

THE INTERACTION AND RESONANCE STATES BETWEEN CHARMED BARYON AND NUCLEON

Saori Maeda

Makoto Oka

Tokyo Institute of technology

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- Summary

INTRODUCTION

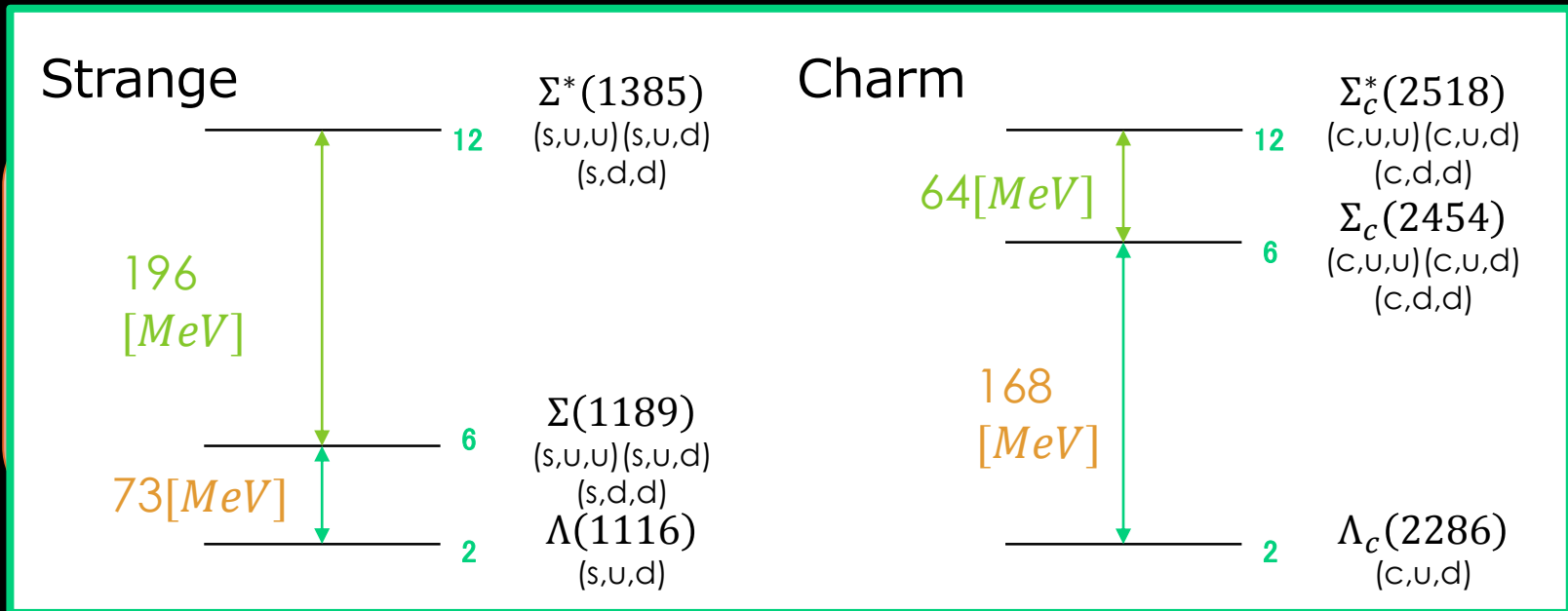
- We have obtained many experimental data related to hypernuclei and hyperon-nucleon (YN) interactions.

the next stage →

**Approaching to charm nuclei structure
with theoretical knowledge**

- Interesting properties of charm nuclei
 - Heavy quark symmetry
 - Channel coupling including higher state than strange sector.

INTRODUCTION



- Interesting properties of charm nuclei
- Heavy quark symmetry
- Channel coupling including higher state than strange sector.

$Y_c N$ INTERACTION

- $Y_c N$ potential ($Y_c = \Lambda_c, \Sigma_c, \Sigma_c^*$)

In this study, we construct a hybrid potential using a hadron model and a quark model

- One Boson Exchange potential [Y.R.Liu, M.Oka, Phys. Rev. D 85, 014015 (2012)]
- Quark Cluster Model [M.Oka, Nuclear Physics A 881 (2012) 6–13]

$$V_{(Y_c N)} = V_{OBEP} + V_{QCM}$$

- Channel coupling

Channels	1	2	3	4	5	6	7
$J^\pi = 0^+$	$\Lambda_c N(^1S_0)$	$\Sigma_c N(^1S_0)$	$\Sigma_c^* N(^5D_0)$				
$J^\pi = 1^+$	$\Lambda_c N(^3S_1)$	$\Sigma_c N(^3S_1)$	$\Sigma_c^* N(^3S_1)$	$\Lambda_c N(^3D_1)$	$\Sigma_c N(^3D_1)$	$\Sigma_c^* N(^3D_1)$	$\Sigma_c^* N(^5D_1)$

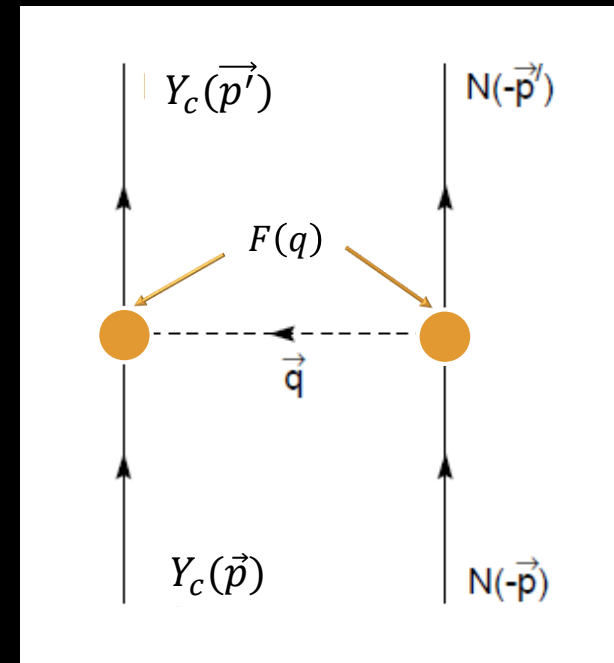
$Y_c N$ INTERACTION

- One Boson Exchange potential

We assume that the pion and the sigma meson exchange between the charm baryon and the nucleon.

At the vertices, we introduce the form factor $F(q)$ as follows

$$F(q) = \frac{\Lambda^2 - m^2}{\Lambda^2 - q^2}$$



$Y_c N$ INTERACTION

- One Boson Exchange potential

We assume that the pion and

$Y_c(\vec{n}')$ $N(-\vec{b}')$

$$V_\pi(i, j) = C_\pi(i, j) \frac{m_\pi^3}{24\pi f_\pi^2} \left\{ \langle \mathcal{O}_{spin} \rangle_{ij} Y_1(m_\pi, \Lambda_\pi, r) + \langle \mathcal{O}_{ten} \rangle_{ij} H_3(m_\pi, \Lambda_\pi, r) \right\}$$

$$V_\sigma(i, j) = C_\sigma(i, j) \frac{m_\sigma}{16\pi} \left\{ \langle 1 \rangle_{ij} 4Y_1(m_\sigma, \Lambda_\sigma, r) + \langle \mathcal{O}_{LS} \rangle_{ij} \left(\frac{m_\sigma}{M_N} \right)^2 Z_3(m_\sigma, \Lambda_\sigma, r) \right\}$$

$$F(q) = \frac{\Lambda^2 - m^2}{\Lambda^2 - q^2}$$

$Y_c(\vec{p})$ $N(-\vec{p})$

$Y_c N$ INTERACTION

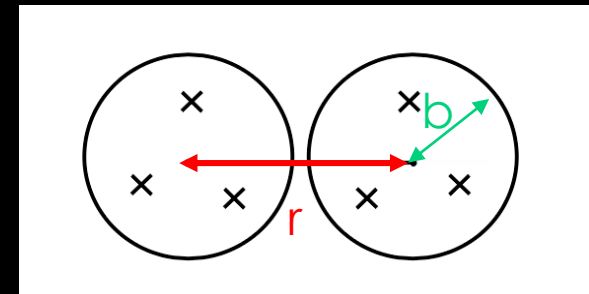
- Quark Cluster Model (QCM)

The QCM considers **two baryon clusters** each made of **three quarks**.

When two baryons overlap completely, $r=0$, all the six quarks occupy the lowest energy orbit with a single center.

Potential equation

$$V_{QCM} = V_0 e^{-\frac{r^2}{b^2}}$$



$Y_c N$ INTERACTION

- Quark Cluster Model (QCM)

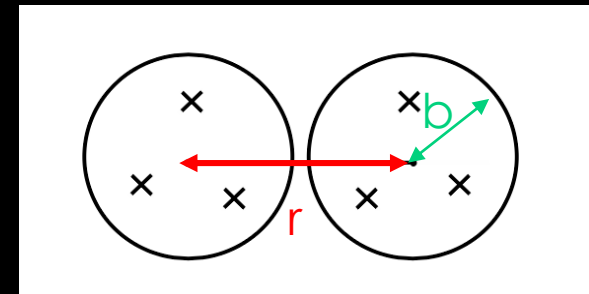
The QCM considers **two baryon clusters** each made of **three quarks**.

When two baryons overlap completely, $r=0$, all the six quarks are at the same center.

$$V(r=0) \approx \langle 6q|H|6q \rangle - 2 \langle 3q|H|3q \rangle$$

Potential equation

$$V_{QCM} = V_0 e^{-\frac{r^2}{b^2}}$$



$Y_c N$ INTERACTION

- Parameter fix

we determine the parameters of the potential so as to reproduce the NN interaction data using the same model.

- Fixed parameter

Pi-baryon coupling constants, Range parameter of QCM

- Determined parameter

Cutoff parameter ($\Lambda_\pi, \Lambda_\sigma$), sigma-baryon coupling constants

$Y_c N$ INTERACTION

- Parameter

$Y_c N$ -Corresponding To NN

we determine the parameters of the potential so as to reproduce the same model.

$Y_c N$ -CTNN	C_σ	b[fm]
parameter a	-67.58	0.6
parameter b	-77.5	0.6
parameter c	-60.76	0.5
parameter d	-70.68	0.5

- Fixed parameter

Pi-baryon coupling

parameter of QCM

- Determined parameter

[Prog. Theor. Exp. Phys. (2016) 023D02]

Cutoff parameter ($\Lambda_\pi, \Lambda_\sigma$), sigma-baryon coupling constants

$Y_c N$ INTERACTION

- Result of binding energy and scattering length

$J^\pi = 0^+$	CTNN-a	CTNN-b	CTNN-c	CTNN-d
B.E. [MeV] (+ Coulomb)	-	-	1.72×10^{-3}	1.37 (0.56)
scattering length [fm]	-3.64	-65.15	130.93	5.31

$J^\pi = 1^+$	CTNN-a	CTNN-b	CTNN-c	CTNN-d
B.E. [MeV] (+ Coulomb)	-	2.62×10^{-4}	1.97×10^{-2}	1.57 (0.72)
scattering length [fm]	-4.11	337.53	39.27	5.01

$Y_c N$ INTERACTION

- Resonance

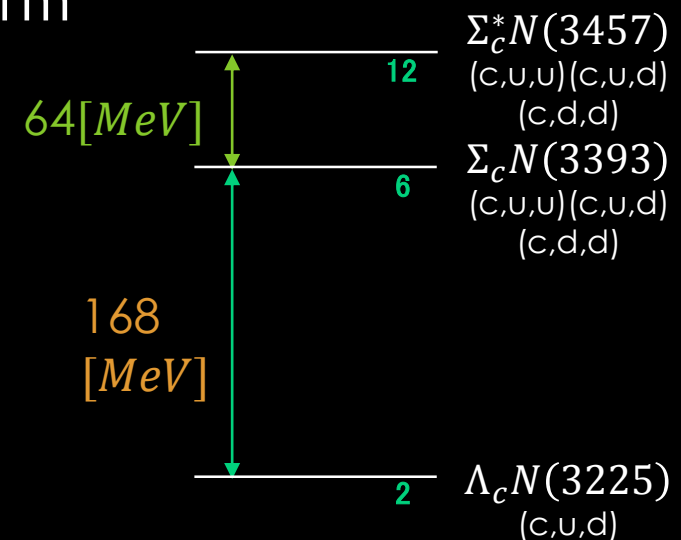
In the previous calculation, we consider only the state under the $\Lambda_c N$ threshold.

So, we calculate with the Complex scaling method

[J. Aguilar, J.M. Combes, Commun. Math. Phys. 22 (1971) 269.]

to search the state above the $\Lambda_c N$ threshold with $Y_c N$ -CTNN d-potential.

Charm



$Y_c N$ INTERACTION

- Resonance

- $J^P = 2^+$

$\Lambda_c N$ and $\Sigma_c N$ channel have no S-wave because of the rule of total angular momentum.

The S-wave and G-wave are the characteristic behavior of Σ_c^* having the spin = $\frac{3}{2}$

Channels	1	2	3	4	5	6	7	8
$J^\pi = 2^+$	$\Lambda_c N(^1D_2)$	$\Sigma_c N(^1D_2)$	$\Lambda_c N(^3D_2)$	$\Sigma_c N(^3D_2)$	$\Sigma_c^* N(^3D_2)$	$\Sigma_c^* N(^5S_2)$	$\Sigma_c^* N(^5D_2)$	$\Sigma_c^* N(^5G_2)$

$Y_c N$ INTERACTION

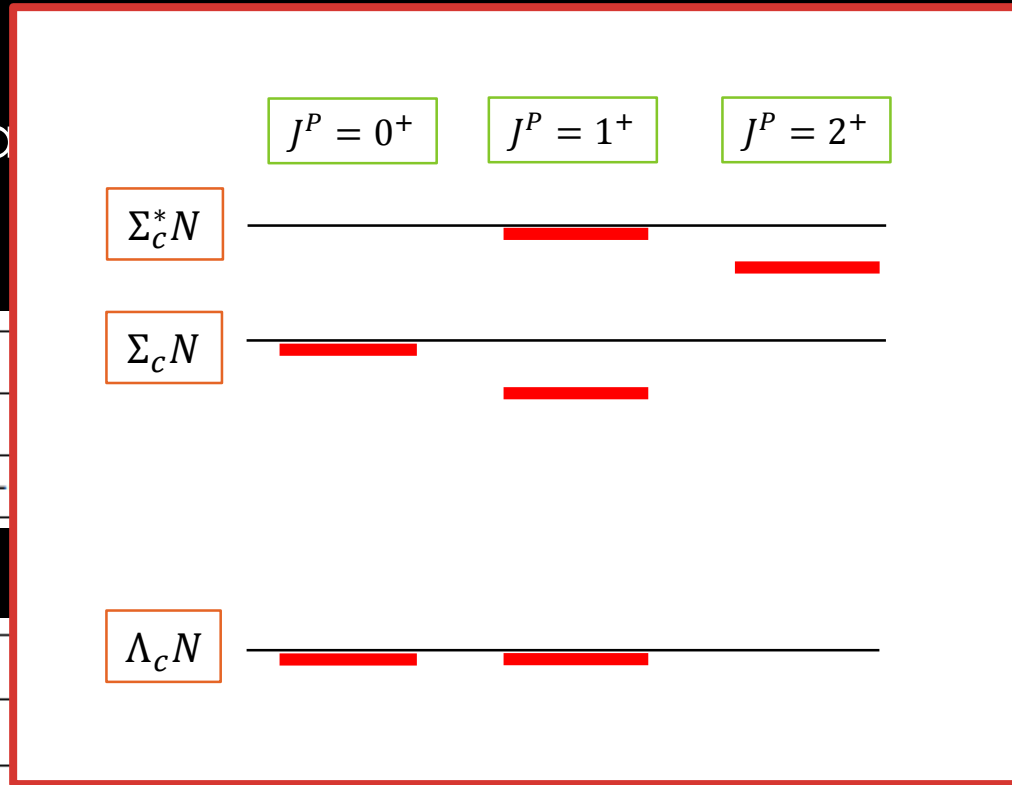
- Resonance
- Result

	$J^\pi = 0^+$ near $\Sigma_c N$		$J^\pi = 1^+$ near $\Sigma_c^* N$	
	resonance	width	resonance	width
CTNN-d	163.09 (-4.01)	1.09	225.00 (-6.51)	1.54

	$J^\pi = 1^+$ near $\Sigma_c N$		$J^\pi = 2^+$ near $\Sigma_c^* N$	
	resonance	width	resonance	width
CTNN-d	144.28 (-22.82)	11.92	206.34 (-25.17)	14.01

$Y_c N$ INTERACTION

- Resonance
- Result



CTNN-

near $\Sigma_c^* N$
width
) 1.54

CTNN-d

near $\Sigma_c^* N$
width
14.01

144.28	(-22.82)	11.92	206.54	(-25.17)
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$Y_c N$ INTERACTION

- Resonance
- Result with partial channel coupling

$\Sigma_c N$ threshold: 167.10 MeV
 $\Sigma_c^* N$ threshold: 231.51 MeV

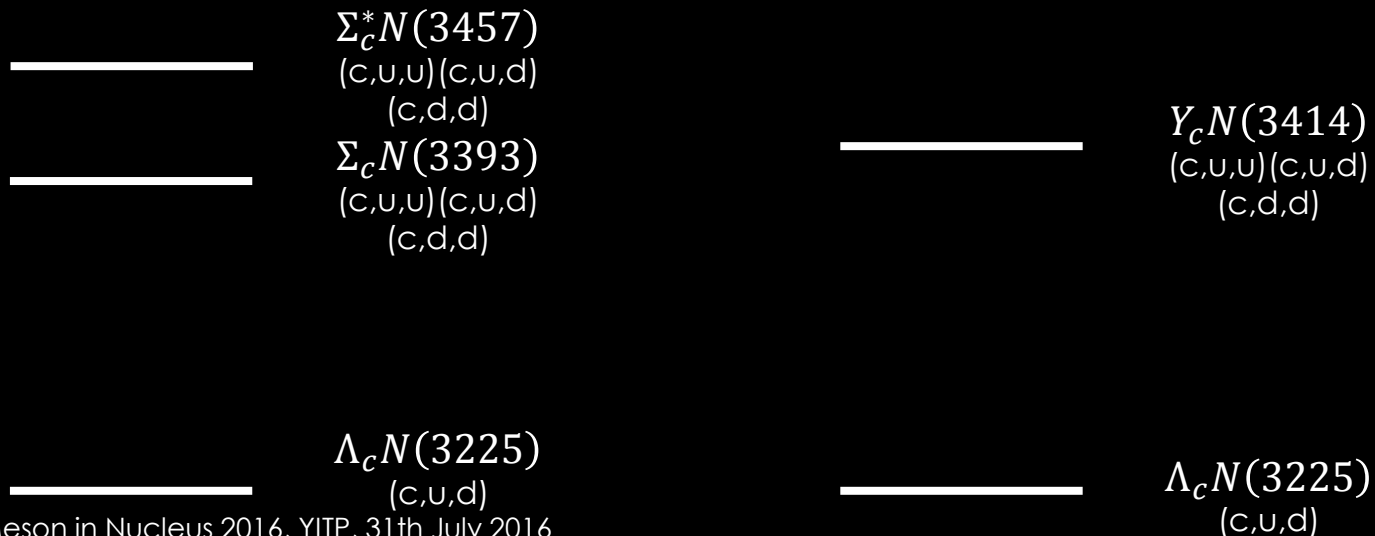
potential $J^P = 0^+(\Sigma_c N)$ $J^P = 1^+(\Sigma_c N)$ $J^P = 1^+(\Sigma_c^* N)$ $J^P = 2^+(\Sigma_c^* N)$

CTNN-d	2.22[MeV]	14.28[MeV]	7.67[MeV]	17.68[MeV]
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$Y_c N$ INTERACTION

- Resonance
- Heavy quark limit

We assume $\Sigma_c N$ and $\Sigma_c^* N$ are doublet, so we set the $Y_c N$ threshold in substitute for $\Sigma_c N$ and $\Sigma_c^* N$ threshold.



$Y_c N$ INTERACTION

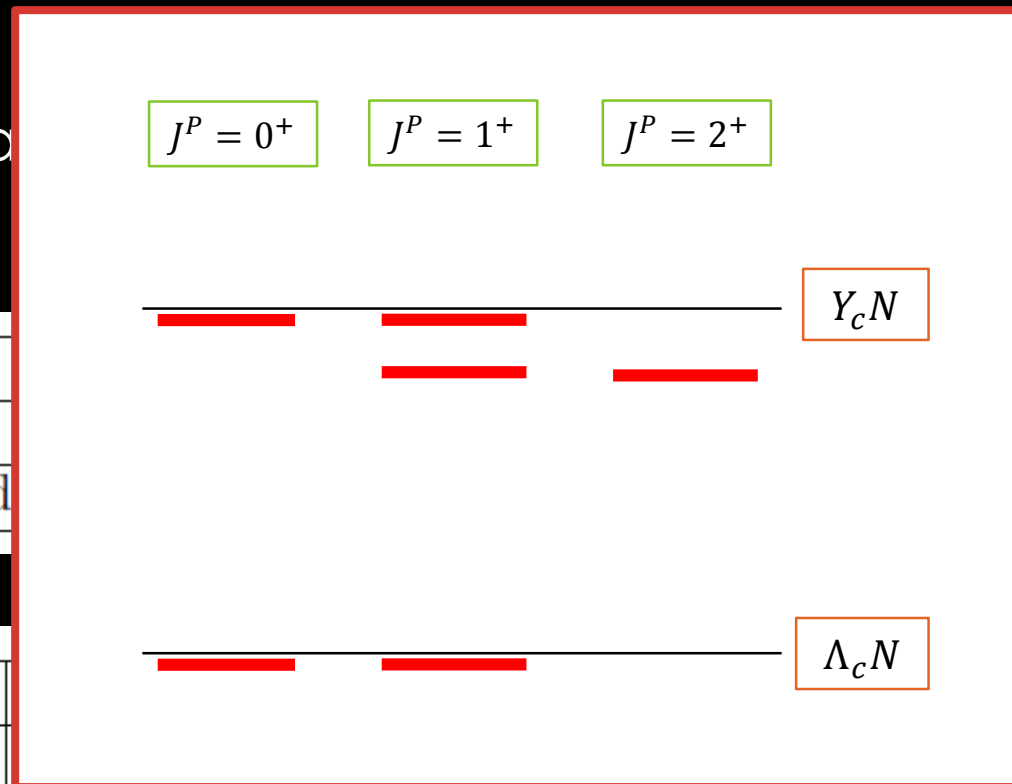
- Resonance
- Result

	$J^\pi = 0^+$ near $\Sigma_c N$		$J^\pi = 1^+$ near $\Sigma_c^* N$	
	resonance	width	resonance	width
CTNN-d	183.79 (-4.78)	0.91	183.72 (-4.85)	0.89

	$J^\pi = 1^+$ near $\Sigma_c N$		$J^\pi = 2^+$ near $\Sigma_c^* N$	
	resonance	width	resonance	width
CTNN-d	163.88 (-24.69)	13.16	163.84 (-24.73)	12.46

$Y_c N$ INTERACTION

- Resonance
- Result



near $\Sigma_c^* N$	
	width
5)	0.89

near $\Sigma_c^* N$	
	width
CTNN-d	12.46

CTNN-d	163.88	(-24.69)	13.16	163.84	(-24.73)	12.46
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SUMMARY

- We propose the $Y_c N$ potential model based on the hadron model and the quark model, and find four parameter set to reproduce experimental data of NN system.
- Calculating the $Y_c N$ 2-body system, we get not only the shallow bound state but also resonance states for several potential models.