

# Modified gravity models, Massive (bi-)gravity

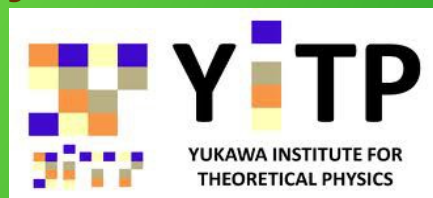
Antonio De Felice

Yukawa Institute for Theoretical Physics, Kyoto U.

*Lunch seminar*

YITP, December 17, 2014

[with prof. Mukohyama, prof. Tanaka, prof. Tsujikawa]



# Introduction – Revolution

- 2011 Nobel Prize: discovery of acceleration at large scales
- What drives it, **dark energy**, accounts for 68% of the total matter distribution
- **What is it?**

# Possibilities

- Cosmological constant
- New matter sector (quintessence, etc.)
- New gravity sector (Deviations from GR)
- New gravity and matter sector (Extra-dims)
- More?
- Only experiments will decide

# f(R) gravity

[Capozziello: IJMP 2002; ADF, Tsujikawa: LRR 2010]

- Phenomenological model  $\mathcal{L}_{GR} = f(R)$
- Working toy models appeared:  $f' > 0, f'' > 0, f(0) = 0$

[Hu et al 2007] 
$$\frac{f}{M_P^2} = R - \mu R_c \left[ \frac{(R/R_c)^{2n}}{1 + (R/R_c)^{2n}} \right]$$

[Starobinsky 2007] 
$$\frac{f}{M_P^2} = R - \mu R_c \left[ 1 - \left( 1 + R^2/R_c^2 \right)^n \right]$$

[Tsujikawa 2008] 
$$\frac{f}{M_P^2} = R - \mu \tanh(R/R_c)$$

# Scalar-tensor theory approach

- Equivalent to the theory described by

$$S = \int d^4x \sqrt{-g} [f(\varphi) + (R - \varphi) f_{,\varphi}]$$

- Important mapping:  $f(R)$  is a scalar tensor theory
- 1 extra scalar field
- Non-minimally coupled to gravity
- Chameleon mechanism

# General modifications

- Other theories of gravity [Nojiri et al 2005]

$$\mathcal{L}_{GR} = f(R, G) \rightarrow f(\lambda, \phi) + \frac{\partial f}{\partial \lambda}(R - \lambda) + \frac{\partial f}{\partial \phi}(G - \phi),$$

- GB-R gravity:
  - A ghost always exist [ADF, Tanaka 2010]
  - Need to tune the theory to make it massive
- Lesson to learn

# dRGT massive gravity

[de Rham, Gabadadze, Tolley: PRL 2011]

- Introducing 4 new scalar fields: Stuckelberg fields
- Then 4 sc dof, 4 vect dof, 2 Gws dof + 4 SF dof
- Unitary gauge (remove 4 SF dof): 4 sc , 4 vect, 2 Gws dof
- Constraints kill 2 sc dof and 2 vect dof:  $2+2+2=6$  dof
- dRGT **kills** one mode, the BD ghost. Finally only 5 dof.

# No stable FLRW solutions

- FLRW background allowed [E. Gumrukcuoglu, C. Lin, S. Mukohyama: JCAP 2011]
- Late de Sitter solutions exist
- But **no** stable FLRW exists: one of the 5 dof is ghost [ADF, E. Gumrukcuoglu, S. Mukohyama: PRL 2012]
- Inhomogeneity? Anisotropies? [D'Amico et al: PRD 2011]  
[E. Gumrukcuoglu, C. Lin, S. Mukohyama: JCAP 2011. ADF, EG, SM: JCAP 2012]
- Something else? Introducing other fields: a quasidilaton scalar field [ADF, Mukohyama: PLB 2013][See also Huang, Piao, Zhou: PRD 2012]



# Bigravity

[Hassan, Rosen: JHEP 2012]

- Promote fiducial metric to a dynamical component
- Introduce for it a new Ricci scalar
- Degrees of freedom in the 3+1 decomposition:
  - Total:  $(4 \text{ sc} + 4 \text{ vt} + 2\text{GW}) \cdot 2$
  - Gauge:  $2 \text{ sc} + 2 \text{ vt}$
  - Constraints:  $(2 \text{ sc} + 2 \text{ vt}) \cdot 2 + 1 \text{ no-BD-ghost}$
  - Finally: T-G-C  $\Rightarrow 1 \text{ sc} + 2 \text{ vt} + 4 \text{ GW}$

# Bimetric Lagrangian

- For the two metrics

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu, \quad d\tilde{s}^2 = \tilde{g}_{\mu\nu} dx^\mu dx^\nu,$$

- Introduce a ghost free action

$$\mathcal{L} = \sqrt{-g} \left[ M_G^2 \left( \frac{R}{2} - m^2 \sum_{n=0}^4 c_n V_n(Y^\mu{}_\nu) \right) + \mathcal{L}_m \right] + \frac{\kappa M_G^2}{2} \sqrt{-\tilde{g}} \tilde{R}$$

where

$$Y^\mu{}_\nu = \sqrt{g^{\mu\alpha} \tilde{g}_{\alpha\nu}},$$

$$[Y^n] = \text{Tr}(Y^n), \quad V_0 = 1, \quad V_1 = [Y],$$

$$V_2 = [Y]^2 - [Y^2], \quad V_3 = [Y]^3 - 3[Y][Y^2] + 2[Y^3],$$

$$V_4 = [Y]^4 - 6[Y]^2[Y^2] + 8[Y][Y^3] + 3[Y^2]^2 - 6[Y^4].$$

# Phenomenology [ADF, Nakamura, Tanaka: PTEP 14]

- Assume FLRW ansatz  $ds^2 = a^2(-dt^2 + d\vec{x}^2)$ ,  $d\tilde{s}^2 = \tilde{a}^2(-\tilde{c}^2 dt^2 + d\vec{x}^2)$
- Two branches  $\Gamma(\xi)(\tilde{c} a H - \dot{\tilde{a}}/\tilde{a}) = 0$ ,  $\Gamma = c_1 \xi + 4c_2 \xi^2 + 6c_3 \xi^3$   
[ $\xi = \tilde{a}/a$ ,  $H = \dot{a}/a^2$ ]
- Physical branch:  $\tilde{c} = \dot{\tilde{a}}/(\tilde{a} a H)$
- GR evolution:  $3H^2 = \frac{\rho_m}{\tilde{M}_G^2}$ ,  $\xi \approx \xi_c$ ,  $\tilde{M}_G^2 = M_G^2(1 + \kappa \xi_c^2)$ ,  $\tilde{c} \approx 1$ ,  $\frac{\rho_m}{M_G^2 m^2} \ll 1$ ,
- Vainshtein mechanism  $\nabla^2 v \approx -\frac{\rho_m}{\tilde{M}_G^2}$  if  $\frac{d \ln \Gamma}{d \ln \xi} \gg 1$ ,
- Gravitons oscillations  $\mu_1^2 = 0$ ,  $\mu_2^2 = \frac{(1 + \kappa \xi_c^2) \Gamma_c m^2}{\kappa \xi_c^2}$

# Conclusions

- Dark Energy/Gravity: active field of research
- What is gravity?
- Yet, a field to investigate
- Can the graviton (or one of them) be massive?
- Experimental and theoretical research is needed