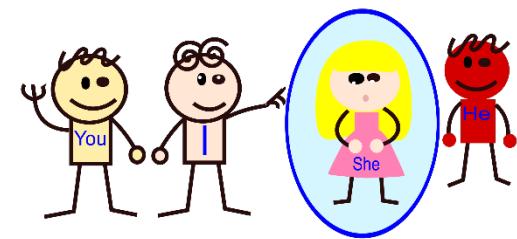
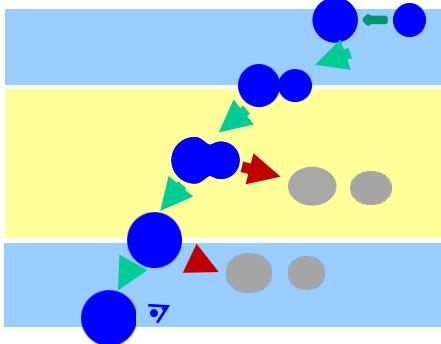


Capture barrier distributions and superheavy elements



Kouichi Hagino

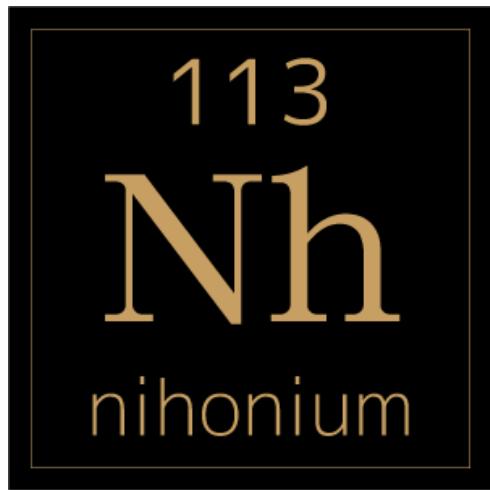
Tohoku University, Sendai, Japan



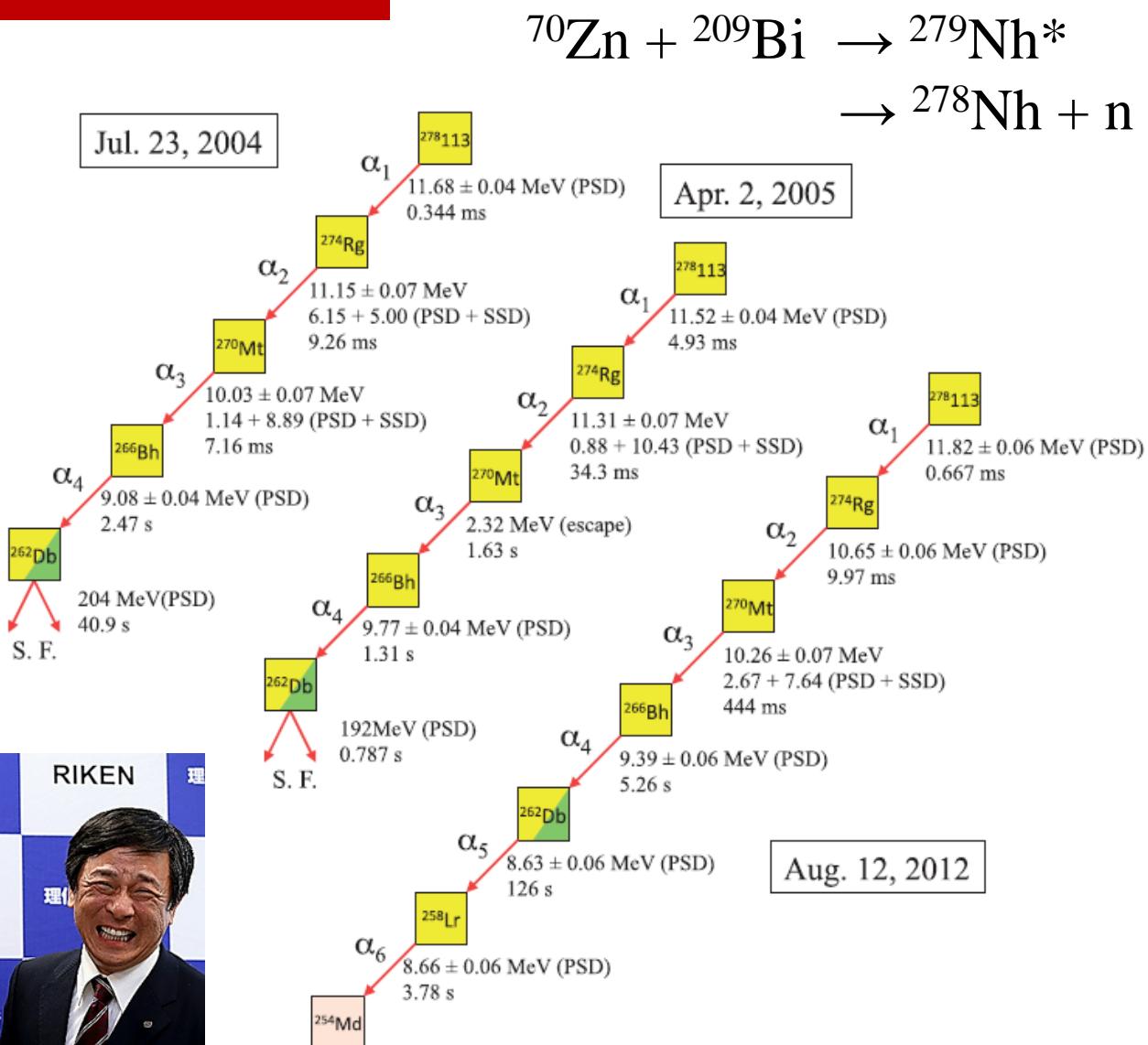
she

1. Introduction: Fusion reactions for SHE
2. Role of deformation in capture reactions
3. Barrier distribution and C.C. analysis
4. Summary

New element 113: Nihonium



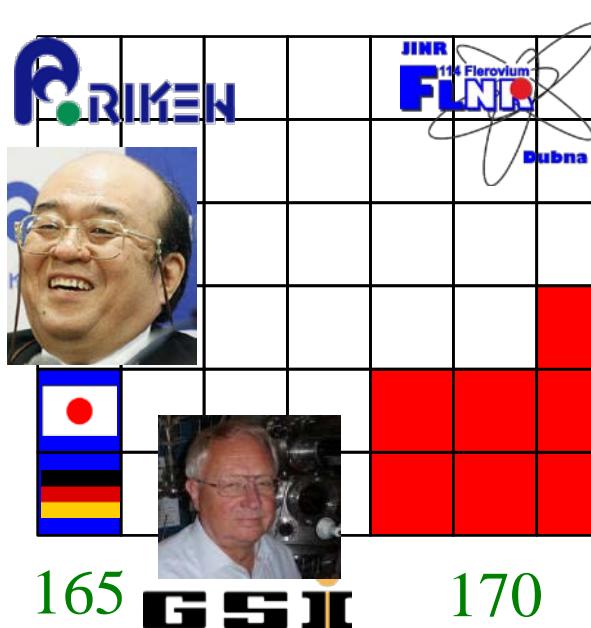
November, 2016



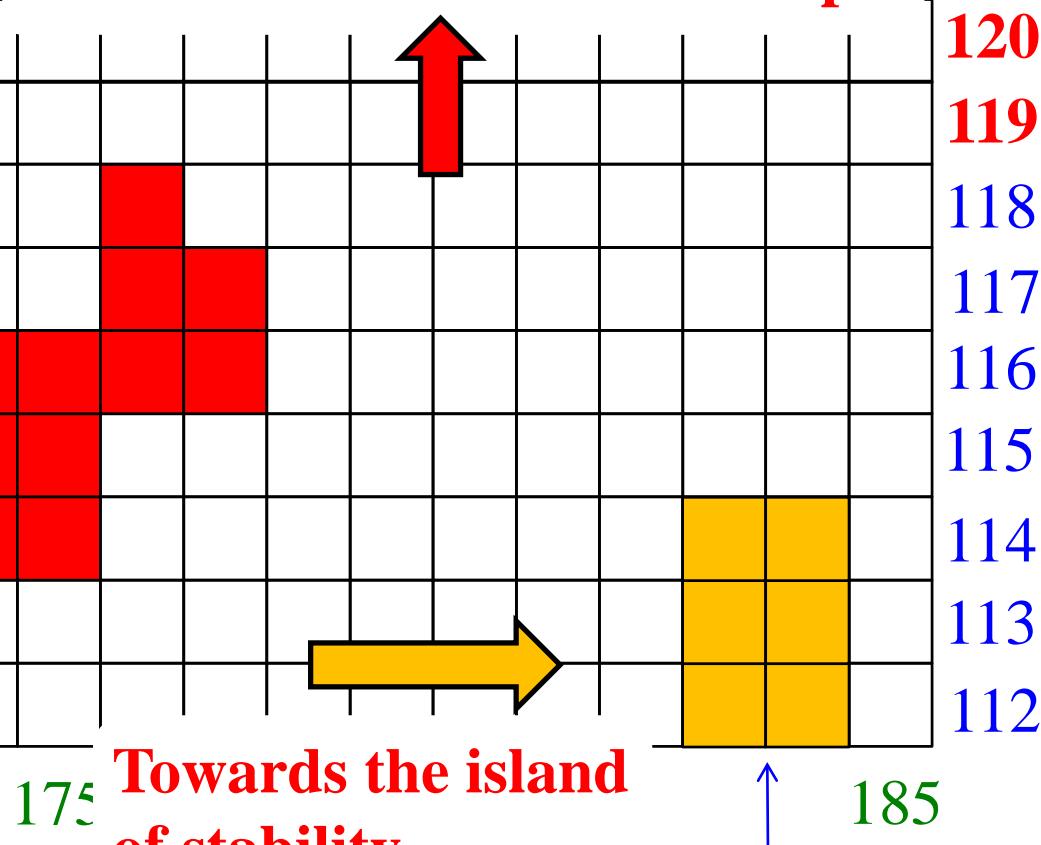
Morimoto-san's talk

Future directions

Superheavy elements
synthesized so far



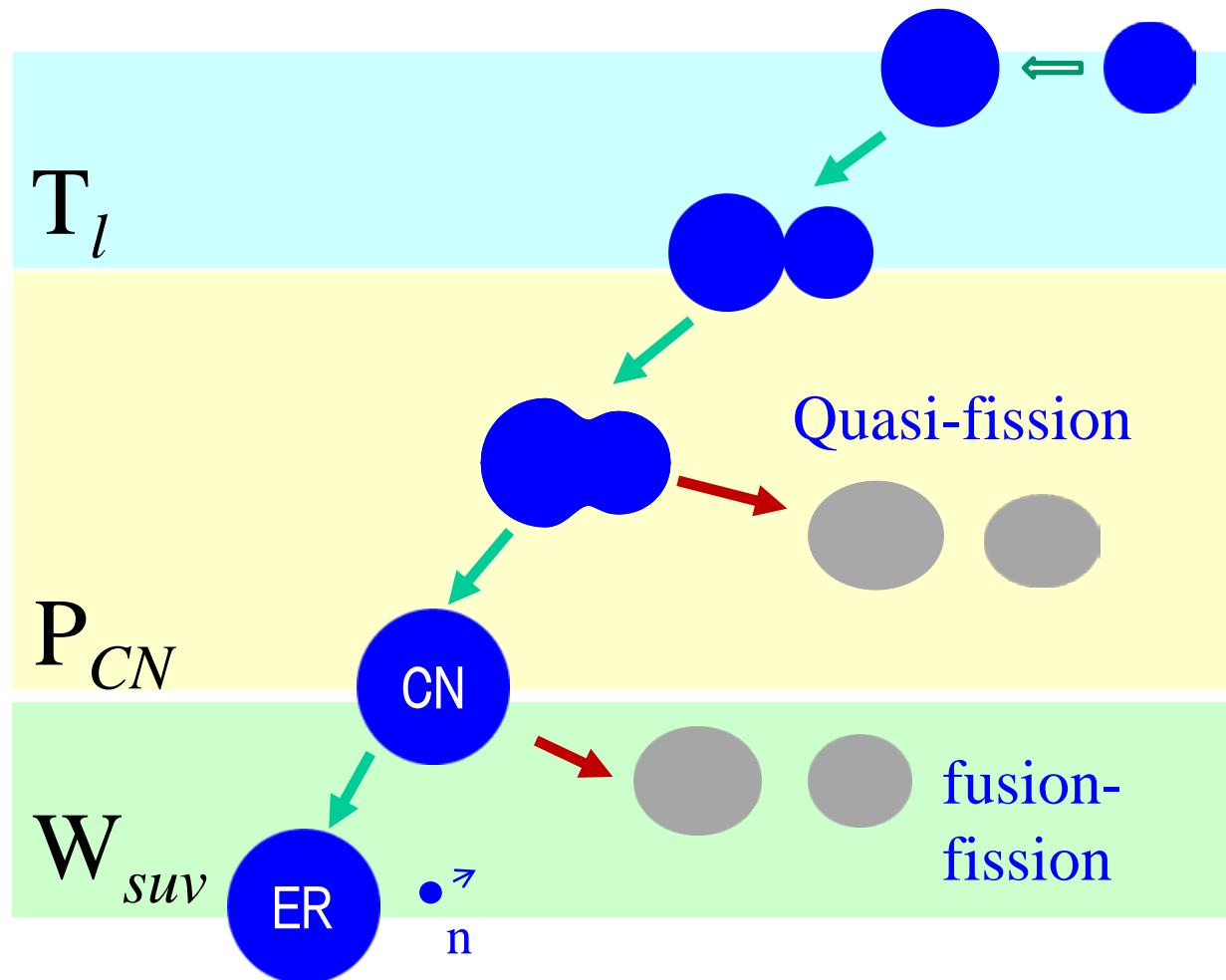
Towards Z=119 and 120 isotopes



Theoretical issues:

- to understand the reaction dynamics
- to make a reliable theoretical prediction for fusion cross sections

Fusion reactions for SHE



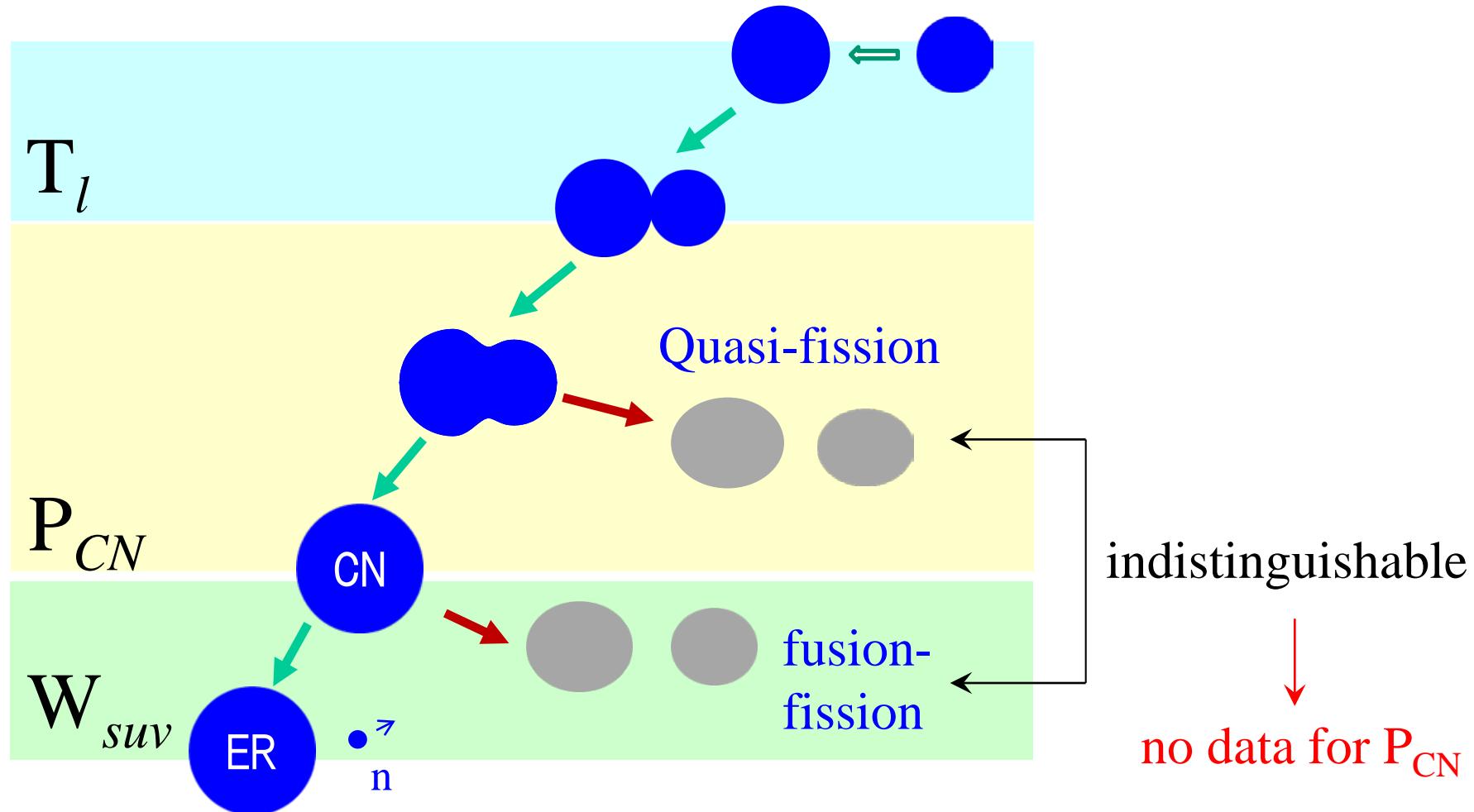
Coupled-channels

Langevin equation

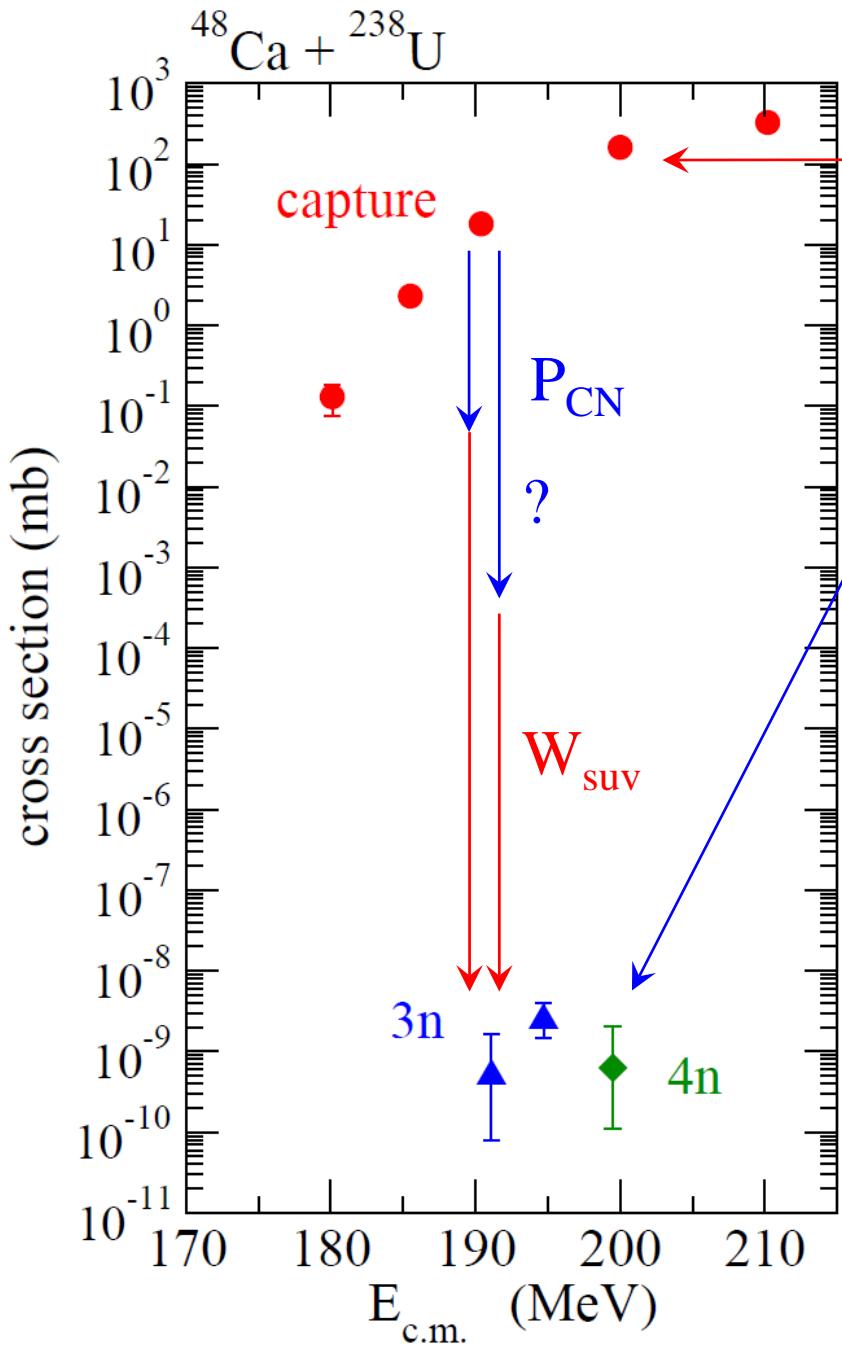
Statistical model

$$\sigma_{ER}(E) = \frac{\pi}{k^2} \sum_l (2l + 1) T_l(E) P_{CN}(E, l) W_{suv}(E^*, l)$$

Fusion reactions for SHE



$$\sigma_{ER}(E) = \frac{\pi}{k^2} \sum_l (2l + 1) T_l(E) P_{CN}(E, l) W_{SUV}(E^*, l)$$



no experimental data for P_{CN}

$$\sigma_{\text{cap}}(E) = \frac{\pi}{k^2} \sum_l (2l + 1) T_l(E)$$

$$\begin{aligned} \sigma_{\text{ER}}(E) &= \frac{\pi}{k^2} \sum_l (2l + 1) T_l(E) \\ &\times P_{\text{CN}} \cdot W_{\text{suv}} \end{aligned}$$

large uncertainties

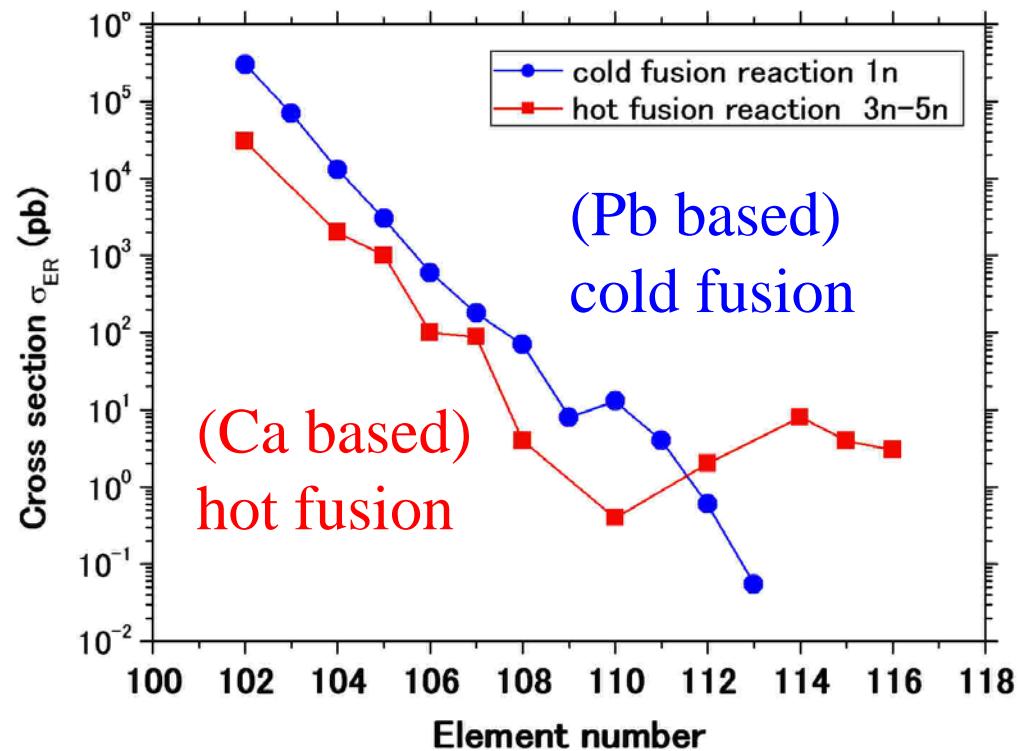
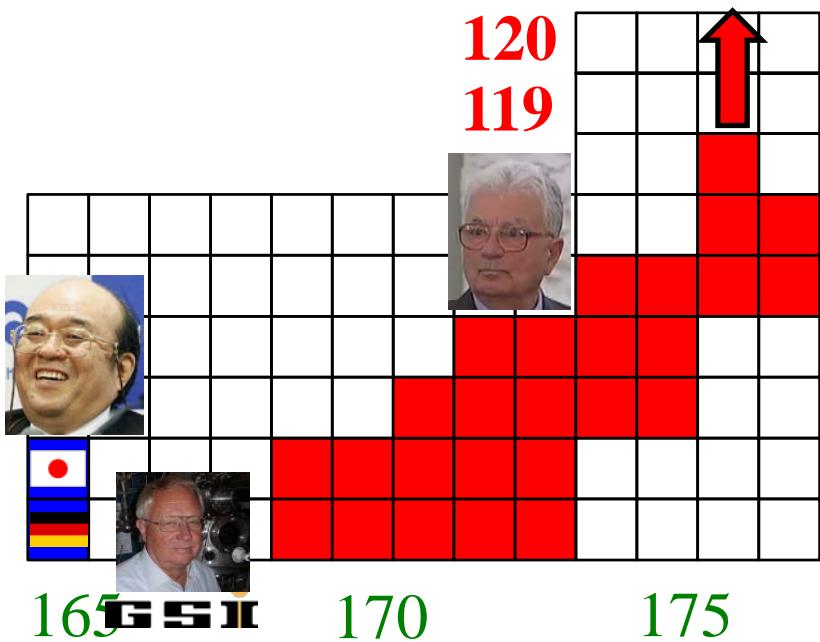
challenges
: reduction of theoretical
uncertainties



a good understanding of
the reaction dynamics

Hot fusion for Z = 119 and 120

Towards Z=119 and 120 isotopes

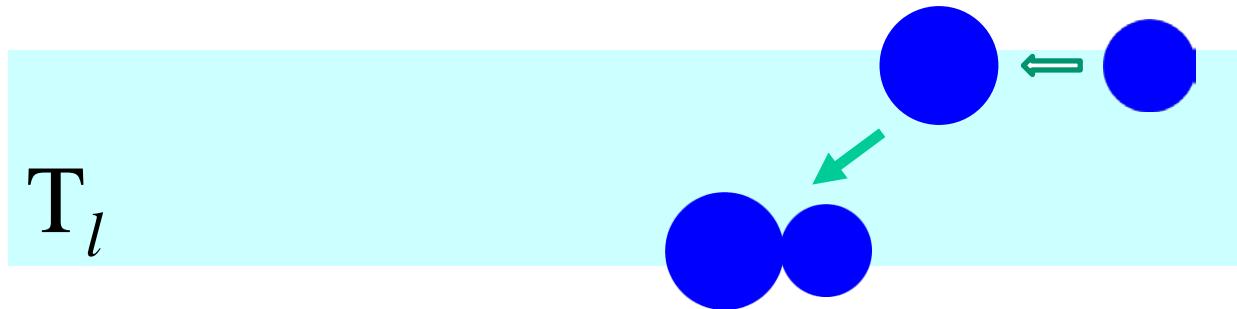


hot fusion: $^{48}\text{Ca} + \text{actinide targets}$

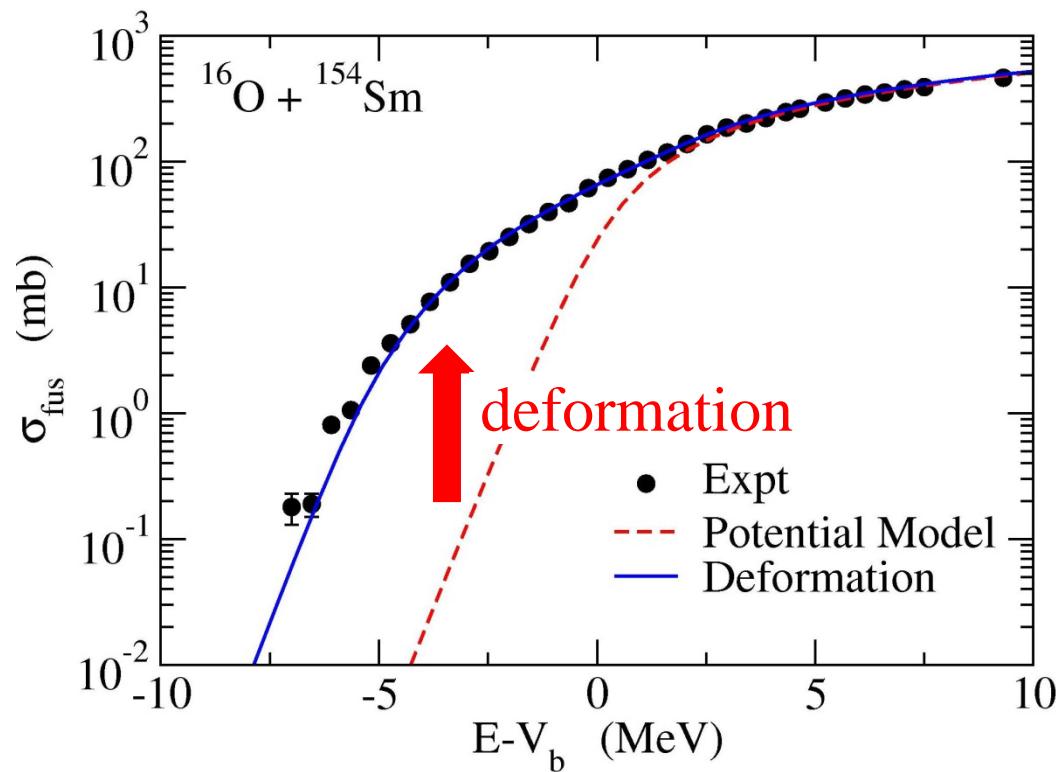
Dubna: $^{48}\text{Ca} + ^{249}\text{Cf}$ ($\beta_2 = 0.235$) $\rightarrow ^{297-x}\text{Og}$ (Z=118) + xn

role of deformation?

Role of deformation in capture cross sections

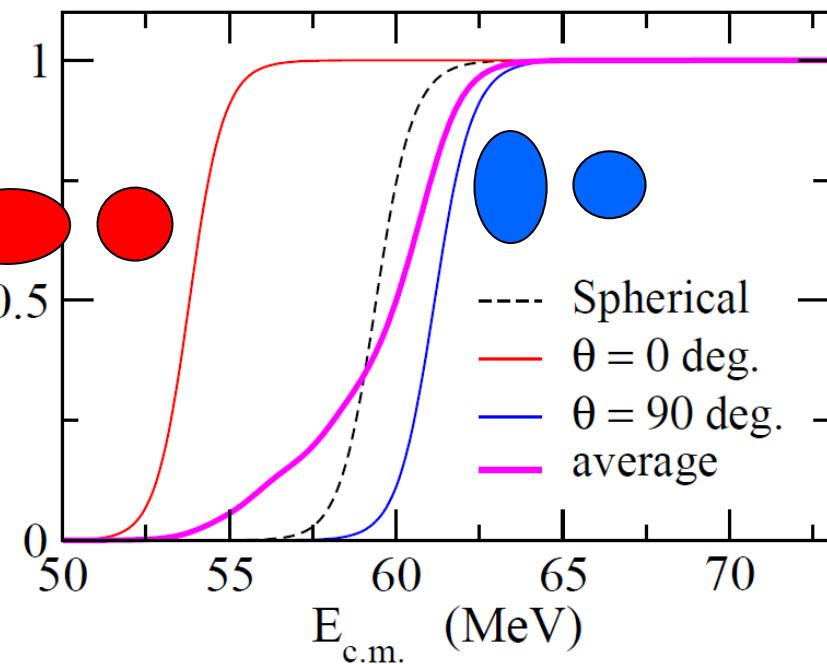
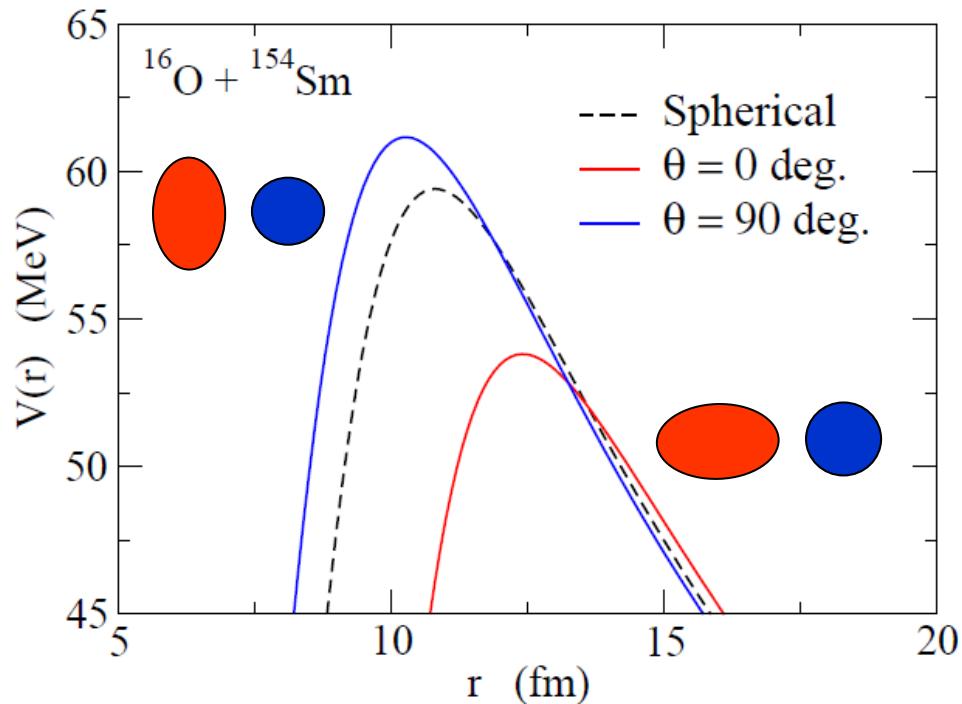


Sub-barrier enhancement of capture cross sections



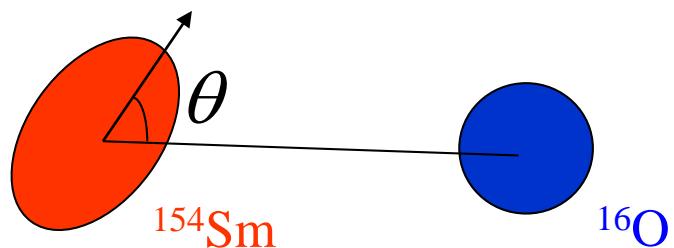
Role of deformation in capture cross sections

Sub-barrier enhancement of capture cross sections



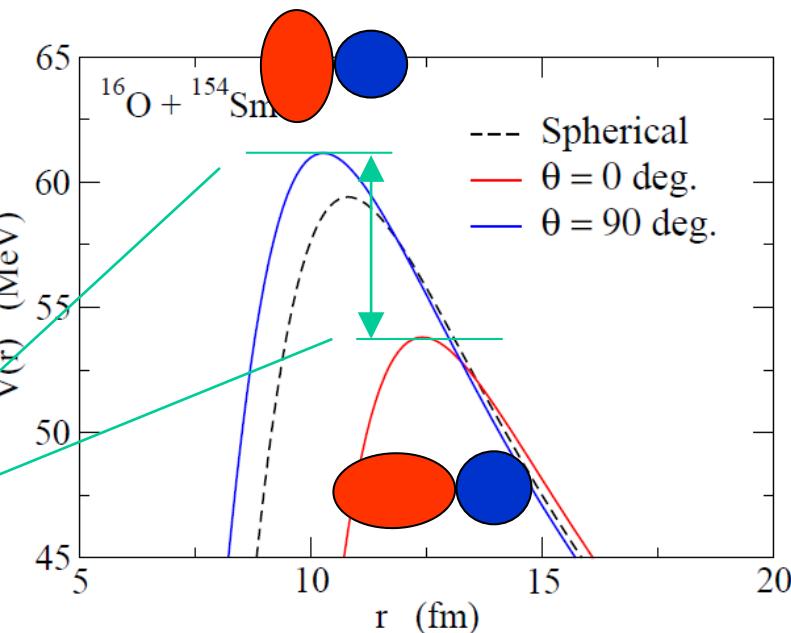
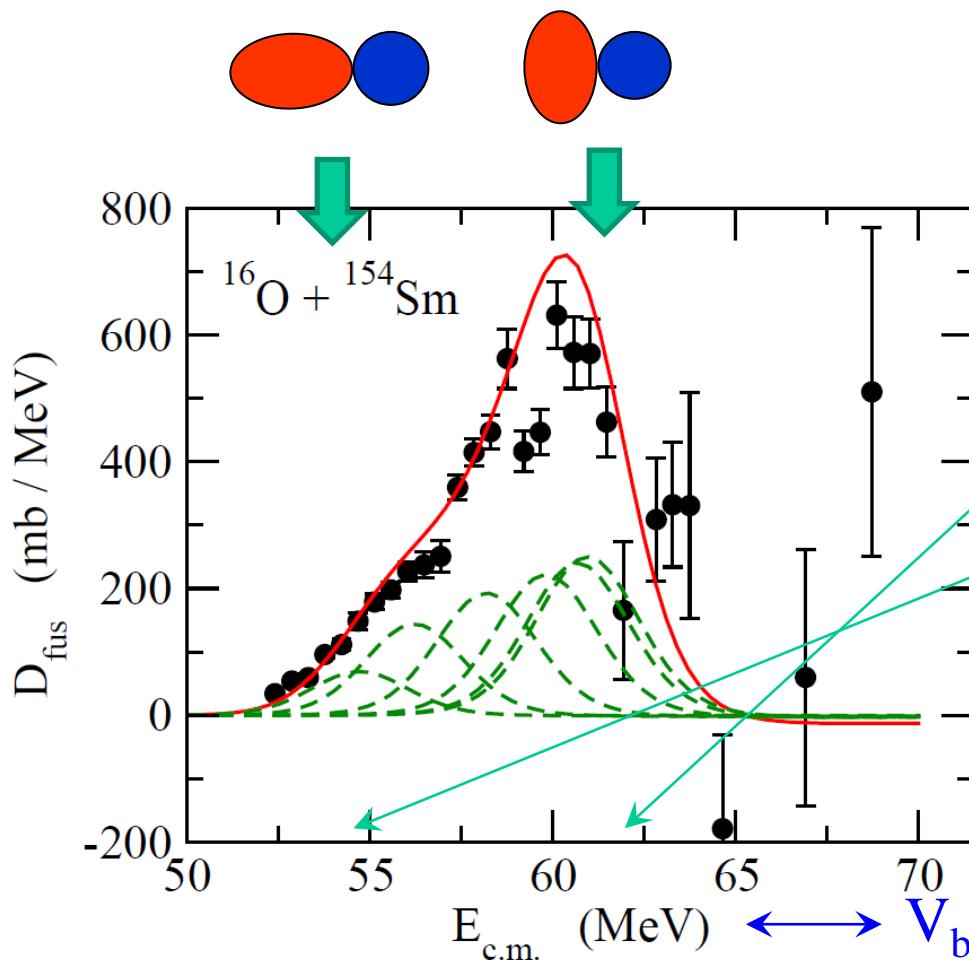
$$\sigma_{\text{cap}}(E) = \int_0^1 d(\cos \theta) \sigma_{\text{cap}}(E; \theta)$$

K.H., N. Takigawa, PTP128 ('12) 1061



✓ Fusion barrier distribution (Rowley, Satchler, Stelson, PLB254('91))

$$D_{\text{fus}}(E) = \frac{d^2(E\sigma_{\text{fus}})}{dE^2}$$

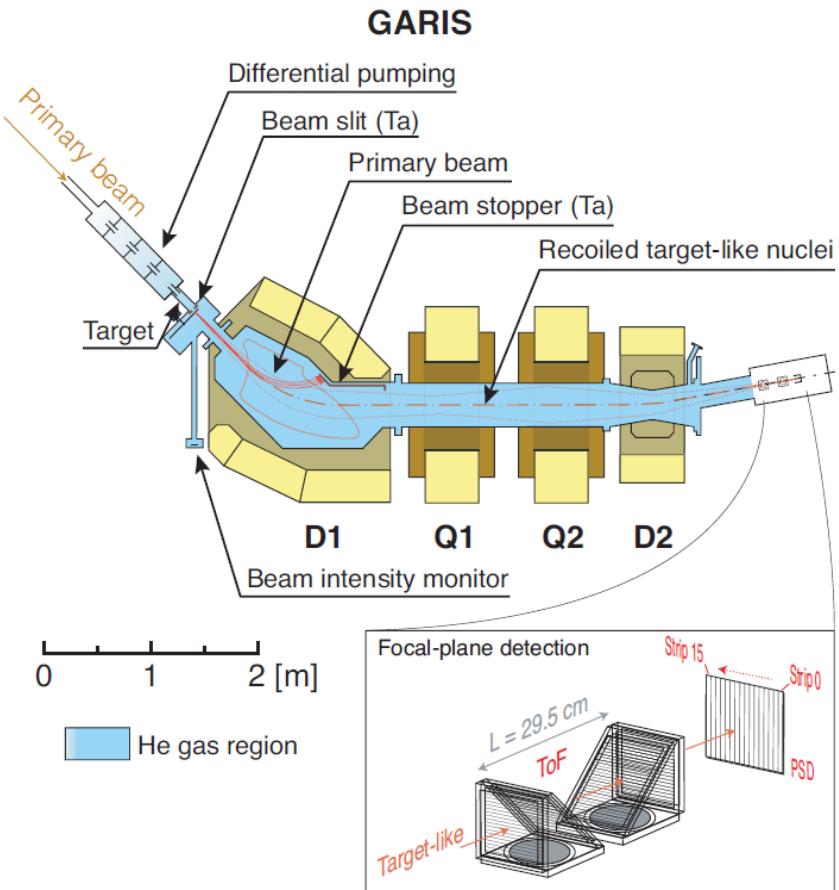


Data: J.R. Leigh et al.,
PRC52 ('95) 3151

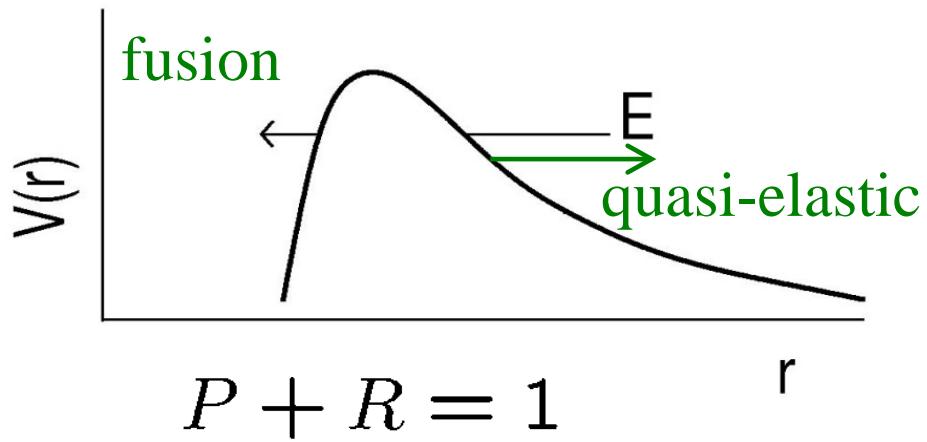
a nice tool to understand the reaction dynamics

Measurements of barrier distributions with GARIS

T. Tanaka, Y. Narikiyo, K. Morita, K. Fujita, D. Kaji,
K. Morimoto,, K.H., J. of Phys. Soc. Japan (JPSJ), in press.



Quasi-elastic barrier distribution



- a sum of elastic, inelastic, and transfer

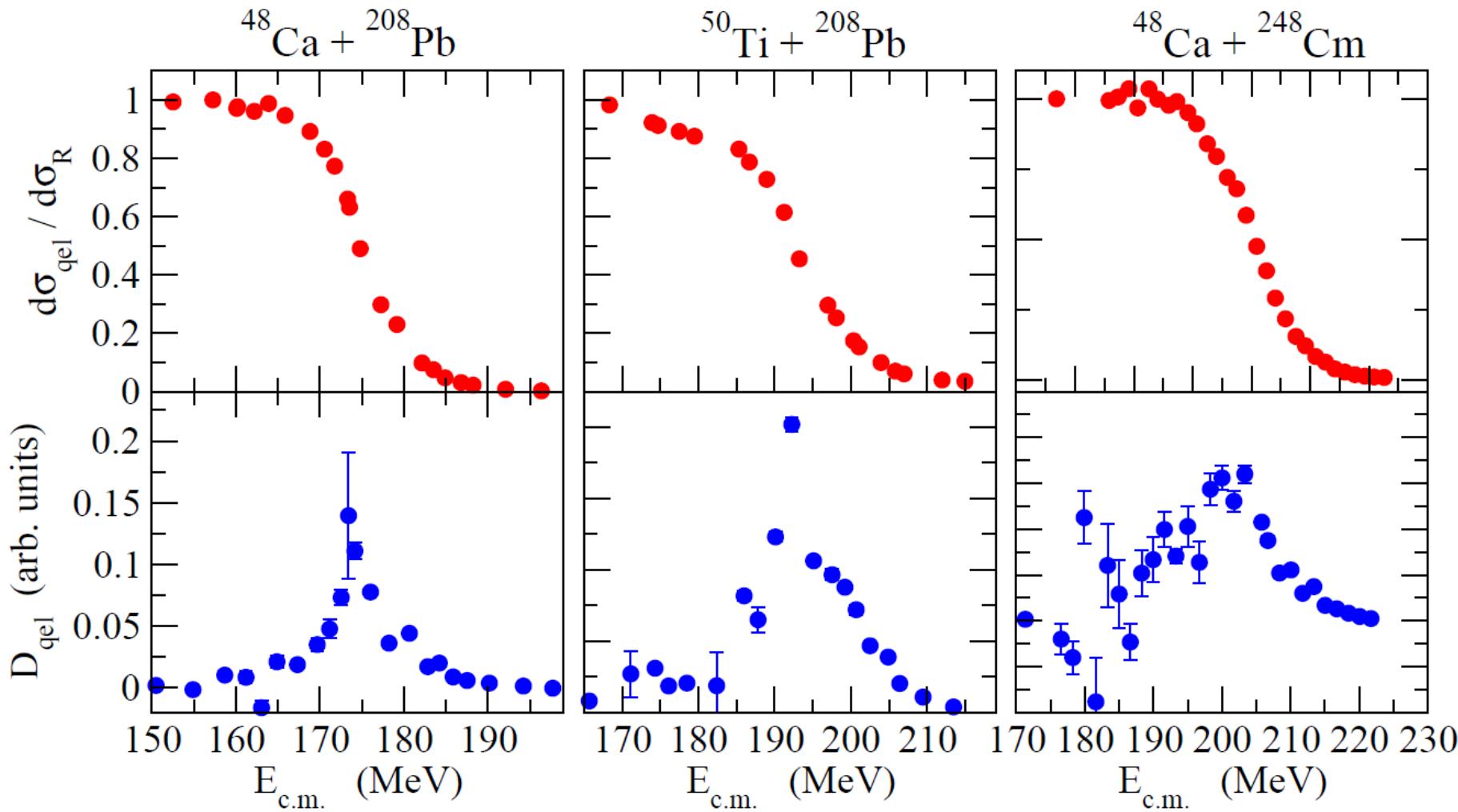
$$D_{\text{qel}}(E) = -\frac{d}{dE} \left(\frac{\sigma_{\text{qel}}(E, \pi)}{\sigma_R(E, \pi)} \right)$$

Measurements of barrier distributions with GARIS

$$D_{\text{qel}}(E) = -\frac{d}{dE} \left(\frac{\sigma_{\text{qel}}(E, \pi)}{\sigma_R(E, \pi)} \right)$$

T. Tanaka et al., K.H.,
JPSJ, in press.

K.H. and N. Rowley, PRC69 ('04) 054610



Analysis for a hot fusion reaction $^{48}\text{Ca} + ^{248}\text{Cm}$

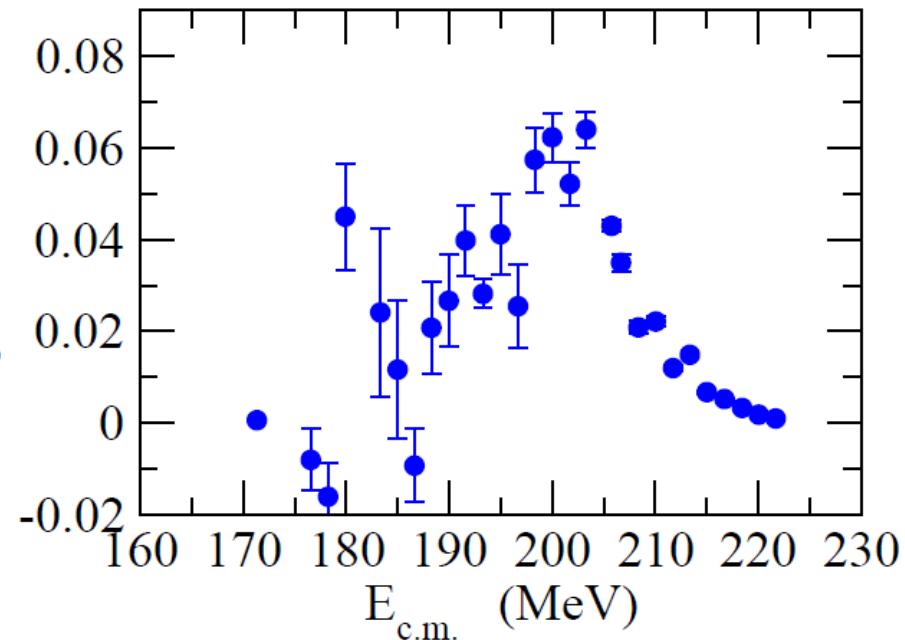
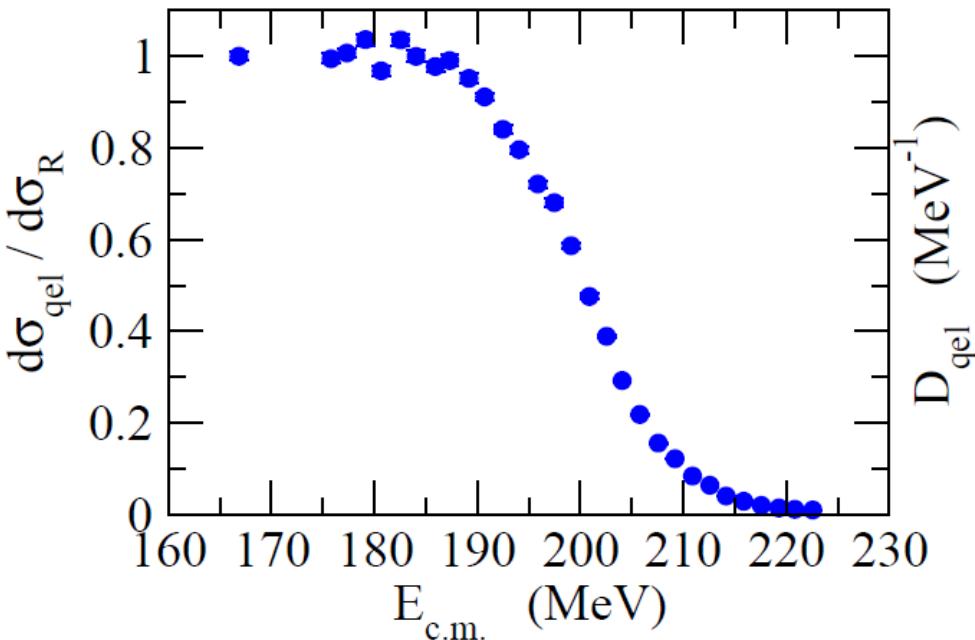
K.H. and T. Tanaka (2017)

(T. Tanaka et al., K.H., JPSJ in press)



[β_2 and β_4 from P. Moller]

$$D_{\text{qel}}(E) = -\frac{d}{dE} \left(\frac{\sigma_{\text{qel}}(E, \pi)}{\sigma_R(E, \pi)} \right)$$

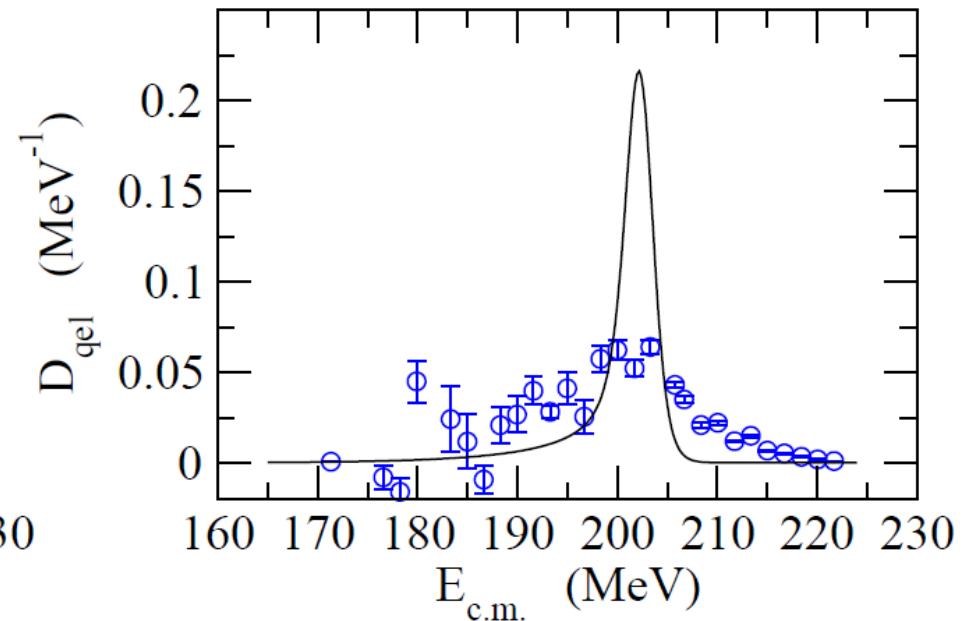
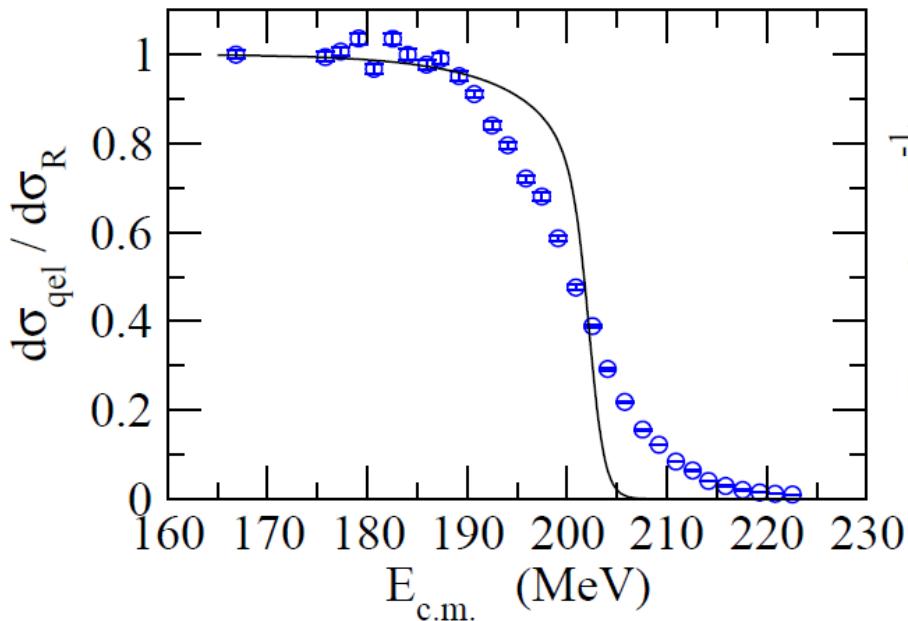


Analysis for a hot fusion reaction $^{48}\text{Ca} + ^{248}\text{Cm}$

K.H. and T. Tanaka (2017)



single-channel calculation (spherical ^{248}Cm)

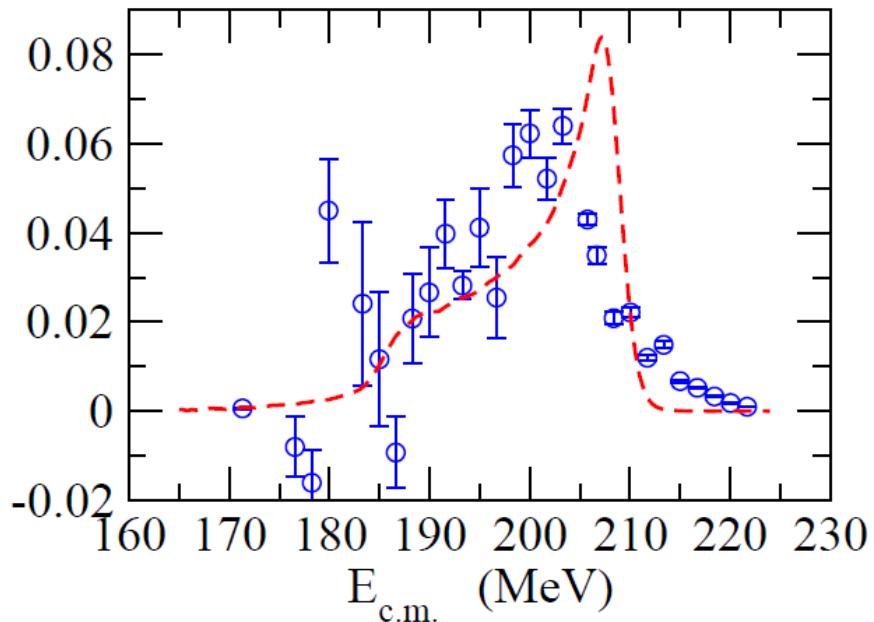
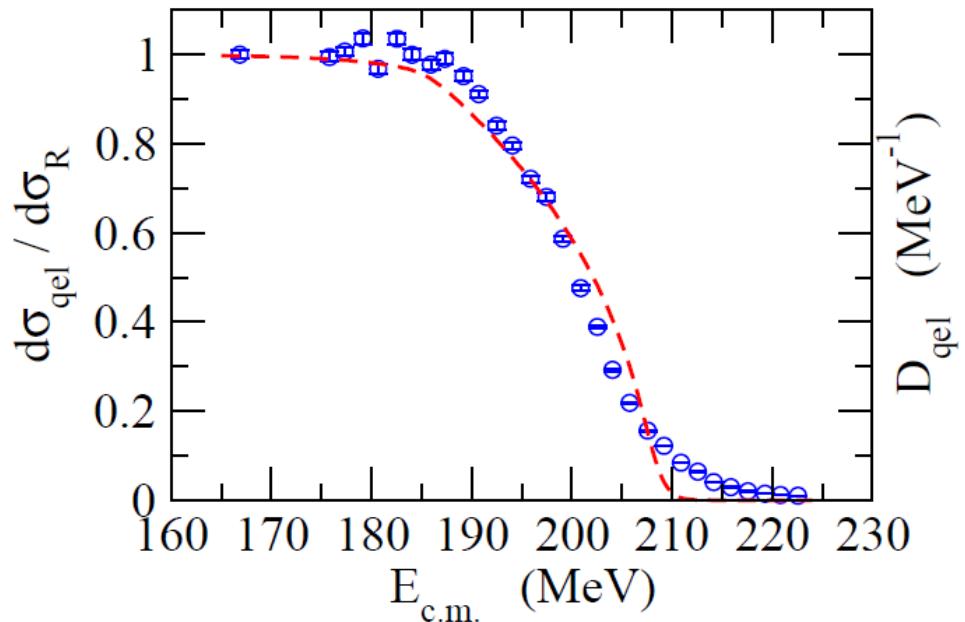
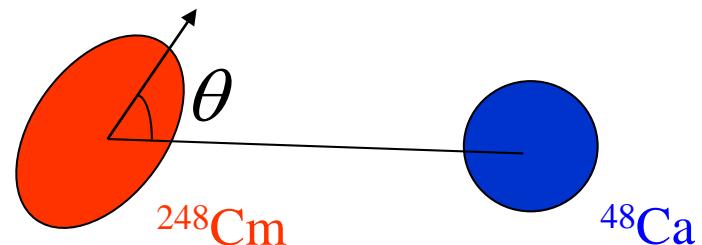


Analysis for a hot fusion reaction $^{48}\text{Ca} + ^{248}\text{Cm}$

K.H. and T. Tanaka (2017)

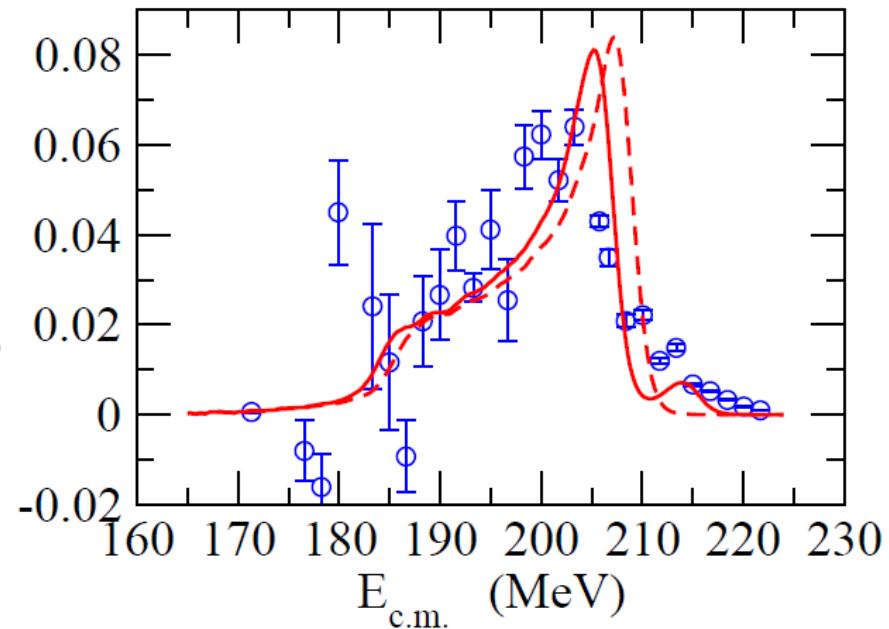
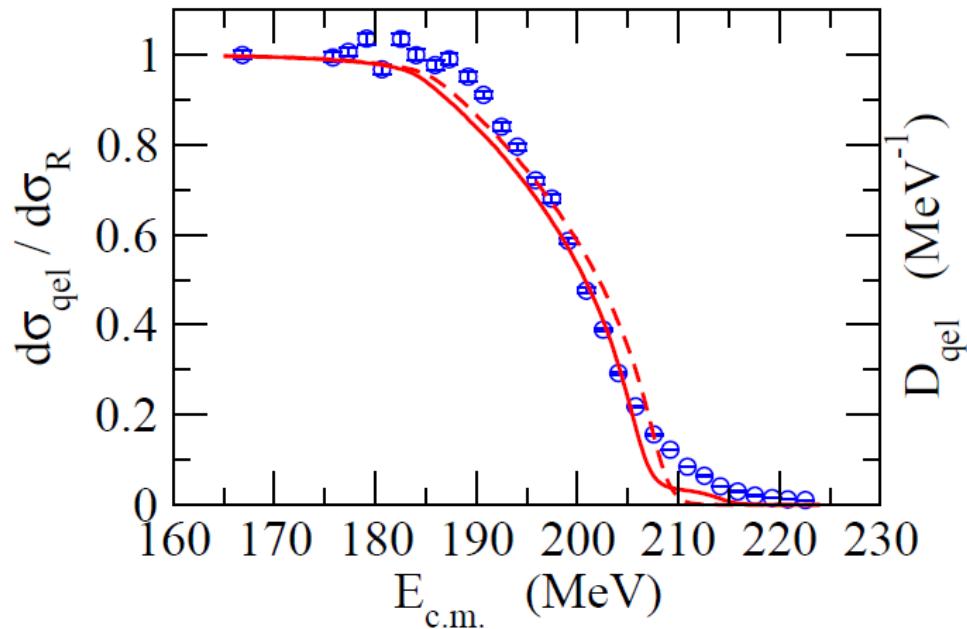
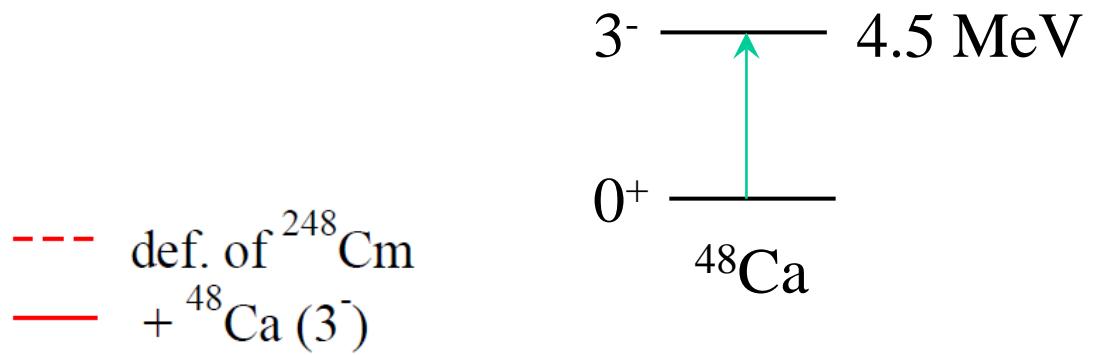


$$\frac{d\sigma_{\text{qel}}}{d\Omega} = \int_0^1 d(\cos \theta) \left(\frac{d\sigma_{\text{el}}}{d\Omega} \right)_\theta$$



Analysis for a hot fusion reaction $^{48}\text{Ca} + ^{248}\text{Cm}$

K.H. and T. Tanaka (2017)

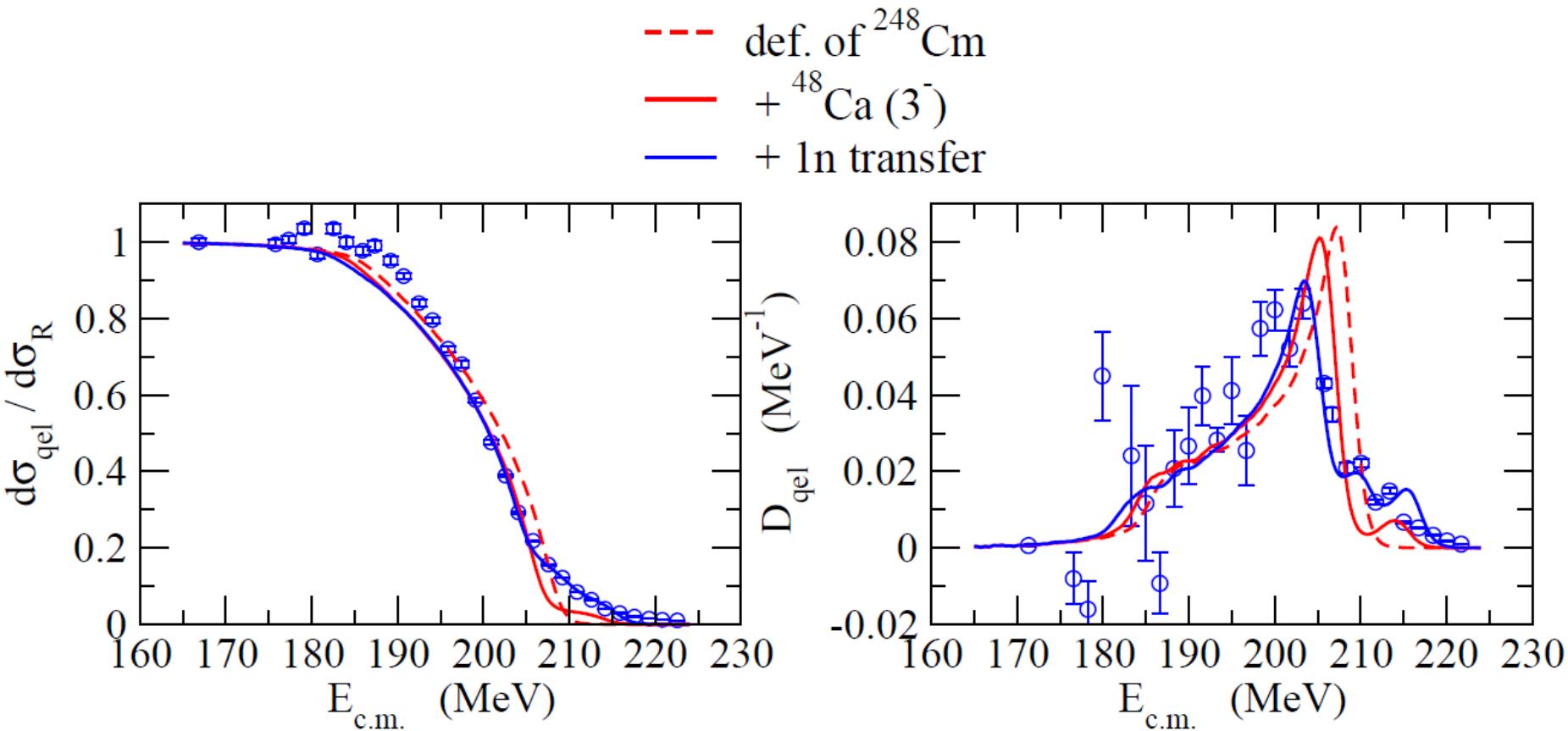
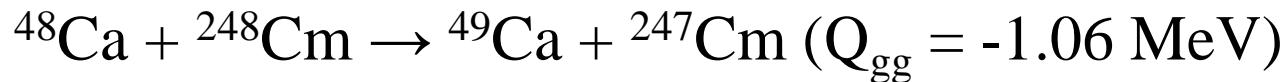


Analysis for a hot fusion reaction $^{48}\text{Ca} + ^{248}\text{Cm}$

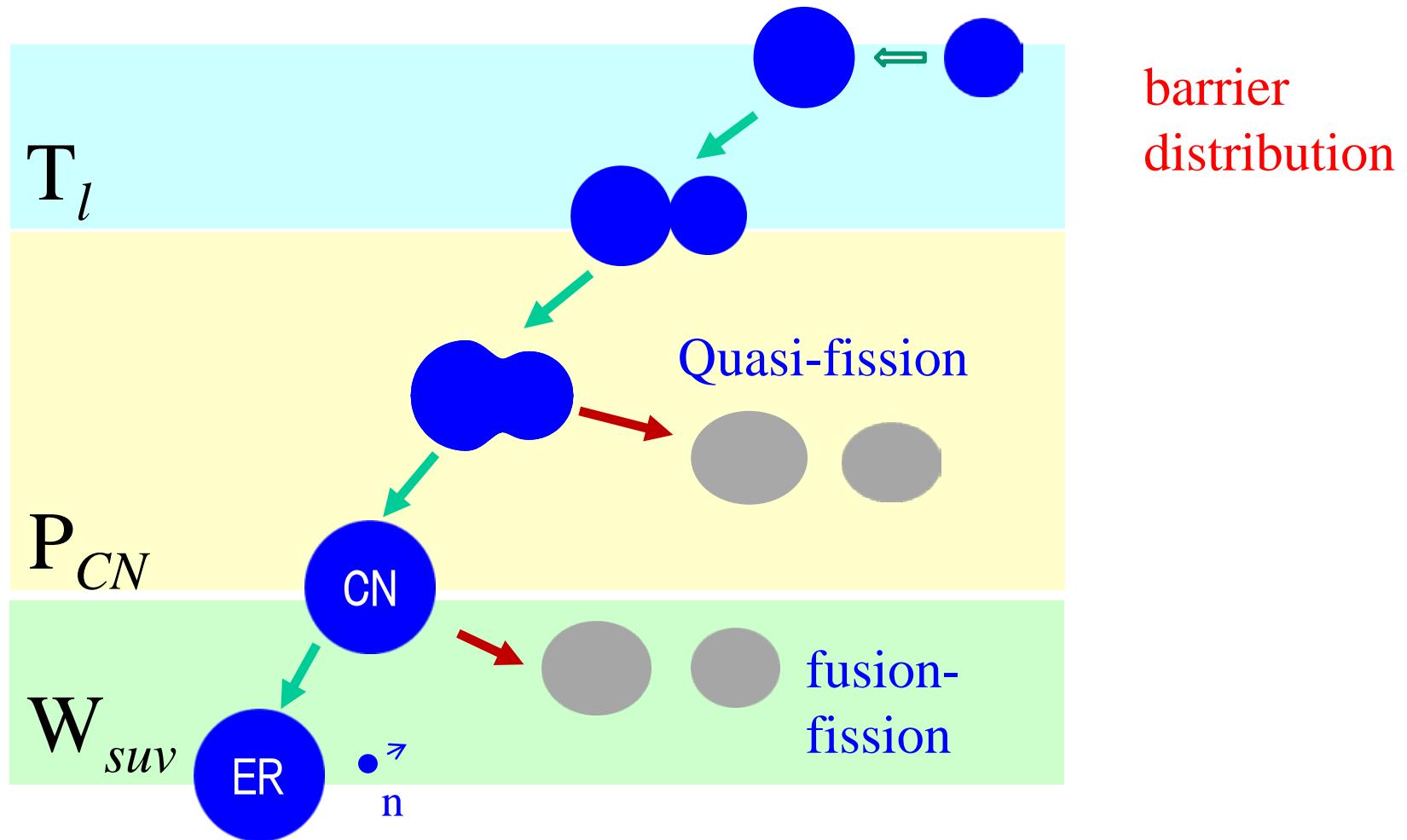
K.H. and T. Tanaka (2017)



1n transfer

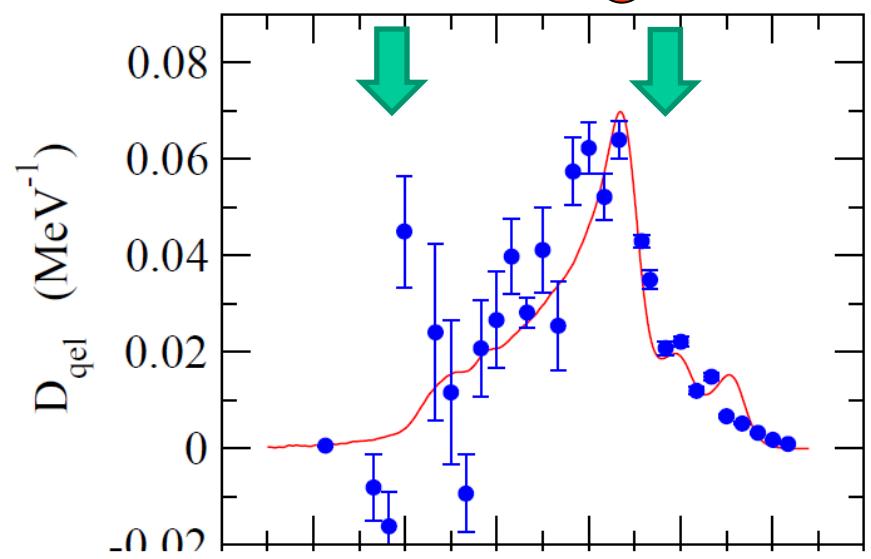
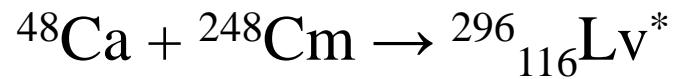
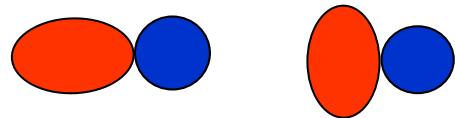


Connection to the ER cross sections

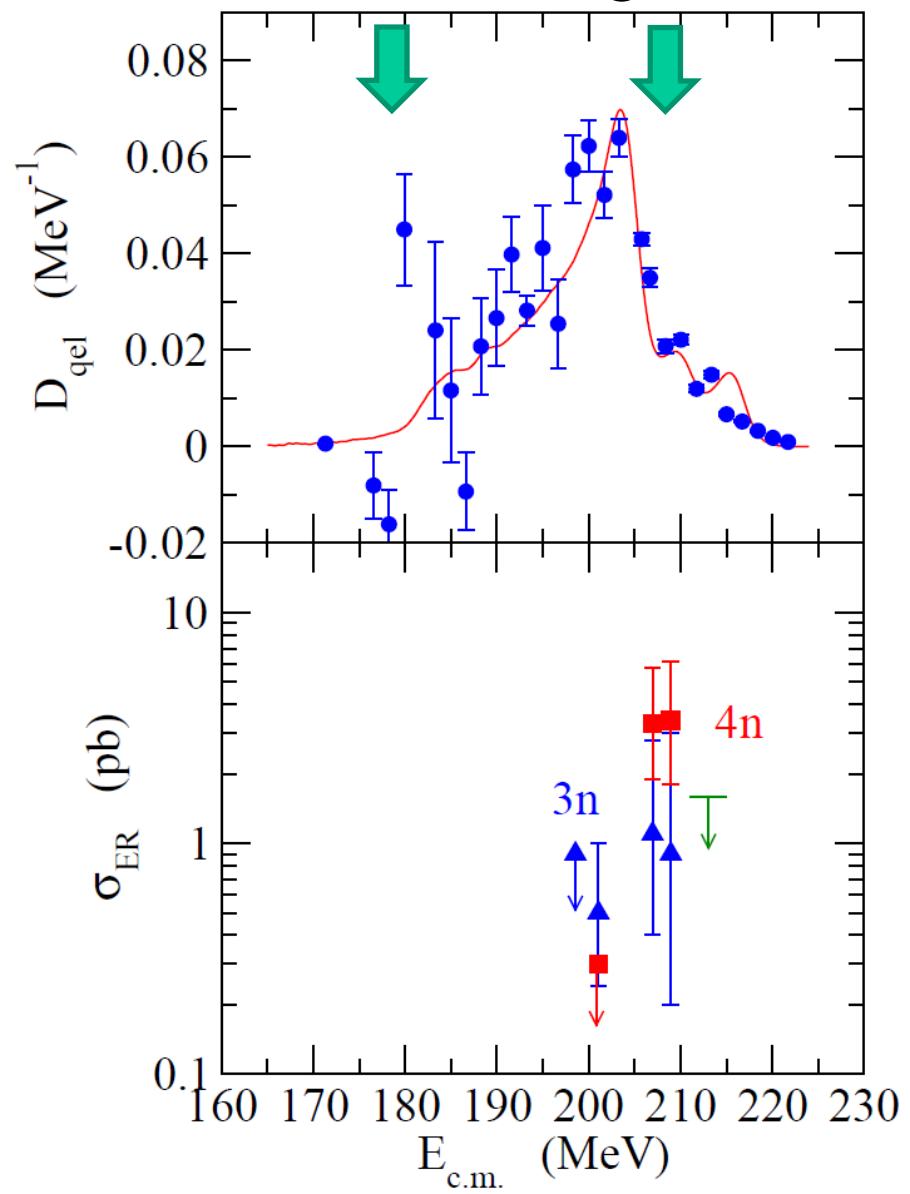
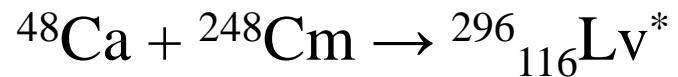
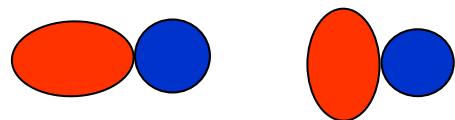


barrier
distribution

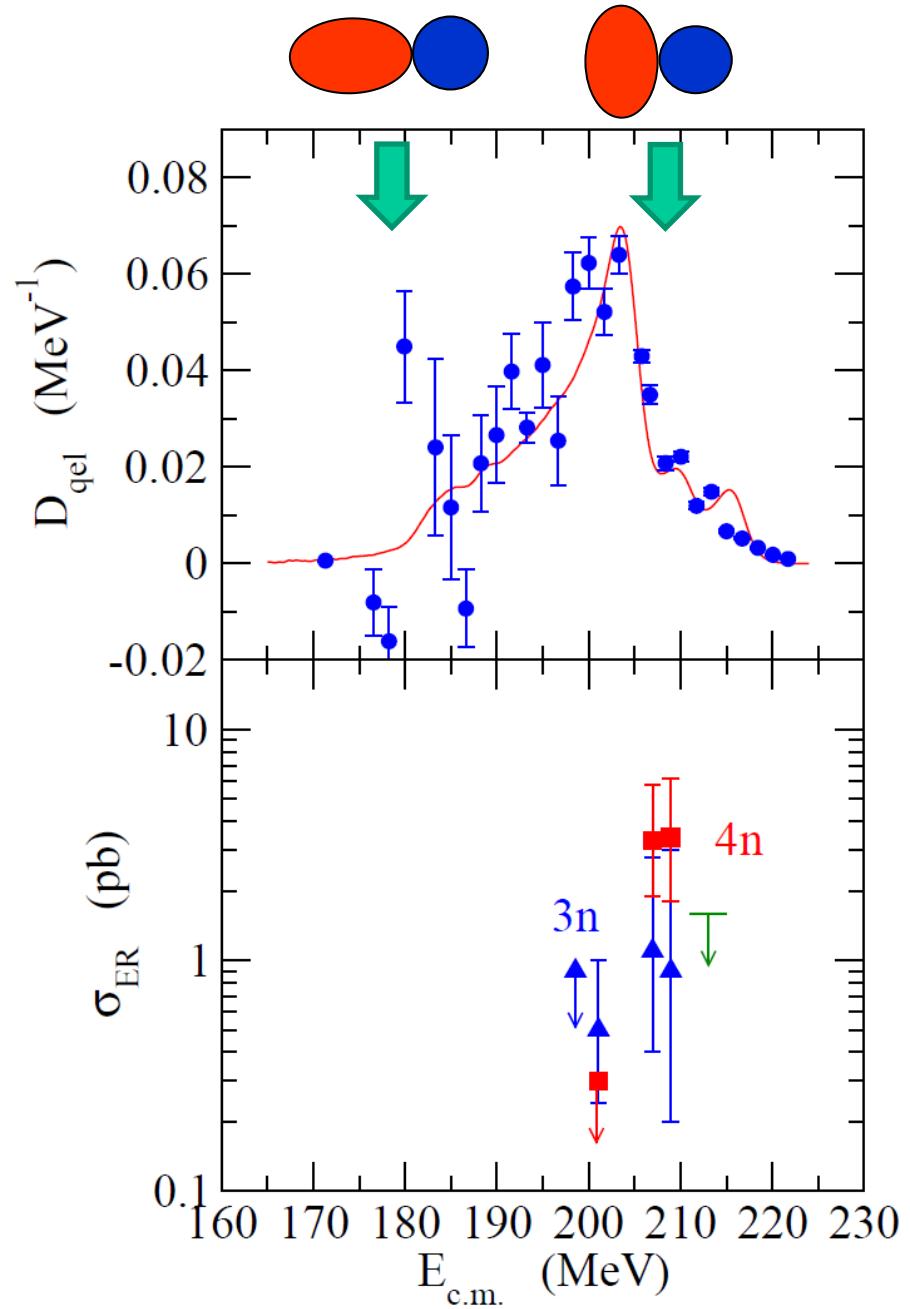
Connection to the ER cross sections



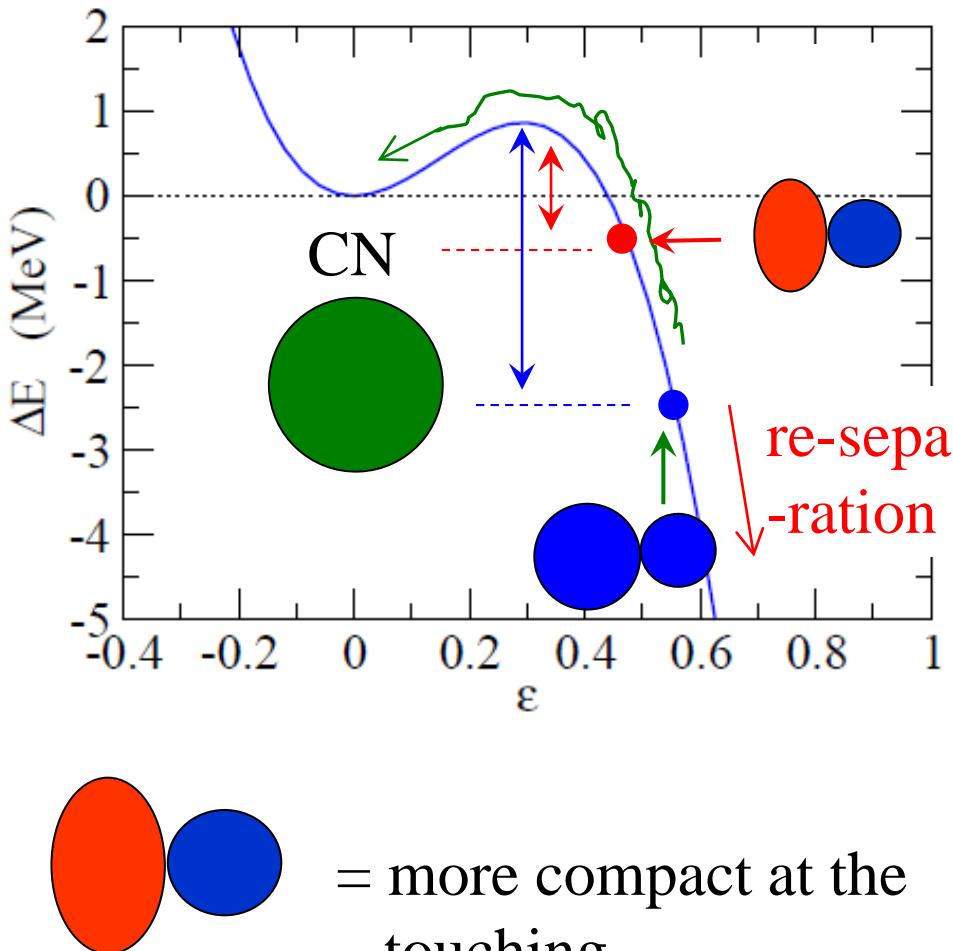
Connection to the ER cross sections



Connection to the ER cross sections

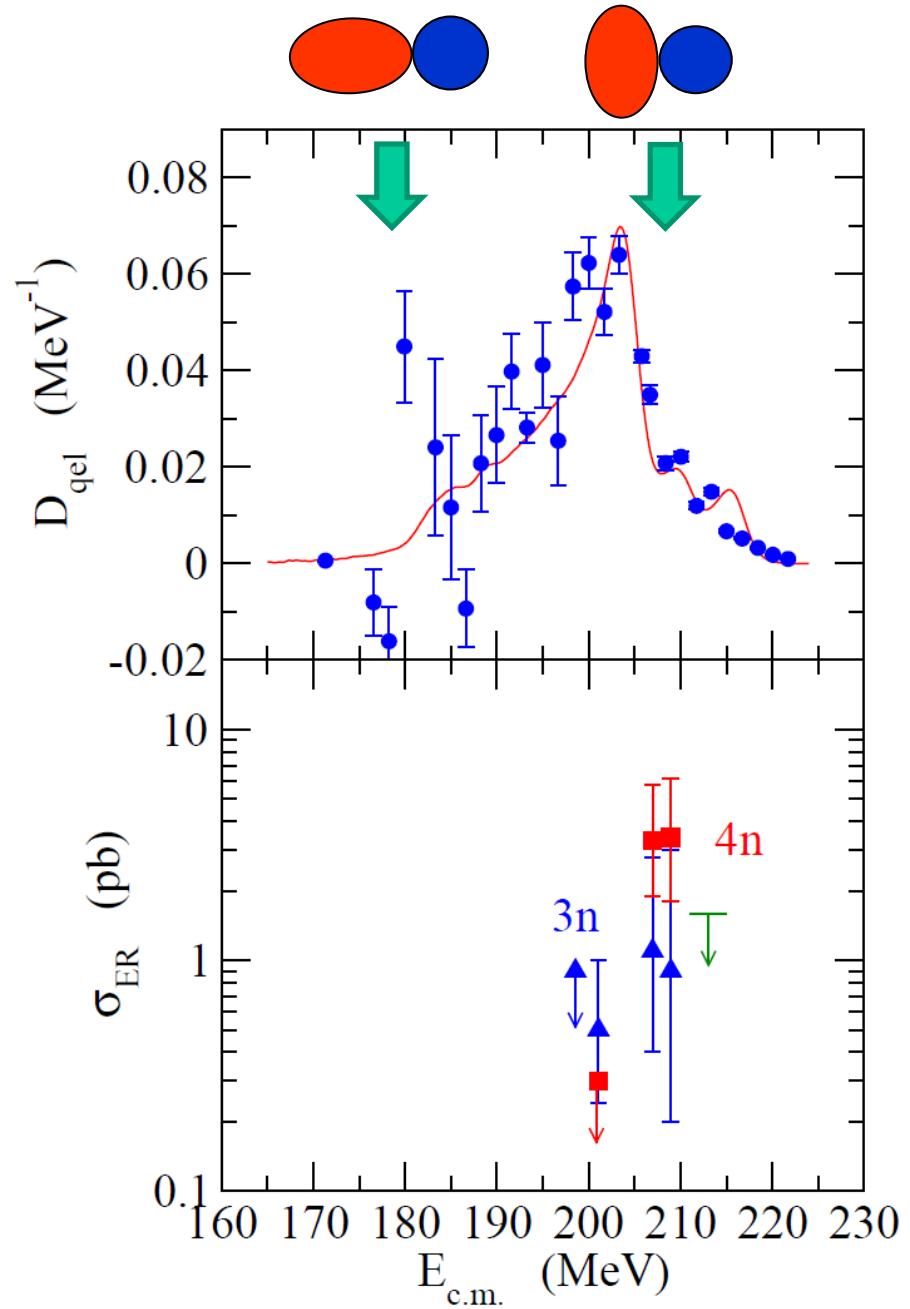


notion of compactness:
D.J. Hinde et al., PRL74 ('95) 1295

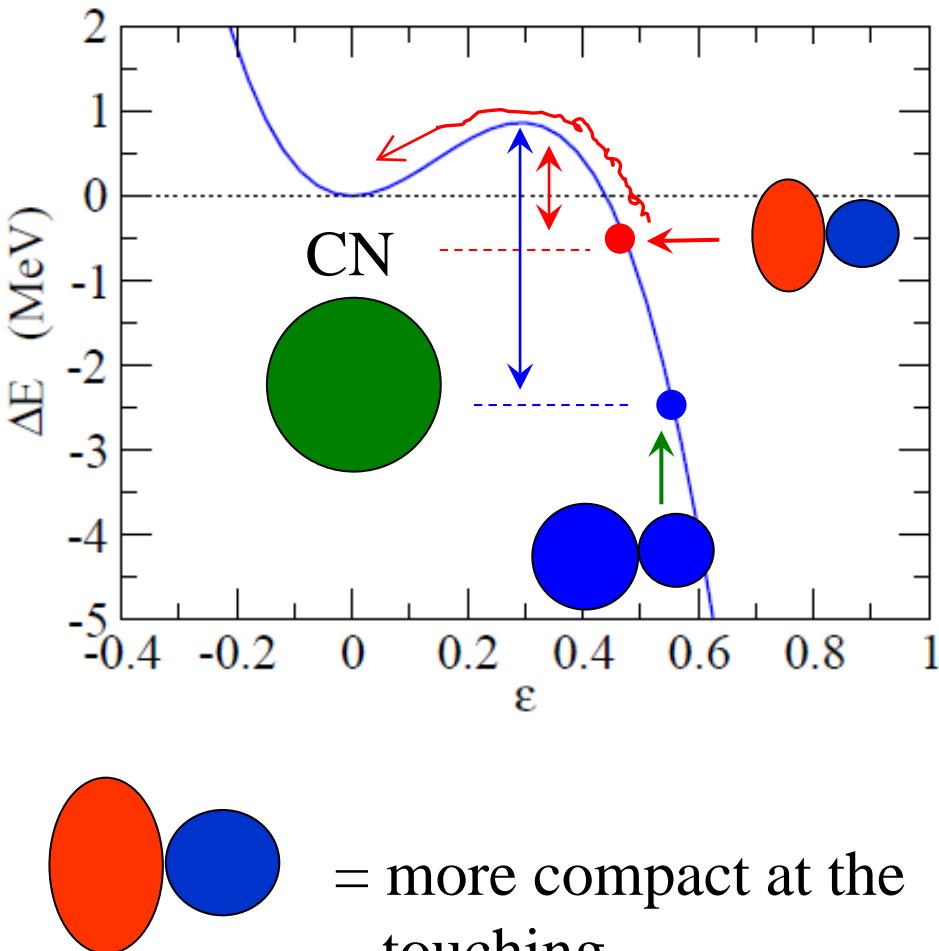


= more compact at the
touching
→ lower barrier height

Connection to the ER cross sections



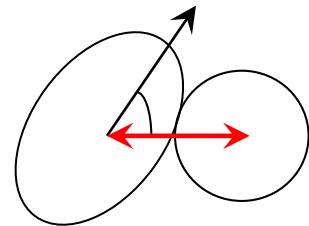
notion of compactness:
D.J. Hinde et al., PRL74 ('95) 1295



= more compact at the
touching
→ lower barrier height

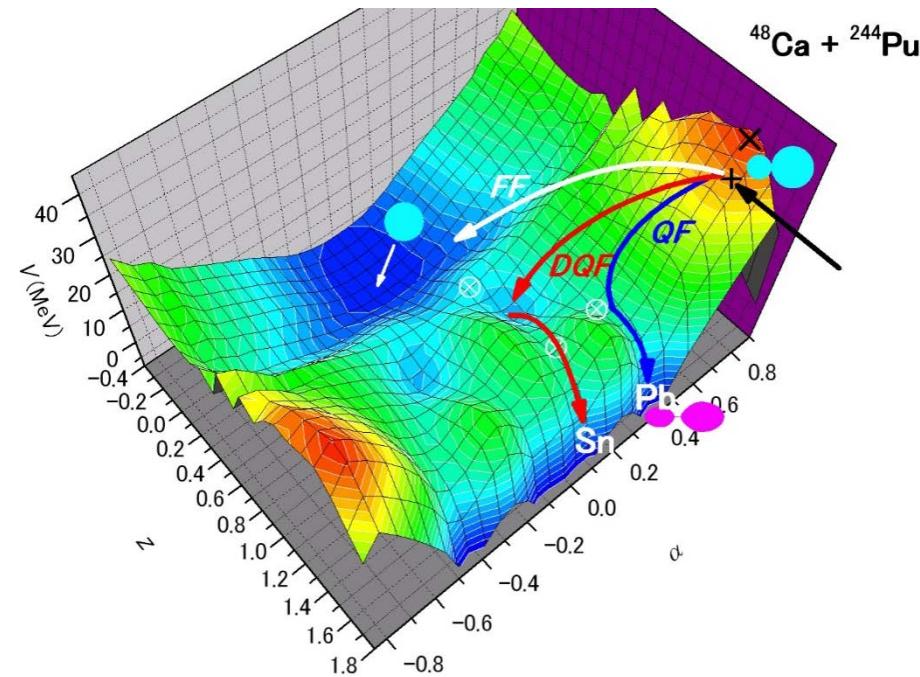
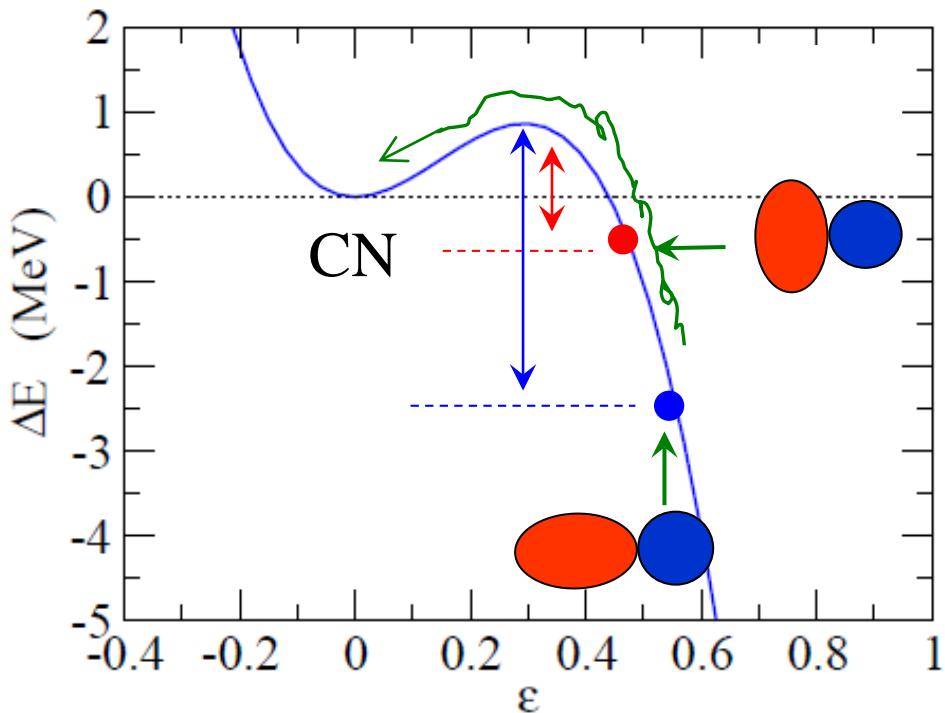
Connection to the ER cross sections

the initial (injection) point of a Langevin calculation:



$$s_{\text{inj}}(\theta)$$

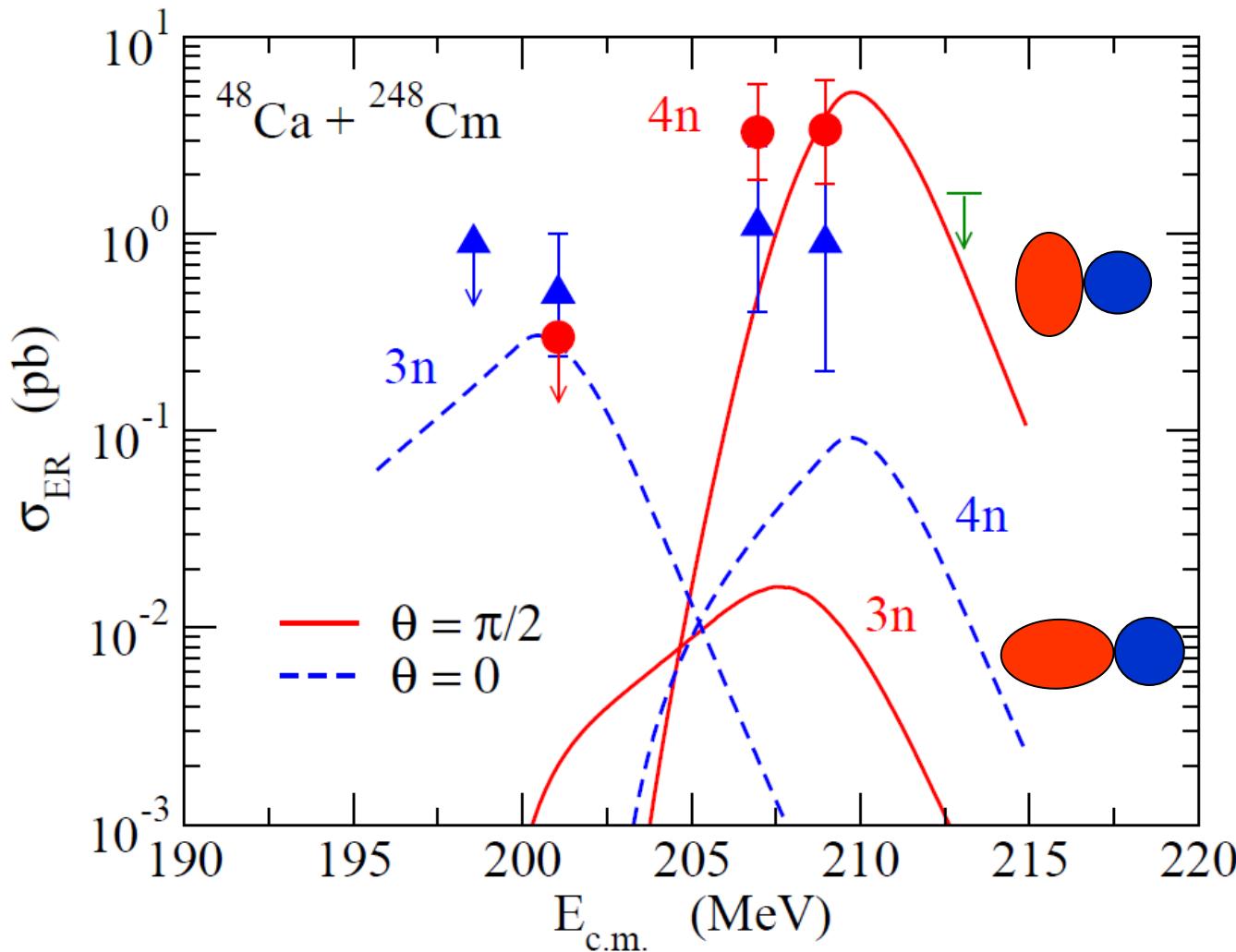
$$s_{\text{inj}}(\theta) = s_0 + \sum_{\lambda} R_T \beta_{\lambda} Y_{\lambda 0}(\theta)$$



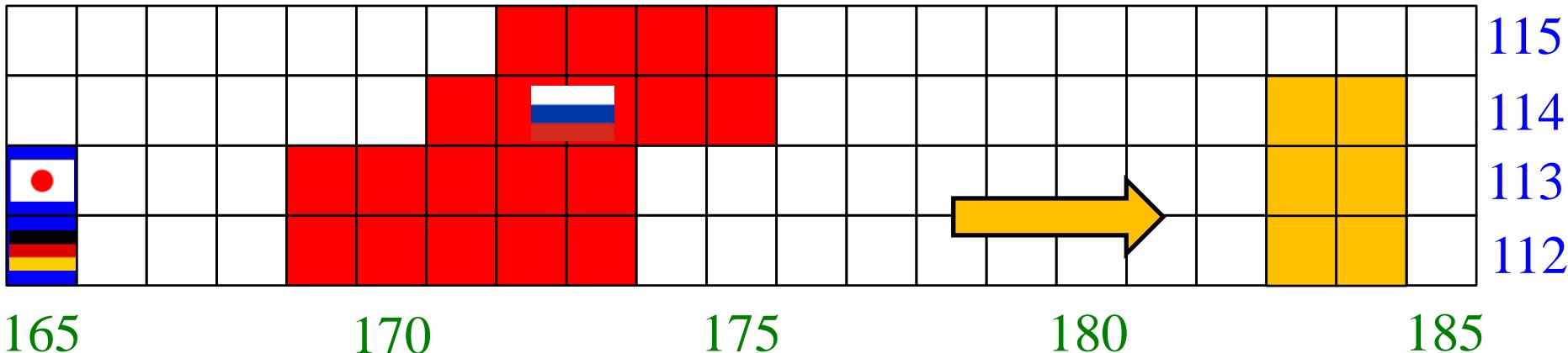
Y. Aritomo, K.H., K. Nishio,
S. Chiba, PRC85 ('12) 044614

role of orientation angle in ER cross sections

Fusion-by-diffusion model (Swiatecki) + deformation



Towards the island of stability



neutron-rich beams: indispensable

- how to deal with low beam intensity?
- reaction dynamics of neutron-rich beams?
 - ✓ capture: role of breakup and (multi-neutron) transfer?
 - ✓ diffusion: neutron emission during a shape evolution?
 - ✓ survival: validity of the statistical model?

structure of exotic nuclei

more studies are required

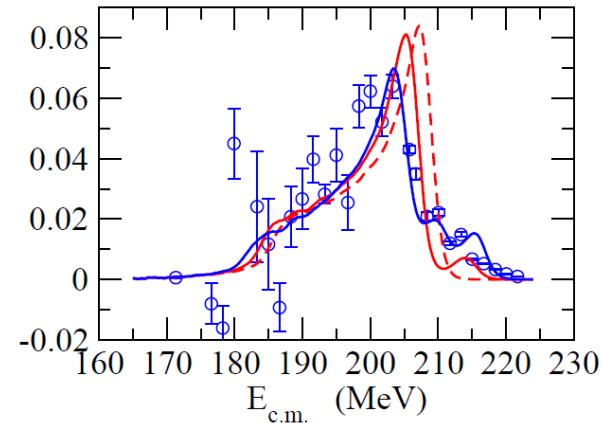
Summary

Reaction dynamics for SHE formation reactions

➤ Recent measurement of barrier distributions with GARIS

- ✓ $^{48}\text{Ca} + ^{248}\text{Cm}$
- ✓ coupled-channels analysis
- ✓ notion of compactness: ER formation with side collisions

more data coming soon



➤ Open problems

- ✓ ^{48}Ca projectile $\rightarrow ^{50}_{22}\text{Ti}, ^{51}_{23}\text{V}, ^{54}_{24}\text{Cr}$ projectiles etc.

how much cross sections will be altered?

- ✓ shape evolution with a deformed target?

how does the deformation disappear during heat-up?

cf. Nakatsukasa-san's conjecture?

- ✓ reaction dynamics with neutron-rich nuclei?

formation of SHE

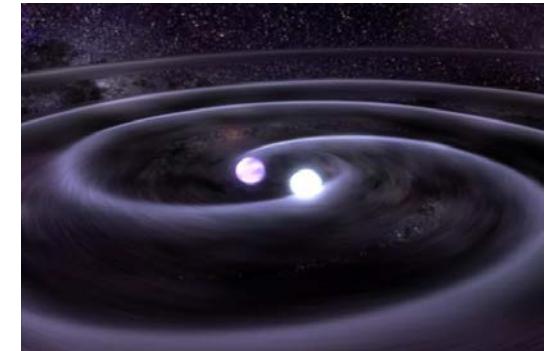


chemistry of SHE

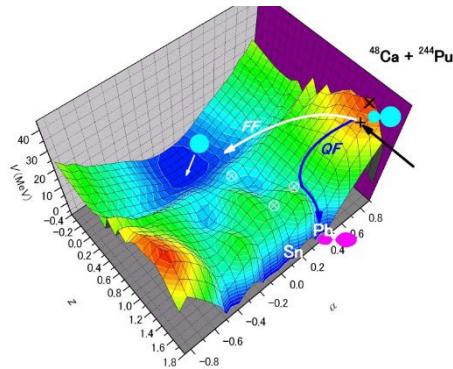
the origin of (S)HE

A periodic table of elements where each element is represented by a small image of its corresponding atom. The table is color-coded by group: 1 (yellow), 2 (orange), 3 (red), 4 (pink), 5 (purple), 6 (blue), 7 (teal), and 18 (light blue). The table includes all elements from hydrogen (H) to oganesson (Og), with some elements marked with an asterisk (*) indicating they are synthetic.

Group	Period	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18
	1	H															He		
	2	Li	Be															Ne	
	3	Na	Mg															Ar	
	4	K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Xe
	5	Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Pt	Cd	In	Sn	Sb	Te	I	Xe
	6	Cs	Ba	La	Hf	Ta	W	Re	Osm	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
	7	Fr	Ra	Ac	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og
*		58	59	60	61	62	63	64	65	66	67	68	69	70	71				
*		90	91	92	93	94	95	96	97	98	99	100	101	102	103				



reaction dynamics



structure of SHE



Haba-san's talk

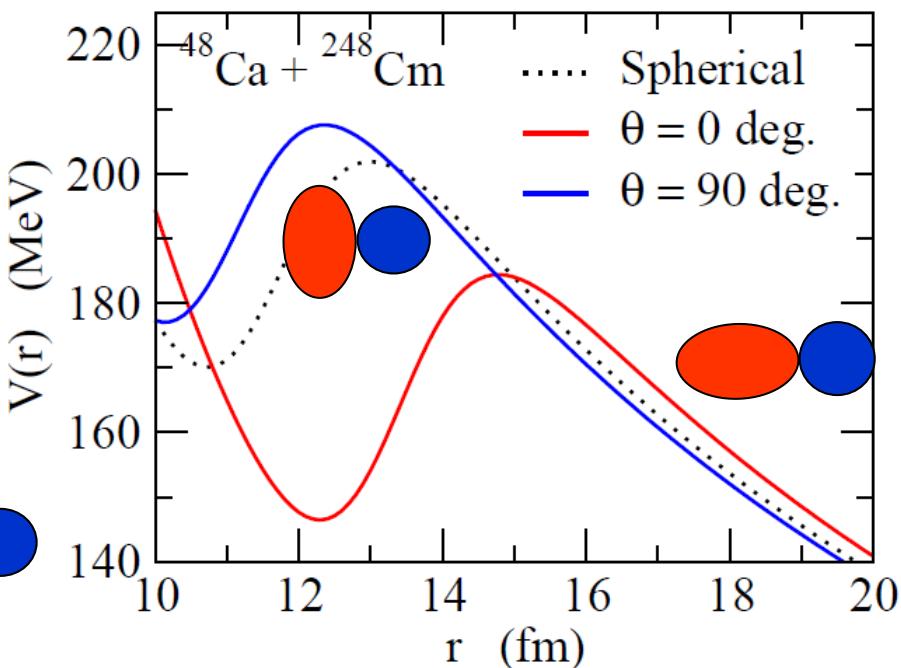
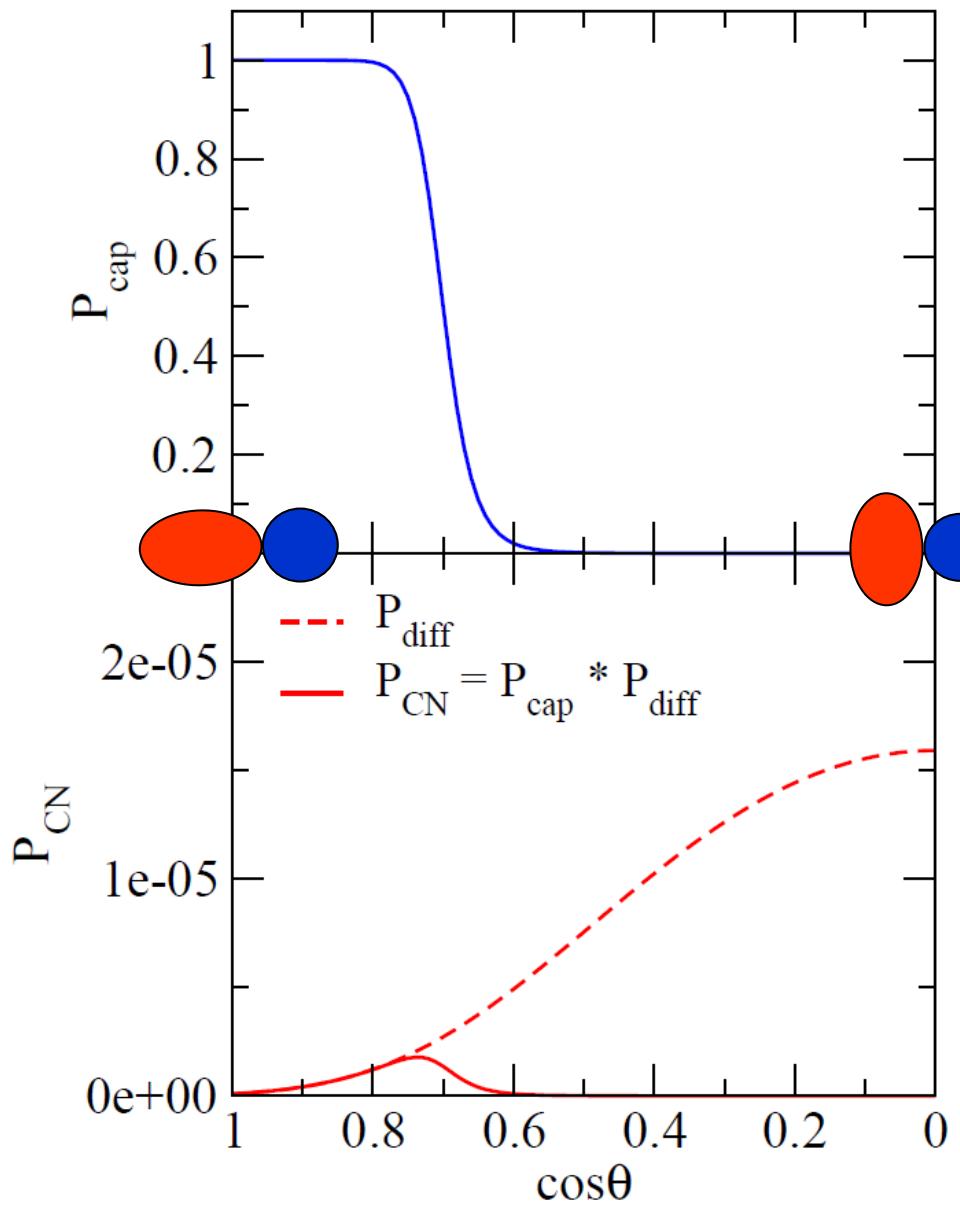
Nuclear Physics (RIBF) Astrophysics

sessions in this morning

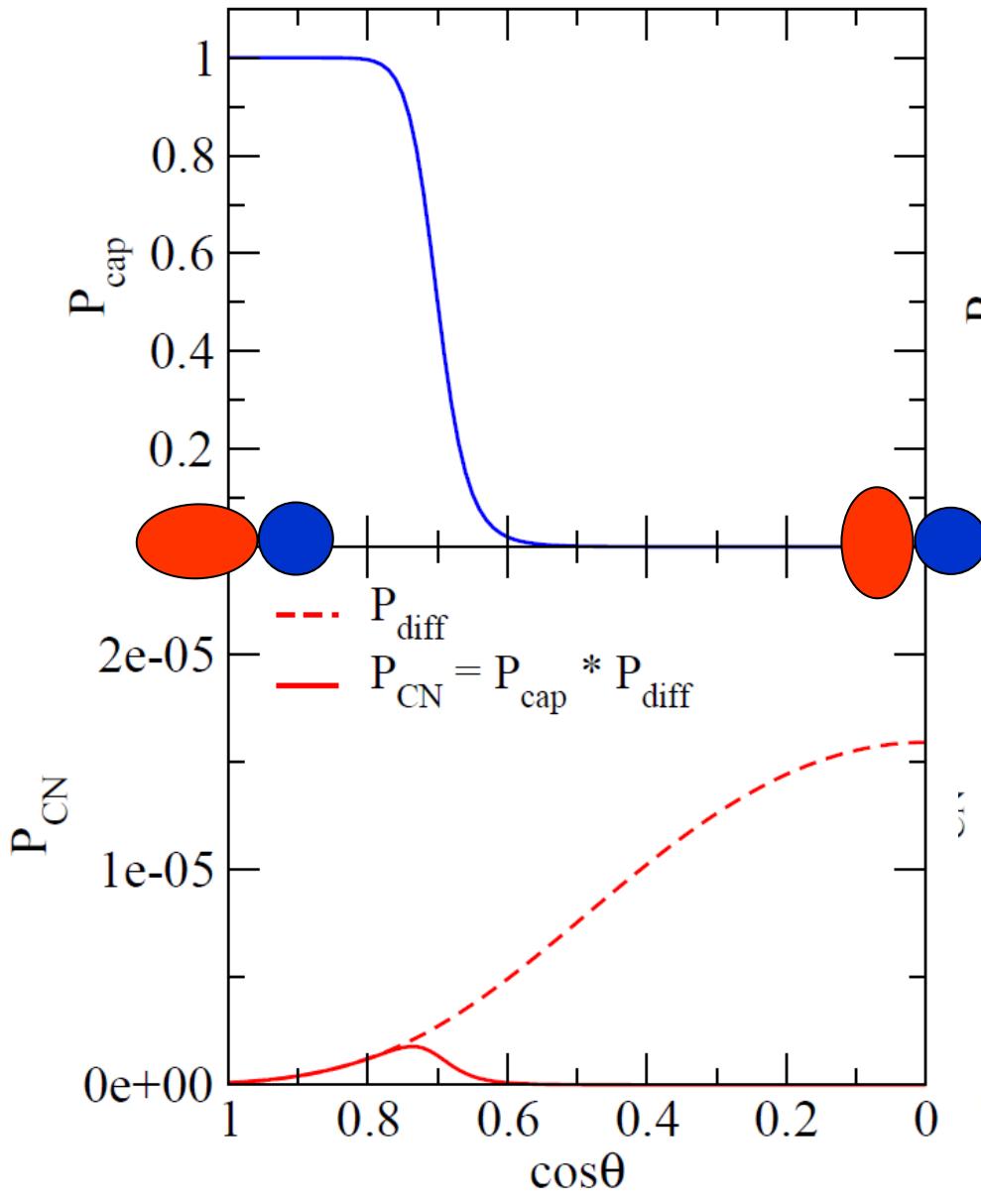
interdisciplinary SHE science

with physics, chemistry, and astronomy

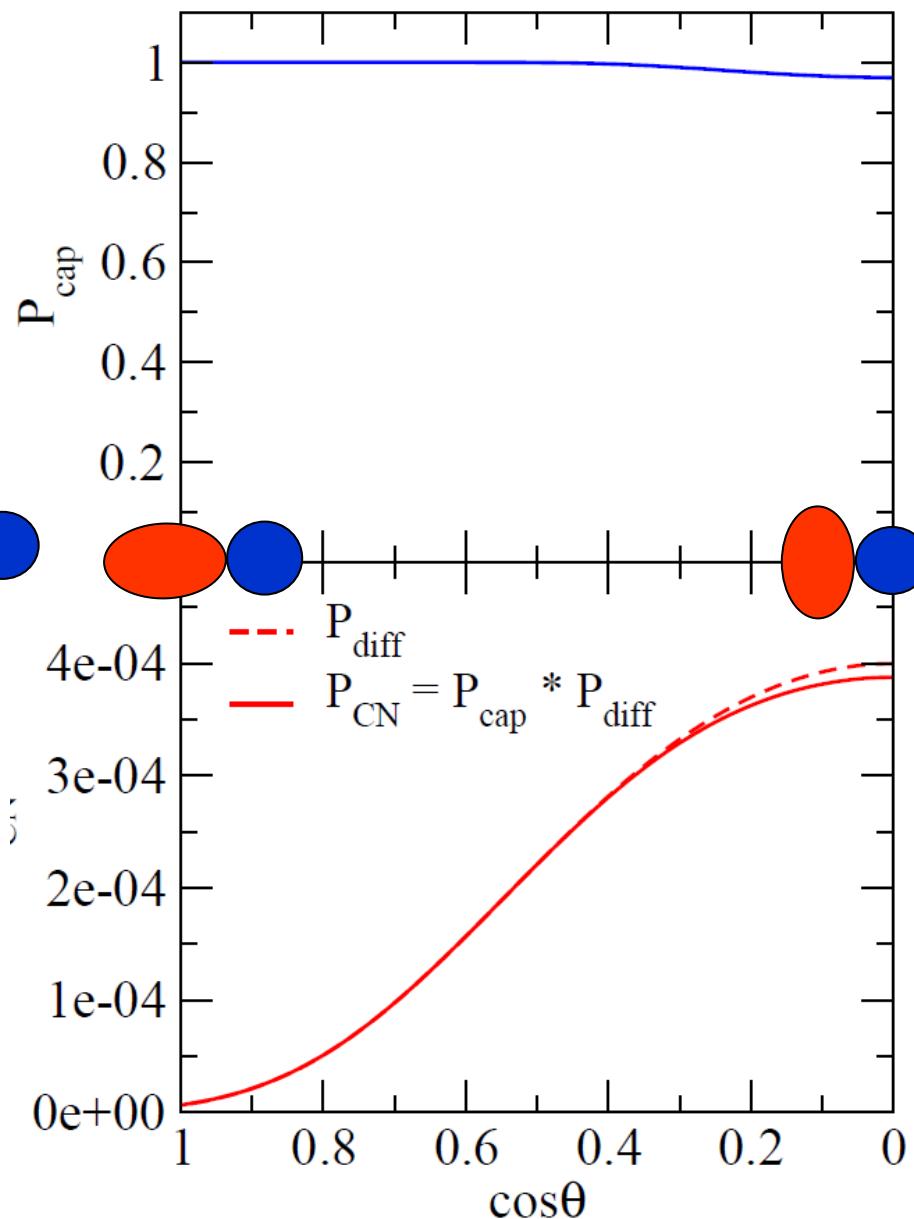
$E_{\text{c.m.}} = 200 \text{ MeV}, l = 0$



$E_{\text{c.m.}} = 200 \text{ MeV}, l = 0$



$E_{\text{c.m.}} = 210 \text{ MeV}, l = 0$



Recent application to SHE : Quasi-elastic B.D.

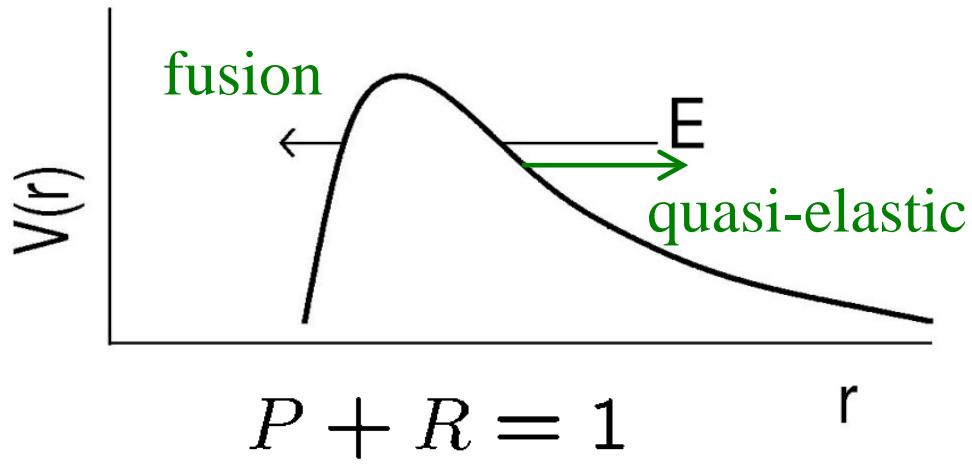
hot fusion reactions



= deformation



reaction dynamics with barrier distributions?



Quasi-elastic scattering
: reflected flux at the barrier

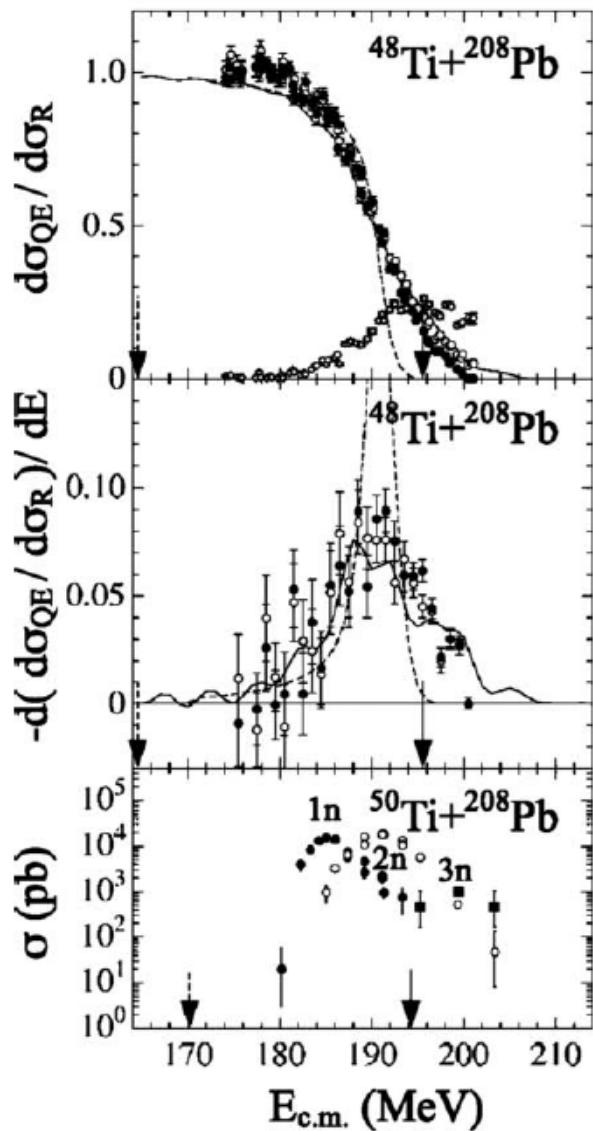
- a sum of elastic, inelastic, and transfer
- easier to measure than capture

Quasi-elastic barrier distribution

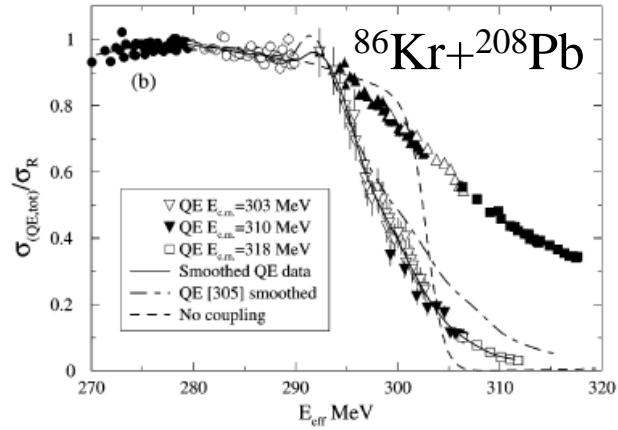
$$D_{\text{qel}}(E) = -\frac{d}{dE} \left(\frac{\sigma_{\text{qel}}(E, \pi)}{\sigma_R(E, \pi)} \right)$$

H. Timmers et al., NPA584('95)190
K.H. and N. Rowley, PRC69('04)054610

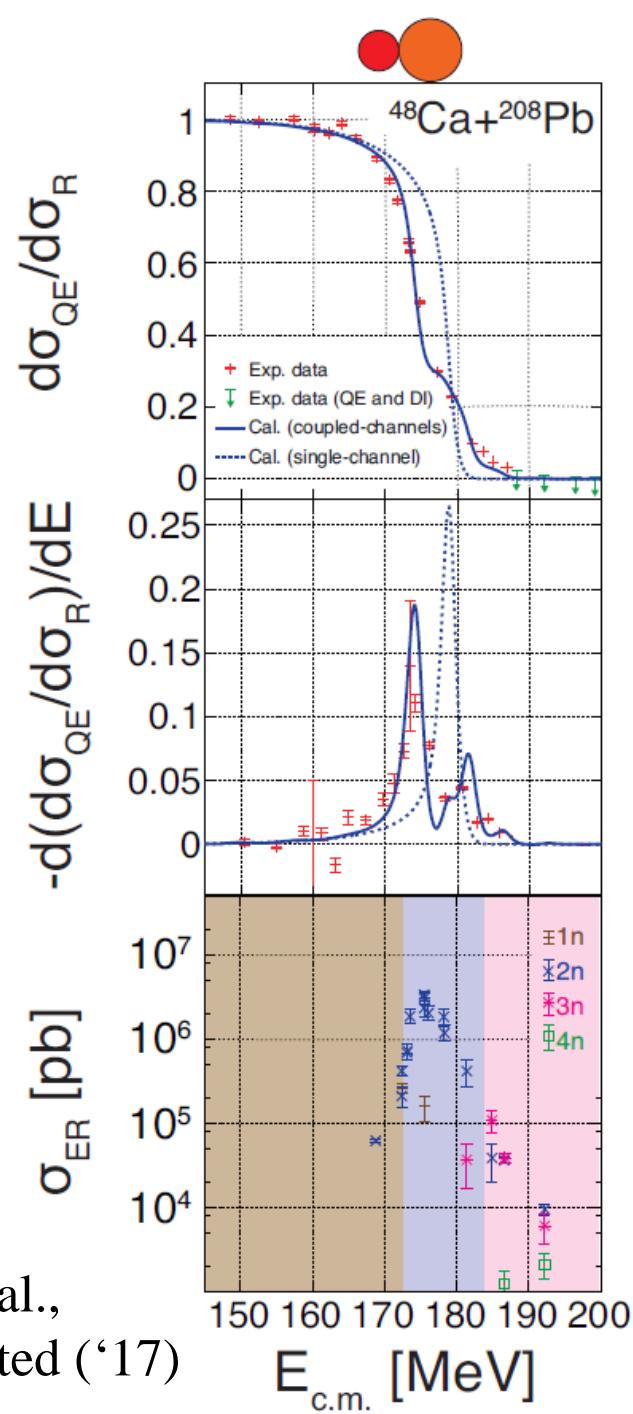
previous attempts



S. Mitsuoka et al.,
PRL99 ('07) 182701

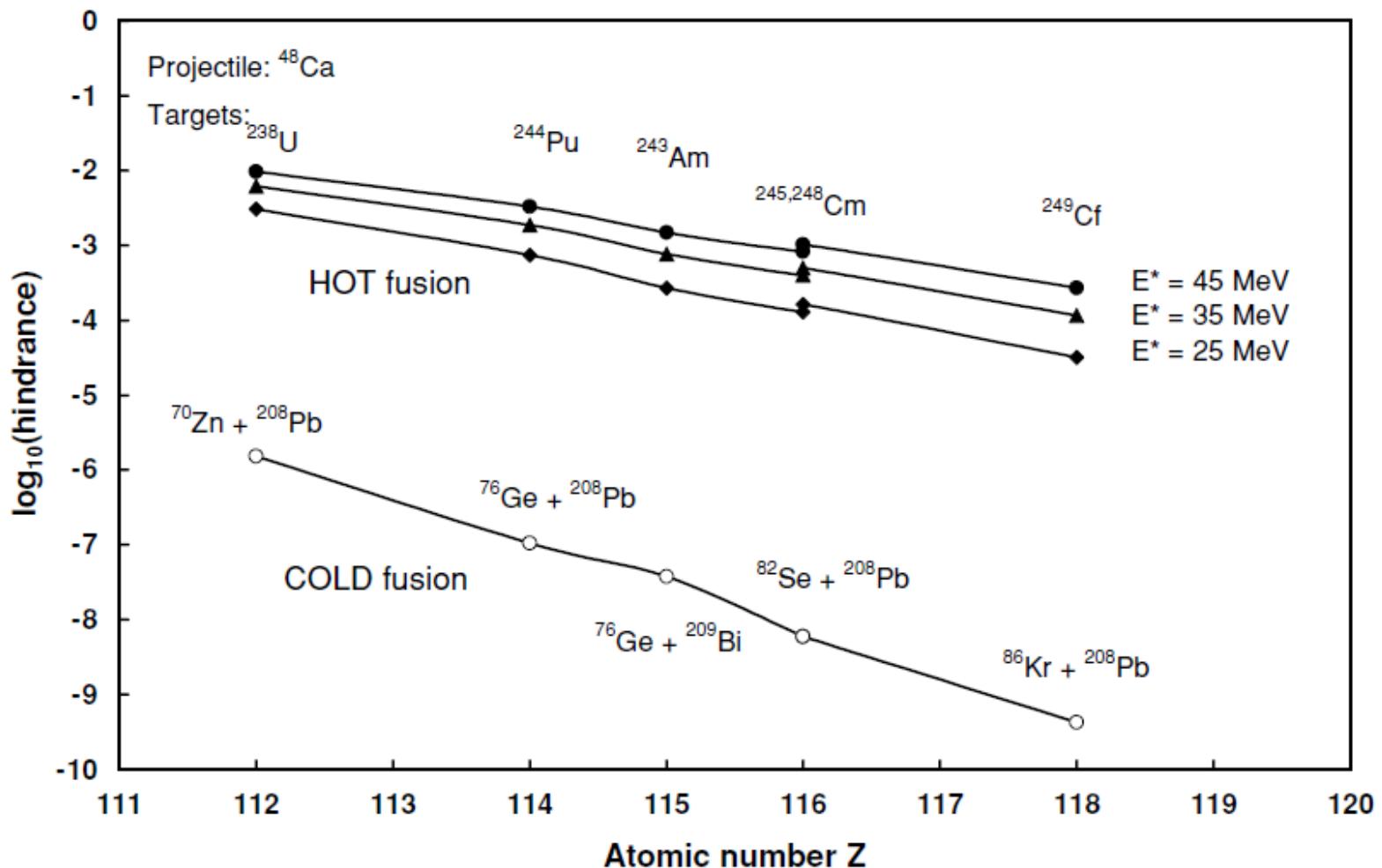


S.S. Ntshangase et al.,
PLB651 ('07) 27



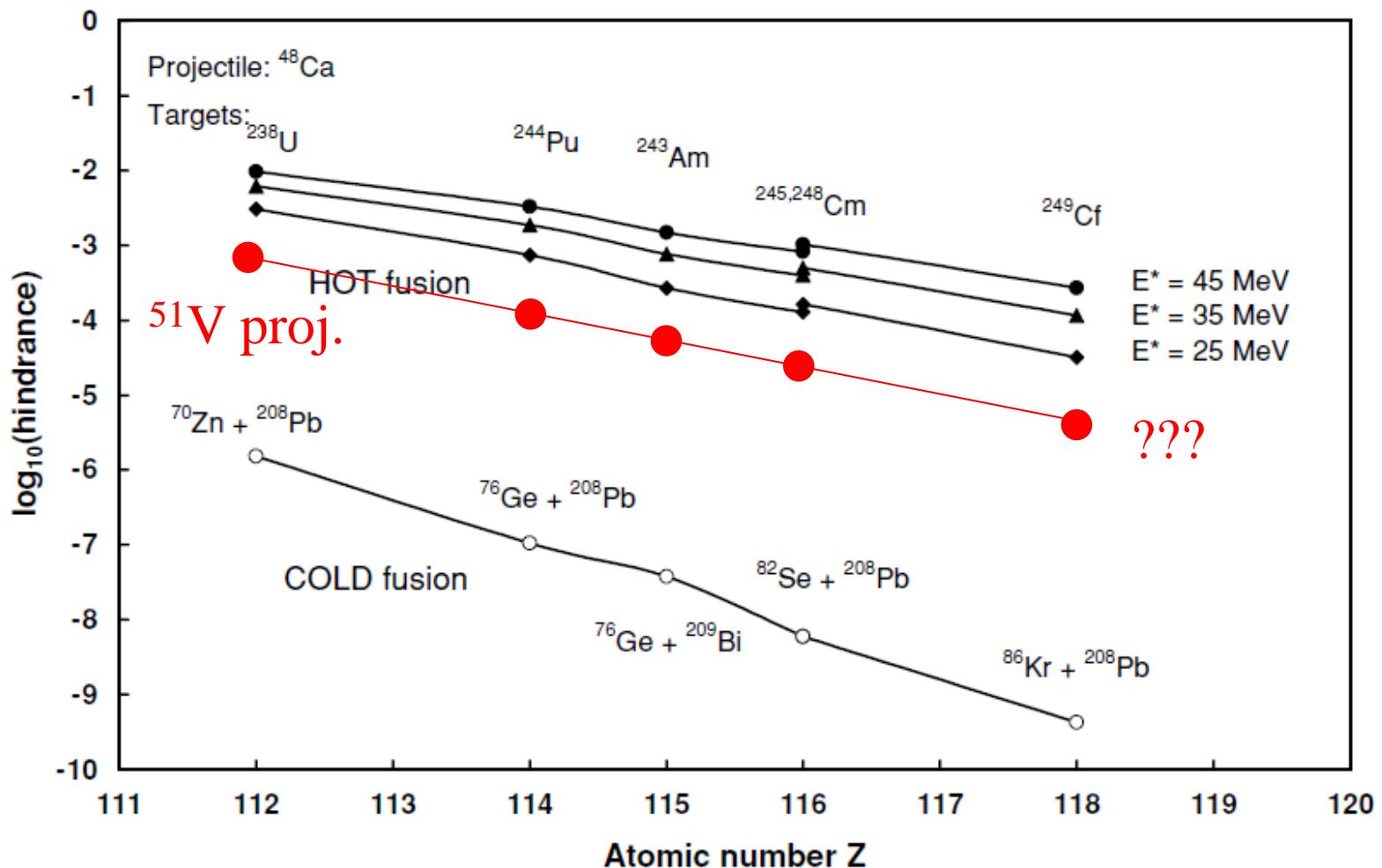
T. Tanaka et al.,
JPSJ, submitted ('17)

fusion-by-diffusion model

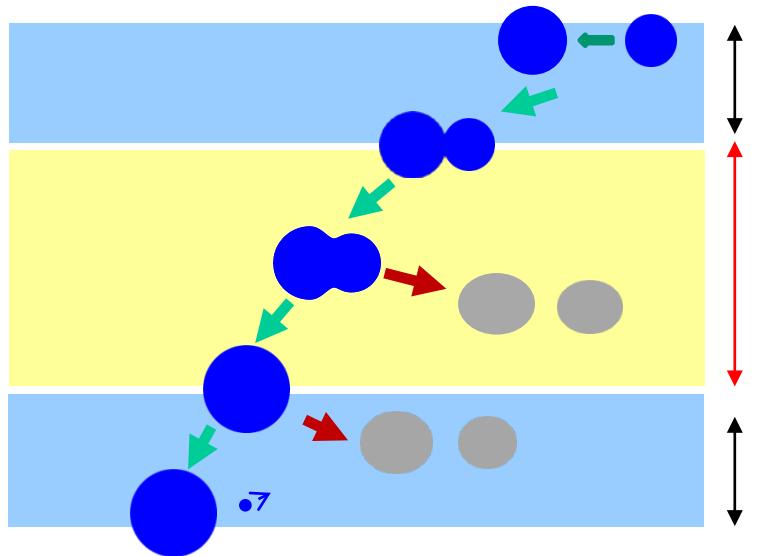


W.J. Swiatecki, K. Siwek-Wilczynska, and J. Wilczynski,
PRC71 ('05) 014602

fusion-by-diffusion model



Super-heavy nuclei



coupled-channels method

Langevin approach

V.I. Zagrebaev and W. Greiner, NPA944('15)257

$$m \frac{d^2 q}{dt^2} = -\frac{dV(q)}{dq} - \gamma \frac{dq}{dt} + R(t)$$

statistical model

