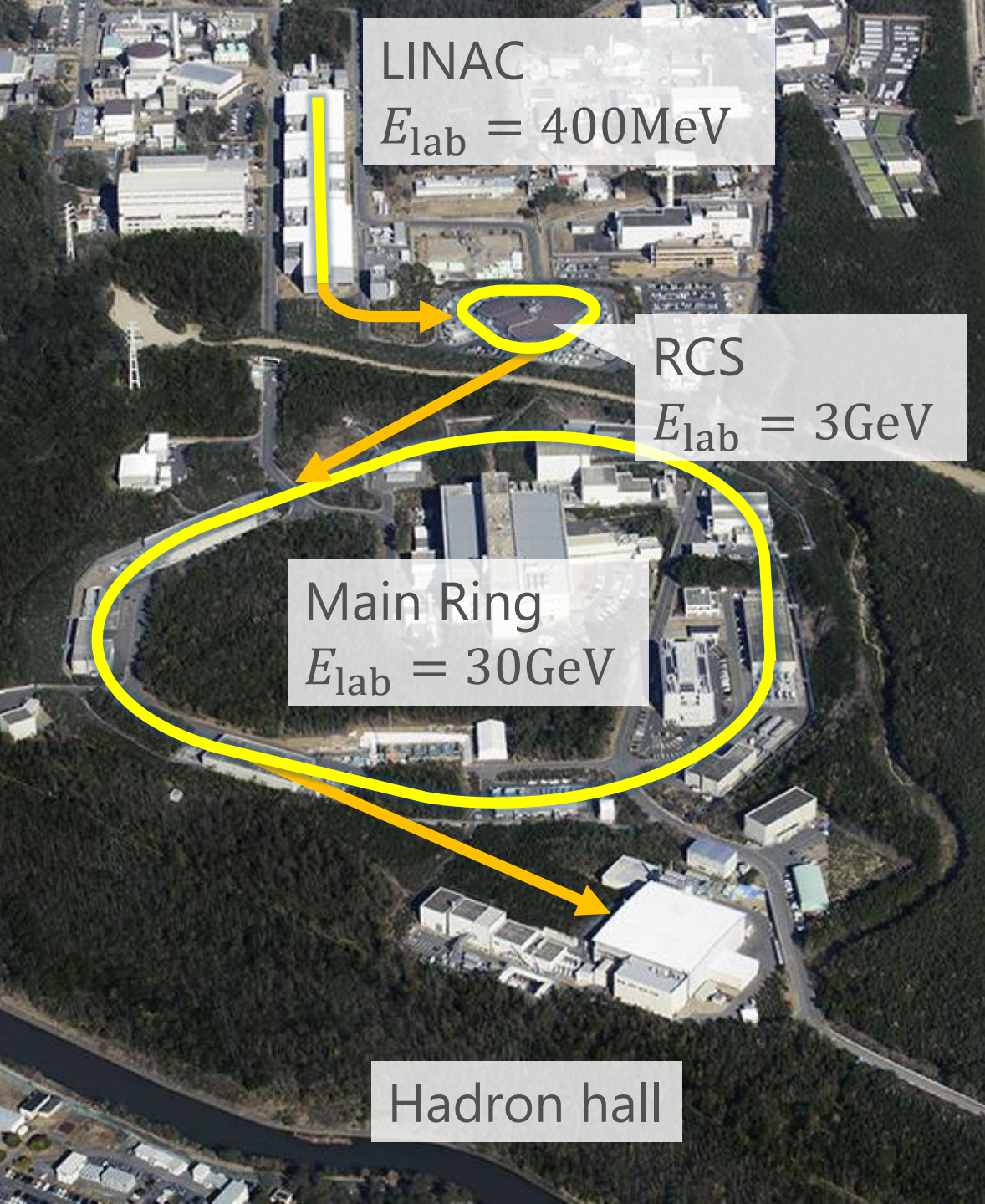


# J-PARC-HI: Theory

Masakiyo Kitazawa  
(YITP, Kyoto)



LINAC  
 $E_{lab} = 400\text{MeV}$

RCS  
 $E_{lab} = 3\text{GeV}$

Main Ring  
 $E_{lab} = 30\text{GeV}$

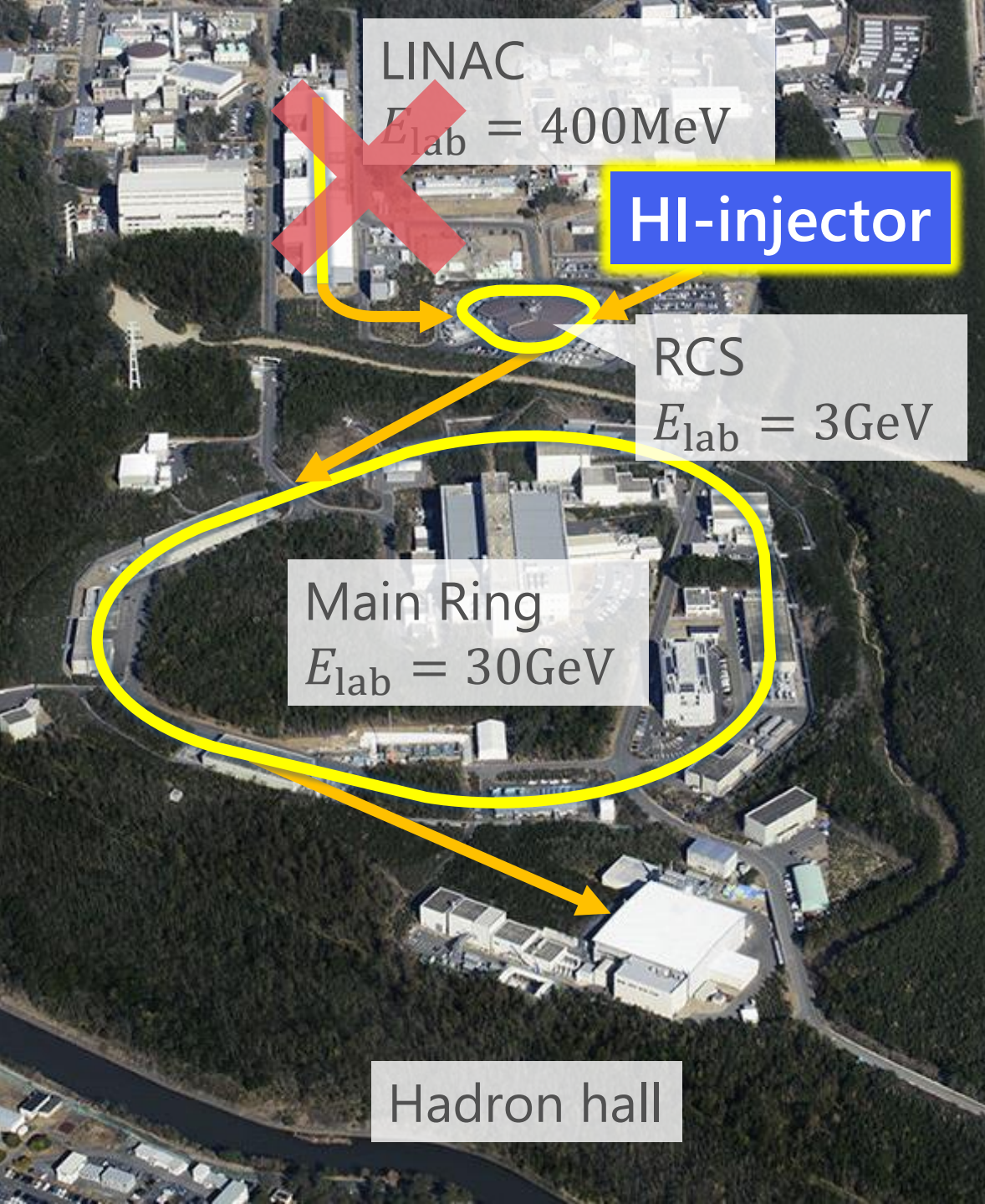
Hadron hall

## Accelerators

- LINAC
- RCS
- Main Ring
- High intensity  $I = 1\text{MW}$

## Purposes

- Hadron/Nuclear physics
- Neutrino physics
- Material/Life science



LINAC

$E_{lab} = 400\text{MeV}$

HI-injector

RCS

$E_{lab} = 3\text{GeV}$

Main Ring

$E_{lab} = 30\text{GeV}$

Hadron hall

## Accelerators

- LINAC
- RCS
- Main Ring
- High intensity  $I = 1\text{MW}$

## Purposes

- Hadron/Nuclear physics
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# J-PARC-HI

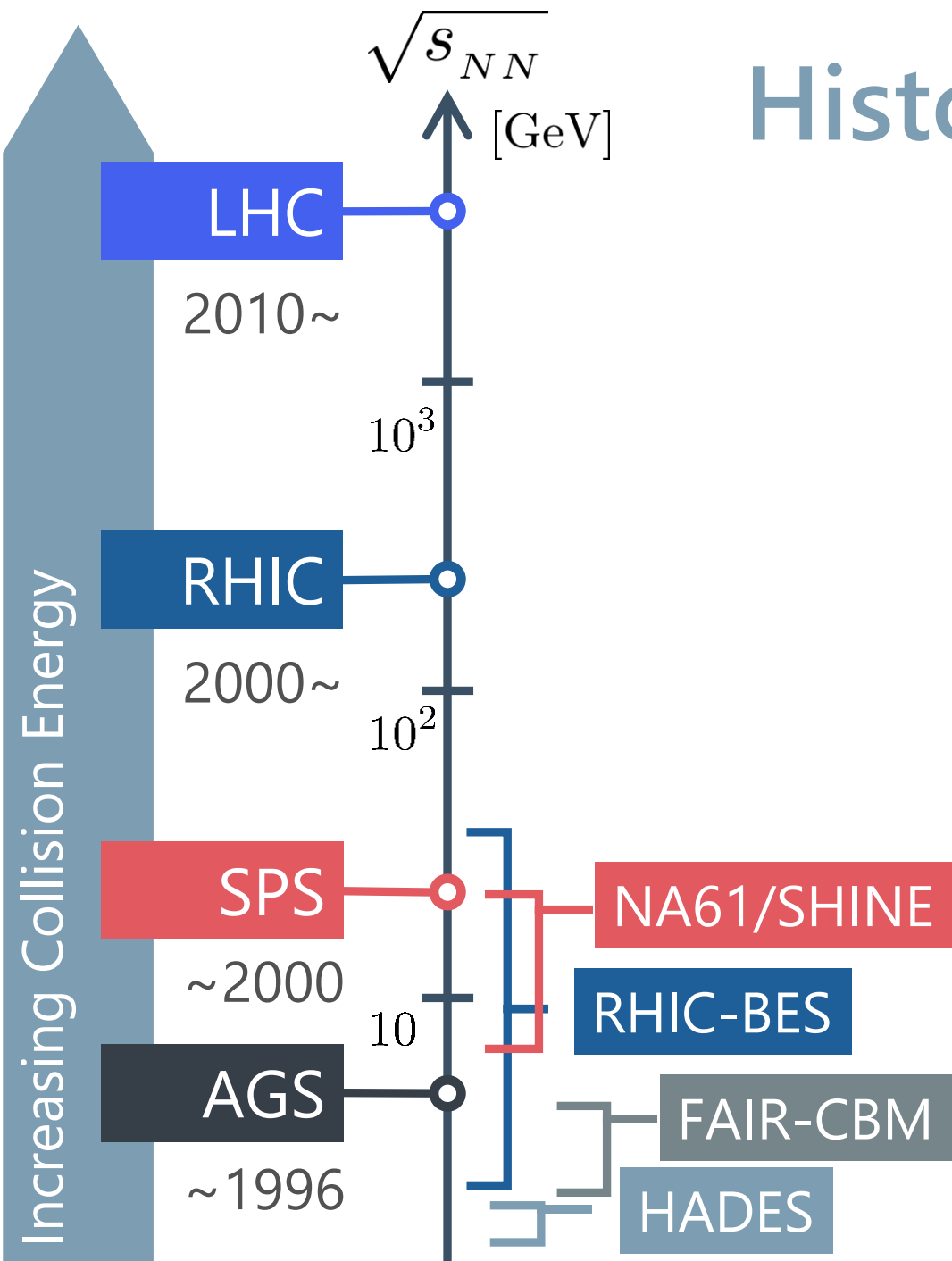
J-PARC Heavy Ion

High intensity

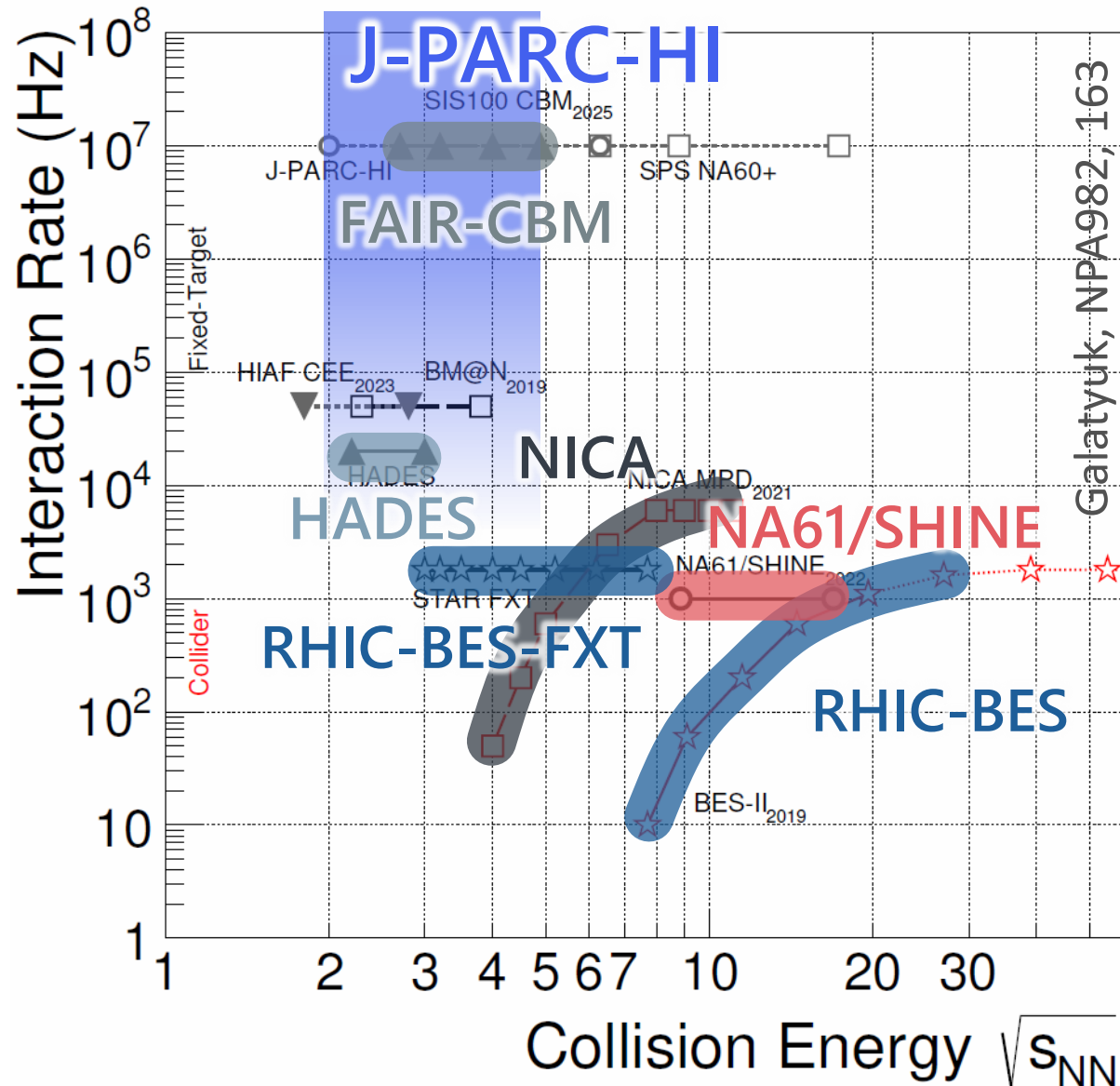
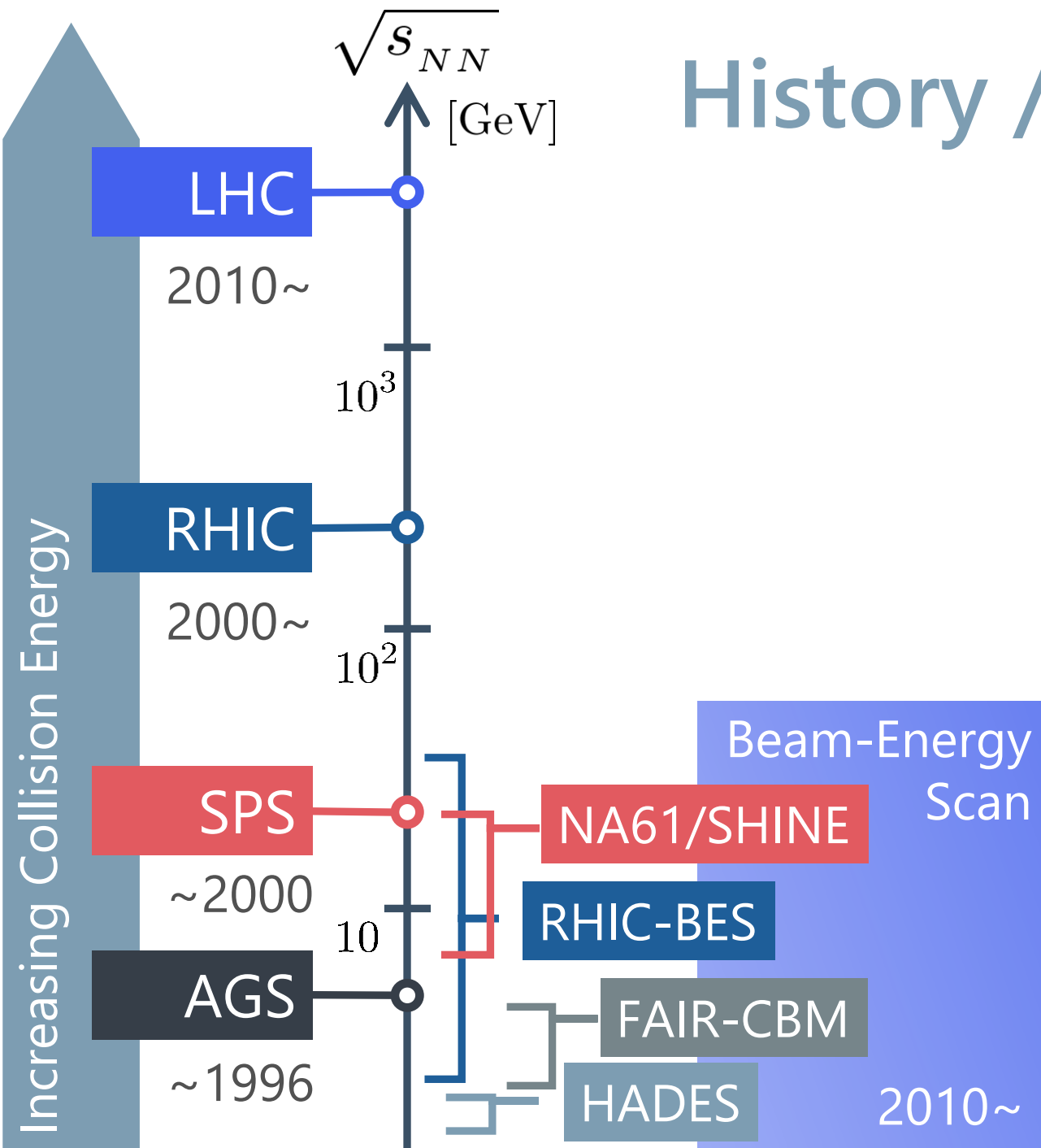


Intermediate energy

# History / Current Status of HIC



# History / Current Status of HIC



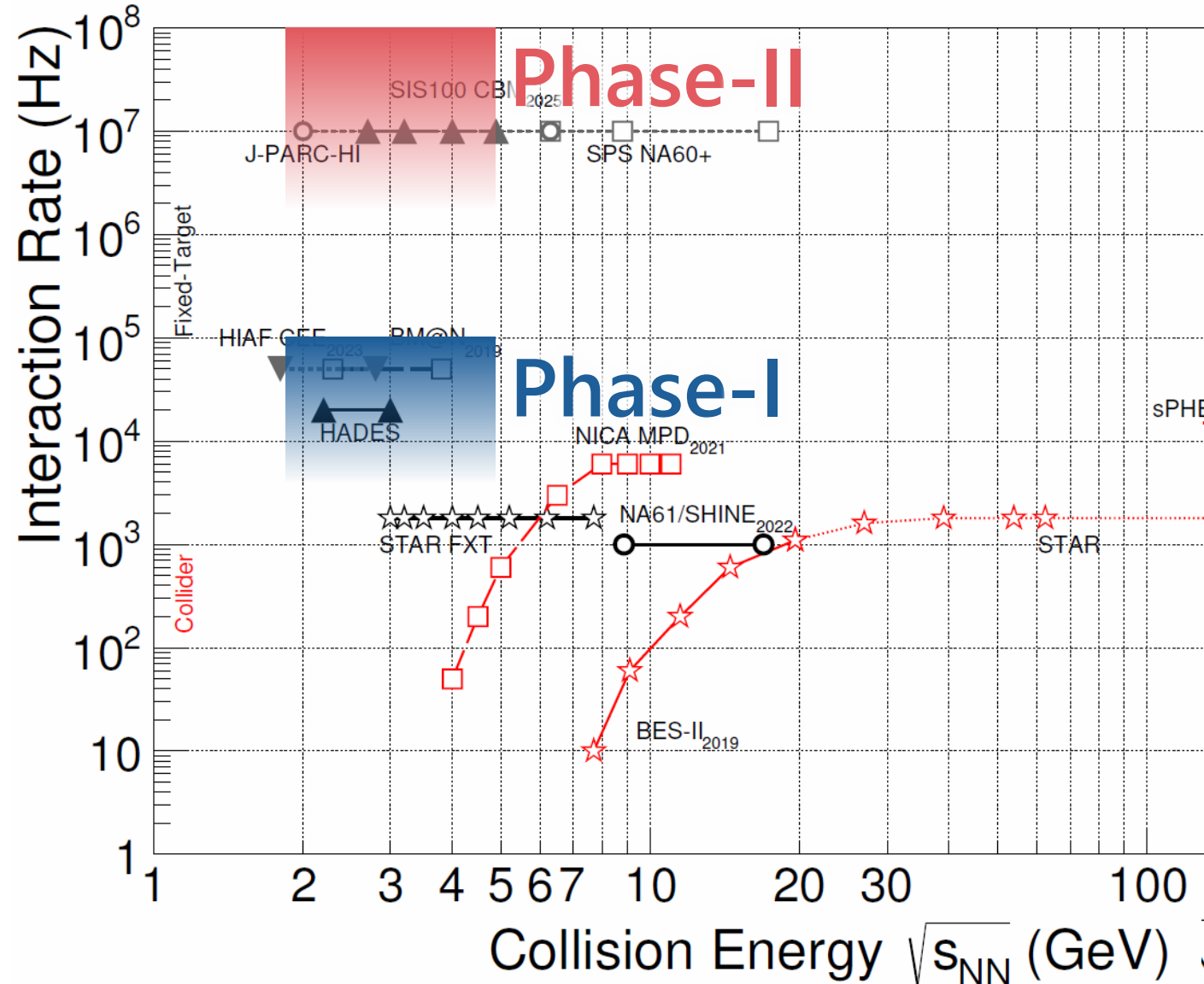
# J-PARC-HI Staging Plan

## Phase-I

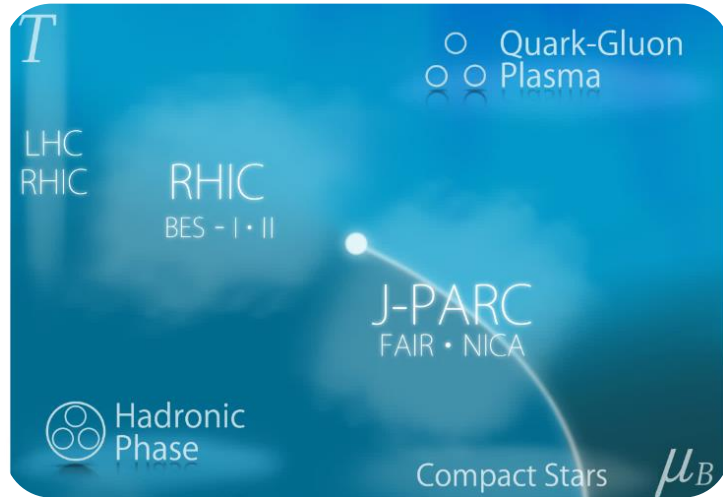
- KEK-BS booster
- E16+ $\alpha$  spectrometer

## Phase-II

- **NEW** HI booster
- **NEW** spectrometer

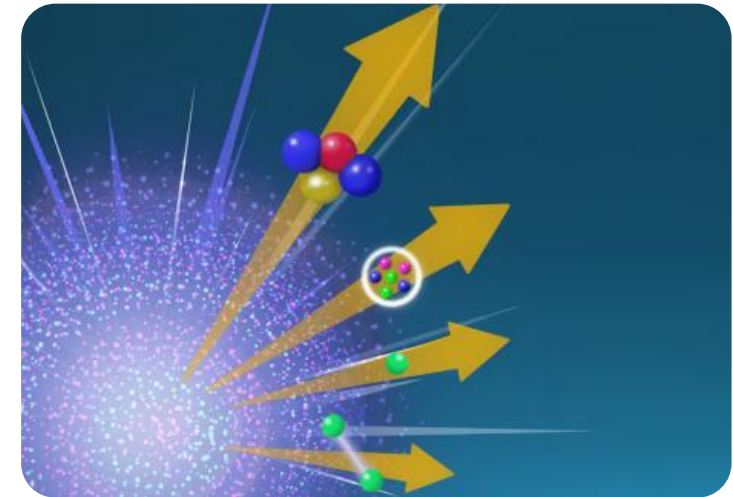


# Physics Goals



Exploring

Extremely Dense Medium

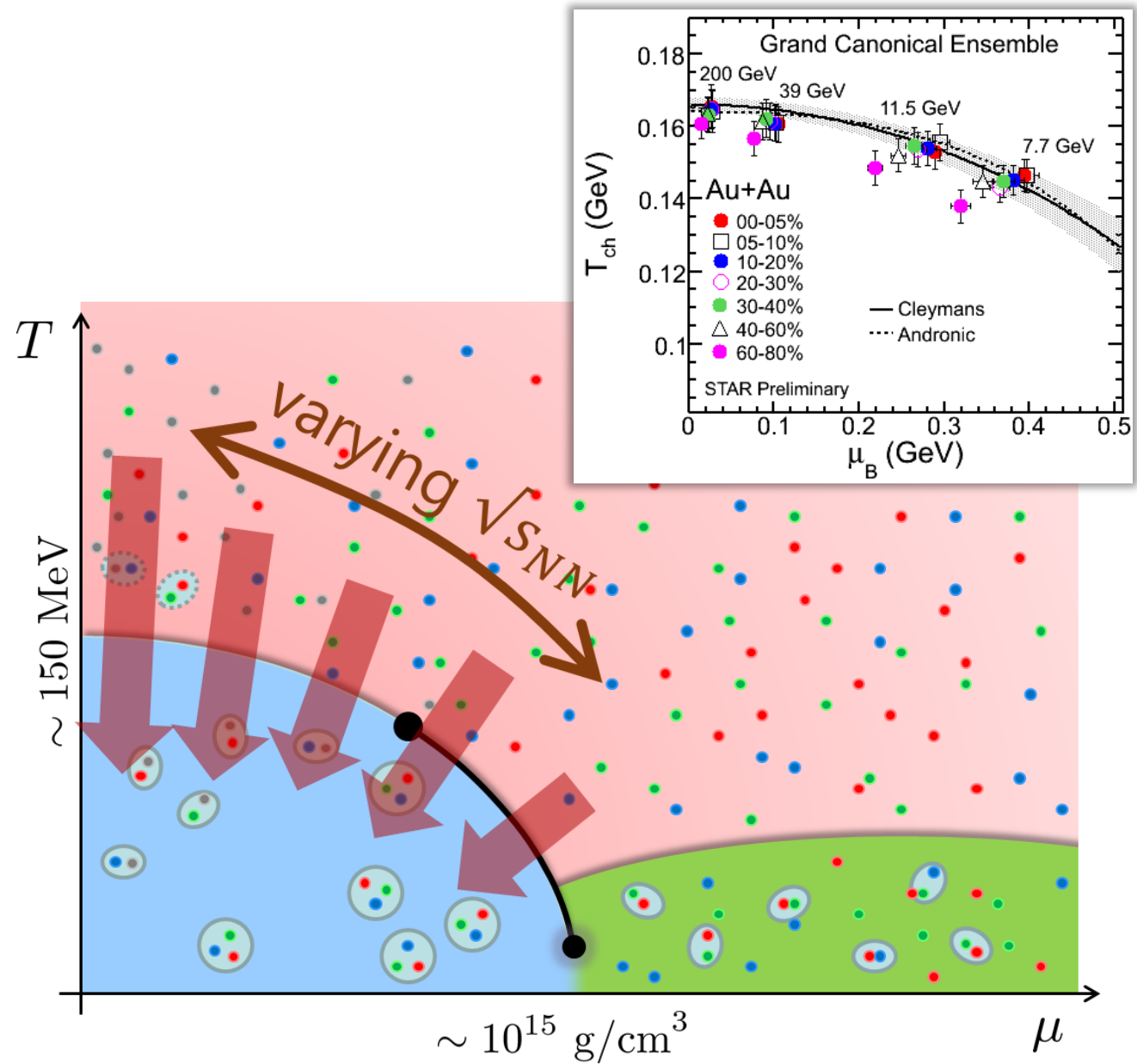
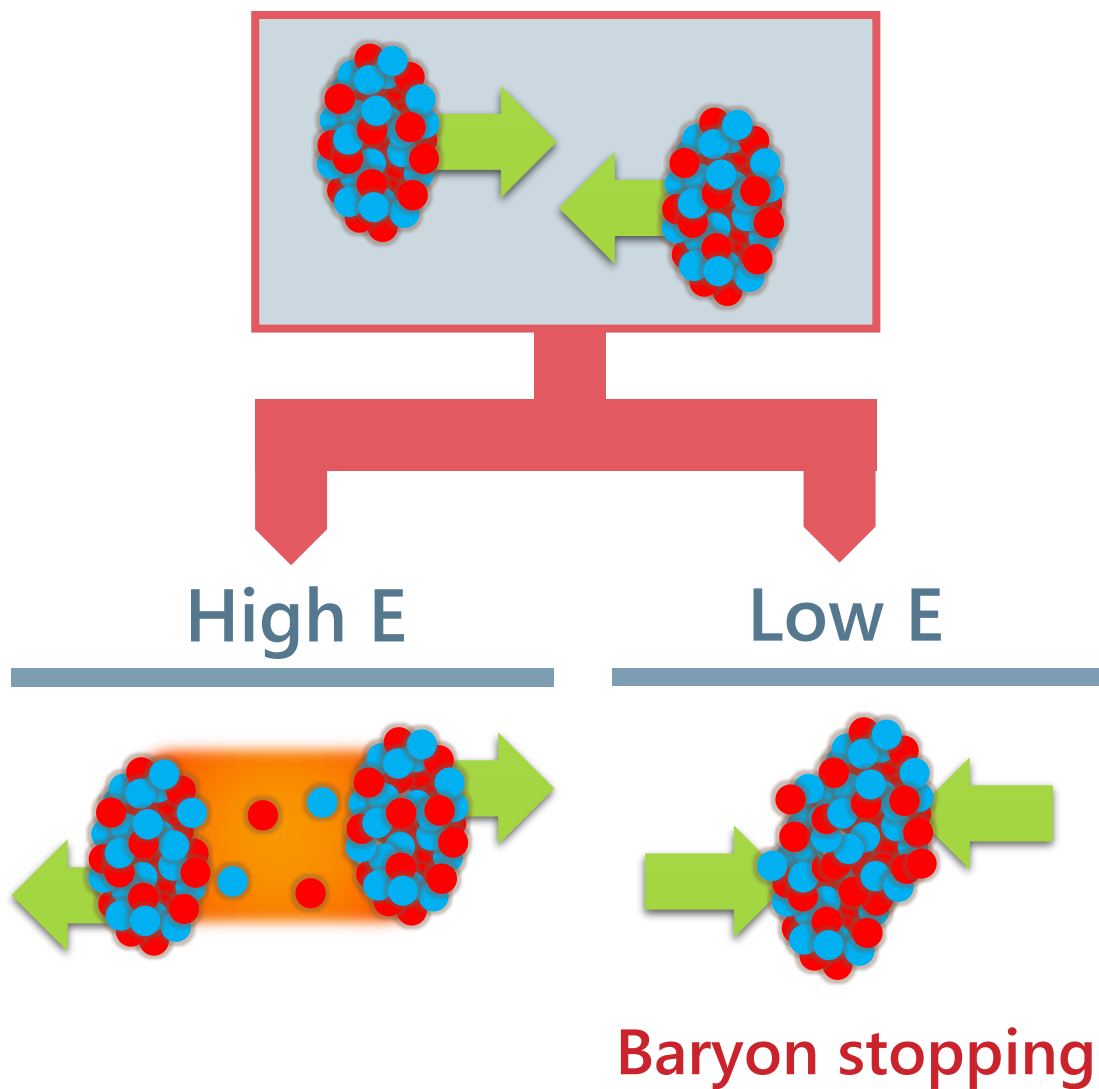


Search for

Rare Hadronic/Hypernuclear  
Events

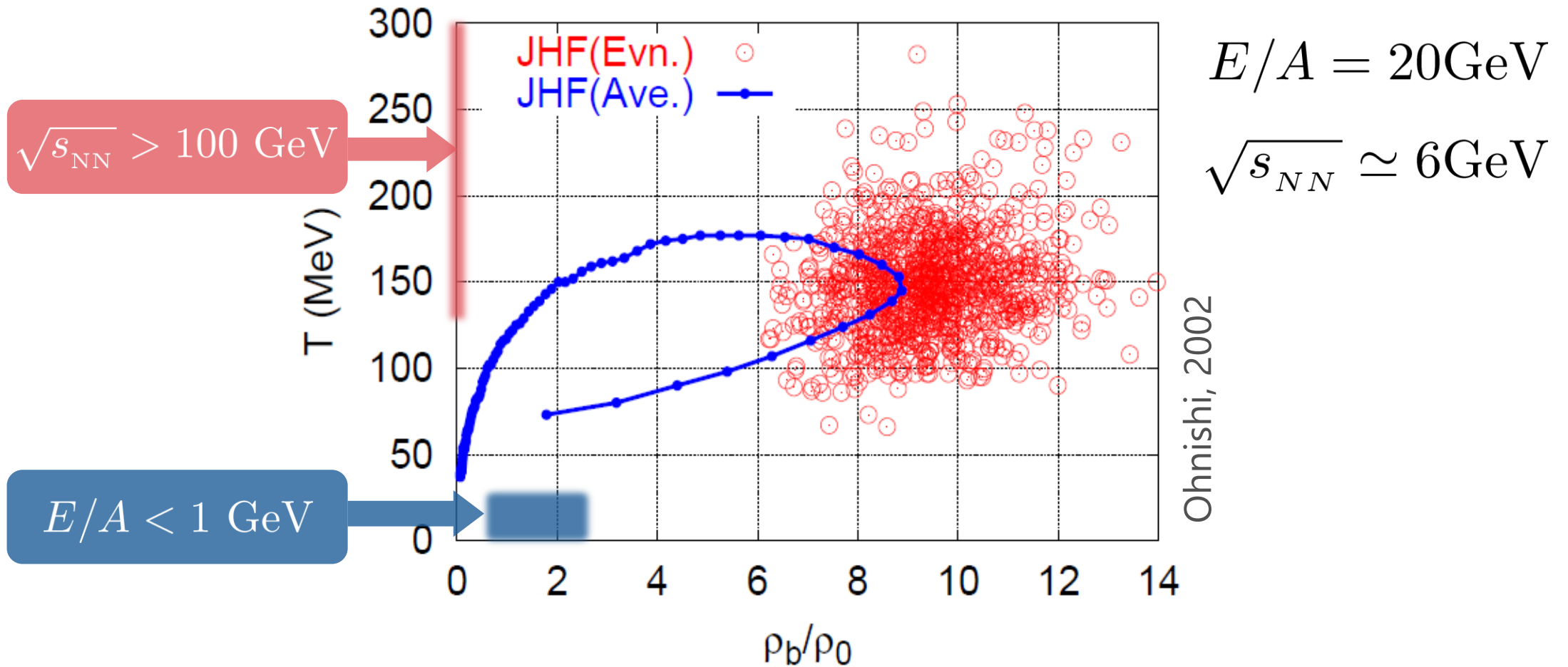
# Beam-Energy Scan

STAR, 2012





# J-PARC-HI = Highest Baryon Density



Quark-Gluon Plasma

# Exploring Dense Medium



Equation of state



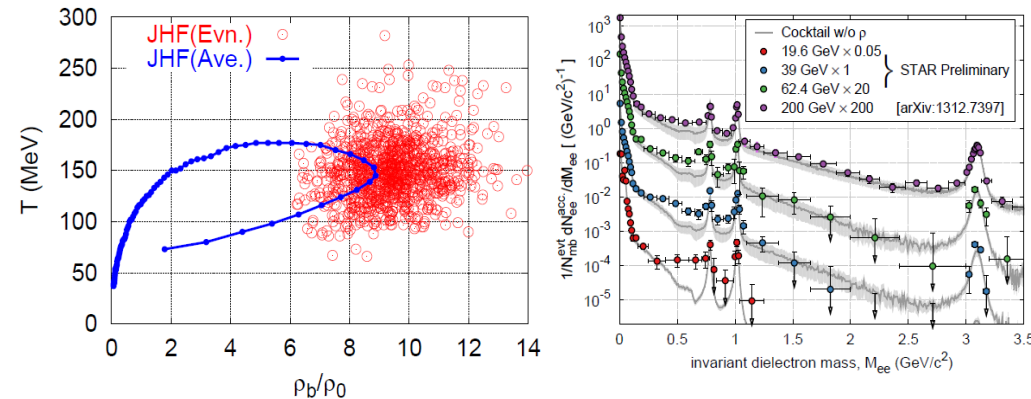
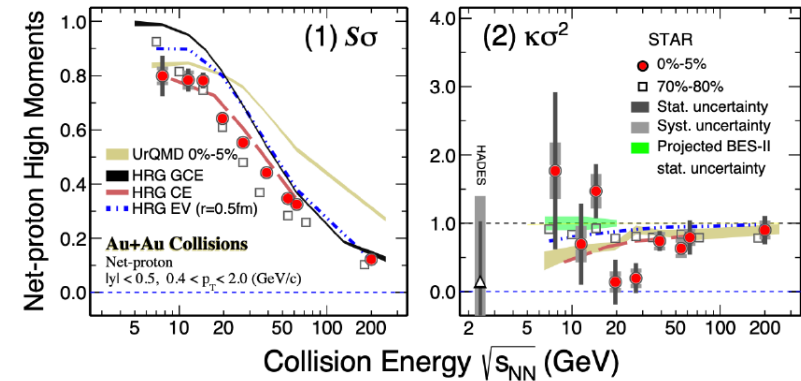
QCD critical point /  
1st order transition /  
Color superconductivity



Dilepton production rate



Event selection /  
Higher correlations

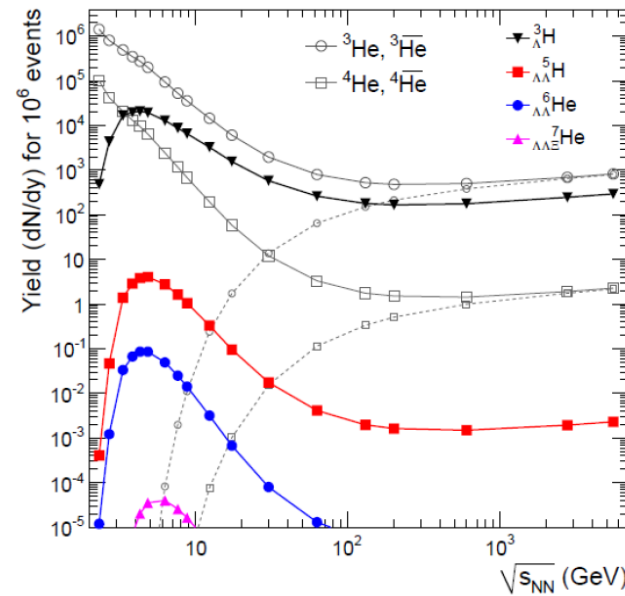


J-PARC  
FAIR • NICA

Compact Stars

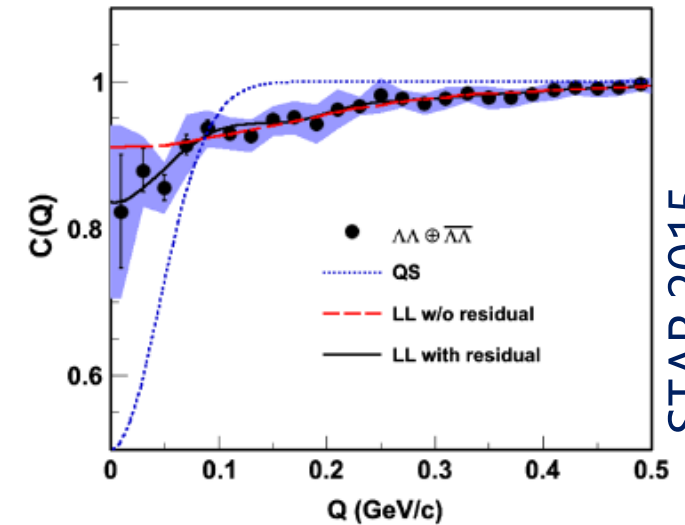
# Hadron/Hypernuclear Physics

## Hypernuclei



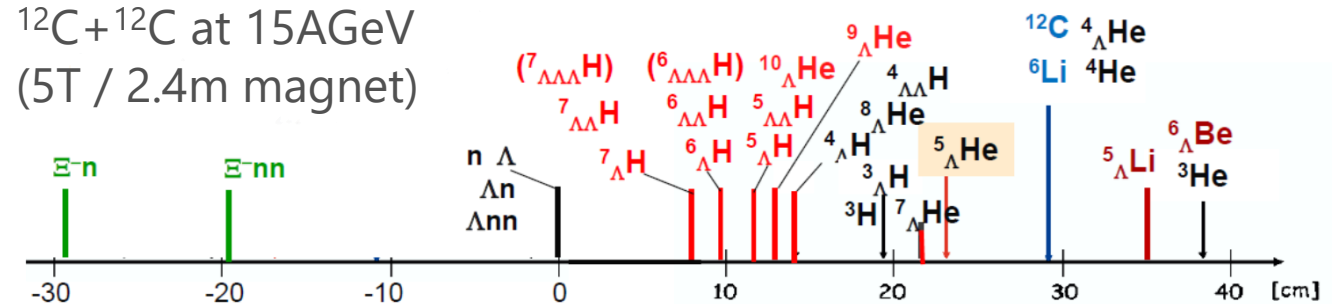
## Correlation functions

→ hadron interaction



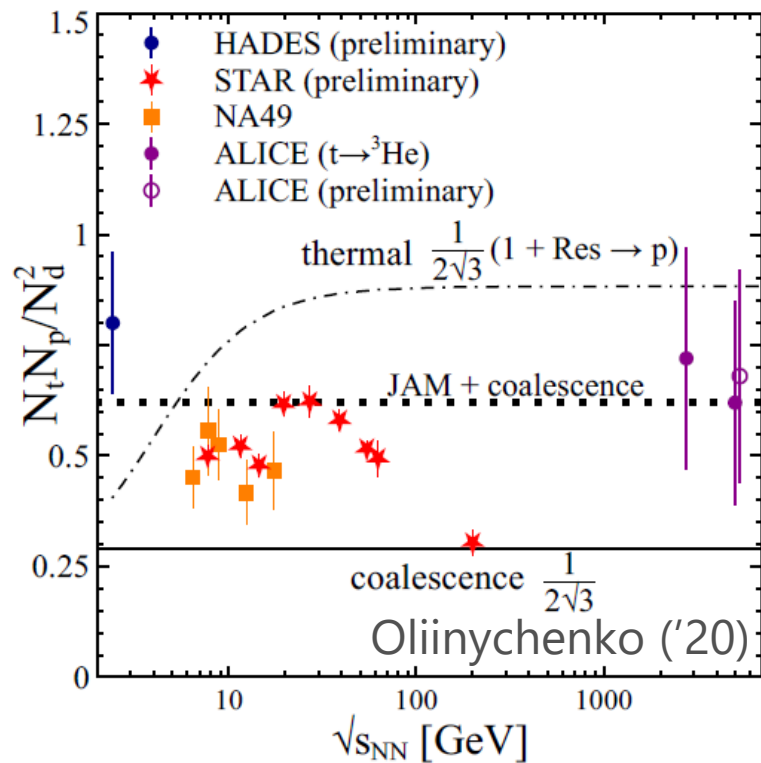
STAR, 2015

${}^{12}\text{C}+{}^{12}\text{C}$  at 15A GeV  
(5T / 2.4m magnet)



# Production Mechanism

## Light-nuclei production as a signal of QCD critical point



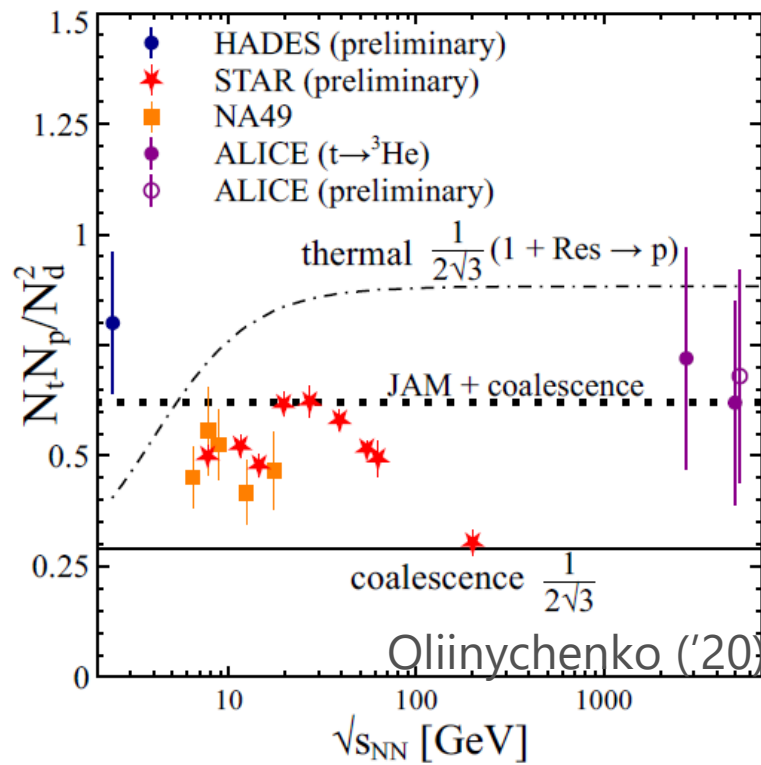
baryon fluctuations

→ enhancement of light nuclei?

Sun+ ('18)

# Production Mechanism

Light-nuclei production  
as a signal of QCD critical point

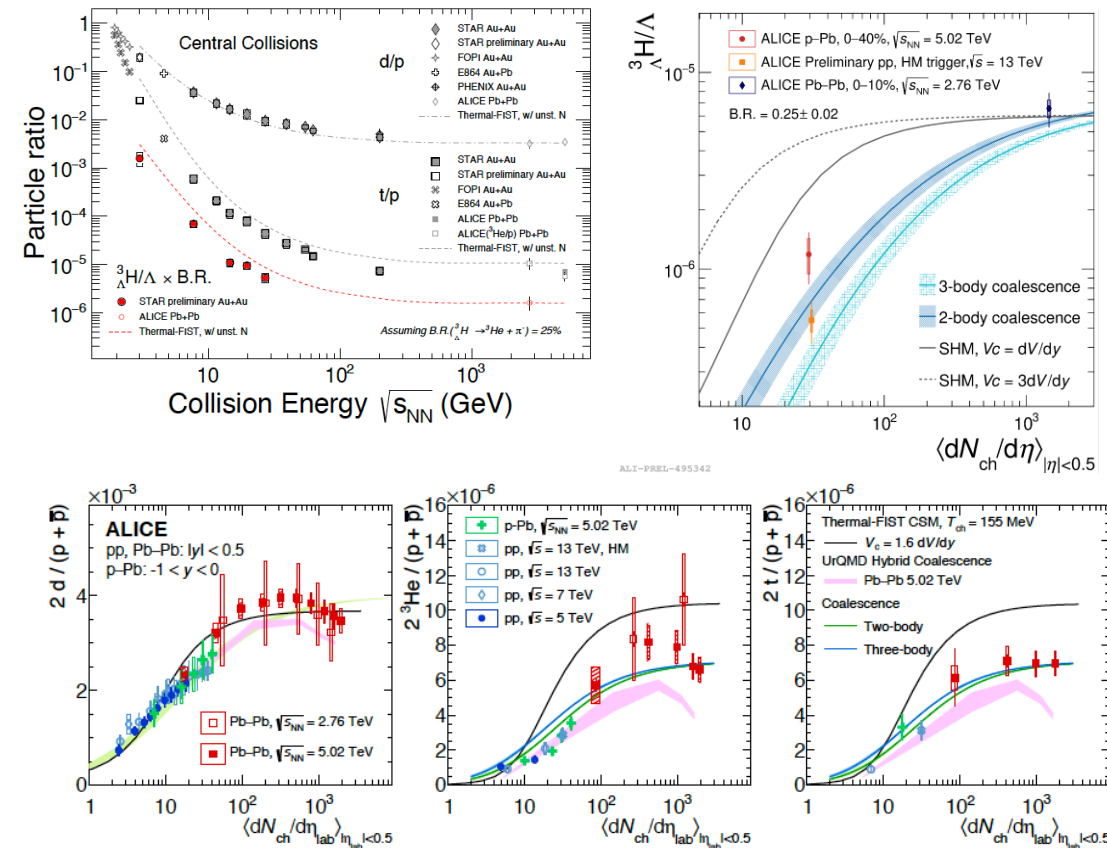


baryon fluctuations

→ enhancement of light nuclei?

Sun+ ('18)

Measurement of light/hyper-nuclei



from QM2023

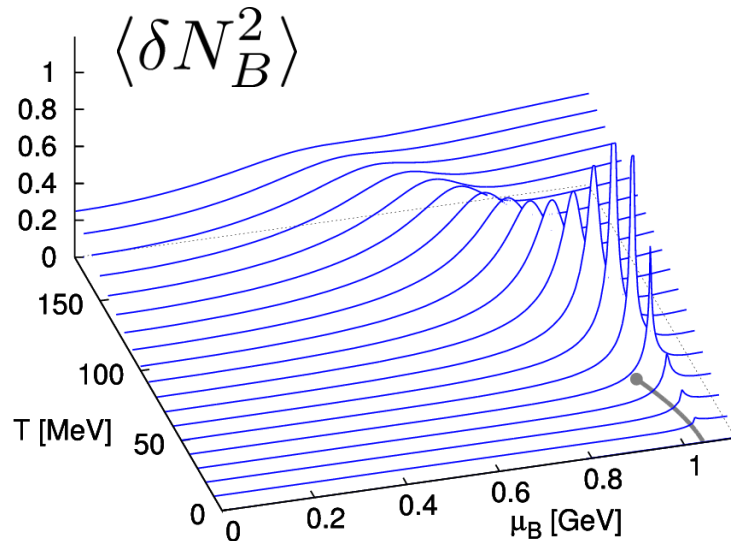
Precise data will lead us to a better understanding of production mechanism

# Event-by-event Fluctuations of Conserved Charges

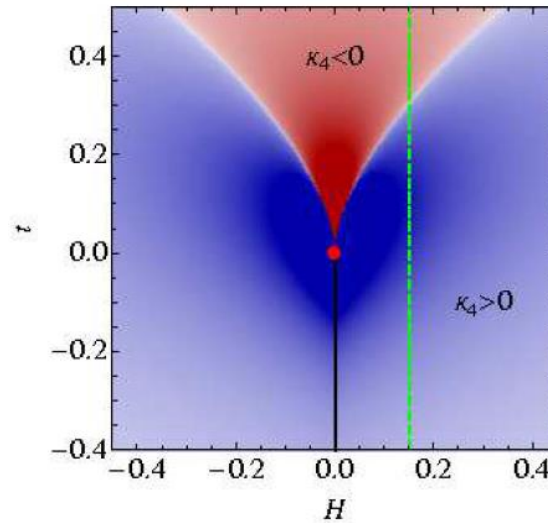
# Fluctuations, Cumulants of Conserved Charges

$$\langle N^m \rangle_c = \chi_m V$$

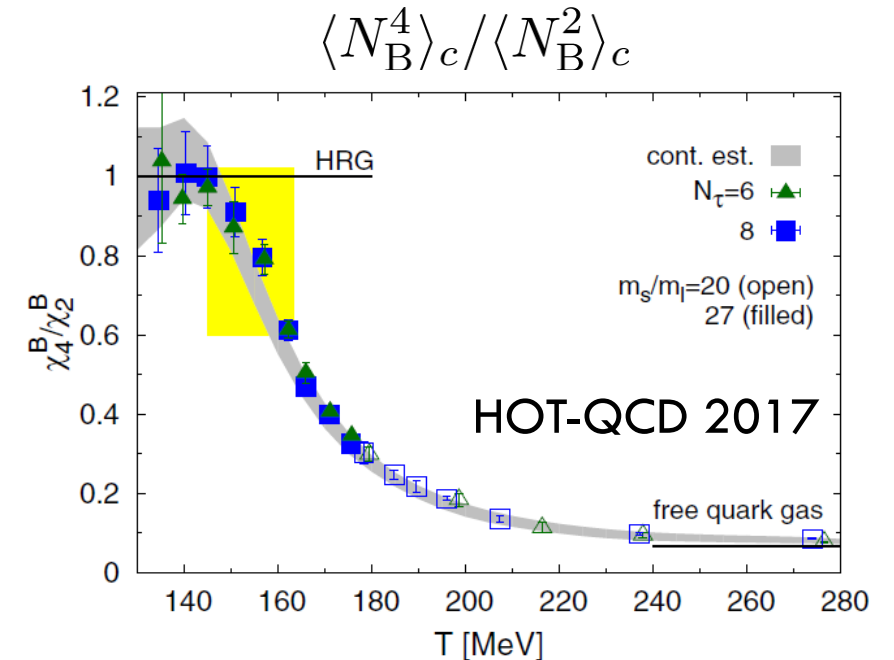
- ❑ Divergence and sign change at the QCD-CP. [Stephanov,'09](#); [Asakawa, Ejiri, MK,'09](#)
- ❑ Volume dependence is canceled out in ratio. [Ejiri, Karsch, Redlich,'05](#)
- ❑ Direct comparison with lattice QCD simulations.
- ❑ Slower diffusion.



Asakawa, Ejiri, MK (2009)

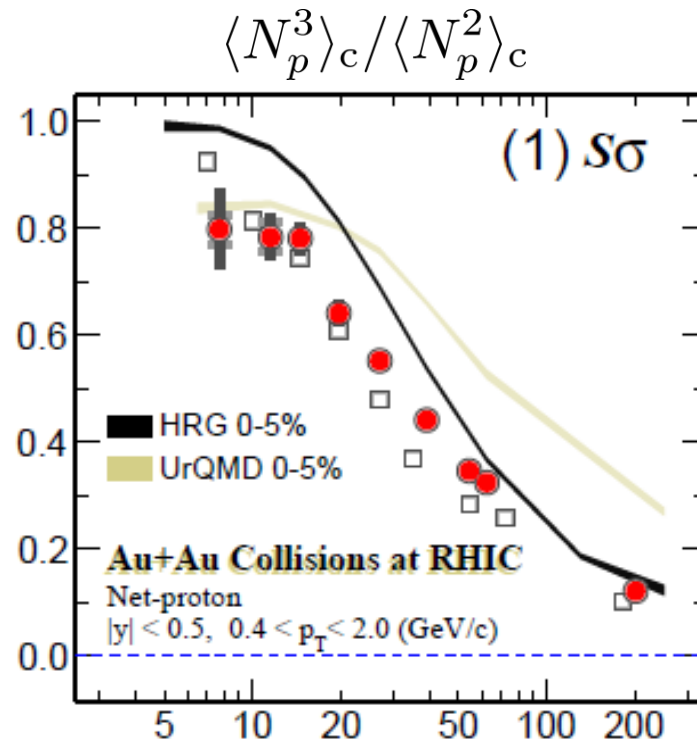
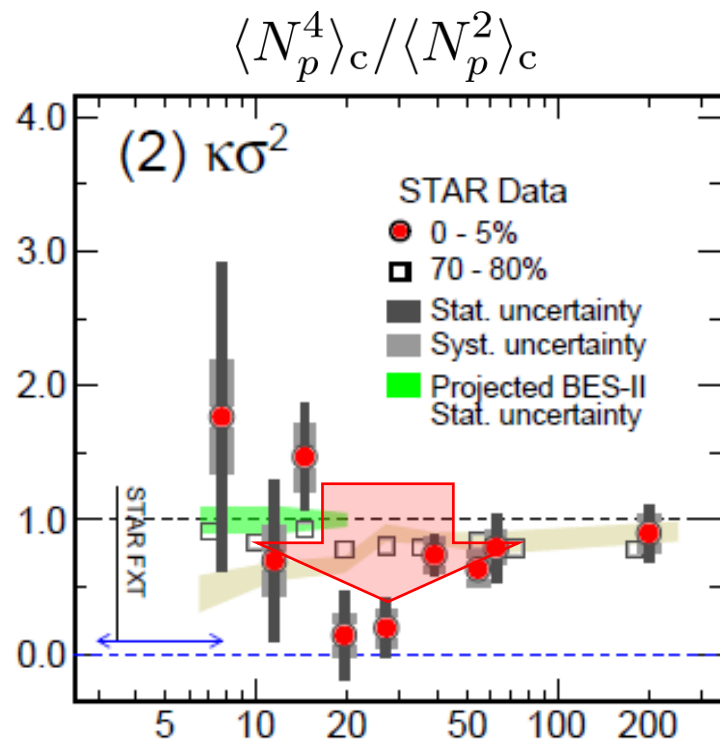


Stephanov (2011)



# Experimental Results

## Net-proton number cumulants

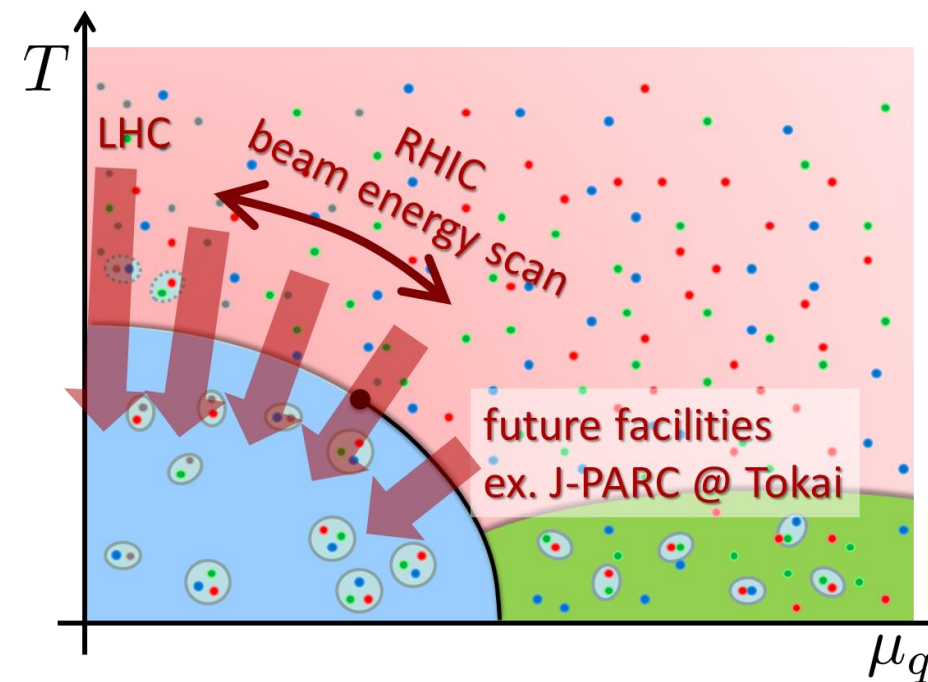


STAR, 2020 (2001.02852)

Non-Poisson and non-monotonic behaviors of the higher order cumulants.

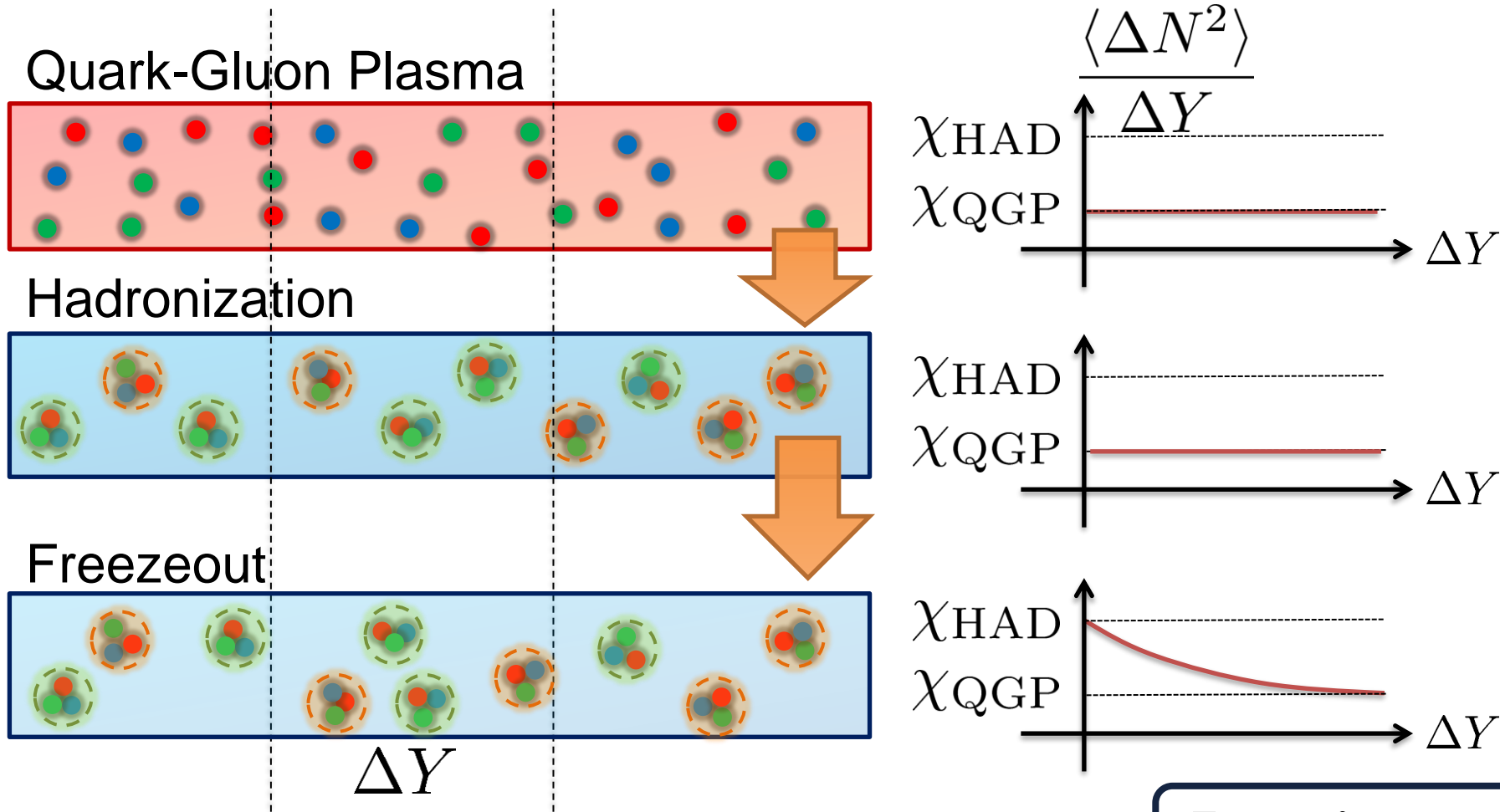
### Questions

- When are these fluctuations generated?
- Is the use of proton # cumulants as a proxy of baryon's justified?





# Evolution of Conserved-charge Fluctuations



Fluctuations of CC are modified by the diffusion.

↓

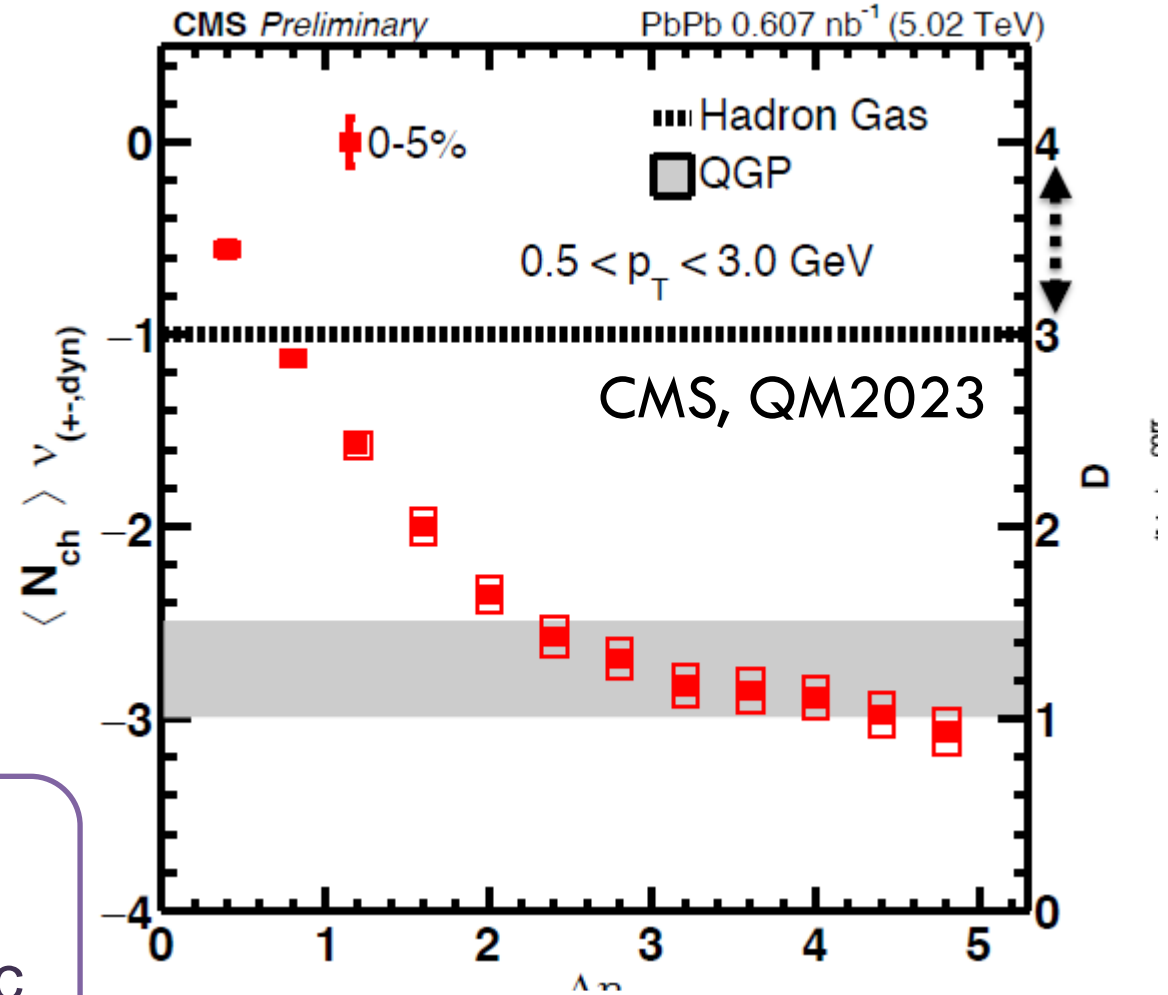
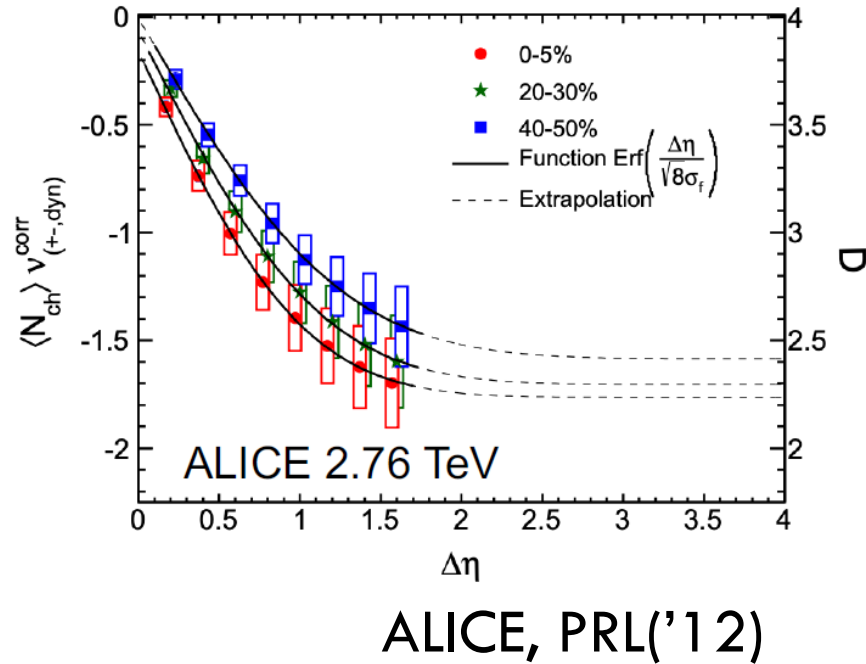
Relaxation time becomes longer as  $\Delta Y \rightarrow$  large.

- Experiments on  $\langle N_Q^2 \rangle$**
- No QGP signal @ RHIC ('02, '03)
  - QGP signal? @ ALICE ('12)

Asakawa, Heinz, Muller, 2000  
 Jeon, Koch, 2000; Shuryak, Stephanov, 2001

# Electric-charge Fluctuations: Wider $\Delta\eta$

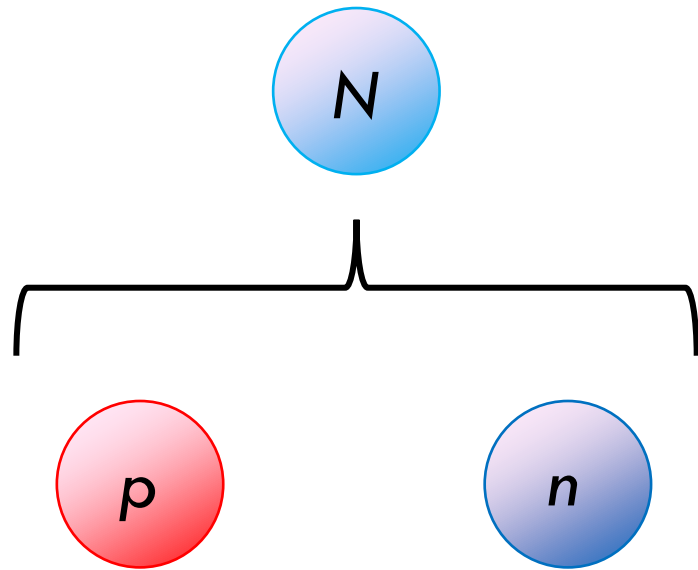
## □ D-measure



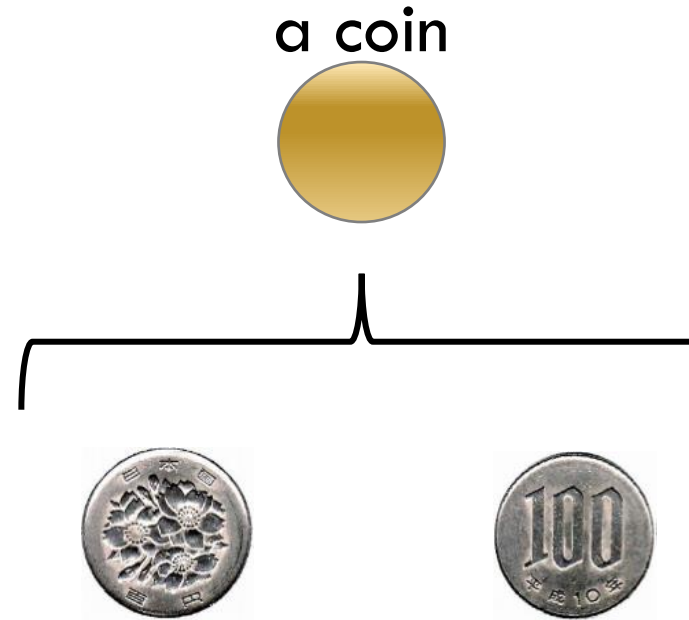
## D-measure

$$D = 4 \frac{\langle \delta N_Q^2 \rangle}{\langle N_Q^+ + N_Q^- \rangle} \left\{ \begin{array}{l} \bullet D \sim 3-4 \text{ Hadronic} \\ \bullet D \sim 1-1.5 \text{ Quark} \end{array} \right.$$

# Nucleon's Isospin as Two Sides of a Coin

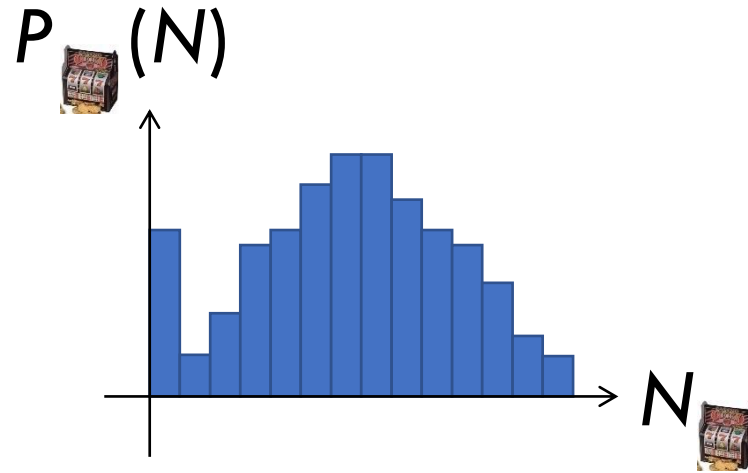


Nucleons have  
two isospin states.

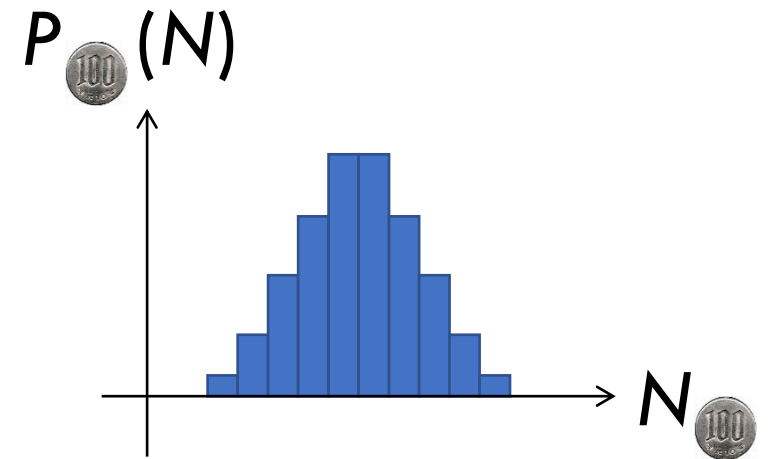
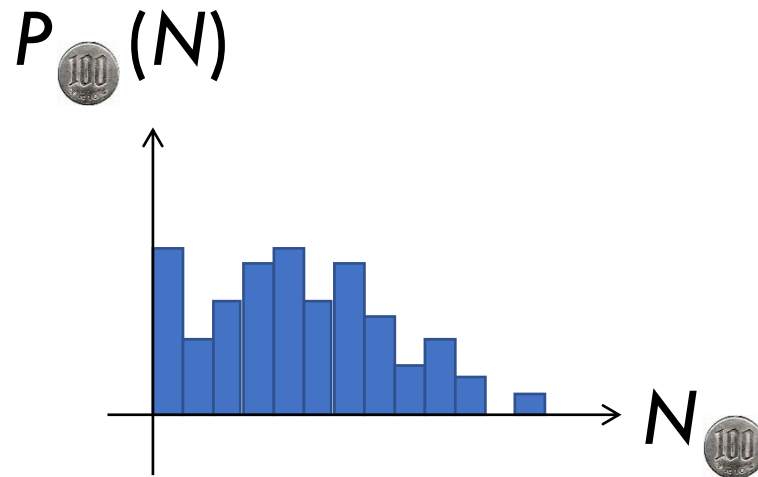
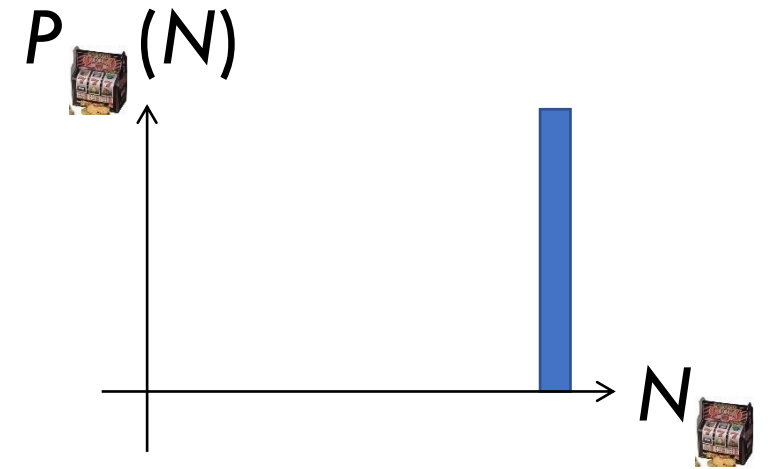


Coins have two sides.

# Slot Machine Analogy



Fixed # of coins



# Reconstruction of Total Coin #

$$P_{\text{100}}(N_{\text{100}}) = \sum_{\text{gold}} P_{\text{slot}}(N_{\text{gold}}) B_{1/2}(N_{\text{100}}; N_{\text{gold}})$$



## □ Example

$$\left\{ \begin{array}{l} 2\langle(\delta N_p^{(\text{net})})^2\rangle = \frac{1}{2}\langle(\delta N_B^{(\text{net})})^2\rangle + \frac{1}{2}\langle(\delta N_B^{(\text{net})})^2\rangle_{\text{free}} \\ 2\langle(\delta N_p^{(\text{net})})^3\rangle = \frac{1}{4}\langle(\delta N_B^{(\text{net})})^3\rangle + \frac{3}{4}\langle(\delta N_B^{(\text{net})})^3\rangle_{\text{free}} \\ 2\langle(\delta N_p^{(\text{net})})^4\rangle_c = \frac{1}{8}\langle(\delta N_B^{(\text{net})})^4\rangle_c + \dots \end{array} \right.$$

genuine info.
Poisson noise

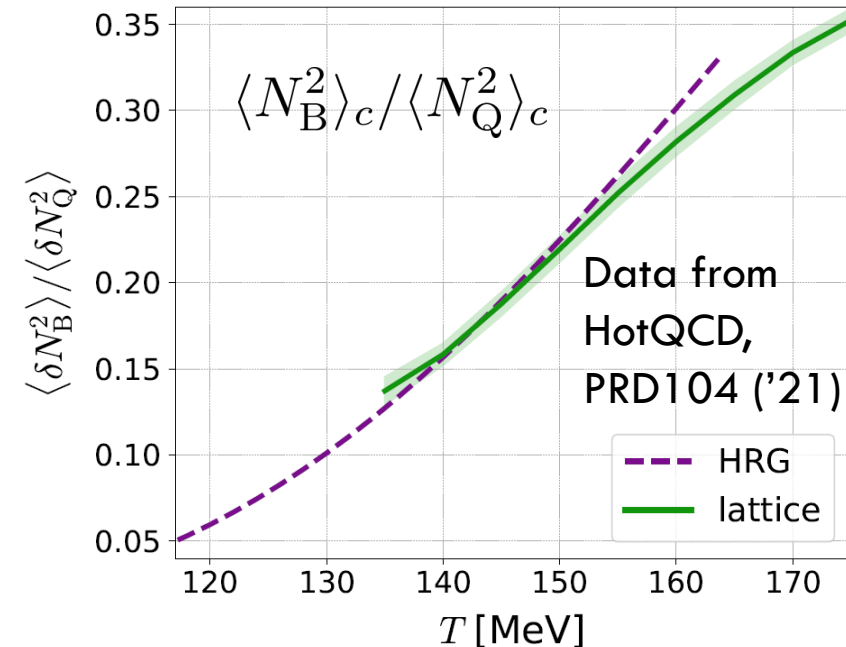
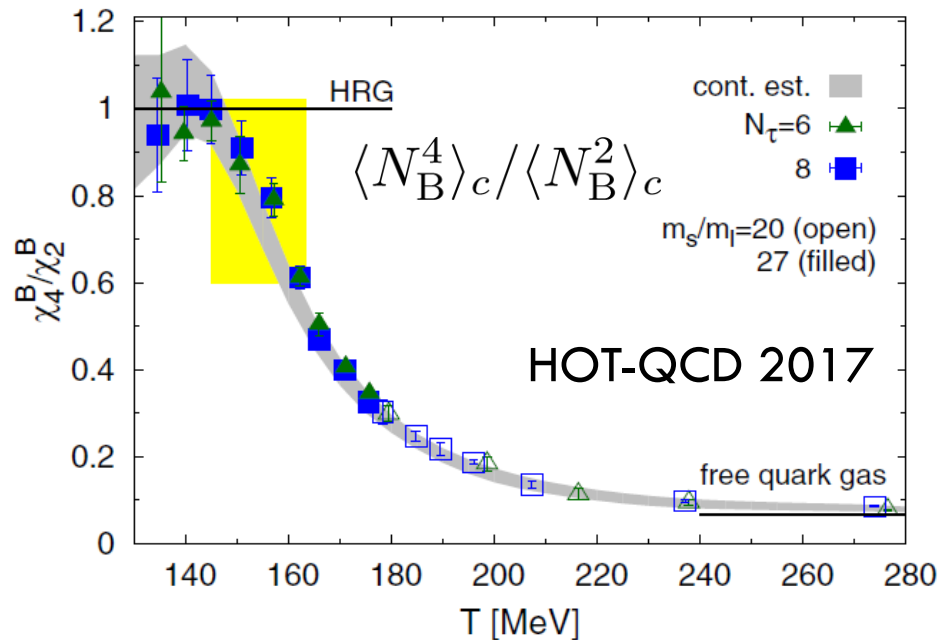
Note: Higher order cumulants are more fragile.

$$\langle N_B^2 \rangle_c / \langle N_Q^2 \rangle_c$$

$$\langle N_B^2 \rangle_c / \langle N_Q^2 \rangle_c$$

- Ratio of 2nd order: Suppress uncertainties from various experimental effects compared with higher orders.
- Almost linear  $T$  dependence around  $T_c^*$ .

- $\sqrt{s_{NN}} = 200\text{GeV}$
- 0-5% centrality
- $\Delta y$  dependence
- Construction of baryon number,  $p_T$ -acceptance correction



# Experimental Data

$$\langle N_p^2 \rangle_c$$

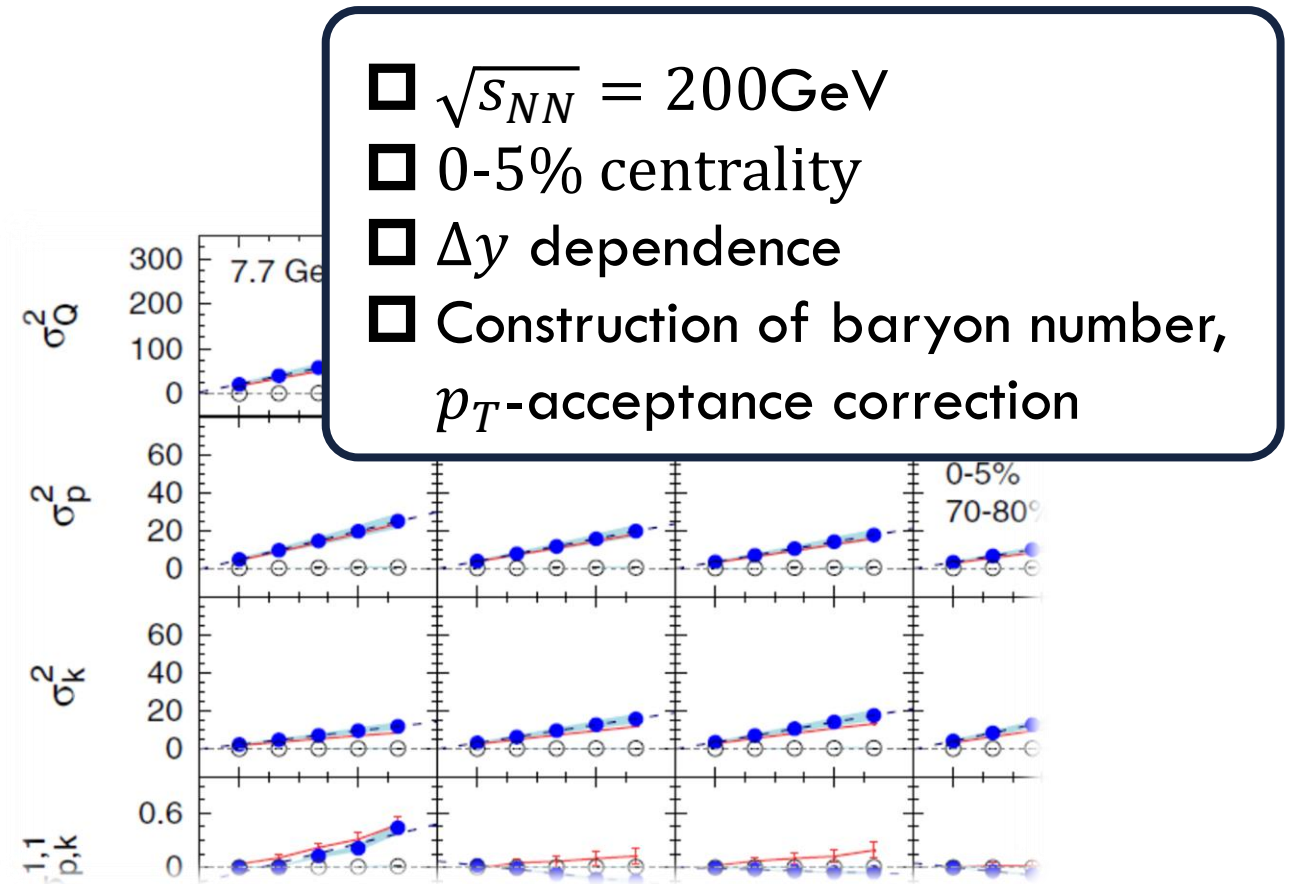
**STAR, PRC104,024902 (2021)**

- proton cumulants up to 4th order
- **rapidity window  $\Delta y$**
- $0.4 < p_T < 2.0 \text{ GeV}/c$

$$\langle N_Q^2 \rangle_c$$

**STAR, PRC100,014902 (2019)**

- 2nd mixed cumulants of p,  $\pi$ , K, Q
- **pseudo-rapidity window  $\Delta \eta$**
- $0.4 < p_T < 1.6 \text{ GeV}/c$
- Total charge: private comm. A. Chattergee



- proton  $\rightarrow$  baryon cumulants [MK, Asakawa, '12; '12](#)
- Rapidity is better than pseudo-rapidity  
[Ohnishi, MK, Asakawa, '16](#)
- Wider acceptance is more desirable.

# $p_T$ -Acceptance Correction

## $p_T$ Acceptance

$$0.4 < p_T < 1.6 \text{ [GeV/c]}$$

PRC100,014902('19)

$$0.4 < p_T < 2.0 \text{ [GeV/c]}$$

PRC104,024902('21)

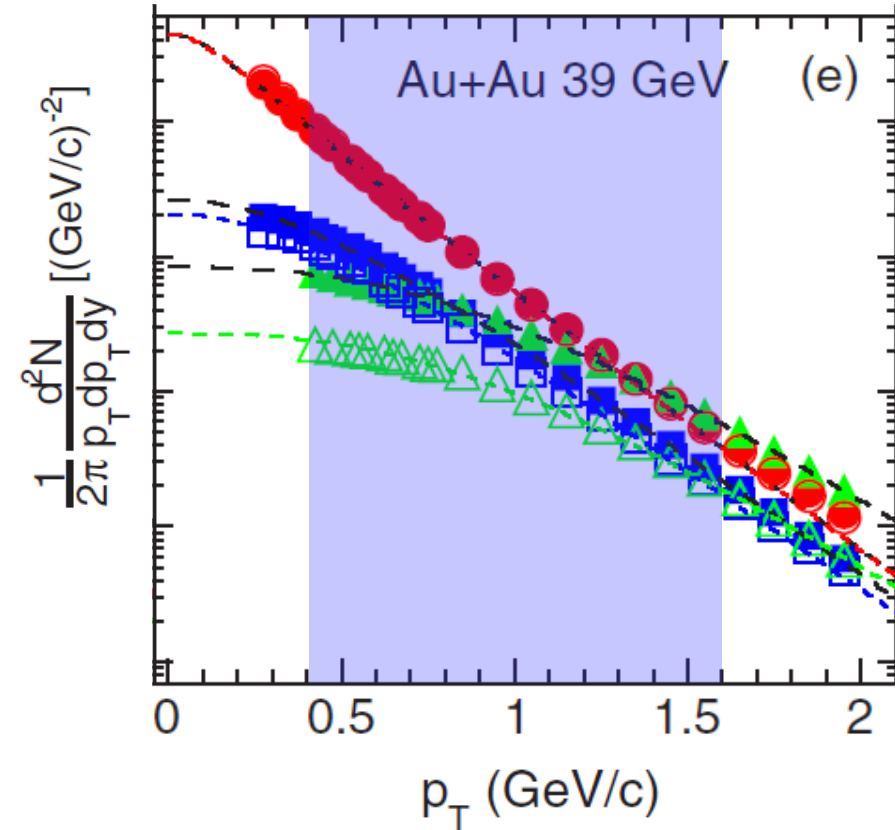


## Particles in $p_T$ space

- Electric charge: **49%**
- Protons: **82%**

blast wave model @  $\sqrt{s_{NN}}=200$  GeV

Modification by  $p_T$ -cut should be corrected.  
This study: Binomial distribution model.



$$\langle N_{\text{net}}^2 \rangle_c^{\text{corrected}} = \frac{1}{p^2} \left( \langle n_{\text{net}}^2 \rangle_c - (1-p) \langle n_{\text{tot}} \rangle_c \right)$$

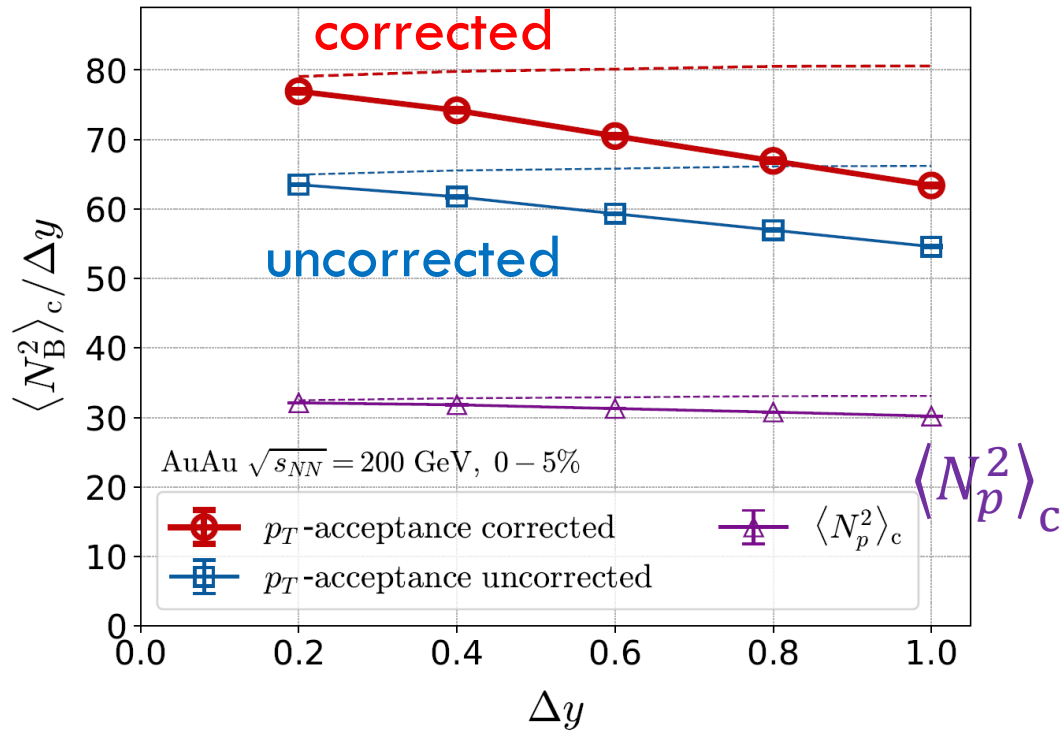
MK, Asakawa, '12, '12



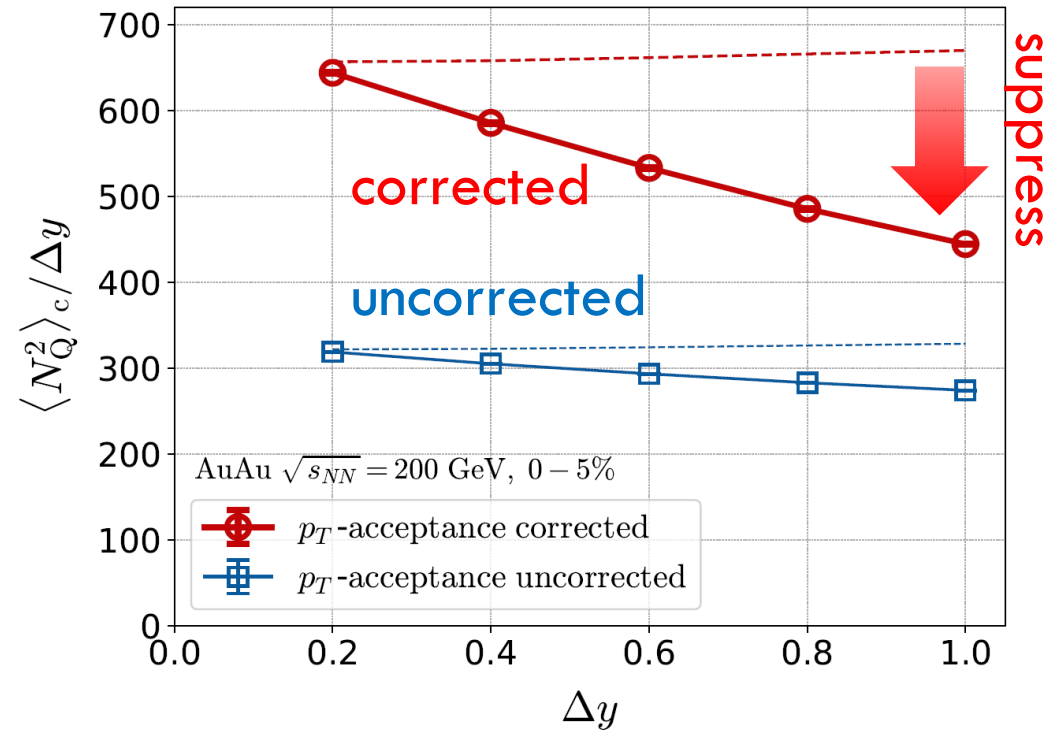
# Cumulants: Proton $\rightarrow$ Baryon & Acceptance Correction

Data from STAR, '19, '21

$$\langle N_B^2 \rangle_c / \Delta y$$



$$\langle N_Q^2 \rangle_c / \Delta y$$



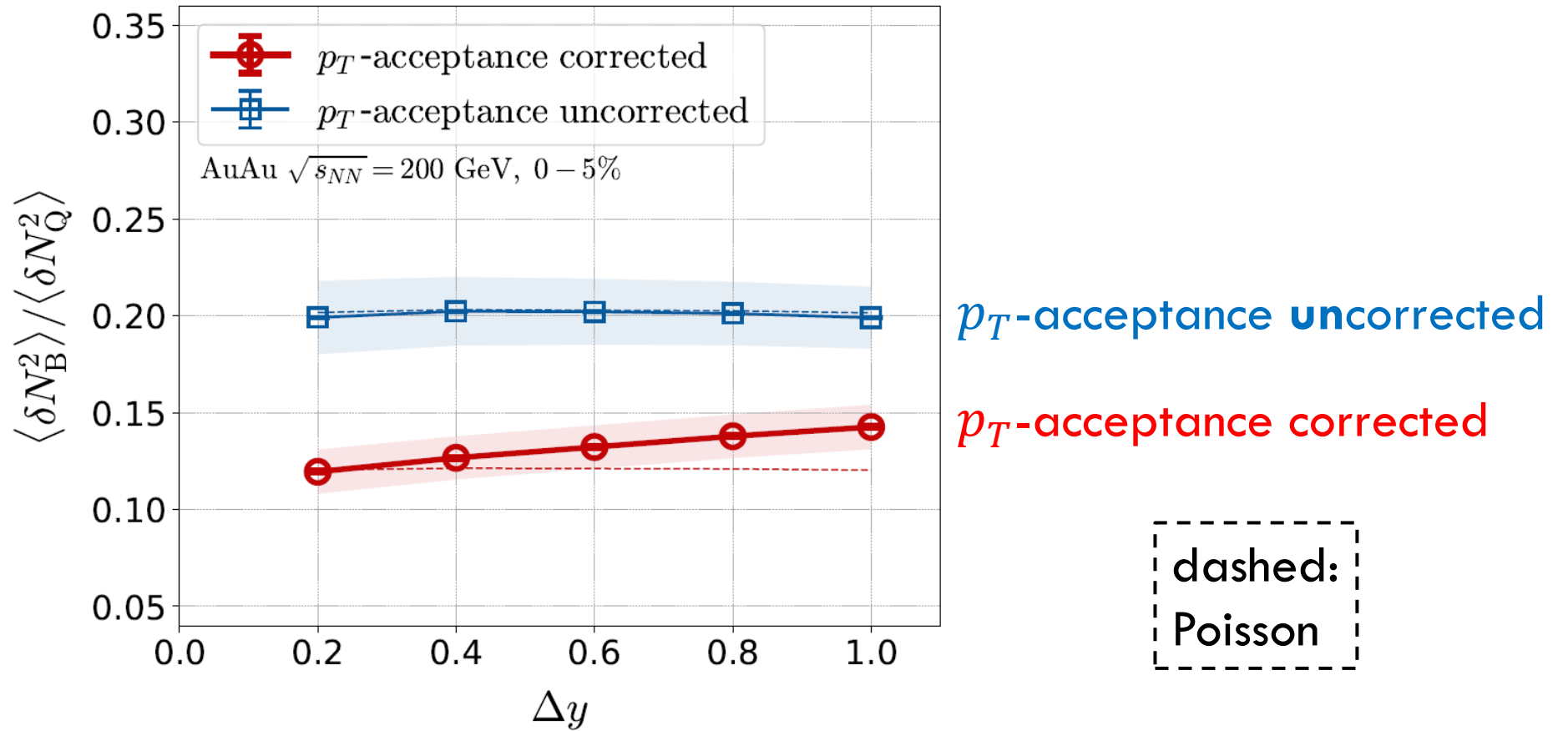
dashed:  
 $\langle N^{\text{tot}} \rangle$   
Poisson

$\square$  Deviation from Poissonian is clarified by the acceptance correction.

$$\langle N_{\text{net}}^2 \rangle_c^{\text{corrected}} = \frac{1}{p^2} \left( \langle n_{\text{net}}^2 \rangle_c - (1-p) \langle n_{\text{tot}} \rangle_c \right)$$

MK, Asakawa, '12, '12

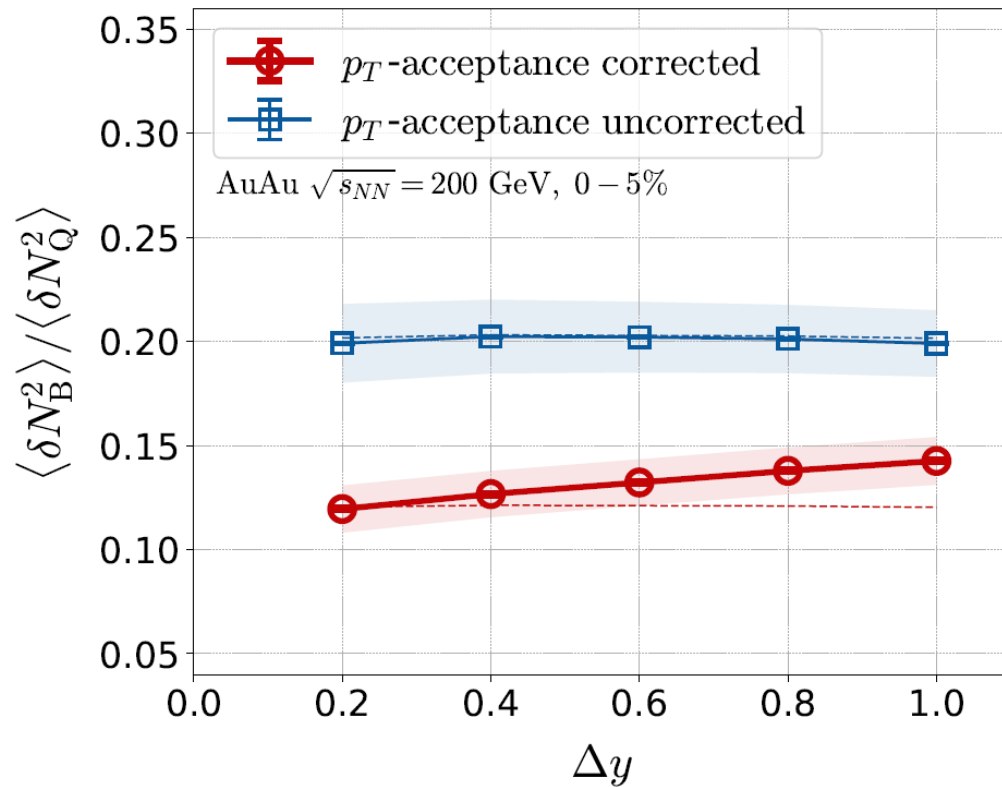
$$\langle N_B^2 \rangle_c / \langle N_Q^2 \rangle_c$$



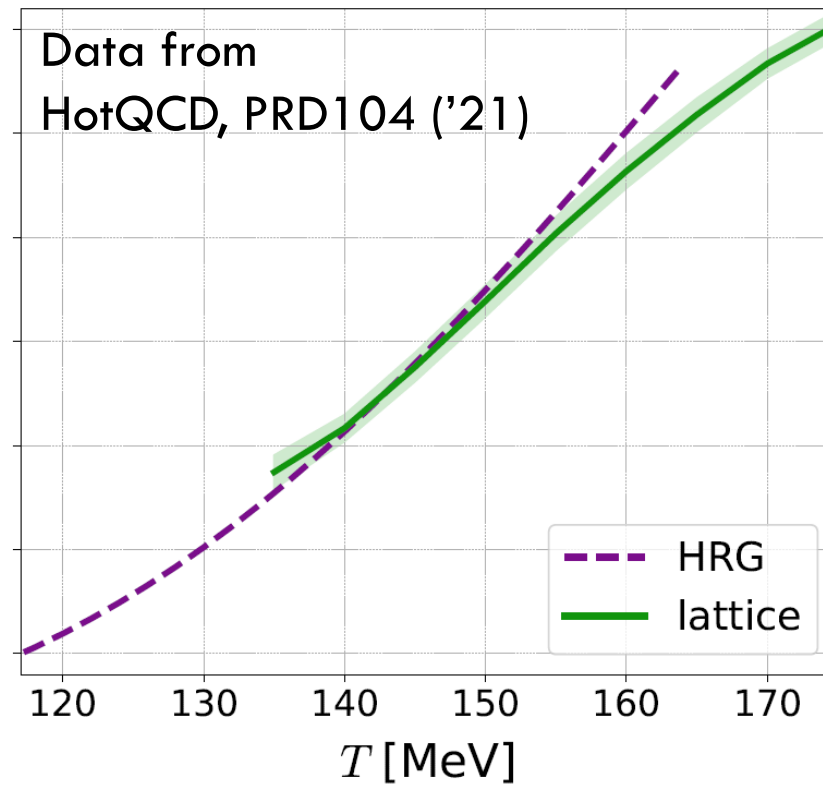
- $\langle N_B^2 \rangle_c / \langle N_Q^2 \rangle_c$  becomes smaller due to the  $p_T$ -acceptance correction.
- Clear  $\Delta y$  dependence → non-thermal effects behind fluctuations

# HIC vs HRG&LAT

## From data @ STAR



## HRG+Lattice

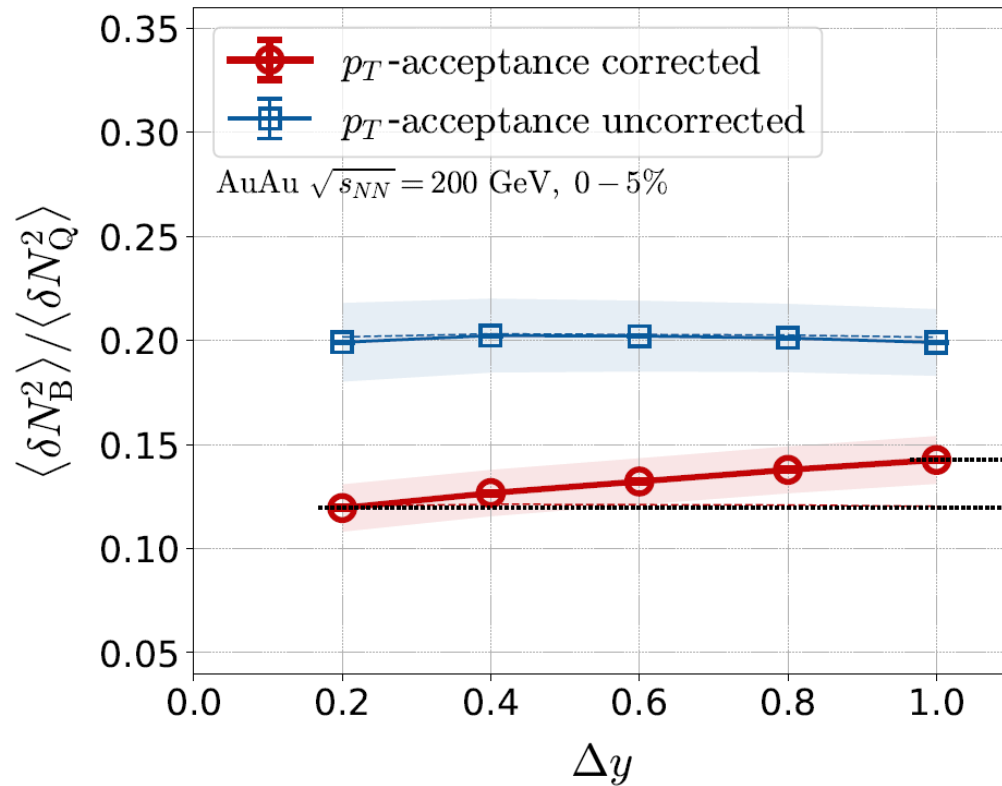


□  $T = 134 \sim 138$  MeV  
□ Significantly lower than  $T_{\text{chem}}$

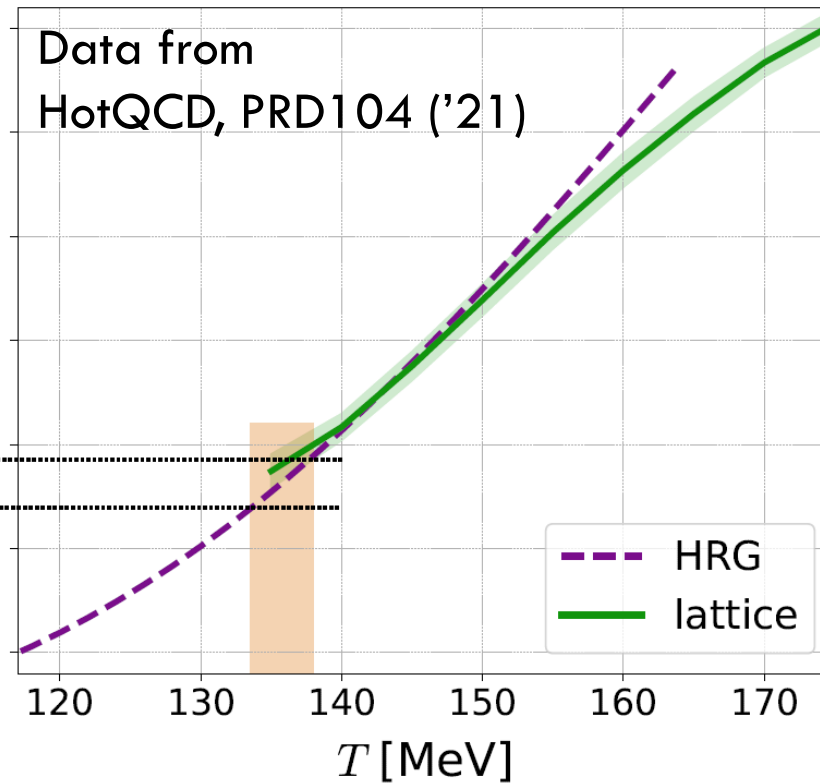
HRG: QMHRG2020  
Bollweg+, PRD104, 7 ('21)  
Volume dep. corrected  
plot by MK

# HIC vs HRG&LAT

## From data @ STAR



## HRG+Lattice



- $T = 134 \sim 138$  MeV
- Significantly lower than  $T_{\text{chem}}$

HRG: QMHRG2020  
Bollweg+, PRD104, 7 ('21)  
Volume dep. corrected  
plot by MK

# Effect of Diffusion and Rapidity Conversion

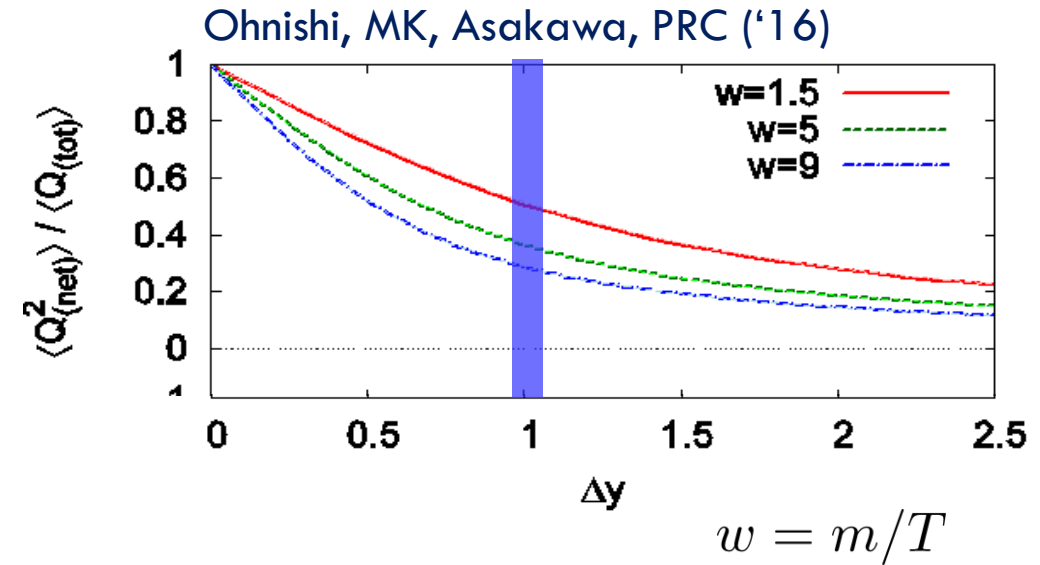
□ Blurring due to diffusion & rapidity conversion ( $Y \rightarrow y$ )

- Stronger modification in Q than B

□ Resonance Decays

- About 30% charged particles come from RD
- Enhancement of charged particles

➔ {  
□ Increase  $\langle N_Q^2 \rangle$   
□ Reduce  $\langle N_B^2 \rangle_c / \langle N_Q^2 \rangle_c$



These effects will be more important  
for higher order cumulants!

# Dilepton Production as experimental observables of Color Superconductivity & QCD-CP

Nishimura, MK, Kunihiro, PTEP2022, 093D02

Nishimura, MK, Kunihiro, PTEP2023, 053D01

# Observing CSC in HIC

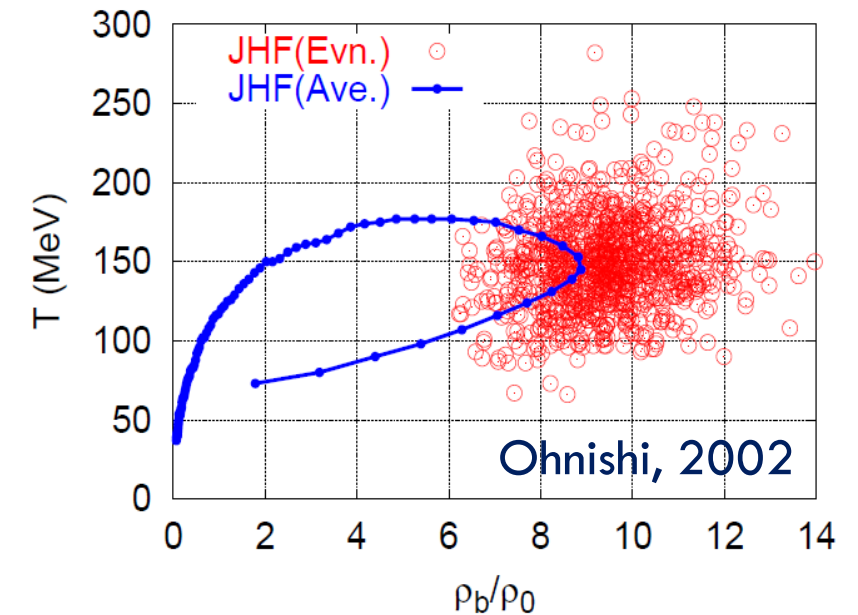
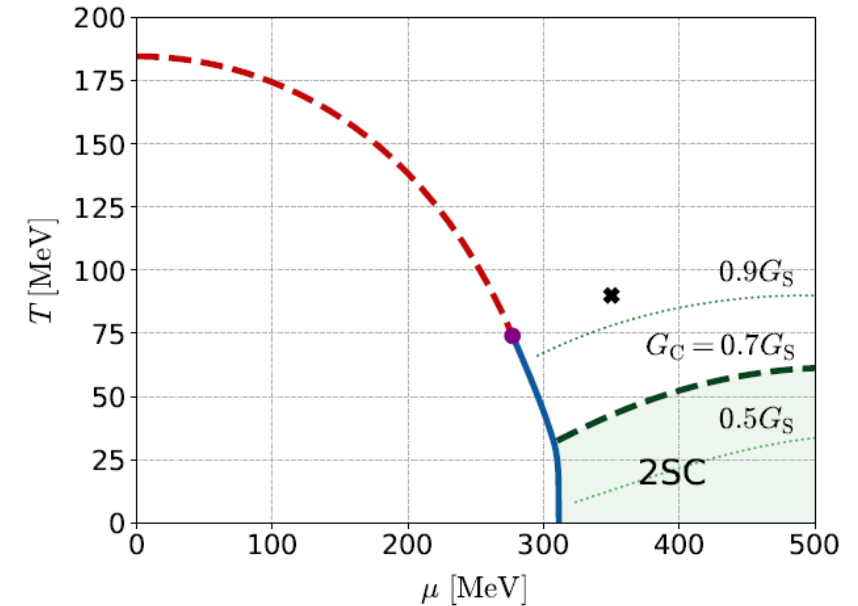
## □ Difficulties

- CSC would not be created if  $T_c$  is not high enough.
- Even if created, its lifetime would be short.
- Since CSC is created in the early stage, its signal would be blurred during the evolution in later stage.



## □ Strategy in the present study:

- Use dilepton production as an observable
- Focus on precursory phenomena of CSC



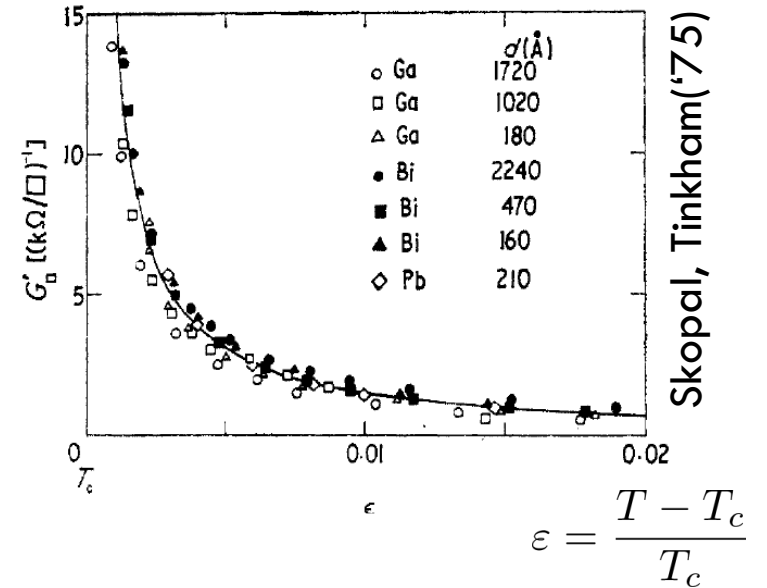
# Precursor of CSC

## □ Anomalous behavior of observables near but above $T_c$ of SC

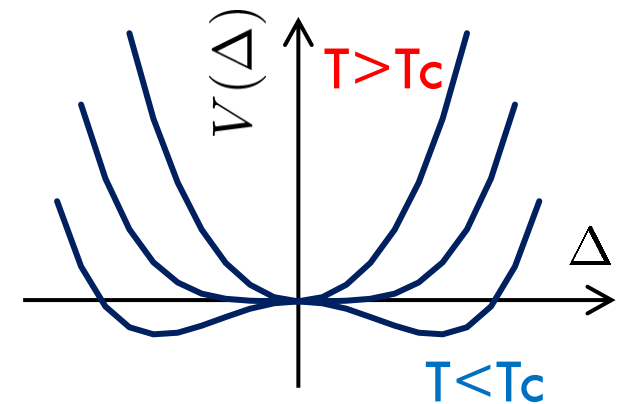
- electric conductivity
- magnetic susceptibility
- pseudogap

- Enhanced pair fluctuations is one of the origins of precursory phenomena.
- More significant phenomena in strongly-coupled systems.

Electric conductivity



Landau's free energy

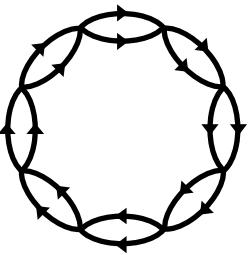




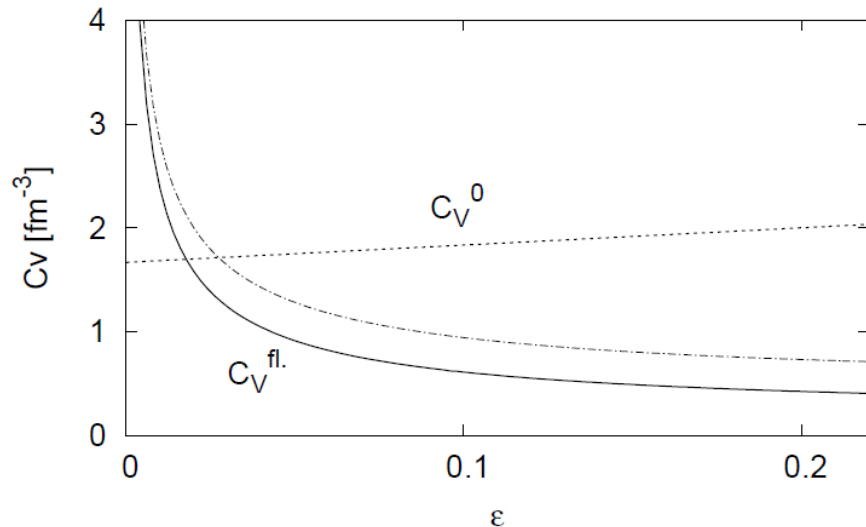
# Precursor of Color Superconductivity

MK, Koide, Kunihiro, Nemoto, '03, '05

## □ Thermodynamic Potential

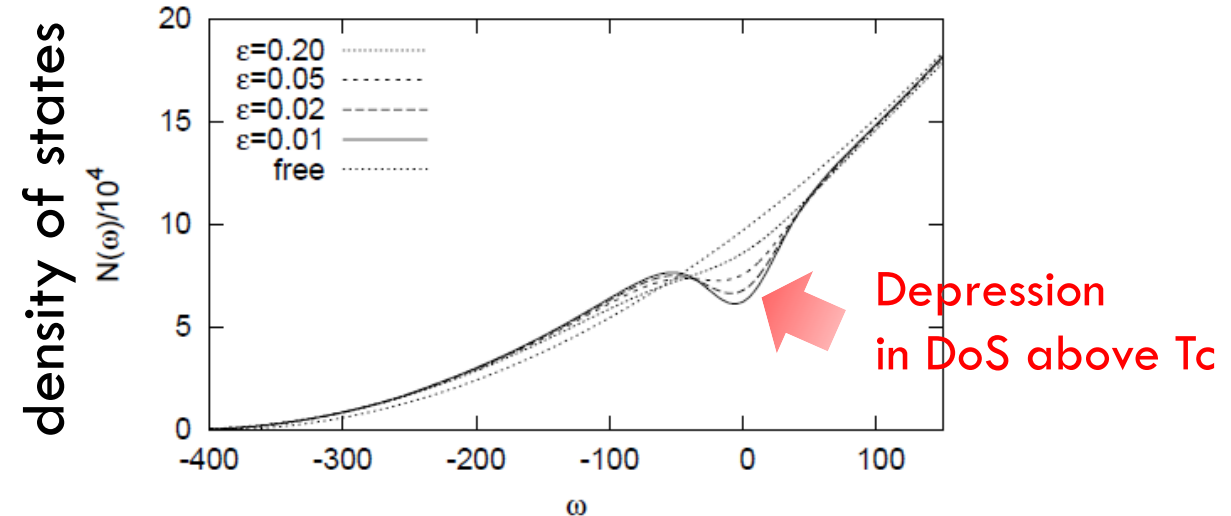
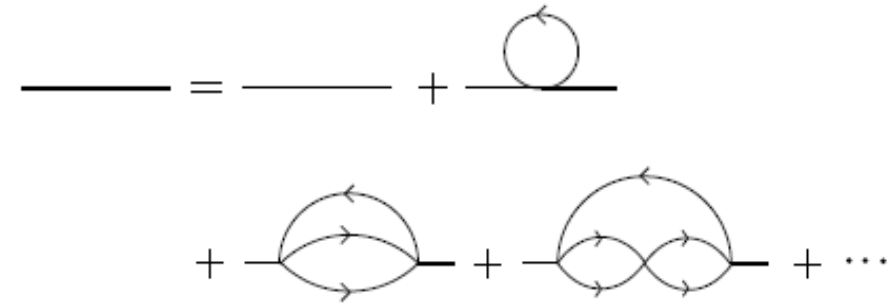
$\Omega =$    $\rightarrow$  Specific heat

$$c = -T \frac{\partial^2 \Omega}{\partial T^2}$$



$$\varepsilon = \frac{T - T_c}{T_c}$$

## □ Pseudogap



# Model

## NJL model (2-flavor)

$$\mathcal{L} = \bar{\psi}i\not{\partial}\psi + \mathcal{L}_S + \mathcal{L}_C$$

$$\mathcal{L}_S = G_S ((\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma_5\tau\psi)^2)$$

$$\mathcal{L}_C = G_C ((\bar{\psi}i\gamma_5\tau_A\lambda_A\psi^C)(\text{h.c.}))$$

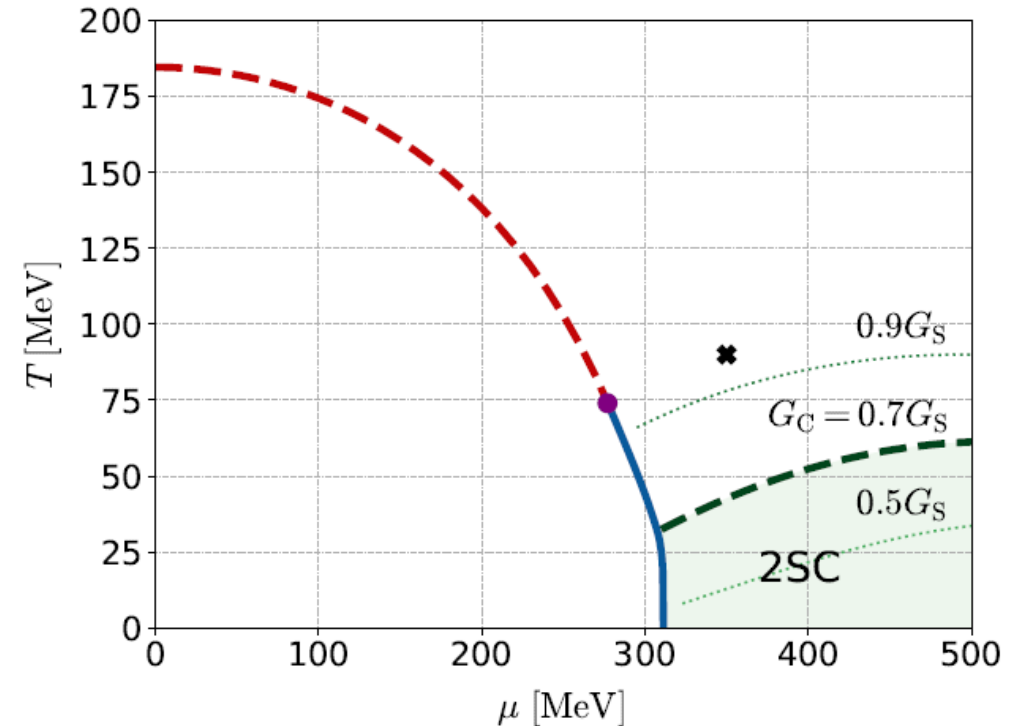
diquark interaction

## Parameters

$$G_S = 5.01 \text{ GeV}^{-2}, \quad \Lambda = 650\text{MeV}, \quad m_q = 0$$



## Phase Diagram in MFA



- Order of phase transition
  - 2nd in the MFA
  - can be 1st due to gauge fluctuation

Matsuura+('04), Giannakis+('04)  
Noronha+('06), Fejos, Yamamoto('19)

# Di-quark Fluctuations

## □ Diquark Propagator

$$D^R(x) = \langle [\Delta^\dagger(x), \Delta(0)] \rangle \theta(t) = \Rightarrow \Rightarrow$$

## □ Random Phase Approximation

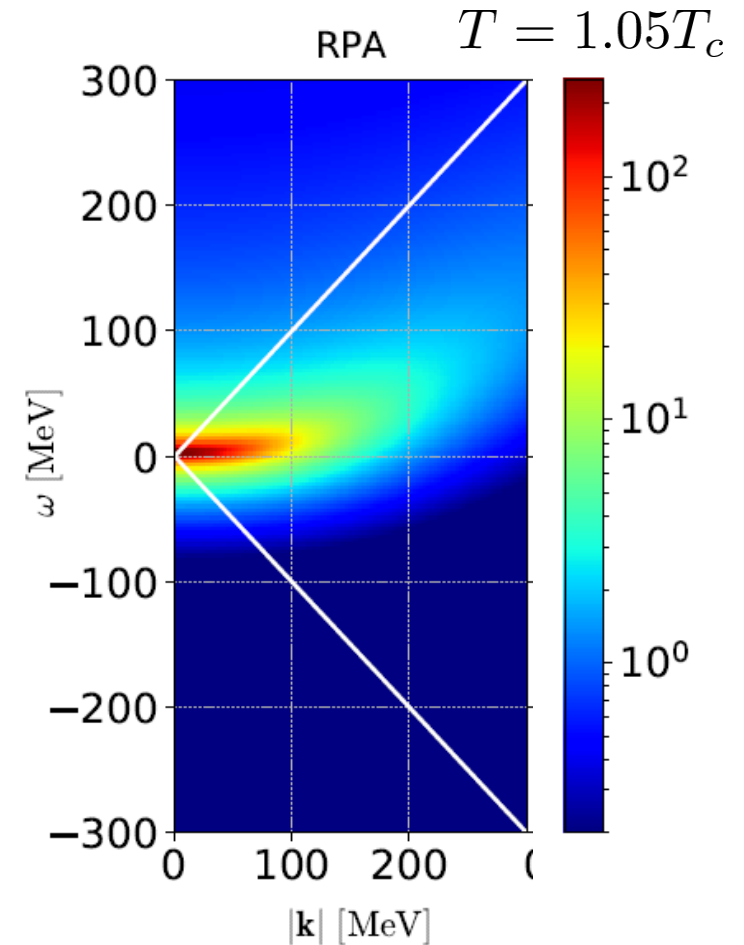
$$\begin{aligned} \Rightarrow \Rightarrow &= \text{loop} + \text{two loops} + \dots \\ &= \frac{Q^R(\mathbf{k}, \omega)}{1 + G_C Q^R(\mathbf{k}, \omega)} \\ Q^R(\mathbf{k}, \omega) &= \text{loop} \end{aligned}$$

- Diquark field becomes massless at  $T=T_c$
- Soft mode of CSC transition
- Strength in the space-like region

MK, Koide, Kunihiro, Nemoto, '01,'05

## Dynamical Structure Factor

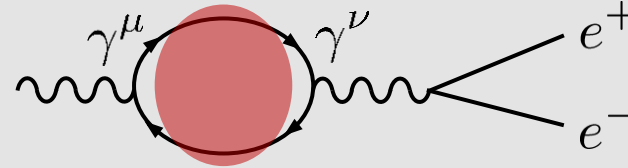
$$S(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{1}{1 - e^{-\beta\omega}} \text{Im} D^R(\mathbf{k}, \omega)$$



# Photon Self-Energy: Precursor of CSC

## □ Dilepton Production Rate

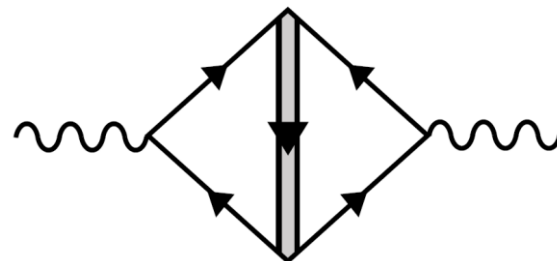
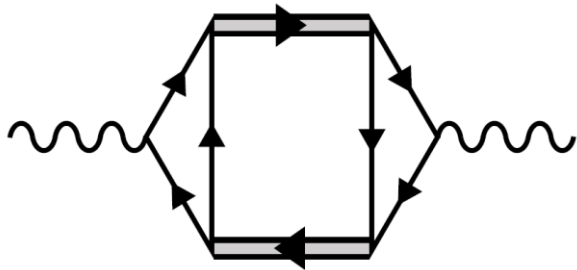
$$\frac{d^4\Gamma}{dk^4} = \frac{\alpha}{12\pi^4} \frac{1}{k^2} \frac{1}{e^{\beta\omega}-1} \text{Im}\Pi^{R\mu}_{\mu}(k)$$



## □ Effect of Di-quarks on $\Pi^{\mu\nu}(k)$

Aslamasov-Larkin term

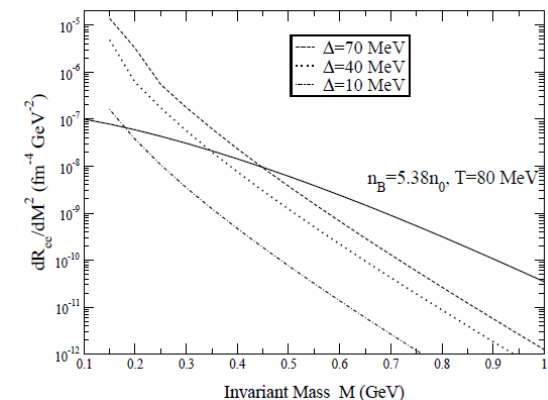
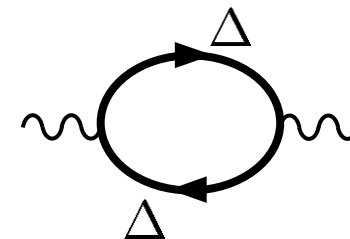
Maki-Thompson term



Well-known diagrams in metallic SC  
for describing paraconductivity

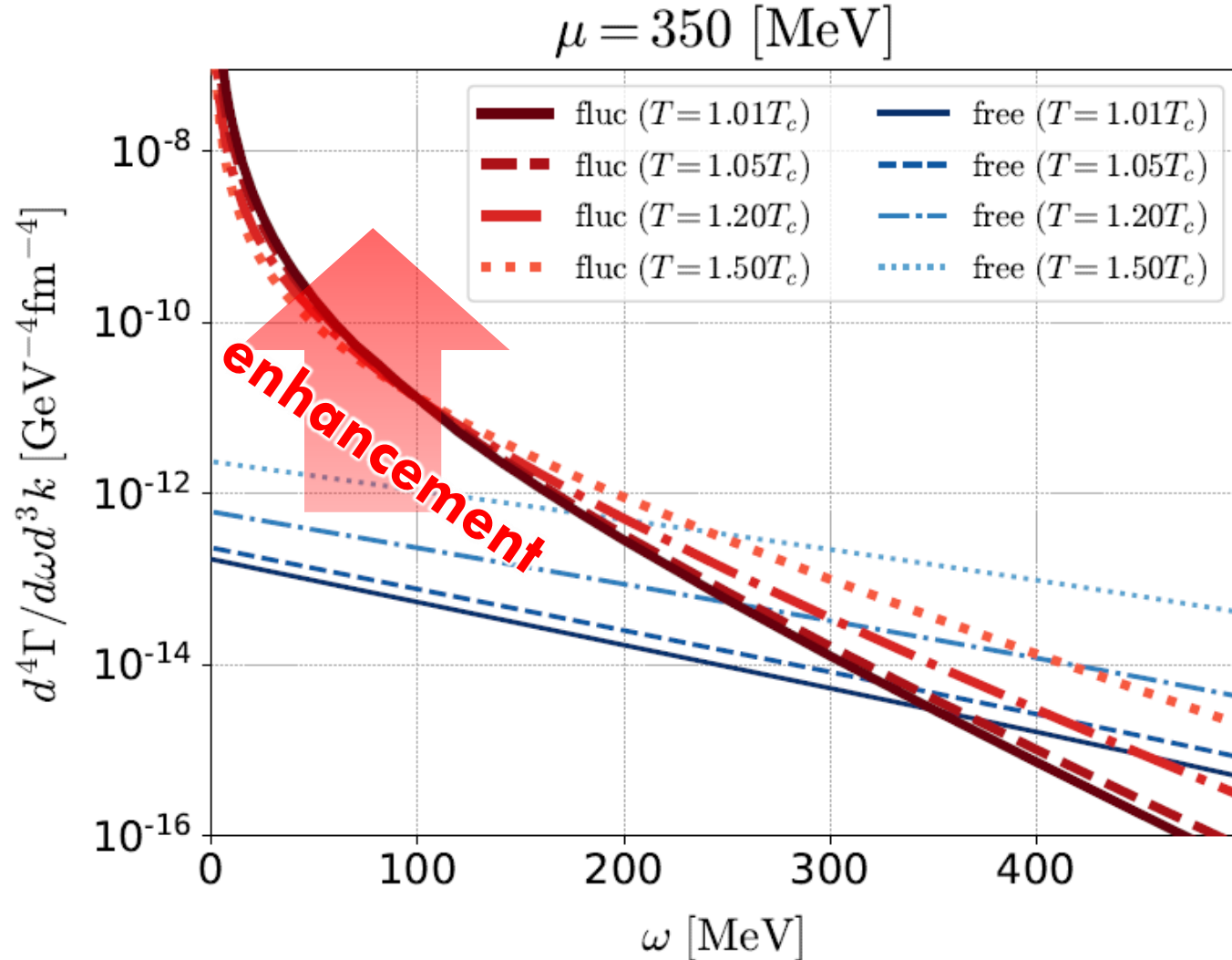
## □ DPR from CFL phase

Jaikumar, Rapp, Zahed ('02)



# Production Rate at $k = 0$

Nishimura, MK, Kunihiro ('22)



**Red:** fluctuation contribution

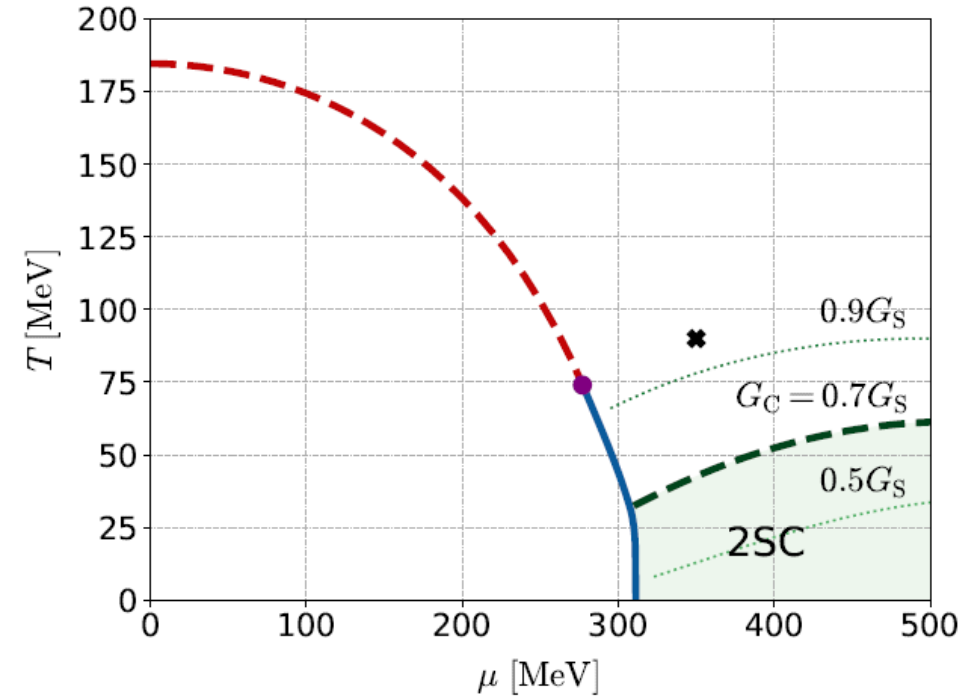
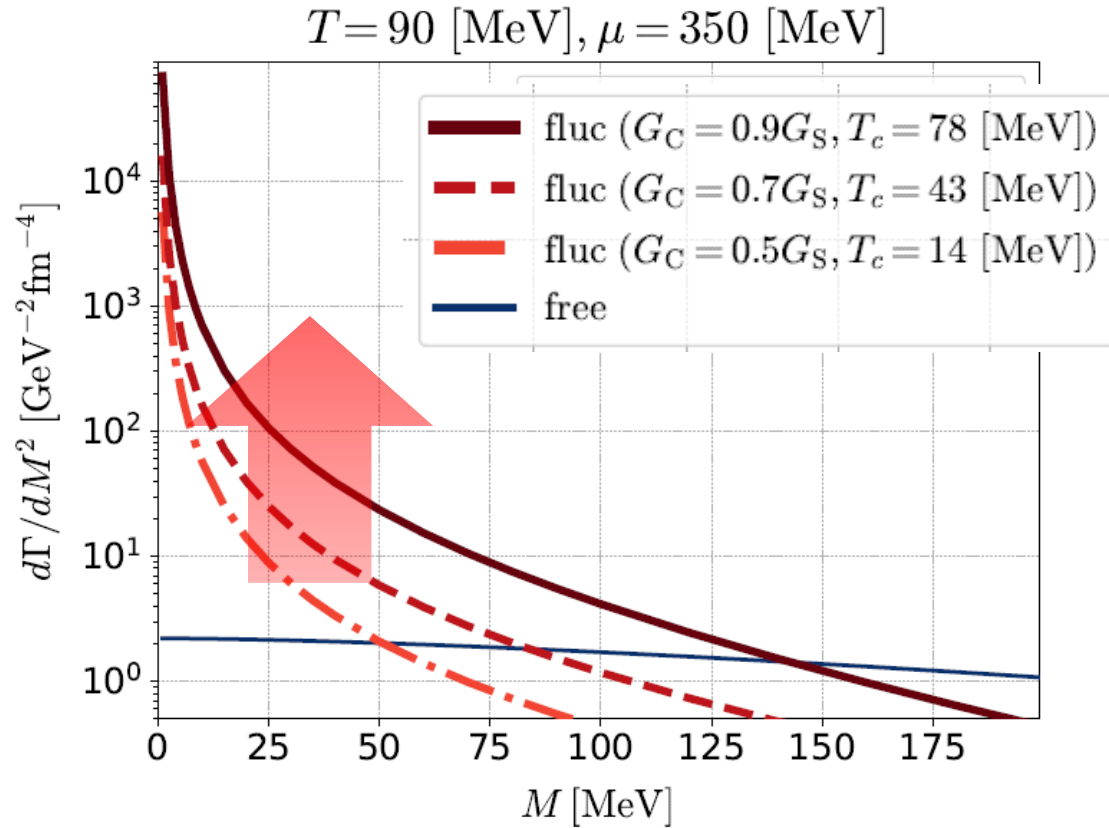
**Blue:** free quarks

$$G_C = 0.7G_S, T_C \simeq 45 \text{ MeV}$$

- Di-quark fluctuations give rise to large enhancement in the low energy region  $\omega < 200$  MeV and  $T < 1.5T_c$ .
- Anomalous enhancement is not sensitive to  $T$ .

# Invariant-Mass Spectrum

Nishimura, MK, Kunihiro ('22)



- ❑ Strong enhancement at low invariant mass.
- ❑ **Observable in the HIC?**

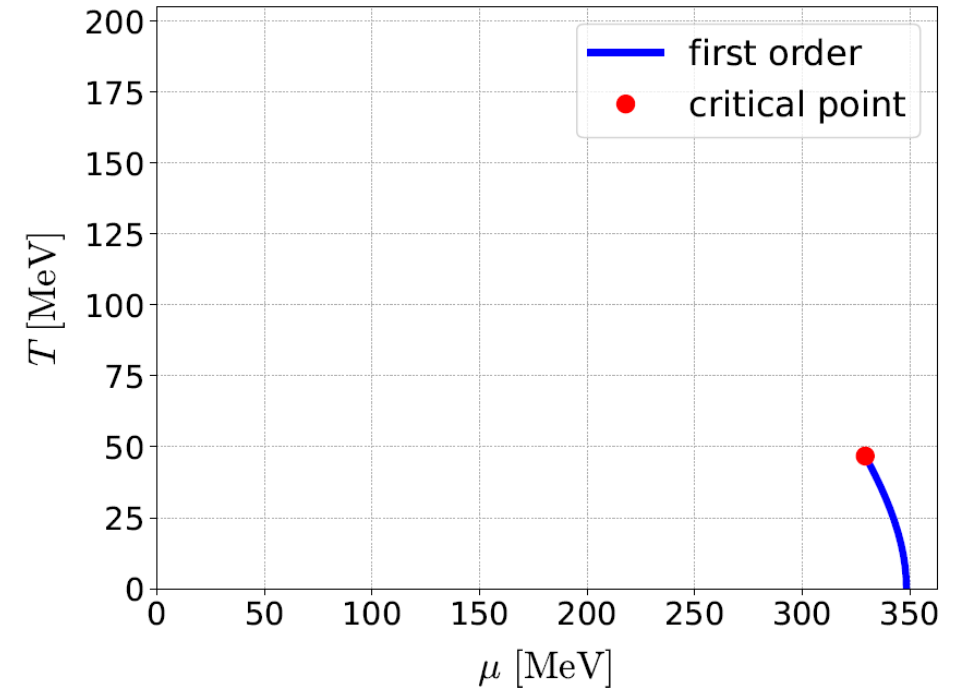
# Dileptons from QCD Critical Point

## NJL model (2-flavor)

$$\mathcal{L} = \bar{\psi}(i\partial - m)\psi + G_S((\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma_5\tau\psi)^2)$$

## Parameters

$$G_S = 5.5 \text{ GeV}^{-2}, \quad \Lambda = 631 \text{ MeV}, \quad m_q = 5.5 \text{ MeV}$$



## Soft Mode of QCD-CP

= fluctuation of scalar ( $\bar{q}q$ ) channel

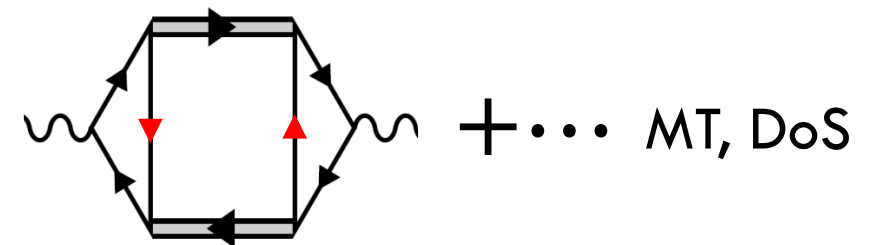
$$D^R(x) = \langle [\bar{\psi}\psi(x), \bar{\psi}\psi(0)] \rangle \theta(t) = \Rightarrow \Rightarrow$$

□ Random Phase Approximation

$$\Rightarrow \Rightarrow = \text{loop} + \text{two-loop} + \dots$$



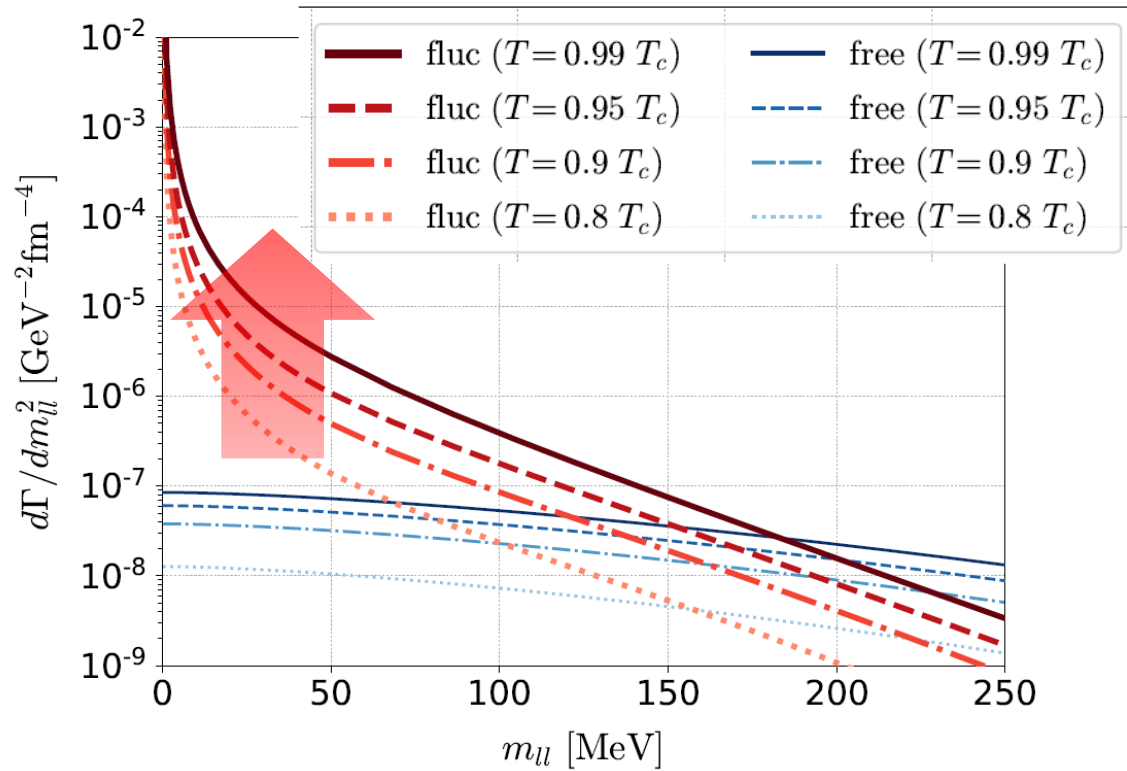
**Modification of dilepton production through**



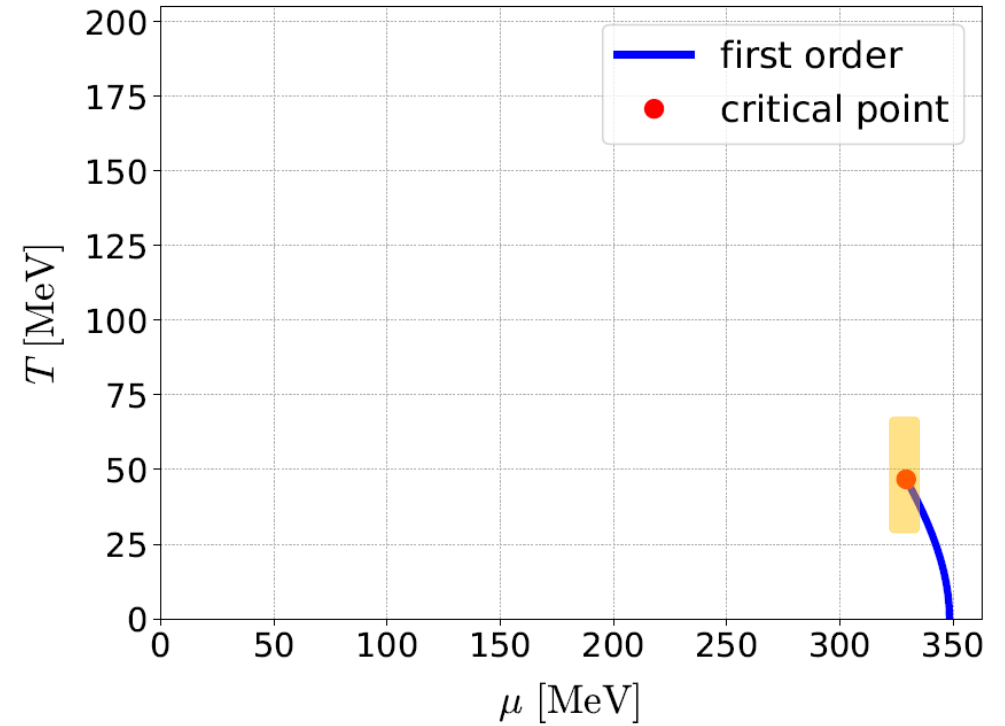
# Dilepton production rate near QCD-CP

Nishimura, MK, Kunihiro ('23)

## Invariant mass spectrum



for fixed chem. pot.:  $\mu = \mu_c$



- Enhancement at low  $M_{\ell\ell}$  region near QCD-CP
- Distinguishment from diquark soft mode may be difficult.

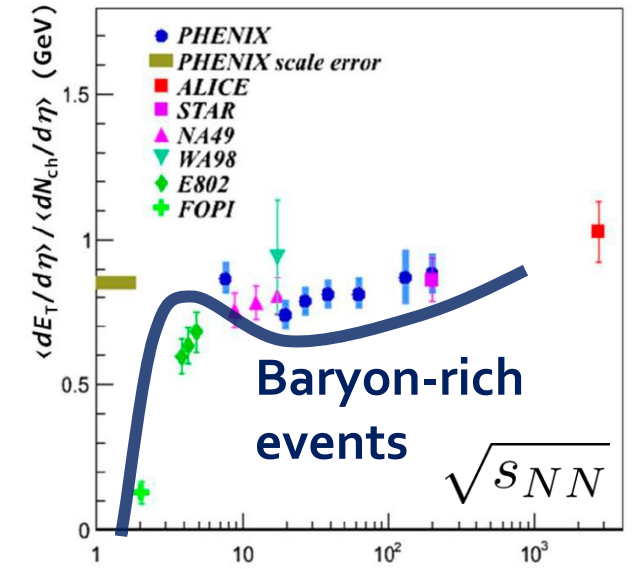
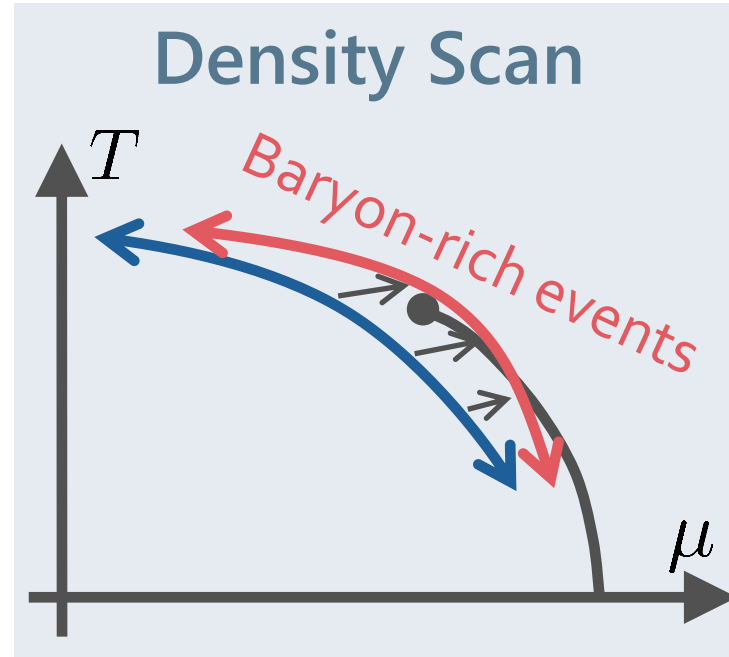
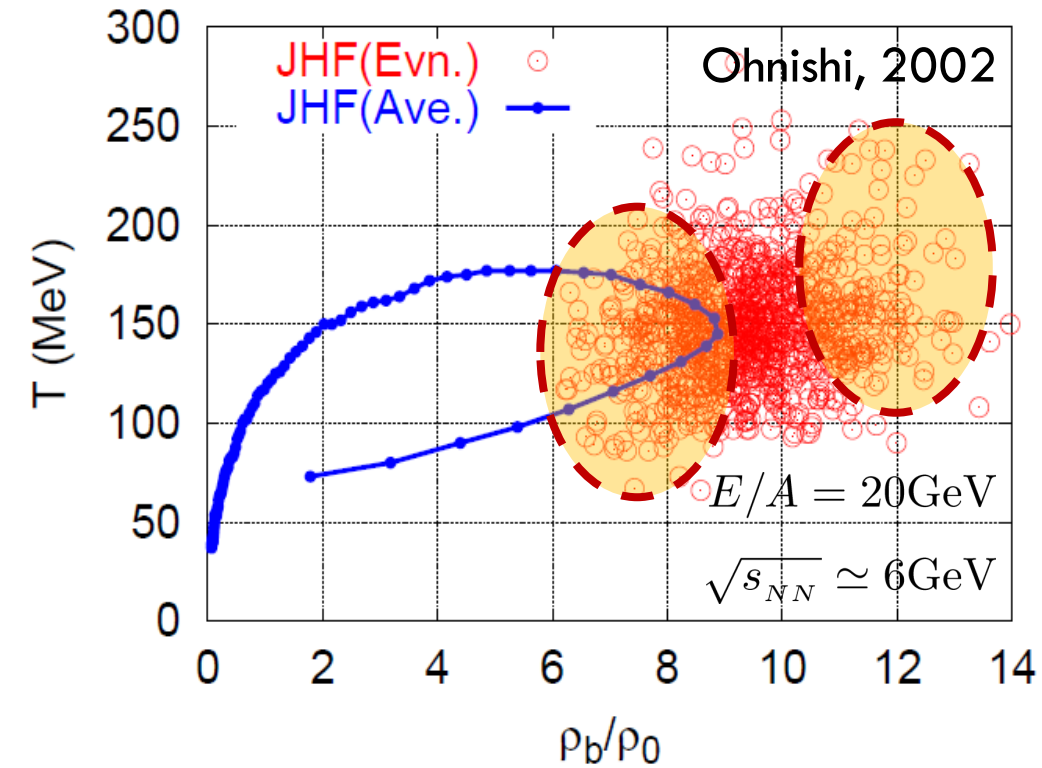


# Event Selection

# Sophisticated Event Selections

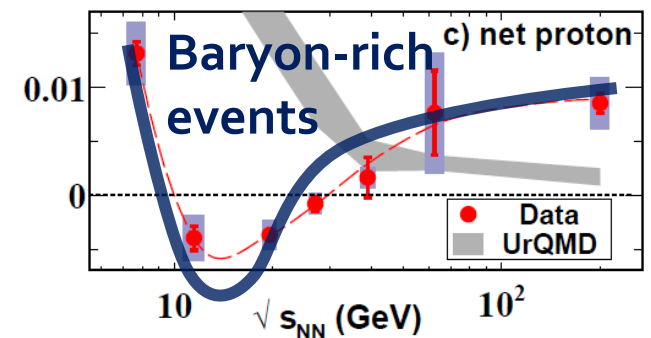
Maximum baryon density has large event-by-event fluctuations

average transverse energy



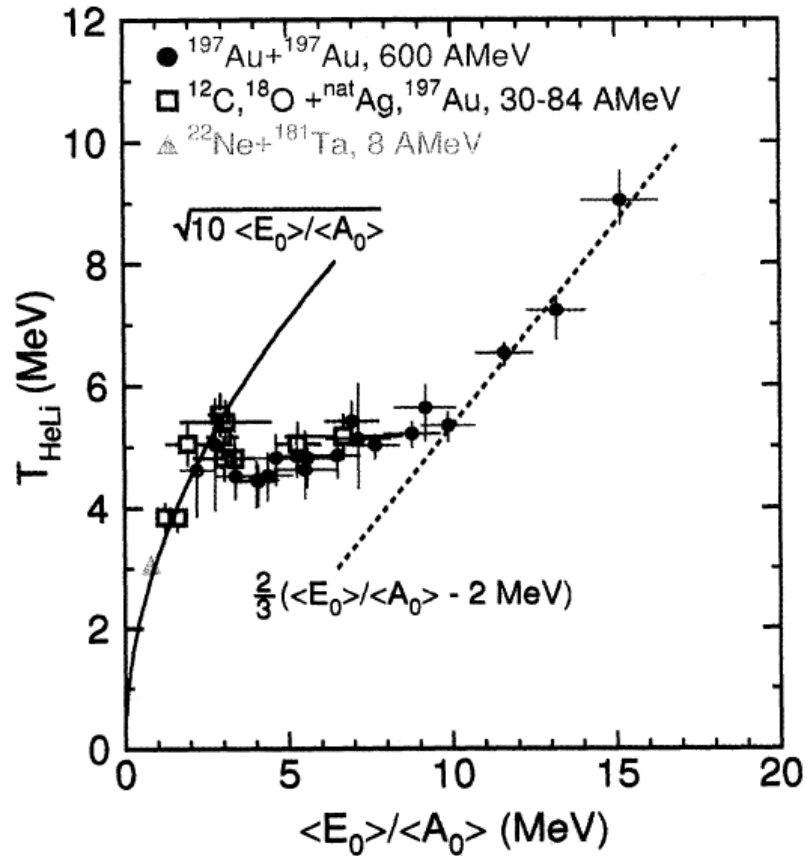
Event selection in terms of maximum baryon density (or, correlation analysis) should be a useful tool.

directed flow



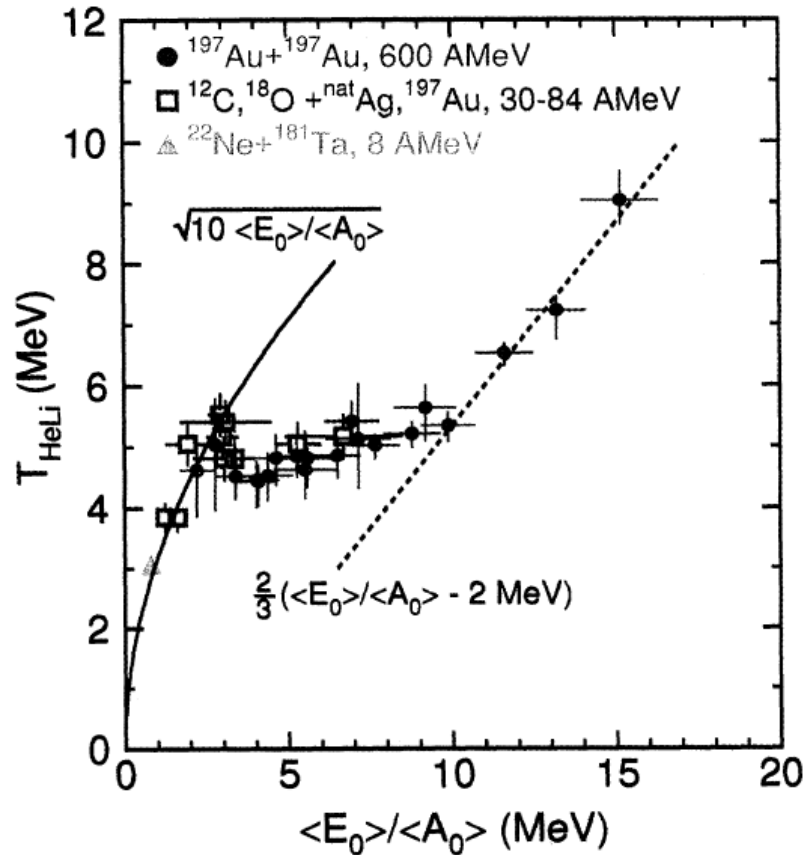
# Nuclear Liquid-Gas Phase Transition

Pochodzalla+, PRL, 75, 1040 ('95)

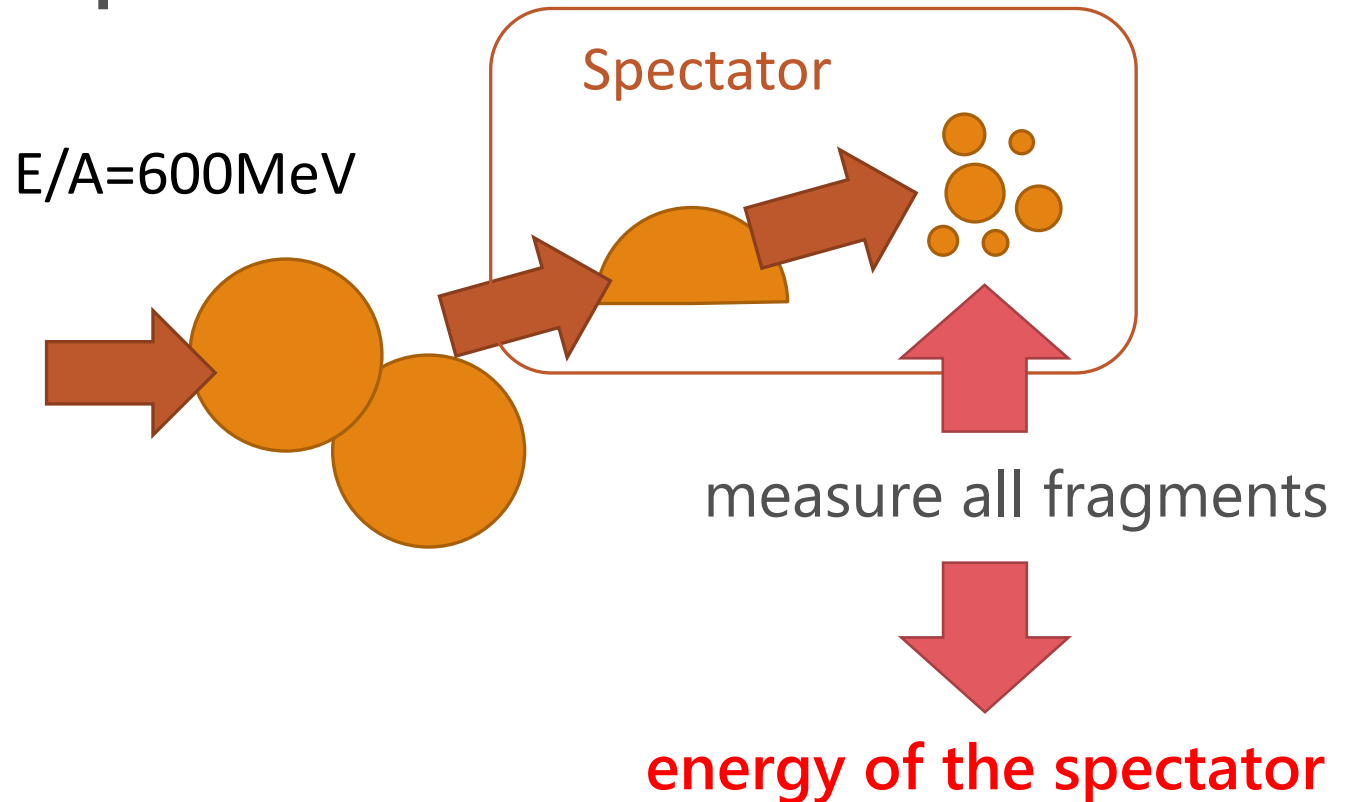


# Nuclear Liquid-Gas Phase Transition

Pochodzalla+, PRL, 75, 1040 ('95)



Experiment:



□ Similar analysis in relativistic HIC requires event-by-event total energy of the fireball.

# Summary

- ❑ Beam-energy scan will reveal phase transitions in dense QCD.
- ❑ J-PARC-HI will play an invaluable role in the future development.
- ❑ Many interesting observables to reveal the QCD phase diagram:
  - ❑ Event-by-event fluctuations of conserved charges
  - ❑ Dilepton production at ultra-low-mass-region
  - ❑ Event selection via baryon/energy density
  - ❑ Light/hyper-nuclei production

# J-PARC-HI Collaboration



and **138** members in total

**Exp.:** J. K. Ahn , K. Aoki, S. Ashikaga, O. Busch, M. Chiu, T. Chujo , P. Cirkovic , T. Csorgo , D. Devetak , G. David, M. Djordjevic, S. Esumi , P. Garg, R. Guernane , T. Gunji , T. Hachiya , H. Hamagaki , S. Hasegawa, B. S. Hong, S. H. Hwang, Y. Ichikawa, T. Ichisawa , K. Imai, M. Inaba, M. Kaneta , H. Kato, B. C. E. J. Kim, X. Luo, Y. Miake , J. Milosevic, D. Mishra, Y. Morino, L. Nadjdjerdj , S. Nagamiya , T. Nakamura, M. Naruki , K. Nishio , T. Nonaka, M. Ogino, K. Oyama , K. Ozawa, T. R. Saito, A. Sakaguchi , T. Sakaguchi , S. Sakai, H. Sako, K. Sato, S. Sato, S. Sawada, K. Shigaki , S. Shimansky , M. Shimomura, M. Stojanovic , H. Sugimura, Y. Takeuchi, H. Tamura, K. H. Tanaka, Y. Tanaka, K. Tanida, N. Xu, S. Yokkaichi, I. K. Yoo

**Theor.:** Y. Akamatsu, M. Asakawa, K. Fukushima, H. Fujii , T. Hatsuda , M. Harada, T. Hirano, K. Itakura M. Kitazawa , T. Maruyama , K. Morita, K. Murase A. Nakamura, Y. Nara, C. Nonaka, A. Ohnishi, M. Oka

**Acc.:** E. Chishiro , H. Harada, Y. Hashimoto, N. Hayashi, K. Hirano, H. Hotchi , K. Ishii, T. Ito, M. Kinsho , R. Kitamura, A. Kovalenko, J. Kamiya , N. Kikuzawa , T. Kimura, Y. Kondo, H. Kuboki , Y. Kurimoto, Y. Liu S. Meigo , A. Miura, T. Miyao , T. Morishita , Y. Morita, K. Moriya, R. Muto, T. Nakanoya , K. Niki, H. Oguri , C. Ohmori , A. Okabe, M. Okamura, P. K. Saha , K. Sato, Y. Sato, T. Shibata, T. Shimokawa , K. Shindo , S. Shinozaki, M. Shirakata , Y. Shobuda , K. Suganuma , Y. Sugiyama, H. Takahashi, T. Takayanagi , F. Tamura, J. Tamura, N. Tani , M. Tomisawa , T. Toyama, Y. Watanabe, K. Yamamoto, M. Yamamoto, M. Yoshii, M. Yoshimoto

J-PARC-HI

# Future Plan

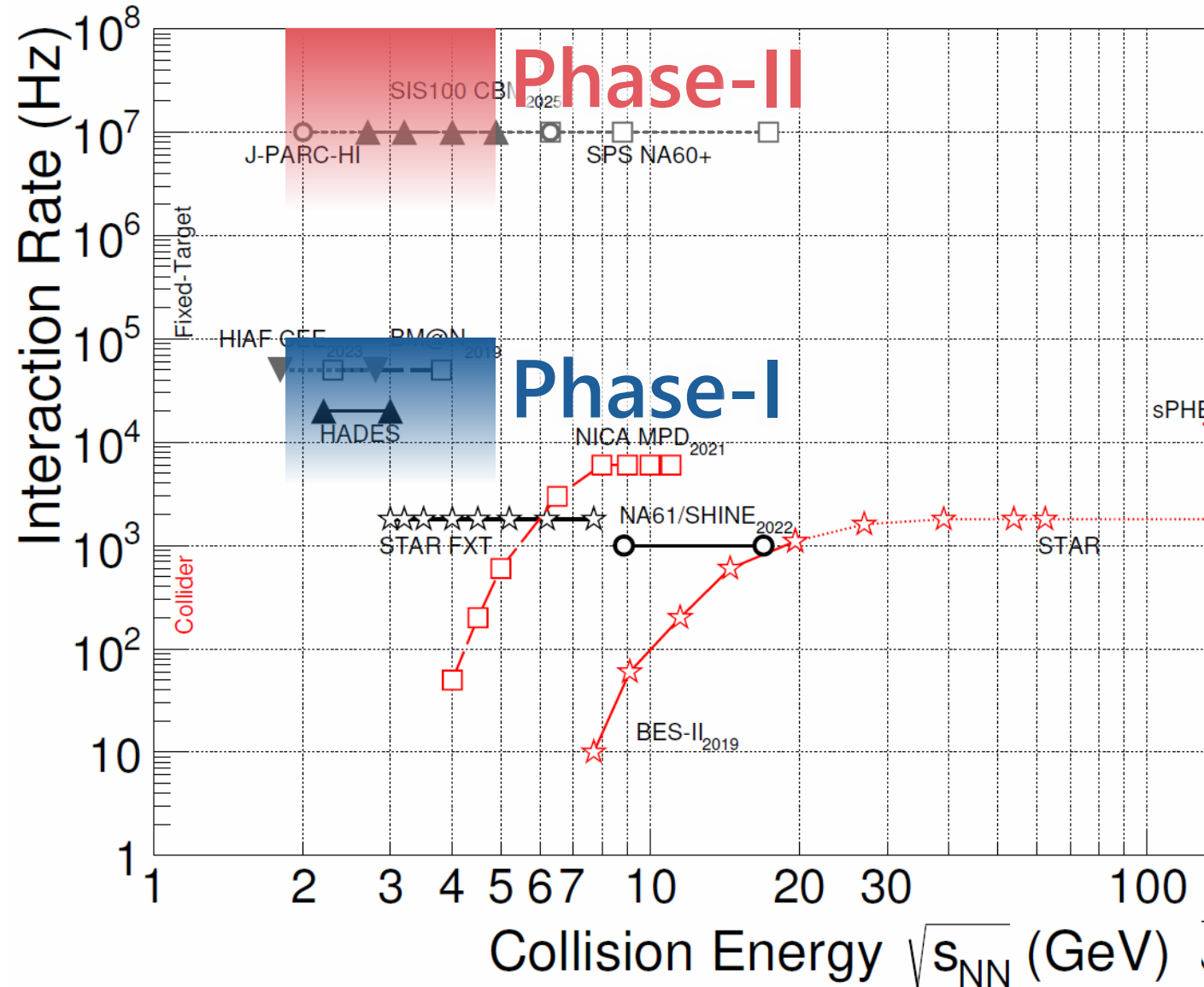
# J-PARC-HI Staging Plan

## Phase-I

- KEK-BS booster
- E16+ $\alpha$  spectrometer

## Phase-II

- NEW HI booster
- NEW spectrometer



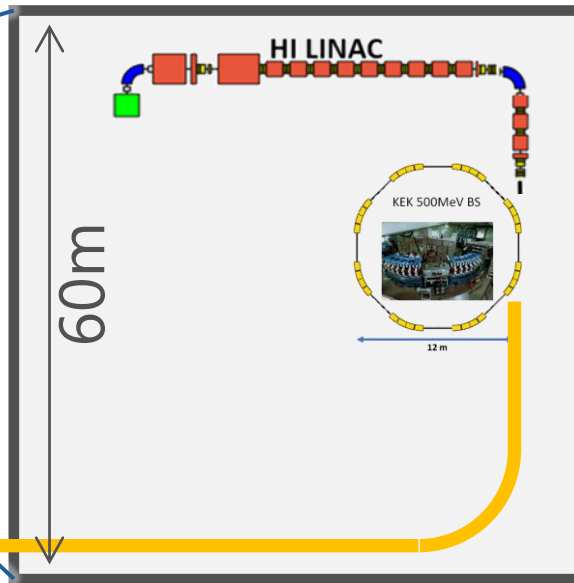




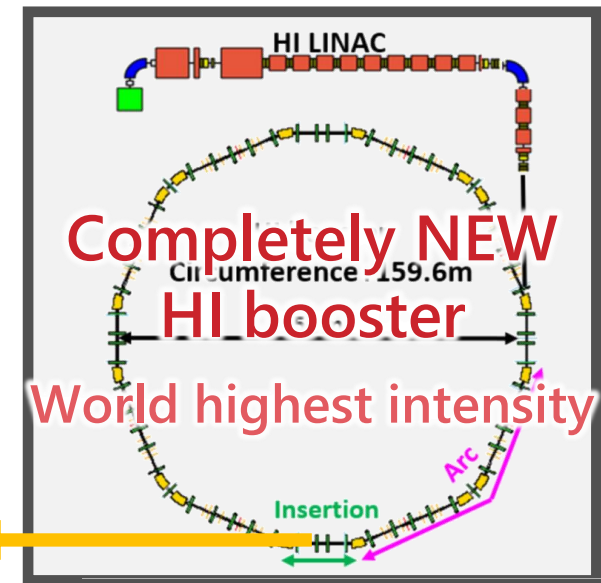
# Staging of HI Booster



## Phase-I



## Phase-II



Interaction rate

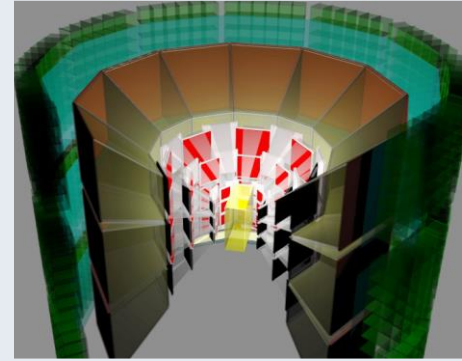
$$\sim 10^5 \text{ Hz}$$

$$\sim 10^8 \text{ Hz}$$

# Detector Phase-I

## E16 Spectrometer

- $\phi \rightarrow e^+e^-$ ,  $\phi \rightarrow K^+K^-$
- In-medium mass modification
- Pilot data taking in June

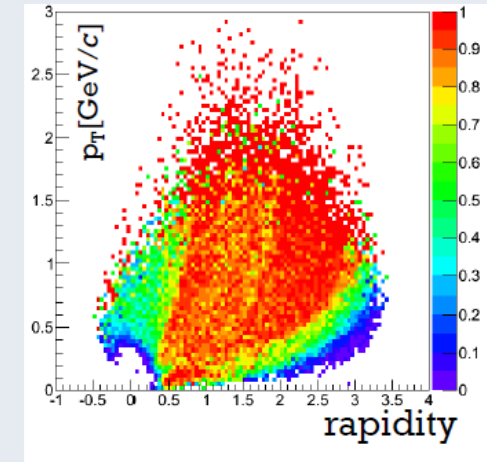
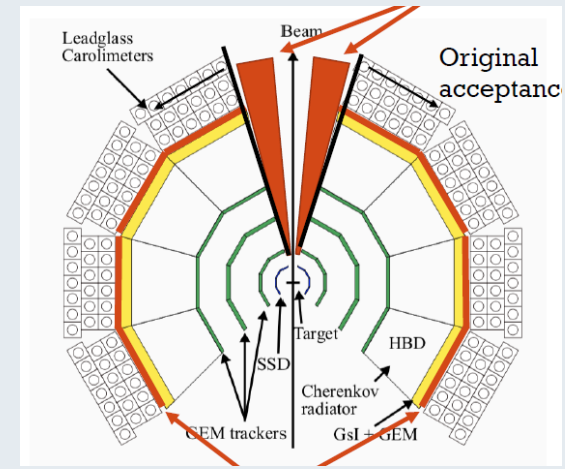


**UPGRADE**

## E16+ $\alpha$

Upgrade forward region for high-multiplicity counting

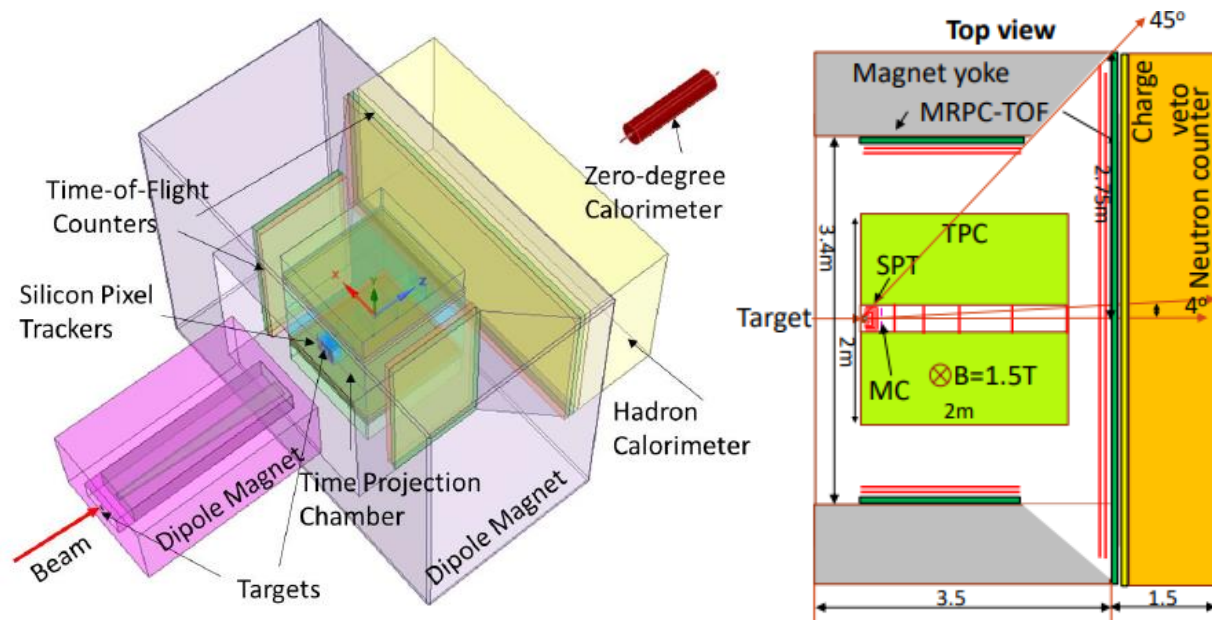
➤ Hadron/lepton measurement at wide acceptance



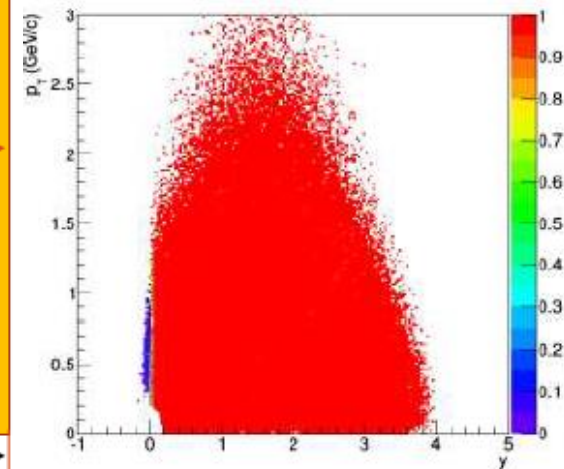
# Detector **Phase-II**

- $4\pi$  acceptance, high-intensity beam
  - Precise measurement of fluctuations, dileptons
  - Detailed design are under discussion

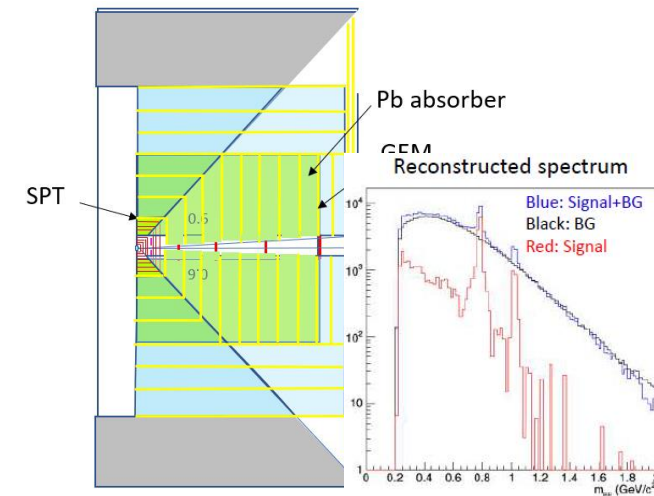
## Hadron calorimeter + hyper-nuclear measurement



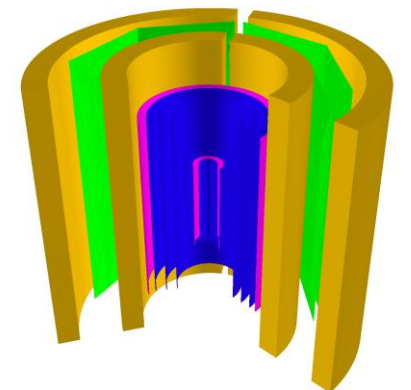
acceptance



## Dimuon Setup

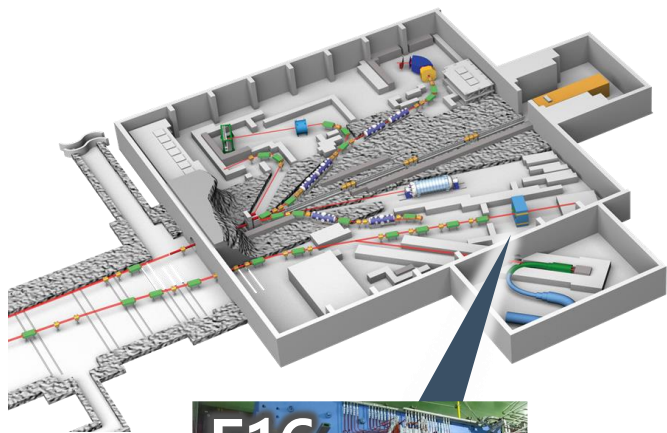


## ALICE3-like dipole

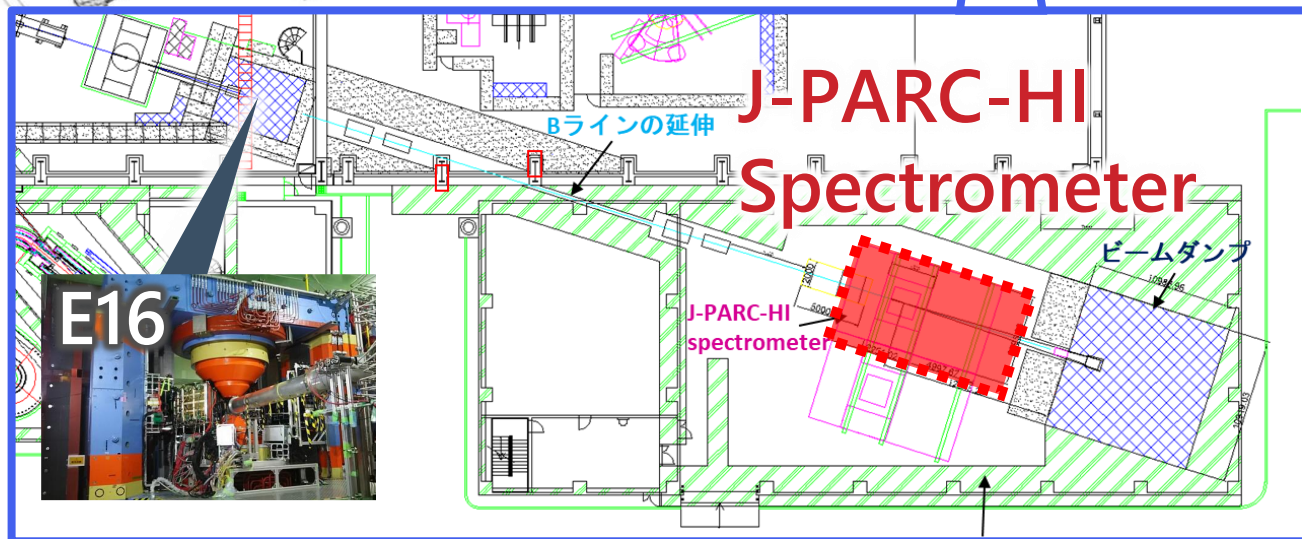
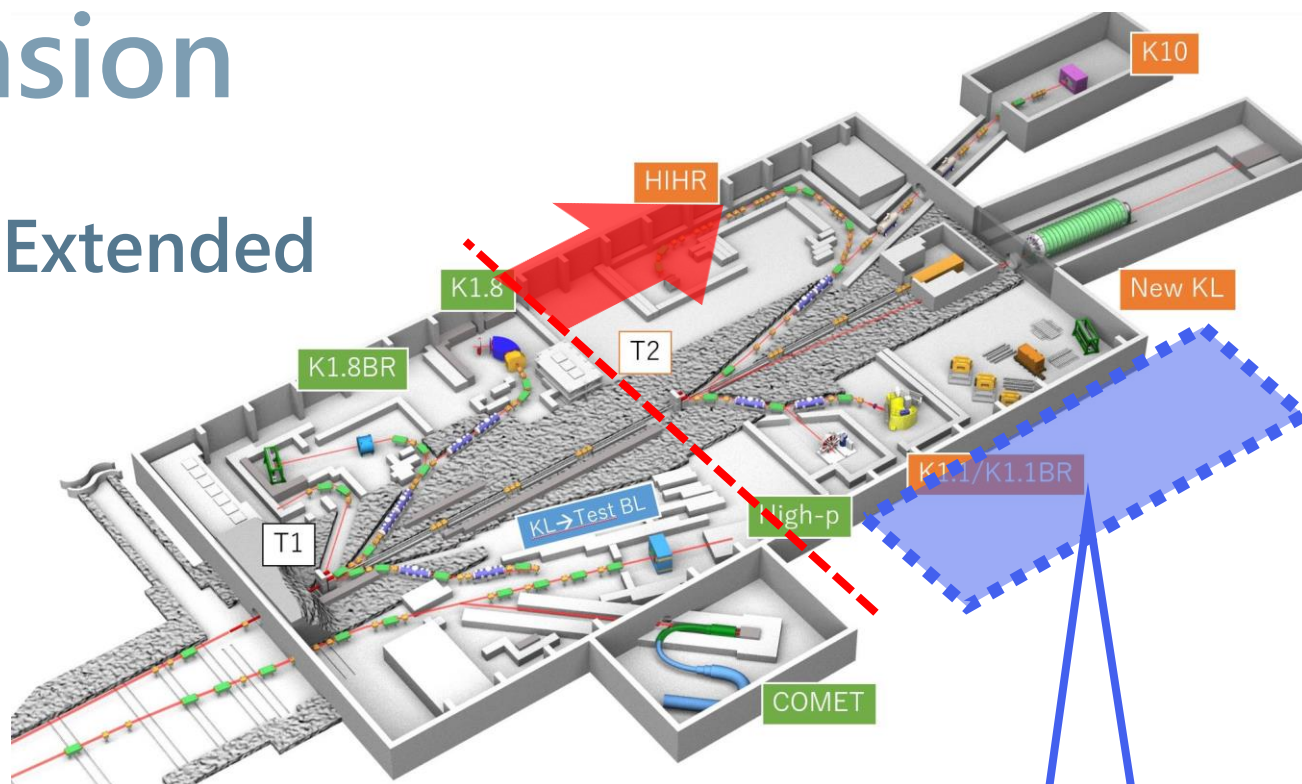


# Hadron Hall Extension

Present



Extended



- Top priority at KEK-PIP2022
- J-PARC-HI spectrometer will be installed in an annex