

Perspectives on nuclear reaction theory and superheavy elements

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1. Nuclear Reactions: overview
2. Coupled-channels approach with a beyond-mean-field method
3. Time-dependent GCM for many-body tunneling
4. Fusion for superheavy elements and TDHF
5. Summary

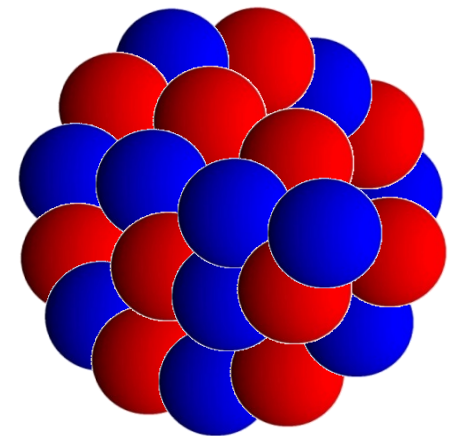
Introduction: low-energy nuclear physics

□ behaviors of atomic nuclei as a quantum many-body systems

← understanding based on strong interaction

➤ static properties: nuclear structure

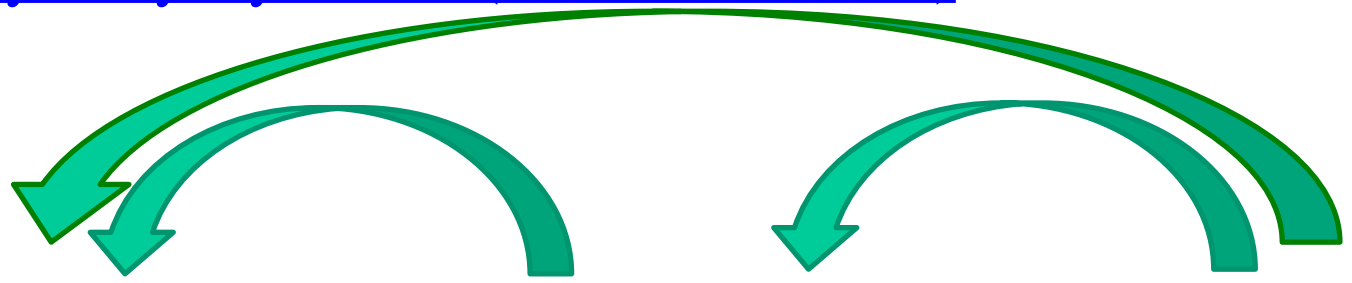
- ✓ ground state properties
(mass, size, shape,....)
- ✓ excitations
- ✓ nuclear matter
- ✓ decays



➤ dynamics: nuclear reactions

an interplay between nuclear structure and nuclear reaction

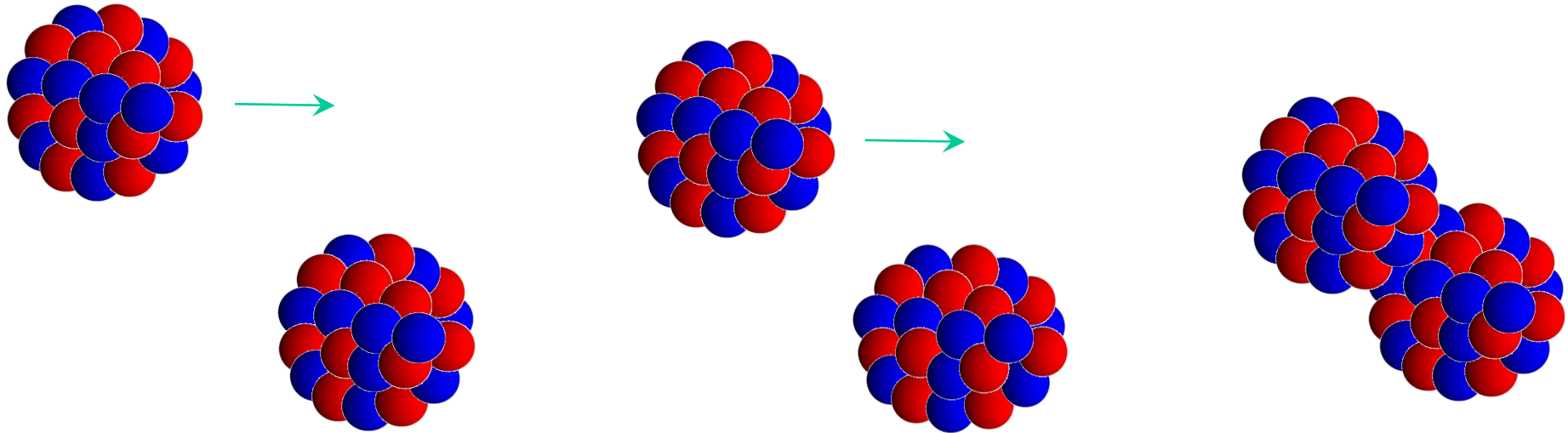
Quantum Many-body Dynamics (nuclear reactions)



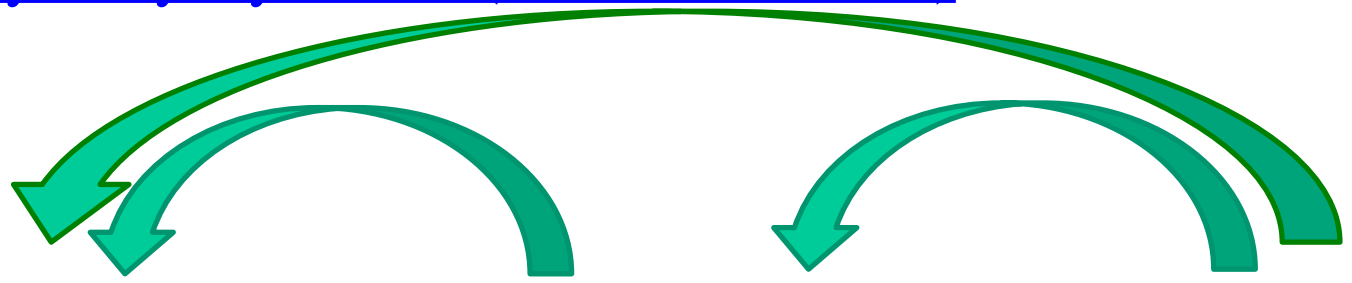
elastic scattering

inel. scattering

fusion



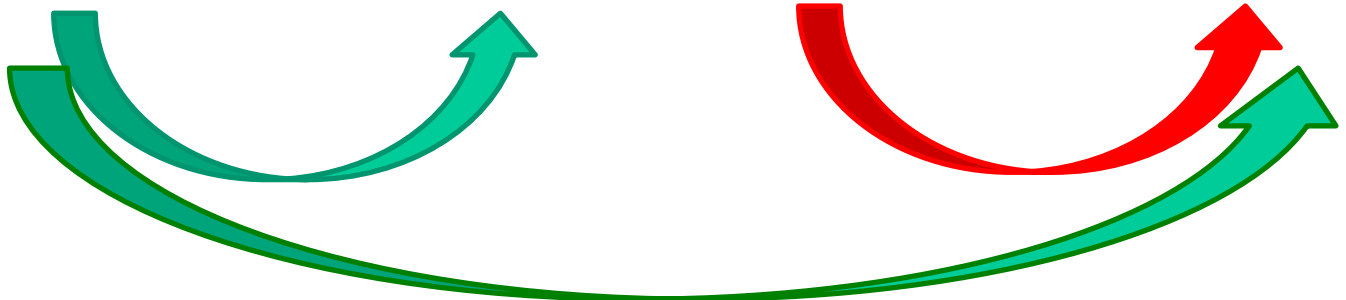
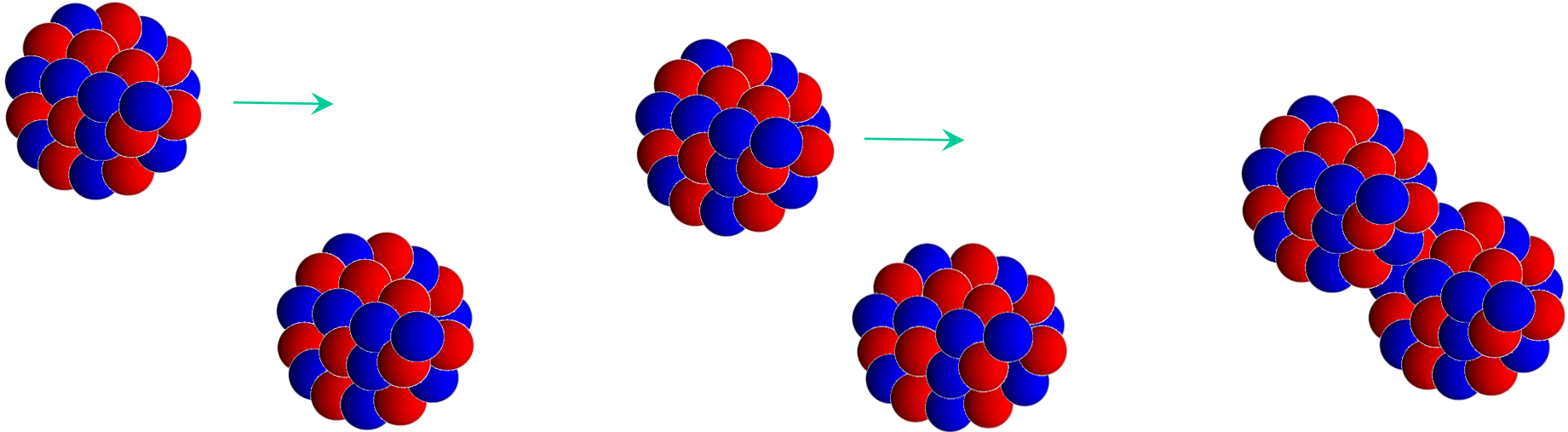
Quantum Many-body Dynamics (nuclear reactions)



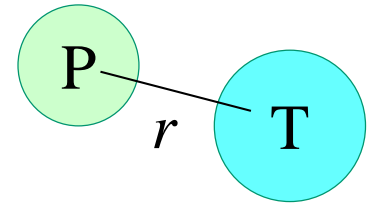
elastic scattering

inel. scattering

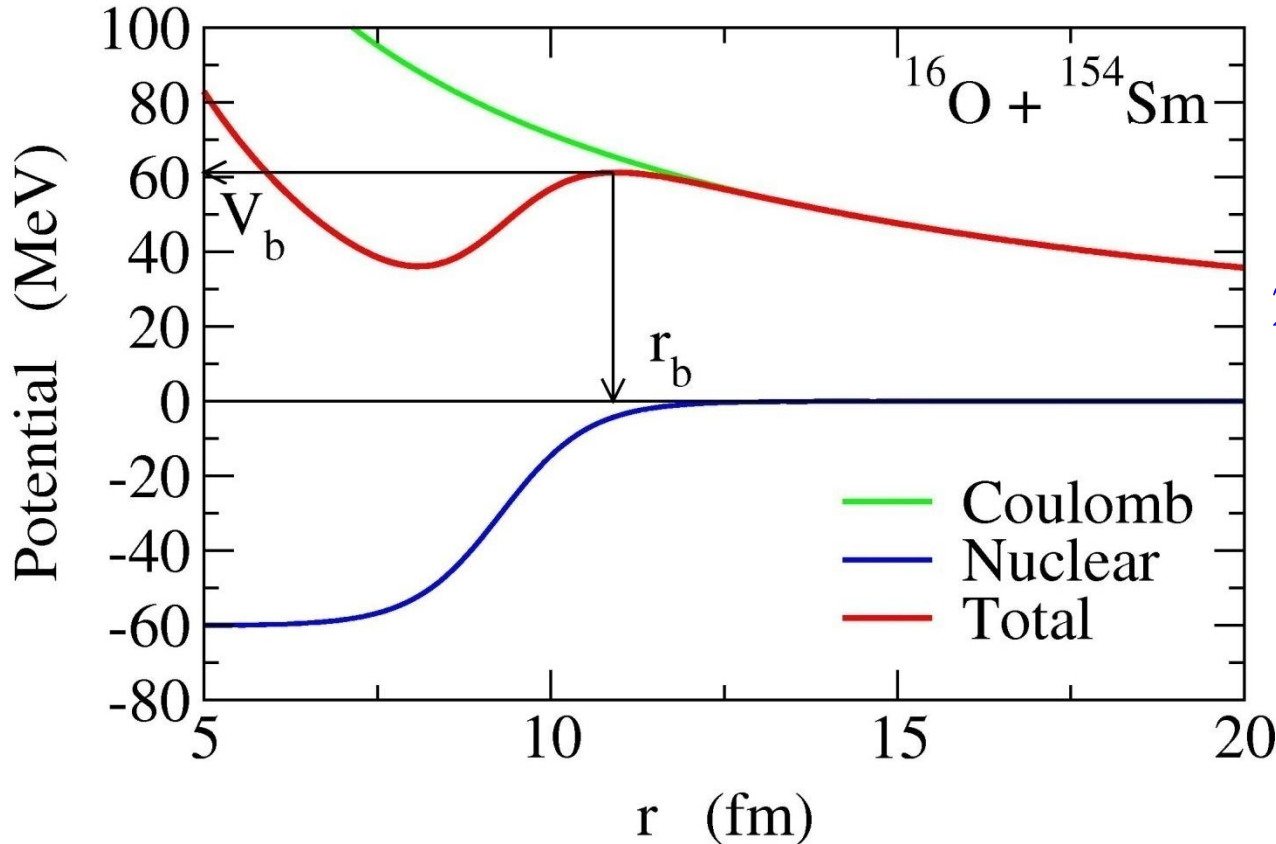
fusion



Coulomb barrier



Coulomb barrier

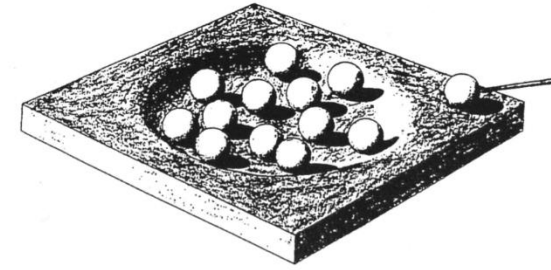
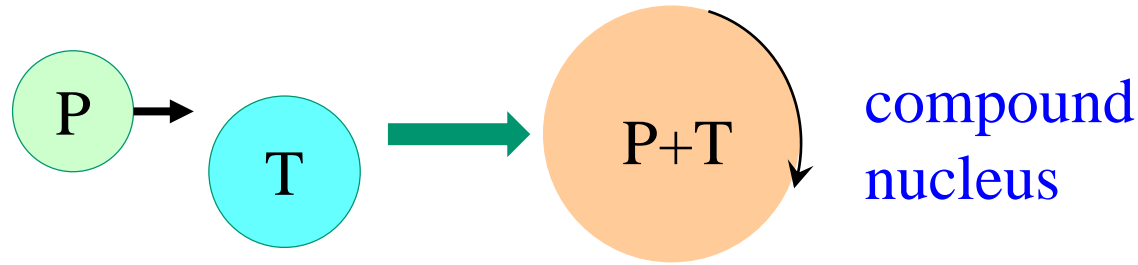


1. Coulomb interaction
long range
repulsion
 2. Nuclear interaction
short range
attraction
- ↓
- Potential barrier
(Coulomb barrier)

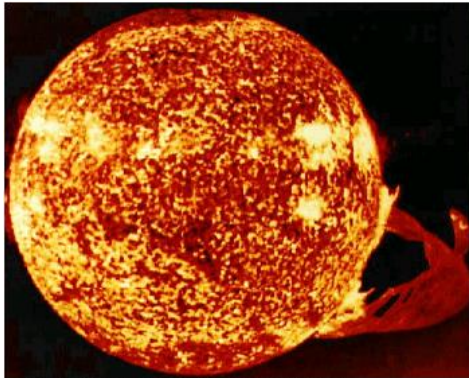
the barrier height \rightarrow defines the energy scale of a system

Fusion reactions at energies around the Coulomb barrier

Fusion reactions: compound nucleus formation

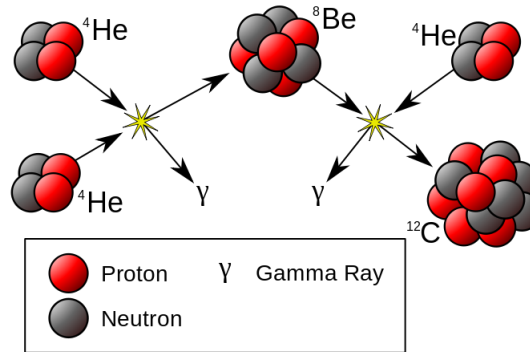


cf. Bohr '36

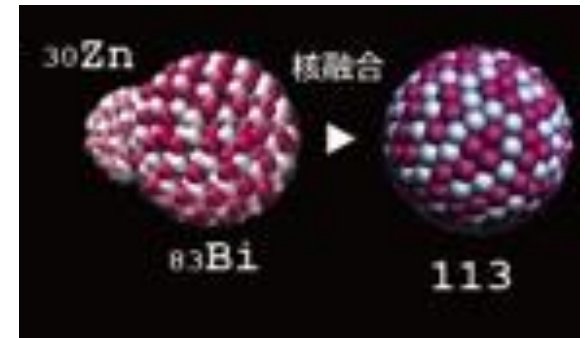


NASA, Skylab space station on December 19, 1973, solar flare reaching 588 000 km off solar surface

energy production
in stars (Bethe '39)



nucleosynthesis



superheavy elements

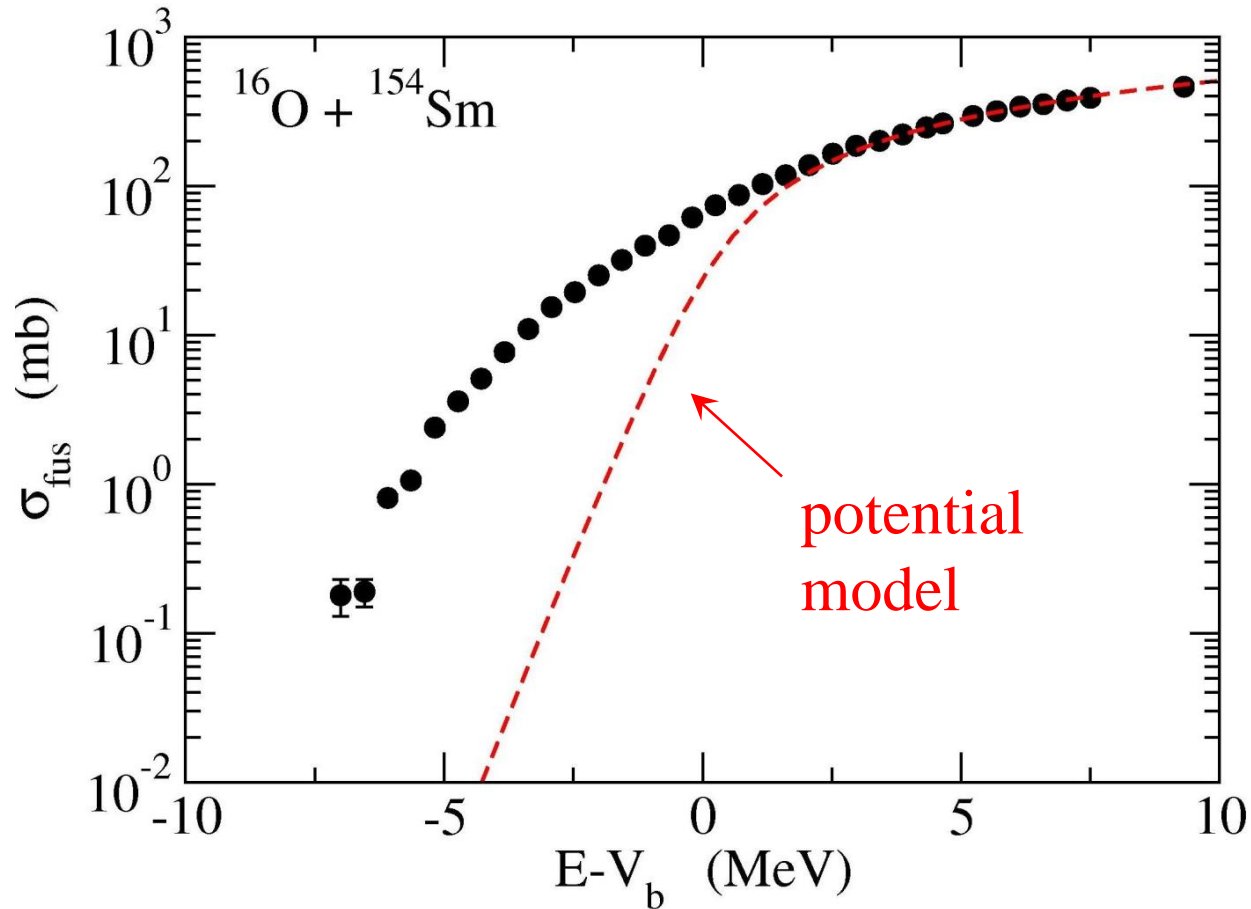
Fusion and fission: large amplitude motions of quantum many-body systems with strong interaction

← microscopic understanding: **an ultimate goal of nuclear physics**

Discovery of large sub-barrier enhancement of σ_{fus} (~ 80 's)

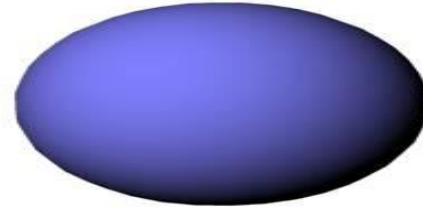
potential model: inert nuclei (no structure)

$$\sigma_{\text{fus}} = \frac{\pi}{k^2} \sum_l (2l + 1)(1 - |S_l|^2)$$

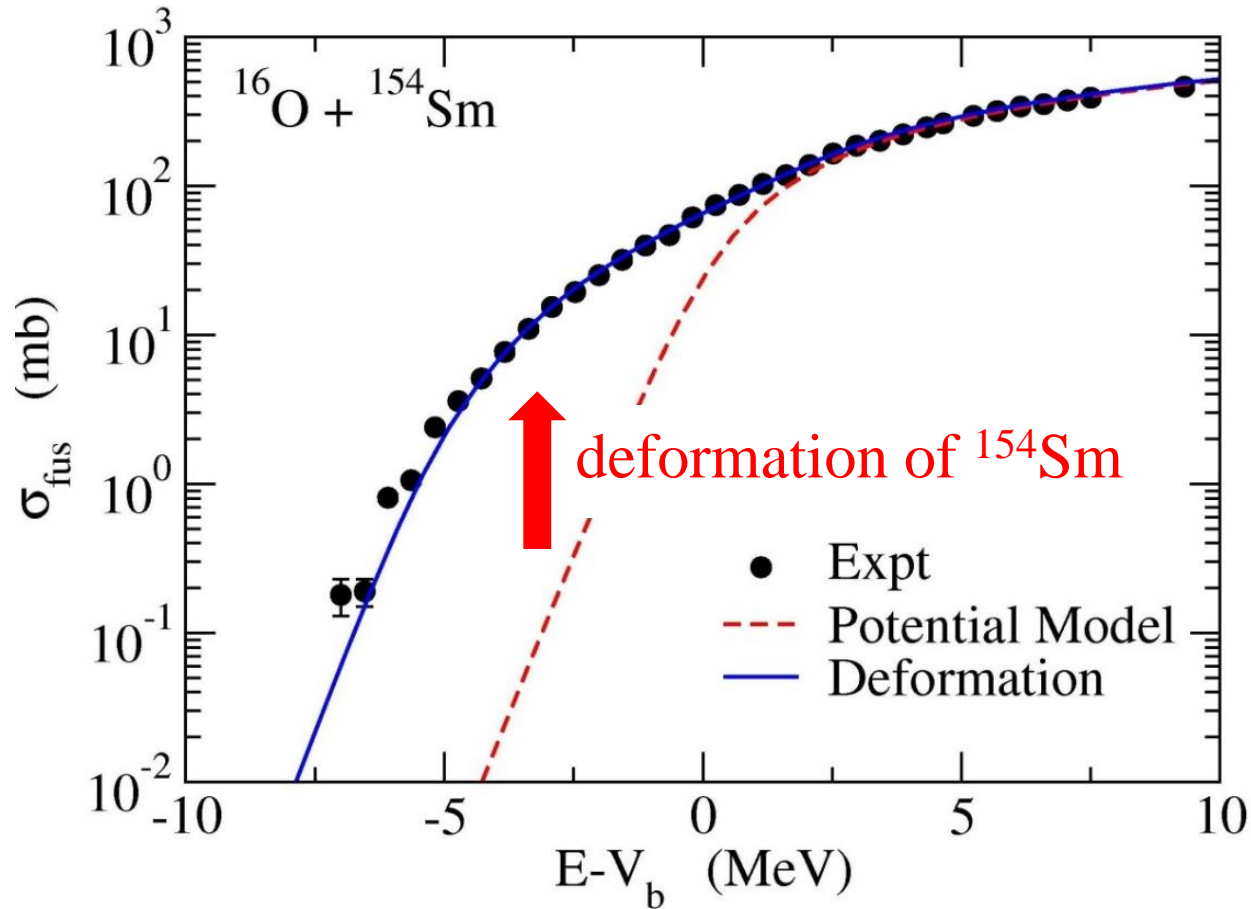


Discovery of large sub-barrier enhancement of σ_{fus} (~ 80 's)

^{154}Sm : a typical deformed nucleus

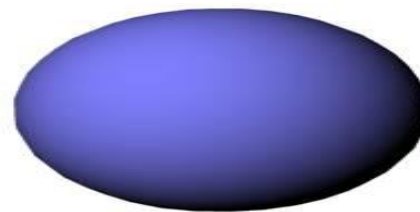


^{154}Sm

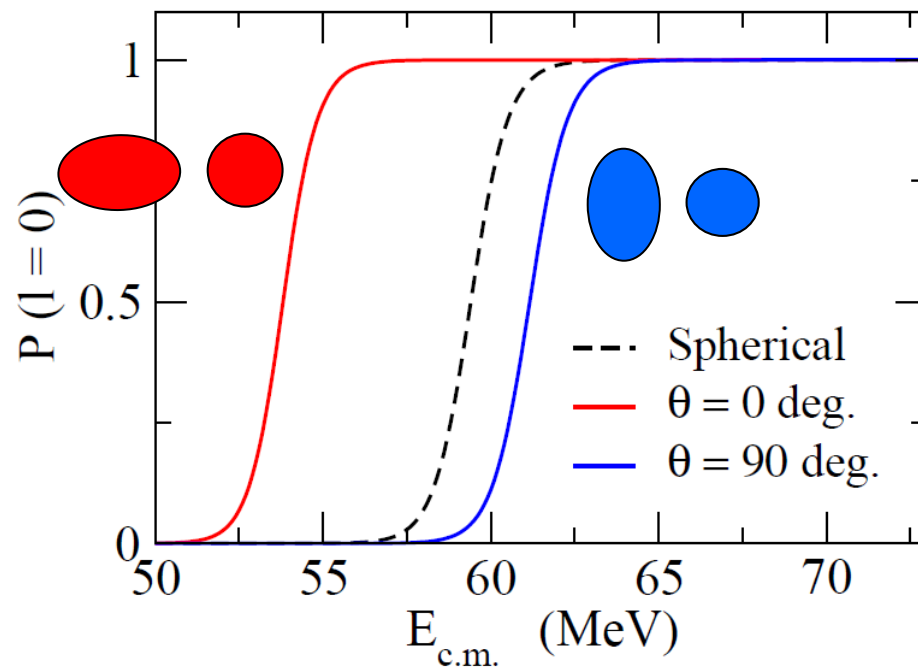
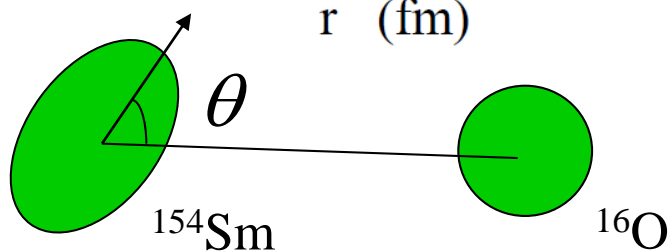
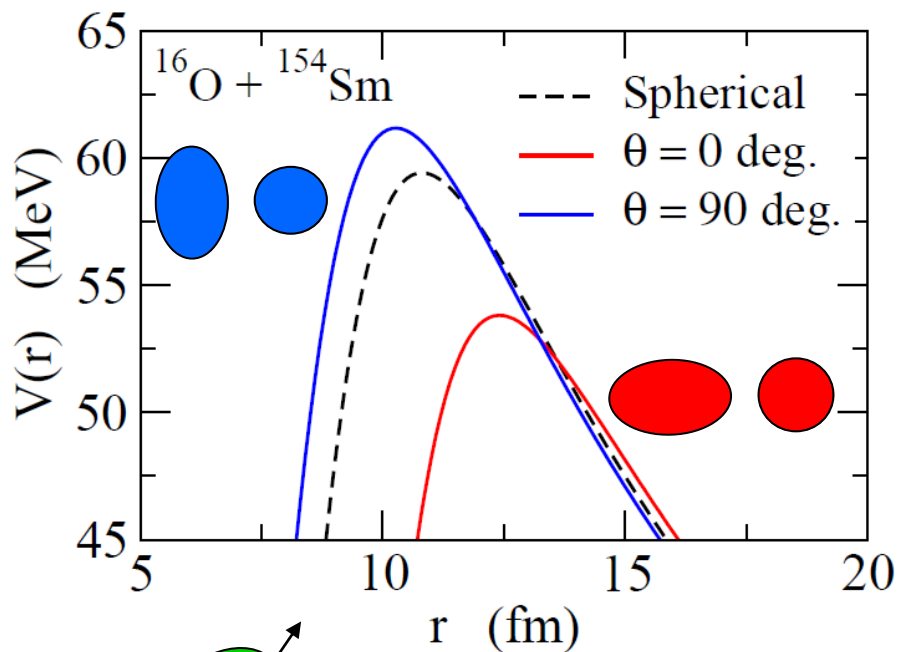


Effects of nuclear deformation

^{154}Sm : a typical deformed nucleus

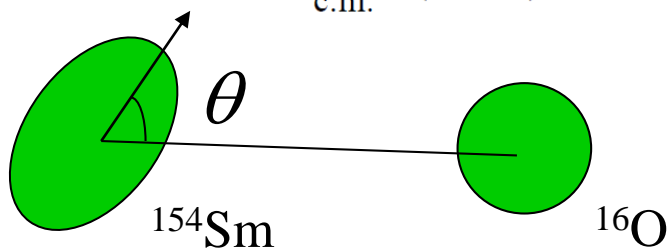
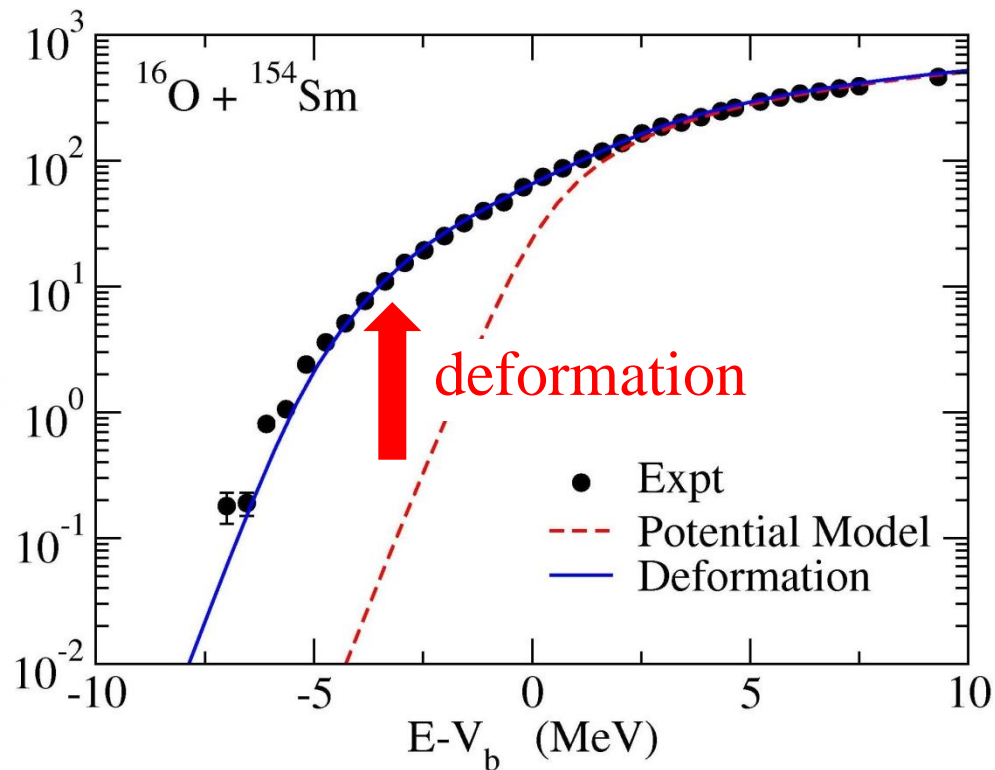
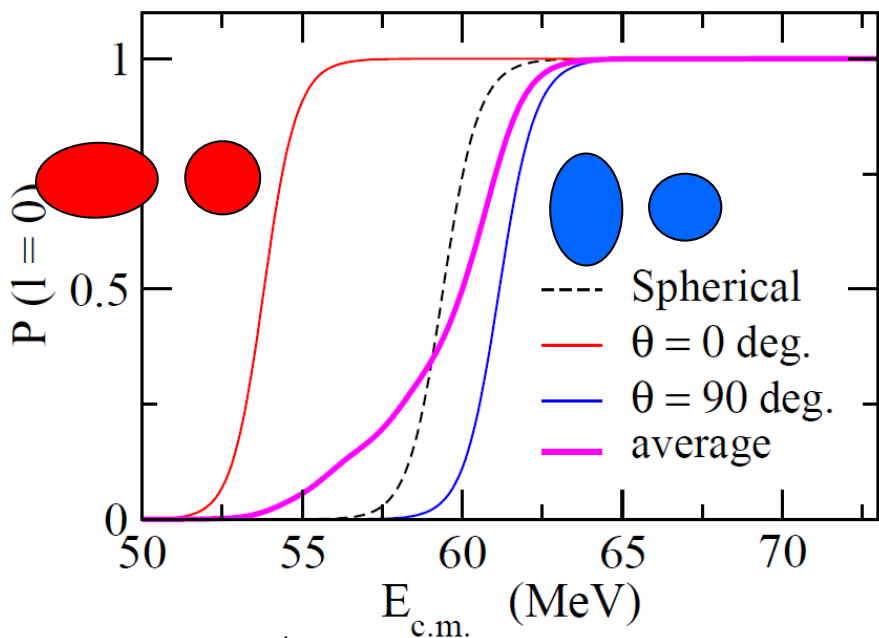
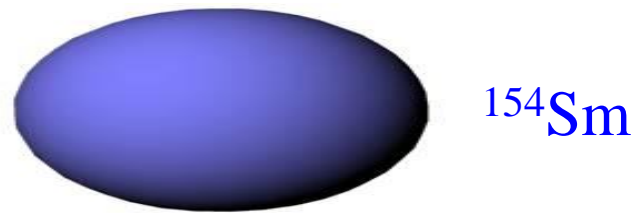


^{154}Sm



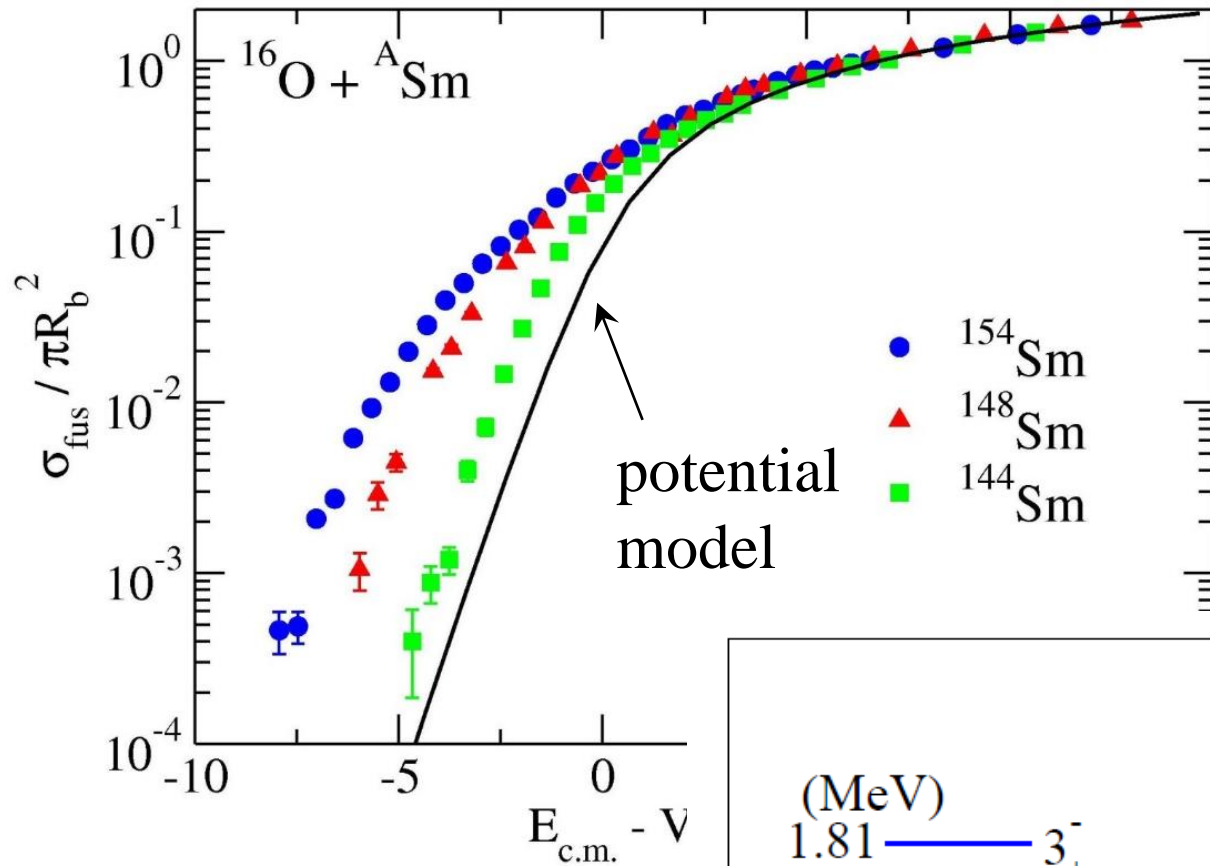
Effects of nuclear deformation

^{154}Sm : a typical deformed nucleus



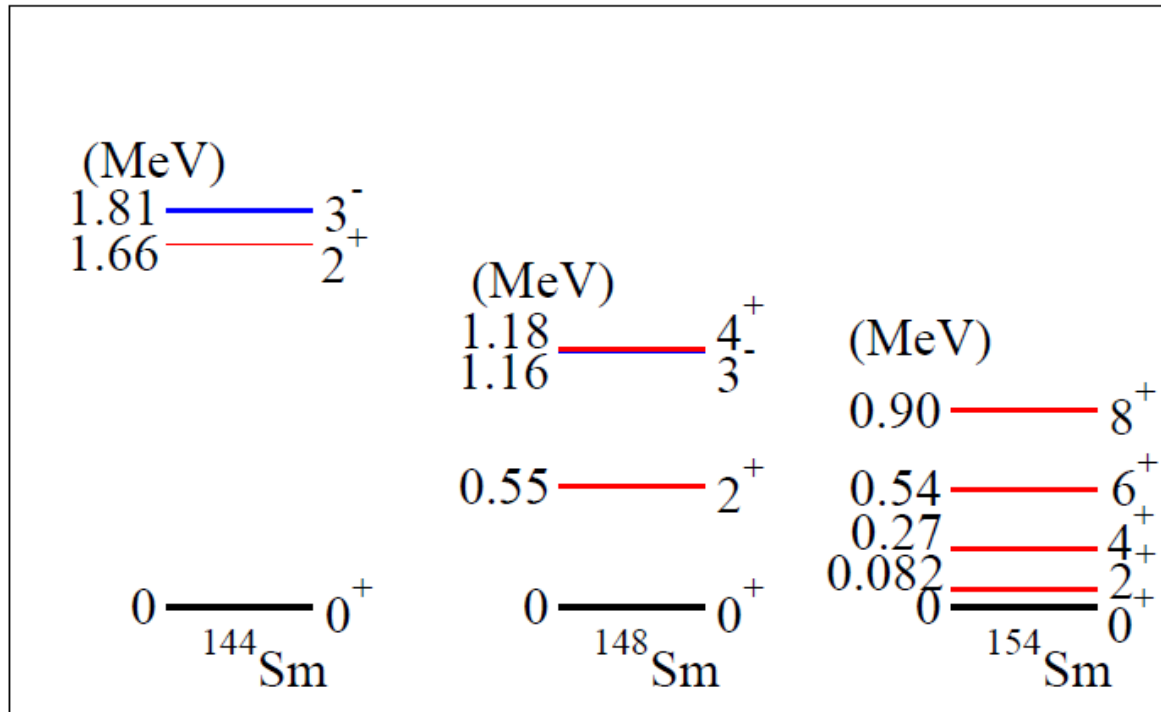
$$\sigma_{\text{fus}}(E) = \int_0^1 d(\cos \theta) \sigma_{\text{fus}}(E; \theta)$$

Fusion: strong interplay between nuclear structure and reaction



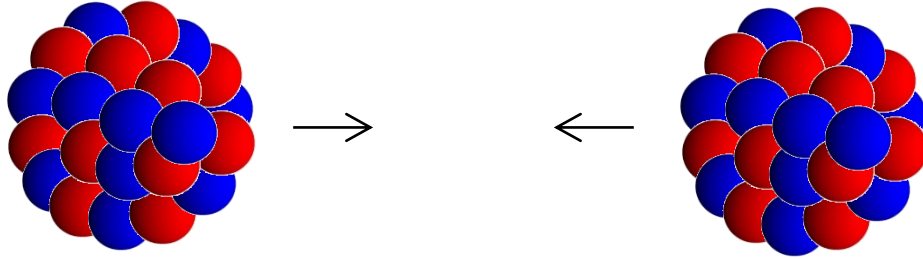
enhancement of fusion cross sections
: a general phenomenon

strong correlation with nuclear spectrum
→ coupling assisted tunneling



Coupled-channels method: a quantal scattering theory with excitations

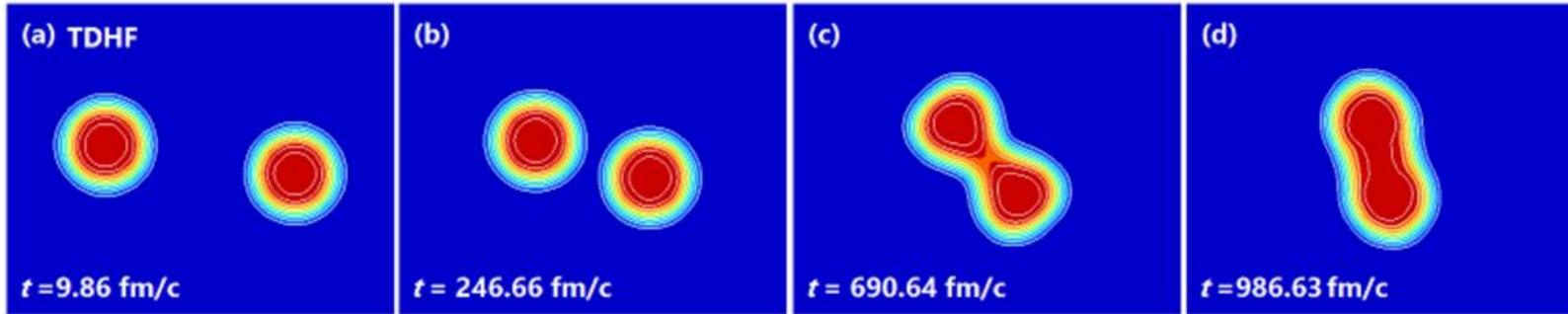
many-body problem



still very challenging

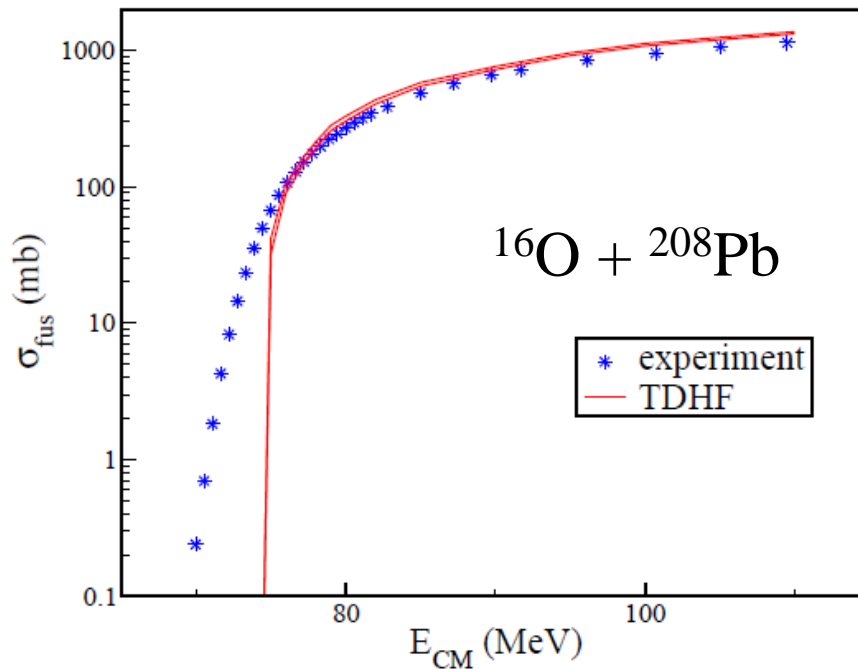
TDHF simulation

TDHF = Time Dependent Hartree-Fock
(a single Slater determinant)



S. Ebata, T. Nakatsukasa, JPC Conf. Proc. 6 ('15) 020056

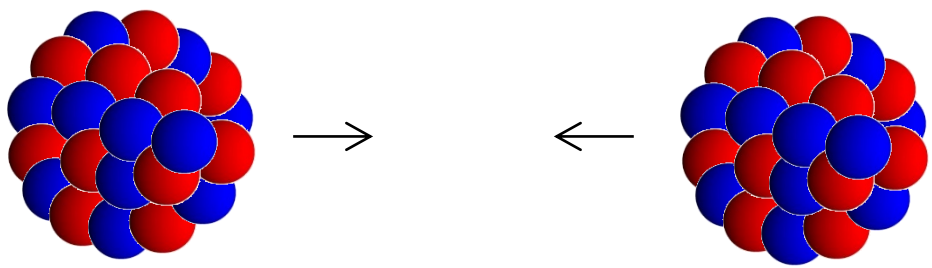
ab-initio, but no tunneling



C. Simenel,
EPJA48 ('12) 152

Coupled-channels method: a quantal scattering theory with excitations

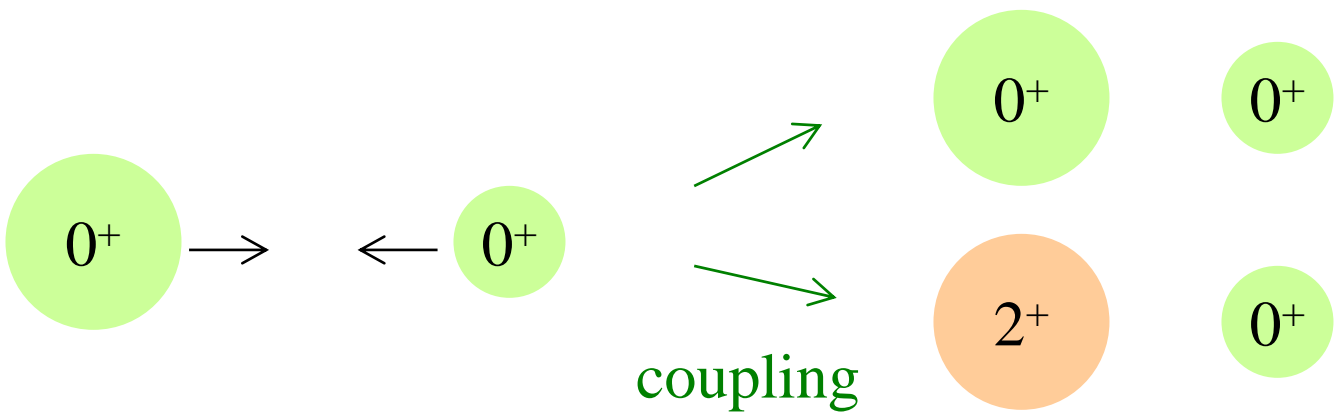
many-body problem



still very challenging



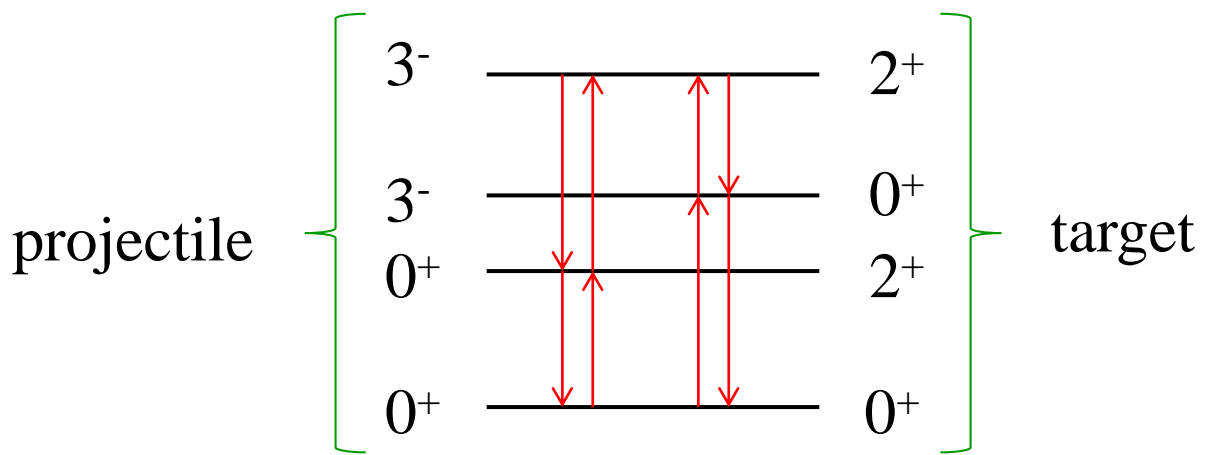
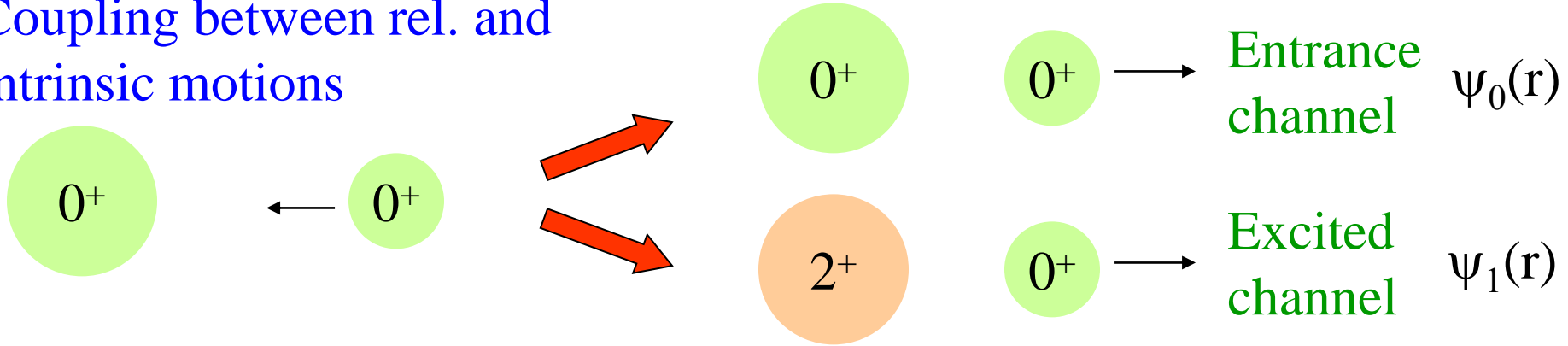
two-body problem, but with excitations
(coupled-channels approach)



scattering theory with excitations

Coupled-channels method: a quantal scattering theory with excitations

Coupling between rel. and intrinsic motions



$$\Psi(\mathbf{r}, \xi) = \sum_k \psi_k(\mathbf{r}) \phi_k(\xi)$$

coupled Schroedinger equations for $\psi_k(\mathbf{r})$

Inputs for C.C. calculations

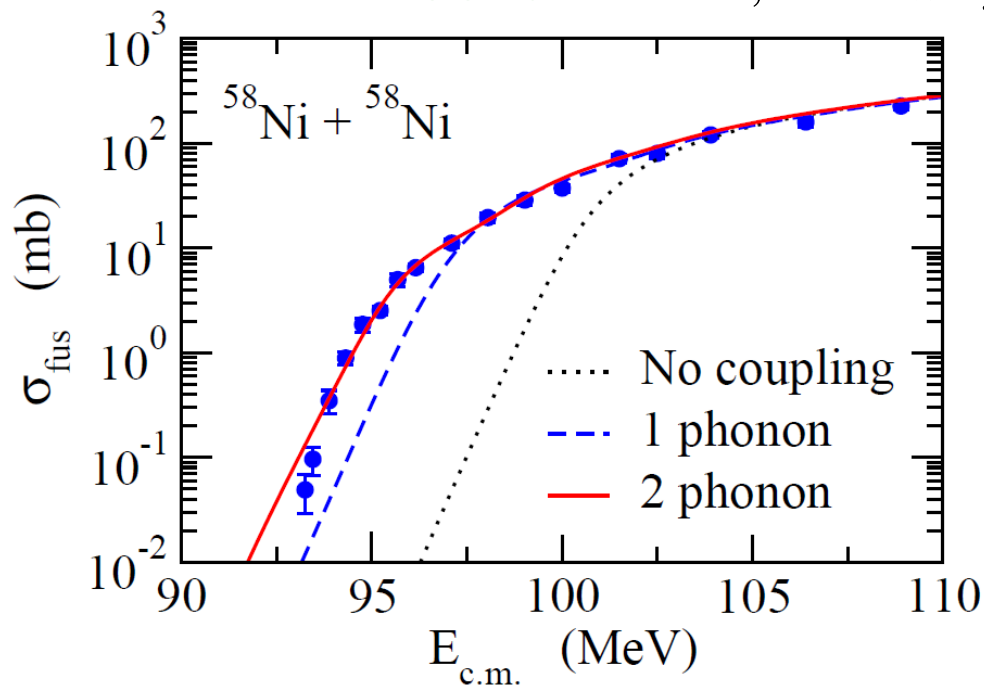
i) Inter-nuclear potential

- ✓ a fit to experimental data at above barrier energies

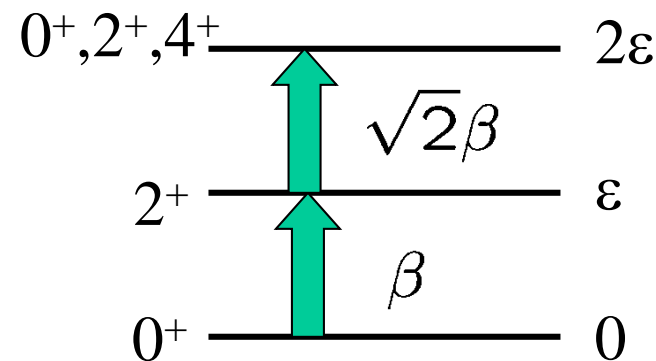
ii) Intrinsic degrees of freedom

- ✓ types of collective motions (rotation / vibration) a/o transfer
- ✓ coupling strengths and excitation energies
- ✓ how many states

CCFULL: K.H., N. Rowley, A.T. Kruppa, CPC123 ('99) 143



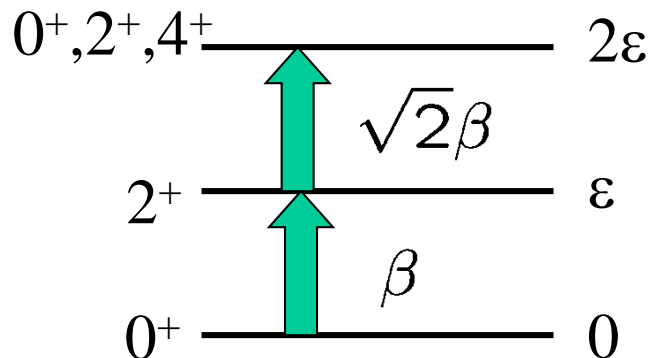
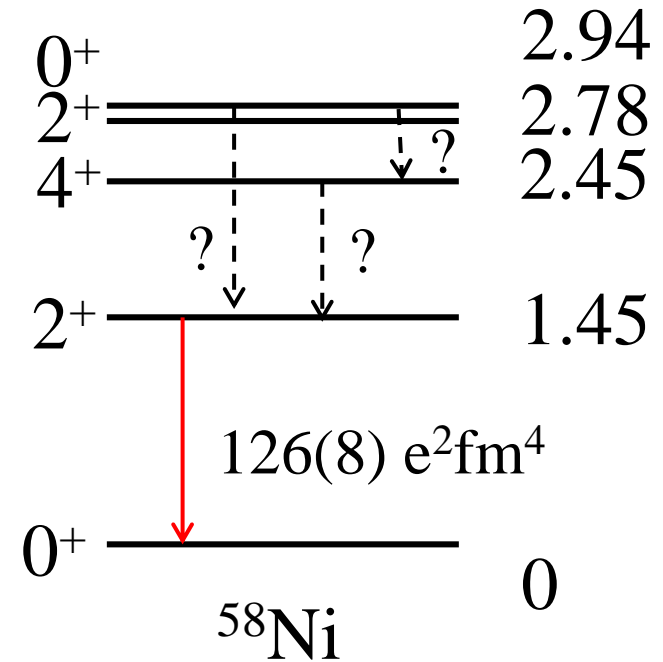
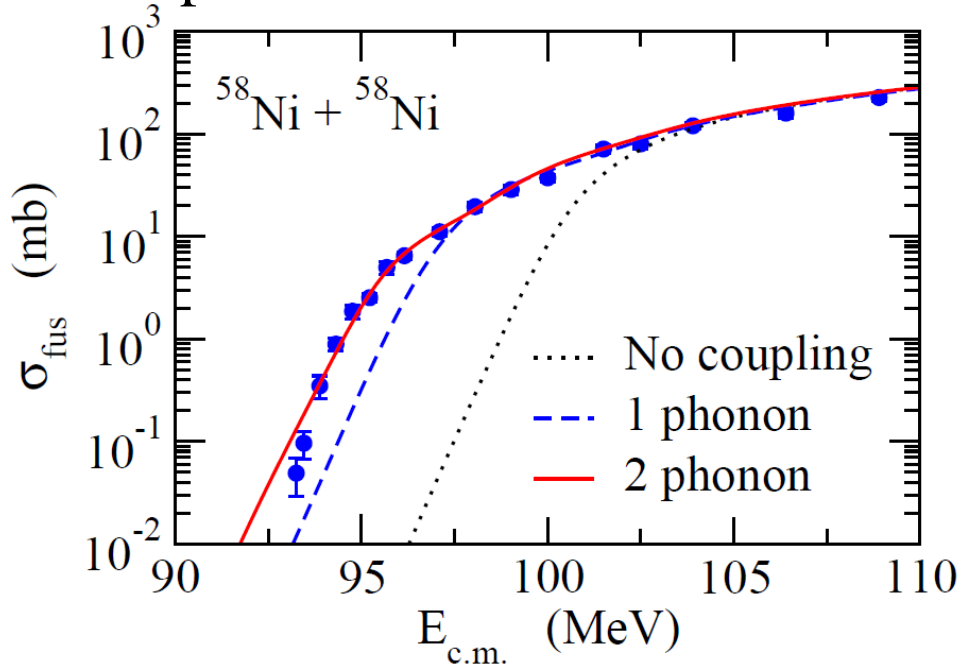
simple harmonic oscillator



Semi-microscopic modeling of sub-barrier fusion

K.H. and J.M. Yao, PRC91('15) 064606

multi-phonon excitations



$$Q(2_1^+) = -10 \pm 6 \text{ efm}^2$$

Simple harmonic oscillator
 → justifiable?

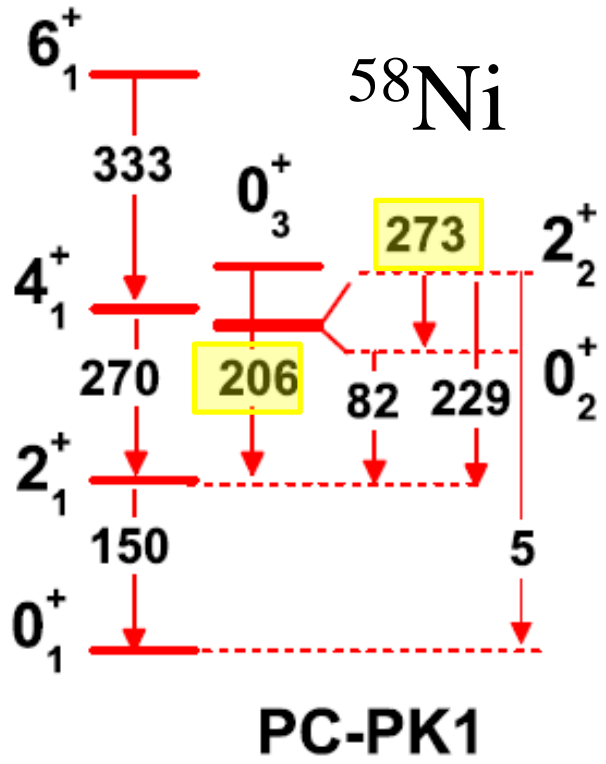
Anharmonic vibrations

- Boson expansion
- Quasi-particle phonon model
- **Shell model**
- Interacting boson model
- **Beyond-mean-field method**

$$|JM\rangle = \int d\beta f_J(\beta) \hat{P}_{M0}^J |\Phi(\beta)\rangle$$

- ✓ **MF + ang. mom. projection**
- + particle number projection
- + **generator coordinate method (GCM)**

M. Bender, P.H. Heenen, P.-G. Reinhard,
 Rev. Mod. Phys. 75 ('03) 121
 J.M. Yao et al., PRC89 ('14) 054306

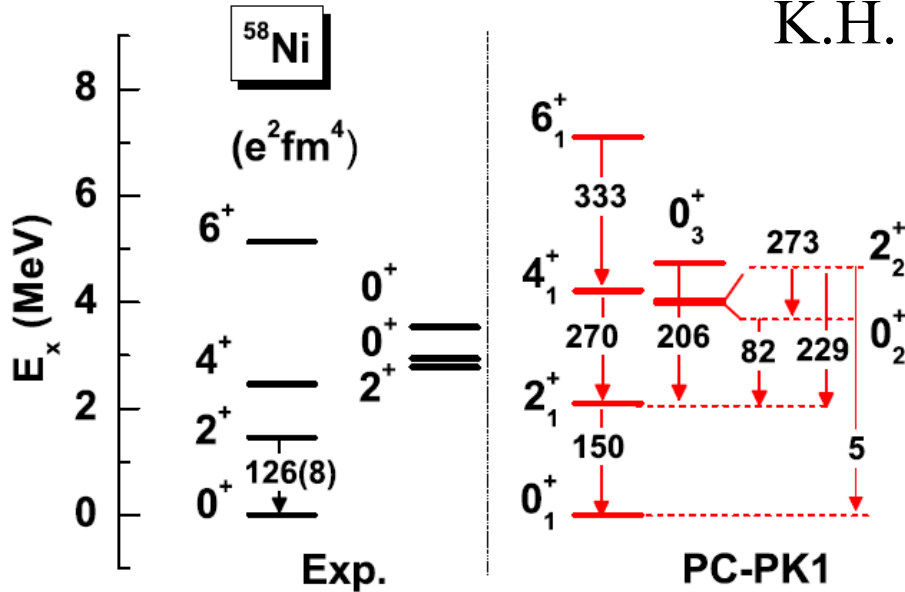


cf. Harmonic limit:
 $B(E2: I_{2ph}^+ \rightarrow 2_1^+)$
 $= 2 \times B(E2: 2_1^+ \rightarrow 0_1^+)$

K.H. and J.M. Yao,
 PRC91('15) 064606

Semi-microscopic coupled-channels model for sub-barrier fusion

K.H. and J.M. Yao, PRC91 ('15) 064606

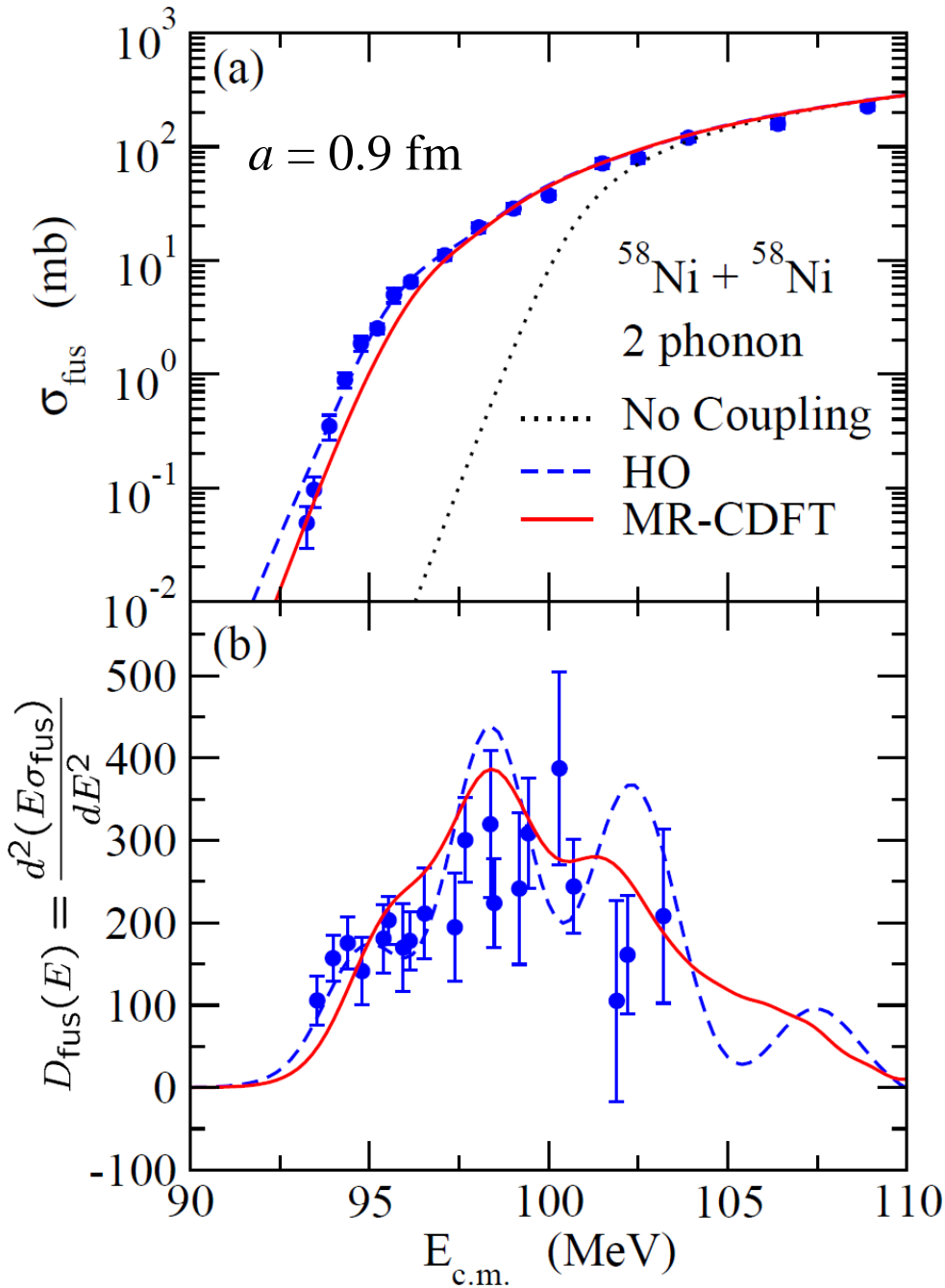


microscopic
multi-pole operator

$$\checkmark \quad V_{\text{coup}} \sim -R_T \frac{dV_N}{dr} \alpha_\lambda \cdot Y_\lambda(\hat{r}) \rightarrow -R_T \frac{dV_N}{dr} Q_\lambda \cdot Y_\lambda(\hat{r})$$

- ✓ $M(E2)$ from MR-DFT calculation ← among higher members of phonon states
- ✓ scale to the empirical $B(E2; 2_1^+ \rightarrow 0_1^+)$
- ✓ still use a phenomenological potential
- ✓ use the experimental values for E_x

* axial symmetry (no 3^+ state)



$^{58}\text{Ni} + ^{58}\text{Ni}$

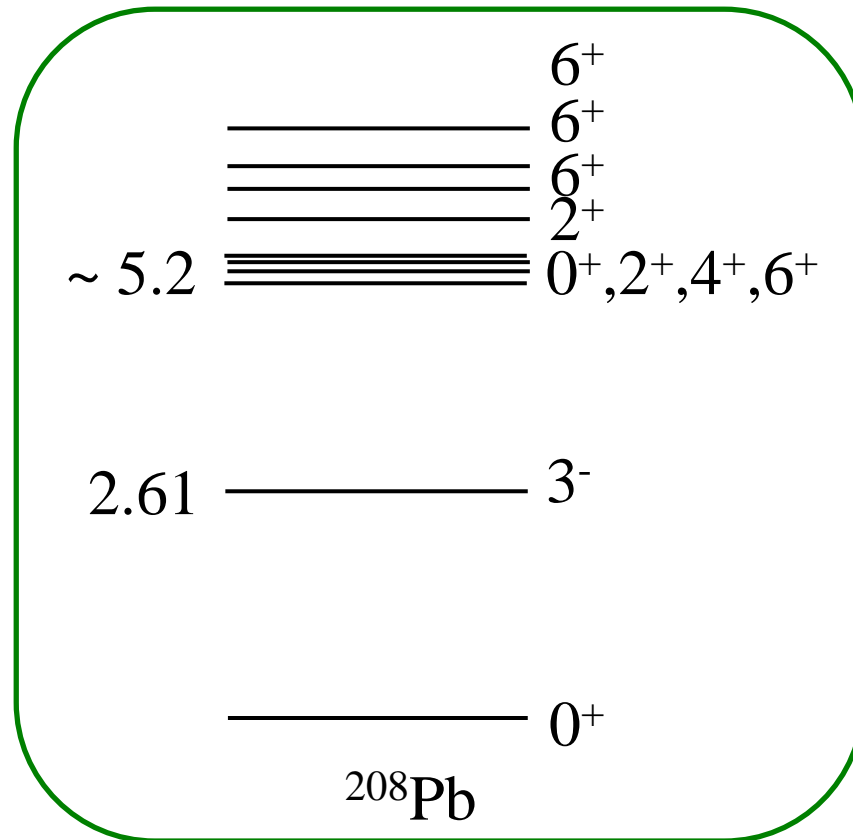
anharmonicity of 2^+ phonon
 \rightarrow only a minor improvement



Next, more non-trivial case
 with $2^+ - 3^-$ coupling:
 anharmonicity of oct. vib.
 in ^{208}Pb

Application to $^{16}\text{O} + ^{208}\text{Pb}$ fusion reaction

double-octupole phonon states in ^{208}Pb



M. Yeh, M. Kadi, P.E. Garrett et al., PRC57 ('98) R2085

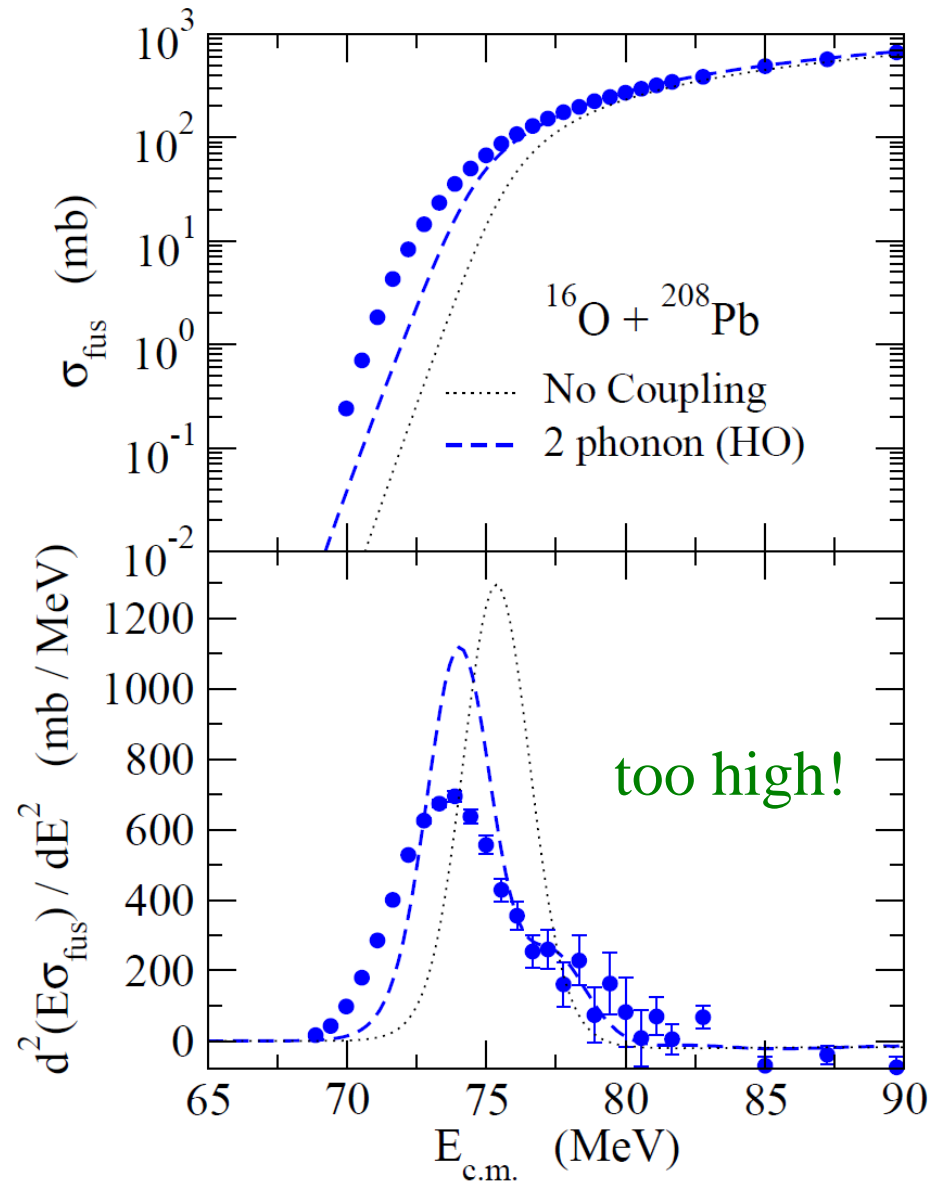
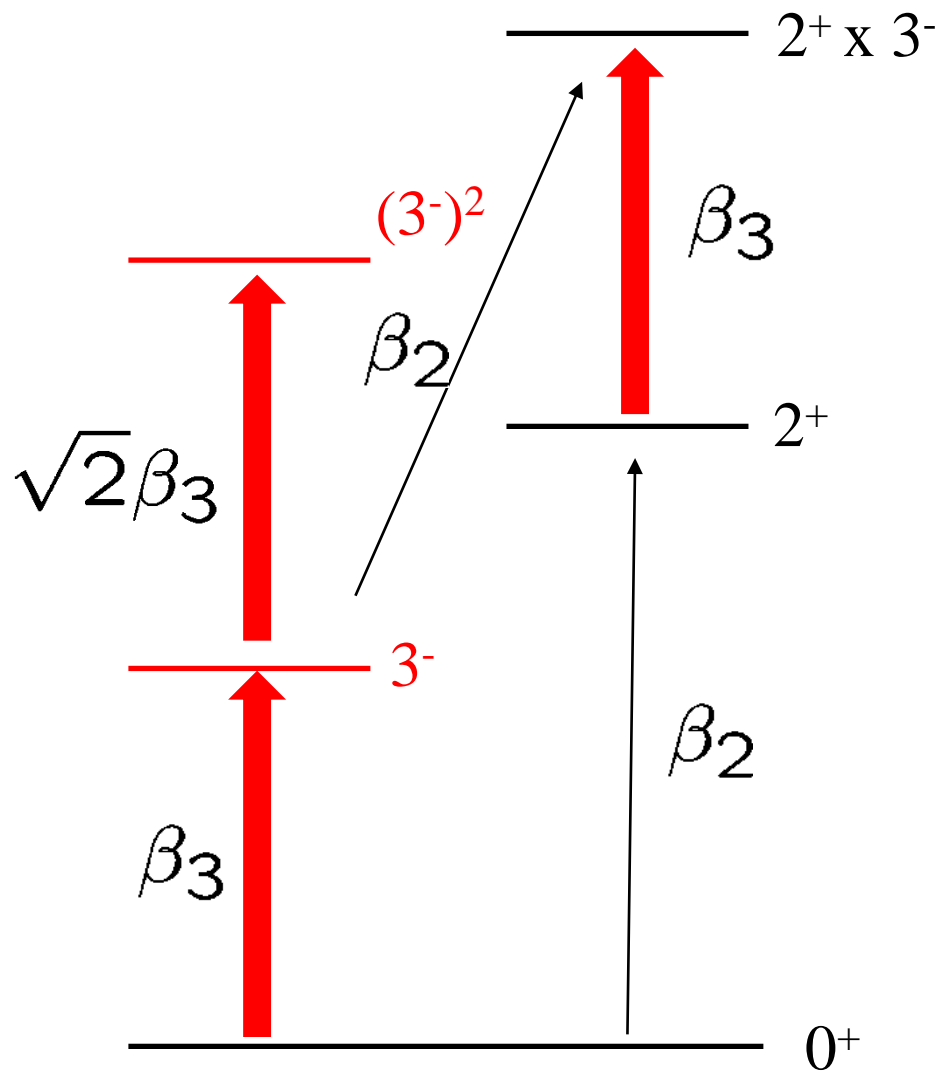
K. Vetter, A.O. Macchiavelli et al., PRC58 ('98) R2631

V. Yu. Pnomarev and P. von Neumann-Cosel, PRL82 ('99) 501

B.A. Brown, PRL85 ('00) 5300

large fragmentations, especially 6^+ state

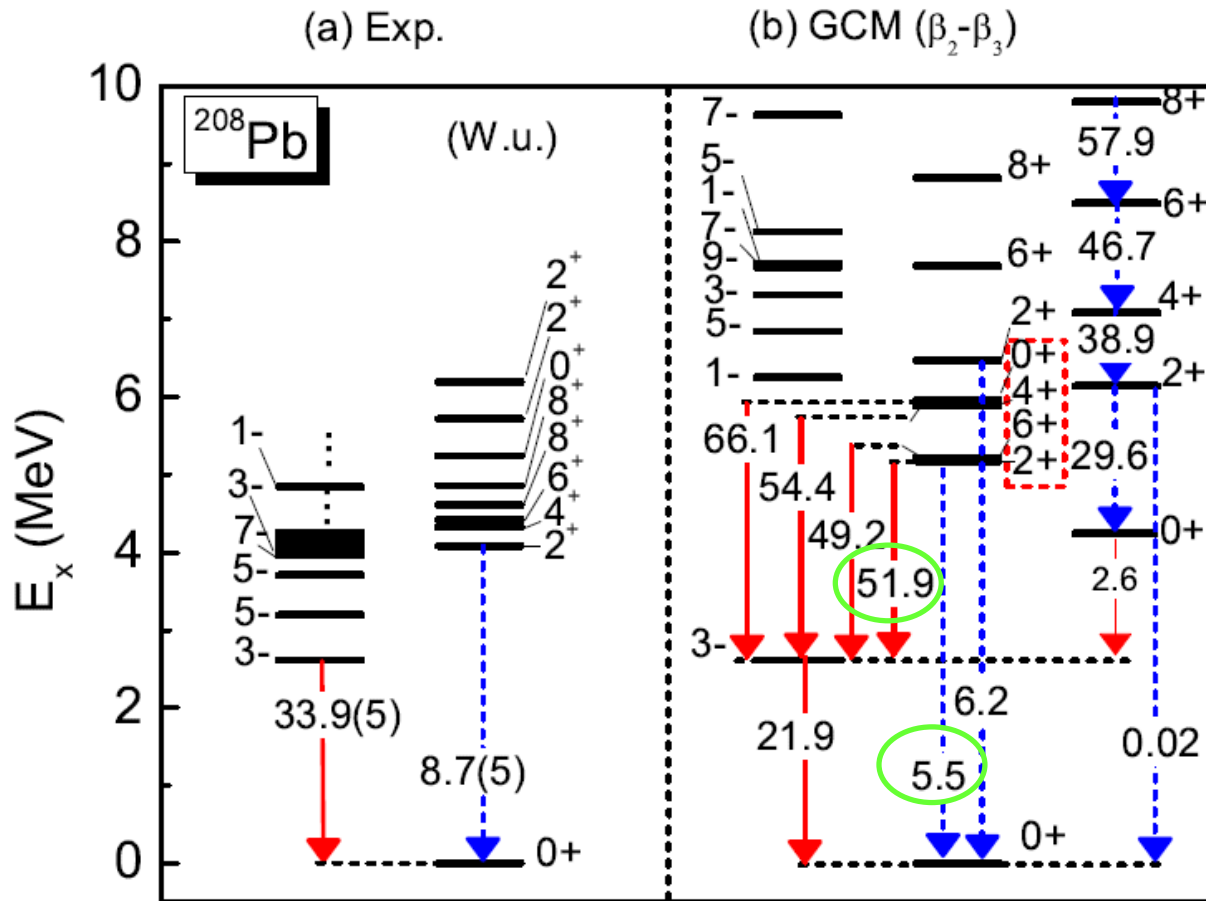
Application to $^{16}\text{O} + ^{208}\text{Pb}$ fusion reaction



cf. C.R. Morton et al., PRC60('99) 044608

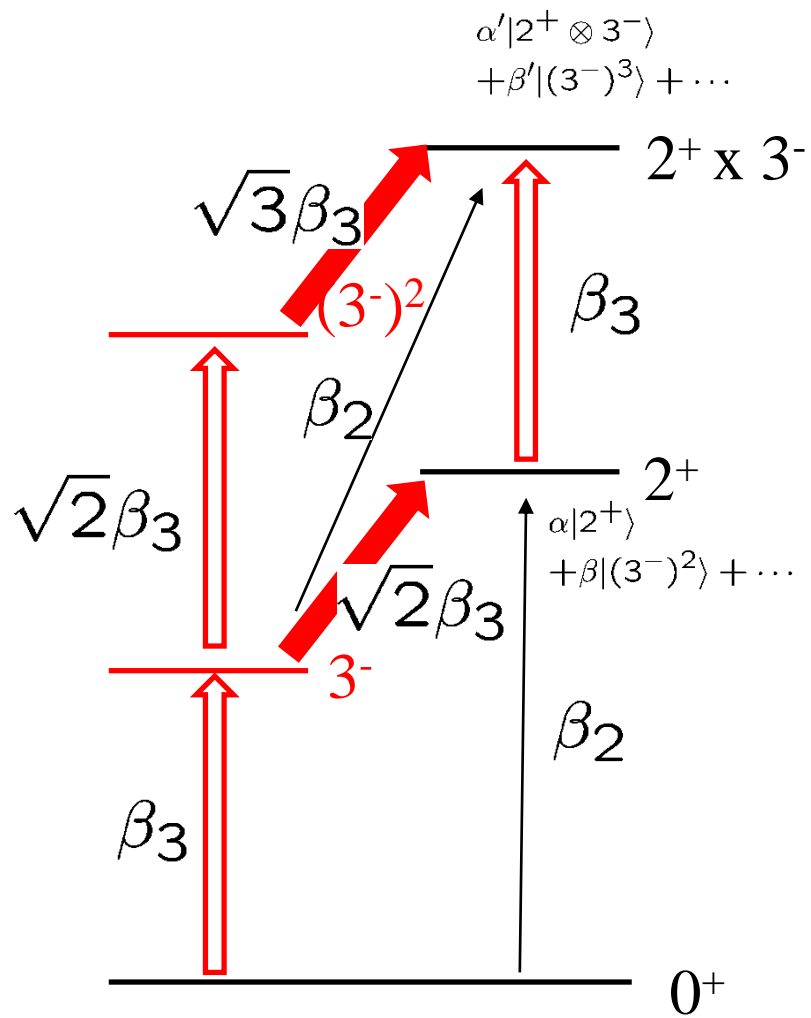
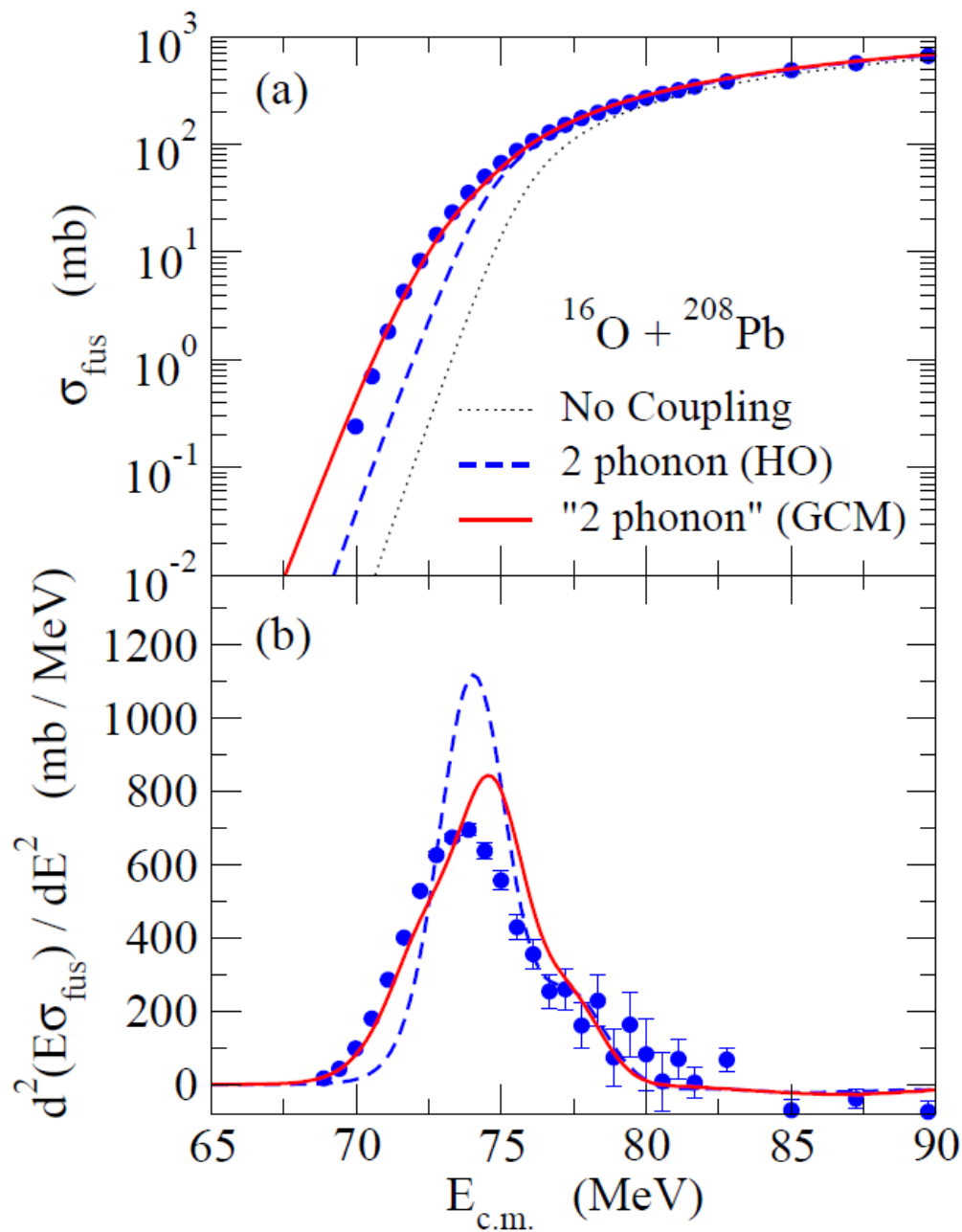
fluctuation both
in β_3 and β_2

expt. data



2_1^+ state: strong coupling both to g.s. and 3_1^-

$$\longrightarrow |2_1^+\rangle = \alpha|2^+\rangle_{\text{HO}} + \beta|[3^- \otimes 3^-]^{(I=2)}\rangle_{\text{HO}} + \dots$$



J.M. Yao and K.H.,
PRC94 ('16) 11303(R)

From phenomenological approach to microscopic approach

Macroscopic (phenomenological)

C.C. with collective model

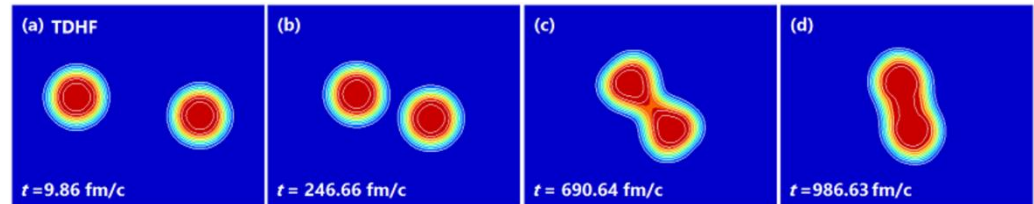
C.C. with inputs from
microscopic nuclear
structure calculations

C.C. with inputs based
on TDHF

TDHF simulations

Microscopic

TDHF = Time Dependent Hartree-Fock



S. Ebata, T. Nakatsukasa, JPC Conf. Proc. 6 ('15)

ab initio, but no tunneling

Time-dependent GCM for many-body tunneling

N. Hasegawa, K.H., and Y. Tanimura, in preparation

TDHF simulations

ab initio, but no tunneling

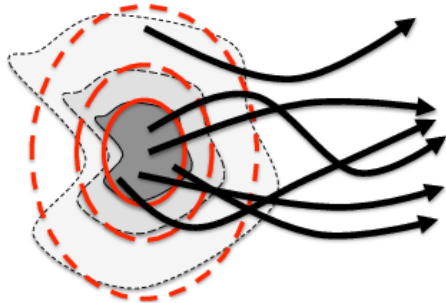


need to go Beyond the mean-field app.

✓ Time-dependent GCM

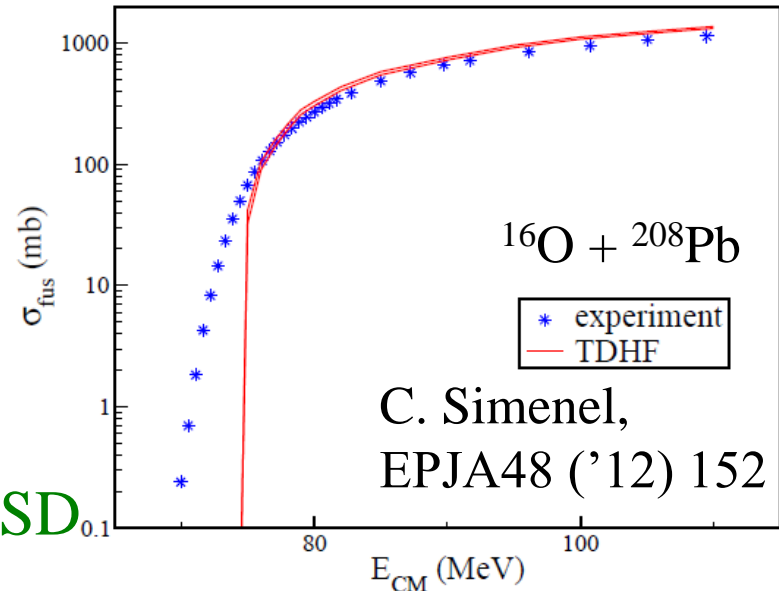
a single Slater determinant (SD) to multi-SD

$$|\Psi(t)\rangle = \int dq f(q, t) |\Phi_q(t)\rangle$$



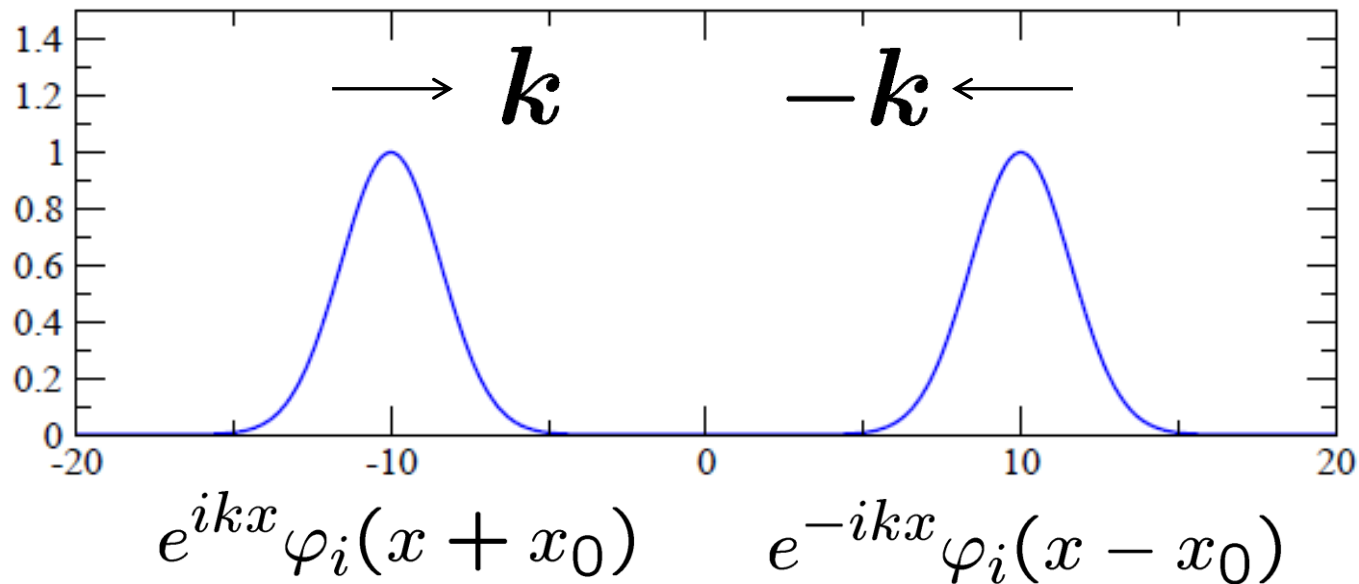
dynamics with a superposition of many
“TDHF trajectories (Slater determinants)”

cf. Stochastic mean-field method
B. Yilmaz et al.,
PRC90 ('14) 054617

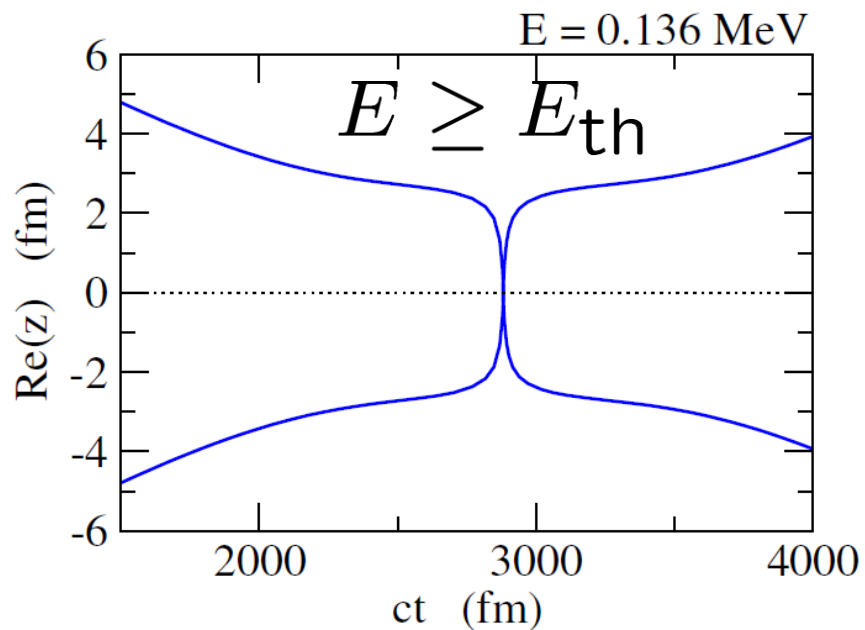
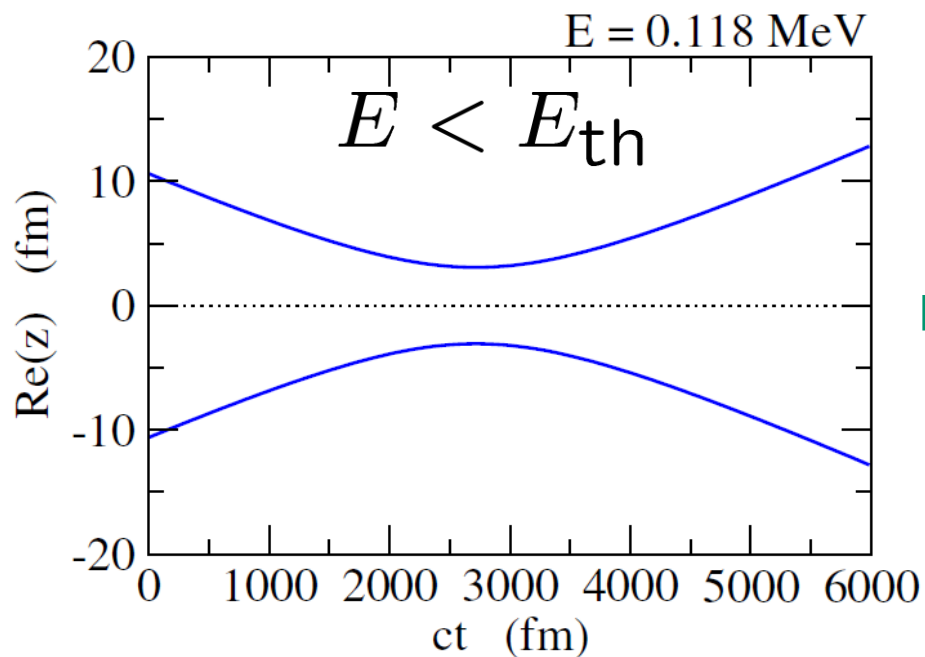


TDHF

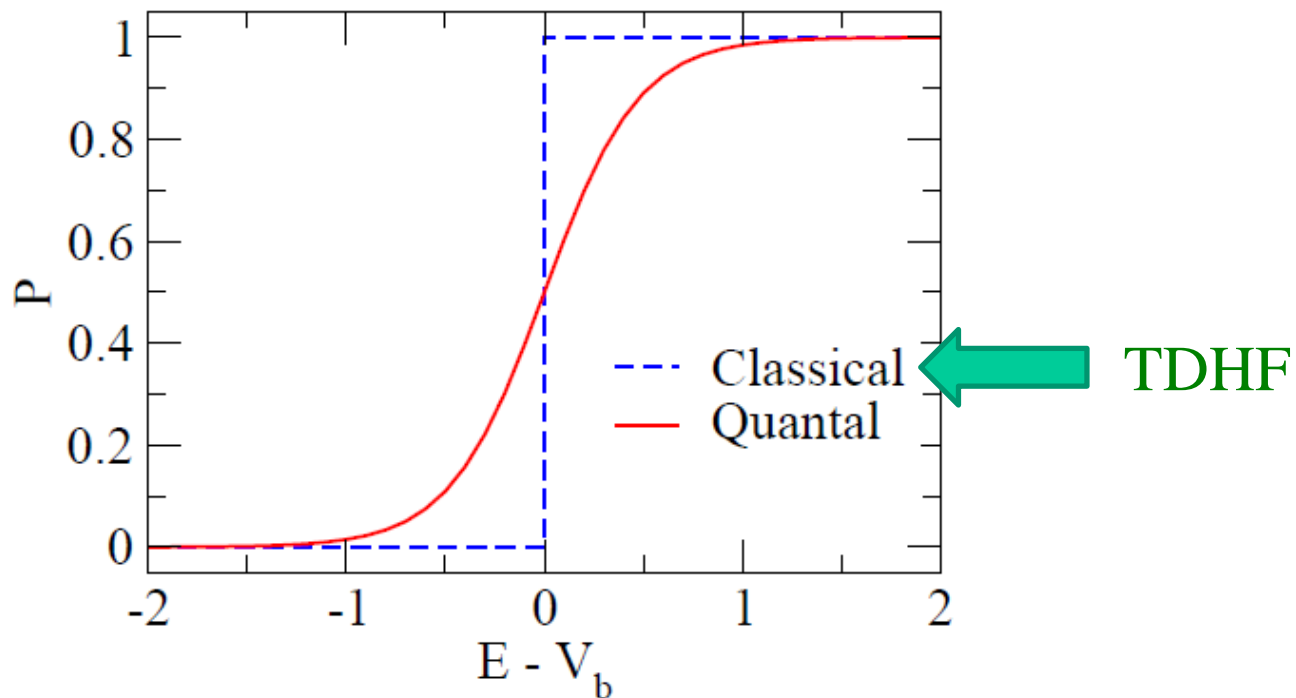
$$\Psi(t) = \Phi_{SD}(t)$$



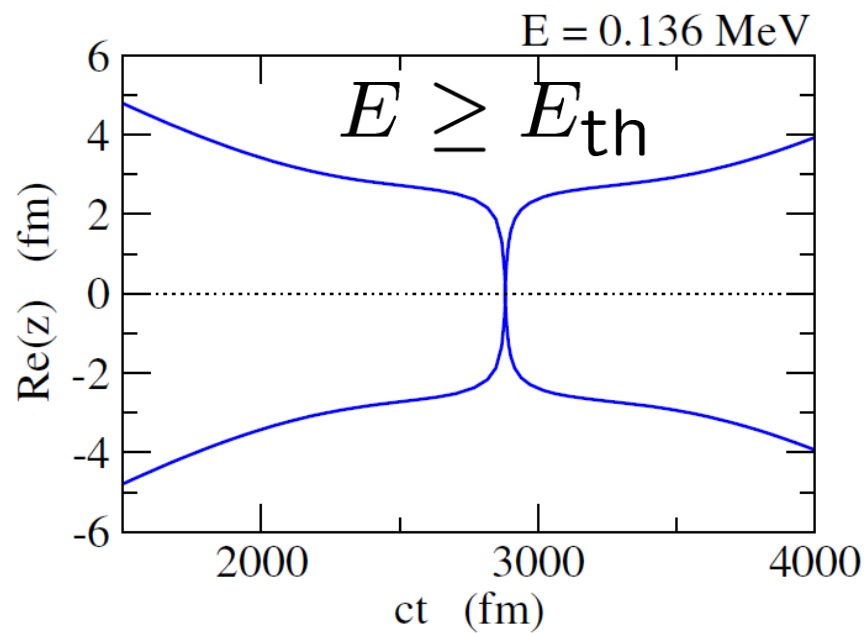
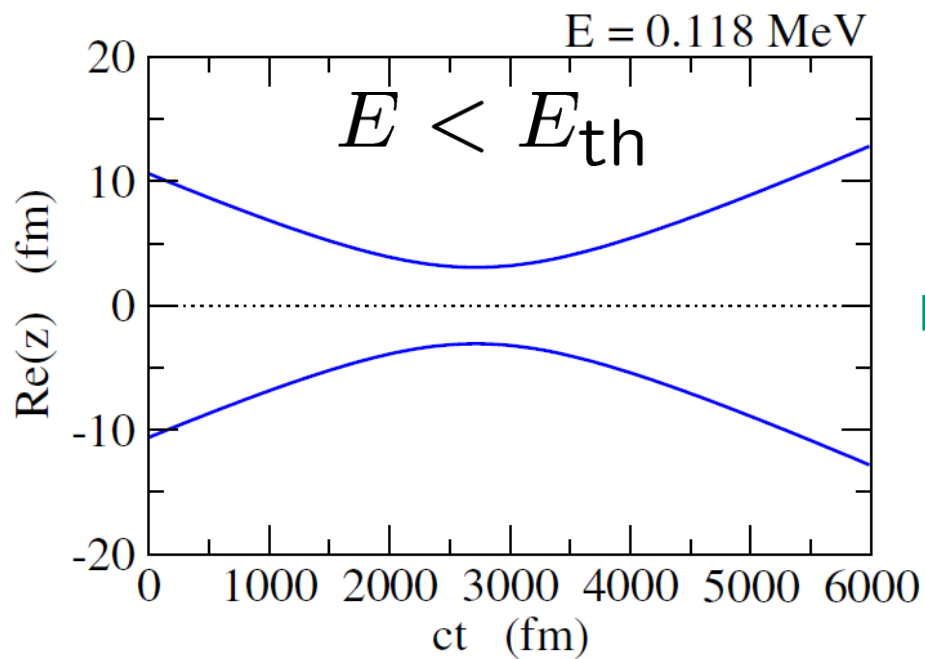
$\alpha + \alpha$ in 1D

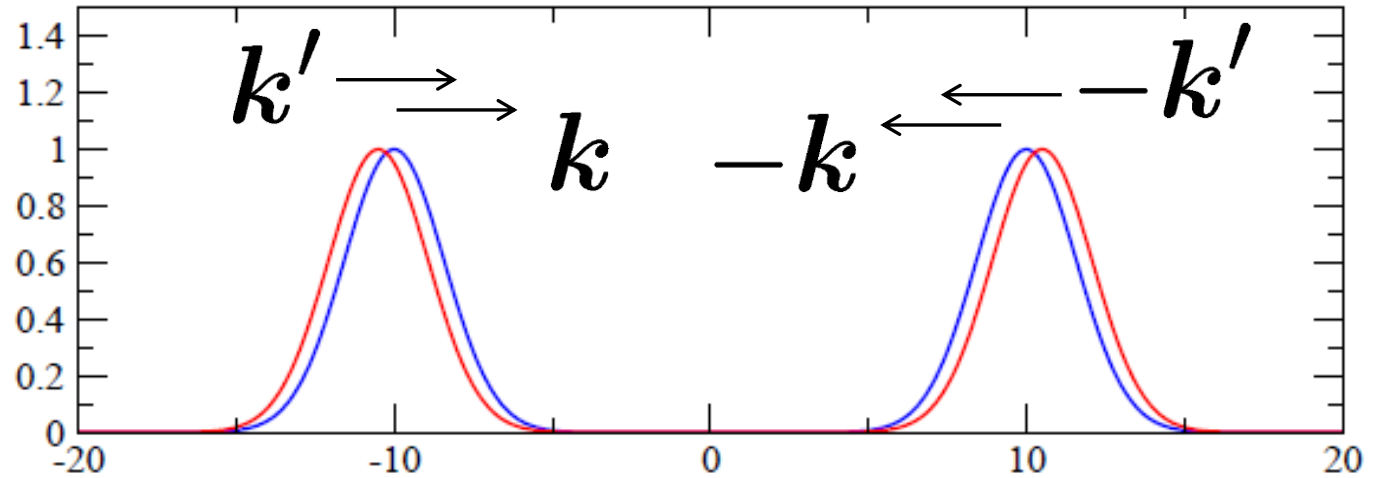


TDHF



$\alpha + \alpha$ in 1D



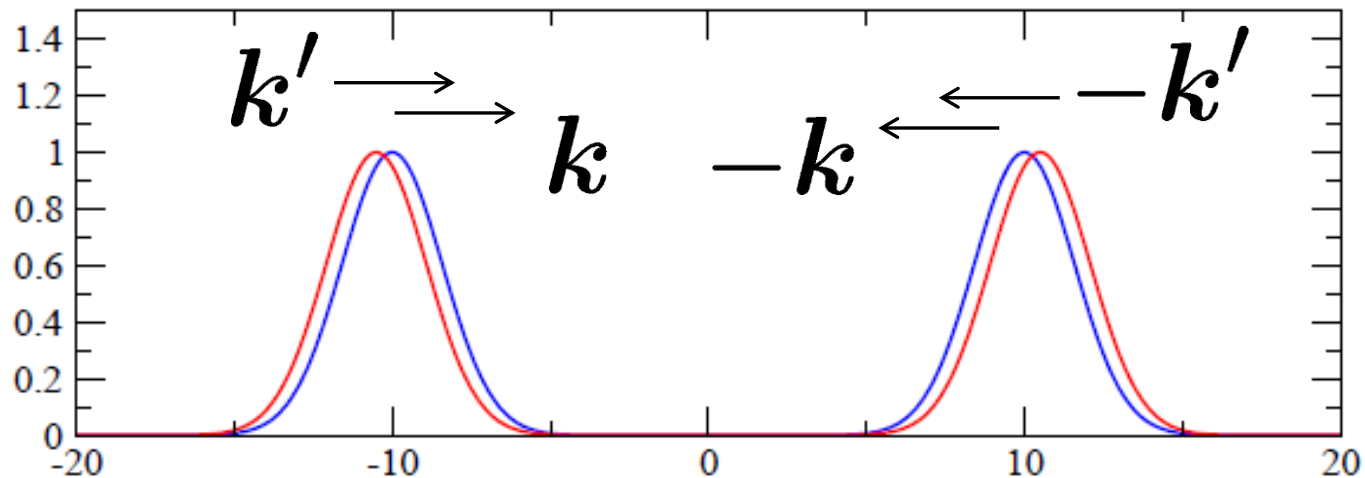


$$\Psi(t) = \sum_k \underbrace{f_k(t)}_{\text{time-dep.}} \underbrace{\Phi_{\text{SD},k}(t)}_{\text{variational principle}}$$

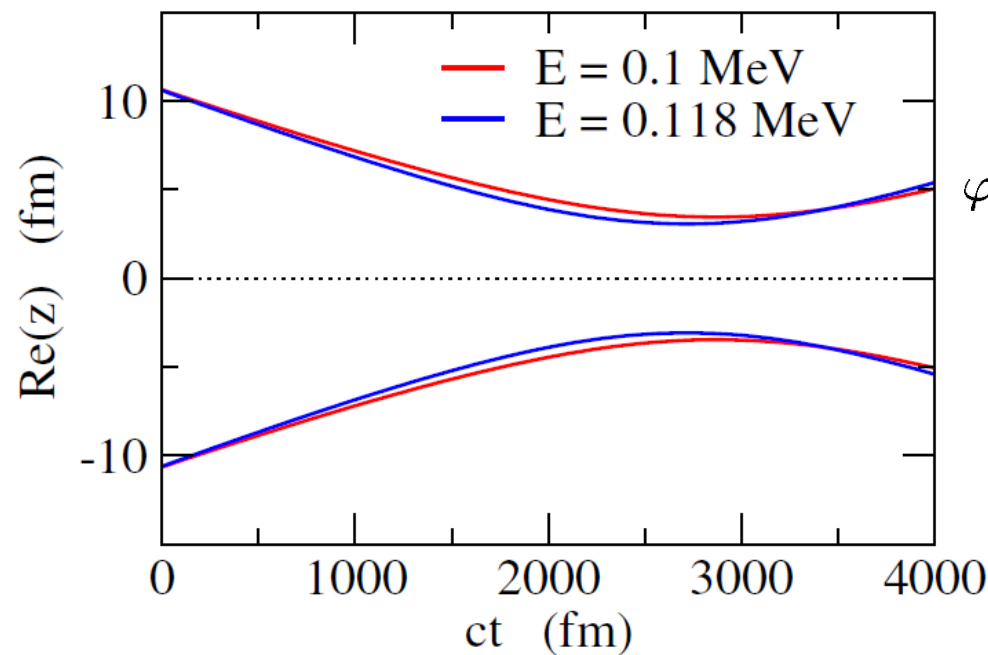
time-dep. variational principle

$$\delta \int dt \frac{\langle \Psi(t) | i\hbar \partial_t - H | \Psi(t) \rangle}{\langle \Psi(t) | \Psi(t) \rangle} = 0$$

TDGCM



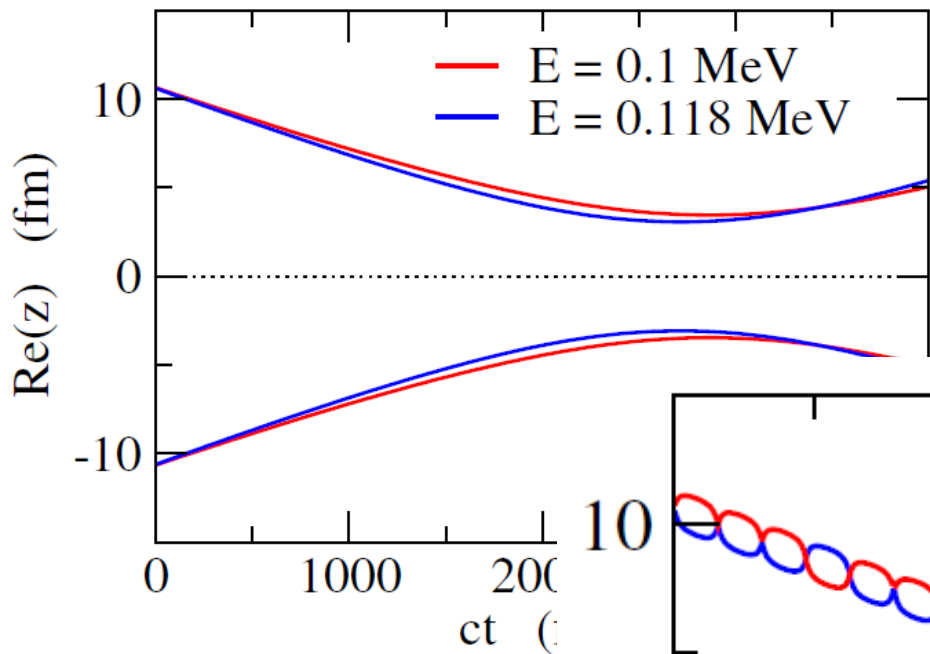
$\alpha + \alpha$ in 1D

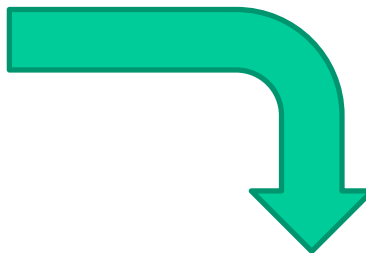


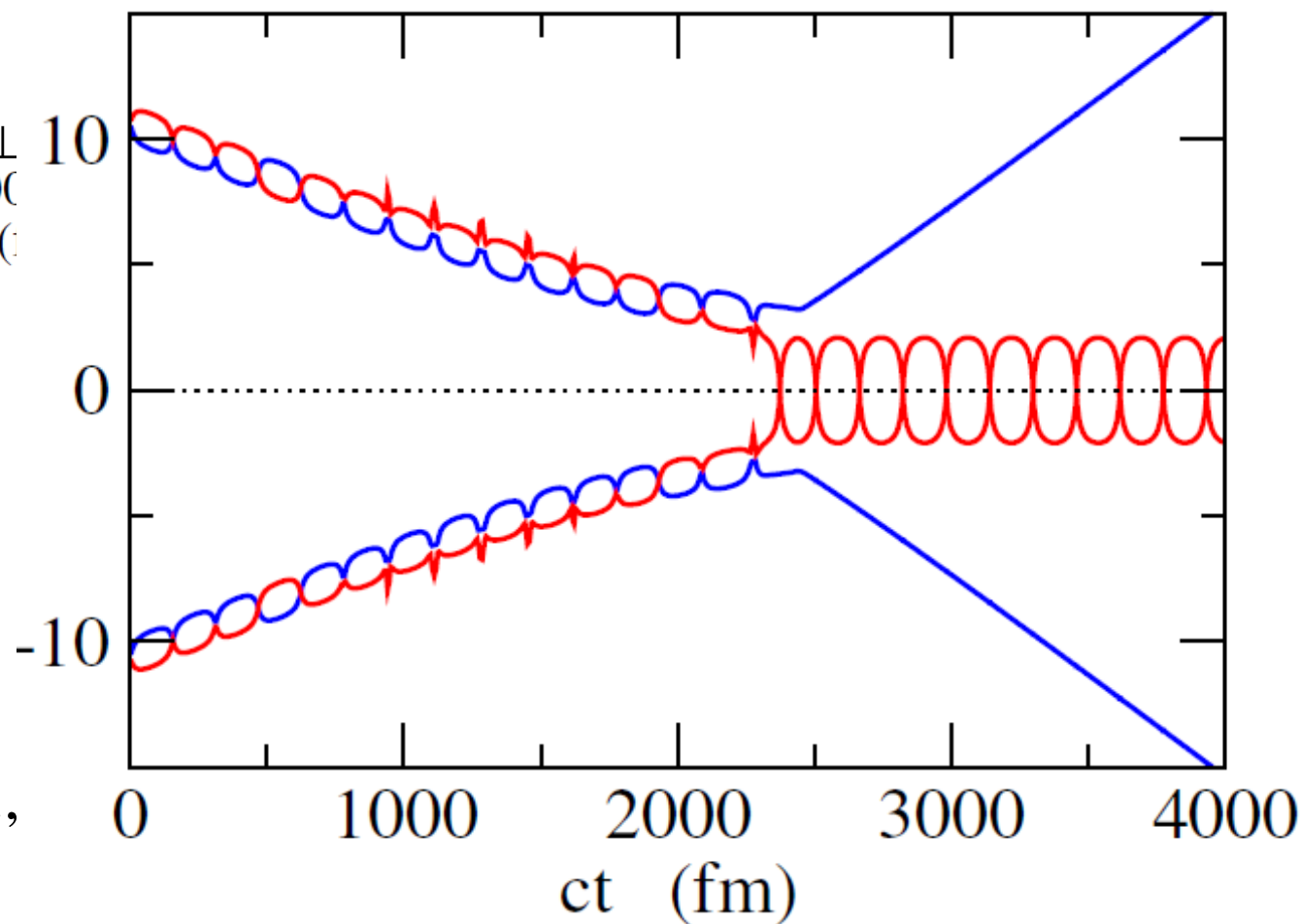
a simplification:

$$\varphi_i^{(k)}(x, t) \sim \exp \left[-\nu \left(x - \frac{Z_i^{(k)}(t)}{\sqrt{\nu}} \right)^2 \right]$$

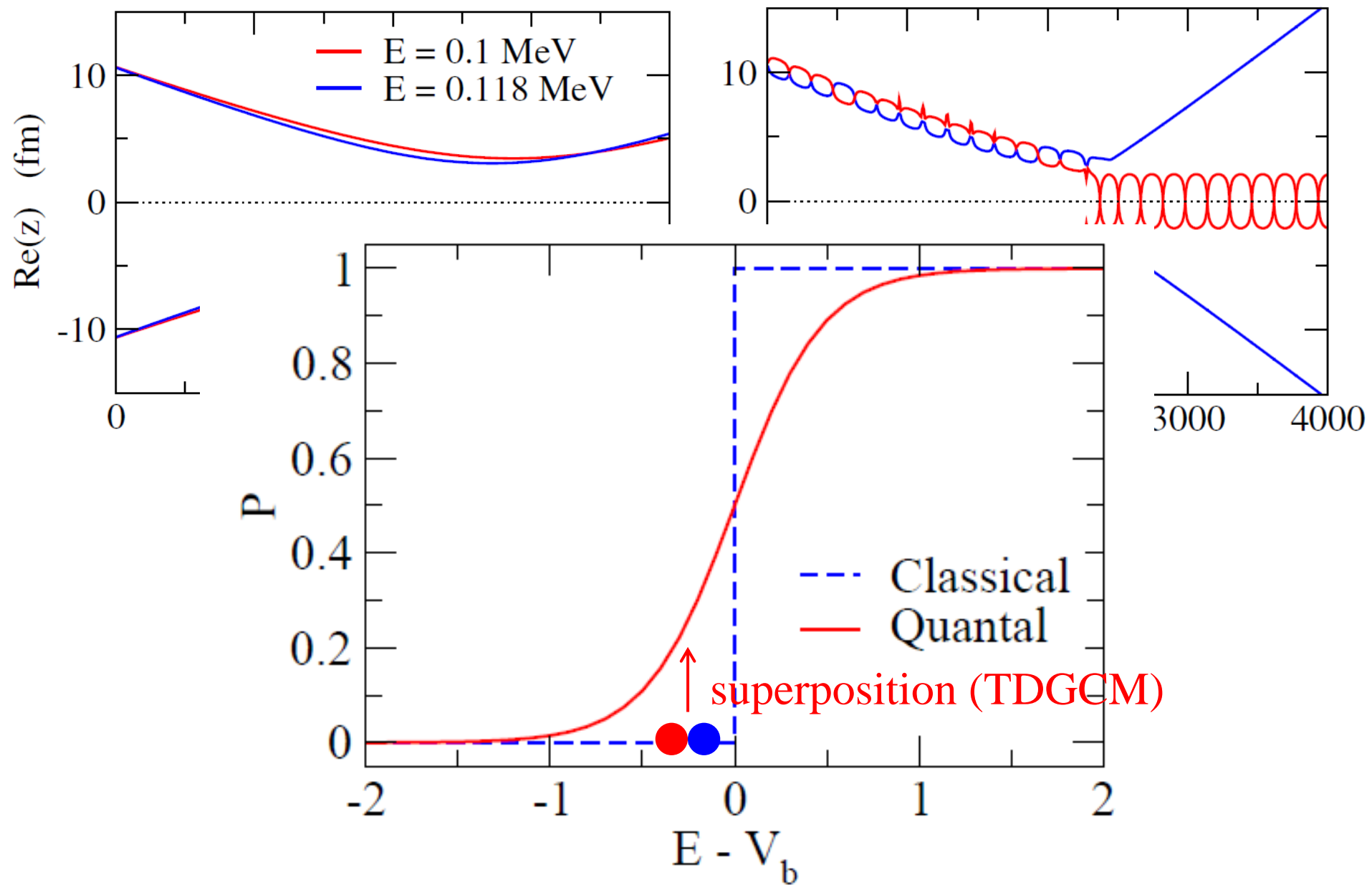
$$\Phi_{SD,k}(t) = \mathcal{A} \left[\{ \varphi_i^{(k)}(x, t) \} \right]$$



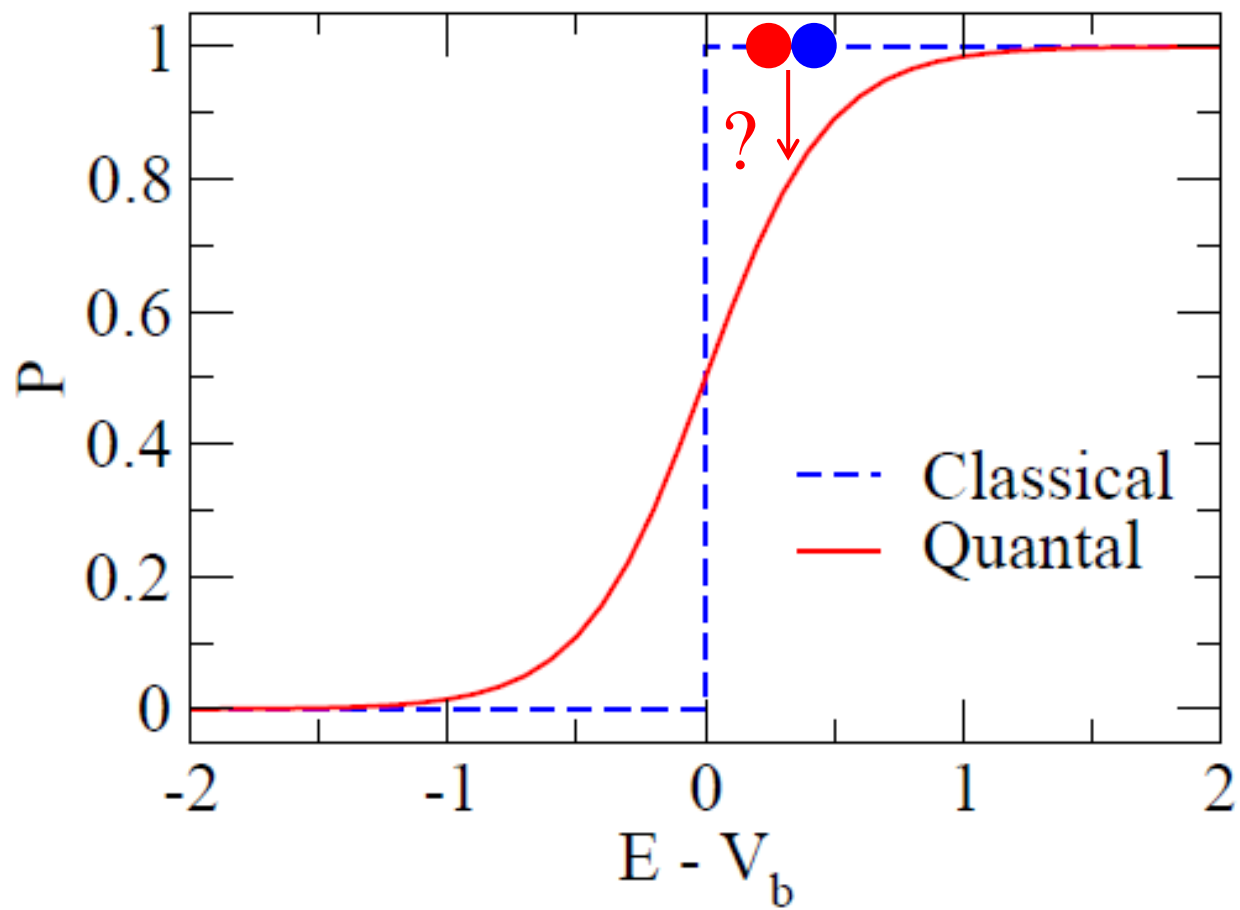

TDGCM
 (a superposition
 of two SD)

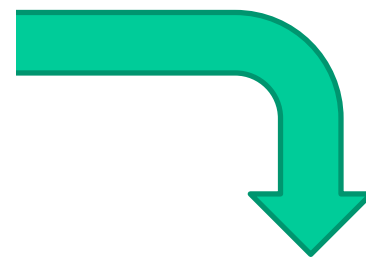
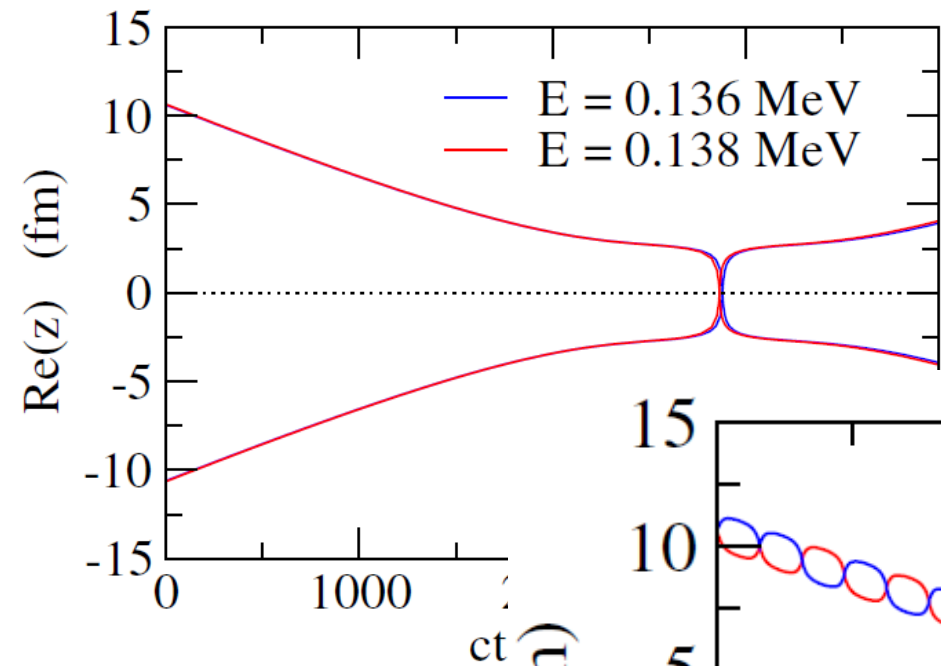


N. Hasegawa, K.H.,
 and Y. Tanimura,
 in preparation

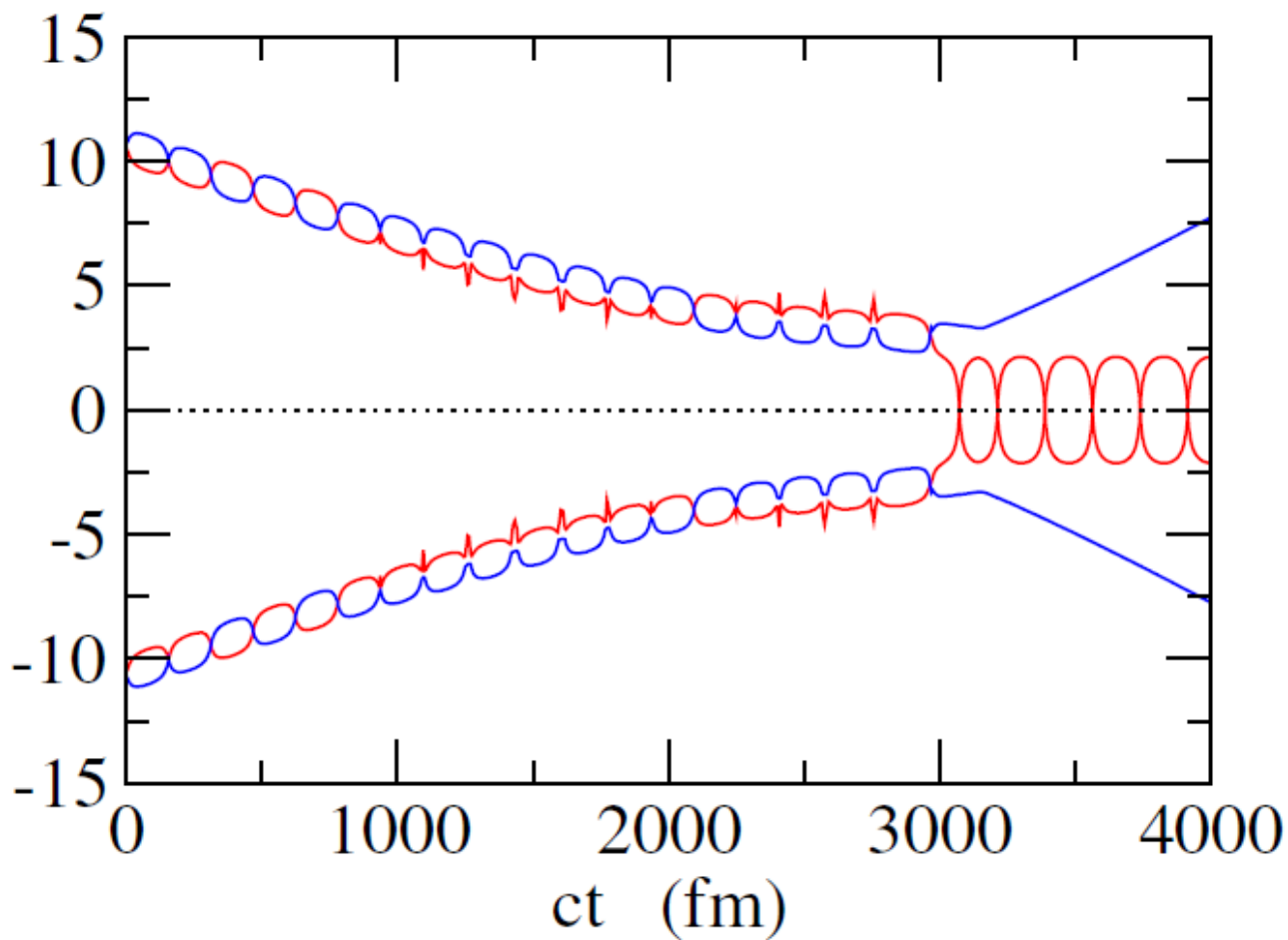


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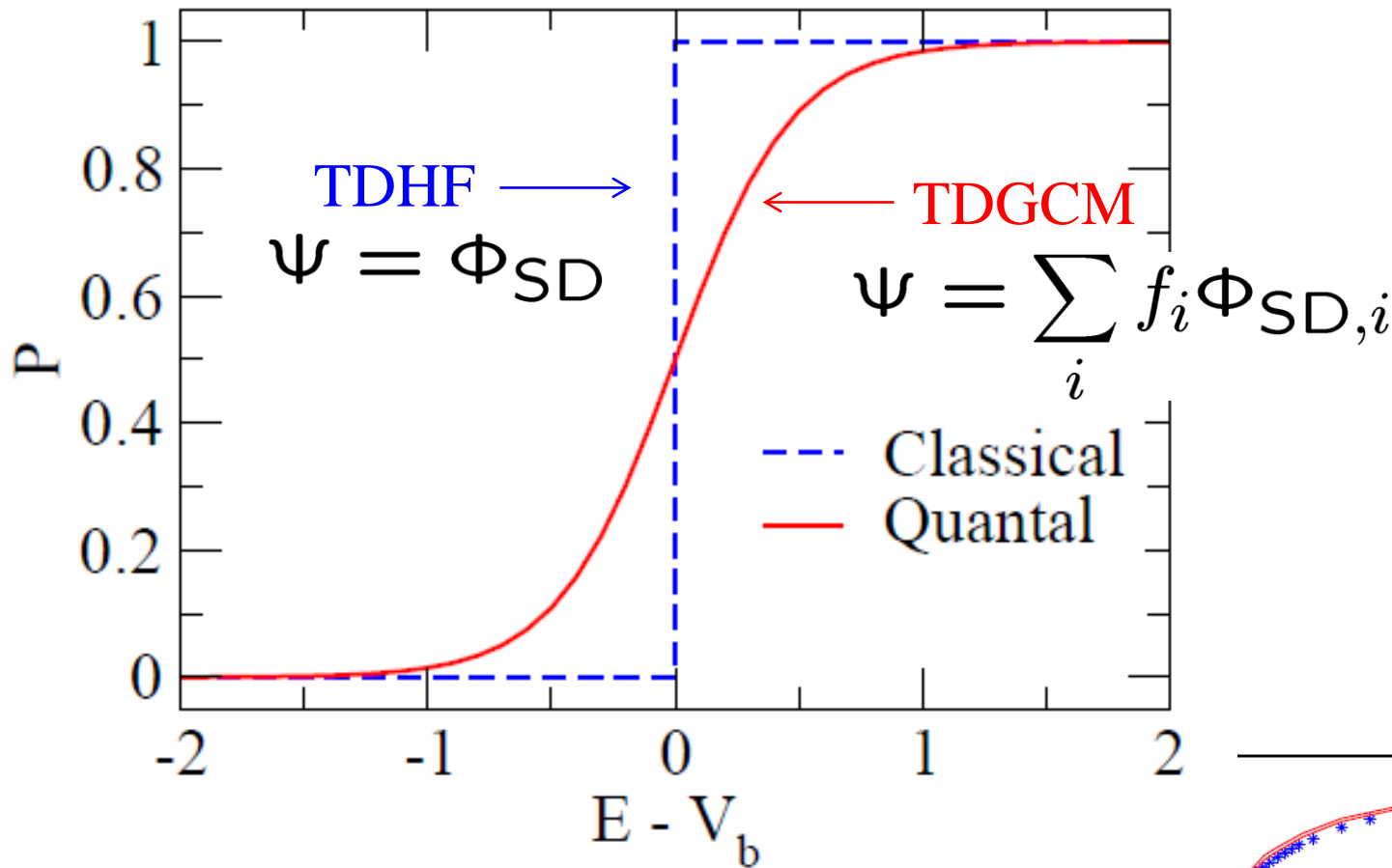




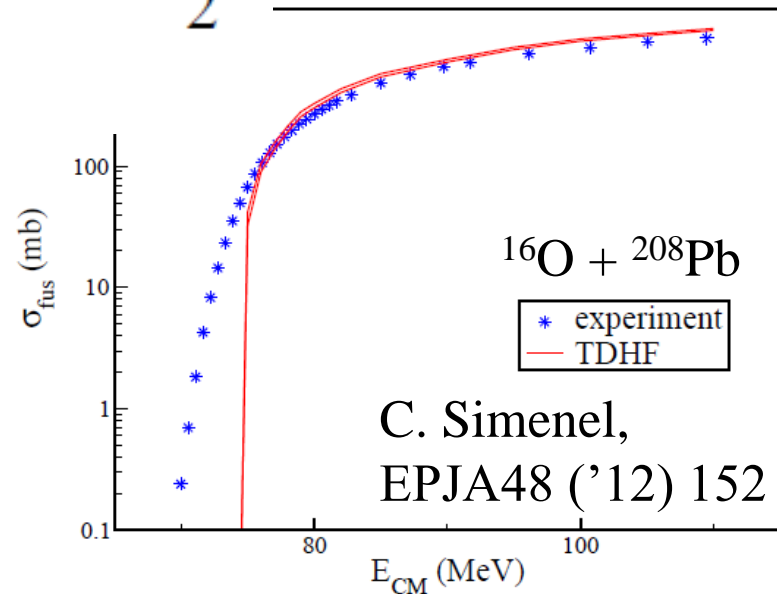
TDGCM
 (a superposition
 of two SD)



N. Hasegawa, K.H.,
 and Y. Tanimura,
 in preparation

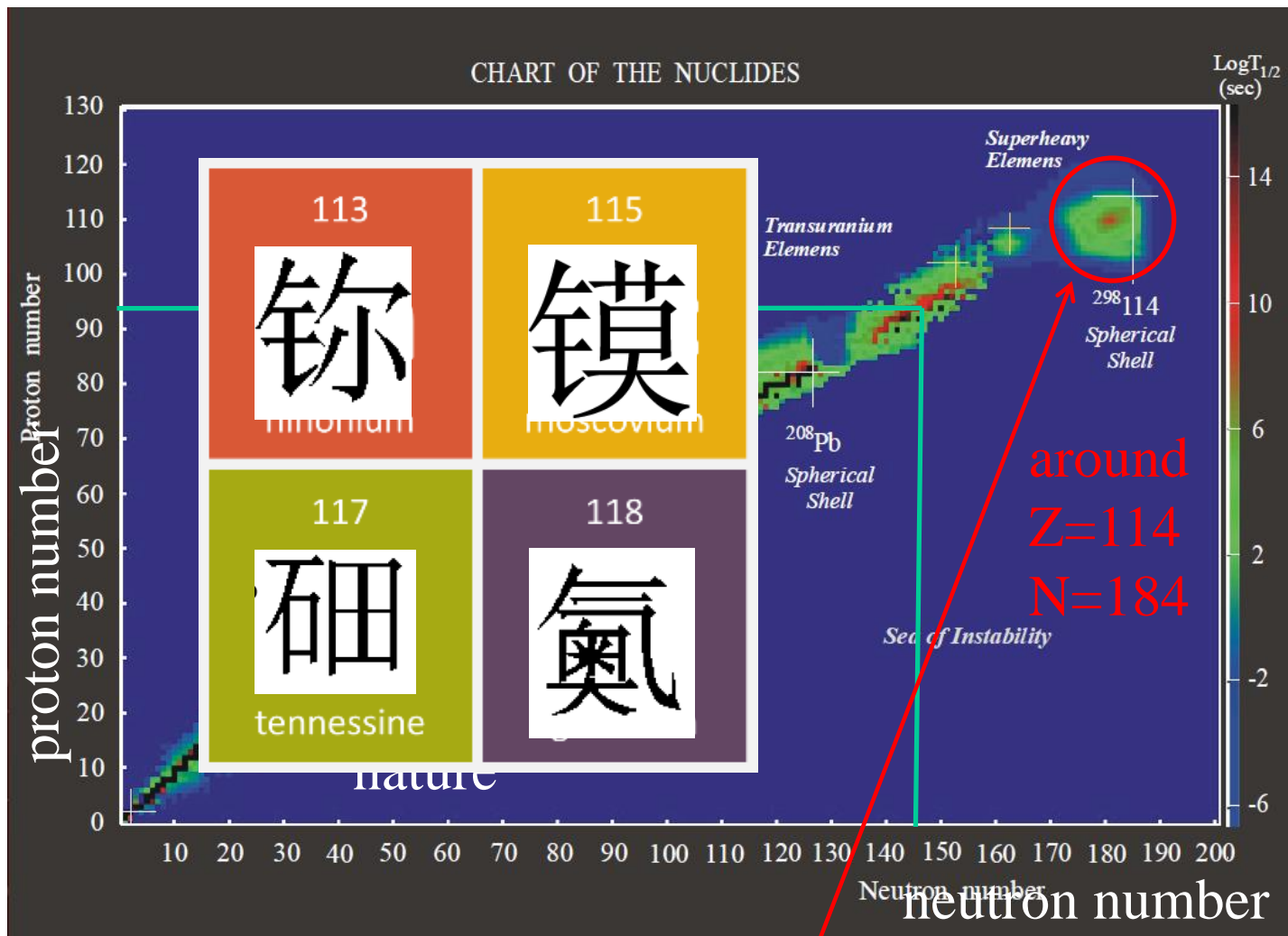


TDGCM:
 a promising microscopic theory
 for many-body tunneling



Fusion for superheavy elements

超重元素

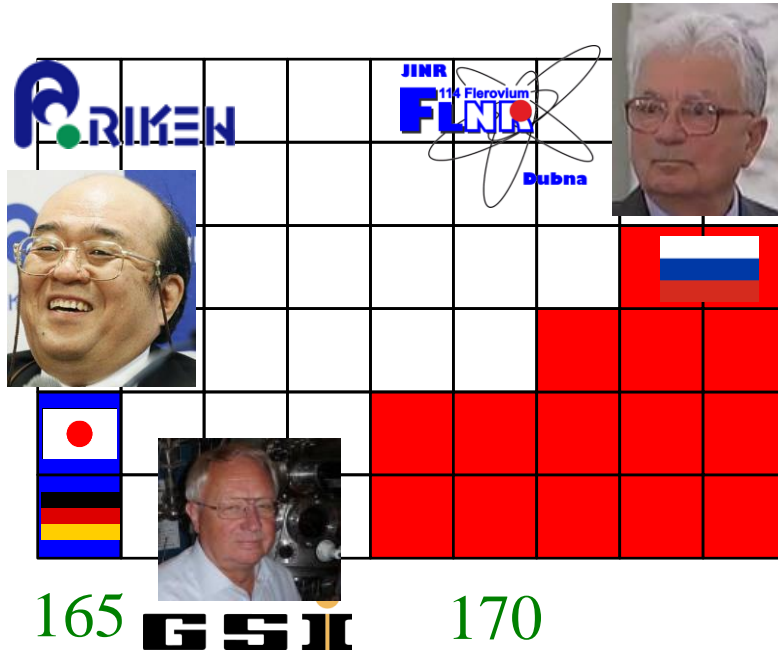


a prediction of island of stability
(Swiatecki et al., 1966)

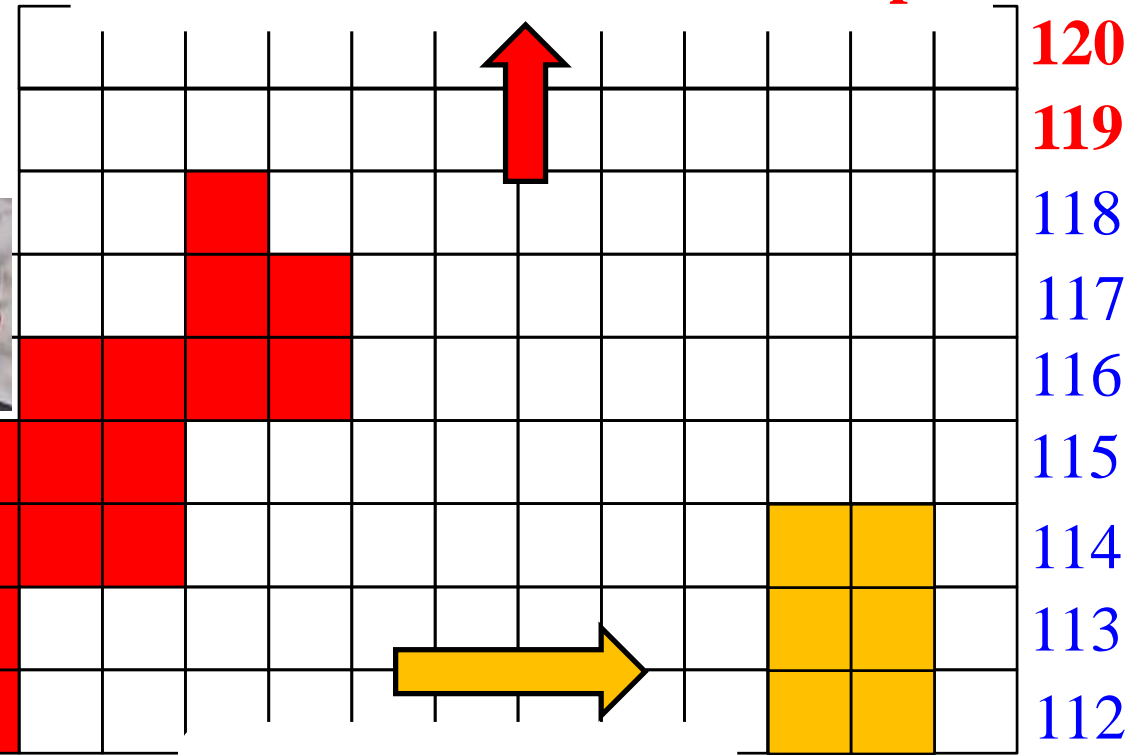
Yuri Oganessian

Future directions of SHE

Superheavy elements synthesized so far



Towards Z=119 and 120 isotopes



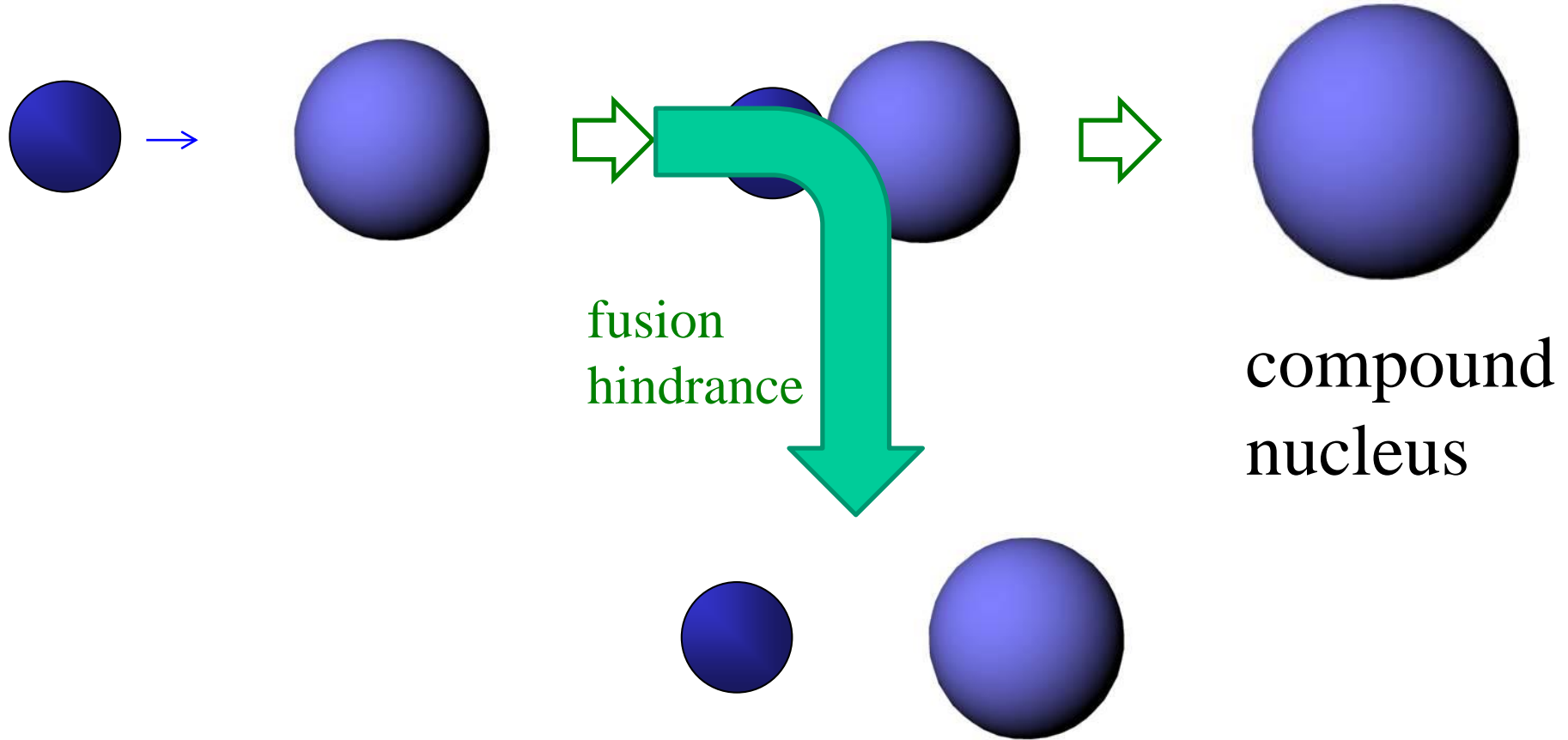
➤ Towards Z=119 and 120 isotopes

Hot fusion reactions with ^{48}Ca , $^{50}_{22}\text{Ti}$, $^{51}_{23}\text{V}$, $^{54}_{24}\text{Cr}$ etc.

➤ Towards the island of stability

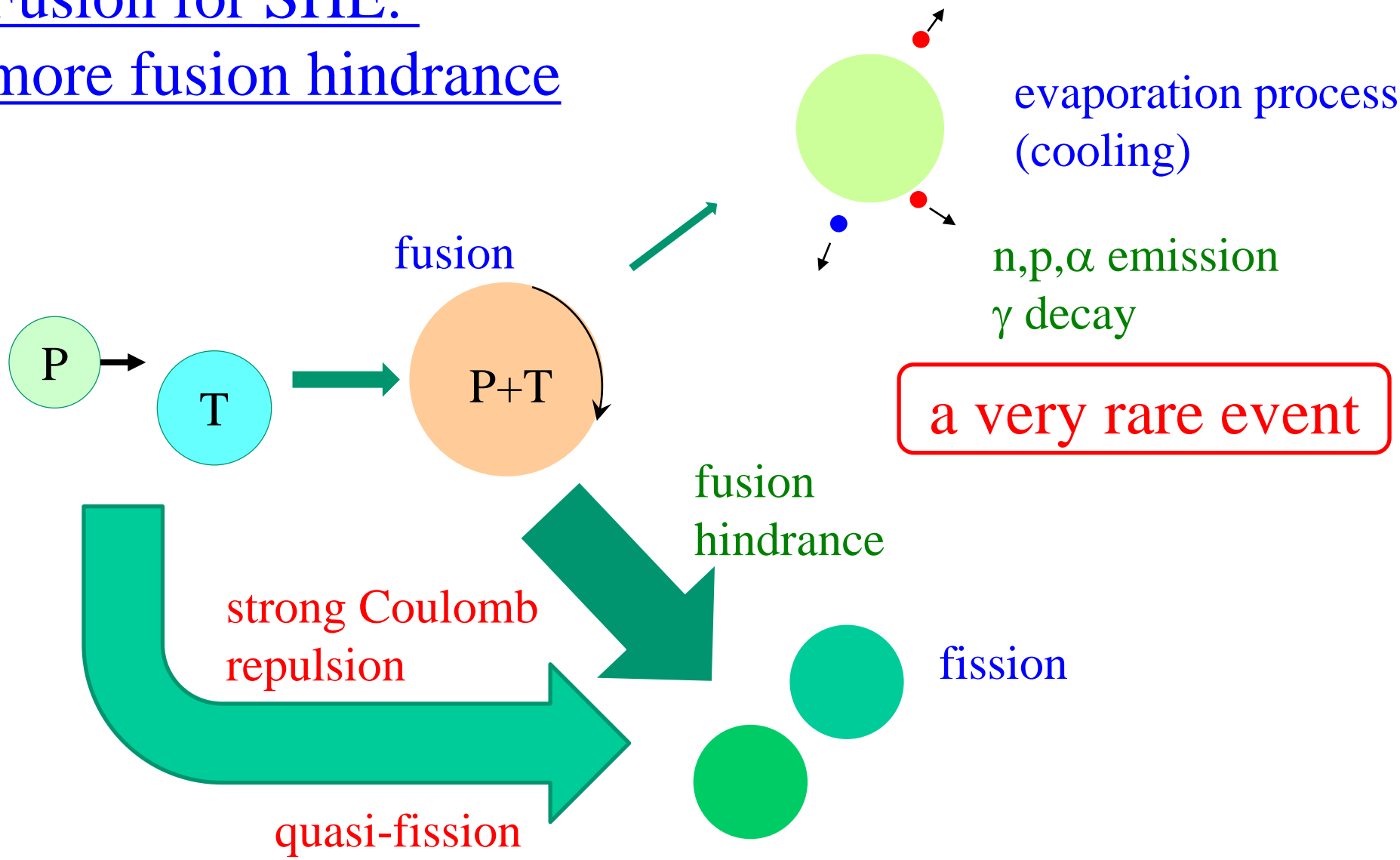
neutron-rich beams: indispensable → reaction dynamics?

Fusion for SHE: fusion hindrance



strong Coulomb repulsion
→ re-separation

Fusion for SHE:
more fusion hindrance



Theoretical challenges

formation of SHE: very rare

→ a large theoretical uncertainty

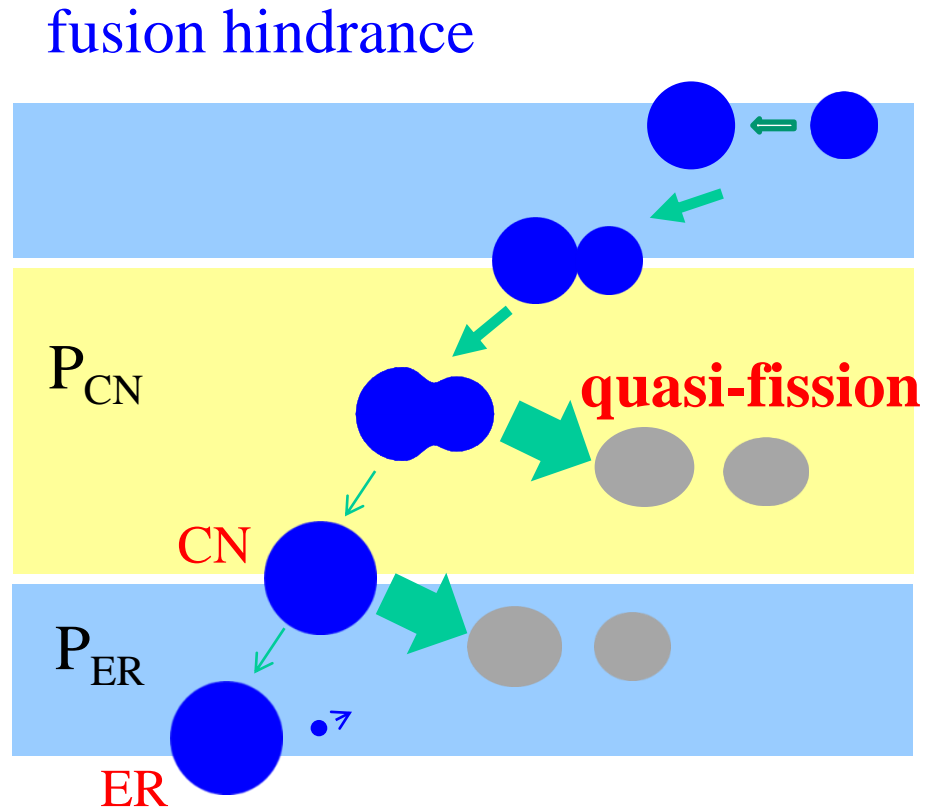
✓ no exp. data for P_{CN}

✓ exp. data: P_{ER} only

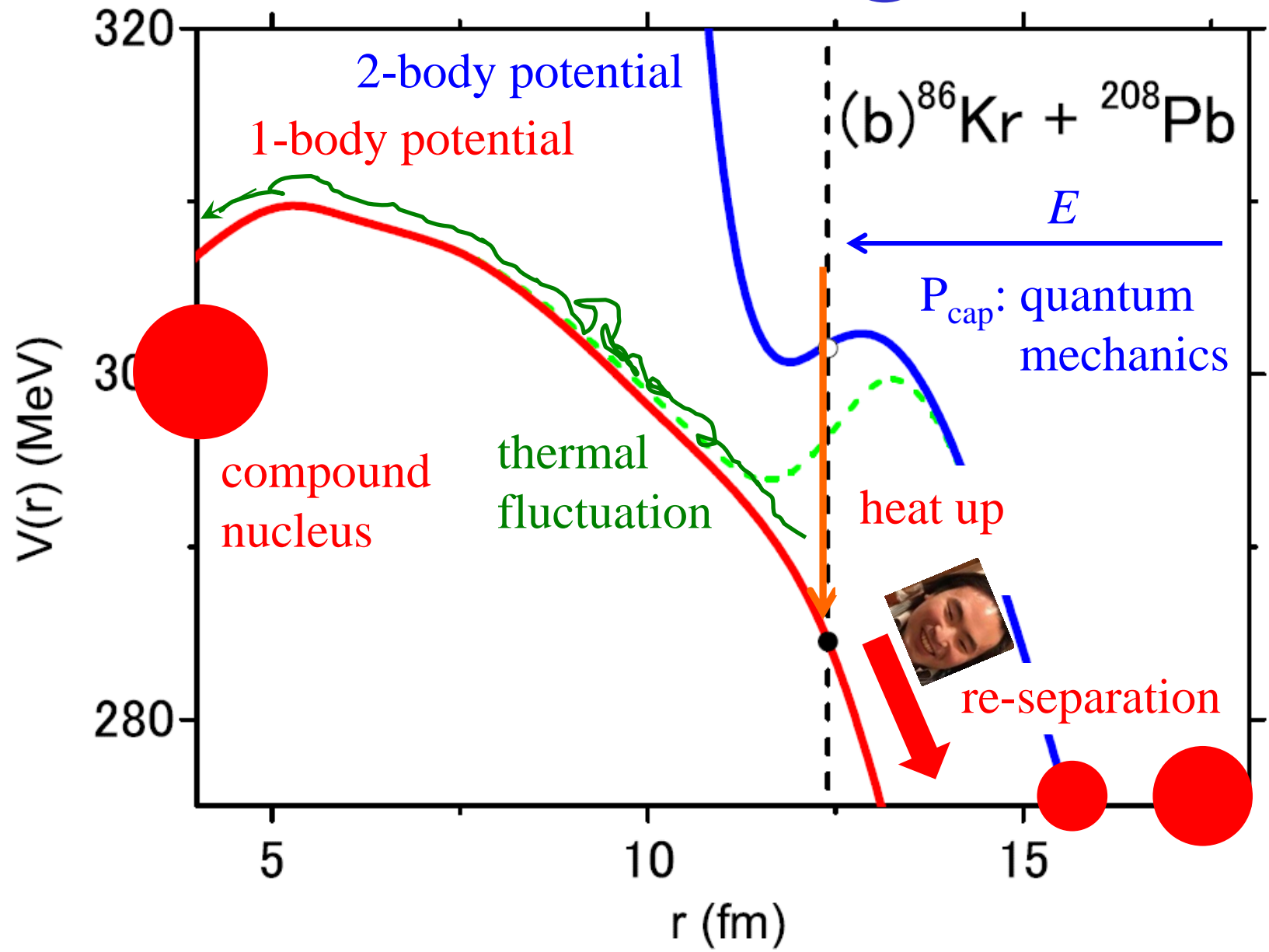
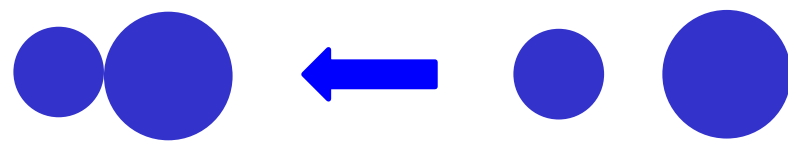
CN=複合核、ER=蒸發殘留核

theoretical challenges:
to reduce the uncertainties and
make reliable predictions

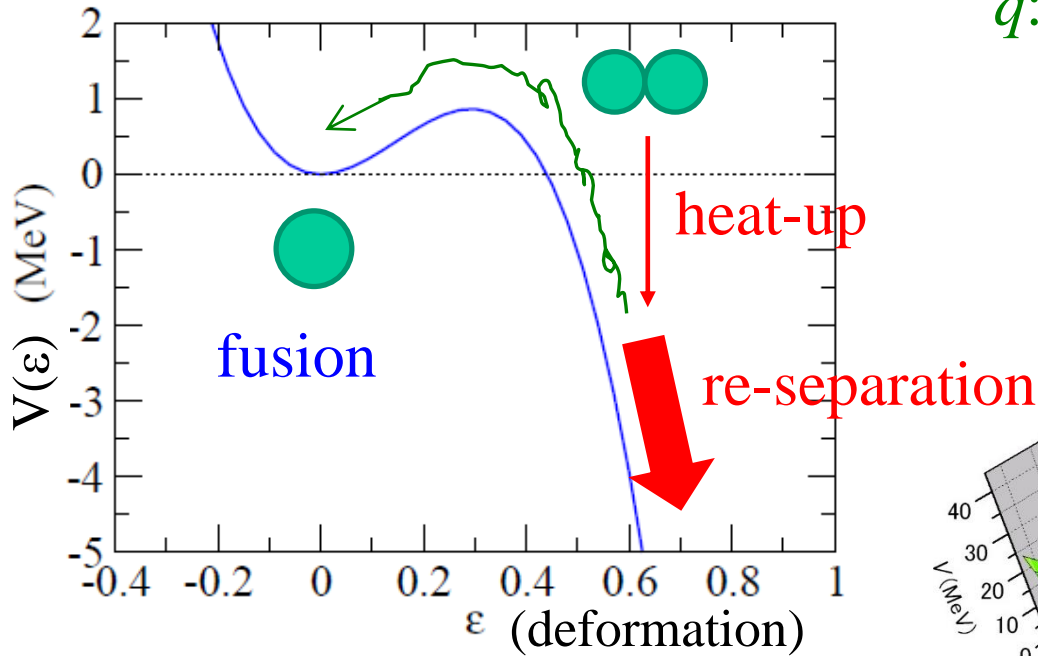
➔ Physics of open quantum systems



SHE formation reactions



Langevin approach



thermal fluctuation

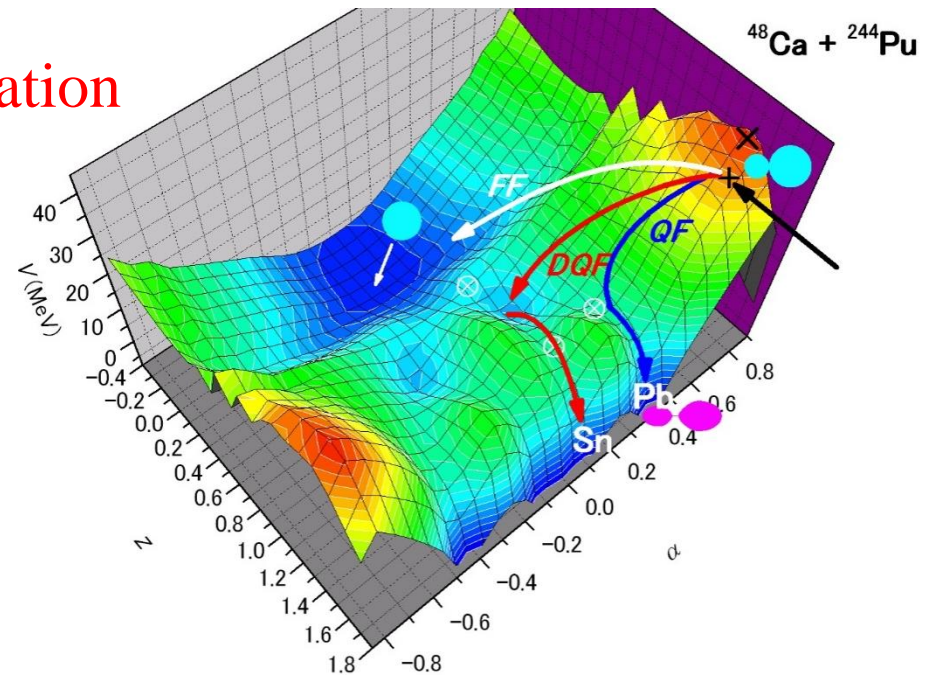
→ Langevin method
(Brownian method)

$$m \frac{d^2 q}{dt^2} = - \frac{dV(q)}{dq} - \gamma \frac{dq}{dt} + R(t)$$

γ : friction coefficient
 $R(t)$: random force

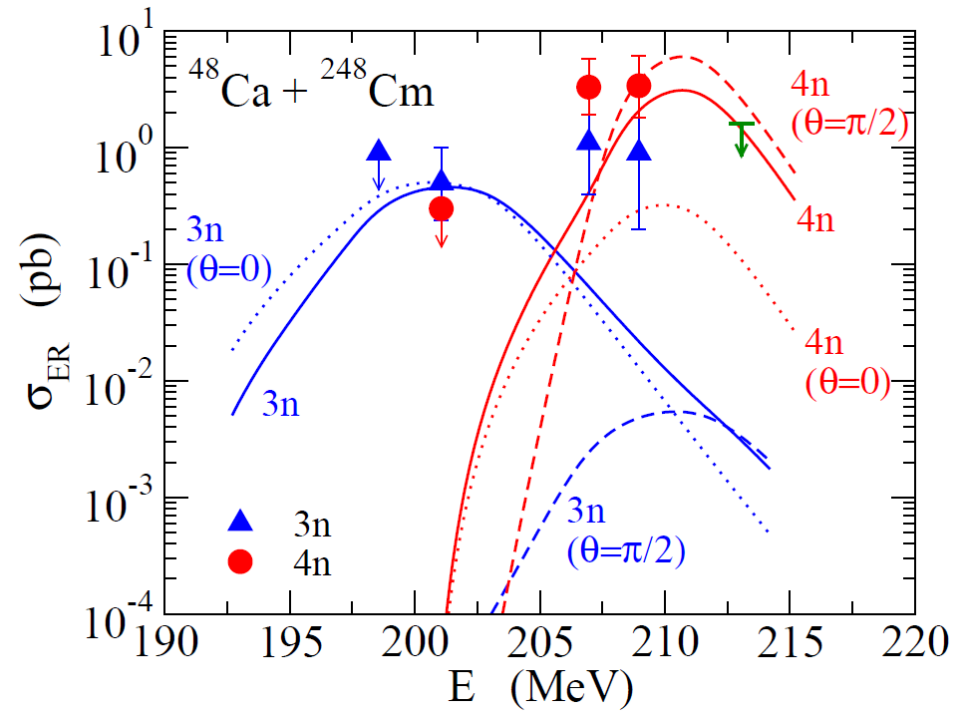
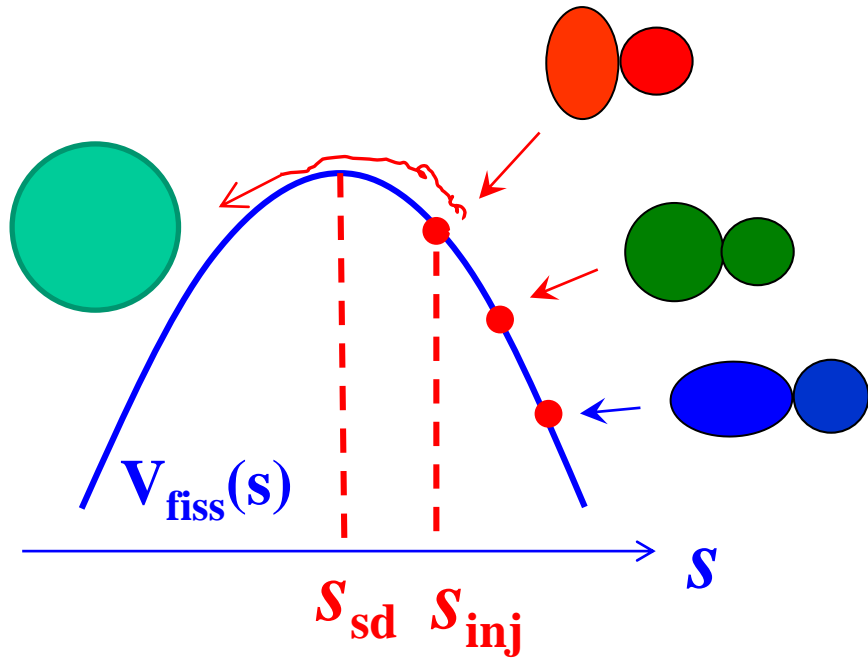
multi-dimensional extention

- internuclear separation,
- deformation,
- asymmetry of the two fragments



Extension of fusion-by diffusion model

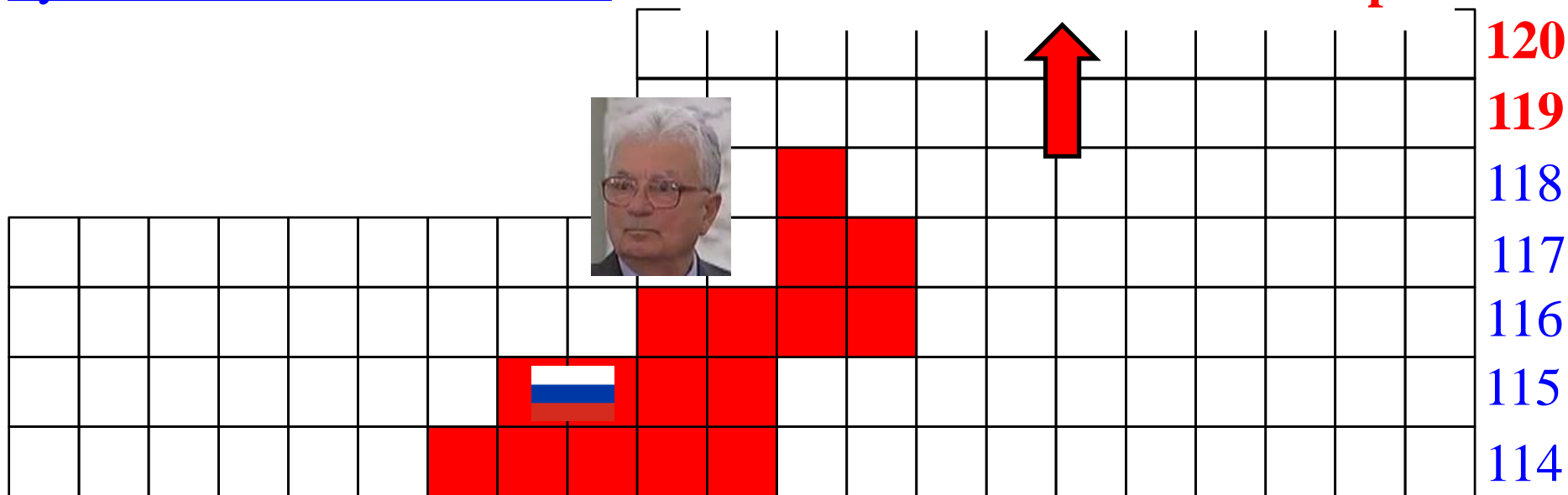
K. Hagino, PRC98 ('18) 014607



cf. barrier distribution measurements by Tanaka et al.

Synthesis of Z=119 and 120

Towards Z=119 and 120 isotopes



hot fusion reactions with ^{48}Ca :



short lived \rightarrow not available with sufficient amounts

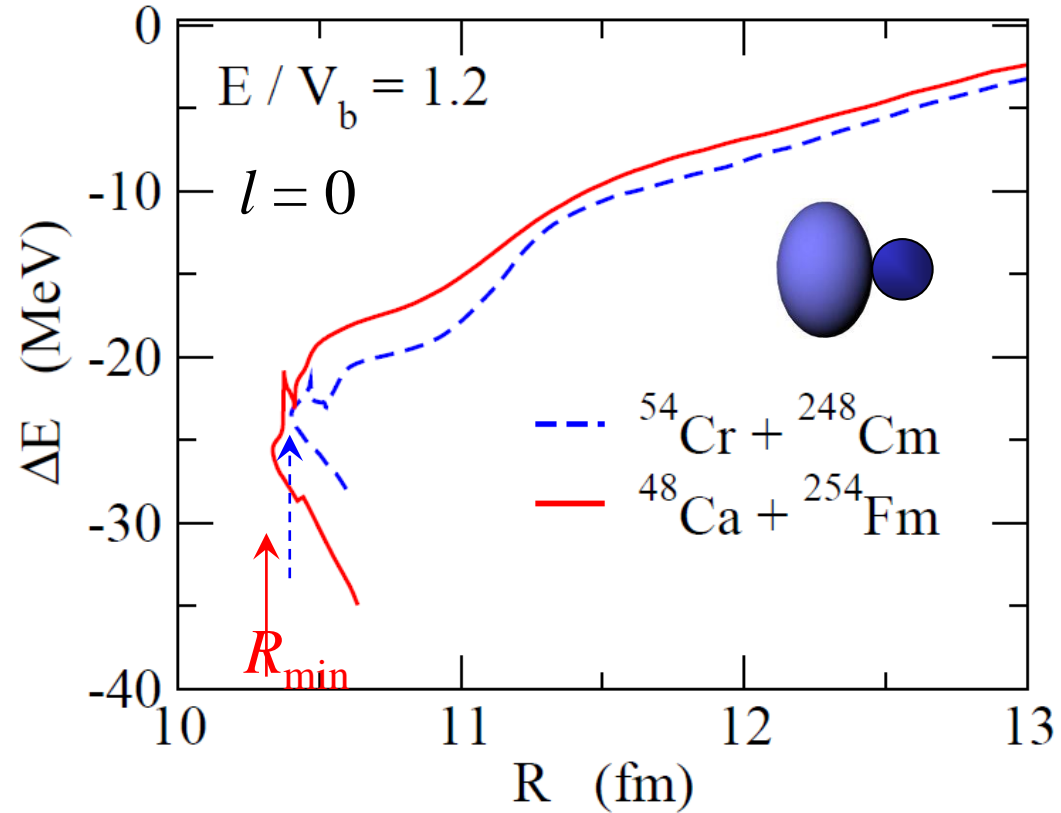
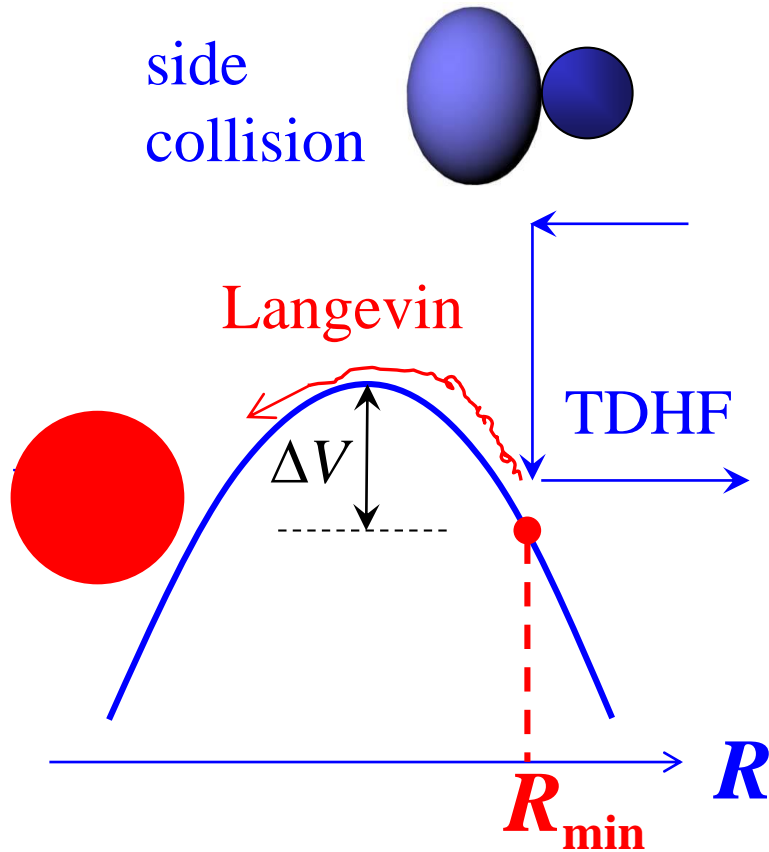
$^{48}\text{Ca} \rightarrow {}^{50}_{22}\text{Ti}, {}^{51}_{23}\text{V}, {}^{54}_{24}\text{Cr}$ projectiles

closed shell \rightarrow open shells

how much will cross sections be affected?

TDHF + Langevin approach

K. Sekizawa and K. H.,
 PRC99 (2019) 051602(R)

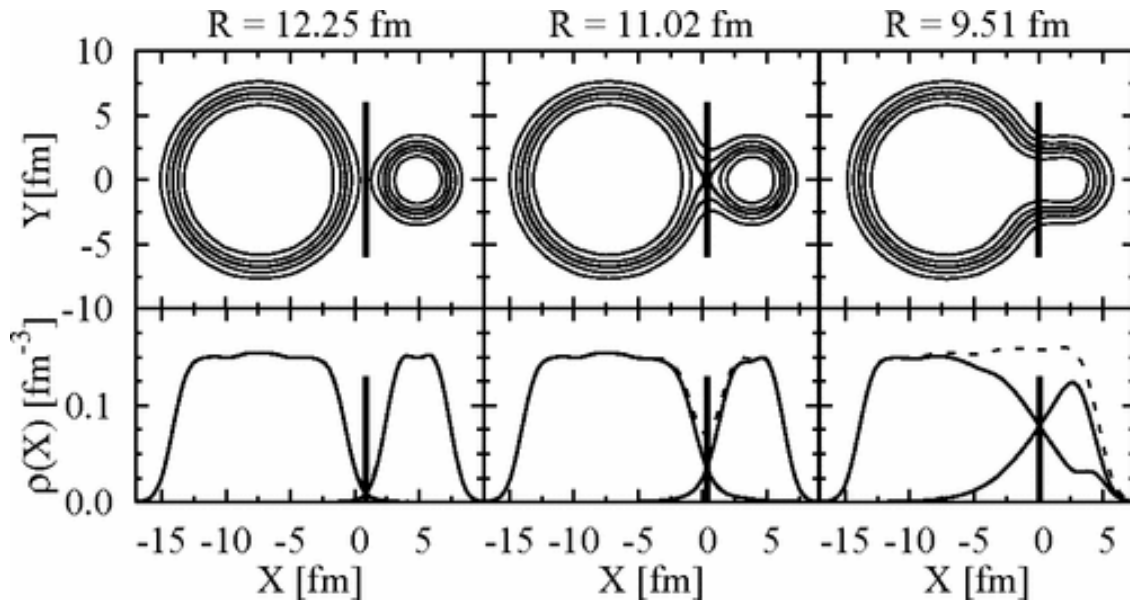


→ Langevin calculation

Mapping TDHF onto a classical equation of motion

K. Washiyama and D. Lacroix, PRC78 ('08) 024610

TDHF simulations

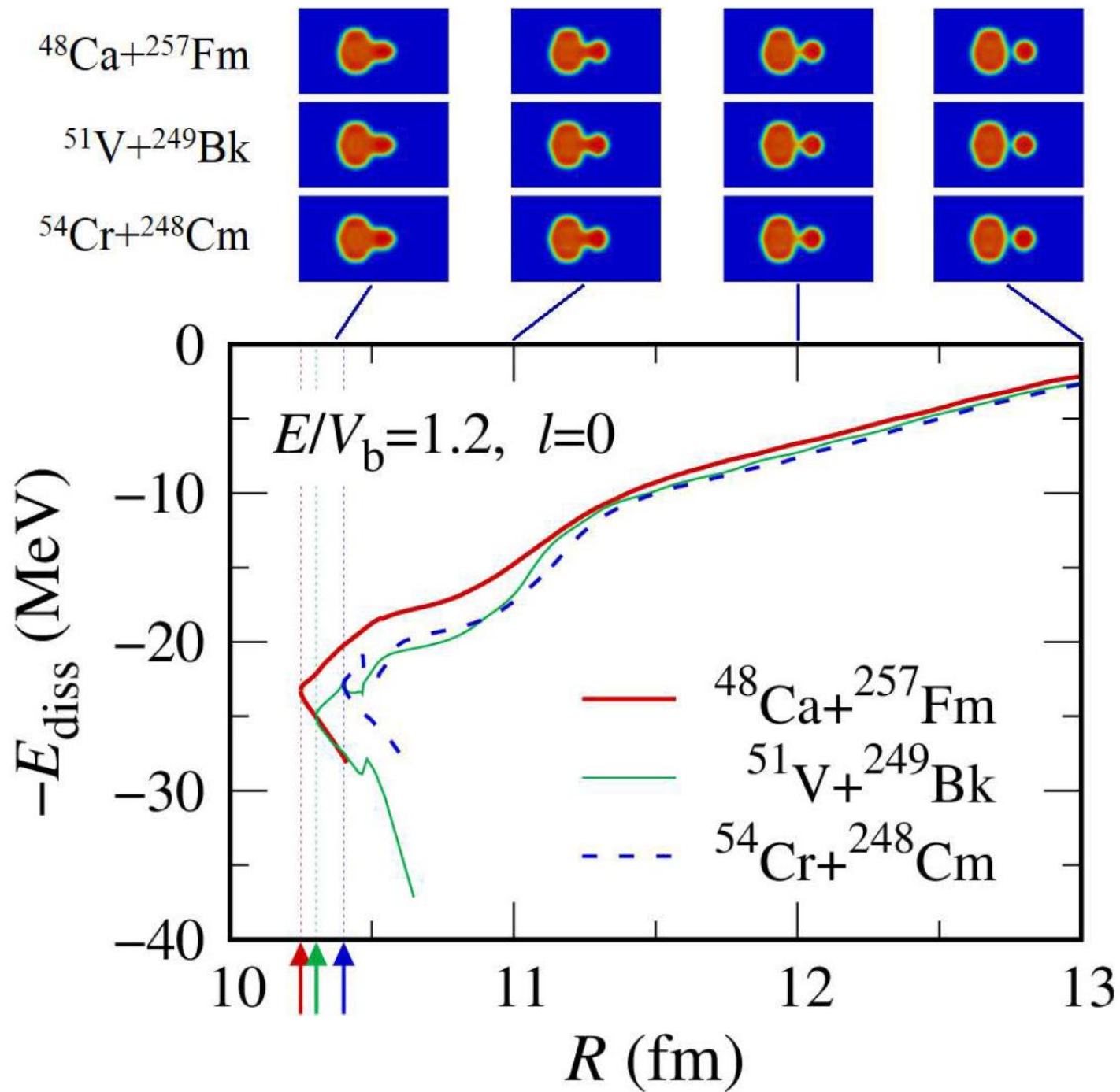


→ $R(t), P(t)$

$$\dot{P} = -\frac{dV}{dR} - \frac{d}{dR} \left(\frac{P^2}{2\mu} \right) - \gamma \dot{R}$$

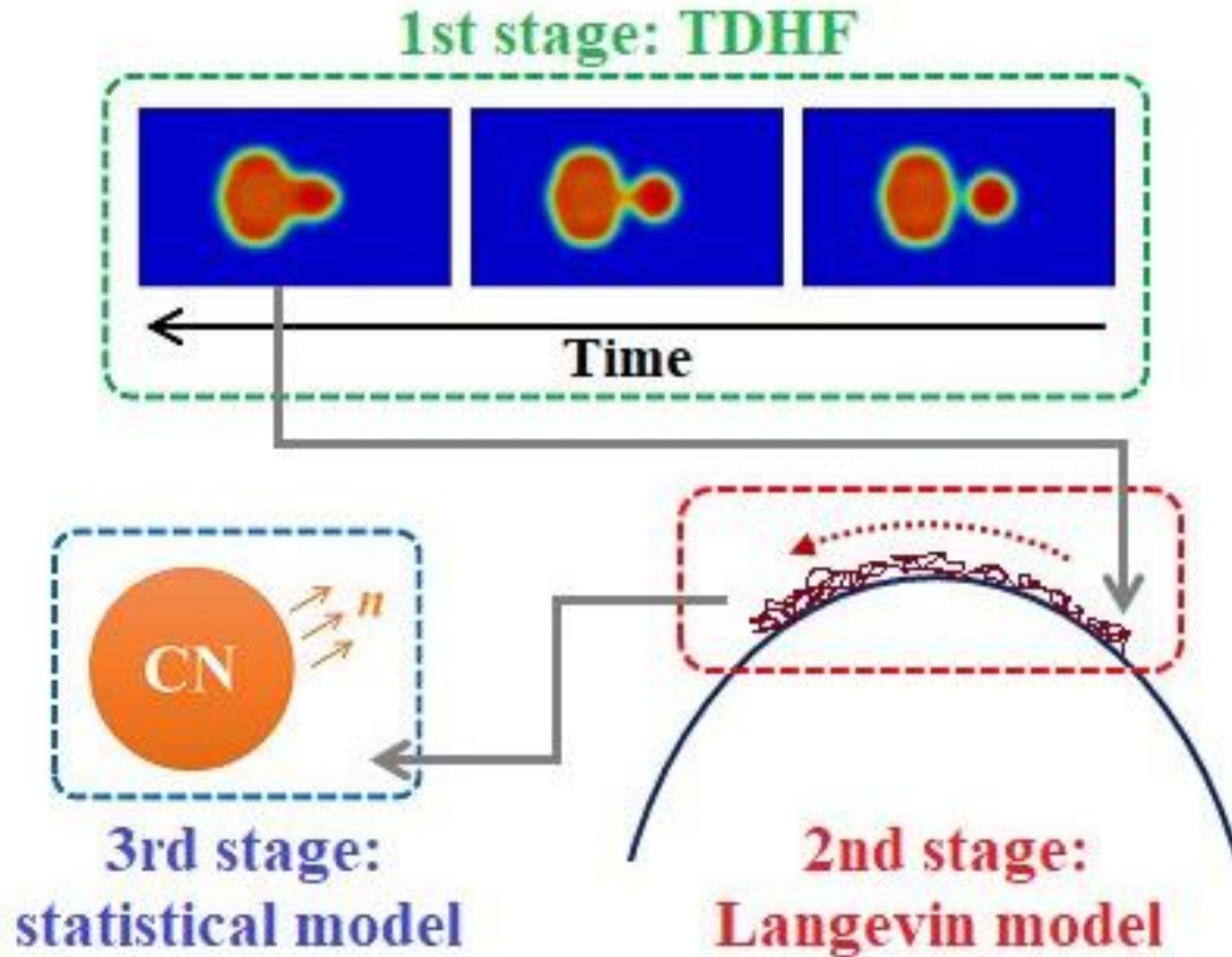
→ $V(R), \gamma(R)$

$$\rightarrow \Delta E(t) = -E_{\text{diss}}(t) = \frac{P(t)^2}{2\mu(R(t))} + V(R(t)) - E_{\text{ini}}$$



New hybrid model: TDHF + Langevin approach

K. Sekizawa and K.H., PRC99 (2019) 051602(R)



New model for fusion for SHE: TDHF + Langevin approach

K. Sekizawa and K.H., PRC99 (2019) 051602(R)



how special is ^{48}Ca ?

System	CN	E^* (MeV)	R_{\min} (fm)	P_{CN} ($\times 10^4$)	W_{sur} ($\times 10^9$)	$P_{\text{CN}} W_{\text{sur}}$ ($\times 10^{13}$)
$^{48}\text{Ca} + ^{254}\text{Fm}$	$^{302}_{120}$	29.0	12.93	1.72	176	302
$^{54}\text{Cr} + ^{248}\text{Cm}$	$^{302}_{120}$	33.2	13.09	1.89	1.31	2.47
$^{51}\text{V} + ^{249}\text{Bk}$	$^{300}_{120}$	37.0	12.94	3.95	0.117	0.461
$^{48}\text{Ca} + ^{257}\text{Fm}$	$^{305}_{120}$	30.5	12.94	2.49	0.729	1.82

similar P_{CN}

no special role of ^{48}Ca in the entrance channel

Summary

From phenomenological to microscopic nuclear reaction theories

Macroscopic (phenomenological)

C.C. with collective model

C.C. with beyond MF

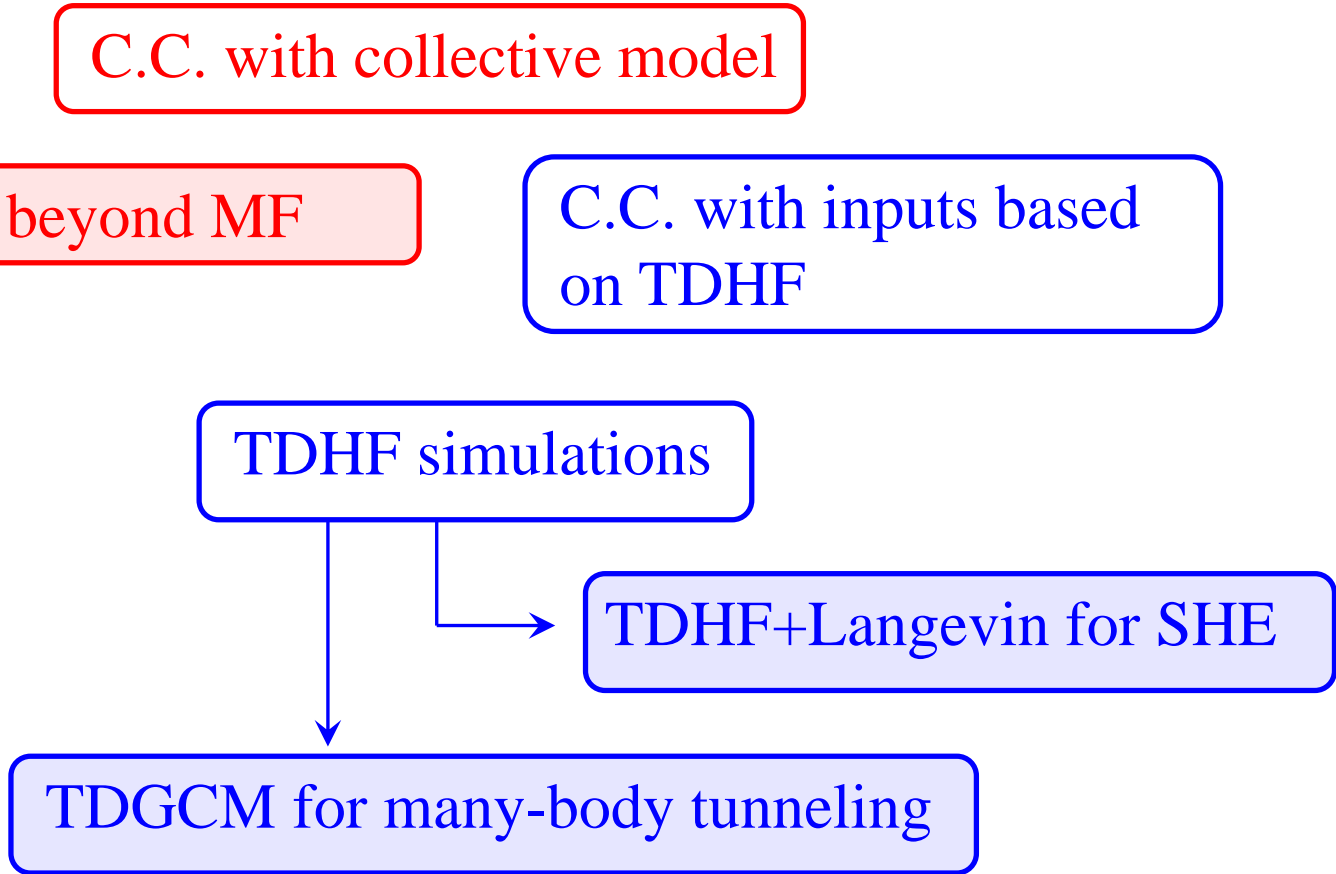
C.C. with inputs based on TDHF

TDHF simulations

TDHF+Langevin for SHE

TDGCM for many-body tunneling

Microscopic



FUSION20

November 15-20, 2020

Shizuoka, Japan

Kouichi Hagino (co-chair) Kyoto University

Katsuhisa Nishio (co-chair) JAEA

Japan-China joint organization

Program Committee

Japanese members

+ L. Guo, X. Tang, S.G. Zhou

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石田

tennessine

