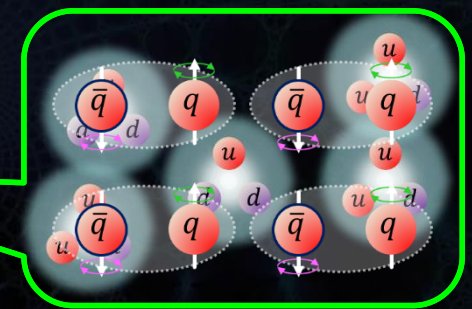
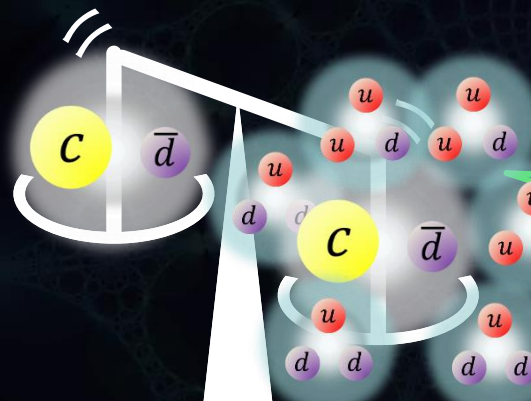


# D meson and chiral symmetry breaking

Kei Suzuki (Yonsei U.)

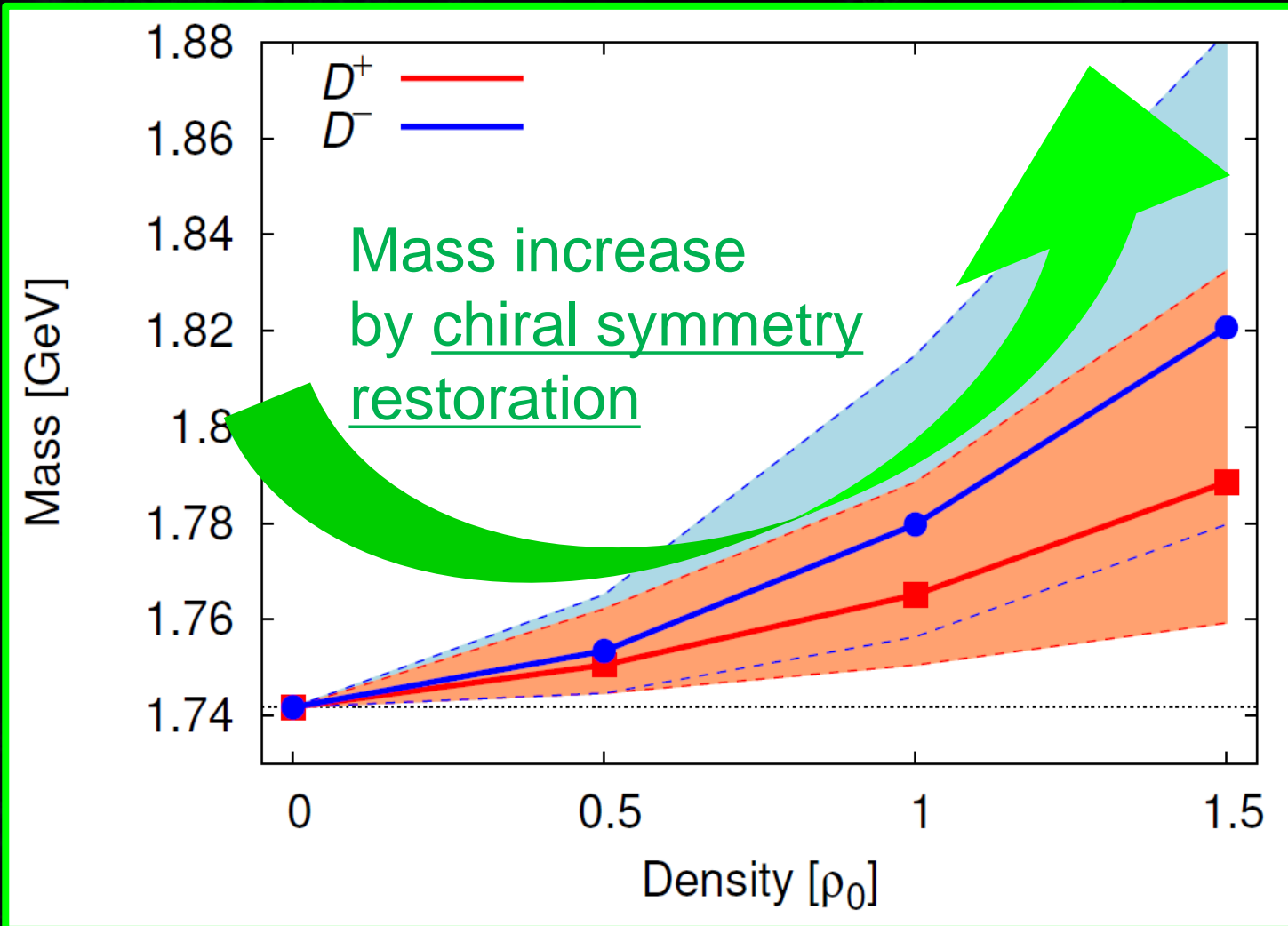


In vacuum



In medium

# $D^\pm$ meson mass in nuclear matter from QCD sum rules



# Outline

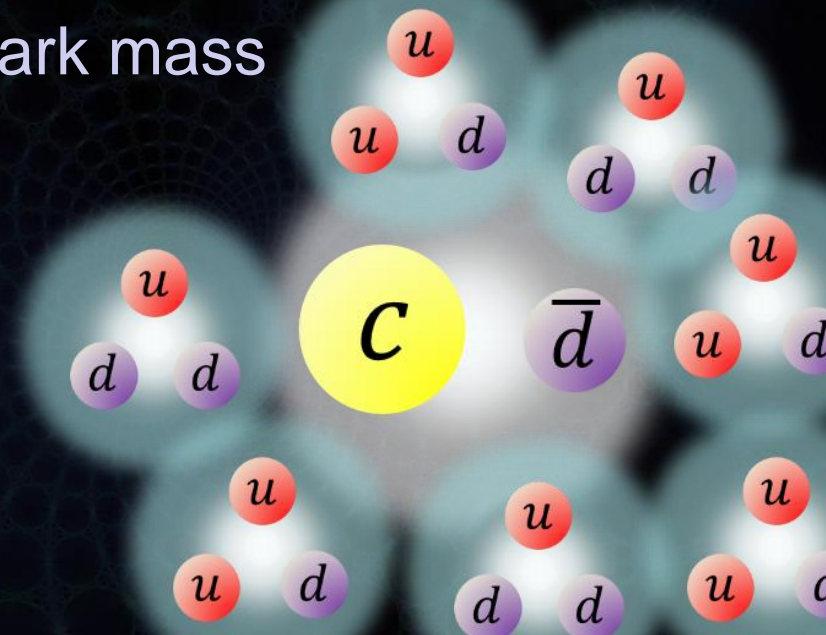
1. Why does  $D$  meson mass increase by  $\chi$ SR in QCD sum rules ?

- $\langle \bar{q}q \rangle$  term is predominant in  $D$  meson OPE
- Opposite sign in OPE for chiral partners

2.  $D$  meson mass in Potential model

- $\chi$ SR = smaller constituent quark mass
- Application

3. Summary



**1. Why does D  
meson mass  
increase in QCD  
sum rules?**

# QCD sum rule

Relation between operator product expansion (OPE) of QCD correlation function and hadron spectral function

$$\Pi_{\text{OPE}}(M^2) = \int_0^\infty K(s, M^2) \rho(s) ds$$

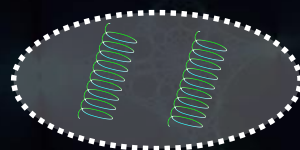
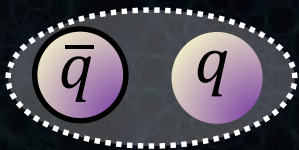
Quark and Gluon dynamics



QCD vacuum condensates

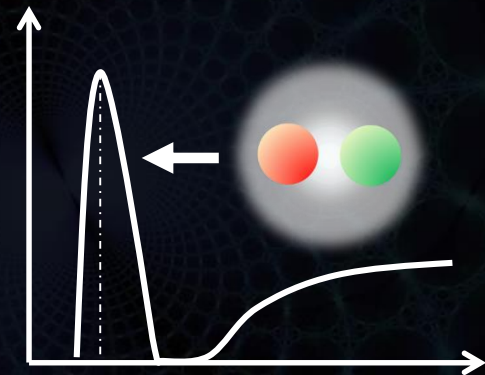
$$\langle \bar{q}q \rangle$$

$$\langle G_{\mu\nu} G^{\mu\nu} \rangle$$



etc...

Hadron properties  
(mass, width...)



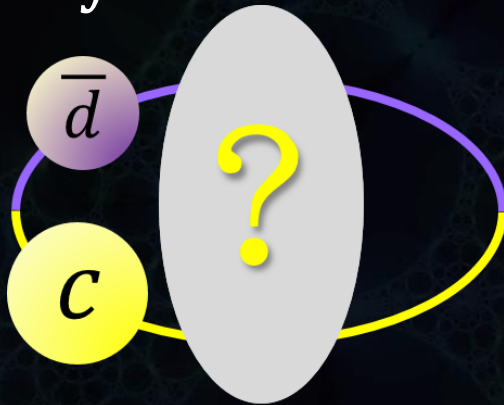
# QCD sum rule

Relation between operator product expansion (OPE) of QCD correlation function and hadron spectral function

$$\Pi_{\text{OPE}}(M^2) = \int_0^\infty K(s, M^2) \rho(s) ds$$

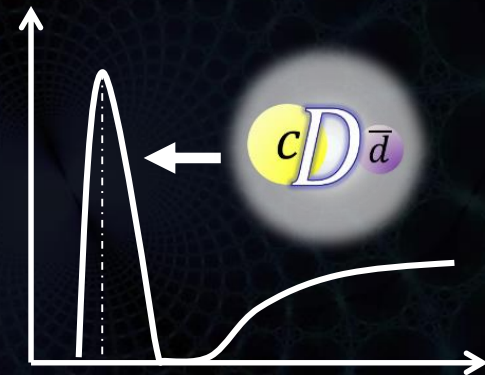
Current-current correlator

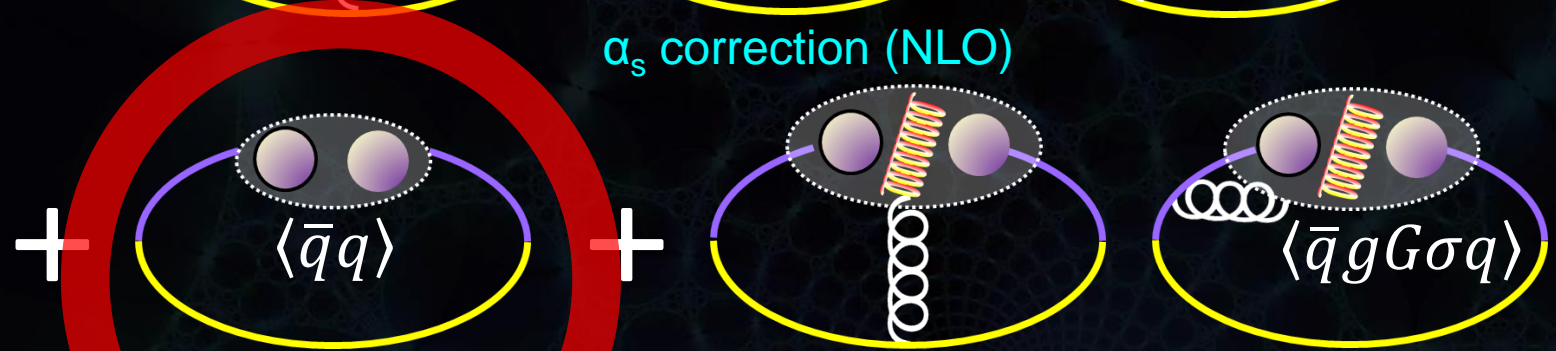
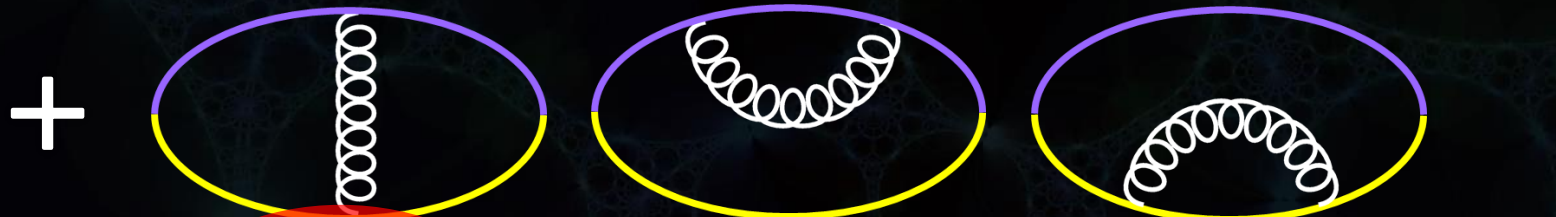
$$\Pi(q) = i \int d^4x e^{iq \cdot x} T[j^\dagger(x)j(0)]$$



Hadron properties

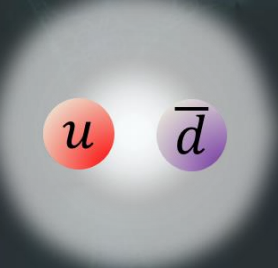
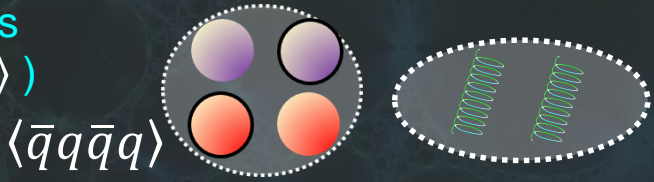
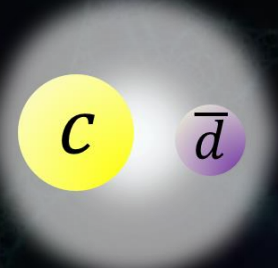

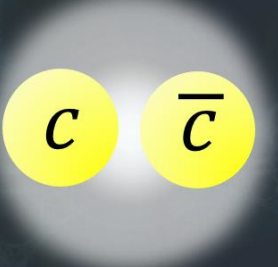
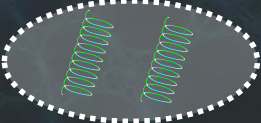
(mass, width...)





+ ...

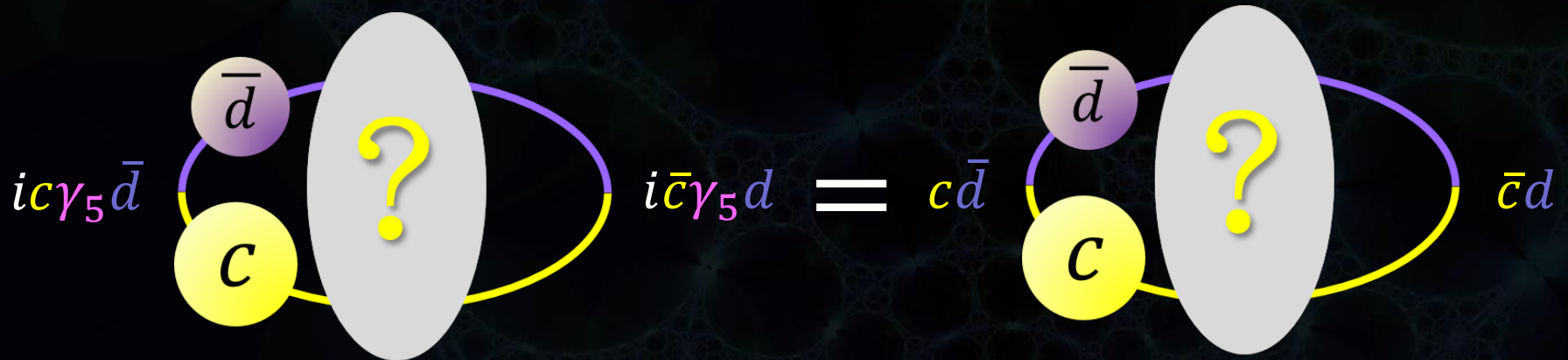
# Different meson systems probe different condensates!

Meson	Dominant contributions in vacuum
Light-Light ( $\rho, \omega$ meson) 	<ul style="list-style-type: none"> <li>• Probe of <u>4-quark</u> and <u>gluon condensates</u>                (2-quark condensate is suppressed as <math>m_q \langle \bar{q}q \rangle</math>)</li> </ul>  $\langle \bar{q}q\bar{q}q \rangle$
Heavy-Light ( $D, B$ meson) 	<ul style="list-style-type: none"> <li>• Probe of <u>2-quark condensate</u> as <math>m_c \langle \bar{q}q \rangle</math></li> </ul>  $\langle \bar{q}q \rangle$
Heavy-Heavy ( $J/\psi, \Upsilon$ ) 	<ul style="list-style-type: none"> <li>• Almost <u>perturbative</u> object                (Probe of gluon condensate)</li> </ul>  $\left\langle \frac{\alpha_s}{\pi} G^{\mu\nu} G_{\mu\nu} \right\rangle$

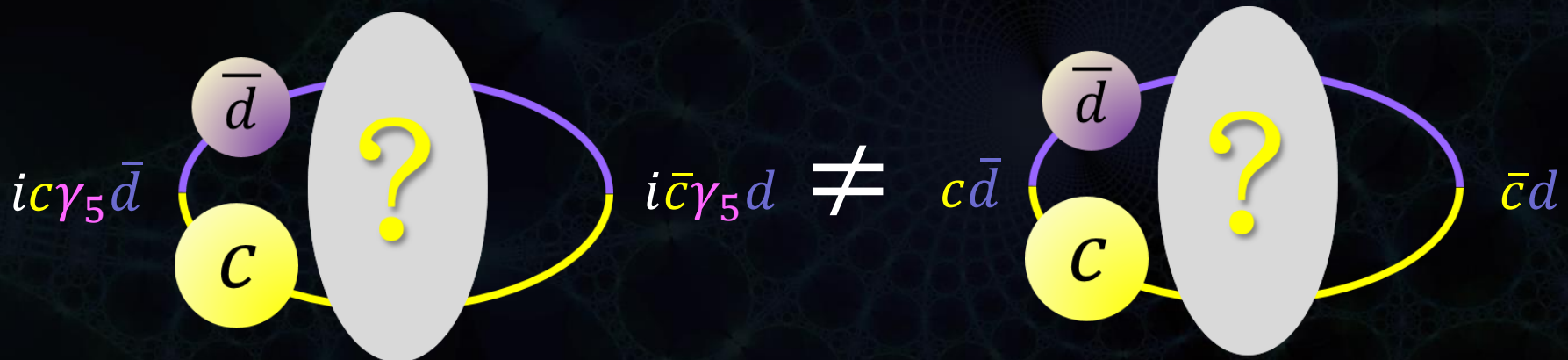


# Chiral partners from OPE

- Chiral symmetric terms  $\Rightarrow$  Pseudoscalar = Scalar



- Chiral breaking terms  $\Rightarrow$  Pseudoscalar  $\neq$  Scalar



# Ex. Chiral symmetric term

$$i c \gamma_5 \bar{d} \quad \text{---} \quad i \bar{c} \gamma_5 d \quad = \quad c \bar{d} \quad \text{---} \quad \bar{c} d$$

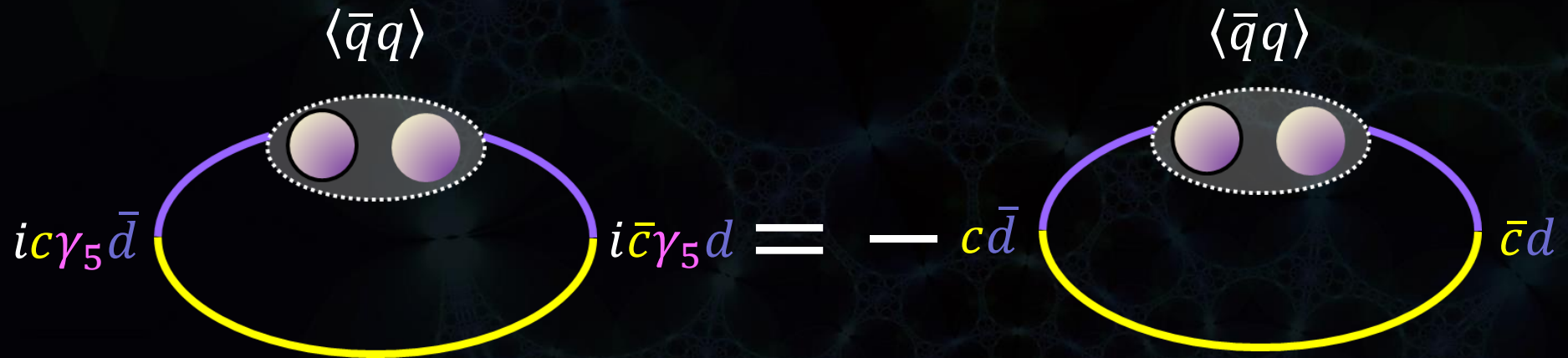
$$c D \bar{d}$$



$$D_0^* \bar{d}$$

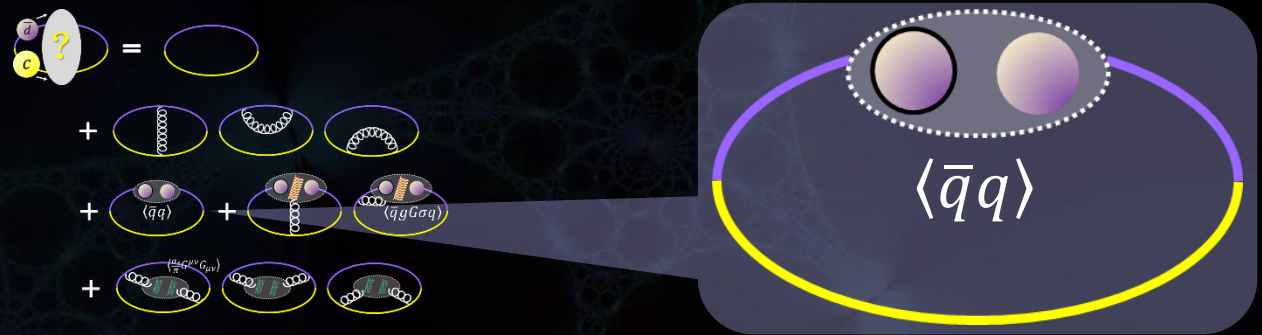
Same contribution  
for chiral partners

# Ex. Chiral breaking term

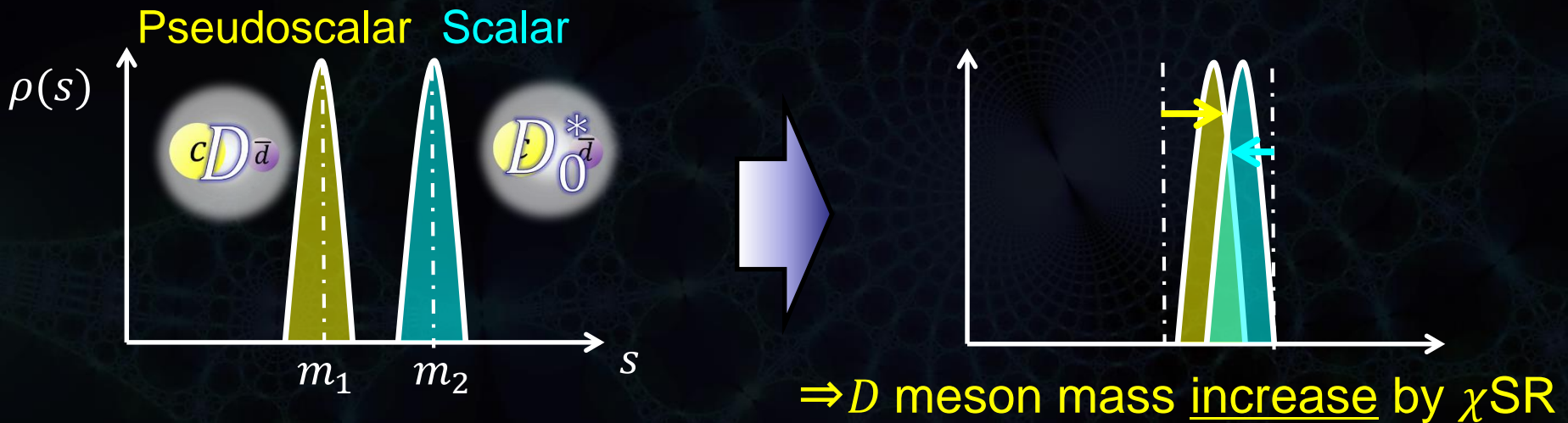


Opposite contribution  
for chiral partners

# Points



- In Heavy-Light meson OPE,  $m_c \langle \bar{q}q \rangle$  diagram is predominant  
 (For Light-Light meson, this term is suppressed by  $m_q \langle \bar{q}q \rangle$ )
- This diagram has opposite sign to the chiral partner  
 $\Rightarrow$  Mass shift in matter has also opposite sign

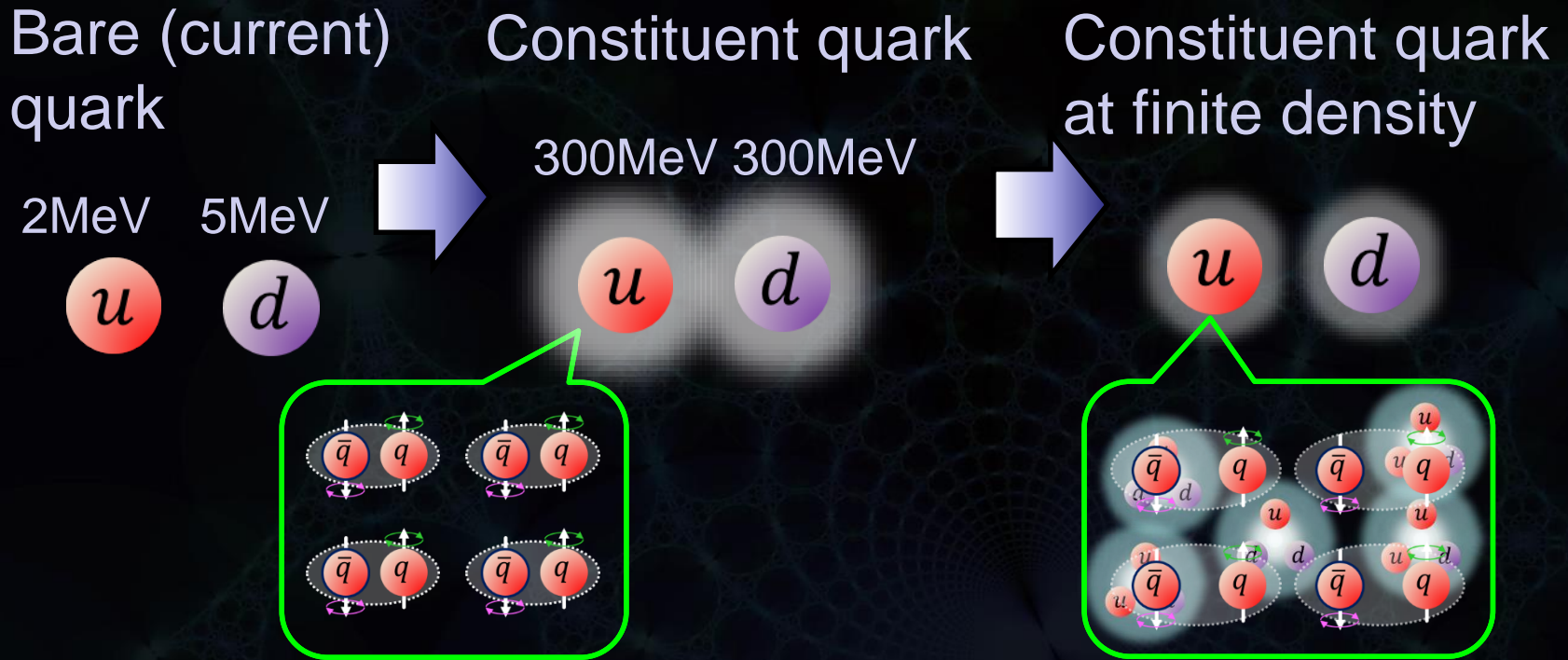


# 2. D meson mass in potential model



Constituent quarks

# Chiral condensate in Constituent quark model



- Contributions of chiral condensate should be included in the (light) constituent quark mass
- $\chi$ SR  $\Rightarrow$  smaller constituent quark mass?

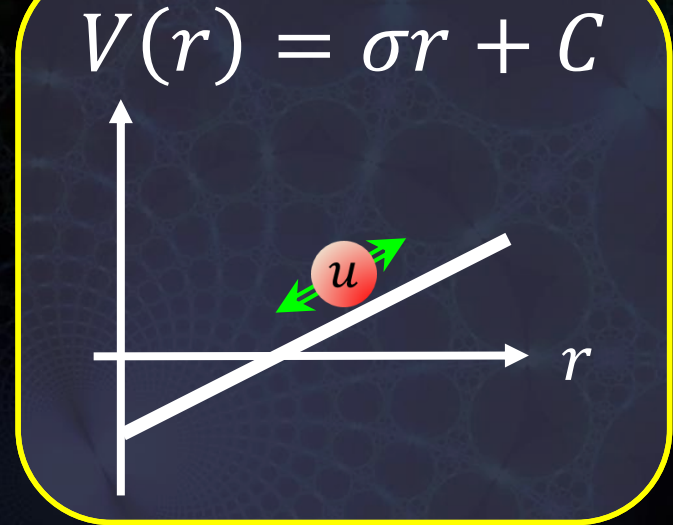
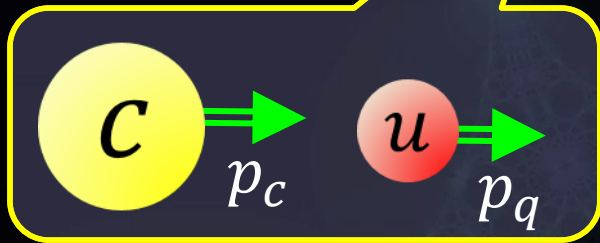
# $m_q$ dependence of quark model for heavy-light meson

$$H = \frac{p_c^2}{2m_c} + \frac{p_q^2}{2m_q} + m_c + m_q + V(r)$$

Kinetic term

Rest mass

Potential term

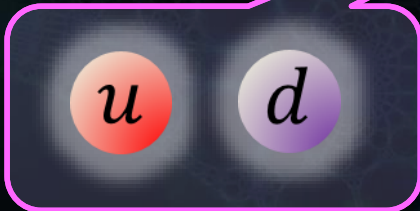
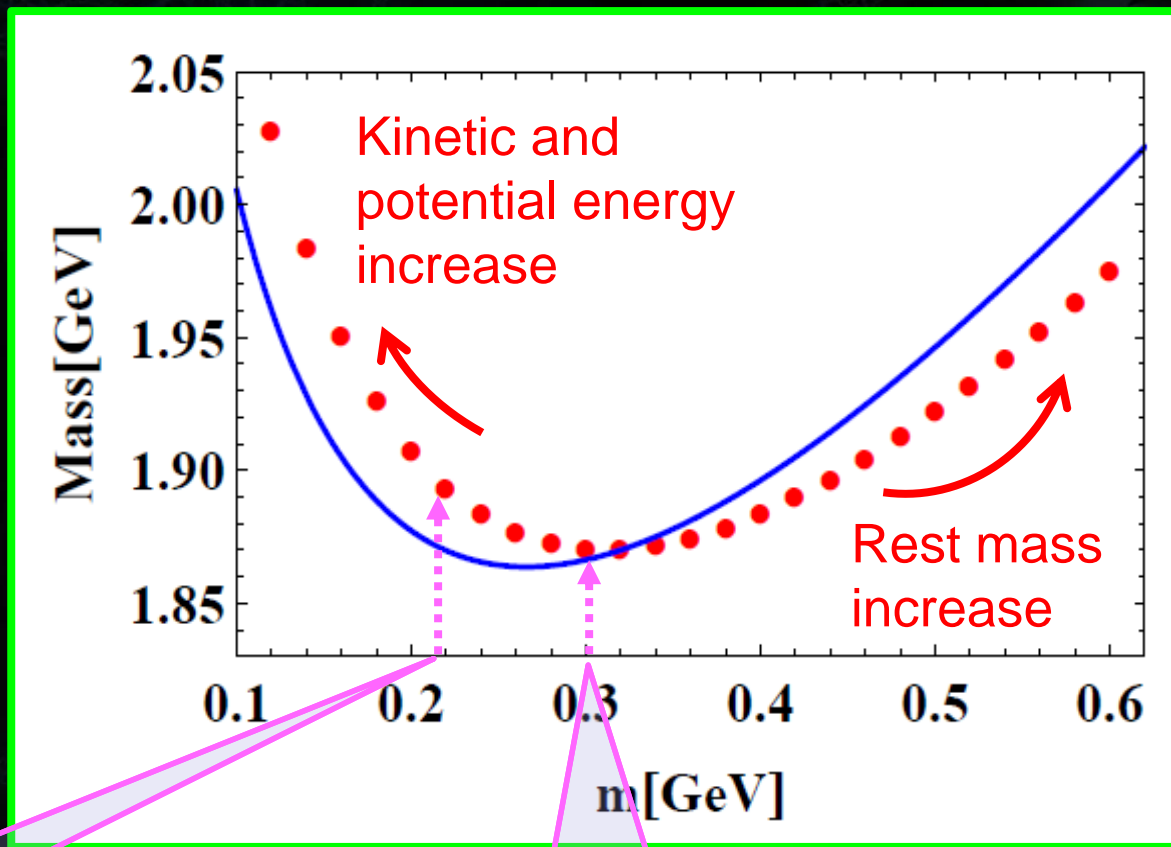


$$E = \frac{p_c^2}{2m_c} + m_c + m_q + \left( \frac{\sigma^2}{m_q} \right)^{1/3} + C$$

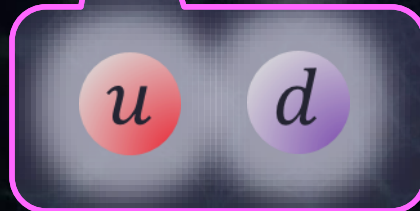
$\Rightarrow$  D meson mass shift = a balance between **rest mass**  $\sim m_q$  and **kinetic and potential energies**  $\sim 1/m_q$

# *D* meson mass shifts = rest mass + kinetic and potential energies

$$E = \frac{p_c^2}{2m_c} + m_c + m_q + \left(\frac{\sigma^2}{m_q}\right)^{1/3} + C$$



$m_q$  at finite density

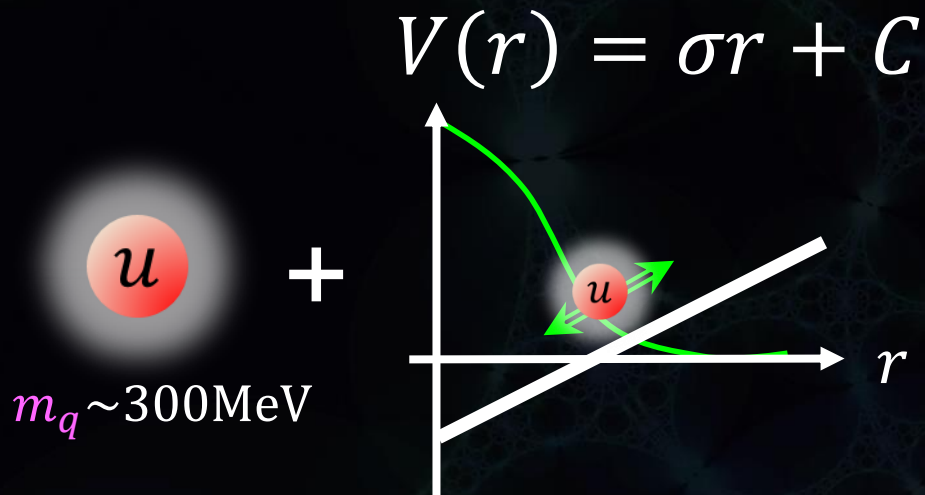


$m_q$  in vacuum



# Points

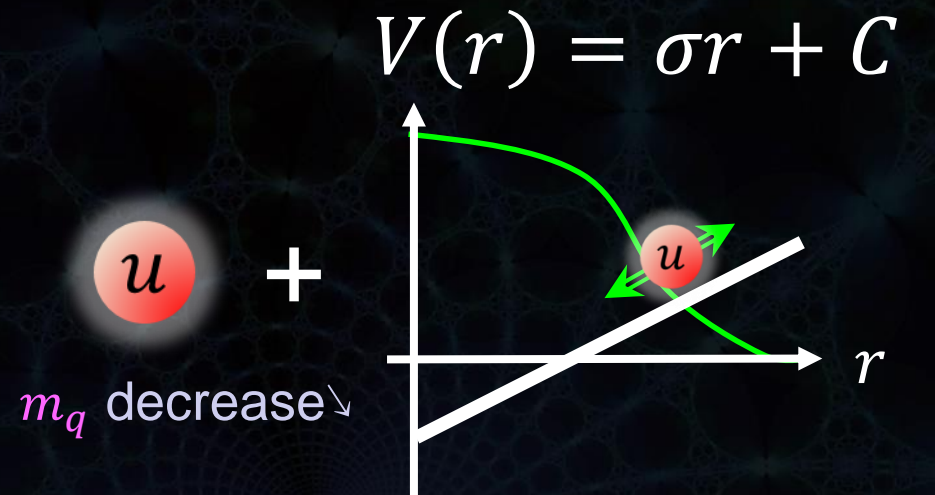
In vacuum



Light quark WF overlaps with confinement potential

$$m_D = m_q + 1/m_q + \dots$$

In nuclear medium



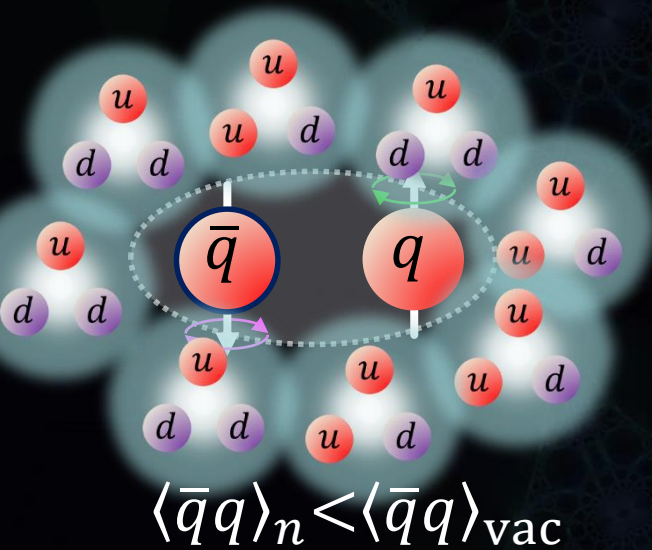
WF expands  $\Rightarrow$  potential energy increase  $\nearrow$

$$m_D = m_q \downarrow + 1/m_q \uparrow + \dots$$

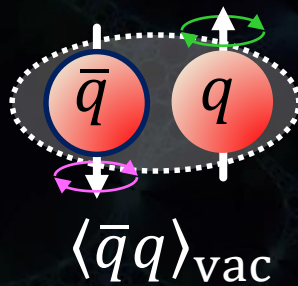
$\Rightarrow$   $D$  meson mass increases by  $\chi$ SR

# Application: Magnetic field enhances $\langle \bar{q}q \rangle$ condensate

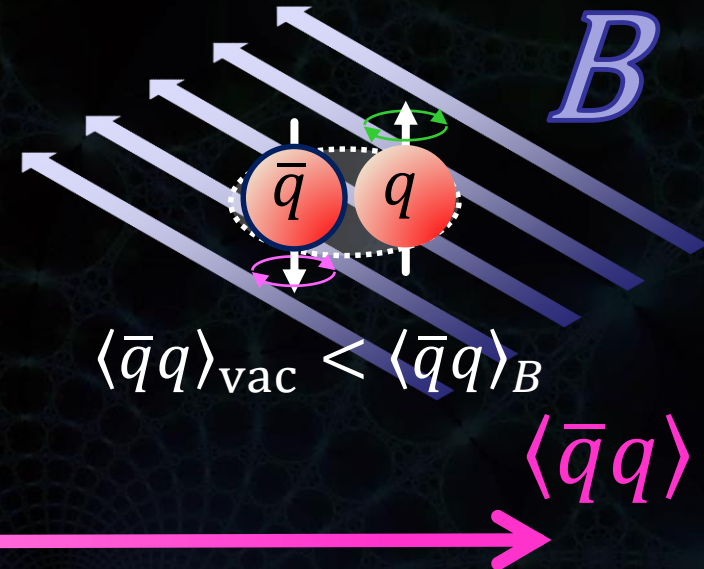
Nuclear matter reduces  $\langle \bar{q}q \rangle$



In vacuum



Magnetic field enhances  $\langle \bar{q}q \rangle$   
(Magnetic catalysis)

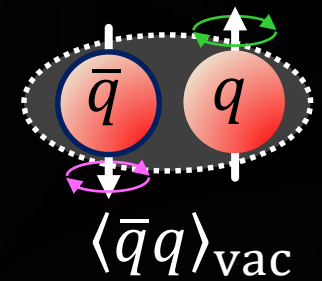


We can tune  $\langle \bar{q}q \rangle$  by external environments!

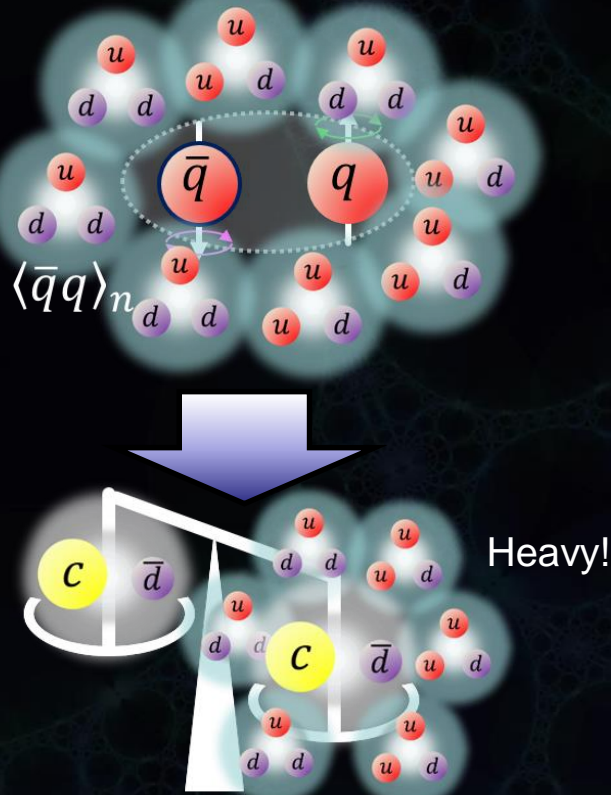
- Realistic in nuclei, neutron star, and low energy HIC at J-PARC and FAIR
- Sign problem in Lattice QCD

- Realistic (?) in relativistic HIC at RHIC and LHC
- NO sign problem in Lattice QCD

# $D$ meson mass shifts can be a probe of $\langle \bar{q}q \rangle$ tuning ?

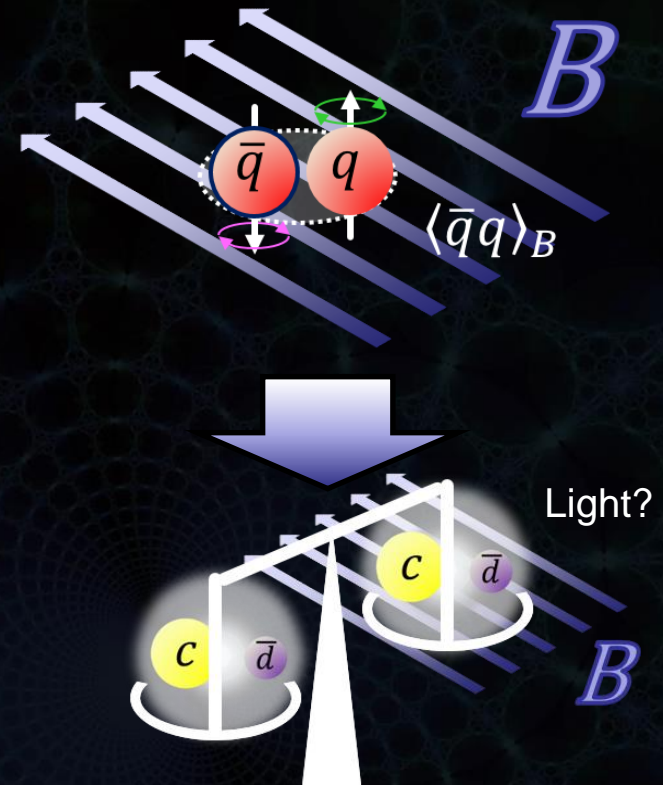


Nuclear matter reduces  $\langle \bar{q}q \rangle$



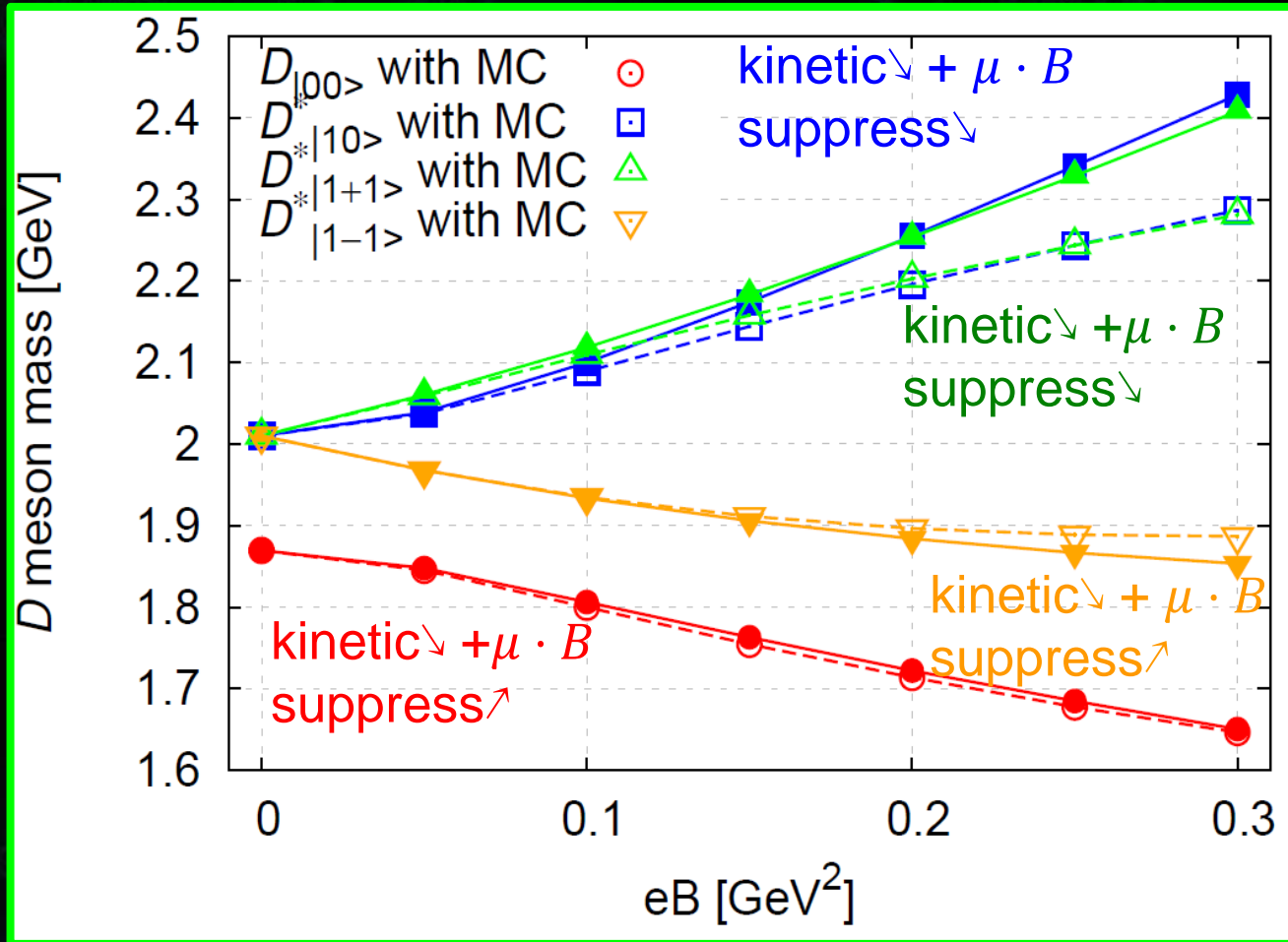
QCD sum rule : KS-Gubler-Oka, PRC93, 045209 (2016)  
 Quark model : Park-Gubler-Harada-Lee-Nonaka-Park, PRD93 054035 (2016)

Magnetic field enhances  $\langle \bar{q}q \rangle$



QCD sum rule : Gubler-Hattori-Lee-Oka-Ozaki-KS, PRD93, 054026 (2016)  
 Quark model : Yoshida-KS, arXiv:1607.04935

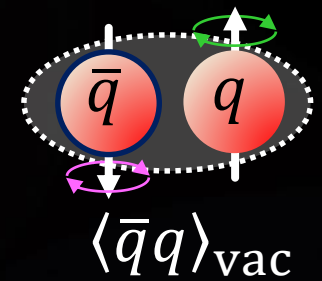
# $D$ meson mass in magnetic field can probe $\langle \bar{q}q \rangle$ enhancement? (from quark model)



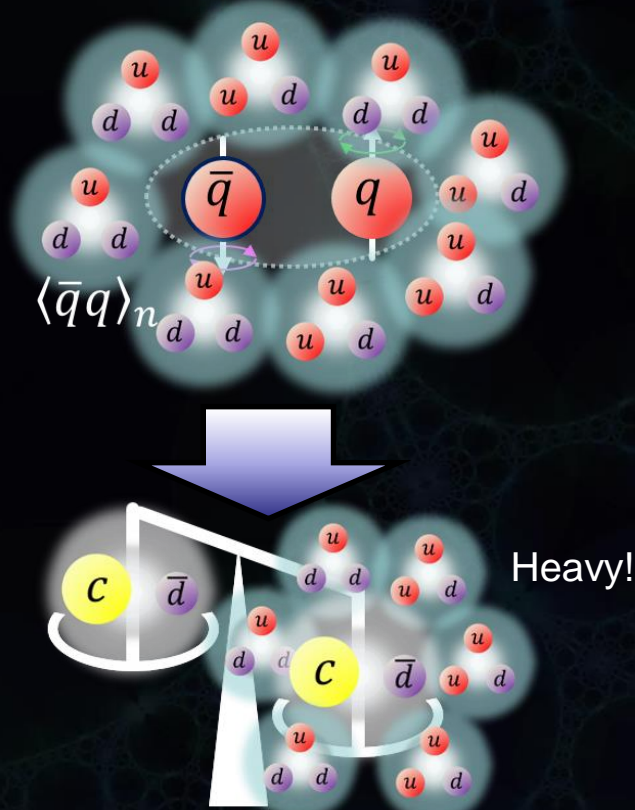
$\Rightarrow$  D meson : mass shift cancelation by  $\chi\text{SB}$

$\Rightarrow$   $D^*$  mesons : mass decrease by  $\chi\text{SB}$

# $D$ meson mass shifts can be a probe of $\langle \bar{q}q \rangle$ tuning !

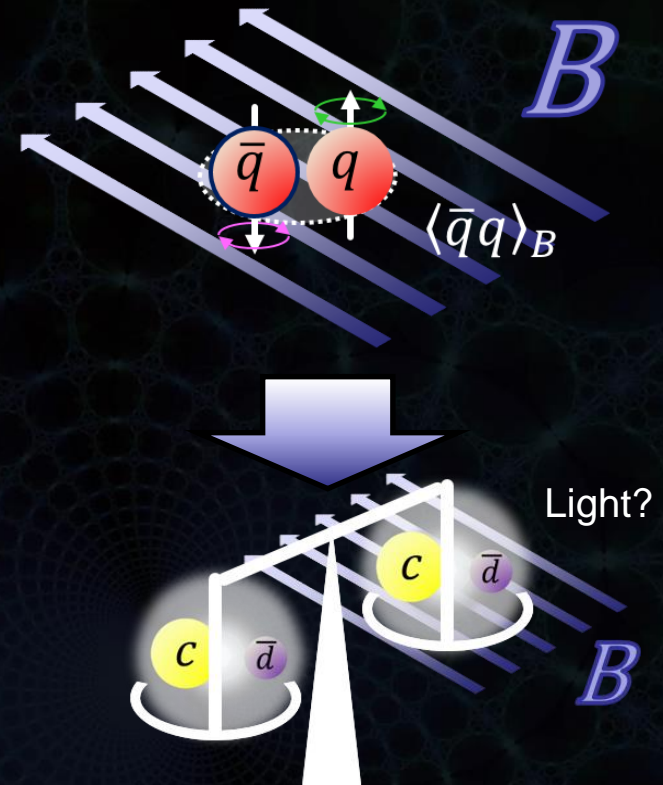


Nuclear matter reduces  $\langle \bar{q}q \rangle$



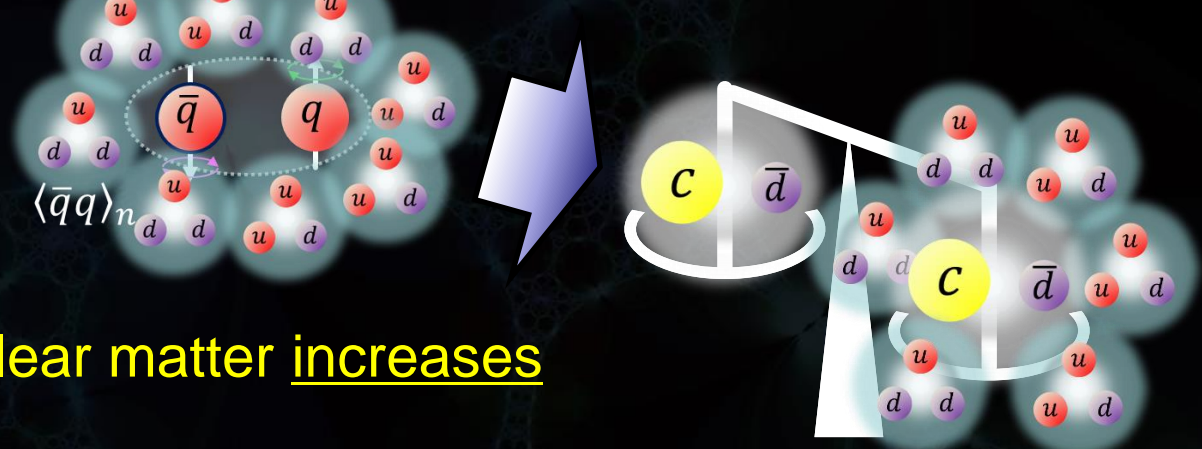
QCD sum rule : KS-Gubler-Oka, PRC93, 045209 (2016)  
 Quark model : Park-Gubler-Harada-Lee-Nonaka-Park, PRD93, 054035 (2016)

Magnetic field enhances  $\langle \bar{q}q \rangle$



QCD sum rule : Gubler-Hattori-Lee-Oka-Ozaki-KS, PRD93, 054026 (2016)  
 Quark model : Yoshida-KS, arXiv:1607.04935

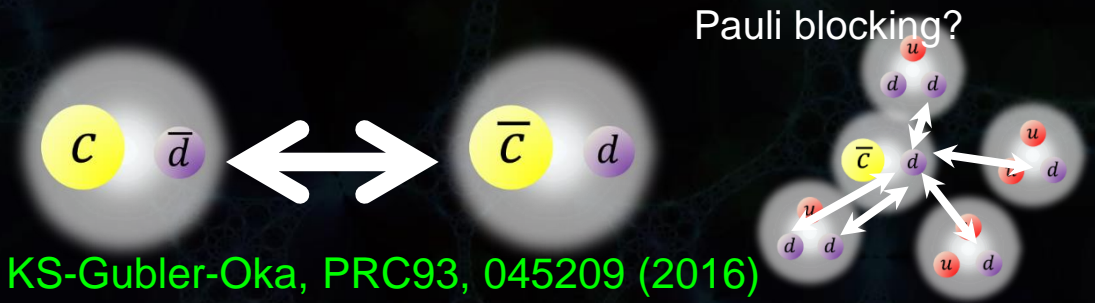
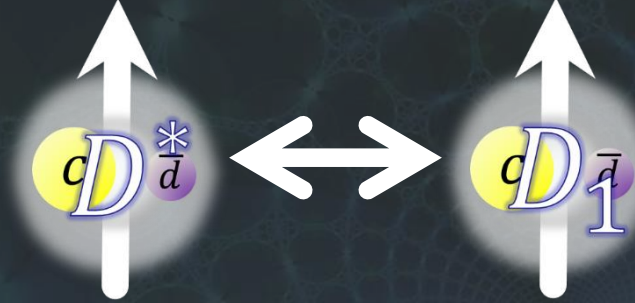
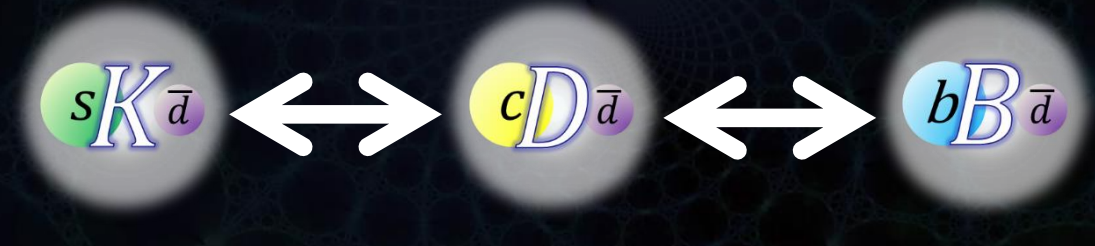
# Summary



D meson mass in nuclear matter increases by  $\chi$ SR !

<p>QCD sum rules</p>	<ul style="list-style-type: none"> <li>• D meson mass shift = density dependence of <math>m_c \langle \bar{q}q \rangle</math> diagram</li> <li>• Opposite sign to the chiral partner</li> </ul>
<p>Quark model</p>	<ul style="list-style-type: none"> <li>• <math>\chi</math>SR = smaller constituent quark mass</li> <li>• D meson mass shift = rest mass + kinetic and potential energies</li> </ul>

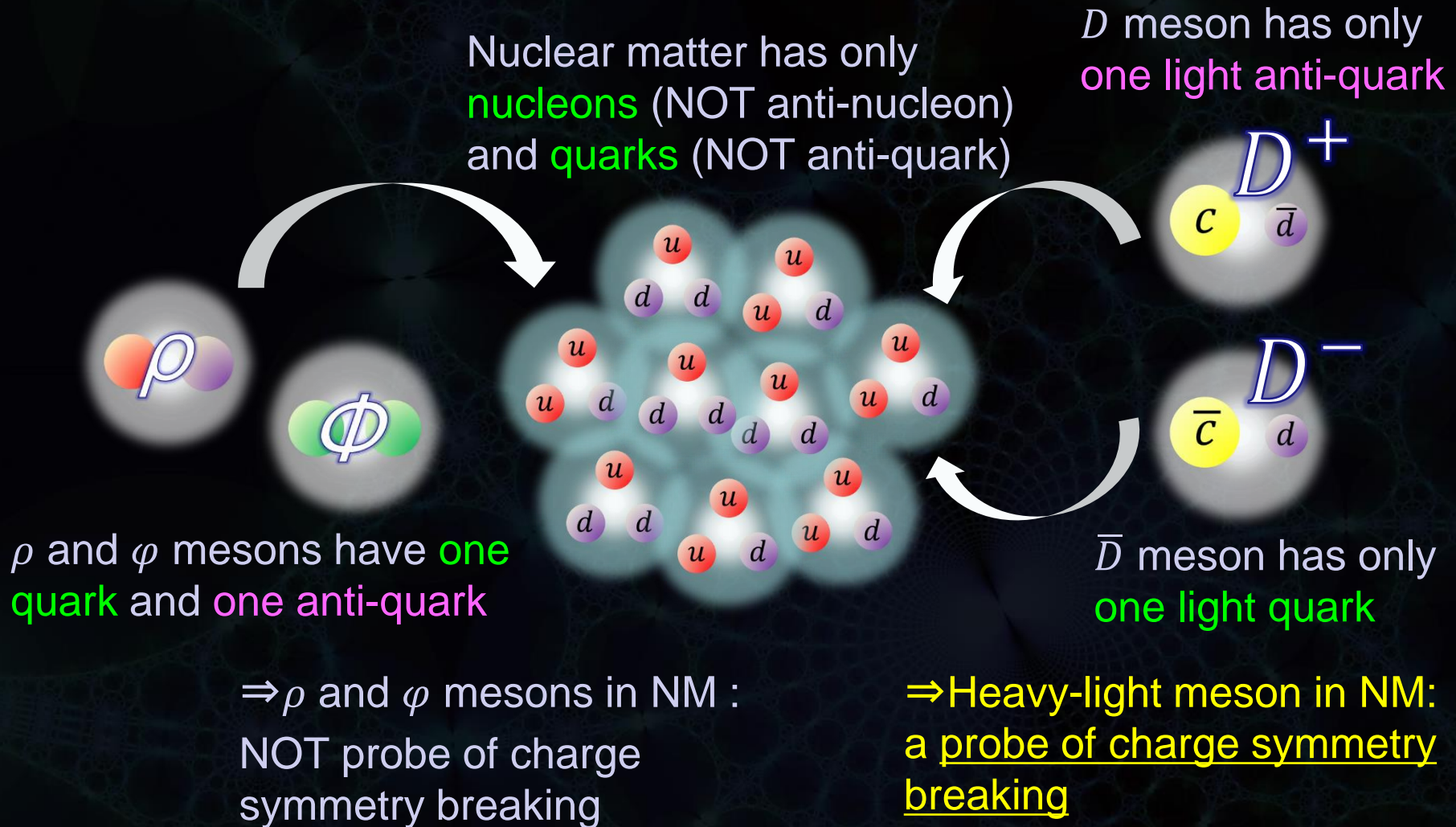
# Skipped topics in this talk are also interesting!

<p><math>D^+ - D^-</math> splitting (Charge symmetry breaking)</p>	 <p>Pauli blocking?</p> <p>KS-Gubler-Oka, PRC93, 045209 (2016)</p>
<p><math>D^* - D_1</math> in matter (Vector-Axialvector Chiral partners)</p>	
<p><math>K - D - B</math> in matter (Other heavy-light mesons)</p>	

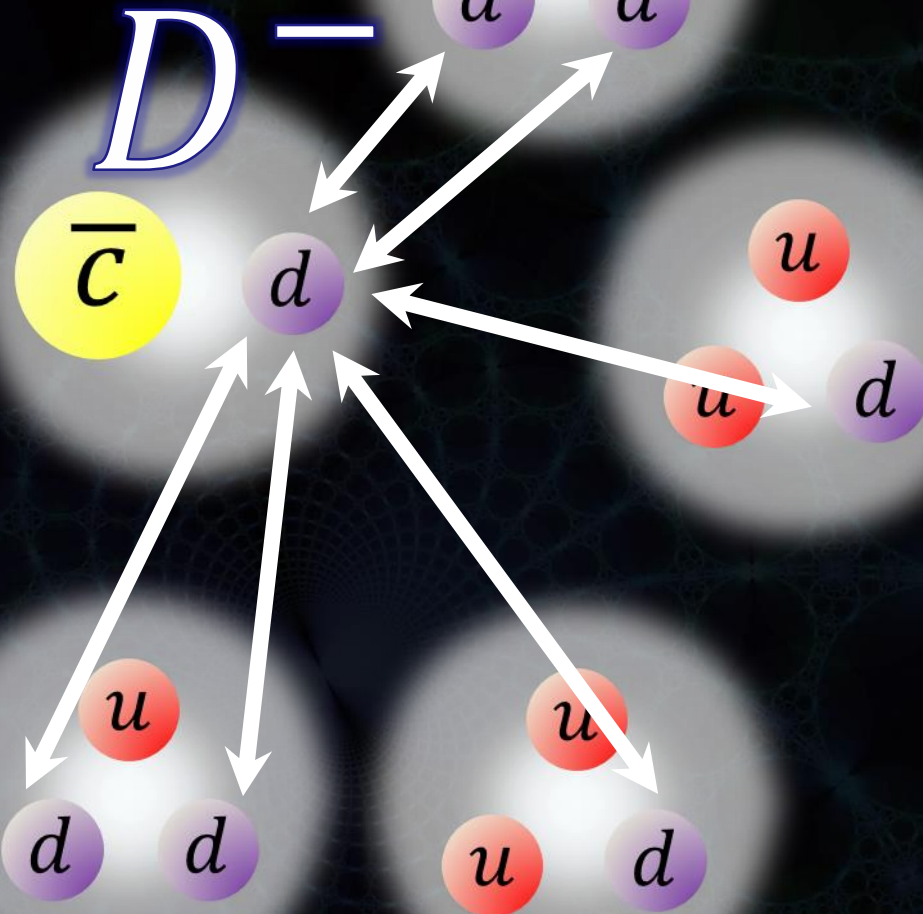
# Backup



# Charge Symmetry Breaking = imbalance b/w **particle** and **anti-particle**

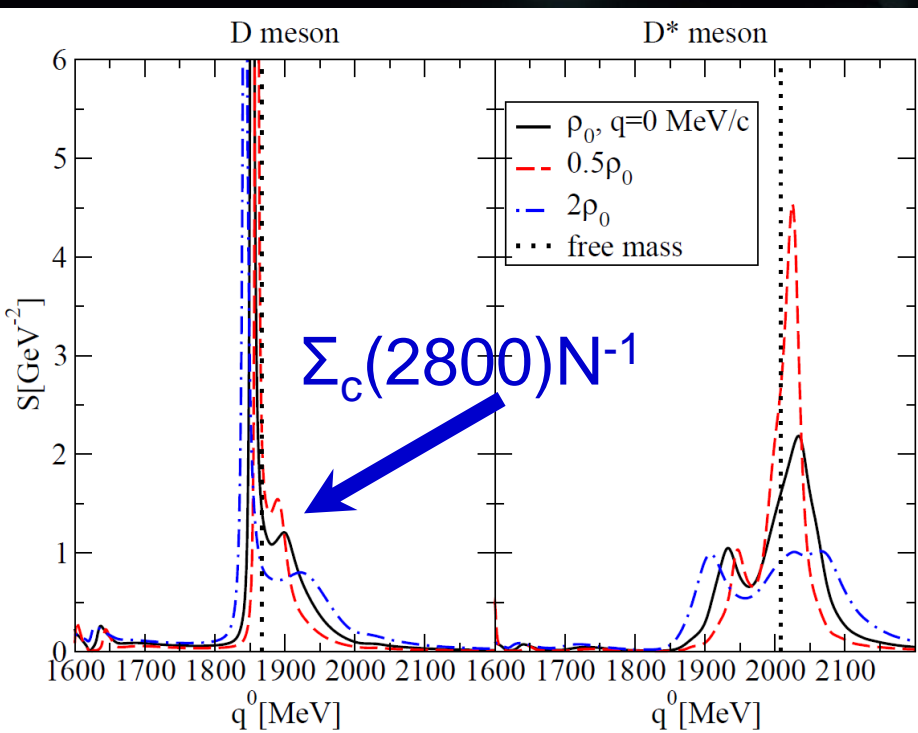
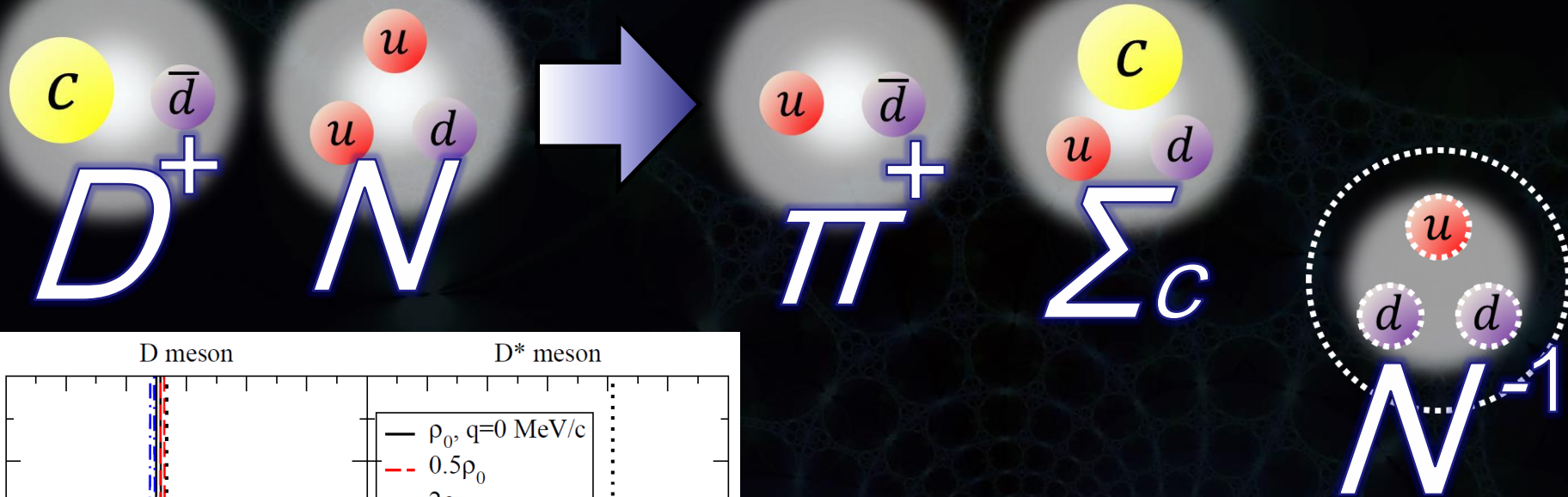


# Ex. Quark Pauli blocking



Only  $D^-$  feels repulsive forces from Pauli effect  
 $\Rightarrow$  positive mass shift

# Ex2. $Y_c$ - $N^{-1}$ excitation



Only  $D^+$  forms excitation from a charmed baryon and a nucleon hole

$\Rightarrow$  Spectral function is deformed

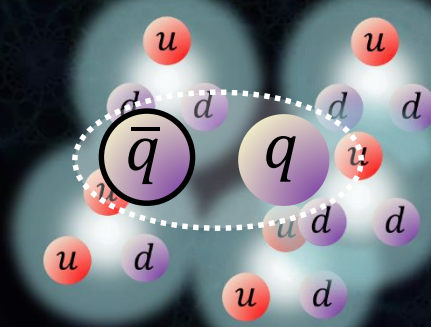
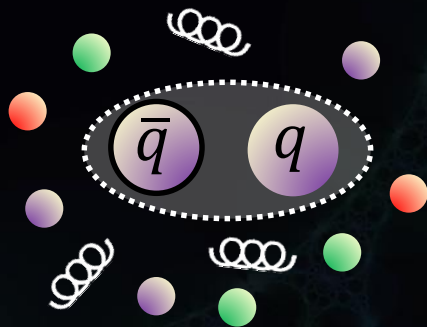
L. Tolos, C. Garcia-Recio, J. Nieves  
 Phys.Rev. C80 (2009) 065202

# QCD sum rules in medium

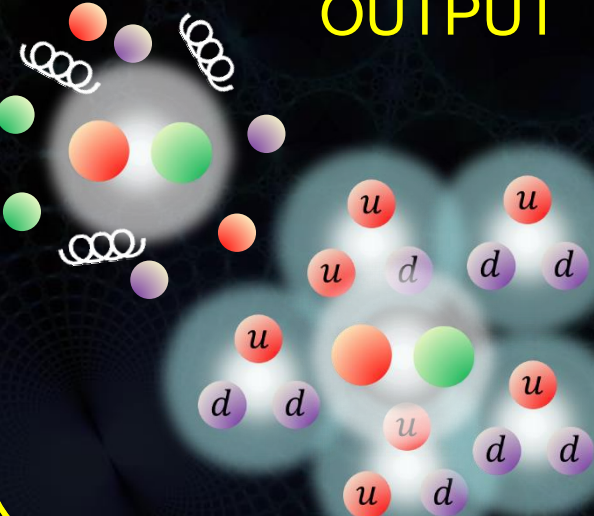
$$\Pi_{\text{OPE}}(M^2) = \int_0^\infty K(s, M^2) \rho(s) ds$$

## Medium modification of OPE INPUT

T- depend. (ex. in hot  $\pi$  gas, QGP)      density depend. (ex. in nuclear matter)



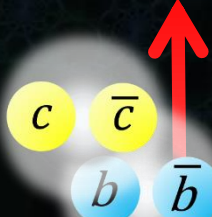
## Hadron modification OUTPUT



⇒ QCD sum rule relates modification of OPE (or condensate) to modification of hadron state

# Applications of QCD sum rules in external field

$T$

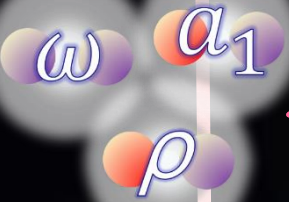


Furnstahl-Hatsuda-Lee '90  
Morita-Lee '08  
Gubler-Morita-Oka '10

Probe of J/psi suppression  
(T-dep. of gluon condensate)

Diagram illustrating the probe of J/psi suppression, showing a central  $c\bar{c}$  pair (yellow circles) surrounded by gluons (wavy lines) and other quarks (colored circles).

Bochkarev-Shaposhnikov '86  
Hatsuda-Koike-Lee '93



$\rho$ - $a_1$  mixing in  $\pi$  gas

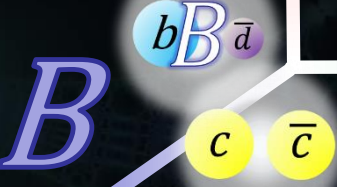
Diagram illustrating  $\rho$ - $a_1$  mixing in  $\pi$  gas, showing  $\rho$  and  $a_1$  mesons interacting with  $\pi$  mesons.

Probe of  $\chi$ SB restoration  
( $\mu$ -dep. of chiral condensate,  
4-quark con., s-bar s con.)

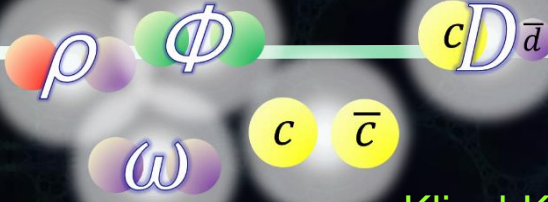
Diagram illustrating the probe of  $\chi$ SB restoration, showing a  $\rho$  meson (orange and purple circles) interacting with a 4-quark condensate (u, d quarks) and s-bar s condensate.

Machado et al. '14

Hatsuda-Lee '92



Hayashigaki '00  
Hilger-Thomas-Kampfer '08



Klingl-Kim-Lee-Morath-Weise '99

Cho-Hattori-Lee-Morita-Ozaki '14

$B$

$\mu$

# QCD sum rules in nuclear matter

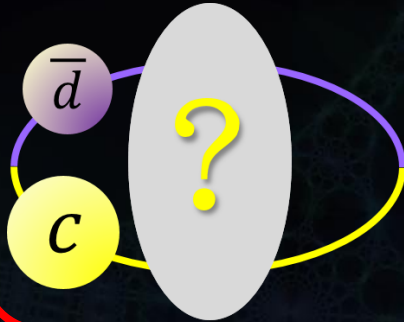
QCD sum rule

$$\Pi_{\text{OPE}}(M) = \int_0^\infty K(s, M) \rho(t) ds$$

② Kernel

Weight of spectral function  
• Gaussian sum rule

① OPE



• dens.-dependence  
of condensates up to  
dim.5

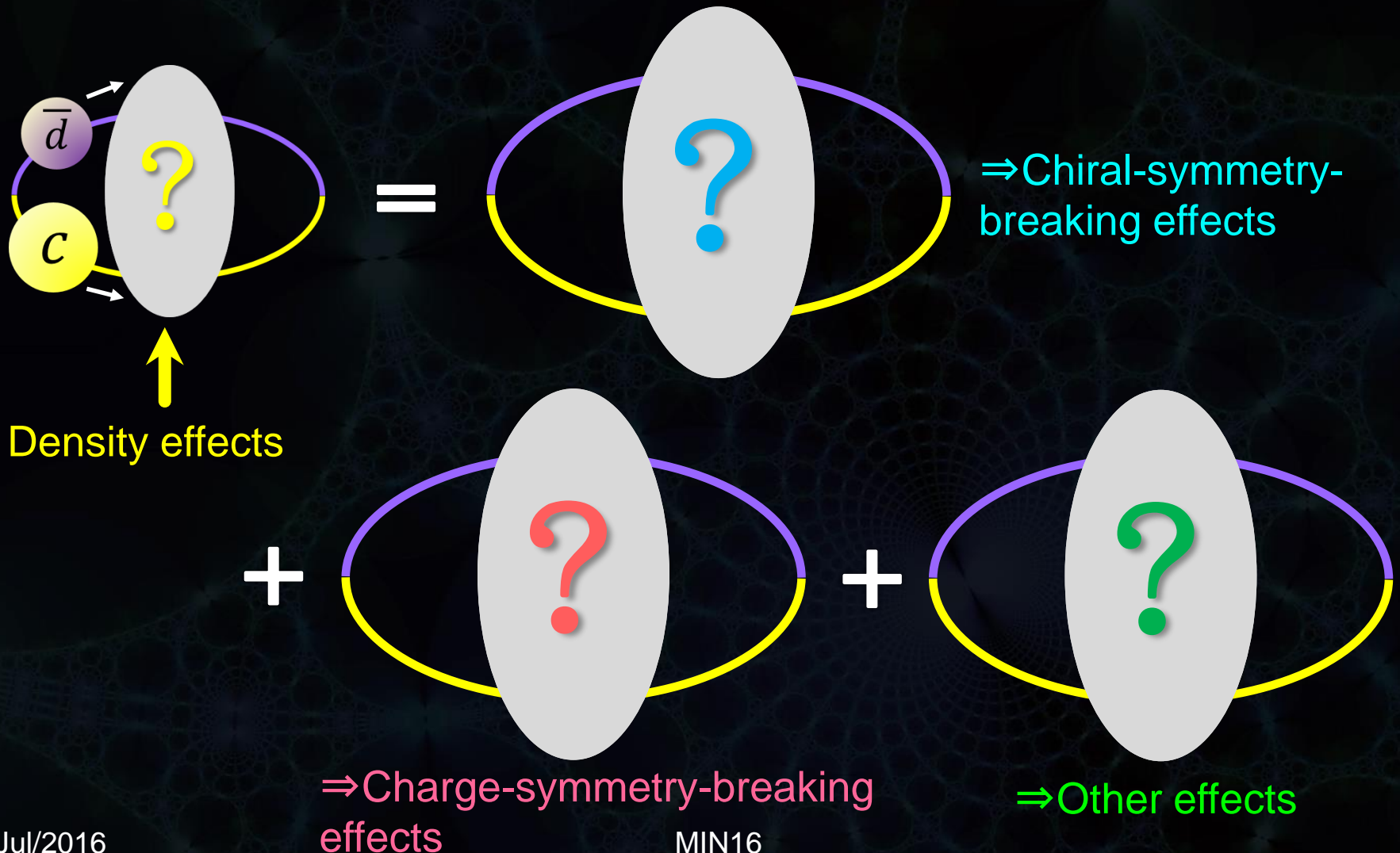
③ Output spectral function

- Maximum entropy method (MEM)  
P. Gubler and M. Oka, PTP124 (2010) 995
- Charge-conjugate projection  
cf.) D. Jido, N. Kodama, and M. Oka,  
PRD54, 4532 (1996)

cf.) A. Hayashigaki, PLB487 (2000) 96

T. Hilger, R. Thomas, B. Kampfer, PRC79 (2009) 025202

In QCD sum rules, we can separate all the **density effects** into QCD condensates



# In QCD sum rules, we can separate all the **density effects** into QCD condensates

- Chiral-symmetry-breaking condensates

$\langle \bar{q}q \rangle_n = \langle \bar{q}q \rangle_{vac} + \frac{\sigma_N}{2m_q} n$	$\langle \bar{q}g\sigma Gq \rangle_n = \lambda^2 \langle \bar{q}q \rangle_n$
$\left[ \langle \bar{q}D_0^2 q \rangle_n - \frac{1}{8} \langle \bar{q}g\sigma Gq \rangle_n \right] = -\frac{3}{4} M_N^2 e_2^q(\mu^2) n$	

- Charge-symmetry breaking condensates

$\langle q^\dagger q \rangle_n = \frac{3}{2} n$	$\langle q^\dagger g\sigma Gq \rangle_n = (0.33 \text{ GeV}^2) n$	$\langle q^\dagger D_0^2 q \rangle_n = -\frac{1}{4} M_N^2 A_3^q(\mu^2) n + \frac{1}{12} \langle q^\dagger g\sigma q \rangle_n$
---	---	--

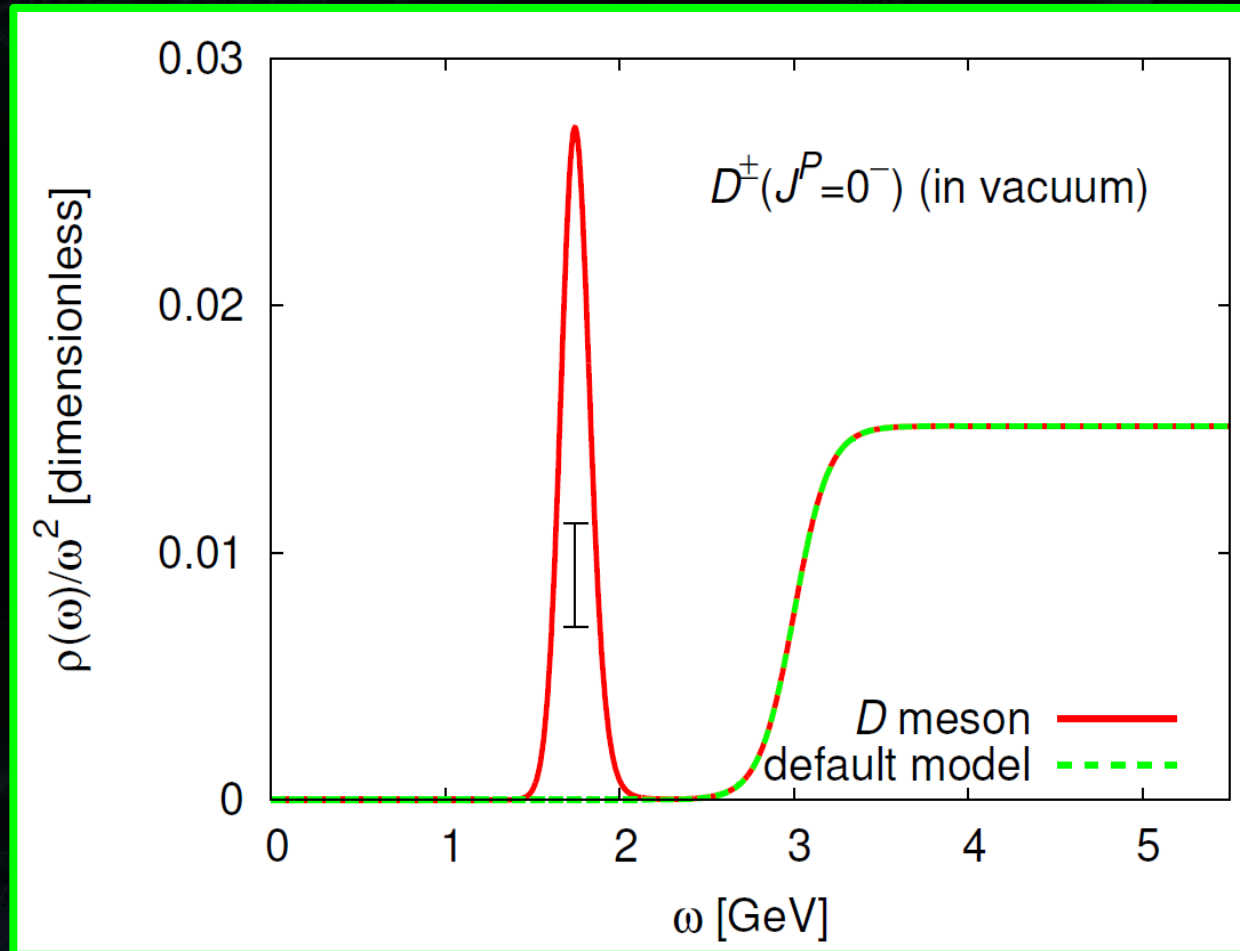
⇒ Opposite signs in particle and Anti-particle

- Other condensates (gluon condensate, twist condensates...)

$\langle \frac{\alpha_s G^2}{\pi} \rangle_n = \langle \frac{\alpha_s G^2}{\pi} \rangle_{vac} - \frac{8M_N^0}{9} n$	$\left\langle \frac{\alpha_s}{\pi} \left( \frac{(vG)^2}{v^2} - \frac{G^2}{4} \right) \right\rangle_n$	$\langle q^\dagger iD_0 q \rangle_n = \frac{3}{8} M_N A_2^q(\mu^2) n$
--	---	---

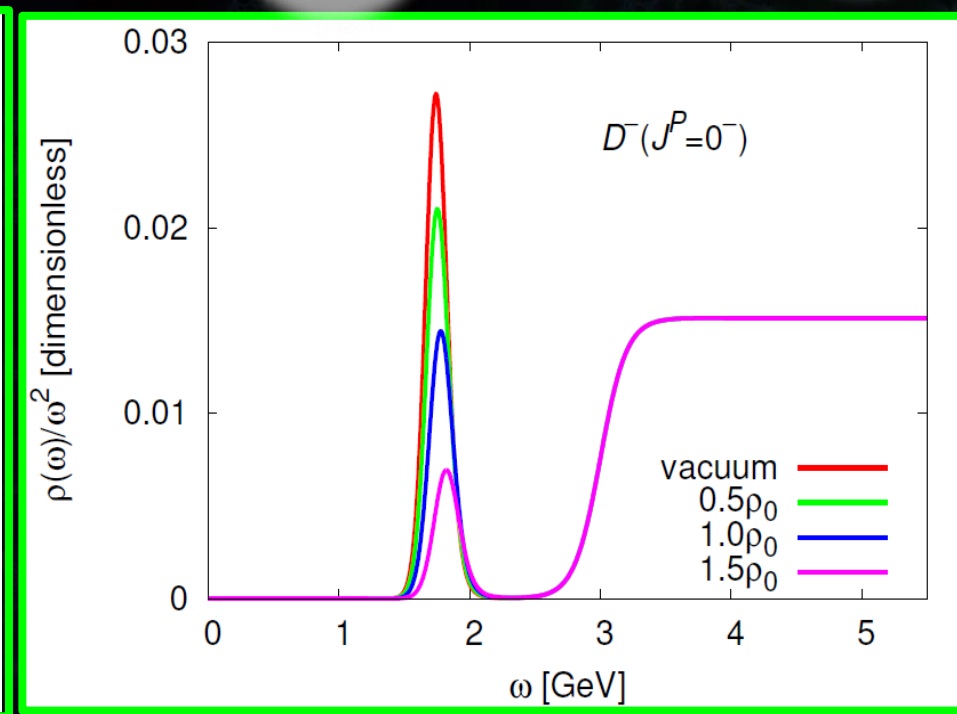
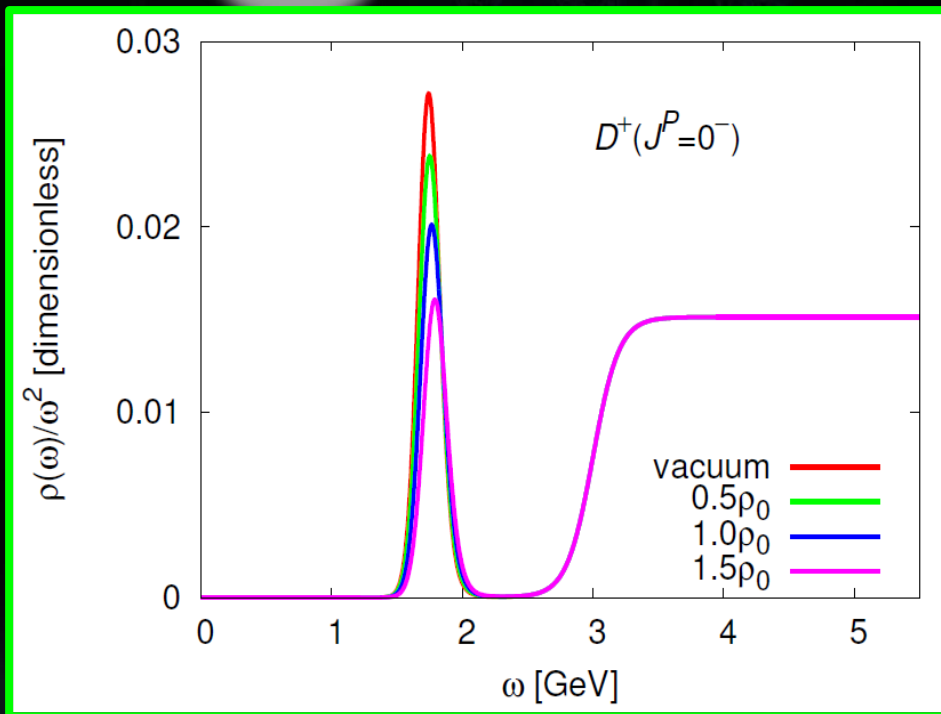
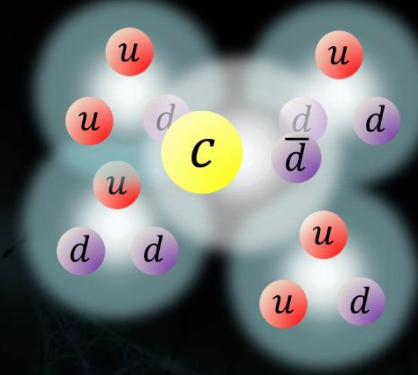


# D meson spectral function (in vacuum)





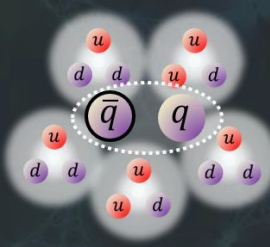
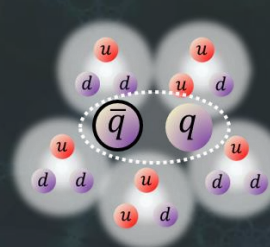
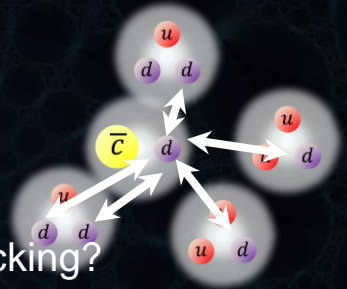
Mass : **1.75 GeV** Exp. : 1.87 GeV

# D meson spectral function (in nuclear medium)



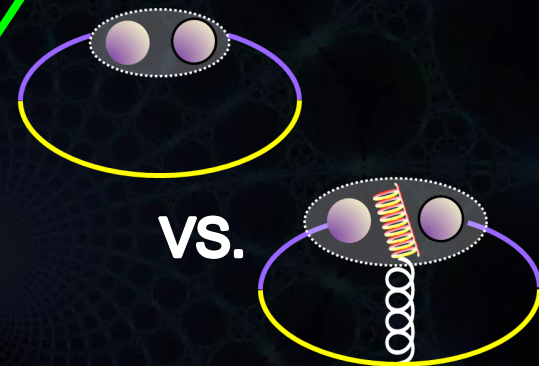
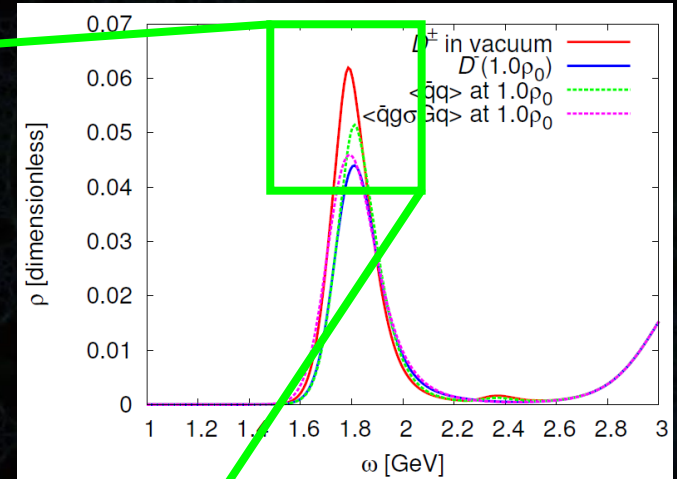
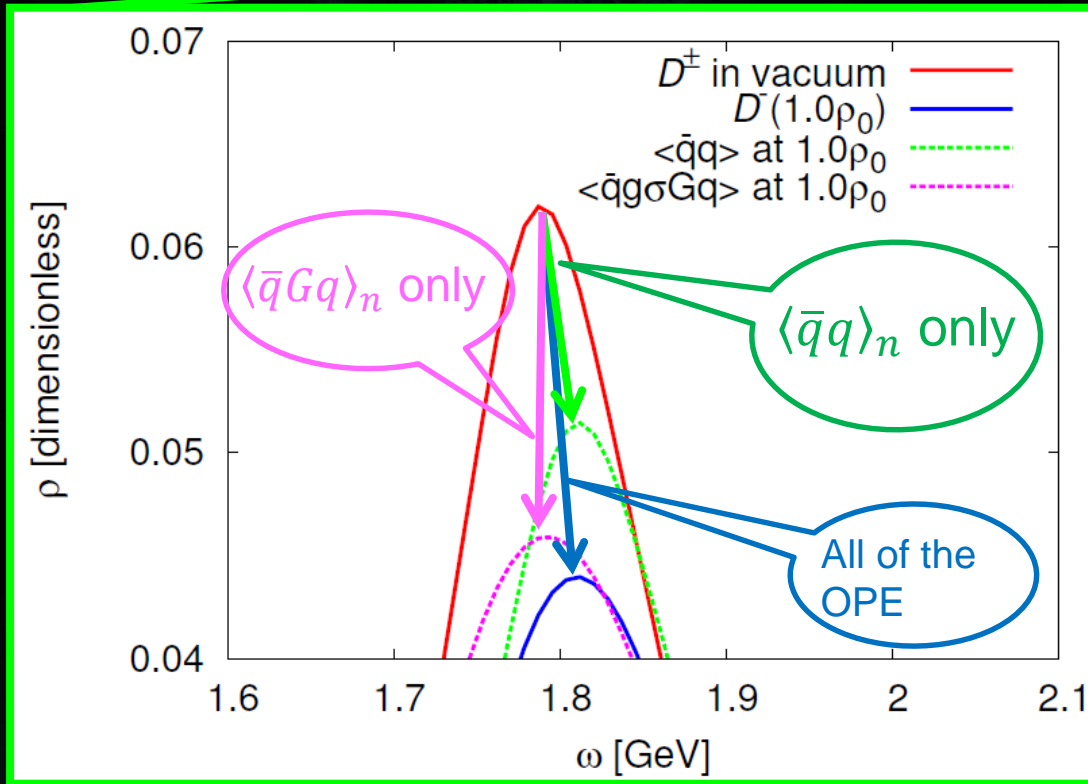
$\Rightarrow$  Peak position in  $D^\pm$  shifts to higher energy side with increasing density ( $D^+$ :  $\sim 25\text{MeV}$   $D^-$ :  $\sim 40\text{MeV}$  at  $\rho_0$ )

# Summary of **D meson** in nuclear matter

	D+ 	D- 
$\chi_{SR} = \langle \bar{q}q \rangle$ reduction	Increase $\uparrow\uparrow$ 	Increase $\uparrow\uparrow$ 
CSB effect	Decrease $\downarrow$	Increase $\uparrow$  Pauli blocking?
Our results	Increase $\uparrow$ (~25MeV)	More increase $\uparrow\uparrow$ (~40MeV)

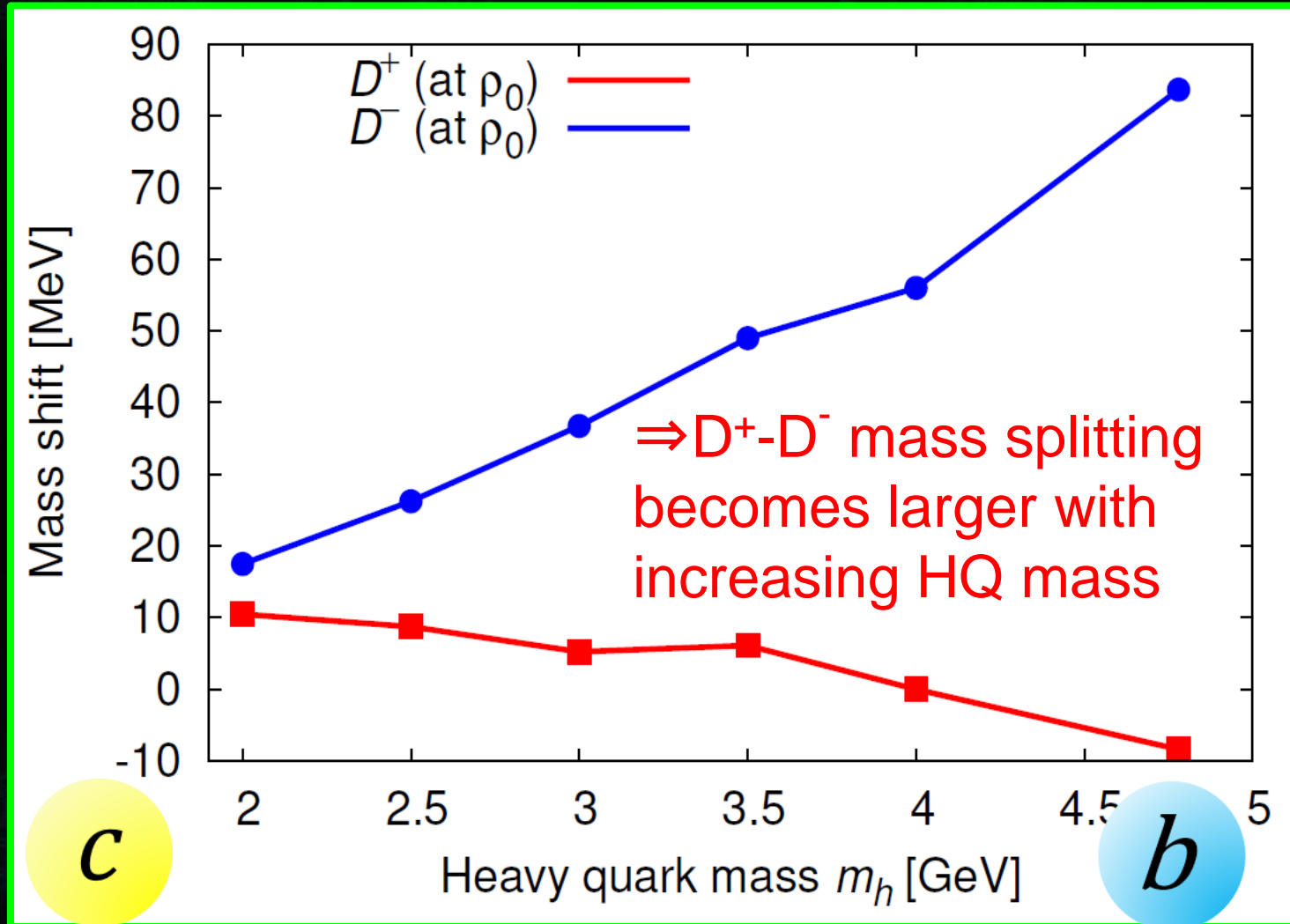
$\Rightarrow$  D meson is a good probe of  $\chi_{SR}$  and CSB

# Contributions of vacuum condensates



⇒ Positive mass shift of D meson is caused by Density dependence of chiral condensate

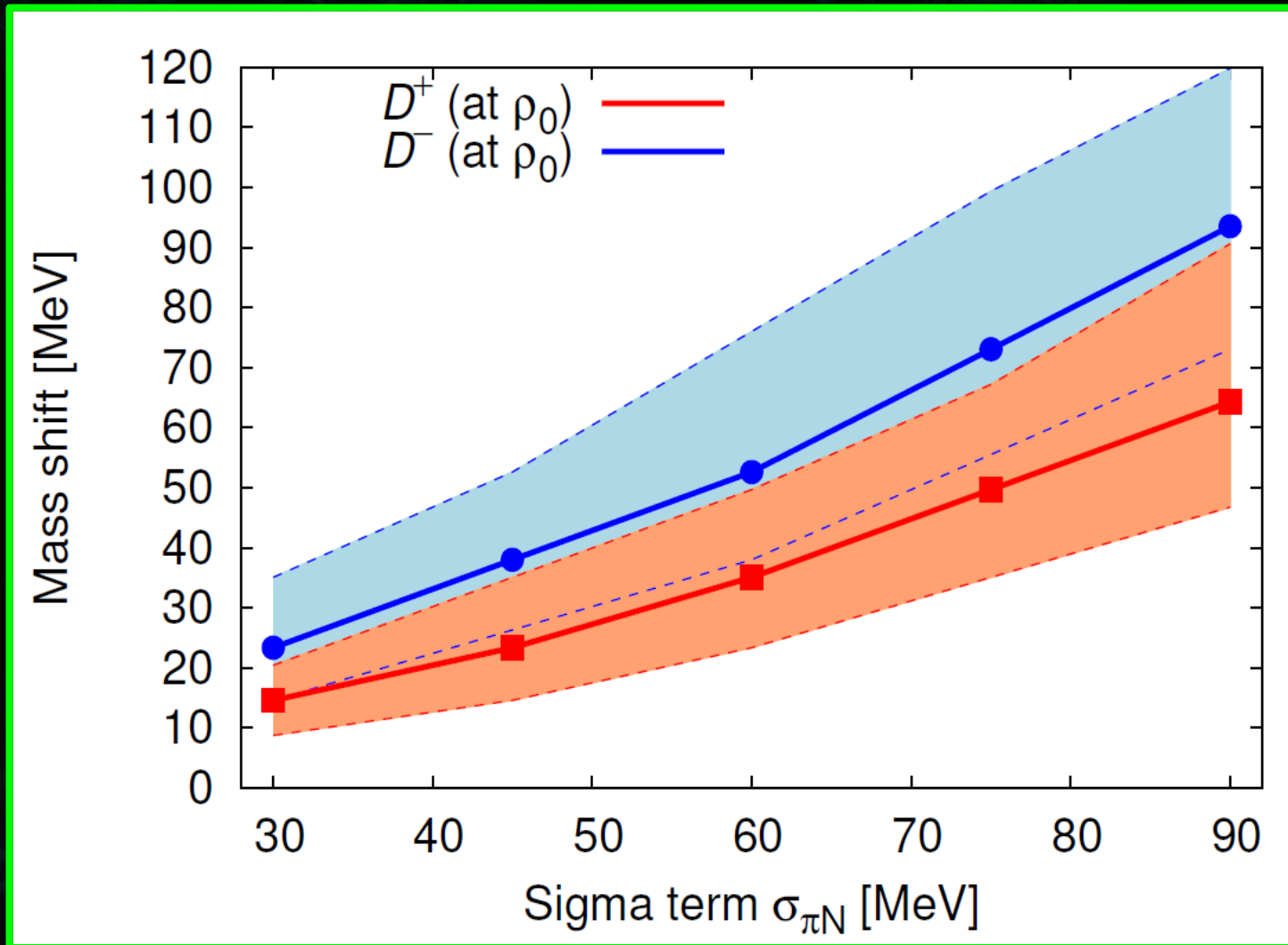
# Heavy quark mass dependence



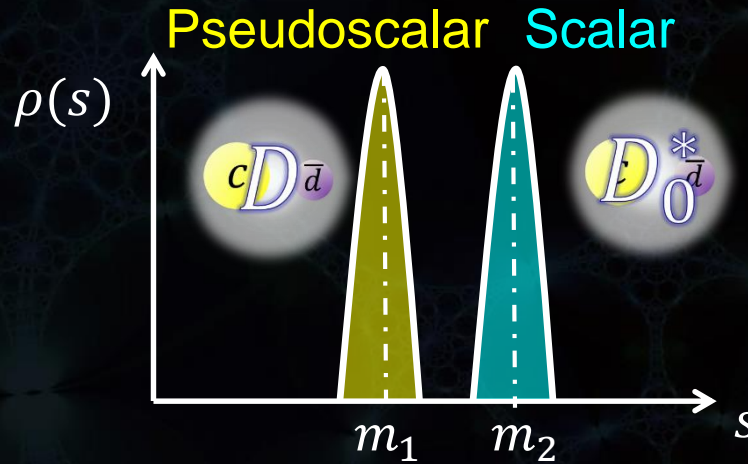
c

b

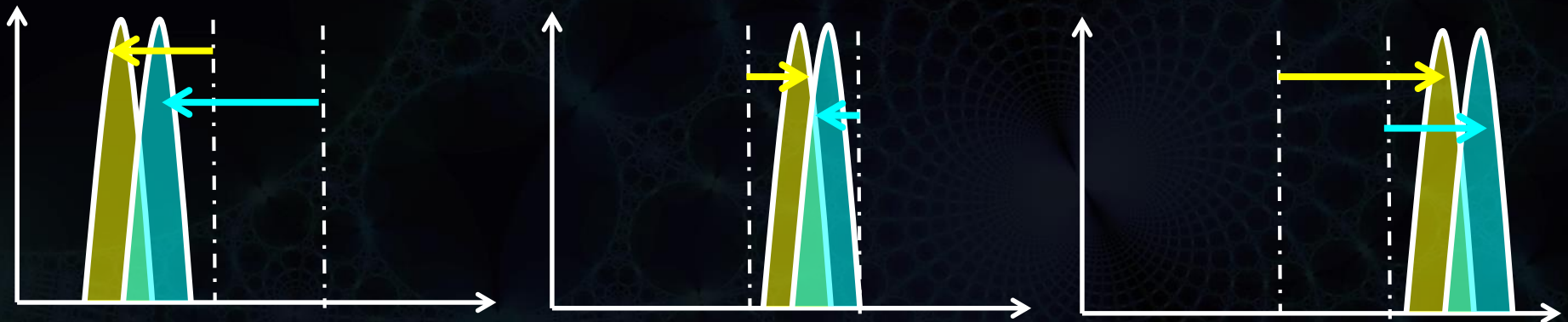
# Sigma term dependence



# 3 scenarios of chiral partners



1. Dropping degen. 2. Approaching degen. 3. raising degen.



⇒ Which pattern should be chosen?

# Chiral symmetric term

$$\begin{aligned}
 & i c \gamma_5 \bar{d} \left[ \frac{k^\mu \gamma_\mu + m_l}{k^2 - m_l^2} \right] \left[ \frac{q^\nu \gamma_\nu + m_c}{q^2 - m_c^2} \right] i \bar{c} \gamma_5 d = i c \bar{d} \left[ \frac{k^\mu \gamma_\mu + m_l}{k^2 - m_l^2} \right] \left[ \frac{-q^\nu \gamma_\nu + m_c}{q^2 - m_c^2} \right] i \bar{c} d \\
 & \quad \quad \quad \gamma_\mu \gamma_5 = -\gamma_5 \gamma_\mu \\
 & \quad \quad \quad \gamma_5^2 = 1
 \end{aligned}$$

$$\begin{aligned}
 & \stackrel{\text{Tr}[\gamma_\mu] = 0}{=} \frac{4kq - m_l m_c}{(k^2 - m_l^2)(q^2 - m_c^2)} \stackrel{m_l \rightarrow 0}{=} c \bar{d} \left[ \frac{k^\mu \gamma_\mu + m_l}{k^2 - m_l^2} \right] \left[ \frac{-q^\nu \gamma_\nu + m_c}{q^2 - m_c^2} \right] i \bar{c} d
 \end{aligned}$$



# Chiral breaking term

$\langle \bar{q}q \rangle$   
 $i c \gamma_5 \bar{d}$

$\frac{q^\nu \gamma_\nu + m_c}{q^2 - m_c^2}$

$i \bar{c} \gamma_5 d = i c \bar{d}$

$\langle \bar{q}q \rangle$   
 $i \bar{c} d$

$\frac{-q^\nu \gamma_\nu + m_c}{q^2 - m_c^2}$

$i \bar{c} d$

$\frac{-m_c \langle \bar{q}q \rangle}{q^2 - m_c^2}$

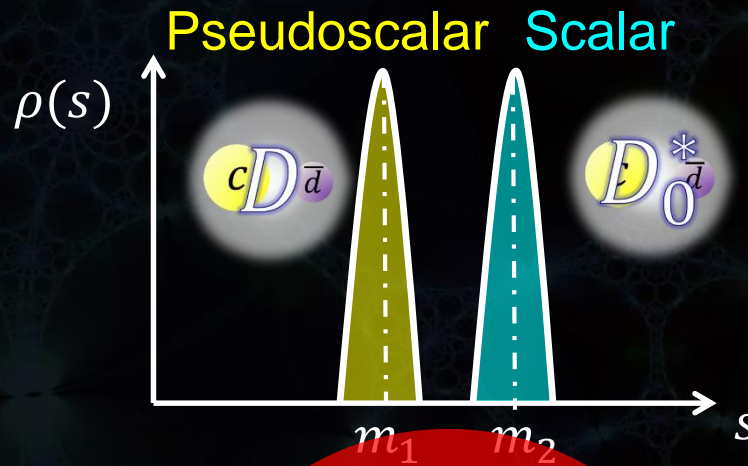
$c \bar{d}$

$\bar{c} d$

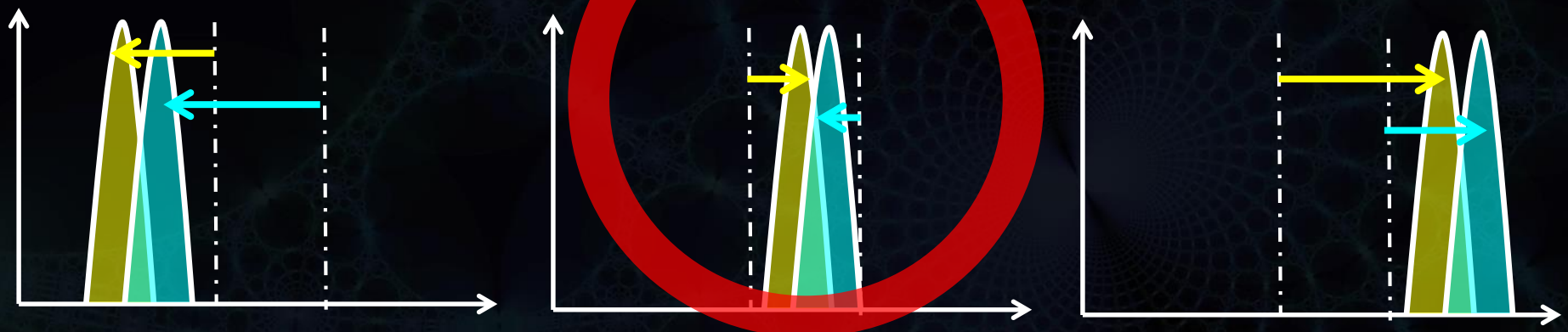
$\gamma_\mu \gamma_5 = -\gamma_5 \gamma_\mu$   
 $\gamma_5^2 = 1$

$Tr[\gamma_\mu] = 0$

# Conclusion from OPE



1. Dropping degen. 2. Approaching degen. 3. raising degen.



$\Rightarrow$  P mass increases and S mass decreases

# Many theoretical works for **D meson** in matter

## Coupled channel approach

- L. Tolos, J. Schaffner-Bielich, and A. Mishra, PRC70, 025203 (2004)
- M. Lutz and C. Korpa, PLB633, 43 (2006)
- T. Mizutani and A. Ramos, PRC74, 065201 (2006)
- L. Tolos, A. Ramos, and T. Mizutani, PRC77, 015207 (2008)
- L. Tolos, C. Garcia-Recio, and J. Nieves, PRC80, 065202 (2009)
- C. Jimenez-Tejero, A. Ramos, L. Tolos, and I. Vidana, PRC84, 015208 (2011)

## Mean field approach

- A. Mishra, E. Bratkovskaya, J. Schaffner-Bielich, S. Schramm, and H. Stoecker, PRC69, 015202 (2004)
- A. Mishra and A. Mazumdar, PRC79, 024908 (2009)
- A. Kumar and A. Mishra, PRC81, 065204 (2010)
- A. Kumar and A. Mishra, EPJ. A47, 164 (2011)

## Pion exchange model for $D\bar{N}$

- S. Yasui and K. Sudoh, PRC87, 015202 (2013)

## QMC model

- K. Tsushima, D.-H. Lu, A. W. Thomas, K. Saito, and R. Landau, PRC59, 2824 (1999)
- A. Sibirtsev, K. Tsushima, and A. W. Thomas, EPJ. A6, 351 (1999)

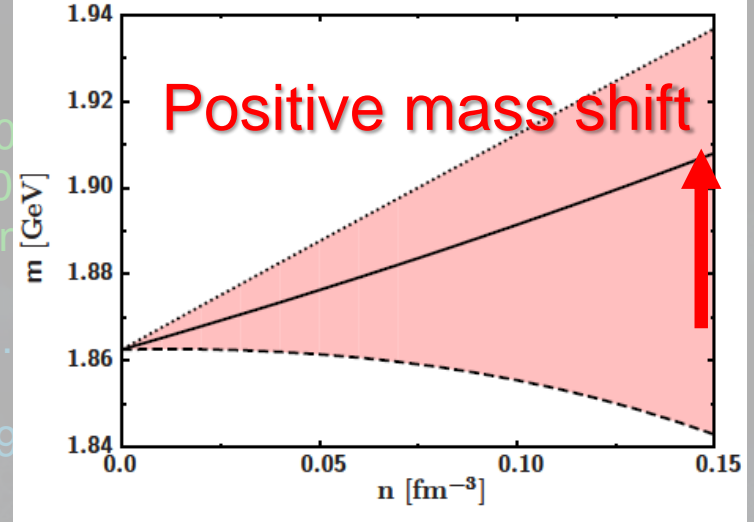
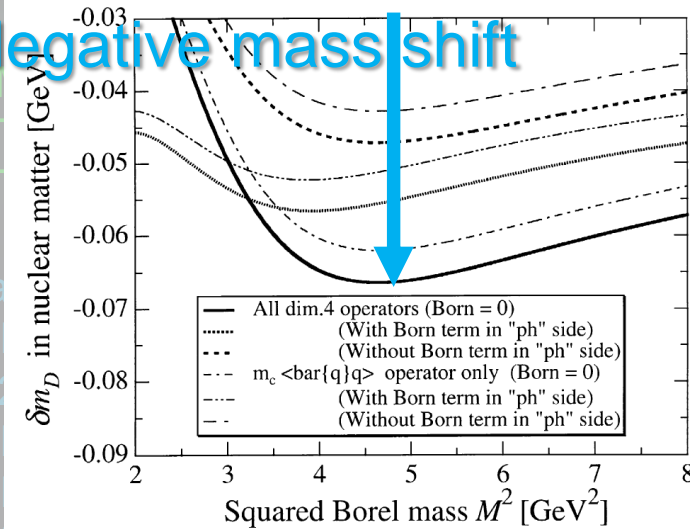
## QCD sum rules

- P. Morath, W. Weise, and S.-H. Lee (1999)
- A. Hayashigaki, PLB487, 96 (2000)
- T. Hilger, R. Thomas, and B. Kampfer, Phys. Rev. C79,025202 (2009)
- K. Azizi, N. Er, and H. Sundu, EPJ. C74, 3021 (2014)
- W.Z. Gang (2015) arXiv:1501.05093 [hep-ph]

# Many previous works for **D meson** in medium

## Coupled channel approach

### Negative mass shift



## Pion exchange model

S. Yasui and K. Sudoh, PRC87, 015202 (2013)

## QMC model

K. Tsushima, D.-H. Lu, A. W. Thomas, K. Saito, and R. Landau, PRC59, 2824 (1999)

A. Sibirtsev, K. Tsushima, and A. W. Thomas, EPJ A6, 351 (1999)

## QCD sum rules

P. Morath, W. Weise, and S.-H. Lee (1999)

A. Hayashigaki, PLB487, 96 (2000)

T. Hilger, R. Thomas, and B. Kampfer, Phys. Rev. C79,025202 (2009)

K. Azizi, N. Er, and H. Sundu, EPJ. C74, 3021 (2014)

W.Z. Gang (2015) arXiv:1501.05093 [hep-ph]

# What is difference between previous works? $\Rightarrow$ Borel window

1. Hayashigaki, PLB487, 96 (2000)

2. K. Azizi, N. Er, and H. Sundu, EPJ. C74, 3021 (2014)

3. W.Z. Gang (2015) arXiv:1501.05093 [hep-ph]

They applied relation to forward D-N scattering amplitude

As a result, they chose higher Borel window ( $1.7 < M < 2.8 \text{ GeV}$ )

$\Rightarrow$  They obtained Negative mass shift by chiral symmetry restoration

4. T. Hilger, R. Thomas, and B. Kampfer, Phys. Rev. C79,025202 (2009)

5. Our results

Hilger et al. applied Delta + step function ansatz

They chose lower Borel window ( $0.9 < M < 1.1 \text{ GeV}$ )

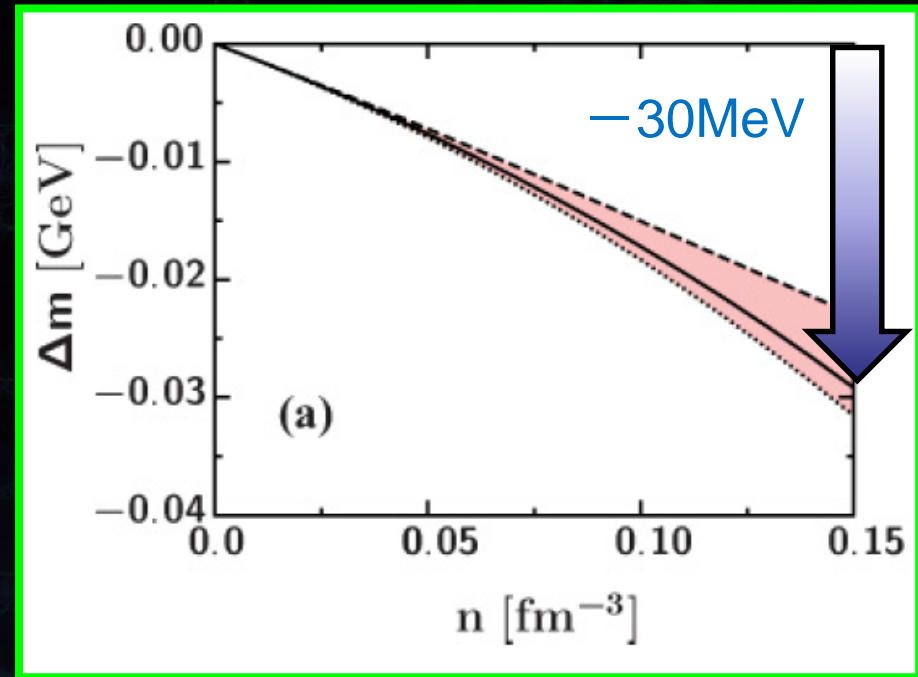
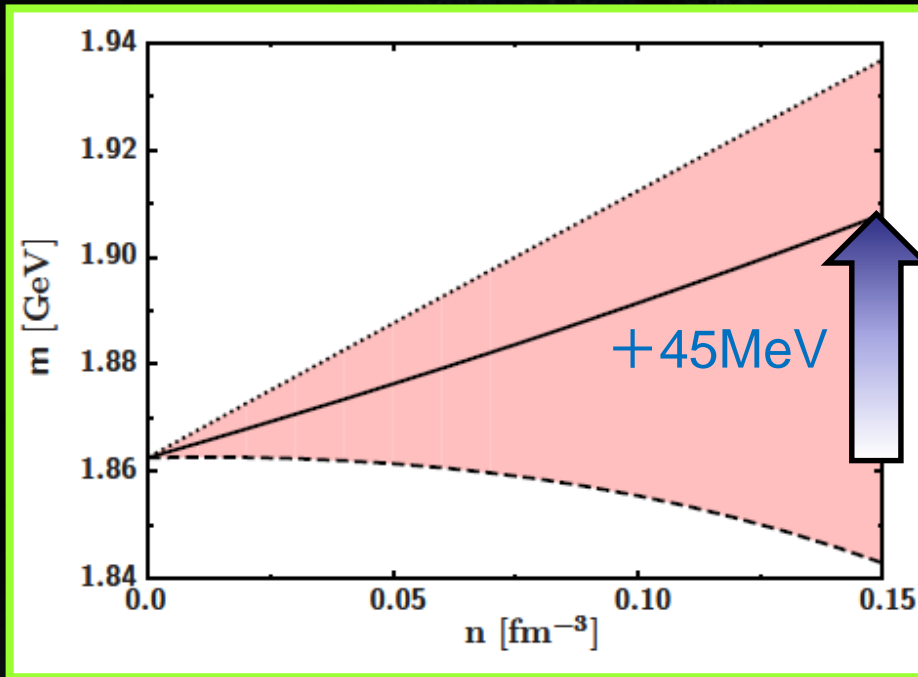
$\Rightarrow$  They obtained Positive mass shift by chiral symmetry restoration

# Previous works from QCD sum rules

4. T. Hilger, R. Thomas, and B. Kampfer, Phys. Rev. C79,025202 (2009)

Mass shift  $(\Delta m_{D^+} + \Delta m_{D^-})/2$

mass splitting  $(m_{D^+} - m_{D^-})/2$



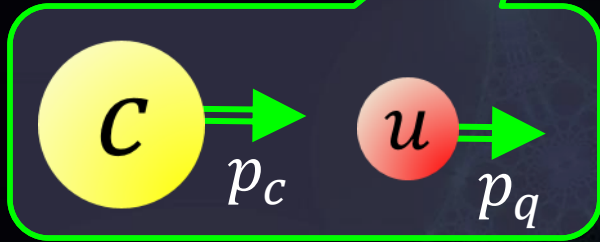
- These results depend on phenomenological parameter  
⇒ We need parameter independent analysis (=MEM)

# $m_q$ dependence of quark model for heavy-light meson

$$H = \frac{p_c^2}{2m_c} + \frac{p_q^2}{2m_q} + m_c + m_q + V(r)$$

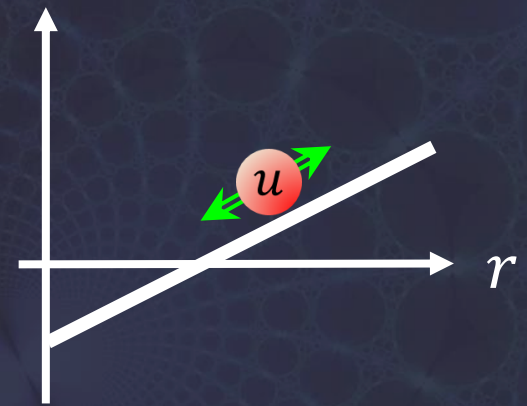
Kinetic term

Mass term



Linear potential

$$V(r) = \sigma r + C$$



When  $r \rightarrow 1/p_q$ ,

$$H = \frac{p_c^2}{2m_c} + \frac{p_q^2}{2m_q} + m_c + m_q + \frac{\sigma}{p_q} + C$$

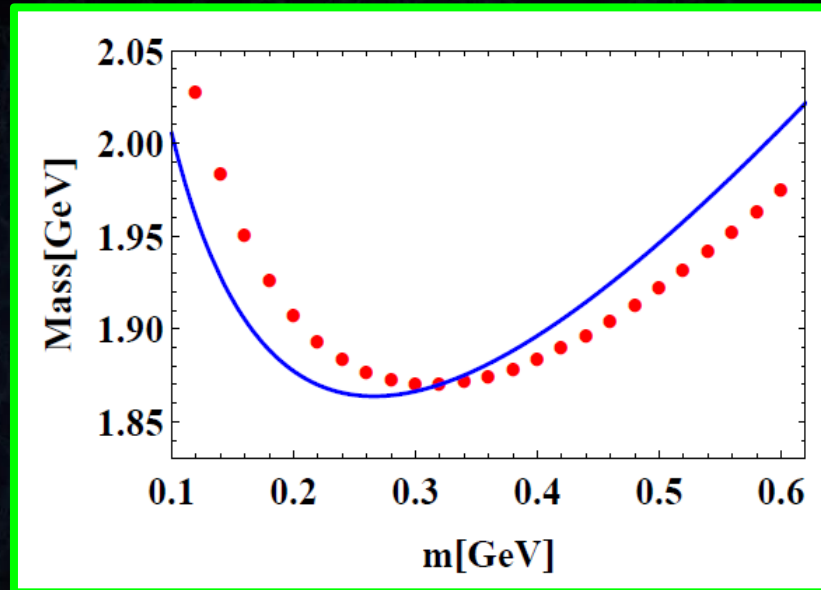
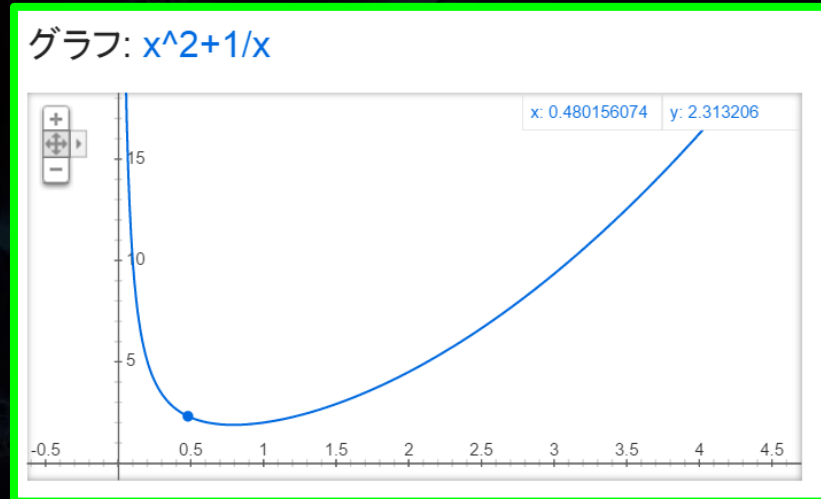
# $m_q$ dependence of quark model for heavy-light meson

$$H = \frac{p_c^2}{2m_c} + \frac{p_q^2}{2m_q} + m_c + m_q + \frac{\sigma}{p_q} + C$$

When  $p_q$  is minimized, we remove  $p_q$  and find  $m_q$ -depend. of the energy

$$E = \frac{p_c^2}{2m_c} + m_c + m_q + \left(\frac{\sigma^2}{m_q}\right)^{1/3} + C$$

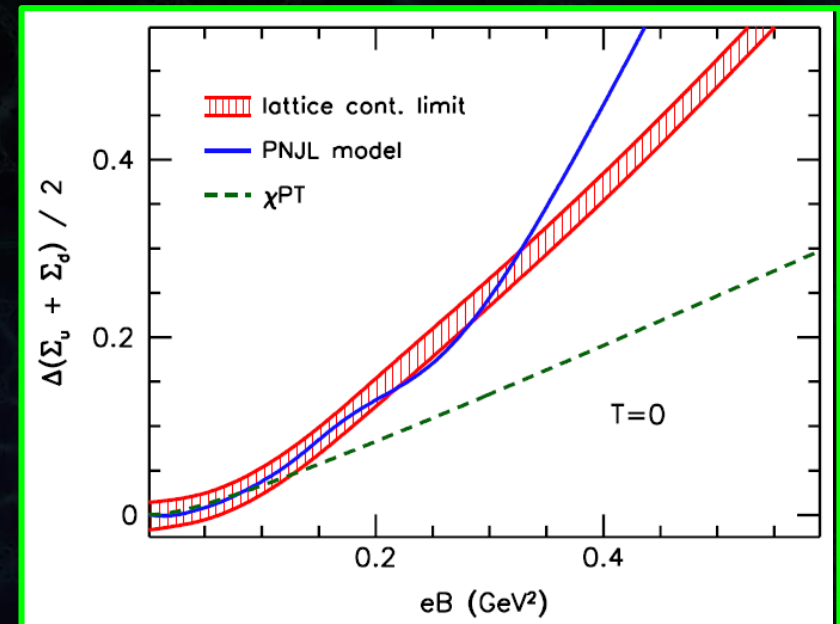
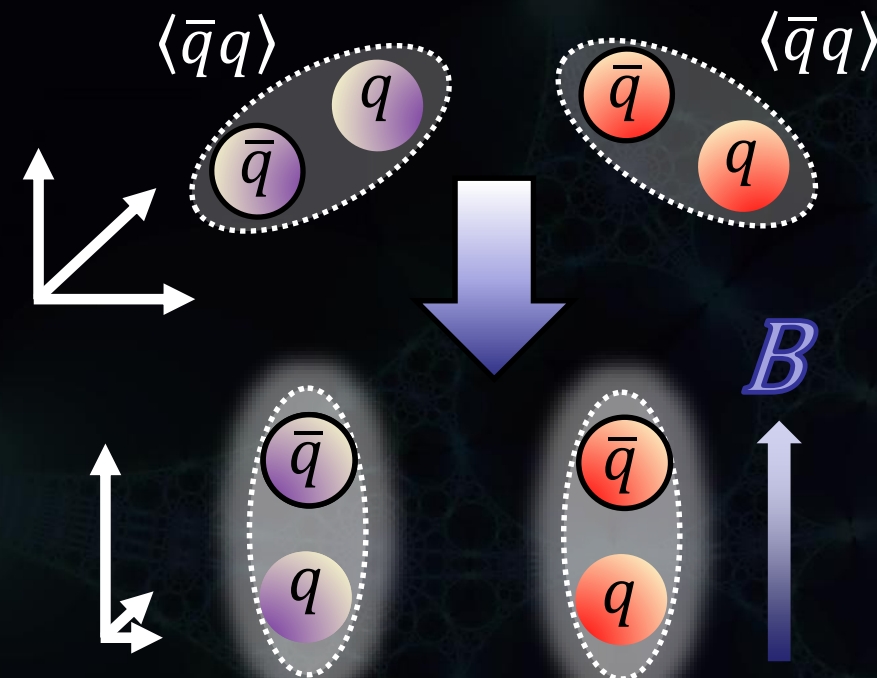
- There is a minimum of energy for a light quark mass  $m_q$
- If  $m_q$  decreases, D meson mass increases





# Magnetic Catalysis

- Charged particle is trapped in 1+1 dimension by magnetic field
- ⇒ chiral condensate is enhanced



G.S. Bali et al., PRD86 (2012) 071502

# Nonrelativistic two-body Hamiltonian in B-field

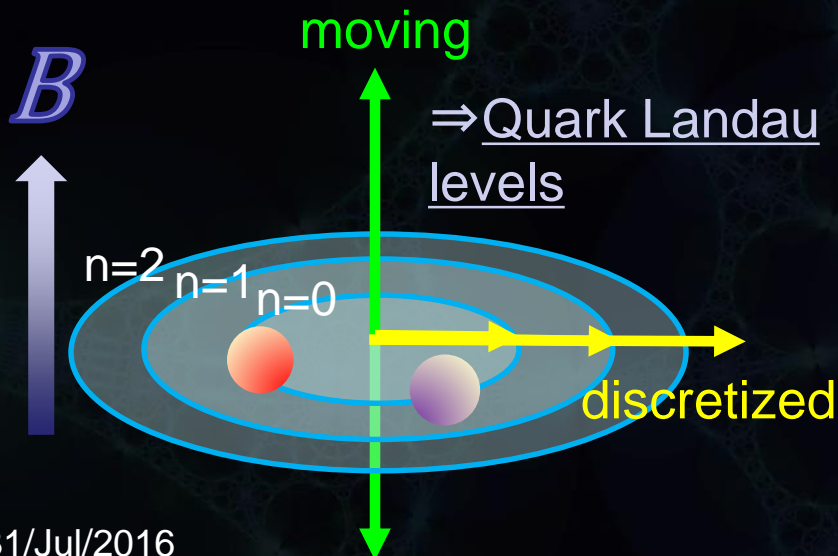
$$H = \sum_{i=1,2} \frac{1}{2m_i} (\mathbf{p}_i - q_i \mathbf{A})^2 - \boldsymbol{\mu}_i \cdot \mathbf{B} + m_i + V(r)$$

$$\mathbf{A} = \frac{1}{2} \mathbf{B} \times \mathbf{r}_i$$

Linear +  
Coulomb

(1) Modification of kinetic energy perpendicular to B

(2) Alignment of magnetic moment

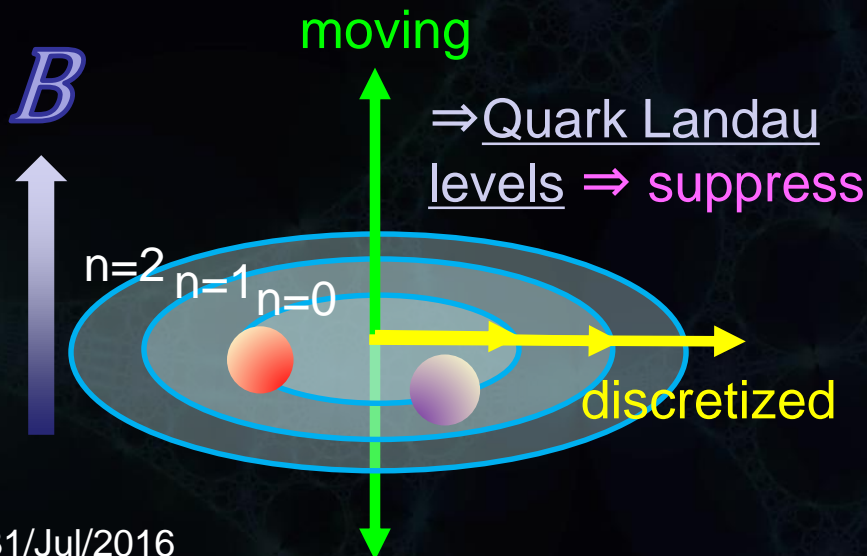


# $m_q$ dependence of quark model for heavy-light meson in B-field

$$H = \sum_{i=1,2} \frac{1}{2m_i} (\mathbf{p}_i - q_i \mathbf{A})^2 - \boldsymbol{\mu}_i \cdot \mathbf{B} + m_i + V(r)$$

$$\boldsymbol{\mu}_i = \frac{gq_i}{2m_i} \mathbf{S}_i$$

(1) Modification of kinetic energy perpendicular to B



(2) Alignment of magnetic moment



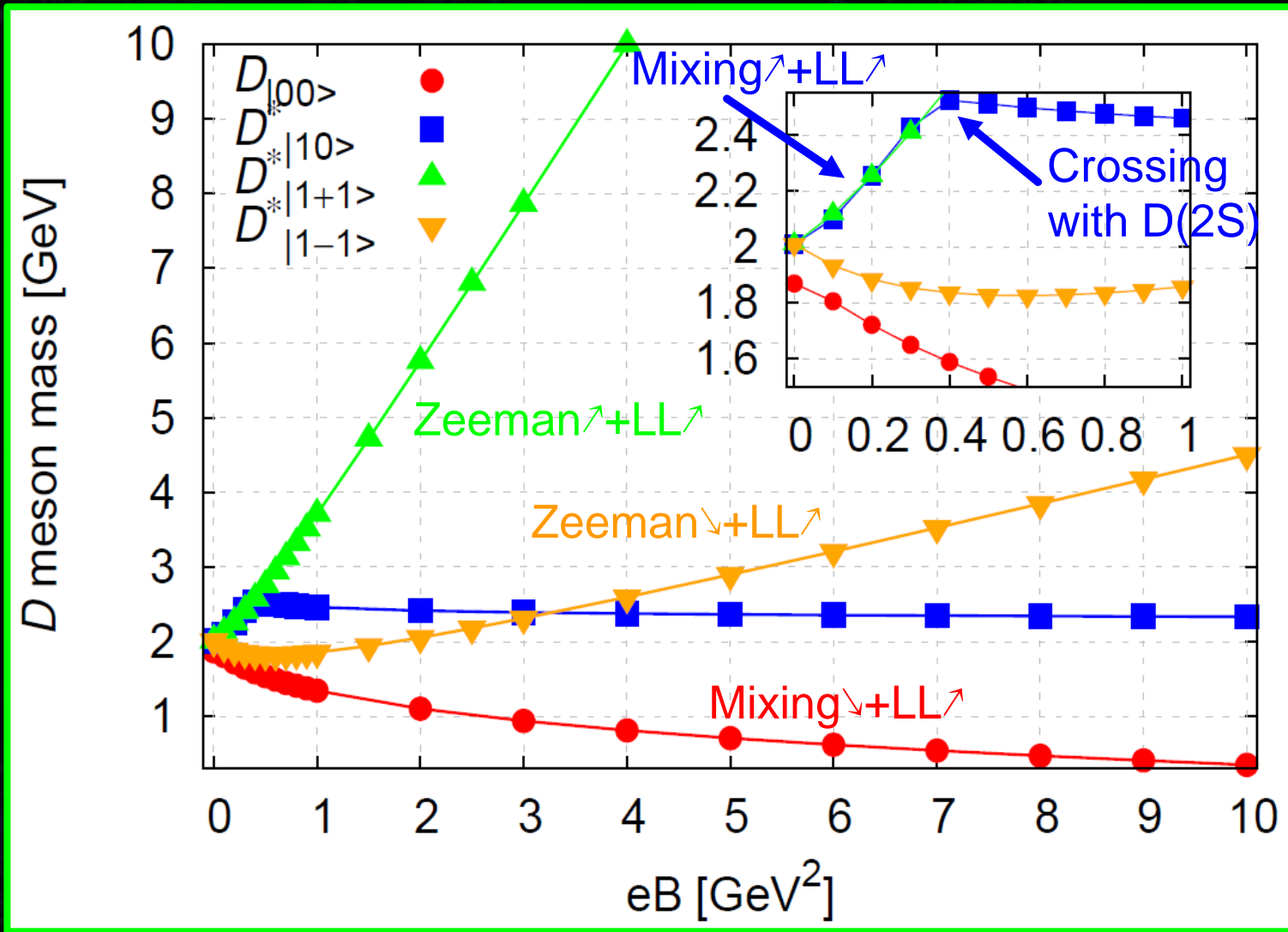
# $m_q$ dependence of quark model for heavy-light meson in B-field

$$H = \sum_{i=1,2} \frac{1}{2m_i} (\mathbf{p}_i - q_i \mathbf{A})^2 - \boldsymbol{\mu}_i \cdot \mathbf{B} + m_i + V(r)$$

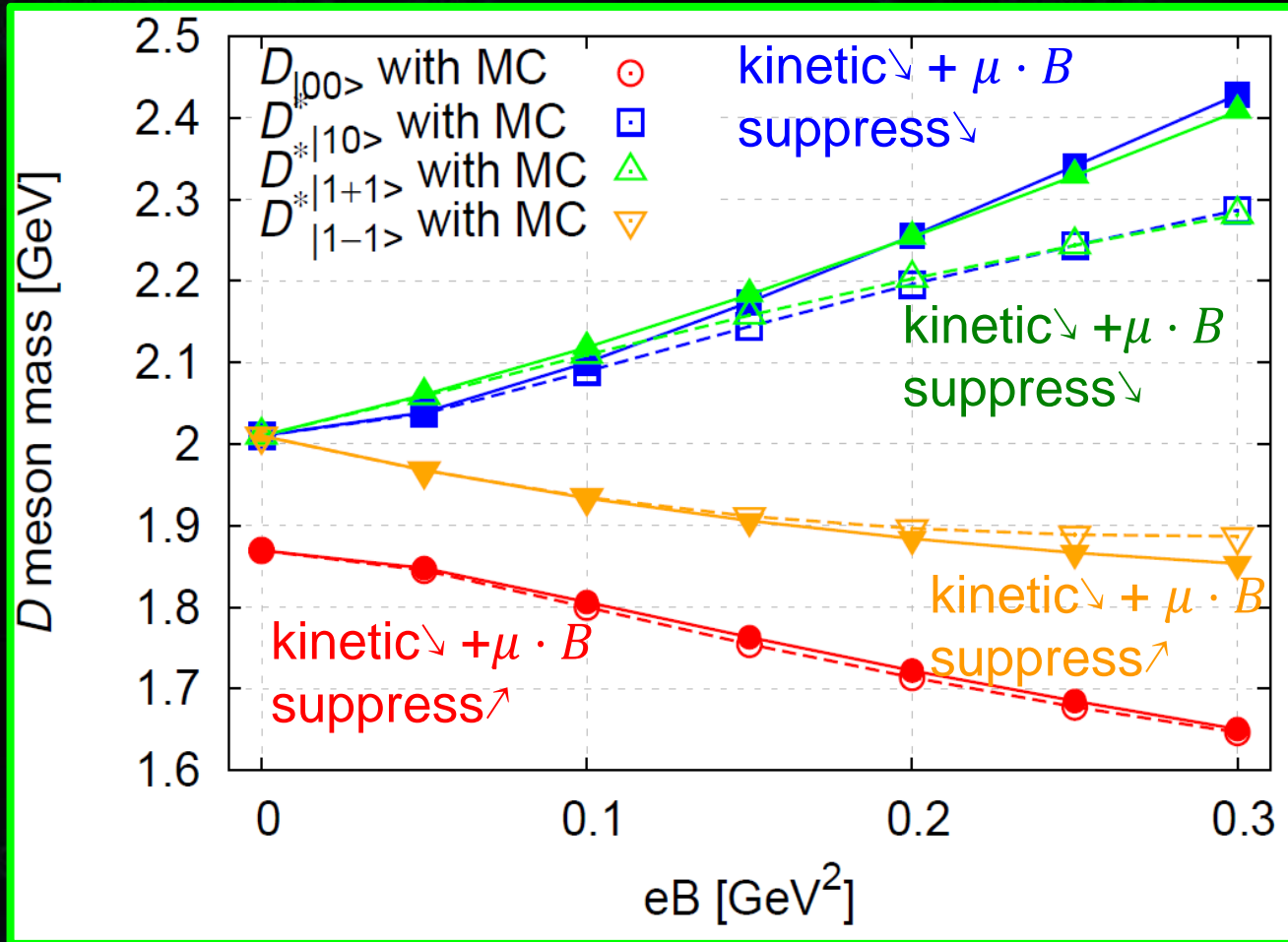
$$\boldsymbol{\mu}_i = \frac{gq_i}{2m_i} \mathbf{S}_i$$

⇒ D meson mass shift = rest mass increase  $\sim m_q$  + kinetic and potential energy suppression  $\sim 1/m_q$  + magnetic moment suppression  $\sim 1/m_q$

# $D$ meson mass in magnetic field w/o MC



# $D$ meson mass in magnetic field can probe $\langle \bar{q}q \rangle$ enhancement? (from quark model)



$\Rightarrow$  D meson : mass shift cancelation by  $\chi$ SB

$\Rightarrow$  D\* mesons : mass decrease by  $\chi$ SB