

A Willful Kick

Photoinduced Charge Order Enhancement

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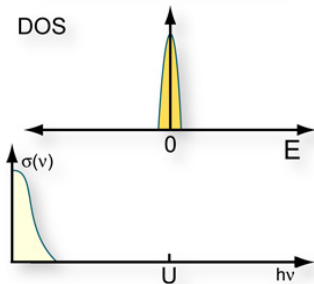
Yukawa Institute for Theoretical Physics, Kyoto University

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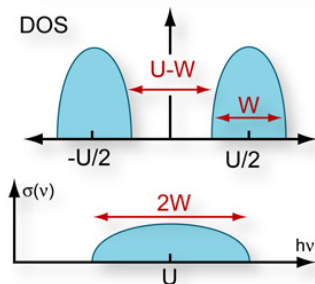
Hubbard Model and Mott Insulators

$$H_{\text{Hubbard}} = -t_h \sum_{\langle ij \rangle, \sigma} (c_{i, \sigma}^\dagger c_{j, \sigma} + \text{H.c.}) + U \sum_i n_{i, \uparrow} n_{i, \downarrow}$$

Drude Metal $U=0$



Mott Insulation $U \gg 0$



Photoexcitation and Nonequilibrium Process

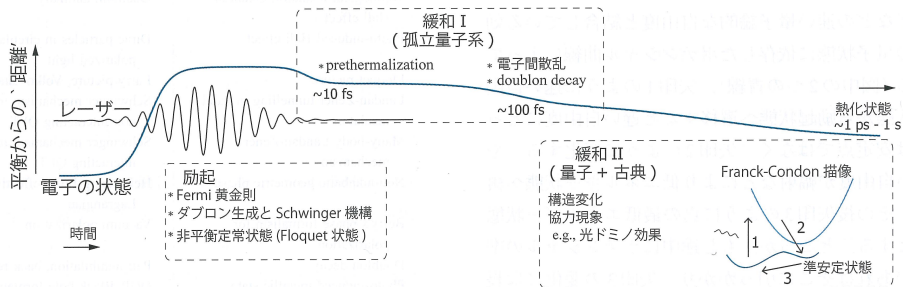
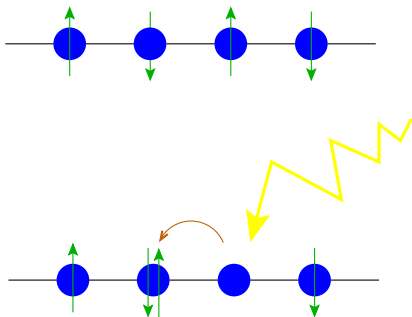


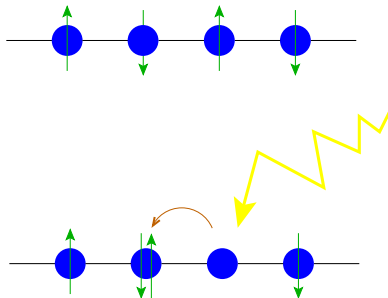
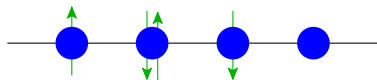
図2 ポンプ・プローブ実験における光誘起相転移と様々な物理的過程。*印はハバード模型のモット絶縁体相に関連深いもの。

Figure: Source: T. Oka and H. Aoki, *Butsuri* **67** (4), 234 (2012).

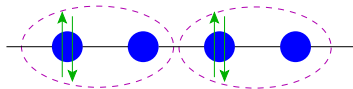
Around Femtoseconds



metallic state



bound state: exciton



Extended Hubbard Model

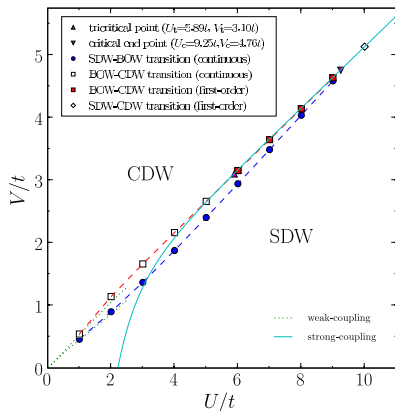


Figure: Phase diagram of the 1D half-filled EHM. Source: S. Ejima and S. Nishimoto, *Phys. Rev. Lett.* **99**, 216403 (2007).

$$\begin{aligned}
 H_{\text{EHM}} = & -t_h \sum_{i,\sigma} \left(c_{i,\sigma}^\dagger c_{i+1,\sigma} + \text{H.c.} \right) \\
 & + U \sum_i \left(n_{i,\uparrow} - \frac{1}{2} \right) \left(n_{i,\downarrow} - \frac{1}{2} \right) \\
 & + V \sum_i (n_i - 1) (n_{i+1} - 1)
 \end{aligned}$$

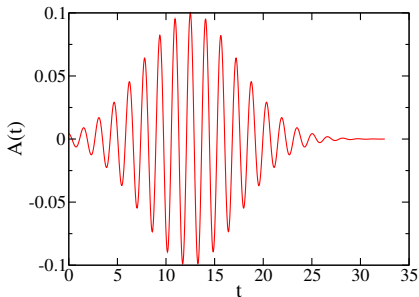
First order phase transition in equilibrium happens around $U \approx 2V$ between spin-density-wave (SDW) and charge-density-wave (CDW), driven by the competition between **energy cost** for doublon generation and **energy reward** due to the attraction between doublon-holon pairs.

Laser Added

In the 1D extended Hubbard model with laser pulse applied, the external field is incorporated by means of the Peierls substitution:

$$c_{i,\sigma}^\dagger c_{i+1,\sigma} + \text{H.c.} \rightarrow e^{iA(t)} c_{i,\sigma}^\dagger c_{i+1,\sigma} + \text{H.c.}$$

$$A(t) = A_0 e^{-(t-t_0)^2/2t_d^2} \cos[\omega_{\text{pump}}(t-t_0)],$$

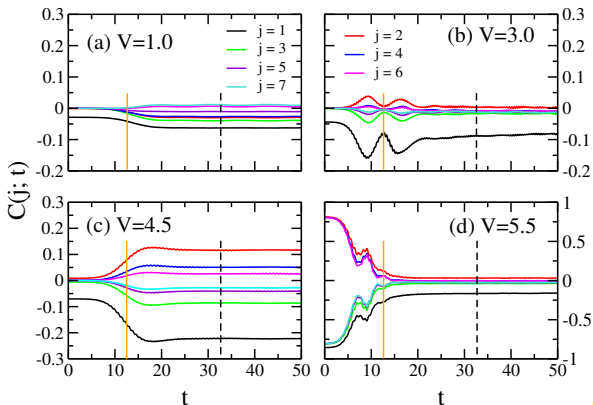
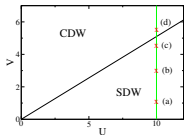
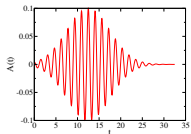


An illustration of the vector potential $A(t)$ with parameters as:

$$A_0 = 0.10, \quad \omega_{\text{pump}} = 4, \\ t_0 = 12.5, \quad t_d = 5$$

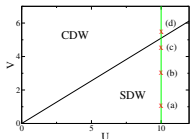
Charge-Charge Correlations (14 sites)

$$C(j; t) = \frac{1}{L} \sum_{i=0}^{L-1} \langle \psi(t) | (n_{i+j} - 1)(n_i - 1) | \psi(t) \rangle$$

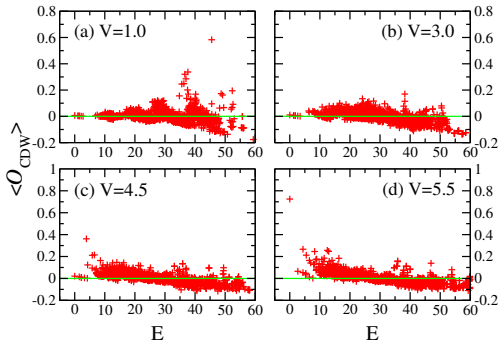


HTL, S. Sota, H. Matsueda, Janez Bonča, and T. Tohyama, [arXiv:1204.1107](https://arxiv.org/abs/1204.1107)

CDW Order Parameter (10 sites)

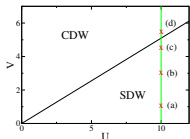


$$\mathcal{O}_{\text{CDW}} := \frac{1}{L(L-1)} \sum_{i=0}^{L-1} \sum_{j \neq 0} (-1)^j (n_{i+j} - 1)(n_i - 1)$$

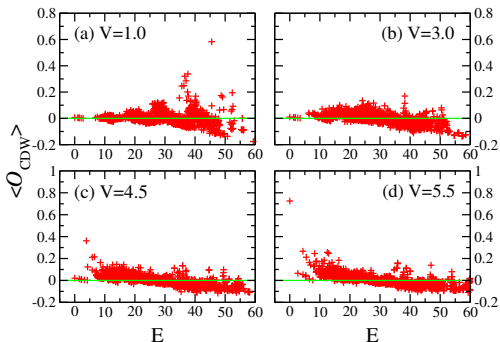


CDW order parameters of eigenstates

CDW Order Parameter (10 sites)



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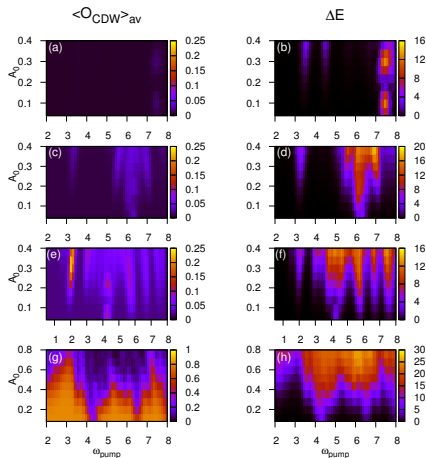


CDW order parameters of eigenstates

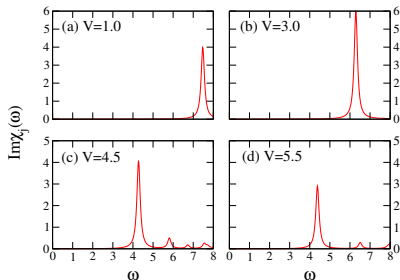
Observations

With increase of V , the states with prominent CDW order move to lower energy regime.

Parameter Sweeping (10 sites)



(I) CDW order vs. A_0 & ω_{pump} at $V = 1.0, 3.0, 4.5$ and 5.5 .



(II) Optical spectra, obtained from the imaginary part of the dynamical current-current correlation functions.