

Evolution of Dense Matter and Experimental Signals in Heavy-Ion Collisions

Masakiyo Kitazawa

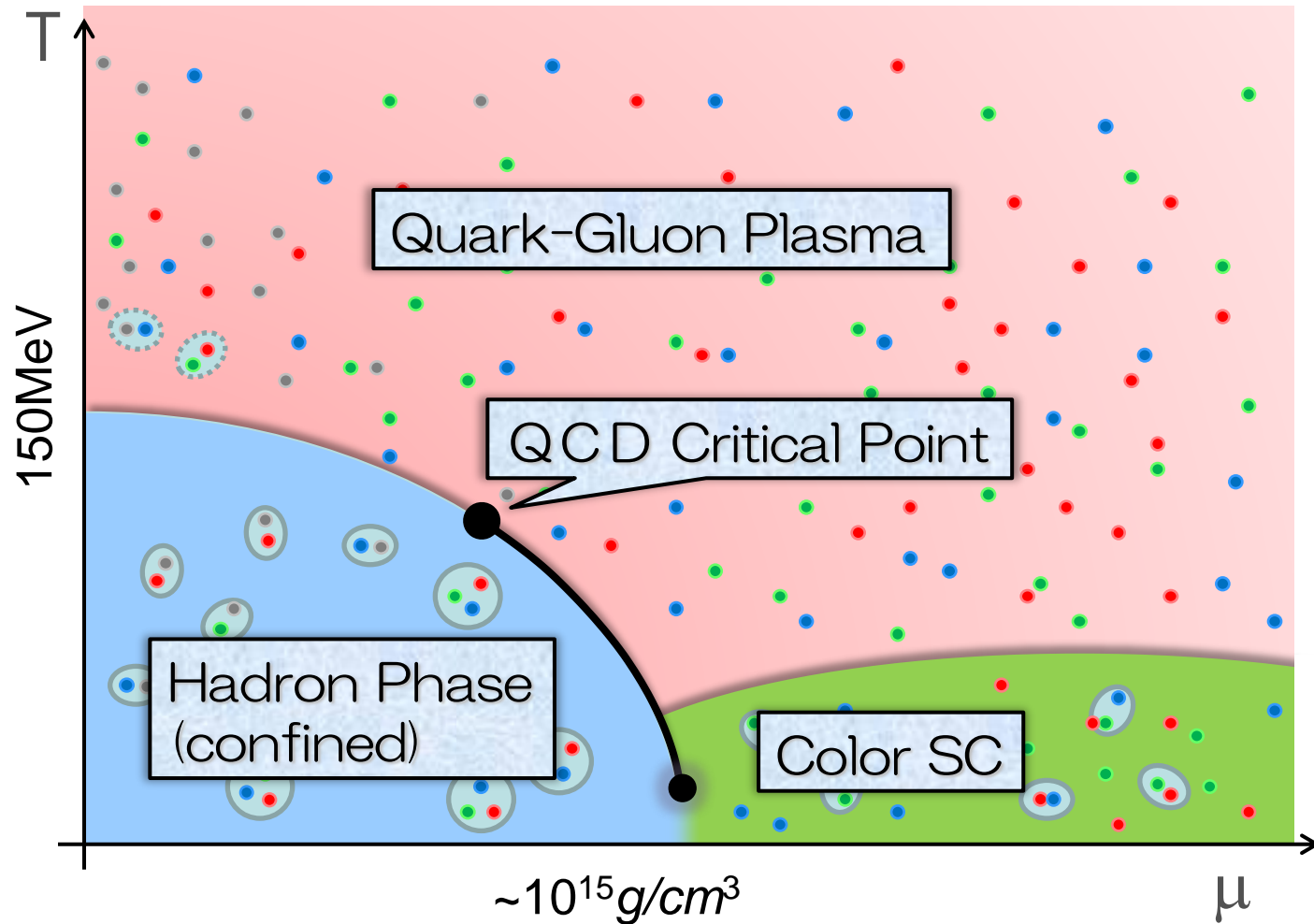
北澤正清

(YITP, Kyoto)

Taya, Jinno, MK, Nara, 2409.07685.

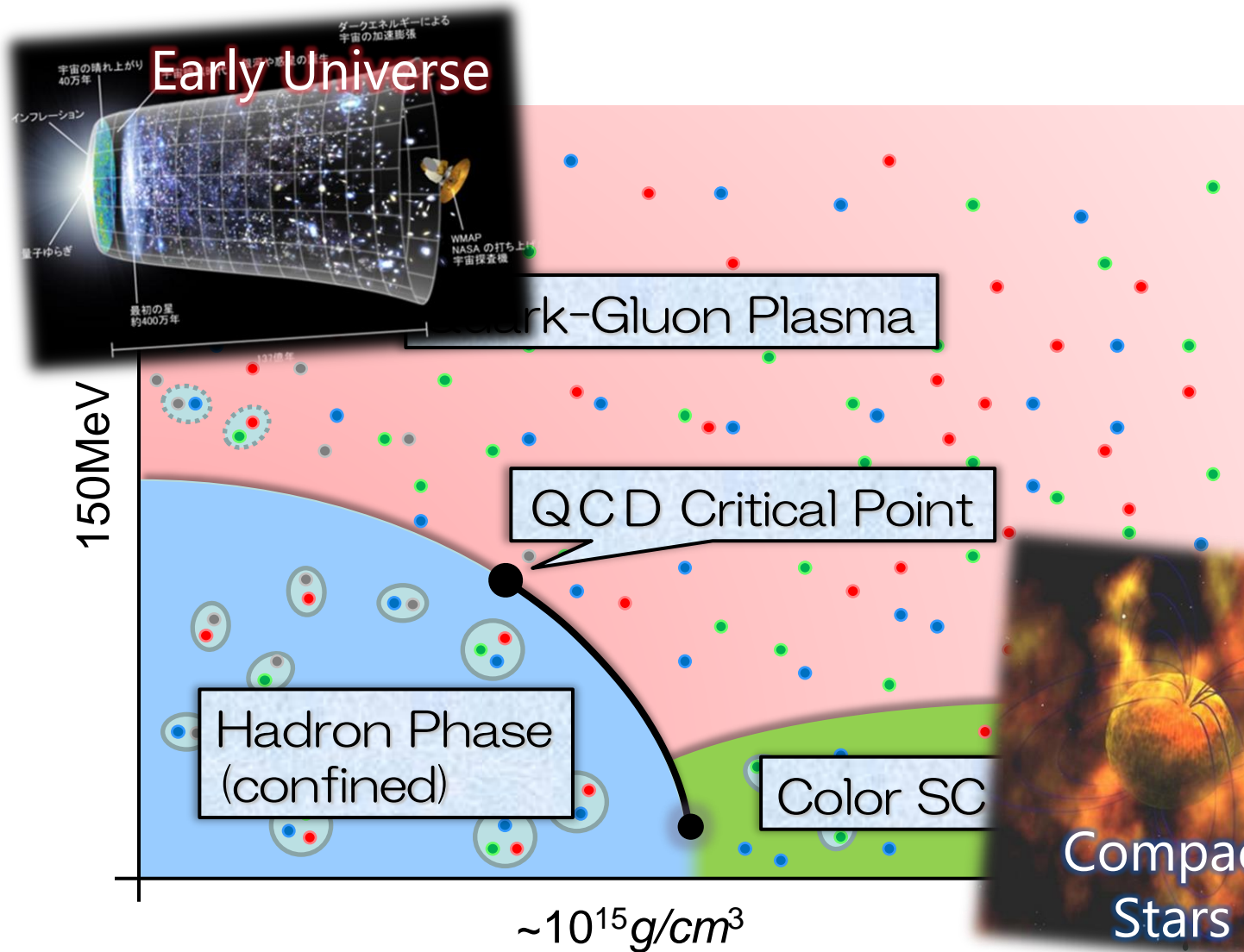
Nishimura, MK, Kunihiro, Ann. Phys. **469**, 169768; PTEP **2023**, 053D01; PTEP **2022**, 093D02.

QCD Phase Diagram



- Crossover at $\mu = 0$
- Possible first-order transition and QCD critical point in dense region
- Multiple QCD-CP? [MK+ \('02\)](#)
- Color superconducting phases in dense and cold quark matter

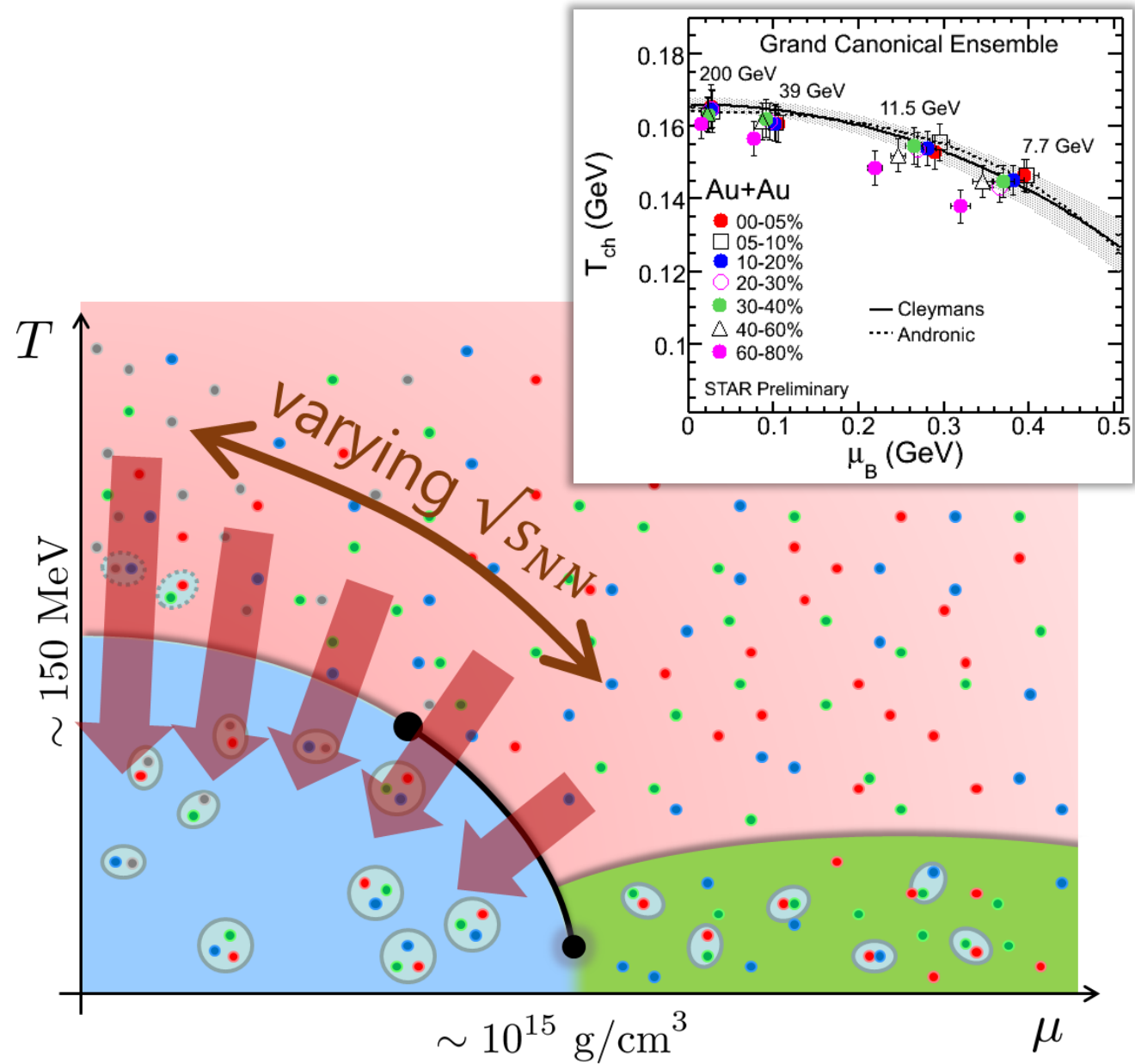
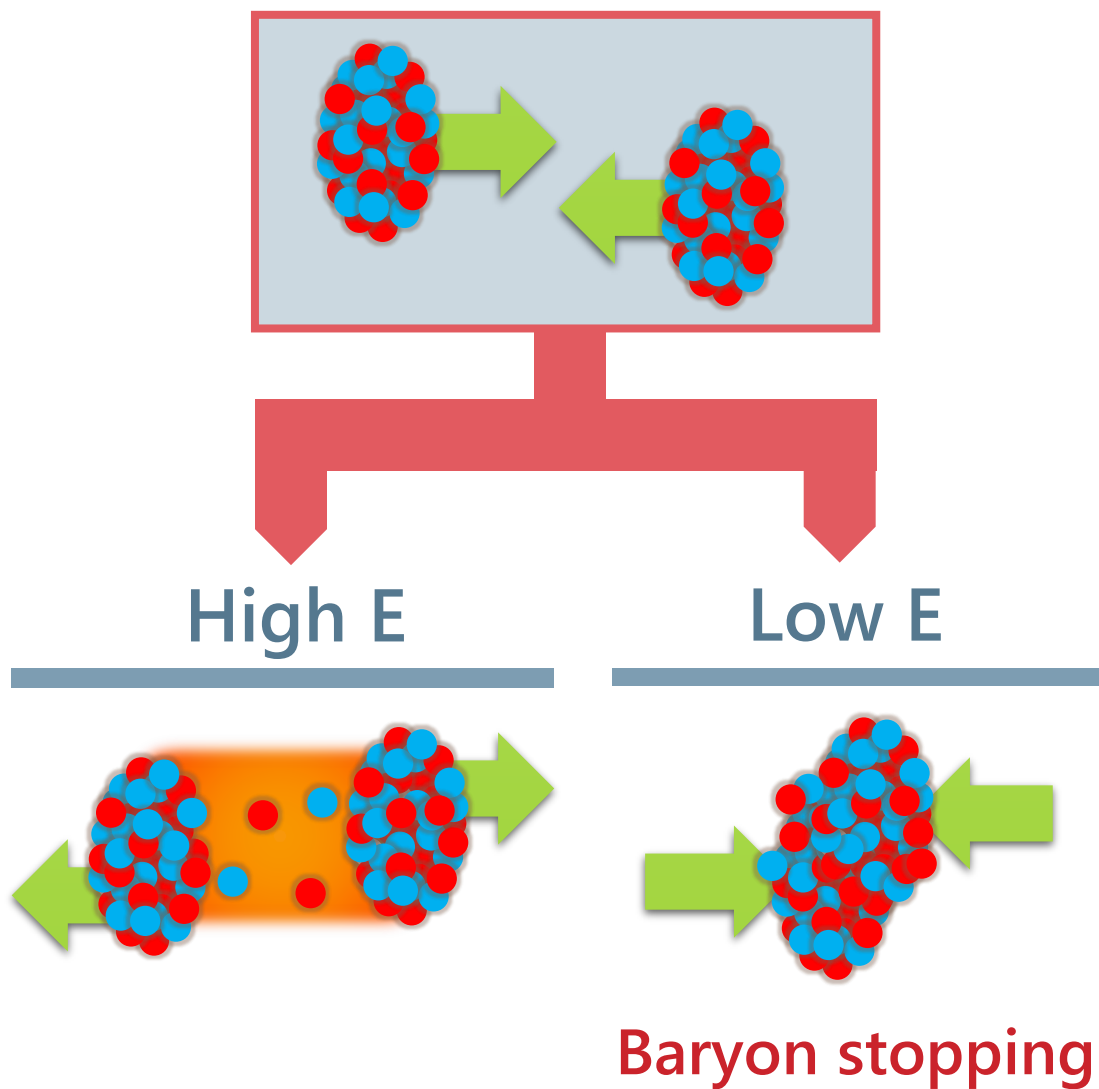
QCD Phase Diagram



- ❑ Crossover at $\mu = 0$
- ❑ Possible first-order transition and QCD critical point in dense region
- ❑ Multiple QCD-CP? MK+ ('02)
- ❑ Color superconducting phases in dense and cold quark matter

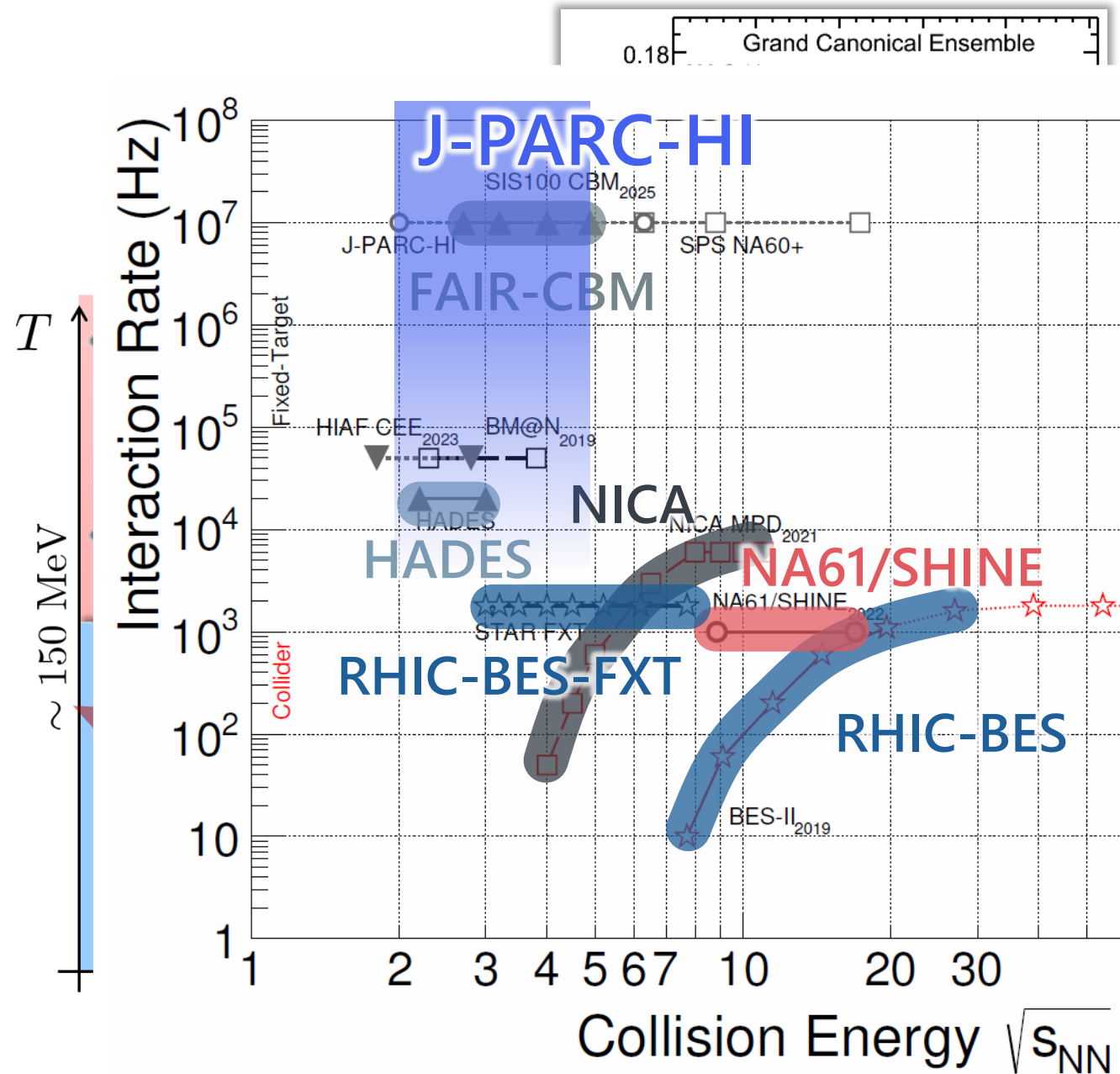
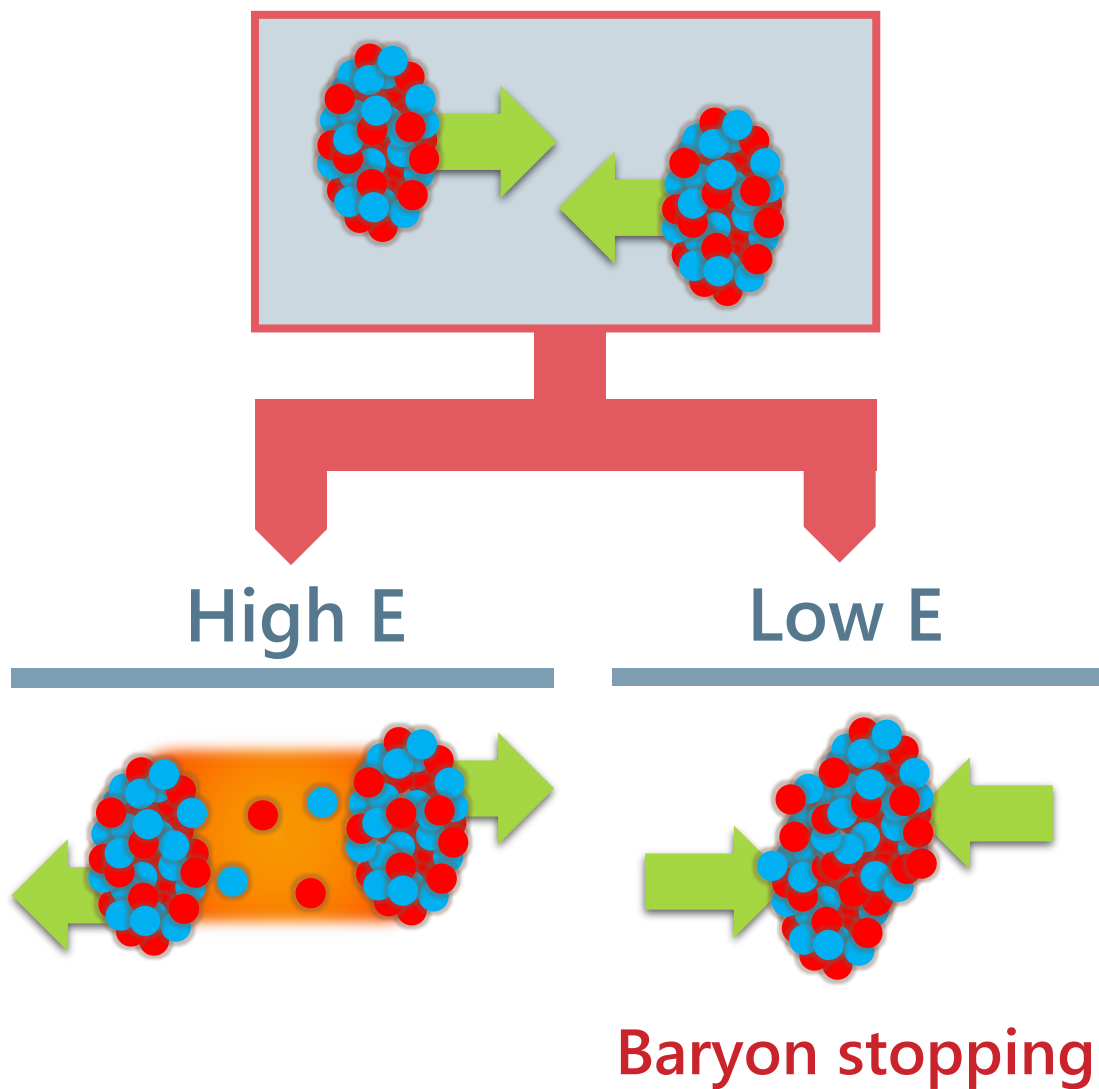
Beam-Energy Scan

STAR, 2012



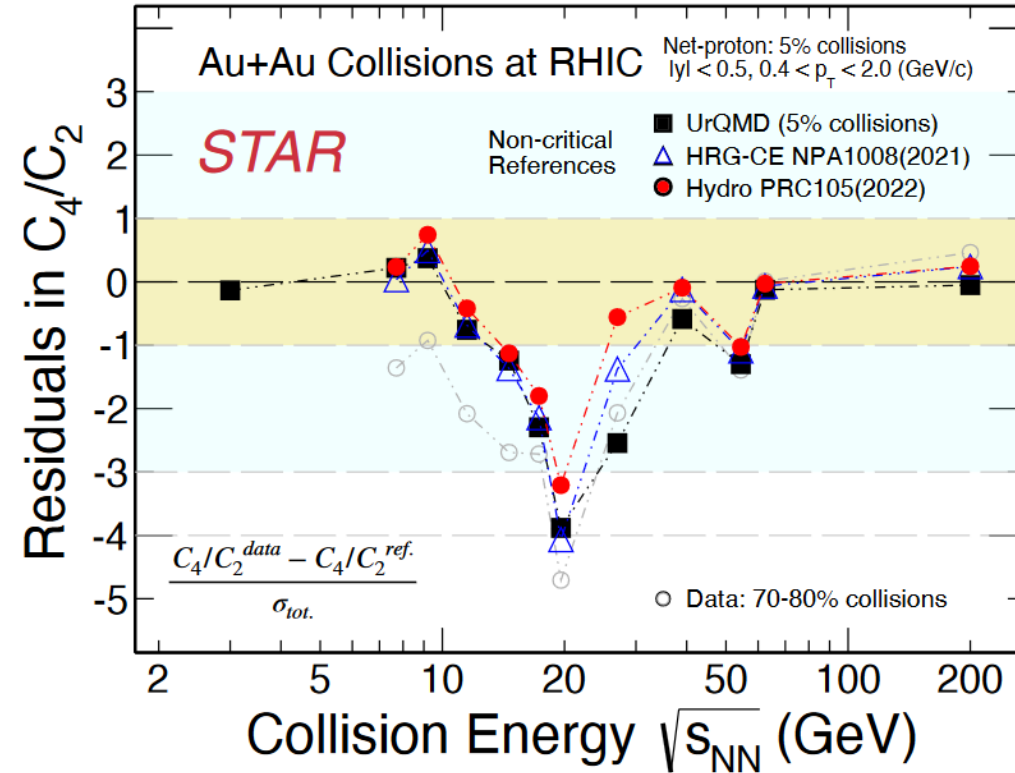
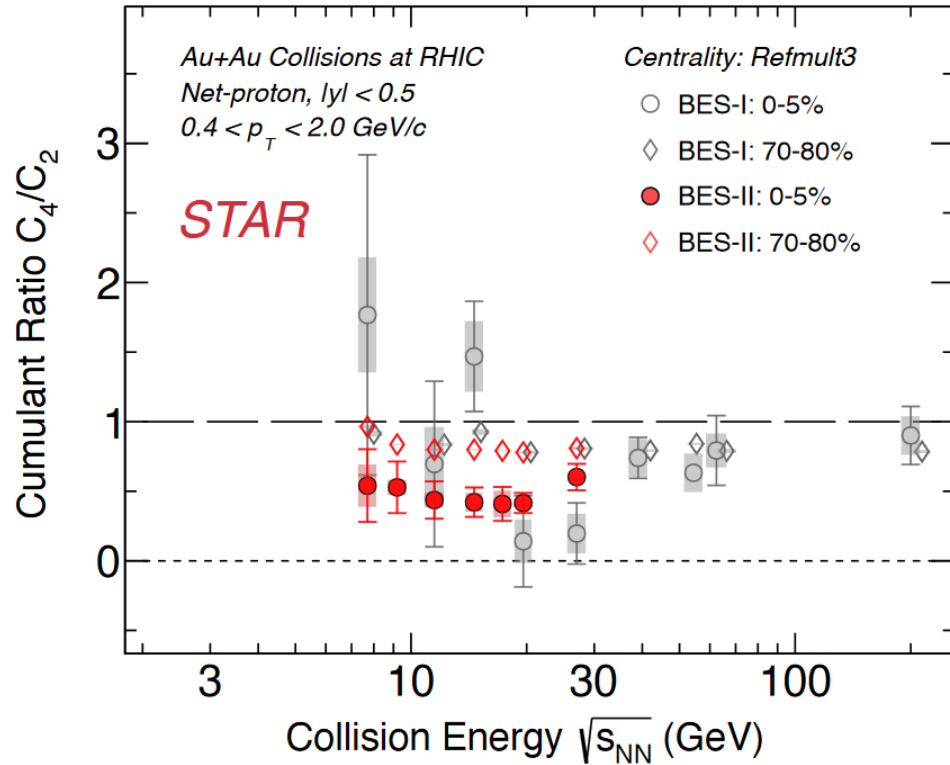
Beam-Energy Scan

STAR, 2012



Kurtosis of Net-proton Number

A. Pandav, CPOD2024

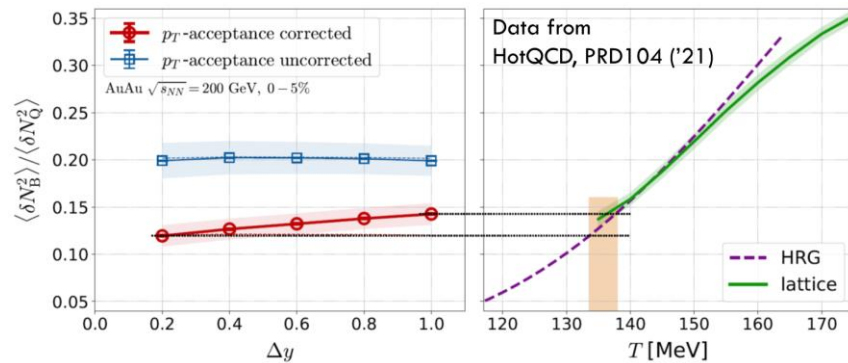


MK's Comments

1

Reconstruct baryon number cumulants.
Correct momentum acceptance dependence.

MK, Asakawa, '12; '12
MK, Esumi, Nonaka, '22

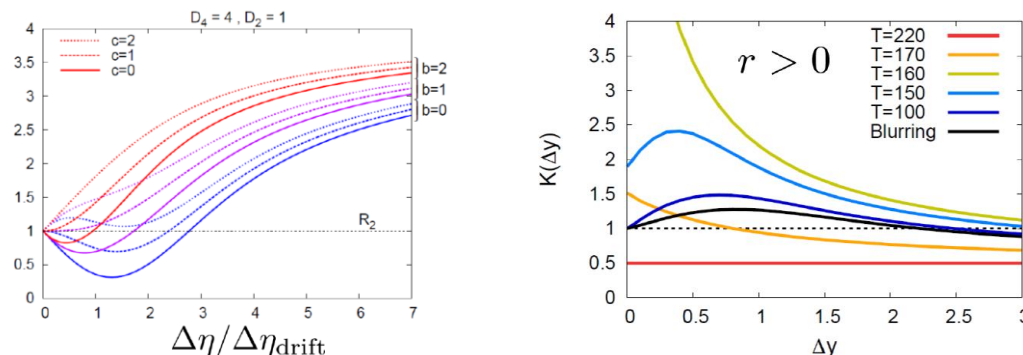


Partial measurement
blurs the signal!

2

Experimental results
 \neq thermal fluctuations at chemical freezeout

MK, Asakawa, Ono, '14
Sakaida, Asakawa, MK, '14
MK, '15
Sakaida, Asakawa, Fujii, MK, '17



Effect of diffusion will be crucial.
Investigate rapidity-window dep.

Contents

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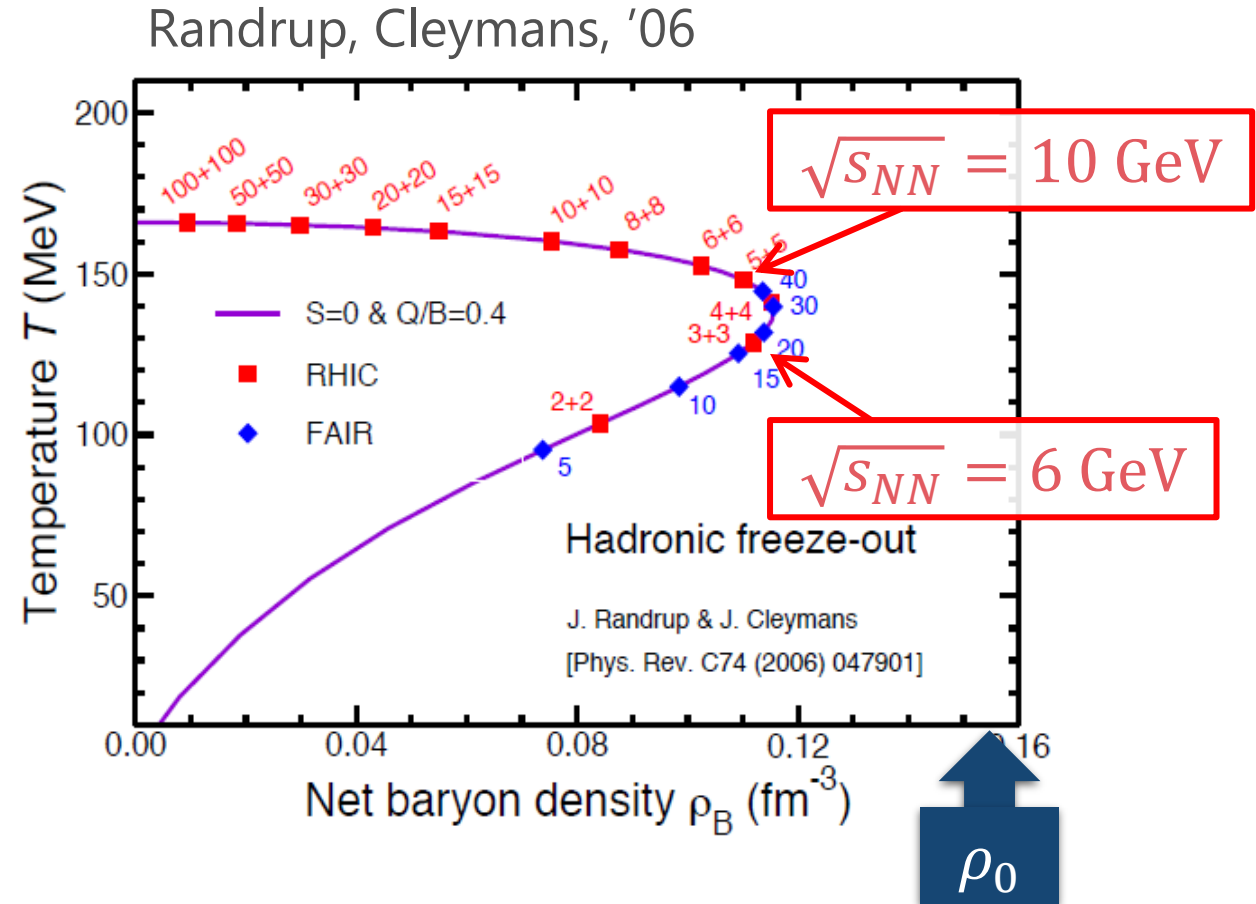
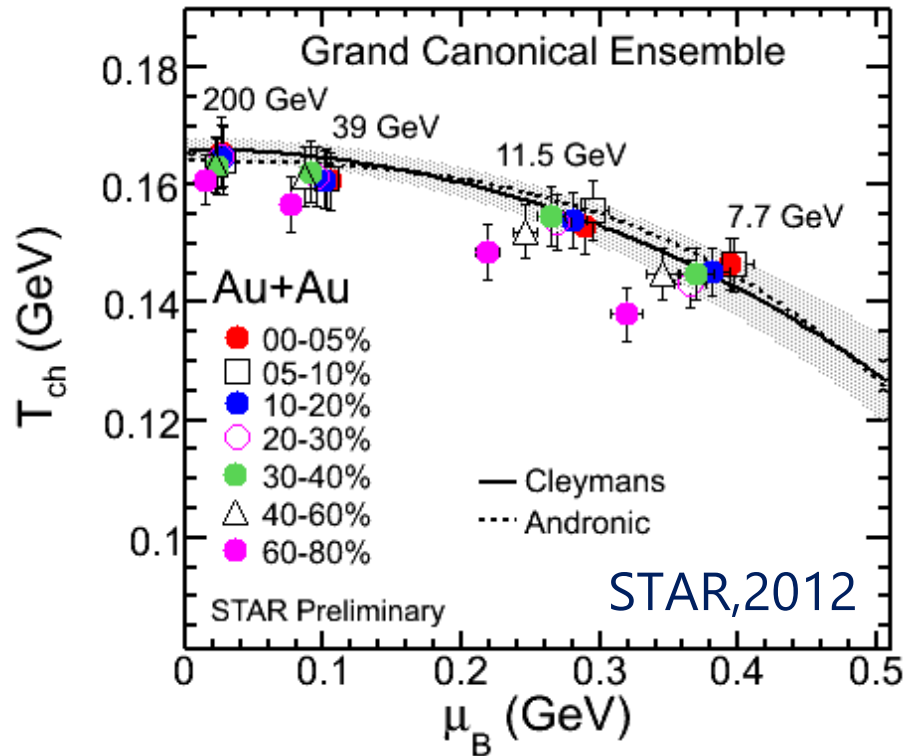
Key Questions

- What is **the optimal collision energy** to explore the baryon-rich matter?
- **How high density** are accessible?

Our Answer

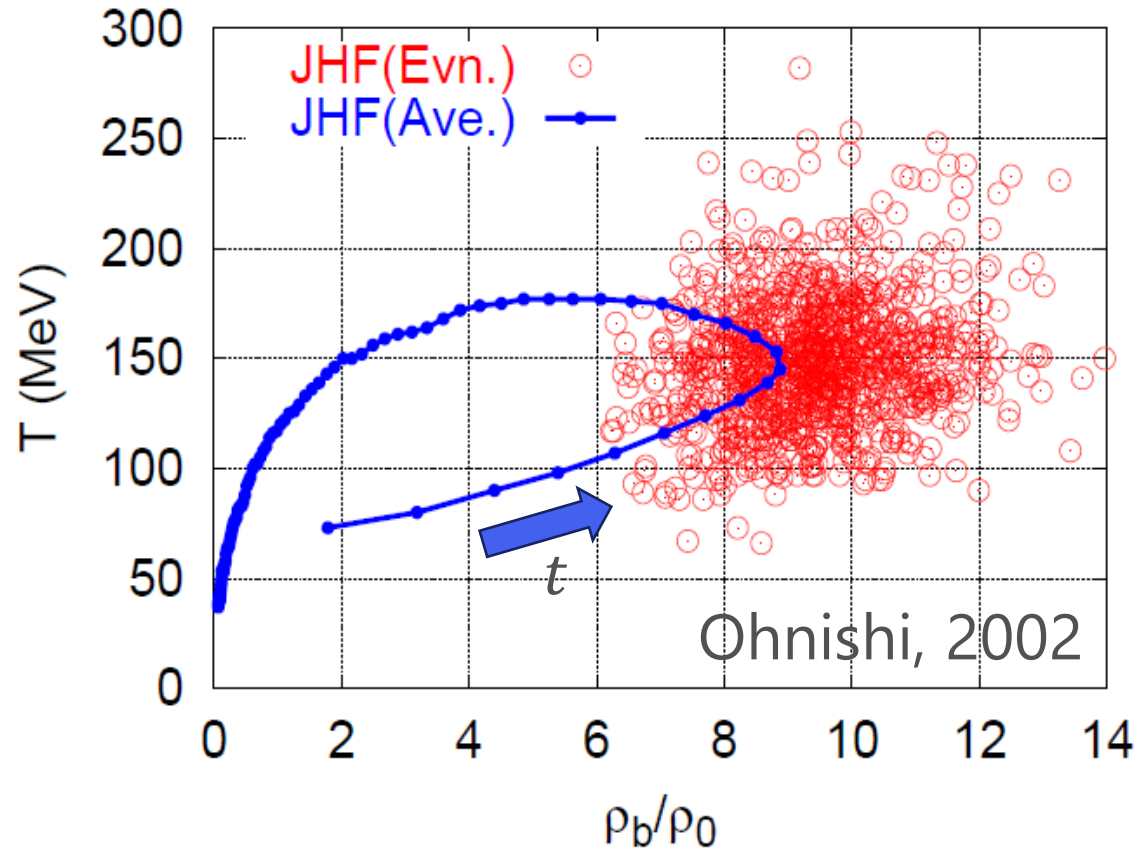
- $\sqrt{s_{NN}} = 3 \text{ GeV}$ is enough to study $\rho = 3\rho_0$.
- $\rho/\rho_0 = 4\sim 5$ may be accessible with $\sqrt{s_{NN}} = 3\sim 6 \text{ GeV}$.

Chemical Freezeout



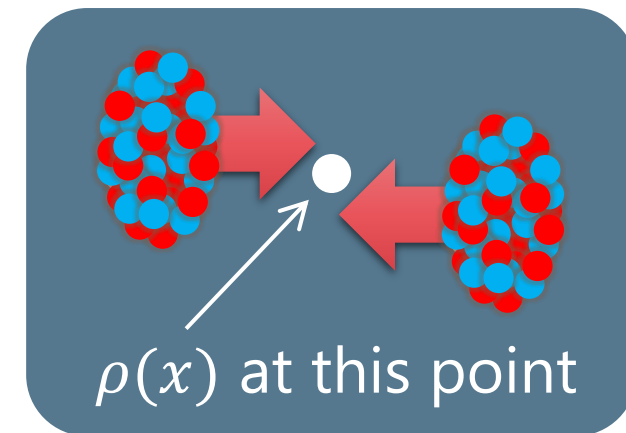
- Highest baryon density **at chemical freezeout** at $\sqrt{s_{NN}} \simeq 6 - 10 \text{ GeV}$?
- Not the highest density at the early stage.
- Density at earlier stage? Analysis in dynamical models

Baryon Density at Collision Point



Simulation by JAM

$$E/A = 20\text{GeV}, \quad \sqrt{s_{NN}} \simeq 6\text{GeV}$$



- Maximum baryon density exceeds $\rho/\rho_0 \simeq 8$!
- Large event-by-event fluctuations
- How large is the high-density region? How long is the lifetime?

Volume of Dense Region

Volume where the local baryon density is larger than a threshold value ρ_{th}

$$V_3(\rho_{\text{th}}, t) = \int_{\rho(x) > \rho_{\text{th}}} d^3 \mathbf{x} \gamma$$

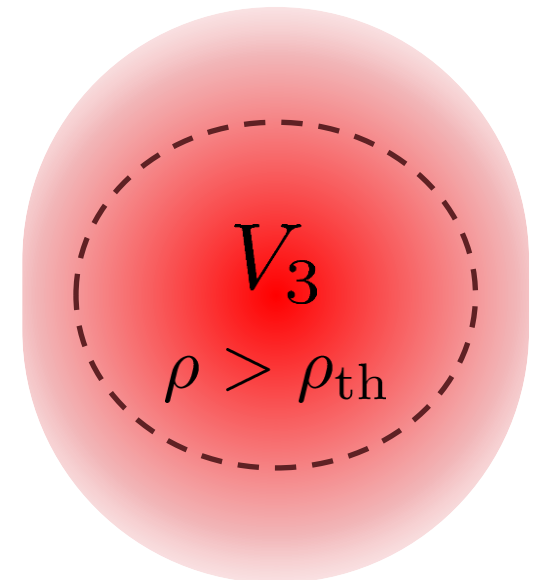
Baryon current $J^\mu(x)$

Baryon density $\rho(x) = \sqrt{J^\mu(x) J_\mu(x)}$

Lorentz factor $\gamma = (1 - (\mathbf{J}/J_0)^2)^{-1/2}$

Note:

- Event-by-event basis / no event average
- Directly calculable in a dynamical model
- We do not care about local thermalization.
 - V_3 is the upper limit of thermalized volume.
 - Even non-thermal, dense region is interesting!



Simulation Setup in JAM

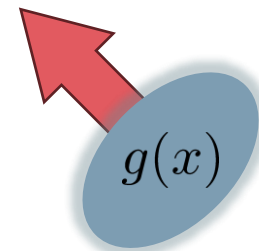
- Au+Au collision for $2.4 \leq \sqrt{s_{NN}} \leq 20$ GeV
- Impact parameter $b \leq 3$ fm : top 5% centrality
- Momentum-dependent mean field (MF2) Nara, Ohnishi, 2022
 - Setup reproducing $\sqrt{s_{NN}}$ dep. of $dv_1/d\eta$ and v_2

Smeared baryon current

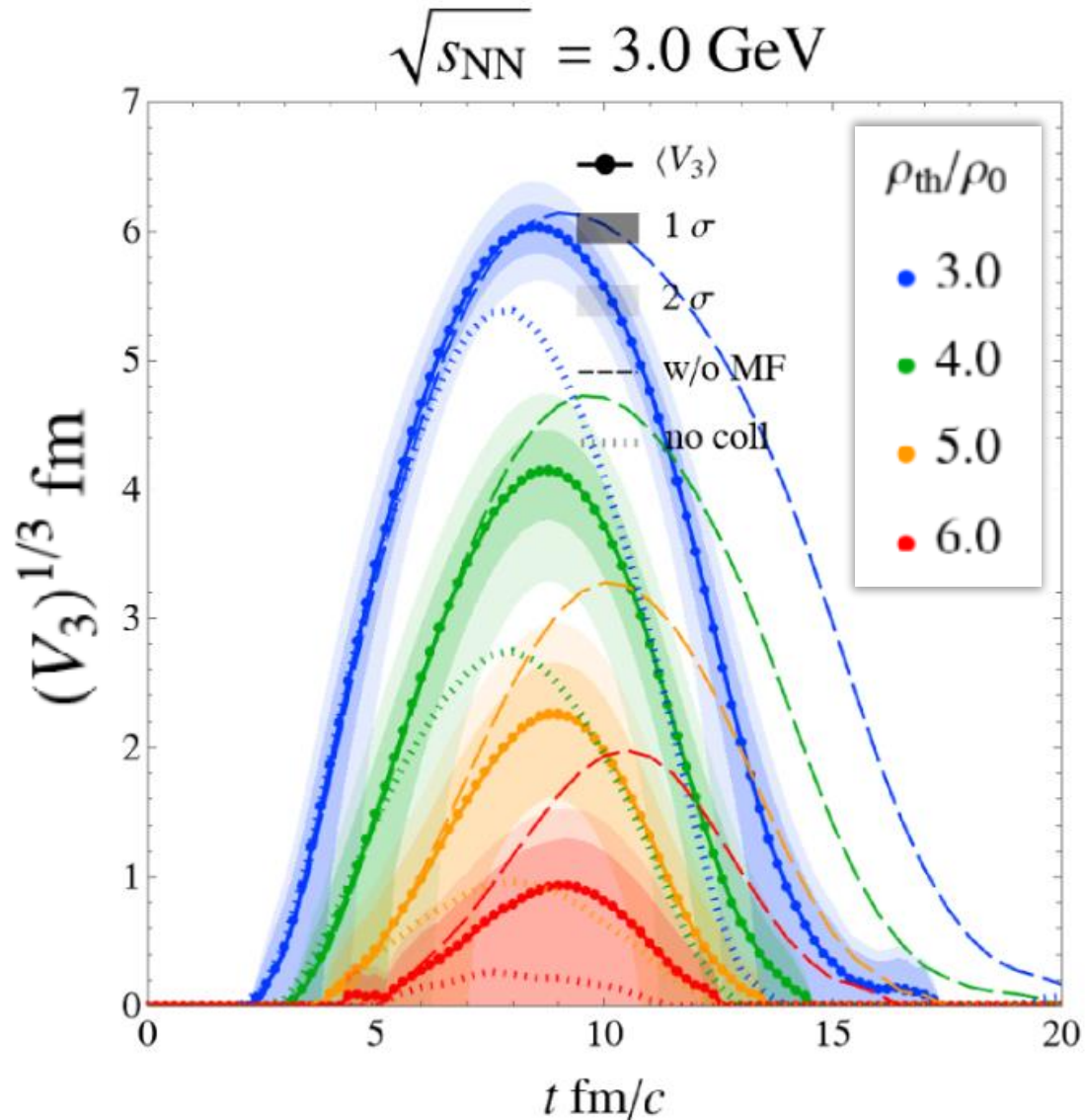
discrete particle distribution \rightarrow continuous current by smearing

$$J^\mu(x) = \sum_{i \in \text{baryons}} B_i g(x; X_i, P_i) \frac{P_i^\mu}{P_i^0}$$

$$g(x; X, P) := \frac{\gamma}{(\sqrt{2\pi}r)^3} e^{-\frac{|\mathbf{x}-\mathbf{X}|^2 + (\gamma\mathbf{V} \cdot (\mathbf{x}-\mathbf{X}))^2}{2r^2}} \quad r = 1 \text{ fm}$$



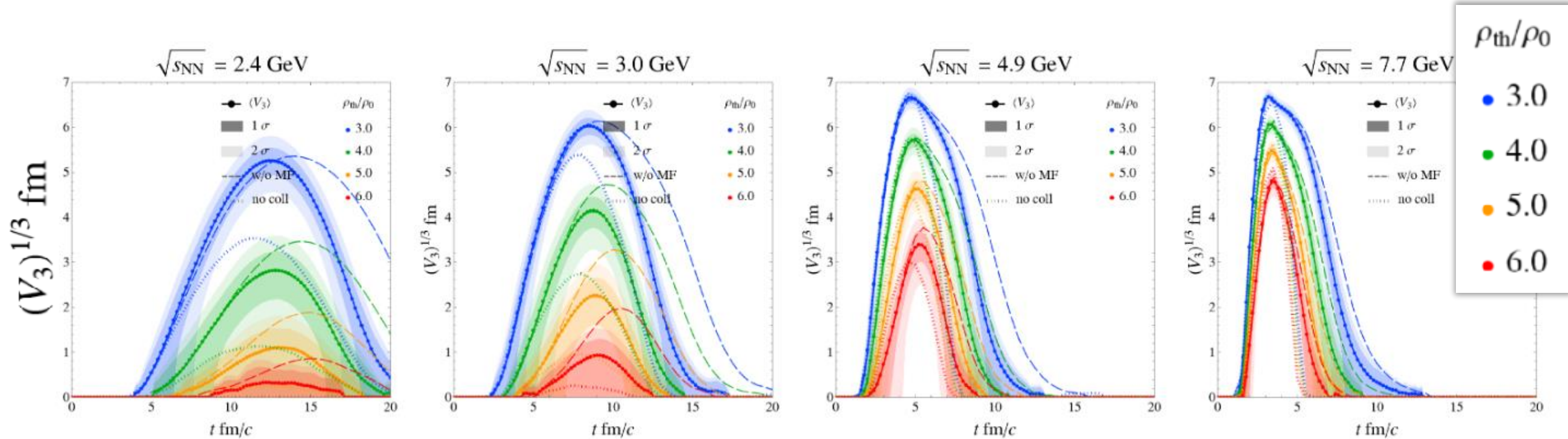
V_3 in JAM



- solid: JAM+MF Nara, Ohnishi, 2022
- shaded band: 1σ and 2σ e-v-e fluct.
- dashed: JAM cascade mode
- dotted: no-collision

- Formation of dense region:
 - $V_3(3\rho_0, t) = (6 \text{ fm})^3$
 - $V_3(4\rho_0, t) = (4 \text{ fm})^3$
- Large e-v-e fluctuations
 - separable by event selection?
- Repulsive MF → weaker compression
- Compression owing to interaction

V_3 for various $\sqrt{s_{NN}}$



As $\sqrt{s_{NN}}$ becomes larger,

- $\max V_3(\rho_{th}, t)$ becomes larger.
- The lifetime of dense region becomes shorter.
- E-v-e fluctuations are more suppressed.

Four-Volume / Lifetime

Four Volume

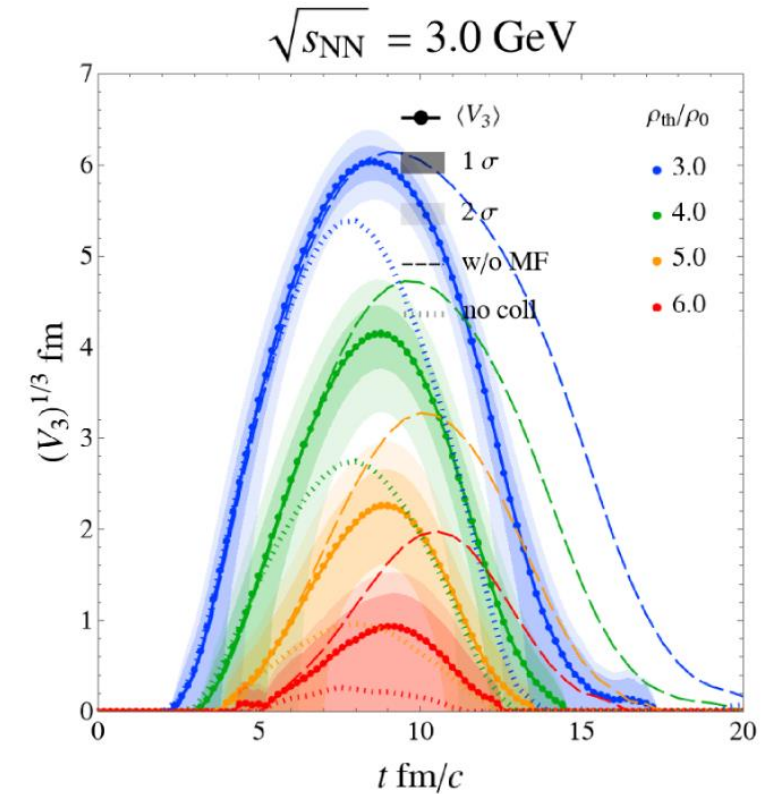
$$V_4(\rho_{\text{th}}) = \int_{-\infty}^{\infty} dt \int_{\rho(x) > \rho_{\text{th}}} d^3 \mathbf{x}$$

Lifetime

$$\tau(\rho_{\text{th}}) = \frac{V_4(\rho_{\text{th}})}{\max V_3(\rho_{\text{th}}, t)}$$

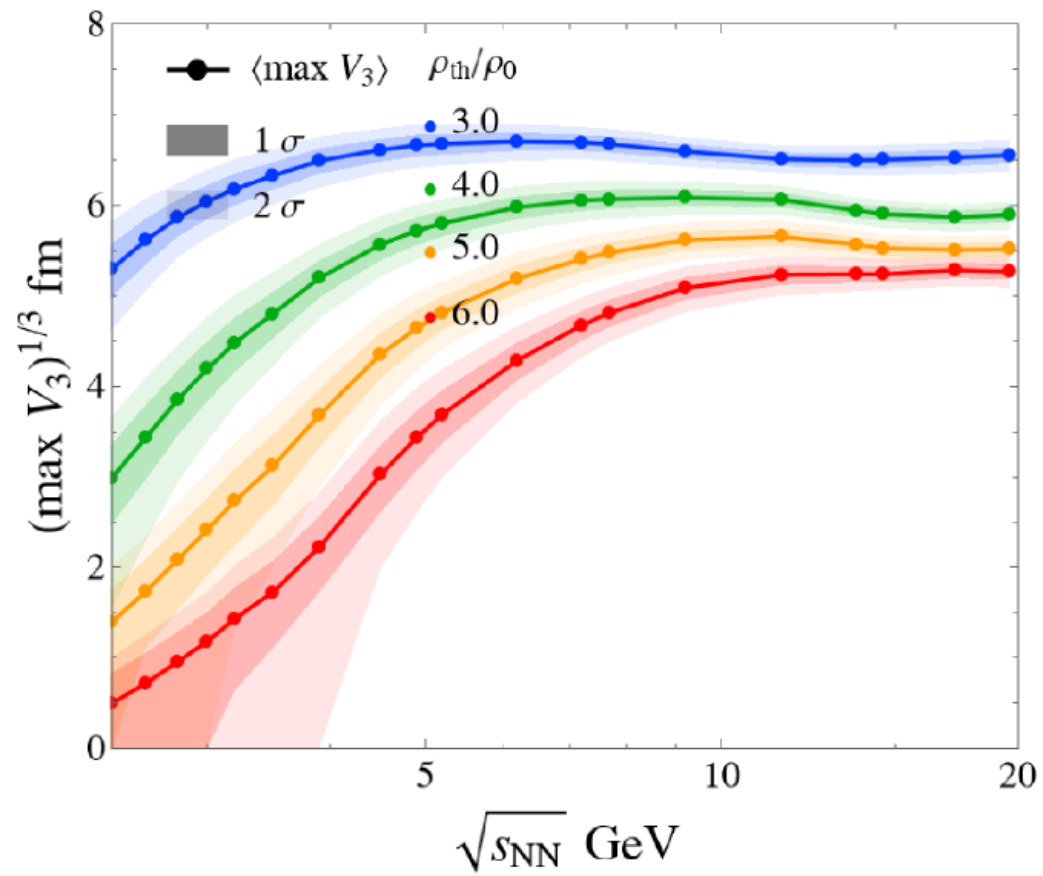
Note

V_4 may be relevant for the dilepton production rate.

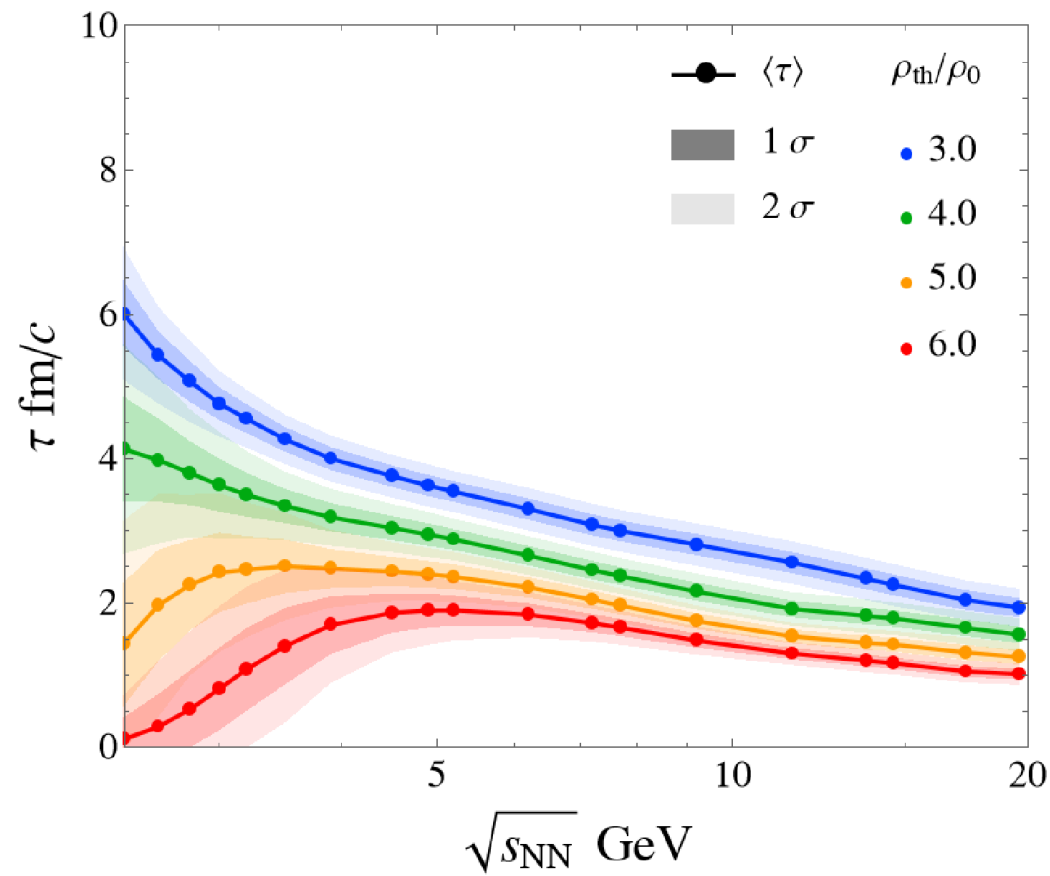


$\sqrt{s_{NN}}$ Dependence

max V_3



Lifetime



ρ_{th}/ρ_0

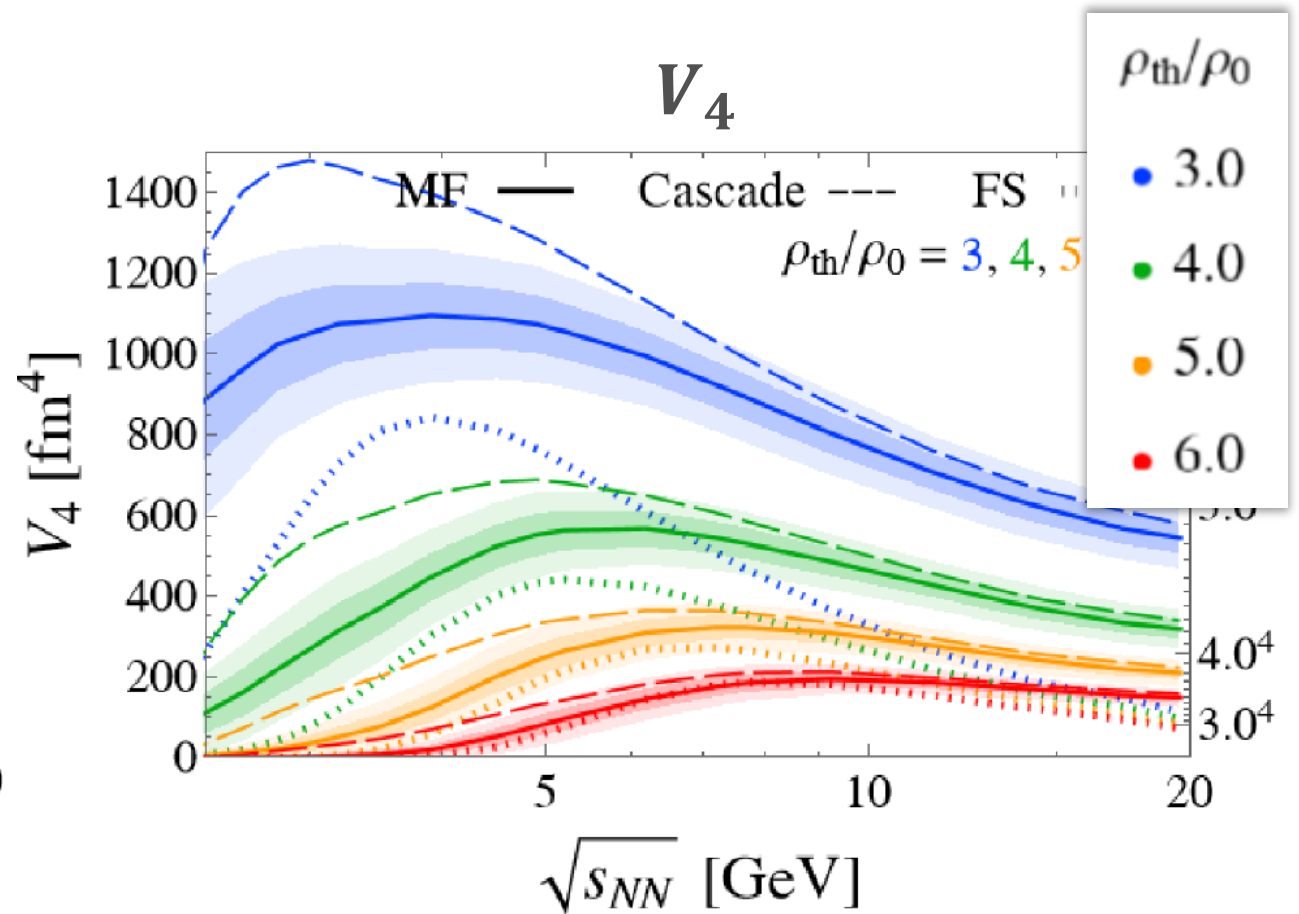
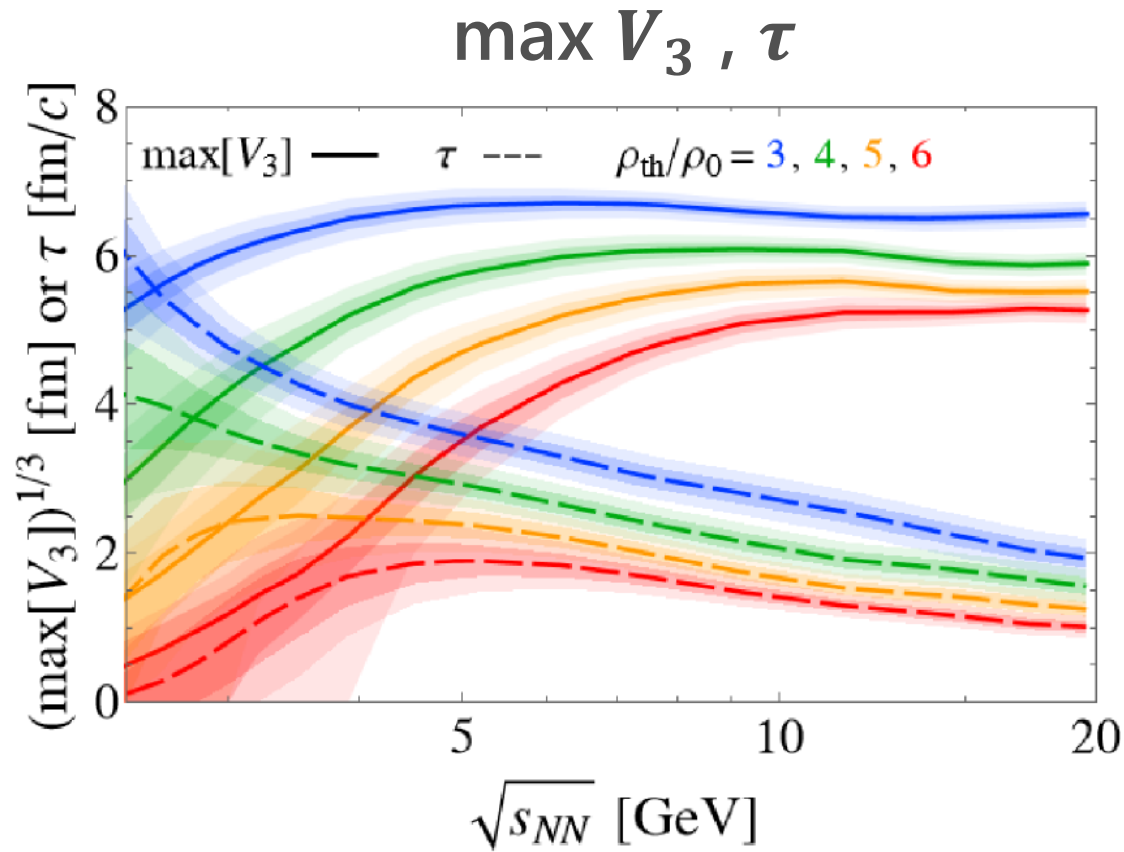
3.0

4.0

5.0

6.0

$\sqrt{s_{NN}}$ Dependence



- $\sqrt{s_{NN}} \approx 3$ GeV would be the best energy to create $\rho = 3 \sim 4\rho_0$ with large V_3 and τ .
- Lower $\sqrt{s_{NN}}$ is suitable to create colder matter.
- All results have large e-v-e fluctuations → Event selection by density?

Short Summary

- $\sqrt{s_{NN}} = 3 \text{ GeV}$ is enough to study $\rho = 3\rho_0$.
- $\rho/\rho_0 = 4\sim 5$ may be accessible with $\sqrt{s_{NN}} = 3\sim 6 \text{ GeV}$.

Future

- Check model independence
 - Analyses in various models
- Experiments at the sweet spot $\sqrt{s_{NN}} = 2.5\sim 6 \text{ GeV}$
 - Future exps. at FAIR, NICA, HIAF, & J-PARC-HI

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Soft Modes of Second-order Phase Transitions

□ Soft modes

- Divergence of the order-parameter fluctuations at a 2nd-order transition.
- **Collective fluctuations become massless** there.

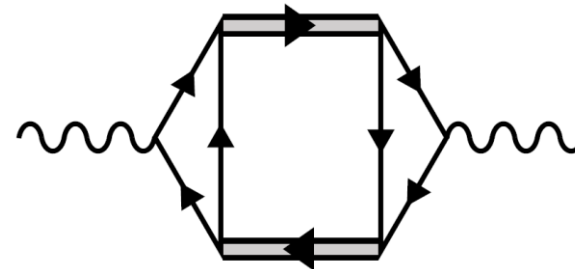
- QCD-CP : density-density fluctuations
- CSC : diquark-pair field

$$\begin{aligned} \text{QCD-CP: } & \text{loop} + \text{two-loop} + \dots \\ \text{CSC: } & \text{loop} + \text{two-loop} + \dots \end{aligned}$$



□ Coupling of soft modes with dynamical observables

- Ex.: dilepton production rate



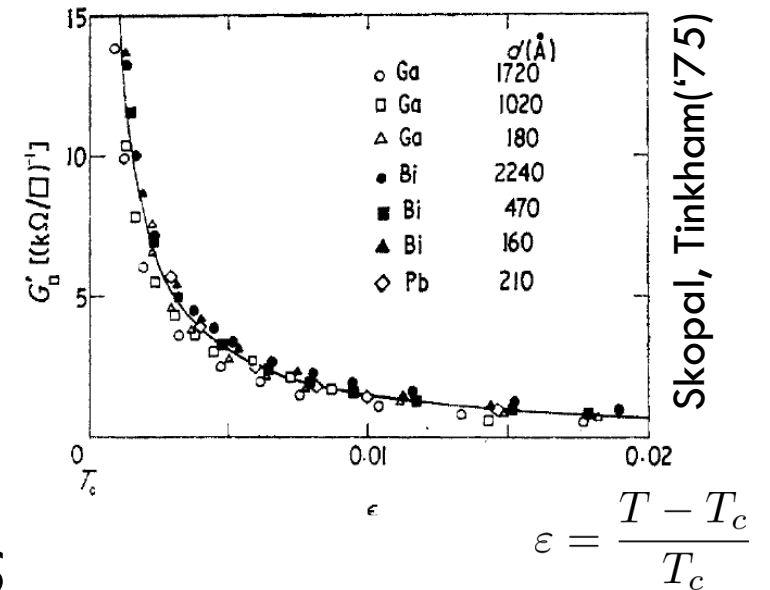
Precursor in Metallic Superconductors

□ Anomalous behavior of observables near but above T_c of SC

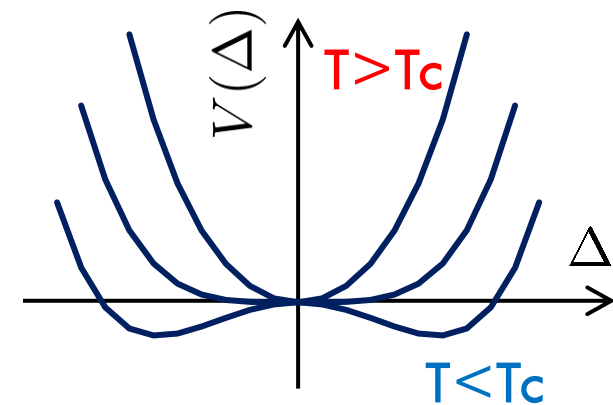
- electric conductivity
- magnetic susceptibility
- pseudogap

- Enhanced pair fluctuations is one of the origins of precursory phenomena.
- More significant phenomena in strongly-coupled systems.

Electric conductivity



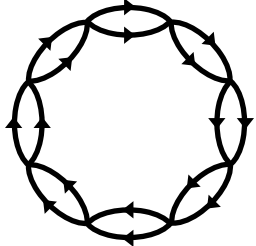
Landau's free energy



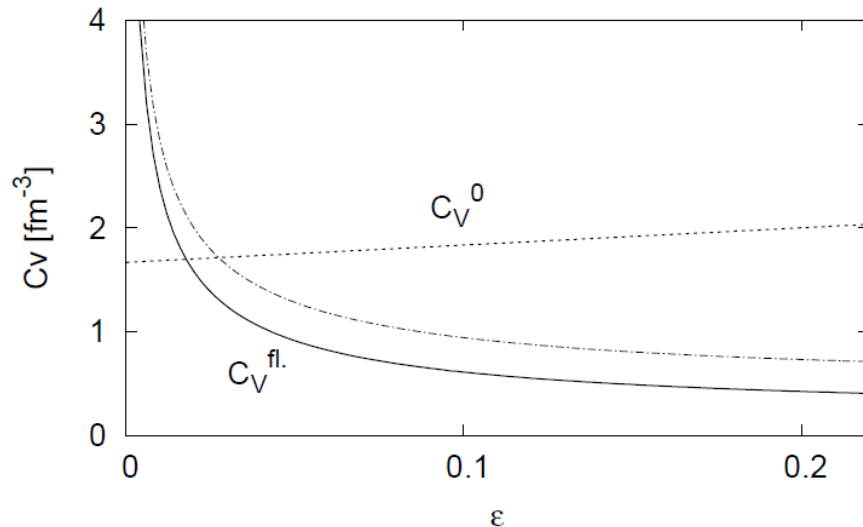
Precursor of Color Superconductivity

MK, Koide, Kunihiro, Nemoto, '03, '05

□ Thermodynamic Potential

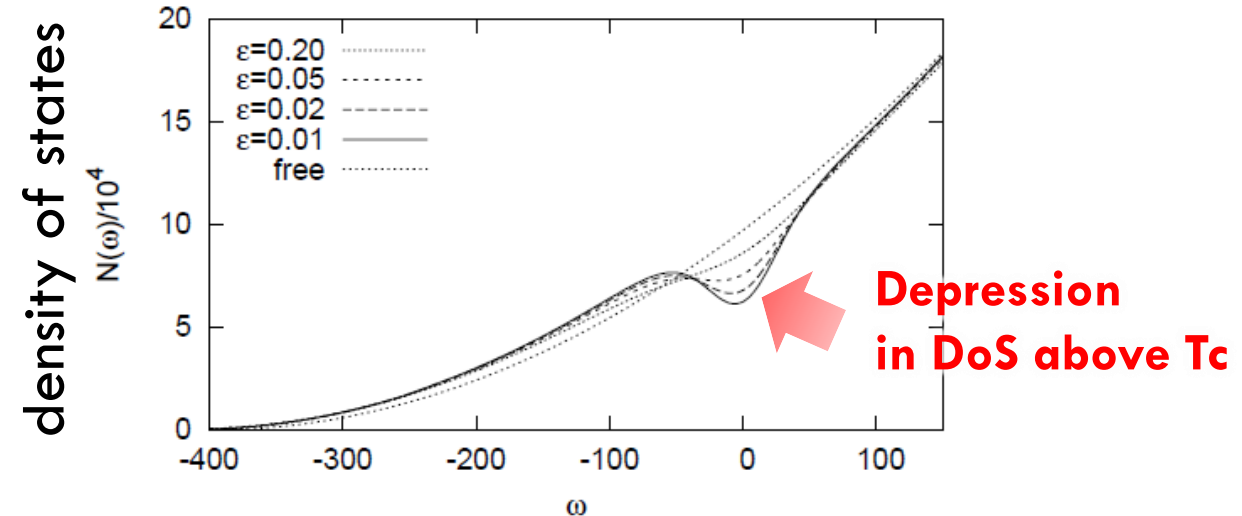
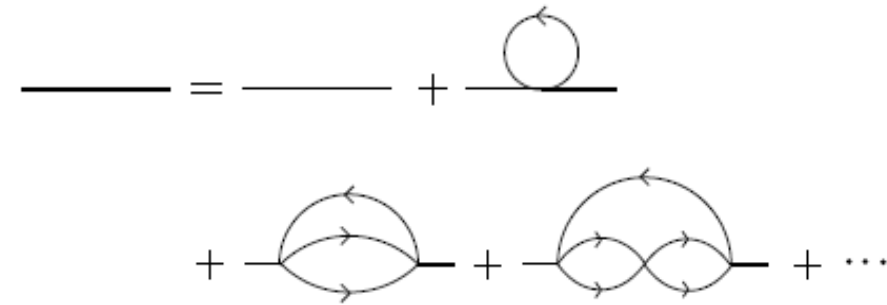
$\Omega =$

 \rightarrow
 Specific heat

$$c = -T \frac{\partial^2 \Omega}{\partial T^2}$$



$$\varepsilon = \frac{T - T_c}{T_c}$$

□ Pseudogap



NJL model (2-flavor)

$$\mathcal{L} = \bar{\psi}i\partial\psi + \mathcal{L}_S + \mathcal{L}_C$$

$$\mathcal{L}_S = G_S((\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma_5\tau\psi)^2)$$

$$\mathcal{L}_C = G_C((\bar{\psi}i\gamma_5\tau_A\lambda_A\psi^C)(\text{h.c.}))$$

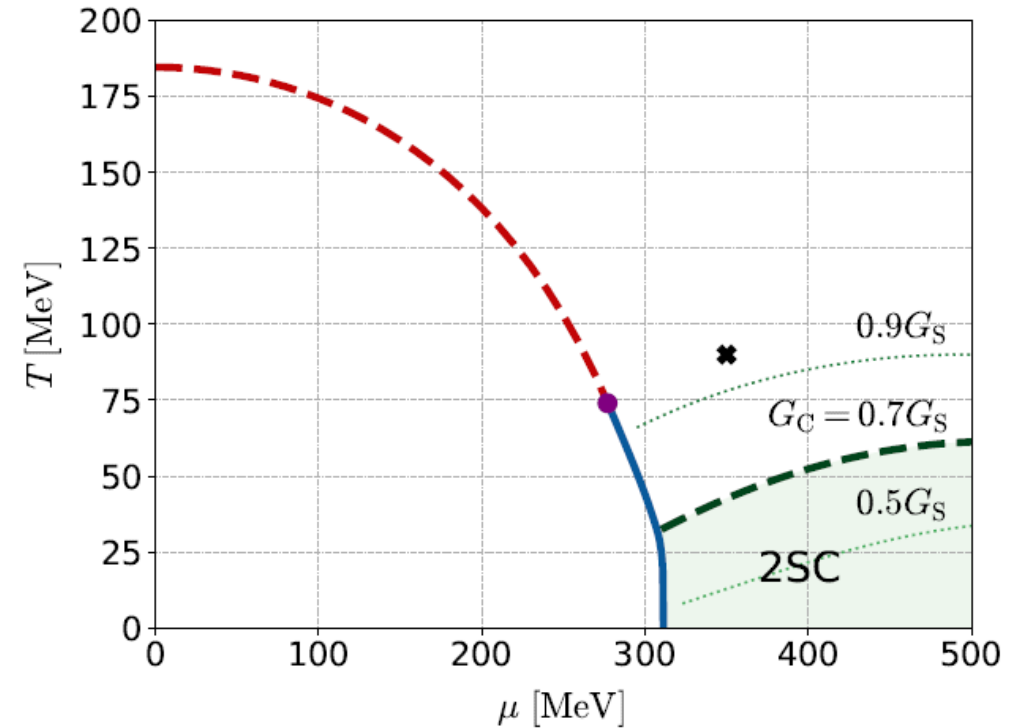
diquark interaction

Parameters

$$G_S = 5.01 \text{ GeV}^{-2}, \quad \Lambda = 650\text{MeV}, \quad m_q = 0$$



Phase Diagram in MFA



- Order of phase transition
 - 2nd in the MFA
 - can be 1st due to gauge fluctuation

Matsuura+('04), Giannakis+('04)
Noronha+('06), Fejos, Yamamoto('19)

Di-quark Fluctuations

□ Diquark Propagator

$$D^R(x) = \langle [\Delta^\dagger(x), \Delta(0)] \rangle \theta(t) = \Rightarrow \Rightarrow$$

□ Random Phase Approximation

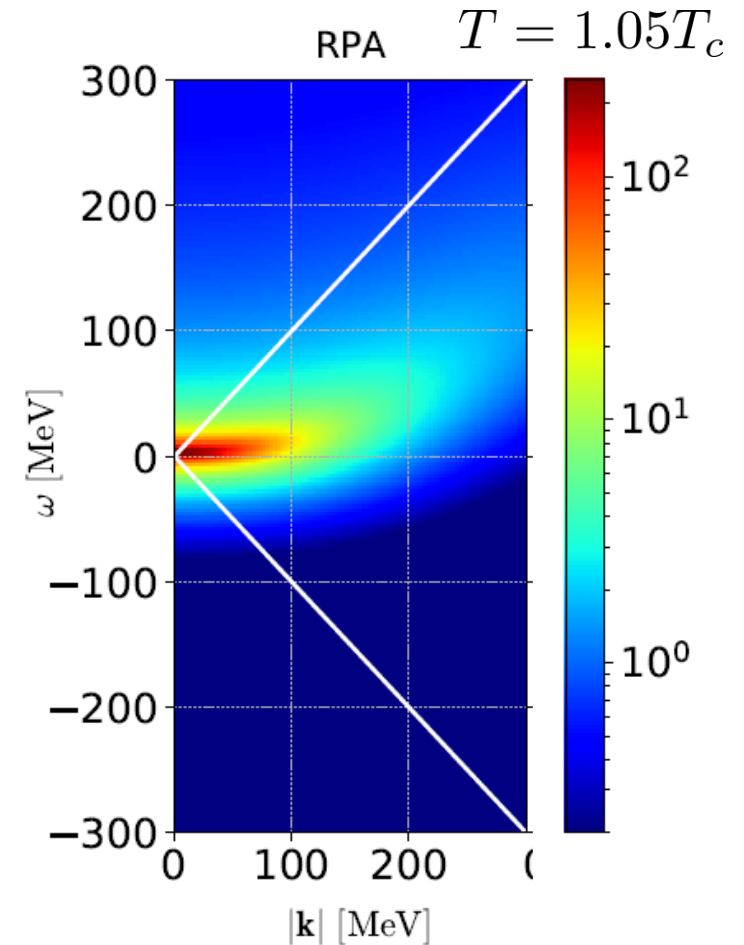
$$\begin{aligned} \Rightarrow \Rightarrow &= \text{loop} + \text{two loops} + \dots \\ &= \frac{Q^R(\mathbf{k}, \omega)}{1 + G_C Q^R(\mathbf{k}, \omega)} \\ Q^R(\mathbf{k}, \omega) &= \text{loop} \end{aligned}$$

- Diquark field becomes massless at $T=T_c$
- Soft mode of CSC transition
- Strength in the space-like region

MK, Koide, Kunihiro, Nemoto, '01,'05

Dynamical Structure Factor

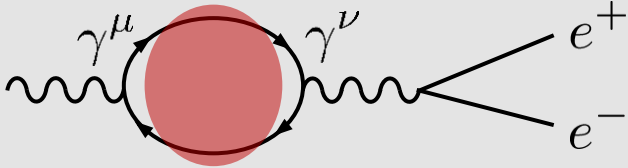
$$S(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{1}{1 - e^{-\beta\omega}} \text{Im} D^R(\mathbf{k}, \omega)$$



Photon Self-Energy: Precursor of CSC

□ Dilepton Production Rate

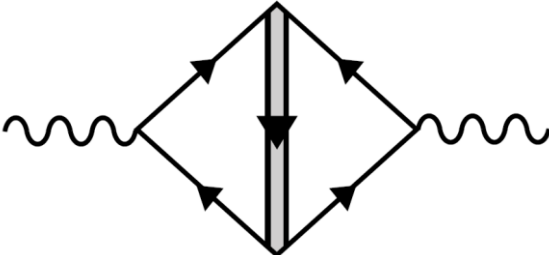
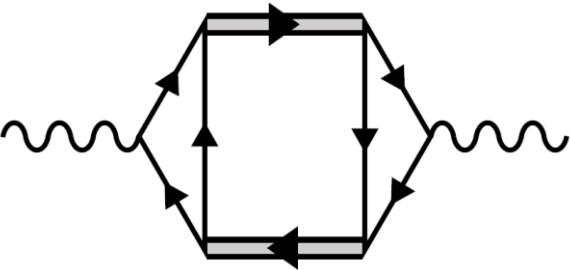
$$\frac{d^4\Gamma}{dk^4} = \frac{\alpha}{12\pi^4} \frac{1}{k^2} \frac{1}{e^{\beta\omega}-1} \text{Im}\Pi^{R\mu}_{\mu}(k)$$



□ Effect of Di-quarks on $\Pi^{\mu\nu}(k)$

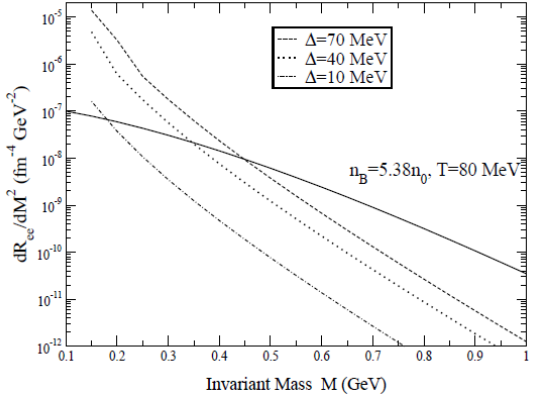
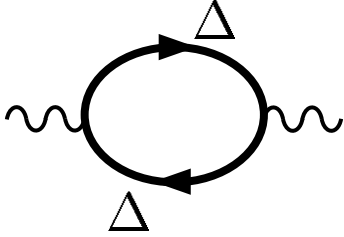
Aslamasov-Larkin term

Maki-Thompson term



□ DPR from CFL phase

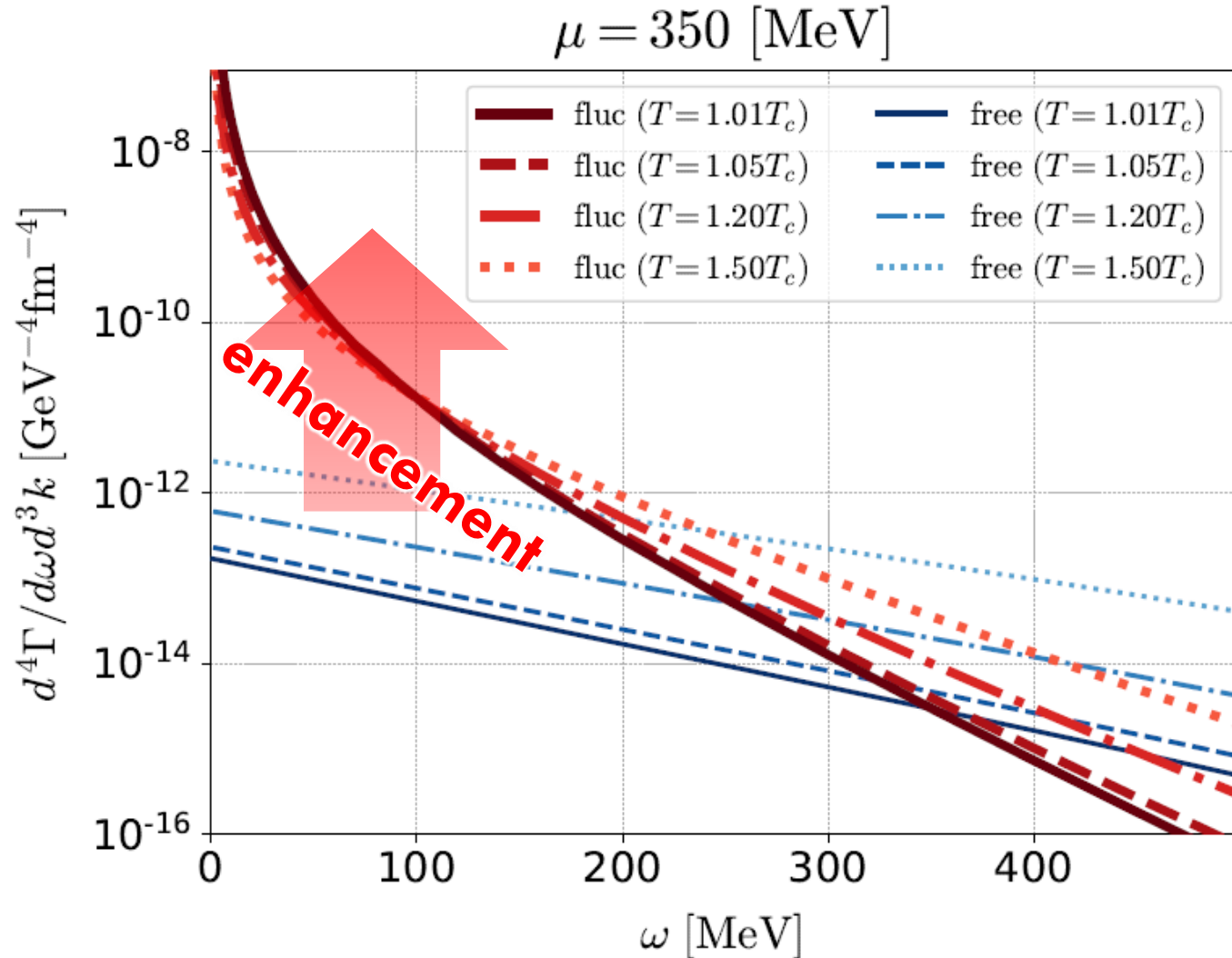
Jaikumar, Rapp, Zahed ('02)



Well-known diagrams in metallic SC for describing paraconductivity

Production Rate at $k = 0$

Nishimura, MK, Kunihiro ('22)



Red: fluctuation contribution

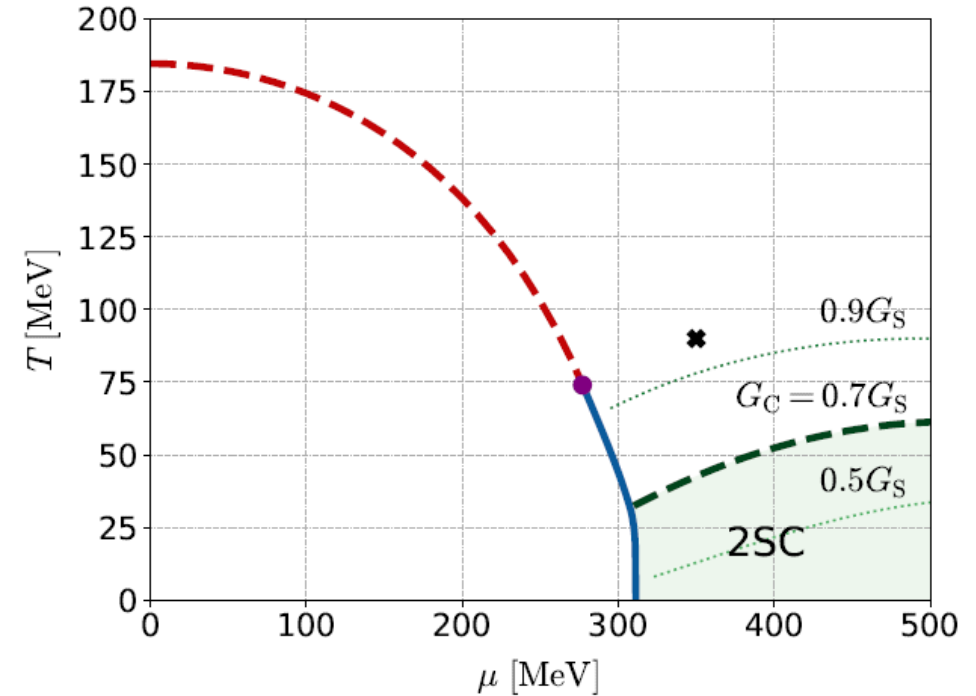
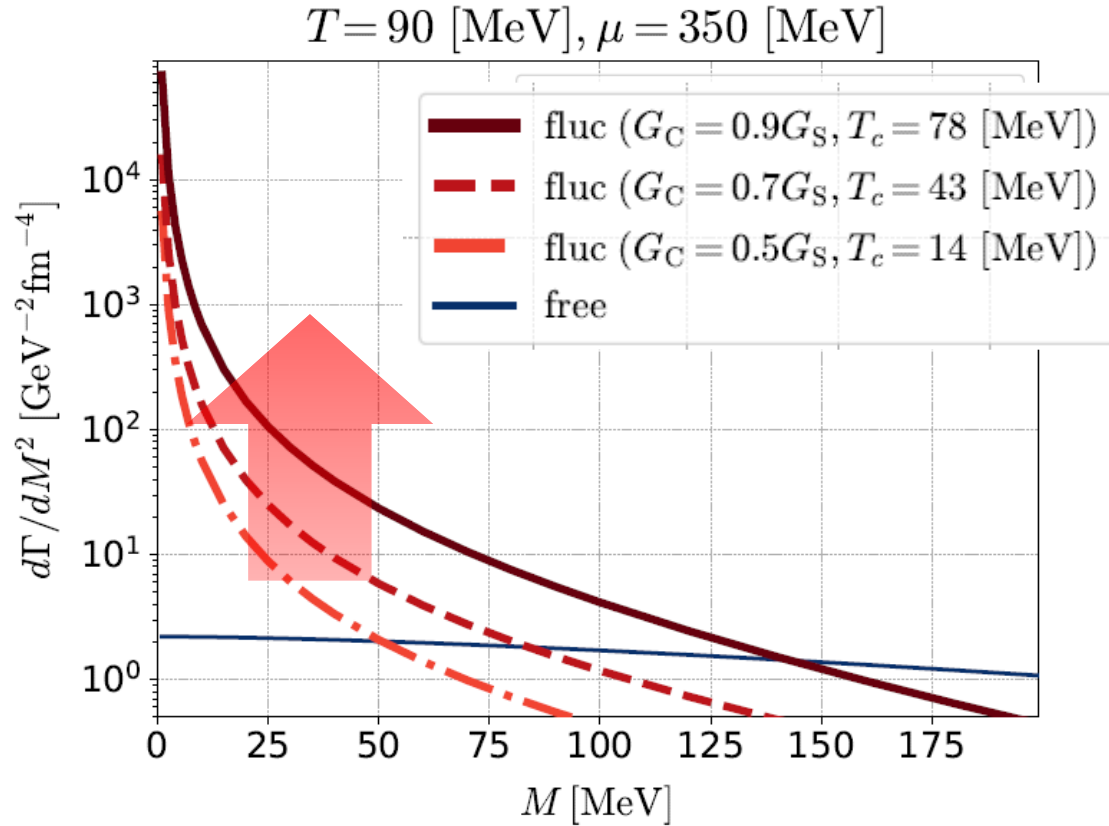
Blue: free quarks

$$G_C = 0.7G_S, T_C \simeq 45 \text{ MeV}$$

- Di-quark fluctuations give rise to large enhancement in the low energy region $\omega < 200$ MeV and $T < 1.5T_c$.
- Anomalous enhancement is not sensitive to T .

Invariant-Mass Spectrum

Nishimura, MK, Kunihiro ('22)



- ❑ Strong enhancement at low invariant mass.
- ❑ **Observable in the HIC?**

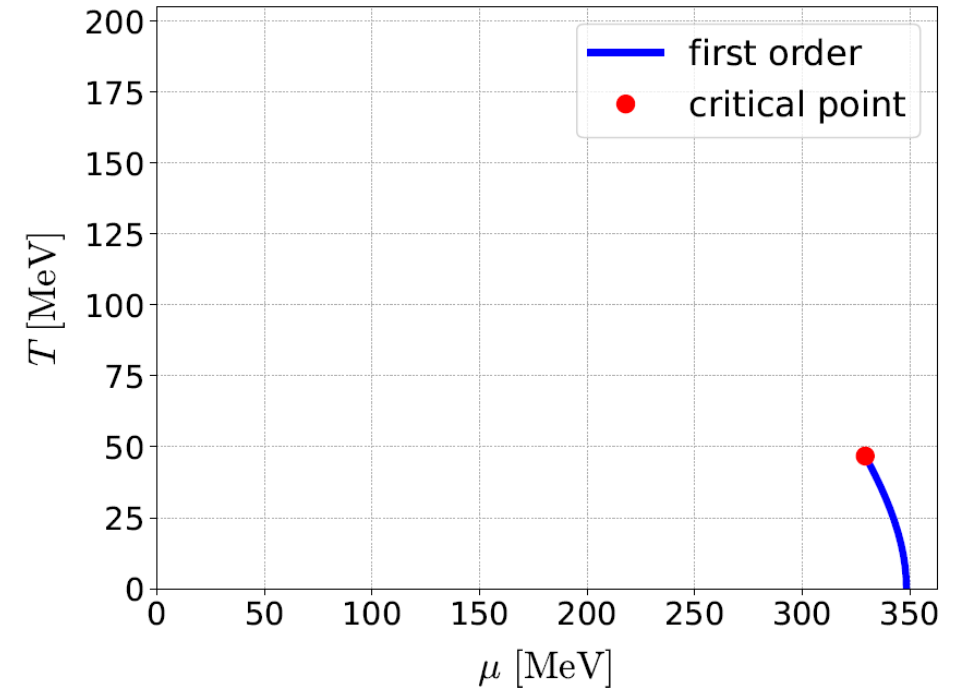
Dileptons from QCD Critical Point

NJL model (2-flavor)

$$\mathcal{L} = \bar{\psi}(i\partial - m)\psi + G_S((\bar{\psi}\psi)^2 + (\bar{\psi}i\gamma_5\tau\psi)^2)$$

Parameters

$$G_S = 5.5 \text{ GeV}^{-2}, \quad \Lambda = 631 \text{ MeV}, \quad m_q = 5.5 \text{ MeV}$$



Soft Mode of QCD-CP

= fluctuation of scalar ($\bar{q}q$) channel

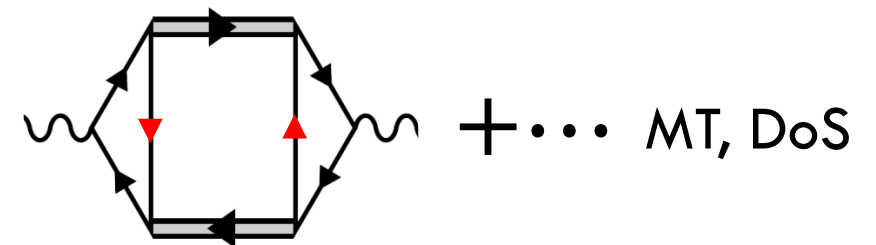
$$D^R(x) = \langle [\bar{\psi}\psi(x), \bar{\psi}\psi(0)] \rangle \theta(t) = \Rightarrow \Rightarrow$$

□ Random Phase Approximaion

$$\Rightarrow \Rightarrow = \text{loop} + \text{two-loop} + \dots$$



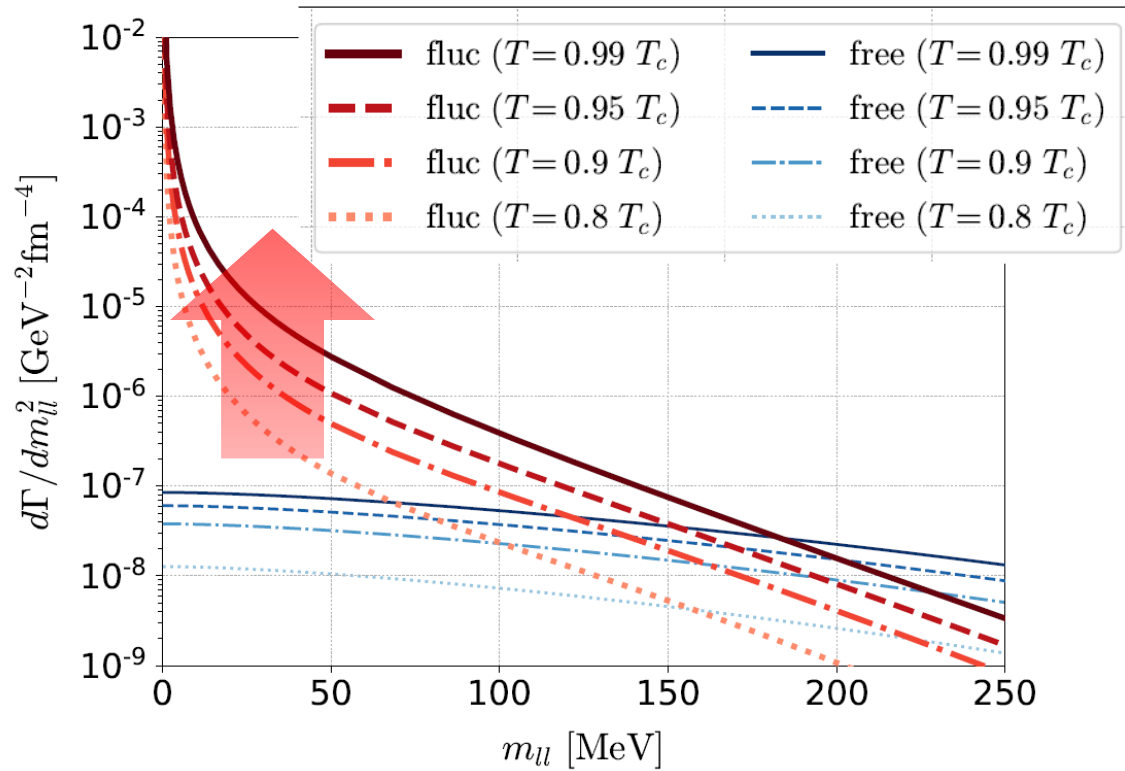
Modification of dilepton production through



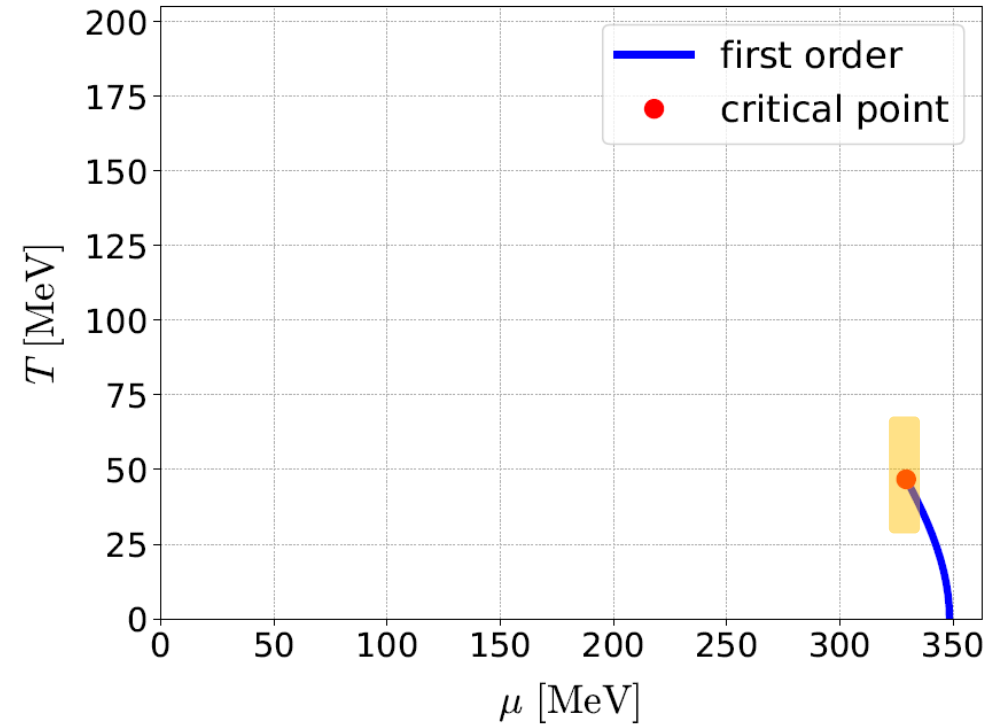
Dilepton production rate near QCD-CP

Nishimura, MK, Kunihiro ('23)

Invariant mass spectrum

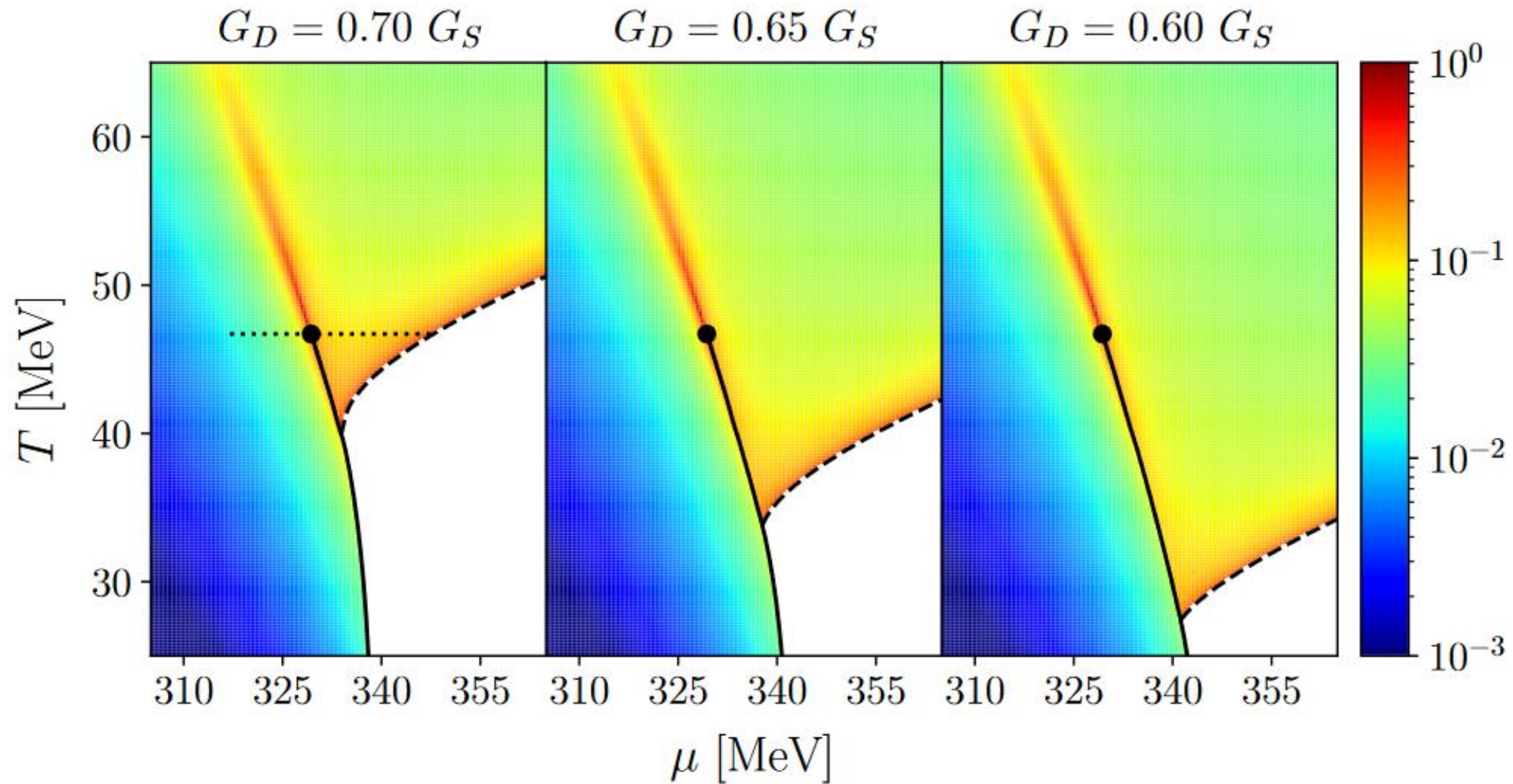


for fixed chem. pot.: $\mu = \mu_c$



- Enhancement at low $M_{\ell\ell}$ region near QCD-CP
- Distinguishment from diquark soft mode may be difficult.

Electric Conductivity on QCD Phase Diagram



- DPR in the low-energy limit = electric conductivity
- Two “hot spots” on the T - μ plane

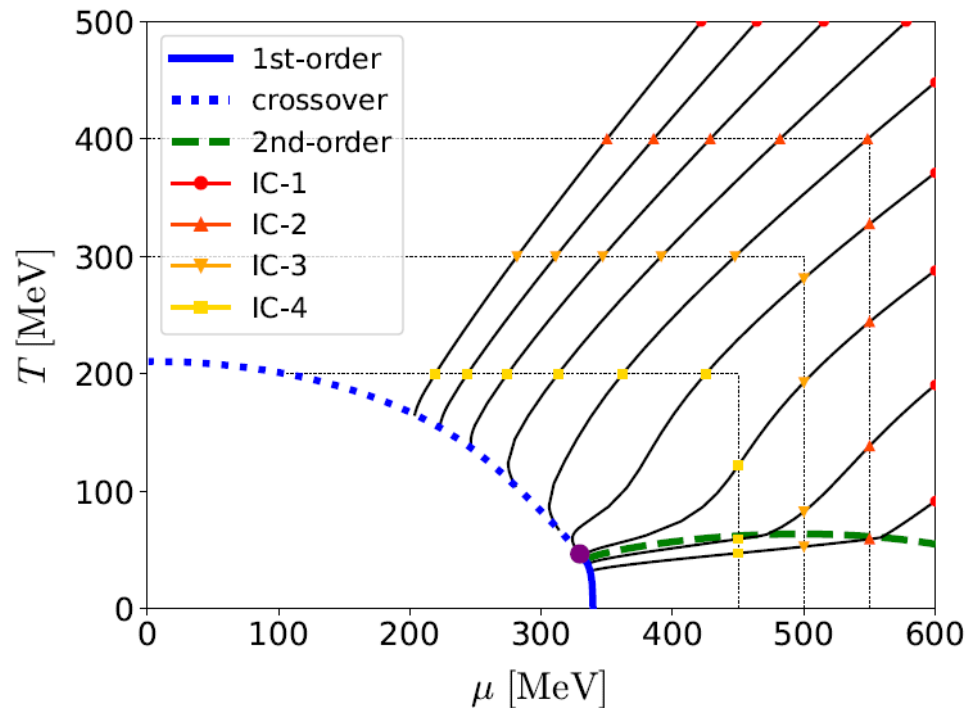
Dilepton Yields: Beam-Energy Scan

Nishimura, Nara, Steinheimer, Eur.Phys.J.A 60, 2024

Dilepton yields

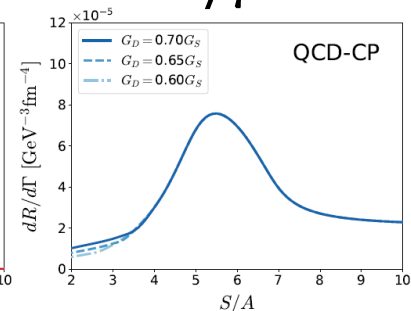
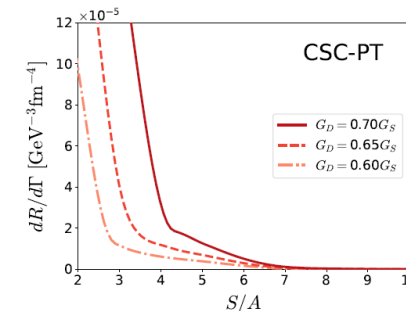
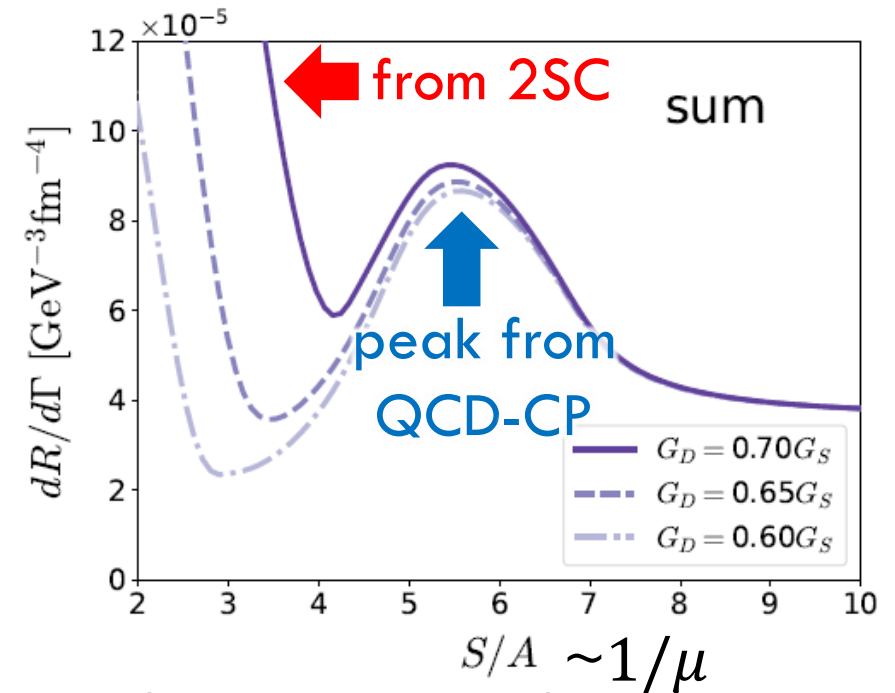
\approx integrated rate along isentropic lines

Isentropic lines in NJL model



Effect of 1st-tr on evolution: Savchuk+ 2209.05267

Dilepton Yields $50 < M < 100$ MeV



Summary

- The beam-energy scan will reveal rich structures on QCD phase diagram, such as the QCD critical point and color superconductivity.
- Quantitative analysis of the size and lifetime of the dense region:
 - $\sqrt{s_{NN}} \simeq 3 \text{ GeV}$ may be an optimal energy to study $\rho = 3 \sim 4 \rho_0$.
- Phase transitions in dense quark matter may be detectable through the enhancement of the dilepton production rate at ultra-low-mass-region.