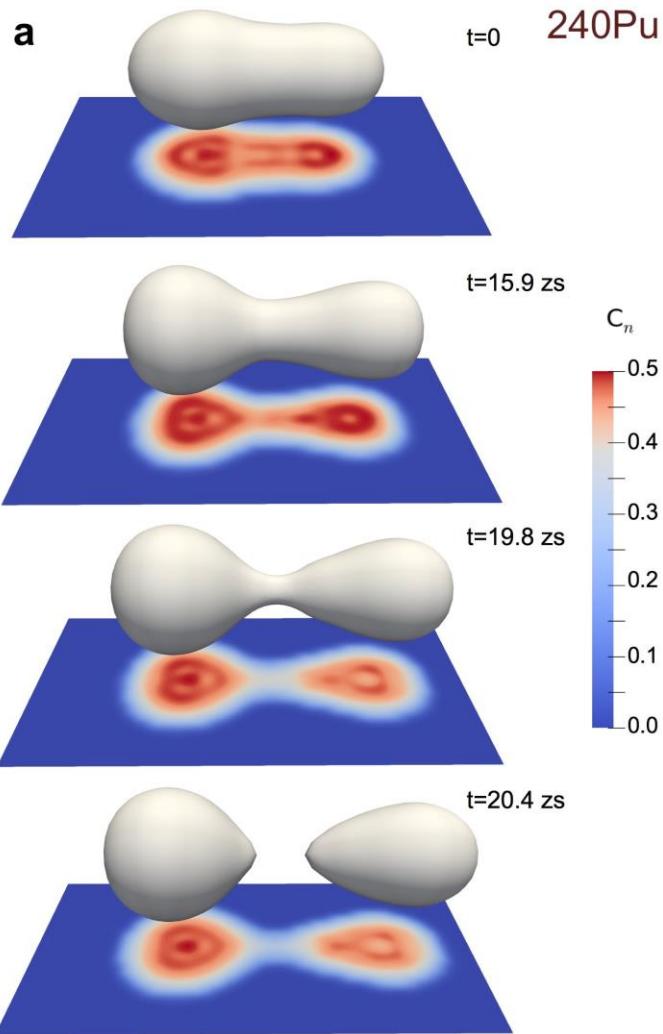


# rプロセスと核分裂:問題提起

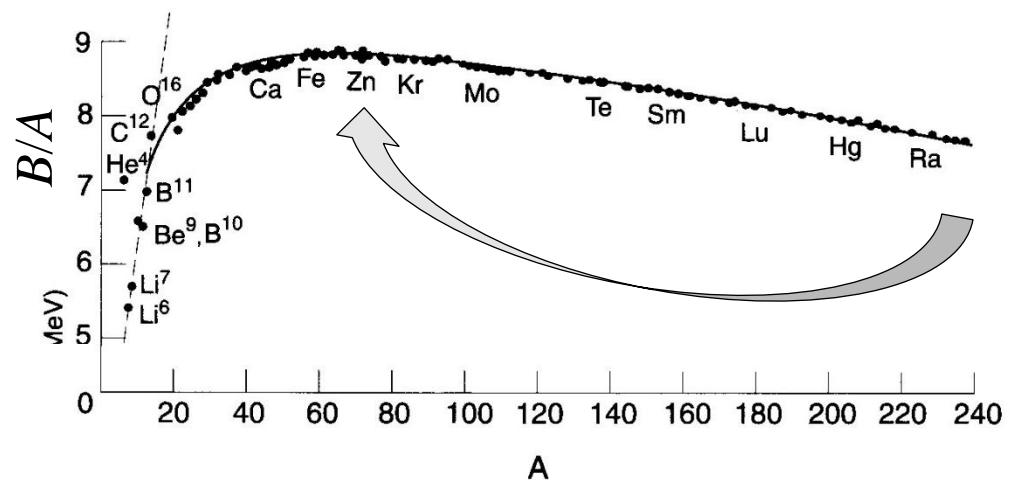
萩野浩一  
京都大学大学院理学研究科



1. introduction: 核分裂のオーバービュー
2. r-process と核分裂:何が問題になるのか?
3. 微視的アプローチの必要性
4. CI アプローチの可能性(最近考えていること)
5. まとめ



- discovered about 80 years ago (in 1938) by Hahn and Strassmann
- a primary decay mode of heavy nuclei

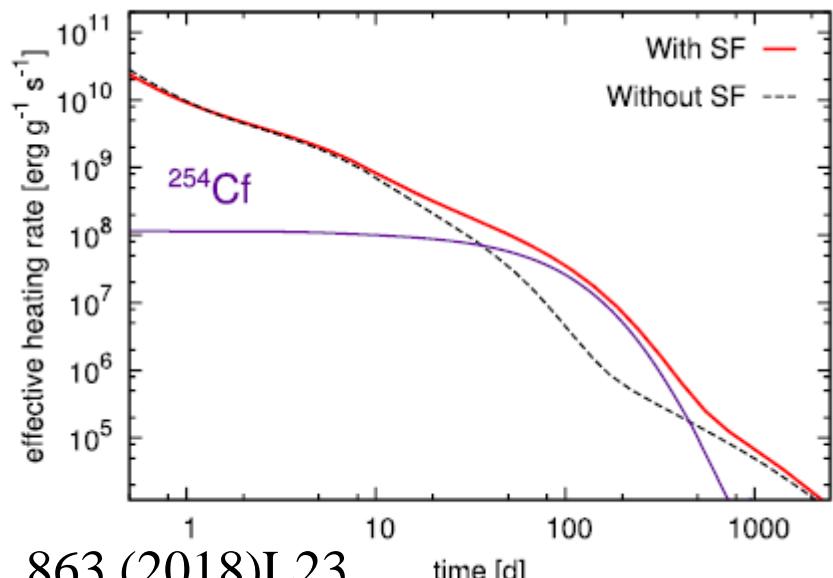
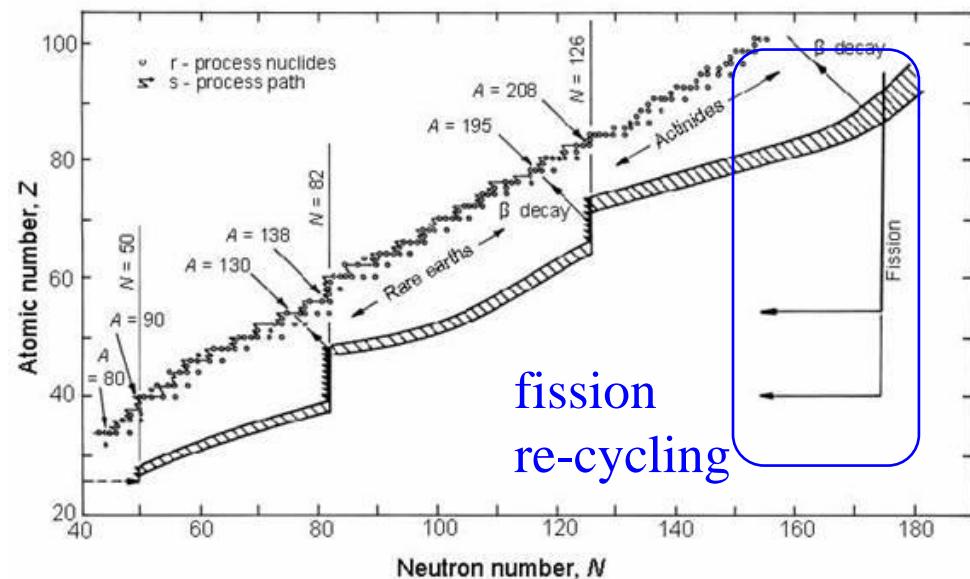
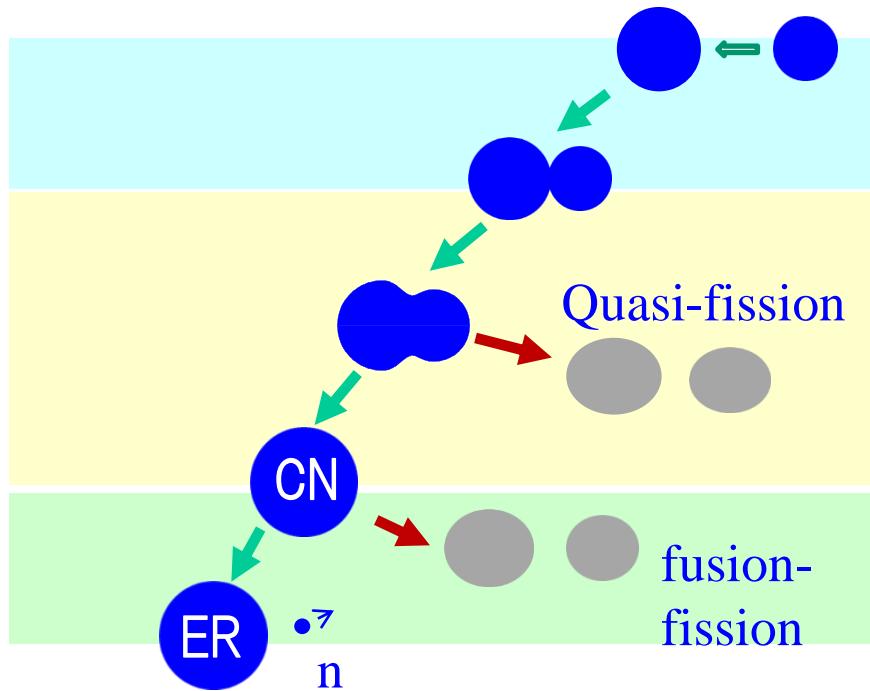


- important role in:
  - energy production
  - superheavy elements
  - r-process nucleosynthesis
  - production of neutron-rich nuclei

G. Scamps and C. Simenel,  
Nature 564 (2018) 382

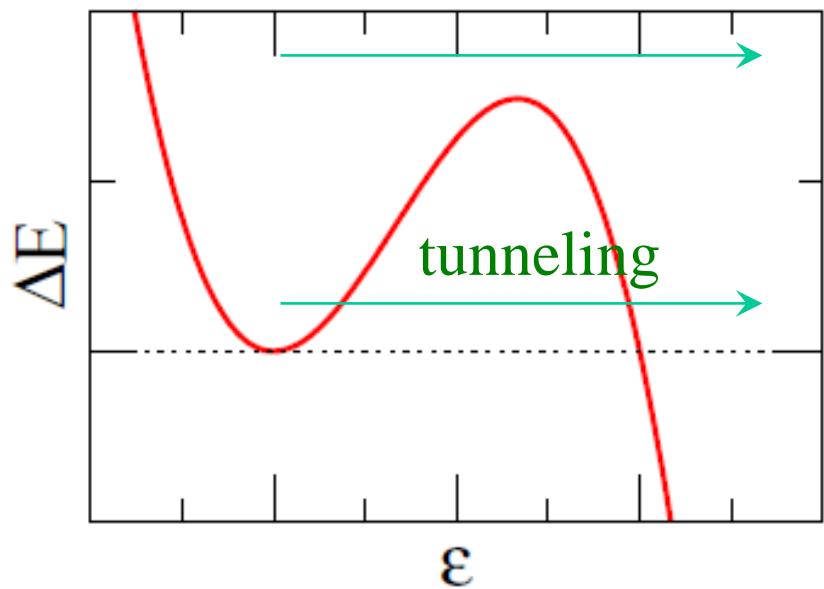
# fission in r-process nucleosynthesis

fission in SHE



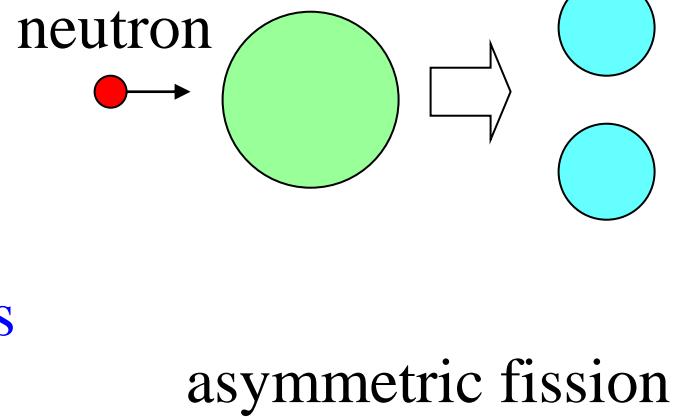
Y. Zhu et al.,  
Astrophys. J. Lett. 863 (2018)L23

## ➤ various fission processes

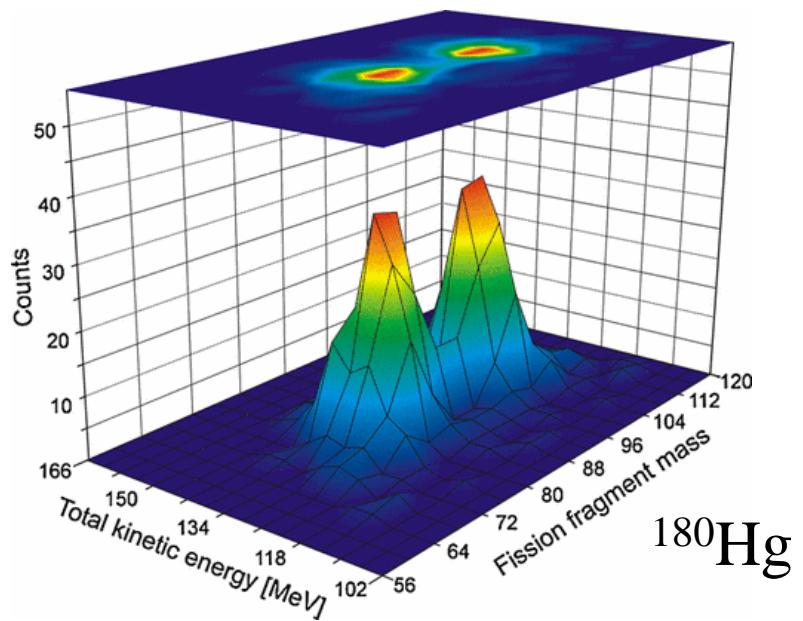


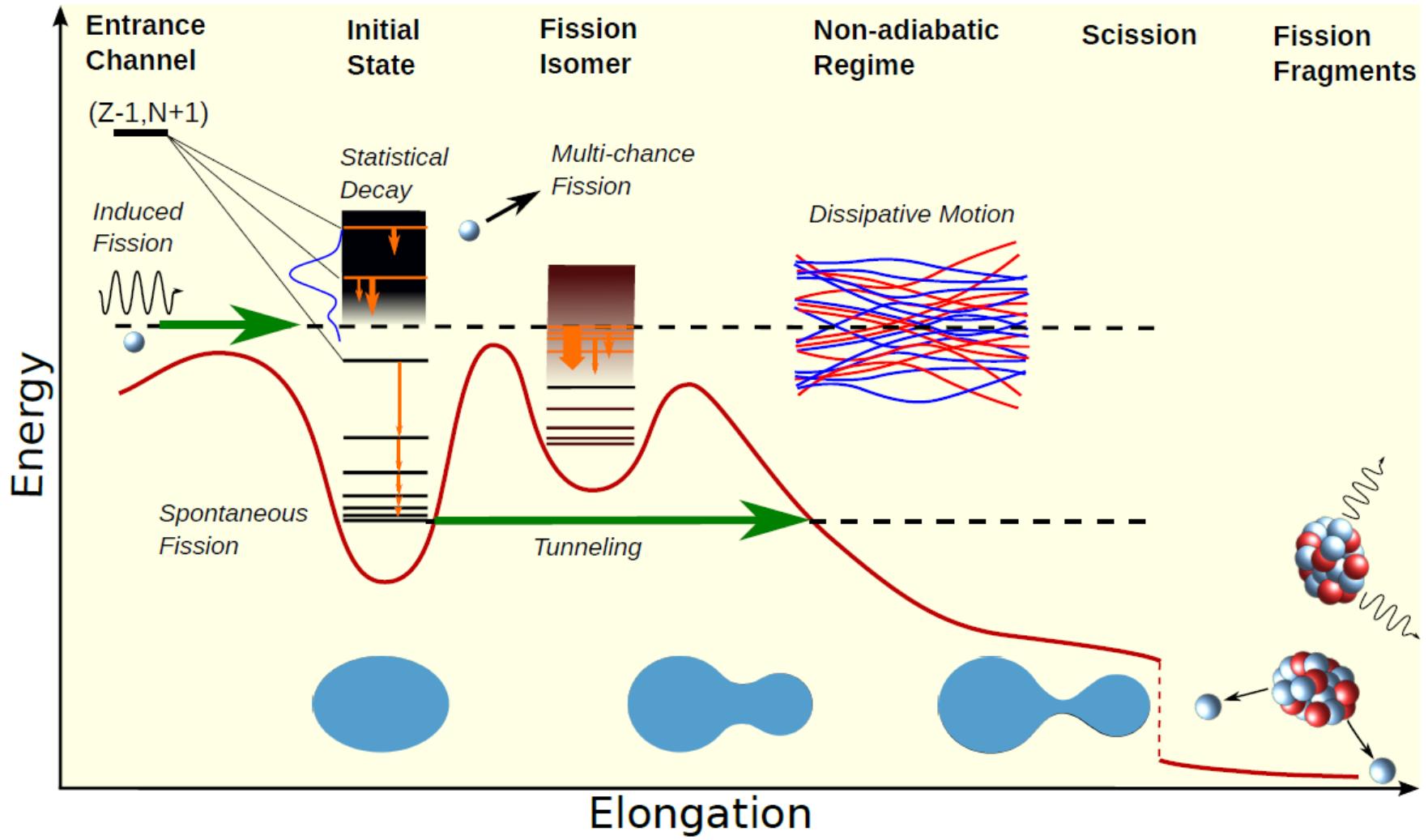
induced  
fission

spontaneous  
fission



beta-delayed fission

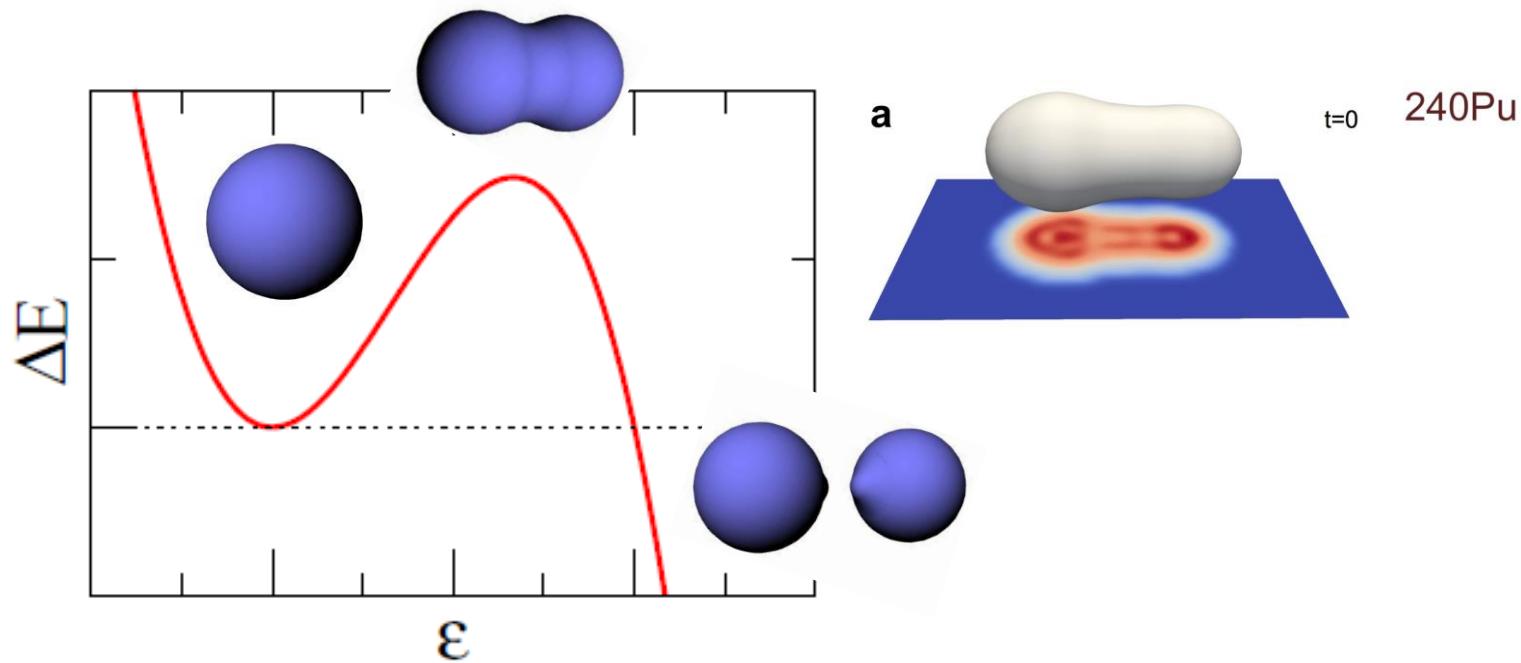




“Future of fission theory”

M. Bender et al., J. of Phys. G47, 113002 (2020)

- macroscopic understanding:  
competition between the surface and the Coulomb energies  
→ fission barrier



- a microscopic understanding:  
far from complete!
  - ✓ large amplitude motion

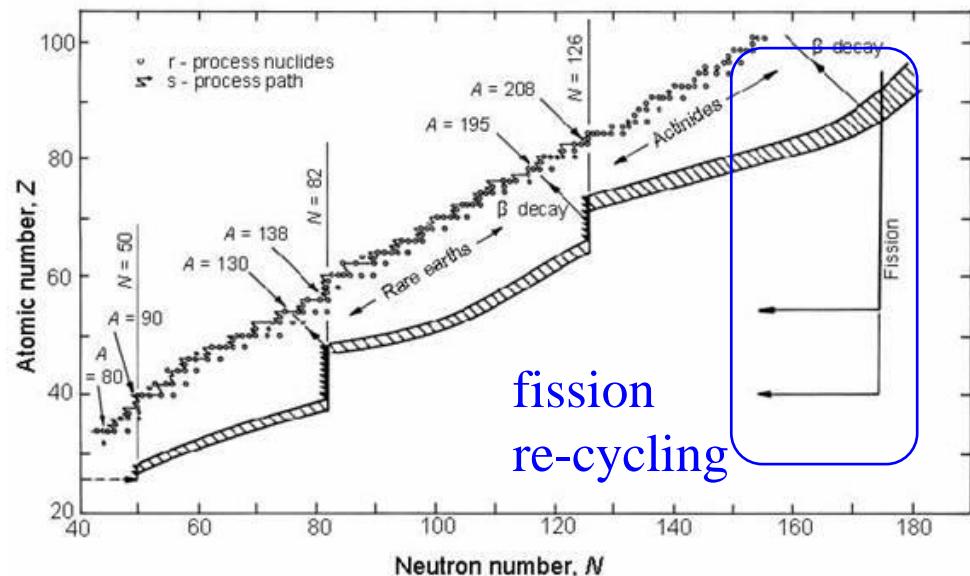
# fission in r-process nucleosynthesis

## ➤ fission of neutron-rich nuclei

- ✓ neutron-induced fission
- ✓ beta-delayed fission

## ➤ important quantities

- ✓ mass distributions
- ✓ charge distributions
- ✓ branching ratios  
(n-cap., fis., beta-decay)



## fission in r-process nucleosynthesis

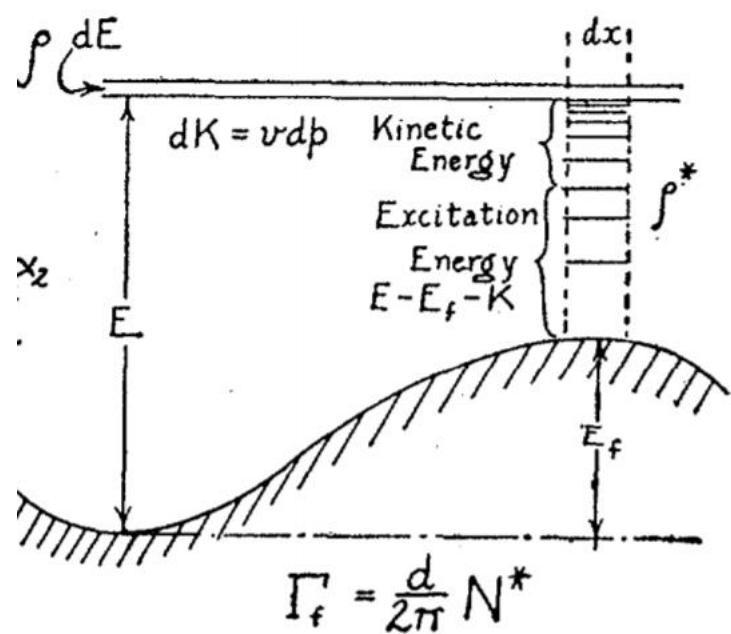
- ✓ low  $E^*$
- ✓ low  $\rho(E^*)$

### ➤ fission of neutron-rich nuclei

- ✓ neutron-induced fission
- ✓ beta-delayed fission

### ➤ important quantities

- ✓ mass distributions
- ✓ charge distributions
- ✓ branching ratios  
(n-cap., fis., beta-decay)



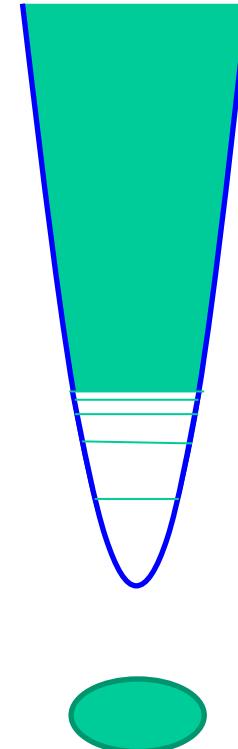
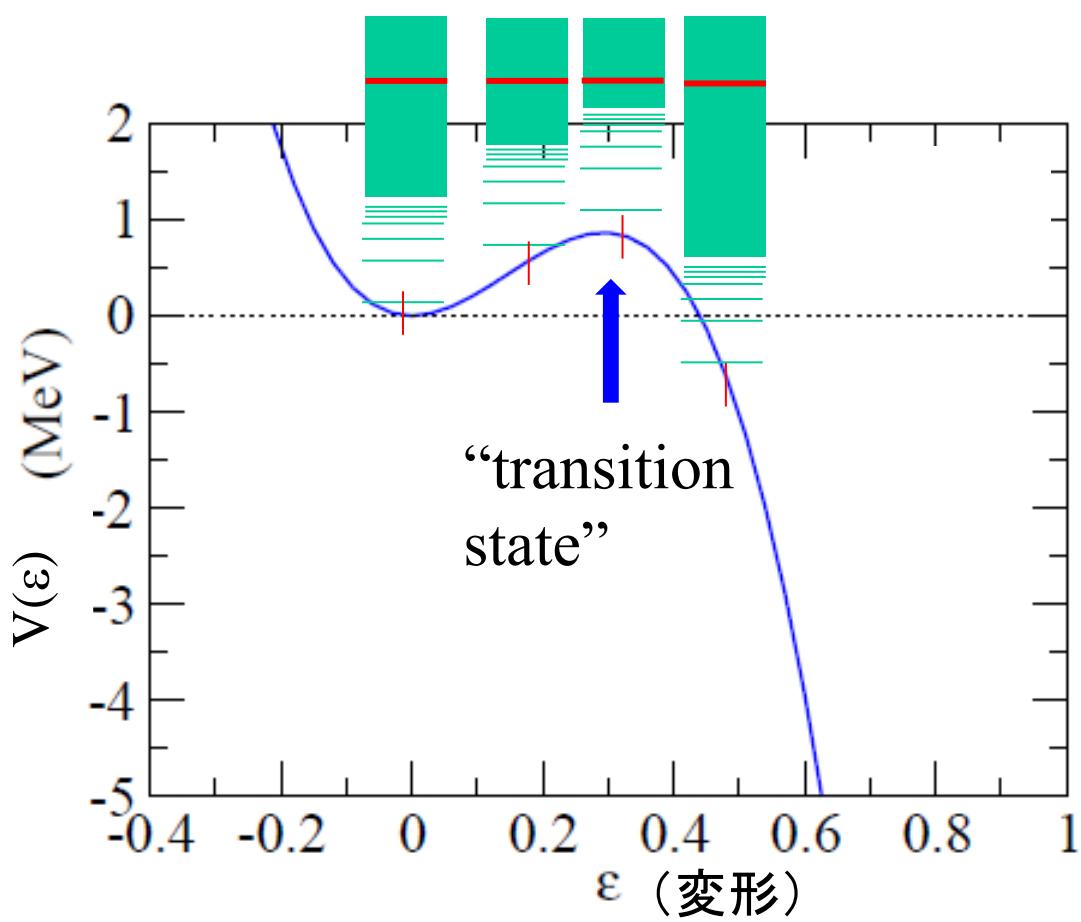
N. Bohr and J.A. Wheeler,  
Phys. Rev. 56, 426 (1939)

→ validity of the BW theory?  
validity of the Langevin?

### ➤ microscopic framework: desired

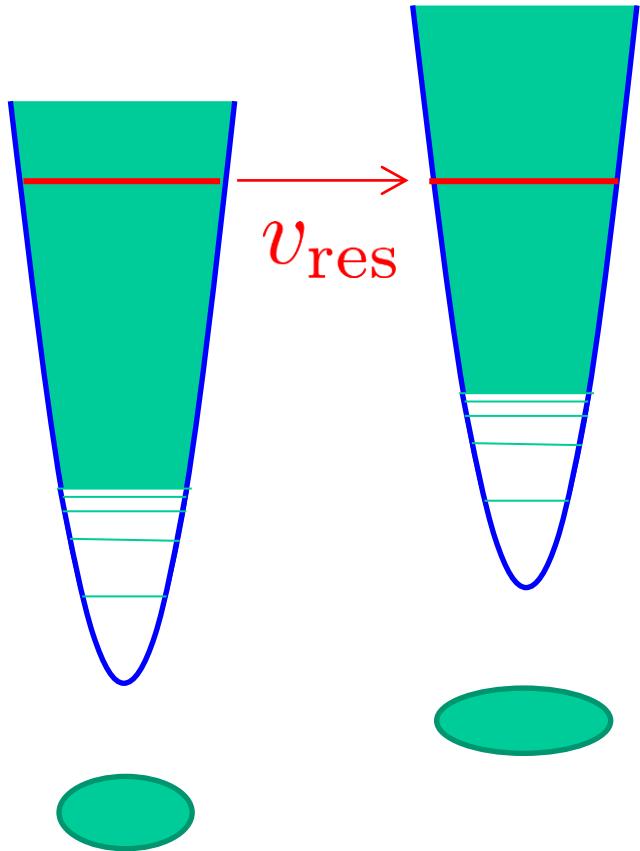
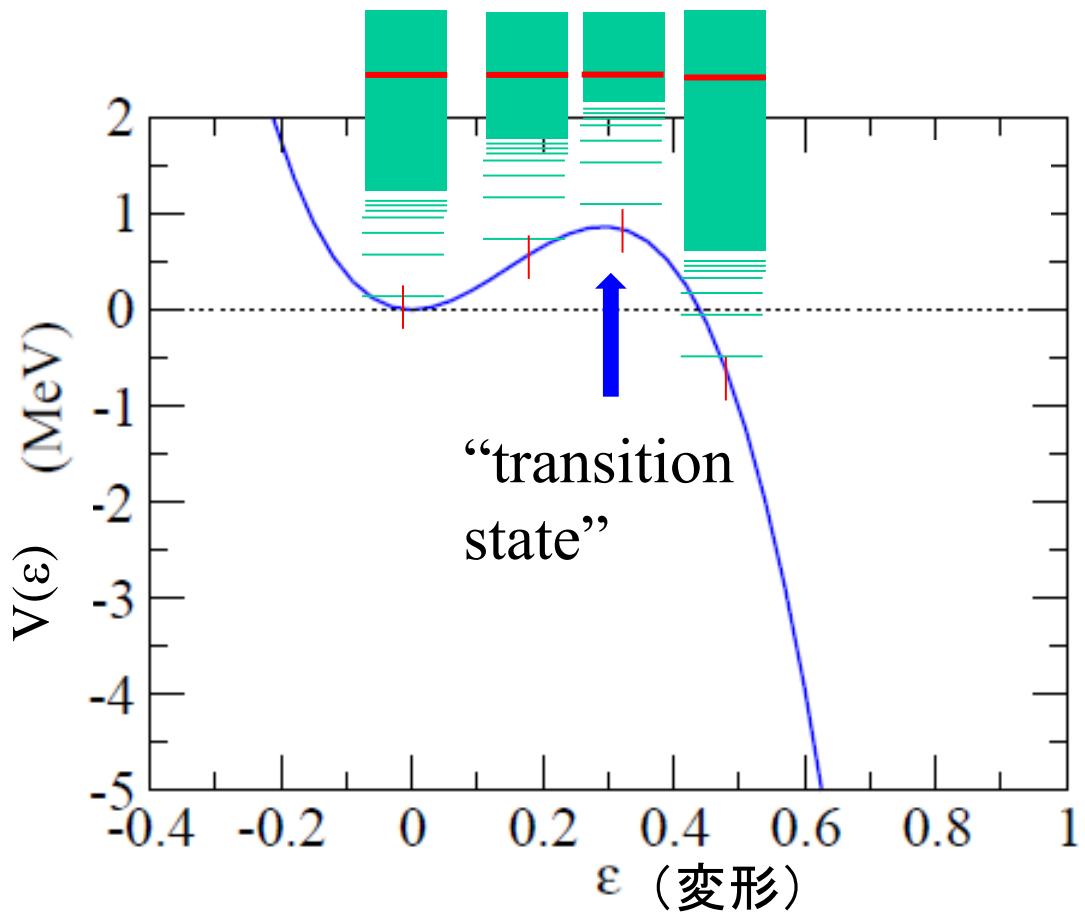
- ✓ how to connect to a many-body Hamiltonian?

# CI アプローチの可能性?



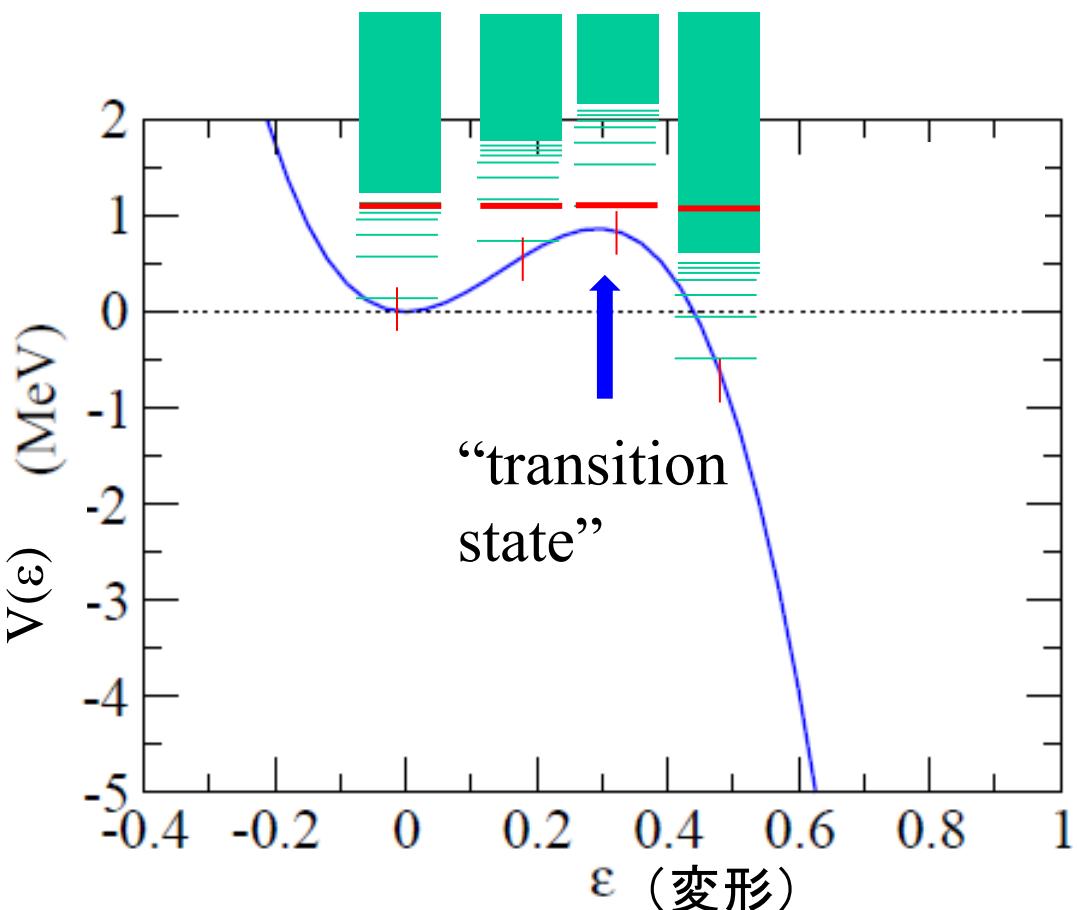
形を決めたときの平均場  
ポテンシャルでの準位

# CI アプローチの可能性?



残留相互作用による  
ホッピング

# CI アプローチの可能性?



励起エネルギーが低い場合には準位密度がスカスカの領域を通過

→transition state theory  
の妥当性が議論できる

どのくらい  $E^*$  が大きければ  
BW公式はよくなるのか?

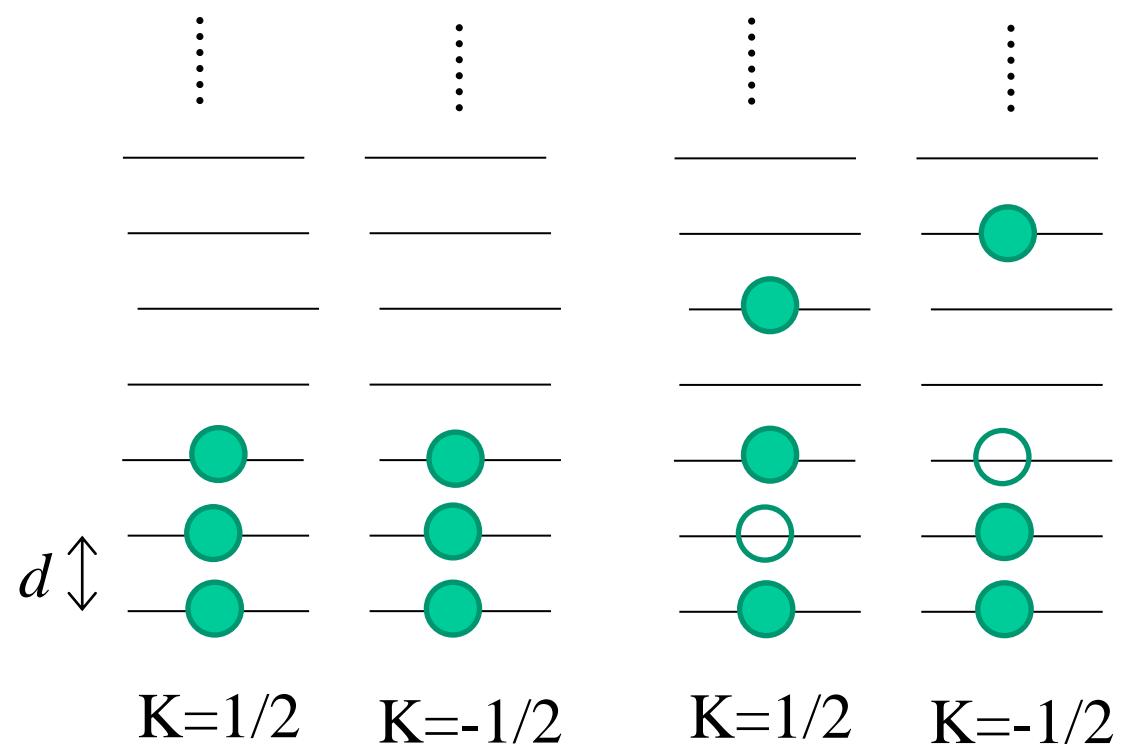
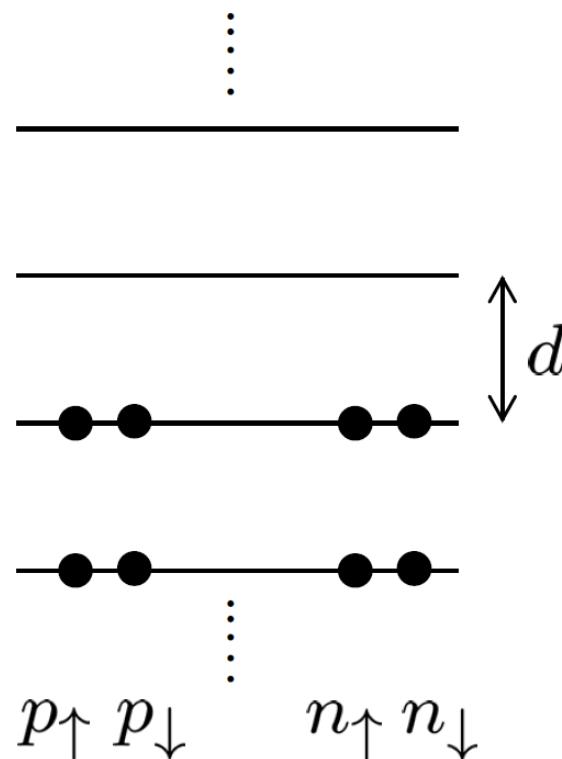
現実的な問題:

- ✓ 模型空間をどのように truncate するのか?
- ✓ 非直交性の問題をどう取り扱うか?

# CI アプローチの実現

G.F. Bertsch and K.H.,  
arXiv: 2102.07084 [nucl-th]

## 一様な一粒子軌道



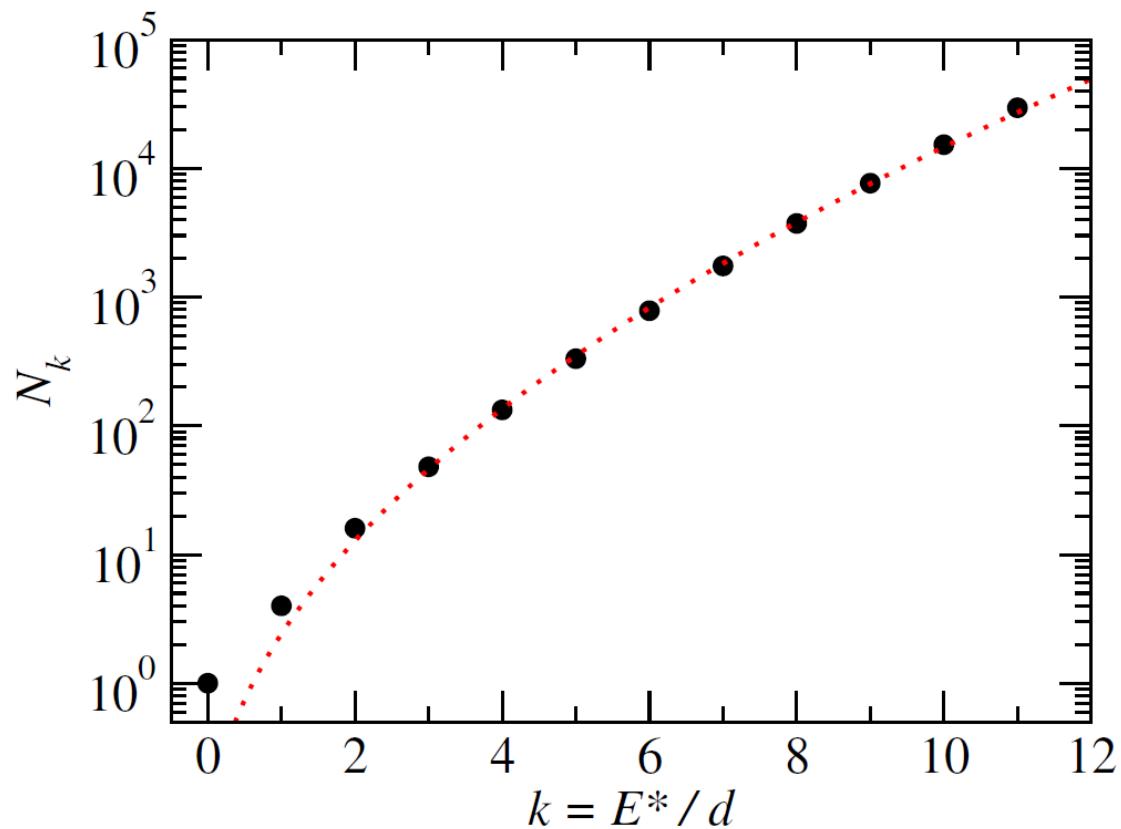
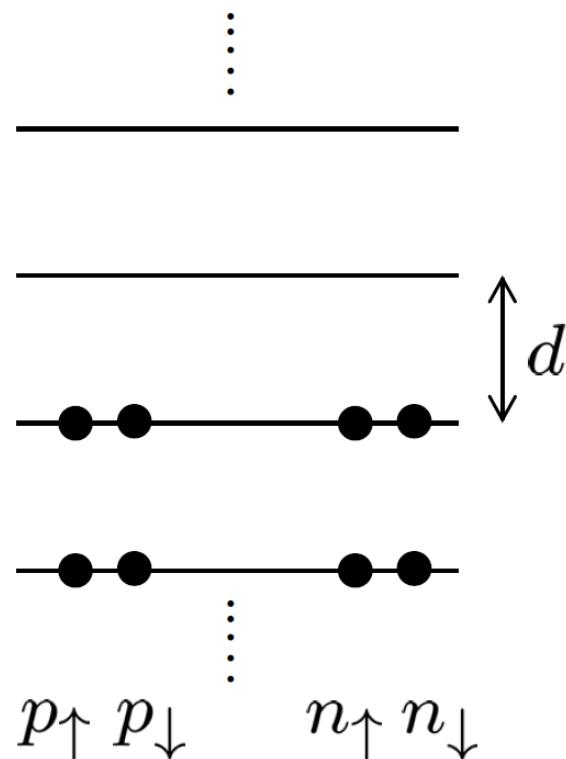
0p0h 状態

2p2h 状態 ( $E^*=6\varepsilon$ )

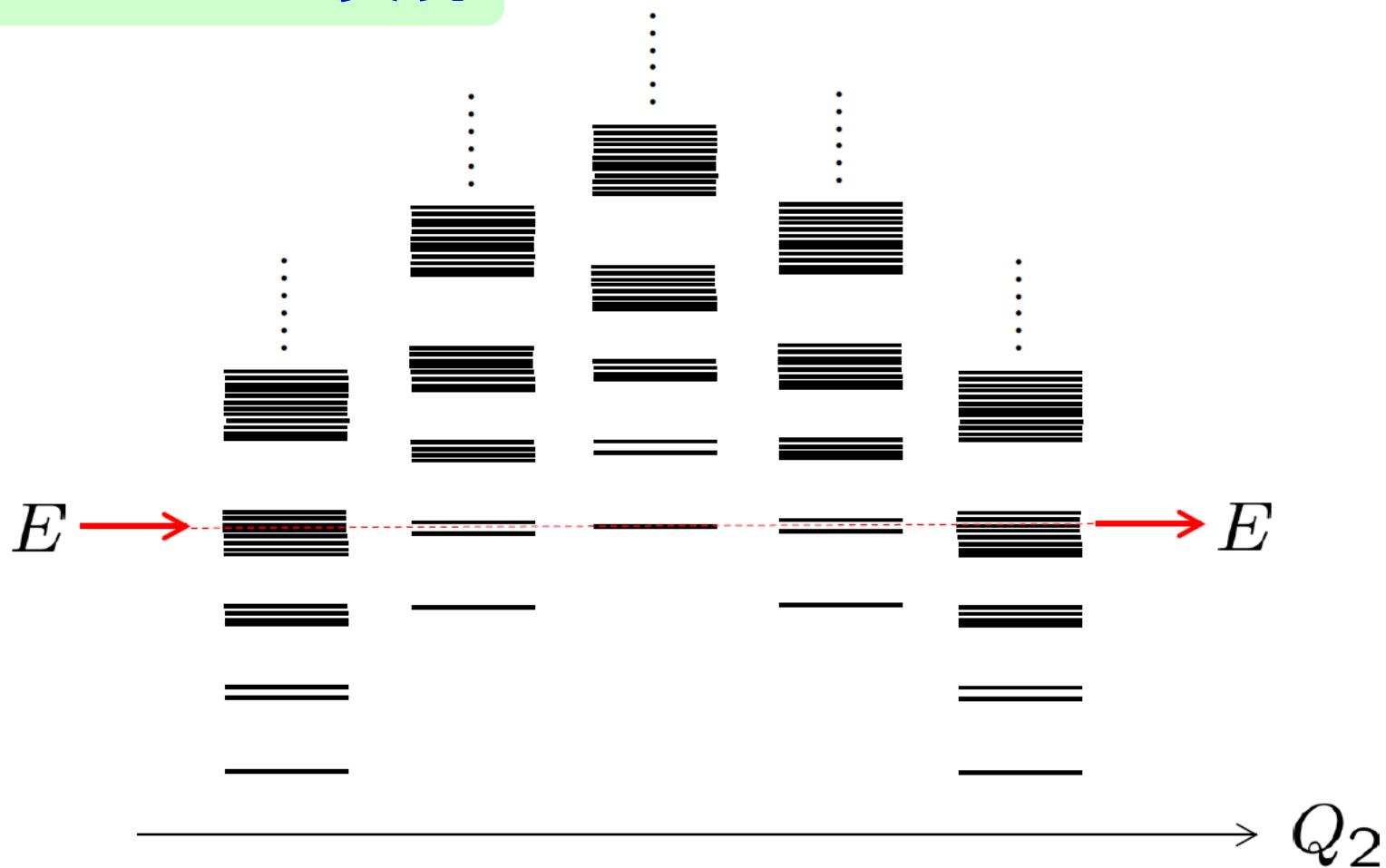
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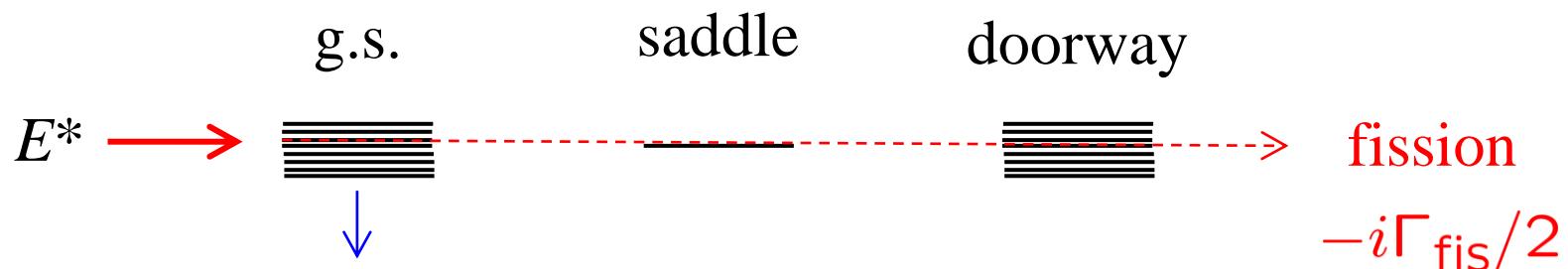
# CI アプローチの実現



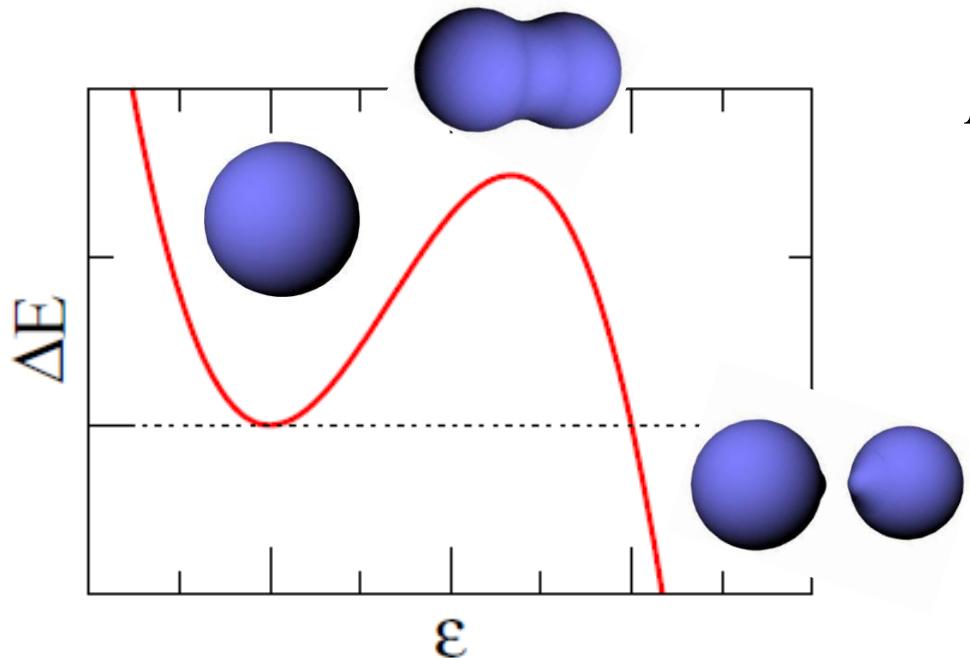
$$H = \sum_{\mu} \epsilon_{\mu} a_{\mu}^{\dagger} a_{\mu} + \sum v_{\mu\nu\mu'\nu'} a_{\mu}^{\dagger} a_{\nu}^{\dagger} a_{\nu'} a_{\mu'}$$

ガウス分布に従ってランダムに発生 (pn 相互作用のみ)

# CI アプローチの実現

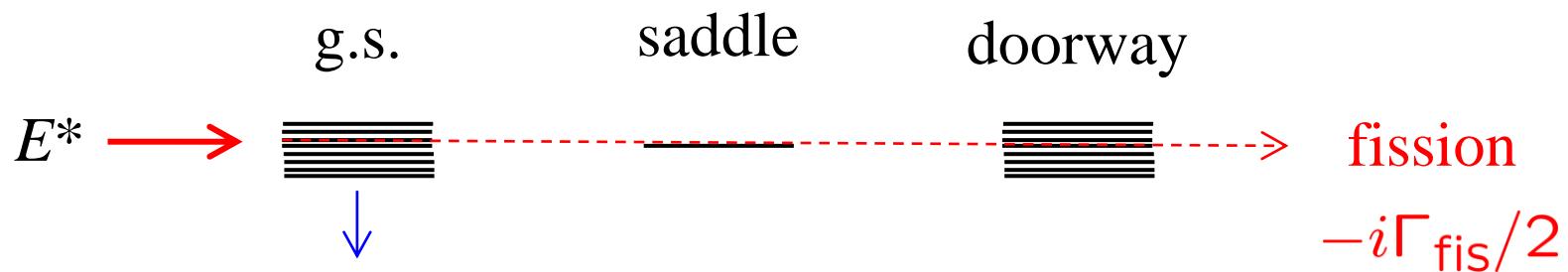


$$H = \begin{pmatrix} H_k - i\Gamma_{\text{cap}}/2 & V & 0 \\ V & H_0 & V \\ 0 & V & H_k - i\Gamma_{\text{fis}}/2 \end{pmatrix}$$



$H_k$ : the Hamiltonian with  
the configurations at  $E_k^*$

# CI アプローチの実現



$$\begin{array}{ll} \text{capture} & H = \begin{pmatrix} H_k - i\Gamma_{\text{cap}}/2 & V & 0 \\ V & H_0 & V \\ 0 & V & H_k - i\Gamma_{\text{fis}}/2 \end{pmatrix} \\ -i\Gamma_{\text{cap}}/2 & \end{array}$$

Reaction theory:

$$T_{\text{cap}}(E) = \mathcal{N} \sum_{k \in 1\text{st}} |(H - E)^{-1}_{ki}|^2 \Gamma_{\text{cap}}$$

$$T_{\text{fis}}(E) = \mathcal{N} \sum_{k \in 3\text{rd}} |(H - E)^{-1}_{ki}|^2 \Gamma_{\text{fis}}$$

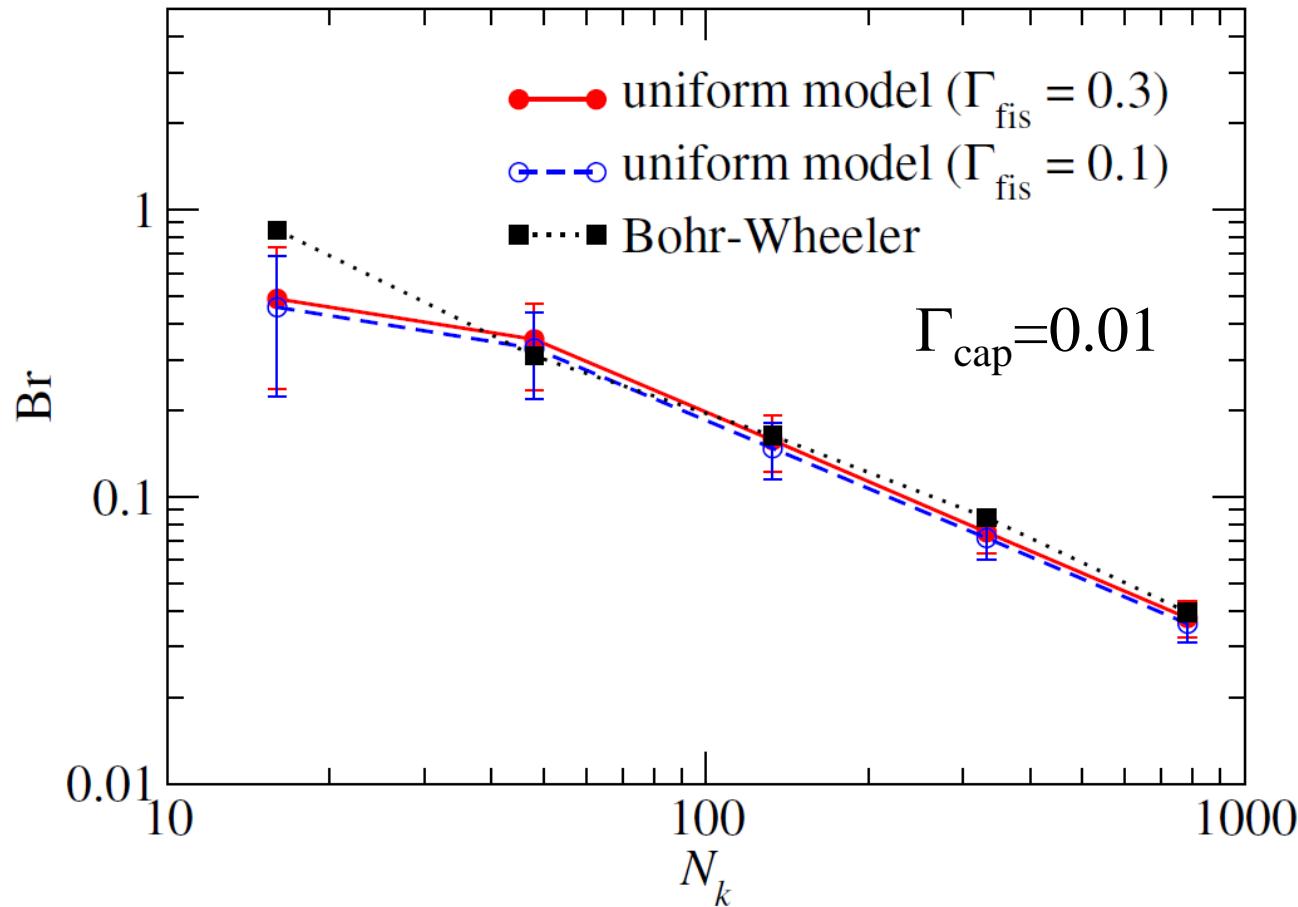
$i$ : 入射チャンネル (1st ブロックのいずれかの config.)

分岐比:  $Br = \frac{\int dE T_{\text{fis}}(E)}{\int dE T_{\text{cap}}(E)}$

cf.  $Br_{\text{BW}} = \frac{1}{2\pi\rho_1} \frac{1}{\Gamma_{\text{cap}}}$

# CI アプローチの実現

G.F. Bertsch and K.H.,  
arXiv: 2102.07084 [nucl-th]



- ✓  $\Gamma_{\text{fis}}$  (scission のダイナミックス)にあまり依存しない
- ✓ BW 公式とよく一致( $k=2$  を除く)

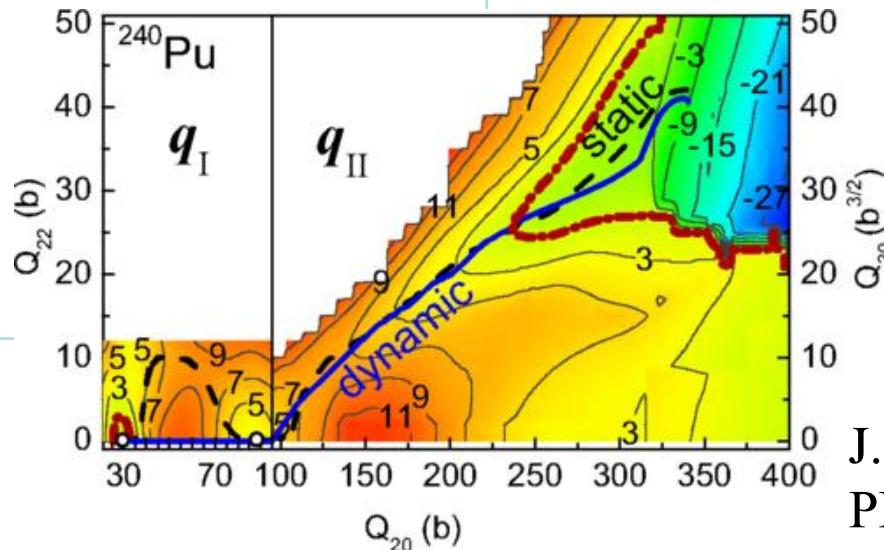
→多体ハミルトニアンを用いて初めて BW 理論を実現

# まとめ

## r-プロセス: 中性子過剰核の核分裂

low  $E^*$ , low  $\rho(E^*)$ に対応できる(微視的)アプローチが必要

	Time-indep. approach	Time-dep. approach
Induced fission	<ul style="list-style-type: none"> <li>✓ Bohr-Wheeler (statistical model)</li> <li>✓ <b>CI approach</b></li> </ul>	<ul style="list-style-type: none"> <li>✓ Langevin-type Wada, Abe, Aritomo, Chiba.....</li> <li>Moller, Randrup</li> </ul>
Spontaneous fission	<ul style="list-style-type: none"> <li>✓ PES+Mass+WKB</li> </ul>	<ul style="list-style-type: none"> <li>✓ Im.-time TDHF (Negele)</li> <li>✓ Time-dep. Hill-Wheeler (Goutte et al.)</li> <li>✓ TDHF(B) (Bulgac.....)</li> </ul>



J. Sadhukhan, W. Nazarewicz, N. Schunck,  
PRC93('16)011304(R)