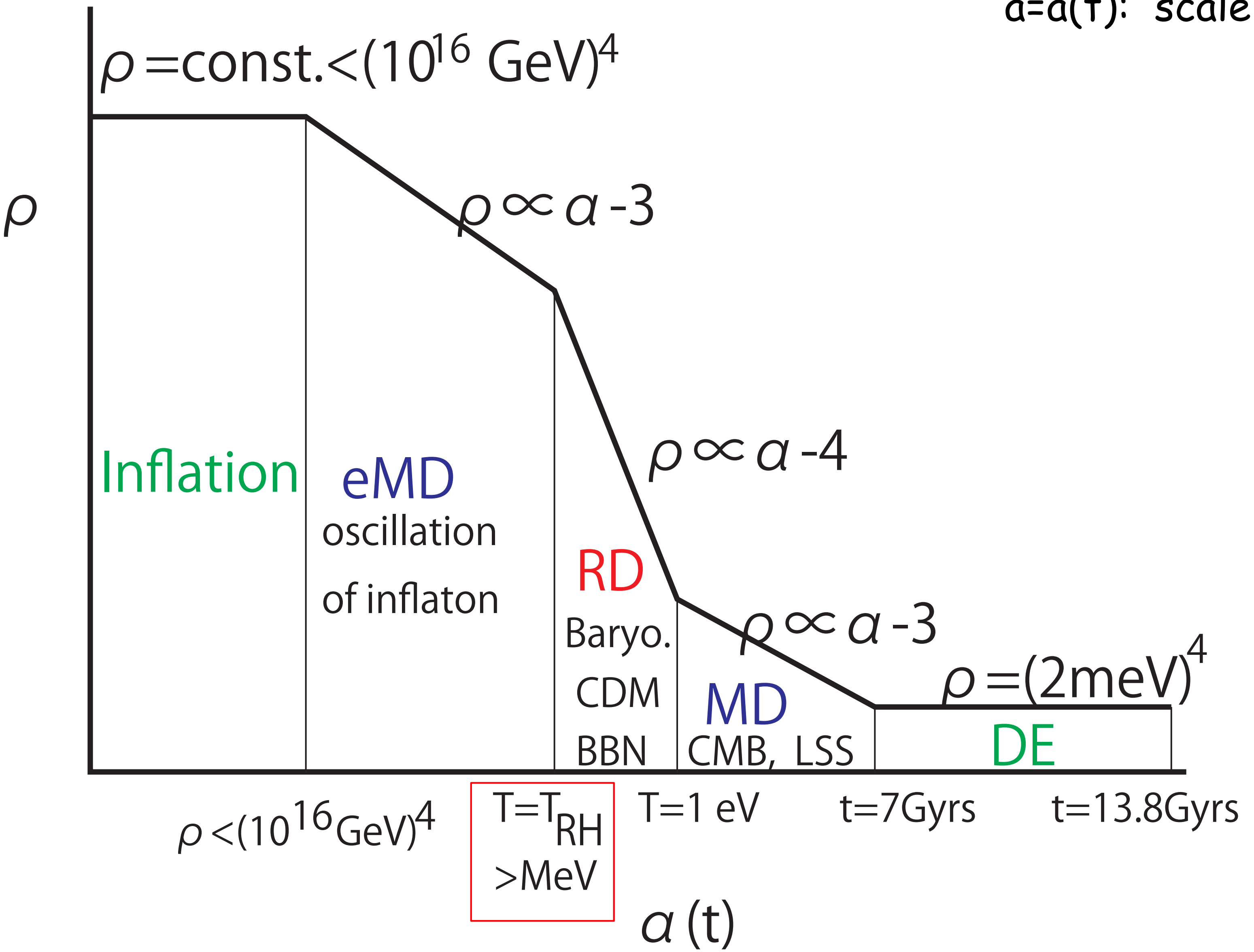


Credible region contours for all candidate events in the plane of chirp mass $\mathcal{M}$ and effective inspiral spin \chieff. Each contour represents the 90\% credible region for a different event. We highlighted the previously published candidate events (cf.\ Fig.~\ref{fig:mtotqpost}), as well as \protect\NAME{GW190517A}\ and \protect\NAME{GW190514A}, which have the highest probabilities of having the largest and smallest \chieff respectively.

R. Abbott, et al, LSC P&P Committee, arXiv:2010.14527 [gr-qc]

Cosmic history of energy density

a=a(t): scale factor



Inflation models

PBH formation and Inflation models

- Multi-field Inflaiton — Kawasaki,Sugiyama,Yanagida (1998)
- At the end of inflation — Lyth, Malik, Sasaki, Zabarra (2006)
- Preheating — Green and Malik (1999)
  Taruya (1998)
- Blue-tilted spectral — Kohri, Lyth and Melchiorri (2007)
- Curvaton — Kawasaki, Kitanijima, Yanagida (2012)
  Kohri, Lin, Matsuda (2012)
- …

Simple parameterization of running of spectral indexes of curvature perturbation

- Curvature perturbation

$$P_\zeta(k) = A_s \left(\frac{k}{k_*}\right)^{n_s - 1 + \frac{\alpha_s}{2}\ln\left(\frac{k}{k_*}\right) + \frac{\beta_s}{6}\left(\ln\left(\frac{k}{k_*}\right)\right)^2}$$

$$A_s \equiv P_\zeta|_* \sim \left.\frac{V}{m_{\rm pl}^4 \varepsilon}\right|_* \sim (\delta T/T)^2$$

$$\varepsilon \equiv \frac{1}{2}\left(m_{\rm pl}\frac{V'}{V}\right)^2$$

- spectral index

$$n_s - 1 = dP_\zeta/d\ln k = 2\eta - 6\varepsilon$$

$$\eta \equiv m_{\rm pl}^2 \frac{V''}{V}$$

- running of n_s

$$\alpha_s = dn_s/d\ln k = -24\varepsilon^2 + 16\varepsilon\eta - \xi^{(2)}$$

$$\xi^{(2)} \equiv m_{\rm pl}^4 \frac{V'V'''}{V^2}$$

- running of running of n_s

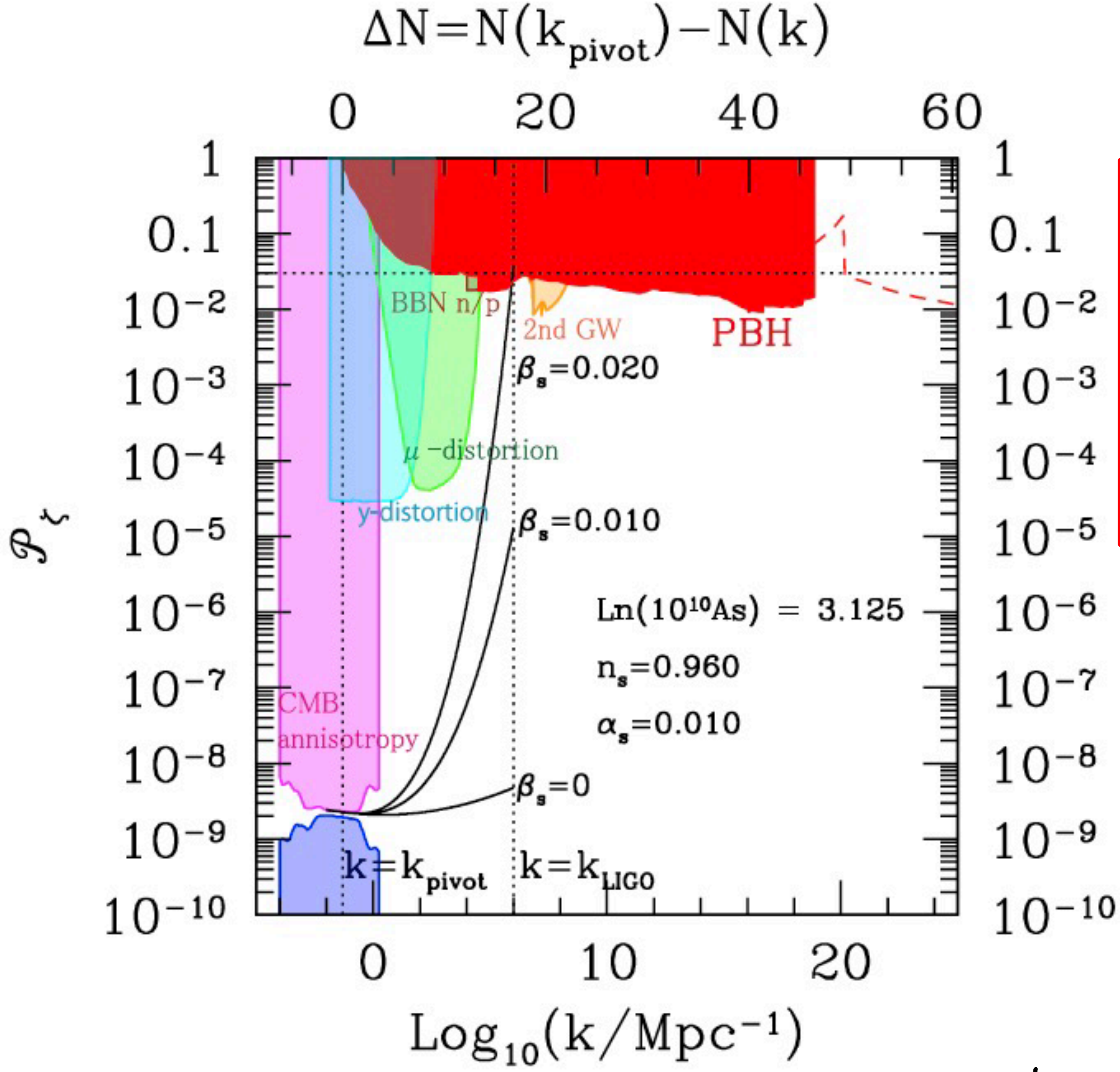
$$\sigma^{(3)} \equiv m_{\rm pl}^6 \frac{(V')^2 V''''}{V^3}$$

$$\beta_s = d\alpha_s/d\ln k = 192\varepsilon^3 + 192\varepsilon^2\eta - 32\varepsilon\eta^2 + (-24\varepsilon + 2\eta)\xi^{(2)} + 2\sigma^{(2)}$$

Curvature perturbation $P_\zeta(k)$

KK and T.Terada, 2018
Alabidi, Kohri, Sendouda, Sasaki, 2013

Amplitude of curvature perturbation



Planck (2015)

$n_s = 0.9586 \pm 0.0056,$

$\alpha_s = 0.009 \pm 0.010,$

$\beta_s = 0.025 \pm 0.013.$

at 68% C.L.

For inflation models with a big running, see Kohri, Lin Lyth (2008)

wave number k = p x a

Type-III Hilltop inflation models

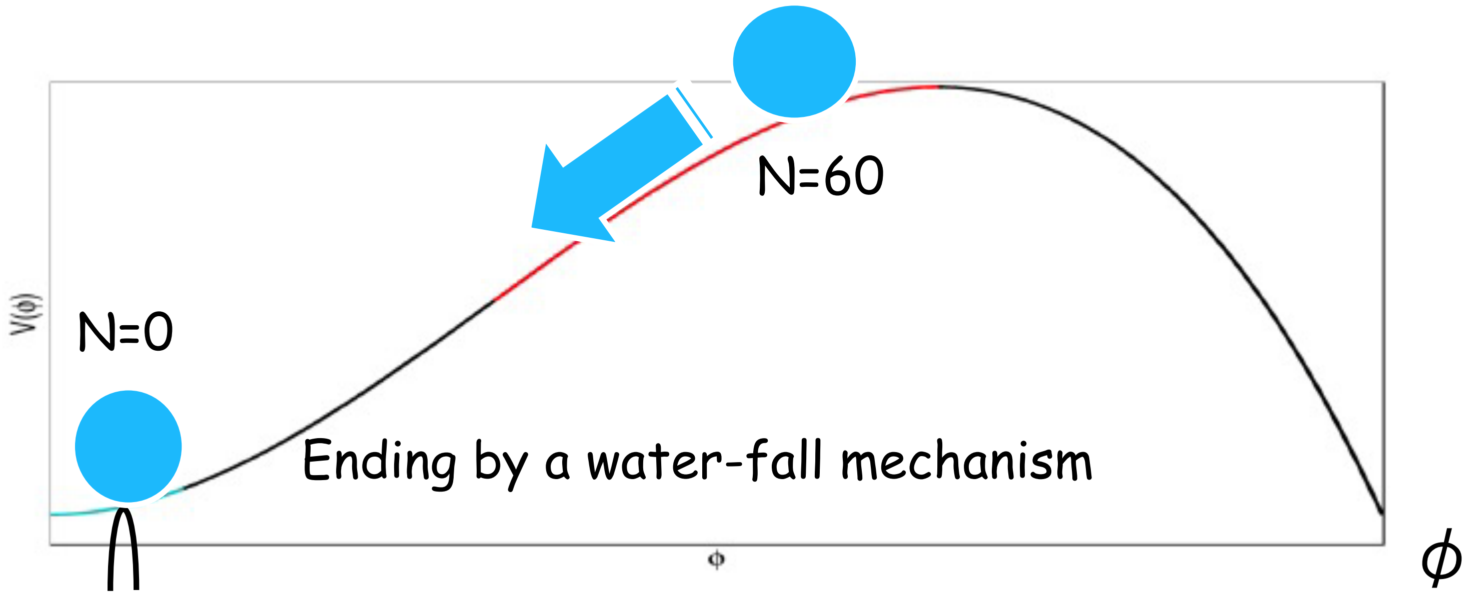
German, Ross, Sarkar (01)
KK, Lin and Lyth (07)

- Potential in supergravity, e.g.,

$$V(\phi) \;=\; V_0 + \frac{1}{2}m^2\phi^2 - \lambda\frac{\phi^p}{M_P^{p-4}} + \cdots$$

$$W = C\frac{\phi^\rho}{M_{pl}^{p-3}}, \quad \lambda \sim C m_{3/2}/M_{pl}$$ in SUGRA

Allahverdi, Kusenko and Mazumdar (06)



Large running spectral index

KK, Lin and Lyth (07)

- Spectrum

$$P_\zeta \sim \frac{V}{m_{\rm pl}^4 \varepsilon}$$

- Enhanced curvature perturbation at small scales due to a large running of running

$$\varepsilon \equiv \frac{1}{2}\left(m_{\rm pl}\frac{V'}{V}\right)^2 \to 0 \text{ for } \phi \downarrow$$

$$\beta_s = \frac{d^3 P_\zeta}{d(\ln k)^3} = 192\epsilon^3 + 192\epsilon^2\eta - 32\epsilon\eta^2 + (-24\epsilon + 2\eta)\xi^{(2)} + 2\sigma^{(3)}$$

Could be large!

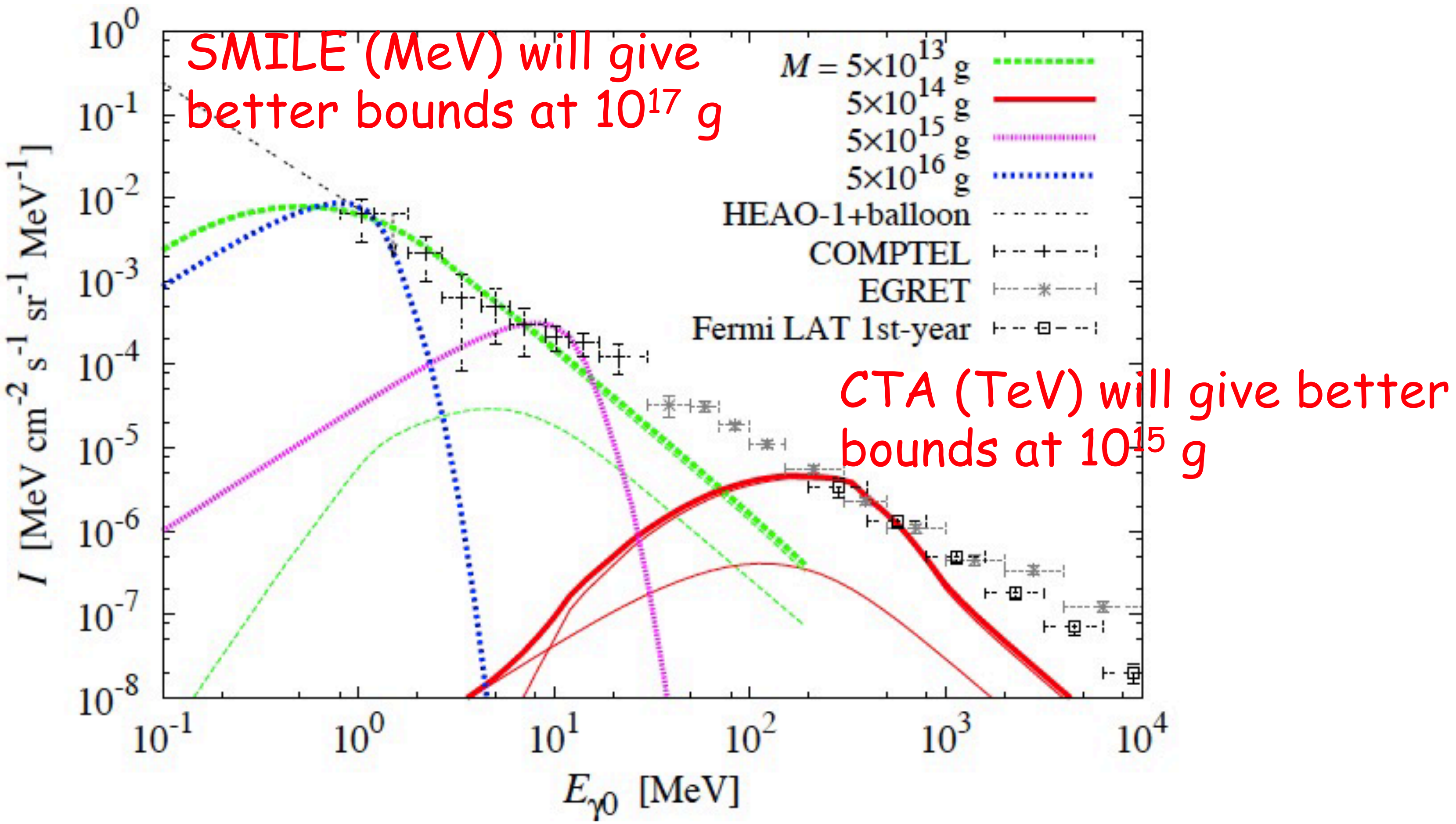
Observational constraints on PBHs

High-energy particles from evaporating PBHs :	$M < 10^{-16}\ M_\odot$
To be dark matter :	$10^{-16} < M < 10^{-10}\ M_\odot$
Gravitational lensing :	$10^{-10} < M < 10^{0}\ M_\odot$
GWs from merging PBHs :	$10^{-4} < M < 10^{1}\ M_\odot$
Emission from accretion disk around a PBH :	$10^{0} < M < 10^{4}\ M_\odot$
CMB distortions by dissipating density perturbation :	$10^{4} < M < 10^{11}\ M_\odot$
Secondary GWs produced from large perturbation :	$10^{-8} < M < 10^{0}\ M_\odot$
…	

Evaporating PBHs through Hawking Process

Carr, Kohri, Sendouda and Yokoyama (2010)

$$d\dot{N}_s = \frac{dE}{2\pi}\frac{\Gamma_s}{e^{E/T_{BH}} - (-1)^{2s}}$$



M31 lensing on PBHs modified by size-distribution and finite-size effects on bright star sources

Nolan Smyth, Stefano Profumo, Samuel English, Tesla Jeltema, Kevin McKinnon, Puragra Guhathakurta, arXiv:1910.01285 [astro-ph.CO]

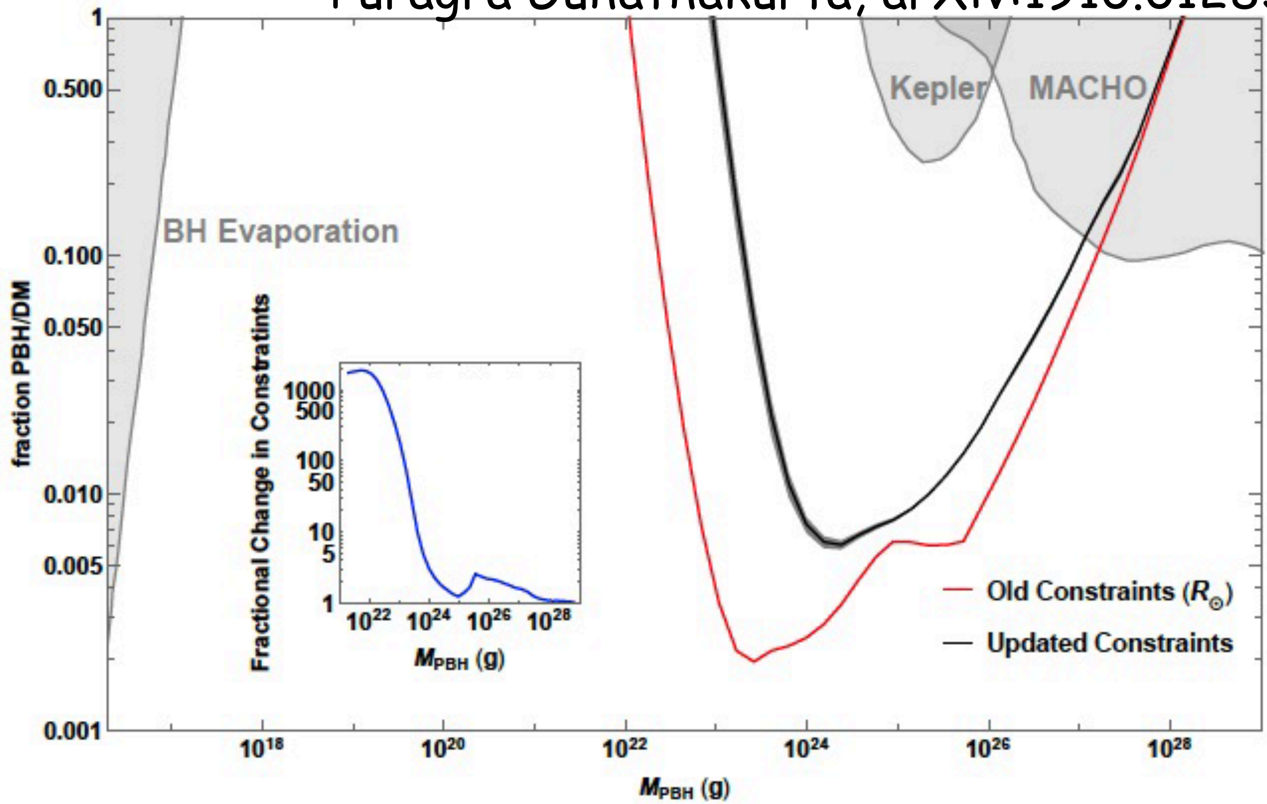
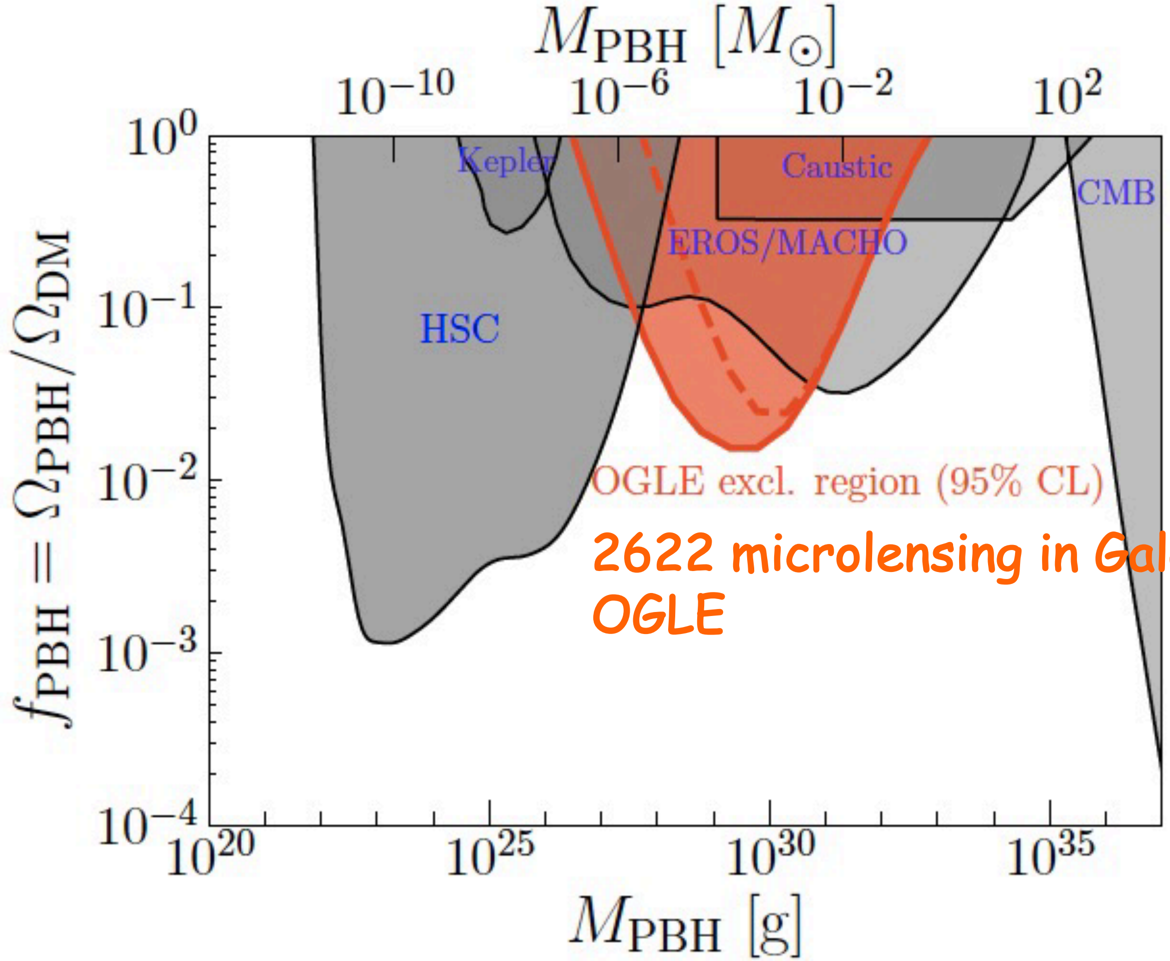


Figure 2. The constraints on primordial black holes as dark matter. The black line is the benchmark constraint and the primary result of this paper. The gray shading comes from the uncertainty in determining the stellar size distribution. The red line is

Gravitational lensing constrains on PBHs

Hiroko Niikura, Masahiro Takada, Shuichiro Yokoyama, Takahiro Sumi, Shogo Masaki,
arXiv:1901.07120 [astro-ph.CO]

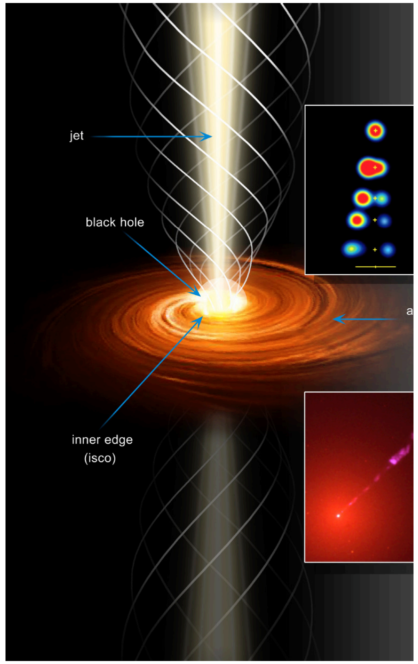


2622 microlensing in Galactic bulge by OGLE

CMB bound on PBHs by disk-accretion in the late MD epoch

Poulin, Serpico, Calore, Clesse, KK (2017)

- A non-spherical accretion disk (ADAF(slim) + Standard disk) around a PBH caused by an angular momentum emits radiation



$$\dot{M}_{\rm HB} \equiv 4\pi\lambda\,\rho_\infty v_{\rm eff} r_{\rm HB}^2 \equiv 4\pi\lambda\,\rho_\infty \frac{(GM)^2}{v_{\rm eff}^3}$$

$$l \simeq \omega\, r_{\rm HB}^2 \simeq \left(\frac{\delta\rho}{\rho} + \frac{\delta v}{v_{\rm eff}}\right) v_{\rm eff} r_{\rm HB}$$

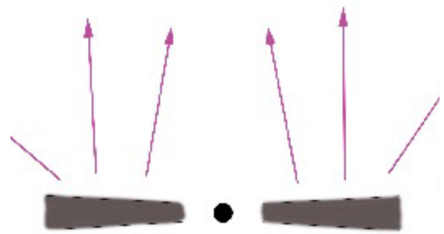
- CMB anisotropies are affected

- From observations, we can constrain the number density of PBHs

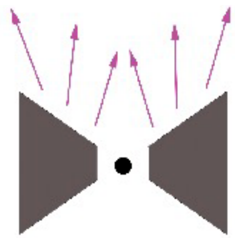
An accretion disk around a black hole

Kohri, Mineshige, 2002
Kohri, Narayan, Piran, 2005

Viscous heating process ⇔ Various cooling processe

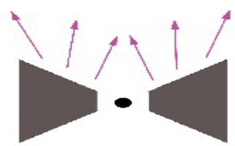


i. Standard Accretion Disk (Standard Disk)
   - Radiative Cooling



ii. Advection Dominated Accretion Flow (ADAF)
   - Advective cooling (entropy going into BH) gives RIAF (optically thin) or Slim Disk (optically-thick)

iii. Convection Dominated Accretion Flow (CDAF)
   - Convective cooling

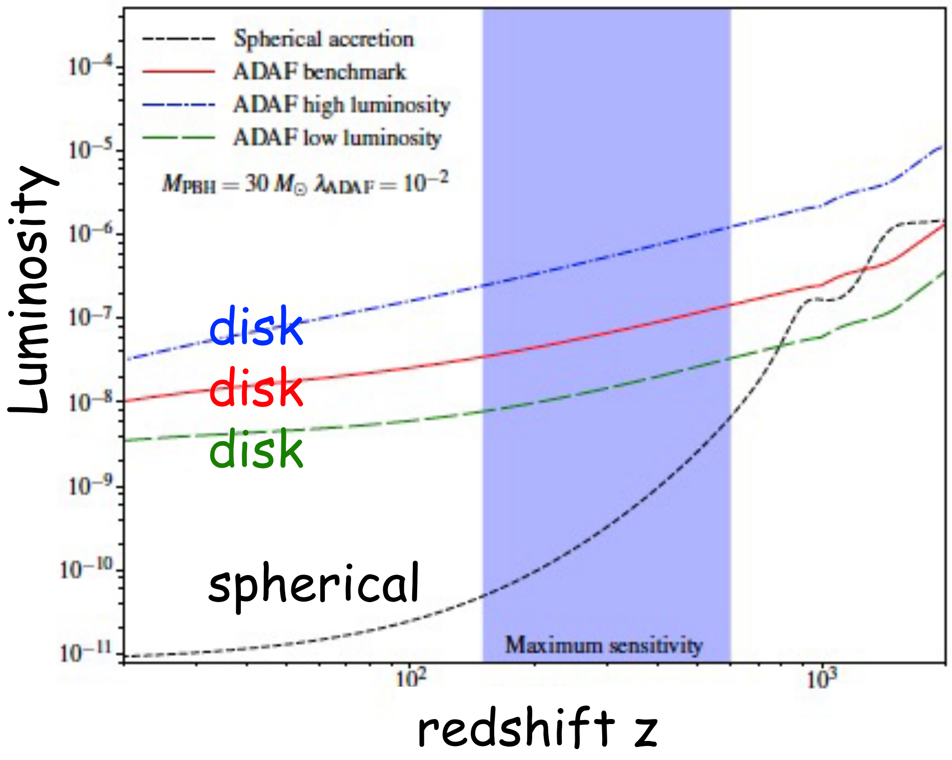


iv. Neutrino-Dominated Accretion Disk (NDAF)
   - Neutrino Cooling

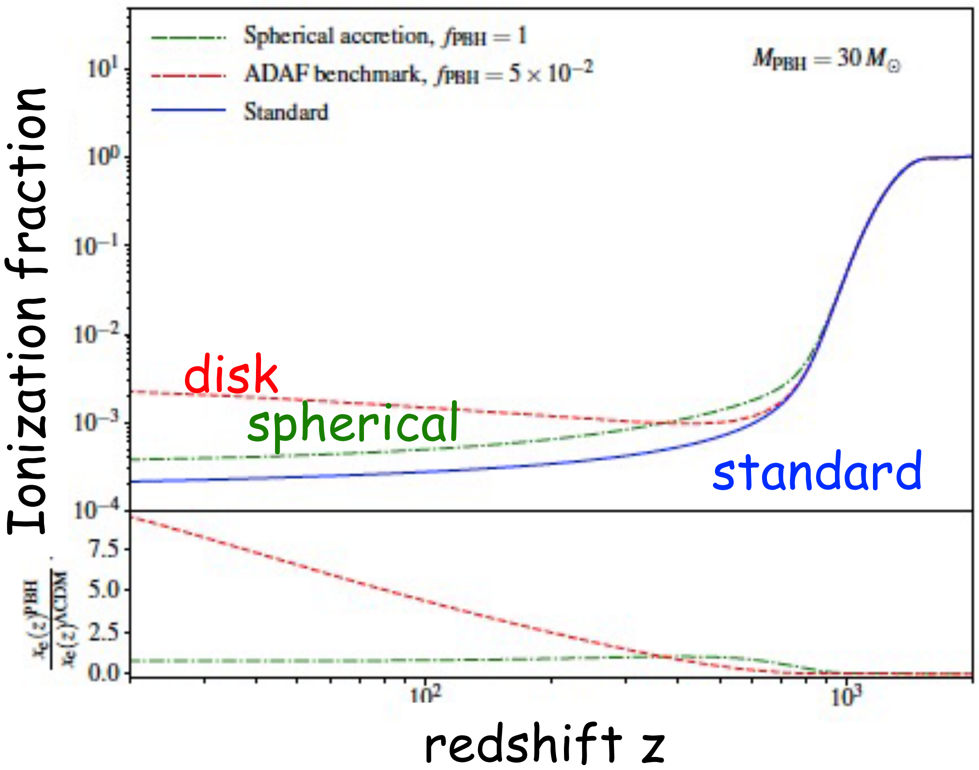
v. …

Modified CMB anisotropy

Poulin, Serpico, Calore, Clesse, Kohri (2017)



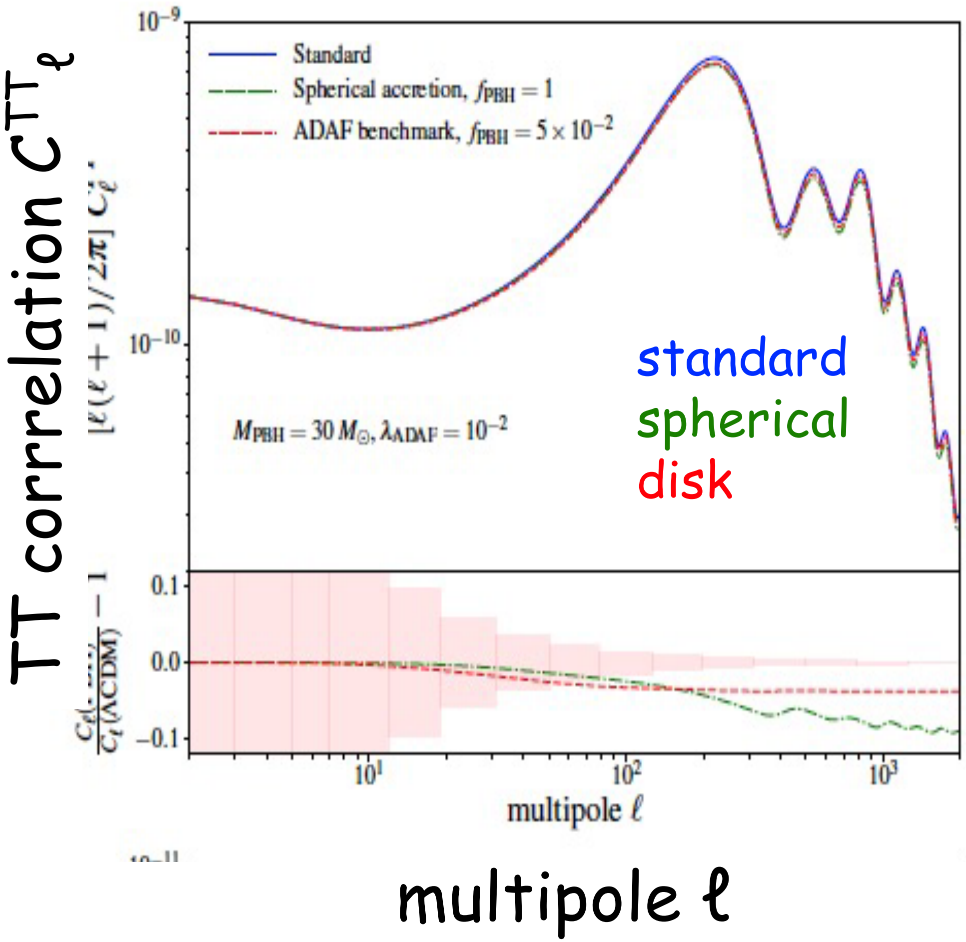
Luminosity

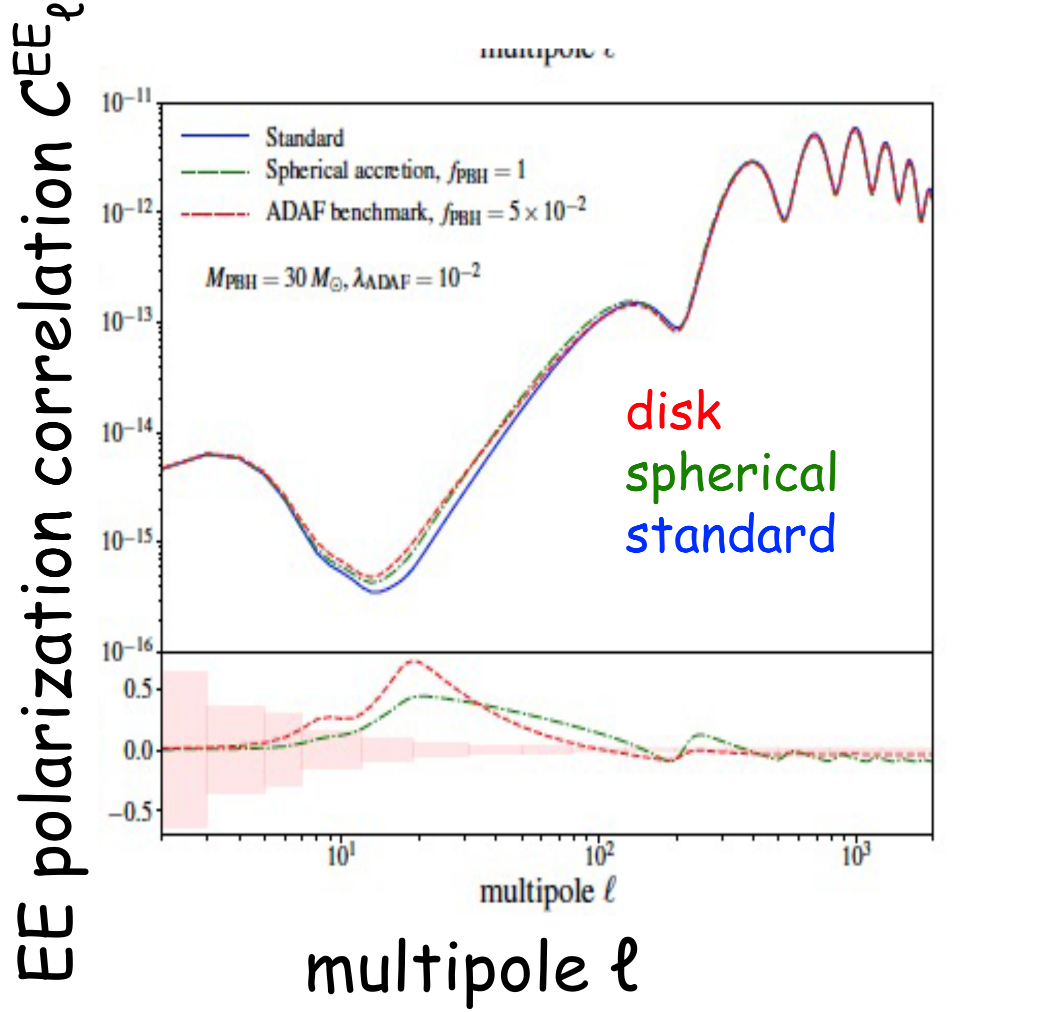


Ionization fraction

Modified CMB anisotropy

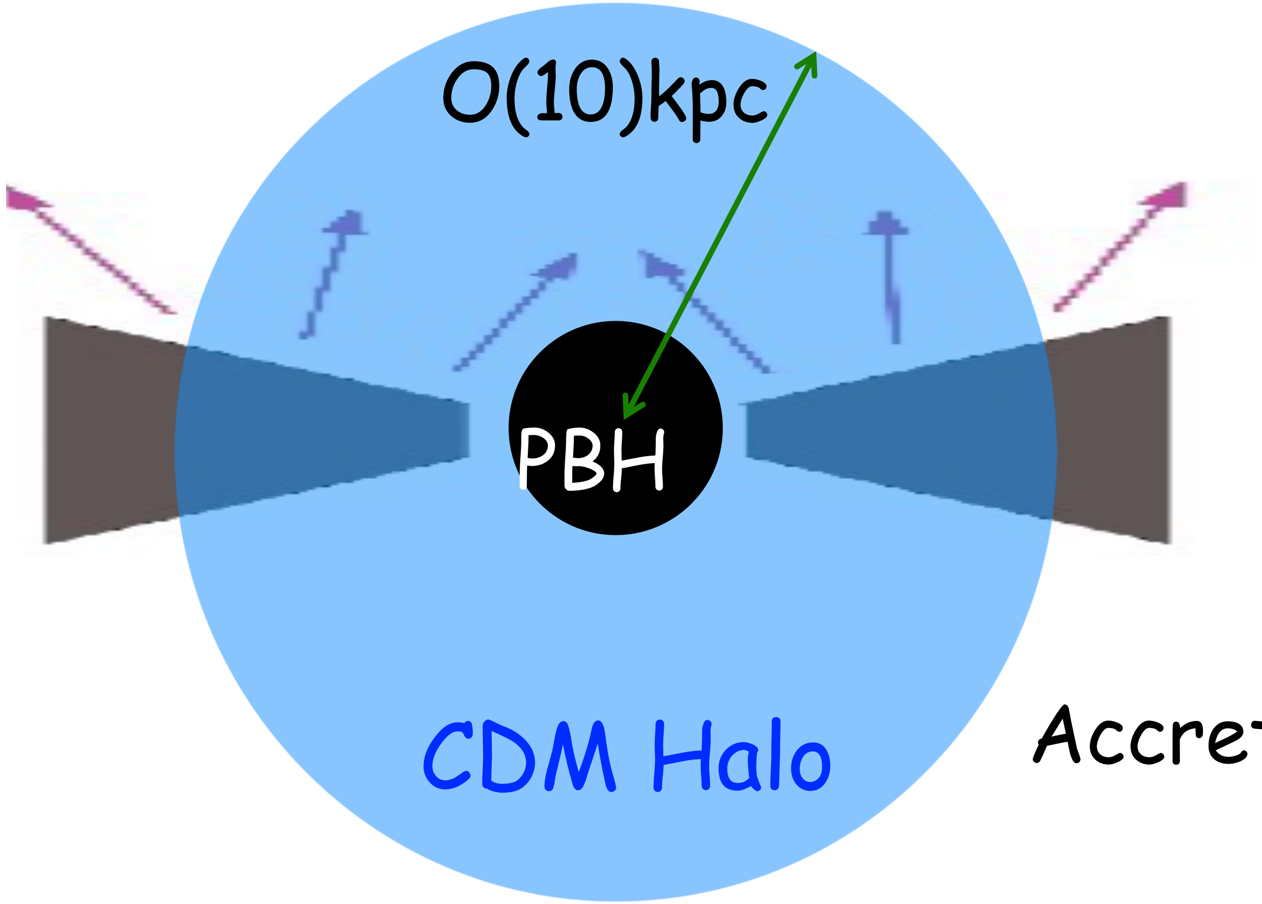
Poulin, Serpico, Calore, Clesse, Kohri (2017)





Cosmological baryon accretion onto the PBH + CDM halo system

Poulin, Serpico, Inman, Kohri (2020)



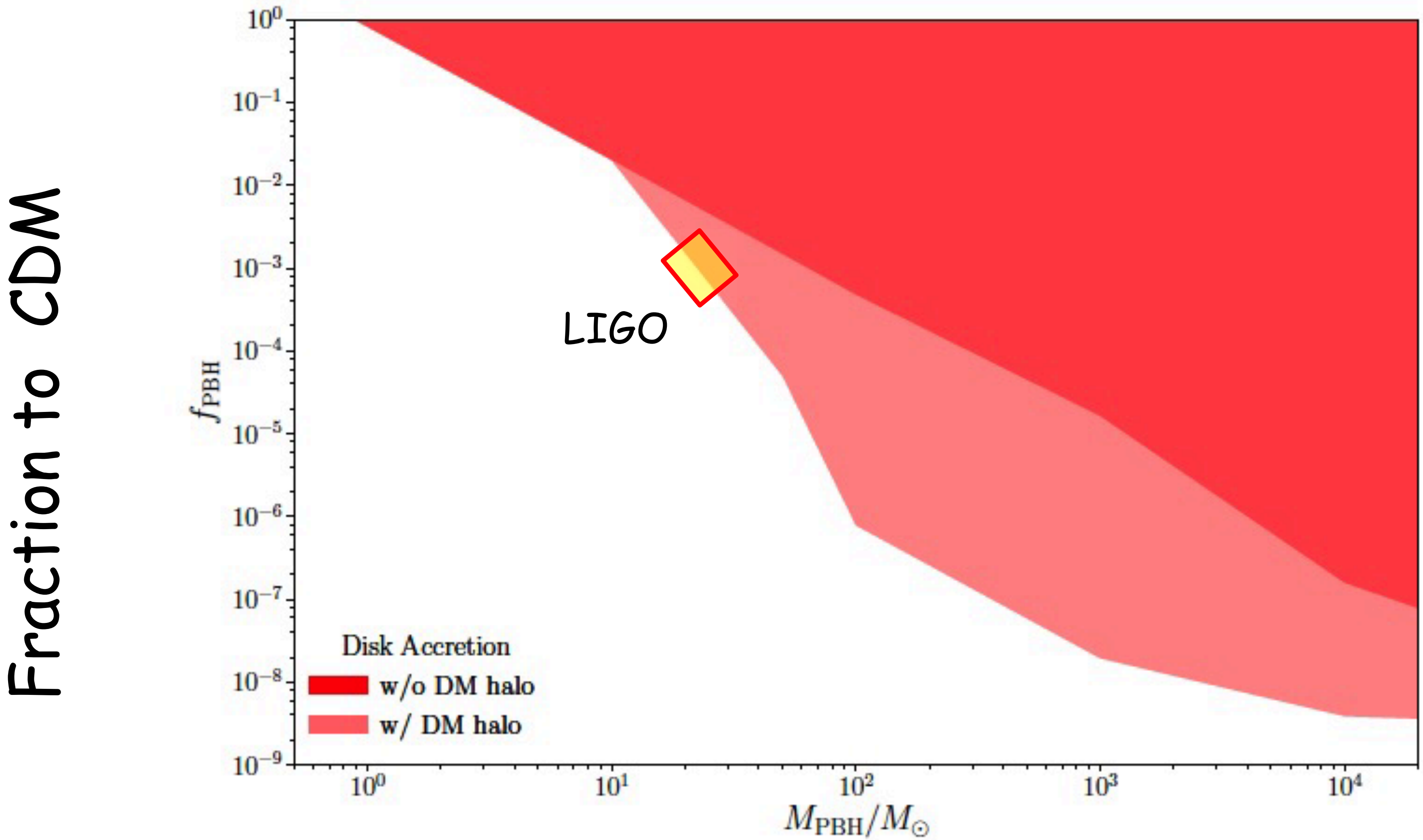
$\rho \propto r^{-2.25}$

Accretion onto CDM + PBH

z ~30 -- 100

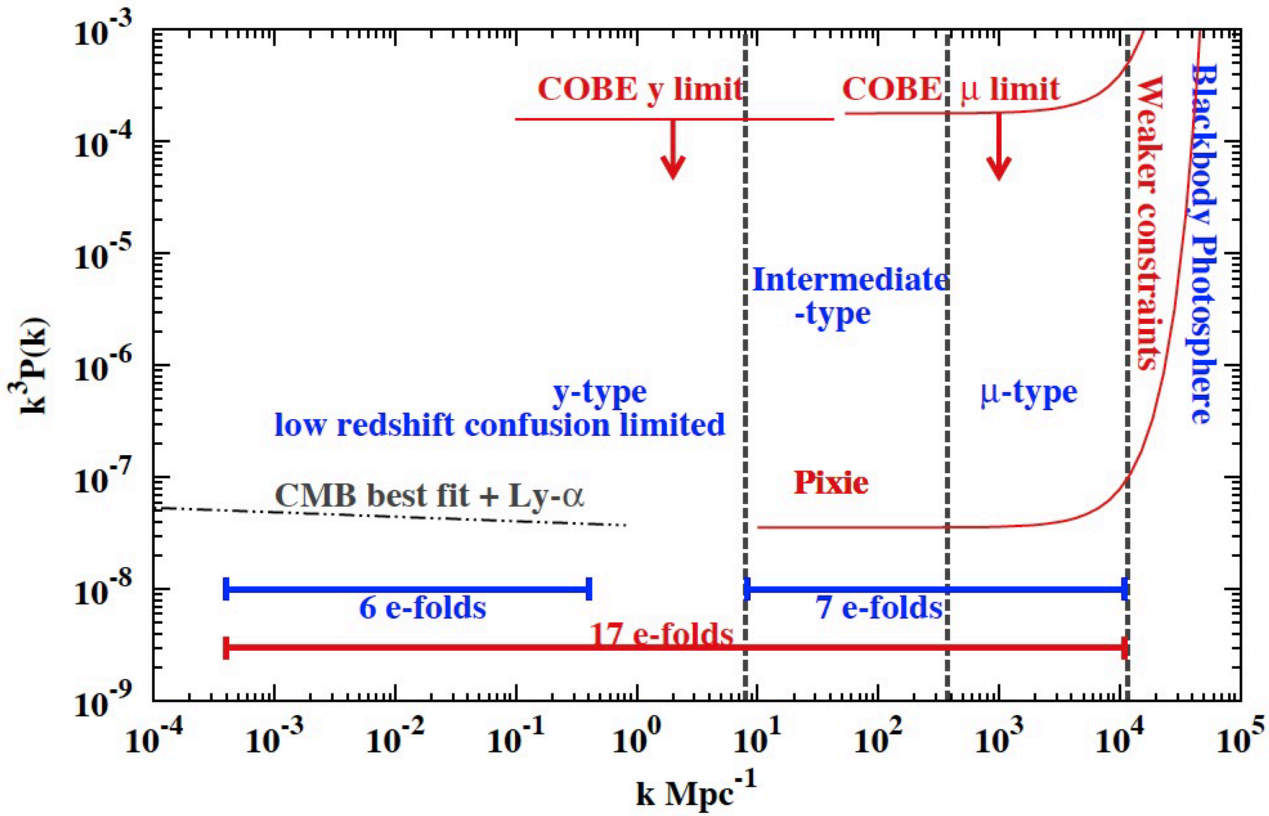
CMB bound by disk-accretion in the latest MD epoch

Poulin, Serpico, Inman, Kohri (2020)



CMB μ- and y- distortion by Large P_ζ

- Large amplitude of fluctuation will be dissipated and produce μ- and y- distortion of CMB after decoupling of double-Compton scatterings



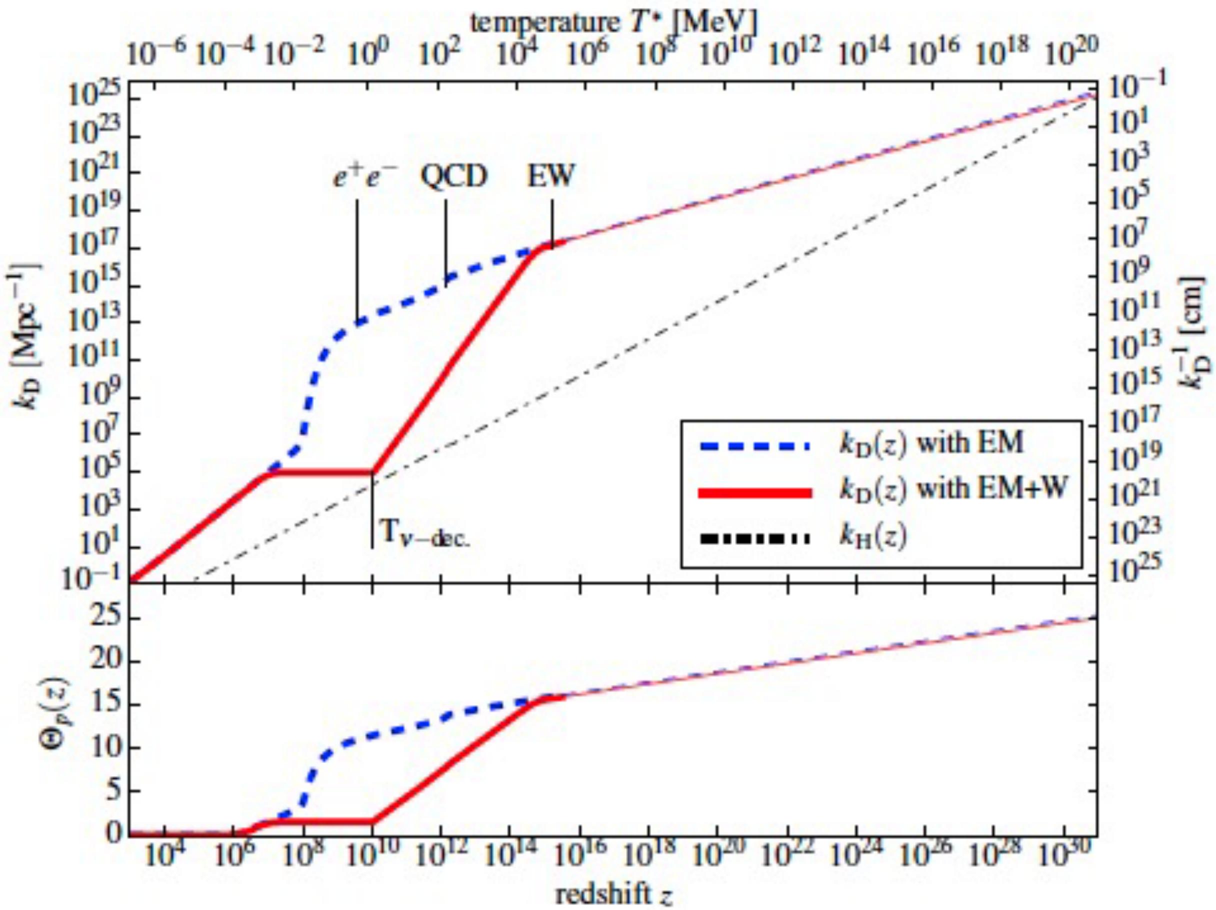
Khatri (2013)

Acoustic reheating

- Nonthermal heating by Silk dumping which can be constrained by BBN and CMB

Jeong,Kamionkowksi, Chluba and Pradler (2014)
Nakama, Suyama, Yokoyama (2014)
Inomata, Tada, Kawasaki (2016)

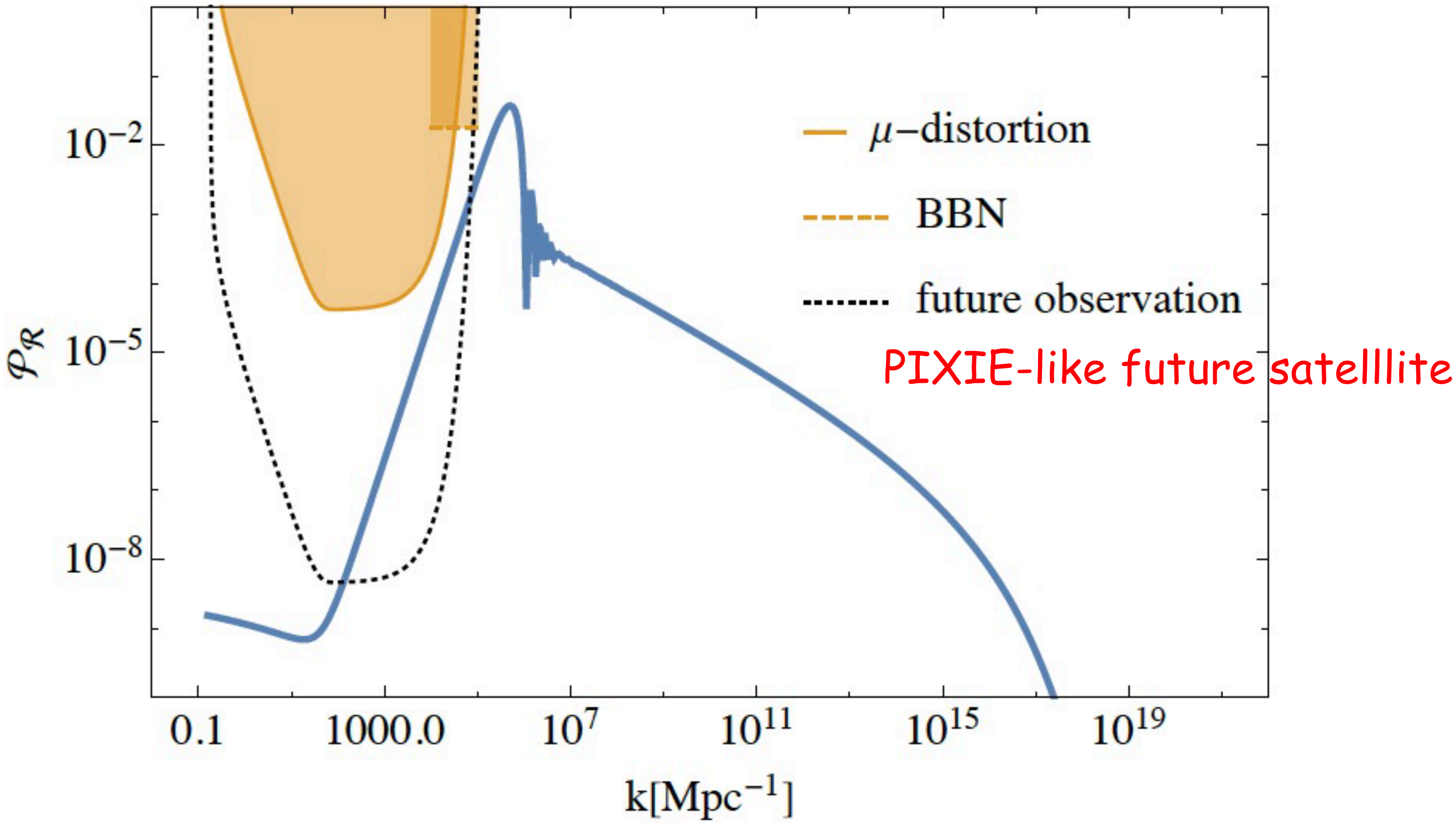
Diffusion scale



μ-distortion and acoustic reheating

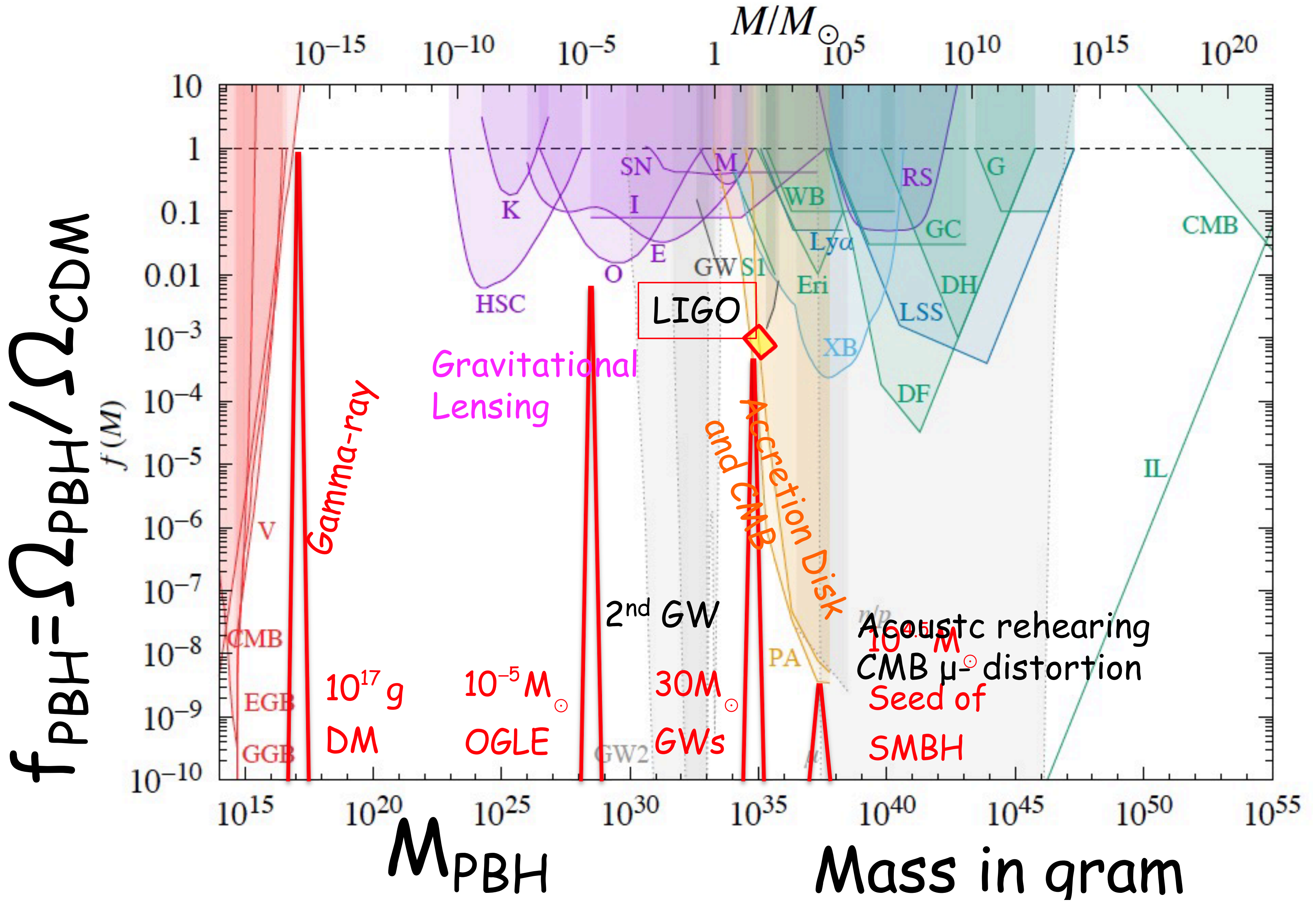
Kohri, Nakama, Suyama (2014)

Inomata, Kawasaki, Mukaida, Tada, Yanagida (2017)



Upper bounds on the fraction to CDM

Carr, Kohri, Sendouda, J.Yokoyama (2009)(2020)



Formations of PBHs in the early Matter Dominated epoch

PBH formation at the (early) matter dominated (MD) Universe

Polnarev and Khlopov (1982)

Harada, Yoo, KK, Nakao, Jhingan (2016)

1. Pressure is negligible, which could induce an immediate collapse and producing more PBHs?

2. Density perturbations can evolve, which produces non-spherical objects and cannot be enclosed by the Horizon. That means less PBHs can be produced?

Matter Domination

- Three radius in Lagrangian coordinate q_i

Zel'dovich Approximation

$$r_1 = (a - \alpha b) q_1$$

$$r_2 = (a - \beta b) q_2$$

$$r_3 = (a - \gamma b) q_3$$

- Eccentricity $$e^2 = 1 - \left(\frac{r_2(t_c)}{r_3(t_c)}\right)^2 = 1 - \left(\frac{\alpha - \beta}{\alpha - \gamma}\right)^2$$
- Hoop with 2nd Elliptic funciton E(x)

$$\mathcal{C} = 16\left(1 - \frac{\gamma}{\alpha}\right) E\left(\sqrt{1 - \left(\frac{\alpha - \beta}{\alpha - \gamma}\right)^2}\right) r_f$$

- Hoop conjecture for PBH production

$$\mathcal{C} \lesssim 2\pi r_g .$$

Abundance of PBHs formed in MD

- Probability distribution by peak statistics (BBKS)

Doroshkevich (1970)

$$
\begin{aligned}
&w(\alpha,\beta,\gamma)d\alpha d\beta d\gamma \\
&= -\frac{27}{8\sqrt{5}\pi\sigma_3^6}\exp\left[-\frac{1}{10\sigma_3^2}(\alpha+\beta+\gamma)^2-\frac{1}{4\sigma_3^2}\{(\alpha-\beta)^2+(\beta-\gamma)^2+(\gamma-\alpha)^2\}\right] \\
&\cdot(\alpha-\beta)(\beta-\gamma)(\gamma-\alpha)d\alpha d\beta d\gamma.
\end{aligned}
$$

$$\sigma_H = \sqrt{5}\sigma_3$$

- Probability

$$\beta_0 = \int_0^\infty d\alpha \int_{-\infty}^{\alpha} d\beta \int_{-\infty}^{\beta} d\gamma\ \theta(1-h(\alpha,\beta,\gamma))w(\alpha,\beta,\gamma)$$

$$h(\alpha,\beta,\gamma) = \frac{2}{\pi}\frac{\alpha-\gamma}{\alpha^2}E\left(\sqrt{1-\left(\frac{\alpha-\beta}{\alpha-\gamma}\right)^2}\right)$$

$$h(\alpha,\beta,\gamma) := \mathcal{C}/(2\pi r_g)$$

Angular momentum produced by perturbations

Harada, Yoo, KK, nad Nakao (2017)

- Angular momentum

1st order effects for nonspherical V

2nd order effects

$$\mathbf{L}_c = \int_{a^3V} \rho \mathbf{r} \times \mathbf{v} d^3\mathbf{r} = \rho_0 a^4 \left(\int_V \mathbf{x} \times \mathbf{u} d^3\mathbf{x} + \int_V \mathbf{x}\delta \times \mathbf{u} d^3\mathbf{x} \right)$$

- Density perturbation δ
- (Peculiar) Velocity perturbation

$$\mathbf{u} := aD\mathbf{x}/Dt$$

$$\mathbf{u}_1 = -\frac{t}{a}\nabla\psi_1$$

- Potential perturbation

$$\psi := \Psi - \Psi_0$$

Effects by finite angular momentum

Harada, Yoo, KK, Nakao (2017)

- Probability distribution

$$a_* := L/(GM^2/c)$$

$$f_{\rm BH(2)}(a_*)da_* \propto \frac{1}{a_*^{5/3}} \exp\left(-\frac{1}{2\sigma_H^{2/3}}\left(\frac{2}{5}\mathcal{I}\right)^{4/3}\frac{1}{a_*^{4/3}}\right) da_*$$

- Probability

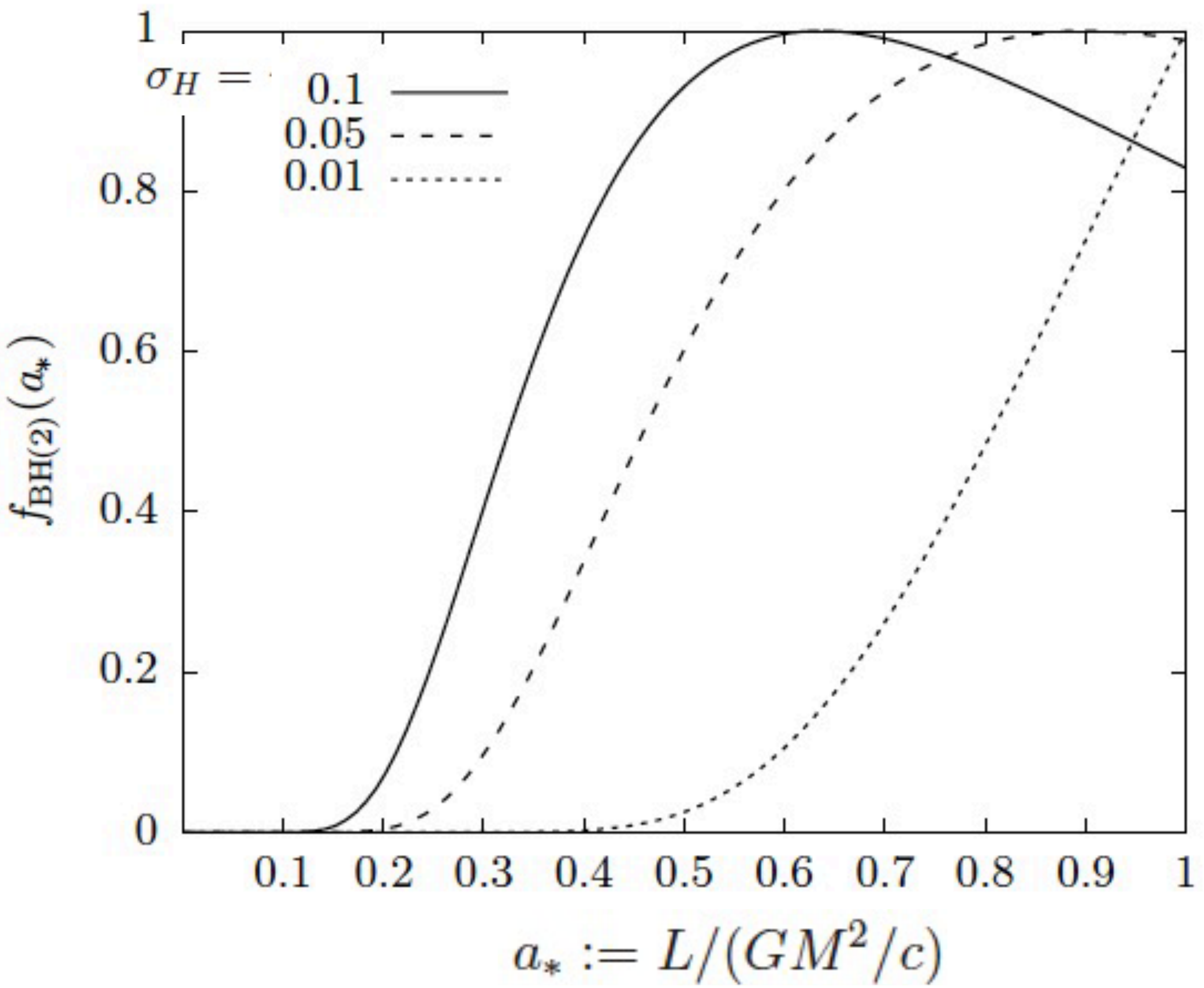
$$\beta_0 \simeq \int_0^\infty d\alpha \int_{-\infty}^{\alpha} d\beta \int_{-\infty}^{\beta} d\gamma \theta[\delta_H(\alpha,\beta,\gamma) - \delta_{\rm th}]\theta[1 - h(\alpha,\beta,\gamma)]w(\alpha,\beta,\gamma)$$

$$\delta_H(\alpha,\beta,\gamma) = \alpha + \beta + \gamma \qquad \delta_{\rm th} := \left(\frac{2}{5}\mathcal{I}\sigma_H\right)^{2/3}$$

Spin distribution

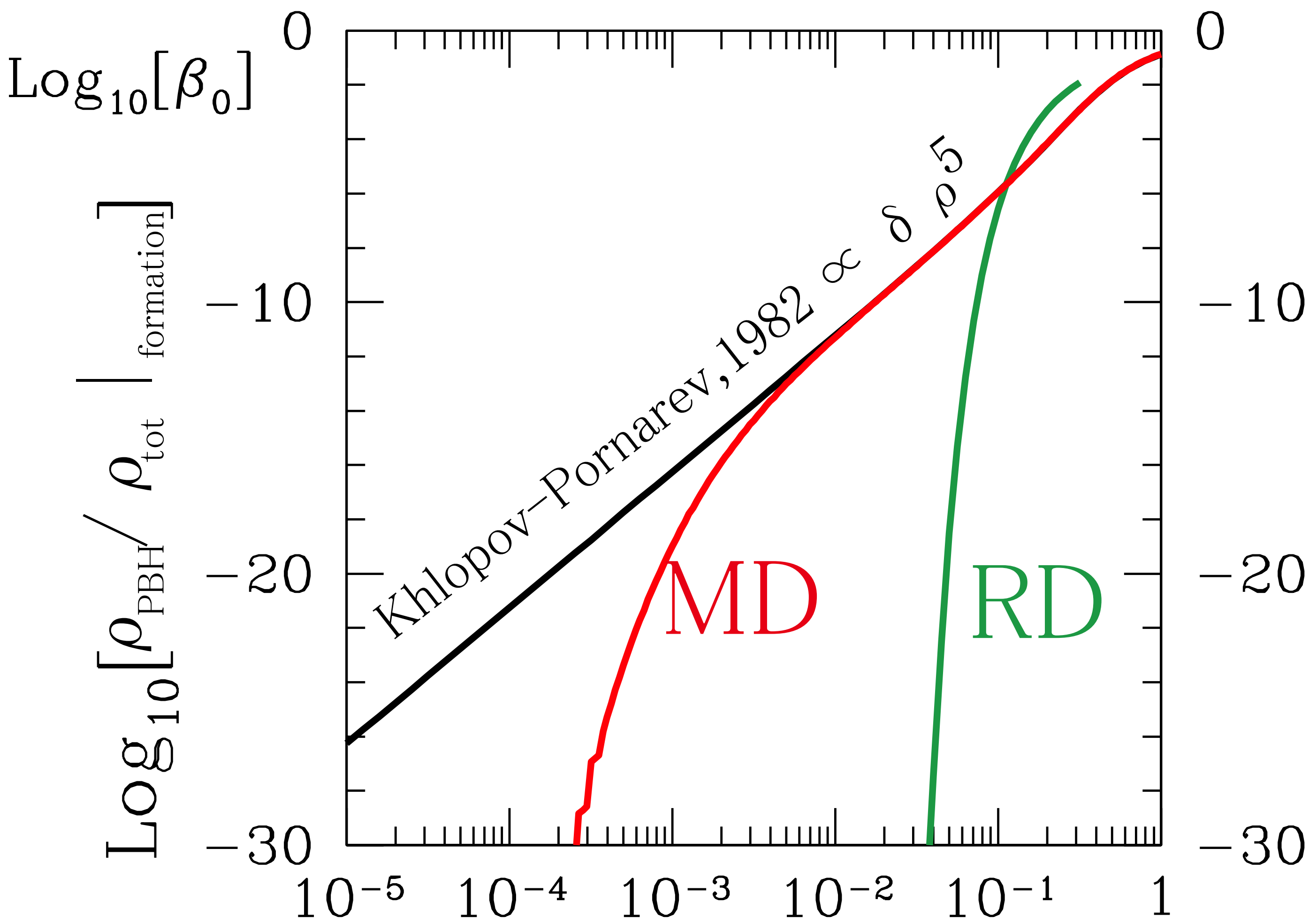
More highly-spinning halos cannot collapse into PBHs, which means that the PBHs produced tend to have high spins in MD

Harada, Yoo, KK, Nakao (2017)



Beta in matter-domination

Harada, Yoo, KK, Nakao (2017)



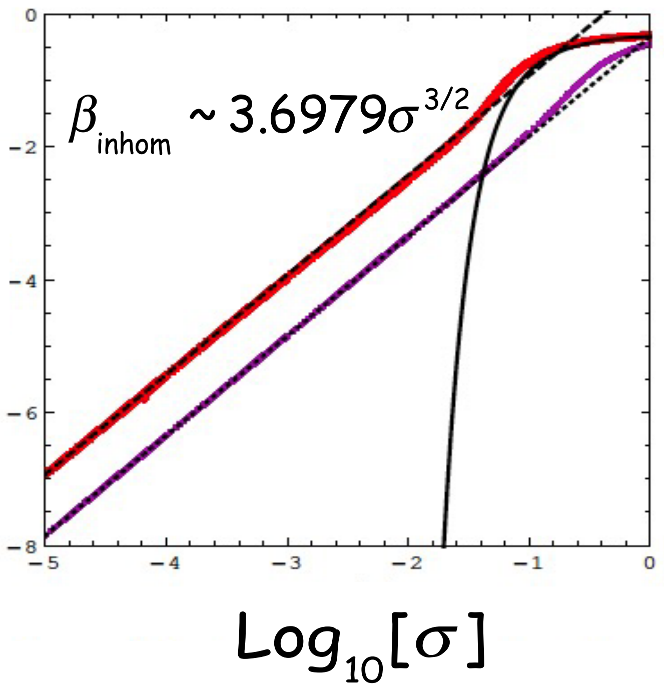
$\sigma_H = \sqrt{5}\sigma_3$ = $\delta\rho/\rho$

Effects of Inhomogeneity on PBH formations in Matter Domination

T.Kokubu, K.Kyutoku, K.Kohri, T.Harada, arXiv:1810.03490

Singularity should be enclosed by (apparent) horizon

$$\beta \equiv \frac{\rho_{PBH}}{\rho_{tot}}$$

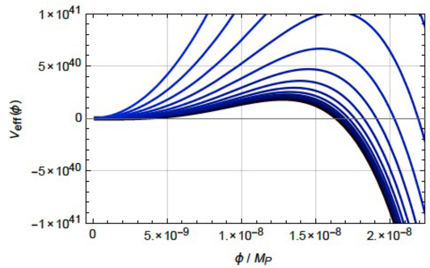


$$\beta_{aniso} \simeq 0.05556\sigma^5$$

$$\sigma \sim \overline{\delta\rho/\rho}$$

$$\beta_{inhom+aniso} \simeq \beta_{inhom} \times \beta_{aniso} = 0.2055\sigma^{13/2}$$

Higgs stabilization due to evaporating PBHs?



Kohri and Matsui (2017)

- Potential with finite-temperature corrections

$$V_{\rm eff}(\phi) \simeq \frac{1}{2}\left(\lambda_{\rm eff}T_{\rm H}^2 + \kappa^2 T_{\rm H}^2\right)\phi^2 + \frac{\lambda_{\rm eff}}{4}\phi^4$$

$$\phi_{\rm max}^2/T_{\rm H}^2 \approx \mathcal{O}(10)$$

- Probability to get over the potential

$$P(\phi > \phi_{\rm max}) \simeq \frac{\sqrt{2\langle\delta\phi^2\rangle_{\rm ren}}}{\pi\phi_{\rm max}} \exp\left(-\frac{\phi_{\rm max}^2}{2\langle\delta\phi^2\rangle_{\rm ren}}\right)$$

$$\langle\delta\phi^2\rangle_{\rm ren}/T_{\rm H}^2 \simeq \mathcal{O}(0.1)$$

- This gives,

$$\phi_{max}^2 / \langle\delta\phi^2\rangle_{rem} \sim 10^2$$

$$\mathcal{N}_{\rm PBH} \cdot P(\phi > \phi_{\rm max}) \lesssim 1$$

or

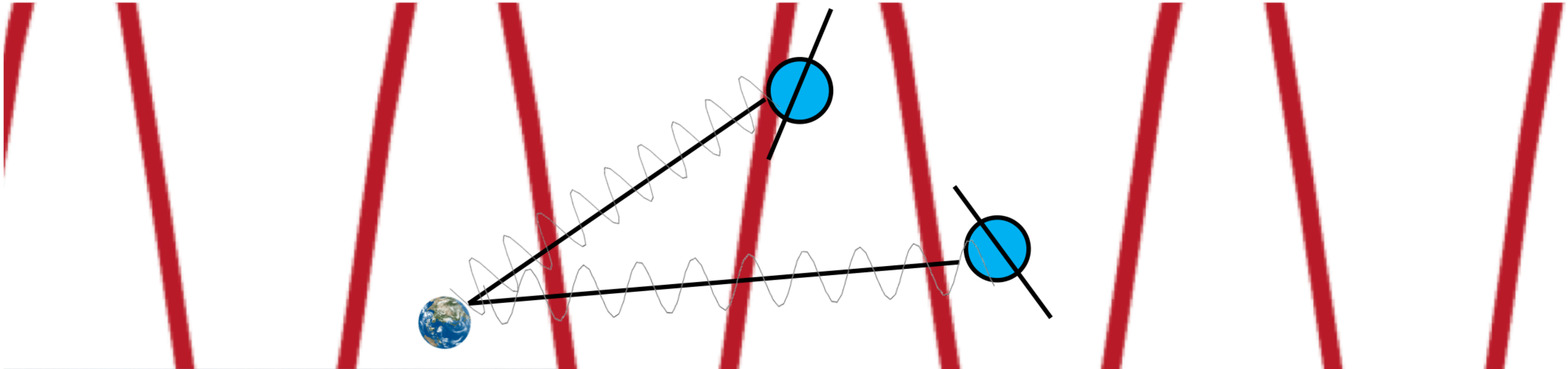
$$\beta \lesssim \mathcal{O}\left(10^{-21}\right)\left(\frac{m_{\rm PBH}}{10^9{\rm g}}\right)^{3/2}$$

Zaven Arzoumanian, et al, The NANOGrav Collaboration, arXiv:2009.04496

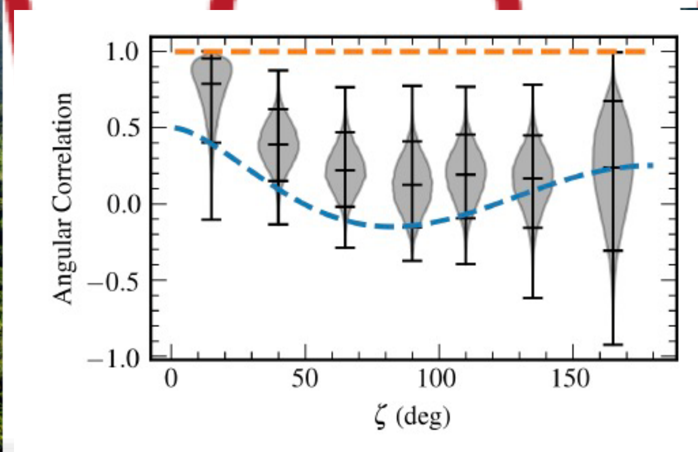
NANOGrav 12.5 yr

(North American Nanohertz Observatory for Gravitational Waves)

found stochastic GWs through pulsar timing ?



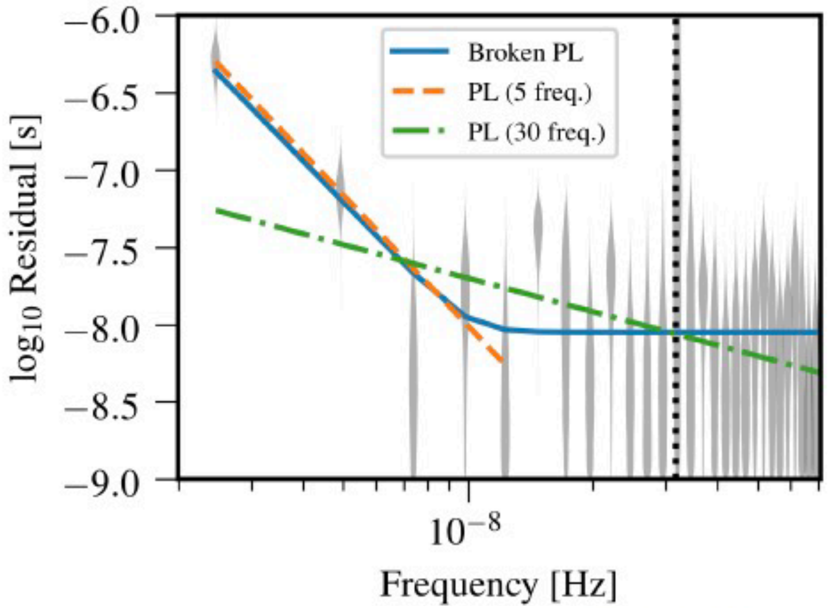
The 305-meter dish of the William E. Gordon Telescope, The Arecibo Obs.

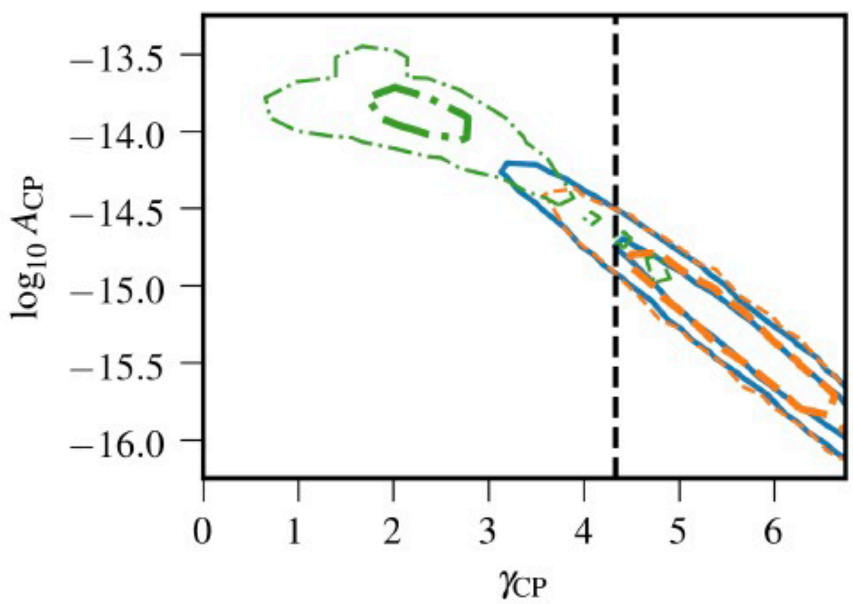


The 100-meter Green Bank Telescope

The NANOGrav 12.5-year Pulsar-timing Data for An Isotropic Stochastic Gravitational-Wave Background

Zaven Arzoumanian, et al, The NANOGrav Collaboration, arXiv:2009.04496





$$h_c(f) = A_{\rm GWB}\left(\frac{f}{f_{\rm yr}}\right)^{\alpha}$$

$$\Omega(f) = \frac{2\pi}{3H_0^2} f^2 h_c(f)^2 = \Omega_{yr}\left(\frac{f}{f_{\rm yr}}\right)^{\beta}$$

$$\gamma = 3 - 2\alpha = 5 - \beta$$

$$\beta = 5 - \gamma$$

Models to fit NANOGrav 12.5 yr

1. Astrophysics

- Binary SMBHs

2. Early Universe

- 2ndary GWs from large ζ at small scales
- Cosmic string produced by GUT phase transition
- 1^{st} order phase transition of unknown scalar
- …

Secondary GWs from large curvature perturbation ζ at small scales

K. Kohri and T. Terada, arXiv:arXiv:2009.11853

Secondary gravitational wave induced from large curvature perturbation (P_ζ >> r) at small scales

K. N. Ananda, C. Clarkson, and D. Wands, 2006
D.Baumann, P.J.Steinhardt, K.Takahashi and K.Ichiki,2007
R.Saito and J.Yokoyama, 2008
KK and T.Terada, 2018
R.-G. Cai, S. Pi, and M. Sasaki, 2019

- Power spectrum of the tensor mode

$$\langle h^r_{\boldsymbol{k}}(\eta) h^s_{\boldsymbol{k}'}(\eta)\rangle = \frac{2\pi^2}{k^3}\mathcal{P}_h(k,\eta)\delta(\boldsymbol{k}+\boldsymbol{k}')\delta^{rs}, \qquad h_{ij}(\boldsymbol{x},\eta) = \int \frac{\mathrm{d}^3k}{(2\pi)^{3/2}} e^{i\boldsymbol{k}\cdot\boldsymbol{x}} \left[h^+_{\boldsymbol{k}}(\eta) \mathrm{e}^+_{ij}(\boldsymbol{k}) + h^\times_{\boldsymbol{k}}(\eta)\mathrm{e}^\times_{ij}(\boldsymbol{k})\right]$$

- Omega parameter well inside the horizon

$$\Omega_{\rm GW}(k,\eta) = \frac{1}{3}\left(\frac{k}{\mathcal{H}}\right)^2 \mathcal{P}_h(k,\eta).$$

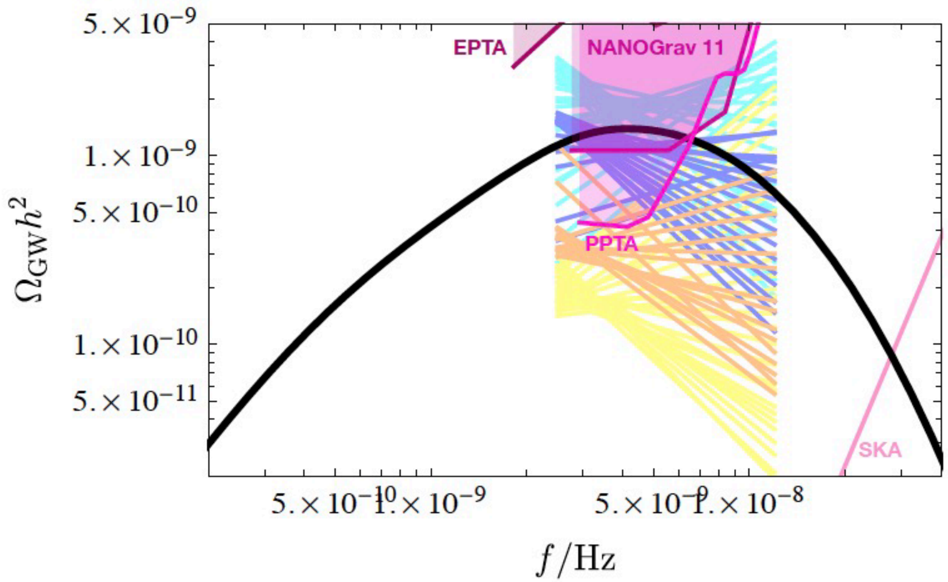
- Substituting the solution into this

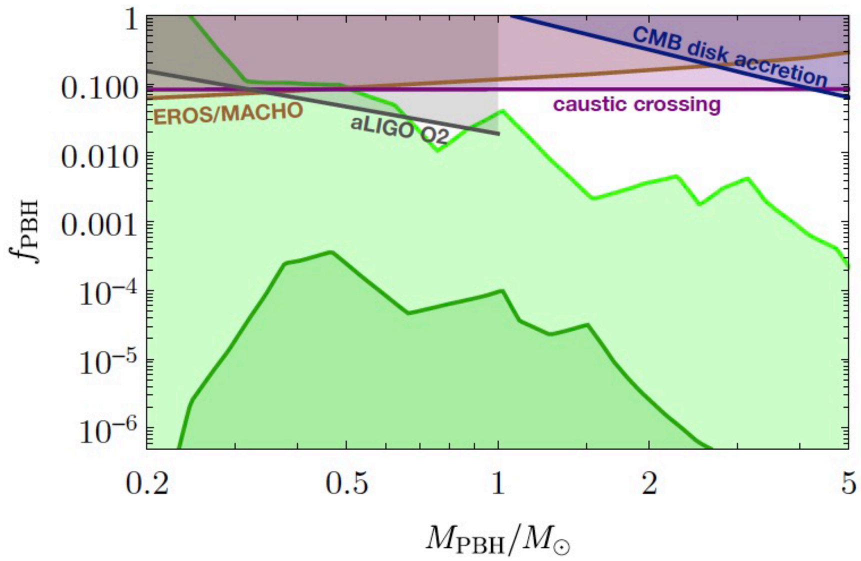
$$\Omega_{\rm GW,c}(f) = \frac{1}{12}\left(\frac{f}{2\pi a H}\right)^2 \int_0^\infty \mathrm{d}t \int_{-1}^1 \mathrm{d}s \left[\frac{t(t+2)(s^2-1)}{(t+s+1)(t-s+1)}\right]^2 \times \overline{I^2(t,s,k\eta_c)}\,\mathcal{P}_\zeta\left(\frac{(t+s+1)f}{4\pi}\right)\mathcal{P}_\zeta\left(\frac{(t-s+1)f}{4\pi}\right)$$

Large P_ζ at $k \sim 10^7 \mathrm{Mpc}^{-1}$ produces both GWs at nHz and O(1) $M_\odot$ PBHs

R.Saito and J.Yokoyama, Phys. Rev. Lett. 102 (2009) 161101
K. Kohri and T. Terada, arXiv:arXiv:2009.11853

$$M_{\mathrm{PBH}} \sim O(1) M_\odot \left(\frac{k}{10^7 \mathrm{Mpc}^{-1}} \right)^{-2} \sim O(1) M_\odot \left(\frac{5 \times 10^{-9} \mathrm{Hz}}{f} \right)^{2}$$



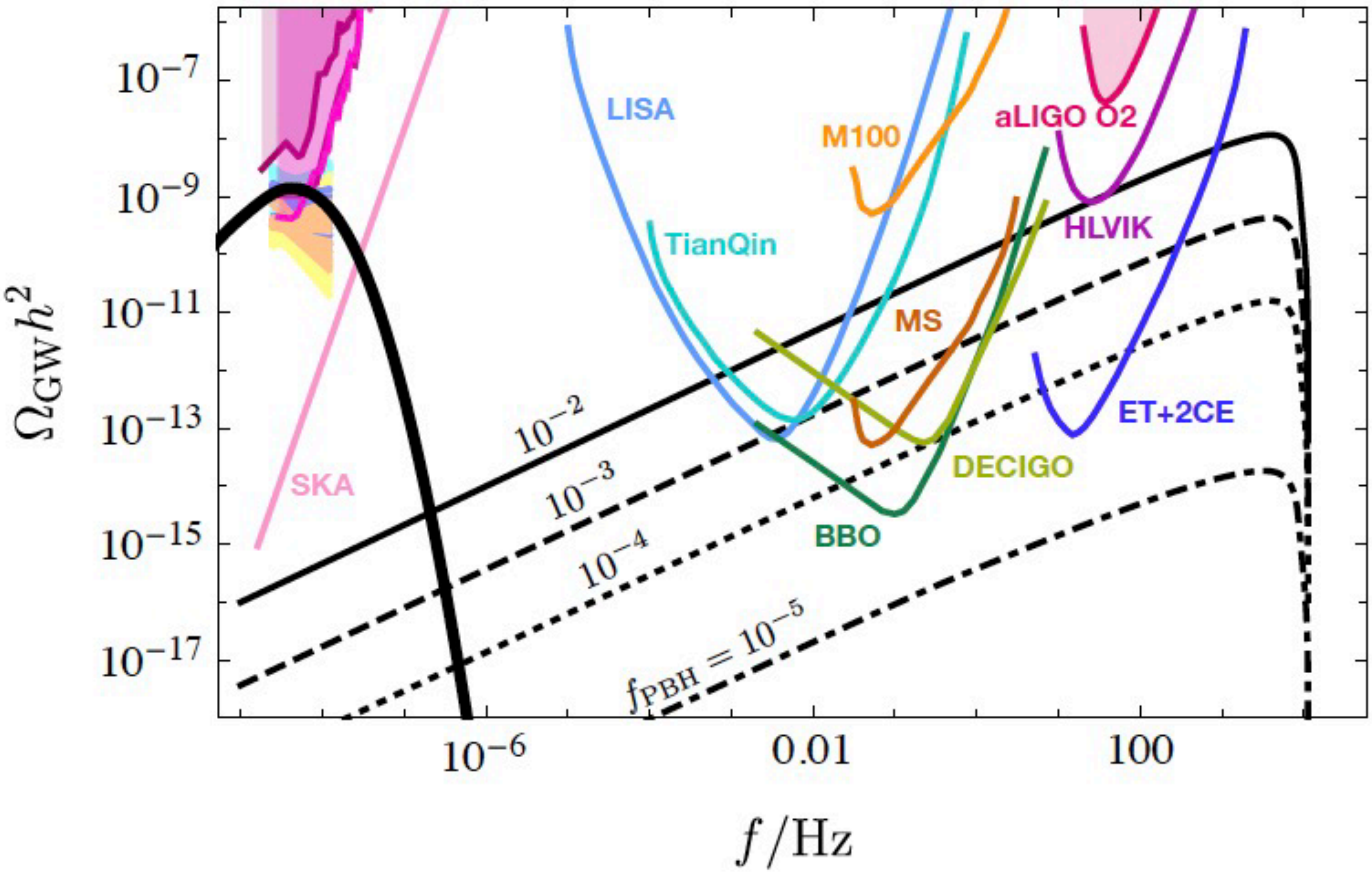


GWs at nHz

PBHs of O(1) $M_\odot$

NANOGrav12.5yr and solar mass PBHs

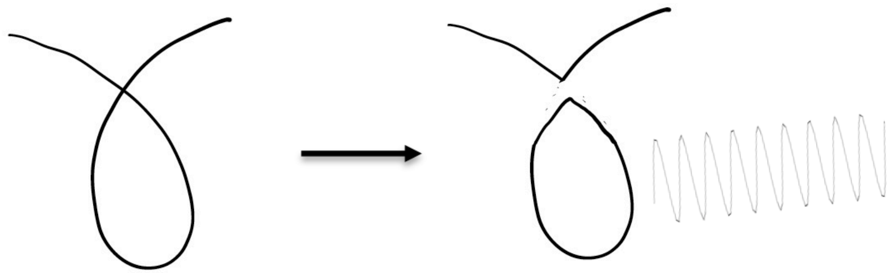
K. Kohri and T. Terada, arXiv:arXiv:2009.11853



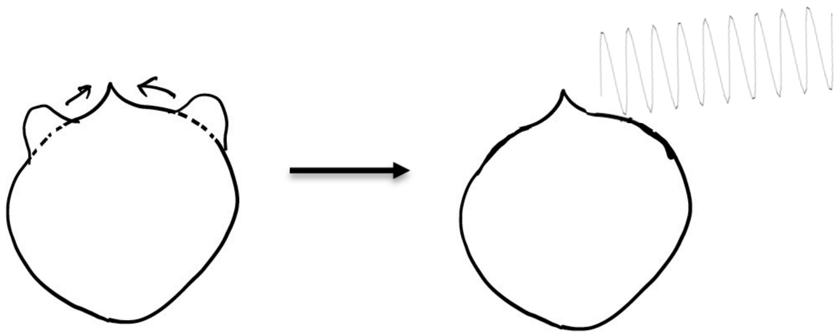
GW emitted from Cosmic string which was produced after GUT phase transition

Jeff A. Dror, Takashi Hiramatsu, Kazunori Kohri, Hitoshi Murayama, Graham White,
arXiv:1908.03227 [hep-ph]

kink



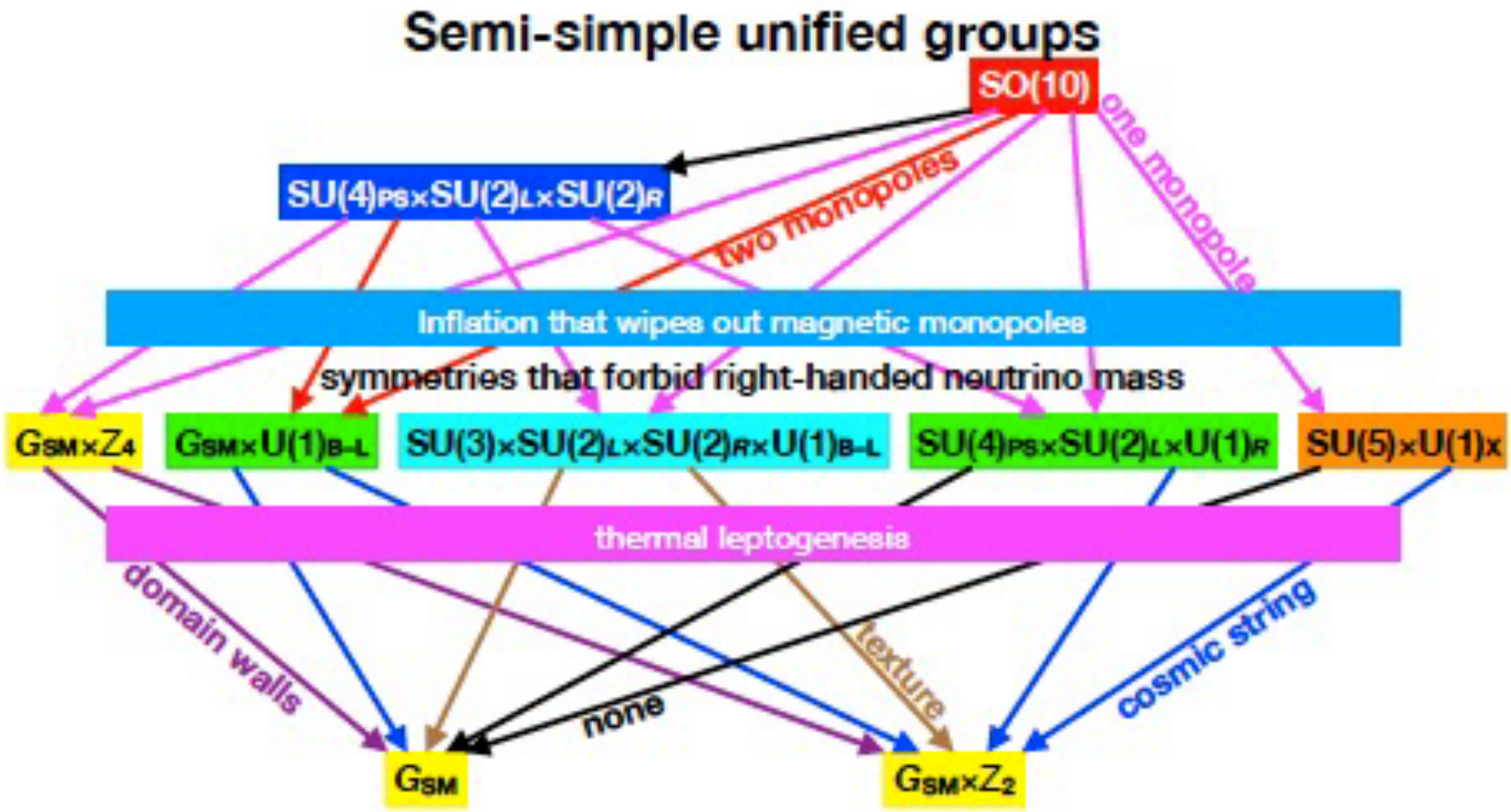
cusp



Seesaw and Leptogenesis searched by future GW

Jeff A. Dror, Takashi Hiramatsu, Kazunori Kohri, Hitoshi Murayama, Graham White,

arXiv:1908.03227 [hep-ph]



Seesaw and Leptogenesis searched by future GW

Jeff A. Dror, Takashi Hiramatsu, Kazunori Kohri, Hitoshi Murayama, Graham White,
arXiv:1908.03227 [hep-ph]

	$H = G_{\rm SM}$		$H = G_{\rm SM} \times \mathbb{Z}_2$	
G	**defects**	**Higgs**	**defects**	**Higgs**
$G_{\rm disc}$	domain wall*	$B - L = 1$	domain wall*	$B - L = 2$
G_{B-L}	abelian string*	$B - L = 1$	$\mathbb{Z}_2$ string†	$B - L = 2$
G_{LR}	texture*	$(\mathbf{1}, \mathbf{1}, \mathbf{2}, \frac{1}{2})$	$\mathbb{Z}_2$ string	$(\mathbf{1}, \mathbf{1}, \mathbf{3}, 1)$
G_{421}	none	$(\mathbf{4}, \mathbf{1}, 1)$	$\mathbb{Z}_2$ string	$(\mathbf{15}, \mathbf{1}, 2)$
$G_{\rm flip}$	none	$(\mathbf{10}, 1)$	$\mathbb{Z}_2$ string	$(\mathbf{50}, 2)$

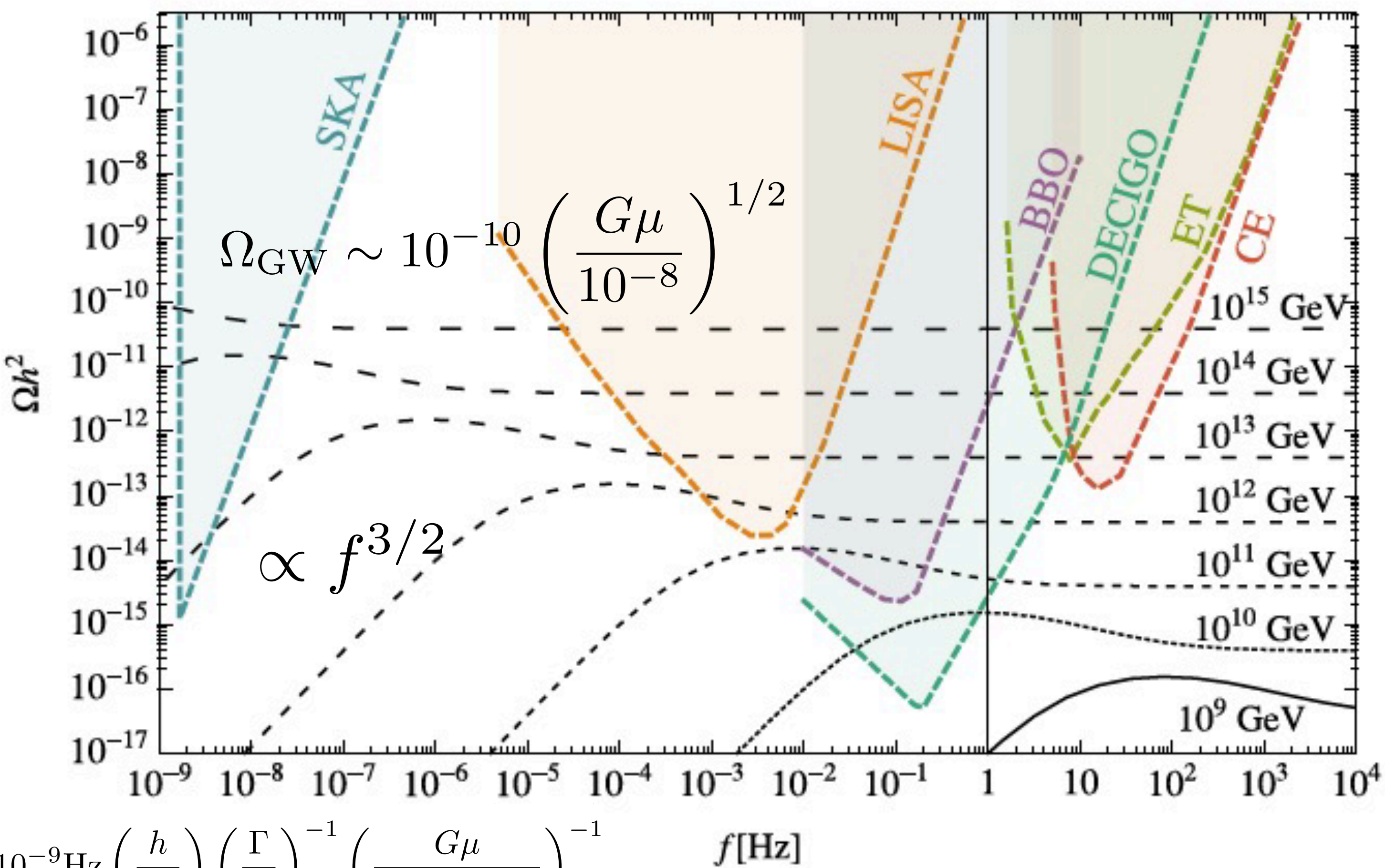
$$
\begin{aligned}
G_{\rm disc} &= G_{\rm SM} \times \mathbb{Z}_N\,, \\
G_{B-L} &= G_{\rm SM} \times U(1)_{B-L}\,, \\
G_{LR} &= SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L} \\
G_{421} &= SU(4)_{\rm PS} \times SU(2)_L \times U(1)_Y\,, \\
G_{\rm flip} &= SU(5) \times U(1)\,.
\end{aligned}
$$

Monopole production rate is small

$$\frac{\Gamma}{L} = \frac{\mu}{2\pi}\frac{g}{4\pi}e^{-\pi m^2/\mu}$$

GW emitted from Cosmic string which was produced after GUT phase transition

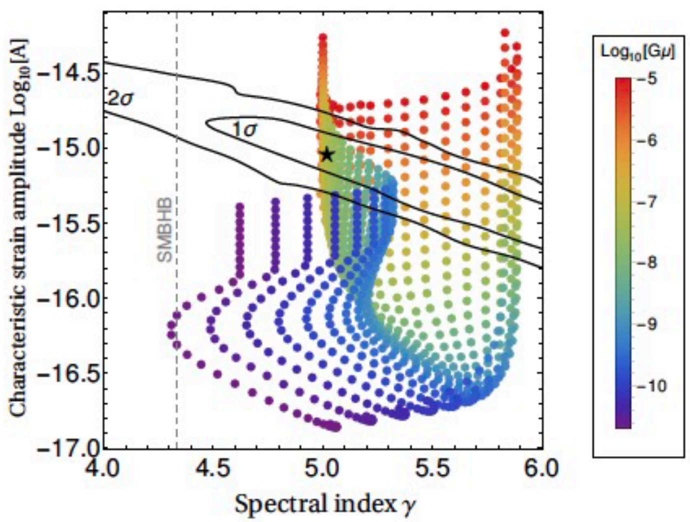
Jeff A. Dror, Takashi Hiramatsu, Kazunori Kohri, Hitoshi Murayama, Graham White,
arXiv:1908.03227 [hep-ph]

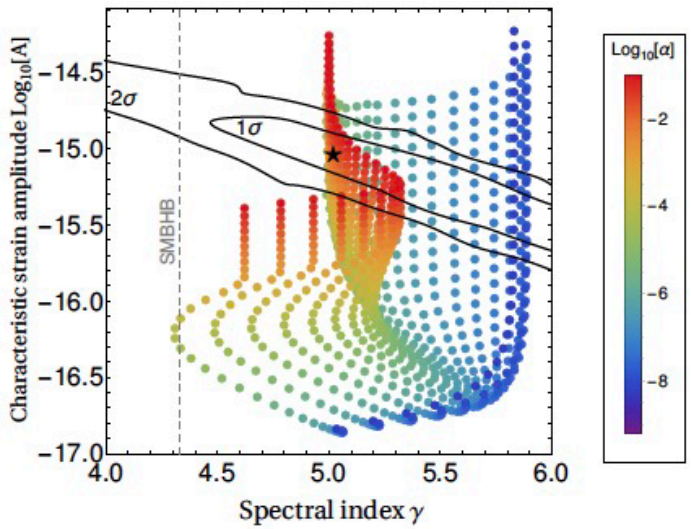


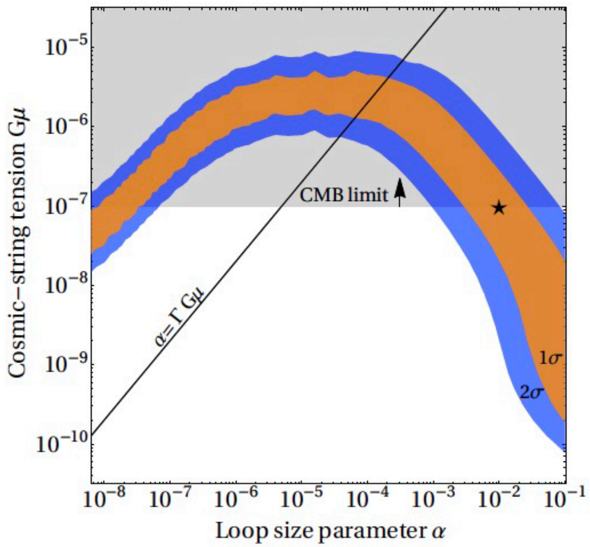
$$f_b \sim 0.7 \times 10^{-9}{\rm Hz} \left(\frac{h}{0.7}\right) \left(\frac{\Gamma}{50}\right)^{-1} \left(\frac{G\mu}{0.7 \times 10^{-10}}\right)^{-1}$$

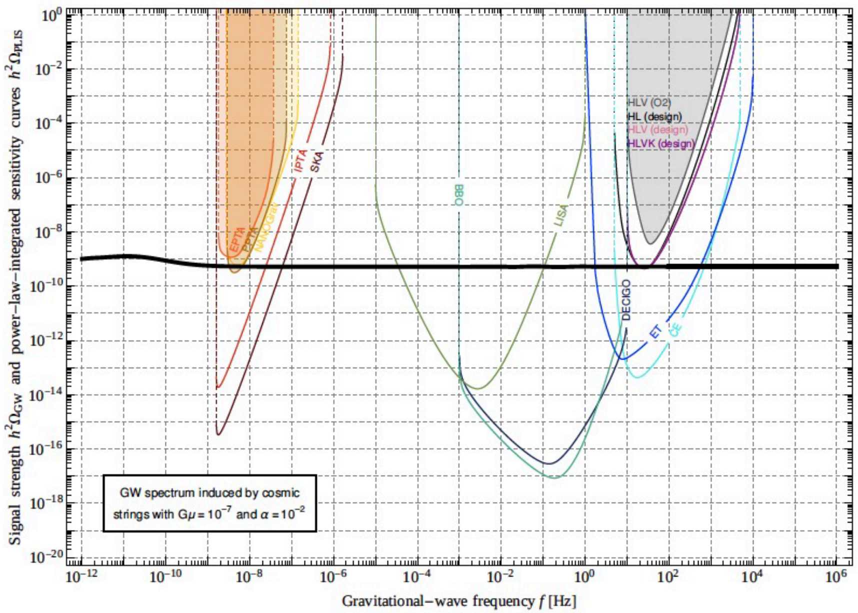
NanoGRAV found GWs from cosmic string

Simone Blasi, Vedran Brdar, Kai Schmitz, arXiv:2009.06607 [astro-ph.CO]









Summary

- Binary PBHs are good candidates for LIGO/Virgo events
- PBHs can be also produced both in the early radiation and matter dominated Universe
- We can probe high-energy physics, the early Universe, and gravity with PBHs
- The NANOGrav 12.5yr data can be fitted by secondary GWs induced by large curvature perturbation, which could have produced PBHs with O(1) $M_\odot$ simultaneously
- We will be able to distinguish a model of PBH formations from others by future observations such as LIGO/Virgo/KAGRA or DECIGO/BBO and so on.