

# Inflation and Beyond

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KIAS-YITP joint workshop  
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# Introduction

# Inflation: the origin of Big Bang

Brout, Englert & Gunzig '77, Starobinsky '79, Guth '81, Sato '81, Linde '82,...

- Inflation is a **quasi-exponential expansion** of the Universe at its very early stage; perhaps at  $t \sim 10^{-36}$  sec.
- It was meant to solve **the initial condition (singularity, horizon & flatness, etc.) problems** in Big-Bang Cosmology:
  - if any of them can be said to be solved depends on precise definitions of the problems.
- **Quantum vacuum fluctuations** during inflation turn out to play the most important role. They give the initial condition for **all the structures in the Universe**.
- **Cosmic gravitational wave background** is also generated.

In summary, the picture that emerges is in complete accord with the kinematic generalities of causal cosmology presented in Section 2. For  $y < y_0$ , one has  $p < 0$  ( $p \simeq -\sigma$ ). For  $y > y_0$ ,  $p$  becomes positive and  $\lambda$  undergoes an inflection. The situation is summarized in Figs. 1 and 2.

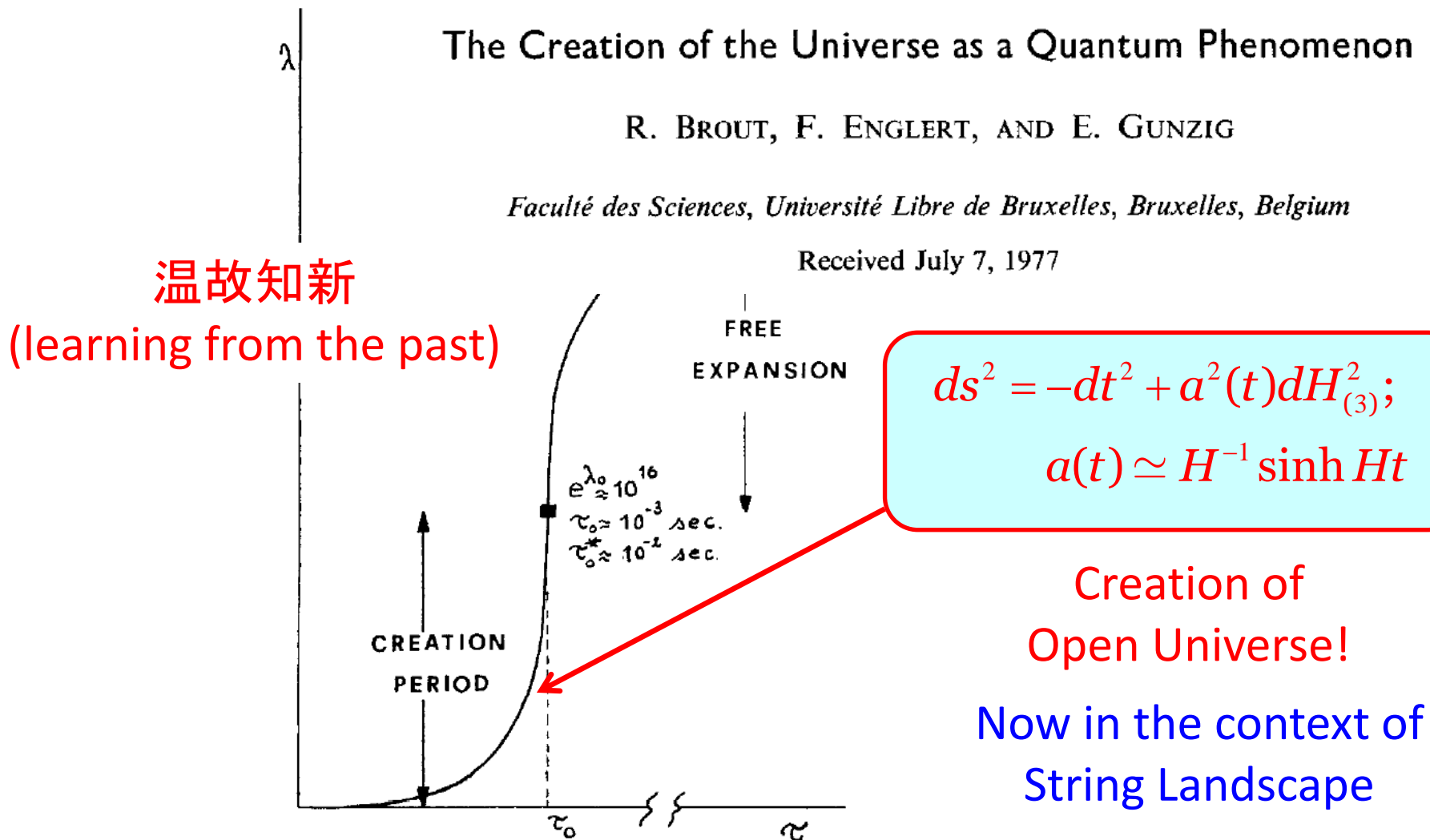
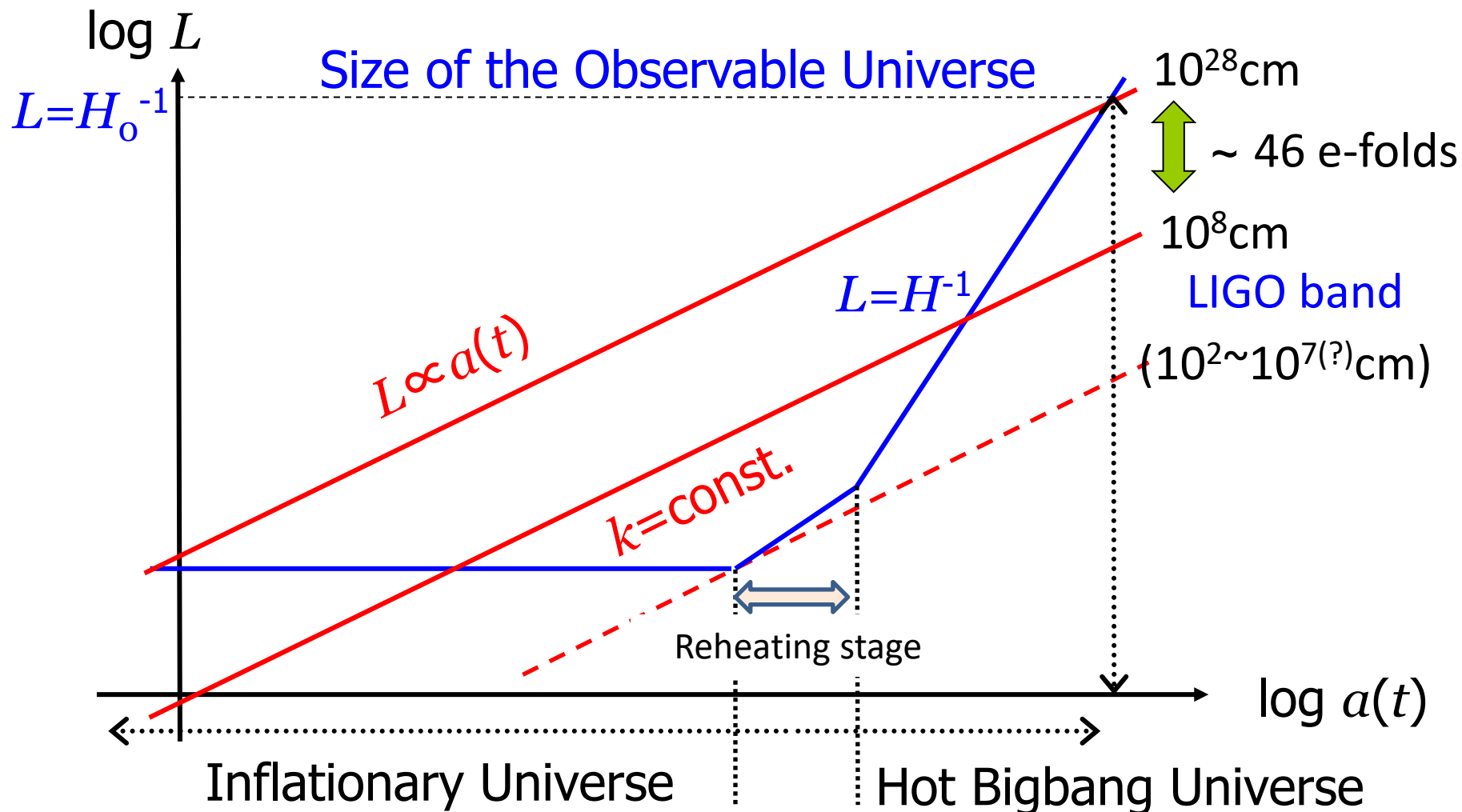


FIG. 1.  $\lambda$  as a function of kinematical time  $\tau$  for  $\delta = 0$ . Time scales are calculated for  $m = 1$  GeV.

# length scales of the inflationary universe

↔ targets for multi-frequency GW astronomy



# Dynamics

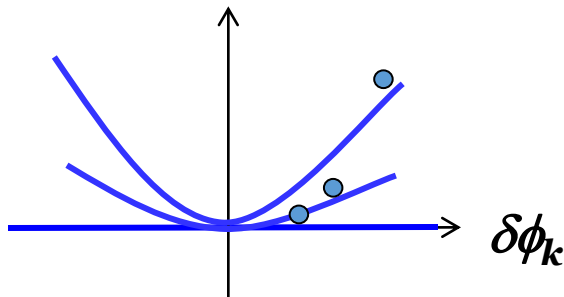
# Seed of cosmological perturbations

Mukhanov '81, ....

Zero-point (vacuum) fluctuations of  $\phi$ : 
$$\delta\phi = \sum_k \delta\phi_k(t) e^{ik \cdot x}$$

$$\delta\ddot{\phi}_k + 3H\delta\dot{\phi}_k + \omega^2(t)\delta\phi_k = 0; \quad \omega^2(t) = \frac{k^2}{a^2(t)}$$

harmonic oscillator with friction term and time-dependent  $\omega$



$$\delta\phi_k \rightarrow \text{const.}$$

... frozen when  $\omega < H$   
(on superhorizon scales)

tensor (gravitational wave) modes also satisfy the same eq.

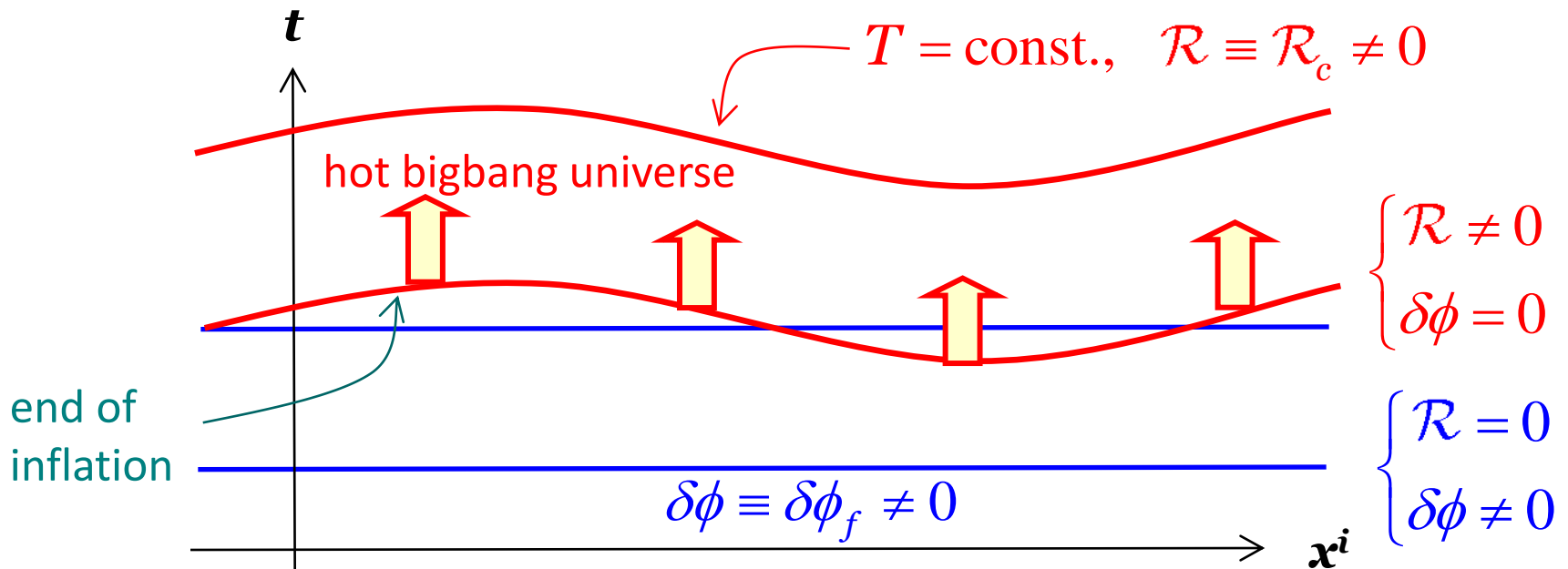
Starobinsky '79

# Generation of Curvature Perturbation

curvature (potential) perturbation  $\mathcal{R}$ : 
$$\delta R^{(3)} = -\frac{4}{a^2} \nabla^2 \mathcal{R}$$

comoving curvature perturbation  $\mathcal{R}_c \sim$  - Newton potential

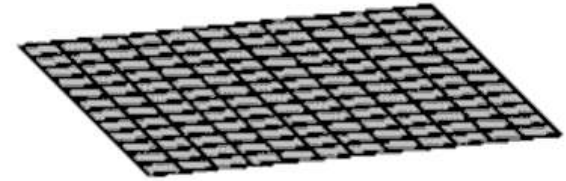
- $\delta\phi$  is frozen on “flat” ( $\mathcal{R}=0$ ) 3-surface ( $t=\text{const.}$  hypersurface) 
$$\mathcal{R}_c = -\frac{H}{\dot{\phi}} \delta\phi_f$$
- Inflation ends/damped osc starts “comoving” ( $\phi=\text{const.}$ ) on 3-surface.





# Generic predictions of inflation

- Spatially **flat** universe
- Almost scale invariant, adiabatic, Gaussian primordial **scalar (curvature)** perturbations
- Almost scale invariant, Gaussian primordial **tensor (gravitational wave)** perturbations



Generates CMB anisotropy  
Origin of galaxies, stars, ...

# Quantitative Predictions

- Amplitude of curvature perturbation:

$$\mathcal{R}_c = \left. \frac{H^2}{2\pi\dot{\phi}} \right|_{k/a=H} \quad \text{Mukhanov (1985), MS (1986)}$$

- Power spectrum index:

$$M_{pl} \equiv \frac{1}{\sqrt{8\pi G}} \sim 2.4 \times 10^{18} \text{ GeV: Planck mass}$$

$$\frac{4\pi k^3}{(2\pi)^3} P_S(k) = \left[ \left. \frac{H^2}{2\pi\dot{\phi}} \right]_{k/a=H}^2 = Ak^{n_s-1} ; \quad n_s - 1 = M_P^2 \left( 2 \frac{V''}{V} - 3 \frac{V'^2}{V^2} \right)$$

Stewart-Lyth (1993)

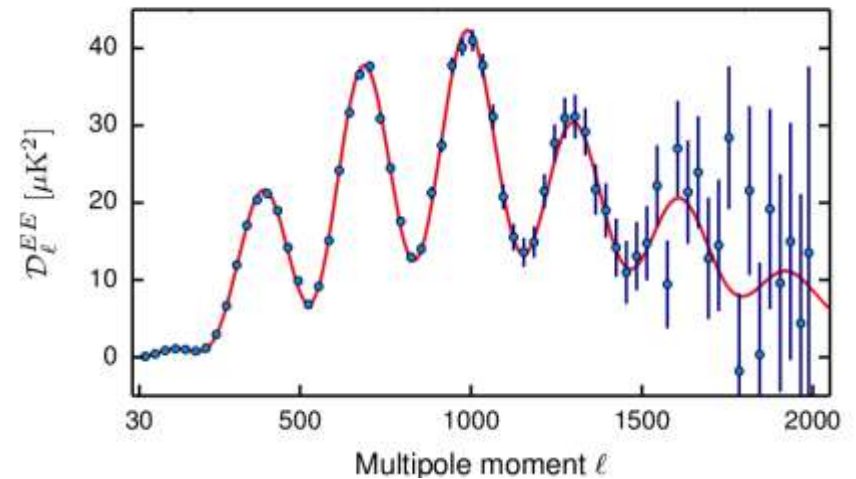
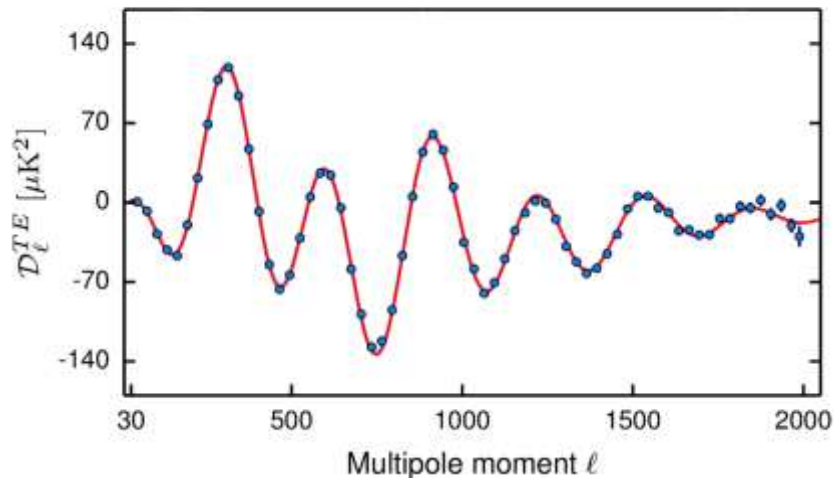
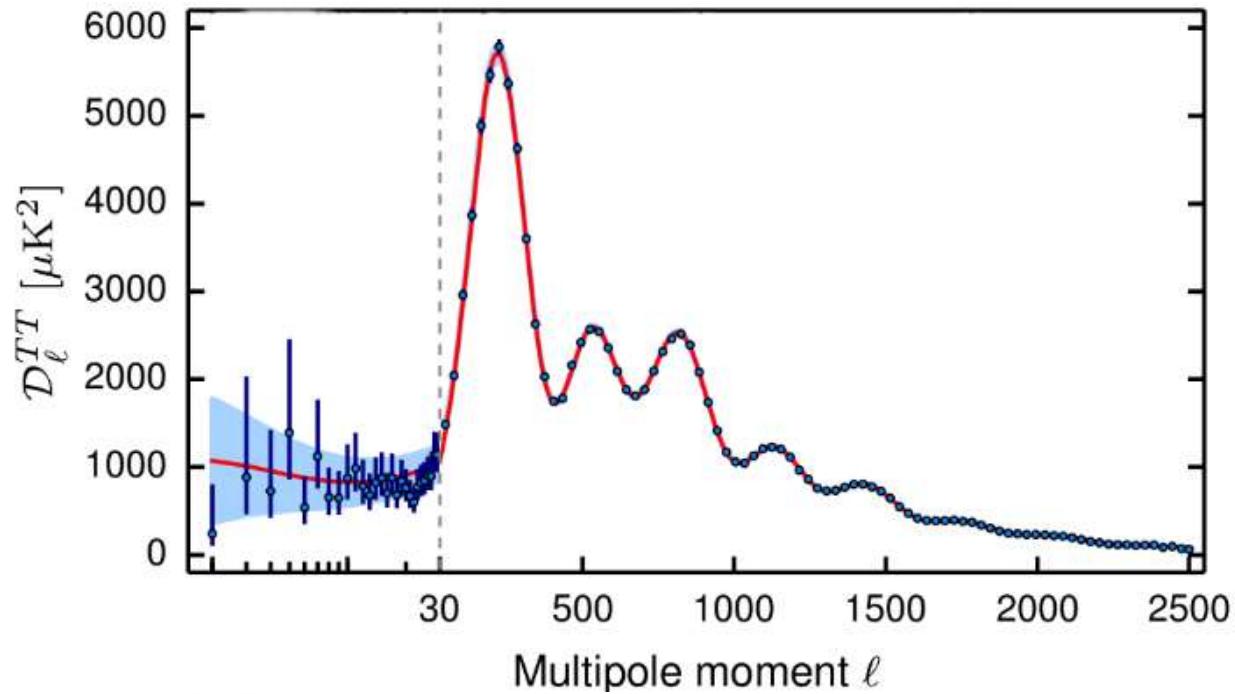
- Tensor (gravitational wave) spectrum:

$$\frac{4\pi k^3}{(2\pi)^3} P_T(k) = Ak^{n_T} ; \quad n_T = -\frac{1}{8} \frac{P_S(k)}{P_T(k)} \equiv -\frac{r}{8} \quad \text{Liddle-Lyth (1992)}$$

“consistency relation”

**Observational results**

# Planck TT, TE & EE spectrum



- Amplitude of curvature perturbation:

$$\mathcal{R}_c = \frac{H^2}{2\pi\dot{\phi}} \Big|_{k/a=H} \quad \text{Mukhanov (1985), MS (1986)}$$

$$\mathcal{R}_{c,\text{obs}} \sim 10^{-5} \Rightarrow V^{1/4}(\phi) \lesssim 10^{16} \text{ GeV?}$$

- Power spectrum index:

$$M_P \equiv \frac{1}{\sqrt{8\pi G}} \sim 2.4 \times 10^{18} \text{ GeV: Planck mass}$$

$$\frac{4\pi k^3}{(2\pi)^3} P_S(k) = \left[ \frac{H^2}{2\pi\dot{\phi}} \right]_{k/a=H}^2 = A k^{n_s-1} ; \quad n_s - 1 = M_P^2 \left( 2 \frac{V''}{V} - 3 \frac{V'^2}{V^2} \right)$$

Stewart-Lyth (1993)

$$n_{S,\text{Planck}} - 1 = -0.0355 \pm 0.0049 \Leftrightarrow n_s - 1 \sim -0.04 \text{ for a typical model}$$

Mukhanov & Chibisov (1981)

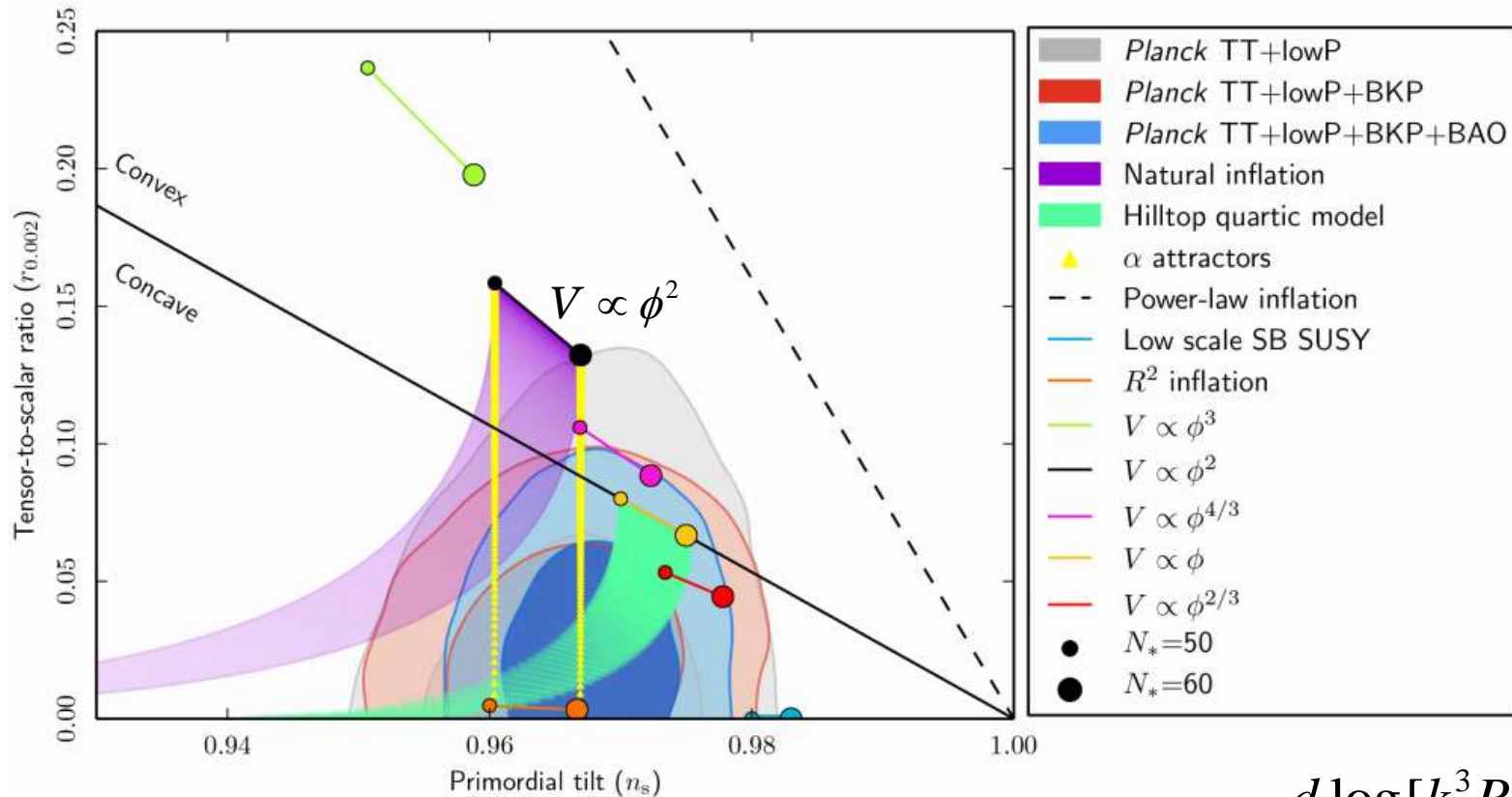
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to be observed ...

# Planck constraints on inflation

Planck 2015 XX



- scalar spectral index:  $n_s \sim 0.96$
- tensor-to-scalar ratio:  $r < 0.1$
- simplest  $V \propto \phi^2$  model is almost excluded

$$n_s - 1 \equiv \frac{d \log[k^3 P_S(k)]}{d \log k}$$

$$r \equiv \frac{P_T(k)}{P_S(k)}$$

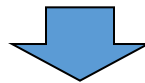
# Implications

Inflation as the Origin of  
**All Structures**  
of the Universe



# Current status

- scalar spectral index:  $n_s < 1$  at  $\sim 5 \sigma$
- tensor/scalar ratio:  $r < 0.1$  implies  $E_{\text{inflation}} < 10^{16} \text{ GeV}$
- simple, **canonical models** are **on verge of extinction** ( $m^2\phi^2$  model excluded at  $> 2 \sigma$ )
- $R^2$  (Starobinsky) model seems to fit best. **But why?** (large  $R^2$  correction but negligible higher order terms)
- $f_{\text{NL}}^{\text{local}} < O(1)$  suggests (effectively) **single-field slow-roll** (but non-slow-roll models with  $f_{\text{NL}}^{\text{local}} = O(1)$  not excluded)



element of **non-canonicity** is needed

Beyond  
(standard model of)  
Inflation

# non-canonical models

- Non-canonical kinetic term? ( $c_s < 1$ ?)

$$P_{\mathcal{R}} \propto \frac{1}{c_s} \quad (c_s: \text{sound speed}), \quad f_{\text{NL}}^{\text{equil}} \propto \frac{1}{c_s^2}$$

Planck:  $c_s > 0.024$  at 95% CL

- non-minimal coupling to gravity?

$$V(\phi) + \xi \phi^2 R \quad \longrightarrow \quad r = \frac{P_T(k)}{P_{\mathcal{R}}(k)} \propto \frac{1}{\xi} \quad \text{Planck: } \xi > \mathcal{O}(10)?$$

- scalar-tensor with derivative couplings (Hordeski) ?

$$c_s < 1, \quad c_{s,T} < 1, \quad c_s \neq c_{s,T}$$



tensor propagation speed

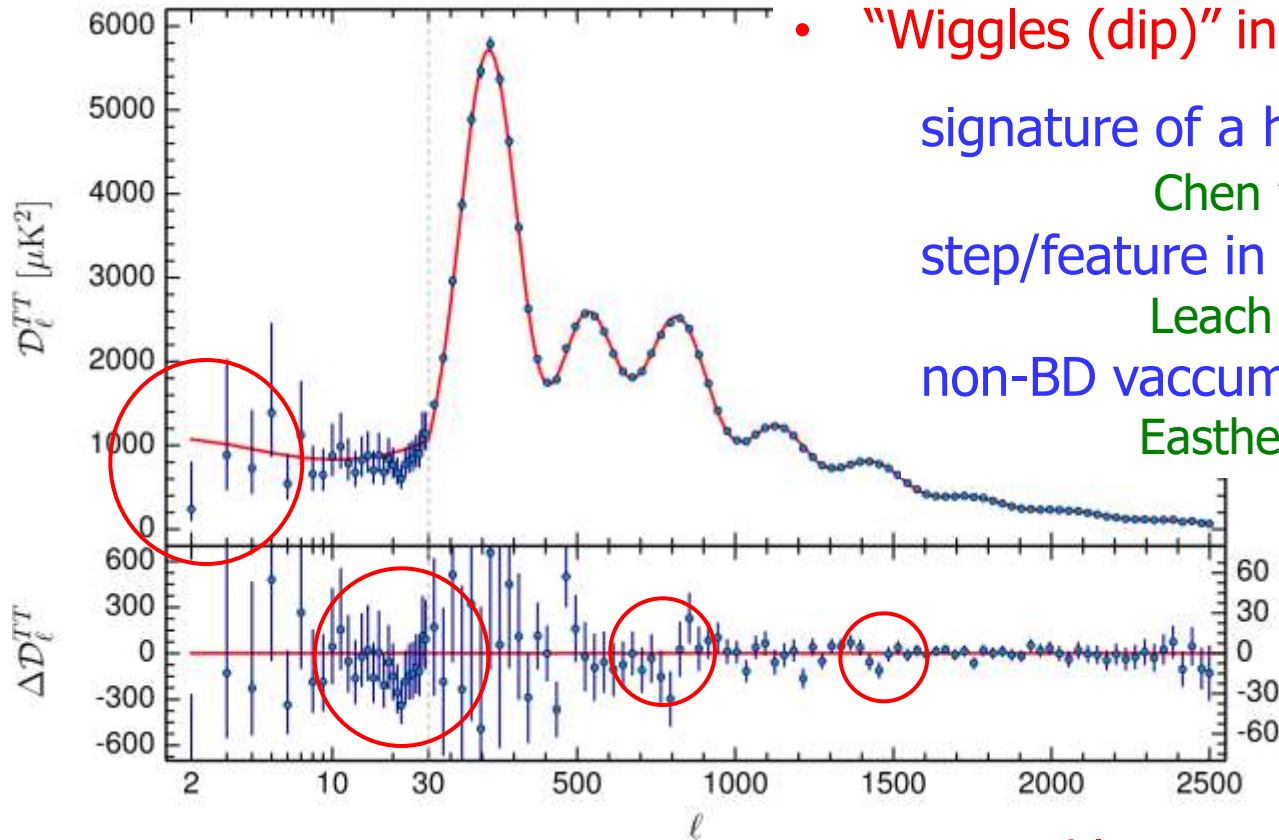
non-existence of Einstein frame?



definition of inflation?

- multi-field models, non-attractor inflation, ...

# Anomalies & Features



- “Wiggles (dip)” in the power spectrum

signature of a heavy field?

Chen '11, ...

step/feature in potential?

Leach et al. '01, ...

non-BD vacuum?

Easter et al. '02, ...

- Suppressed large scale fluctuations

featured potential? open inflation?

Linde, MS & Tanaka '99, ...

# Cosmic Landscape?

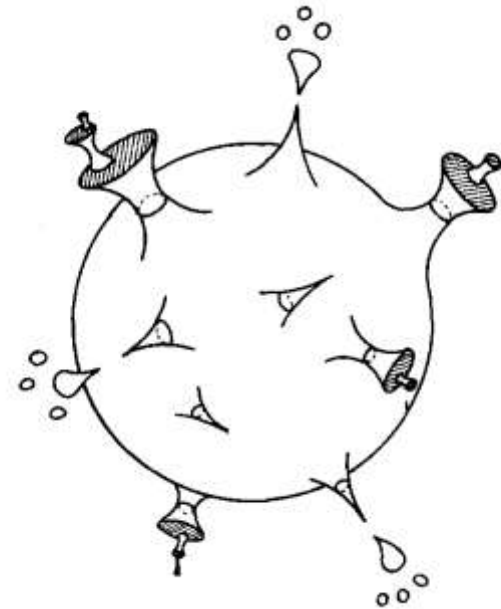
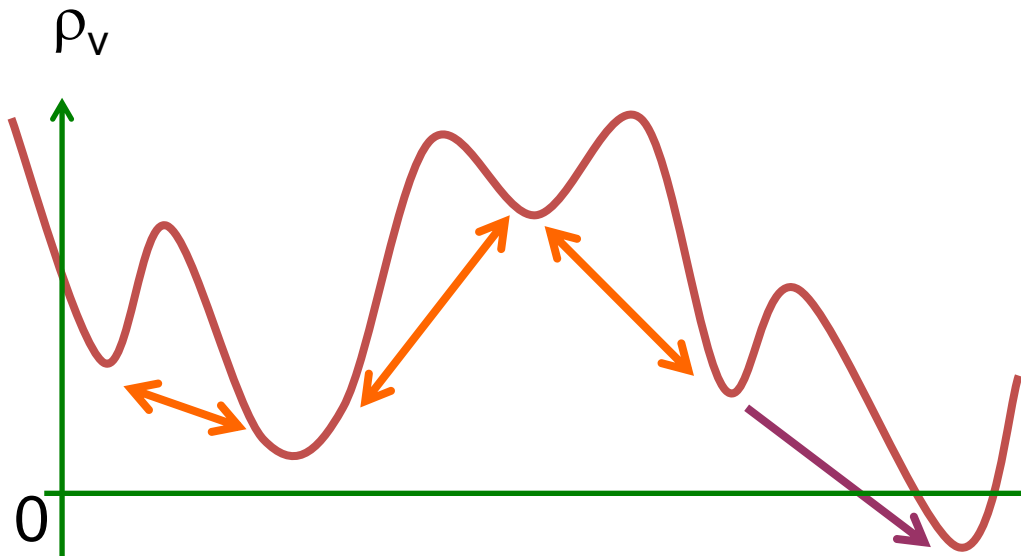
string theory suggests an intriguing picture of the early universe



**Maybe we live in one of these vacua...**

- Universe jumps around in the landscape by quantum tunneling
  - it can go up to a vacuum with larger  $\rho_v$  de Sitter (dS) space ~ thermal state with  $T = H/2\pi$ 

expansion rate  
↓
  - if it tunnels to a vacuum with negative  $\rho_v$ , it collapses within  $t \sim M_p/|\rho_v|^{1/2}$ .
  - so we may focus on vacua with positive  $\rho_v$ : dS vacua



Sato, Kodama, MS & Maeda ('81)

# Open Inflation in Cosmic Landscape

Universe inside nucleated bubble = spatially open universe

Friedmann eq.

$$H^2 \equiv \left( \frac{\dot{a}}{a} \right)^2 = \frac{\rho}{3M_P^2} + \frac{1}{a^2}$$

negative  
spatial  
curvature

$$1 = \frac{\rho}{3M_P^2 H^2} + \frac{1}{a^2 H^2} \equiv \Omega + \Omega_K$$

density parameter

Observational data indicate  $1 - \Omega_0 = \Omega_{K,0} \sim < 10^{-2}$  : almost flat

("0" stands for current value)

# What if this is the case?

## ➤ two possibilities

1. inflation after tunneling was short enough ( $N \sim 60$ )

$$\Omega_{K,o} = 1 - \Omega_o = 10^{-2} \sim 10^{-3} \quad \text{“open universe”}$$

➡ signatures in **large angle CMB anisotropies?**

Kanno, MS & Tanaka ('13), White, Zhang & MS ('14), ...

2. inflation after tunneling was long enough ( $N \gg 60$ )

$$\Omega_{K,o} = 1 - \Omega_o \ll 1 \quad \text{“flat universe”}$$

➡ signatures from **bubble collisions**

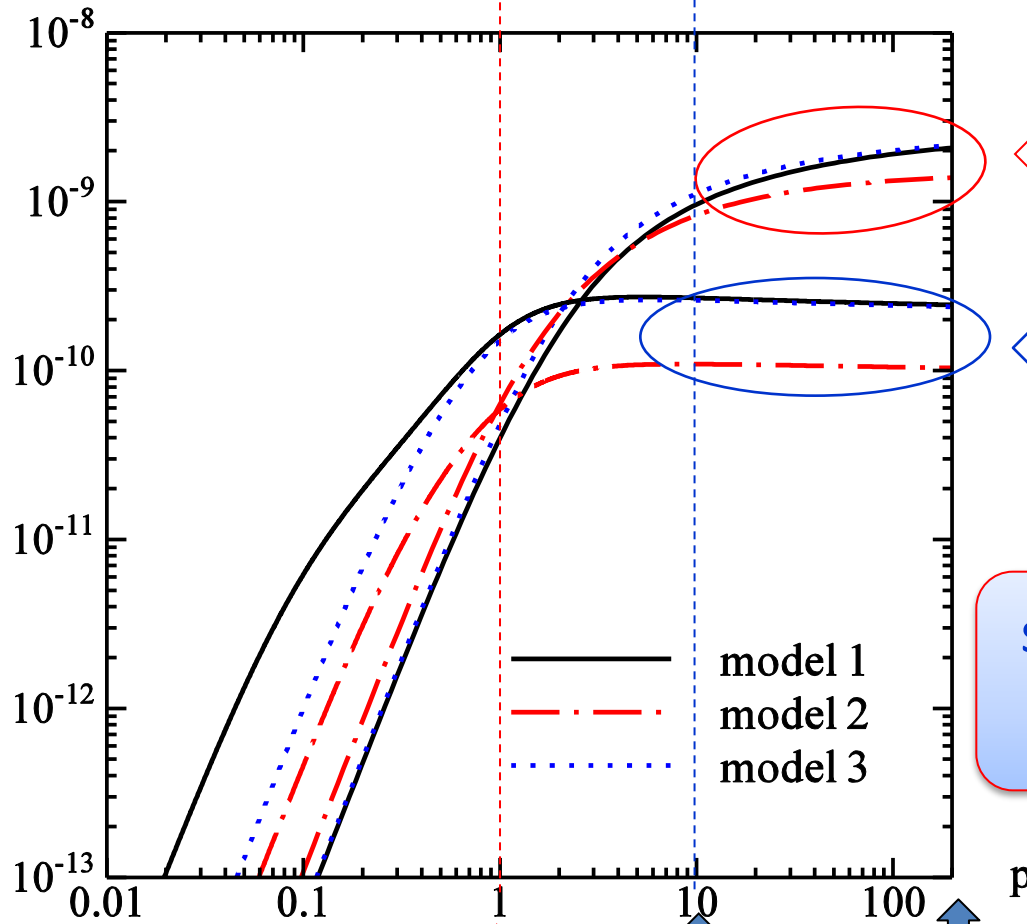
Sugimura, Yamauchi & MS ('12), ...



# scalar suppression on large scales

Linde, MS & Tanaka (1999)  
White, Zhang & MS (2014)

$$(|R_p|^2, |U_p|^2) p^3 / (2\pi^2)$$



← scalar

← tensor  
(no suppression)

scalar suppression begins at  
smaller scale

↕  
break scale

curvature  
radius

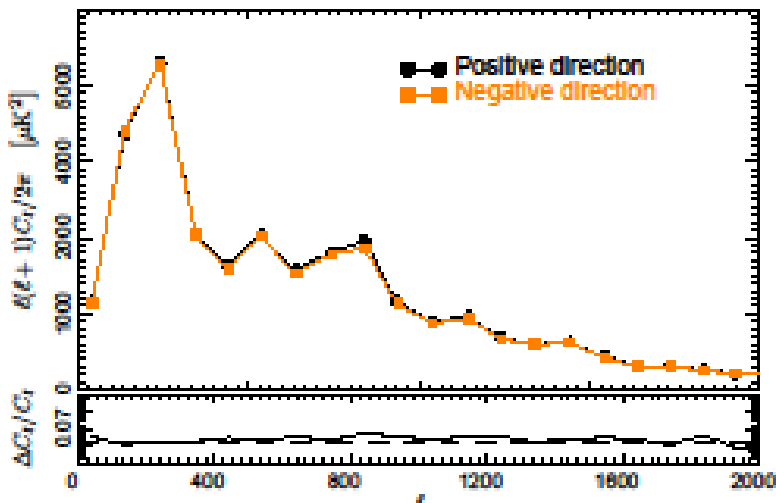
$H_0^{-1}$  if  $\Omega_K \approx 0.01$

# dipole power asymmetry

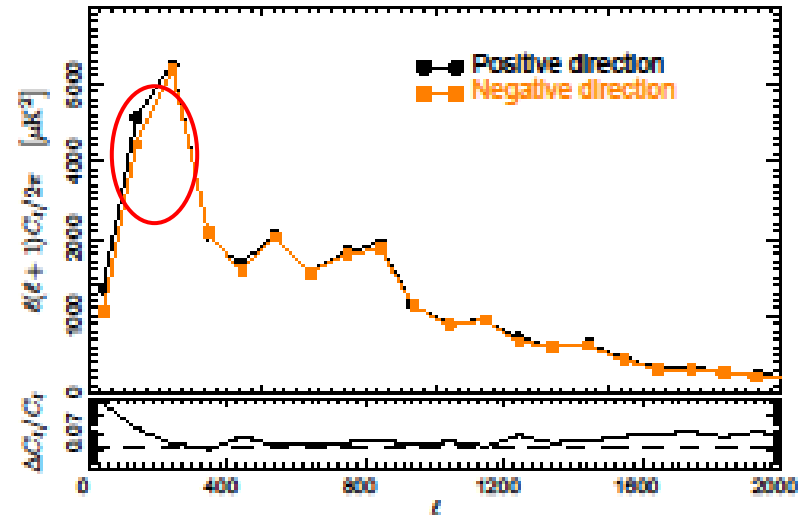
$$P(k; \mathbf{n}) = \left( 1 + 2A \hat{\mathbf{d}} \cdot \mathbf{n} \right) P_{iso}(k)$$

↑
↑

line of sight                      dipole



↑  
no asymmetry in the direction of  $ell=1$



↑  
dipole asymmetry in the direction  
maximizing the asymmetry

## Planck 2013 XXIII

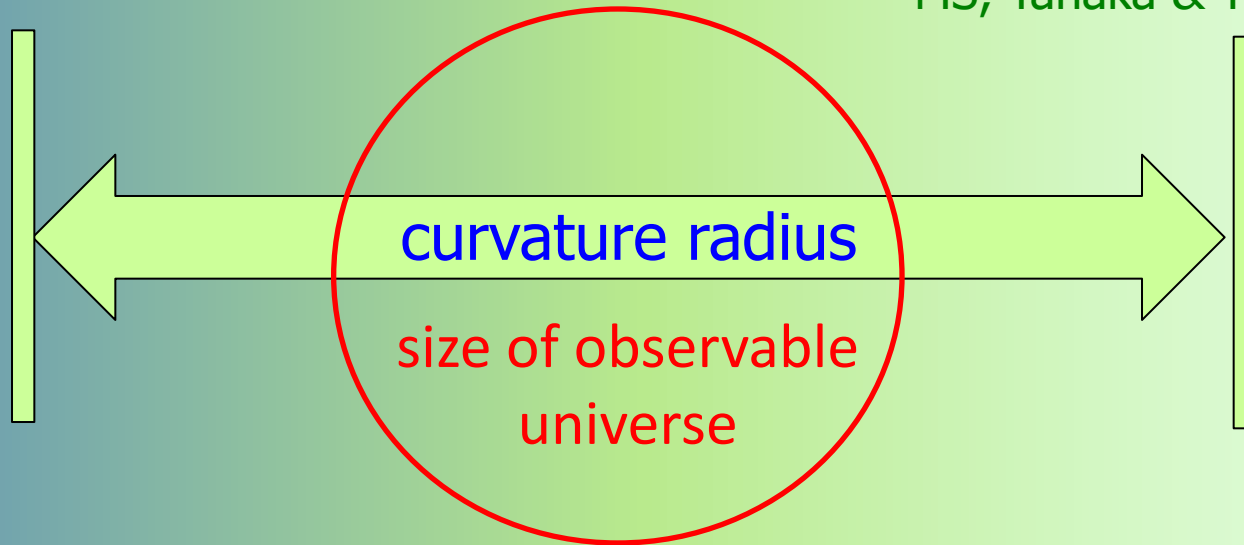
$$\frac{\delta T}{T} = (1 + A \cos \theta) \left( \frac{\delta T}{T} \right)_{iso}$$

$$A \approx 0.07$$

Data set	FWHM [°]	A	$(l, b)$ [°]	$\Delta \ln \mathcal{L}$	Significance
Commander	5	$0.078^{+0.020}_{-0.021}$	$(227, -15) \pm 19$	8.8	$3.5\sigma$
NILC	5	$0.069^{+0.020}_{-0.021}$	$(226, -16) \pm 22$	7.1	$3.0\sigma$
SEVEM	5	$0.066^{+0.021}_{-0.021}$	$(227, -16) \pm 24$	6.7	$2.9\sigma$
SMICA	5	$0.065^{+0.021}_{-0.021}$	$(226, -17) \pm 24$	6.6	$2.9\sigma$
WMAP5 ILC	4.5	$0.072 \pm 0.022$	$(224, -22) \pm 24$	7.3	$3.3\sigma$
Commander	6	$0.076^{+0.024}_{-0.025}$	$(223, -16) \pm 25$	6.4	$2.8\sigma$
NILC	6	$0.062^{+0.025}_{-0.026}$	$(223, -19) \pm 38$	4.7	$2.3\sigma$
SEVEM	6	$0.060^{+0.025}_{-0.026}$	$(225, -19) \pm 40$	4.6	$2.2\sigma$
SMICA	6	$0.058^{+0.025}_{-0.027}$	$(223, -21) \pm 43$	4.2	$2.1\sigma$
Commander	7	$0.062^{+0.028}_{-0.030}$	$(223, -8) \pm 45$	4.0	$2.0\sigma$
NILC	7	$0.055^{+0.029}_{-0.030}$	$(225, -10) \pm 53$	3.4	$1.7\sigma$
SEVEM	7	$0.055^{+0.029}_{-0.030}$	$(226, -10) \pm 54$	3.3	$1.7\sigma$
SMICA	7	$0.048^{+0.029}_{-0.029}$	$(226, -11) \pm 58$	2.8	$1.5\sigma$
Commander	8	$0.043^{+0.032}_{-0.029}$	$(218, -15) \pm 62$	2.1	$1.2\sigma$
NILC	8	$0.049^{+0.032}_{-0.031}$	$(223, -16) \pm 59$	2.5	$1.4\sigma$
SEVEM	8	$0.050^{+0.032}_{-0.031}$	$(223, -15) \pm 60$	2.5	$1.4\sigma$
SMICA	8	$0.041^{+0.032}_{-0.029}$	$(225, -16) \pm 63$	2.0	$1.1\sigma$
Commander	9	$0.068^{+0.035}_{-0.037}$	$(210, -24) \pm 52$	3.3	$1.7\sigma$
NILC	9	$0.076^{+0.035}_{-0.037}$	$(216, -25) \pm 45$	3.9	$1.9\sigma$
SEVEM	9	$0.078^{+0.035}_{-0.037}$	$(215, -24) \pm 43$	4.0	$2.0\sigma$
SMICA	9	$0.070^{+0.035}_{-0.037}$	$(216, -25) \pm 50$	3.4	$1.8\sigma$
WMAP3 ILC	9	0.114	$(225, -27)$	6.1	$2.8\sigma$
Commander	10	$0.092^{+0.037}_{-0.040}$	$(215, -29) \pm 38$	4.5	$2.2\sigma$
NILC	10	$0.098^{+0.037}_{-0.039}$	$(217, -29) \pm 33$	5.0	$2.3\sigma$
SEVEM	10	$0.103^{+0.037}_{-0.039}$	$(217, -28) \pm 30$	5.4	$2.5\sigma$
SMICA	10	$0.094^{+0.037}_{-0.040}$	$(218, -29) \pm 37$	4.6	$2.2\sigma$

Gradient of a field over the horizon scale  
 = **Super-curvature mode** in open inflation

MS, Tanaka & Yamamoto '95



may modulate the amplitude of  
 perturbation depending on the direction.

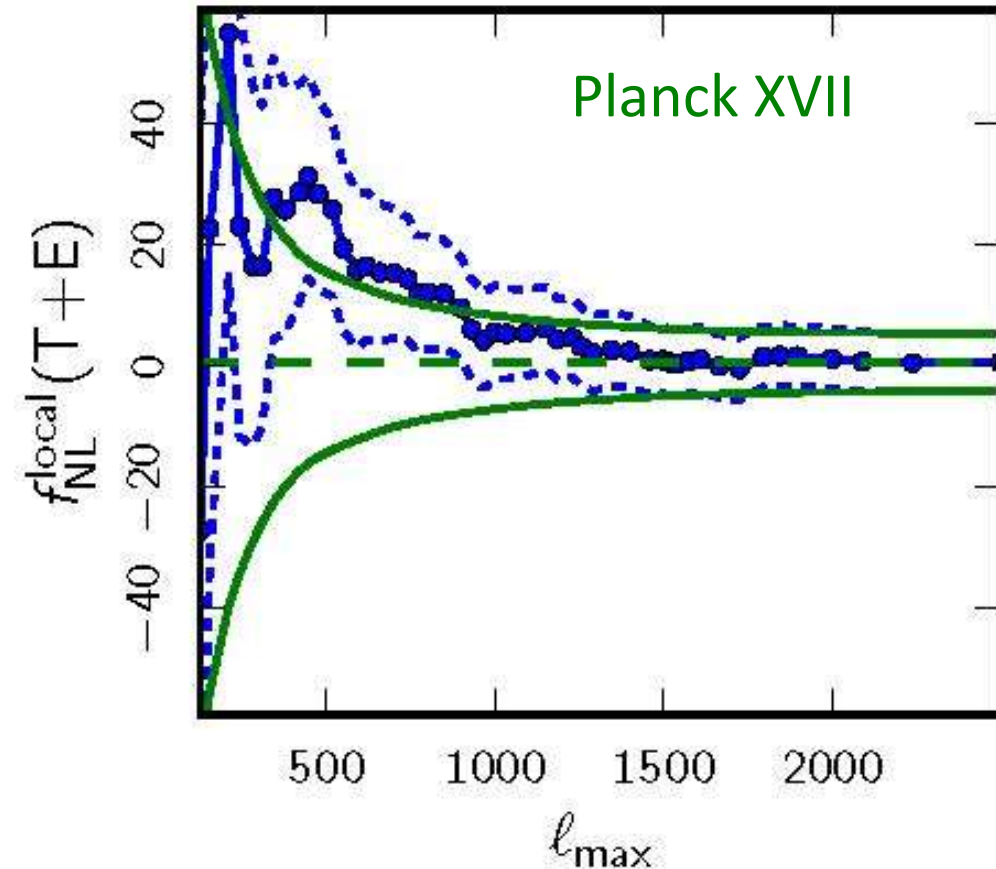
**leading order effect is dipolar**

if this is the case, then  $\Omega_K \gtrsim 10^{-3}$

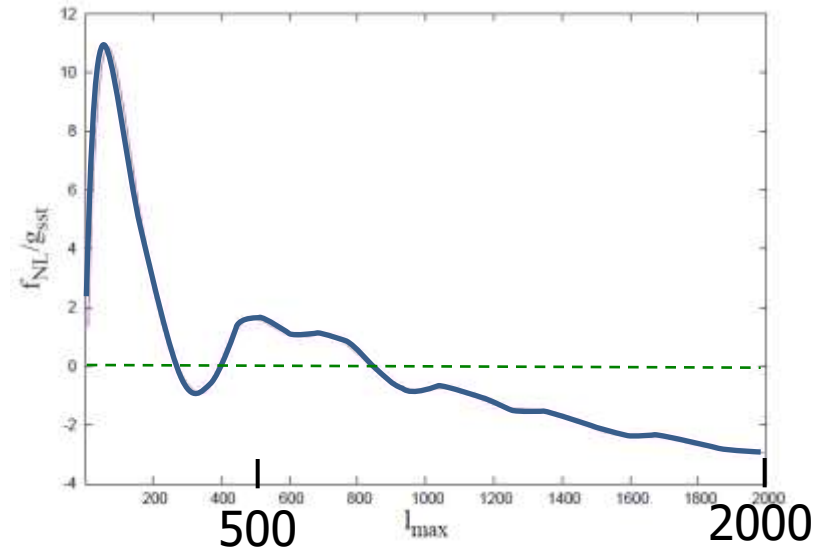
Kanno, MS & Tanaka '13

Brynes, Domenech, MS & Takahashi '16

# Scale-dependent non-Gaussianity?



- Slightly above 1- $\sigma$  deviation from zero
- What if this is primordial?

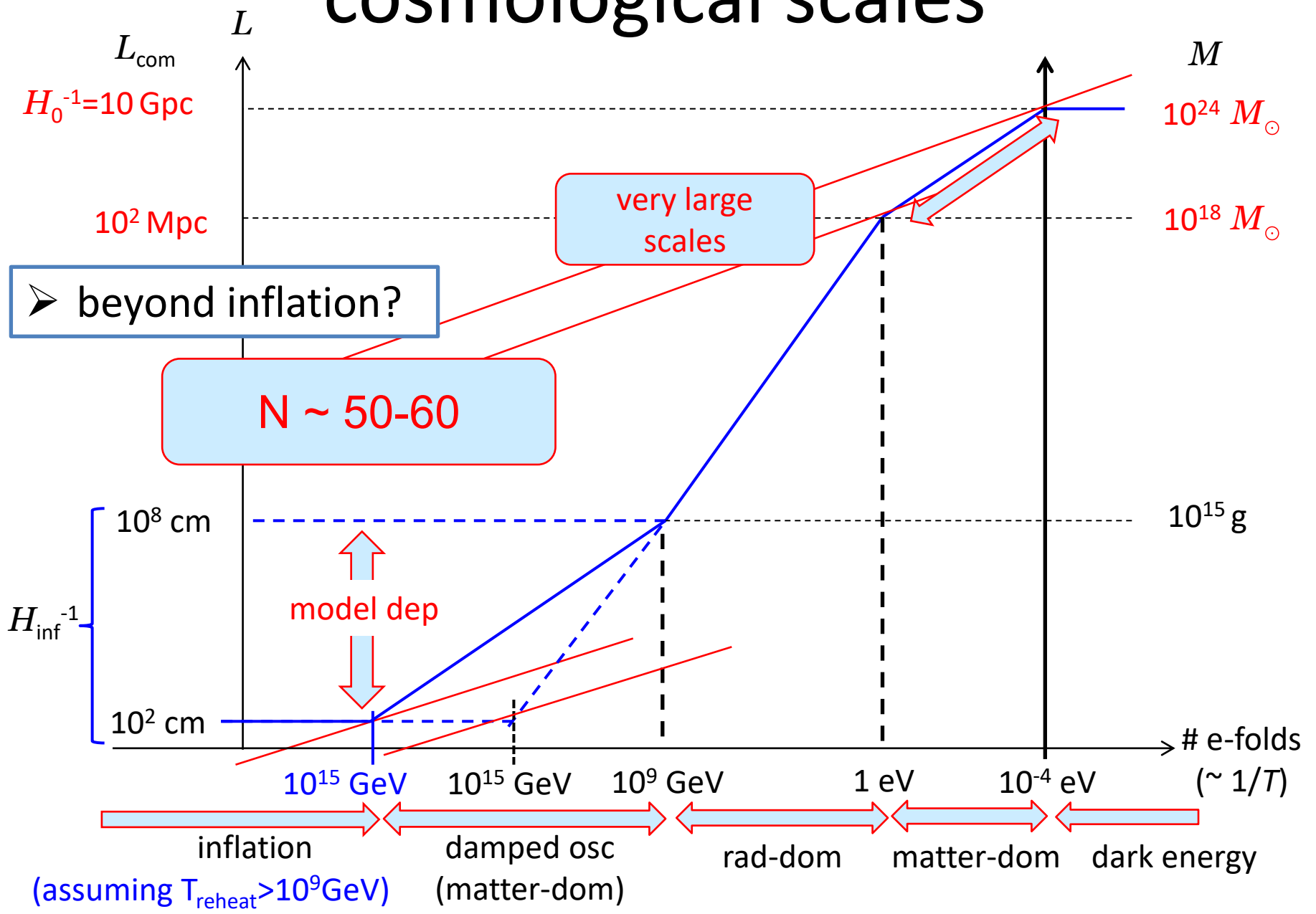


may be due to TSS coupling in a **massive tensor** theory

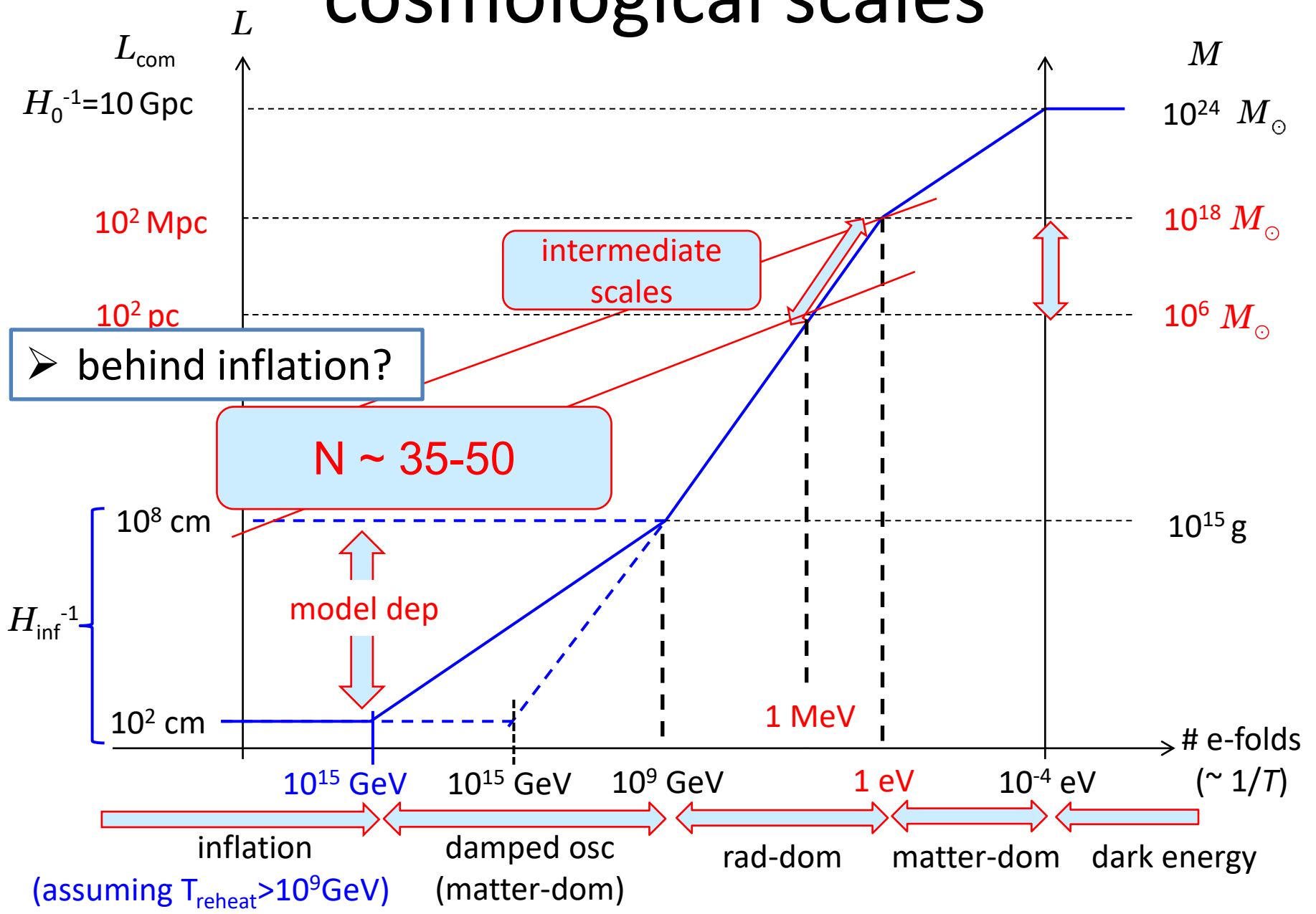
Domenech, Hiramatsu, Lin, MS, Shiraishi, Wang '16

Future issues

# cosmological scales

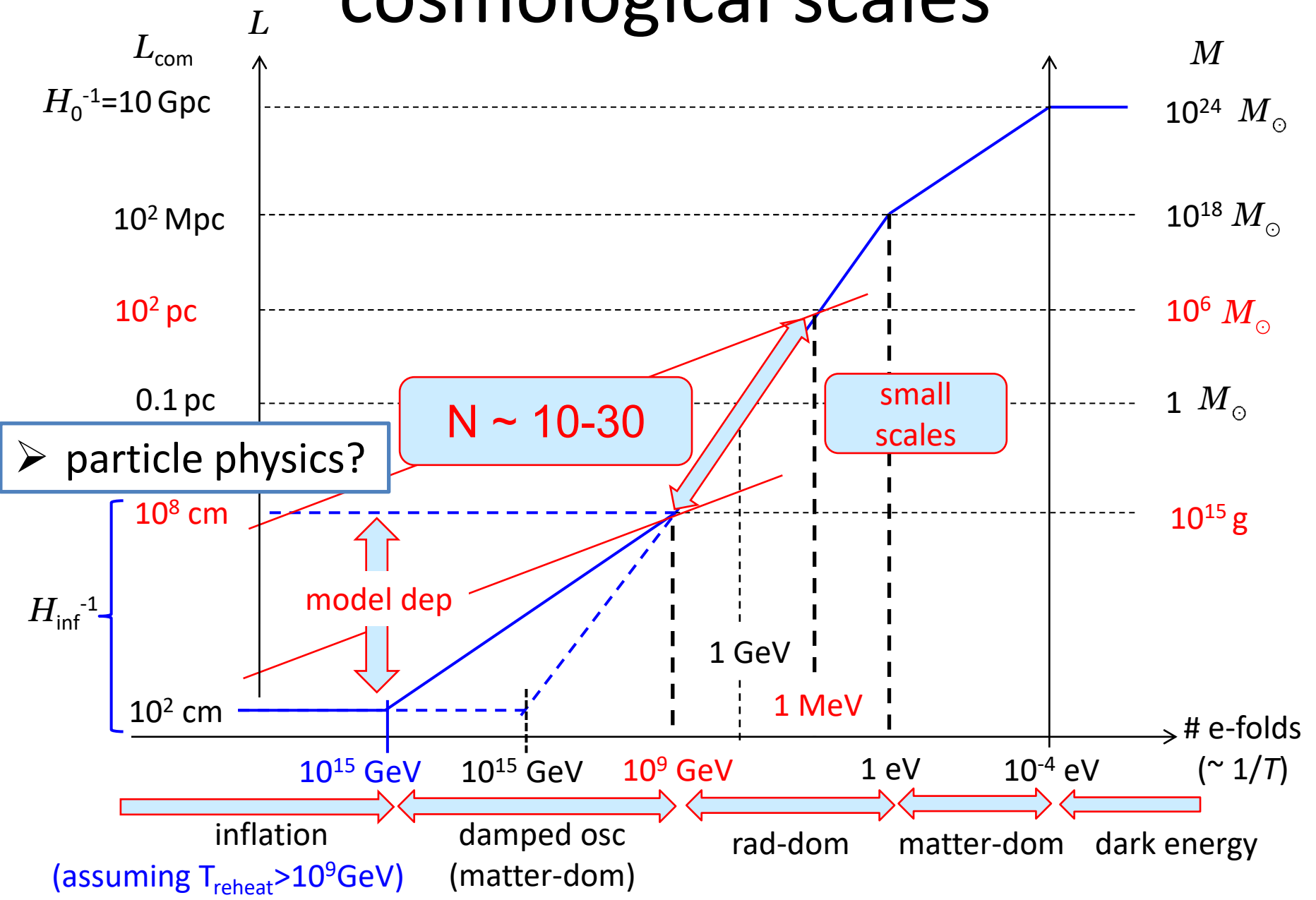


# cosmological scales





# cosmological scales



- definition of inflation?

(conformal trans can give any expansion law)

Domenech & MS '15

$$ds^2 = -dt^2 + a^2(t)d\vec{x}^2$$

$$d\tilde{s}^2 = \Omega^2(t)ds^2 \Rightarrow d\tilde{t} = \Omega(t)dt, \tilde{a}(\tilde{t}) = \Omega(t)a(t)$$

- initial condition before inflation, multiverse?
- successful reheating?
- non-linear effects, non-Gaussianities?
- gravitational waves at second order, PBHs?
- massive gravity?
- .....

Identification of Inflaton!

# Inflation as the tool to explore physics of the early Universe

Era of

Observational Inflationary  
Cosmology!

# Appendix: recollections

May 2004 : [MOU between KIAS and YITP](#) (renewed in March 2008)

- 2005 KIAS Cosmological Landscape: [Strings](#), [Gravity](#), and [Inflation](#)

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one zodiac cycle  
(12 years)



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- 2013 YITP [String](#) Theory, [Black Holes](#) and Holography
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- 2017 YITP [Strings](#), [Gravity](#) and [Cosmology](#)

Organizers:

Kimyeong Lee (KIAS) Sungjay Lee (KIAS)

Shinji Mukhoyama (YITP) Misao Sasaki (YITP)

Shigeki Sugimoto (YITP, Chair) Tadashi Takayanagi (YITP)

Piljin Yi (KIAS)



# Appendix: recollections

May 2004 : [MOU between KIAS and YITP](#) (renewed in March 2008)

- 2005 KIAS Cosmological Landscape: **Strings**, **Gravity**, and **Inflation**

Organizers:

Leonard Susskind (Stanford Univ.& KIAS)

Kimyeong Lee (KIAS, Seoul) Piljin Yi (KIAS, Seoul)

Misao Sasaki (YITP, Kyoto) Shigeki Sugimoto (YITP, Kyoto)

- 2007 YITP **String** Phenomenology and **Cosmology**
- 2009 KIAS Extended Workshop on DM, LHC and **Cosmology**
- 2011 KIAS **String** Theory, Holography, and Beyond
- 2013 YITP **String** Theory, **Black Holes** and Holography
- 2015 KIAS Geometry in Gauge Theories and **String** Theory
- 2017 YITP **Strings**, **Gravity** and **Cosmology**

Organizers:

Kimyeong Lee (KIAS) **Sungjay Lee (KIAS)**

**Shinji Mukhoyama (YITP)** Misao Sasaki (YITP)

Shigeki Sugimoto (YITP, Chair) **Tadashi Takayanagi (YITP)**

Piljin Yi (KIAS)

**New Generation!**

some say ...

old **physicists** never die,  
they just fade away...

some say ...

old **physicists** never die,  
they just fade away...

but I will **NOT** disappear yet!

**Thank You!**